A Cosmologist's Perspective on Higgs Factories

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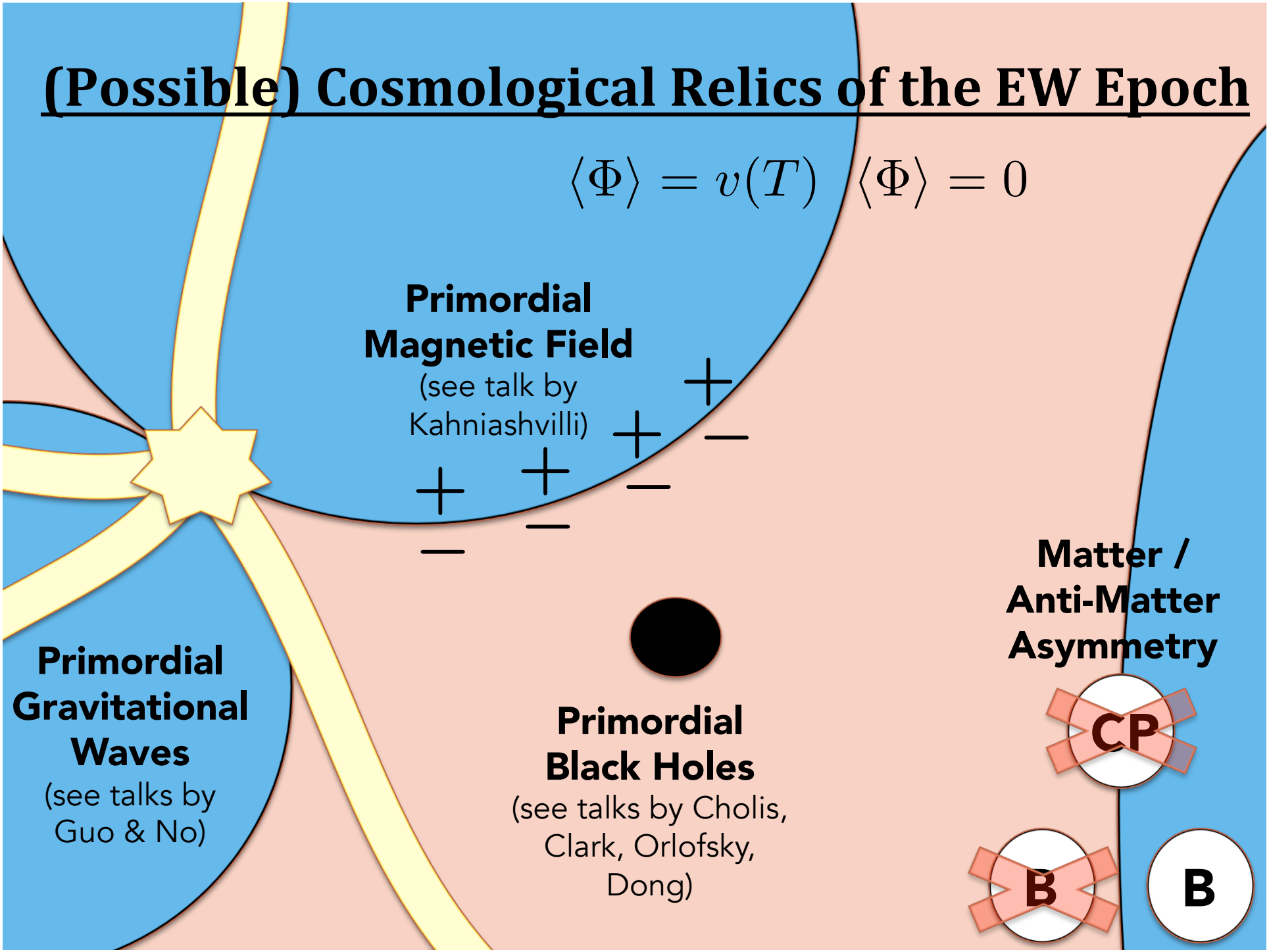
based on [1608.06619, PRD] with *Peisi Huang* & Lian-Tao Wang

Why are cosmologists interested in Higgs factories?

(Possible) Cosmological Relics of the EW Epoch



Cosmologists want to better understand the EW phase transition:

First Order (bubbles)?

Critical temperature?

Latent heat?

Wall velocity?

Duration?

Turbulence?

Charge transport?

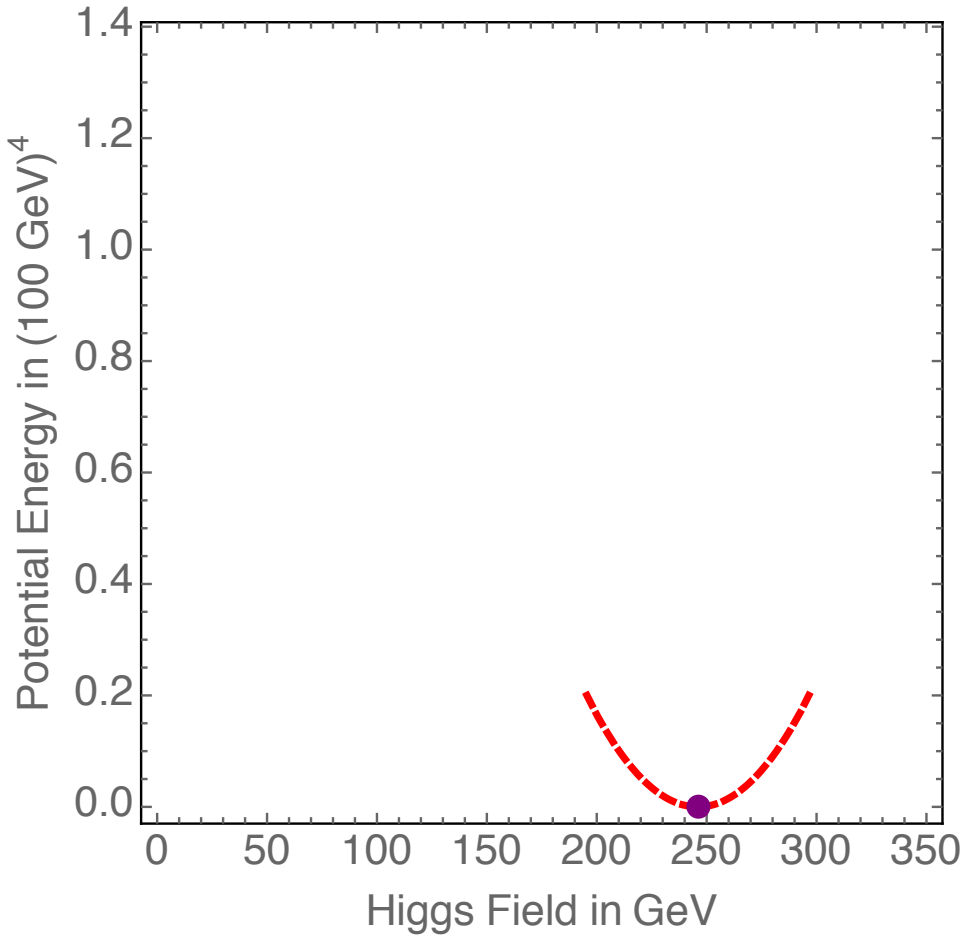
…

In order to make robust predictions, for these cosmological relics, we must first have a firm understanding of the physics of the Higgs boson.

We discovered the Higgs!

We know that it's responsible for EW symmetry breaking!

Isn't that enough information to let us study the EW phase transition?

