

# Enhancing lepton flavour violation in the (SUSY) inverse seesaw

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# Neutrino oscillations

- $P_{\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta} \neq 0$  only if  $\Delta m_{kj}^2 = m_k^2 - m_j^2$  and  $U_\nu \neq \mathbb{1}$
- **Best fit** (nu-fit.org)
 

solar	$\theta_{12} \simeq 33^\circ$	$\Delta m_{12}^2 \simeq 7.5 \times 10^{-5} \text{eV}^2$
atmospheric	$\theta_{23} \simeq 49^\circ$	$ \Delta m_{23}^2  \simeq 2.4 \times 10^{-3} \text{eV}^2$
reactor	$\theta_{13} \simeq 8.5^\circ$	
- Different mixing pattern from CKM,  $\nu$  lightness  $\stackrel{?}{\leftarrow}$  Majorana  $\nu$
- SM: no  $\nu$  mass term, lepton flavour is conserved  
 $\Rightarrow$  **need new Physics**
  - Radiative models
  - Extra dimensions
  - R-parity violation in supersymmetry
  - **Seesaw mechanism**  $\rightarrow$  BAU through leptogenesis ?
- Neutrino oscillations = Neutral lepton flavour violation  
 What about **charged lepton flavour violation (cLFV)** ?

# cLFV

- In the Standard Model: cLFV from higher order processes  
⇒ negligible
- If cLFV observed:
  - Clear evidence of physics at a higher scale
  - Probe the origin of lepton mixing
  - Probe the origin of New Physics
- Complementary to other New Physics searches
  - High energy: LHC
  - High intensity:
    - B factories: Rare decays, etc
    - Neutrino dedicated experiments:  $U_{PMNS}$  non-unitarity...
    - Other low energy experiments:  $(g - 2)_\mu$ , EDM, LUV...



# cLFV

- Radiative decays, e.g.  $\text{Br}(\mu \rightarrow e\gamma) < 5.7 \times 10^{-13}$  [MEG, 2013]
- 3-body lepton decays,  
e.g.  $\tau \rightarrow 3\mu < 2.1 \times 10^{-8}$  [Belle, 2010]
- Neutrinoless muon conversion,  
e.g.  $\mu^-, \text{Au} \rightarrow e^-, \text{Au} < 7 \times 10^{-13}$  [SINDRUM II, 2006]
- Meson decays, e.g.  $B_d^0 \rightarrow e\mu < 2.8 \times 10^{-9}$  [LHCb, 2013]
- Z decays, e.g.  $Z^0 \rightarrow e\mu < 1.7 \times 10^{-6}$  [OPAL, 1995]



# Higgs boson: discovery to precision measurements

- Discovery of a Higgs boson at the LHC in 2012, with properties compatible with the SM Higgs [ATLAS, 2012; CMS, 2012]
- Evidence for  $H \rightarrow \tau^+ \tau^-$  (CMS:  $3.2\sigma$ , ATLAS:  $4.5\sigma$ )  
Active searches of  $H \rightarrow \mu^- \mu^+$  and  $H \rightarrow e^+ e^-$
- CMS search for  $H \rightarrow \tau \mu$  [CMS, 2015]:  $2.4\sigma$  signal excess (best fit:  $\text{Br} = 0.84^{+0.39}_{-0.37}\%$ , UL:  $\text{Br} < 1.51\%$  at 95% CL)
- Timely to consider LFV Higgs decays, e.g.  $H \rightarrow \bar{\tau} \mu$



# The inverse seesaw mechanism

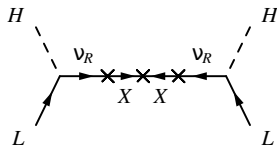
- Inverse seesaw  $\Rightarrow$  Consider fermionic gauge singlets  $\nu_{Ri}$  ( $L = +1$ ) and  $X_i$  ( $L = -1$ ) [Mohapatra and Valle, 1986]

$$\mathcal{L}_{inverse} = -Y_{\nu}^{ij} \bar{L}_i \tilde{H} \nu_{Rj} - M_R^{ij} \bar{\nu}_{Ri}^C X_j - \frac{1}{2} \mu_X^{ij} \bar{X}_i^C X_j + \text{h.c.}$$

$$\text{with } m_D = Y_{\nu} \nu, M^{\nu} = \begin{pmatrix} 0 & m_D & 0 \\ m_D^T & 0 & M_R \\ 0 & M_R^T & \mu_X \end{pmatrix}$$

$$m_{\nu} \approx \frac{m_D^2 \mu_X}{m_D^2 + M_R^2}$$

$$m_{N_{1,2}} \approx \mp \sqrt{m_D^2 + M_R^2} + \frac{M_R^2 \mu_X}{2(m_D^2 + M_R^2)}$$

