# Probing the Higgs self coupling via single Higgs production at the LHC

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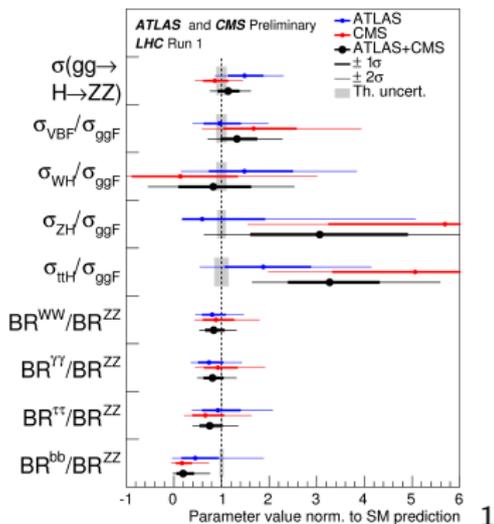
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Based mainly on: G. Degrassi, PPG, F. Maltoni, D. Pagani; JHEP 1612 (2016) 080;

G. Degrassi, M. Fedele, PPG; JHEP 1704 (2017) 155

- The Higgs still appears to be quite "Standard".
- The couplings with the vector bosons are compatible with the SM within a $\sim 10\%$ uncertainty,
- for the couplings to fermions the compatibility is within a $\sim 15 - 20\%$ uncertainty.

But the situation with the Higgs self couplings is quite different.
This talk is dedicated to the trilinear coupling:
for the quartic "Abandon hope all".

[1] ATLAS-CONF-2015-044
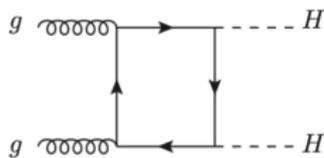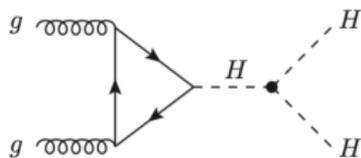
## One vs. Two at 13 TeV

$gg \rightarrow H \sim 40$ pb
$gg \rightarrow HH \sim 30$ fb

Very small Cross Section.

- Heavier final state.
- Additional weak coupling.
- Destructive interference.

## Assuming no change in the other Higgs couplings at 8 TeV,

ATLAS and CMS constraint $\lambda_3$ in the region[2] $\mathcal{O}(\pm(15-20)\lambda_3^{\mathrm{SM}})$

At 3000 fb$^{-1}$ $\lambda_3$ is constrained in the region[3] $(-1.3, 8.7)\lambda_3^{\mathrm{SM}}$

[2] Phys.Rev. D92 (2015) 092004; Eur.Phys.J. C75 (2015) no.9, 412; Phys.Rev. D94 (2016) no.5, 052012.

[3] ATL-PHYS-PUB-2014-019; ATL-PHYS-PUB-2015-046.

The trilinear appears also in Single Higgs processes at NLO.
We assume $V_{H^3} = \lambda_3 v H^3 \equiv \kappa_\lambda \lambda_3^{\mathrm{SM}} v H^3$ and study its effects.[4]
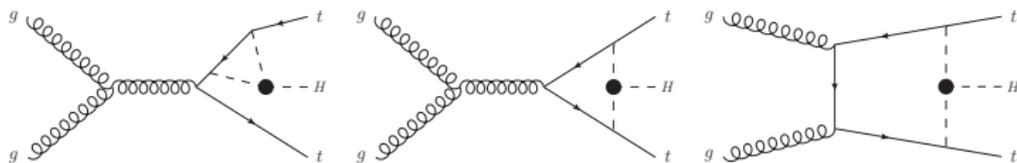


Due to the presence of different Loop structures these
contributions cannot be captured by a local rescaling.

[4] For similar ideas: M. McCullough Phys. Rev. D90 (2014), no. 1 015001, M. Gorbahn and U. Haisch JHEP
1610 (2016) 094

# Calculation

### Processes at NLO

$$\Sigma_{NLO} = Z_H \Sigma_{LO}(1 + \kappa_\lambda C_1)$$

- $\Sigma_{LO}$ contains QCD corrections.
- $C_1$ depends on the process.

