

Lines, Boxes, and Energy Duality: Unmasking Dynamical Dark Matter in Indirect-Detection Data



Brooks Thomas

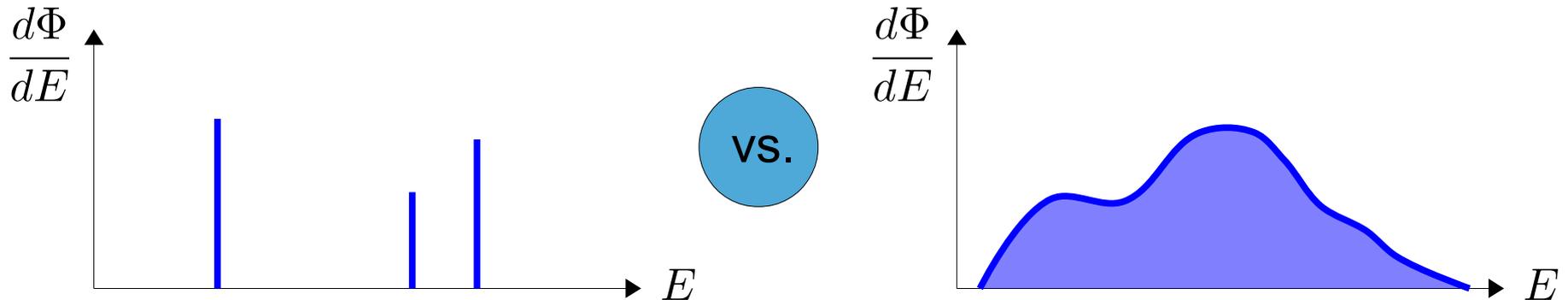
LAFAYETTE
COLLEGE

Based on work done in collaboration with:

- **Kimberly Boddy, Keith Dienes, Doojin Kim, Jason Kumar, and Jong-Chul Park [arXiv:1609.07440, arXiv:1609.09104].**

A General Observation:

- Extracting information about the dark matter from **continuum features** observed at indirect-detection experiments is notoriously challenging.



- Complicated **showering/cascade dynamics** obscures the relationship between the shape of the signal spectrum and the properties of the underlying dark sector.
- Moreover, it's not easy to tell conclusively that such a signal spectrum has a dark-matter origin and isn't due to more **mundane astrophysics** (e.g., pulsars).



It's important to identify techniques which can serve to distinguish between dark-matter models on the basis of continuum features in indirect-detection spectra!

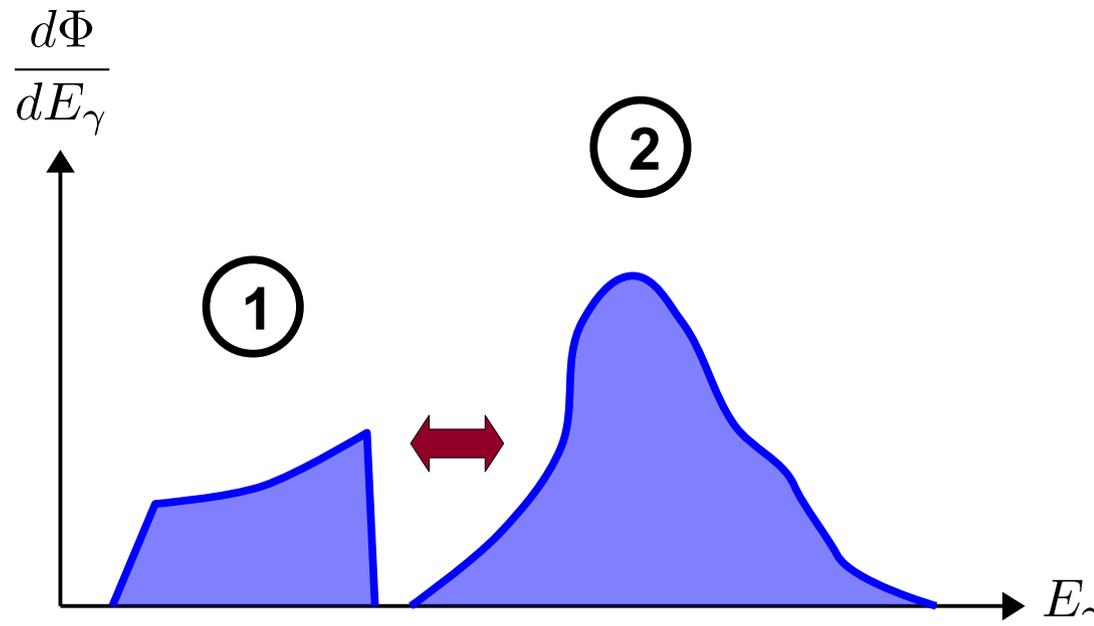
- One natural context in which continuum features with characteristic (and particularly simple) kinematics arise is the **Dynamical Dark Matter** (DDM) framework. [Dienes, BT, '11]

In DDM scenarios...

- The dark-matter candidate is an **ensemble** consisting of a potentially vast number of constituent particle species.
 - The individual abundances of the constituents are **balanced against decay rates** across the ensemble such that constraints are satisfied.
 - The DM abundance and equation of state also exhibit a **non-trivial time-dependence** beyond that associated with Hubble expansion.
-
- Continuum signals can arise from a decaying (or annihilating) DDM ensemble wherein the mass splittings between the constituents are smaller than the energy resolution of the detector.
 - Since the continuum nature of these spectral features results from a spearing of the total DM abundance features across the ensemble, the **annihilation/decay kinematics** can nevertheless be **straightforward**.

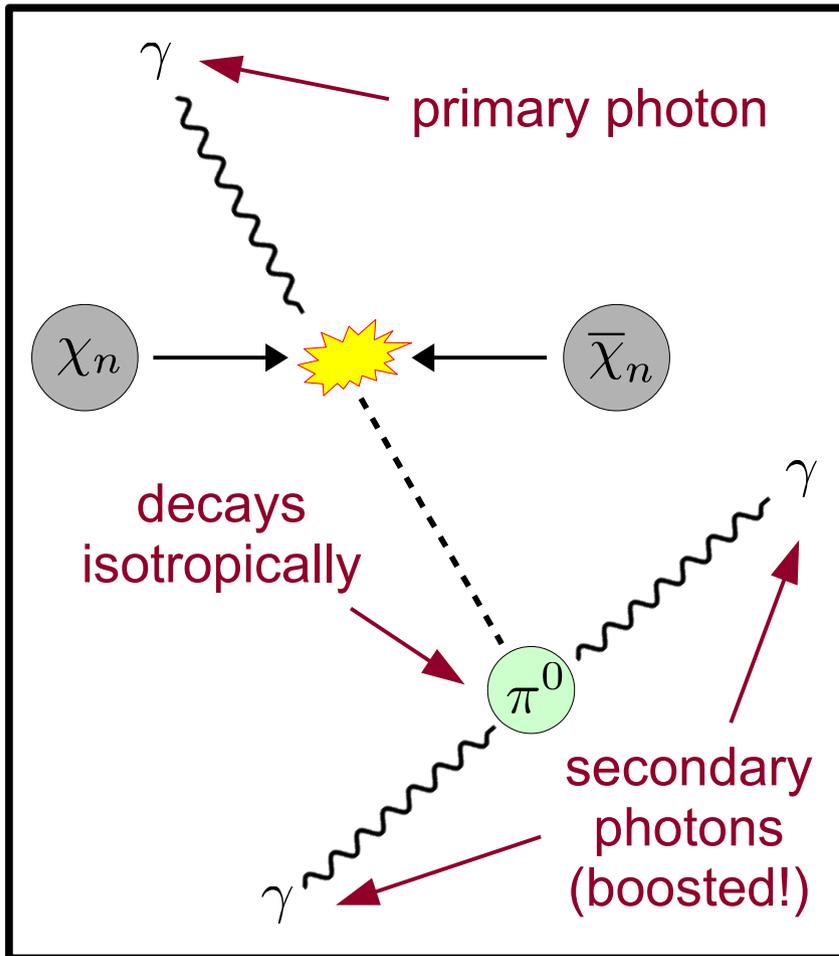
Technique I: Correlating Spectral Features

- One technique which can potentially uncover information about the origin of a continuum signal is to look for **correlations** between the shapes (and normalizations) of **different spectral features** within the same signal spectrum.
- Such correlations can arise when the features are produced via the same underlying annihilation/decay process.
- They can also be analyzed even if the spectral features in question overlap.

