

Probing Dark Matter Properties Using Dilepton Distributions at the LHC

(Arxiv:1706.XXXX)

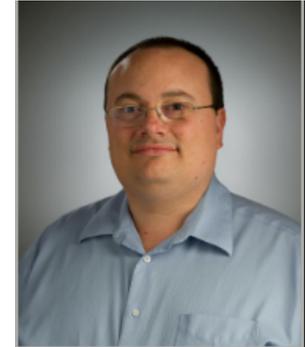
Rodolfo M. Capdevilla
University of Notre Dame
Particle Physics Group



Adam Martin
Assistant Professor
University of Notre Dame



Nirmal Raj
Postdoctoral Research Associate
University of Notre Dame



Antonio Delgado
Associate Professor
University of Notre Dame

Conclusions

- Besides jet+MET: Search for DM from interference effects e.g. Dilepton kinematical distributions (models with t-channel mediators).

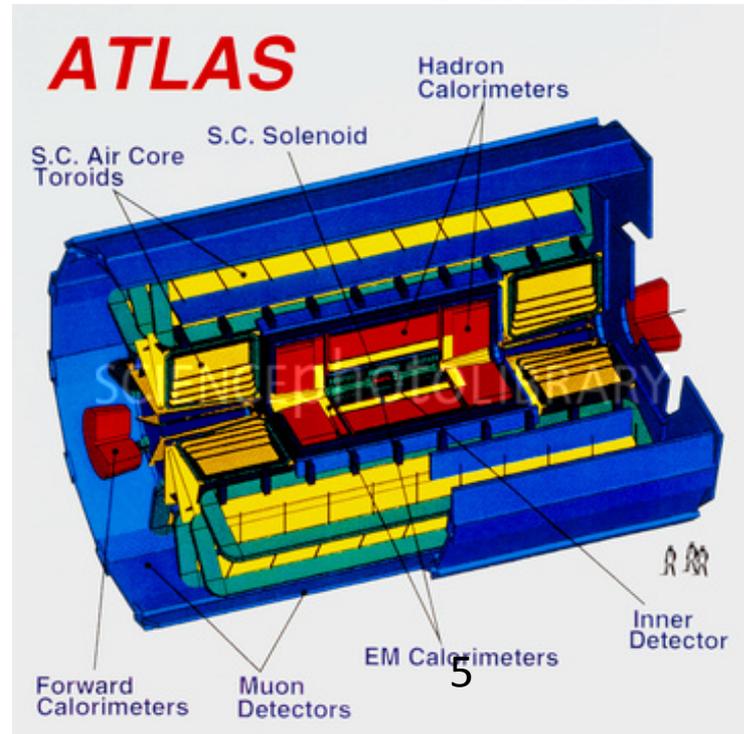
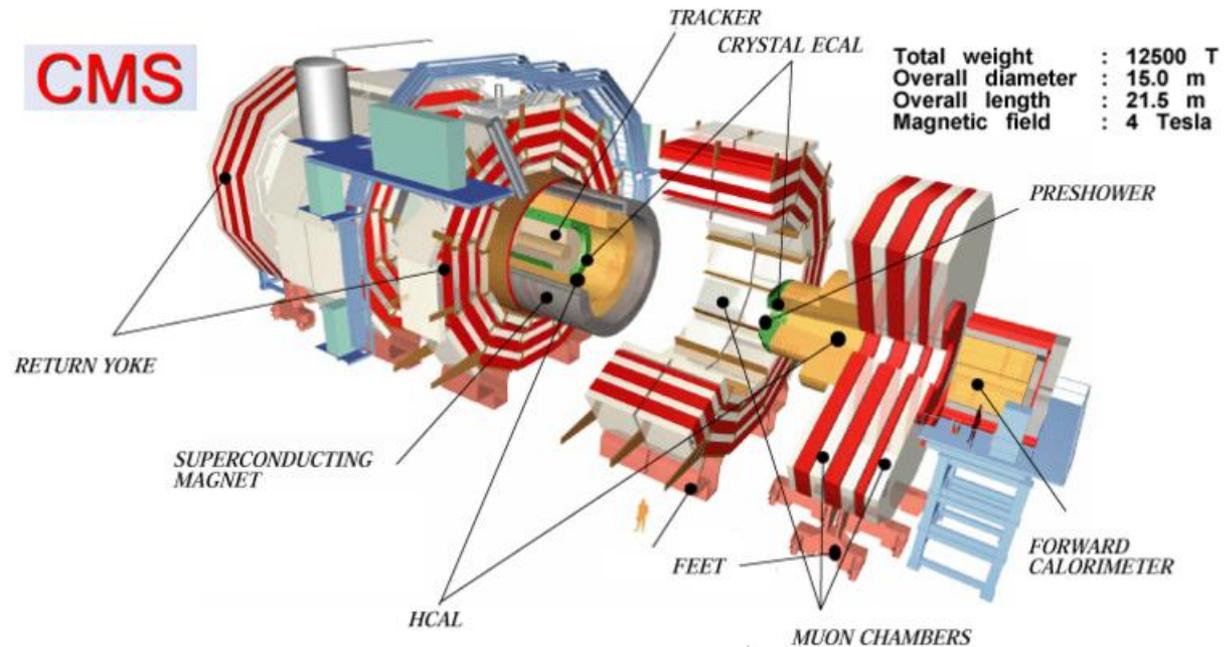
Conclusions

- Besides jet+MET: Search for DM from interference effects e.g. Dilepton kinematical distributions (models with t-channel mediators).
- We also get information about DM properties e.g.
 - Dilepton invariant mass: DM mass (fermionic), DM spin (almost degenerate DM-mediators).
 - Dilepton angular distribution: SM chiralities (mediators' quantum numbers).

Conclusions

- Besides jet+MET: Search for DM from interference effects e.g. Dilepton kinematical distributions (models with t-channel mediators).
- We also get information about DM properties e.g.
 - Dilepton invariant mass: DM mass (fermionic), DM spin (almost degenerate DM-mediators).
 - Dilepton angular distribution: SM chiralities (mediators' quantum numbers).
- Dilepton distributions provide competitive bounds with those from jets+MET and Direct Detection searches.

The LHC:



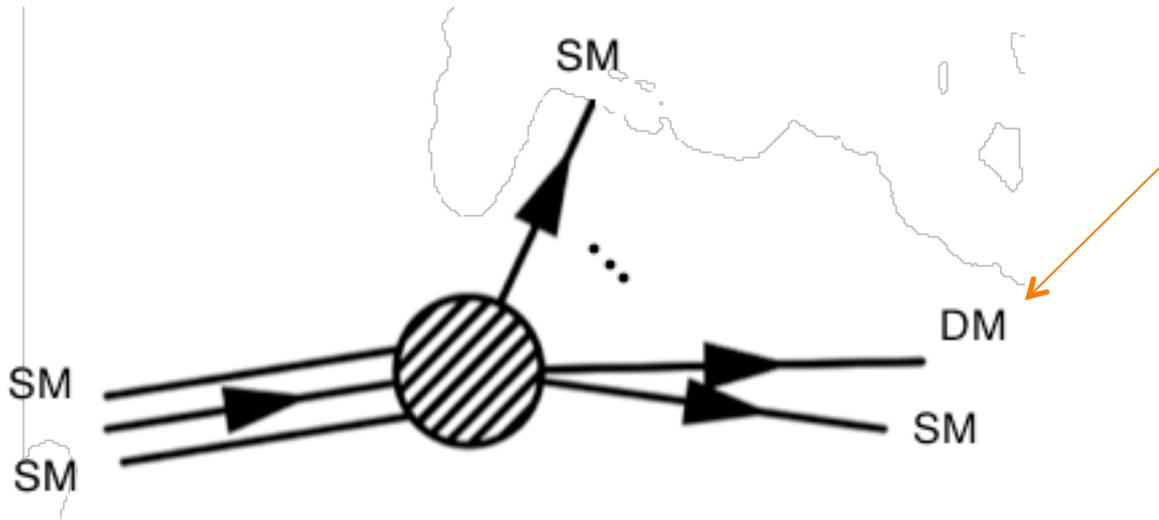
- Energy Frontier:
($E_{\text{CM}} = 13 \text{ TeV}$)
- Sensitivity Frontier:
($\sigma \approx 10^{-4} \text{ pb}$)

What can the LHC tell us about Dark Matter?

1. Can we discover DM?

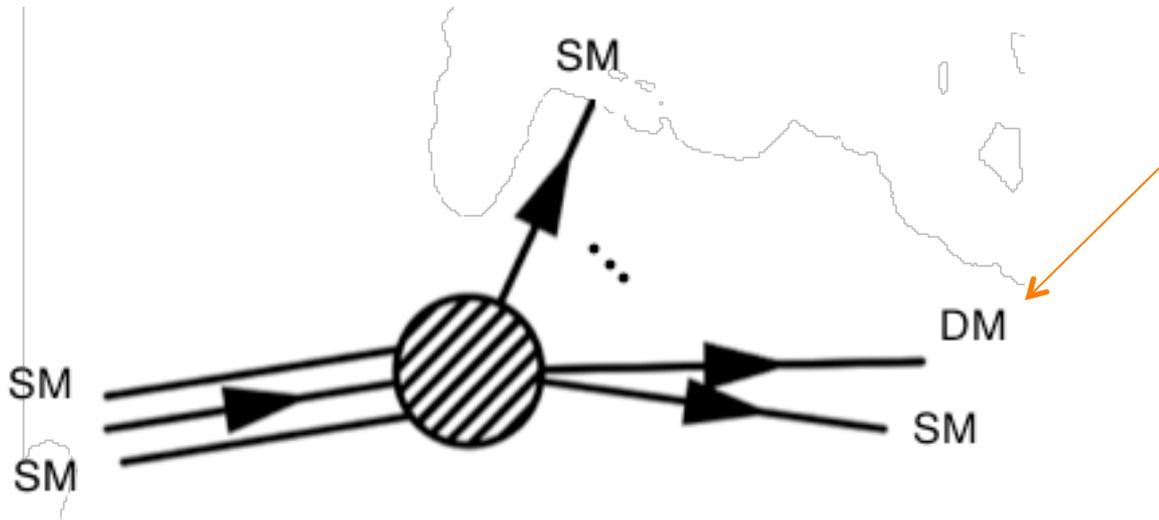
2. Can we learn something about DM properties?

Jets + MET Searches



*If DM is produced,
we have Missing
Transverse Energy
(MET)*

Jets + MET Searches



*If DM is produced,
we have Missing
Transverse Energy
(MET)*

Search for physics beyond the standard model in events with two leptons of same sign, missing transverse momentum, and jets in proton-proton collisions at $\sqrt{s} = 13$ TeV

CMS Collaboration

24 April 2017

Submitted to *Eur. Phys. J. C*

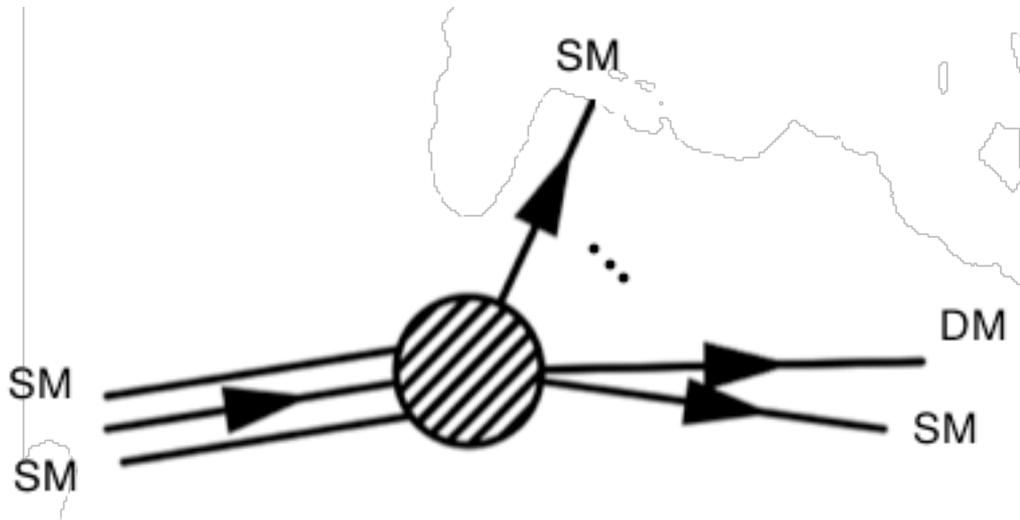
Search for supersymmetry in multijet events with missing transverse momentum in proton-proton collisions at 13 TeV

CMS Collaboration

25 April 2017

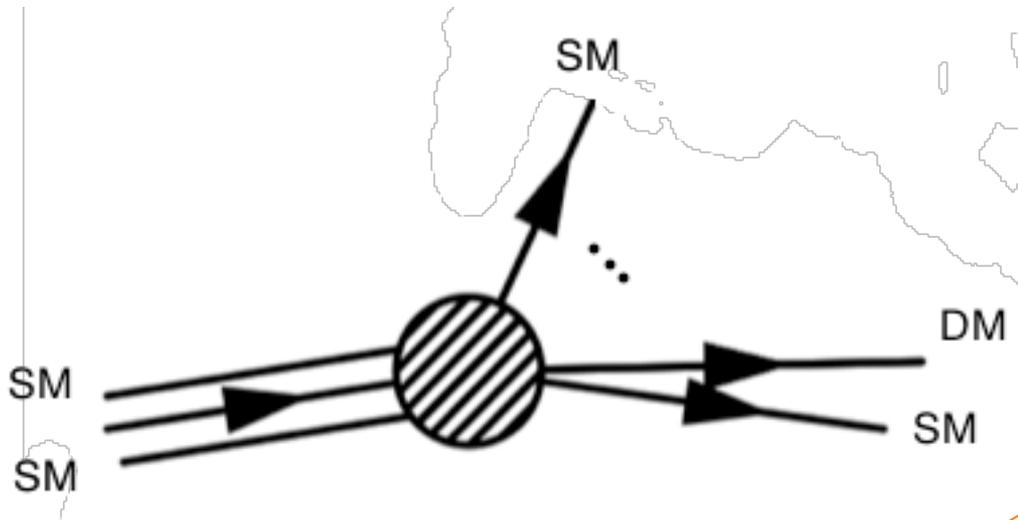
Submitted to *Phys. Rev. D*

Jets + MET Searches

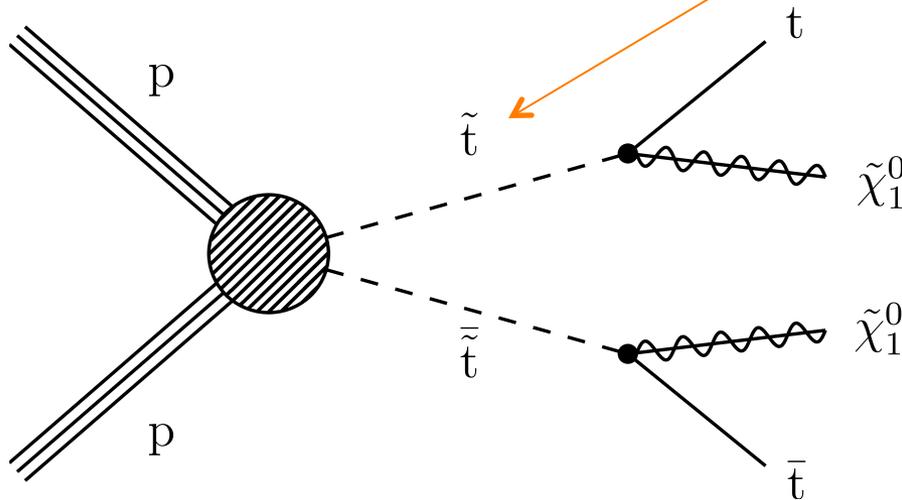


But, what happens when DM is produced with low energy (low MET)?

Jets + MET Searches

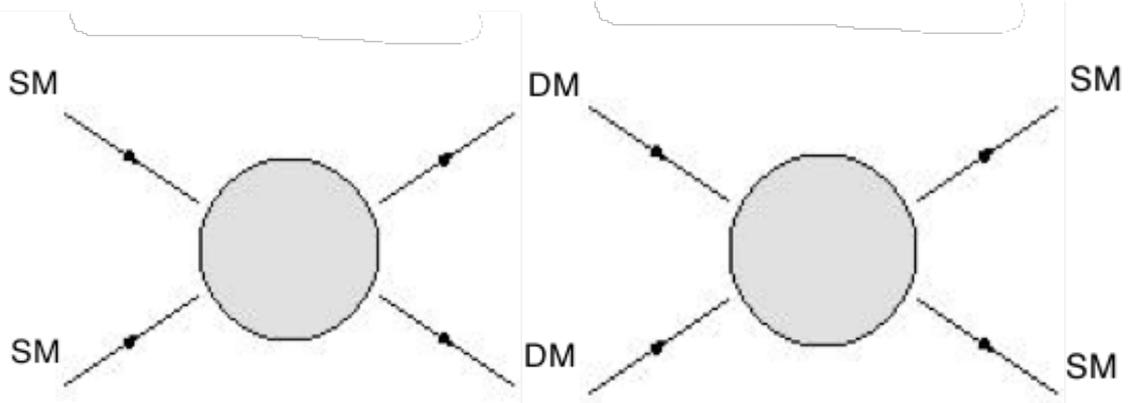
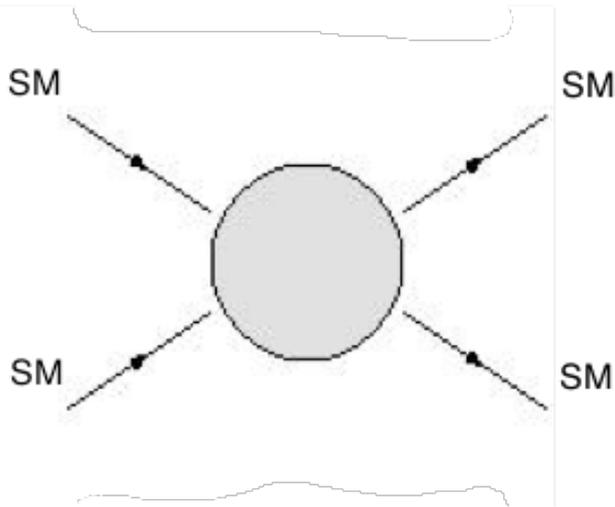


*e.g.
Intermediate
state nearly
degenerate with
DM*



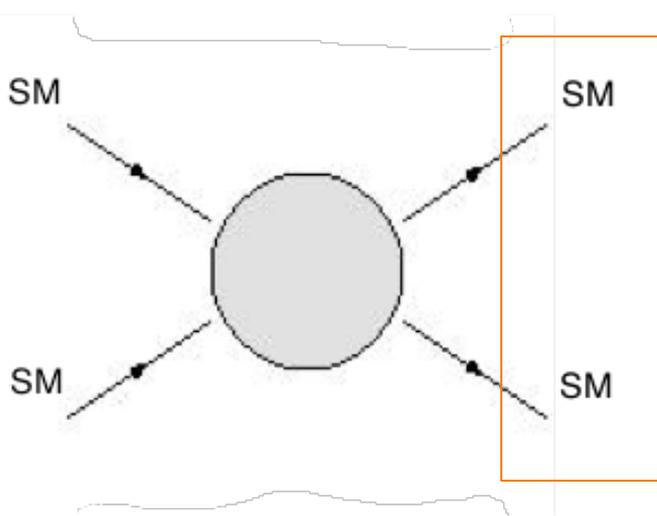
Can we perform other types of searches?

How about interference effects?

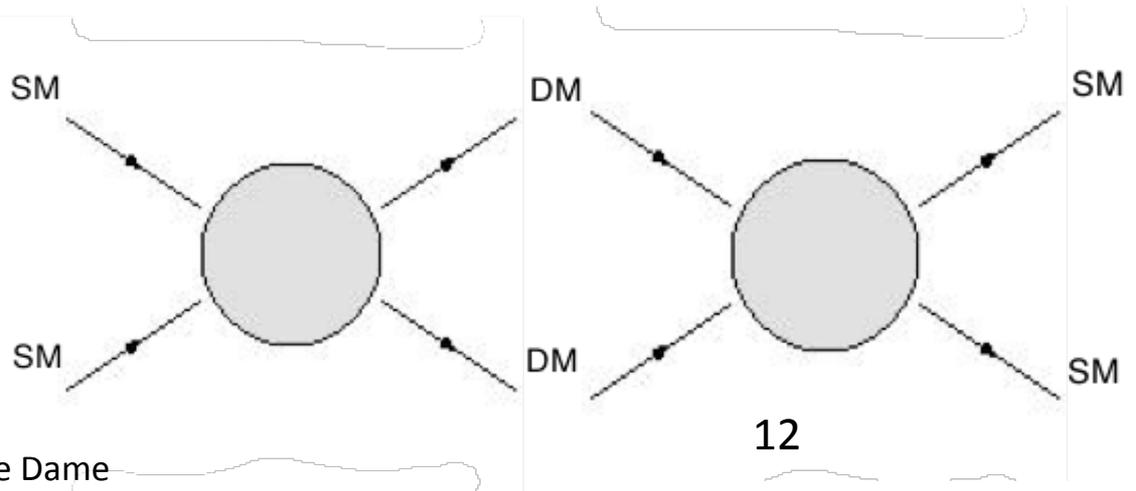


Can we perform other types of searches?

How about interference effects?

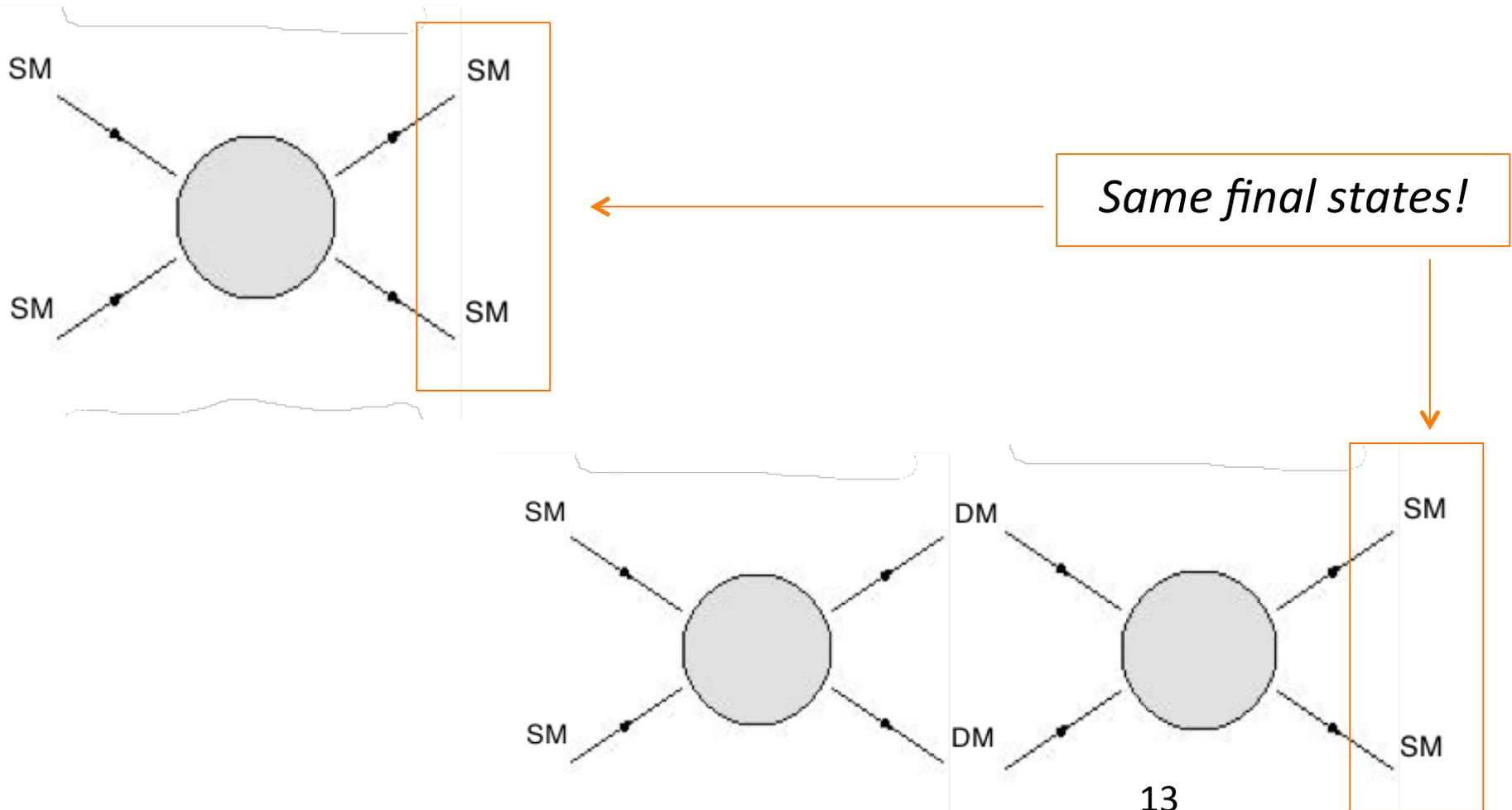


*Very well understood
final states!*

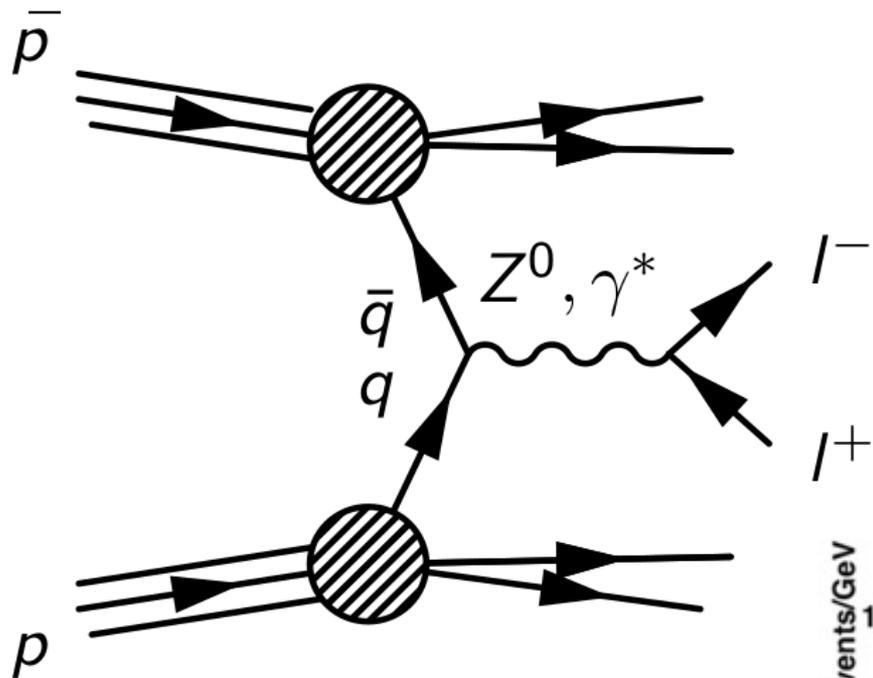


Can we perform other types of searches?

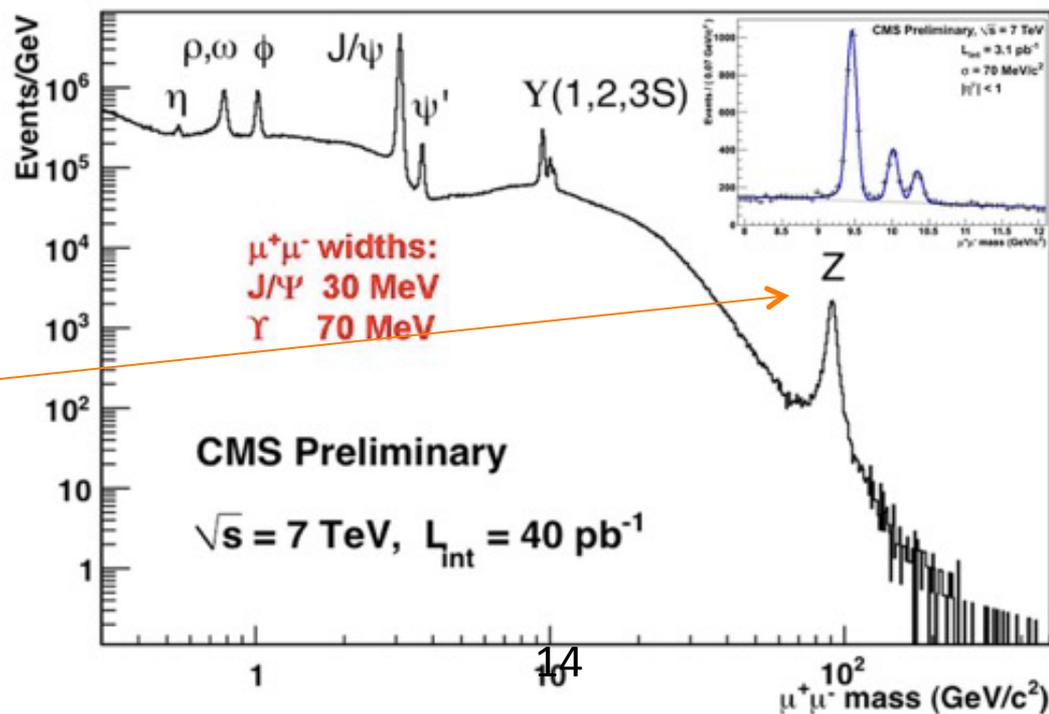
How about interference effects?