- $Z_H$ is the Higgs wave function renormalization,
- $Z_H = \frac{1}{1 - \kappa_\lambda^2 \delta Z_H}$

The range of validity of our calculation is $|\kappa_\lambda| \lesssim 20$

### In general an Observable $O$ can be written as

$$O = O^{\mathrm{SM}}[1 + (\kappa_\lambda - 1)C_1 + (\kappa_\lambda^2 - 1)C_2]$$

## Calculation

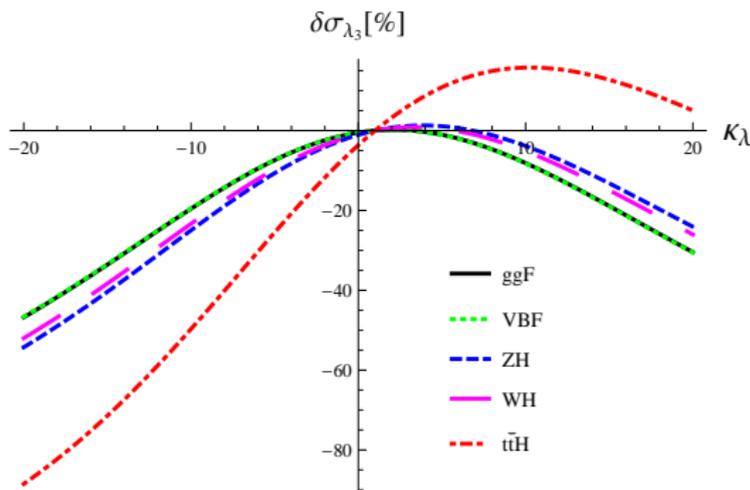$$O = O^{\mathrm{SM}}[1 + (\kappa_\lambda - 1)C_1 + (\kappa_\lambda^2 - 1)C_2]$$

$C_1$ depends on the specific observable, $\sqrt{s}$, $p_t$ cuts...

$$C_1 = \frac{\int 2\Re(\mathcal{M}^{0*}\mathcal{M}^1_{\lambda_3^{\mathrm{SM}}})}{\int |\mathcal{M}^0|^2}$$

Amplitudes generated by FeynArts, computed by FormCalc interfaced to Loop-Tools, checked with FeynCalc.

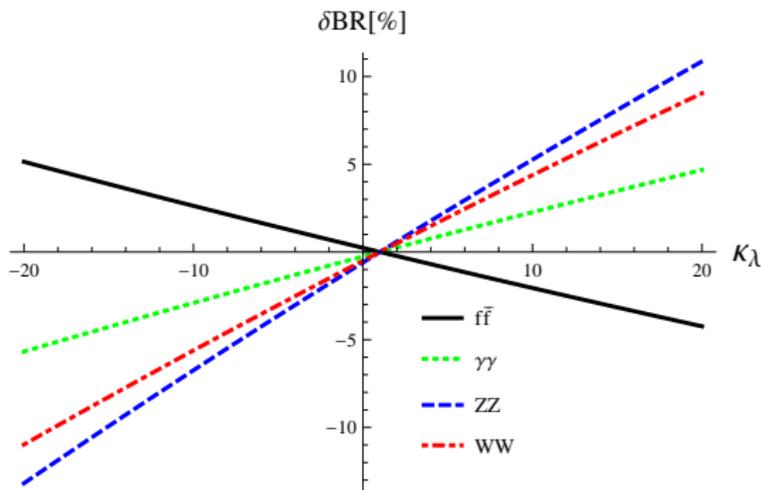$C_2$ is obtained from $Z_H$ and do not depend on the observable.