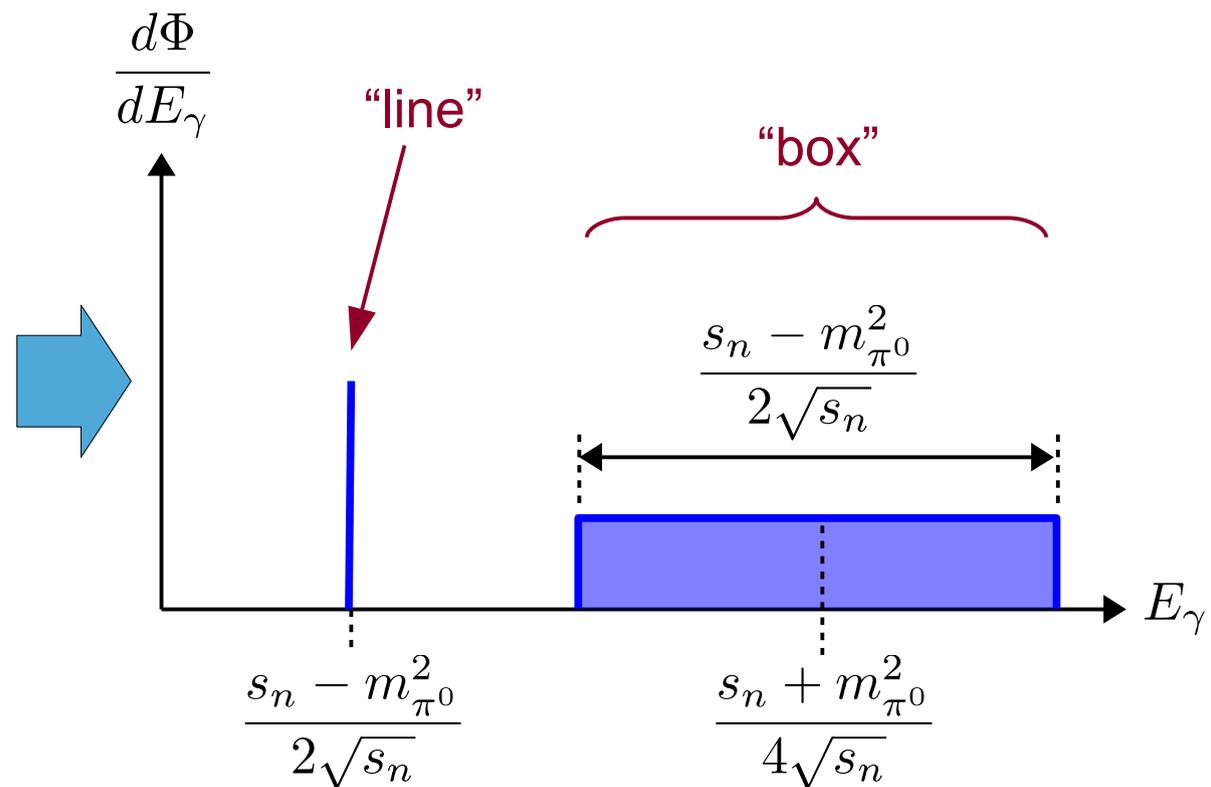


Decay Kinematics: Lines and Boxes

- Ensemble of DM particles χ_n with masses m_n , where $n = 0, 1, 2, \dots, N$.
- Each annihilates via $\chi_n \bar{\chi}_n \rightarrow \pi^0 \gamma \rightarrow \gamma \gamma \gamma$
- Secondary photons produced by π^0 decay are **boosted**. Resulting photon spectrum includes both a line-like feature and a spectral “box.”

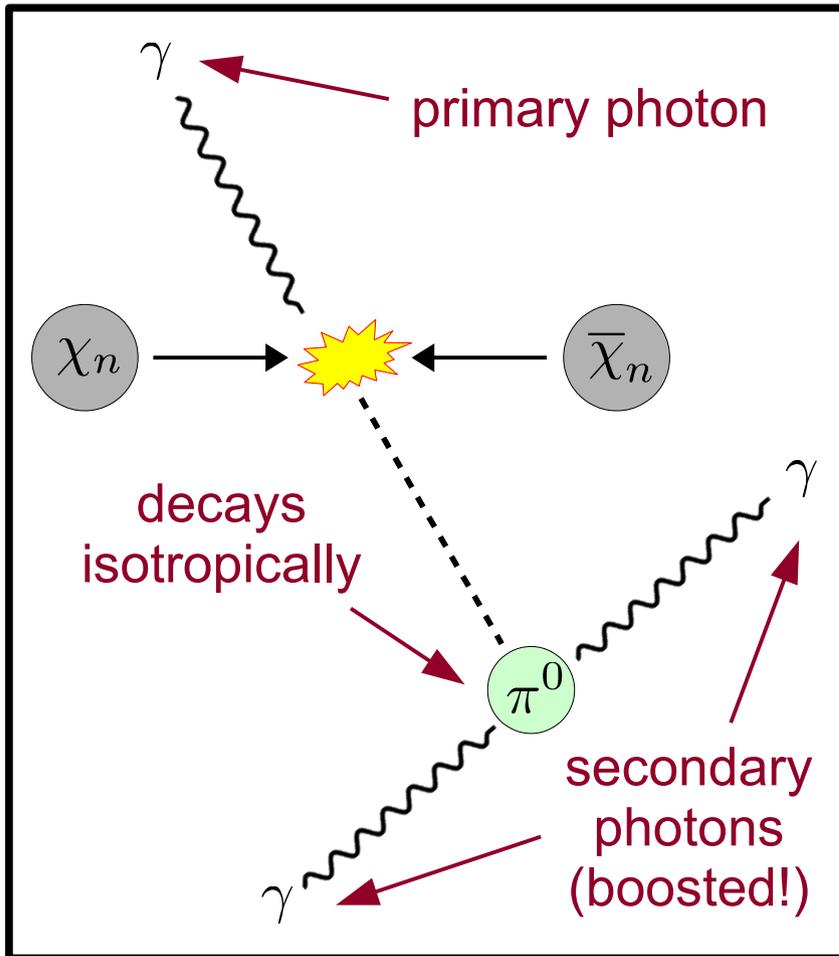


Photon Spectrum (One DM Particle)