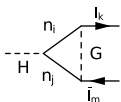


2 scales:  $\mu_X$  (LNV)  
and  $M_R$  (LNC)

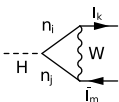


# Diagrams

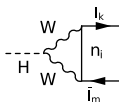
- In the Feynman-'t Hooft gauge, same as [Arganda et al., 2005]:



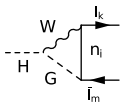
(1)



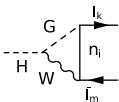
(2)



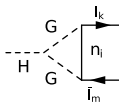
(3)



(4)



(5)

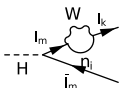


(6)

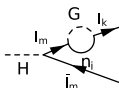
- Formulas adapted from [Arganda et al., 2005]

- Diagrams 1, 8, 10 → **dominate** at large  $M_R$

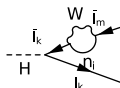
- Enhancement** from:
  - $-\mathcal{O}(1) Y_\nu$  couplings
  - TeV scale  $n_i$



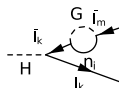
(7)



(8)



(9)



(10)

# Constraints

- Neutrino data → Use **specific parametrizations** (modified Casas-Ibarra [Casas and Ibarra, 2001] or  $\mu_X$  parametrization)

$$\nu Y_\nu^T = V^\dagger \text{diag}(\sqrt{M_1}, \sqrt{M_2}, \sqrt{M_3}) R \text{diag}(\sqrt{m_1}, \sqrt{m_2}, \sqrt{m_3}) U_{PMNS}^\dagger$$

$$M = M_R \mu_X^{-1} M_R^T$$

OR

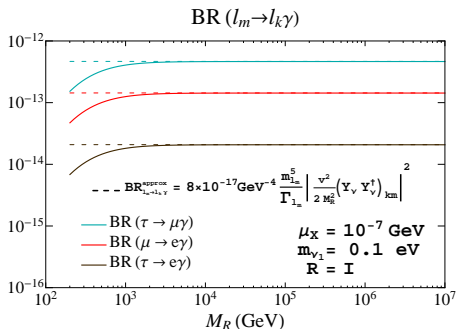
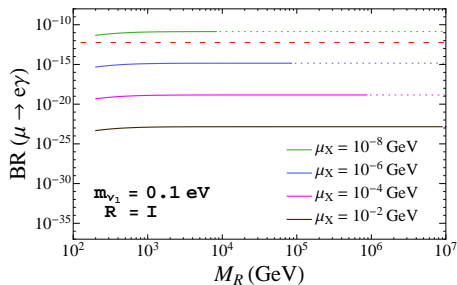
$$\mu_X = M_R^T m_D^{-1} U_{PMNS}^* m_\nu U_{PMNS}^\dagger m_D^{T-1} M_R$$

- Charged lepton flavour violation  
→ **Most constraining**:  $\text{Br}(\mu \rightarrow e\gamma) < 5.7 \times 10^{-13}$  [MEG, 2013]
- Lepton universality violation: less constraining than  $\mu \rightarrow e\gamma$
- Electric dipole moment: **0** with **real** PMNS and mass matrices
- Invisible Higgs decays:  $M_R > m_H$ , **does not apply**



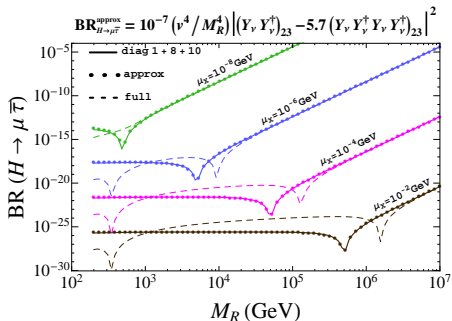
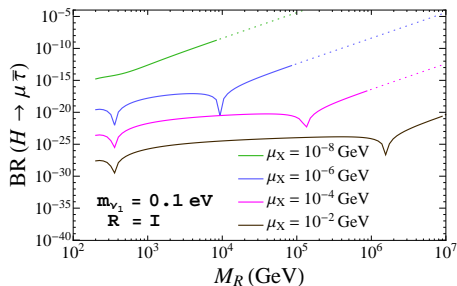