Dilepton Production

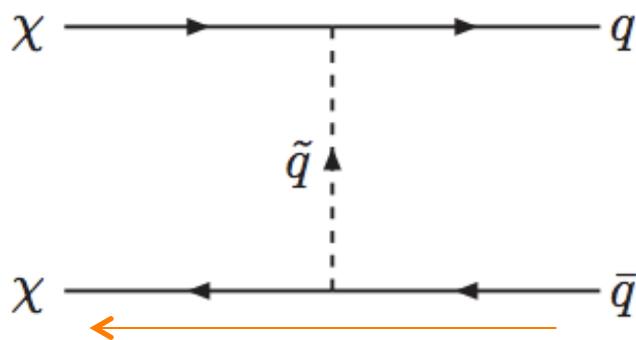
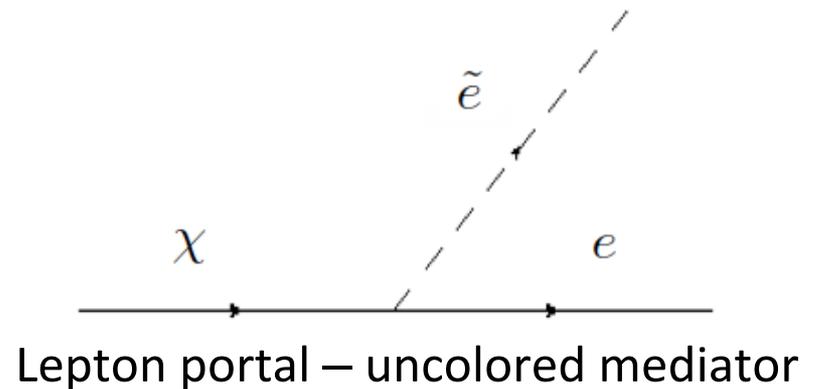
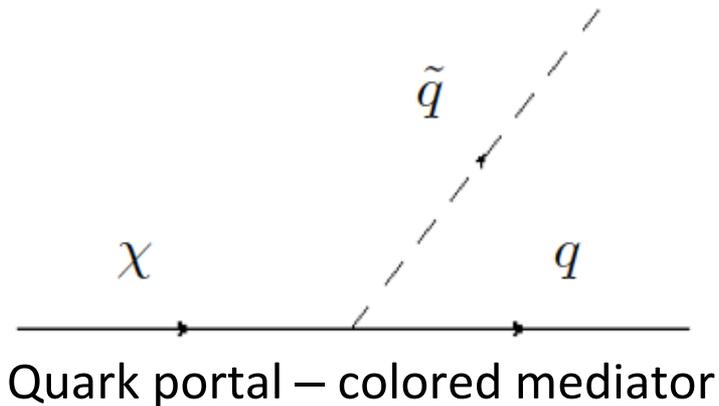


*High rates, low uncertainties
(Historically important discovery mode!)*

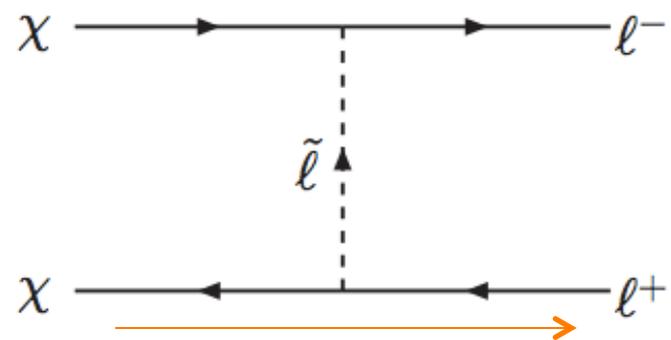


How can DM produce dilepton signals?

- DM with t-channel mediators:



DM production in pp collider

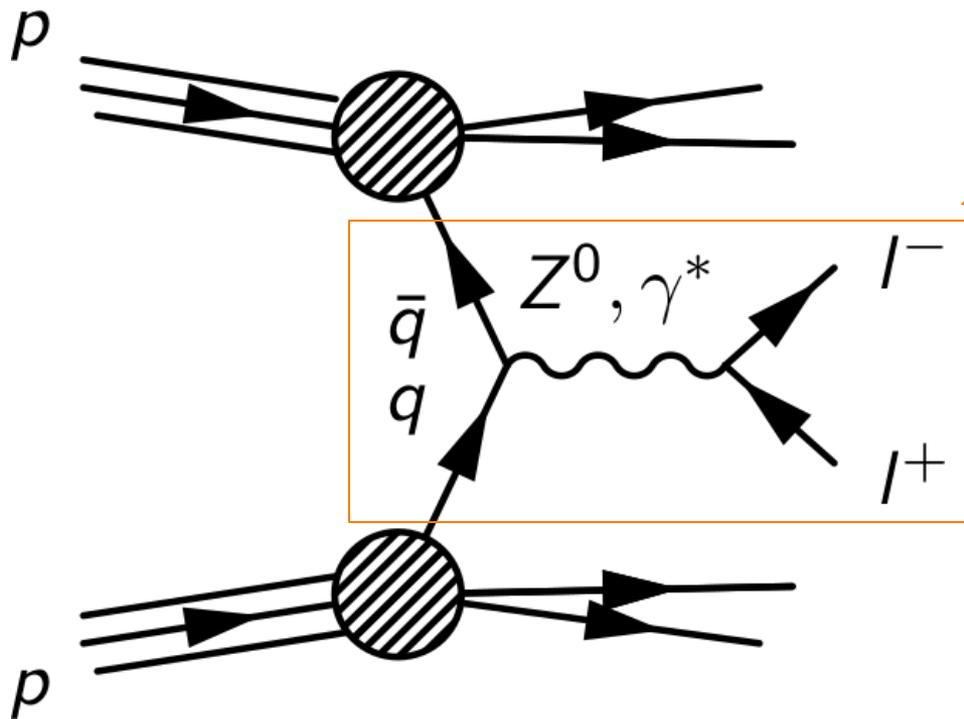


Dilepton production

Dilepton Distributions at the LHC

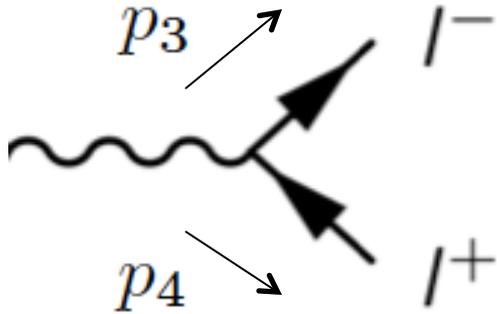
(what do we measure?)

- Drell-Yan production



*Partonic scattering
amplitude*

1) Dilepton Invariant Mass

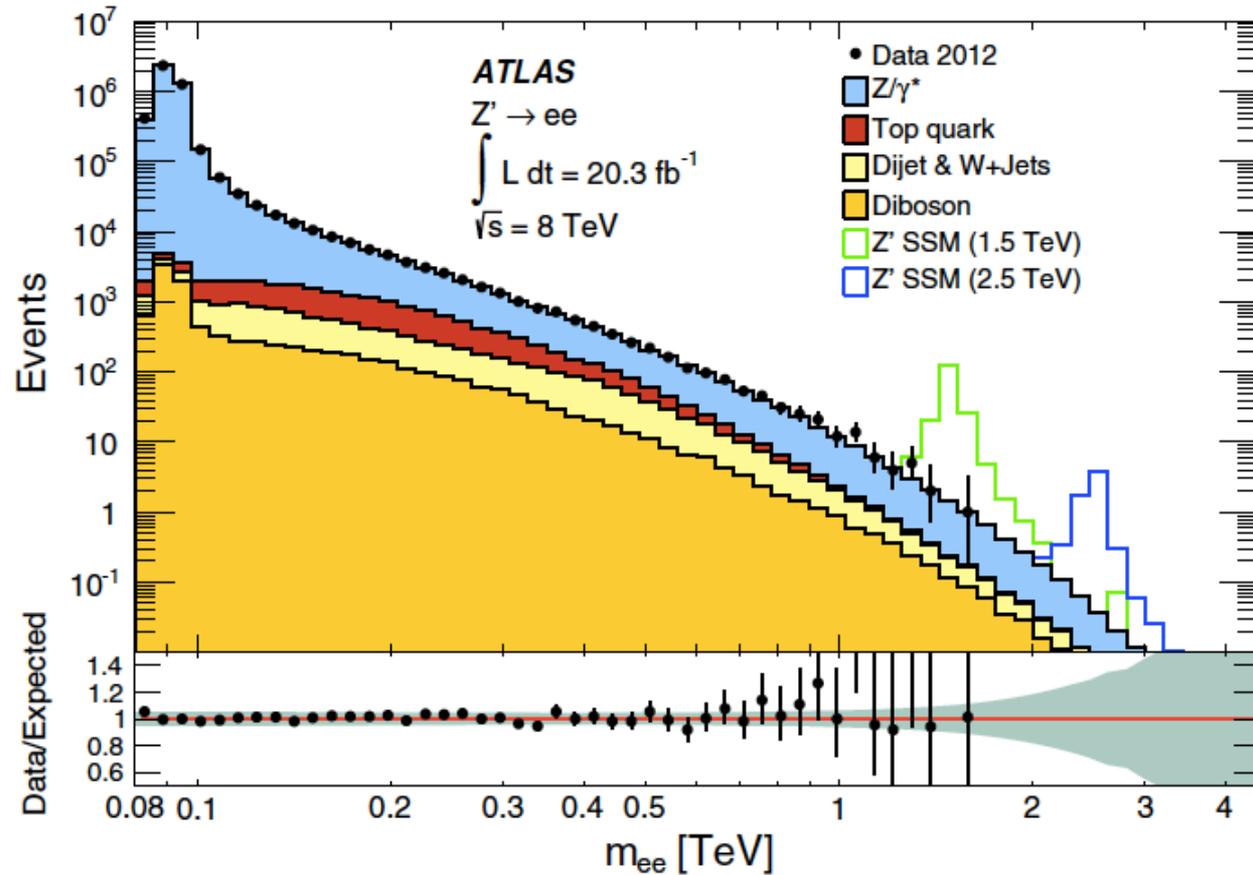


$$\hat{s} = (p_3 + p_4)^2$$

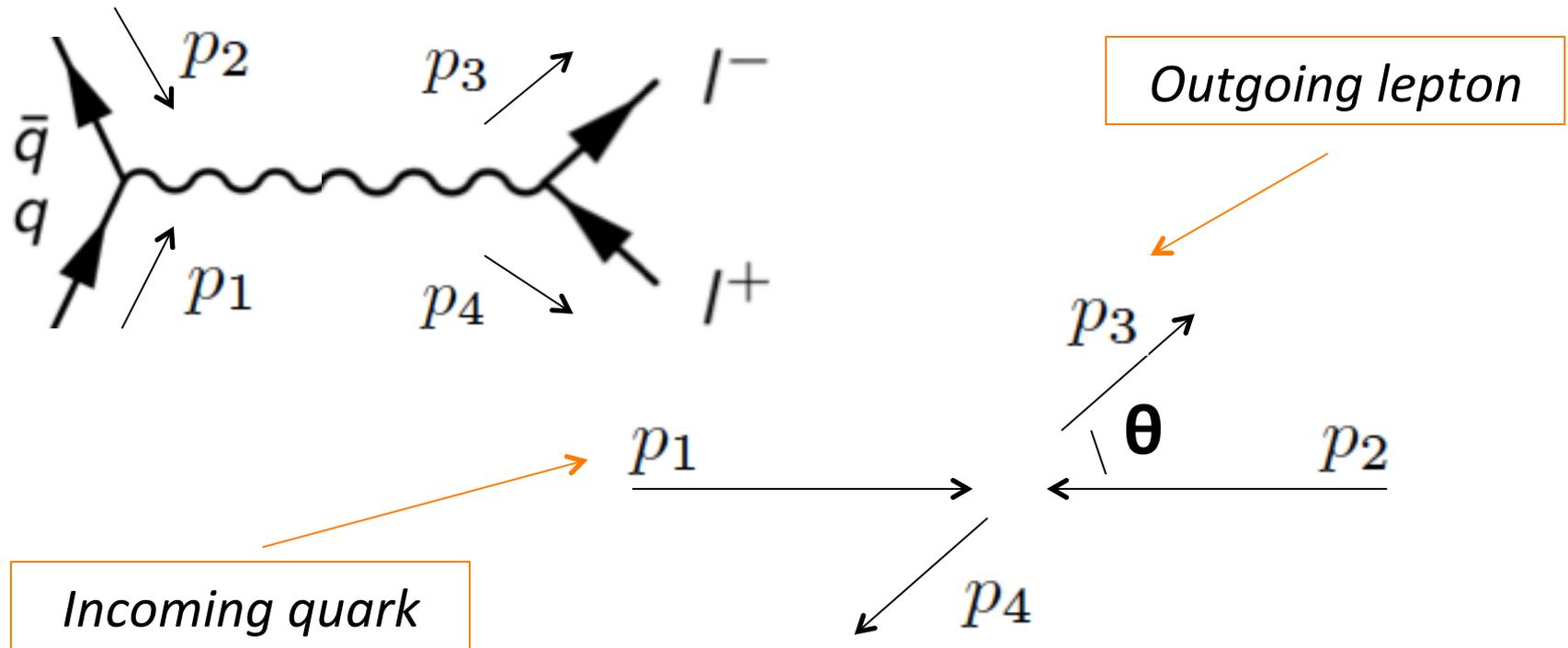
$$m_{ll} = \sqrt{\hat{s}}$$



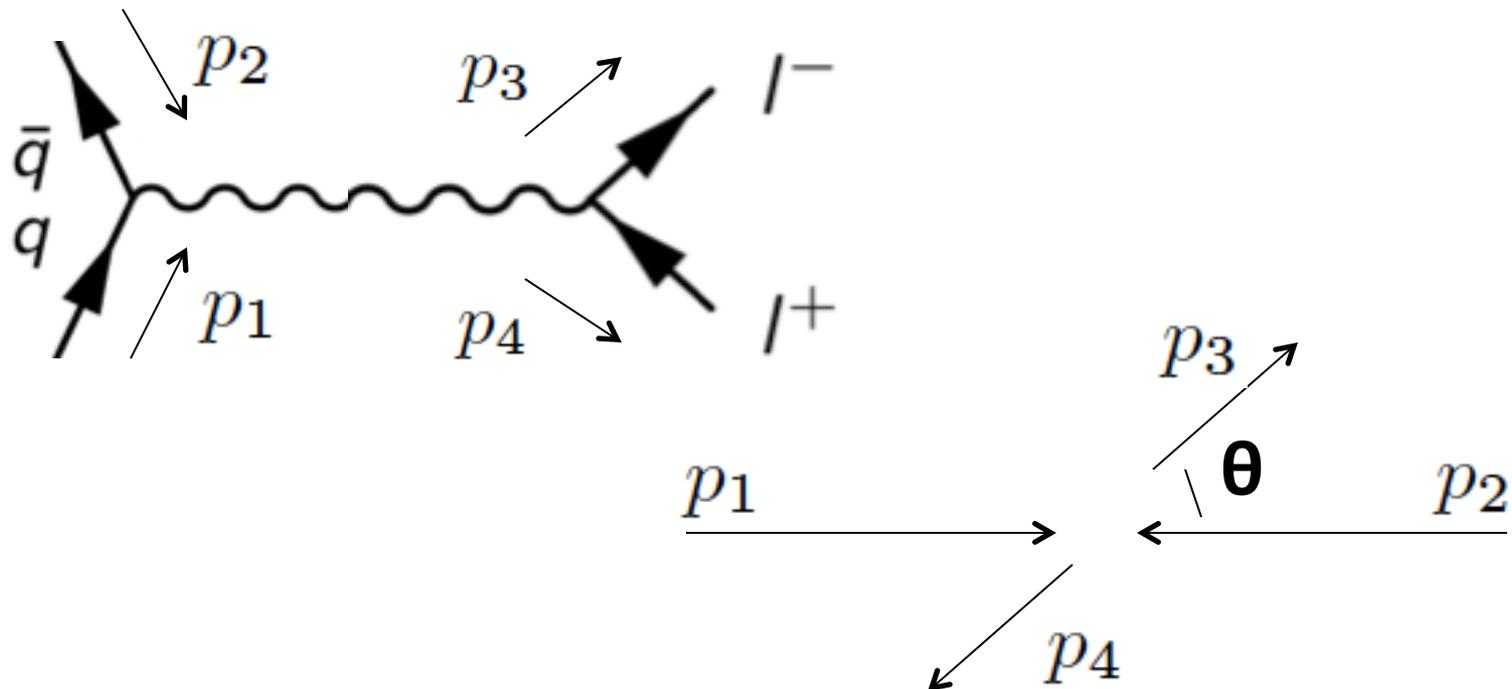
Dilepton invariant mass = C.M. energy



2) Dilepton Angular Distribution

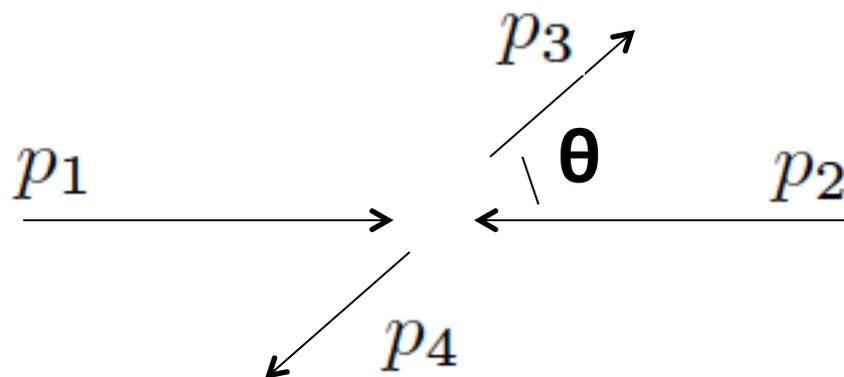
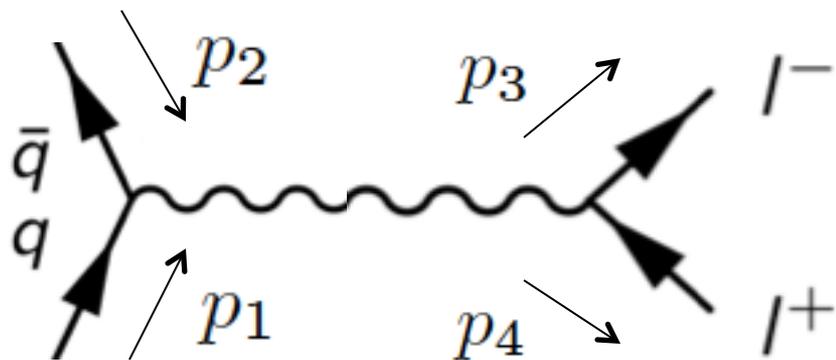


Dilepton Angular Distribution



*But, in pp collisions
we do not know the direction of the
incoming quark!*

Dilepton Angular Distribution



proton level

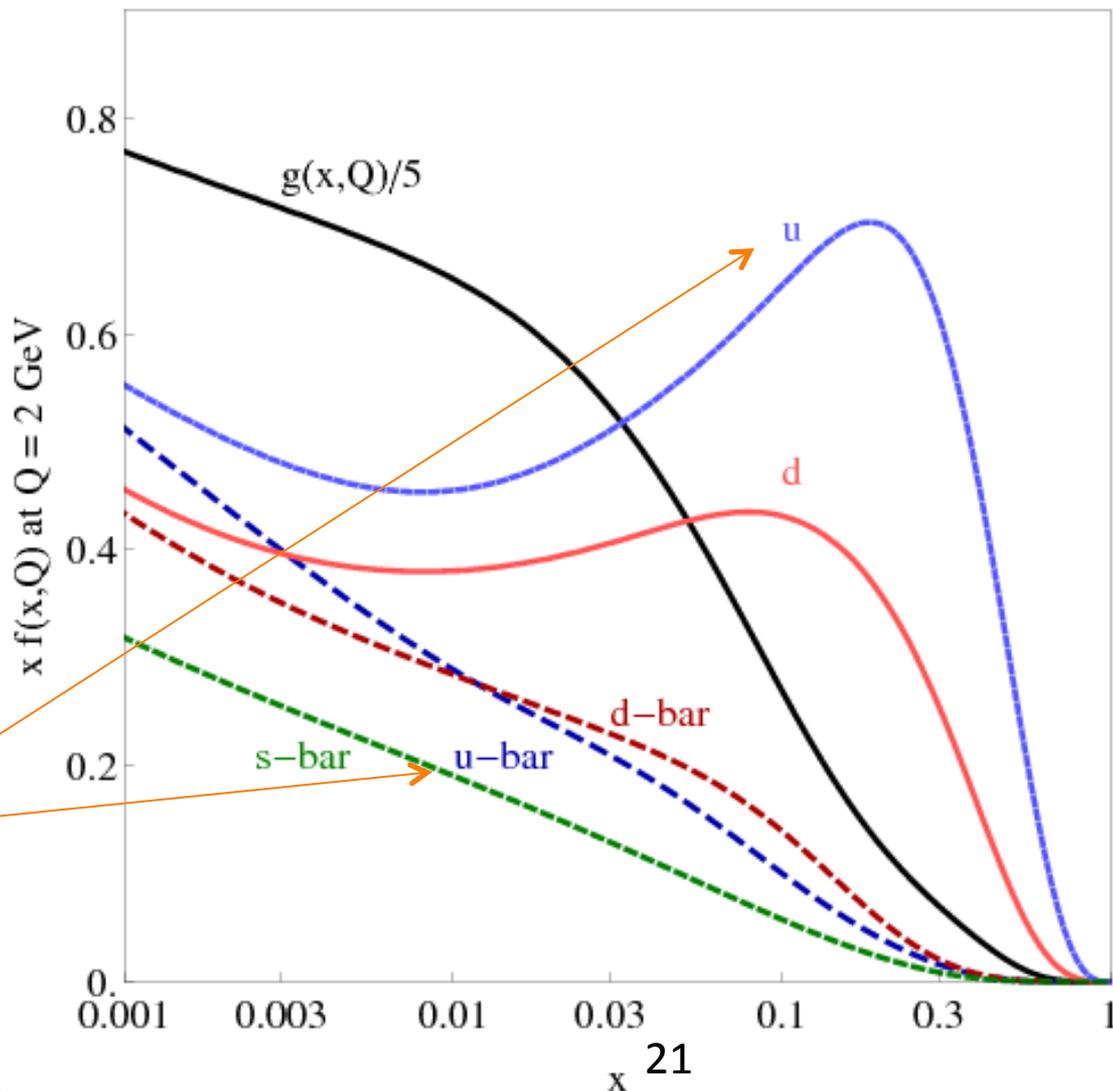
*parton distribution
functions (PDF)*

parton level

$$\frac{d\sigma}{dC\theta} = \int dx_1 dx_2 [f_q(x_1) f_{\bar{q}}(x_2) + f_q(x_2) f_{\bar{q}}(x_1)] \frac{d\hat{\sigma}}{dC\theta}$$

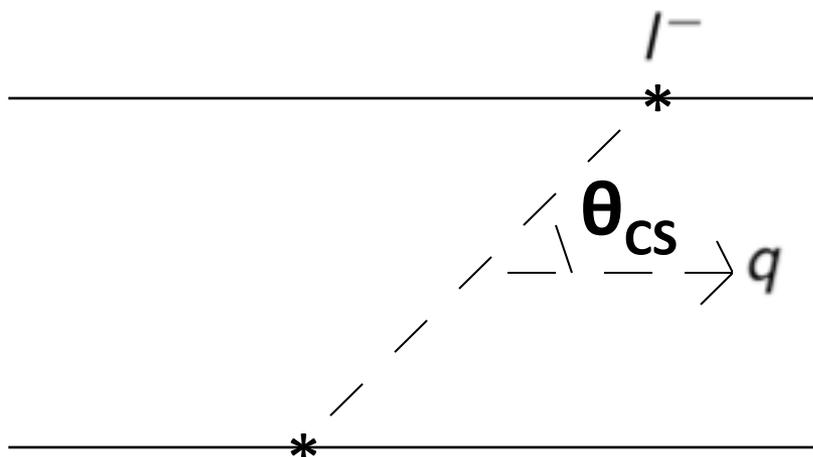
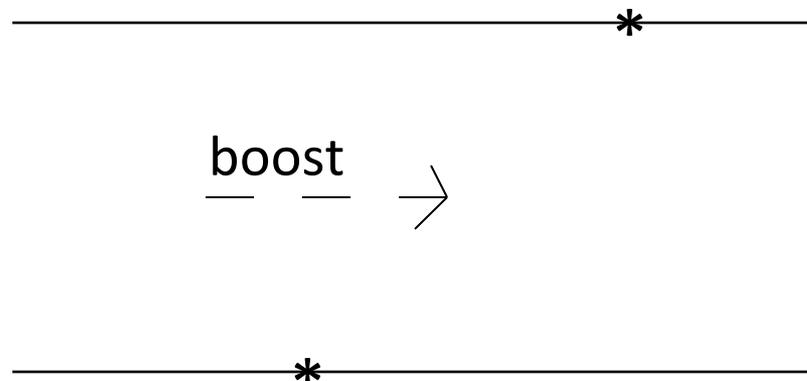
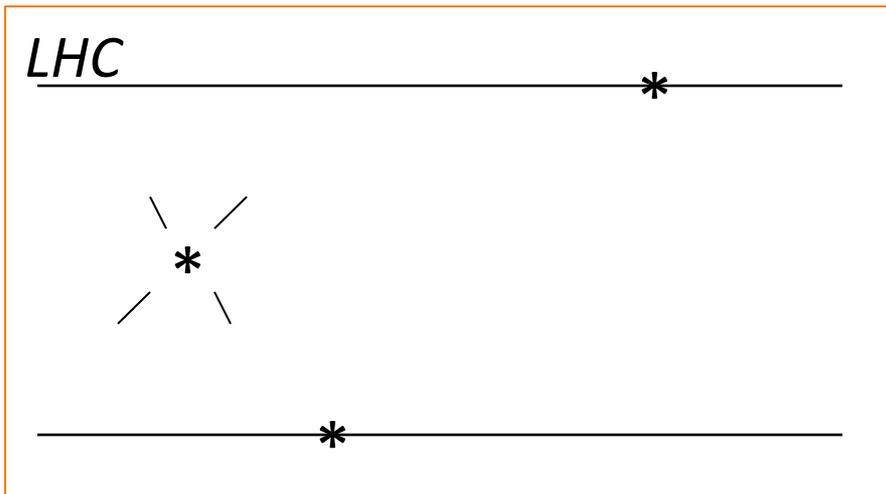
Parton Distribution Functions

CT14 NNLO

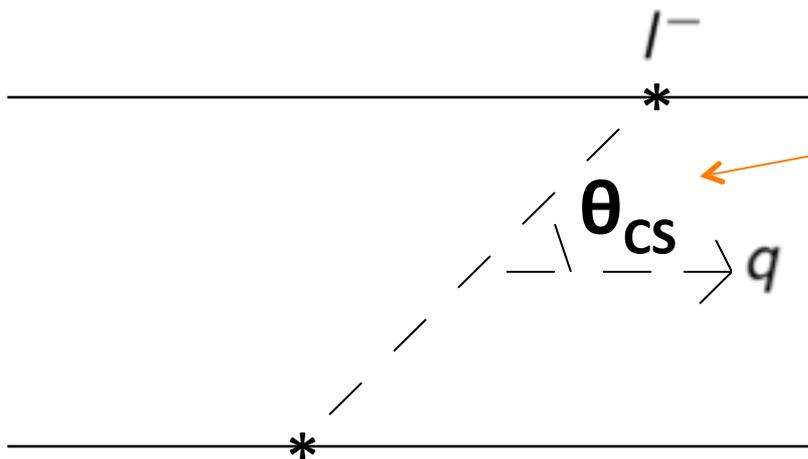
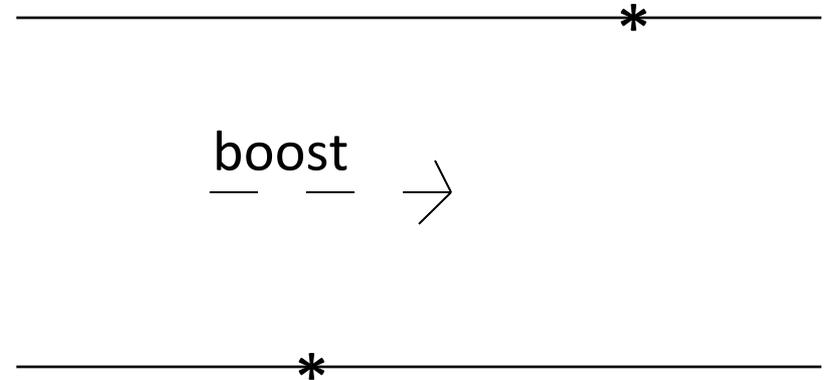
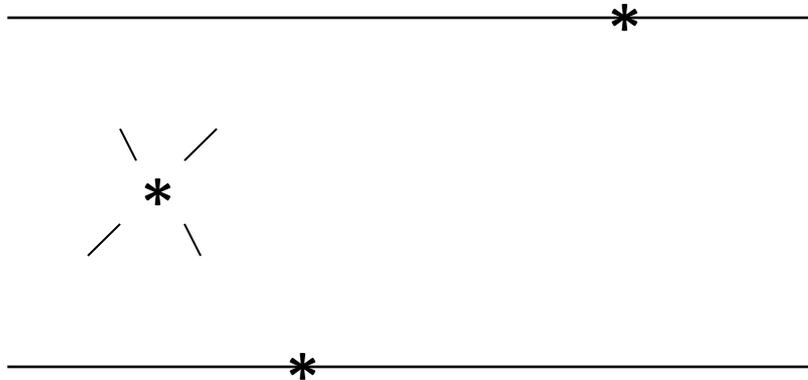