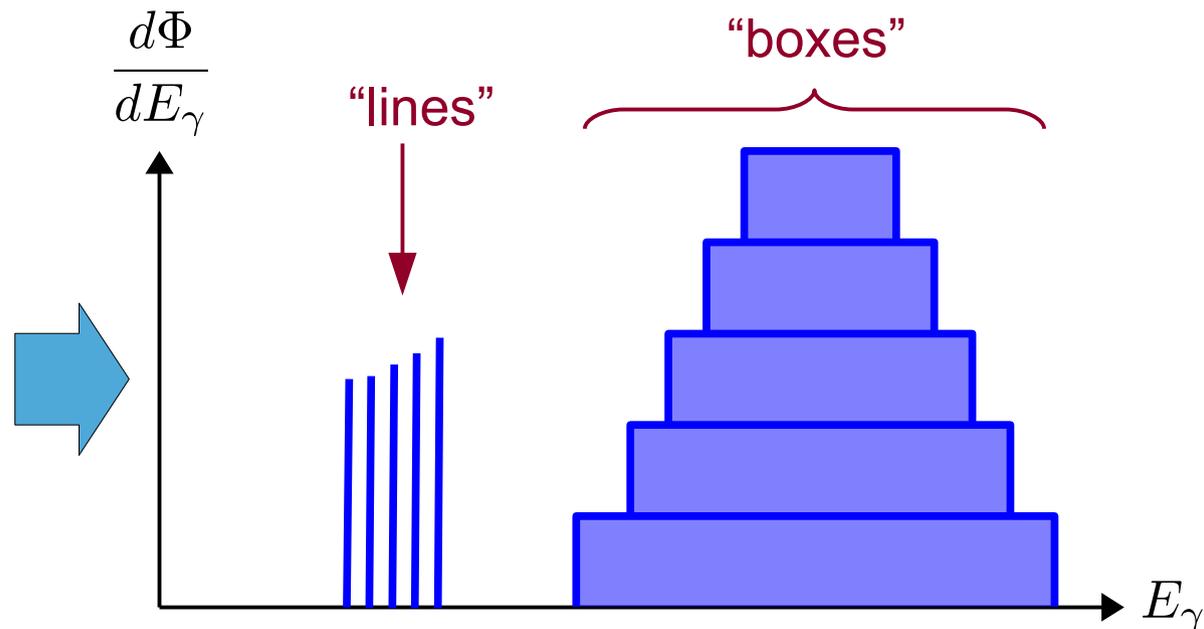


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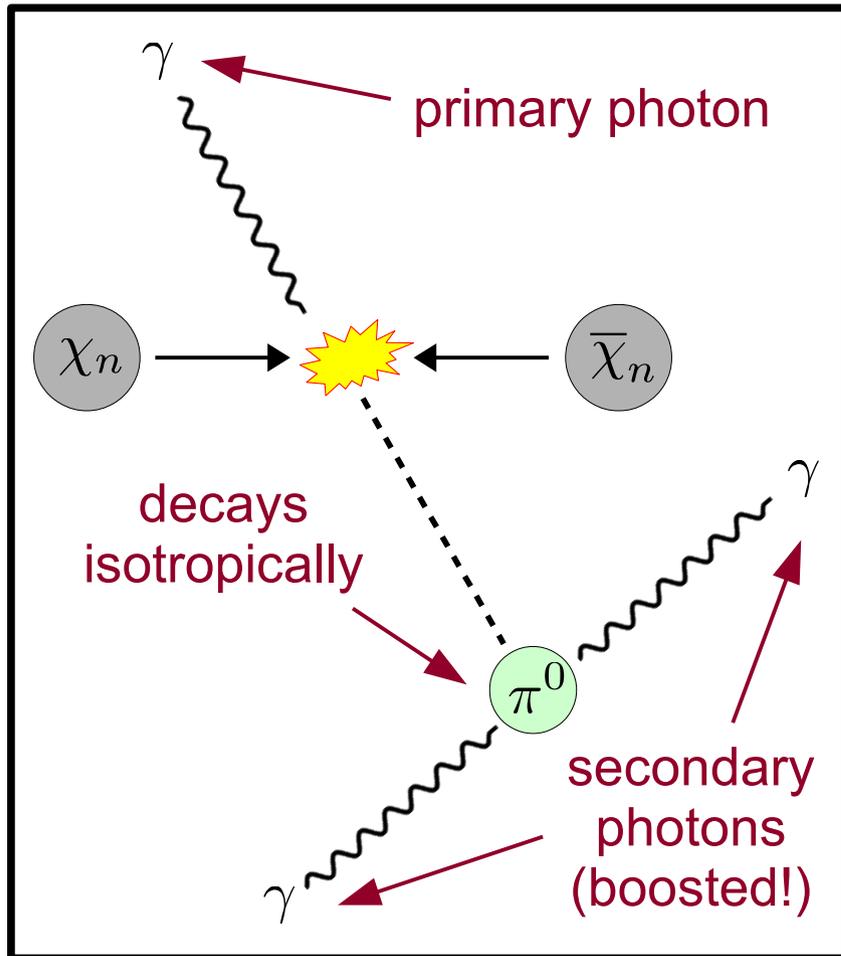


Photon Spectrum (Whole Ensemble)



