

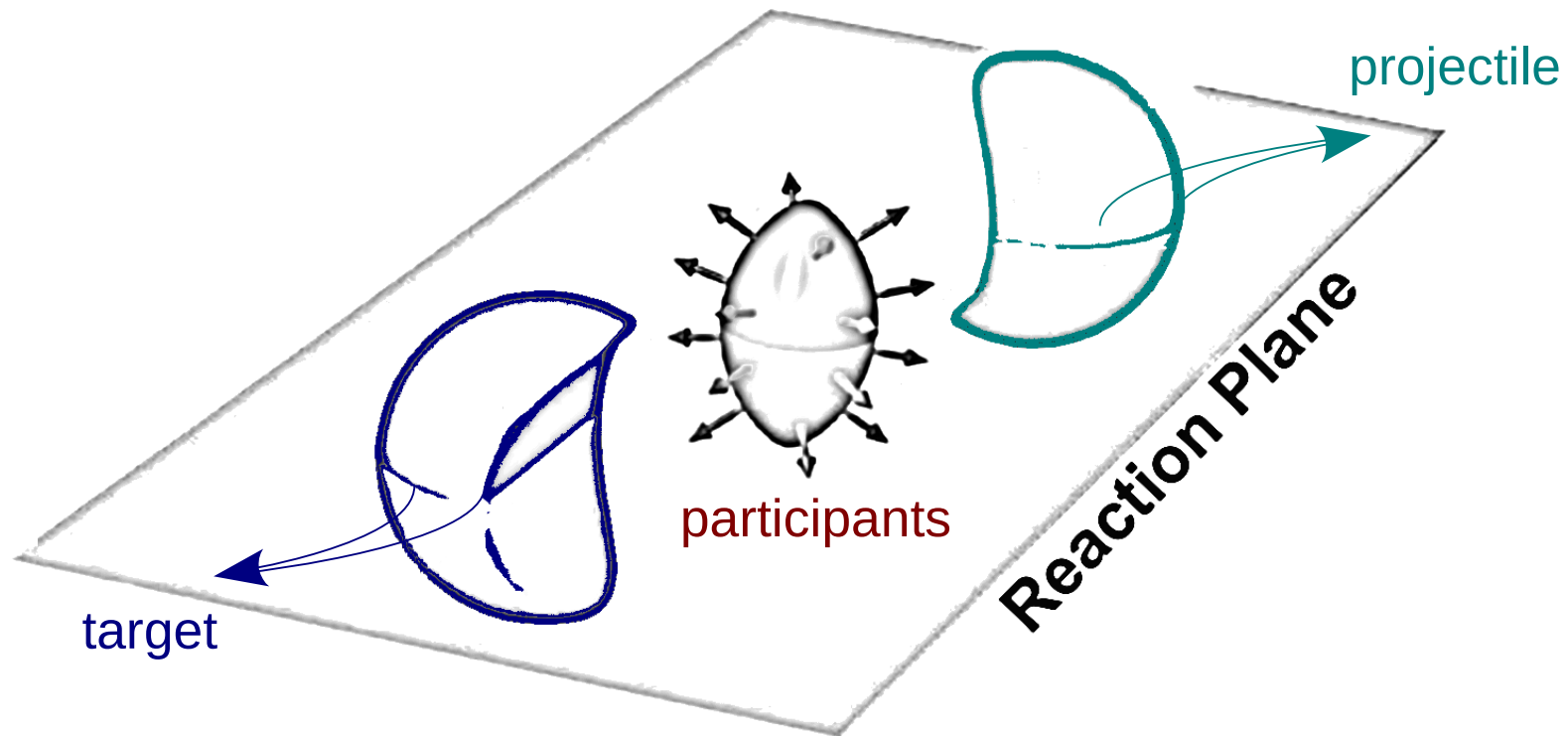
# Anisotropic flow observables and how to measure them

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"Relativistic Heavy Ion Collisions, Cosmology and Dark Matter, Cancer Therapy"

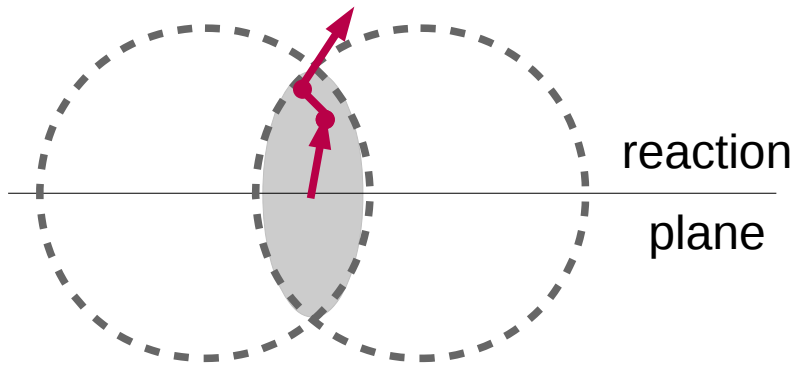
May 20, 2017

# Reaction plane



# Spatial and momentum space asymmetries

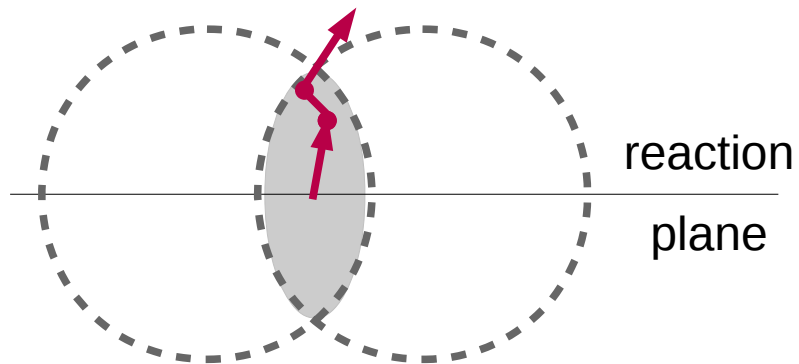
out-of-plane



Multiple interactions with medium

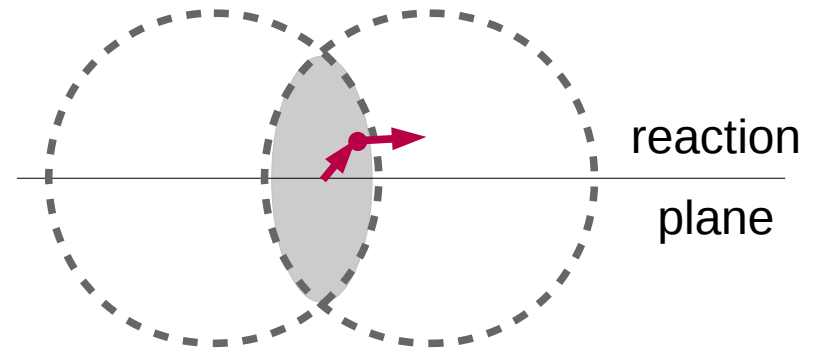
# Spatial and momentum space asymmetries

out-of-plane



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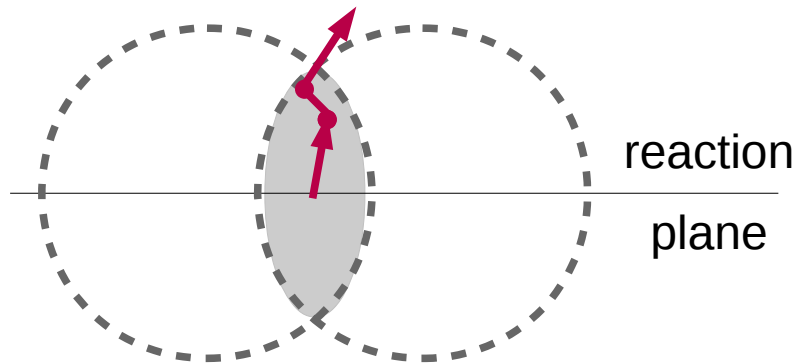
in-plane