IMPORTANT! the PDF are higher for q than for $q\text{-bar}$

Collin-Soper Frame

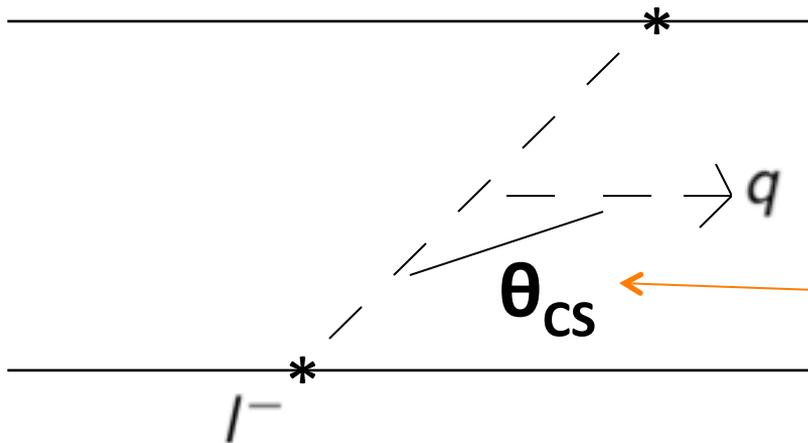
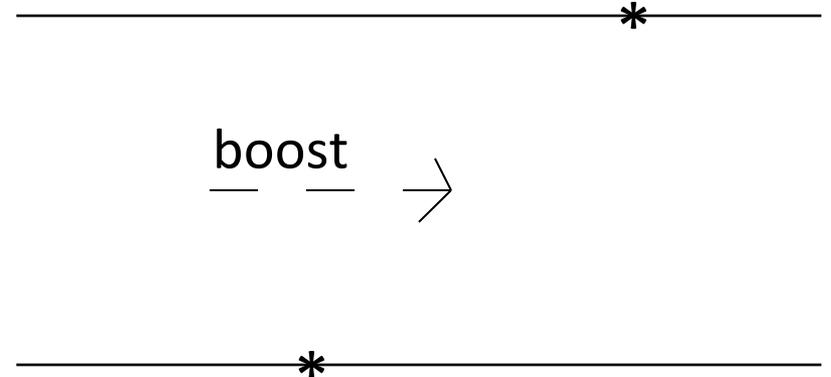
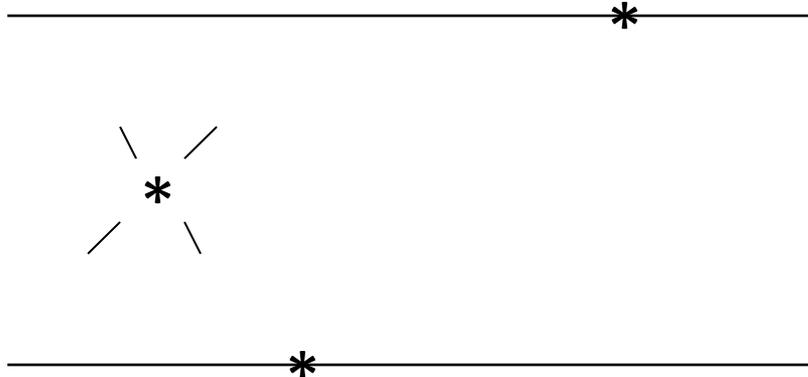


Collin-Soper Frame



*This is a
forward event!*

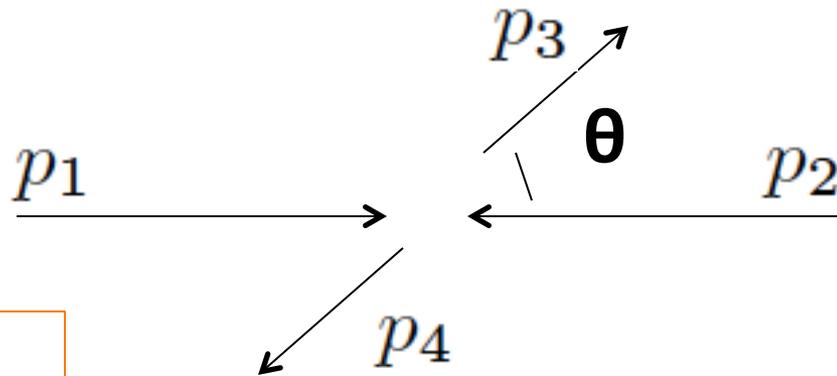
Collin-Soper Frame



*This is a
backward event!*

How can we calculate θ_{CS} ?

$$\frac{d\sigma}{dC\theta} = \int dx_1 dx_2 [f_q(x_1) f_{\bar{q}}(x_2) + f_q(x_2) f_{\bar{q}}(x_1)] \frac{d\hat{\sigma}}{dC\theta}$$



Split integration:
 $(X_1 > X_2)$ and $(X_1 < X_2)$

Here quark carries

X_1

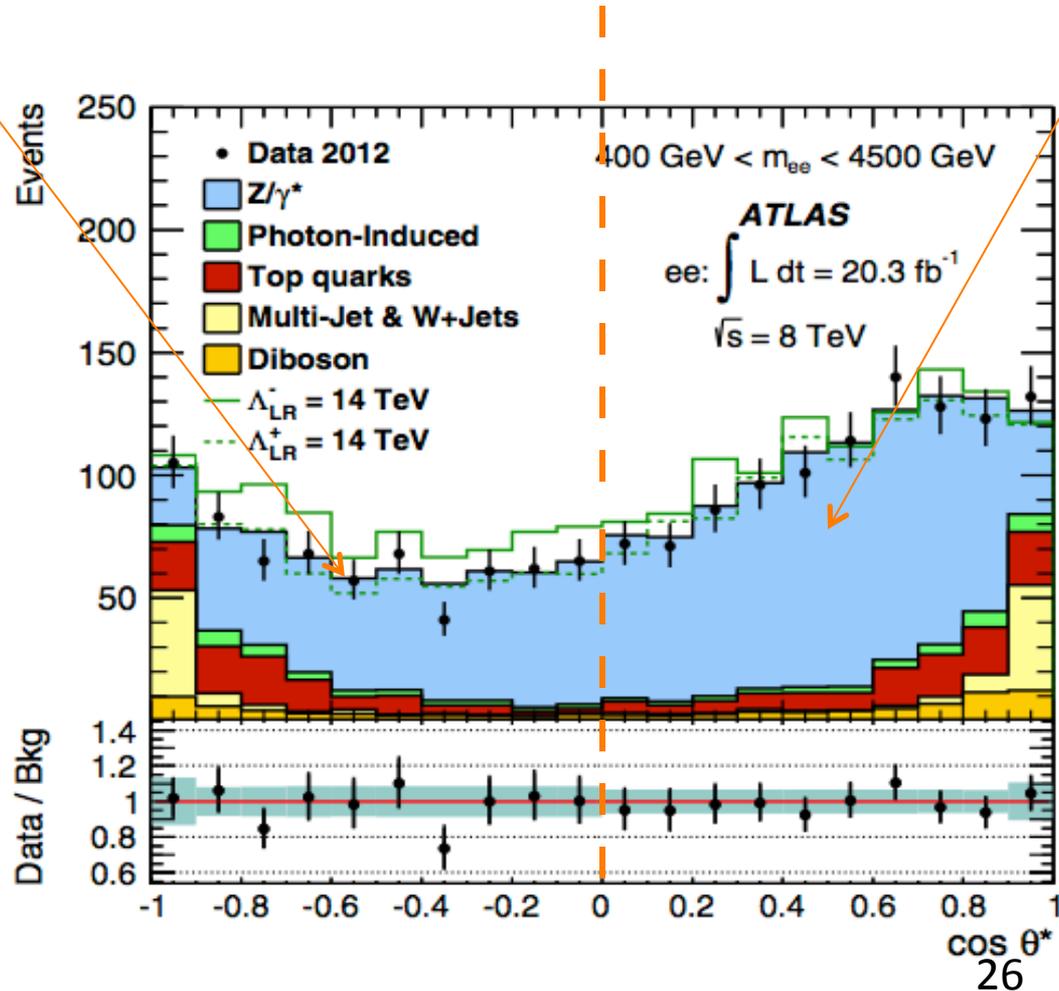
Here quark carries

X_2

Lepton Angular Distribution

Backward events

Forward events



Models to Study:

Model	DM Spin	Lepton Chirality	Interactions
pD_{RR}	1/2	right-handed	$\tilde{u} (\bar{u}P_L\chi) + \tilde{e} (\bar{e}P_L\chi)$
pD_{RL}	1/2	left-handed	$\tilde{u} (\bar{u}P_L\chi) + \tilde{e} (\bar{e}P_R\chi)$
pCS_{RR}	0	right-handed	$\chi (\bar{u}P_L\tilde{u}) + \chi (\bar{e}P_L\tilde{e})$
pCS_{RL}	0	left-handed	$\chi (\bar{u}P_L\tilde{u}) + \chi (\bar{e}P_L\tilde{e})$

- Two DM particles χ and χ^c
- If same masses \longrightarrow Dirac, if mixing \longrightarrow Majorana

Models to Study:

Model	DM Spin	Lepton Chirality	Interactions
pD_{RR}	1/2	right-handed	$\tilde{u} (\bar{u}P_L\chi) + \tilde{e} (\bar{e}P_L\chi)$
pD_{RL}	1/2	left-handed	$\tilde{u} (\bar{u}P_L\chi) + \tilde{e} (\bar{e}P_R\chi)$
pCS_{RR}	0	right-handed	$\chi (\bar{u}P_L\tilde{u}) + \chi (\bar{e}P_L\tilde{e})$
pCS_{RL}	0	left-handed	$\chi (\bar{u}P_L\tilde{u}) + \chi (\bar{e}P_L\tilde{e})$

- Two DM particles χ and χ^c
- If same masses \rightarrow Dirac, if mixing \rightarrow Majorana

Mass spectrum
(GeV)

DM eigenstates almost degenerate (1 MeV)

$\tilde{u} \tilde{e}$
 χ_2
 χ_1

Models to Study:

Model	DM Spin	Lepton Chirality	Interactions
pD_{RR}	1/2	right-handed	$\tilde{u} (\bar{u}P_L\chi) + \tilde{e} (\bar{e}P_L\chi)$
pD_{RL}	1/2	left-handed	$\tilde{u} (\bar{u}P_L\chi) + \tilde{e} (\bar{e}P_R\chi)$
pCS_{RR}	0	right-handed	$\chi (\bar{u}P_L\tilde{u}) + \chi (\bar{e}P_L\tilde{e})$
pCS_{RL}	0	left-handed	$\chi (\bar{u}P_L\tilde{u}) + \chi (\bar{e}P_L\tilde{e})$

- Two DM particles χ and χ^c
- If same masses \rightarrow Dirac, if mixing \rightarrow Majorana

Mass spectrum
(GeV)

DM eigenstates almost degenerate (1 MeV)

$\tilde{u} \tilde{e}$

χ_2

χ_1

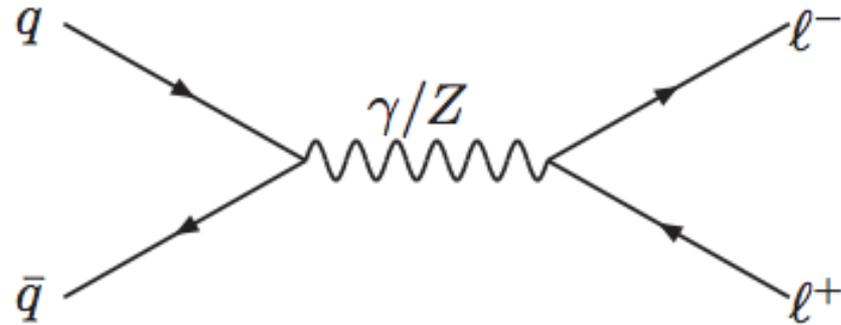
Vary DM-mediator Splitting (10-100%)

Model	DM Spin	Lepton Chirality	Interactions
pD_{RR}	1/2	right-handed	$\tilde{u} (\bar{u}P_L\chi) + \tilde{e} (\bar{e}P_L\chi)$
pD_{RL}	1/2	left-handed	$\tilde{u} (\bar{u}P_L\chi) + \tilde{e} (\bar{e}P_R\chi)$
pCS_{RR}	0	right-handed	$\chi (\bar{u}P_L\tilde{u}) + \chi (\bar{e}P_L\tilde{e})$
pCS_{RL}	0	left-handed	$\chi (\bar{u}P_L\tilde{u}) + \chi (\bar{e}P_L\tilde{e})$

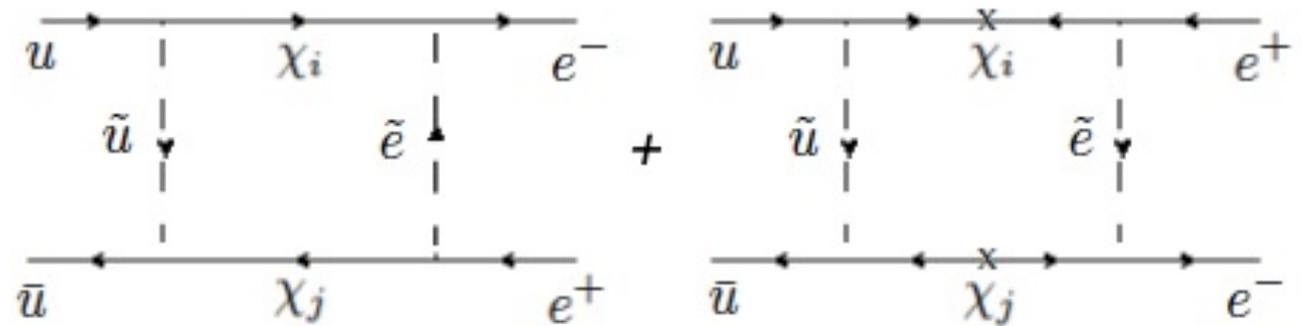
Discussion:

- For a given DM spin, what happens if we change the lepton's chirality?
- For a given lepton's chirality, what happens if we change DM spin?

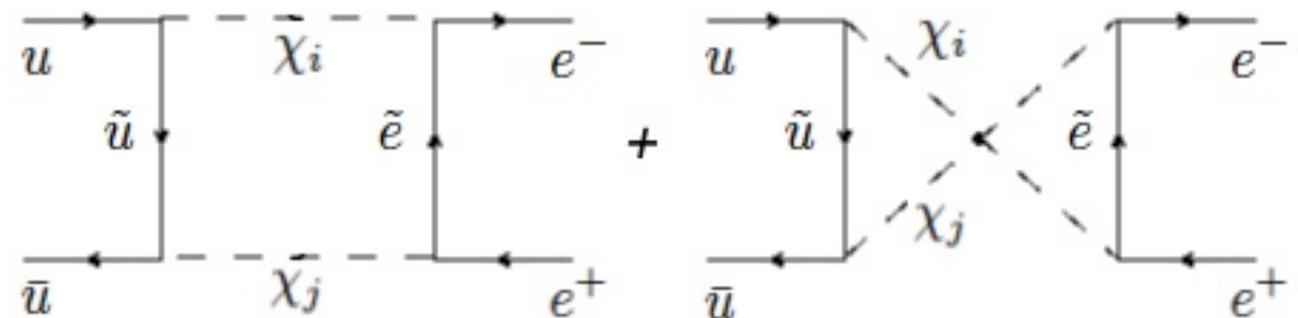
Contributions to dilepton production



$pD :$

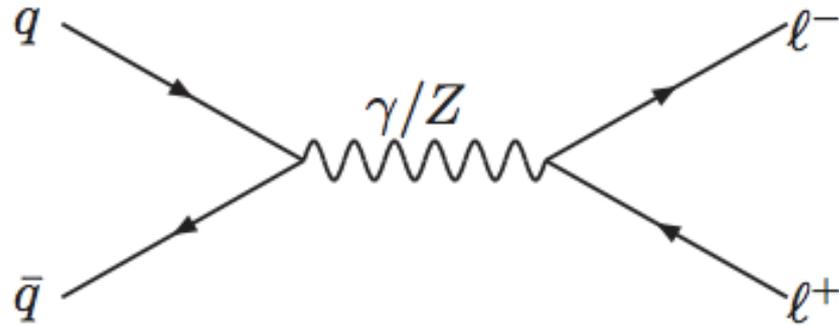


$pCS :$

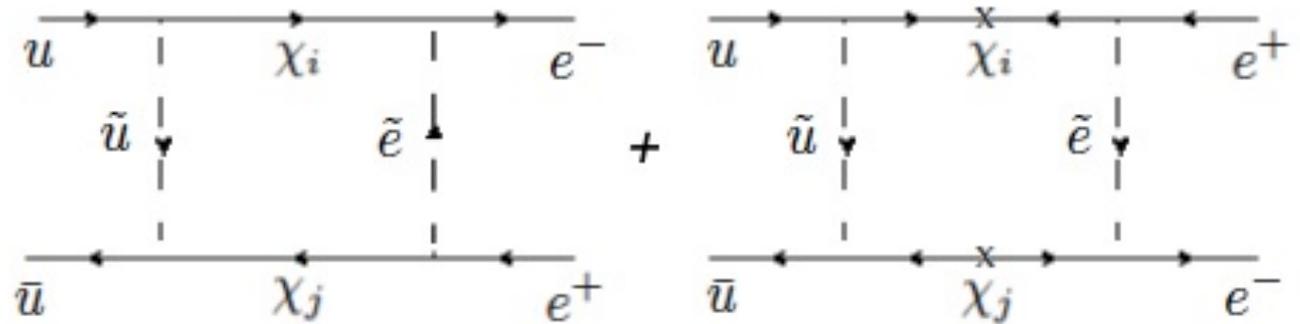


Contributions to dilepton production

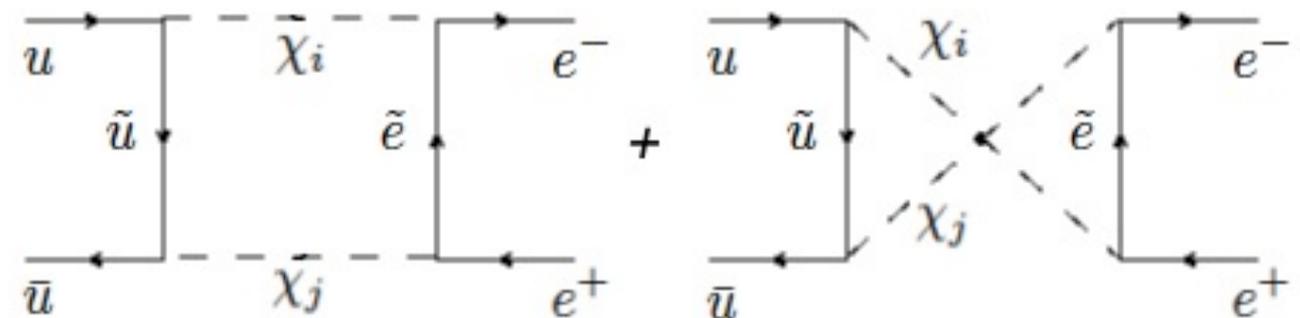
Drell-Yan, SM
dominating
background



pD :

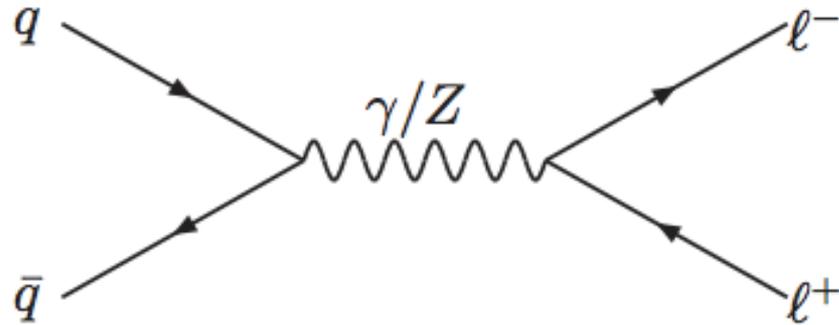


pCS :

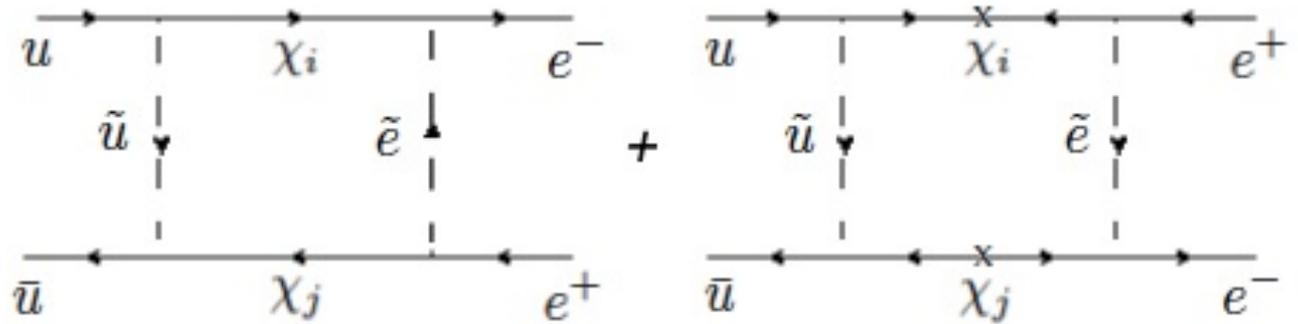


Contributions to dilepton production

*Drell-Yan, SM
dominating
background*

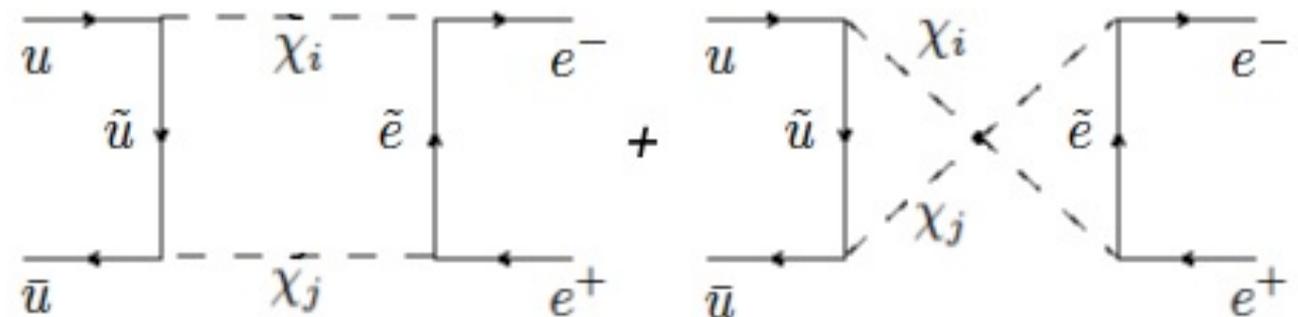


pD :



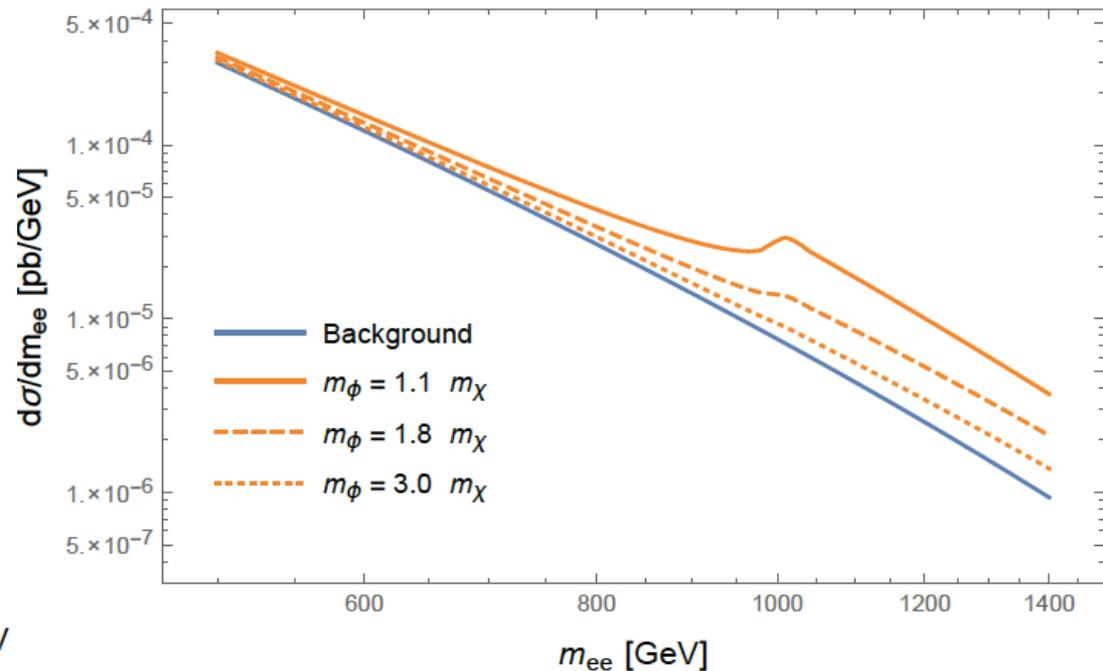
*New physics
contributions*

pCS :