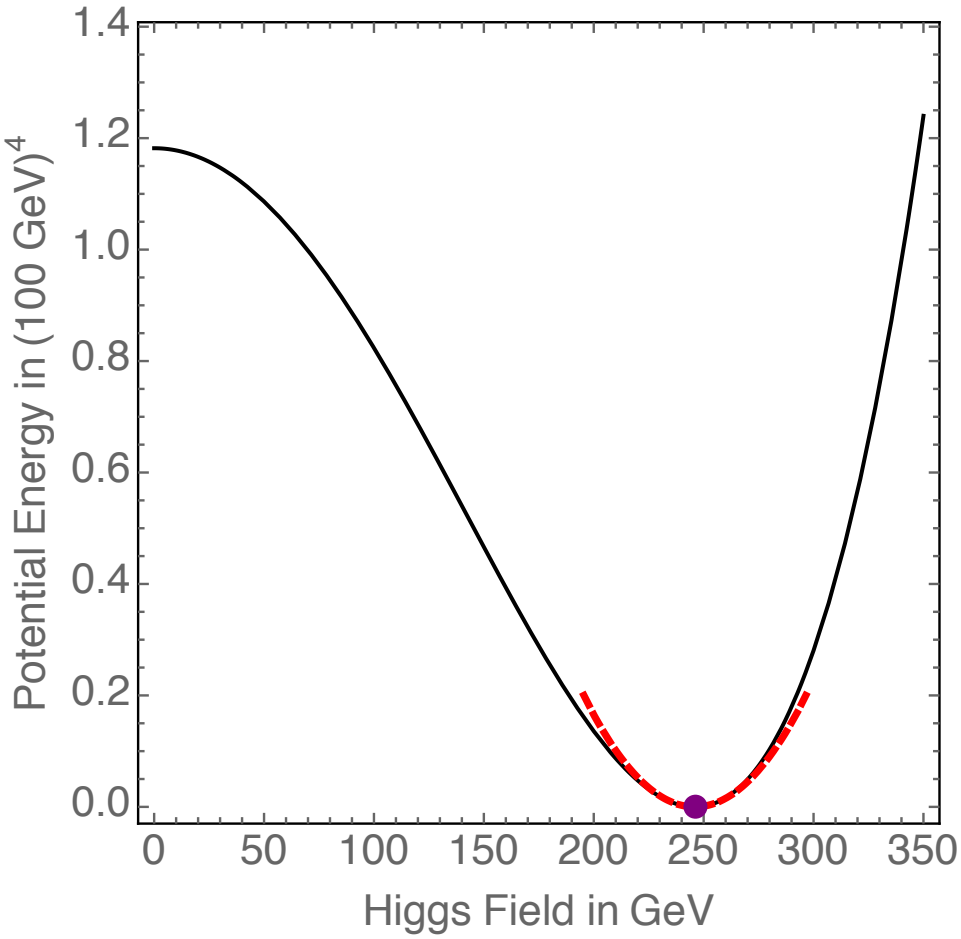


Measured Directly:

$$v \simeq 246 \text{ GeV}$$

$$M_h \simeq 125 \text{ GeV}$$

Assuming SM particle content & interactions



$$V = -\mu^2 H^\dagger H + \lambda_h (H^\dagger H)^2$$

$$\begin{cases} \mu^2 = M_h^2/2 \simeq (88\ \mathrm{GeV})^2 \\ \lambda_h = M_h^2/(2v^2) \simeq 0.13 \end{cases}$$

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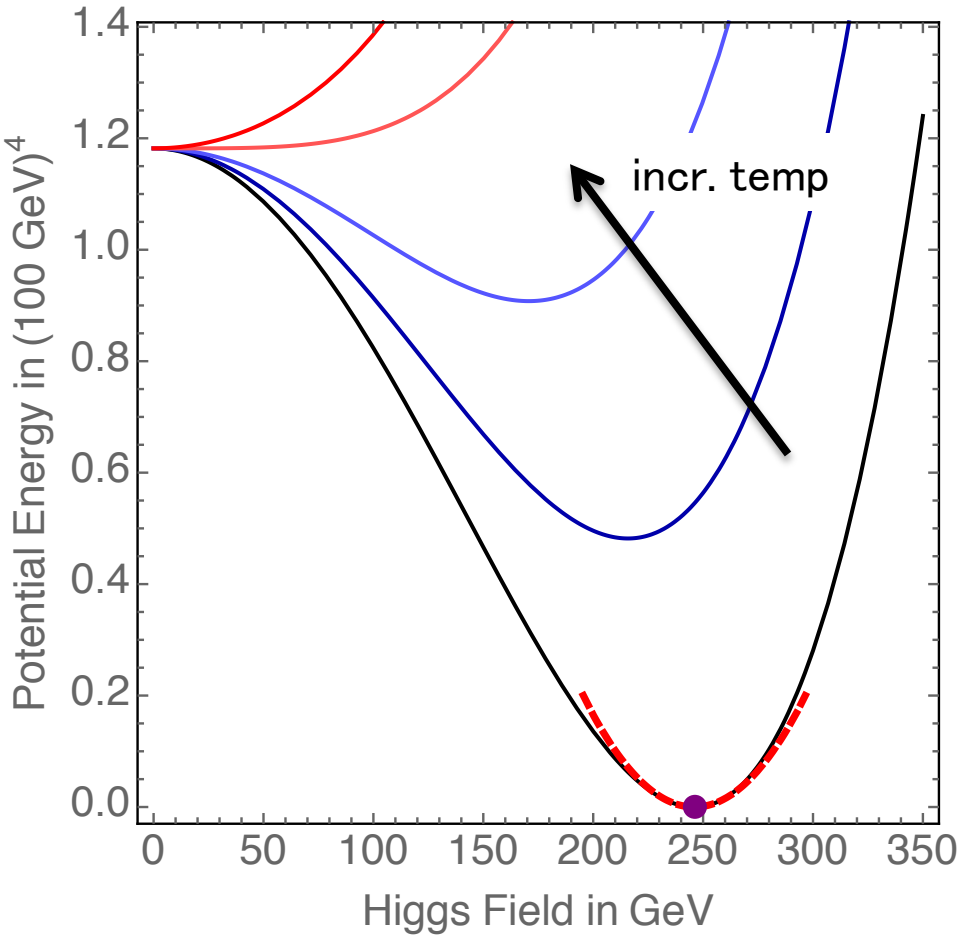

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Thermal support from Higgs interactions with W, Z, t, ...

- EWPT is continuous crossover
- v(T) changes smoothly
- No energy barrier; no bubbles; no cosmological relics

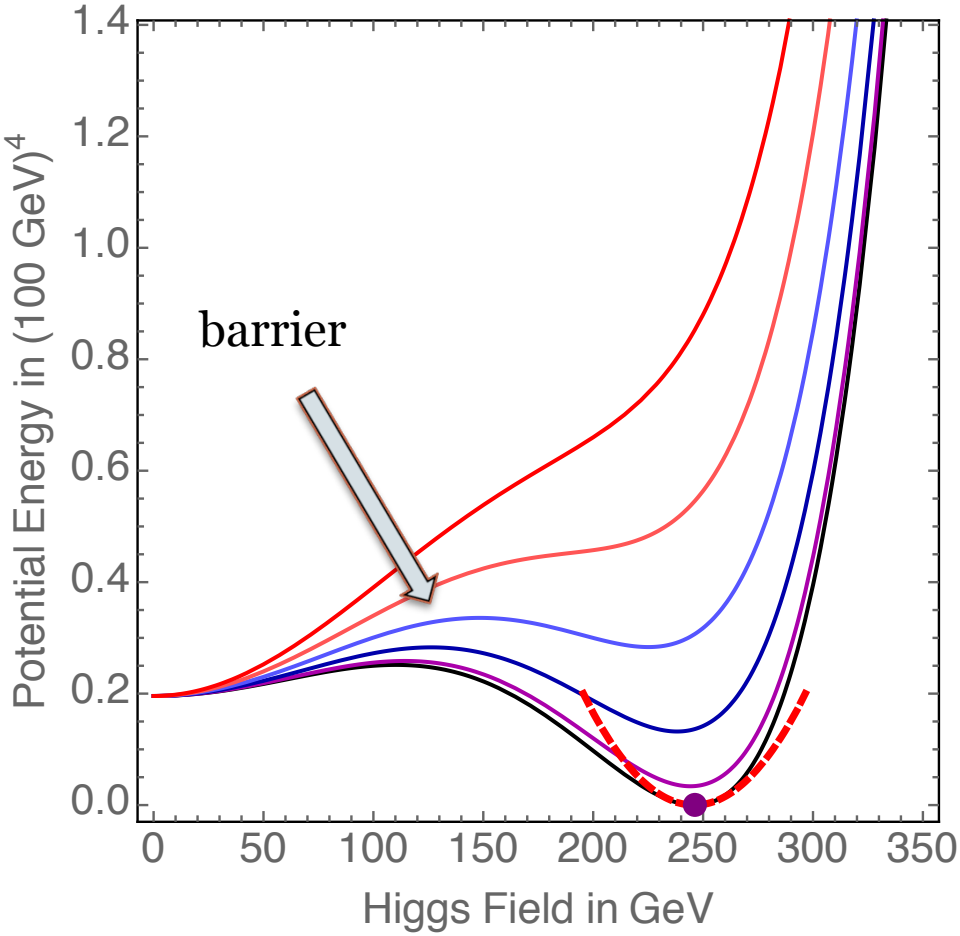
Measured Directly:

$$v \simeq 246\ \mathrm{GeV}$$

$$M_h \simeq 125\ \mathrm{GeV}$$

Variant #1 –SM with low cutoff

Recently studied by
P. Huang, Jokelar, Li, Wagner (2015)
F.P. Huang, Gu, Yin, Yu, Zhang (2015)
F.P. Huang, Wan, Wang, Cai, Zhang (2016)



$$V = \mu^2 H^\dagger H - \lambda_h (H^\dagger H)^2 + \Lambda^{-2}(H^\dagger H)^3$$

$$\begin{cases} \mu^2 \simeq (44\ \text{GeV})^2 \\ \lambda_h \simeq 0.19 \\ \Lambda \simeq 530\ \text{GeV} \end{cases}$$