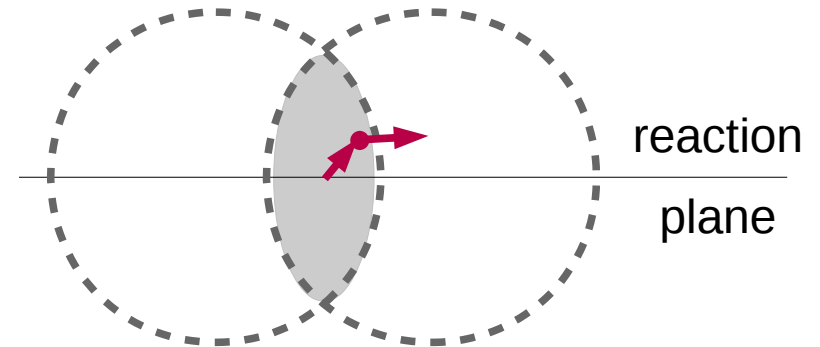
Less interaction - small modification

# Spatial and momentum space asymmetries

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in-plane



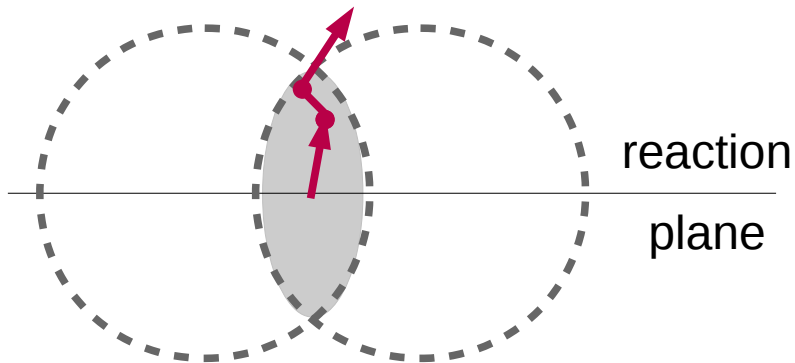
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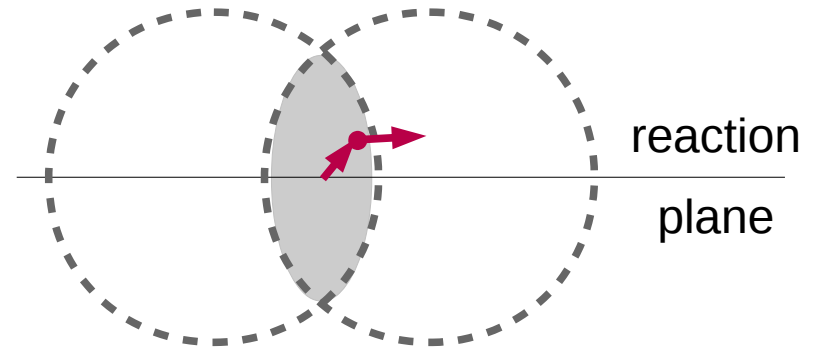
Initial spatial asymmetry converts into azimuthal anisotropy in the momentum space

# Spatial and momentum space asymmetries

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in-plane



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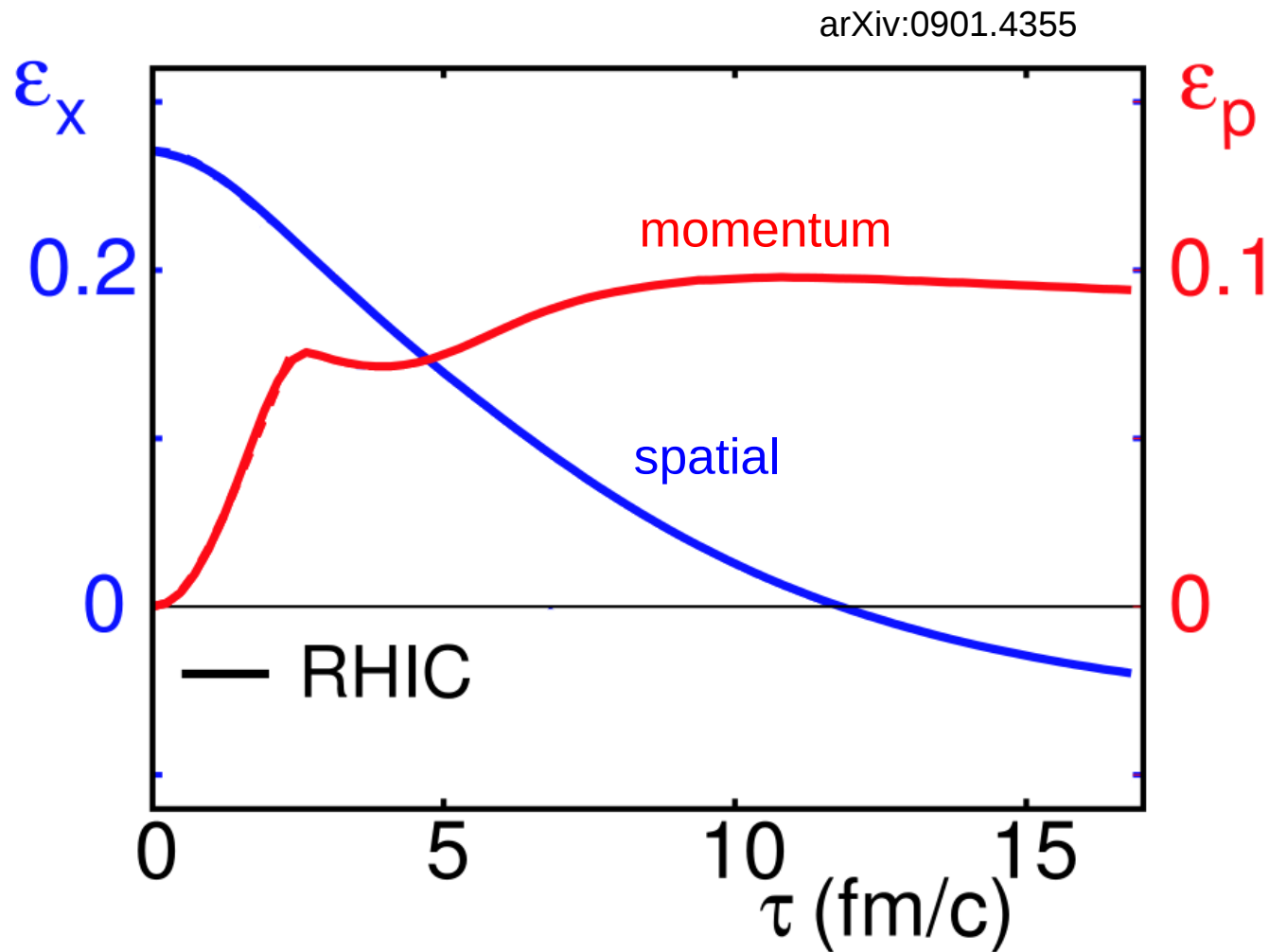
Initial spatial asymmetry converts into azimuthal anisotropy in the momentum space

Quantified with the Fourier coefficients:

$$\frac{dN}{d(\phi_i - \Psi_n)} \sim 1 + 2 \sum_{n=1} v_n \cos[n(\phi_i - \Psi_n)]$$

