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The Resonant Multi-Pulse Ionization Injection

P. Tomassini, L. Labate, P. Londrillo,
R. Fedele, D. Terzani,
F. Nguyen, G. Dattoli

L.A. Gizzi

Intense Laser Irradiation Laboratory, INO-CNR,
Pisa (Italy)

INAF Bologna (Italy)

Dip. Fisica Università' di Napoli Federico II
(Italy)

ENEA, Frascati (Italy)

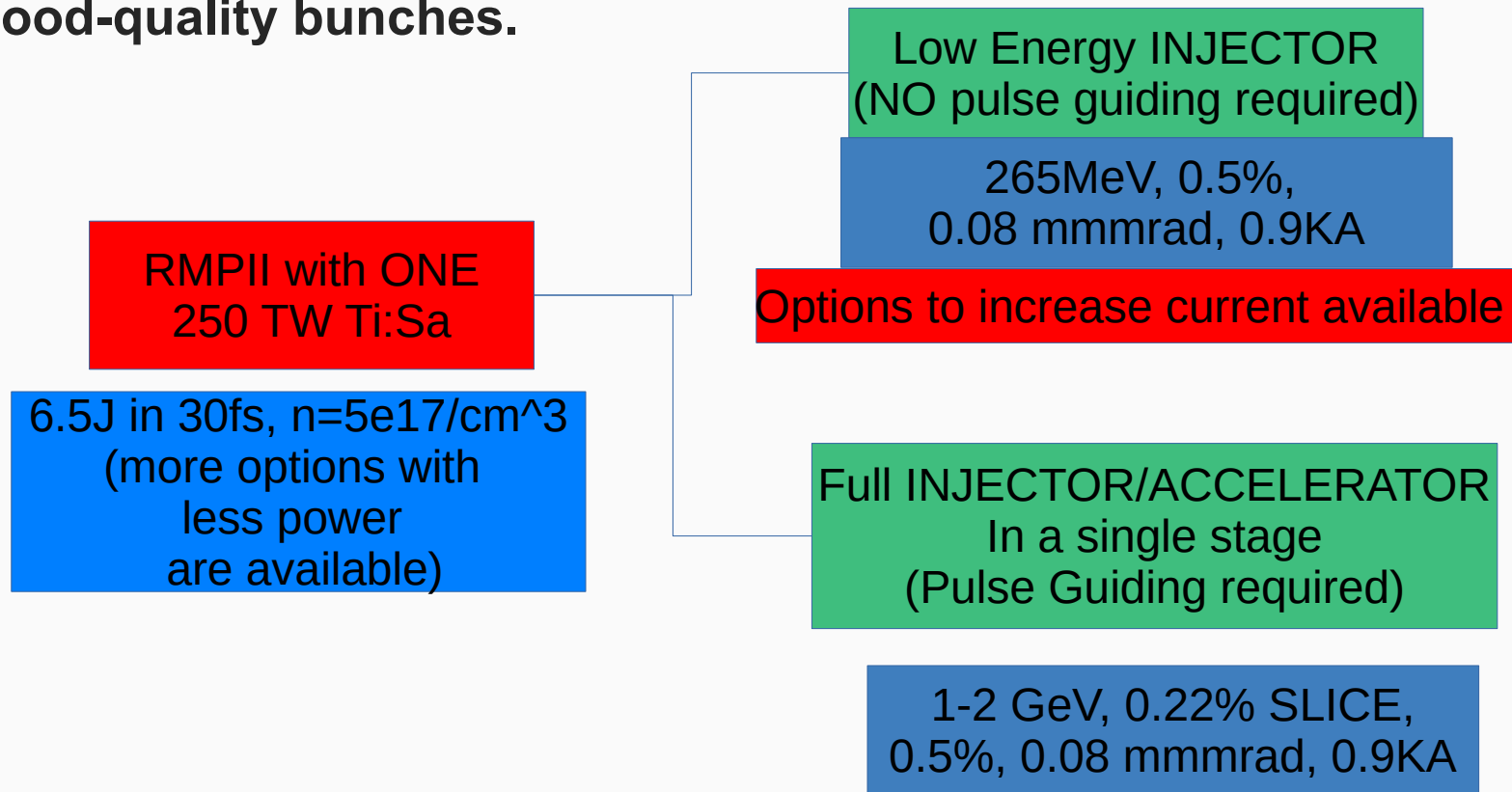
***EUPRAXIA Meeting, DESY, 19-23
June 2017***



- **High-quality bunches generation roadmap**
- **The new Resonant Multi-Pulse Ionization injection**
- **265 MeV and >1 GeV high-quality [$dE/E=0.5\%$, 0.08 mm mrad] electron bunches**
- **Linear vs Circular polarization (Driver pulse)**
- **Second vs Third harmonics of Ti:Sa (Ionization pulse)**
- **FEL preliminary results**
- **Towards experimental demonstration at ILIL-PW**



The new Resonant Multi-Pulse Ionization Injection is a **SINGLE LASER System** (e.g. Ti:Sa) scheme that can generate extremely good-quality bunches.





High-quality bunches generation roadmap



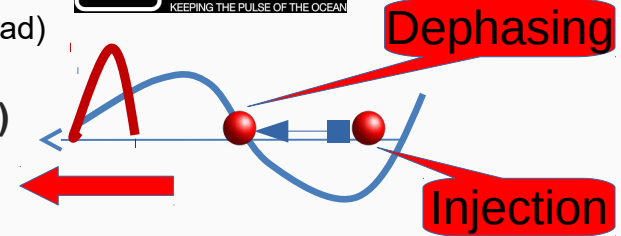
Low energy spread/emittance bunches require *accurate control* in

- Particle's injection (either internal trapping or external injection)



At injection/trapping **transverse emittance** ε_n must be very low ($\ll 1$ mm mrad)

- Phase evolution (longitudinal position variation into the bucket)

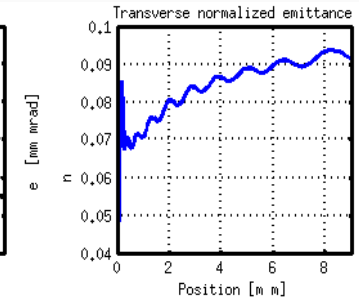
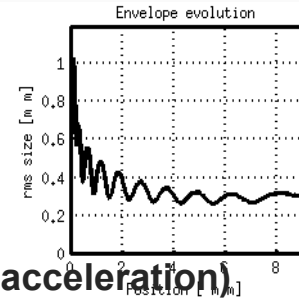
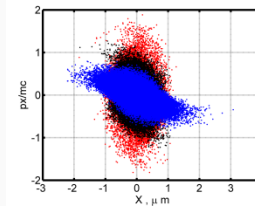


Dephasing length $L_{deph} \approx \lambda_p^3 / \lambda_0^2 \cong \lambda_0 (n_c / n_e)^{3/2}$

- Betatron oscillation induced emittance growth

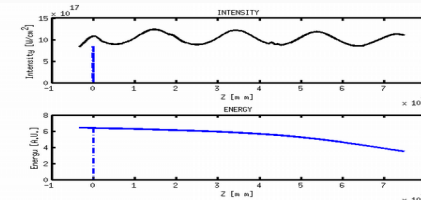
Matched radius

$$r_{matched}(s) \cong 4 \sqrt{\frac{1}{\gamma(s)} \cdot \frac{\varepsilon_n(s)}{k_{ext}(s)}}$$



- Laser pulse guiding, pump depletion (only for high energy acceleration)

Diffraction is compensated by positive-lens effect of plasma channels (and nonlinear effects)



- Beam loading detrimental effects must be reduced

- Bunch extraction from the plasma and beam optics

Phase/amplitude variation of wakefield @ plasma exit; space charge issues:

- Possible strong deviations OF FORCES from azimuthal symmetry
- Standard beam optics/plasma lens optimization after plasma exit

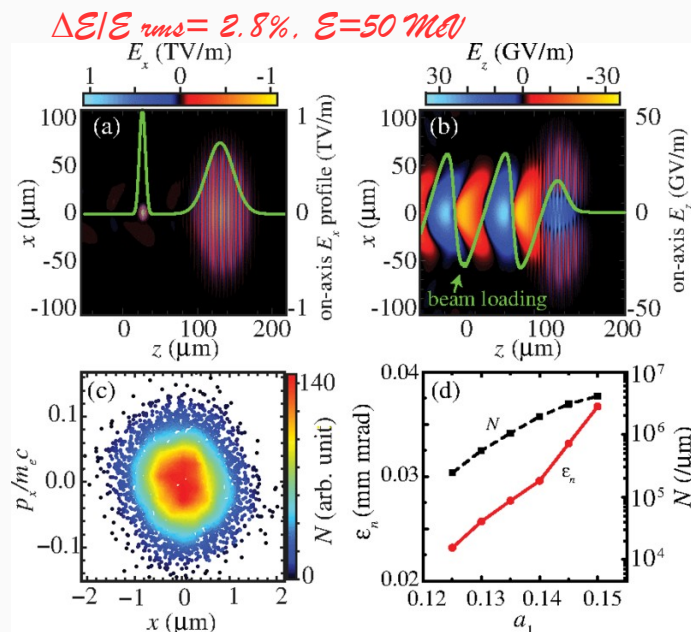
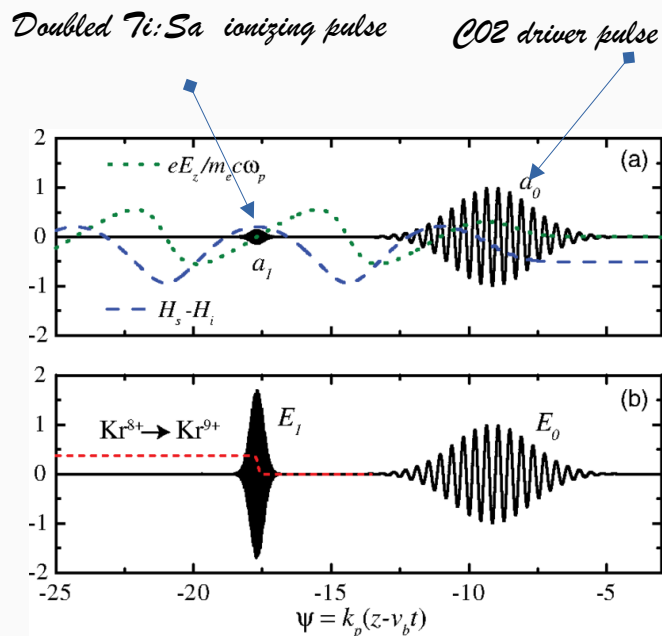
Not (yet) implemented



The “two-colour” ionization injection scheme



Two-colour injection [L. L. Yu et al. PRL 112 (2014)] is a very promising scheme aiming at generating extremely low-emittance bunches but requires two [synchronized] laser systems: a long-wavelength (e.g. CO₂) for wake driving and a short (e.g. a frequency doubled Ti:Sa) for electron extraction.



