

Diffractive dijet production in DLS compared to NNLO QCD predictions

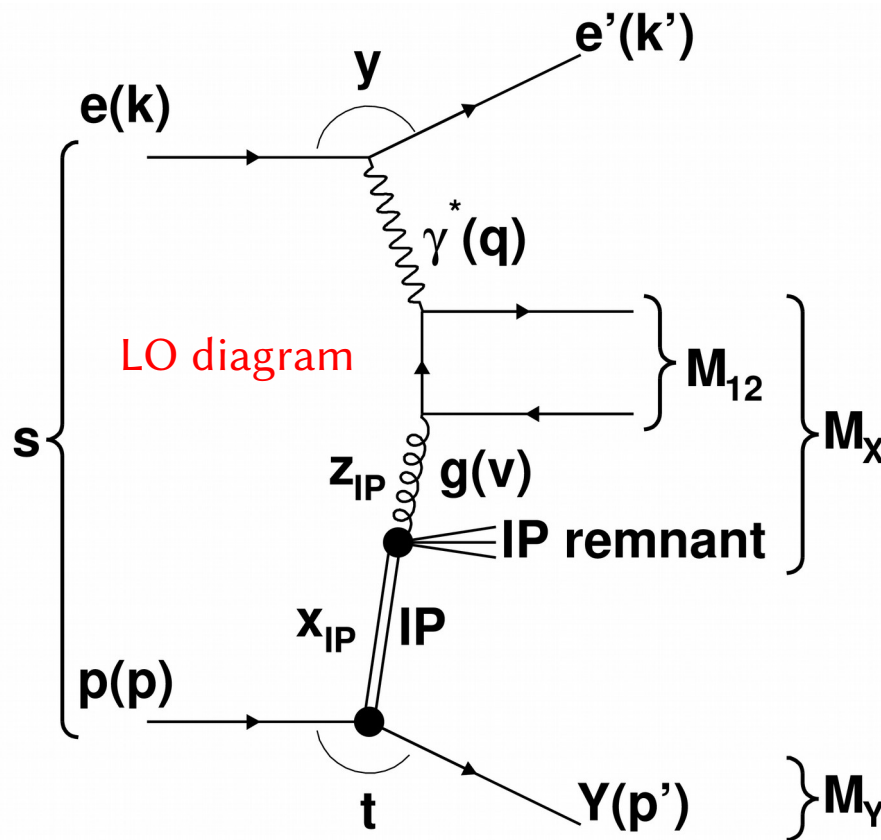
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WE-Heraeus Physics School
*QCD – Old Challenges and
New Opportunities*
Bad Honnef, September 27



Diffractive Dijet Production in ep

In diffractive events the beam proton stays intact or dissociates into low mass hadronic system Y



DIS variables:

$$Q^2 = -(k - k')^2 \quad y = \frac{p \cdot q}{p \cdot k}$$

Dijet mass: M_{12}

Diffractive variables:

$$x_{IP} = 1 - \frac{E'_p}{E_p} \quad t = (p - p')^2$$

At LO: The momentum fraction entering the hard subprocess with respect to the diffractive exchange

$$z_{IP} = \frac{M_{12}^2 + Q^2}{M_X^2 + Q^2}$$

At HERA about 10% of low- x events are diffractive

Collinear QCD factorization theorem in hard diffraction

- For diffractive events with a **hard scale** (e.g Q^2 or jets p_T)
- Factorization of the diffractive cross section into **process independent DPDs** and **partonic cross sections**

$$d\sigma(ep \rightarrow epX) = \sum_i f_i^D(x, Q^2, x_{IP}, t) \otimes d\sigma^{ie}(x, Q^2)$$

- For diffractive processes (including dijets) with Q^2 high enough factorization proven by Collins within perturbative QCD, for low Q^2 factorization breaking suggested

