

Evidence of Dark Matter in the Sun?

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Dark Matter in the Sun

Based on work with **Pat Scott** (Imperial College London)
Aldo Serenelli (U. Autònoma Barcelona)

arXiv:1311.2074 / JCAP/04019

Thermal conduction by dark matter with velocity and momentum-dependent cross-sections

arXiv:1411.6626/ PRL 114.081302

Possible Indication of Momentum-Dependent Asymmetric Dark Matter in the Sun

arXiv:1504.04378

Generalised form factor dark matter in the Sun

Motivation

Motivation

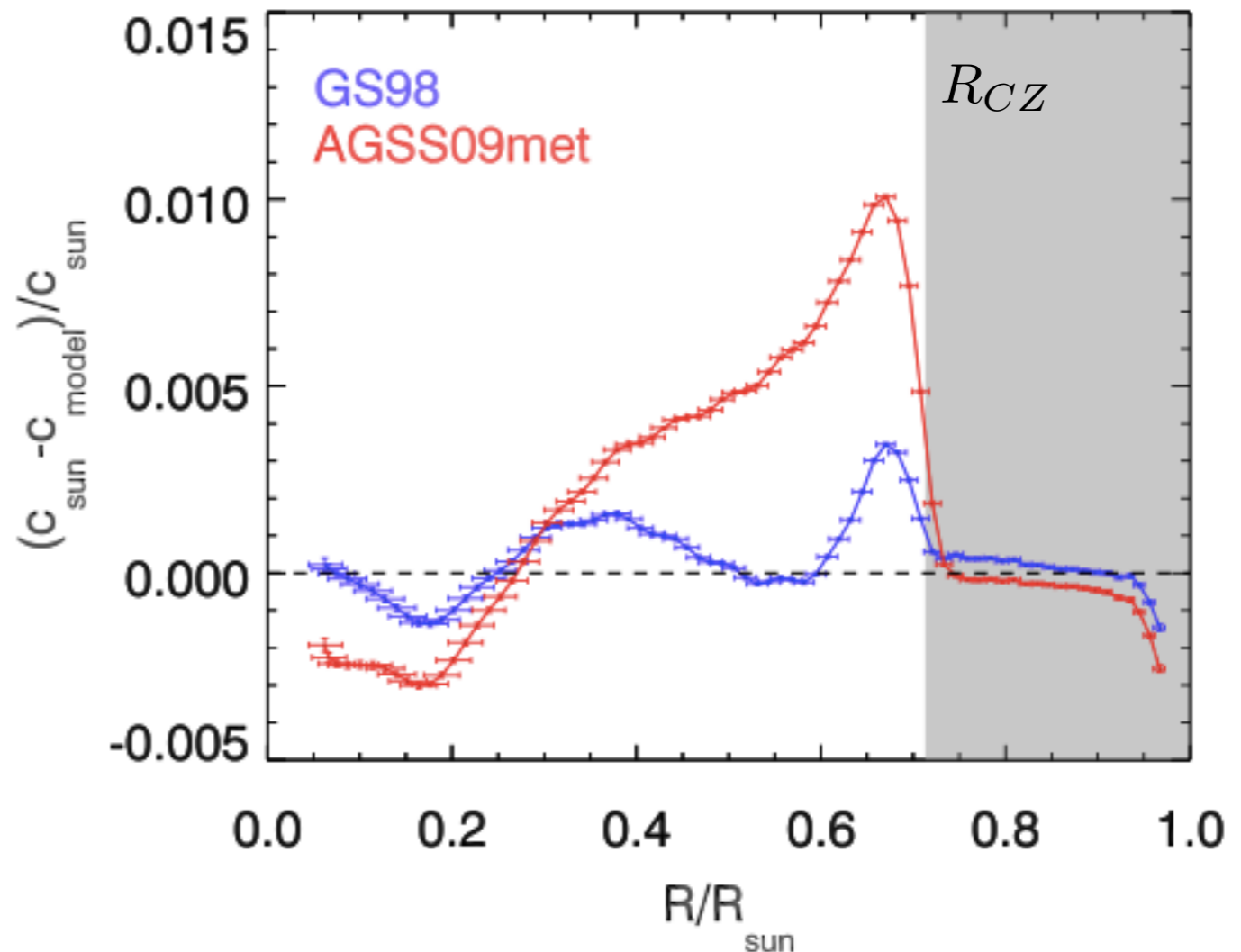
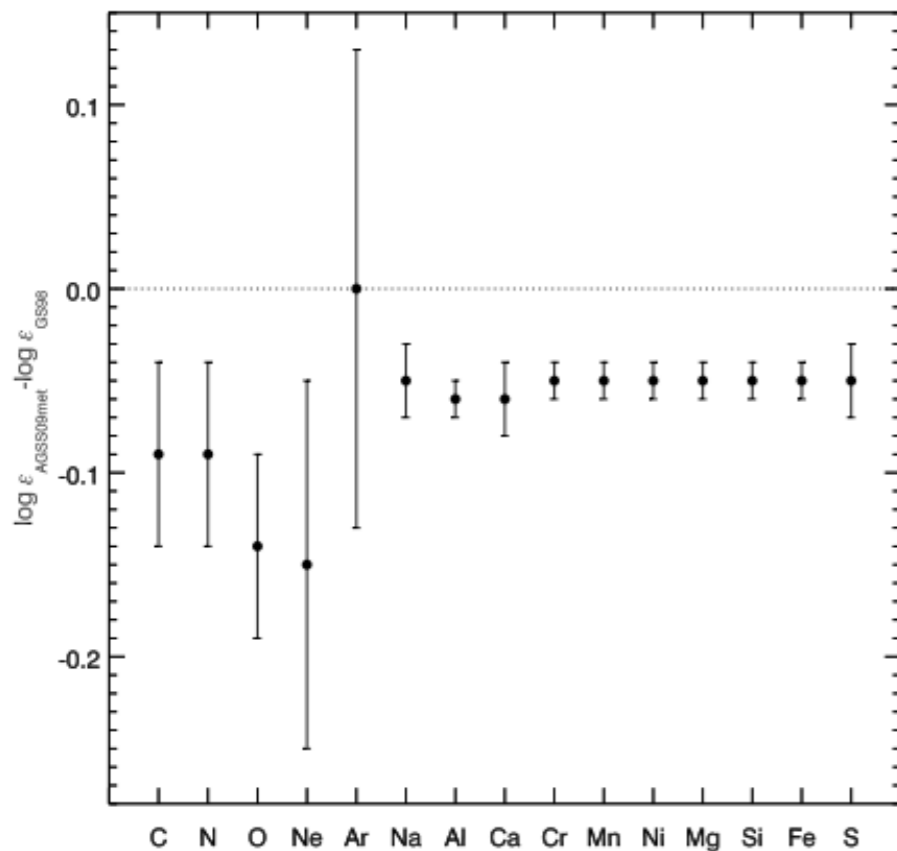
- Discovering the interactions of dark matter

Motivation

- Discovering the interactions of dark matter
- but also: the Solar Composition Problem

Solar composition problem

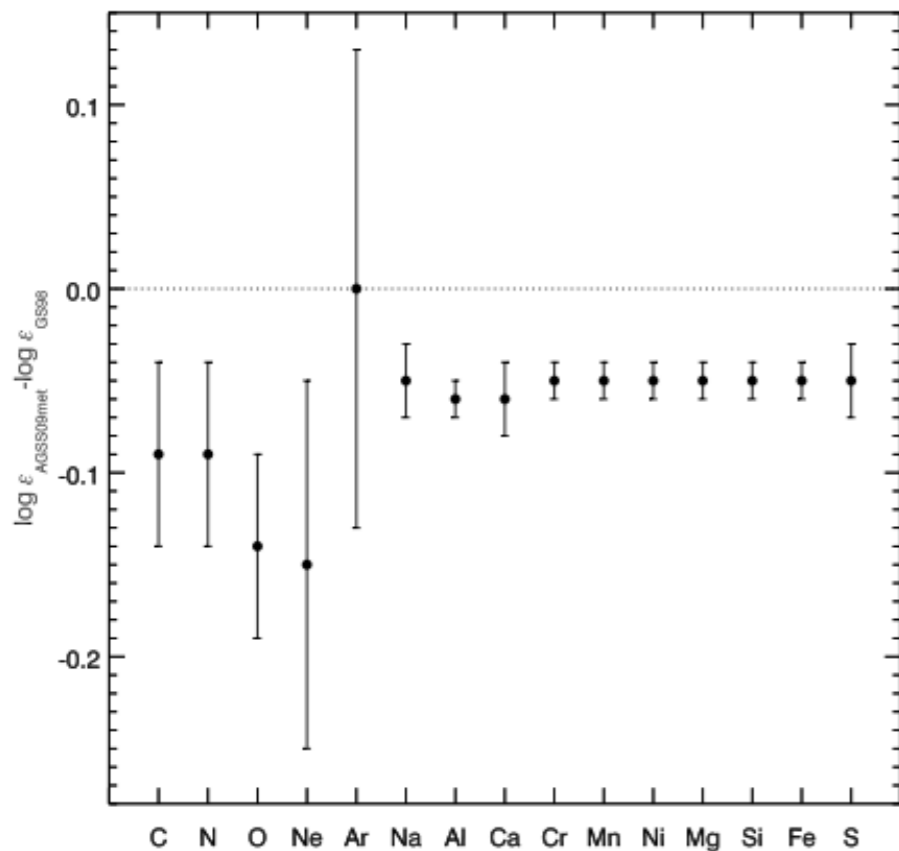
After more accurate measurements of the abundances of metals in the early 2000s, it was found that the sound speed from the *Standard Solar Model* are **not in agreement with measurements** inferred from **helioseismology**.



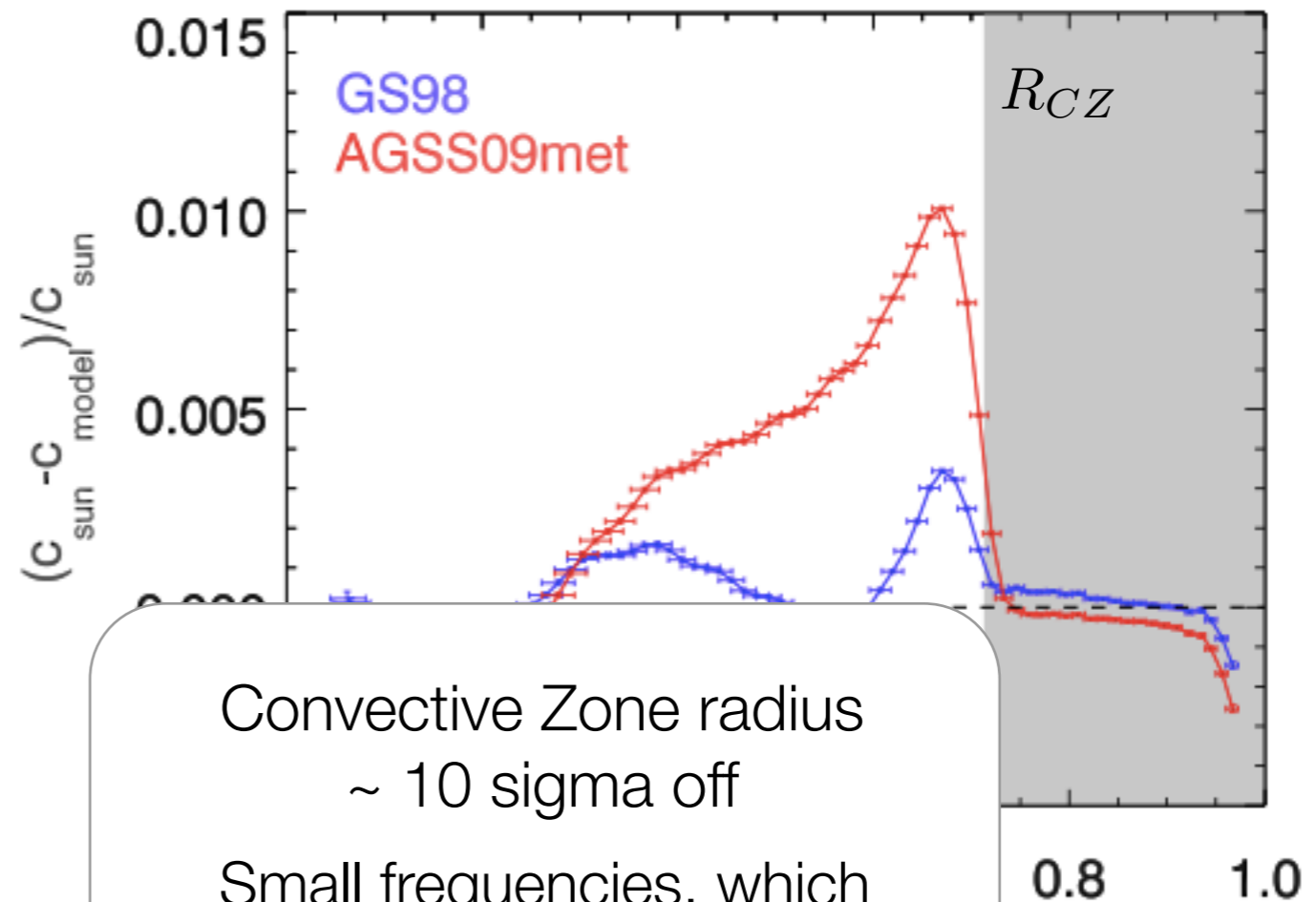
revised - old composition

Solar composition problem

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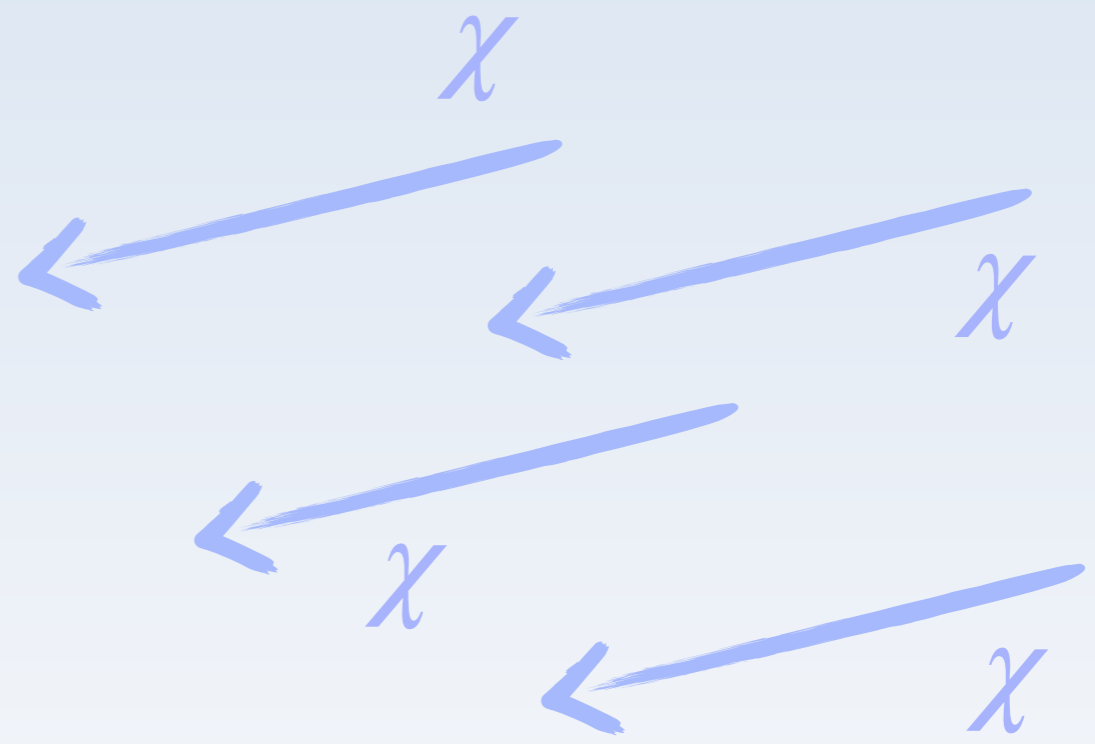
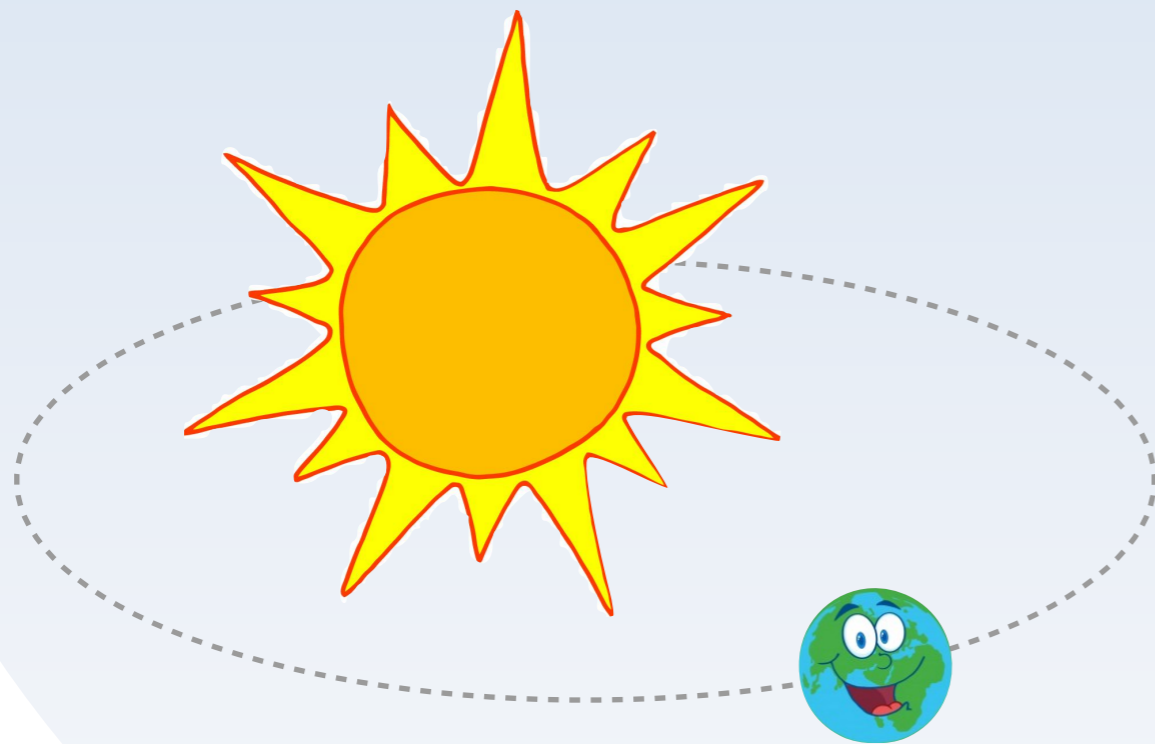
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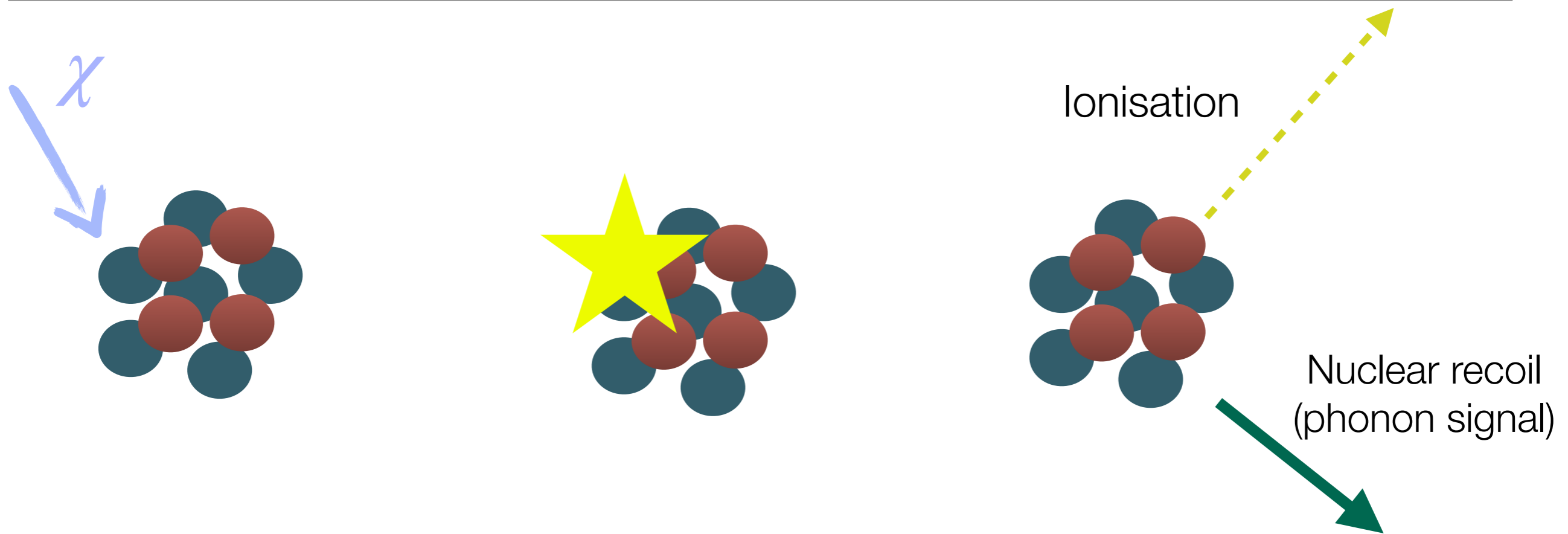
Convective Zone radius
~ 10 sigma off

Small frequencies, which
probe the core, as much as 5
sigma

Direct detection



Direct detection



Seek to measure the interaction of “ambient” DM with quarks:

$$R = \int_{E_T}^{\infty} dE_R \frac{\rho_0}{m_N m_\chi} \int_{v_{min}}^{\infty} v f(v) \frac{d\sigma_{WN}}{dE_R}(v, E_R) dv$$

Dark matter: Beyond σ_{SI} and σ_{SD}

Until recently, people have focused on two constant cases:

$$\chi\bar{\chi}Q\bar{Q} \rightarrow \sigma_{SI}$$

$$\chi\gamma_{\mu}\gamma_5\bar{\chi}Q\gamma^{\mu}\gamma_5\bar{Q} \rightarrow \sigma_{SD}$$

However, in general

$$\sigma = \sigma(s, t, u)$$

Non-relativistic observables:

$$q = \sqrt{2m_{\text{target}}E_R} \simeq m_{\text{target}}\Delta v_{\text{target}} \left. \vphantom{q} \right\} \text{small!}$$

Dark matter: Beyond σ_{SI} and σ_{SD}

Dipole coupling	p-wave	other effective operators
Anapole coupling	d-wave	
Multiple massive mediators	Massive mediator	...