The CO₂ pulse is needed because the long wavelength assures a large amplitude Wakefield though the electric field is lower than the ionization threshold for Kr⁹⁺

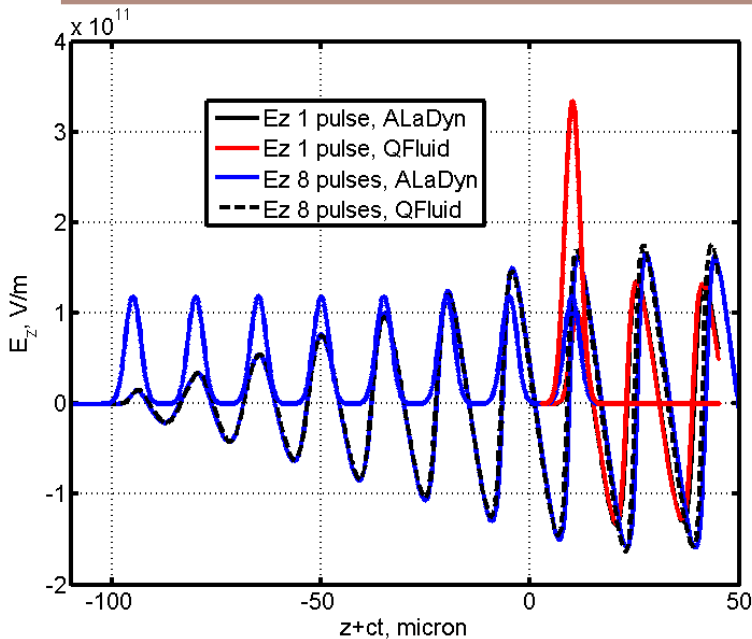


Multi-Pulse LWFA is available!



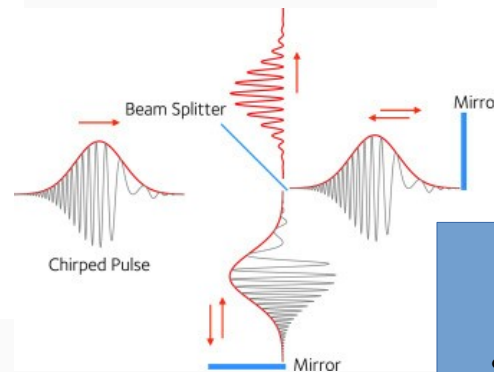
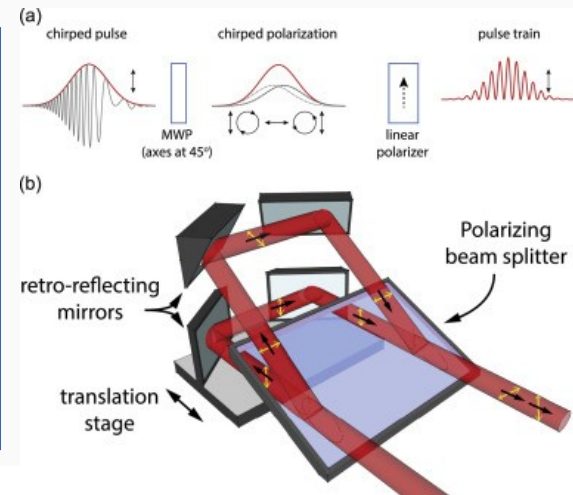
The multi-pulse approach to LWFA has been proposed so far [D. Umstadter et al, PRL 72, (1994)]. A multi-pulse train can generate plasma waves with larger amplitude than those driven by a single pulse with the same energy.

AlaDyn code, PIC 2D slice



QFluid code (self-consistent hybrid fluid+kinetic, 2D CYL)

Two possible pulse-shaping schemes have been proposed very recently



R.J. Shallow et al,
NIM A 829 (2016)

Older methods include either multiple beam-splitters setup or phase masks



- **Accepted in PRL yesterday!**
- **Uses a Michelson interferometer to induce beating**

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Accepted Paper

Excitation and control of plasma wakefields by multiple laser pulses

Phys. Rev. Lett.

J. Cowley, C. Thornton, C. Arran, R. J. Shalloo, L. Corner, G. Cheung, C. D. Gregory, S. P. D. Mangles, N. H. Matlis, D. R. Symes, R. Walczak, and S. M. Hooker

Accepted 20 June 2017

ABSTRACT

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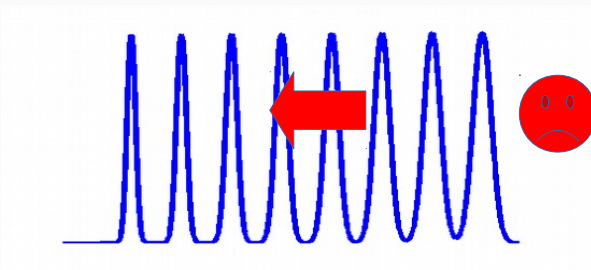
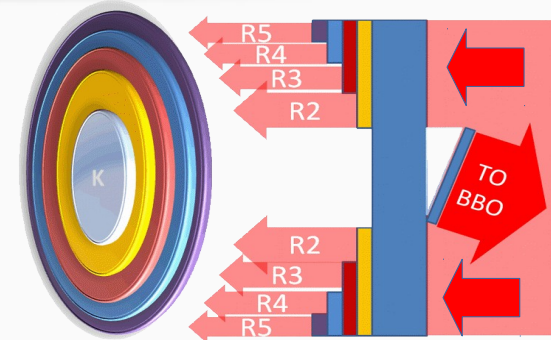
We demonstrate experimentally the resonant excitation of plasma waves by trains of laser pulses. We also take an important first step to achieving an energy recovery plasma accelerator by showing that a plasma wave can be damped by an out-of-resonance trailing laser pulse. The measured laser wakefields are found to be in excellent agreement with analytical and numerical models of wakefield excitation in the linear regime. Our results indicate a promising direction for achieving highly controlled, GeV-scale laser-plasma accelerators operating at multi-kilohertz repetition rates.

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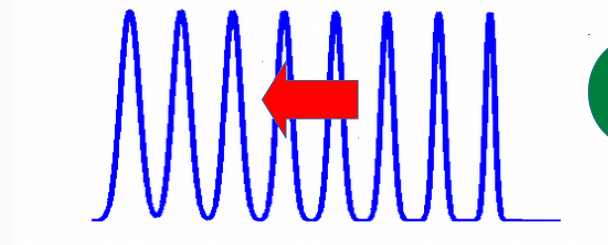


C3ANDEL (Comb by Chirp Compensated ANnular DELay Line)

- The pulse is time shaped with an annular delay line of fused silica.
- Each ring thickness is accurately determined by the selected delay of the sub-pulse
- Natural pulses lengthening is in the wrong direction (the longer pulses should arrive first [D. Umstadter et al, PRL 72, (1994)]).



CHIRP COMPENSATION



- The use of a negative chirp (shorter wavelengths on the head of the pulse) will compensate for the lengthening of the last pulse.
- A tilted pick-up mirror for the Injection Pulse is placed in the center of the rings.