Factorization of Hard Processes in QCD

John C. Collins (IIT, Chicago & SUNY, Stony Brook), Davison E. Soper (Oregon U.), George F. Sterman (SUNY, Stony Brook). May 30, 1989. 91 pp.
Published in *Adv.Ser.Direct.High Energy Phys.* 5 (1989) 1-91
ITP-SB-89-31
DOI: [10.1142/9789814503266_0001](https://doi.org/10.1142/9789814503266_0001)
e-Print: [hep-ph/0409313](https://arxiv.org/abs/hep-ph/0409313) | [PDF](#)

[References](#) | [BibTeX](#) | [LaTeX\(US\)](#) | [LaTeX\(EU\)](#) | [Harvmac](#) | [EndNote](#)
[ADS Abstract Service](#)

[Detailed record](#) - [Cited by 716 records](#) 500+

Proof of factorization for diffractive hard scattering

John C. Collins (Penn State U.). Sep 1997. 12 pp.
Published in *Phys.Rev. D57* (1998) 3051-3056, Erratum: *Phys.Rev. D61* (2000) 019902
PSU-TH-189
DOI: [10.1103/PhysRevD.61.019902](https://doi.org/10.1103/PhysRevD.61.019902), [10.1103/PhysRevD.57.3051](https://doi.org/10.1103/PhysRevD.57.3051)
e-Print: [hep-ph/9709499](https://arxiv.org/abs/hep-ph/9709499) | [PDF](#)

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[ADS Abstract Service](#); [OSTI Information Bridge Server](#)

[Detailed record](#) - [Cited by 384 records](#) 250+

NLO DPDFs

- DPDF sets differ mainly in gluon component which is weakly constrained from inclusive diffractive data
- For gluon dominated diffractive dijet production we have sizable DPDF uncertainty
- DPDFs obey standard DGLAP evolution equation

Fits of **inclusive** data

~~H1 2006 Fit A~~
H1 2006 Fit B

Combined **inclusive** + **dijets** data fits

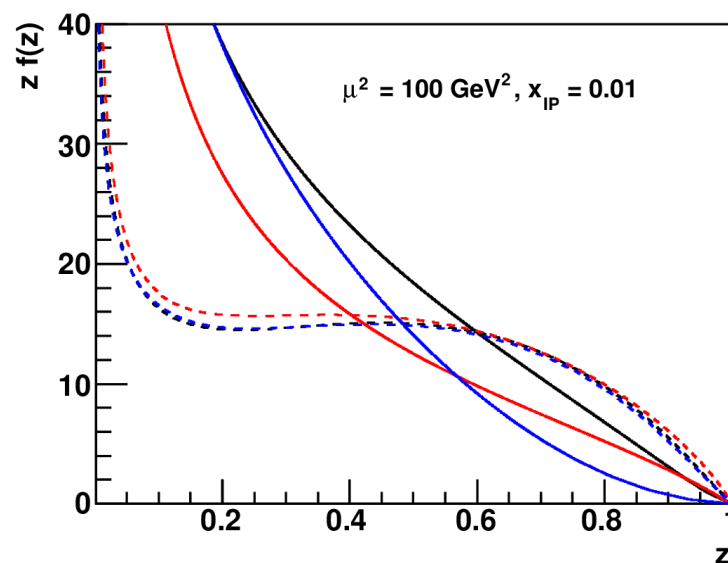
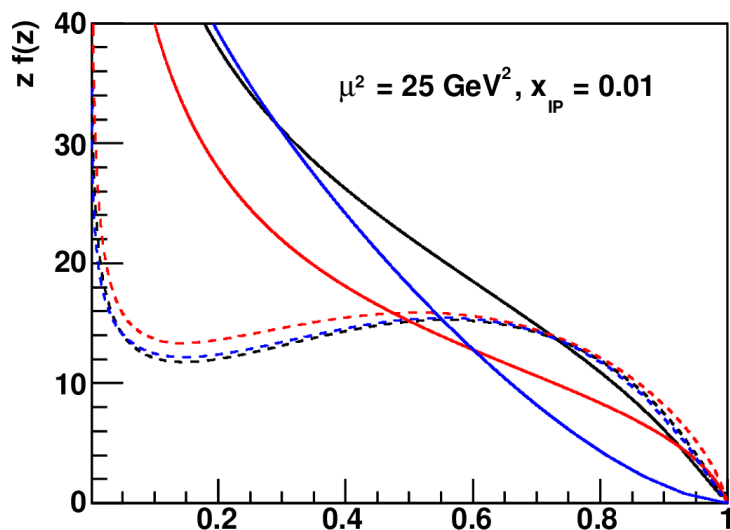
H1 2007 Fit Jets
ZEUS 2009 Fit SJ