$v_1$  - directed,  $v_2$  - elliptic, and  $v_3$  - triangular flow

# Time evolution of the spatial and momentum asymmetries



Spatial asymmetry  
drops very fast



Momentum asymmetry  
develops very early

# Anisotropic flow measurement techniques

$$\frac{dN}{d(\phi_i - \Psi_n)} \sim 1 + 2 \sum_{n=1} v_n \cos[n(\phi_i - \Psi_n)]$$

If orientation of the collision symmetry plane is known

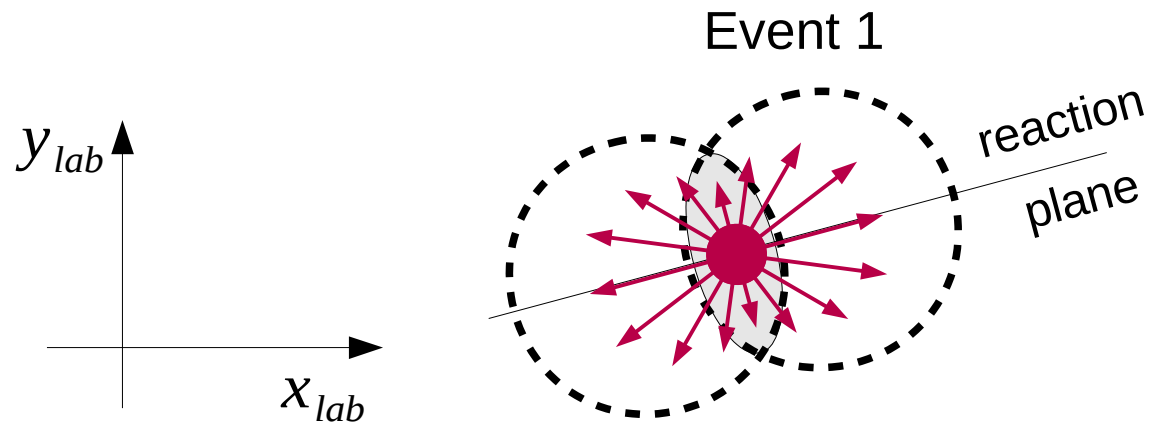
$$v_n = \langle \cos[n(\phi_i - \Psi_n)] \rangle$$

BUT: experimentally the collision symmetry plane orientation is unknown



# Estimating the reaction plane angle

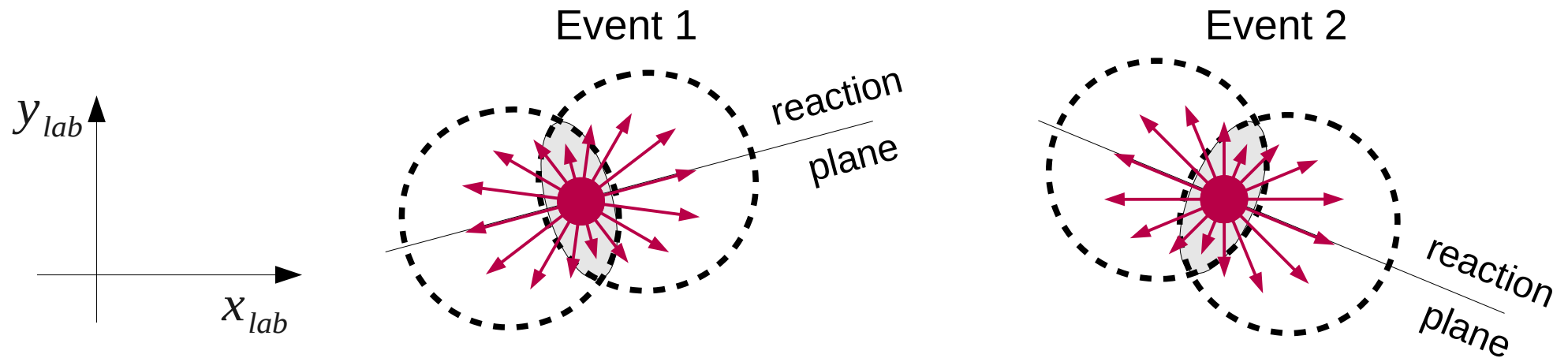
Reaction plane is not known experimentally  
Orientating wrt. to the laboratory frame changes event-by-event



# Estimating the reaction plane angle

Reaction plane is not known experimentally

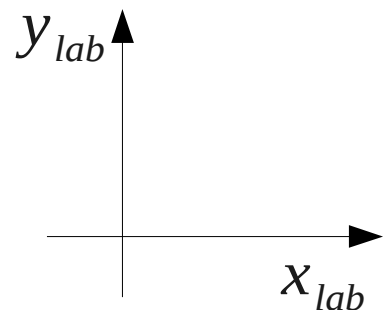
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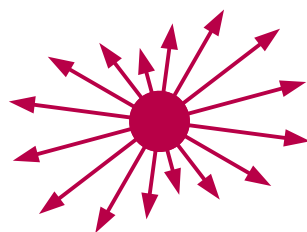
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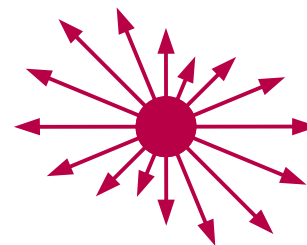
Orientating wrt. to the laboratory frame changes event-by-event