# Constraints: focus on $\mu \rightarrow e\gamma$



- $M_R$  and  $\mu_X$  real and degenerate
- Constrains  $\mu_X$
- Perturbativity  $\rightarrow \left| \frac{Y_\nu^2}{4\pi} \right| < 1.5$  (Dotted line = non-perturbative couplings)
- **Good agreement** between the full calculation and the approximate formula

# Dependence on ISS parameters



- $M_R$  and  $\mu_X$  degenerate and real,  $R = I$
- Perturbativity  $\rightarrow \left| \frac{y_\nu^2}{4\pi} \right| < 1.5$  (Dotted line = non-perturbative couplings)
- Dips from **interferences** between diagrams
- **Good agreement** with the approximate formula
- Can be understood using the mass insertion approximation
- $\text{Br}(H \rightarrow \bar{\tau} \mu) \leq 10^{-9} - 10^{-10}$

# Scenarios with large LFV Higgs decay rates

- Strongest experimental constraint:  $\mu \rightarrow e\gamma$

$$BR_{\mu \rightarrow e\gamma}^{\text{approx}} = 8 \times 10^{-17} \text{GeV}^{-4} \frac{m_\mu^5}{\Gamma_\mu} \left| \frac{v^2}{2M_R^2} (Y_\nu Y_\nu^\dagger)_{12} \right|^2$$

$$BR_{H \rightarrow \mu\bar{\tau}}^{\text{approx}} = 10^{-7} \frac{v^4}{M_R^4} \left| (Y_\nu Y_\nu^\dagger)_{23} - 5.7 (Y_\nu Y_\nu^\dagger Y_\nu Y_\nu^\dagger)_{23} \right|^2$$

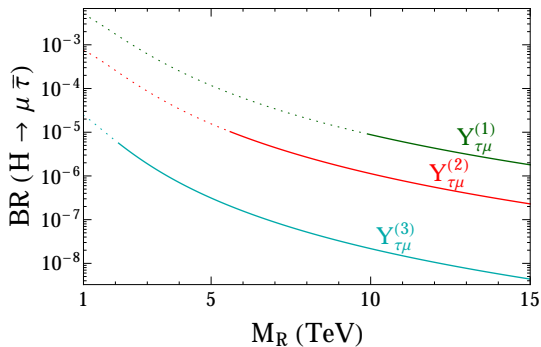
$$\underset{(Y_\nu Y_\nu^\dagger)_{12}=0}{=} 10^{-7} \frac{v^4}{M_R^4} \left| 1 - 5.7 [(Y_\nu Y_\nu^\dagger)_{22} + (Y_\nu Y_\nu^\dagger)_{33}] \right|^2 \left| (Y_\nu Y_\nu^\dagger)_{23} \right|^2$$

- Solution: Textures with  $(Y_\nu Y_\nu^\dagger)_{12} = 0$  and  $\frac{|Y_\nu^{ij}|^2}{4\pi} < 1.5$
- Examples:

$$Y_{\tau\mu}^{(1)} = \sqrt{6\pi} \begin{pmatrix} 0 & 1 & -1 \\ 0.9 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix}, Y_{\tau\mu}^{(2)} = \sqrt{6\pi} \begin{pmatrix} 0 & 1 & 1 \\ 1 & 1 & -1 \\ -1 & 1 & -1 \end{pmatrix}, Y_{\tau\mu}^{(3)} = \sqrt{6\pi} \begin{pmatrix} 0 & -1 & 1 \\ -1 & 1 & 1 \\ 0.8 & 0.5 & 1 \end{pmatrix}$$

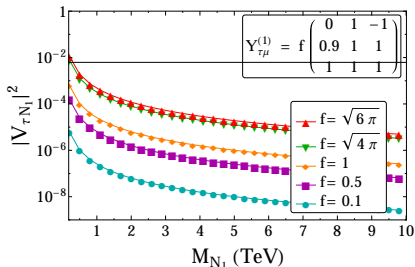
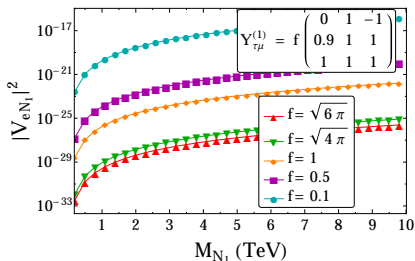