# Cross Sections

| $C_1^\sigma$ [%] | $gg$F | VBF | $WH$ | $ZH$ | $t\bar{t}H$ |
|---|---|---|---|---|---|
| 8 TeV | 0.66 | 0.65 | 1.05 | 1.22 | 3.78 |
| 14 TeV | 0.66 | 0.64 | 1.03 | 1.18 | 3.47 |



- $t\bar{t}H$ receives sizeable positive corrections.
- The other $\sigma$ receive very small positive corrections.
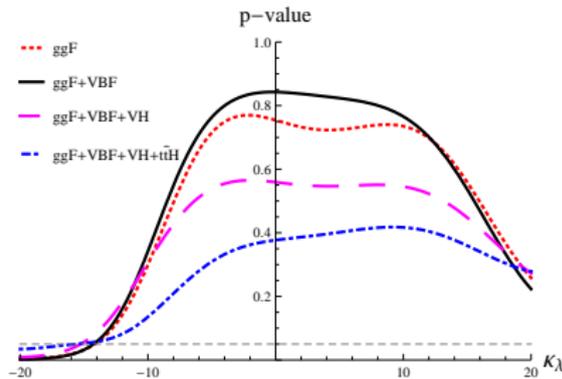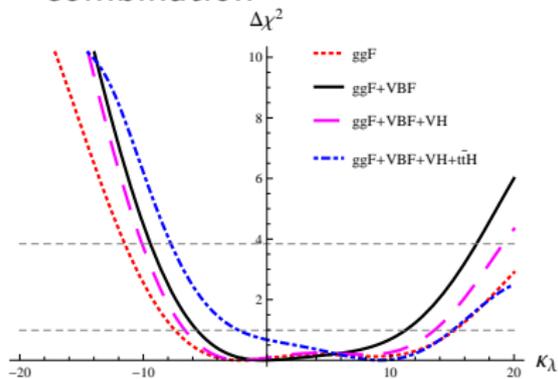- The corrections have a parabolic shape around the SM.

# Branching Ratios

| $C_1^\Gamma$ [%] | $\gamma\gamma$ | $ZZ$ | $WW$ | $f\bar{f}$ | $gg$ |
|---|---|---|---|---|---|
| on-shell $H$ | 0.49 | 0.83 | 0.73 | 0 | 0.66 |



- The BR do not depend on $k_\lambda^2$.
- The (positive) $\delta$BR are usually larger than the $\delta\sigma$.
- In other words, in the range close to the SM, the decays are more sensitive to $\kappa_\lambda$ than the production processes.
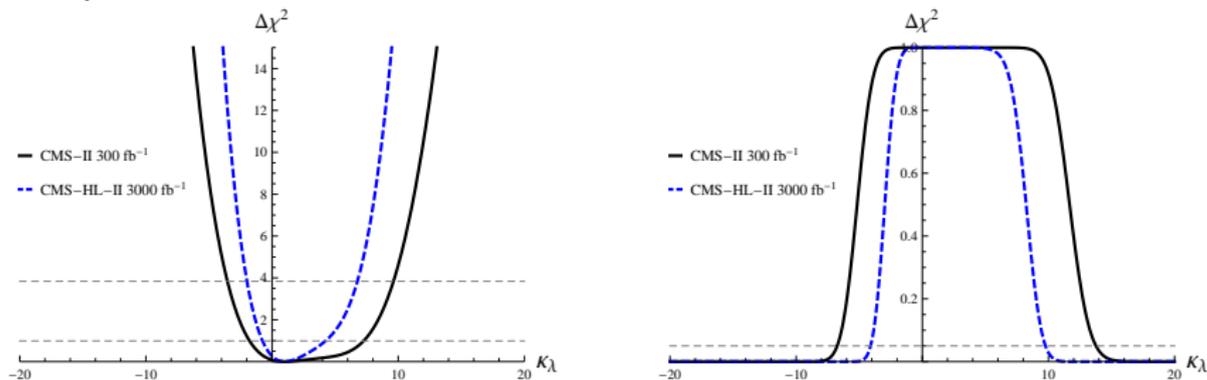
Fit on different "scenarios". Data from ATLAS-CMS 8 TeV data combination[5]