Event 1



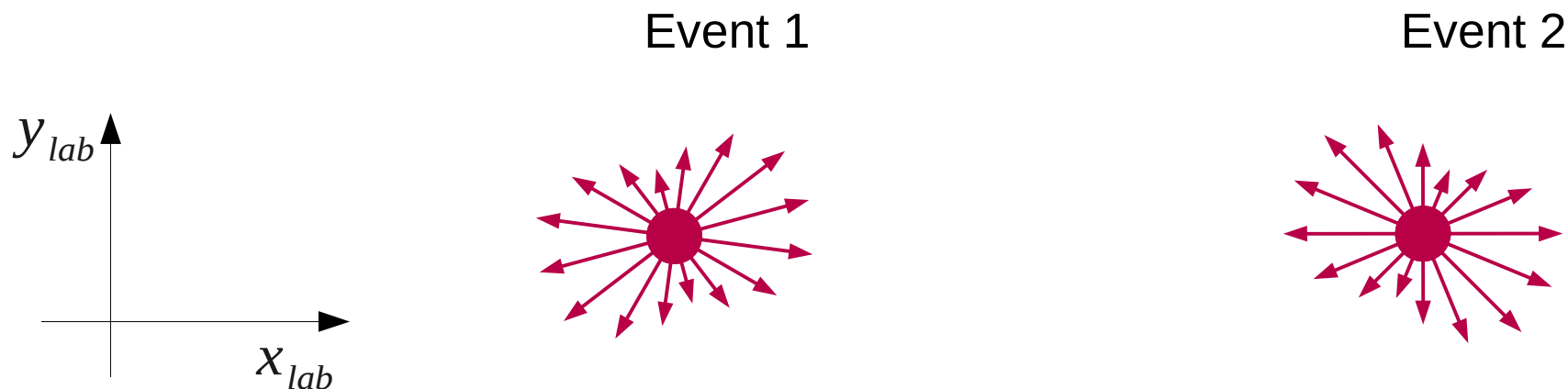
Event 2



# Estimating the reaction plane angle

Reaction plane is not known experimentally

Orientating wrt. to the laboratory frame changes event-by-event

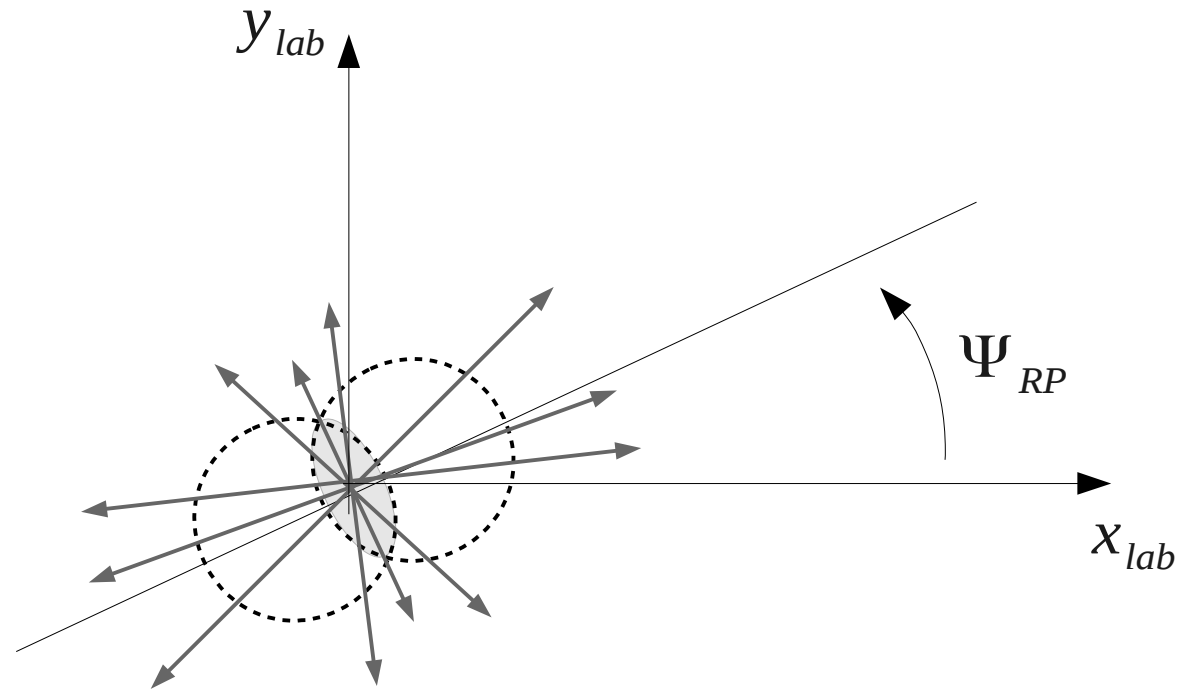


Only measuring particles distribution in the momentum space

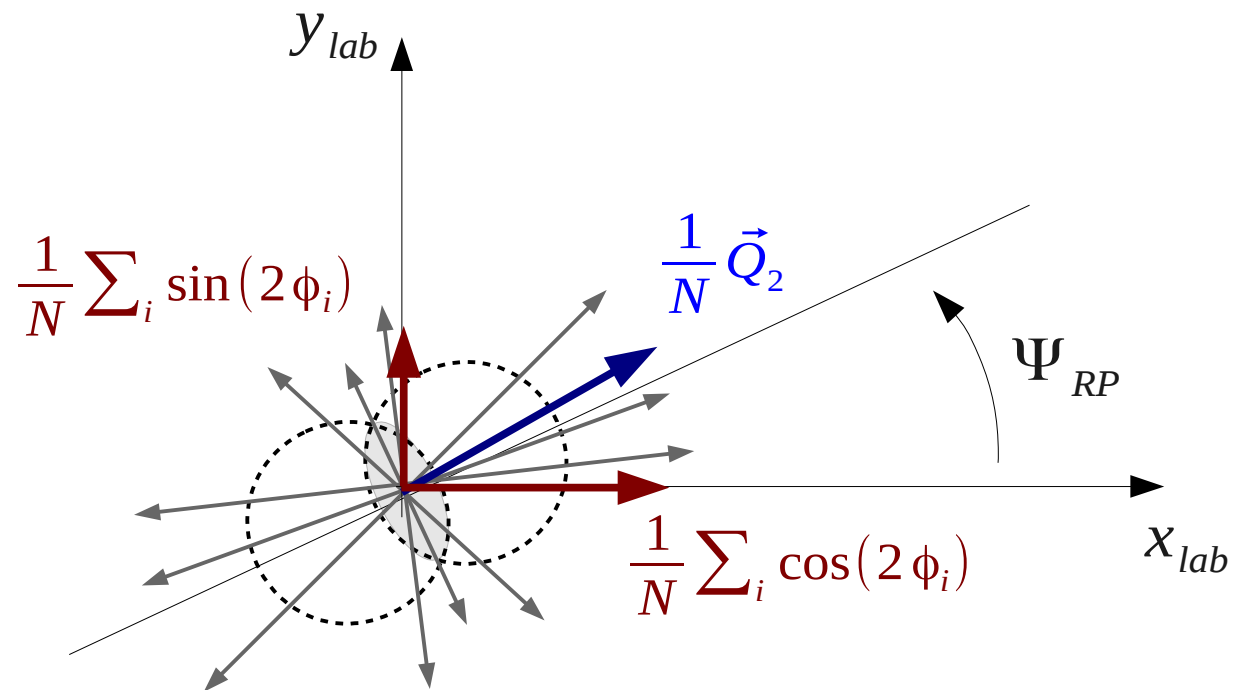
If the momentum distribution is azimuthally asymmetric due to flow, then this asymmetry should be correlated with the impact parameter direction (reaction plane orientation)

Use particle azimuthal distribution in the event to estimate the reaction plane angle – event plane vector