Decay Kinematics: Lines and Boxes

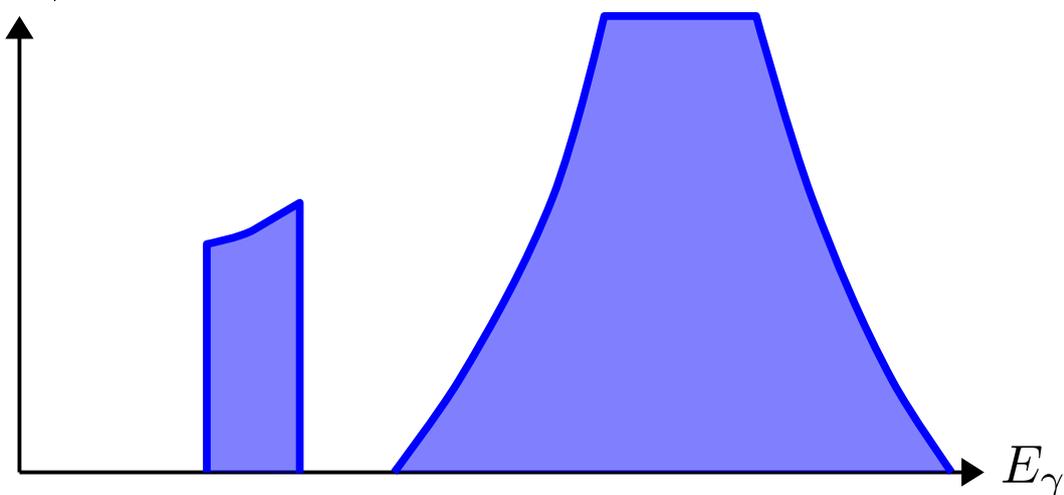
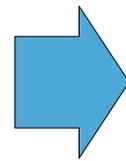
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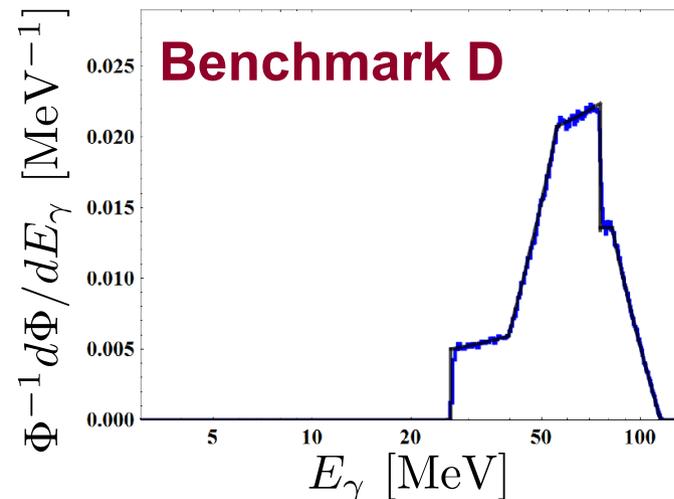
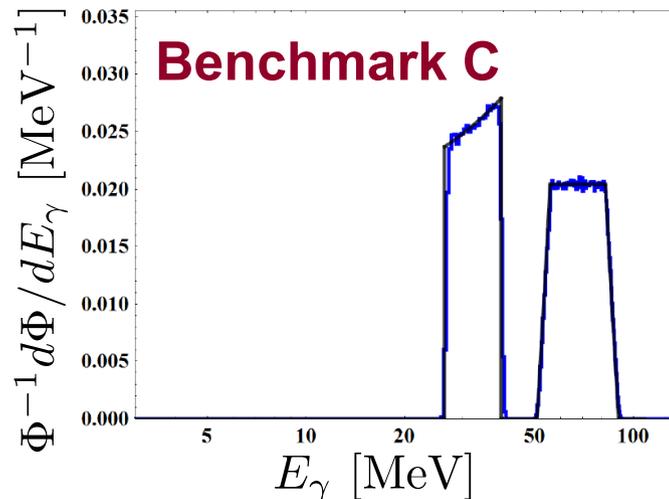
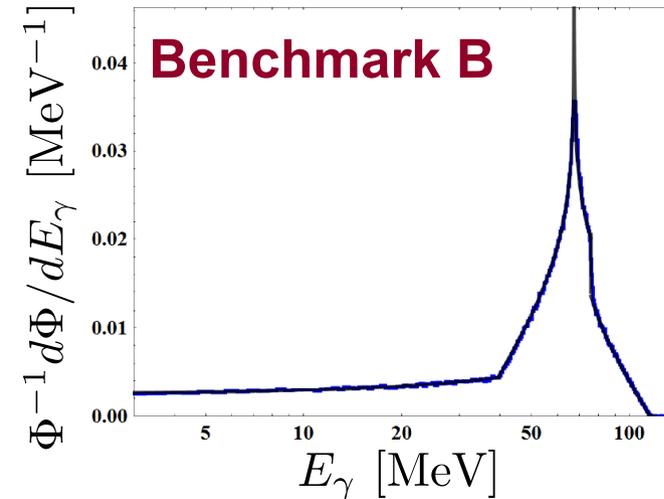
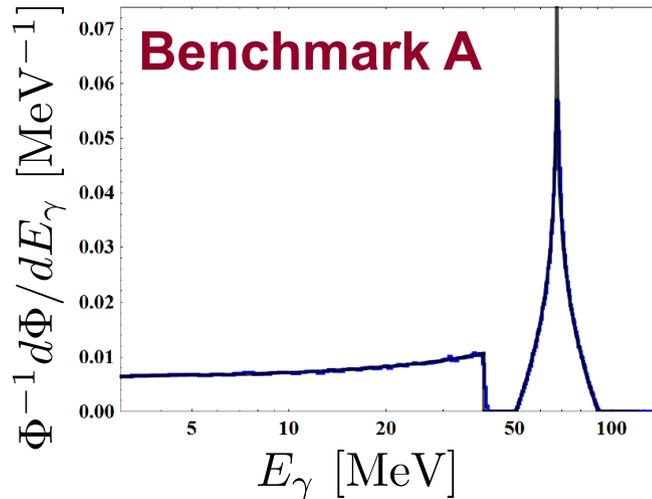
$$\frac{d\Phi}{dE_\gamma}$$

two correlated spectral features



- We adopt four **benchmark scenarios** which represent four qualitatively different cases of interest:

Benchmark	$\sqrt{s_0}$ (MeV)	$\sqrt{s_N}$ (MeV)	N	Behavior at $E_\gamma = m_{\pi^0}/2$	Spectral overlap
A	135	181	23	spike	negligible
B	135	231	48	spike	significant
C	164	180	8	plateau	negligible
D	164	230	33	plateau	significant

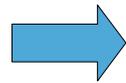


Looking for a Signal

- Dwarf galaxies:
 - Dark-matter dominated [Mateo, '98; McConnachie, '12].
 - More reliable estimates of astrophysical backgrounds/foregrounds
- For concreteness, we choose...



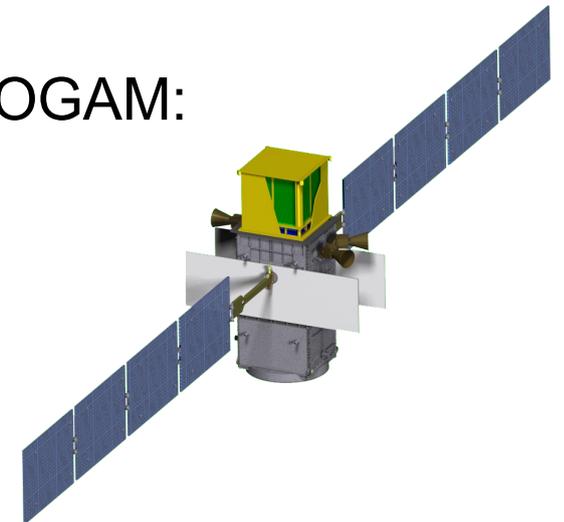
Draco Dwarf



$$\begin{cases} \log_{10}(J/\text{GeV}^2\text{cm}^{-5}) = 19.05_{-0.21}^{+0.22} \text{ (annihilation)} \\ \log_{10}(J/\text{GeV}^2\text{cm}^{-2}) = 18.97_{-0.24}^{+0.17} \text{ (decay)} \end{cases}$$

- Hypothetical space-based detector similar to ASTROGAM:

- Energy range: $0.3 \text{ MeV} \lesssim E_\gamma \lesssim 3000 \text{ MeV}$
- Energy resolution: 1% over full range of E_γ
- Effective area: 500 cm^2
- One year of continuous running



Parametrizing the Ensemble

- For concreteness, we consider an annihilating DDM scenario in which the individual masses m_n and flux contributions Φ_n associated with the ensemble constituents scale as follows:

$$m_n = m_0 + n\Delta m$$

$$\Phi_n = \Phi_0 \left(\frac{\sqrt{s_n}}{\sqrt{s_0}} \right)^\xi$$

Where: $\sqrt{s_n} \approx \begin{cases} 2m_n & \text{(annihilation)} \\ m_n & \text{(decay)} \end{cases}$

- Background N_B : diffuse background model based on COMPTEL, EGRET data.
- Signal N_S : minimum number of events necessary for initial 5σ discovery based on simple counting analysis.