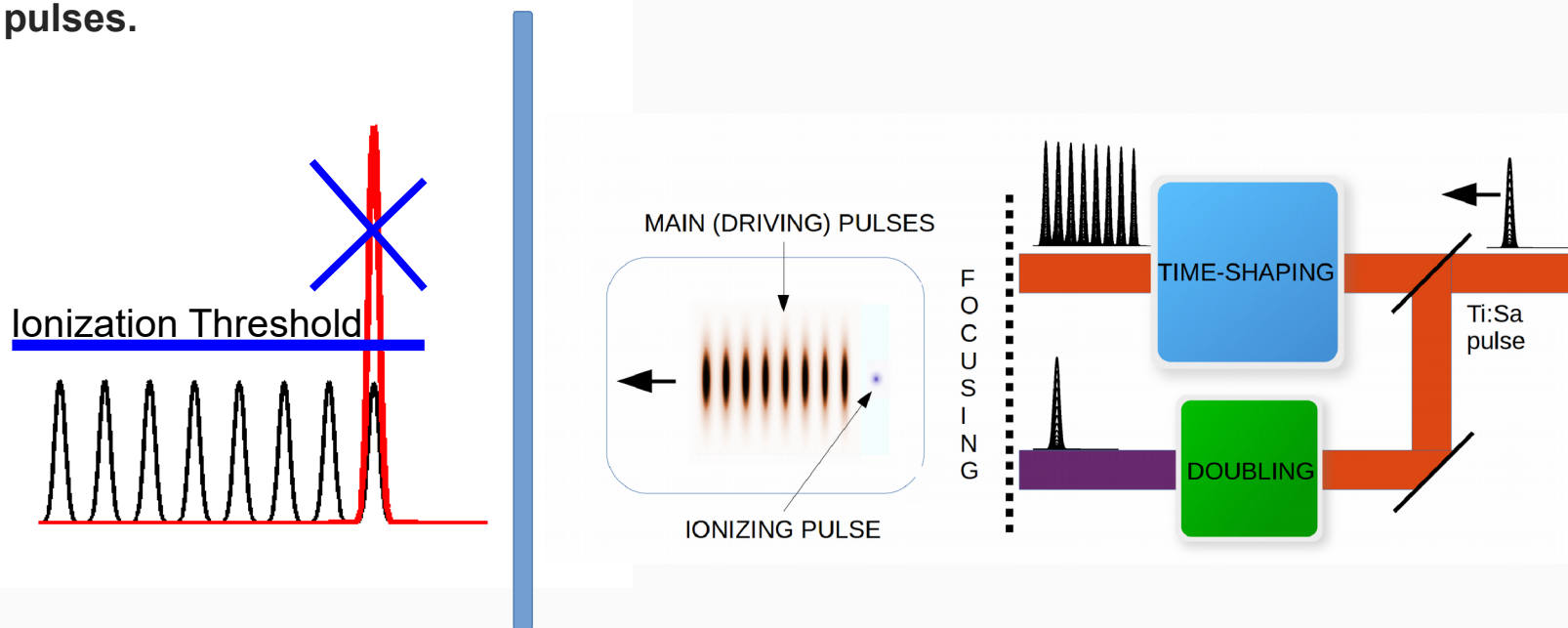


A new injection scheme: Resonant Multi-Pulse Ionization Injection



The Resonant Multi-Pulse Ionization injection [P. Tomassini et al, 2017 (submitted)] is a new bunch injection scheme aiming at generating extremely low-emittance bunches [as low as 0.07 mm mrad]

RMPII requires ONE short-pulse 100-TW class (e.g Ti:Sa) laser system. Since a unique very large-amplitude Ti:Sa pulse would fully ionize the atoms (Ar⁸⁺ in our selected example), the pulse is shaped as a resonant sequence of sub-threshold amplitude pulses.

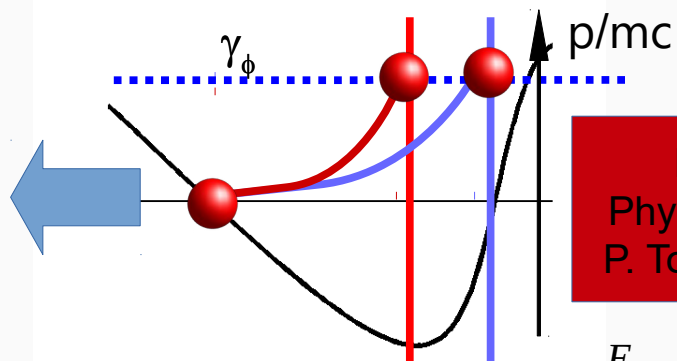




RMPII trapping analysis



Pulse-train amplitude must be above the trapping threshold for the extracted electrons



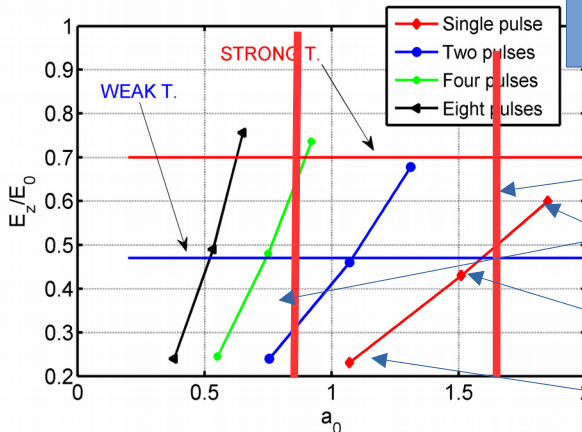
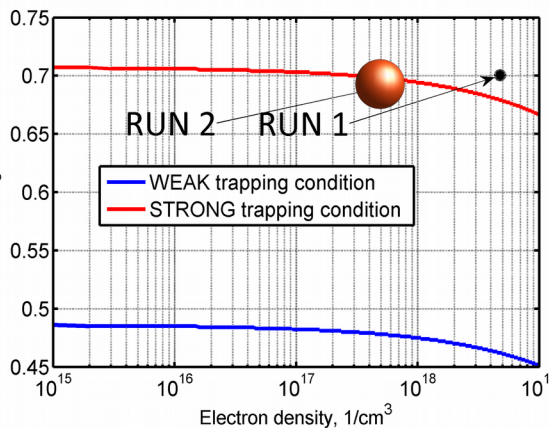
E. Esarey et al.;
Phys. Plasmas 2 (1997)
P. Tomassini et al (2017)

$$E_{norm} = E_z / E_0; E_0 = mc \omega_p / e$$

$$E_{norm}^2 / 2 + \beta_{ph} \sqrt{(1 + E_{norm}^2 / 2)^2 - 1} > 1 - 1 / \gamma_{ph}$$

$$2\beta_{ph} \sqrt{(1 + E_{norm}^2 / 2)^2 - 1} > 1 - 1 / \gamma_{ph}$$

STRONG trapping
WEAK trapping



Trapping analysis with commonplace parameters reveals that optimal trapping is reached with $a_0 > 1.6$ in a single pulse setup. This value is close to ionization threshold $N5+ \rightarrow N6+$. A simple two-pulses train allows us to deal with Nitrogen ($U_i = 552$ eV). To get advantage of the lower U_i of $Ar8+ \rightarrow Ar9+$ ($U_i = 422$ eV) at least a 4-pulses train is needed

Ionization thr. $N5+ \rightarrow 6+$
Ionization thr. $Ar8+ \rightarrow 9+$

7.5J
5.0J
2.5J



RMPII ionization analysis



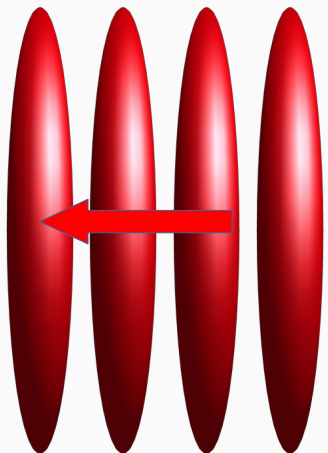
The frequency-doubled minor portion of the pulse acts as “ionizing pulse” as in two-colour ionization.

The key concept is that of “minimal transverse momentum rms” $p_{tr}/mc \simeq \Delta a_{0e}$ where

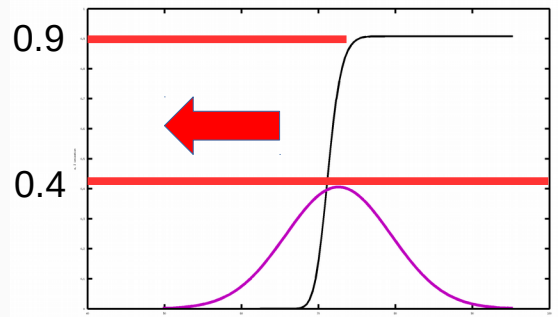
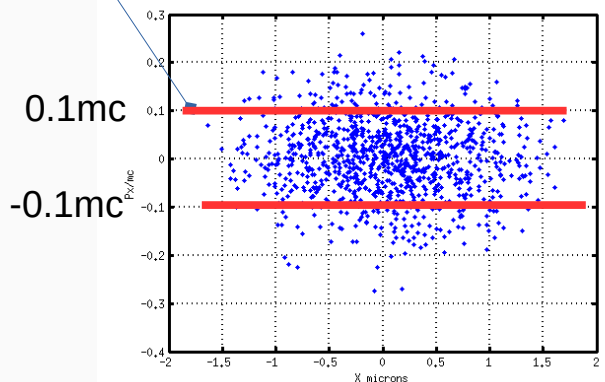
$$\Delta = \sqrt{a_{0e}/a_c}; a_c = 0.107 (U_I/U_H)^{3/2} \lambda$$

To reduce emittance a tightly focused beam is chosen

C.B. Schroeder et al.,
PRAB 17 (2014)
P. Tomassini et al (2017)



$w_{0,ion} = 3.5-4.5 \mu m$
 $\lambda_{ion} = 0.4 \mu m$
 $Z_{R,ion} = 100-160 \mu m$
 $T_{ion} = 50 fs; a_0 = 0.4$



Ionization Ar8+ -> Ar9+

Newborn electrons (one time-step)
transverse phase space
 $\epsilon_{ps_n} = 0.05 \text{ mm mrad}$