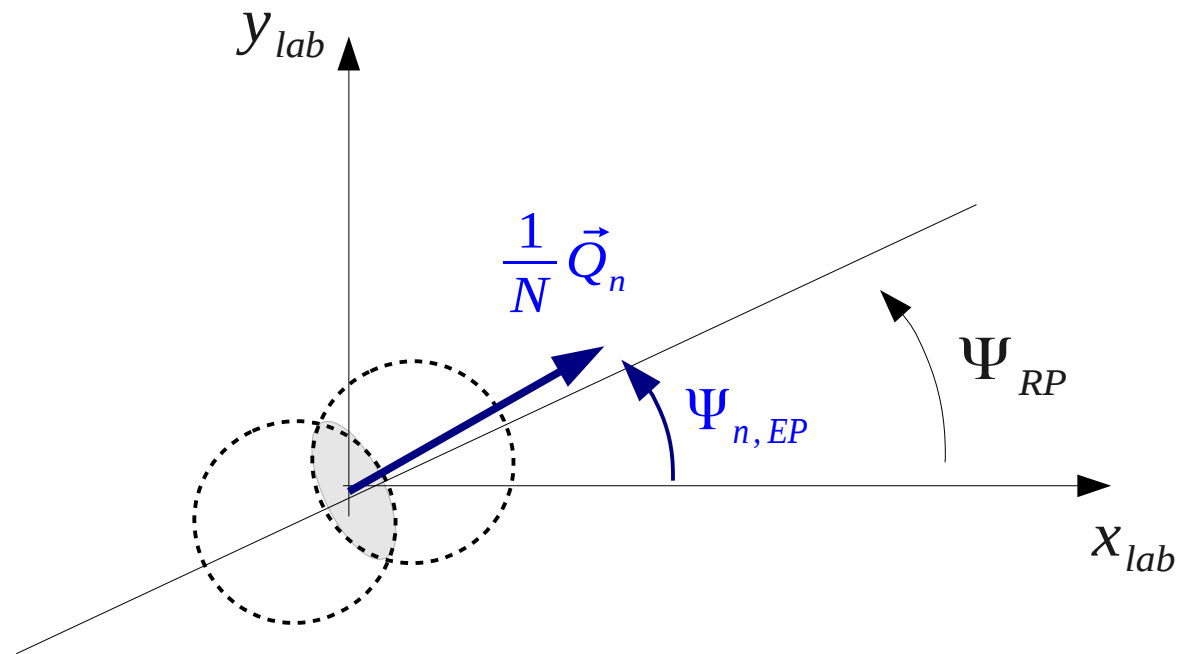
# Event plane vector



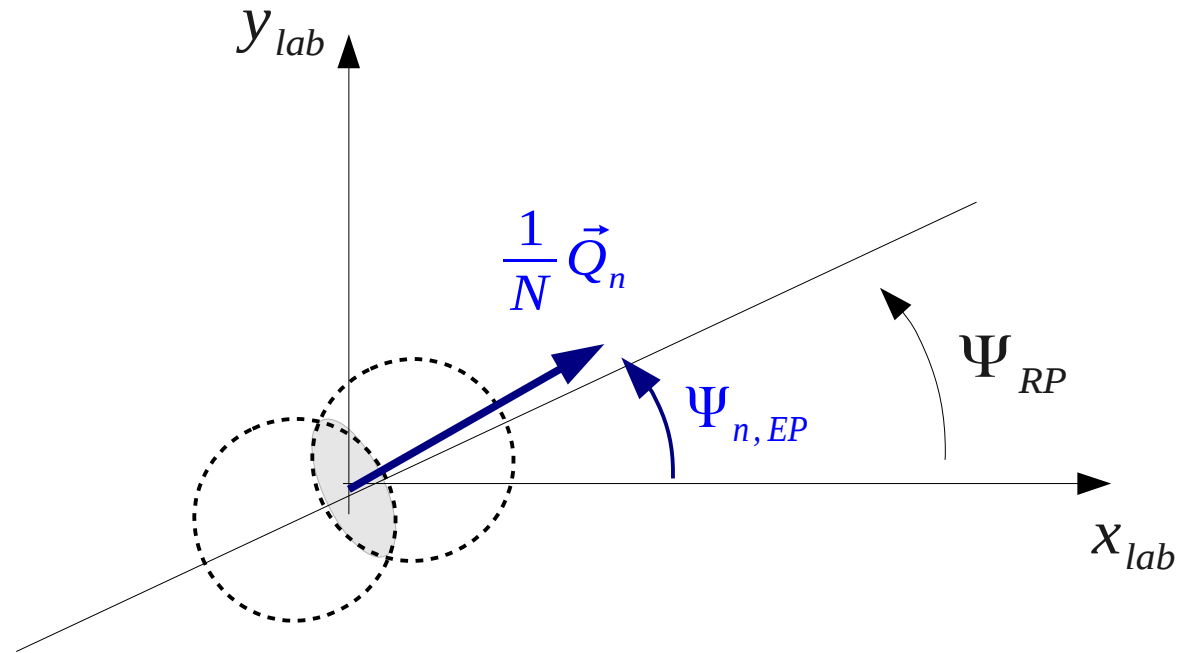
# Event plane vector



# Event plane vector



# Event plane (flow) vector

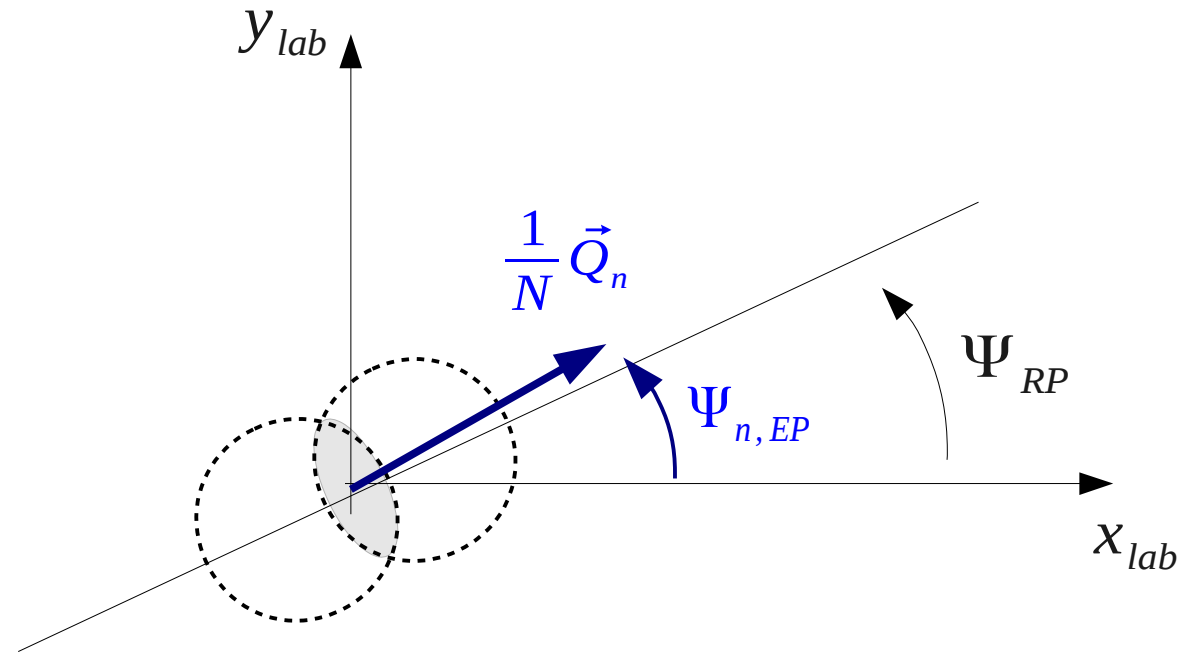


Vector sum of all particles direction:

$$Q_{n,x} = \sum_i w_i \cos(n\phi_i) \qquad Q_{n,y} = \sum_i w_i \sin(n\phi_i)$$



# Event plane (flow) vector



Vector sum of all particles direction:

$$Q_{n,x} = \sum_i w_i \cos(n\phi_i) \quad Q_{n,y} = \sum_i w_i \sin(n\phi_i)$$

Experimental estimate of the reaction plane:

Event plane vector: 
$$\Psi_{n,EP} = \frac{1}{n} \tan^{-1} \left( \frac{Q_{n,y}}{Q_{n,x}} \right)$$

# Measuring flow with the event plane vector

$$\frac{dN}{d(\phi - \Psi_{RP})} \sim 1 + 2 \sum_{i=1} v_n(p_t, \eta) \cos[n(\phi - \Psi_{RP})]$$

Want to measure:

$$v_n = \langle \cos[n(\phi - \Psi_{RP})] \rangle$$

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$$v_n^{obs} = \langle \cos[n(\phi - \Psi_{n,EP})] \rangle$$