- Primary and secondary spectra fit separately when they don't overlap, each with its own normalization factor Ψ :

Fit parameters:

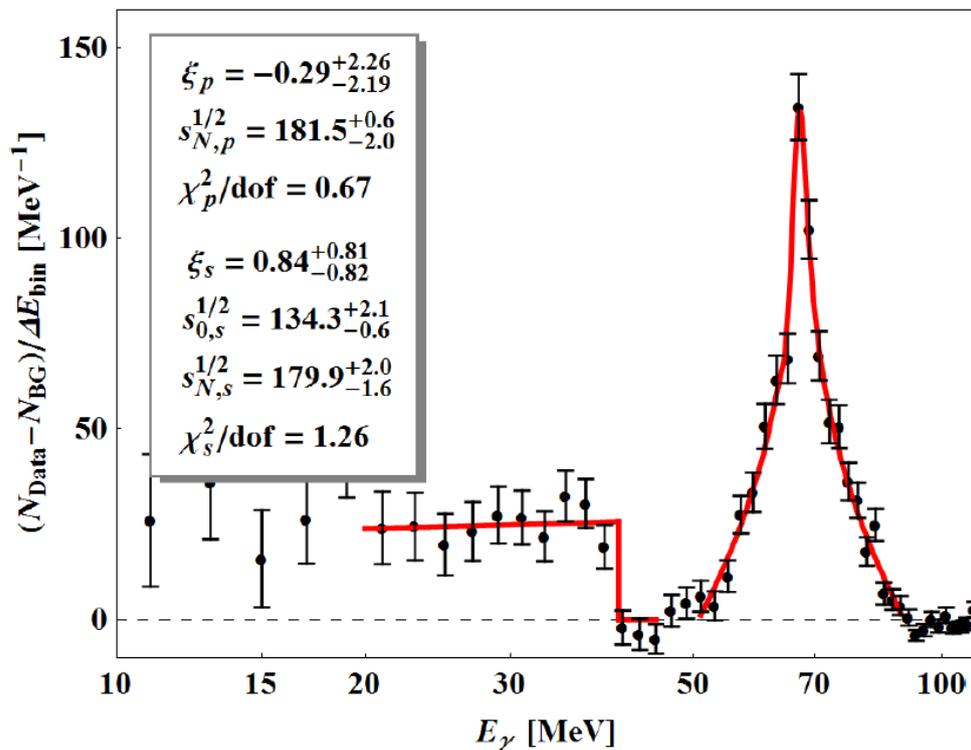
$$\left\{ \sqrt{s_{0p}}, \sqrt{s_{Np}}, \xi_p, \Psi_p \right\} \quad \text{and} \quad \left\{ \sqrt{s_{0s}}, \sqrt{s_{Ns}}, \xi_s, \Psi_s \right\}$$

- Both spectra fit together with a common normalization factor when there is significant overlap:

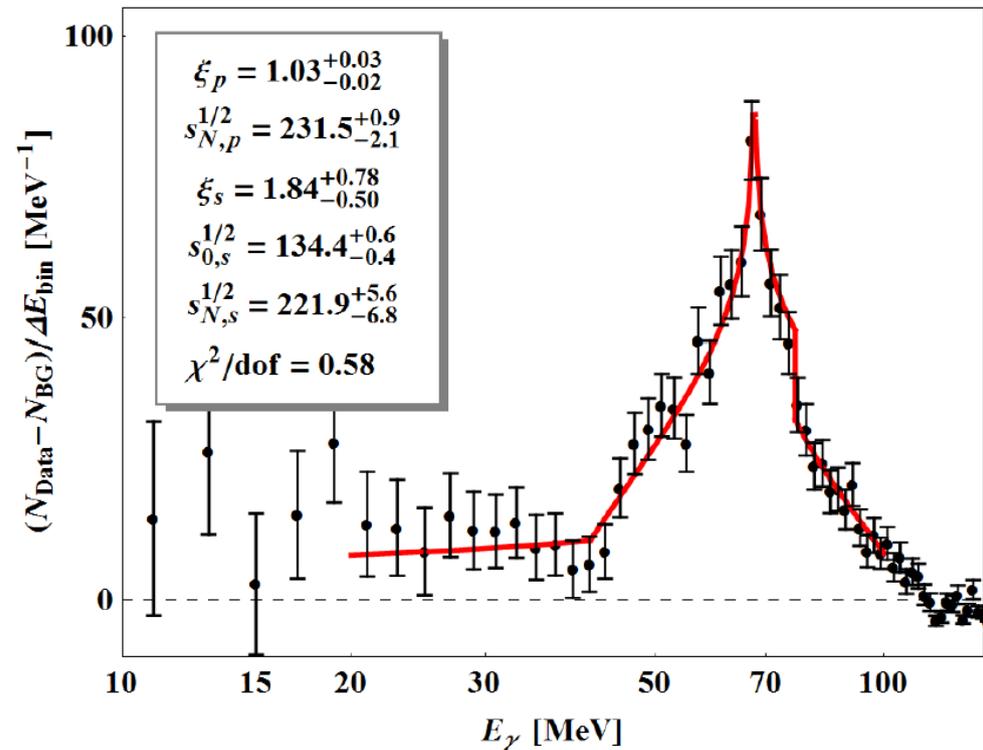
Fit parameters:

$$\left\{ \sqrt{s_{0p}}, \sqrt{s_{Np}}, \xi_p, \sqrt{s_{0s}}, \sqrt{s_{Ns}}, \xi_s, \Psi \right\}$$

Benchmark A



Benchmark B



Technique II: Exploiting Energy Duality

- An interesting duality arises in the gamma-ray signal spectra associated with certain dark-matter annihilation/decay topologies. In particular, whenever...
 - The DM particles annihilate/decay down to **on-shell intermediaries**
 - Each intermediary decays **isotropically** to photons within its own, proper frame
 - These photons are line-like (i.e., produced only with certain specific energies) in the frame of the decaying intermediary.

...the resulting photon spectrum is **invariant** under:

$$E_\gamma \rightarrow \frac{E_*^2}{E_\gamma} \quad \leftarrow \text{“Energy duality”}$$

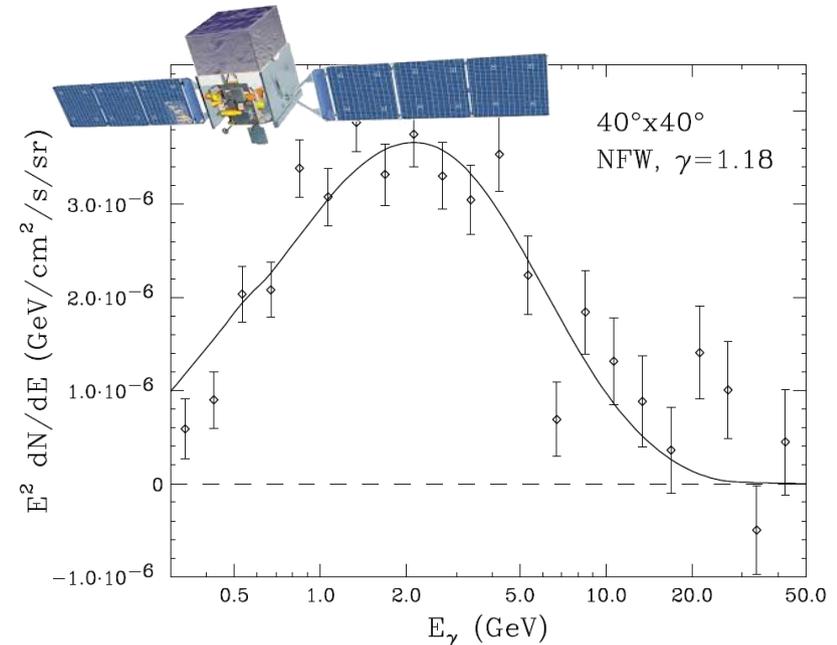
- Such a duality has been discussed before in other contexts
 - Cosmic-ray pion decay [Stecker, '71]
 - Particle production at colliders [Agashe, Franceschini, Kim, '12]
- It can also be exploited to distinguish certain dark matter models on the basis of indirect-detection data.

Application: Galactic Center Gamma-Ray Excess

- Observed excess of gamma rays coming from the Galactic Center.