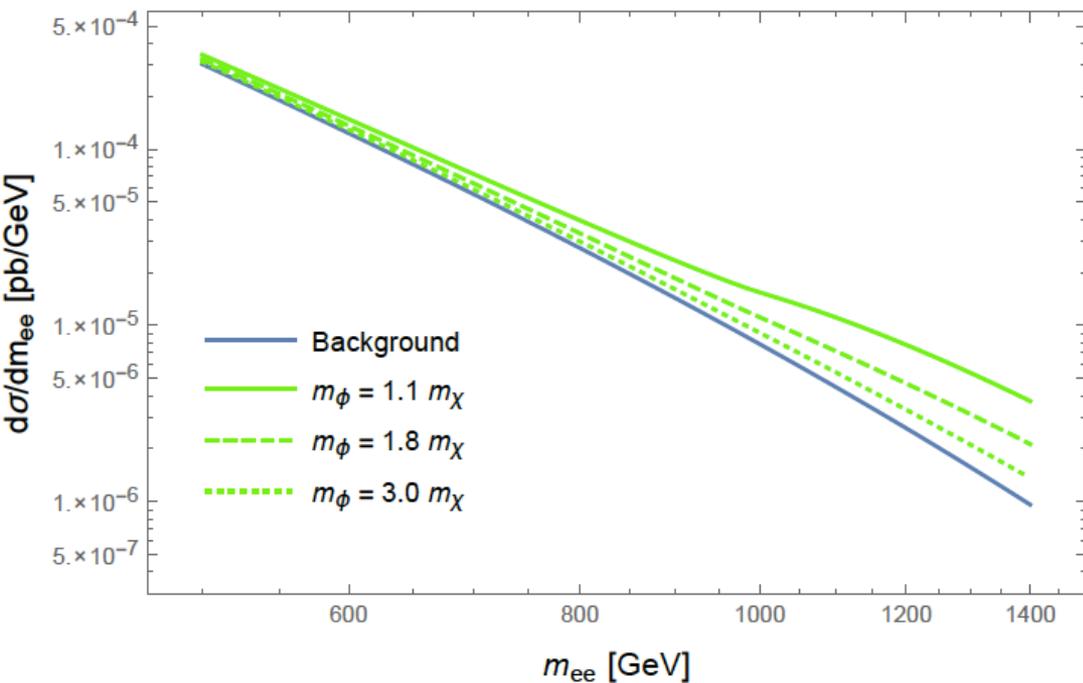


Results: Invariant Mass

Case pD_{RR}, $m_\chi = 500$ GeV



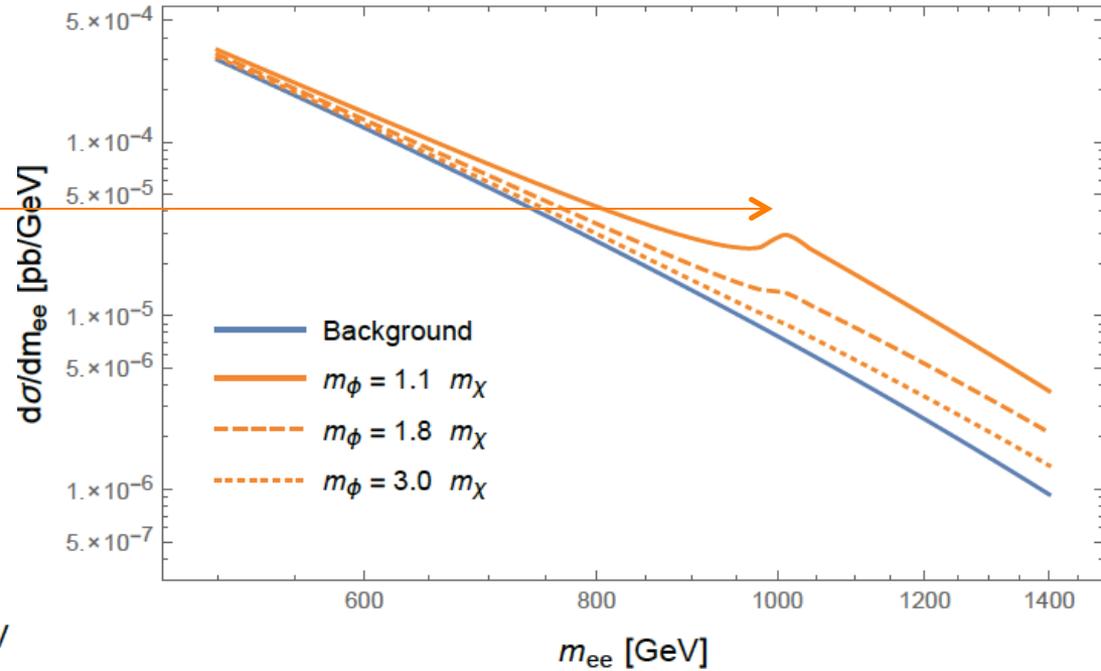
Case pC_{SRR}, $m_\chi = 500$ GeV



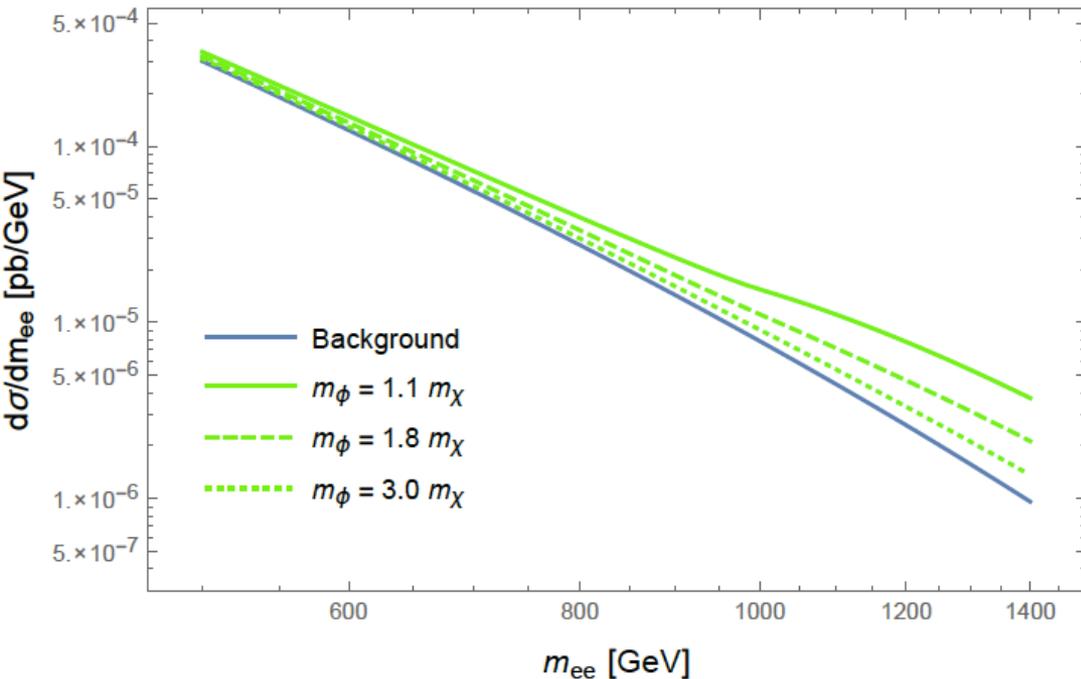
Results: Invariant Mass

Case pD_{RR}, $m_\chi = 500$ GeV

*Fermionic DM;
Monocline feature*
*N. Raj et al Phys. Rev. D 91,
115006 (2015)*



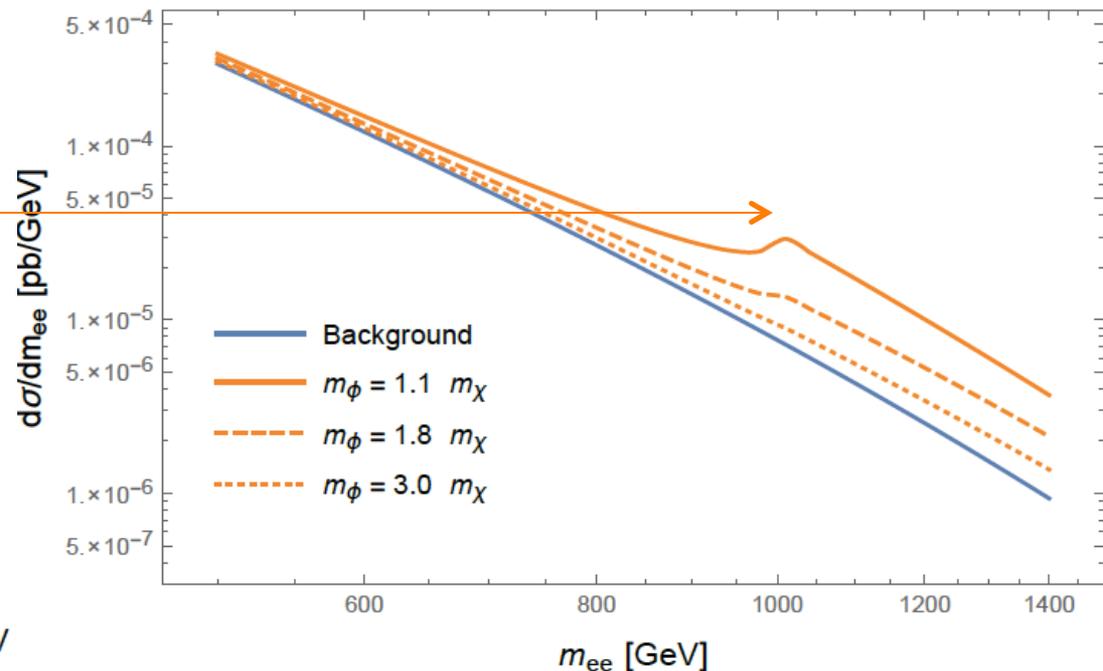
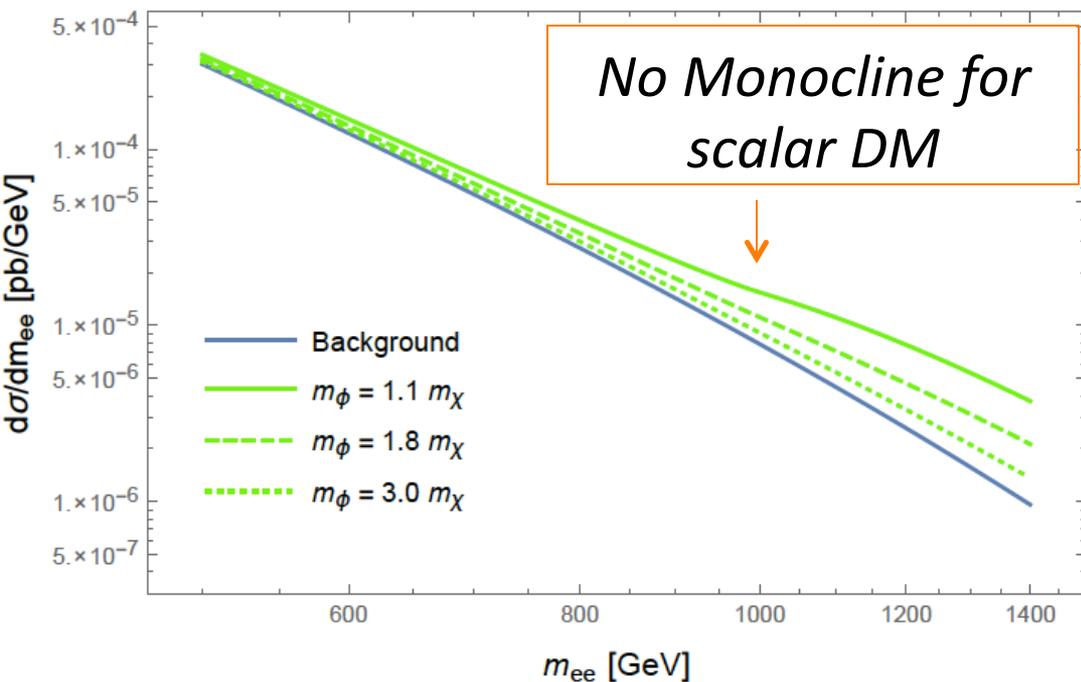
Case pC_{SRR}, $m_\chi = 500$ GeV



Results: Invariant Mass

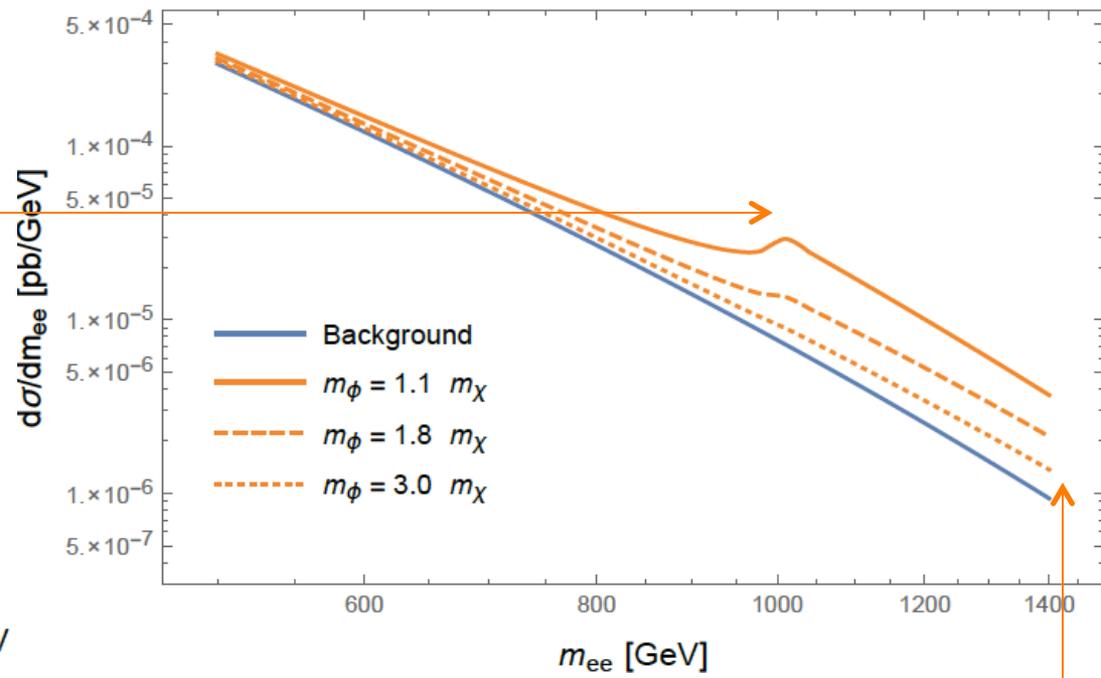
*Fermionic DM;
Monocline feature*

*N. Raj et al Phys. Rev. D 91,
115006 (2015)*

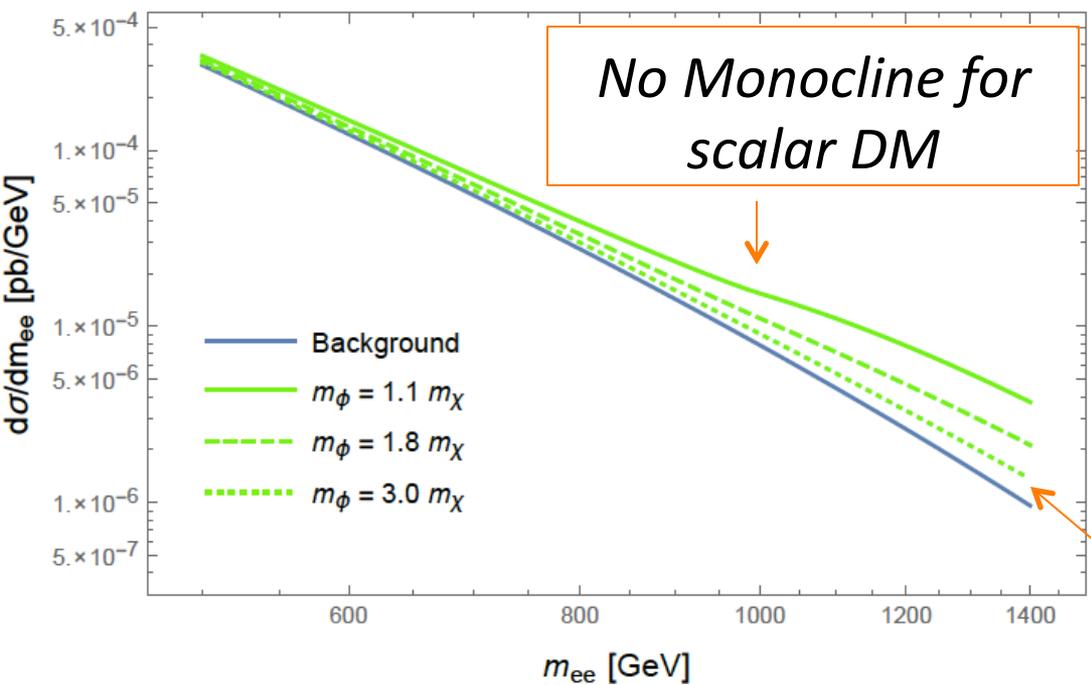
Case pC_{SRR}, $m_\chi = 500$ GeV

Results: Invariant Mass

*Fermionic DM;
Monocline feature*
N. Raj et al Phys. Rev. D 91,
115006 (2015)



Case pC_{SRR}, $m_\chi = 500$ GeV



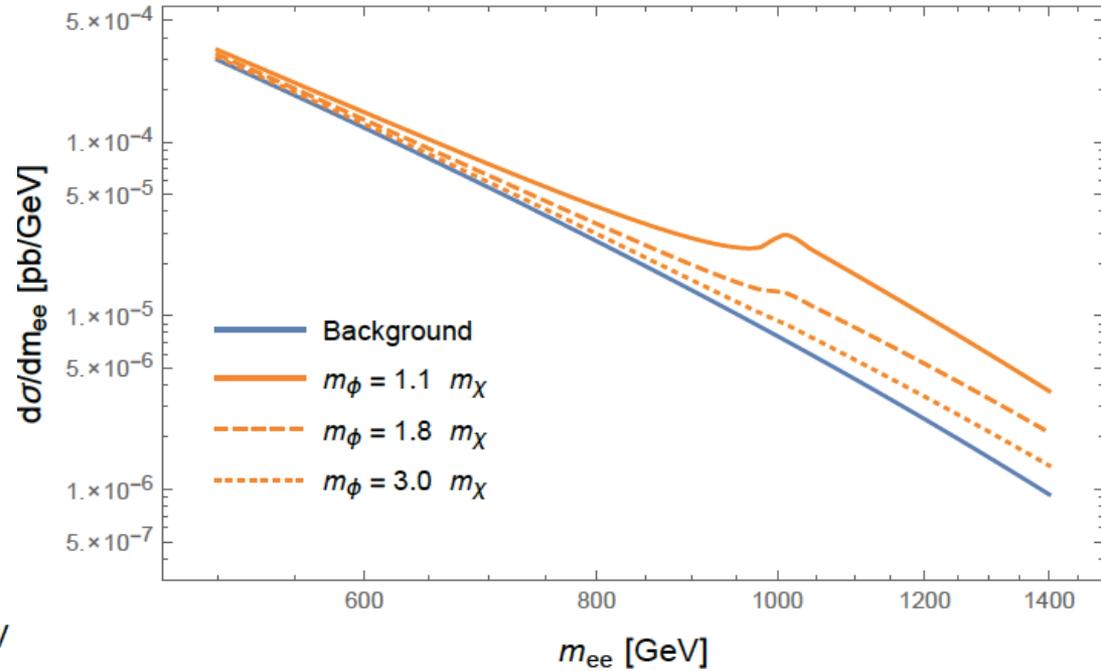
*No Monocline for
scalar DM*

*Monocline appears for
very compress
spectrum!*

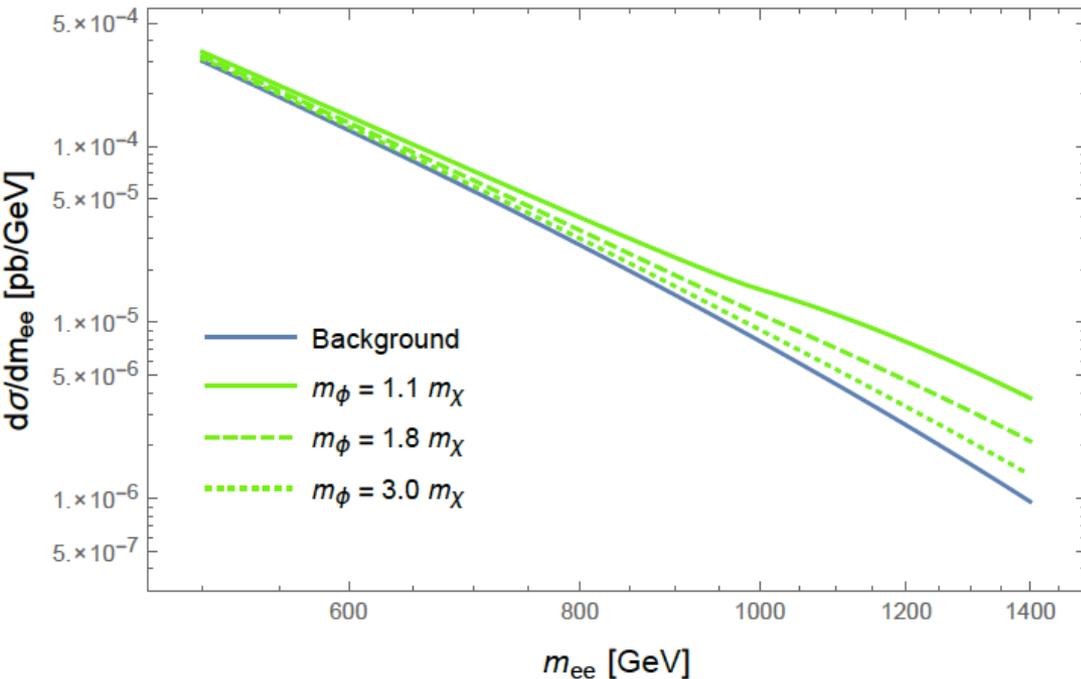
*For large splitting the
distributions look the same*

Results: Invariant Mass

Case pD_{RR}, $m_\chi = 500$ GeV



Case pC_{RR}, $m_\chi = 500$ GeV

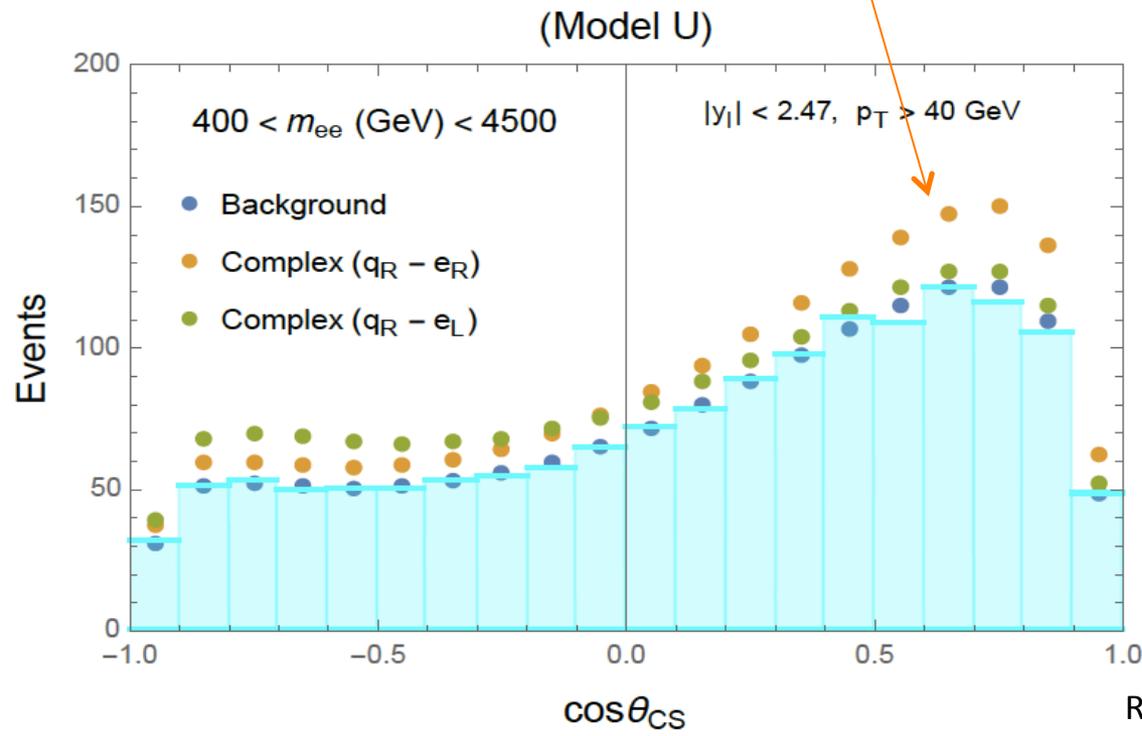
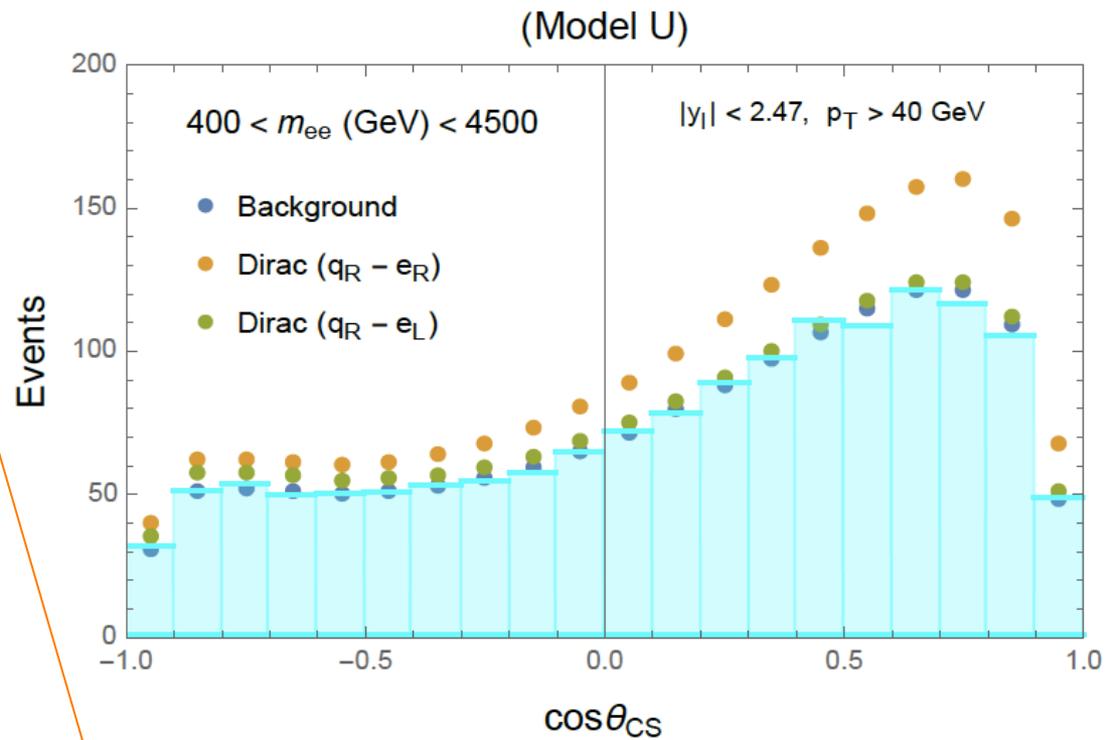


The invariant mass identifies:

- *The MASS (fermion case)*
- *the SPIN (very compressed spectrum)*

Results: Angular Distribution

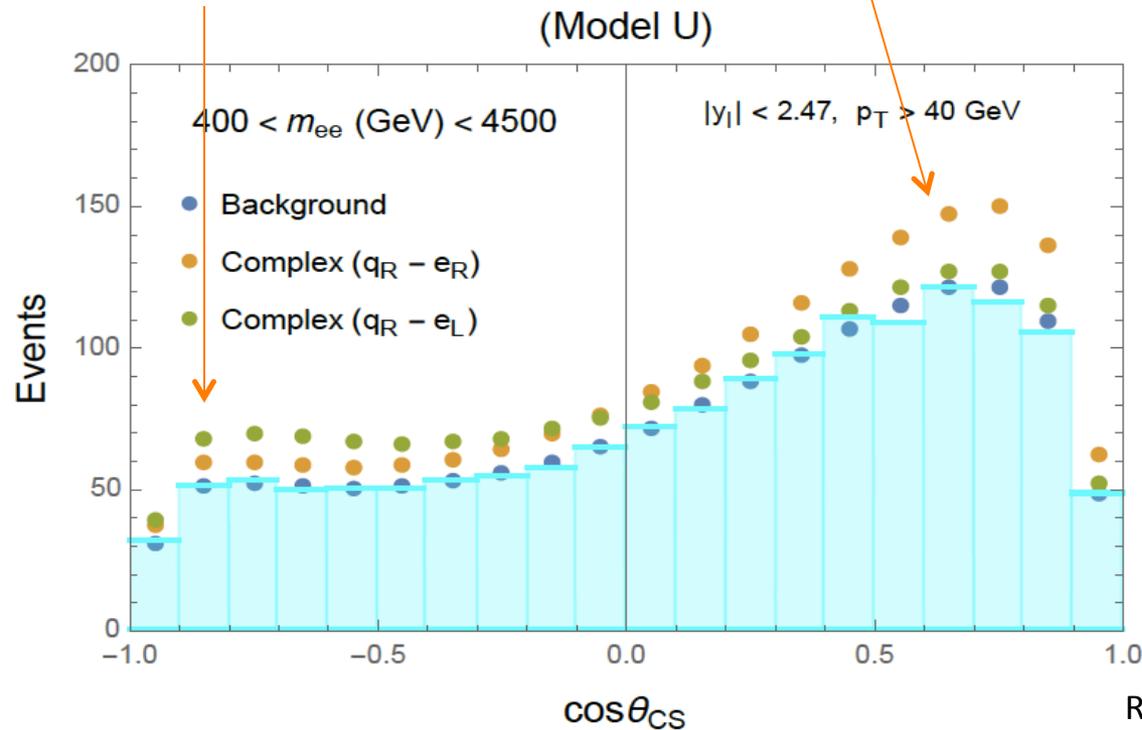
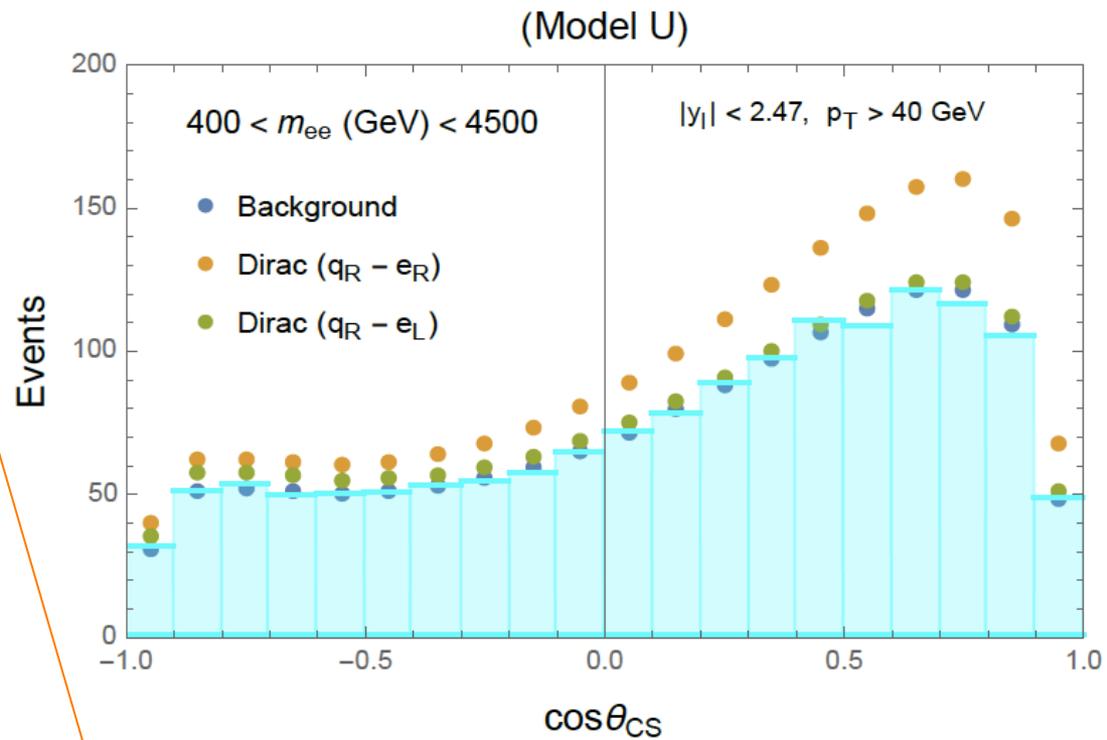
The chirality choice RR produces more forward events