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		...
		$\sigma(q, v_{rel})$

Dark matter: Beyond σ_{SI} and σ_{SD}

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...

$$\sigma(q, v_{\text{rel}})$$

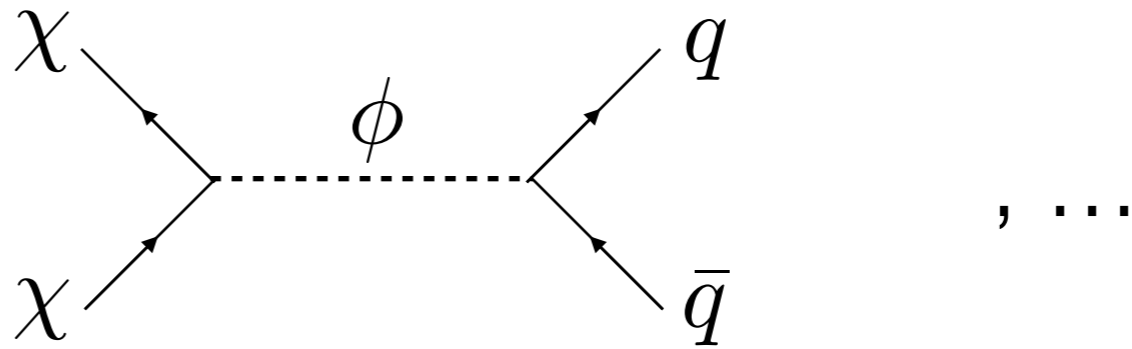
For concreteness, let's look at two forms:

$$\sigma = \sigma_0 \left(\frac{v_{\text{rel}}}{v_0} \right)^n \qquad \sigma = \sigma_0 \left(\frac{q}{q_0} \right)^n$$

where $n = \{-2, 2, 4\}$

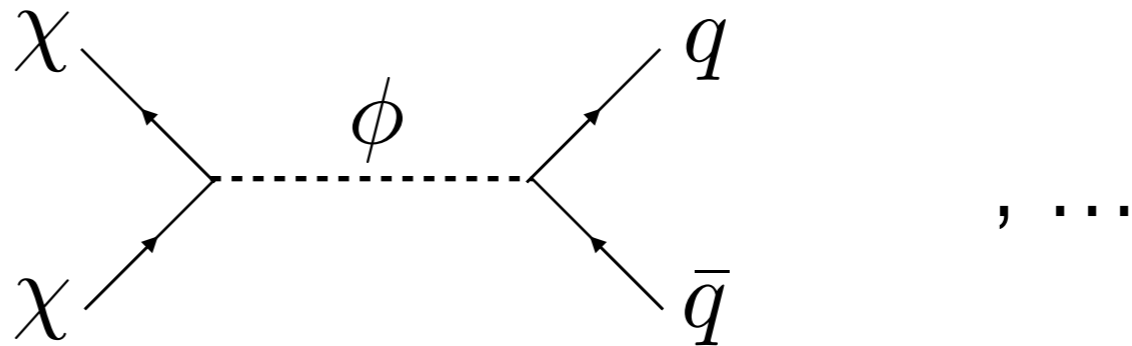
Side-note: 3 popular approaches

Simplified models



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Simplified models

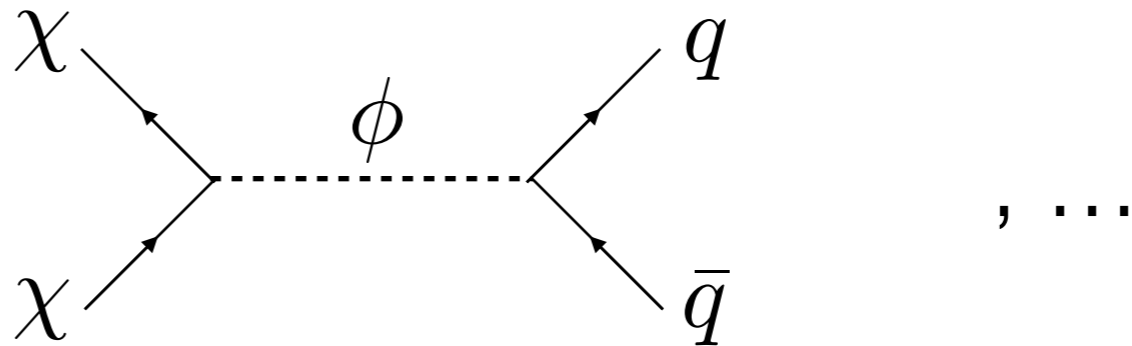


Effective operators (EFTs)

$$\chi\gamma^5\chi\bar{q}\gamma^5q, \dots$$

Side-note: 3 popular approaches

Simplified models



Effective operators (EFTs)

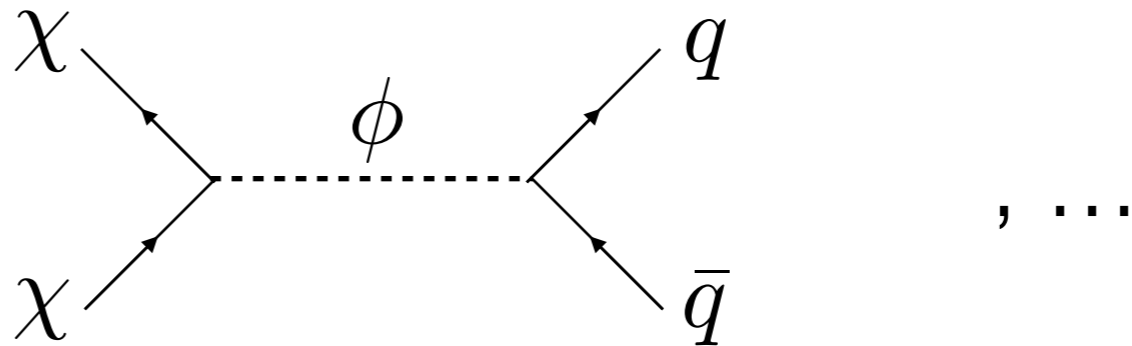
$$\chi\gamma^5\chi\bar{q}\gamma^5q, \dots$$

Effective cross sections

$$\sigma_{SD} = \sigma_0 \left(\frac{q}{q_0} \right)^4, \dots$$

Side-note: 3 popular approaches

Simplified models



Effective operators (EFTs)

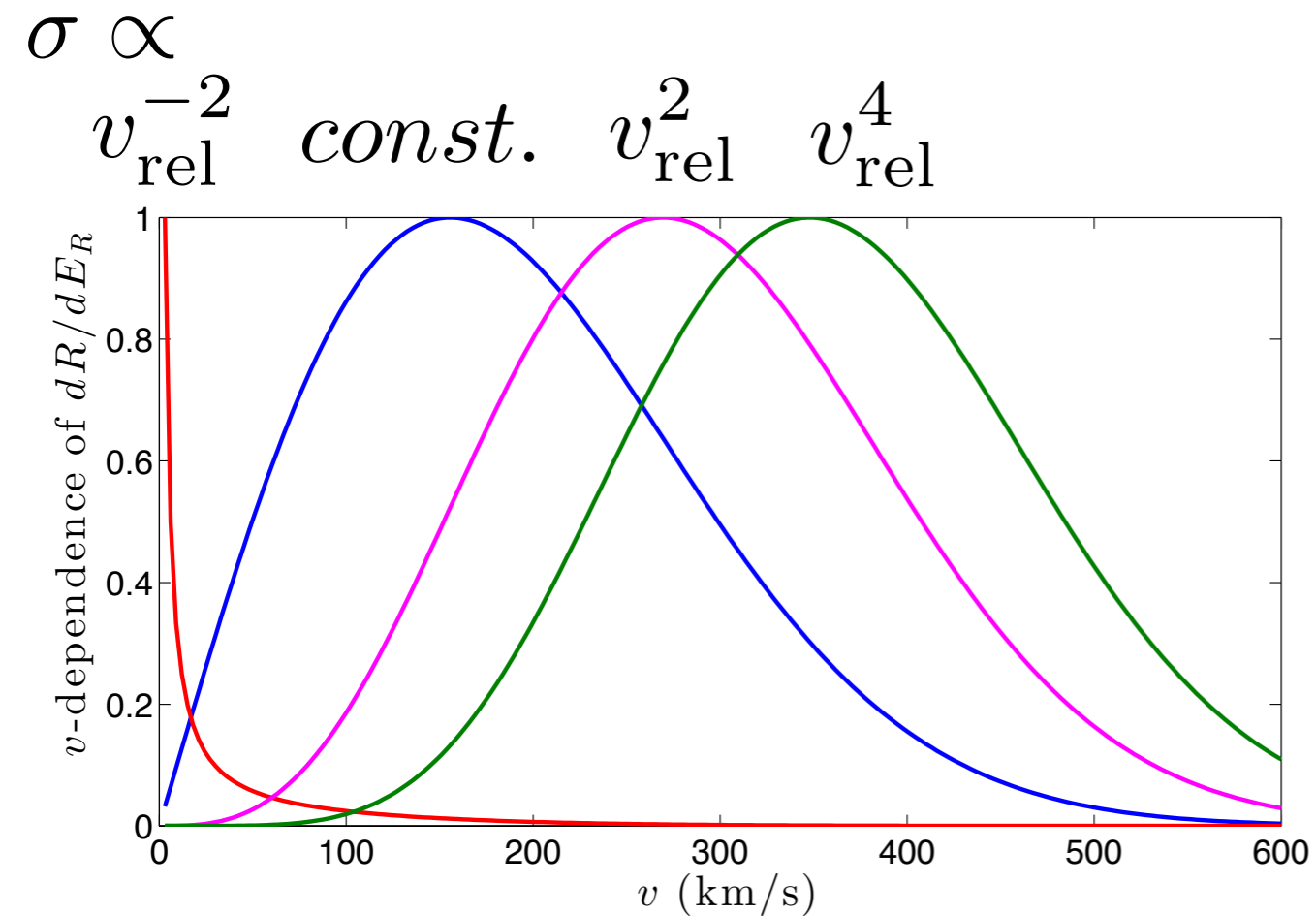
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Effective cross sections

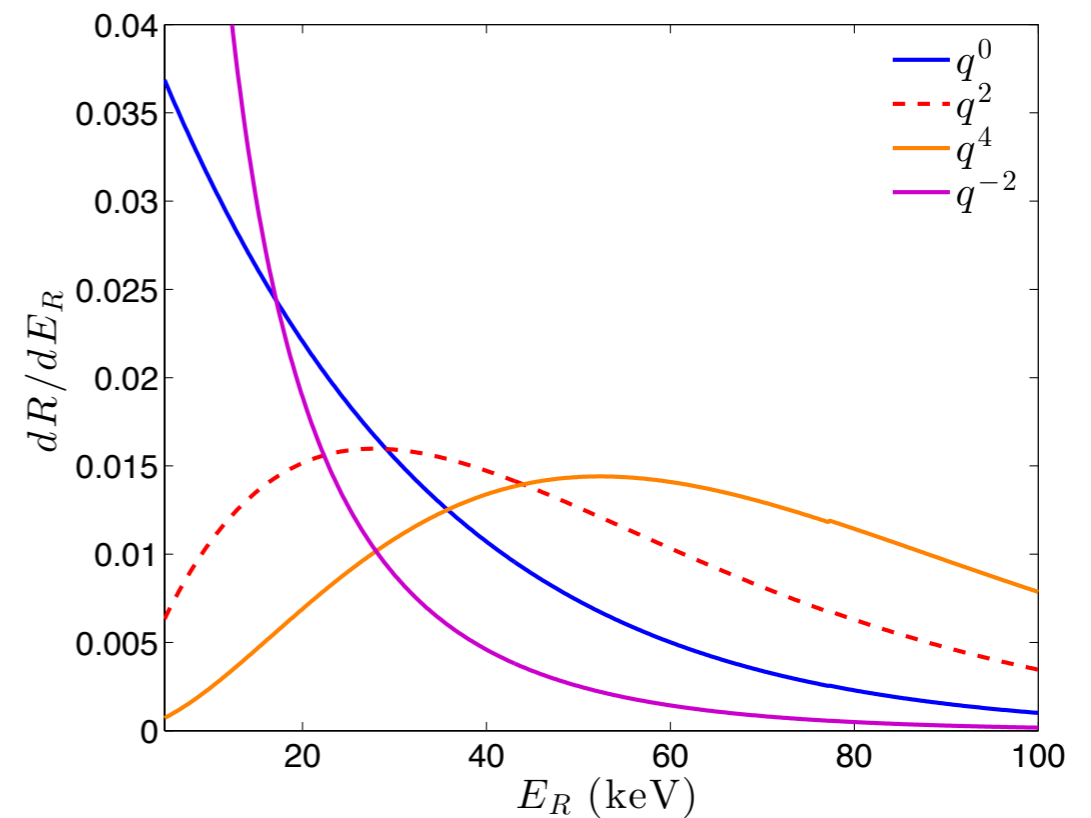
$$\sigma_{SD} = \sigma_0 \left(\frac{q}{q_0} \right)^4, \dots$$

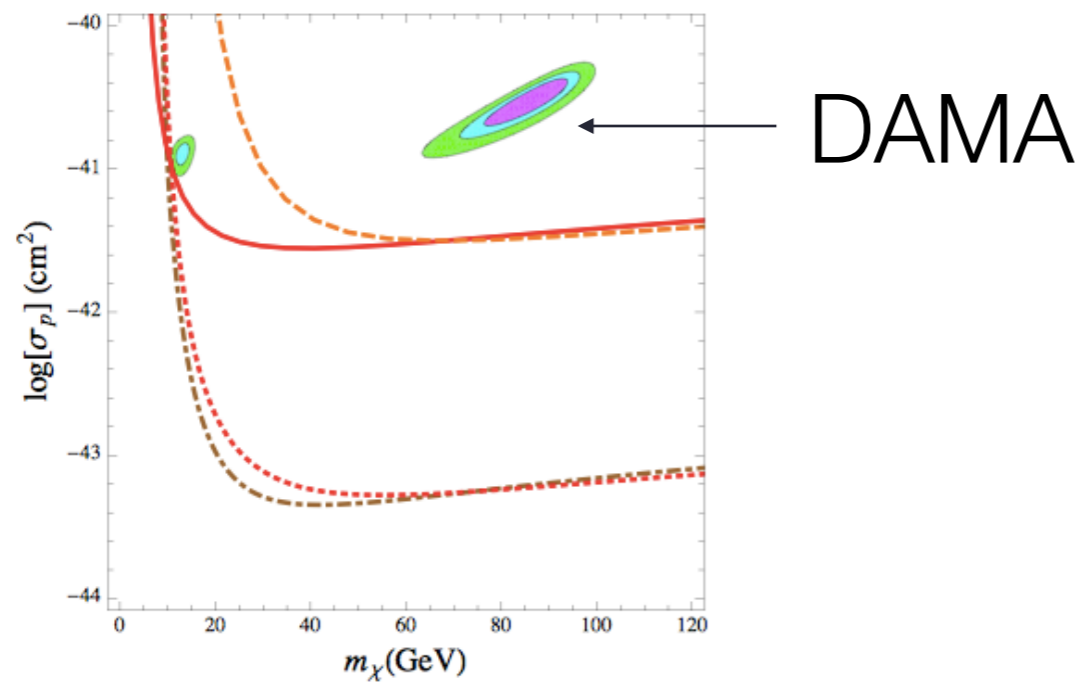
Velocity and momentum-dependent DM

Probing different parts of the DM velocity distribution with a given experiment:

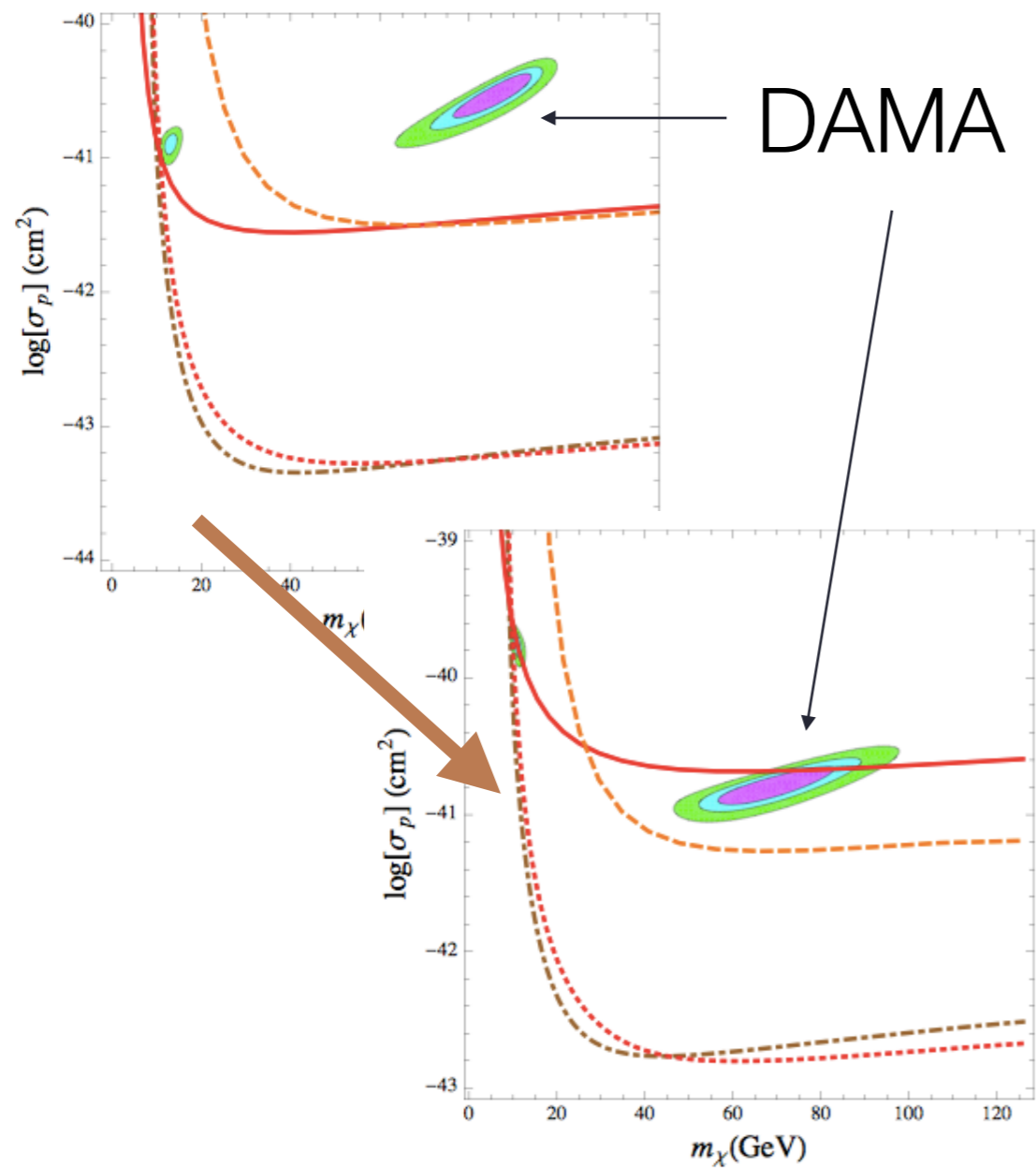


Different recoil spectra, mass dependence

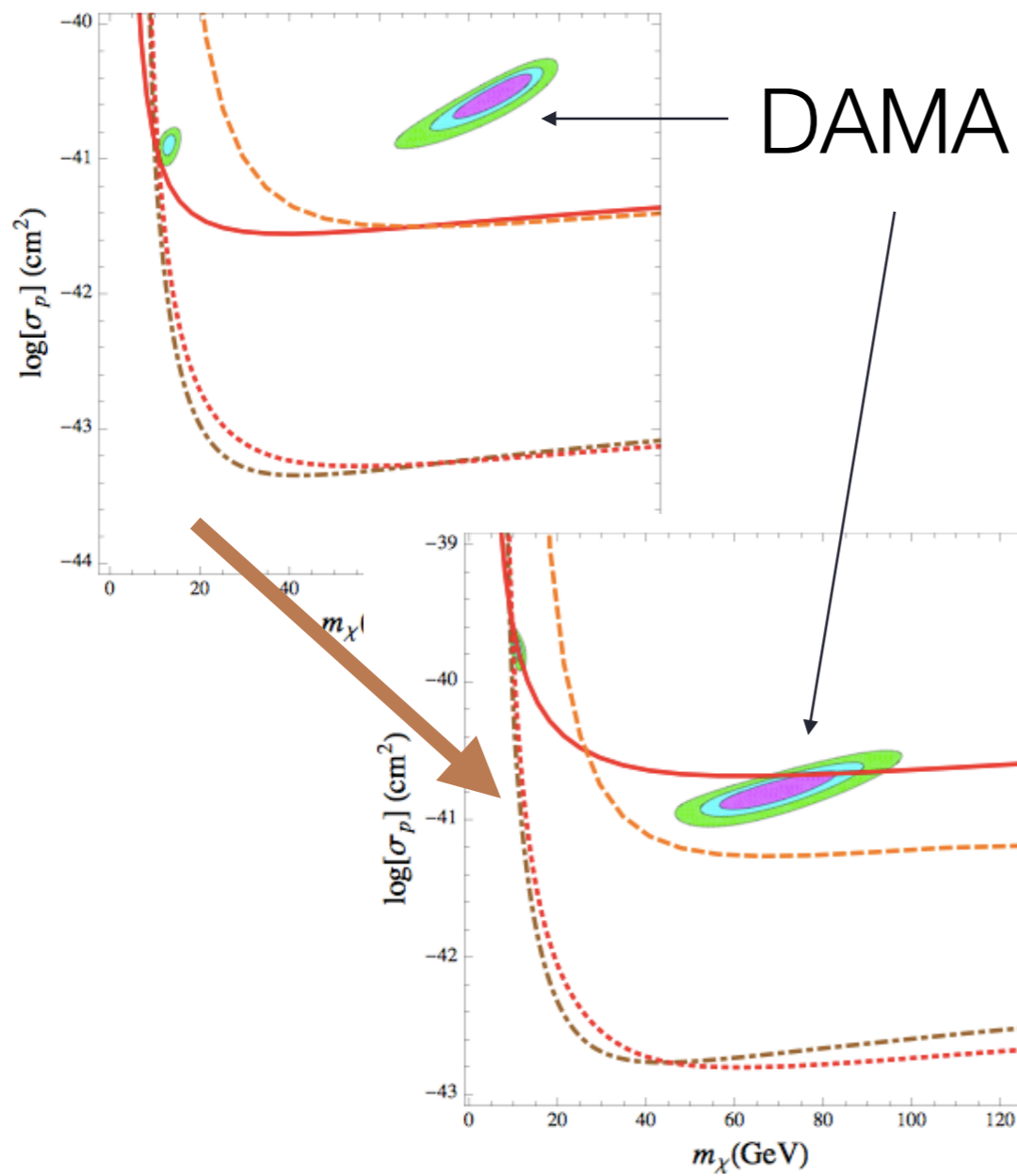




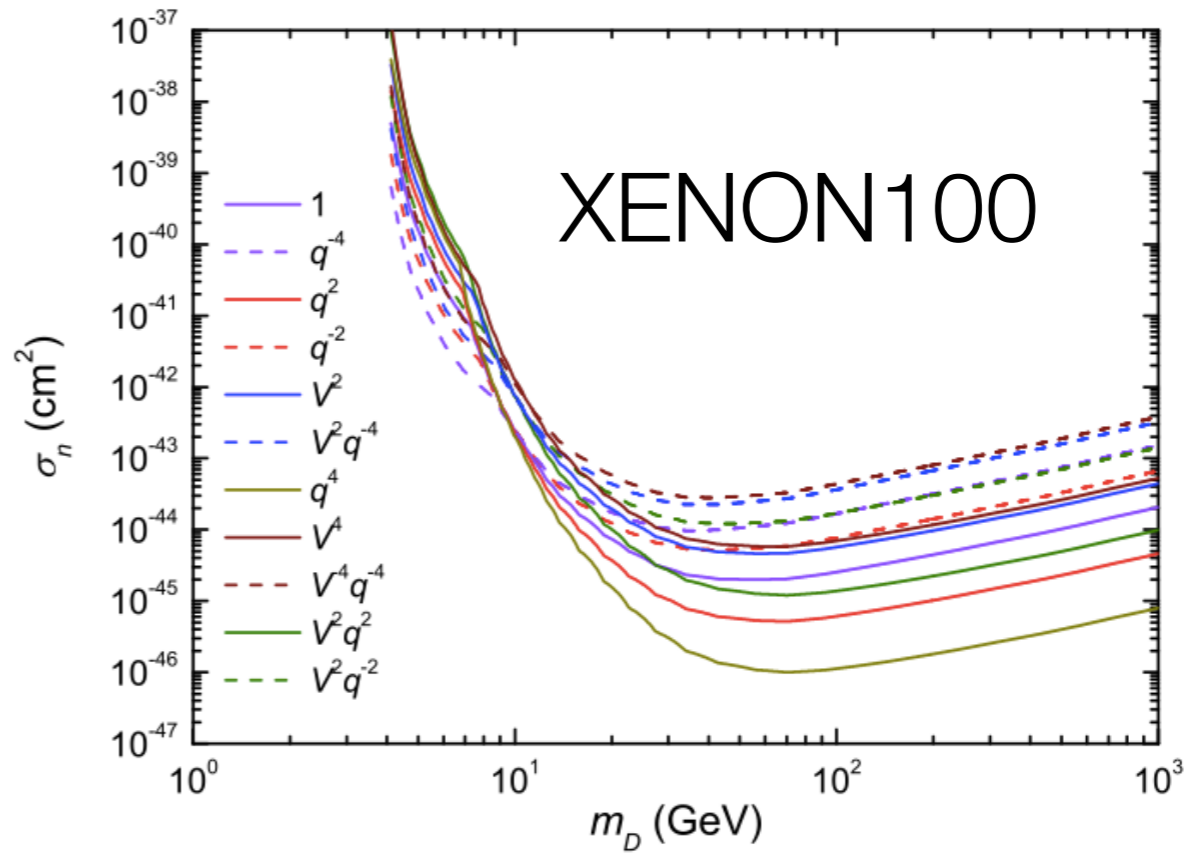
(Chang, Pierce, Weiner 2009)



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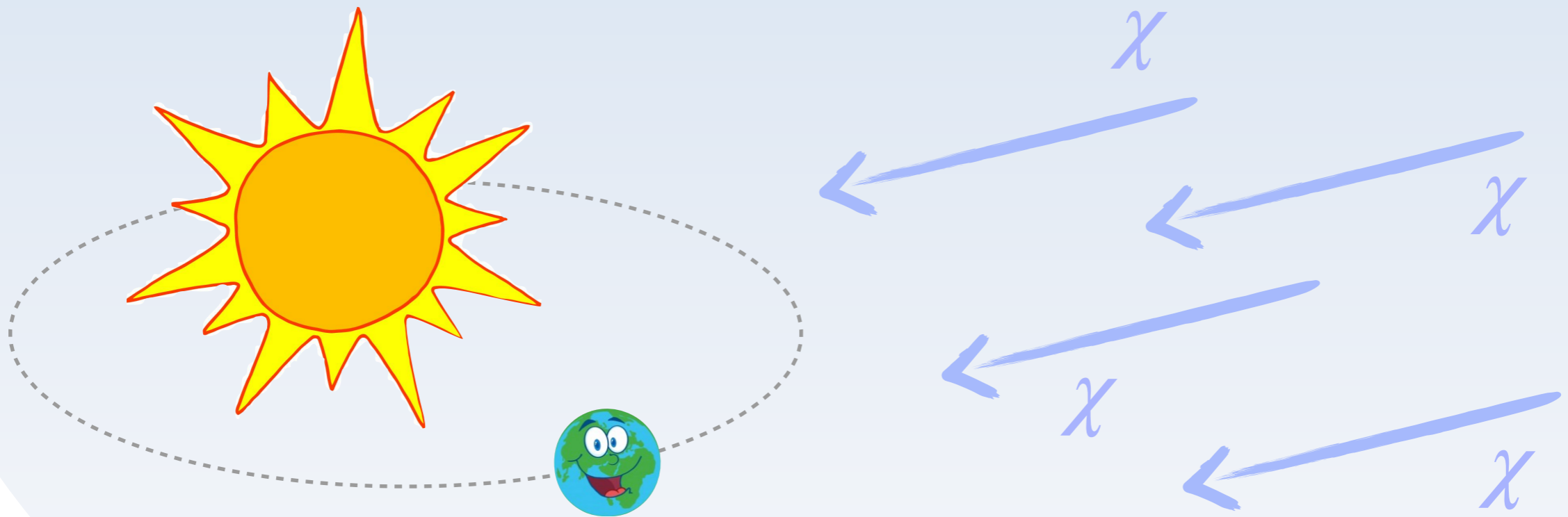
(Chang, Pierce, Weiner 2009)



(Guo, Liang, Wu 2014)

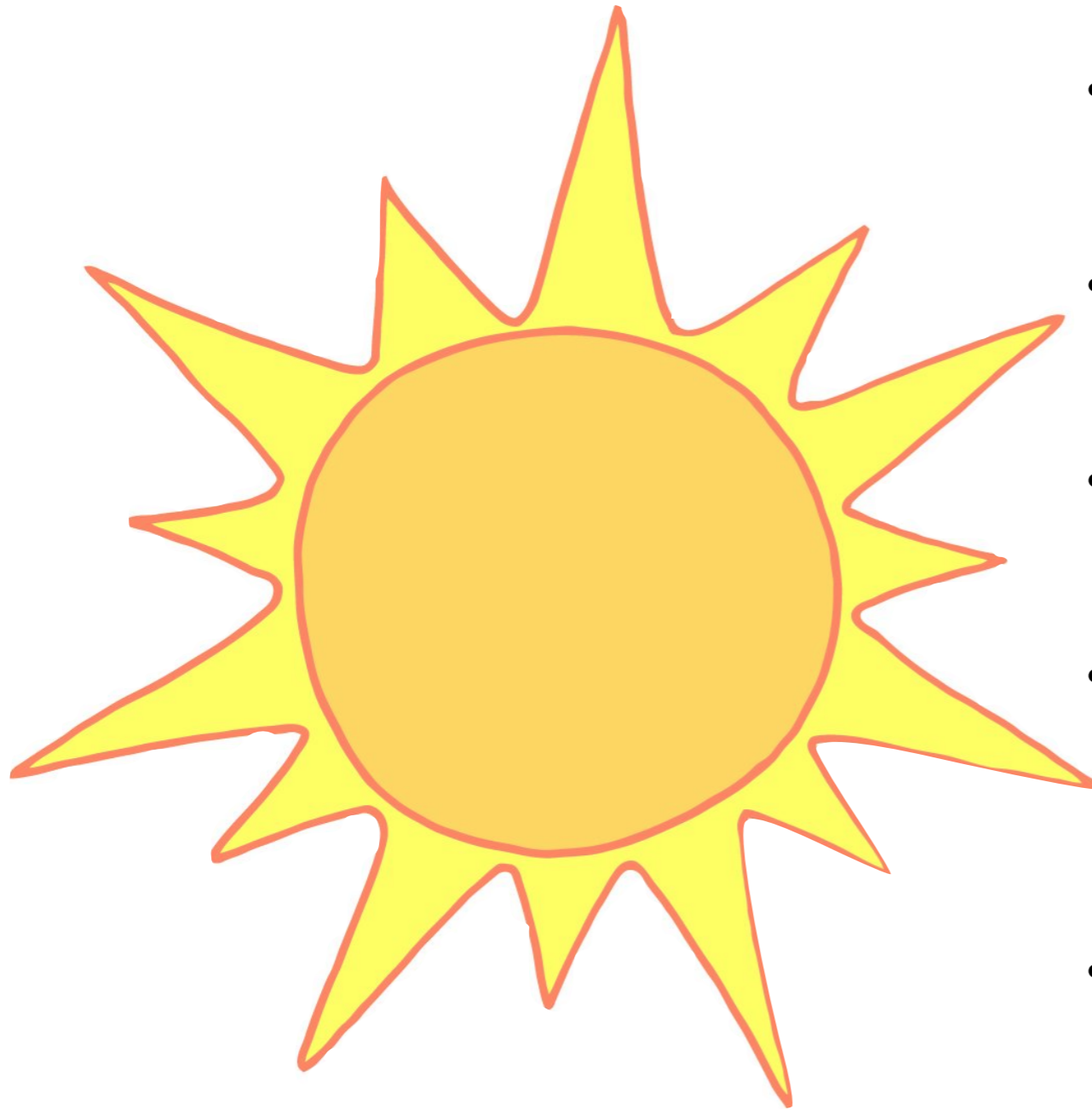
Dark Matter in the Sun

Direct detection



Probing the scattering cross-section between DM and quarks

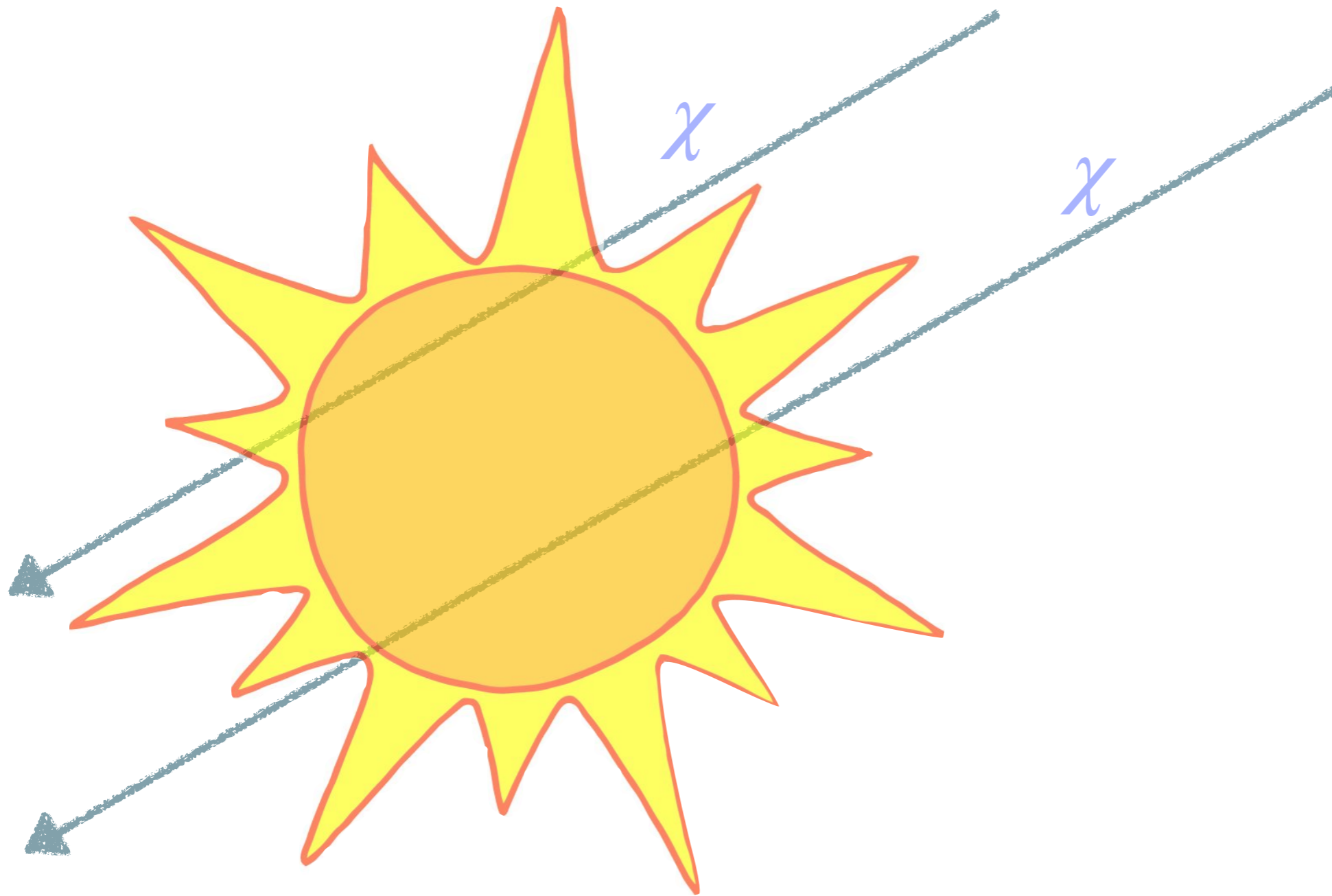
The sun is a direct detection experiment



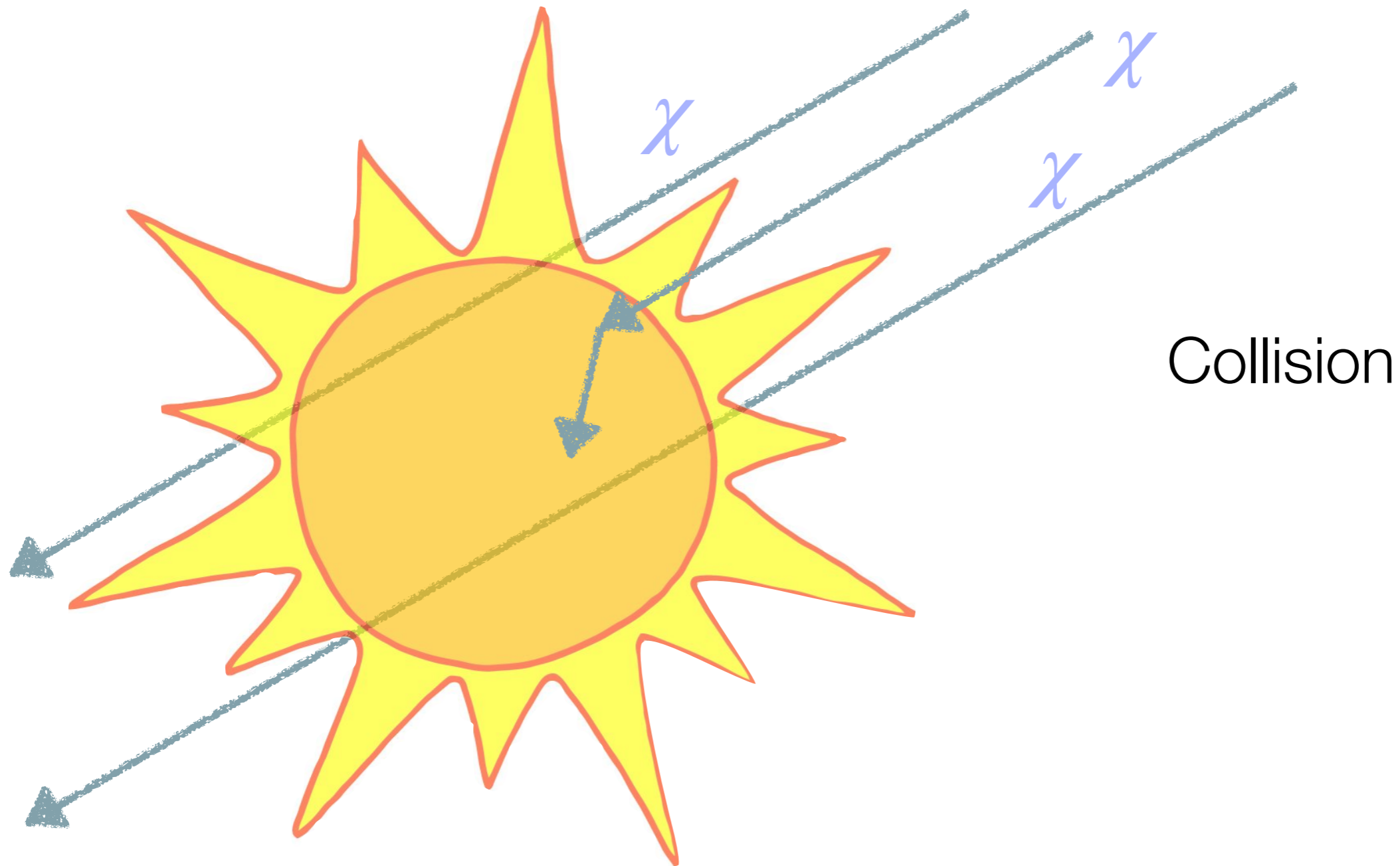
- $M = 2 \times 10^{30}$ kg
- 73% Hydrogen
- 25% Helium
- 2% Heavier elements
(important since $\sigma_{\chi N} \propto A^2$)
- $T = 4.57$ Gyr