Quark Singlet Densities

- H1 Fit B - $z \Sigma(z)$
- H1 Fit Jets - $z \Sigma(z)$
- ZEUS SJ - $z \Sigma(z) \times 1.2$

Gluon Densities

- H1 Fit B - $z G(z)$
- H1 Fit Jets - $z G(z)$
- ZEUS SJ - $z G(z) \times 1.2$



70% of diffractive exchange momentum carried by gluons

NNLO QCD Predictions

- **NNLOJET** program based on antenna subtraction

J. Currie, T. Gehrmann, A. Huss and J. Niehues, JHEP 07 (2017) 018, [1703.05977]

A bit of history

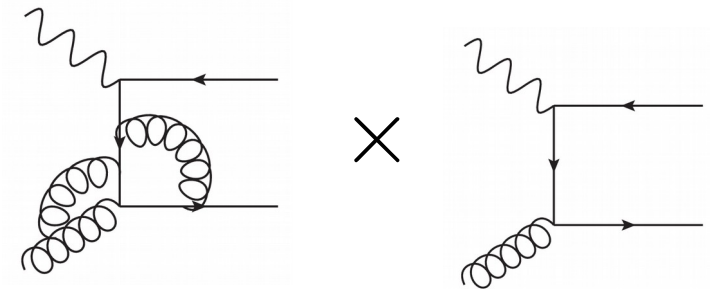
- **1973** Asymptotic freedom of QCD
- **1993** NLO studies of DIS jets
- **2016** NNLO corrections for DIS jets

Cookbook

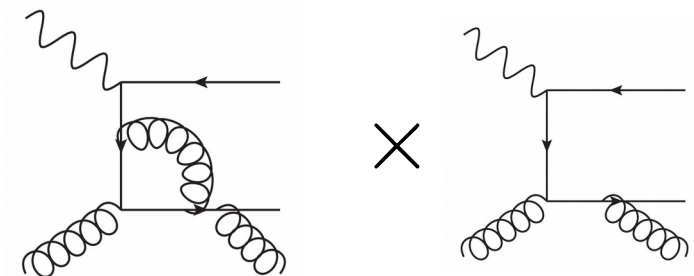
- 1) The matrix element tables precalculated by **NNLOJET** program (~1M CPU hours)
- 2) Then convoluted with DPDFs and α_S using **fastNLO** (<1s)