Results: Angular Distribution

*The chirality choice RR produces **more forward** events*

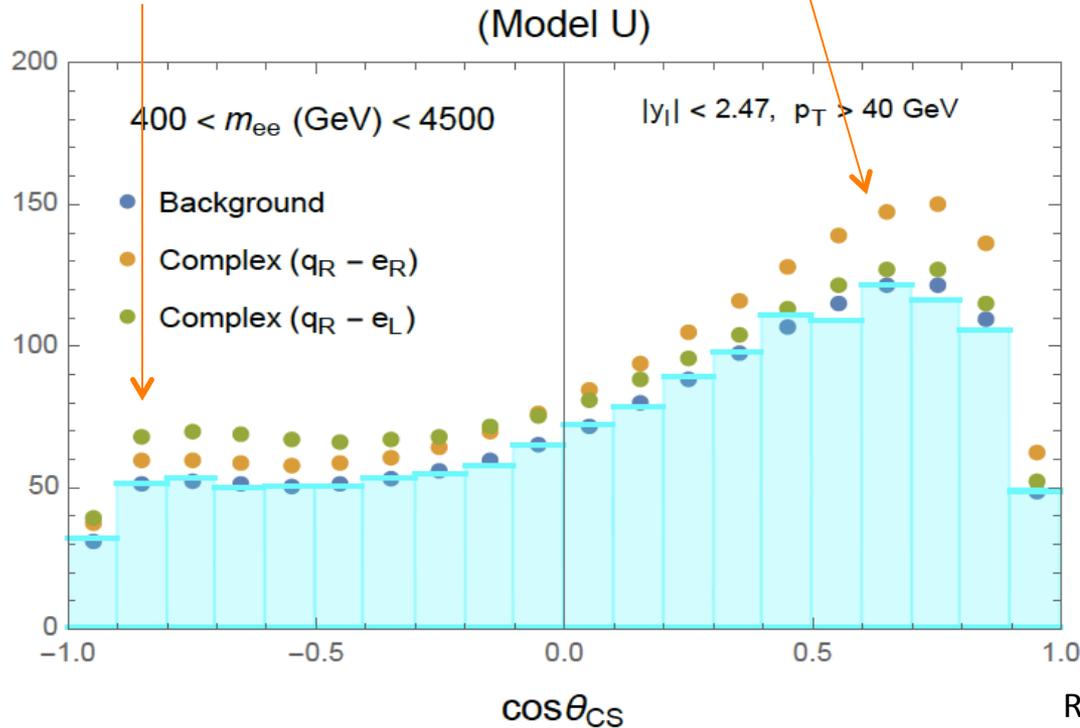
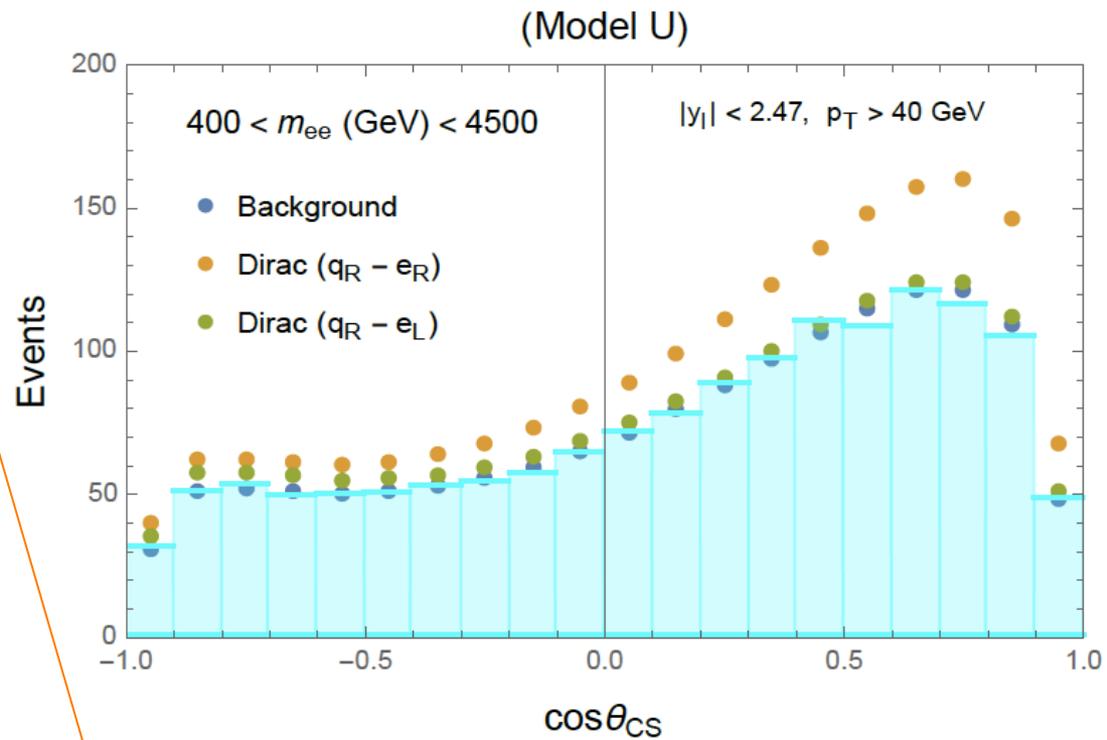
*Choosing RL produces **more backward** events*



Results: Angular Distribution

The chirality choice RR produces more forward events

Choosing RL produces more backward events



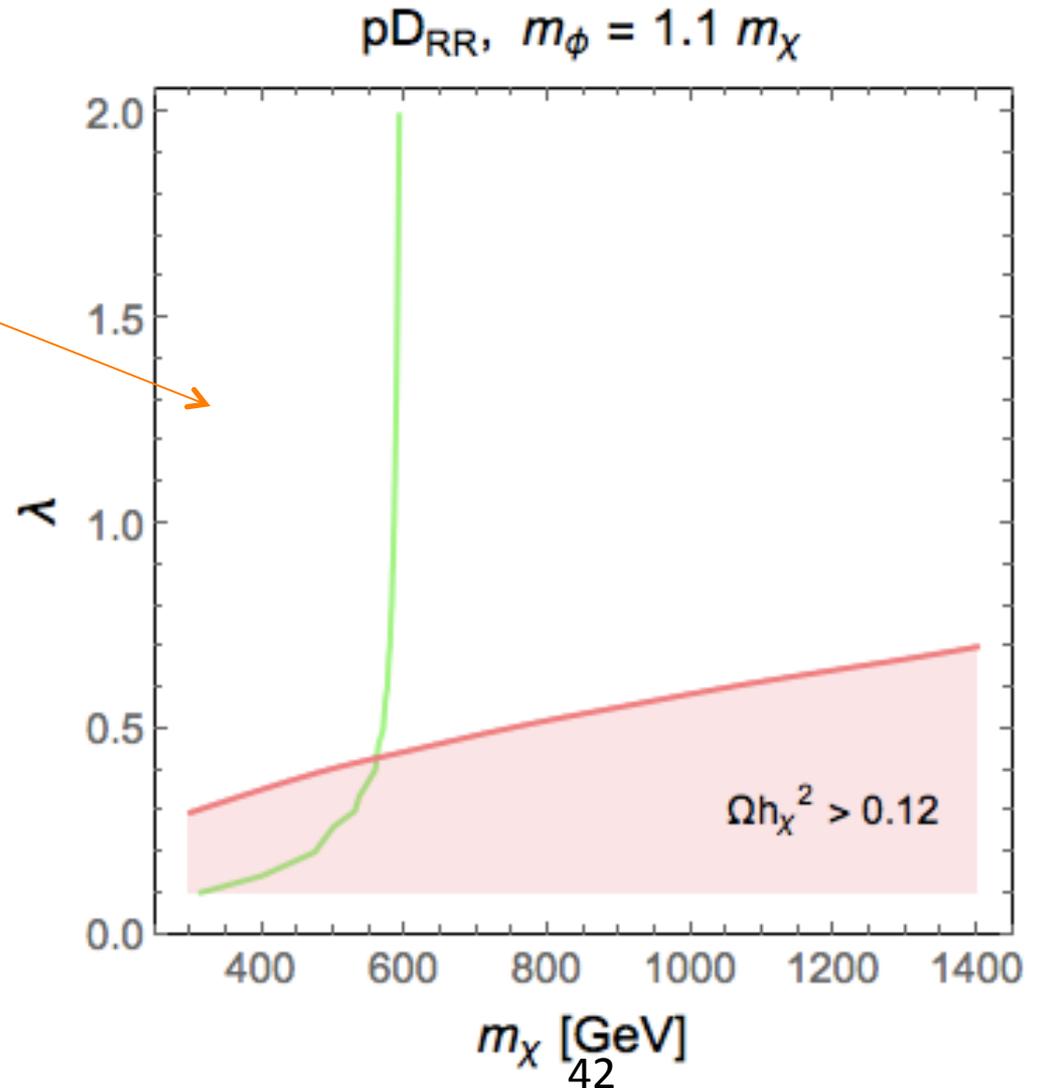
The angular distribution distinguishes relative chirality of SM particles!

Other Bounds:

- Direct Detection of DM

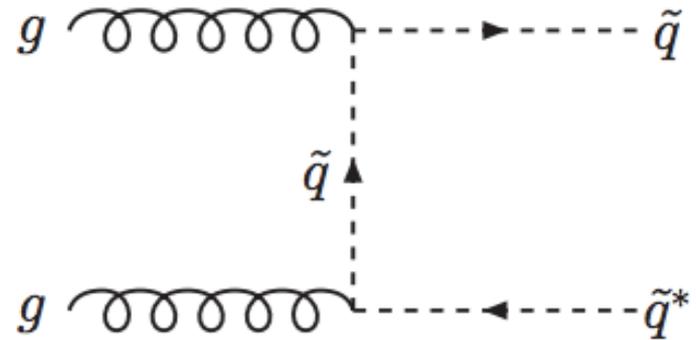
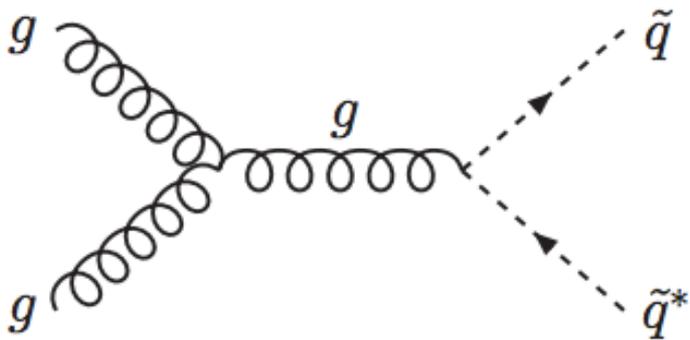
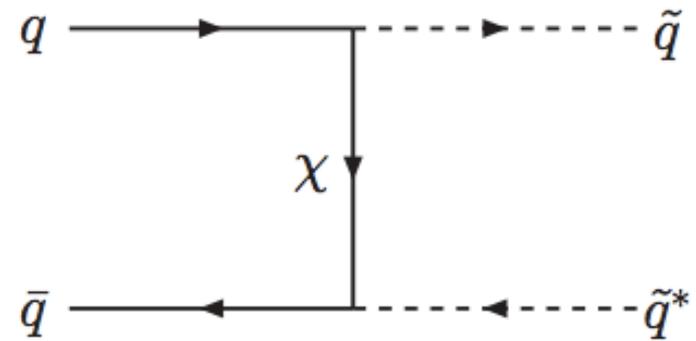
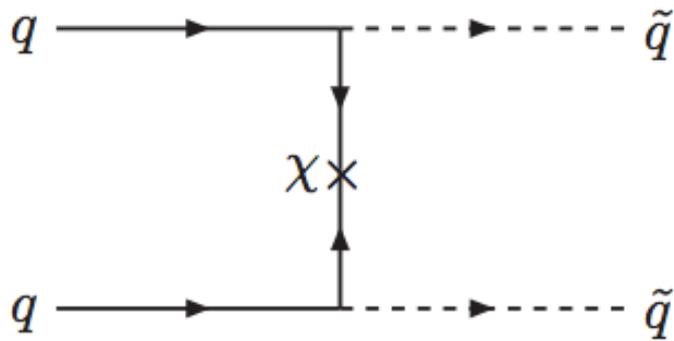
*Region Excluded by
Direct Detection*

*Bounds disappear for
100% splitting!*

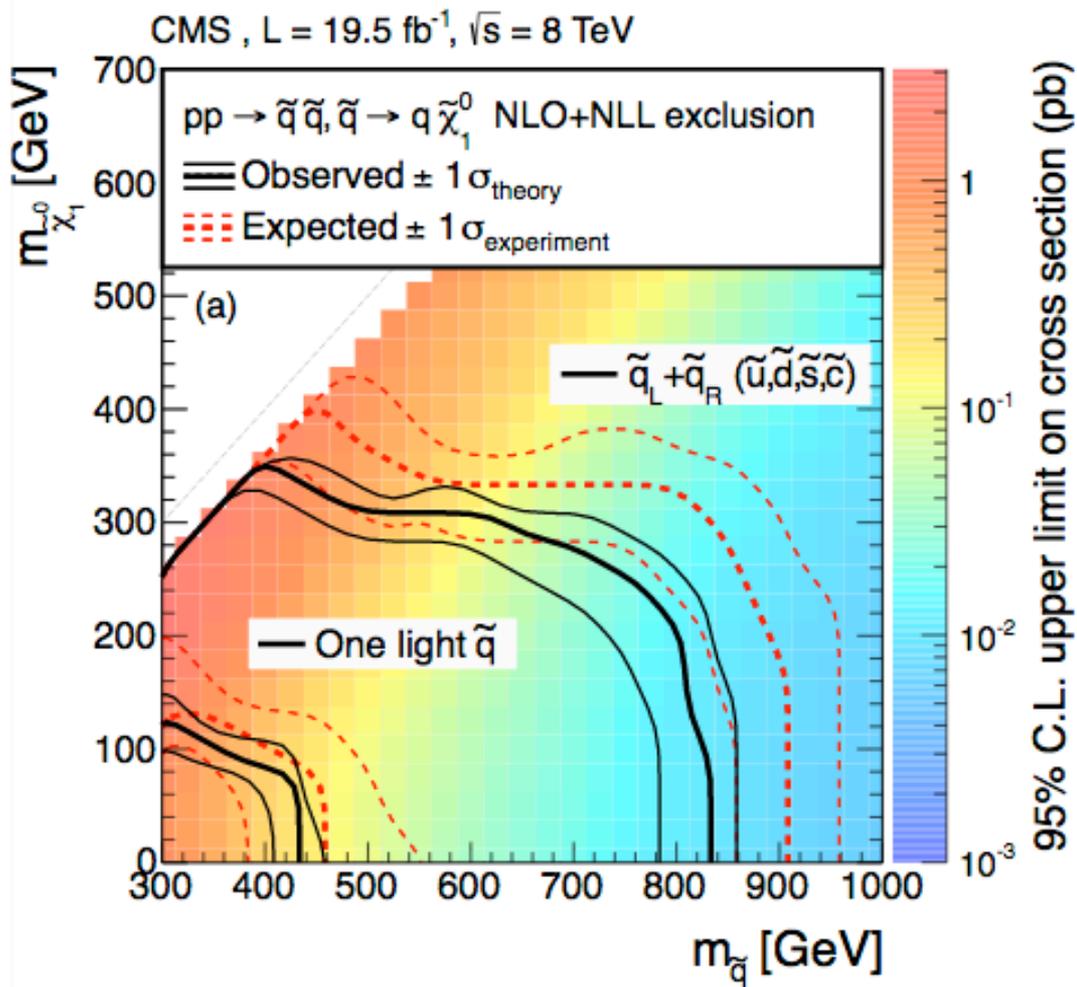
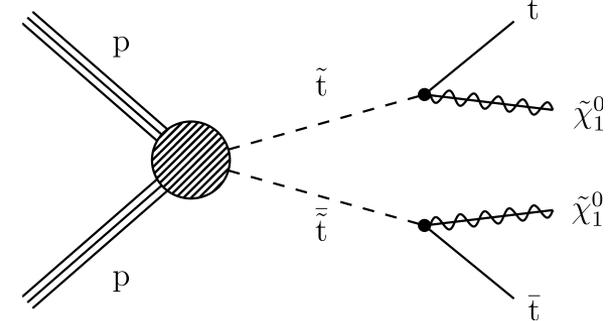


Other Bounds:

- Searches for jets+MET at the LHC

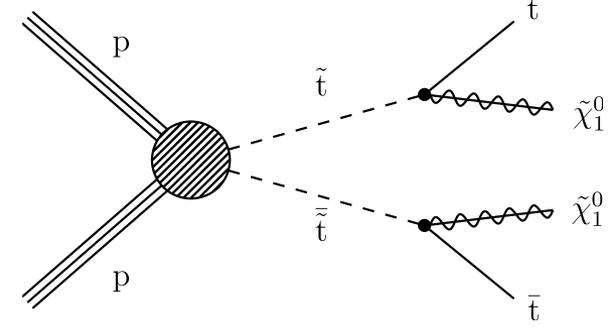


- Jets + MET

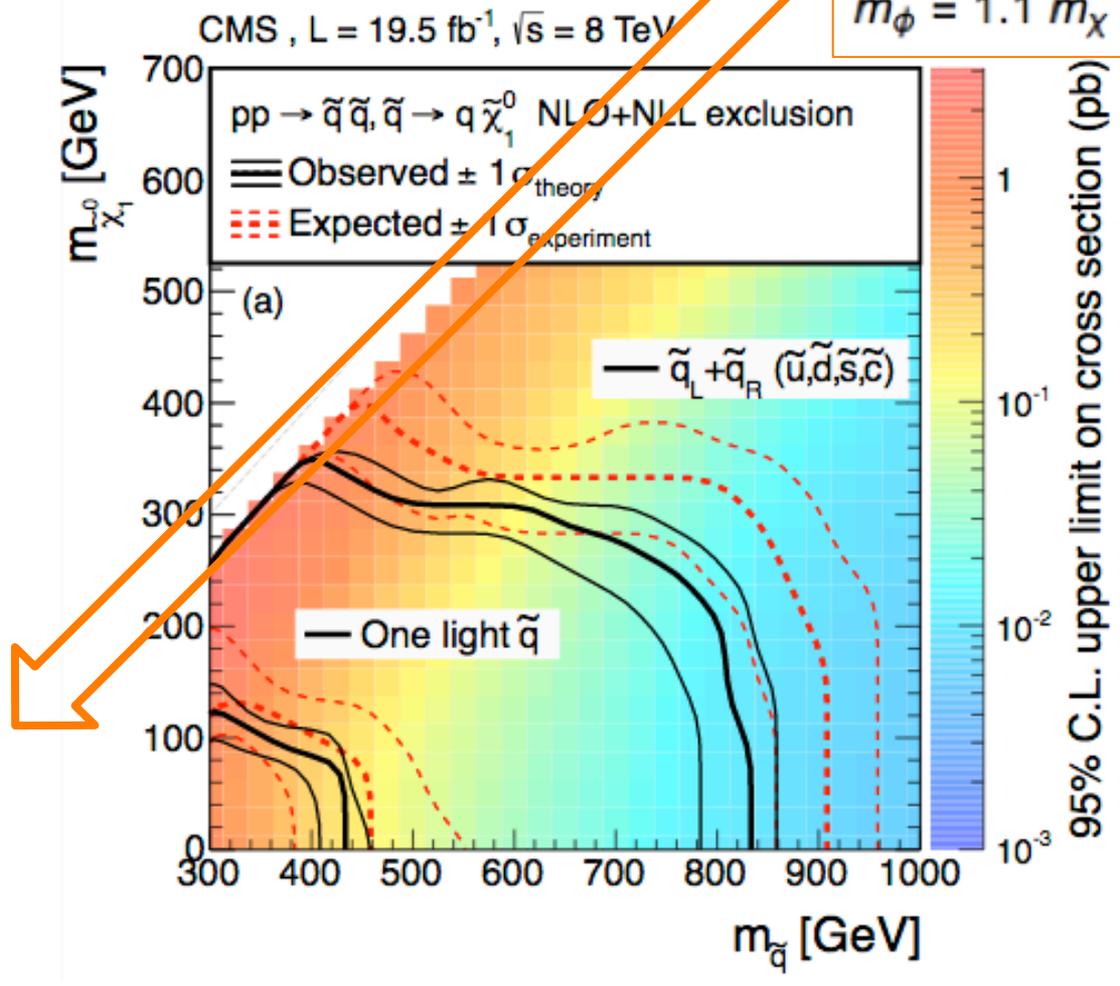


- Jets + MET

Compressed spectrum

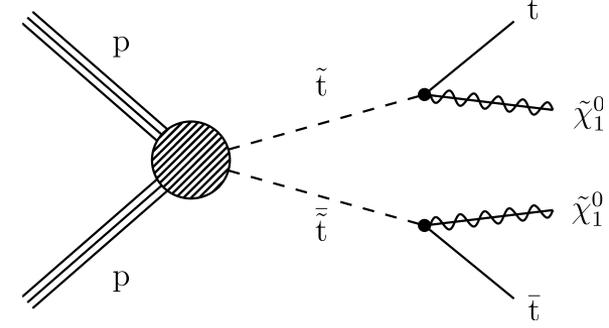


$$m_\phi = 1.1 m_\chi$$



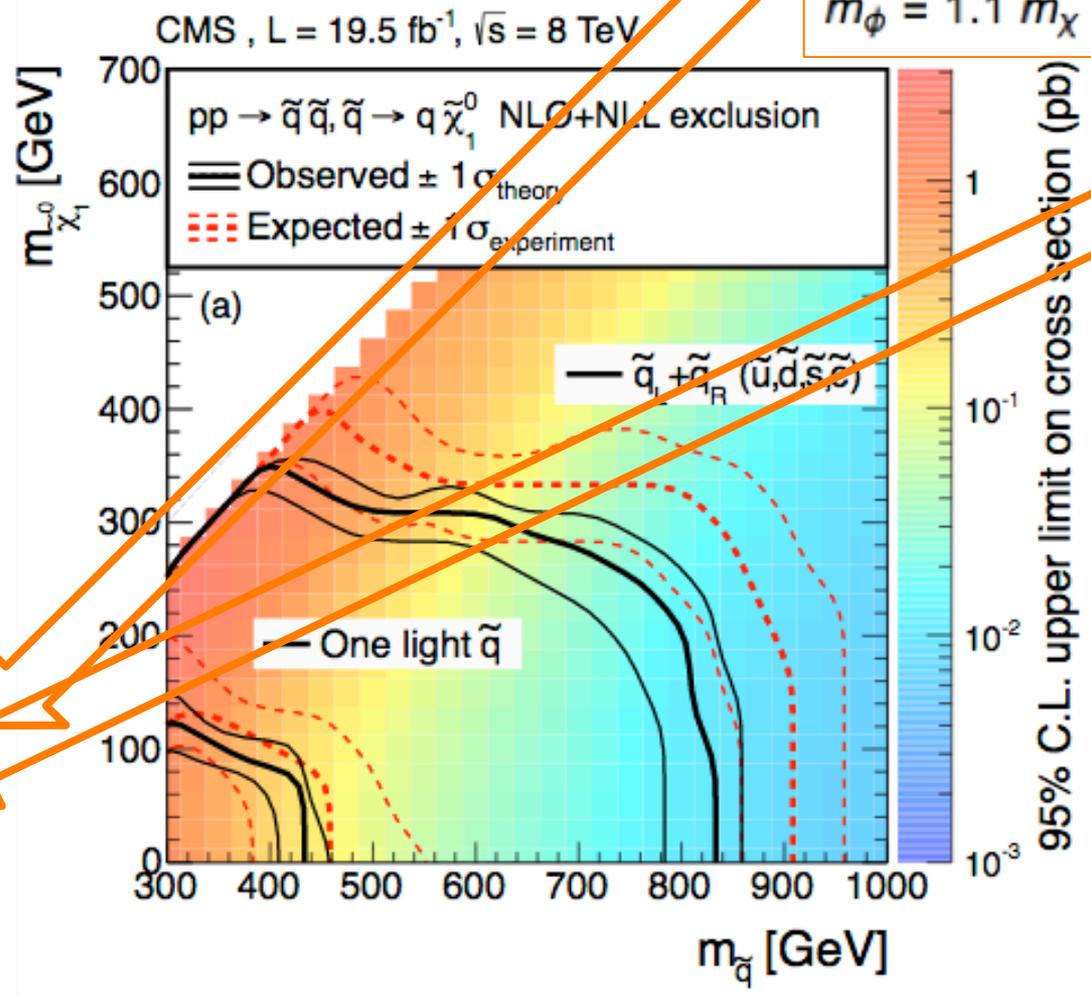
- Jets + MET

Compressed spectrum



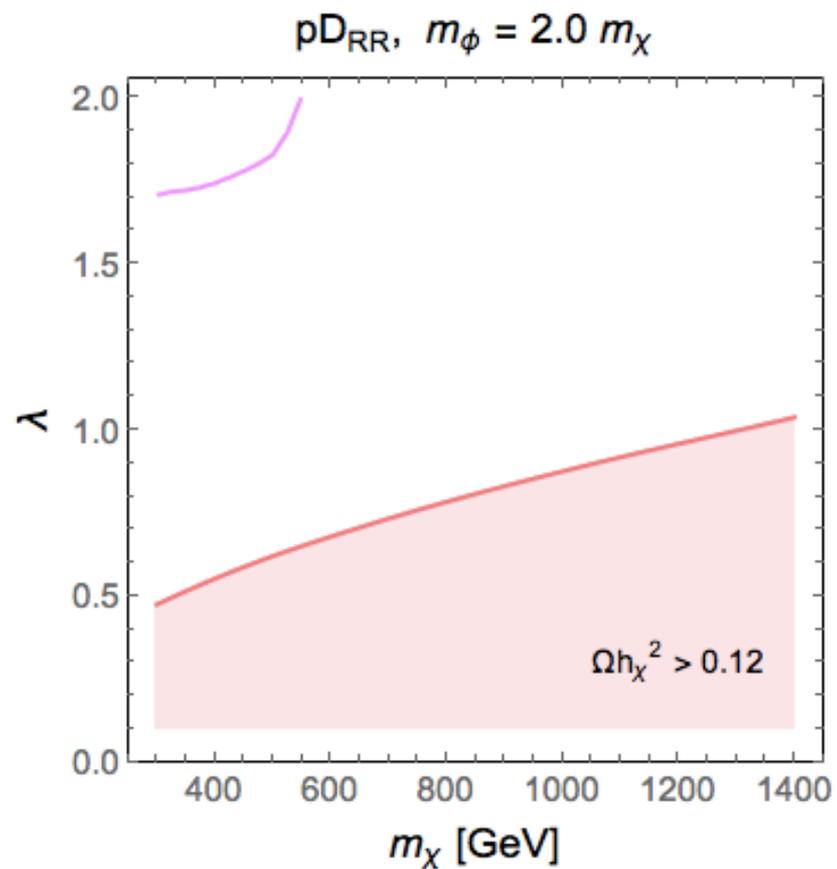
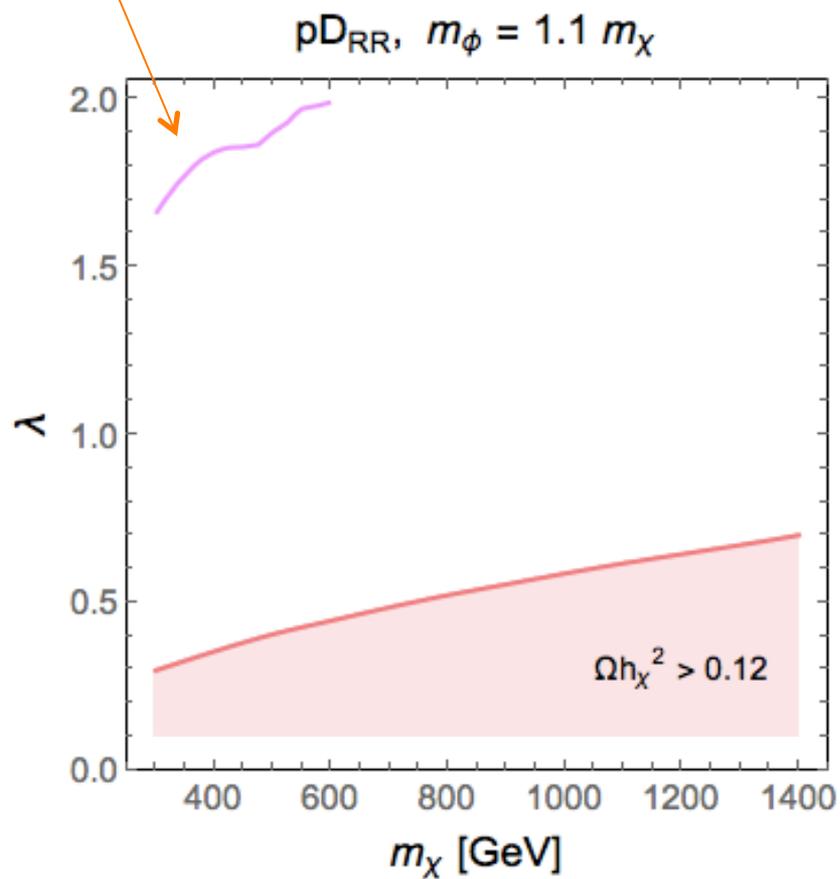
$m_\phi = 1.1 m_\chi$