QFluid4 in brief



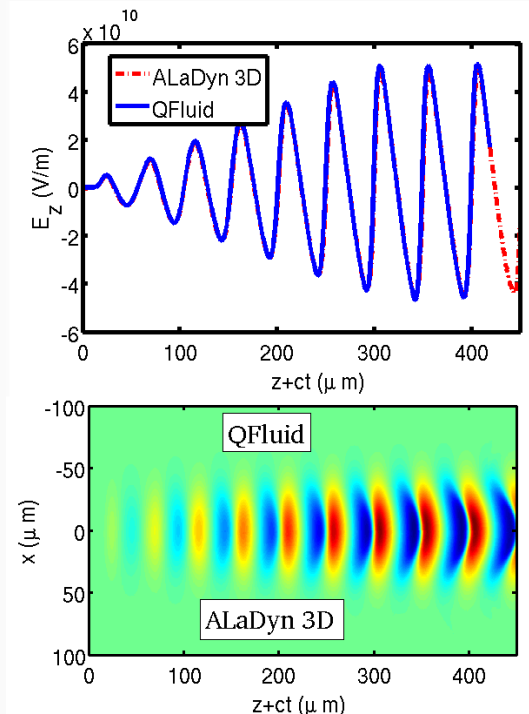
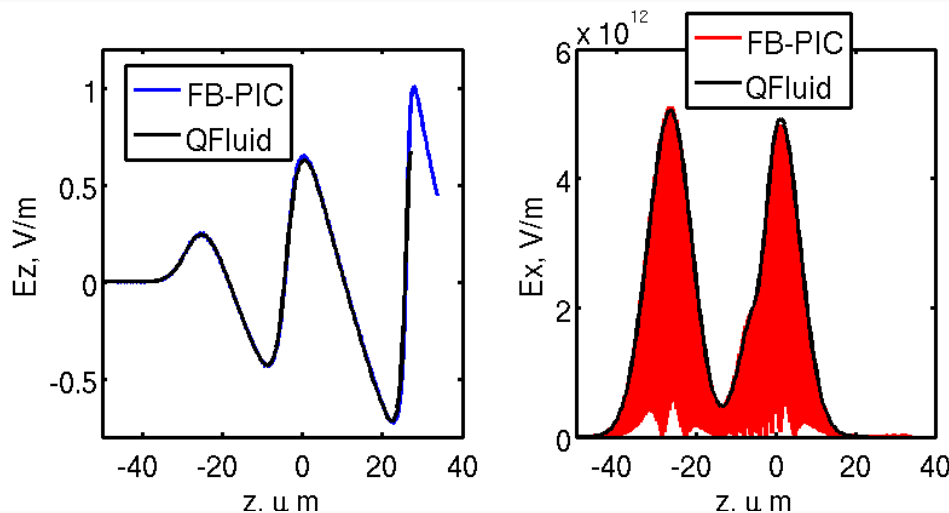
QFluid is a 2D CYLINDRICAL hybrid code for LWFA and PWFA in the plasma fluid and quasi-static regime that is suitable for long propagation simulations.

Laser pulse evolution is solved with the Envelope Evolution Approximation (second time derivative included!)

Plasma dynamics is solved via the pseudopotential computation in the QSA

Electrons of the beam move as macroparticles under the 3D force that includes the ponderomotive effect.

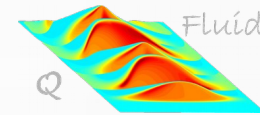
NOTE: Qfluid can't be properly used with fast varying density profiles (as those @ plasma exit. Validated with EPOCH, AlaDyn and FB-PIC (also in the multi-pulse case)



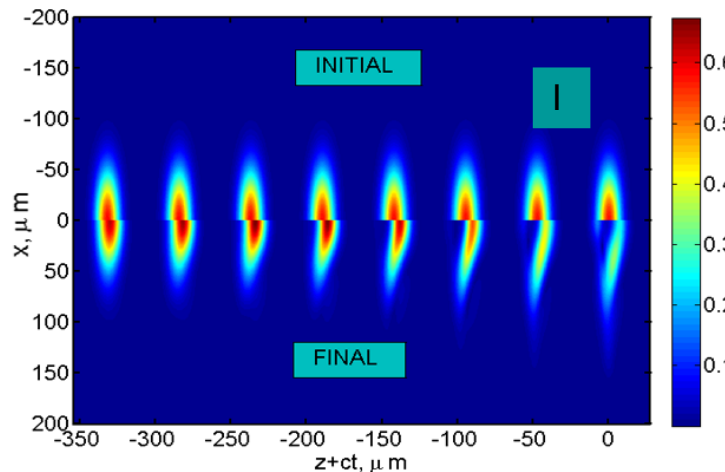
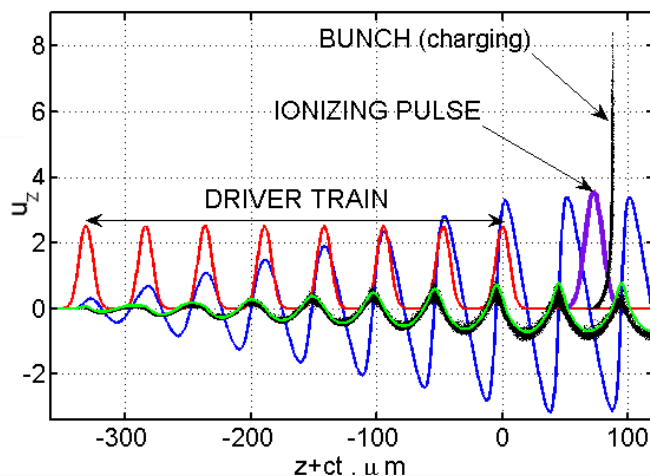
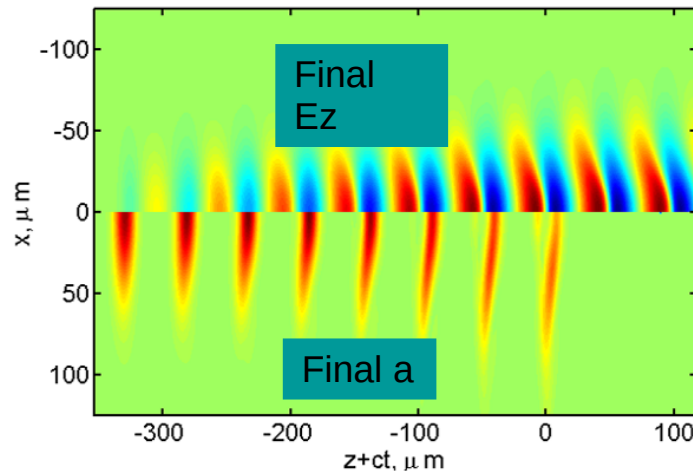
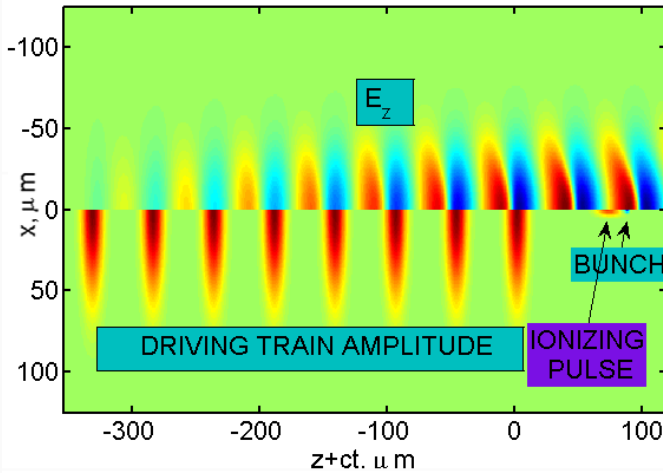
Thanks to M. Kirchen (DESY) FB-PIC



SETUP A -INJECTOR (not guided)



A first possible parameters set is presented here. It is intended either as a bunch injector or a 100 MeV-class accelerator. A flat-density (no guiding) Ar+8 pre-plasma is assumed.



PLASMA
 $n_0 = 5 \cdot 10^{17} \text{ 1/cm}^3$

DRIVER
 $E = 0.83 \times 8 J$
 $T = 30 \text{ fs}$
 $w_0 = 45 \mu\text{m}$
 $a_0 = 0.61$

IONIZATION
 $E = 12 \text{ mJ}$
 $T = 35 \text{ fs}$
 $w_0 = 3.5 \mu\text{m}$
 $a_0 = 0.41$

BOX
 $\delta r = \delta z = 0.1 \mu\text{m}$

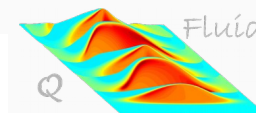
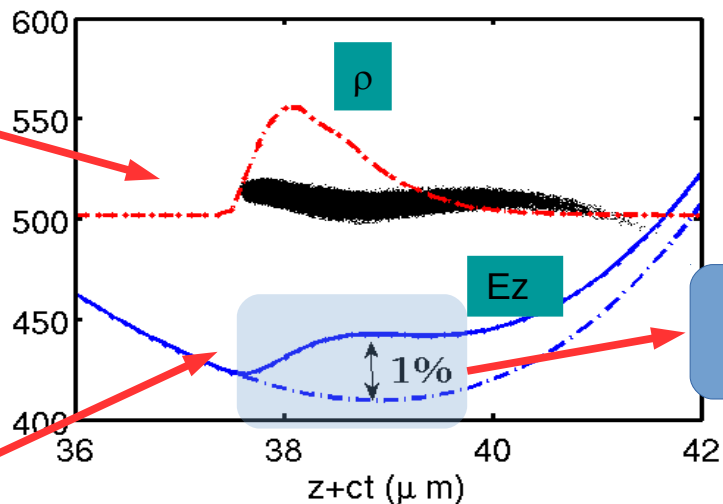
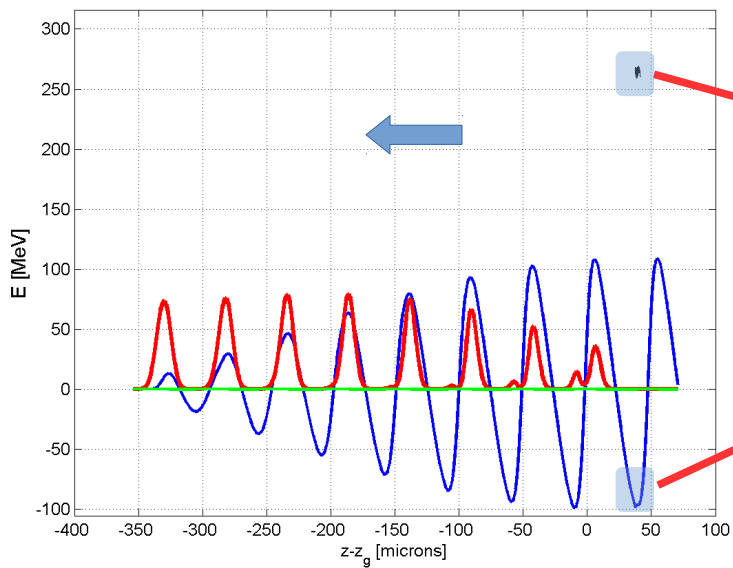