[Hooper, Goodenough, '09]

- Roughly spherical emission region
- **Continuum feature** spanning the energy range $0.3 \text{ GeV} \lesssim E_\gamma \lesssim 50 \text{ GeV}$
- Peaked around $E_\gamma \sim 1 \text{ GeV}$



[Daylan et al., '14]

- Potential signal of annihilating/decaying **dark matter**...

- ...or millisecond pulsars

[Bartels, Krishnamurthy, Weniger, '15; Lee, Lisanti, Safdi, Slatyer, Xue, '15]

- ... or π^0 produced by collisions of cosmic-ray particles with interstellar gas

[Hooper, Goodenough, '10; Abazajian, Kaplinghat, '12; Gordon, Macias, '13]

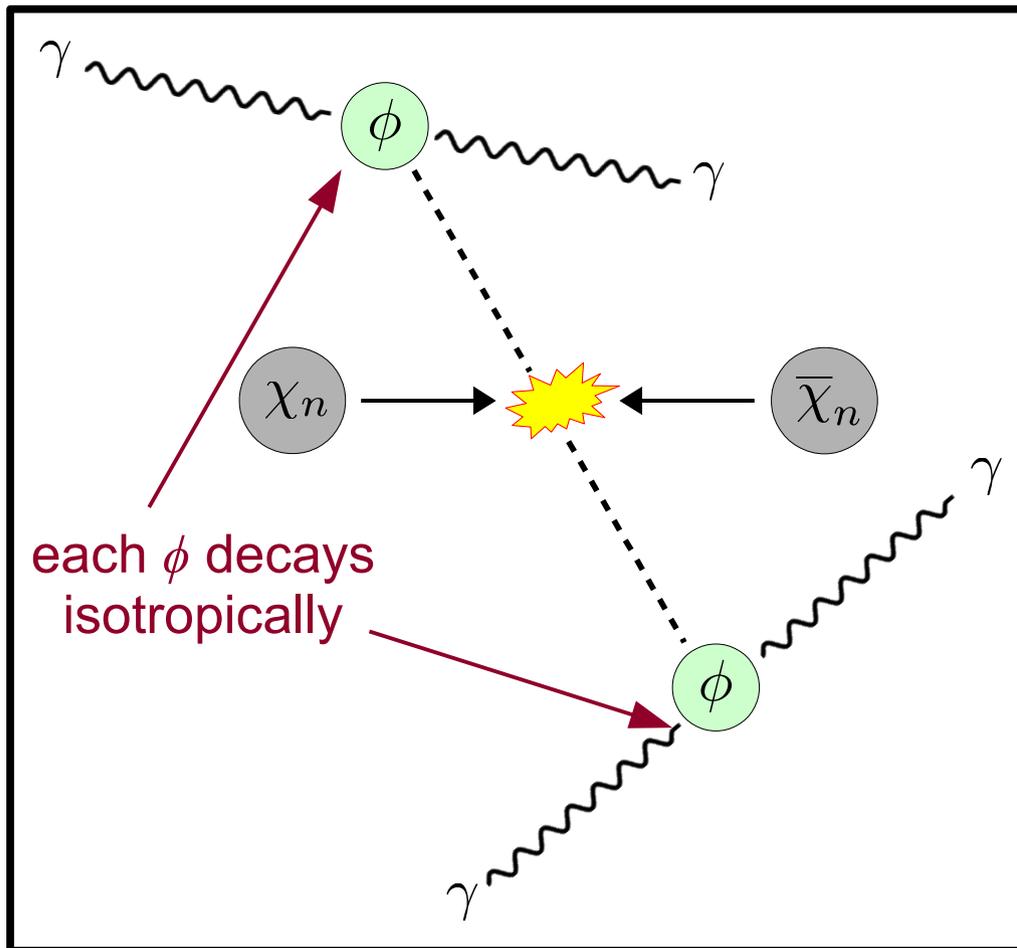
- ...or leptonic cosmic-ray bursts

[Petrovic, Serpico, Zaharijas, '14; Cholis, Evoli, Calore, Linden, Weniger, Hooper, '15]

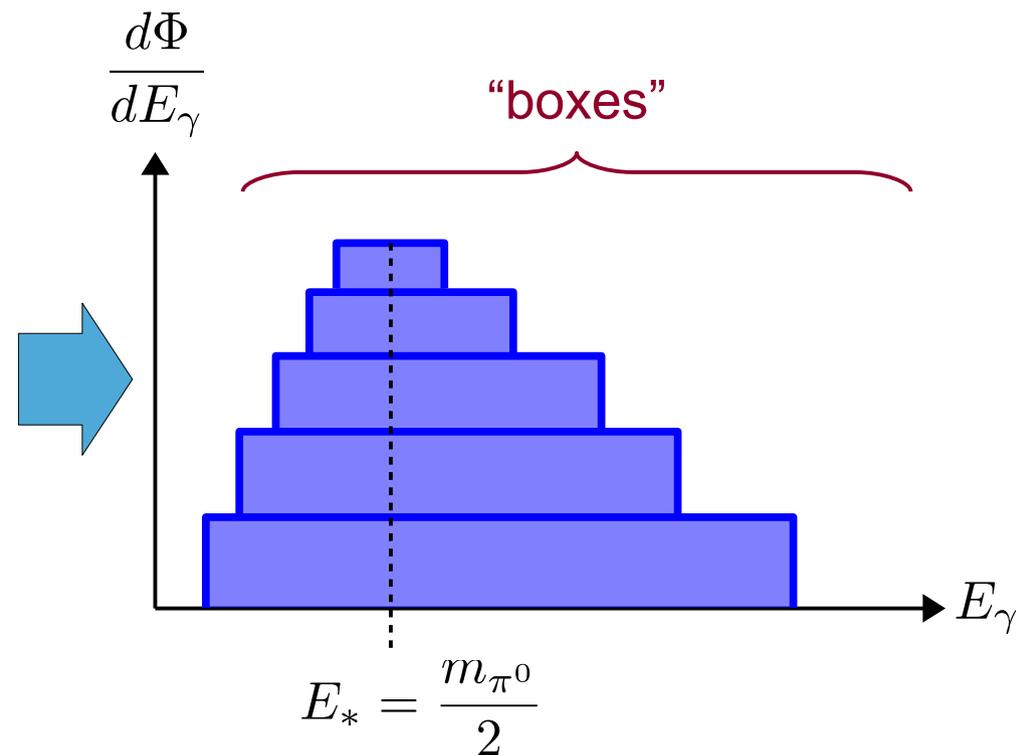
Decay Kinematics: Stacking Boxes

- Ensemble of DM particles χ_n with masses m_n , where $n = 0, 1, 2, \dots, N$.
- Each annihilates via $\chi_n \bar{\chi}_n \rightarrow \phi\phi \rightarrow 4\gamma$, where ϕ is a light scalar.
- The resulting photon spectrum is energy-dual around $E_* = m_\phi/2$