10^{37} ton-year exposure (c.f. LZ: 5 ton-year)

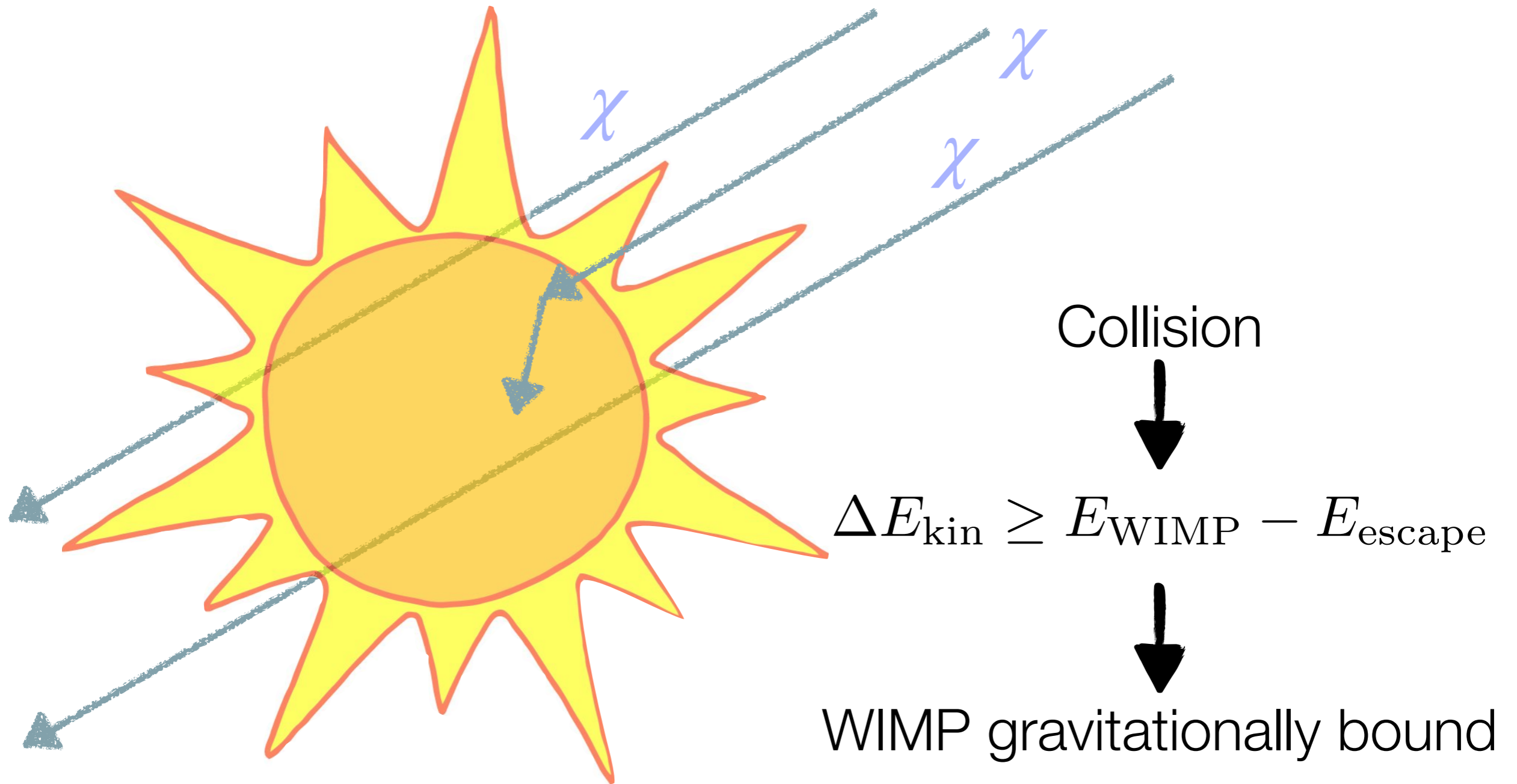
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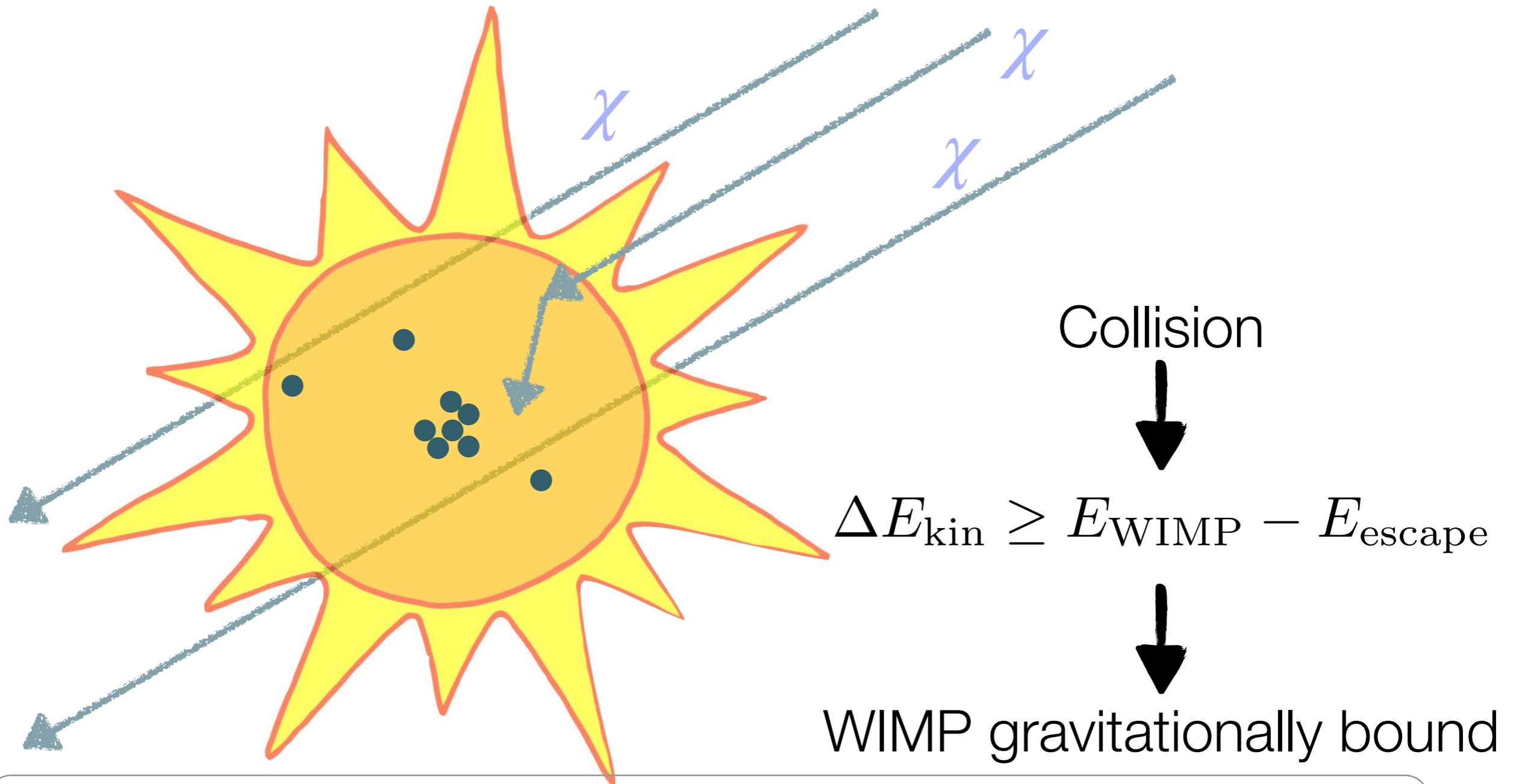
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The sun is a direct detection experiment



Population:

$$\frac{dN_{\chi}}{dt} = C(t) - 2A(t) - E(t)$$

Capture rate

$$C(t) = 4\pi \int_0^{R_\star} r^2 \int_0^\infty \frac{f(u)}{u} w \Omega_v^-(w) du dr,$$

$$f(u)$$

Halo DM velocity distribution

$$w(r) = \sqrt{u^2 + v_{esc}^2(r, t)}$$

Velocity at r , due to gravity

$$\Omega(w) \propto w \sum_i n_i \int |F_i(E_R)|^2 \frac{d\sigma_i}{dE_R} dE_R$$

Rate at which a WIMP of velocity w can scatter below v_{esc}

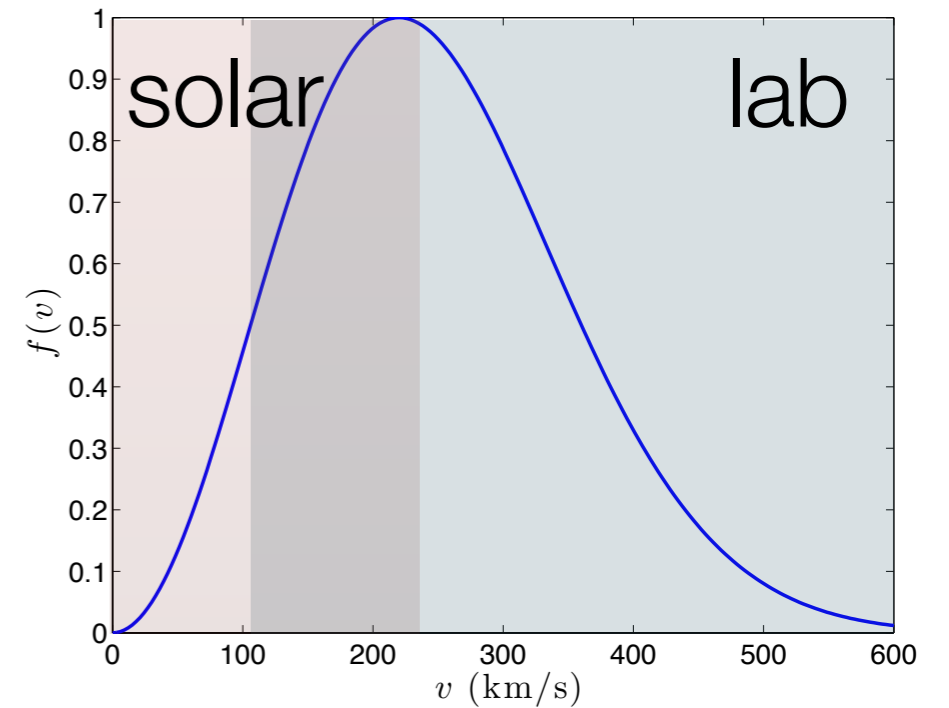
c.f. direct detection:

$$R = \int_{E_T}^\infty dE_R \frac{\rho_0}{m_N m_\chi} \int_{v_{min}}^\infty v f(v) \frac{d\sigma_{WN}}{dE_R}(v, E_R) dv$$

Differences with earth-based DD

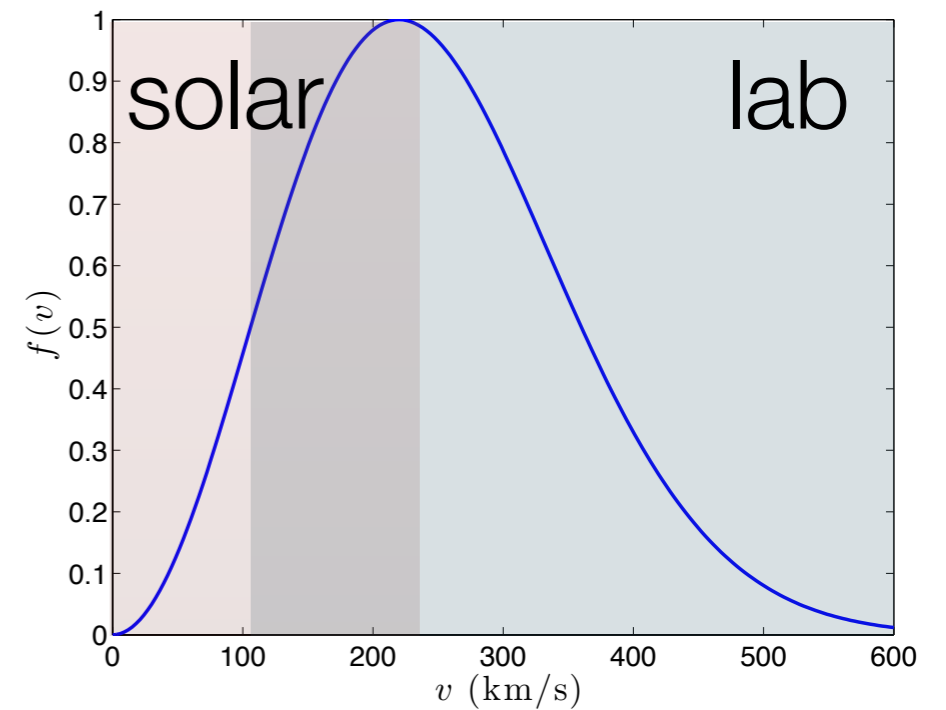
Differences with earth-based DD

- Probing different parts of the halo velocity distribution
 - DD: above threshold
 - Solar: low part (v_{esc})



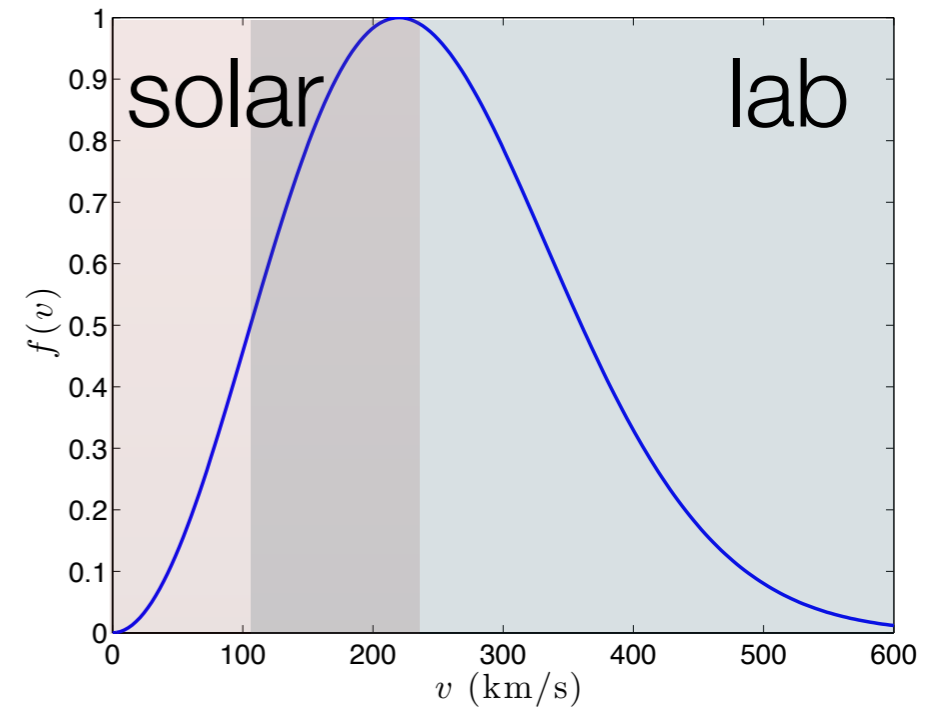
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- Probing different kinematic range (scattering with lighter elements)



Differences with earth-based DD

- Probing different parts of the halo velocity distribution
 - DD: above threshold
 - Solar: low part (v_{esc})
- Probing different kinematic range (scattering with lighter elements)
- Spin sensitivity

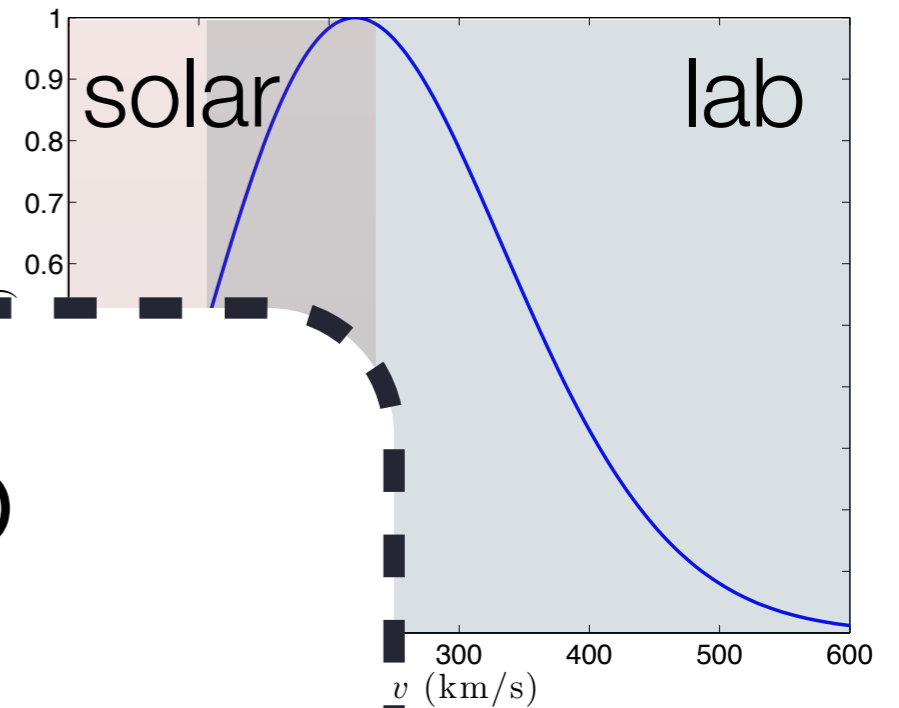


More sensitive to
lighter DM

Different couplings?

Differences with earth-based DD

- Probing different parts of the halo velocity distribution



- DD: ak

Sensitive to

- Solar: l

q v_{rel}

- Probing different range (scattering elements)

Sensitive to

lighter DM

- Spin sensitivity

Different couplings?