$m_\phi = 2.0 m_\chi$



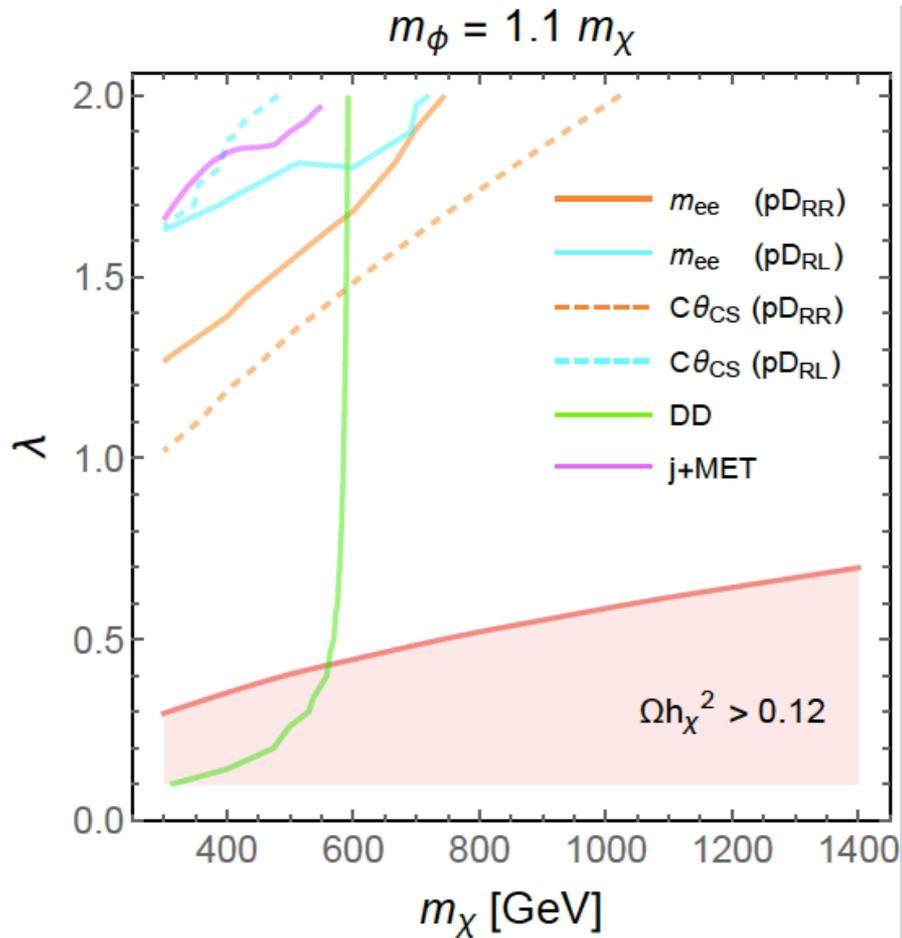
- Jets + MET

Excluded



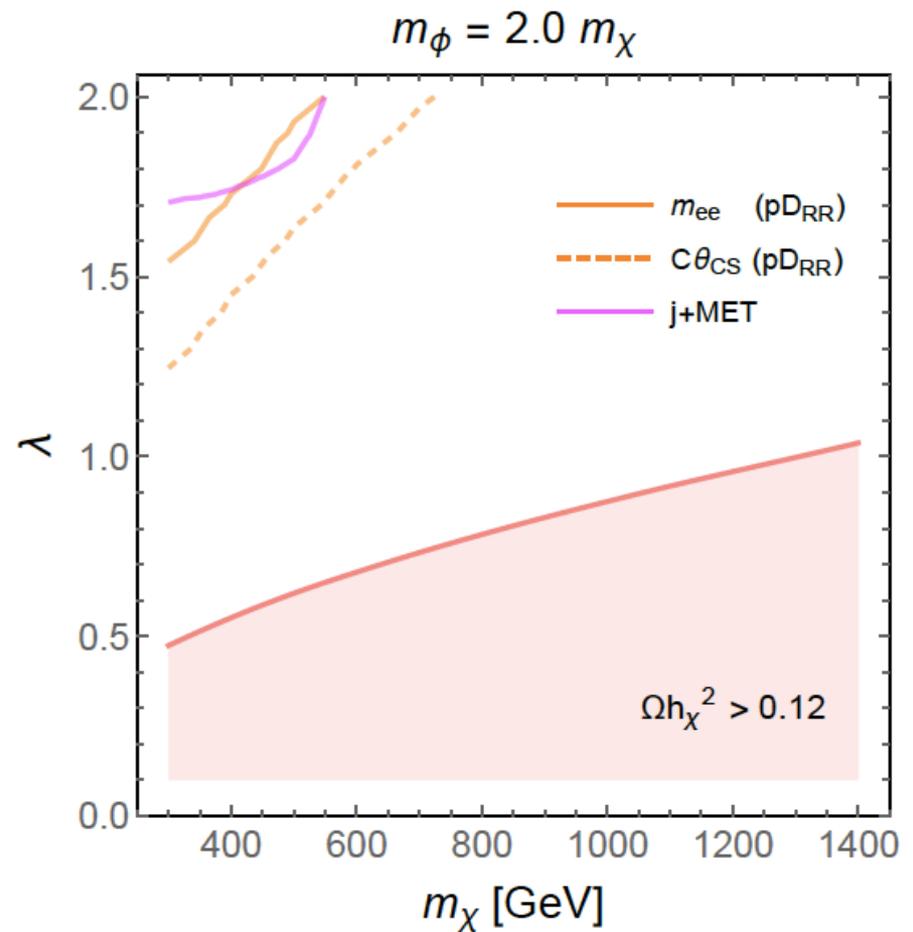
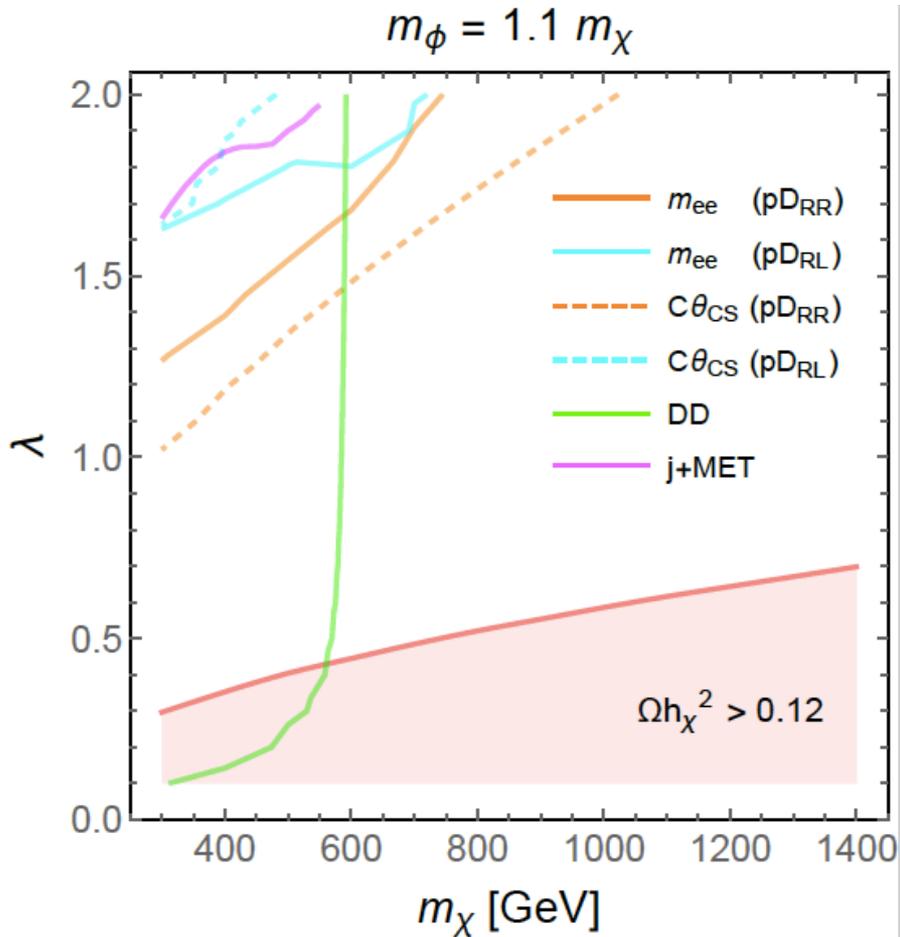
Bounds:

- Bounds for Fermionic DM cases



Bounds:

- Bounds for Fermionic DM cases



Conclusions

- Dilepton distributions can give bounds for DM simplified models with t-channel mediators. These bounds are competitive with those from jets+MET and direct detection searches.
- The dileptonic invariant mass distribution can provide information about the mass and spin of DM in the limit of almost degenerate DM-mediator masses.
- The dileptonic angular distribution can provide information about the relative chirality of the SM fermions that interact with DM (Telling us something about the quantum numbers of the mediators).

Conclusions

- Dilepton distributions can give bounds for DM simplified models with t-channel mediators. These bounds are competitive with those from jets+MET and direct detection searches.
- The dileptonic invariant mass distribution can provide information about the **mass** and **spin** of DM in the limit of almost degenerate DM-mediator masses.
- The dileptonic angular distribution can provide information about the relative chirality of the SM fermions that interact with DM (Telling us something about the quantum numbers of the mediators).

Conclusions

- Dilepton distributions can give bounds for DM simplified models with t-channel mediators. These bounds are competitive with those from jets+MET and direct detection searches.
- The dileptonic invariant mass distribution can provide information about the mass and spin of DM in the limit of almost degenerate DM-mediator masses.
- The dileptonic angular distribution can provide information about the relative **chirality** of the SM fermions that interact with DM (Telling us something about the **quantum numbers of the mediators**).

What can the LHC tell us about Dark Matter?

1. Can we discover DM?

2. Can we learn something about DM properties?

*Yes, we
can!!!*

What can the LHC tell us about Dark Matter?

1. Can we discover DM?

2. Can we learn something about DM properties?

Yes, we can!!!

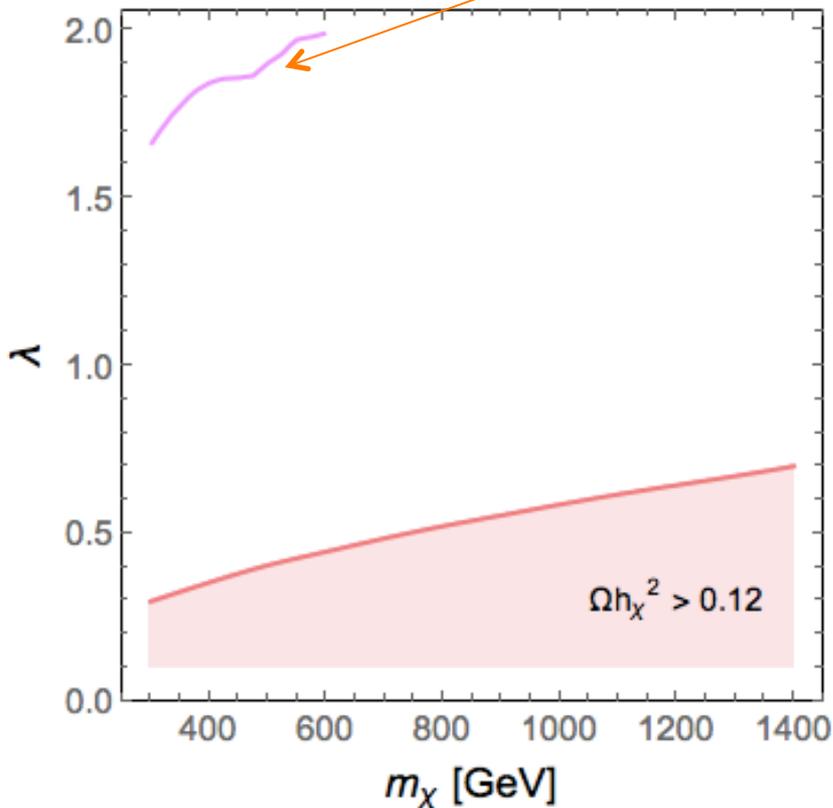


THANK YOU!

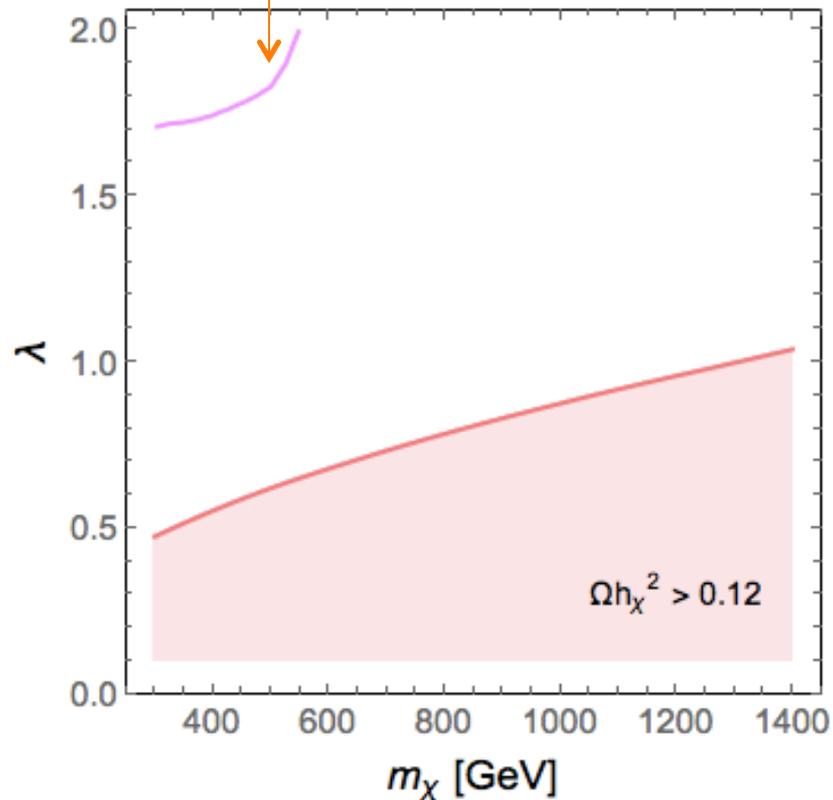
- Jets + MET

Similar bounds;
As mediator is heavier, the cross section drops but bounds also decrease

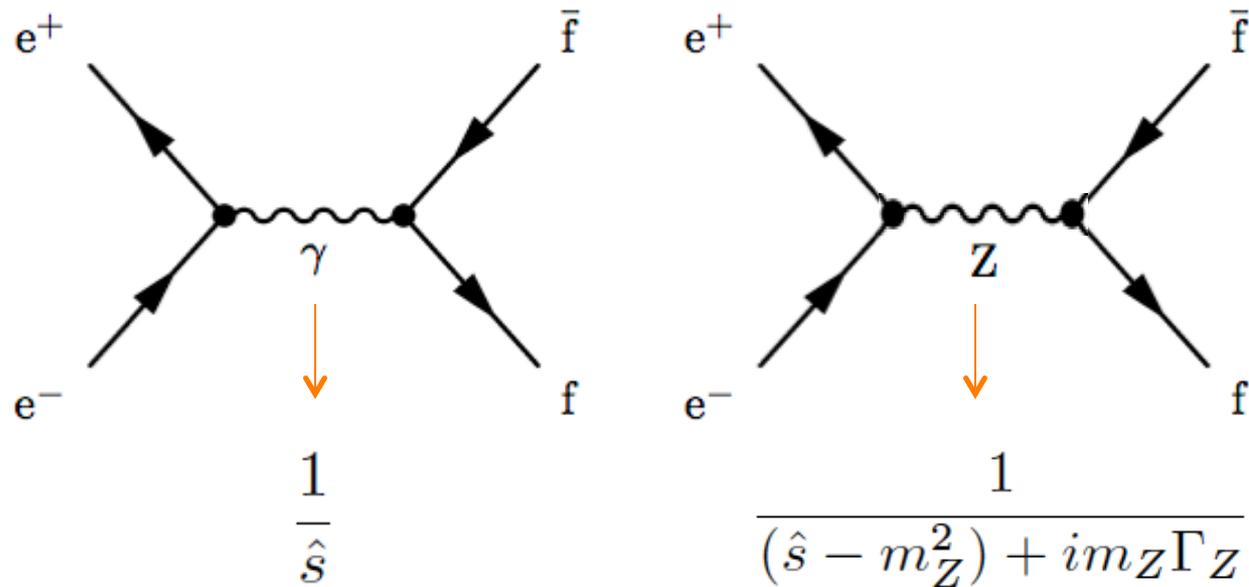
$pD_{RR}, m_\phi = 1.1 m_\chi$



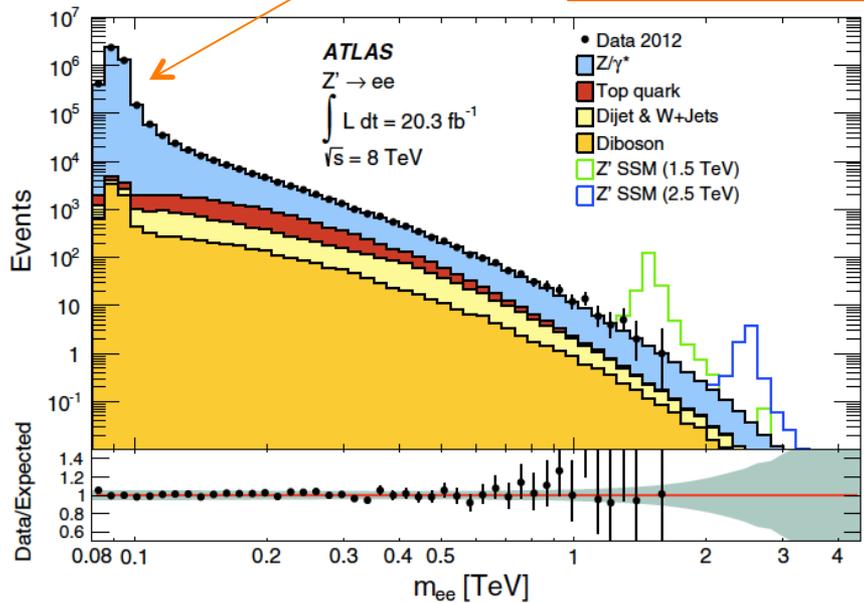
$pD_{RR}, m_\phi = 2.0 m_\chi$



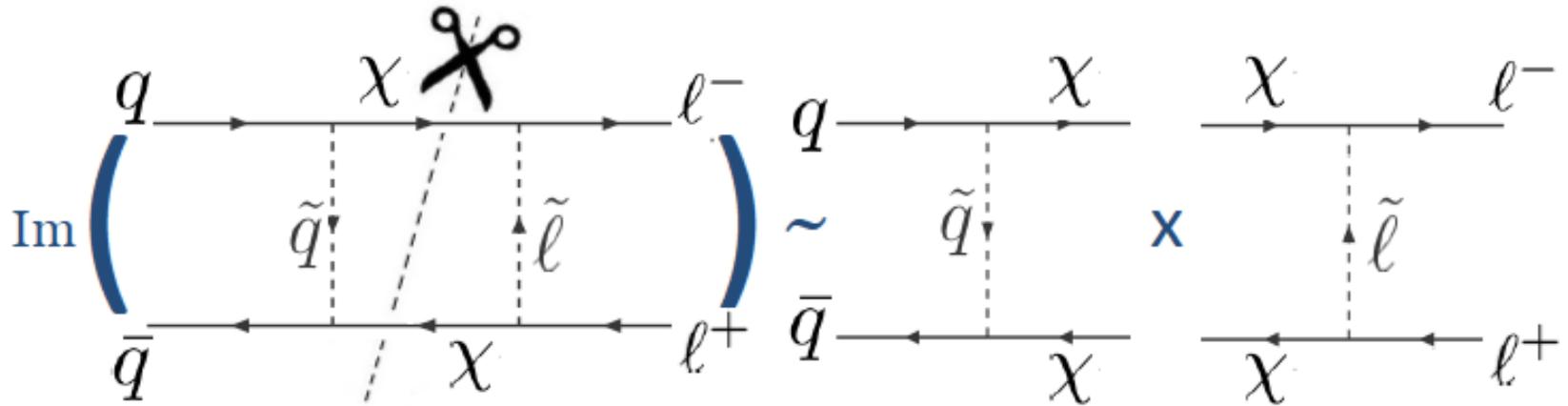
1) Threshold Effects



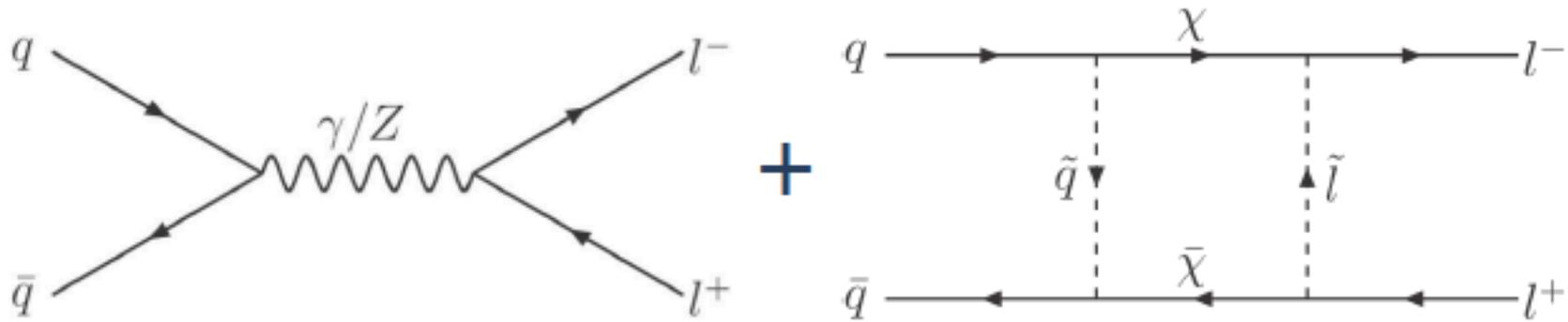
Resonant production of the Z boson



Optical theorem



Optical theorem



$$|A_{\text{tree}} + A_{\text{box}}|^2$$

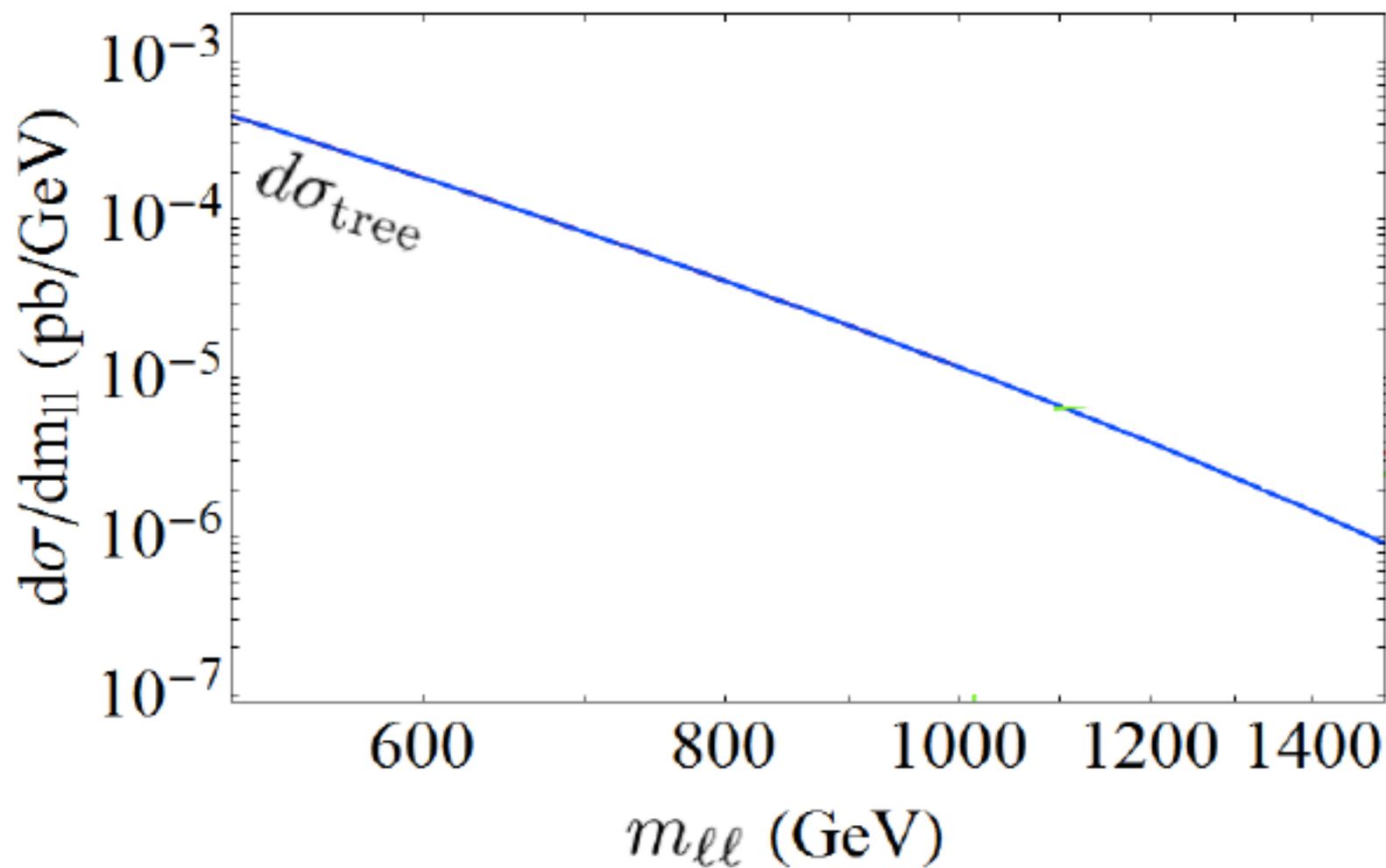
$$d\sigma_{\text{tree}} + d\sigma_{\text{int}} + d\sigma_{\text{box}}$$

$$|A_{\text{tree}} + A_{\text{box}}^{\text{real}} + iA_{\text{box}}^{\text{imag}}|^2$$

$$d\sigma_{\text{tree}} + d\sigma_{\text{int}} + d\sigma_{\text{box}}^{\text{real}} + d\sigma_{\text{box}}^{\text{imag}}$$