# Scenarios with large LFV Higgs decay rates



- Numerics done with the full one-loop formulas
- Dotted: excluded by  $\tau \rightarrow \mu\gamma$   
Solid: allowed by LFV, LUV, etc
- $\text{Br}^{\max}(H \rightarrow \mu\bar{\tau}) \sim 10^{-5}$
- Same maximum branching ratio with hierarchical heavy N
- Similarly,  $\text{Br}^{\max}(H \rightarrow e\bar{\tau}) \sim 10^{-5}$  for  $Y_{\tau e}^{(i)}$  ( $=Y_{\tau\mu}^{(i)}$  with rows 1 and 2 exchanged)

# Constraints from EWPO (work in progress)



- Active sterile mixing is controlled by  $\theta \sim m_D M_R^{-1}$
- Large mixing  $\rightarrow$  possible conflict with EWPO
- Limits taken from [del Aguila et al., 2008] at 90% C.L. :

$$|V_{eN}|^2 < 3.0 \times 10^{-3}$$

$$|V_{\mu N}|^2 < 3.2 \times 10^{-3}$$

$$|V_{\tau N}|^2 < 6.2 \times 10^{-3}$$

- See X. Marciano's poster

## Another possibility: SUSY inverse seesaw

- MSSM extended by singlet chiral superfields  $\hat{N}_i$  and  $\hat{X}_i$  ( $i = 1, 2, 3$ ) with respectively  $L = -1$  and  $L = +1$
- Defined by the superpotential:

$$\mathcal{W} = W_{MSSM} + \varepsilon_{ab} \hat{N} Y_\nu \hat{H}_u^b \hat{L}^a + \hat{N} M_R \hat{X} + \frac{1}{2} \hat{X} \mu_X \hat{X}$$

- **New couplings**, e.g.

$$\tilde{\nu}_R^\dagger (A_\nu Y_\nu) \tilde{\nu}_L H_u^0 + \text{h.c.} \in -\mathcal{L}$$

- **Light** right-handed sneutrinos:

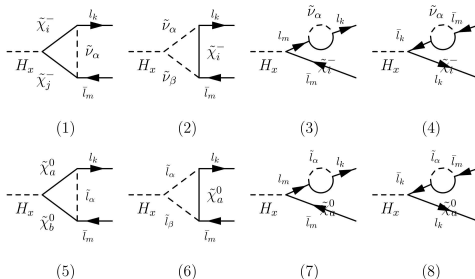
$$M_{\tilde{N}}^2 \simeq m_{\tilde{\nu}_R}^2 + M_R^2 + m_D^2 \sim (1\text{TeV})^2$$

- Could generate large  $\text{Br}(h \rightarrow \mu\tau)$  [Abada et al., 2012]



# LFV Higgs decays in the SUSY ISS

- Work in progress, focus on the supersymmetric contributions



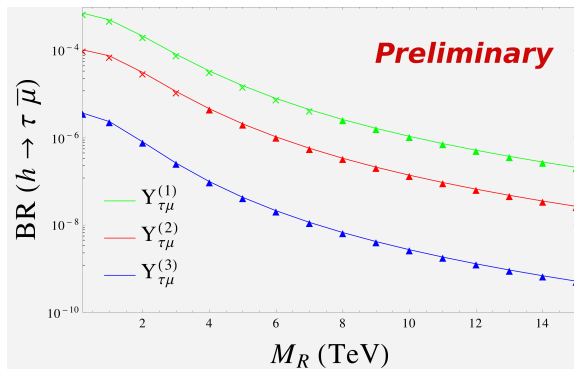
- Chargino contributions induced by  $Y_{ij}^\nu \neq 0$

- Neutralino contributions require  $(\Delta m_L^2)_{ij} \neq 0$

→ from RGE [Hisano et al., 1996]

$$(\Delta m_L^2)_{ij} \propto (Y_\nu^\dagger Y_\nu)_{ij} \ln \frac{M_{GUT}}{M_R}$$