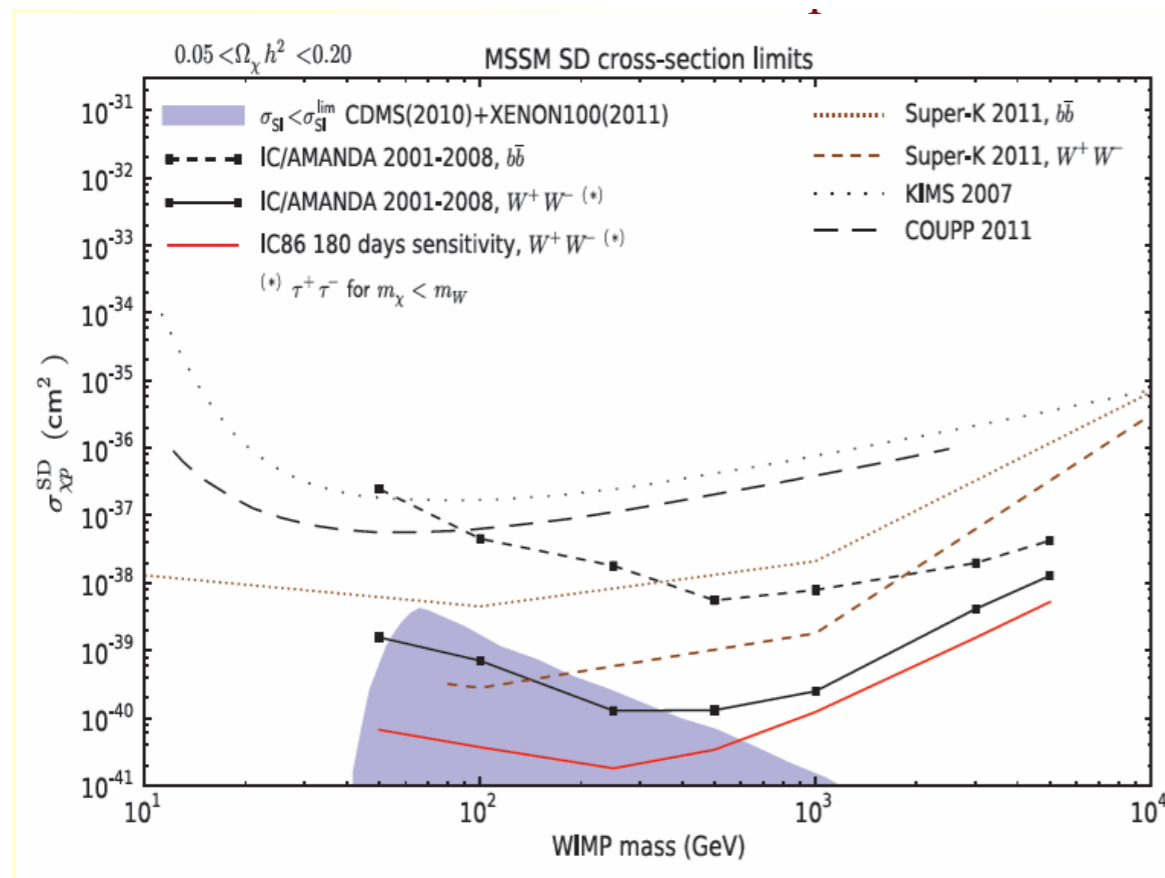
DM in the sun: observable effects

DM in the sun: observable effects

Annihilation

The most obvious observable effect is annihilation:

- DM-DM \longrightarrow neutrinos: direct observation



Very competitive

but

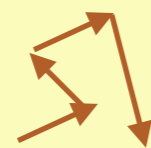
Model-dependent

DM in the sun: observable effects

Energy transport

If the self-annihilation is suppressed enough (e.g. in as in **asymmetric DM**), the “cloud” of DM accumulated in the solar core can transport kinetic energy outwards:

Core



nucleus mean free path $\lambda_{\text{nuc}} \ll r_{\text{core}}$

DM mean free path $\lambda_{\chi} \gg \lambda_{\text{nuc}}$

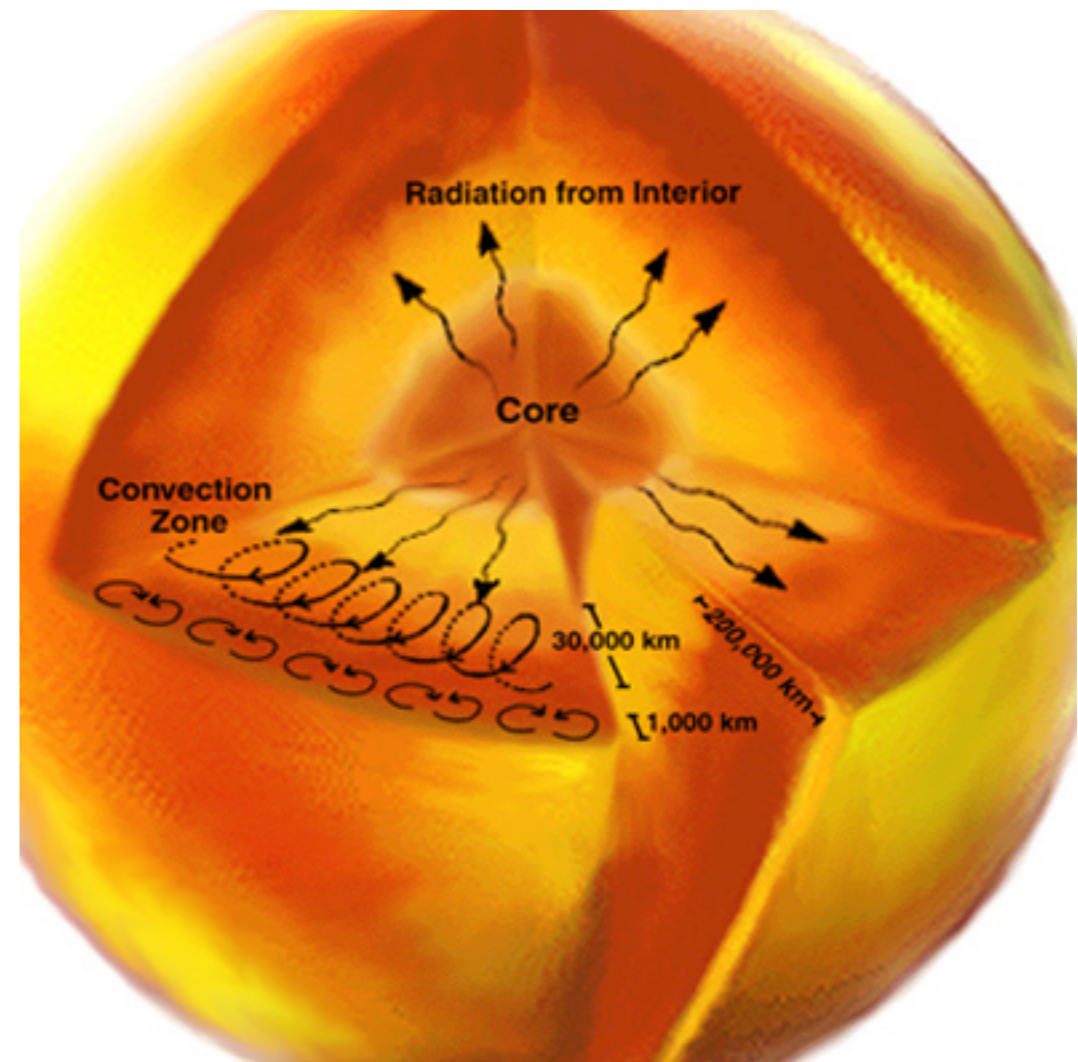
Wimps in the sun: observable effects

Energy transport

Heat transport away from the core — effects:

Change in temperature
visible with ^8B **neutrinos**

$$\phi_{\nu, ^8\text{B}} \propto T_c^\beta; \beta \sim 20 - 25 !!$$



Wimps in the sun: observable effects

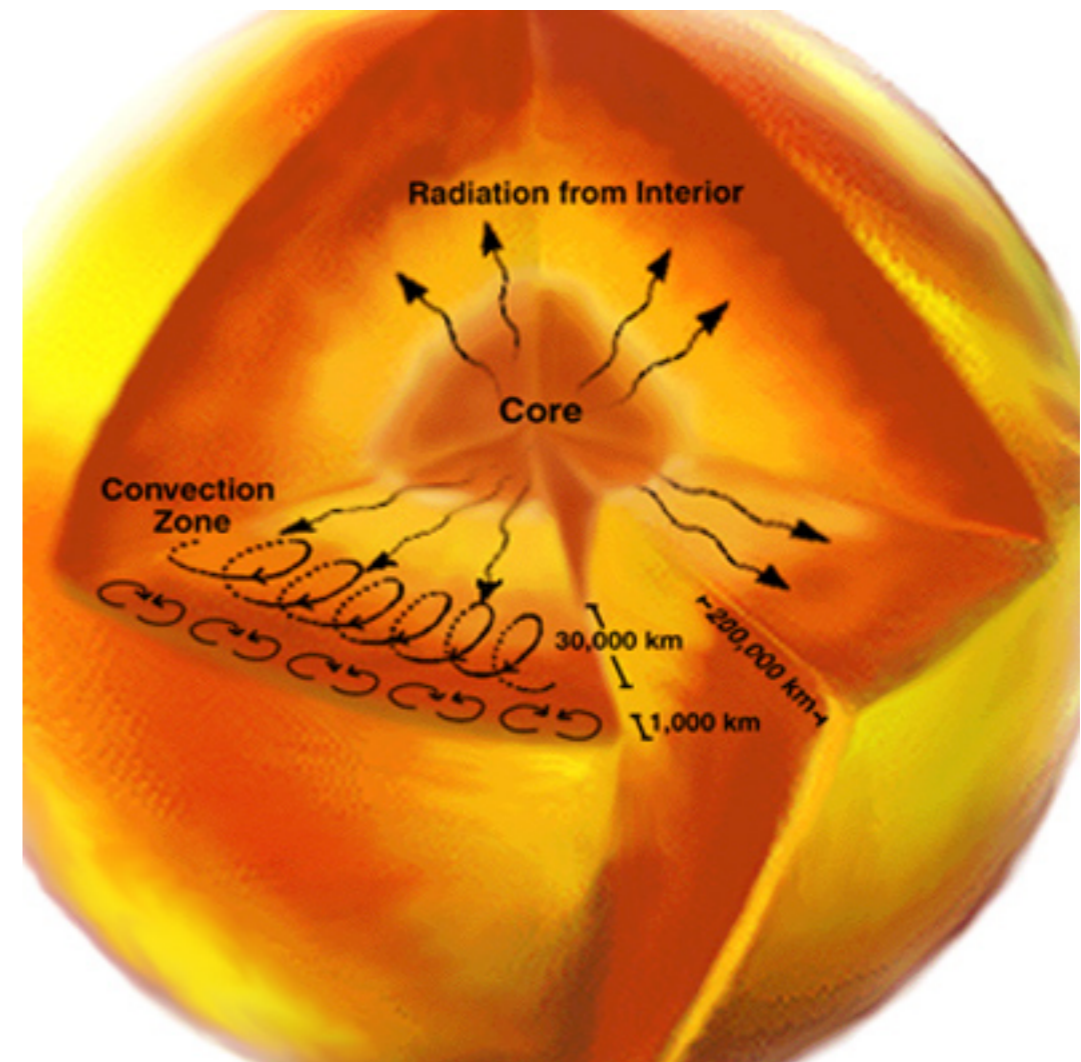
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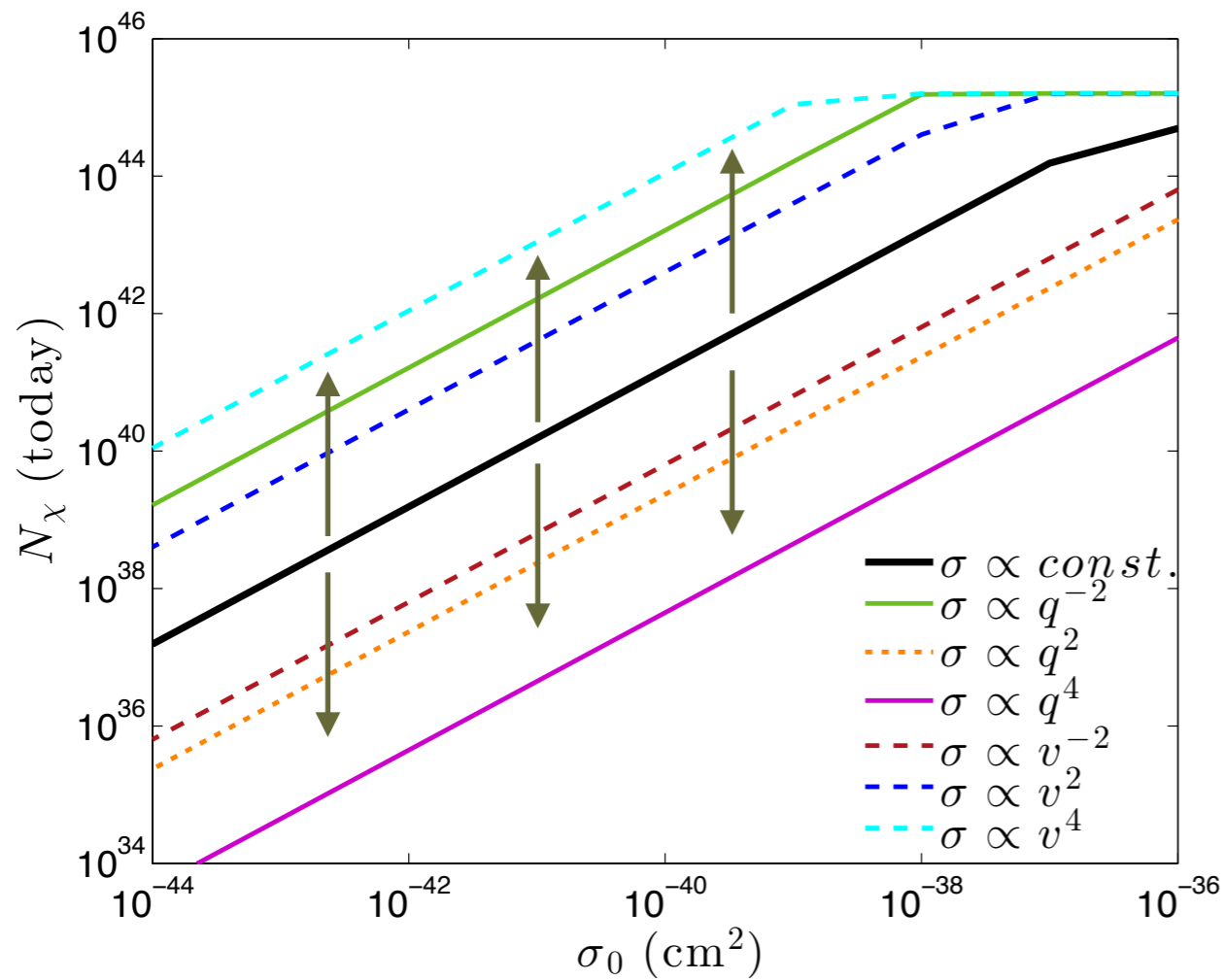
Change in structure
sound speed and
height of the convective
zone can be inferred
from **helioseismology**