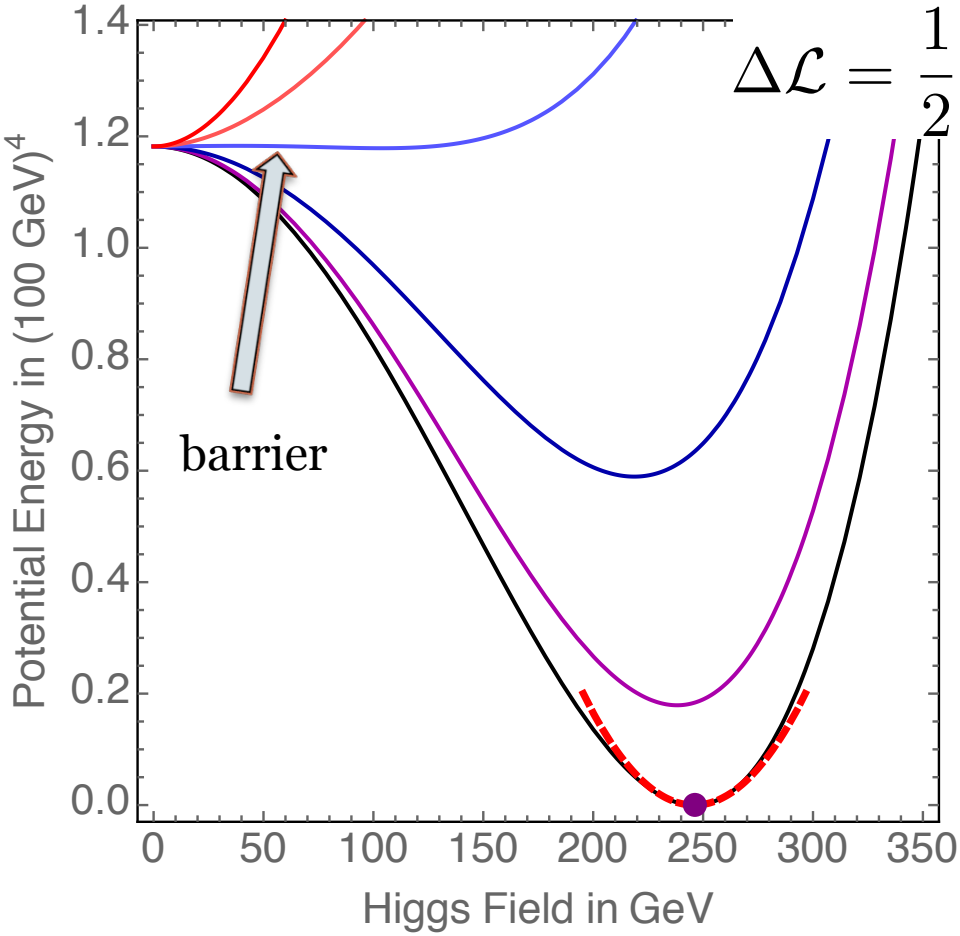
Energy barrier may be present already at T=0.

- EWPT is first order
- Possibly interesting cosmological relics!

Measured Directly:

$$v \simeq 246\ \text{GeV}$$
$$M_h \simeq 125\ \text{GeV}$$

Variant #2 –SM with new EW-scale matter coupled to Higgs



$$\Delta\mathcal{L} = \frac{1}{2}\left(\partial\phi_s\right)^2 - \frac{1}{2}m_s^2\phi_s^2 - \lambda_{hs}H^\dagger H\phi_s^2$$

The presence of new particles in the EW plasma can induce an energy barrier.

Heuristic understanding: these particles get their mass (in part) from the Higgs. It costs energy to bring <H> away from zero.

Measured Directly:

$$v \simeq 246 \text{ GeV}$$

$$M_h \simeq 125 \text{ GeV}$$

What can future colliders teach us about the electroweak phase transition?

In models with a first order EW phase transition, there must be new physics coupled to the Higgs.

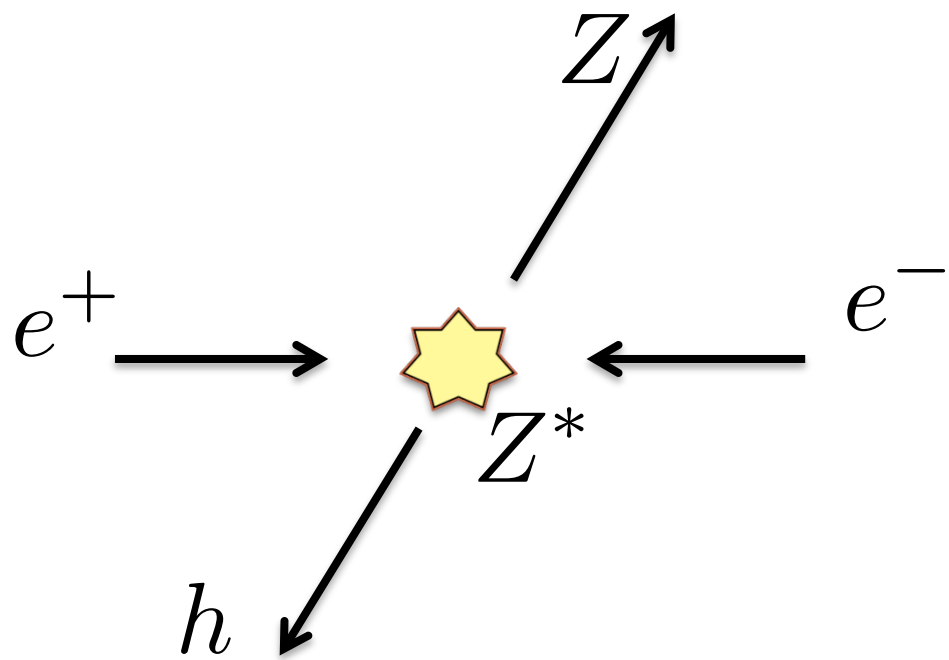
It is reasonable to expect that this NP may also induce deviations in the Higgs couplings with other SM fields.

Precision Measurements w/ Higgs Factories

Lepton colliders provide "clean" environment for studying Higgs physics.