SETUP A (INJECTOR) -Final Bunch quality



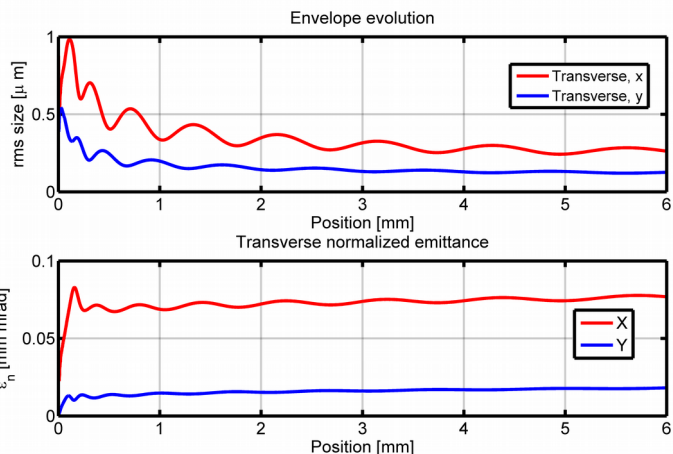
After about 6mm of acceleration the 265 MeV beam possesses an outstanding beam-quality: $dE/E = 0.5\%$, $\epsilon_{n} < 0.08$ mm mrad,

$n_0 = 500e15$ 1/cm³, Pos: $-72 \cdot 10^2$ microns, $\sigma_z = 0.56$ microns, Charge = 3.7996 pC, dE/E rms = 0.50428%



BEAM
LOADING

$Q = 3.8$ pC ; $I_{peak} = 0.9$ kA
 $(\delta E/E)_{rms} = 5 \cdot 10^{-3}$; $\delta\theta_{rms} = 0.4$ mrad
 $\epsilon_{nx} = 0.078$ mm · mrad ; $\epsilon_{ny} = 0.018$ mm · mrad
 $\sigma_l = 0.56$ μm ; $\sigma_r = 0.23$ μm



MATCHED
BEAM



SETUP A (INJECTOR) – Increase Charge?



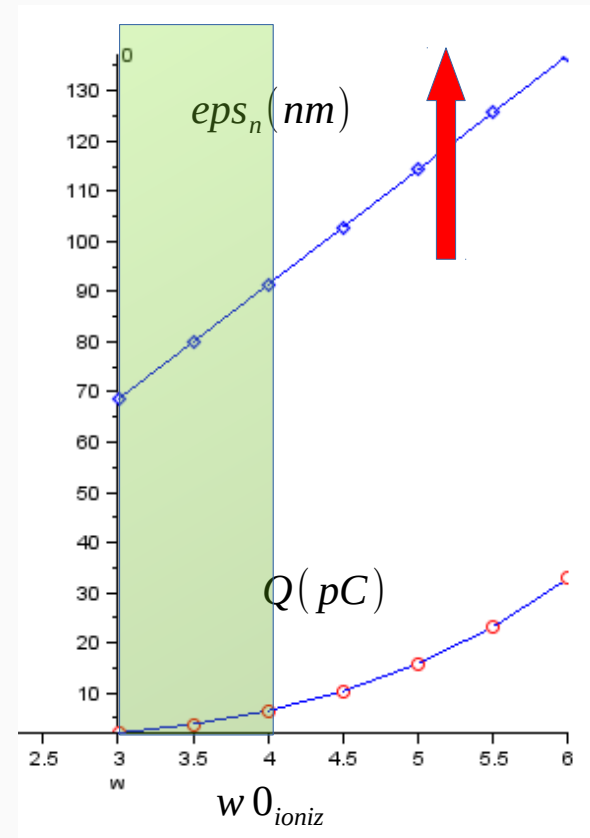
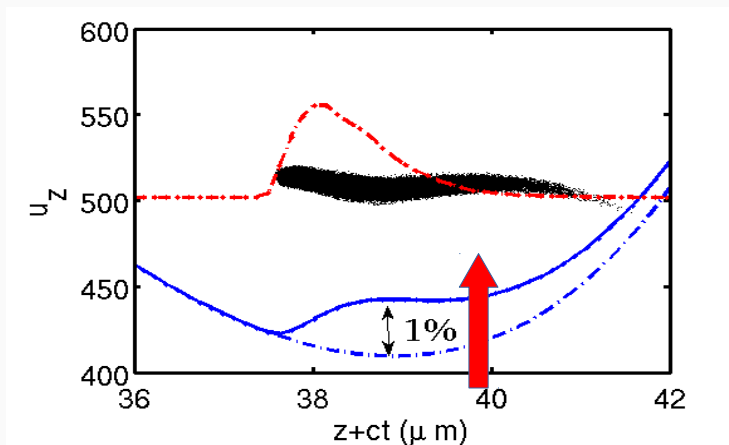
Energy spread and emittance with $Q=3.8$ pC are very low so the natural question is

If we want to use the bunch as a pre-accelerated bunch suitable for energy boosting, is it possible to increase its charge?

$$Q \propto w_{0ion}^4 \quad \epsilon_{ps_n} \propto w_{0ion}$$

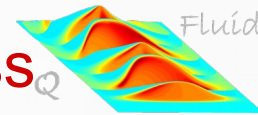


So answer is YES (nonlinear emittance increase due to bunch hopping not included) BUT energy spread will increase to above 1% for a 10pC bunch





SETUP B,D – (guided) GeV-class



To extend the acceleration beyond one Rayleigh length guiding with a preformed channel is assumed. A capillary is placed close to gas-jet nozzle to assure a gentle transition from a flat (pure Ar) plasma to a He plasma channel

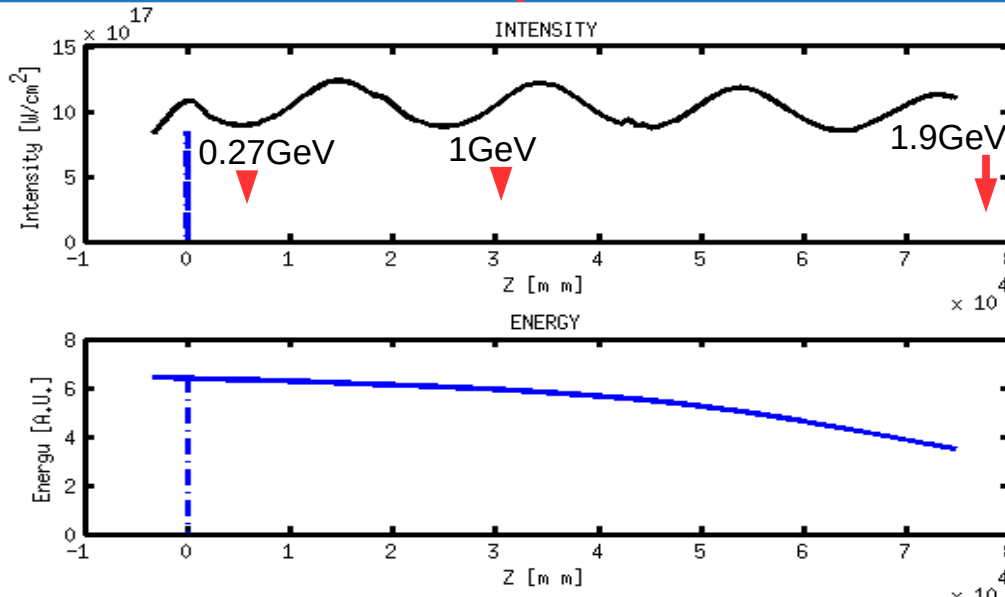
Gas-Jet nozzle
265MeV injector



He filled capillary

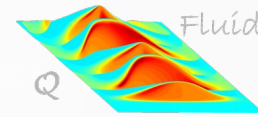
BUNCH B- 3cm
1.15 GeV, 0.81% rms,
 $\epsilon_n = 0.08$ mm mrad

BUNCH D- 8cm
1.9 GeV, 0.67% rms,
 $\epsilon_n = 0.08$ mm mrad



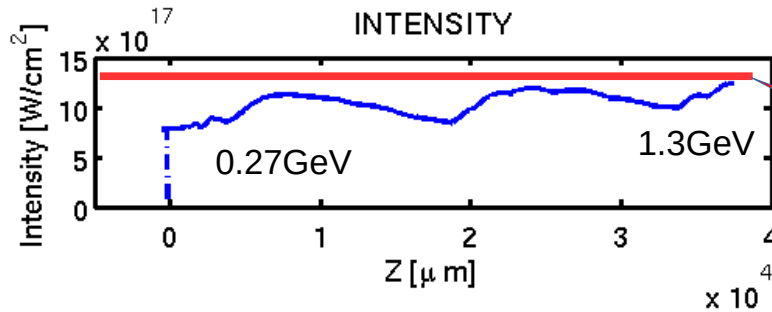


SETUP C – (guided) GeV-class

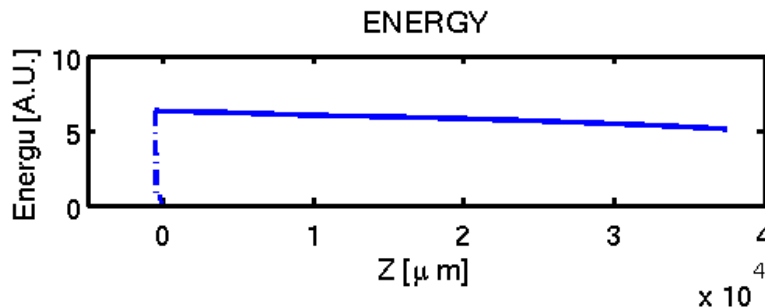


A single capillary filled with Argon could be a valid alternative to the jet+capillary since the Intensity threshold for Ar9+ is $I_{tr}=1.4 \times 10^{18} \text{ W/cm}^2$ (no strong defocusing from further ionization occur)