# No charged slepton mixing

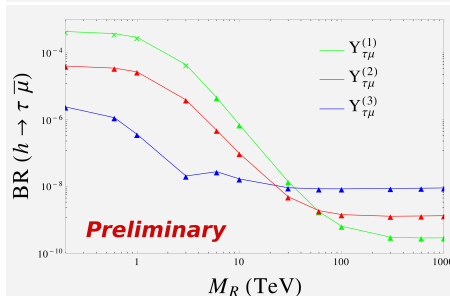
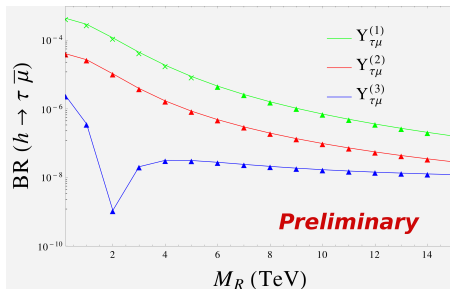


- $\Delta$ : Allowed by  $\tau \rightarrow \mu\gamma$   
 $\times$ : Excluded
- Dominated by the **chargino contributions**
- Behaviour similar to the non-SUSY case

•  $m_{\tilde{L}} = m_{\tilde{\nu}_R} = m_{\tilde{X}} = 1 \text{ TeV}, A_{\nu} = 0, \tan \beta = 10, m_{A^0} = 800 \text{ GeV}$

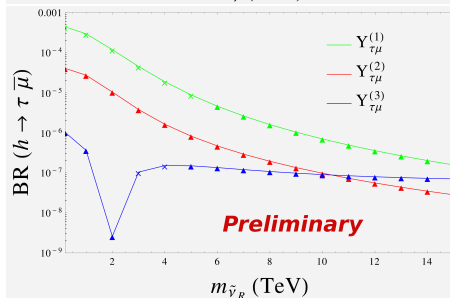
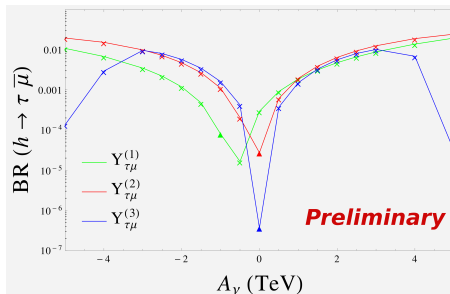


# Full SUSY contribution



- $\Delta$ : Allowed by  $\tau \rightarrow \mu\gamma$
- $\times$ : Excluded
- $(\Delta m_{\tilde{L}}^2)_{ij} \propto (Y_{\nu}^{\dagger} Y_{\nu})_{ij} \ln \frac{M_{GUT}}{M_R}$
- Dip for  $Y_{\tau\mu}^{(3)} \rightarrow$  cancellation between chargino and neutralino contributions
- Low  $M_R$ : chargino-loops dominate
- High  $M_R$ : neutralino-loops dominate
- $m_{\tilde{L}} = m_{\tilde{\nu}_R} = m_{\tilde{\chi}} = 1 \text{ TeV}$ ,  
 $A_{\nu} = 0$ ,  $\tan \beta = 10$ ,  
 $m_{A^0} = 800 \text{ GeV}$

# Full SUSY contribution



- $\Delta$ : Allowed by  $\tau \rightarrow \mu \gamma$
- $\times$ : Excluded
- Very sensitive to  $A_\nu$
- Low  $m_{\tilde{\nu}_R}$ : chargino-loops dominate
- High  $m_{\tilde{\nu}_R}$ : neutralino-loops dominate
- Dip for  $Y_{\tau\mu}^{(3)} \rightarrow$  cancellation between chargino and neutralino contributions
- $m_{\tilde{L}} = 1$  TeV,  $\tan \beta = 10$ ,  
 $m_{A^0} = 800$  GeV  
 when not varied  $A_\nu = 0$  and  
 $m_{\tilde{\nu}_R} = m_{\tilde{X}} = 1$  TeV

# Conclusions

- cLFV  $\Rightarrow$  **Clear evidence** of new physics
- LFV Higgs decays: **complementary** to other cLFV searches
- **Enhancement** from the inverse seesaw  
 $\text{Br}(H \rightarrow \bar{\tau}\mu) \leq 10^{-5}$   
 $\text{Br}(H \rightarrow \bar{\tau}e) \leq 10^{-5}$
- **Enhancement** from the SUSY inverse seesaw  
 $\text{Br}(H \rightarrow \bar{\tau}\mu) \simeq 10^{-4} - 10^{-5}$  possible (work in progress)
- In the (SUSY) ISS,  $H \rightarrow \bar{\tau}\mu$  is **within the reach of future colliders**
- If CMS signal is confirmed, very strong constraints on the inverse seesaw parameter space



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