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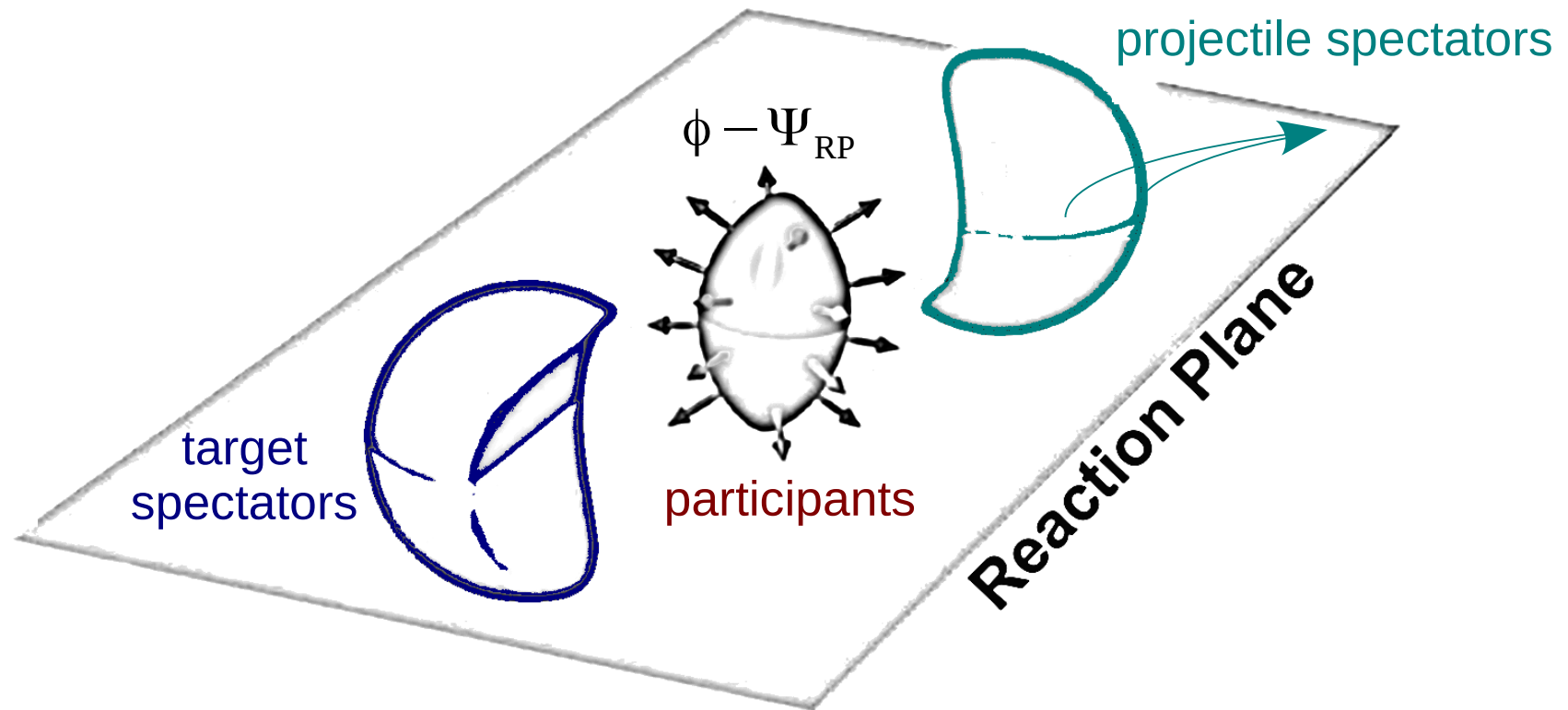
Measured:

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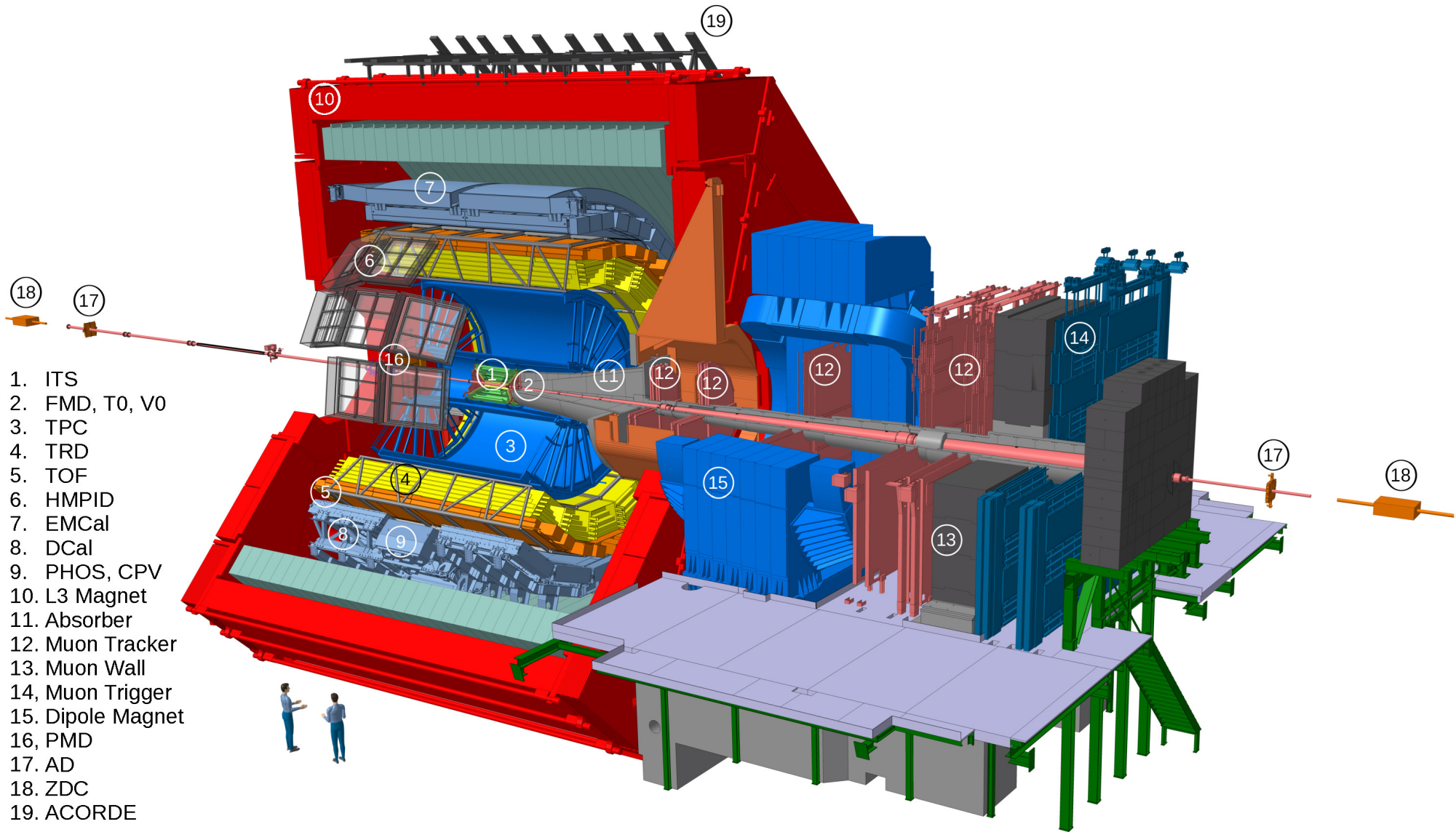
Event plane vector and the reaction plane are correlated with finite resolution:

$$v_n = \frac{\langle \cos[n(\phi - \Psi_{n,EP})] \rangle}{\langle \cos[n(\Psi_{n,EP} - \Psi_{RP})] \rangle} = \frac{v_n^{obs}}{R_n}$$