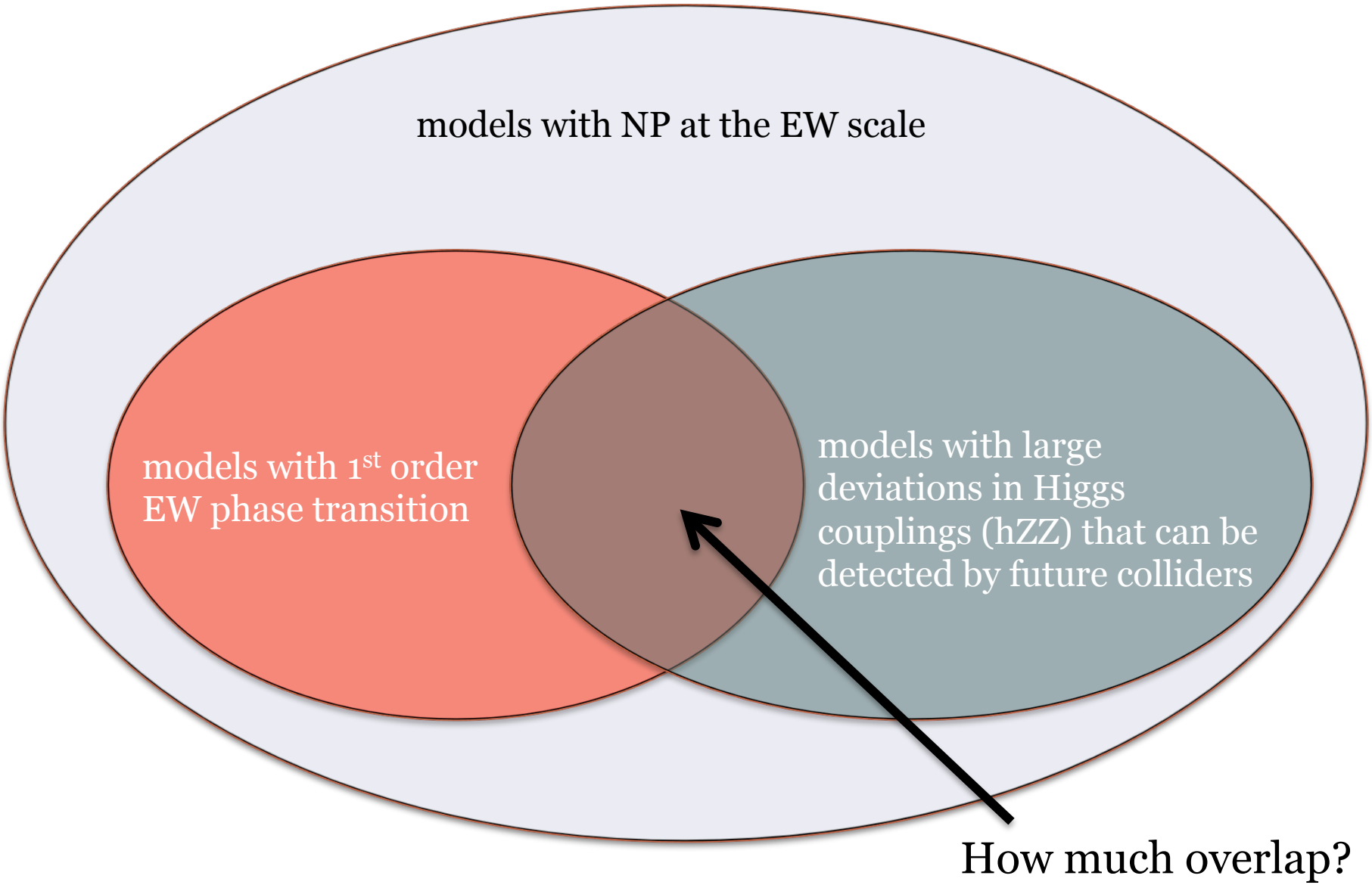
At E ~ 250 GeV, the production of Higgs + Z-boson is optimized.

Expect to achieve precision Higgs-Z-Z measurements at the sub-percent level!



Projected Sensitivities to various Higgs couplings at different future colliders:

	current	HL-LHC	CEPC-250	ILC-500	FCC-ee	FCC-hh
hZZ	27%	7%	0.25%	0.25%	0.15%	-
$\Gamma(h\rightarrow\gamma\gamma)$	20%	8%	4%	-	1.5%	-
hhh	N/A	-	-	27%	-	10%


models with NP at the EW scale
models with 1st order EW phase transition
models with large deviations in Higgs couplings (hZZ) that can be detected by future colliders
How much overlap?

What Kinds of Models?

Model	References
SM + Scalar Singlet	Espinosa & Quiros, 1993; Benson, 1993; Choi & Volkas, 1993; McDonald, 1994; Vergara, 1996; Branco, Delepine, Emmanuel-Costa, & Gonzalez, 1998; Ham, Jeong, & Oh, 2004; Ahriche, 2007; Espinosa & Quiros, 2007; Profumo, Ramsey-Musolf, & Shaughnessy, 2007; Noble & Perelstein, 2007; Espinosa, Konstandin, No, & Quiros, 2008; Ashoorioon & Konstandin, 2009; Das, Fox, Kumar, & Weiner, 2009; Espinosa, Konstandin, & Riva, 2011; Chung & AL, 2011; Wainwright, Profumo, & Ramsey-Musolf, 2012; Barger, Chung, AL, & Wang, 2012; Huang, Shu, Zhang, 2012; Jiang, Bian, Huang, Shu, 2015; Huang & Li 2015; Chen, Kozaczuk, & Lewis (2017)
SM + Scalar Doublet	Davies, Froggatt, Jenkins, & Moorhouse, 1994; Huber, 2006; Fromme, Huber, & Seniuch, 2006; Cline, Kainulainen, & Trott, 2011; Kozhushko & Skalozub, 2011;
SM + Scalar Triplet	Patel, Ramsey-Musolf, 2012; Patel, Ramsey-Musolf, Wise, 2013; Huang, Gu, Yin, Yu, Zhang 2016
SM + Chiral Fermions	Carena, Megevand, Quiros, Wagner, 2005
MSSM	Carena, Quiros, & Wagner, 1996; Delepine, Gerard, Gonzales Felipe, & Weyers, 1996; Cline & Kainulainen, 1996; Laine & Rummukainen, 1998; Cohen, Morrissey, & Pierce,; Carena, Nardini, Quiros, & Wagner, 2012;
NMSSM / nMSSM / μνSSM	Pietroni, 1993; Davies, Froggatt, & Moorhouse, 1995; Huber & Schmidt, 2001; Ham, Oh, Kim, Yoo, & Son, 2004; Menon, Morrissey, & Wagner, 2004; Funakubo, Tao, & Toyoda, 2005; Huber, Kontandin, Prokopec, & Schmidt, 2006; Chung, AL, 2010, Huang, Kang, Shu, Wu, Yang, 2014
EFT-like Approach (H^6 operator)	Grojean, Servant, Wells, 2005; Huang, Gu, Yin, Yu, Zhang 2015; Huang, Joglekar, Li, Wagner, 2015; Huang, Wan, Wang, Cai, Zhang 2016; Huang, Gu, Yin, Yu, Zhang 2016

A Survey of Simplified Models

Model #1 – SM + chiral fermions (like MSSM gauginos)

Model #2 – SM + scalar doublet (like MSSM stops)

Model #3 – SM + real scalar singlet (like NMSSM singlet)

In the simplified / minimal models, the new degrees of freedom are responsible for *both* the 1PT and hZZ

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SM + Scalar Doublet ("stops")

In the MSSM, the stops play a critical role in making the EWPT first order. Here we considered a simplified version of the SUSY stop sector.

$$\tilde{Q} \sim (\mathbf{1}, \mathbf{2}, 1/3) \times 3 \text{ flavor}$$

$$\tilde{U} \sim (\mathbf{1}, \mathbf{1}, 4/3) \times 3 \text{ flavor}$$

four model parameters

The full Lagrangian is

$$\begin{aligned}\mathcal{L} = \mathcal{L}_{\text{SM}} &+ \left(D_\mu \tilde{Q}\right)^\dagger \left(D^\mu \tilde{Q}\right) + \left(D_\mu \tilde{U}\right)^* \left(D^\mu \tilde{U}\right) - \left[a_{hQU} \tilde{Q} \cdot H \tilde{U}^* + \text{h.c.}\right] \\ &- m_Q^2 \tilde{Q}^\dagger \tilde{Q} - m_U^2 \tilde{U}^* \tilde{U} - \lambda_Q \left(\tilde{Q}^\dagger \tilde{Q}\right)^2 - \lambda_U \left(\tilde{U}^* \tilde{U}\right)^2 \\ &- \lambda_{QU} \left(\tilde{Q}^\dagger \tilde{Q}\right)\left(\tilde{U}^* \tilde{U}\right) - \lambda_{hU} \left(H^\dagger H\right)\left(\tilde{U}^* \tilde{U}\right) \\ &- \lambda_{hQ} \left(H^\dagger H\right)\left(\tilde{Q}^\dagger \tilde{Q}\right) - \lambda'_{hQ} \left(\tilde{Q} \cdot H\right)^* \left(\tilde{Q} \cdot H\right) - \lambda''_{hQ} \left(\tilde{Q}^\dagger H\right)^* \left(\tilde{Q}^\dagger H\right)\end{aligned}$$

and for simplicity we focus on

$$\langle \tilde{Q} \rangle = (0\,,\,0) \qquad \text{and} \qquad \langle \tilde{U} \rangle = 0$$

$$\lambda_Q = \lambda_U = \lambda_{QU} = \lambda_{hU} = \lambda_{hQ} = \lambda'_{hQ} = \lambda''_{hQ} \equiv \lambda$$