✓ The NLO 2jet and 3jet contributions verified against Sherpa and NLOJET++

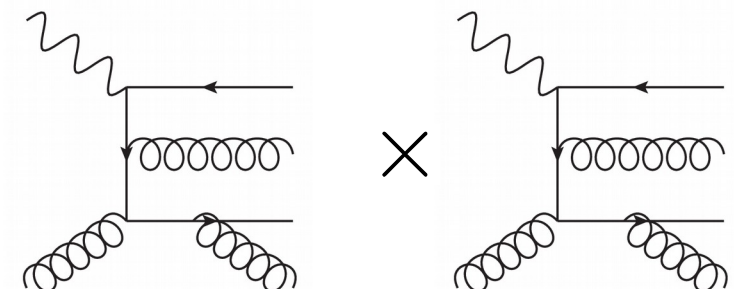
virtual-virtual



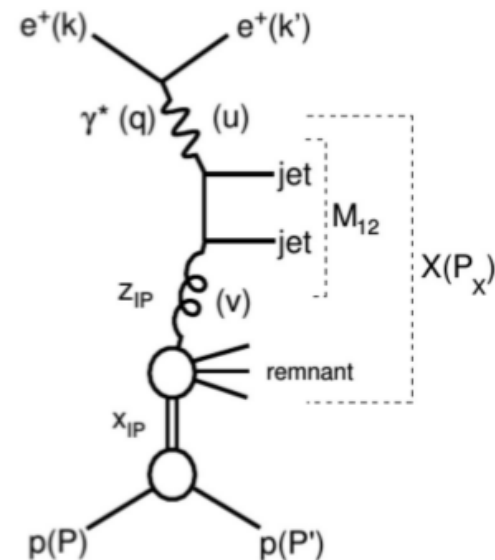
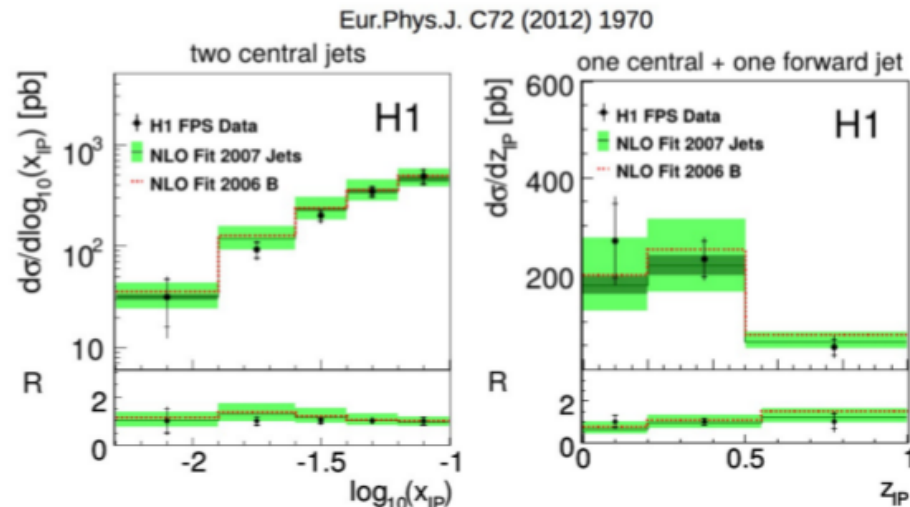
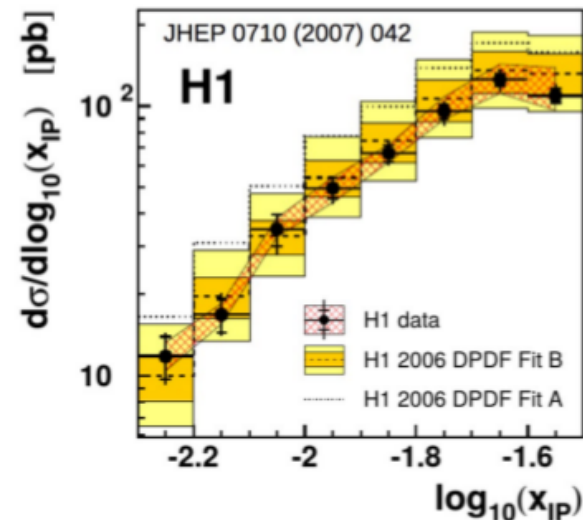
real-virtual