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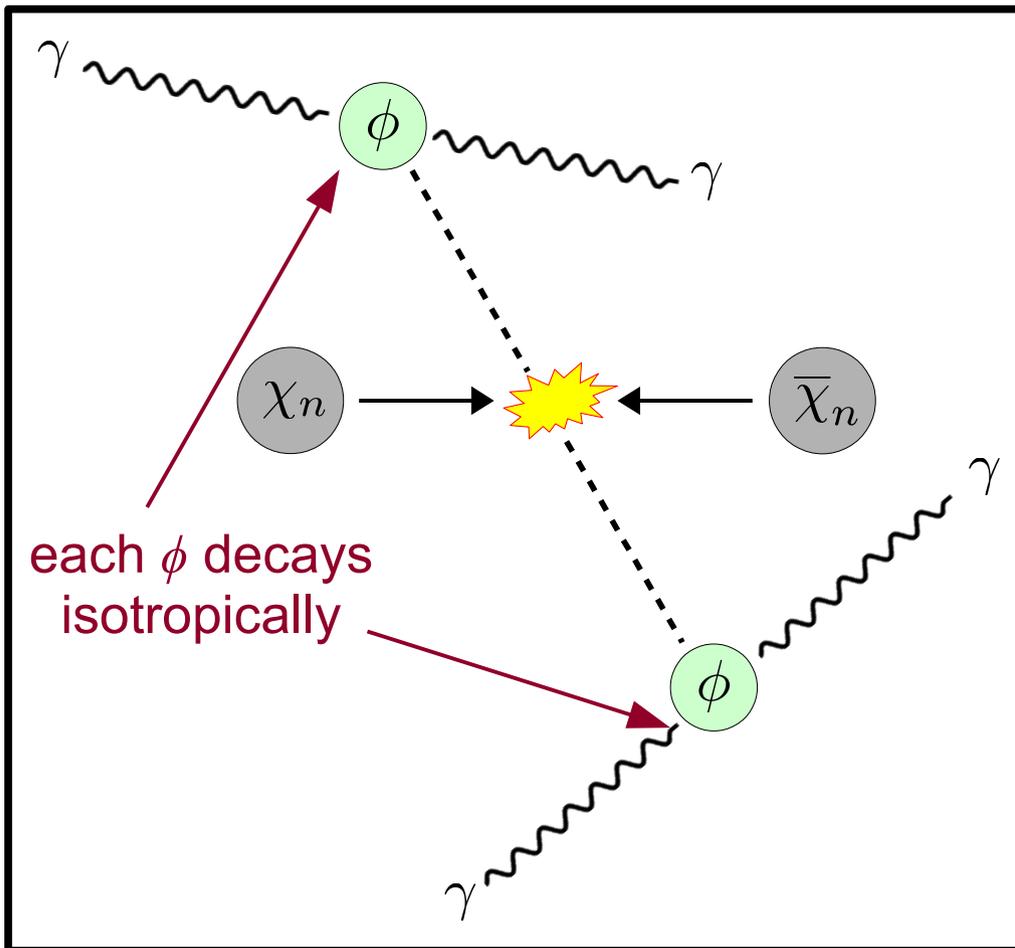
Photon Spectrum (Whole Ensemble)



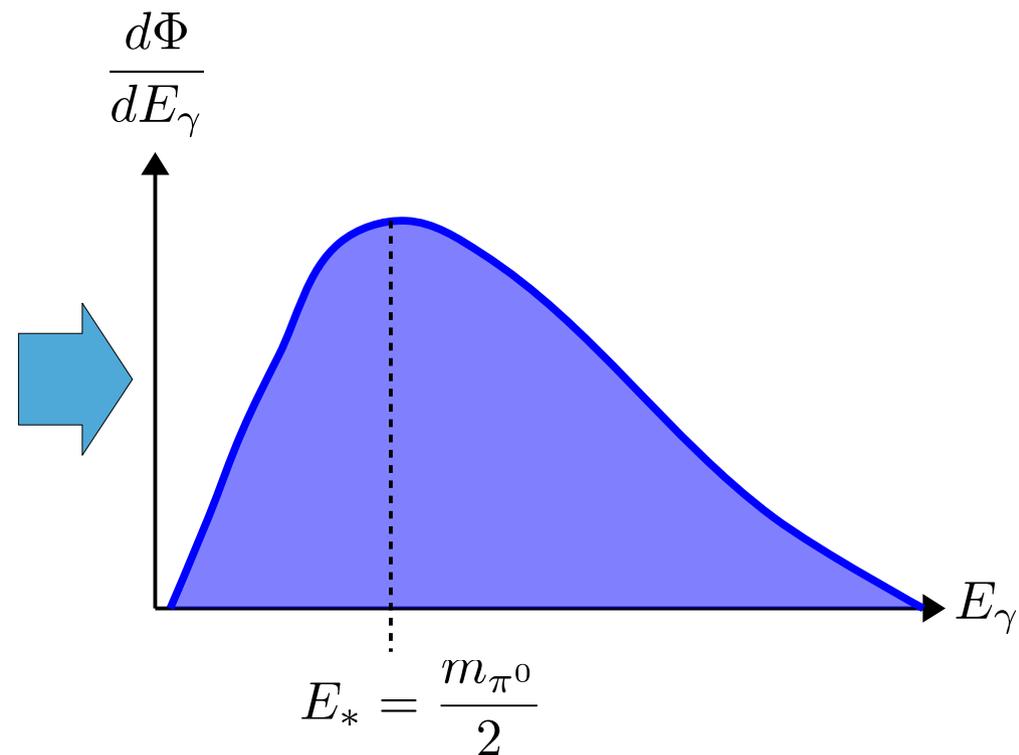
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Photon Spectrum (What We See)



Signal Spectrum

- For concreteness, we consider an annihilating DDM scenario in which the individual masses m_n and flux contributions Φ_n associated with the ensemble constituents scale as follows:

$$m_n = m_0 + n\Delta m$$

$$\Phi_n = \Phi_0 \left(\frac{m_n}{m_0} \right)^\xi$$



Closed-form solution for the signal spectrum!

- ... and here is is:

Euler beta functions

$$E_\gamma^2 \frac{d^2\Phi}{dE_\gamma d\Omega} = \frac{E_\gamma^2}{\Delta\Omega} \Xi \left(\frac{4E_*}{\sqrt{s_0}} \right)^\xi \left[B_{z_+} \left(-\frac{\xi}{2}, \frac{1}{2} \right) - B_{z_-} \left(-\frac{\xi}{2}, \frac{1}{2} \right) \right]$$