Spectrum

$$M_{\tilde{t}}^2 = \begin{pmatrix} m_Q^2 + \frac{1}{2}(\lambda_{hQ} + \lambda'_{hQ})v^2 & \frac{a_{hQU}v}{\sqrt{2}} \\ \frac{a_{hQU}v}{\sqrt{2}} & m_U^2 + \frac{1}{2}\lambda_{hU}v^2 \end{pmatrix}$$

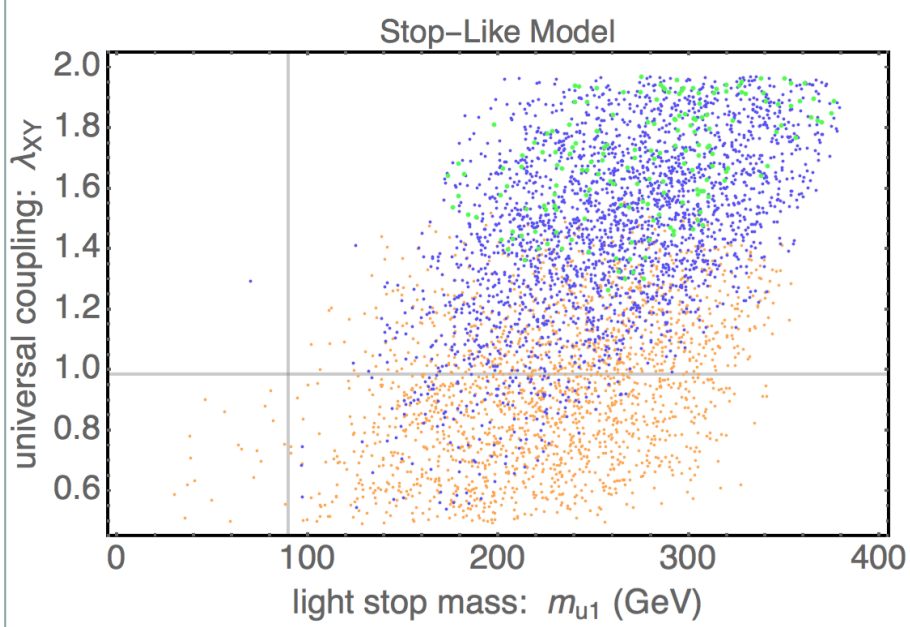
2 “stops”

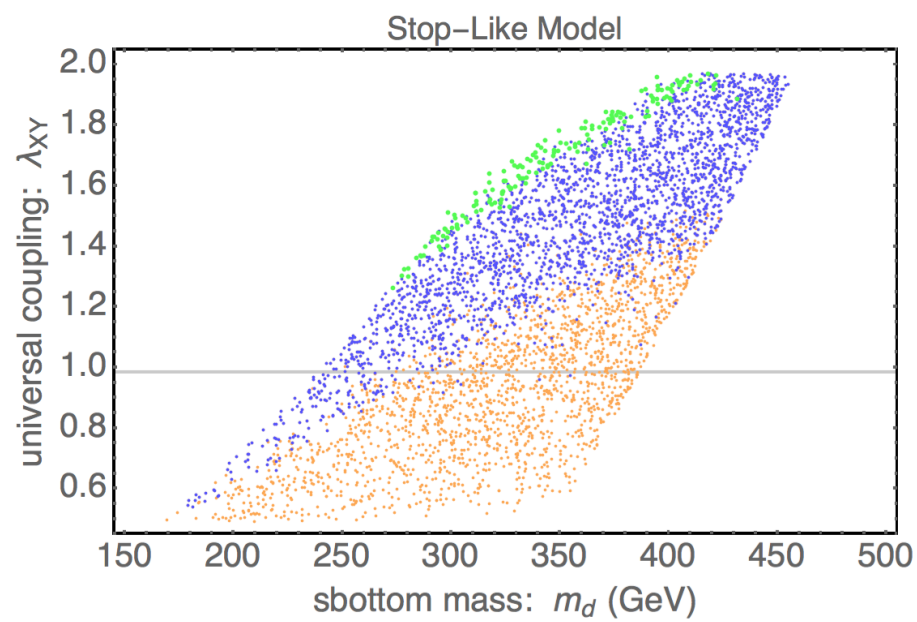
$$\tan 2\theta = \frac{\sqrt{2}a_{hQU}v}{m_Q^2 - m_U^2 + \frac{1}{2}(\lambda_{hQ} + \lambda'_{hQ} - \lambda_{hU})v^2}$$

(mixing)

$$M_{\tilde{b}}^2 = m_Q^2 + \frac{1}{2}(\lambda_{hQ} + \lambda''_{hQ})v^2$$

1 “sbottom”



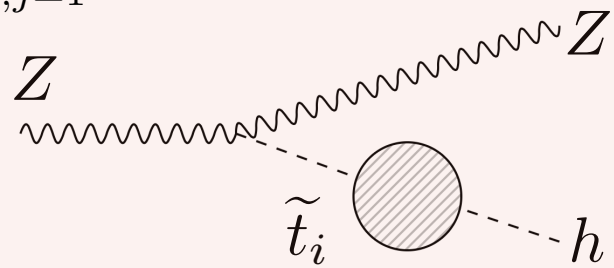


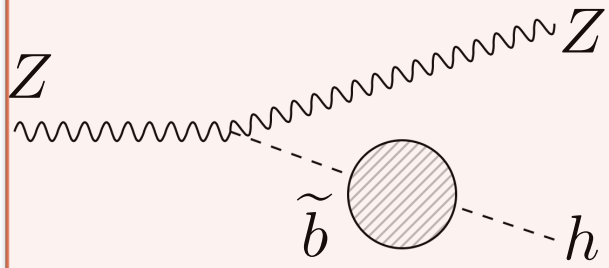
Effective hZZ coupling

(adapted from: Fan, Reece, Wang, 2014)

+vertex correction (suppressed by g/λ)

$$\delta g_{hZZ} = n_f \sum_{i,j=1}^{2} \frac{|g_{h\tilde{t}_i\tilde{t}_j}|^2}{32\pi^2} I_B(M_h^2; M_{\tilde{t}_i}^2, M_{\tilde{t}_j}^2) + n_f \frac{|g_{h\tilde{b}\tilde{b}}|^2}{32\pi^2} I_B(M_h^2; M_{\tilde{b}}^2, M_{\tilde{b}}^2)$$





$$g_{h\tilde{t}_1\tilde{t}_1} = -\cos^2\theta\,(\lambda_{hQ} + \lambda'_{hQ})v - \sin^2\theta\,\lambda_{hU}v + \frac{a_{hQU}\sin 2\theta}{\sqrt{2}}$$

$$g_{h\tilde{t}_2\tilde{t}_2} = -\sin^2\theta\,(\lambda_{hQ} + \lambda'_{hQ})v - \cos^2\theta\,\lambda_{hU}v - \frac{a_{hQU}\sin 2\theta}{\sqrt{2}}$$

$$g_{h\tilde{t}_1\tilde{t}_2} = -\frac{\sin 2\theta}{2}(\lambda_{hQ} + \lambda'_{hQ})v + \frac{\sin 2\theta}{2}\lambda_{hU}v - \frac{a_{hQU}\cos 2\theta}{\sqrt{2}}$$

$$g_{h\tilde{b}\tilde{b}} = -(\lambda_{hQ} + \lambda''_{hQ})v$$

$$\delta g_{hZZ} \equiv \frac{g_{hZZ}}{g_{hZZ,\mathrm{SM}}} - 1\Big|_{s=(250\ \mathrm{GeV})^2}$$