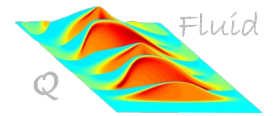
Gas-Jet nozzle
265MeV injector



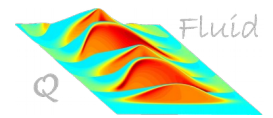
Ar9+ Intensity
threshold



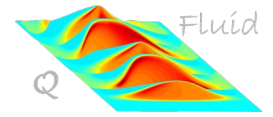
2D (cyl) maps



Longitudinal phase-space+fields



Driver(s) evolution



INJECTED

EVOLVED

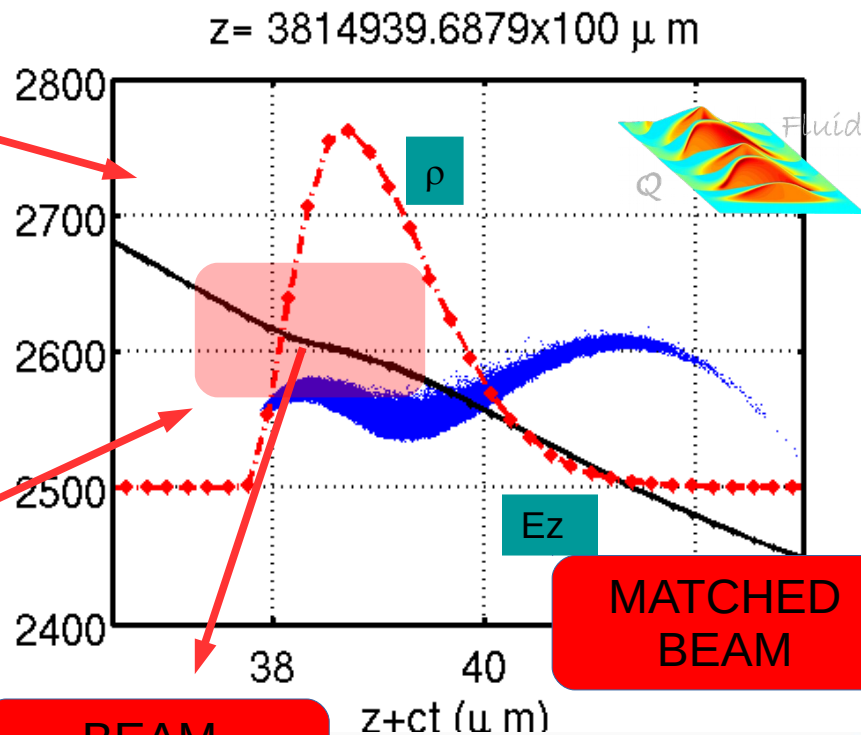
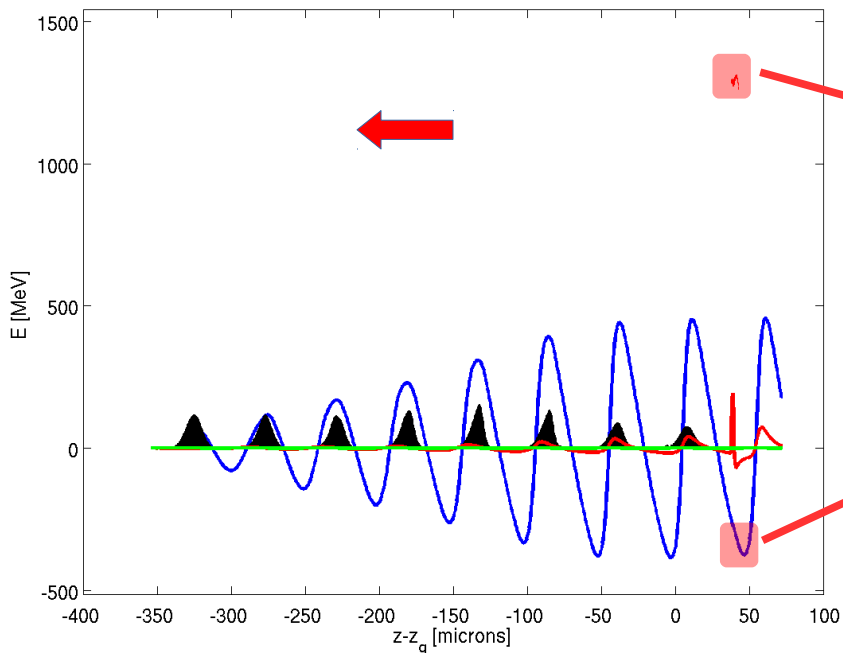


SETUP C (Guided) -Final Bunch quality



Minimum energy spread is reached after about 3.5 cm of acceleration with mean energy of 1.3 GeV , $dE/E = 0.5\%$, $\epsilon_{n,0} = 0.08 \text{ mm mrad}$,

$n_0 = 500 \times 10^{15} \text{ 1/cm}^3$, Pos: $-373 \times 10^2 \text{ } \mu\text{m}$, $\sigma_z = 0.66 \text{ } \mu\text{m}$, $Q = 4.2718 \text{ pC}$, $\sigma_E/E = 0.49843\%$



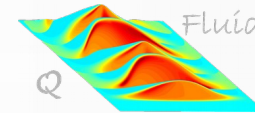
MATCHED BEAM

BEAM LOADING

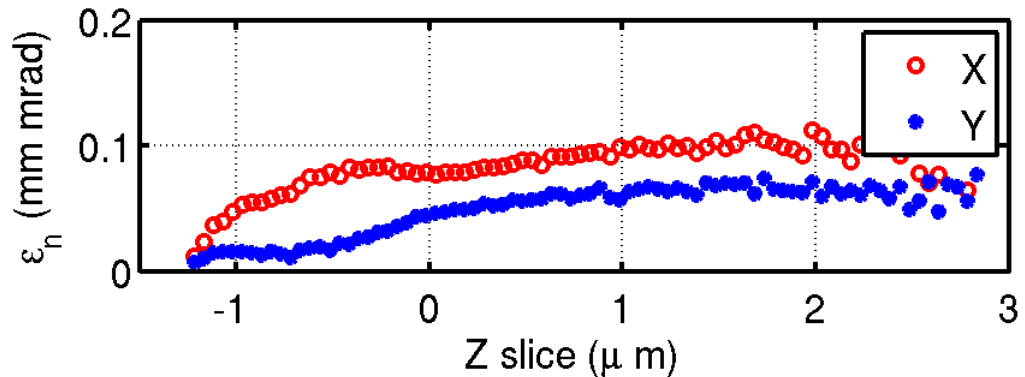
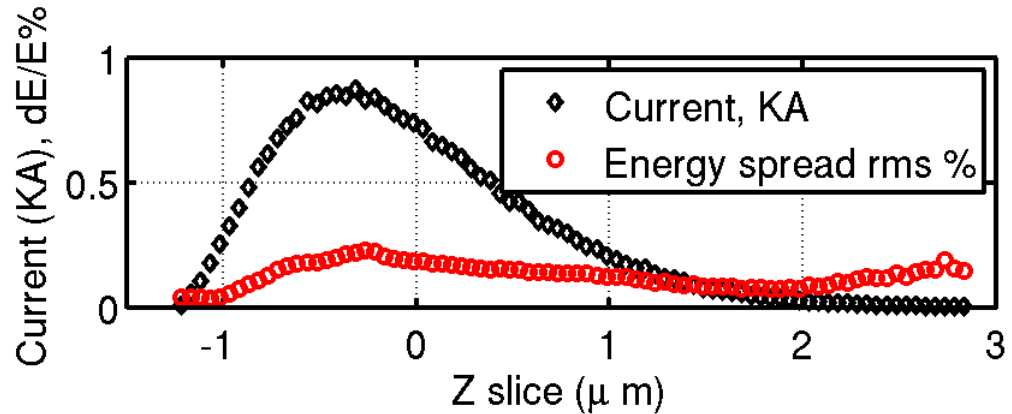
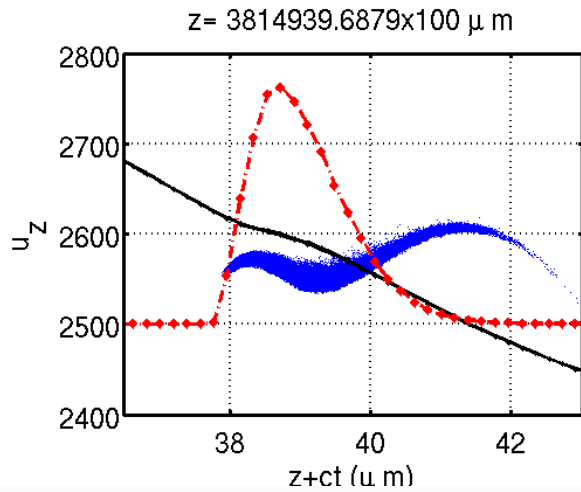
$Q = 4.3 \text{ pC}$; $I_{peak} = 0.85 \text{ kA}$
 $(\delta E/E)_{rms} = 5 \cdot 10^{-3}$; $\delta \theta_{rms} = 0.2 \text{ mrad}$
 $\epsilon_{nx} = 0.081 \text{ mm} \cdot \text{mrad}$; $\epsilon_{ny} = 0.021 \text{ mm} \cdot \text{mrad}$
 $\sigma_l = 0.66 \text{ } \mu\text{m}$; $\sigma_r = 0.19 \text{ } \mu\text{m}$



SLICE analysis for Bunch C



Slice analysis with coherence length $l_c=0.05$ micron (See FEL slices below) reveals a slice energy spread of $dE/E_{\text{slice}}=0.22\%$ @peak current (integrated $dE/E = 0.5\%$),



$(\delta E/E)_{\text{SLICE}} \text{rms} = 2.2 \cdot 10^{-3} @ \text{peak}$
 $I = 0.85 \text{ KA} @ \text{peak}$



LINEAR vs CIRCULAR polarizations (Driver)

The use of circular polarization can help in either reducing the number N of pulses or increasing the intensity of the driver(s).