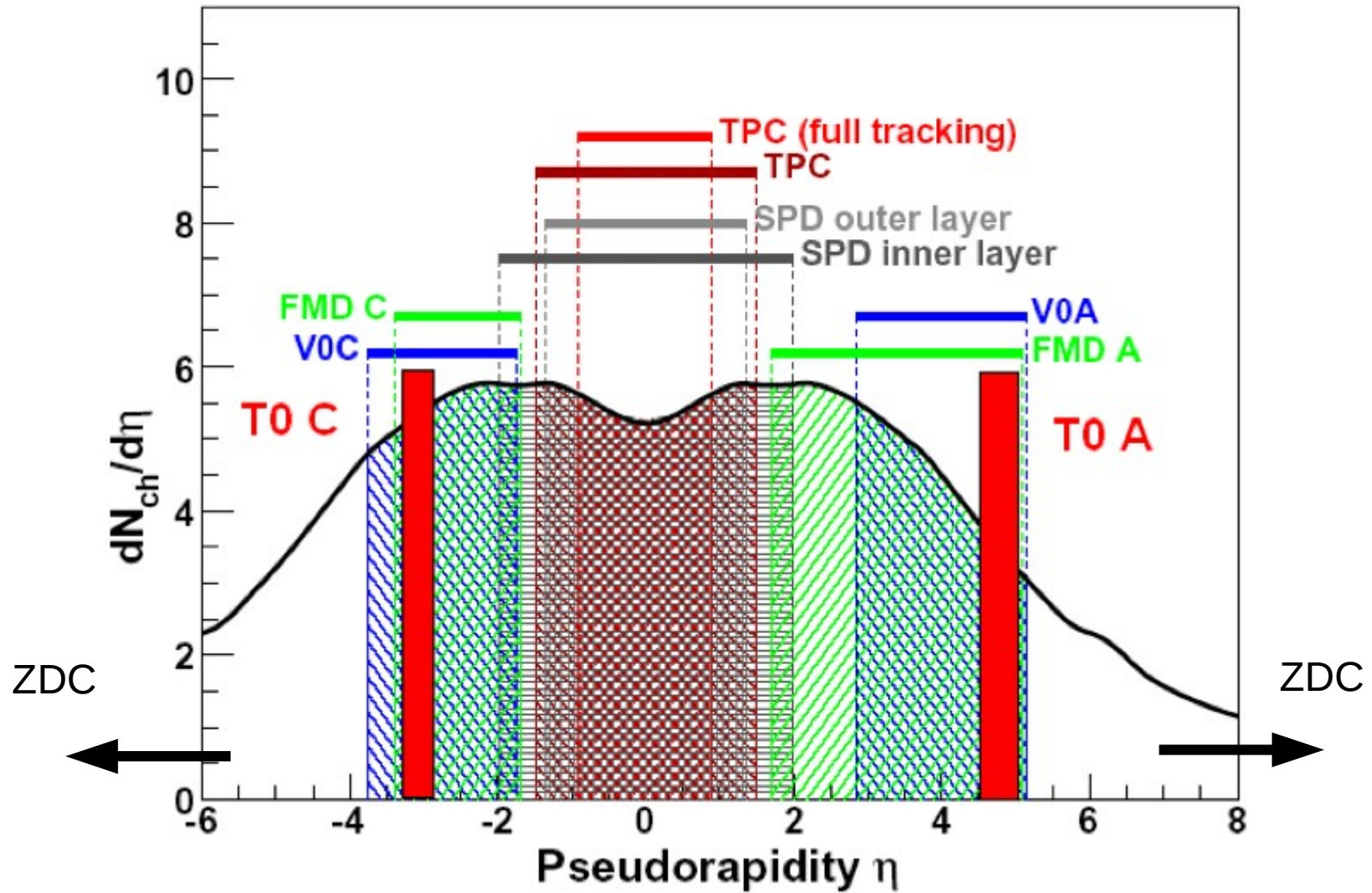
# What can be used in ALICE for reaction plane estimate



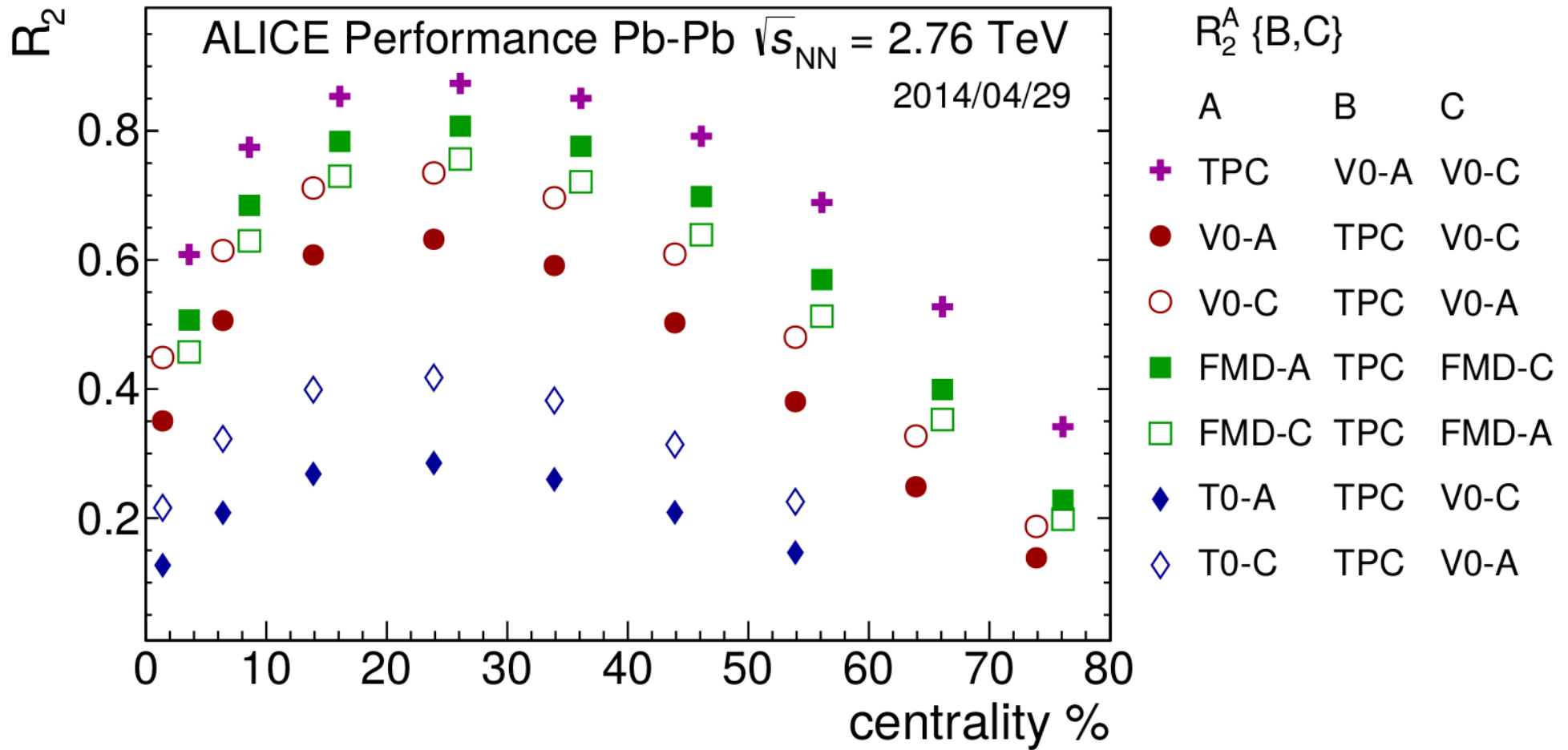
# Where we can get an event plane angle in ALICE?