- For ggF+VBF:
  $\kappa_\lambda^{\mathrm{best}} = -0.24$, $\kappa_\lambda^{1\sigma} = [-5.7, 11.2]$, $\kappa_\lambda^{2\sigma} = [-9.4, 17.0]$.
- Requiring $p > 0.05$, we exclude at more than $2\sigma$ $\kappa_\lambda < -14.3$

[5] JHEP 1608 (2016) 045

# Future

Using the uncertainties presented in arXiv:1312.4974, and assuming that LHC will measure SM, we can estimate the future capabilities of LHC.
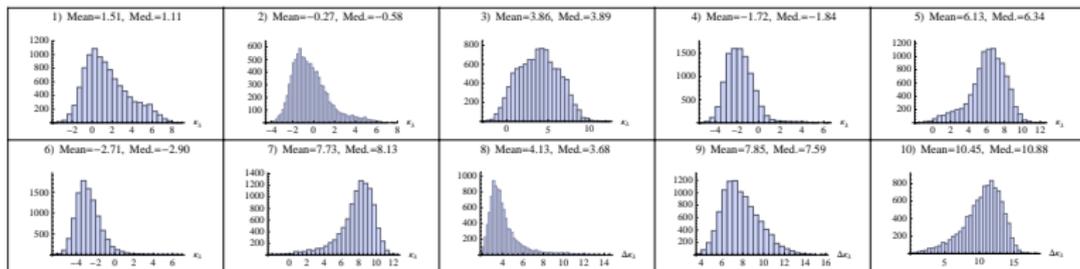


For CMS-HL-II 3000 fb$^{-1}$:
$\kappa_\lambda^{1\sigma} = [-0.8, 4.2]$, $\kappa_\lambda^{2\sigma} = [-2.0, 6.8]$, $\kappa_\lambda^{p>0.05} = [-4.1, 9.8]$.

## Future

A more reliable approach is to consider central values compatible with SM.
We produce a collection of pseudo-measurements randomly generated with a gaussian distribution around the SM.



1) best values, 2) $1\sigma$ region lower limit, 3) $1\sigma$ region upper limit, 4) $2\sigma$ region lower limit, 5) $2\sigma$ region upper limit, 6) $p > 0.05$ region

lower limit, 7) $p > 0.05$ region upper limit, 8) $1\sigma$ region width, 9) $2\sigma$ region width, 10) $p > 0.05$ region width.

$$\kappa_\lambda^{p>0.05} = [-2.8, 7.9]$$

For ATLAS 3000 fb$^{-1}$ $\kappa_\lambda^{p>0.05} = [-1.3, 8.7]$

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Precision physics can also give informations on the trilinear. [6]
The theoretical predictions of $m_W$ and $\sin^2\theta_{\rm eff}^{\rm lep}$ can be expressed in terms of physical quantities:

$$m_W^2 = \frac{\hat{\rho}\, m_Z^2}{2} \left\{ 1 + \left[ 1 - \frac{4\hat{A}^2}{m_Z^2\hat{\rho}}(1 + \Delta\hat{r}_W) \right]^{1/2} \right\}$$