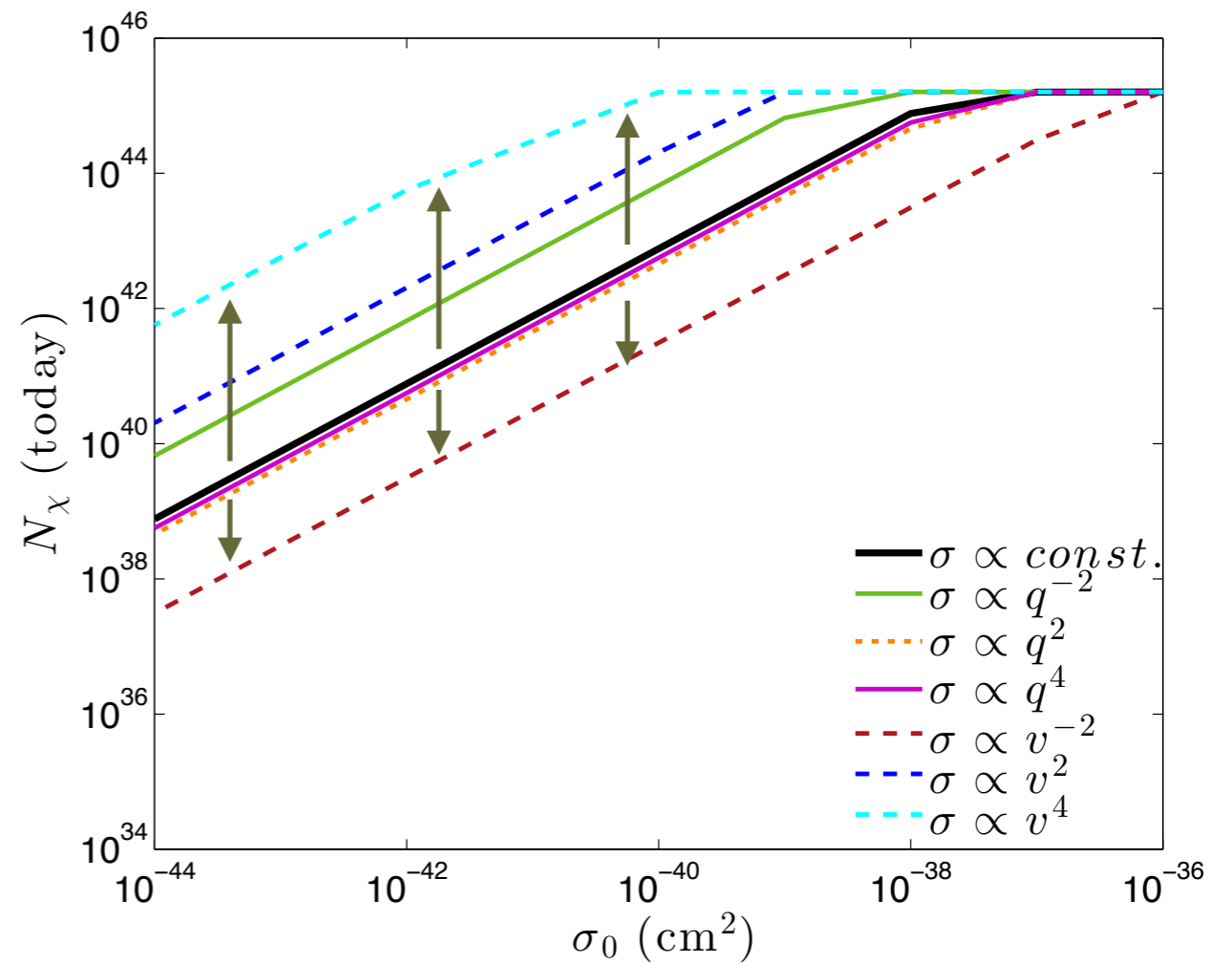
q and v-dependent DM in the Sun

Capture rates

Spin-dependent

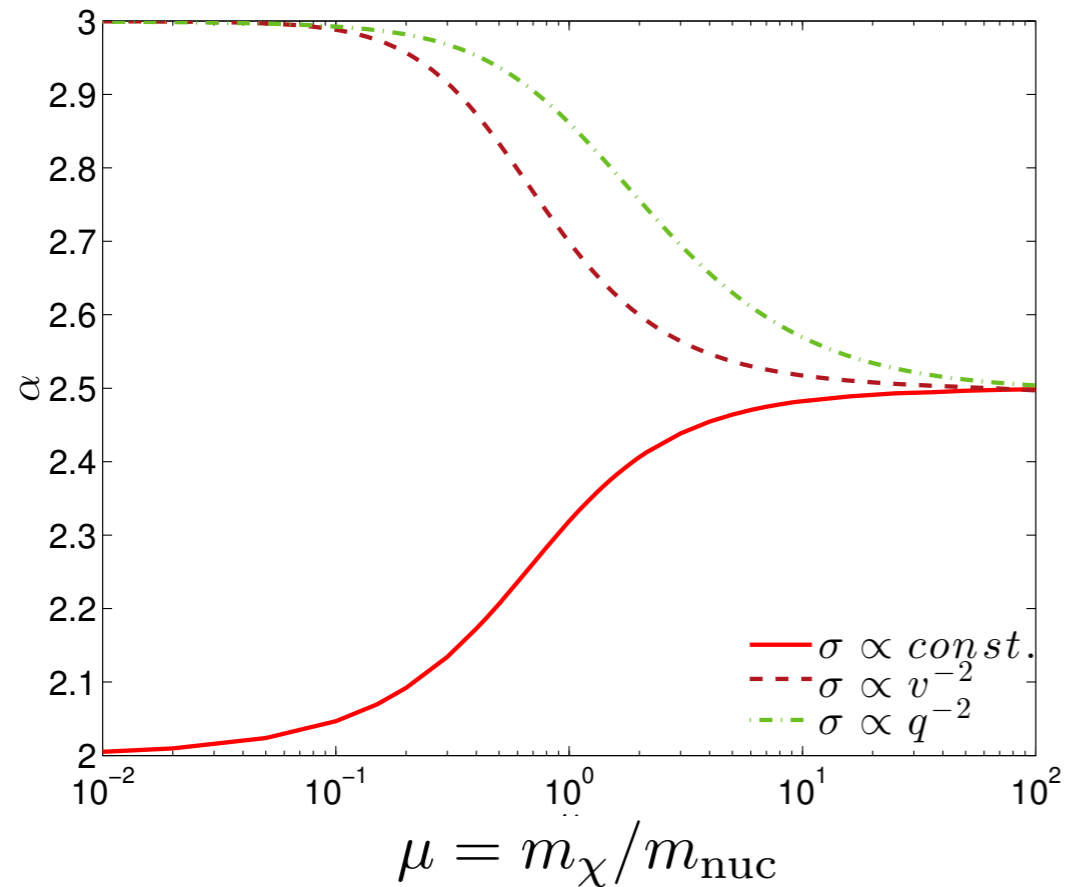


Spin-independent

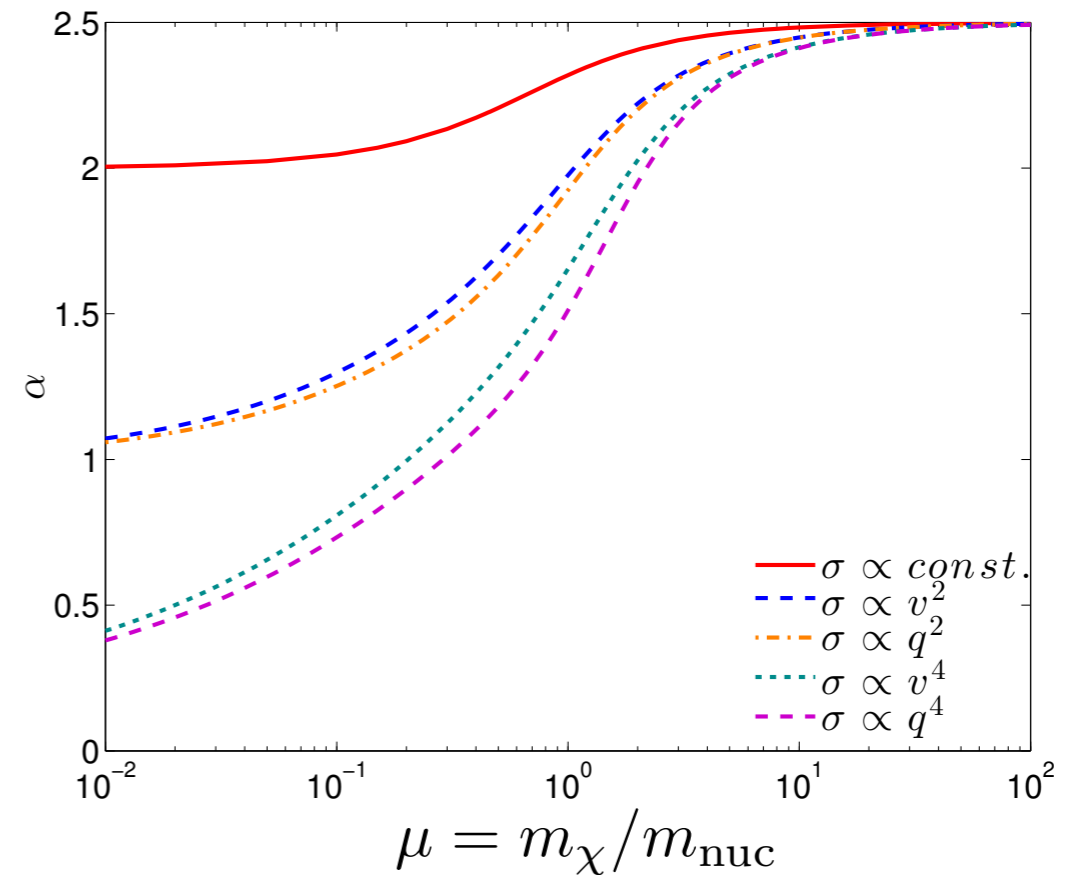


Enhancement: v^{+n} or q^{-n}

Diffusion coefficient α

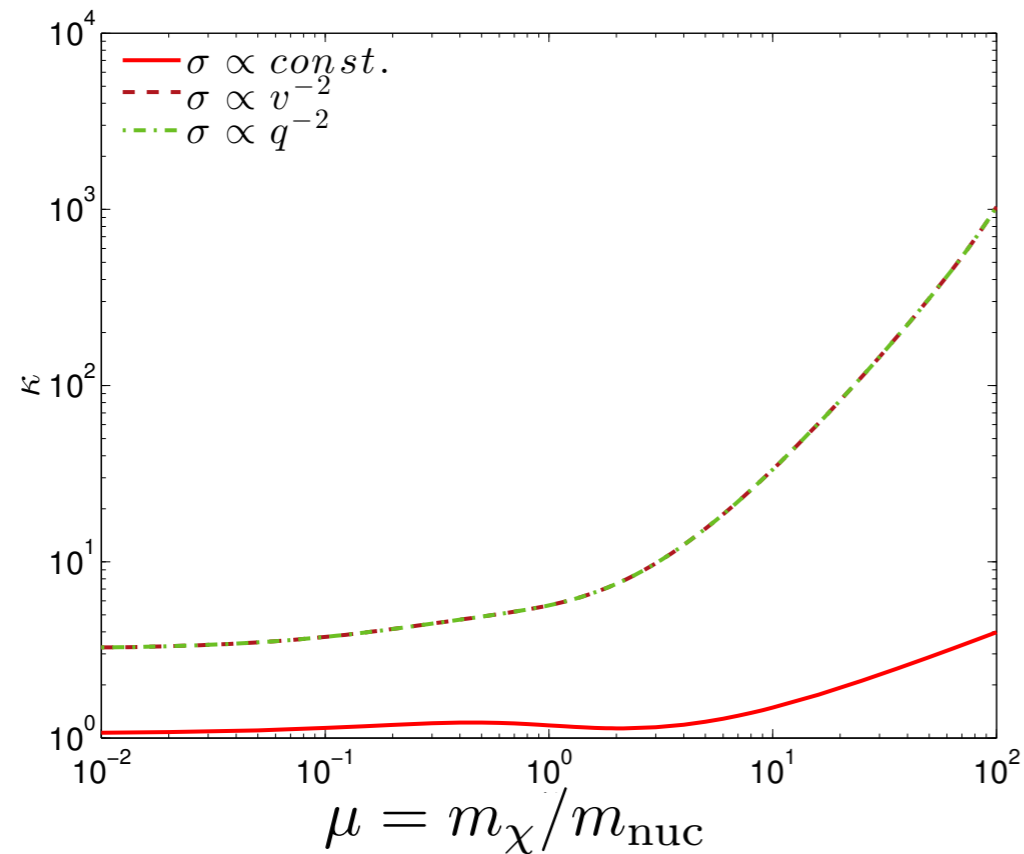


$n < 1$: “fluffier” dark matter core

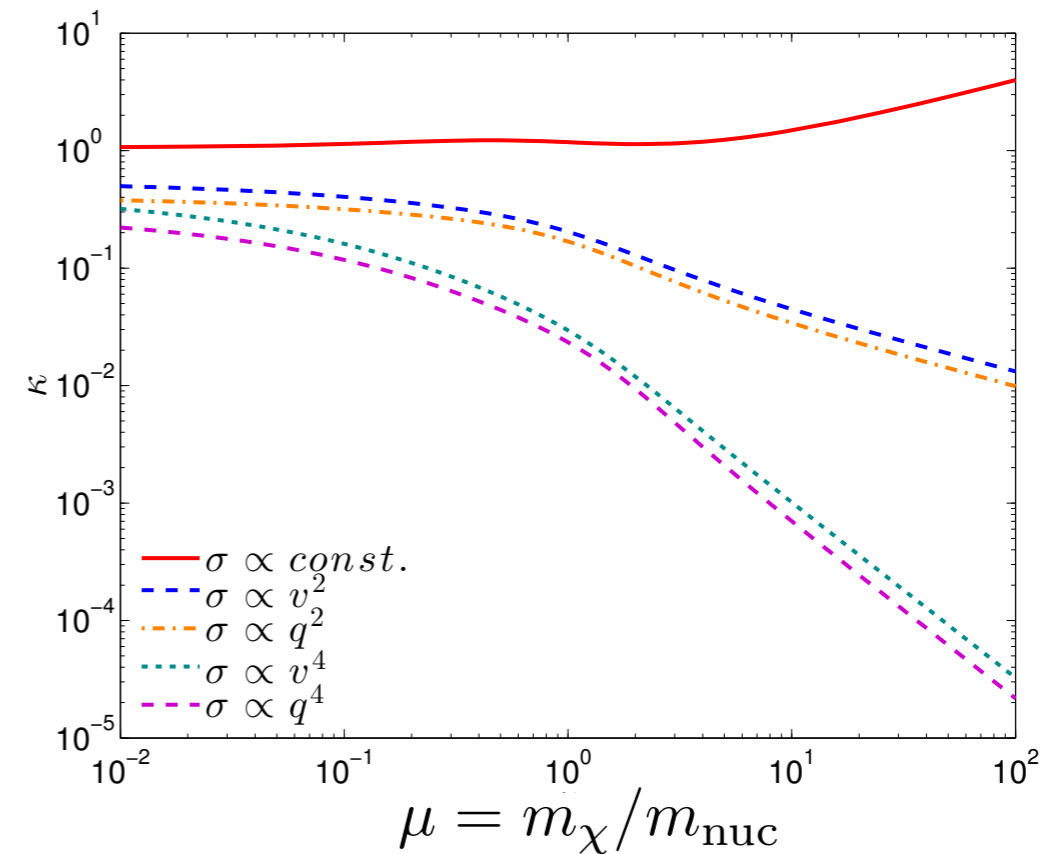


$n > 1$: “tighter” dark matter core

Conduction coefficient κ




$n < 1$: more efficient
energy transport



$n > 1$: less efficient
energy transport

Heat transport

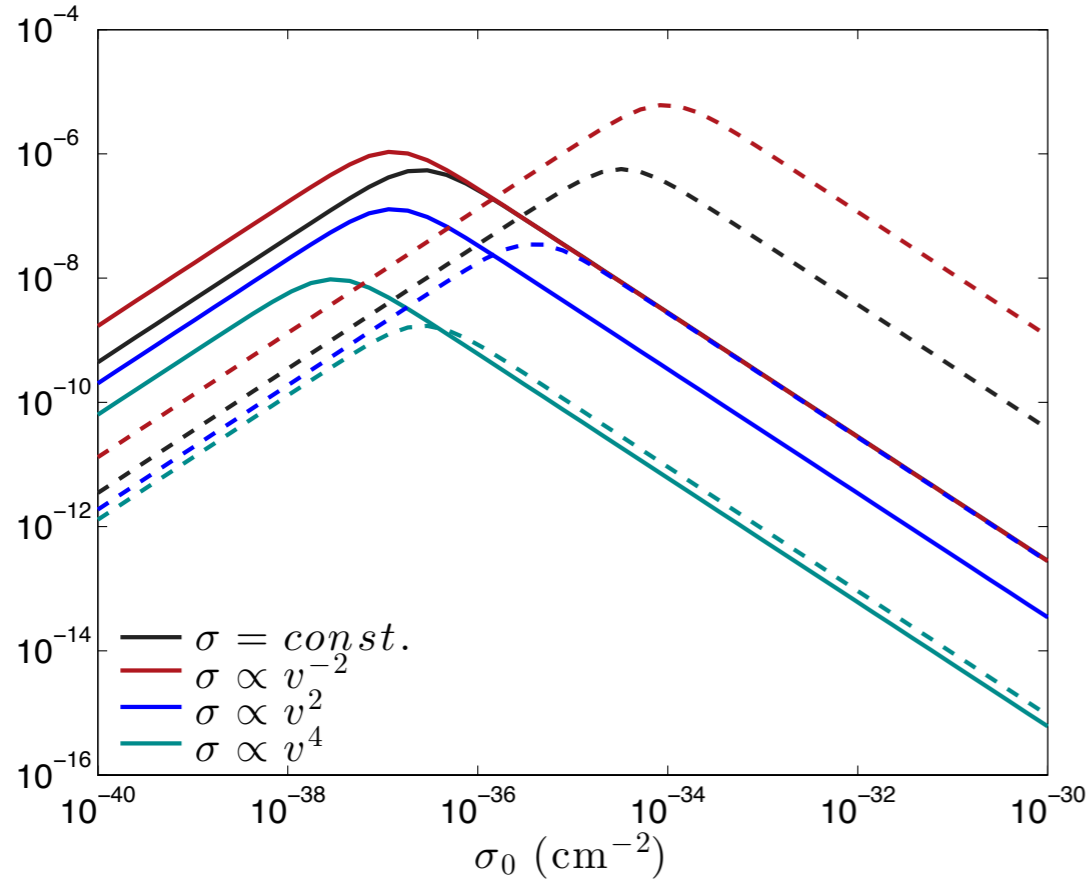
$$L_\chi(r) = 4\pi r^2 \zeta^{2n}(r) \kappa(r) n_\chi(r) l_\chi(r) \left[\frac{k_B T(r)}{m_\chi} \right]^{1/2} k_B \frac{dT(r)}{dr}$$


$$\propto \frac{1}{\langle \sigma \rangle}$$

Smaller cross-section: DM can deposit energy farther away

Local vs non-local

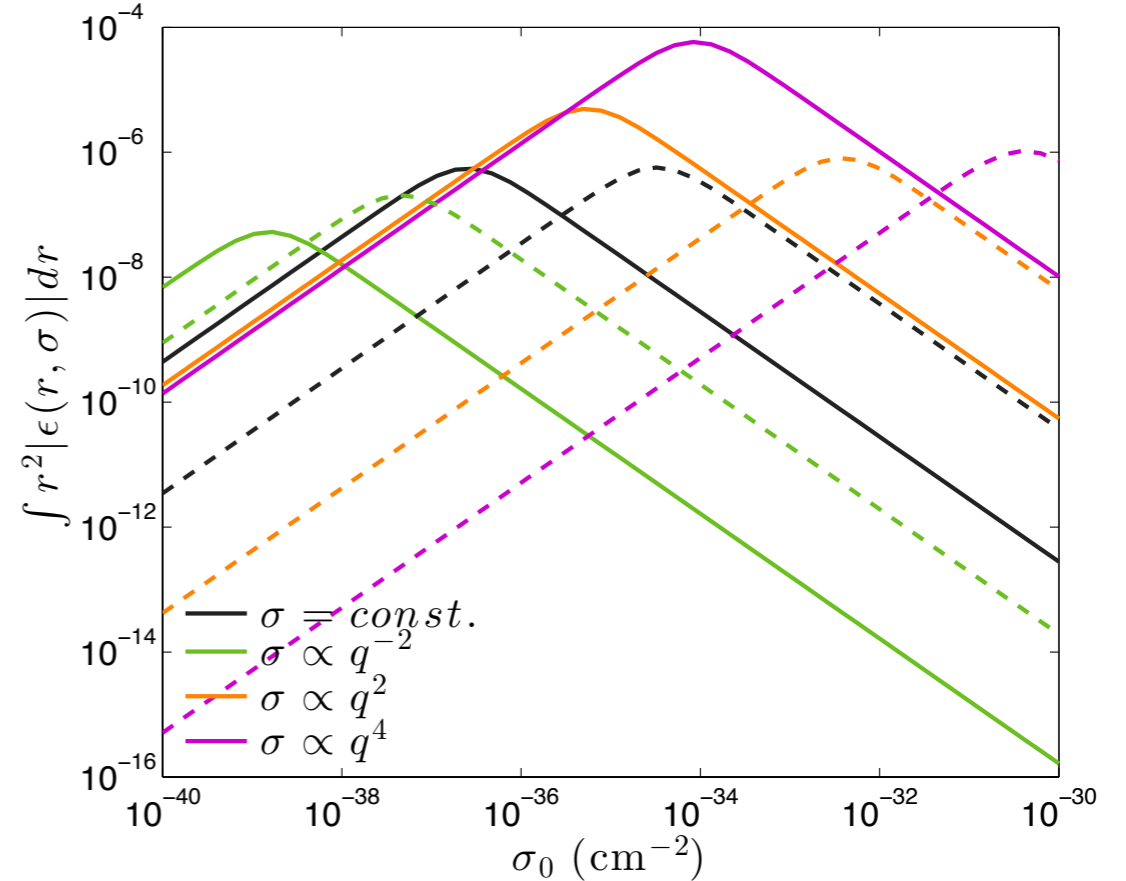
Knudsen ← Local



$$n_{\chi}(r) = f(K)n_{\chi,\text{LTE}} + [1 - f(K)]n_{\chi,\text{iso}},$$

$$L_{\chi,\text{total}}(r, t) = f(K)\mathfrak{h}(r, t)L_{\chi,\text{LTE}}(r, t).$$

Knudsen ← Local



$$\mathfrak{h}(r) = \left(\frac{r - r_{\chi}}{r_{\chi}} \right)^3 + 1,$$

$$f(K) = \frac{1}{1 + \left(\frac{K}{K_0} \right)^{1/\tau}},$$

DarkStars

(Scott, Edsjo, Fairbairn 2009)

STARS + DarkSUSY

WIMP capture, annihilation and heat transport

Generic stellar evolution



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STARS + DarkSUSY

WIMP capture, annihilation and heat transport

Generic stellar evolution



+

GARSTEC

(Weiss & Schlattl 2008)

High-precision (10^{-5}) solar simulation code

Standard Solar Model: Full evolution from protostar to current age (4.57 Gyr)

Nuclear burning, heat transport, convection, accurate EOS, molecular diffusion.



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DarkStec

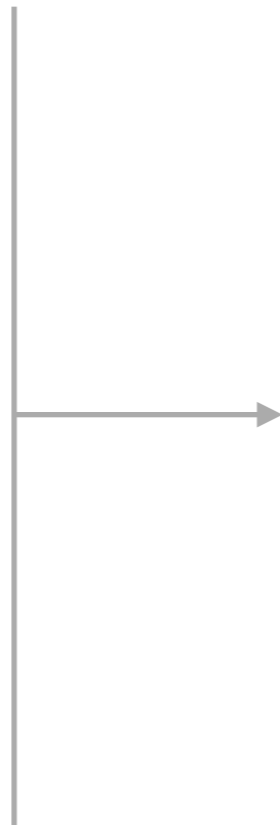
High-precision solar DM code including v and q -dependence



Net effect of asymmetric DM in the Sun

Large cross-section:
more captured DM

Optimal transport at
Knudsen-LTE
boundary

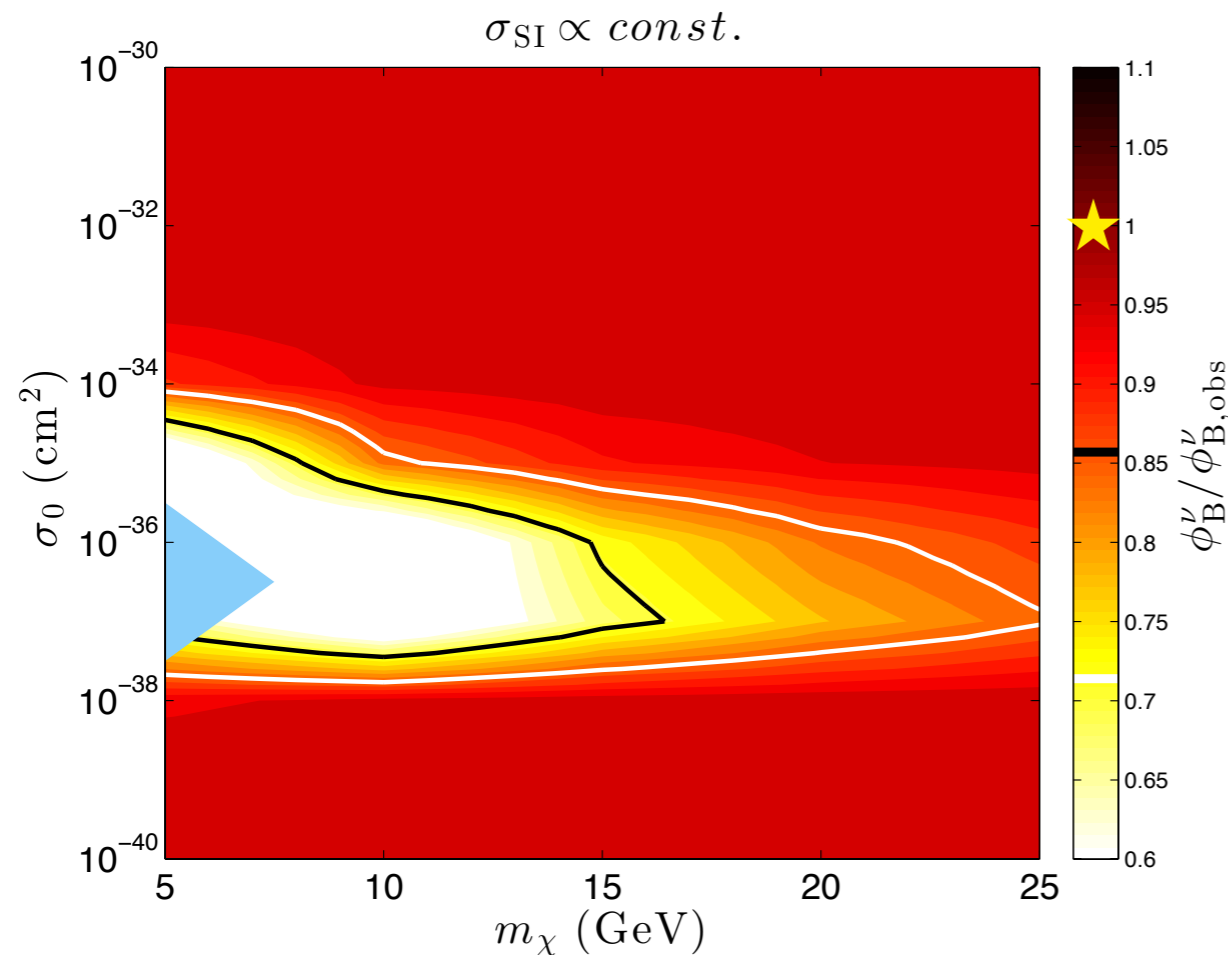


Maximum effect:

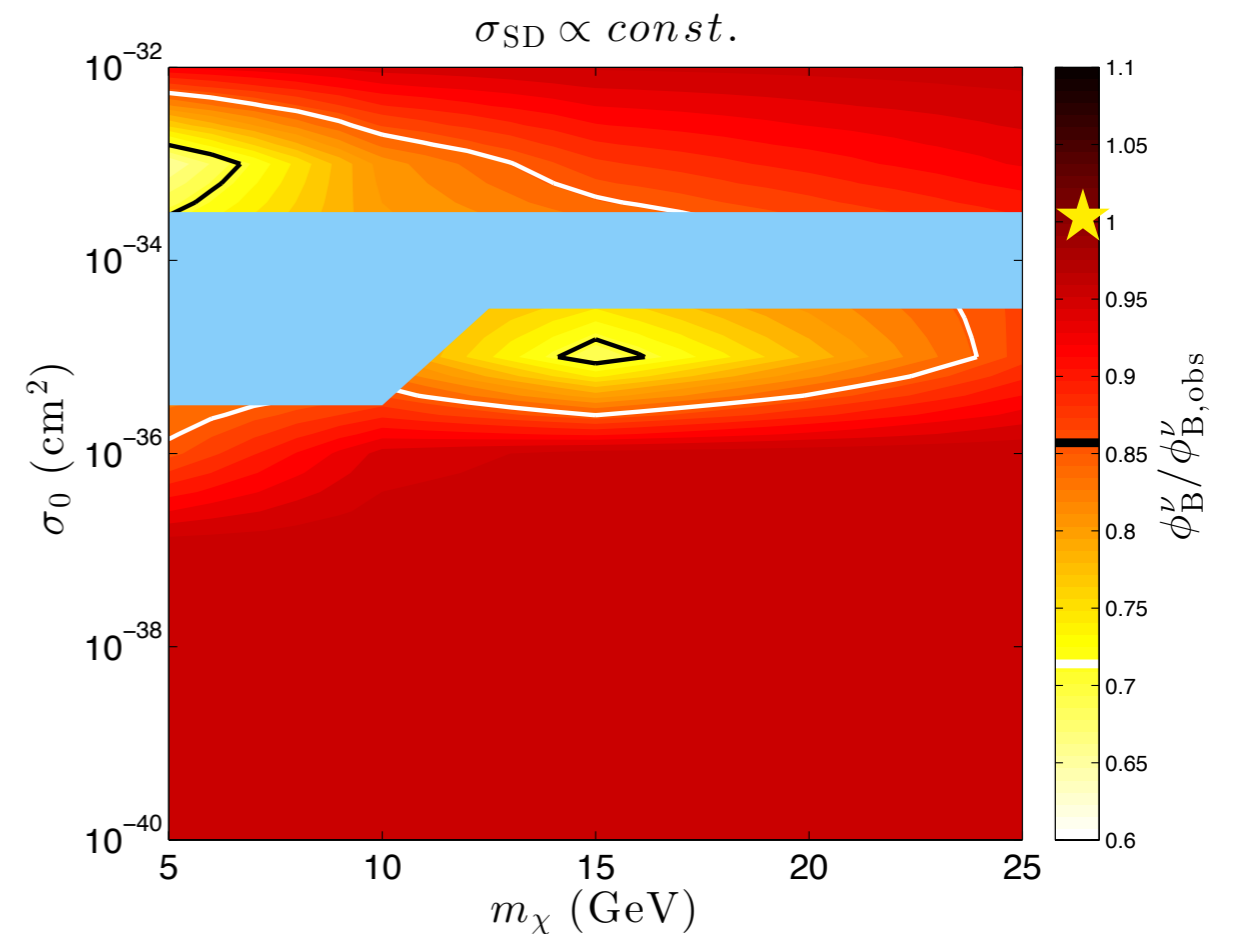
$$\sigma_{SD} \sim 10^{-34} \text{ cm}^2$$

$$\sigma_{SI} \sim 10^{-37} \text{ cm}^2$$

Neutrino fluxes: constant cross-section



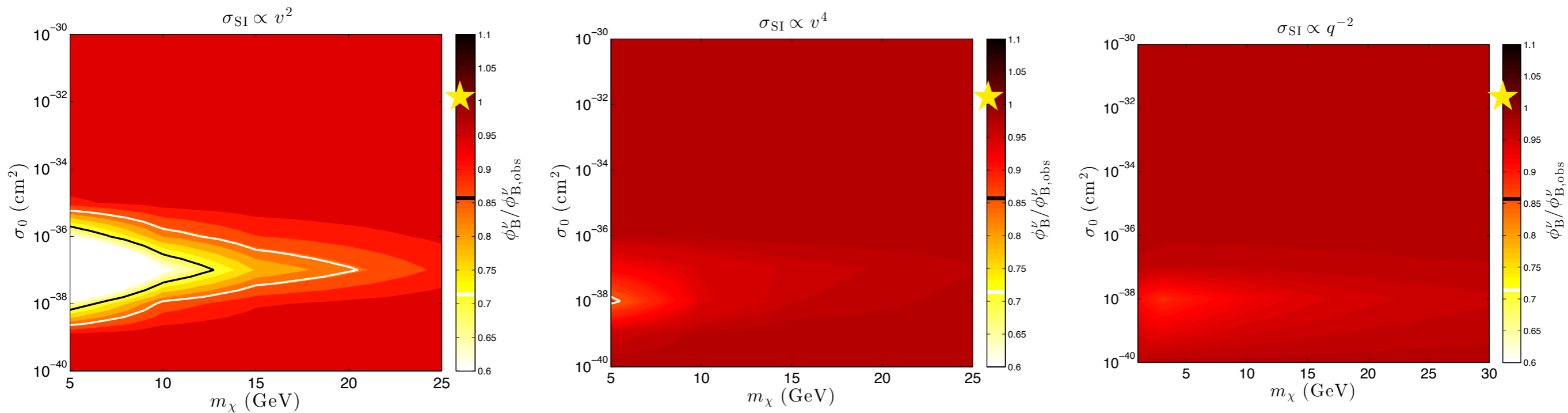
Spin dependent



Spin dependent

Unconverged models (changes too drastic)

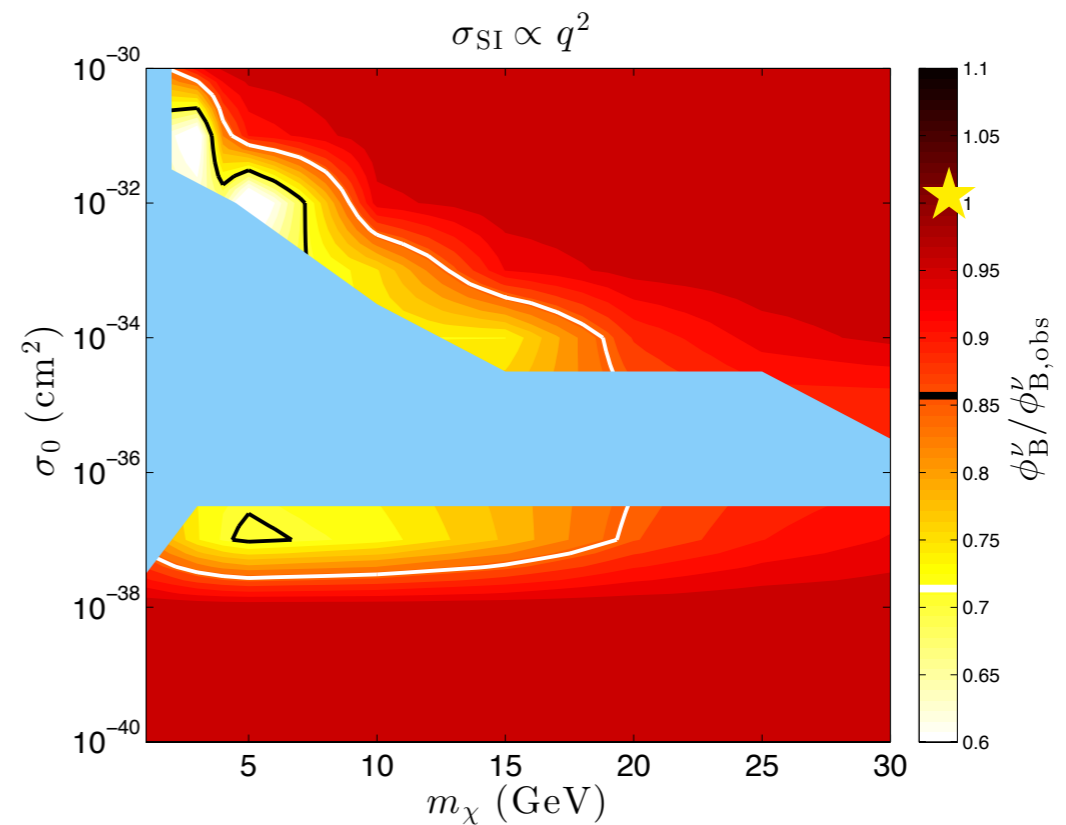
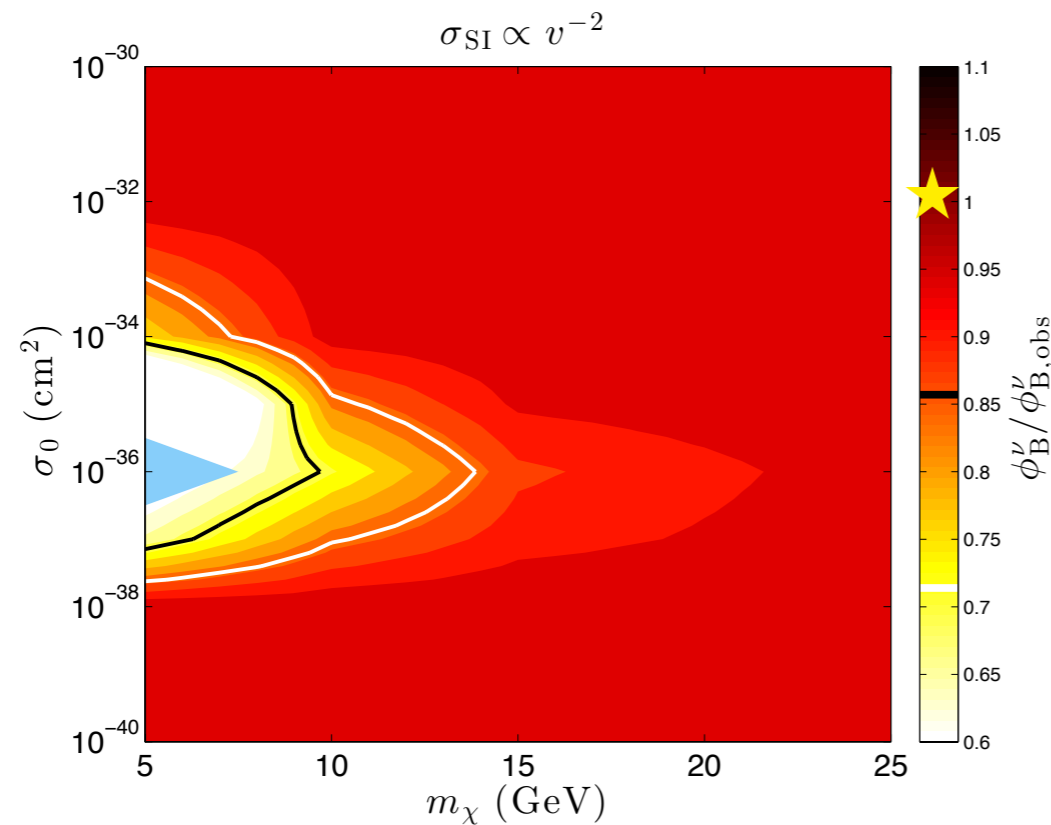
Neutrino fluxes: $\sigma \sim v^2, v^4, q^{-2}$



Enhanced capture rate:
maximum transport
window at lower cross-
section

**Suppressed mean free
path:**
Less overall heat conduction

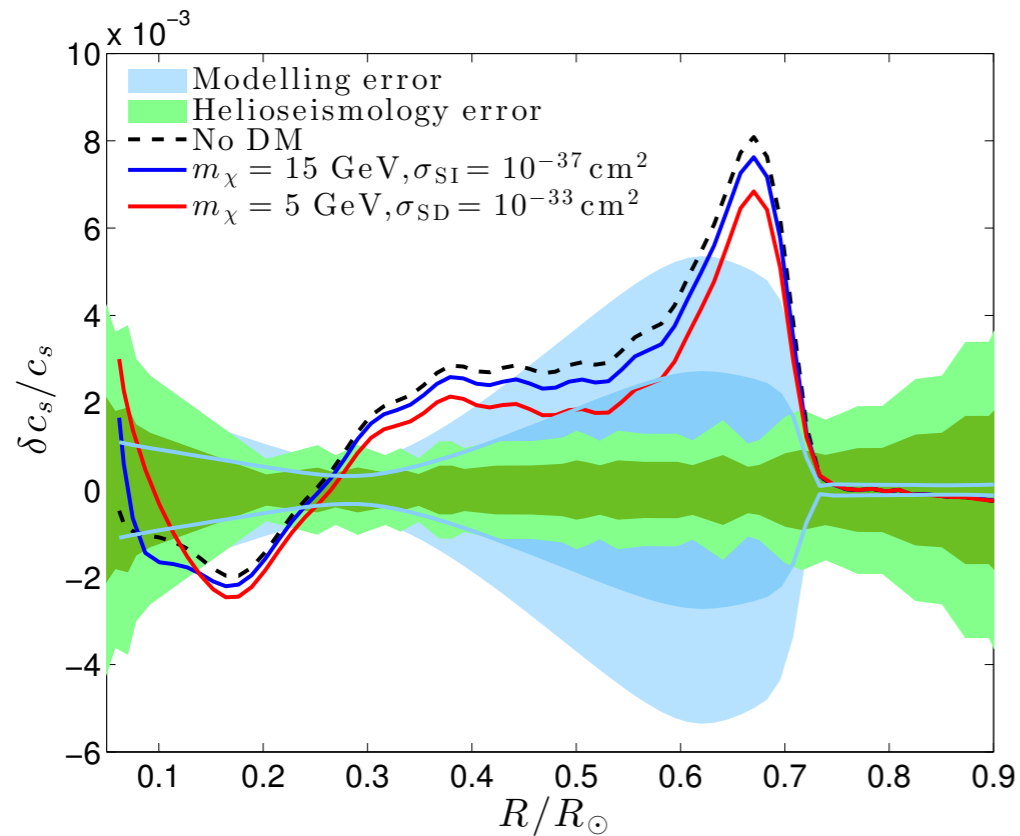
Neutrino fluxes: $\sigma \sim v^{-2}, q^2$



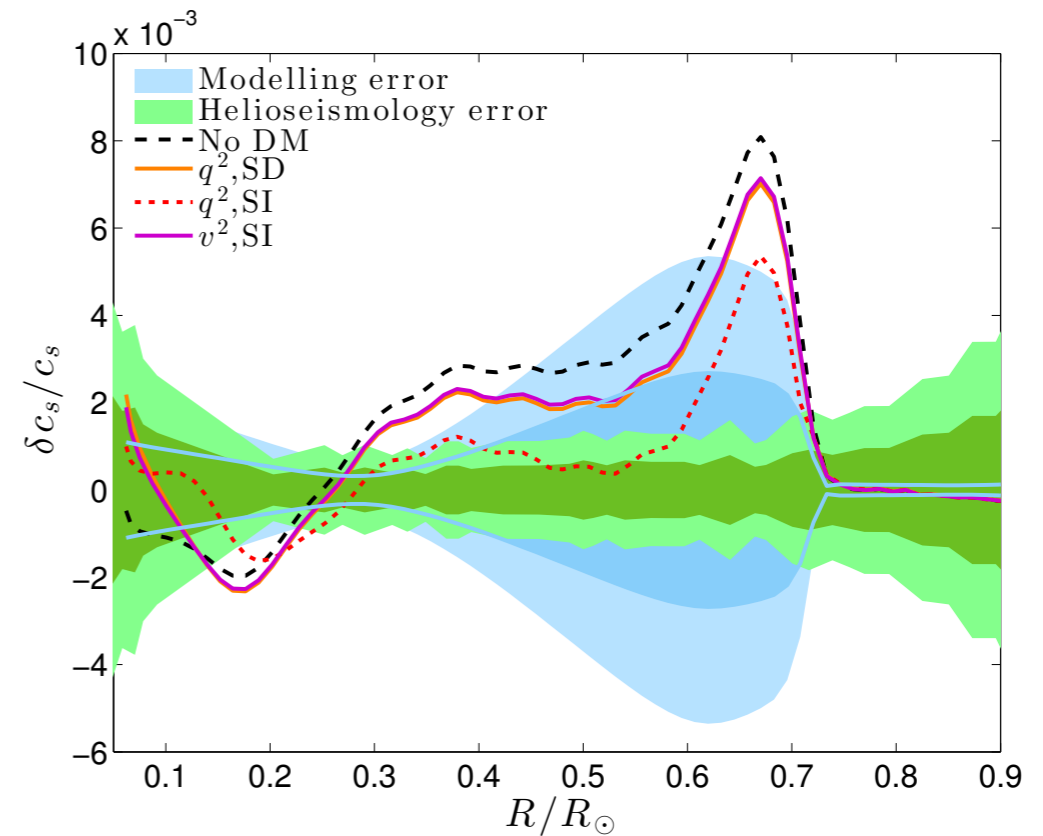
Suppressed cap. rate:
maximum transport
window at higher cross-
section

Enhanced mean free path:
Much more overall heat
conduction

Sound speed: Constant cross-section



Excluded by direct
detection experiments



Best improvement: q^2

$$\sigma_0 = 10^{-37} \text{ cm}^2$$

$$m_\chi = 3 \text{ GeV}$$

Probing the core

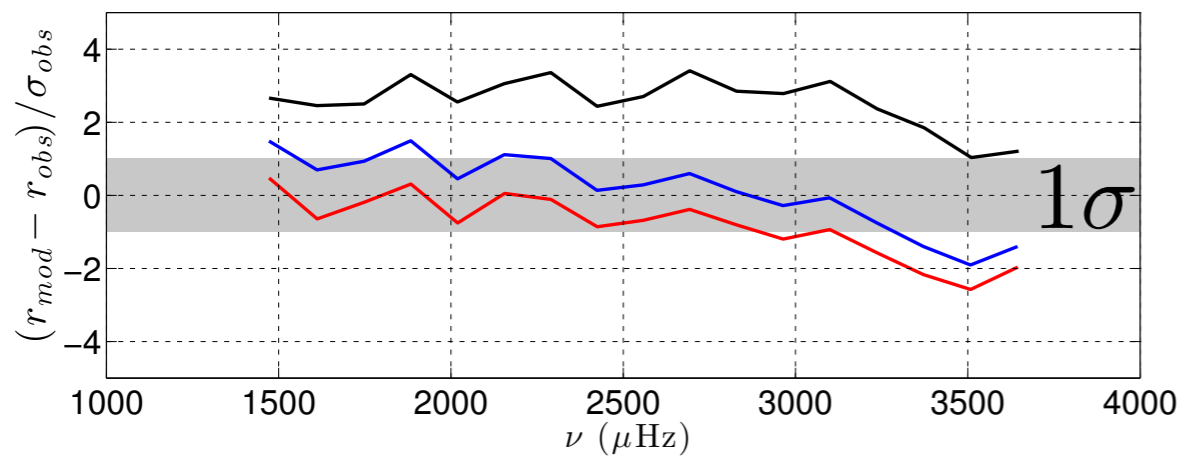
Measuring the frequency separation between the low- ν helioseismological modes allows us to probe the core while removing sources of error.

$$r_{02}(n) = \frac{d_{02}(n)}{\Delta_1(n)}, \quad r_{13}(n) = \frac{d_{13}(n)}{\Delta_0(n+1)},$$