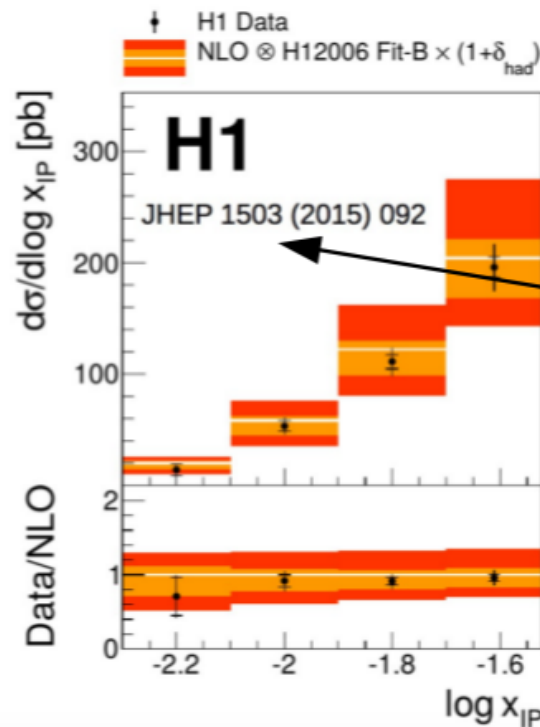
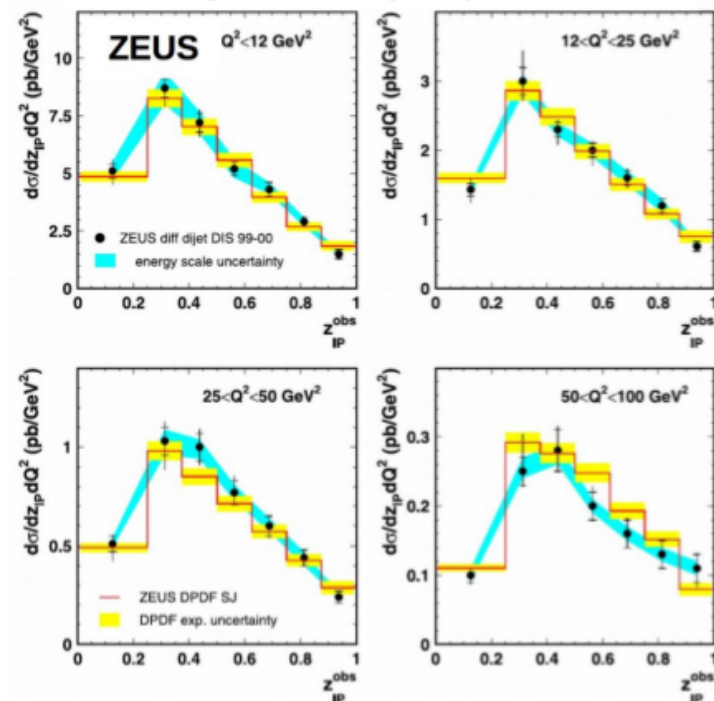
real-real



Diffractive di-jets in DDIS



Nucl. Physics B 831 (2010) 1-25



Katarzyna Wichmann:
Soft and hard QCD processes at
HERA
Sunday, 24.9.