with $\hat{A} = (\pi\hat{\alpha}(m_Z)/(\sqrt{2}G_\mu))^{1/2}$.
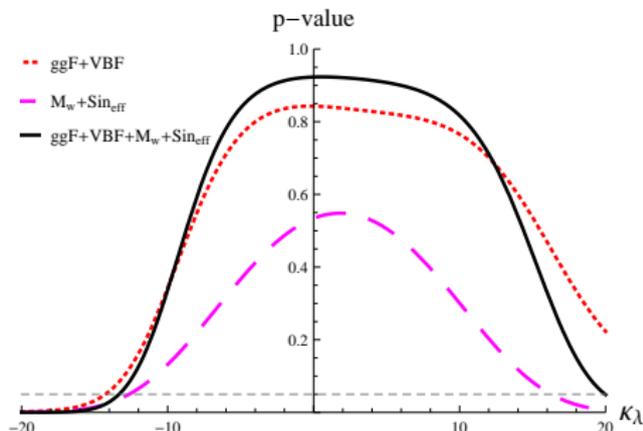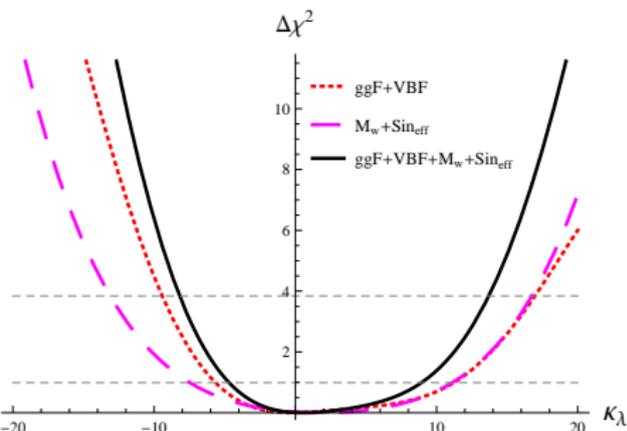$\hat{\rho}$ and $\Delta\hat{r}_W$ are related to the Peskin-Takeuchi parameters T and S.

$$O = O^{\rm SM}[1 + (\kappa_\lambda - 1)C_1 + (\kappa_\lambda^2 - 1)C_2]$$

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[6] see also Kribs , Maier, Rzehak, Spannowsky, Waite arXiv:1702.07678

|                              | $C_1$                  | $C_2$                  |
|------------------------------|------------------------|------------------------|
| $m_w$                        | $6.27 \times 10^{-6}$  | $-1.72 \times 10^{-6}$ |
| $\sin^2 \theta_{\text{eff}}^{\text{lep}}$ | $-1.56 \times 10^{-5}$ | $4.55 \times 10^{-6}$  |



- $\kappa_\lambda^{\text{best}} = 0.5$, $\kappa_\lambda^{1\sigma} = [-4.7, 8.9]$, $\kappa_\lambda^{2\sigma} = [-8.2, 13.7]$.
- Requiring $p > 0.05$ we exclude at more than $2\sigma$
  $\kappa_\lambda < -13.3$ and $\kappa_\lambda > 20.0$

## Conclusions

- No direct measurement of the Higgs self couplings. In particular of the trilinear.

- The Higgs trilinear coupling can be investigated from single Higgs processes.

- Compared to Higgs pair production, the bounds obtained are competitive and complementary.

- This approach is model dependent, however the condition for the other couplings to be SM can be lifted. Marc's talk!

- Precision physics can help further constraint the allowed region.

# Backup Slides

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# The dimension 6 operator

$V^{\mathrm{dim}-6}(\Phi) = V^{\mathrm{SM}}(\Phi) + \frac{c6}{v^2}(\Phi^\dagger \Phi)^3$, with $\Phi = \frac{1}{\sqrt{2}} \begin{pmatrix} \phi^+ \\ v + H + i\phi^0 \end{pmatrix}$

From the conditions $\left| \frac{dV^{\mathrm{dim}-6}(\Phi)}{d\Phi} \right|_{|\Phi|=v/\sqrt{2}} = 0$,

$$\kappa_\lambda = 1 + \frac{2c_6 v^2}{m_H^2}$$

We need to impose that $\Phi = \frac{v}{\sqrt{2}}$ is still a global minimum.