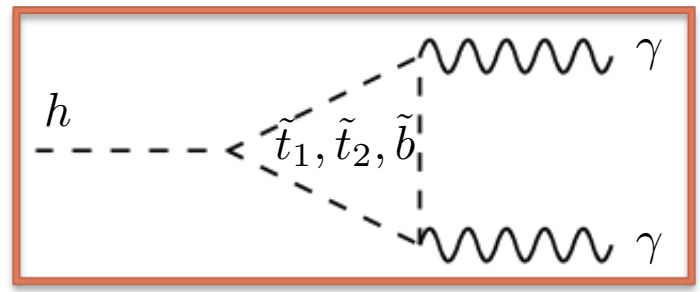
Higgs di-photon decay width

(adapted from: Djouadi, Driesen, Hollik, Illana, 2005)

$$\Gamma_{h\to\gamma\gamma} = \frac{1}{64\pi}\frac{\alpha^2 M_h^3}{16\pi^2}\left|\bar{A}_W + \bar{A}_t + \bar{A}_{\tilde{t}} + \bar{A}_{\tilde{b}}\right|^2$$

$$\bar{A}_W = \frac{g_{hWW}}{M_W^2} F_1\left(M_h^2/4M_W^2\right)$$

$$\bar{A}_t = 2N_c Q_t^2 \frac{g_{htt}}{M_t} F_{1/2}\left(M_h^2/4M_t^2\right)$$



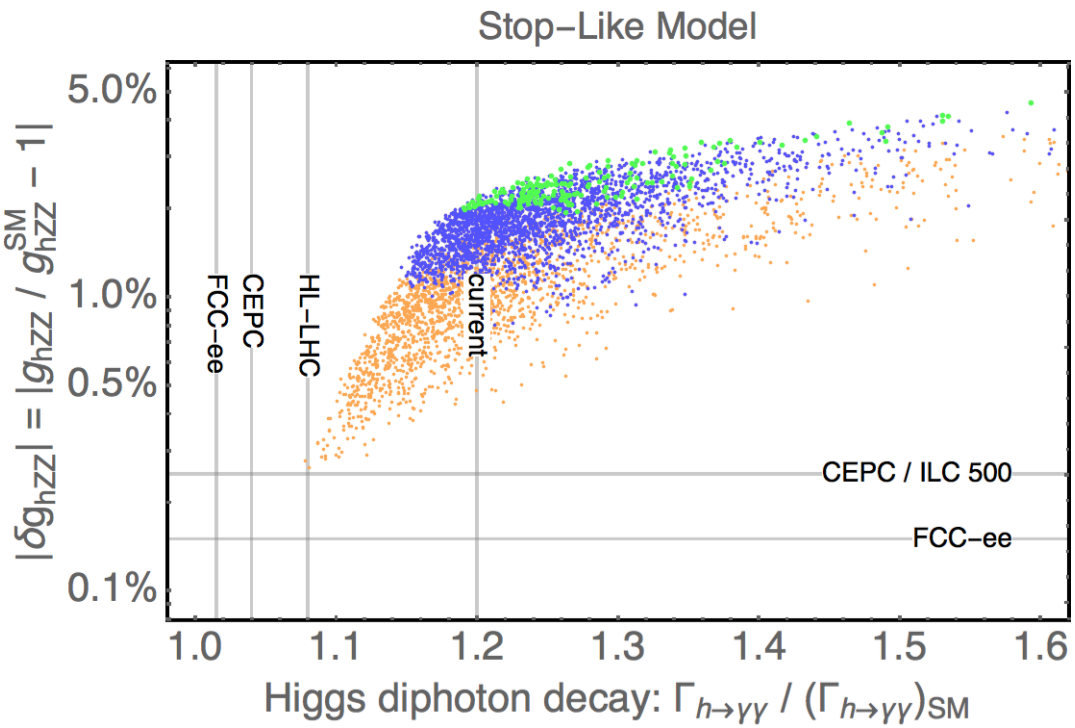
$$\bar{A}_{\tilde{t}} = \sum_{i=1}^{2} N_c Q_t^2 \frac{g_{h\tilde{t}_i\tilde{t}_i}}{M_{\tilde{t}_i}^2} F_0\left(M_h^2/4M_{\tilde{t}_i}^2\right)$$

$$\bar{A}_{\tilde{b}} = N_c Q_b^2 \frac{g_{h\tilde{b}\tilde{b}}}{M_{\tilde{b}}^2} F_0\left(M_h^2/4M_{\tilde{b}}^2\right)$$

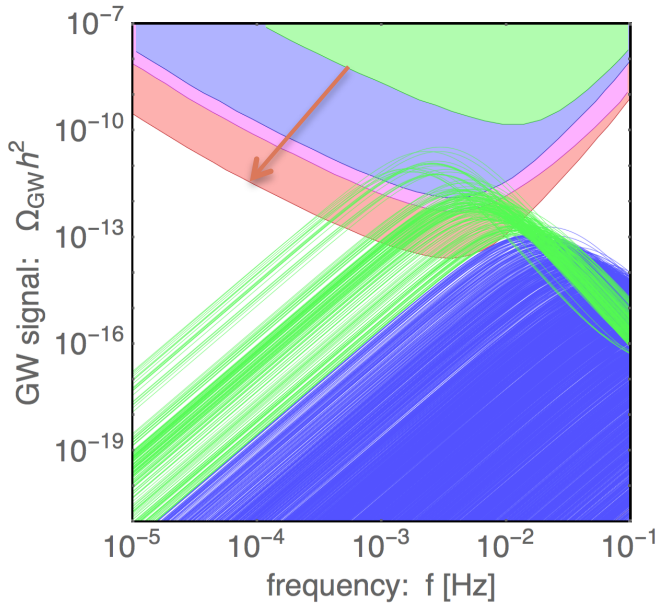
$$F_1(\tau) = \frac{2\tau^2 + 3\tau + 3(2\tau - 1)\arcsin(\tau^{1/2})^2}{\tau^2}$$

$$F_{1/2}(\tau) = -2\frac{\tau + (\tau - 1)\arcsin(\tau^{1/2})^2}{\tau^2}$$

$$F_0(\tau) = \frac{\tau - \arcsin(\tau^{1/2})^2}{\tau^2}$$



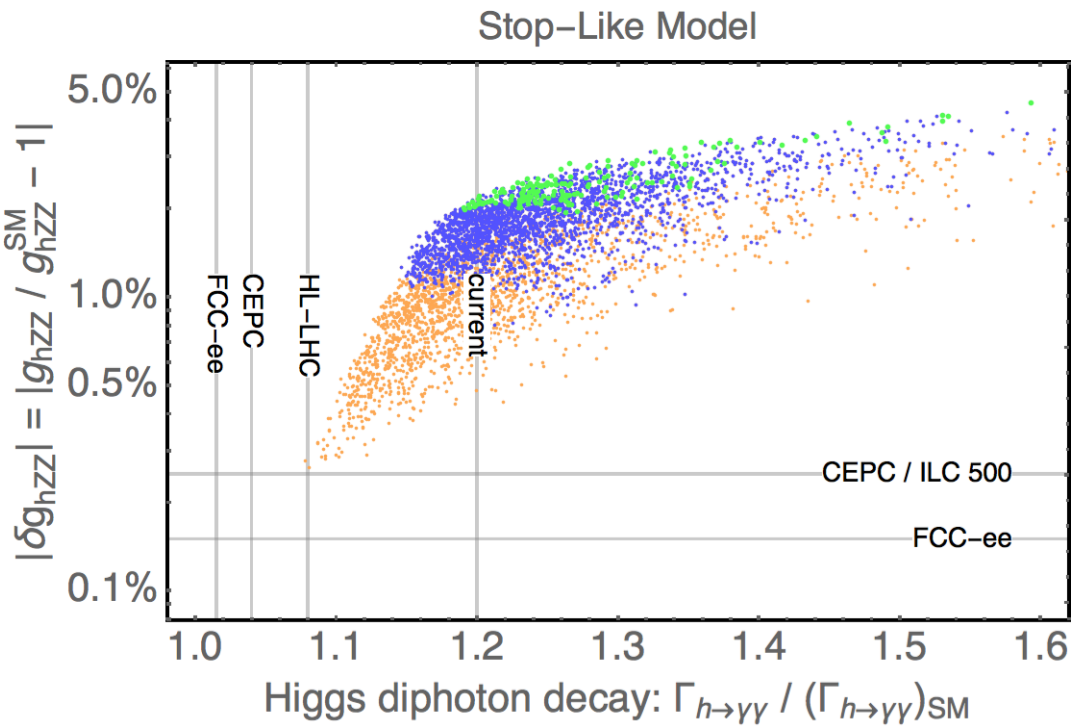
(sensitivities of four different proposed eLISA configurations)



Orange = first order phase transition, $v(T_c)/T_c > 0$

Blue = "strongly" first order phase transition, $v(T_c)/T_c > 1.3$

Green = very strongly 1PT, could detect GWs at LISA



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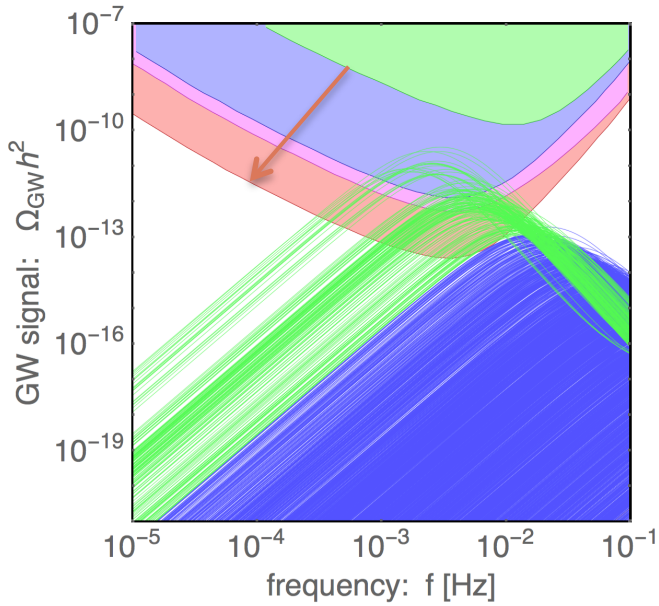

Models with a first order electroweak phase transition (orange, blue, or green) have large **deviation in hZZ** that can be probed by Higgs factories.