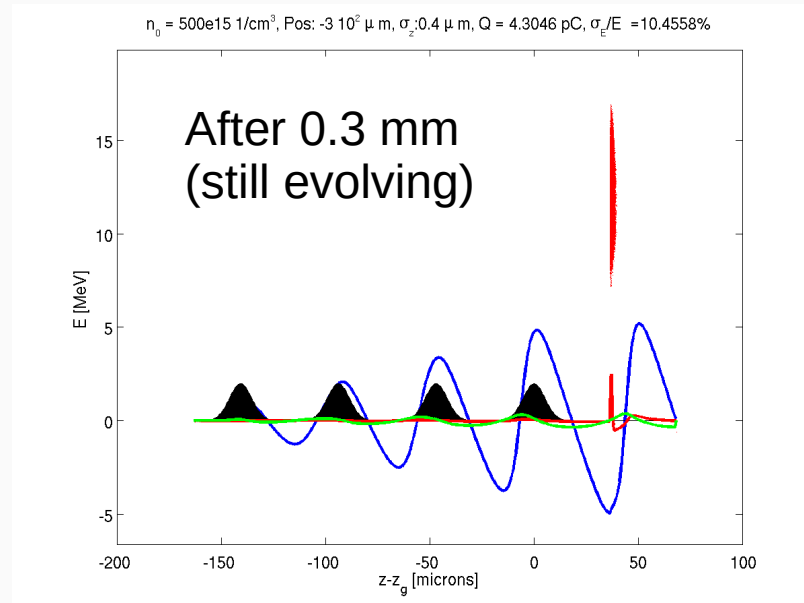
CAUTIONARY NOTE: Some authors [CITE] claim that non-adiabatic effects can modify the outcomes of ADK model especially for circularly polarized pulses. Is there a detailed experimental comparison between linear and circular polarization for the same parameters used here? [30-50fs, $a_0=0.6-0.8$]?

Analytical/numerical results from ADK theory [P. Tomassini 2017] show that the saturation intensity I_C (circular pol.) for Ar $^{9+}$ is related to I_L (linear pol.) as

$$I_C \approx 1.7 I_L$$

**TEST RUN with 4 pulses.
Same parameters as before
but in circular polarization**

**Snapshot after 300 micron
(same results as with an
8-pulses train)**





SECOND vs THIRD harmonics (Ionization)



After the ionization pulse passage, the extracted particles possess transverse momentum that essentially depends on pulse amplitude.

$$p_{tr}/mc \propto a_{0ion} \propto \lambda^{-1} [QUIVERING, UNCORRELATED]$$

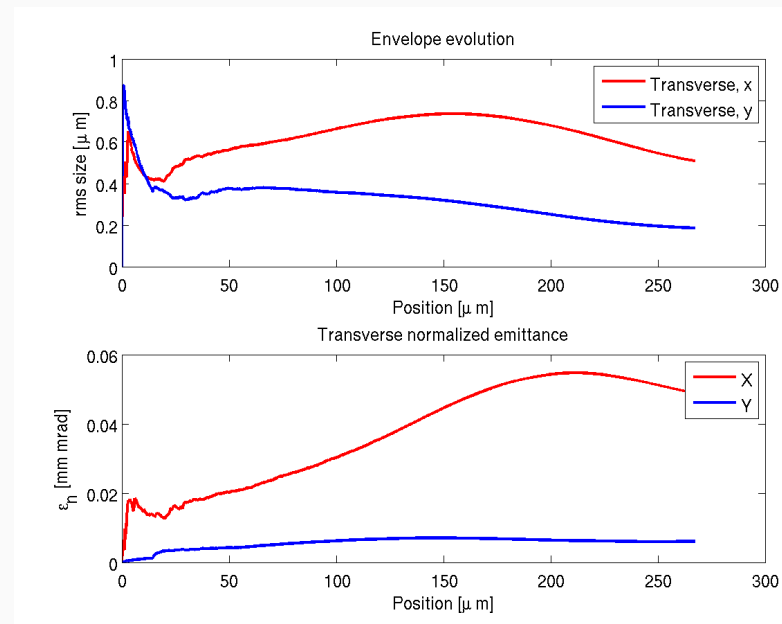
$$p_{tr}/mc \propto a_{0ion}^2 \propto \lambda^{-2} [PONDEROMOTIVE, CORRELATED]$$

With the same BBO crystal used for the 2nd harmonics it is possible (and experimentally feasible) to generate a 3rd harmonics. Only phase-matching angle and efficiency change.

With a 1st→3rd harmonics conversion efficiency of 8% and 150mJ of incoming 0.8 energy a pulse delivering 12mJ @267nm.

Since minimum emittance scales as a_0 (correlated x-px give no contribution) we expect that (WITH NO SPACE-CHARGE included) **the emittance scales as $1/\lambda$** .

SAME parameters a C-bunch, but emittance after the injection phase is now 0.05 mm mrad (III harm.) instead of 0.07 mmrad (II harm.) Not negligible space-charge effects Are present.





FEL preliminary results

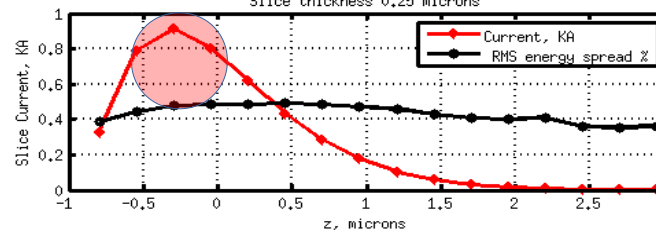
Detailed FEL simulation are ongoing. Preliminary analytical results with bunches A (0.265 GeV) and B (1.0GeV) are shown here. Slice analysis is necessary to fully understand coherent spikes generation and lasing.

Bunch parameters

Bunch parameters			
	A	B	C
beam energy [GeV]	0.265	1.15	1.3
long. beam size (rms) σ_L [μm]	0.56	0.25	0.655
current intensity [A]	812	2200	785
norm. emittance [mm \times mrad]	0.078	0.08	0.08
energy spread σ_E/E (%)	0.65	0.81	0.5
Common FEL parameters			
undulator magnetic field [T]	1		
undulator period [cm]	1.4		
deflection parameter	1.3		
Output FEL parameters			
FEL wavelength [nm]	48	2.6	2.0
Twiss β [m]	1.26	5.45	6.16
Pierce parameter ρ	0.009	0.003	0.0018
inh. broad. gain length [m]	0.096	1.38	2.14
saturation power [MW]	2291	323	86
saturation length [m]	2.5	33	49
coherence length [μm]	0.25	0.04	0.05
sat. power with slippage [MW]	995	253	82

$$\rho = \frac{8.36 \times 10^{-3}}{\gamma} \sqrt[3]{\lambda_U^2 \frac{I_{\text{peak}}[\text{A}]}{2\pi\beta\gamma^{-1}\epsilon_n} K^2 f_B^2(\text{K})}$$

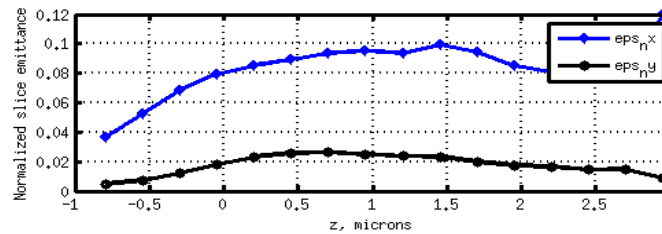
Slice thickness 0.25 microns



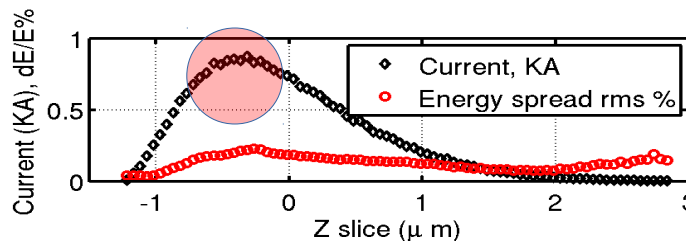
$$K \simeq 0.94 B[\text{T}] \lambda_U[\text{cm}]$$

$$\lambda_{\text{FEL}} = \frac{\lambda_U}{2\gamma^2} \left(1 + \frac{K^2}{2}\right)$$