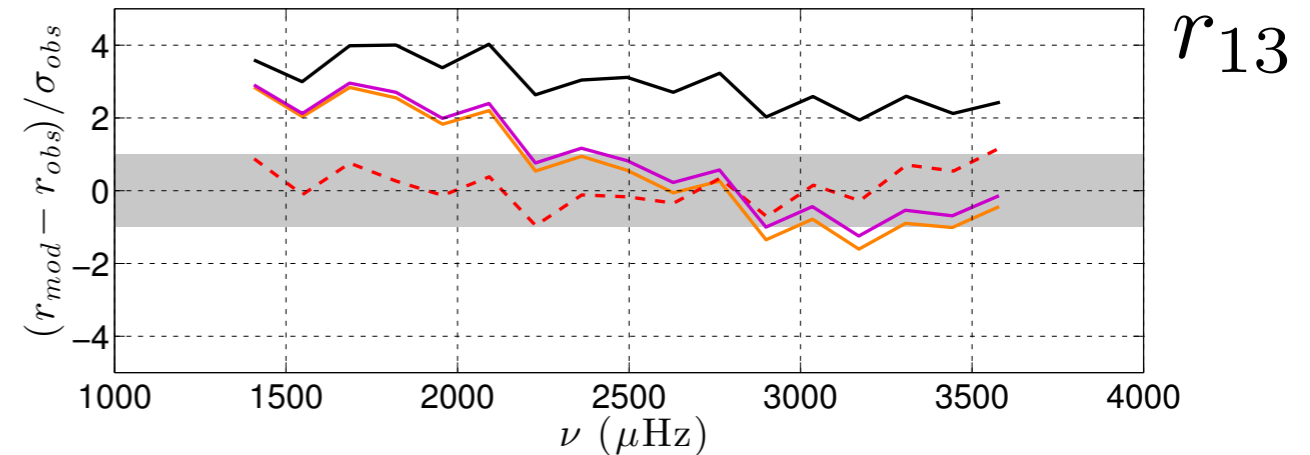
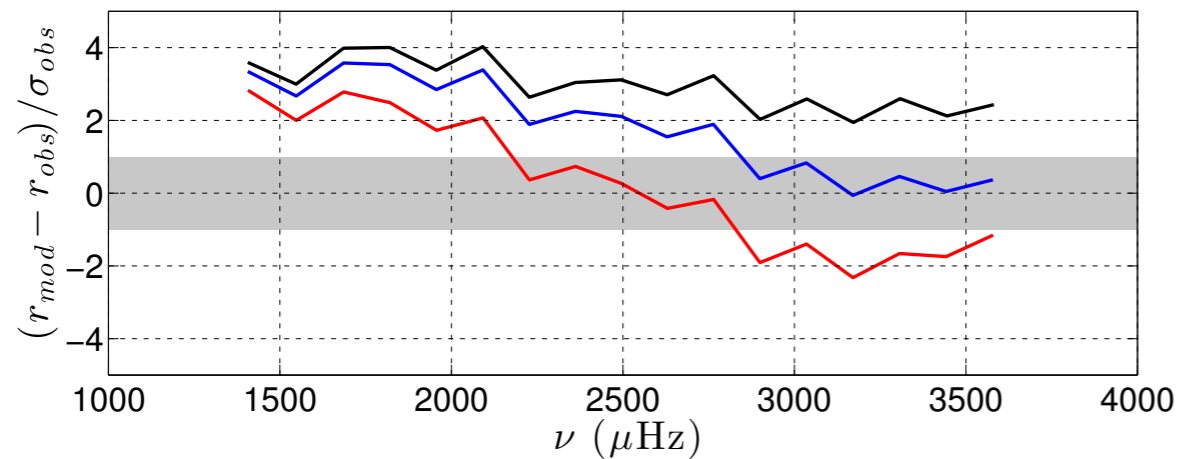
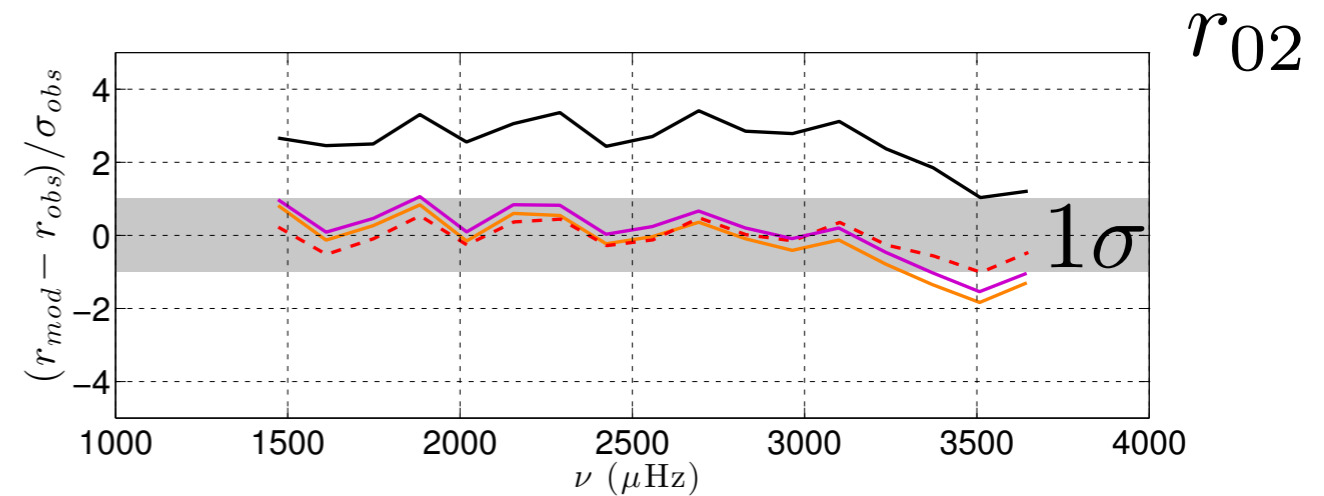
$$d_{l,l+2}(n) \equiv \nu_{n,l} - \nu_{n-1,l+2} \simeq -(4l+6) \frac{\Delta_l(n)}{4\pi^2 \nu_{n,l}} \int_0^{R_\odot} \frac{dc_s}{dr} \frac{dr}{r}.$$

Solar core observable: model — observation

Constant cross section



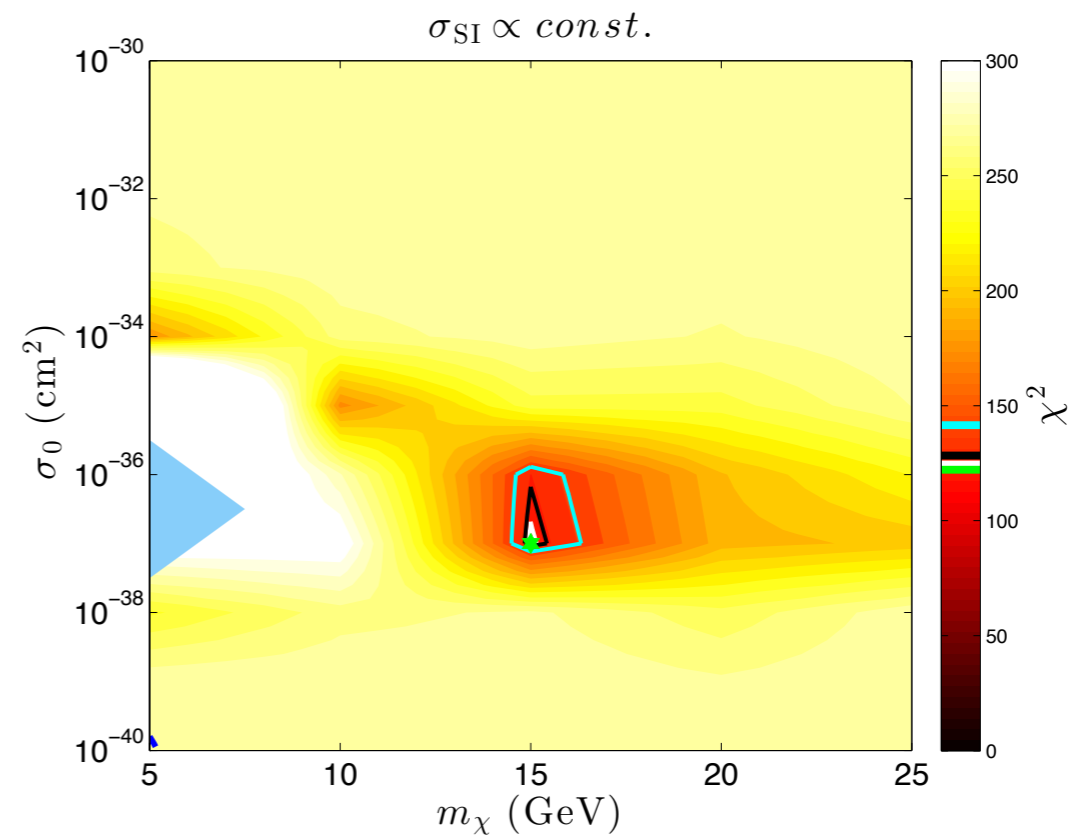
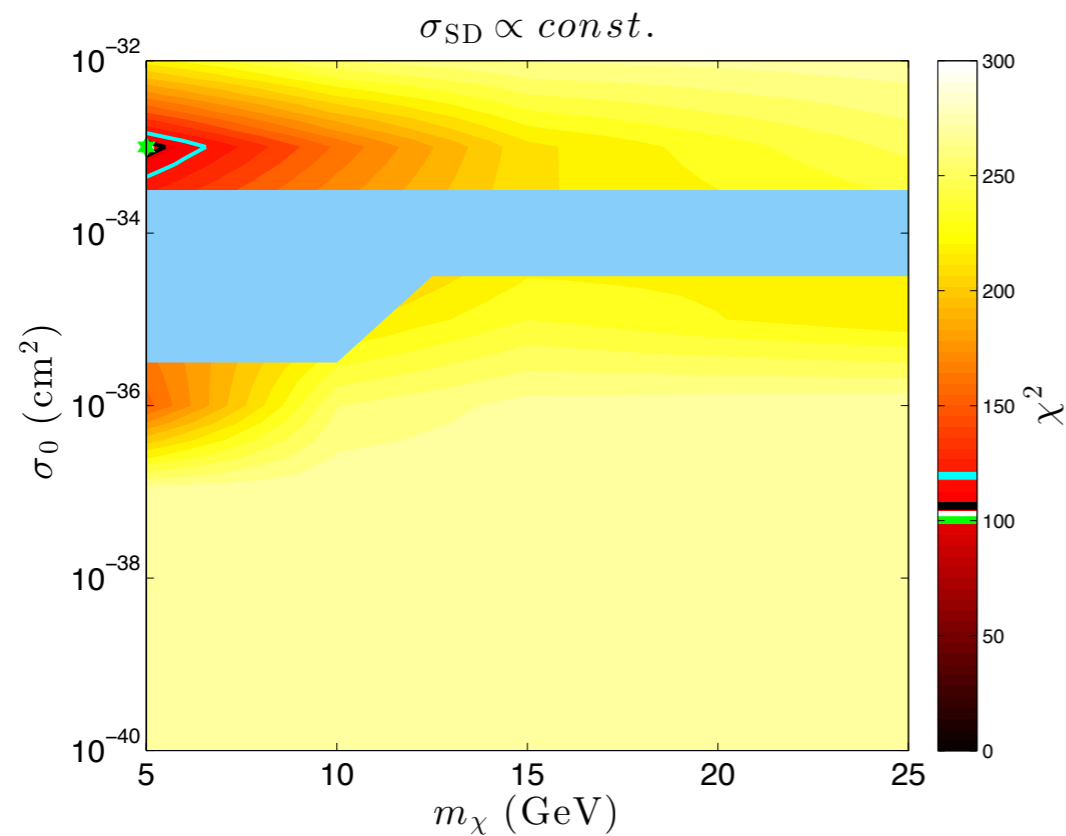
q, v dependent



- Standard solar model
- - - q2 dark matter

Combined limits

$$\chi^2 = \underbrace{\frac{(1 - \phi_{\text{B,obs}}^\nu / \phi_{\text{B}}^\nu)^2}{\sigma_{\text{B}}^2}}_{\text{neutrinos}} + \underbrace{\frac{(1 - \phi_{\text{Be,obs}}^\nu / \phi_{\text{Be}}^\nu)^2}{\sigma_{\text{Be}}^2}}_{\text{CZ radius}} + \underbrace{\frac{(r_{\text{CZ}} - r_{\text{CZ,obs}})^2}{\sigma_{\text{CZ}}^2}}_{\text{surf. He}} + \underbrace{\frac{(Y_{\text{S}} - Y_{\text{S,obs}})^2}{\sigma_{Y_{\text{S}}}^2}}_{\text{small freq.}} + \chi_{r_{02}}^2 + \chi_{r_{13}}^2.$$



Combined limits: best models

TABLE I. Measured and predicted solar observables.

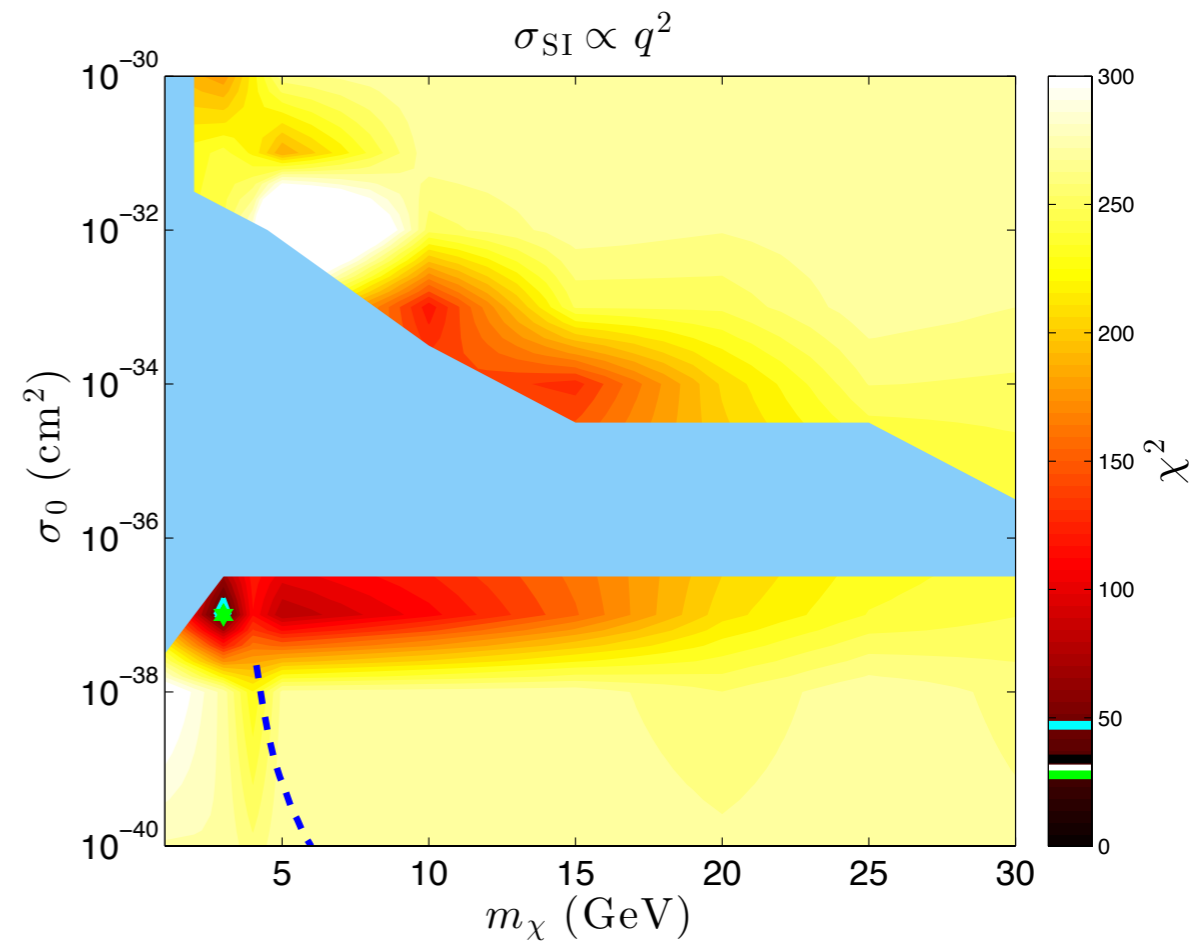
	SSM	SD	SI	q^2 SI	Obs. ^a	σ_{obs}	σ_{model}
$\phi_\nu^{8\text{B}}$ ^b	4.95	4.39	4.58	3.78	5.00	3%	14%
$\phi_\nu^{7\text{Be}}$ ^c	4.71	4.58	4.62	4.29	4.82	5%	7%
R_{CZ}/R_\odot	0.722	0.721	0.721	0.718	0.713	0.001	0.004
Y_s	0.2356	0.2351	0.2353	0.2327	0.2485	0.0034	0.0035
$\chi_{8\text{B}}^2$	0.0	0.9	0.9	4.9			
$\chi_{7\text{Be}}^2$	0.1	0.4	0.4	1.9			
$\chi_{R_{\text{CZ}}}^2$	4.8	3.8	3.8	1.5			
$\chi_{Y_s}^2$	7.0	7.5	7.3	10.5			
$\chi_{r_{02}}^2$	156.6	95.3	105.2	5.6			
$\chi_{r_{13}}^2$	119.3	50.7	67.2	3.1			
χ_{total}^2	287.8	158.5	185.2	27.5			
p	$<10^{-10}$	$<10^{-10}$	$<10^{-10}$	0.845			

^a Neutrino data and obs. errors inferred from Borexino data [4].

^b In units of $10^6 \text{ cm}^{-2}\text{s}^{-1}$.

^c In units of $10^9 \text{ cm}^{-2}\text{s}^{-1}$.

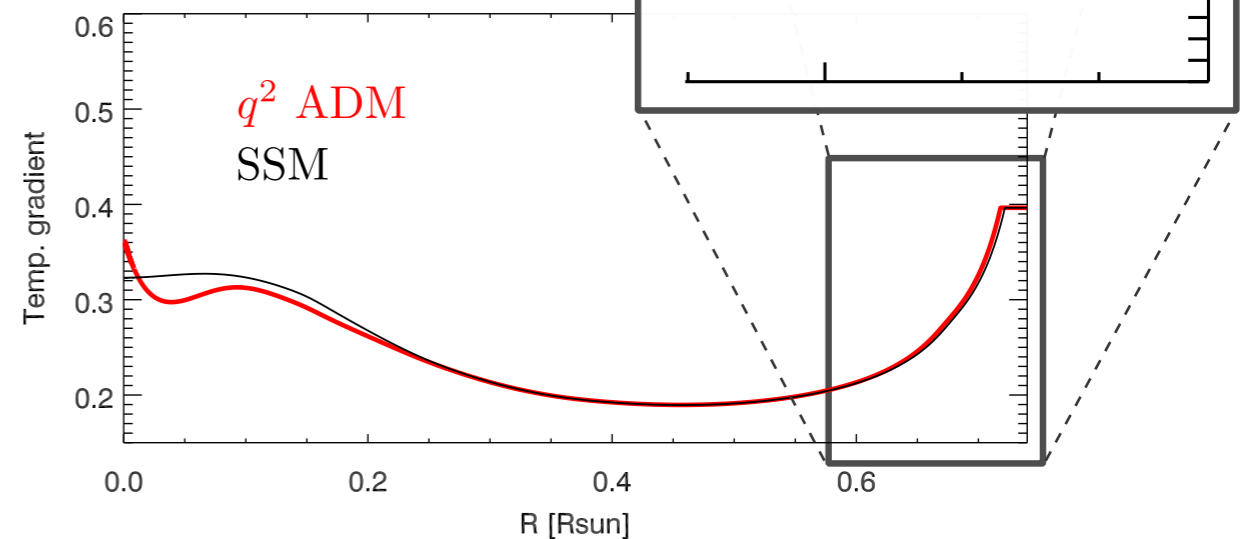
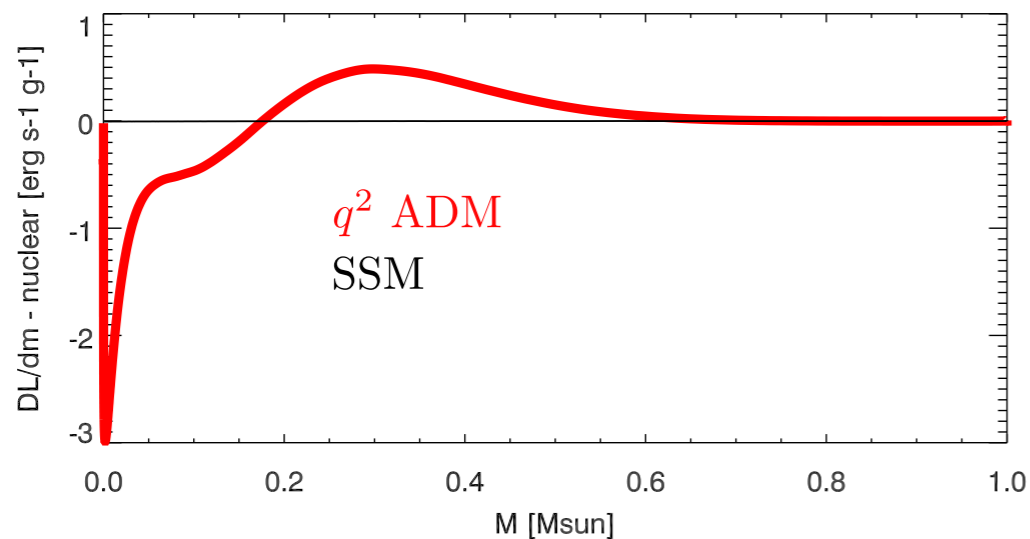
$$\sigma_{SI} \propto q^2 \quad m_\chi = 3 \text{ GeV}$$



6 sigma improvement over SSM!

What is going on?

- Energy extracted from core to intermediate radii ($0.2 < R < 0.6$)
- Change in sound speed, core state variables \rightarrow small freq separations
- Temp. gradient readjustment up to R_{CZ}
 - \rightarrow Convection sets in at slightly lower R



Other constraints

- **Direct detection**

- Mass (3 GeV) still too low to have been seen
- CDMSlite, DAMIC, SuperCDMS should probe this range

- **Collider limits**

- Effective operators $\sim \bar{\chi}\gamma^5\chi\bar{q}q$ still ok.

To summarise

- SI, SD constant cross-sections bring some observables closer to agreement but
 - Suppress neutrino fluxes too much
 - Do not do that well in the core (small-freq separations)
 - Do not yield significantly better fit than SSM
- All DM models we looked at give *some* improvement, but only q^2 gives a good fit, and a significant, **6 sigma improvement over the standard solar model.**
- Mass is low - evaporation?
- Could the solution to the solar abundance problem be the first hint of particle DM?

Thank you