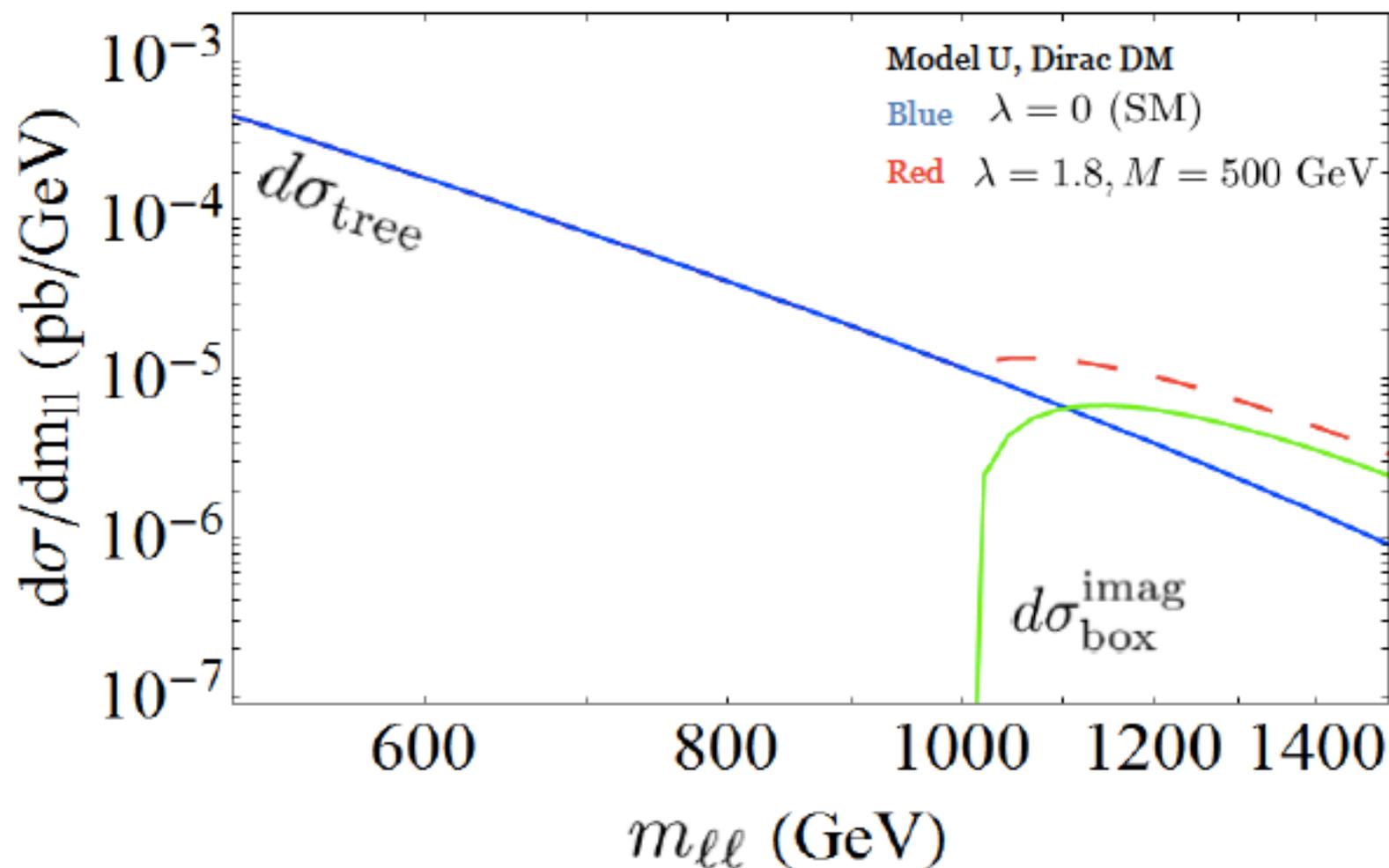
from Optical Theorem

Breakdown of rates



$d\sigma_{\text{tree}}$

Breakdown of rates

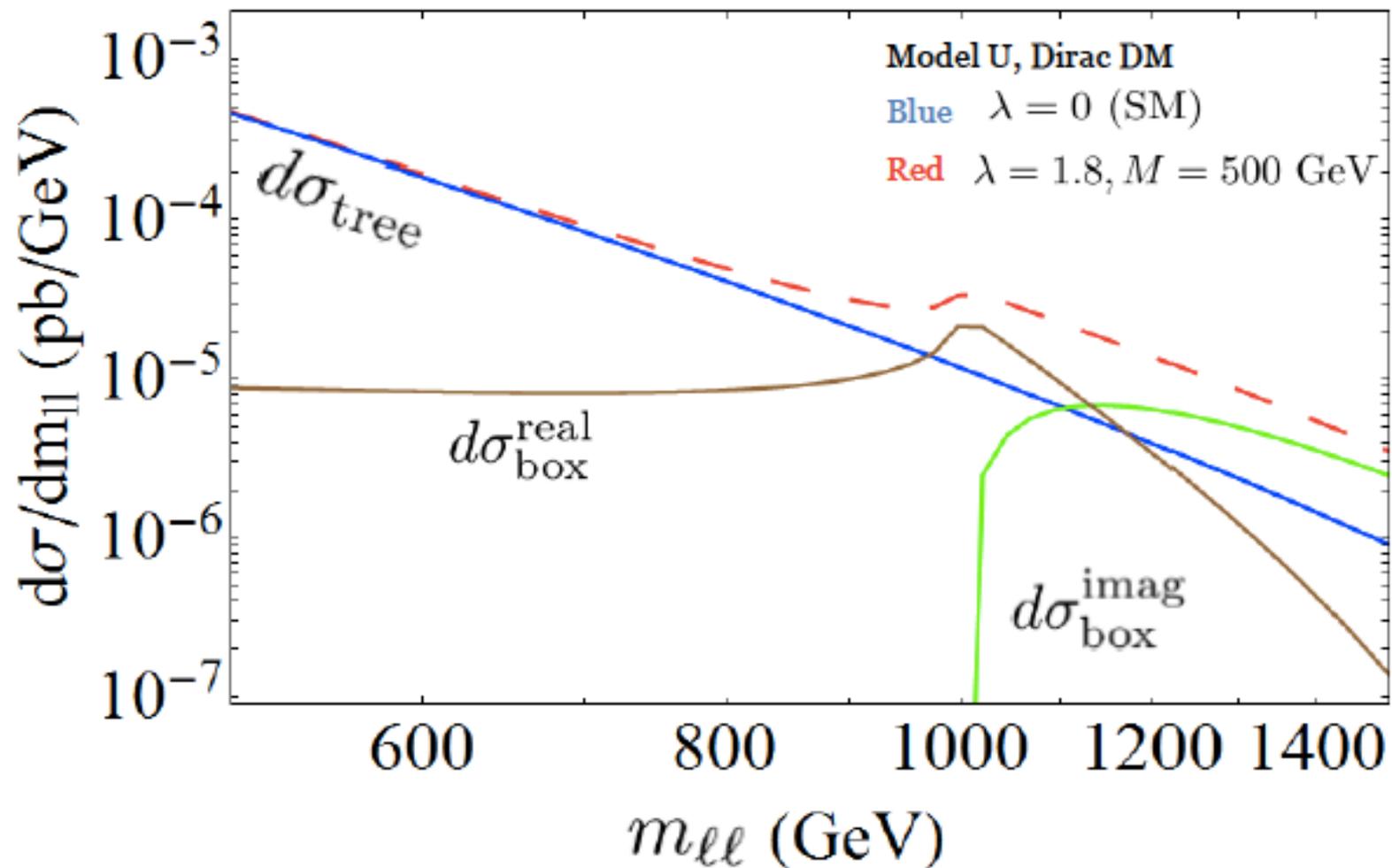


$d\sigma_{\text{tree}}$

$+ d\sigma_{\text{box}}^{\text{imag}}$

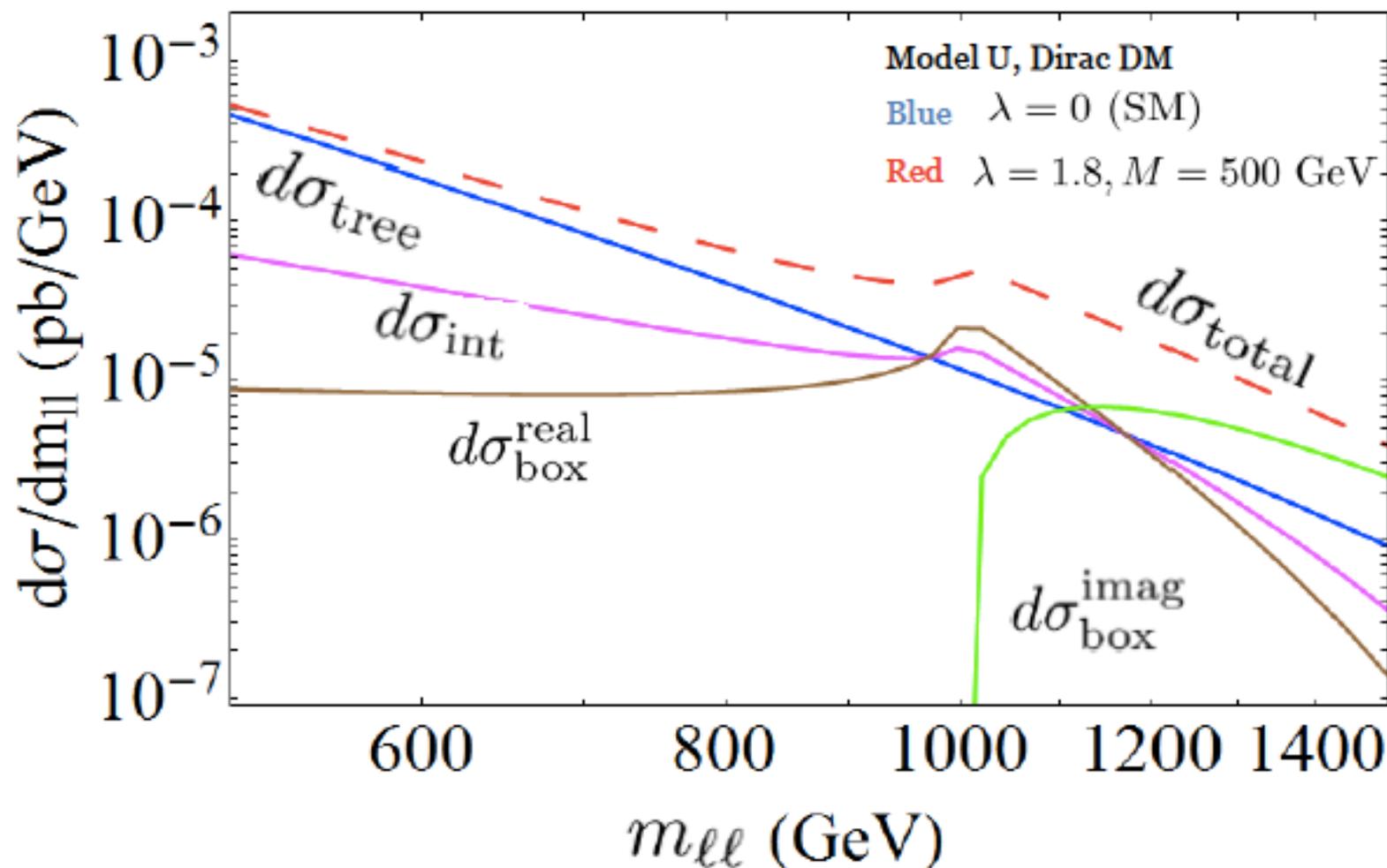
62

Breakdown of rates



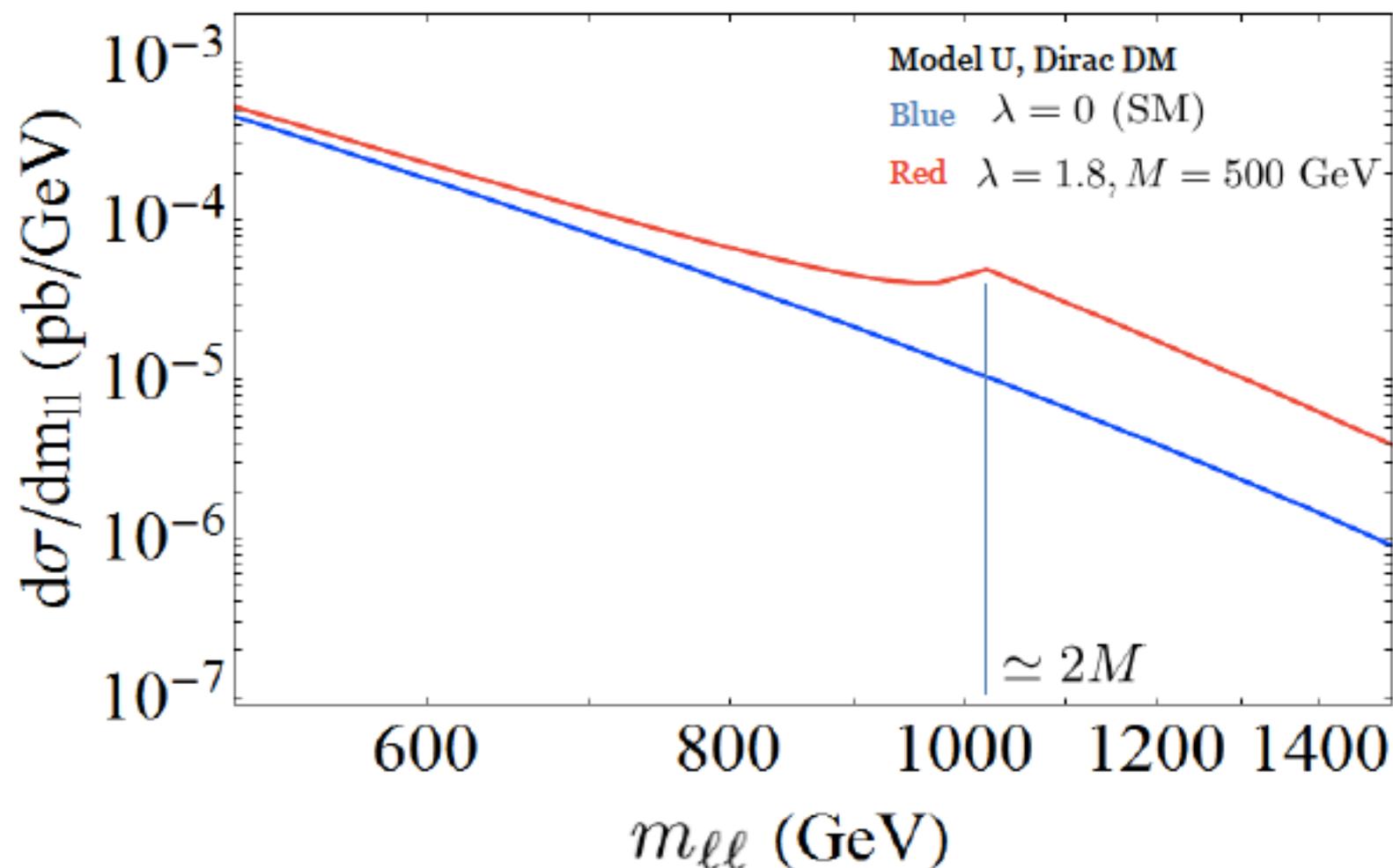
$$d\sigma_{\text{tree}} + d\sigma_{\text{box}}^{\text{real}} + d\sigma_{\text{box}}^{\text{imag}}$$

Breakdown of rates

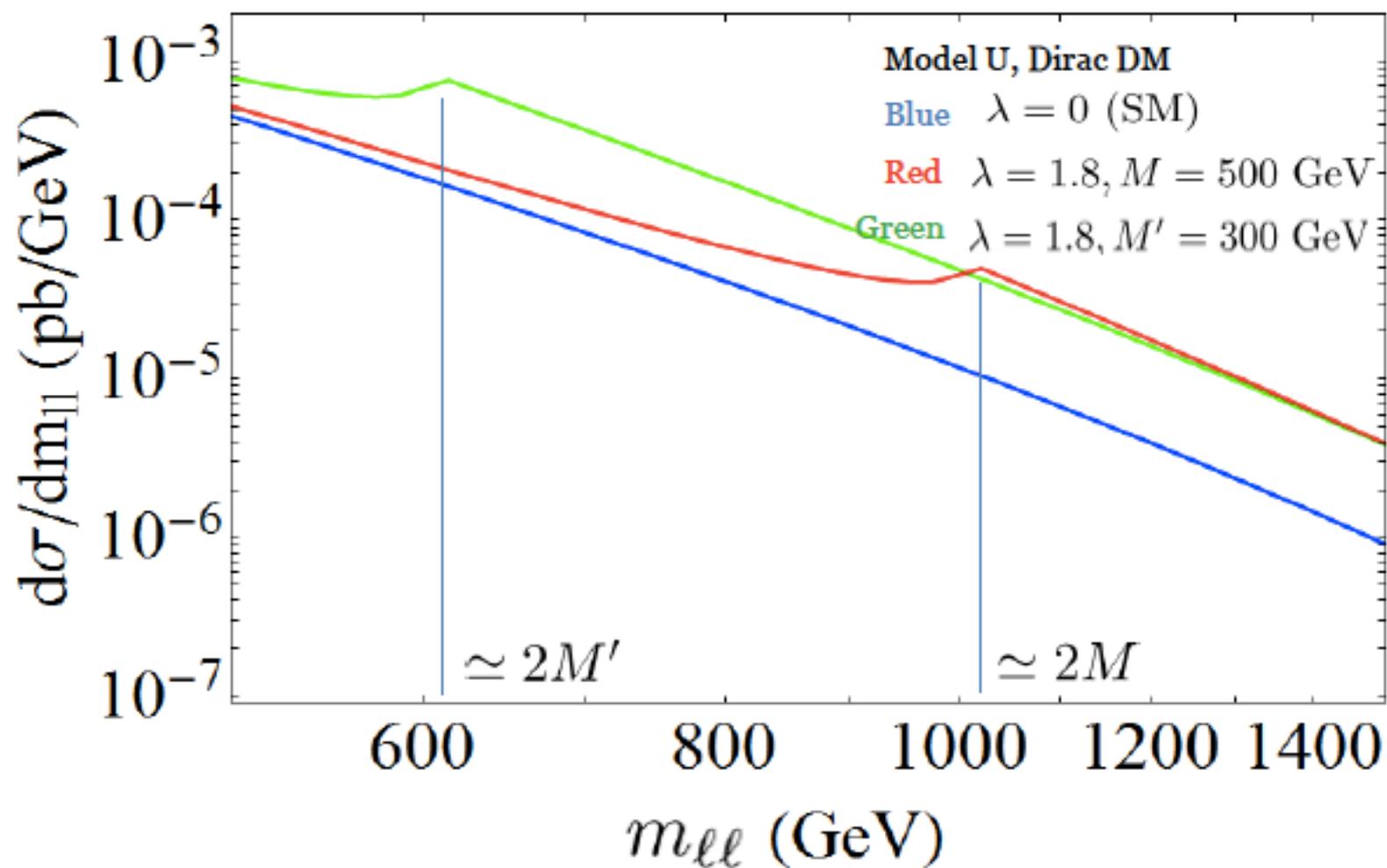


$$d\sigma_{\text{tree}} + d\sigma_{\text{int}} + d\sigma_{\text{box}}^{\text{real}} + d\sigma_{\text{box}}^{\text{imag}}$$

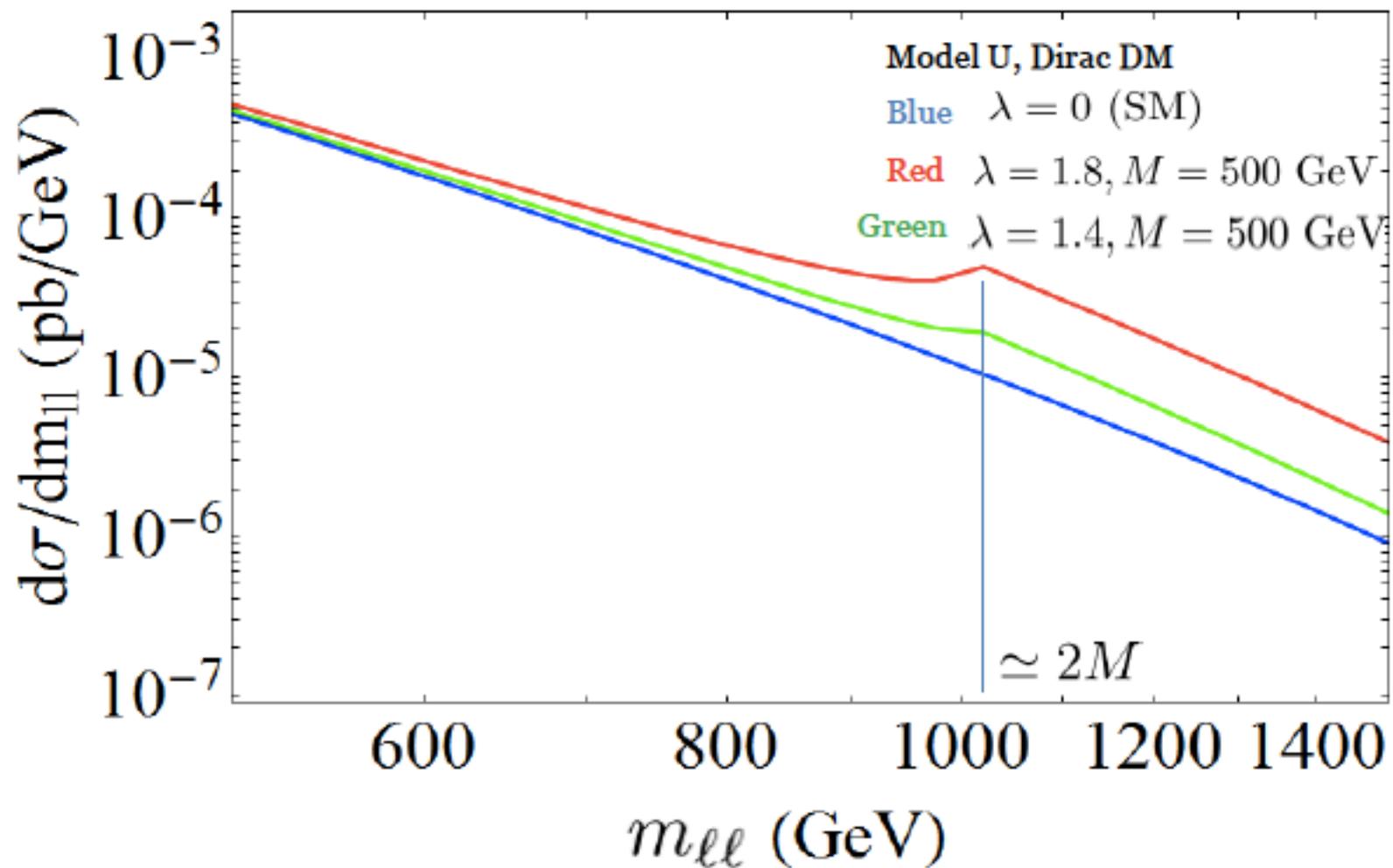
The signal (again)



Mass information

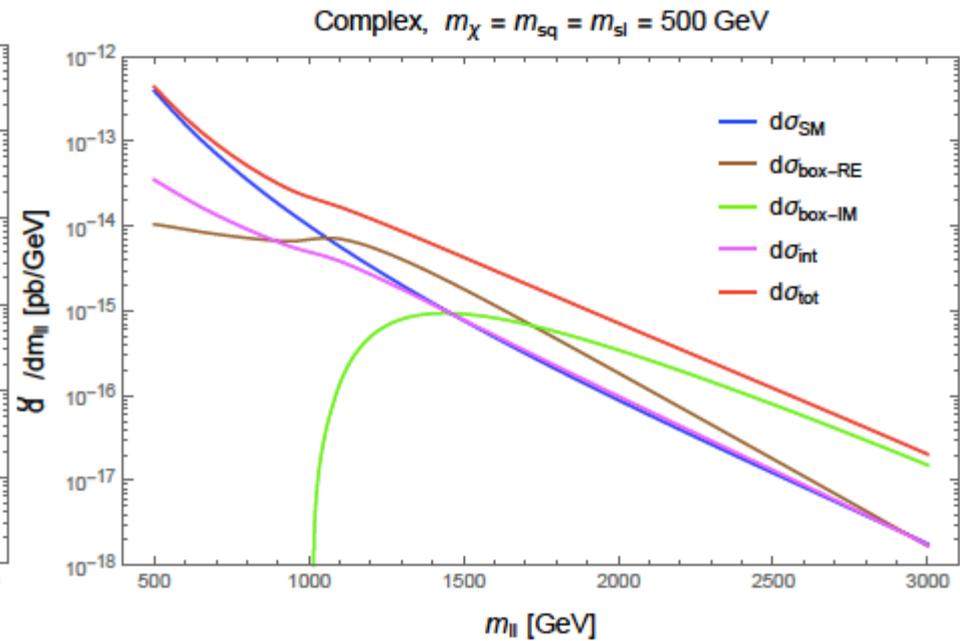
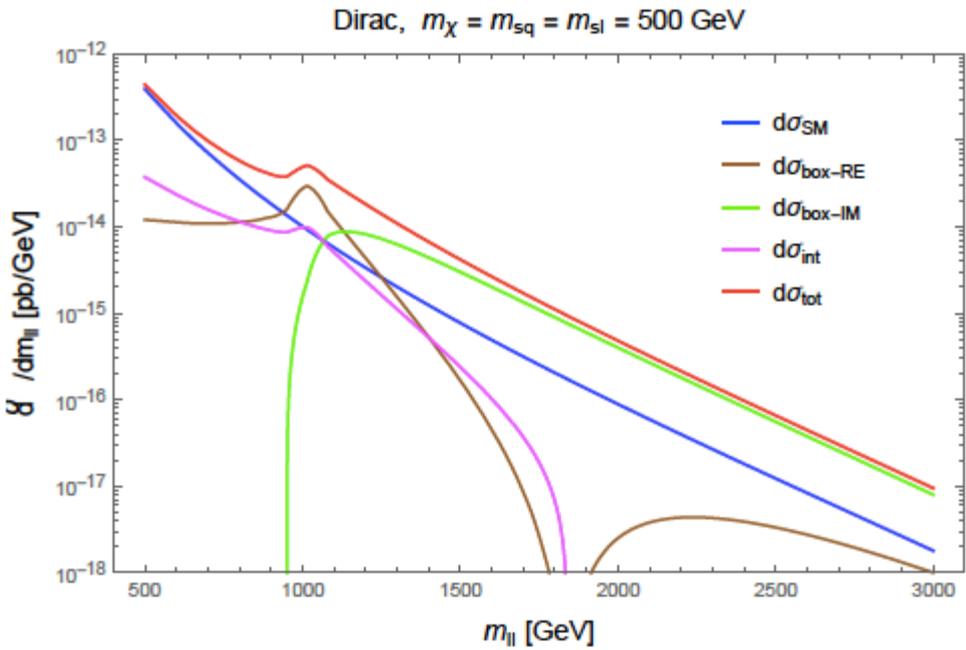


λ large: $d\sigma_{\text{box}}$ dominance



2) Numeric of Box Diagrams

Scalar vs. Fermion Boxes

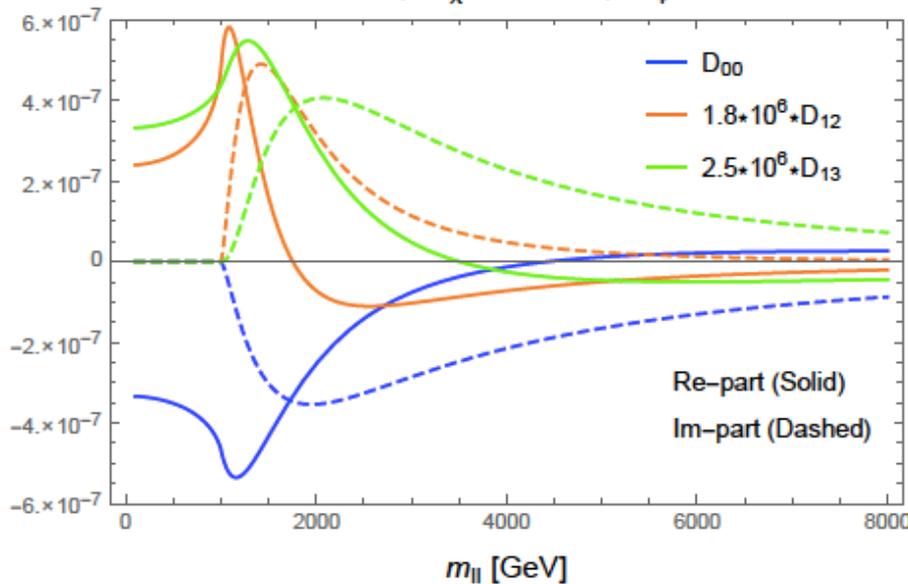


Scalar vs. Fermion Boxes

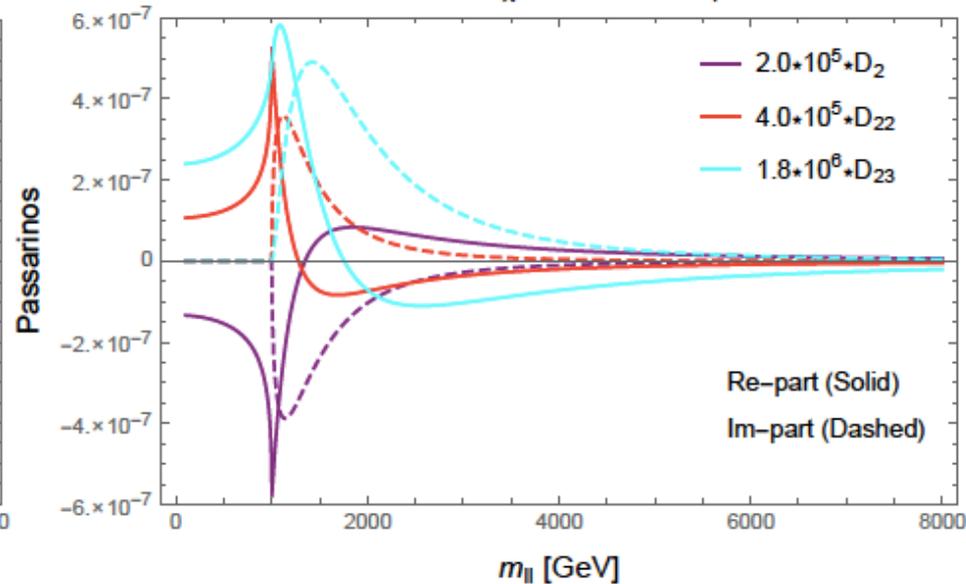
$$\left(\frac{d\hat{\sigma}}{d\hat{t}}\right)_{\text{Fermion } \chi}^{\text{Re}} = \frac{\lambda^8}{64\pi^4} (\hat{s} + \hat{t})^2 \text{Re} [2D_{00} + \hat{s} (D_2 + D_{12} + D_{22} + D_{23})]^2 \equiv d\sigma_{pD},$$

$$\left(\frac{d\hat{\sigma}}{d\hat{t}}\right)_{\text{Scalar } \chi}^{\text{Re}} = \frac{\lambda^8}{64\pi^4} (\hat{s} + \hat{t})^2 \text{Re} [-2D_{00} + \hat{t} D_{13}]^2 \equiv d\sigma_{pCS},$$

Case 1: $\hat{t} = 0$, $m_\chi = 0.5 \text{ TeV}$, $m_\phi = 0.5 \text{ TeV}$



Case 1: $\hat{t} = 0$, $m_\chi = 0.5 \text{ TeV}$, $m_\phi = 0.5 \text{ TeV}$



Scalar vs. Fermion Boxes

Assuming $\hat{t} = 0$, one can expand the functions $d\sigma_{pD}$ and $d\sigma_{pCS}$ (using Package-X)

$$d\sigma_{pD} (\hat{t} = 0) = \frac{1}{64\pi^4} m_{ll}^4 \lambda^8 \text{Re} [A_D + B_D + C_D]^2,$$

$$d\sigma_{pCS} (\hat{t} = 0) = \frac{1}{64\pi^4} m_{ll}^4 \lambda^8 \text{Re} [A_{CS} + B_{CS} + C_{CS}]^2,$$

where, for the Dirac case:

$$A_D = -\frac{2}{m_{ll}^2} \frac{m_\phi^2 (m_{ll}^2 + 2m_\phi^2 - 2m_\chi^2) \log (m_\phi^2/m_\chi^2)}{m_{ll}^2 [m_{ll}^2 m_\phi^2 + (m_\phi^2 - m_\chi^2)^2]},$$

$$B_D = -\frac{\sqrt{m_{ll}^2 (m_{ll}^2 - 4m_\chi^2)} [m_{ll}^2 m_\phi^2 + 2 (m_\phi^2 - m_\chi^2)^2]}{[m_{ll}^2 m_\phi^2 + (m_\phi^2 - m_\chi^2)^2]} \log [\text{Arg} (m_{ll}^2)],$$

$$C_D = -\frac{2 (m_\phi^2 - m_\chi^2)}{m_{ll}^2} \text{ScalarC0} [0, 0, m_{ll}^2, m_\chi^2, m_\phi^2, m_\chi^2],$$

$$\text{Arg} (m_{ll}^2) = \frac{-m_{ll}^2 + 2m_\chi^2 + \sqrt{m_{ll}^2 (m_{ll}^2 - 4m_\chi^2)}}{2m_\chi^2},$$

For degenerate DM-mediator masses, this contribution vanishes!