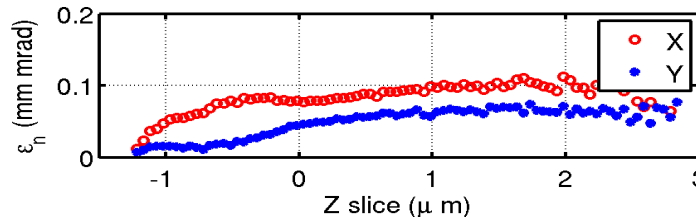
$$\beta_{\text{Twiss}}[\text{m}] = \frac{\sqrt{2}\gamma}{2\pi K} \lambda_U[\text{m}]$$



BUNCH A



BUNCH C





FEL preliminary results



Gain length

$$L_G = \left[1 + \frac{0.641}{\rho^2} \left(\frac{\sigma_E}{E} \right)^2 \right] \exp \left[\frac{0.136}{\rho^2} \left(\frac{\sigma_E}{E} \right)^2 \right] \frac{\lambda_U}{4\pi\sqrt{3}\rho}$$

Saturation Power

$$P_S = \sqrt{2} \Phi \left(\rho, \frac{\sigma_E}{E} \right) \rho P_{e\text{-beam}}$$

Coherence length

$$L_C = \frac{\lambda_{FEL}}{4\pi\sqrt{3}\rho}$$

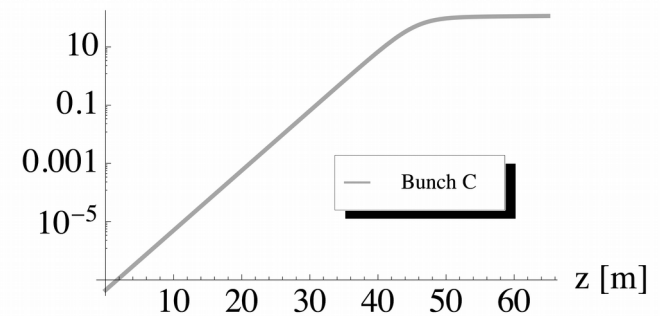
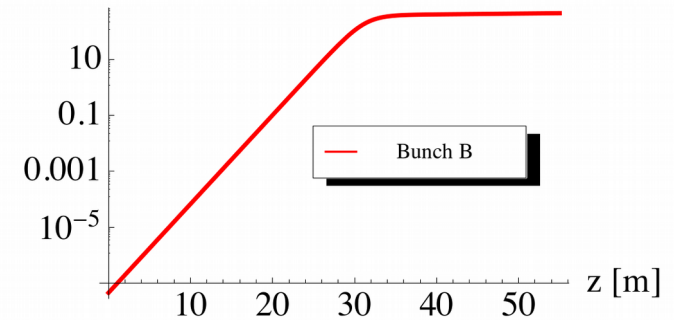
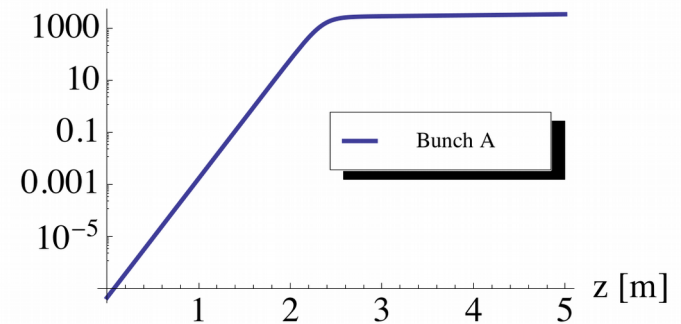
Slippage corrections

$$\tilde{P}_S = \left(1 - e^{-0.25 \frac{\sigma_L}{L_C}} \right) P_S$$

FEL results from G. Dattoli and F. Nguyen ENEA, Frascati

BOOKLET for FEL design,
G.Dattoli et al
http://fel.enea.it/booklet/pdf/Booklet_for_FEL_design.pdf

growth Power [MW]

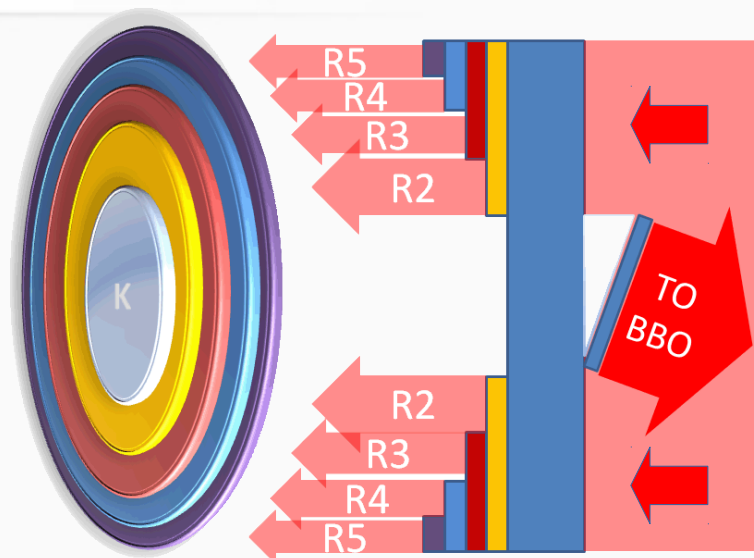
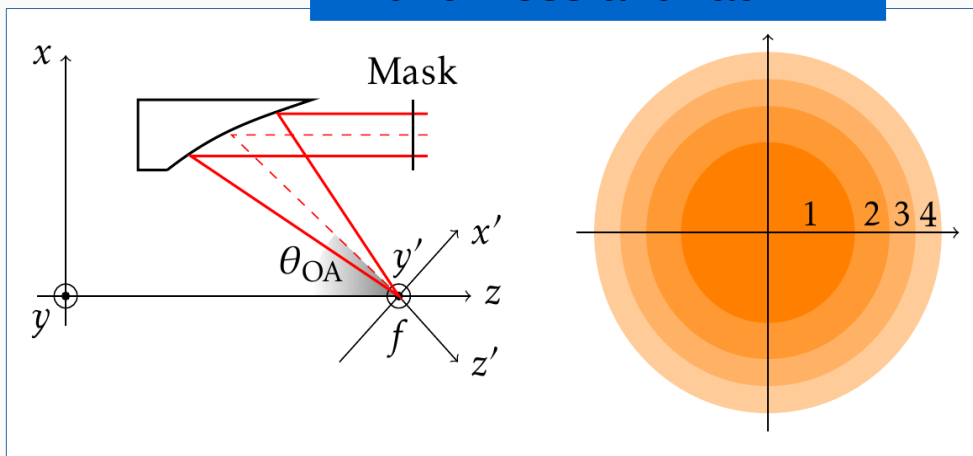




C3ANDLE working status

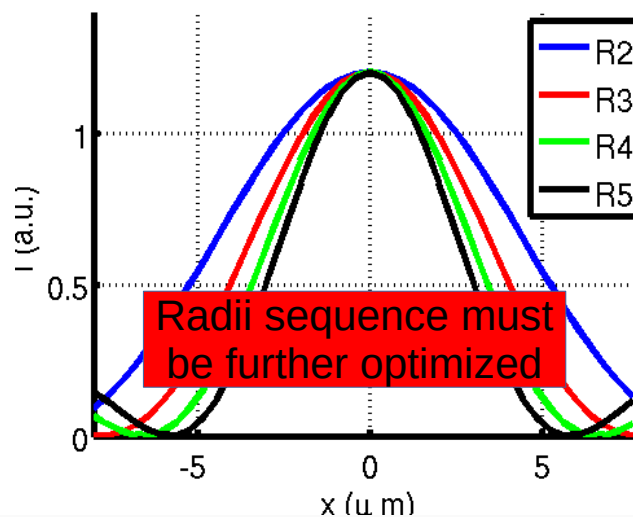
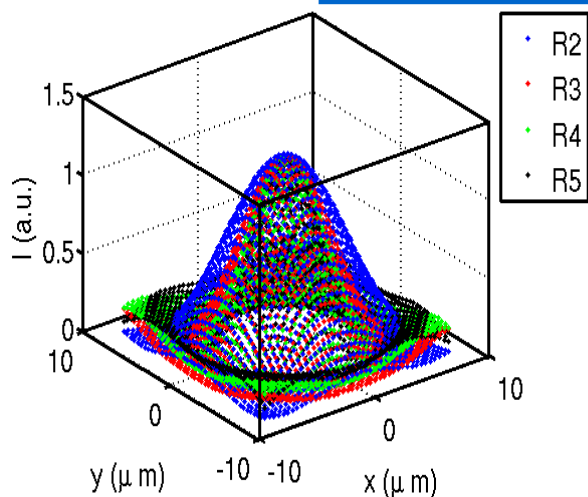


Delay masks with tuned thickness and radii



SIDE VIEW

On focus intensities



PARAMETERS
 $n_0 = 5 \times 10^{17} \text{ 1/cm}^3$

Substrate:

$l_0 = 0.5 \text{ mm}$

Rings:

$\Delta l = 0.104 \text{ mm}$

BBO:

$L = 0.2 \text{ mm}$





Conclusion



- **Resonant Multi-Pulse ionization injection is a new reliable method to obtain an injector/accelerator with a SINGLE 100-TW class Ti:Sa laser system**
- **Using Argon an 8-pulses scheme is capable to generate a 265MeV bunch in 6mm (gas-jet, flat profile), 1GeV in 3 cm and 2GeV in 10cm (guided)**
- **Charge can be increased to meet EUPRAXIA requirements (INJECTOR) but emittance and energy spread will increase. More simulations are required**
- **Bunch quality is outstanding, mainly concerning emittance (below 0.1 mm mrad along E and 0.02 mm mrad along B)**
- **FEL preliminary results show that those bunches are suitable for lasing, generating a few-spikes radiation.**
- **We are working on the choice of the pulse time shaper. A possible configuration with delay masks is being studied.**
- **Bunch quality can be further optimized by changing the trapping point [in progress]**