first measurement of α_s
in DDIS

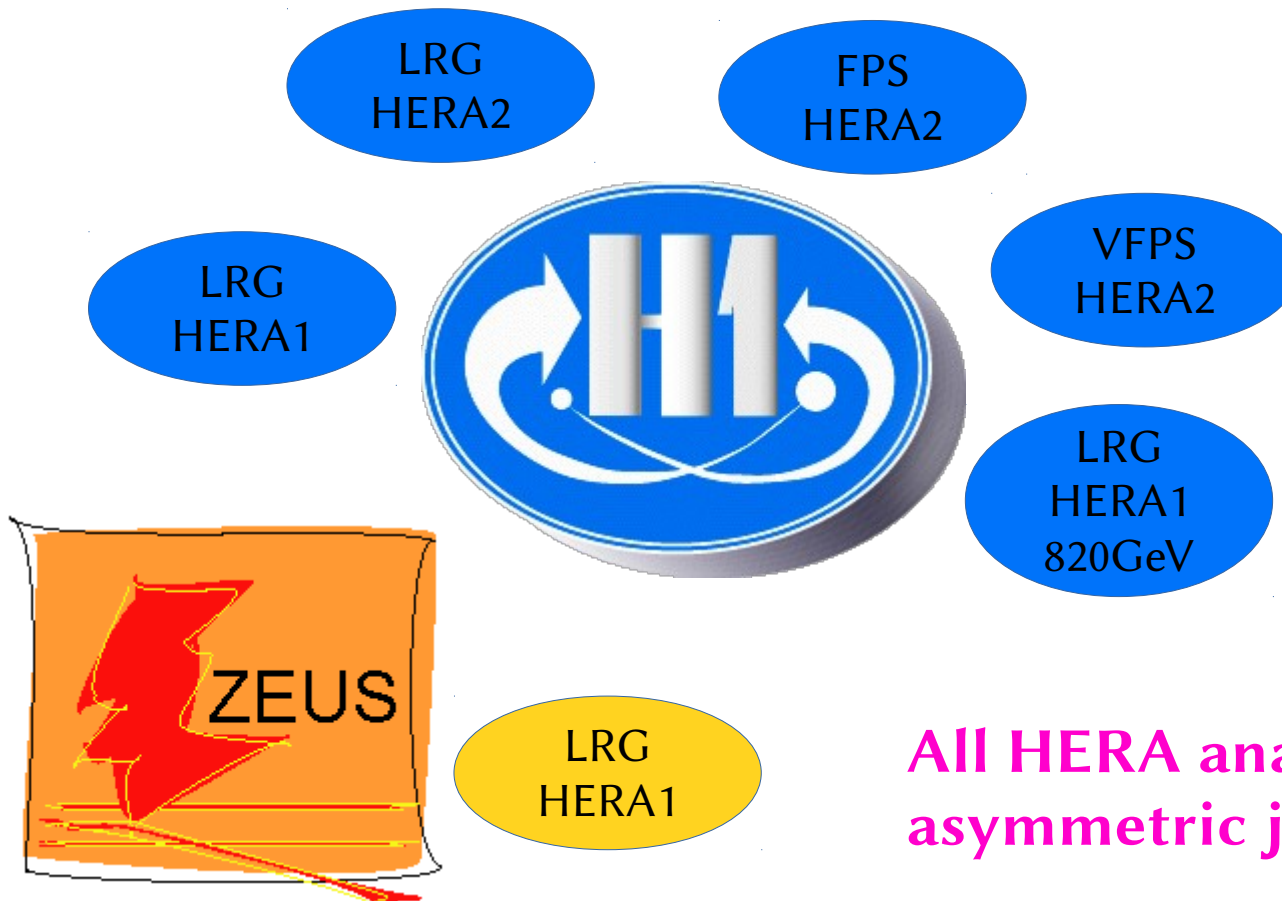
$$\alpha_s(M_Z) = 0.119 \pm 0.004(exp) \pm 0.012(DPDF, theo)$$

Factorisation holds in DDIS jets

The DIS dijets measurements

- 5times e+p 27.6 GeV + 920 GeV
1times e+p 27.5 GeV + 820 GeV
- 4times Large rapidity gap selection (LRG)
2times Proton spectrometer (FPS, VFPS)

H1 LRG HERA2 Phase Space
$4 < Q^2 < 100 \text{ GeV}^2$ $0.1 < y < 0.7$
$x_P < 0.03$ $ t < 1 \text{ GeV}^2$ $M_Y < 1.6 \text{ GeV}$
$p_{T,1}^* > 5.5 \text{ GeV}$ $p_{T,2}^* > 4.0 \text{ GeV}$ $-1 < \eta_{1,2}^{\text{lab}} < 2$