# ALICE rapidity coverage



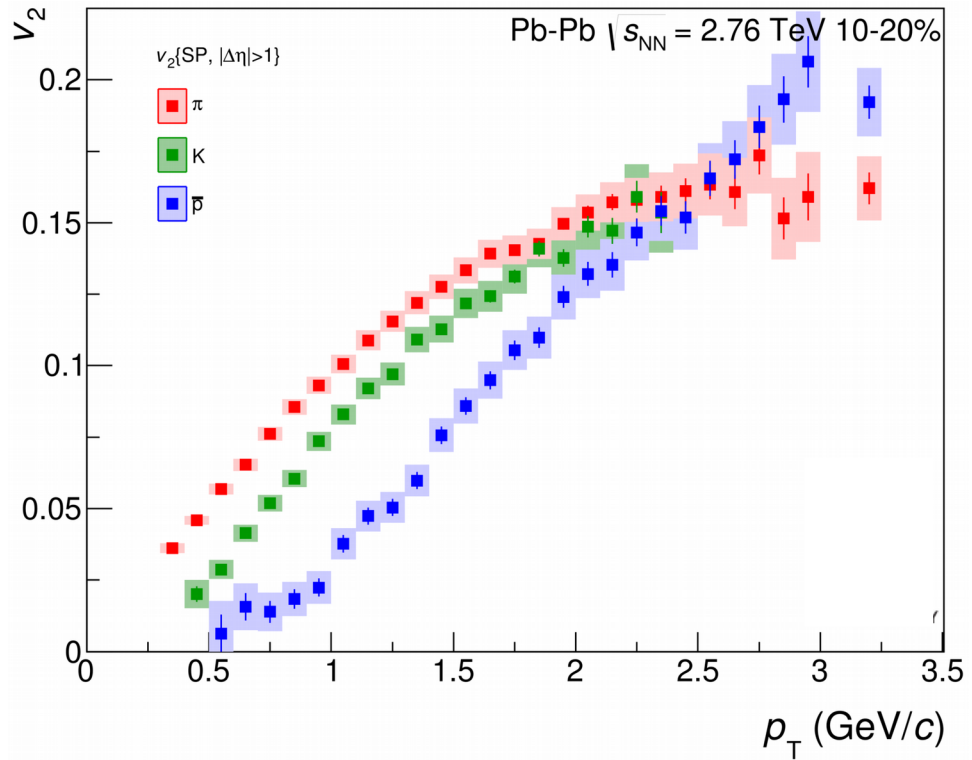
# Reaction plane resolution





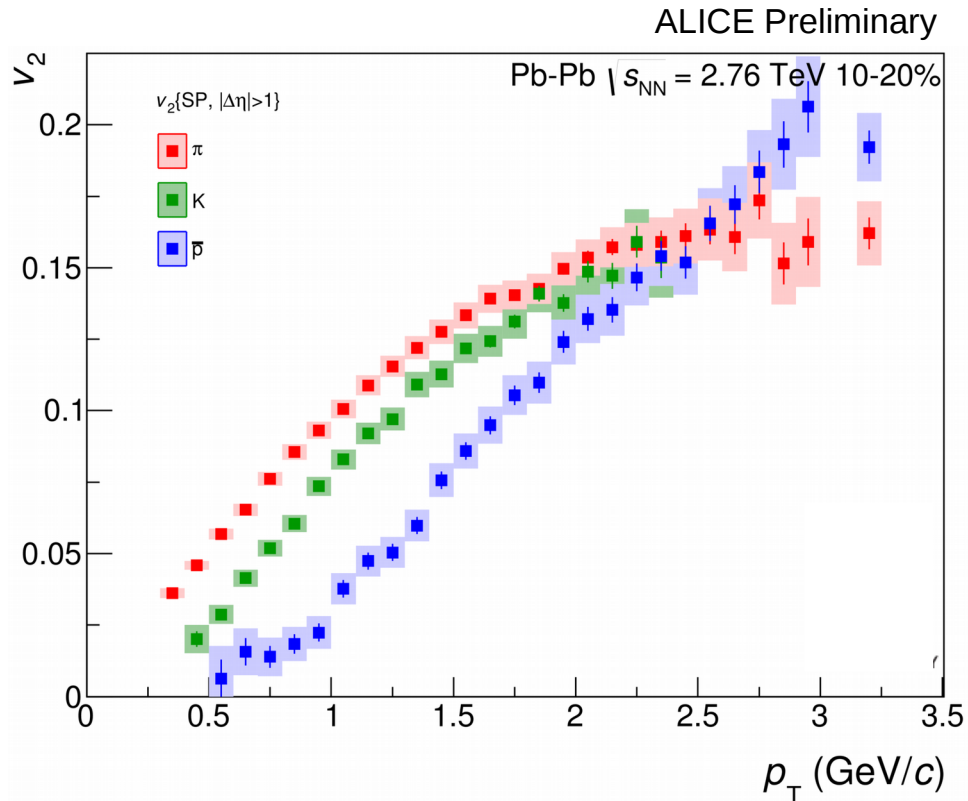
# Particle type dependence of $v_2$

$\pi^\pm, K^\pm, p(\bar{p})$

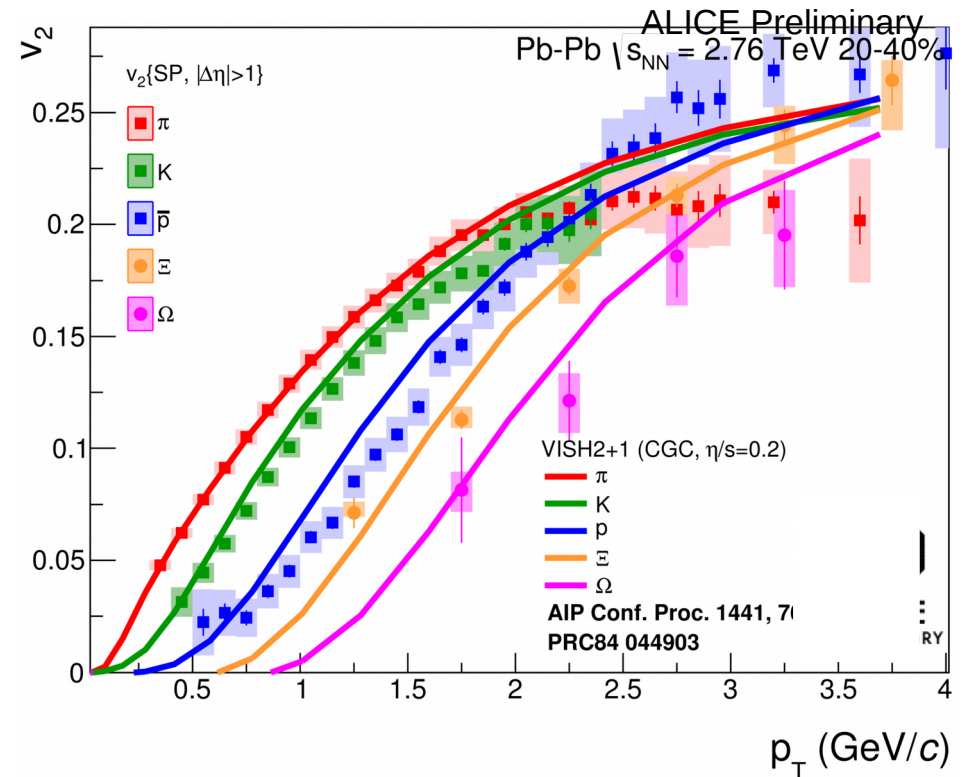


# Particle type dependence of $v_2$

$\pi^\pm, K^\pm, p(\bar{p})$



$\pi^\pm, K^\pm, p(\bar{p})$  and multi-strange ( $\Xi, \Omega$ )



Viscous hydrodynamics reproduce mass dependence of  $v_2$ :  
Sensitive to the initial conditions  
Suggest low viscosity of the matter