$V^{\mathrm{dim}-6}(v/\sqrt{2}) = \frac{c_6 v^4 - m_H^2 v^2}{8} < 0 = V^{\mathrm{dim}-6}(0) \rightarrow \kappa_\lambda < 3$

C. Grojean, G. Servant and J. D. Wells; Phys. Rev. D71 (2005) 036001

P. Huang, A. Joglekar, B. Li and C. E. M. Wagner; Phys. Rev. D93 (2016) 055049

$\kappa_\lambda < 3$ is not very interesting for present phenomenology
More in general one can write $V^{NP} = \sum_{n=1}^{N} c_{2n}(\Phi^\dagger\Phi)^n$.
We ask the series to be convergent but we do not impose other
conditions on $c_{2n}$.
Expanding up to $\phi^4$ ($\xi = \phi^+\phi^- + \frac{1}{2}\phi_2^2$)

$$
\begin{aligned}
V_{4\phi}^{NP} &= \frac{m_H^2}{2v^2}\,\xi^2 + \left(\frac{m_H^2}{2v^2} + d\lambda_4\right)\frac{1}{4}\,\phi_1^4 + \left(\frac{m_H^2}{2v^2} + 3\,d\lambda_3\right)\xi\,\phi_1^2 \\
&\quad + \left(\frac{m_H^2}{2v} + d\lambda_3\right)\phi_1^3 + \frac{m_H^2}{v}\,\xi\,\phi_1 + \frac{1}{2}m_H^2\,\phi_1^2\,.
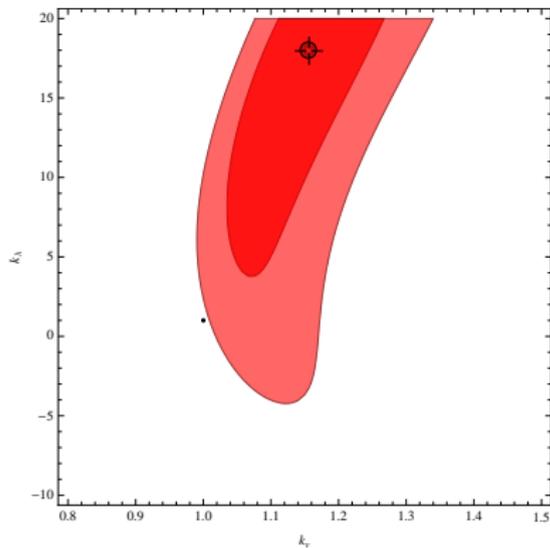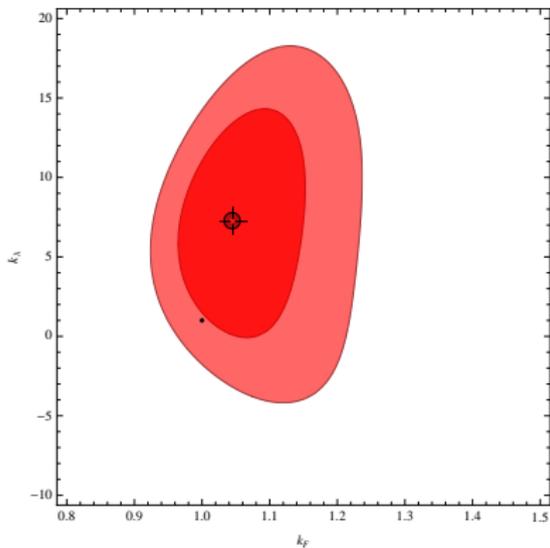\end{aligned}
$$

$V_{4\phi}^{NP}$ gives the same results of the anomalous coupling, since
contributions due to $d\lambda_4$ are zero at the order of our calculations.

| $C_1^\sigma[\%]$ | 25 GeV | 50 GeV | 100 GeV | 200 GeV | 500 GeV |
|---|---|---|---|---|---|
| $WH$ | 1.71 | 1.56 | 1.29 | 1.09 | 1.03 |
| $ZH$ | 2.00 | 1.83 | 1.50 | 1.26 | 1.19 |
| $t\bar{t}H$ | 5.44 | 5.14 | 4.66 | 3.95 | 3.54 |

Table: $C_1^\sigma$ at 13 TeV obtained by imposing the cut $p_T(H) < p_{T,\mathrm{cut}}$, for several values of $p_{T,\mathrm{cut}}$.

The two-loop diagrams in the W self energy that are sensitive to a modification of the Higgs self couplings are depicted in figure.