Scalar vs. Fermion Boxes

$$\text{ScalarC0} \rightarrow \frac{1}{2m_{ll}^2} \log [\text{Arg} (m_{ll}^2)]^2.$$

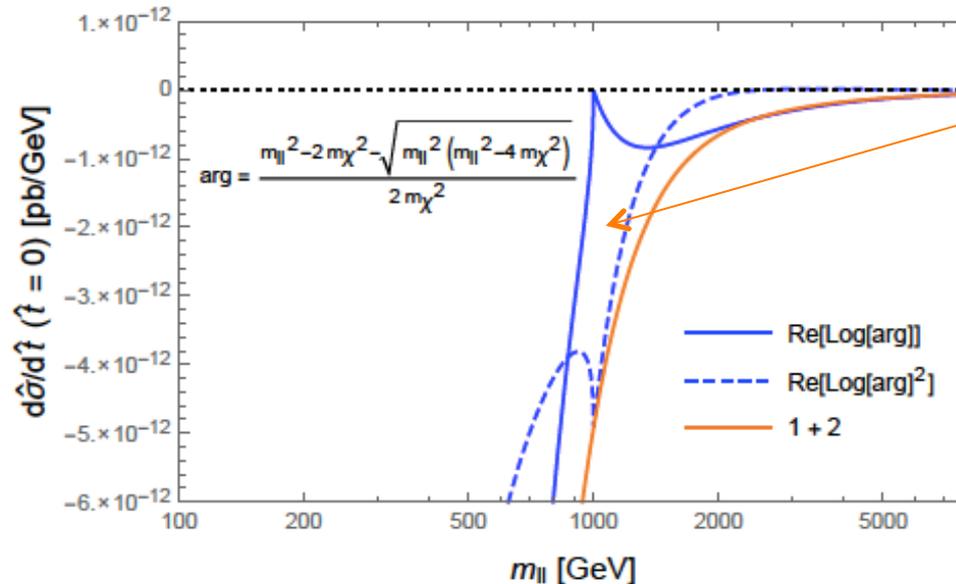
and for the scalar case:

$$A_{CS} = -\frac{2}{m_{ll}^2} - \frac{2m_\phi^2 \log (m_\phi^2/m_\chi^2)}{m_{ll}^2 (m_\phi^2 - m_\chi^2)},$$

$$B_{CS} = -\frac{2\sqrt{m_{ll}^2 (m_{ll}^2 - 4m_\chi^2)}}{m_{ll}^4} \log [\text{Arg} (m_{ll}^2)],$$

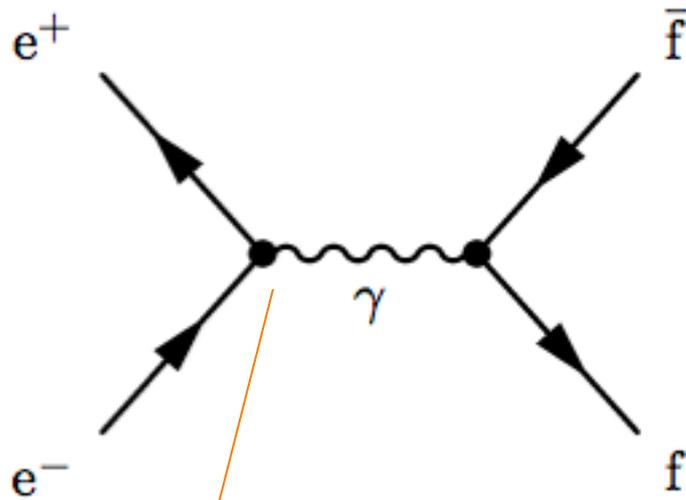
$$C_{CS} = -\frac{m_{ll}^2 + 2 (m_\phi^2 - m_\chi^2)}{m_{ll}^2} \text{ScalarC0} [0, 0, m_{ll}^2, m_\chi^2, m_\phi^2, m_\chi^2].$$

Scalar case presents log vs. log-squared cancellations at the threshold



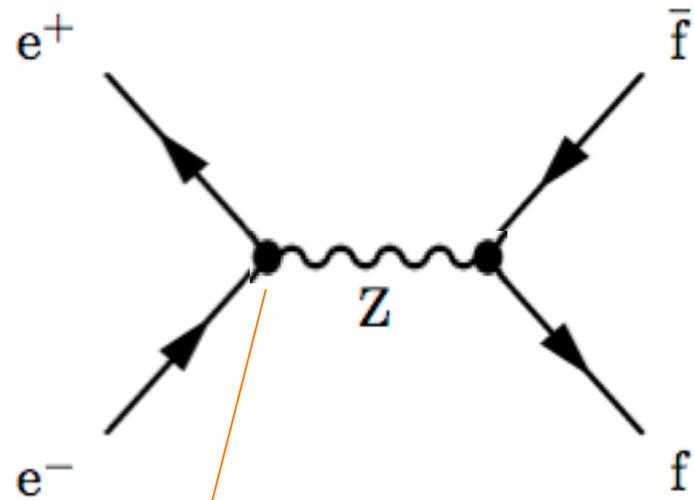
The line 1 + 2 is the sum of the purple solid and dashed lines.

3) Forward-Backward Asymmetry



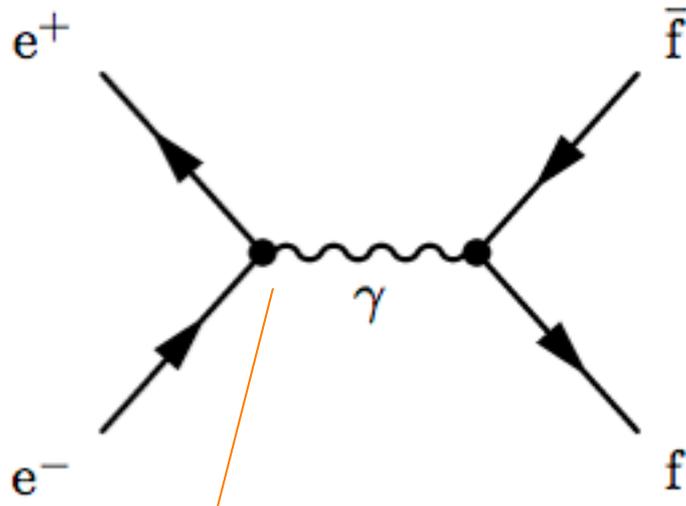
$$\gamma_\mu$$

$$\frac{d\sigma}{d\Omega} \propto (1 + \cos^2 \theta)$$



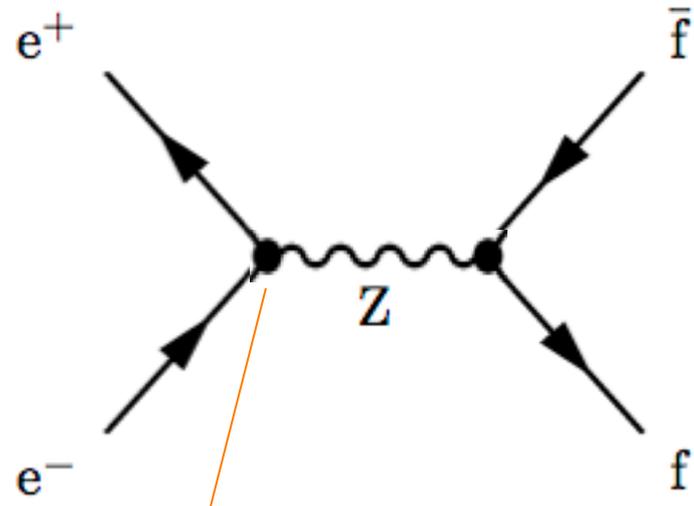
$$(c_V + c_A \gamma_5) \gamma_\mu$$

$$\frac{d\sigma}{d\Omega} \propto (1 + \cos^2 \theta) + a \cos \theta$$



$$\gamma_\mu$$

$$\frac{d\sigma}{d\Omega} \propto (1 + \cos^2 \theta)$$



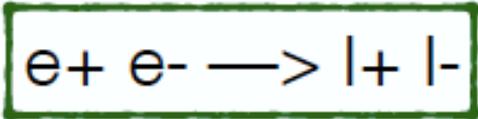
$$(c_V + c_A \gamma_5) \gamma_\mu$$

$$\frac{d\sigma}{d\Omega} \propto (1 + \cos^2 \theta) + a \cos \theta$$

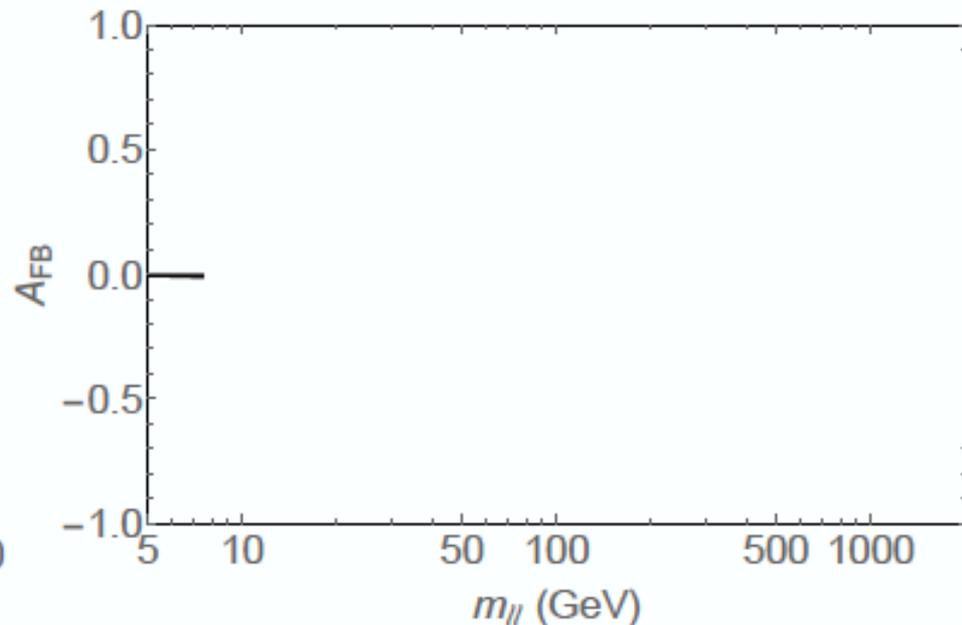
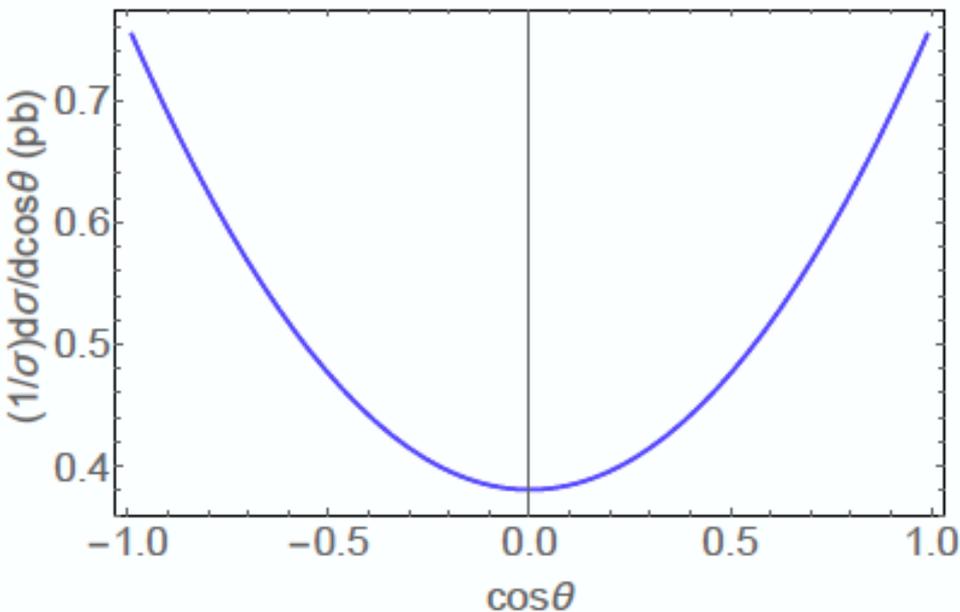
Out[87]= $(1 + \cos^2 \theta) e^4 Q_f^2$

Out[86]=
$$\frac{(8 a_l a_q b_l b_q \cos \theta + a_l^2 (a_q^2 + b_q^2) (1 + \cos^2 \theta) + b_l^2 (a_q^2 + b_q^2) (1 + \cos^2 \theta)) g^4 \sin^2 \theta}{16 c_W^4 (m_Z^4 + \sin^2 \theta + m_Z^2 (-2 \sin^2 \theta - 5 \Gamma_Z^2))}$$

Forward-backward asymmetry



$m_{ll} \sim 10 \text{ GeV}$

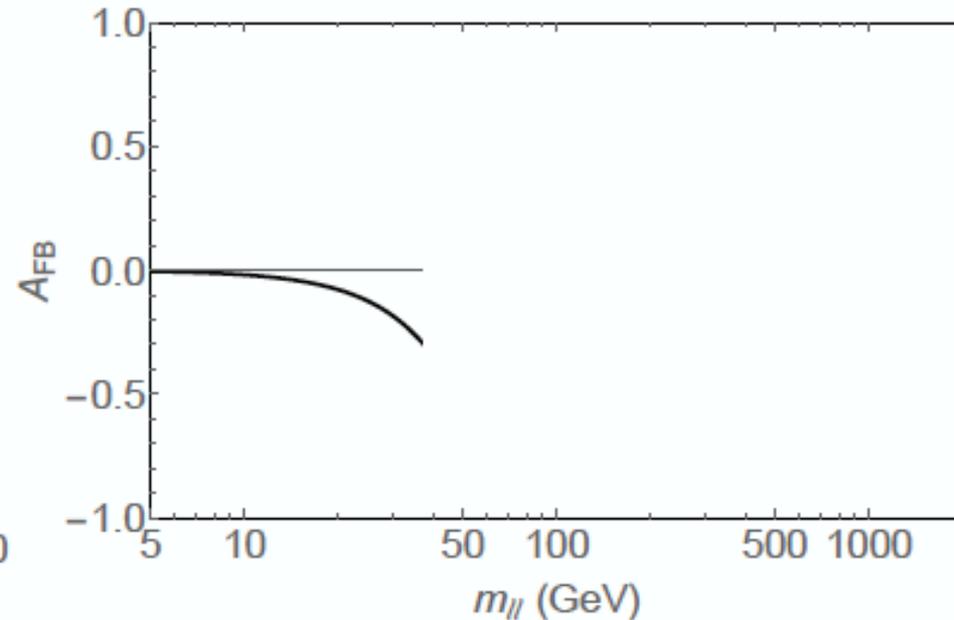
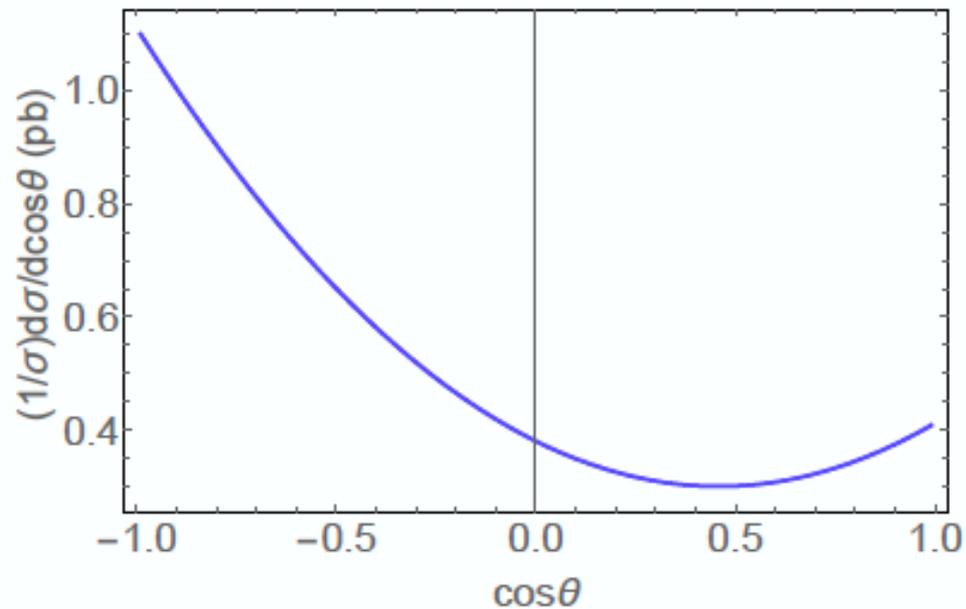


$A_{\text{FB}} = \text{area of right half minus left half}$
(normalized with total area)

Forward-backward asymmetry

$$e^+ e^- \longrightarrow l^+ l^-$$

$m_{ll} = 40 \text{ GeV}$

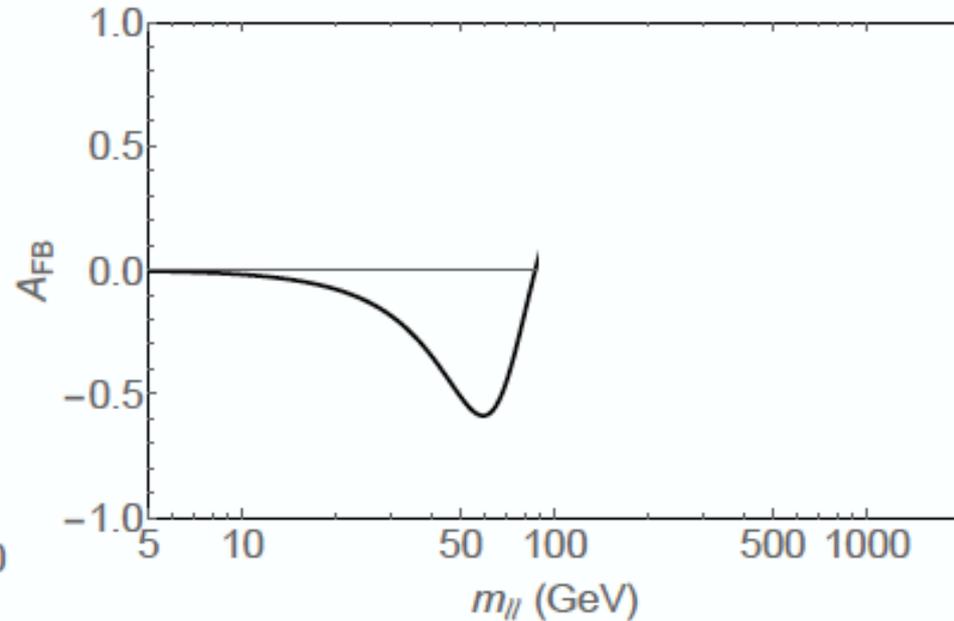
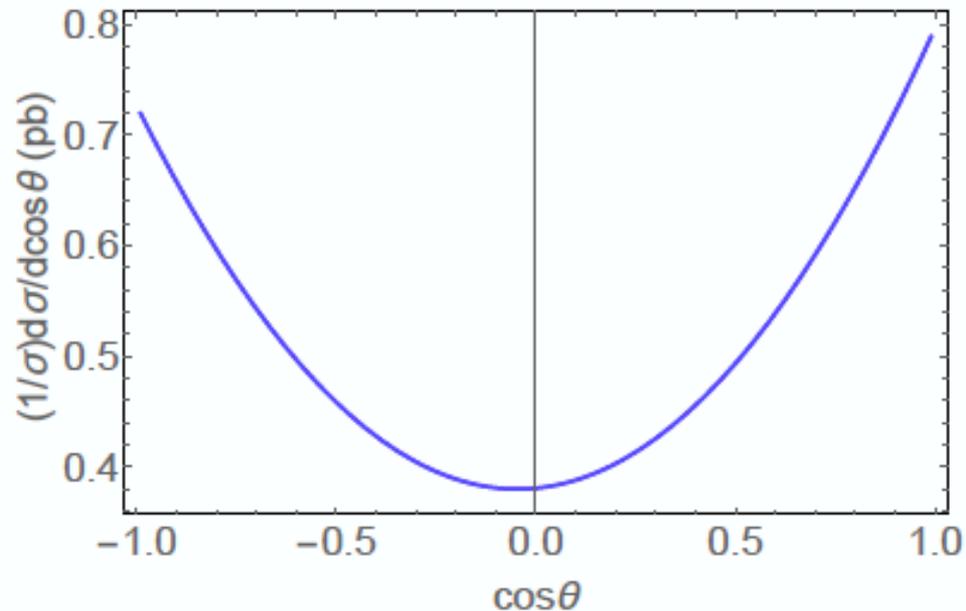


$A_{FB} = \text{area of right half minus left half}$
(normalized with total area)

Forward-backward asymmetry

$$e^+ e^- \longrightarrow l^+ l^-$$

$m_{ll} = 88 \text{ GeV}$

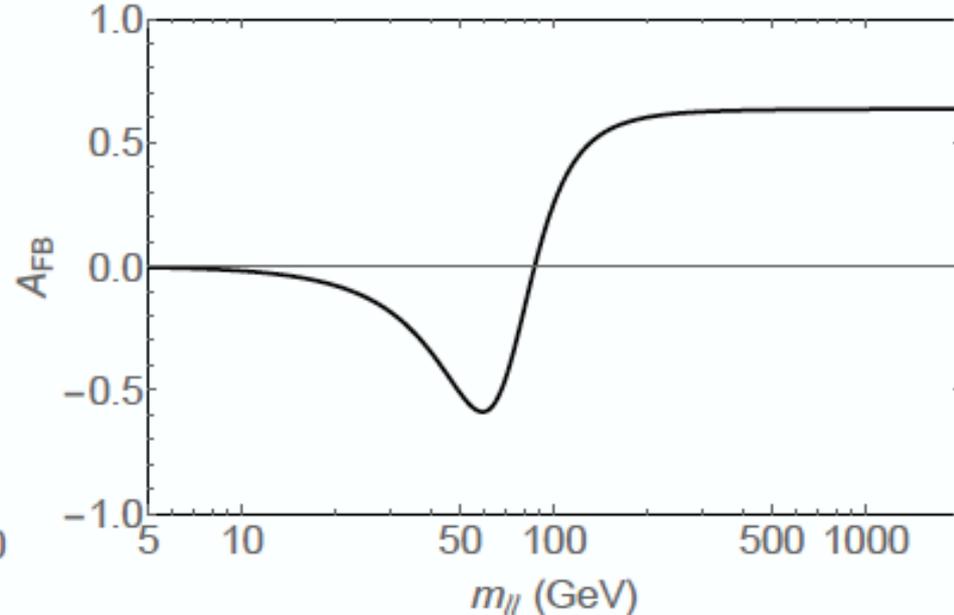
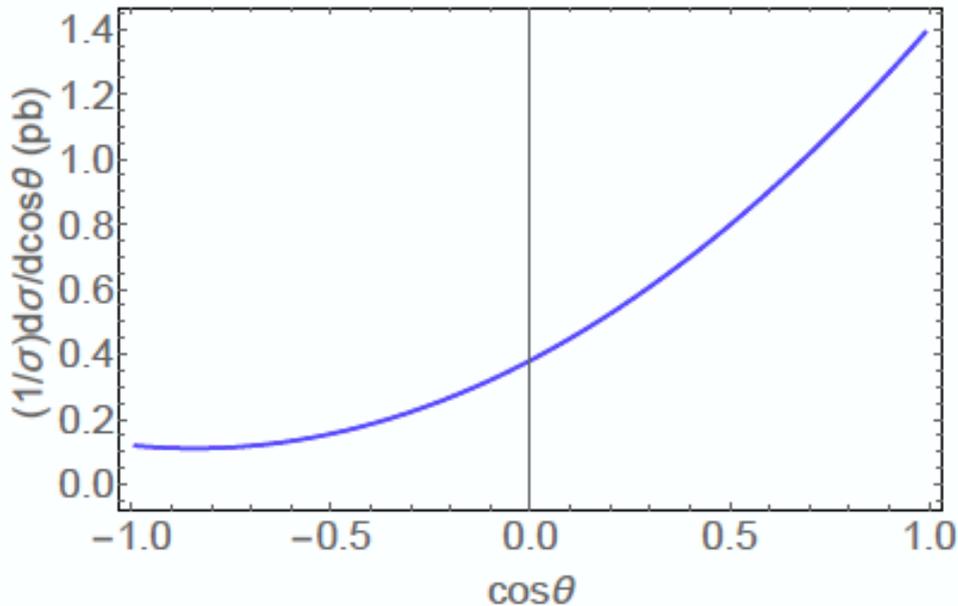


$A_{FB} = \text{area of right half minus left half}$
(normalized with total area)

Forward-backward asymmetry

$$e^+ e^- \rightarrow l^+ l^-$$

$m_{ll} \gg M_Z$



A_{FB} = area of right half minus left half
(normalized with total area)