These models also have large enhancement to **Higgs diphoton decay** rate (b/c of charged particles) that can be probed by HL-LHC & Higgs factories.

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In the simplified / minimal models, the new degrees of freedom are responsible for *both* the 1PT and hZZ

SM + Real Scalar Singlet

five model parameters

Consider

$$\mathcal{L} = \mathcal{L}_{\rm SM} + \frac{1}{2}(\partial\phi_s)^2 - \frac{m_s^2}{2}\phi_s^2 - \frac{a_s}{3}\phi_s^3 - \frac{\lambda_s}{4}\phi_s^4 - \underbrace{\lambda_{hs}H^\dagger H\phi_s^2 - 2a_{hs}H^\dagger H\phi_s}_{\text{Higgs portal}}$$

real scalar singlet

In the vacuum

$$\langle H\rangle = (0\,,\, v/\sqrt{2}) \qquad \text{and} \qquad \langle\phi_s\rangle = v_s$$

$$\sin 2\theta = \frac{4v(a_{hs} + \lambda_{hs}v_s)}{M_h^2 - M_s^2}$$

(Higgs-singlet mixing)

Effective hhh coupling

(adapted from: McCullough, 2014; Curtin, Meade, Yu, 2014)

$$\lambda_3 = \left(6\lambda_h v\right)\cos^3\theta + \left(6a_{hs} + 6\lambda_{hs}v_s\right)\sin\theta\cos^2\theta + \left(6\lambda_{hs}v\right)\sin^2\theta\cos\theta + \left(2a_s + 6\lambda_s v_s\right)\sin^3\theta$$

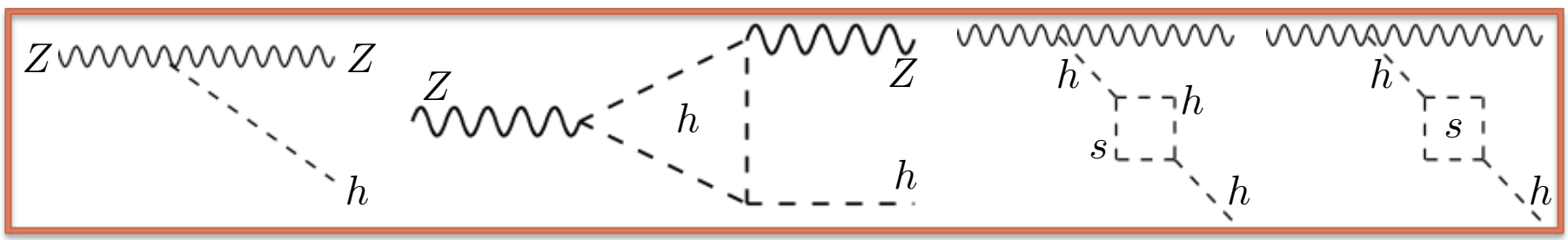
Effective hZZ coupling

(adapted from: Craig, Englert, & McCullough, 2013)

$$\delta g_{hZZ} \approx \left(\cos\theta - 1\right) - 2\frac{|a_{hs} + \lambda_{hs}v_s|^2}{16\pi^2} I_B(M_h^2; M_h^2, M_s^2) - \frac{|\lambda_{hs}|^2 v^2}{16\pi^2} I_B(M_h^2; M_s^2, M_s^2) + 0.006\left(\frac{\lambda_3}{\lambda_{3,\mathrm{SM}}} - 1\right)$$

(one-loop)

(leading effect is from mixing)



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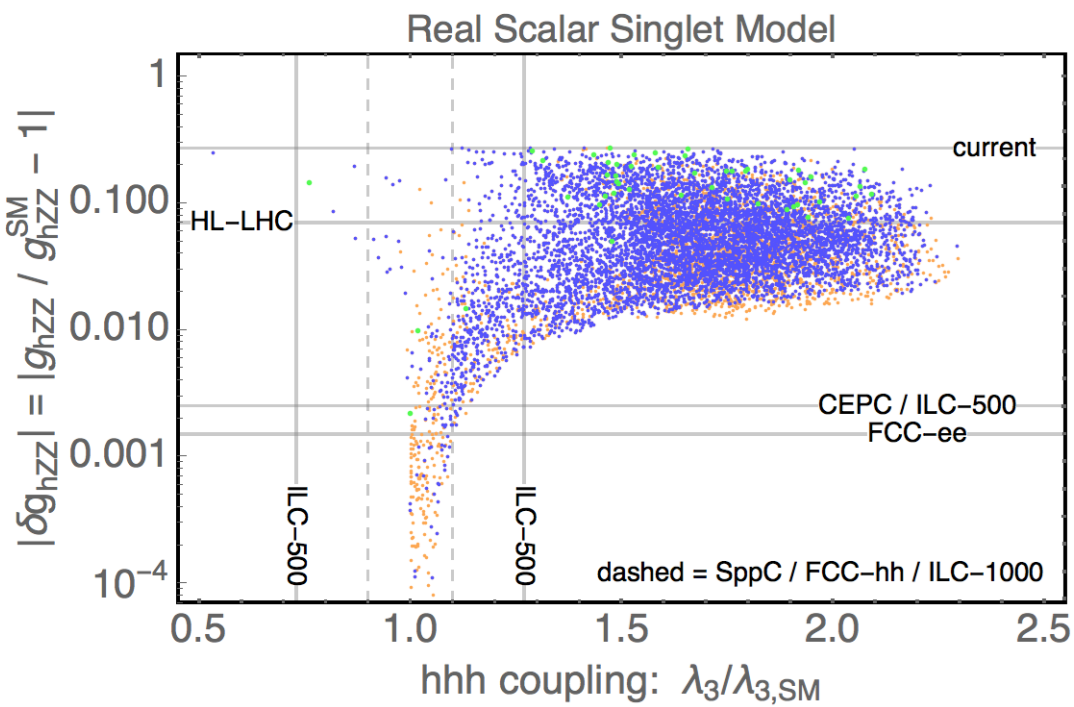