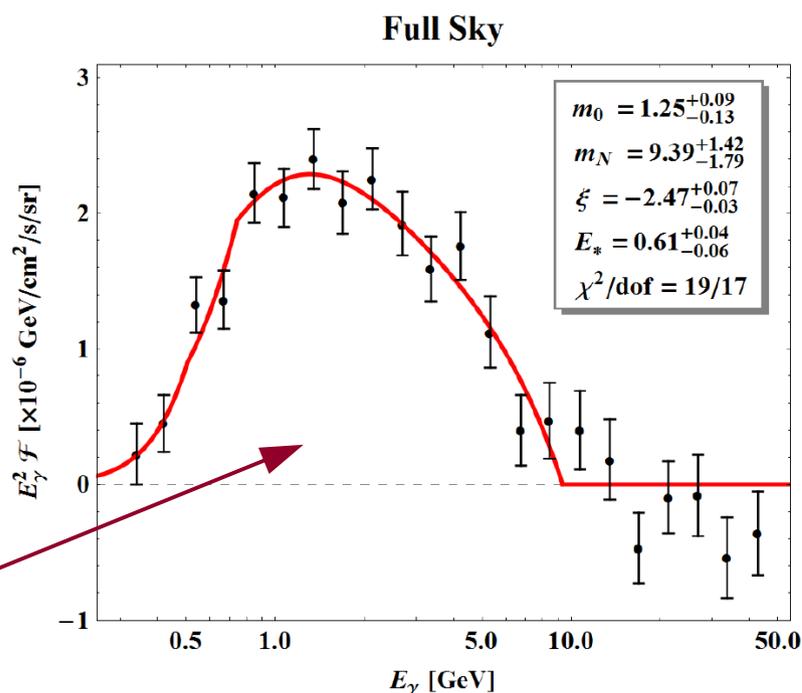
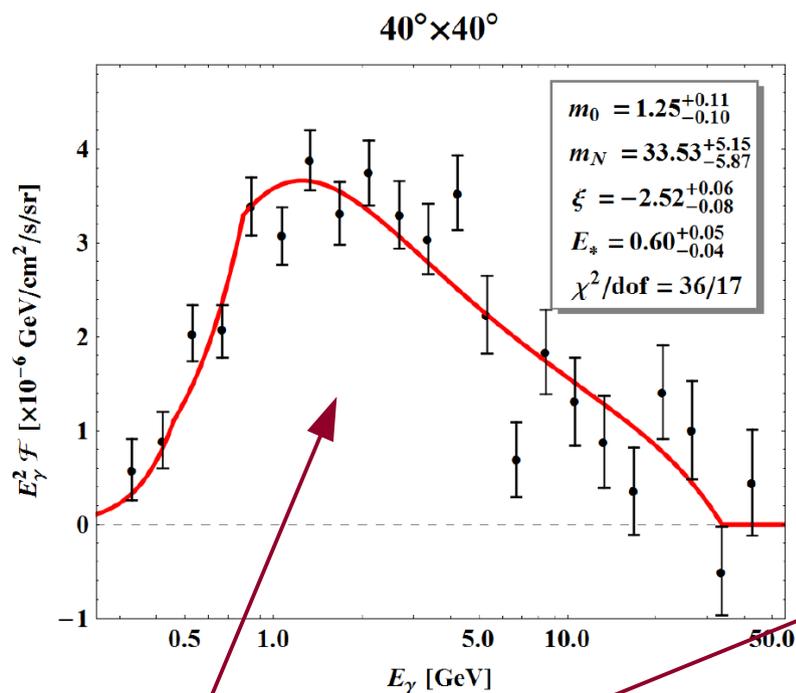
With:
$$\left\{ \begin{array}{l} z_+ = \max \left(\frac{8E_*^2}{m_N}, \min \left[\frac{8E_*^2}{m_0}, \frac{4}{(E_*/E_\gamma + E_\gamma/E_*)^2} \right] \right) \\ \Xi \equiv \frac{\Phi_0}{2\Delta m} \end{array} \right. , \quad z_- = \frac{8E_*^2}{m_N}$$

Fitting the Observed Excess

- We fit this spectrum to the residual signal spectrum of the observed GC gamma-ray excess two different ROI ($40^\circ \times 40^\circ$ and full sky).

Fit parameters:

$$\{m_0, m_N, \xi, E_*, \Xi\}$$



Good agreement with data and with each other (save for m_N)



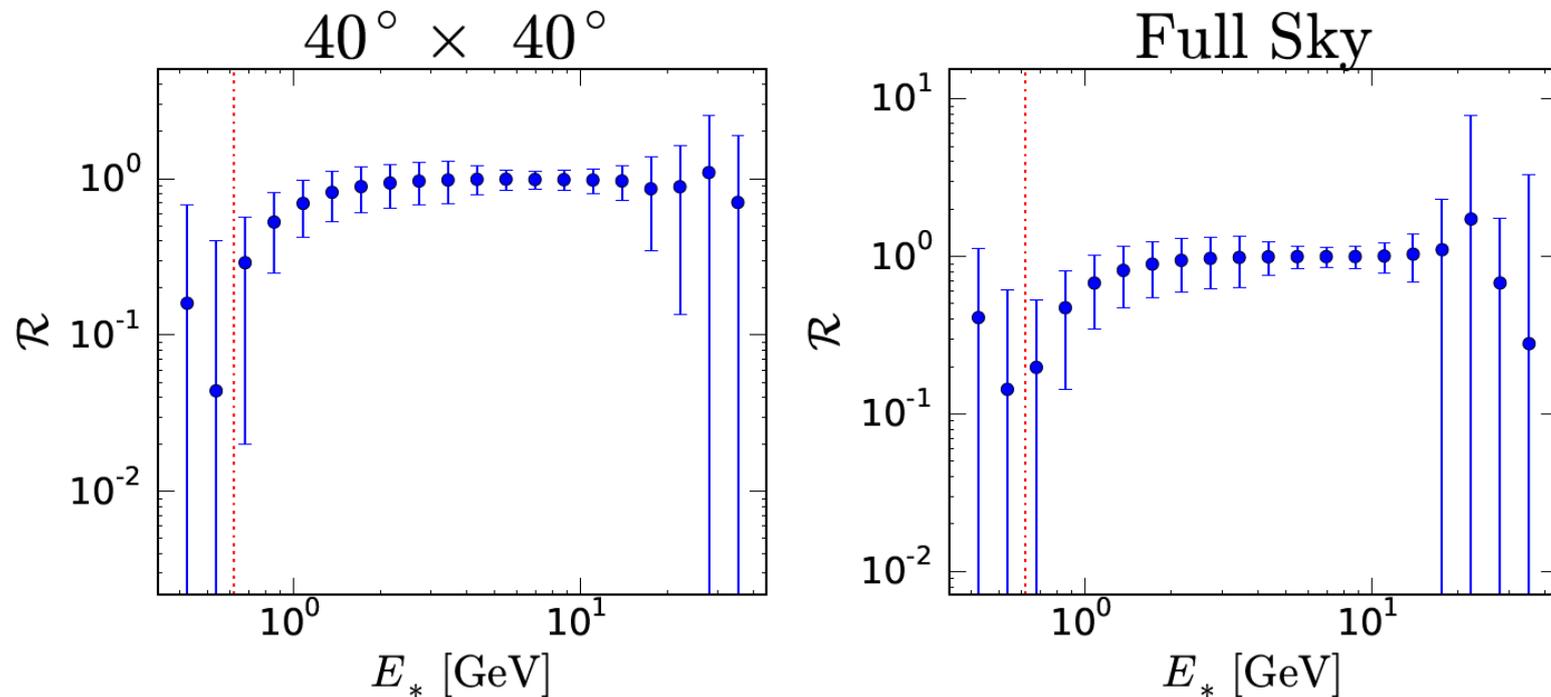
GC signal excess [Daylan et al., '14]



Best fit

But Is the GC Gamma-Ray Excess Really Energy-Dual?

- Very possibly... but at this point, it's a bit hard to tell.



$$\mathcal{R}(n_*) \equiv \frac{\sum_{n=1}^{n_{\max}} |\mathcal{F}_{n_*+n} - \mathcal{F}_{n_*-n}|}{\sum_{n=1}^{n_{\max}} |\mathcal{F}_{n_*+n} + \mathcal{F}_{n_*-n}|}$$

← antisymmetric part of the flux
← symmetric part of the flux

- Future gamma-ray telescopes such as GAMMA-400 or ASTROGAM should provide better **energy resolution**, better **statistics** for energies in the range $10 \text{ MeV} \lesssim E_\gamma \lesssim 1 \text{ GeV}$, or both.

Summary

- Extracting detailed information about the dark matter from indirect detection data is challenging – especially when the signal is a **continuum feature** rather than a narrow line.
- Nevertheless, techniques for extracting information from continuum features do exist. In this talk, we have highlighted two of them.
- **Correlations** between the shapes (and normalizations) of different spectral features produced via the same underlying physical process can
- Particular classes of dark-matter annihilation/decay processes give rise to spectral features invariant under $E_\gamma \rightarrow E_*^2/E_\gamma$. Such an **energy duality** can be used to distinguish between different dark-sector models.
- Indeed, an energy duality of this sort may even be lurking in the signal spectrum for the observed **Galactic-Center excess!**