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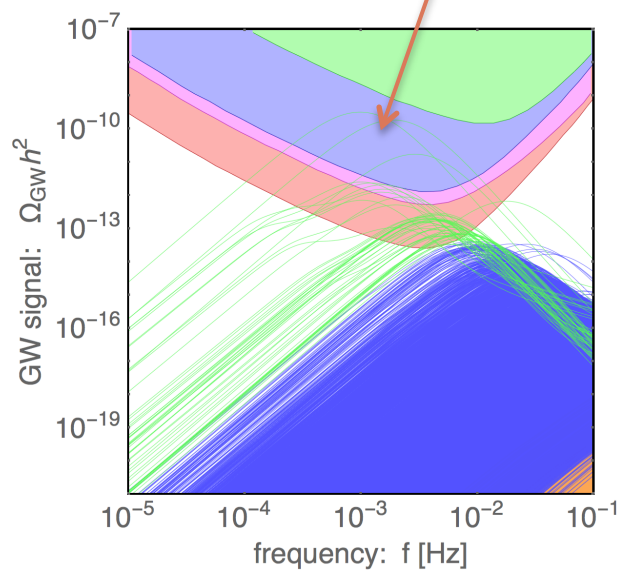
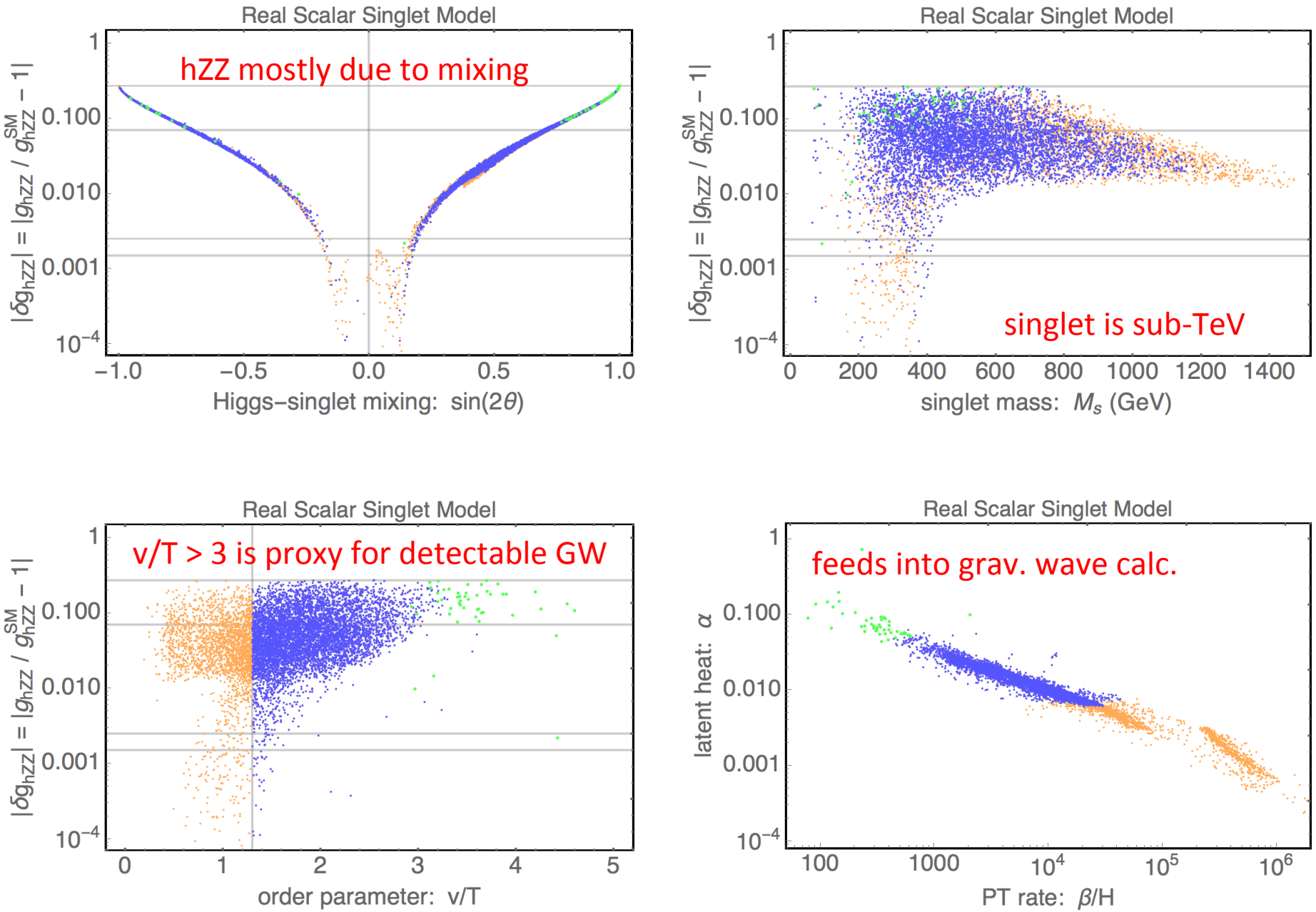


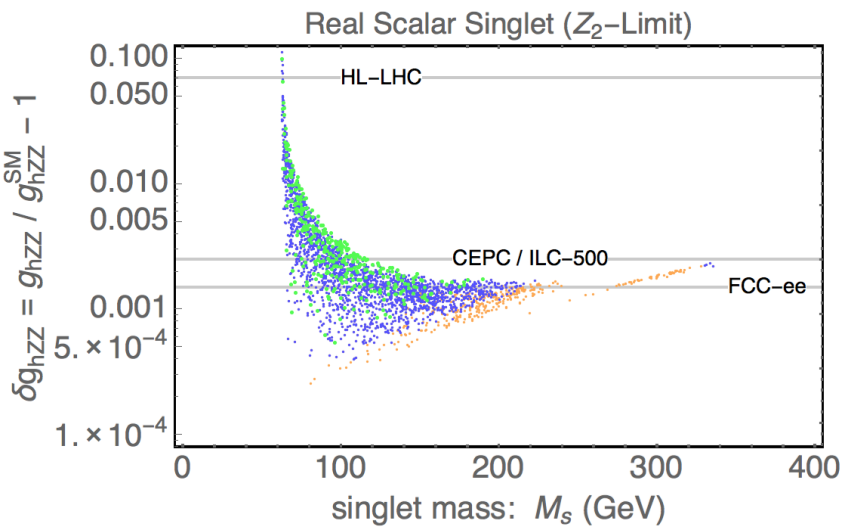
Parameter space with first order electroweak phase transition has large deviation in hZZ, which can be probed by Higgs Factories


Real Scalar Singlet Model
hZZ mostly due to mixing
$|\delta g_{hZZ}| = |g_{hZZ} / g_{hZZ}^{SM} - 1|$
Higgs–singlet mixing: sin(2θ)
Real Scalar Singlet Model
singlet is sub-TeV
singlet mass: M_s (GeV)
Real Scalar Singlet Model
v/T > 3 is proxy for detectable GW
order parameter: v/T
Real Scalar Singlet Model
feeds into grav. wave calc.
latent heat: α
PT rate: β/H

Challenging Limits

Z2-Symmetric

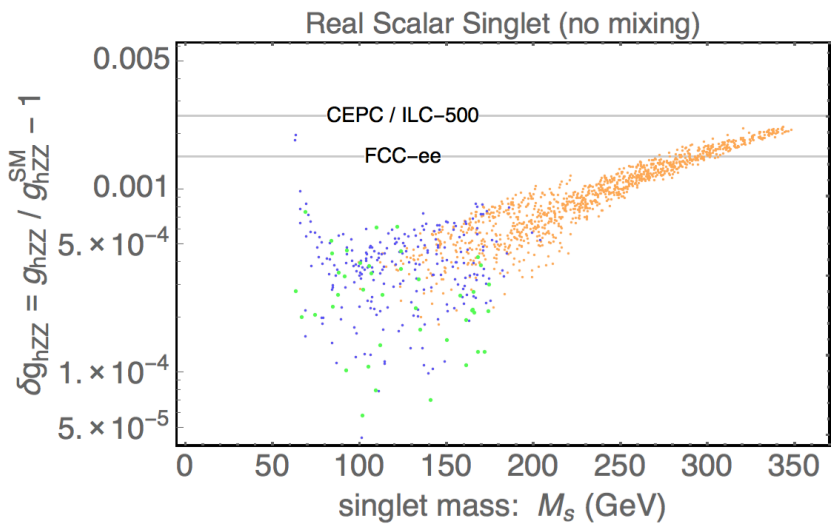
$$a_s = a_{hs} = v_s = 0$$



- Dubbed the "nightmare scenario" by Curtin, Meade, & Yu (2014).
- Singlet may be the dark matter. See talk by Huaike Guo.

Tuned Zero Mixing

$$a_{hs} + \lambda_{hs} v_s = 0$$



- hZZ not within reach of Higgs factory
- Instead look for double singlet production
- Recently studied by Chen, Kozaczuk, & Lewis (2017). See also Ian Lewis's talk.

Summary

The Standard Model predicts a continuous electroweak crossover (no bubbles).

It is easy to extend the SM and find a first order phase transition (bubbles!).

A first order electroweak phase transition is more fun for cosmologists

→ Matter / anti-matter asymmetry
→ Primordial gravitational waves
→ Primordial black holes
→ Primordial magnetic field
→ ....

but our predictions are subject to large uncertainties.

Precision measurements of Higgs couplings may uncover new physics at the EW scale, and thereby indirectly probe the electroweak phase transition.

A large deviation in the hZZ coupling seems to be generic in models with first order EWPT, allowing these models to be tested by Higgs factories.