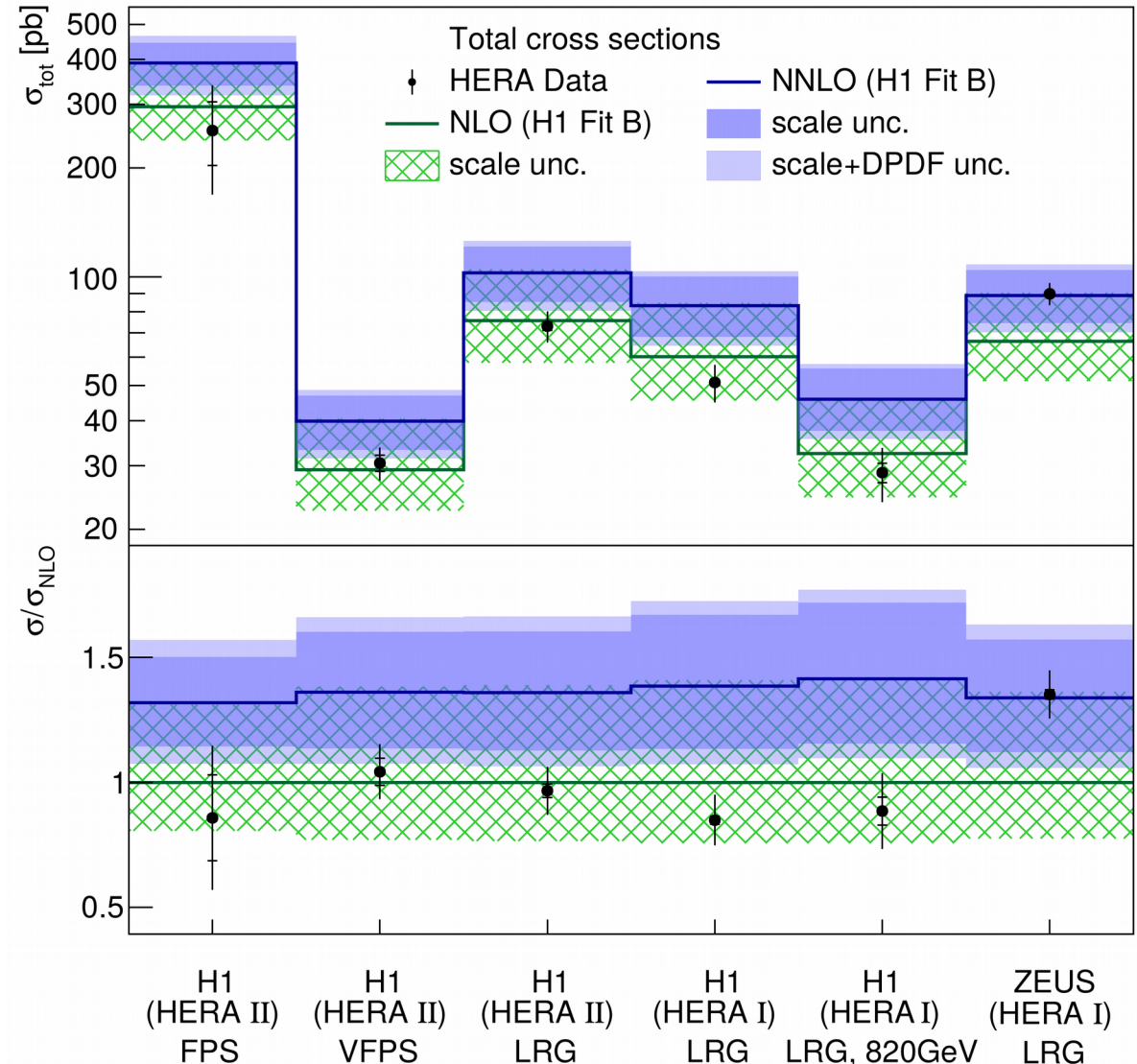


All HERA analyses with
asymmetric jet p_T cuts included

Total Cross Sections - NLO vs NNLO

- For NNLO the inner bar represents the scale uncertainty, the outer includes DPDF uncertainties
- Total cross sections well described by NLO
- NNLO predictions systematically overestimate the data with exception of ZEUS measurement

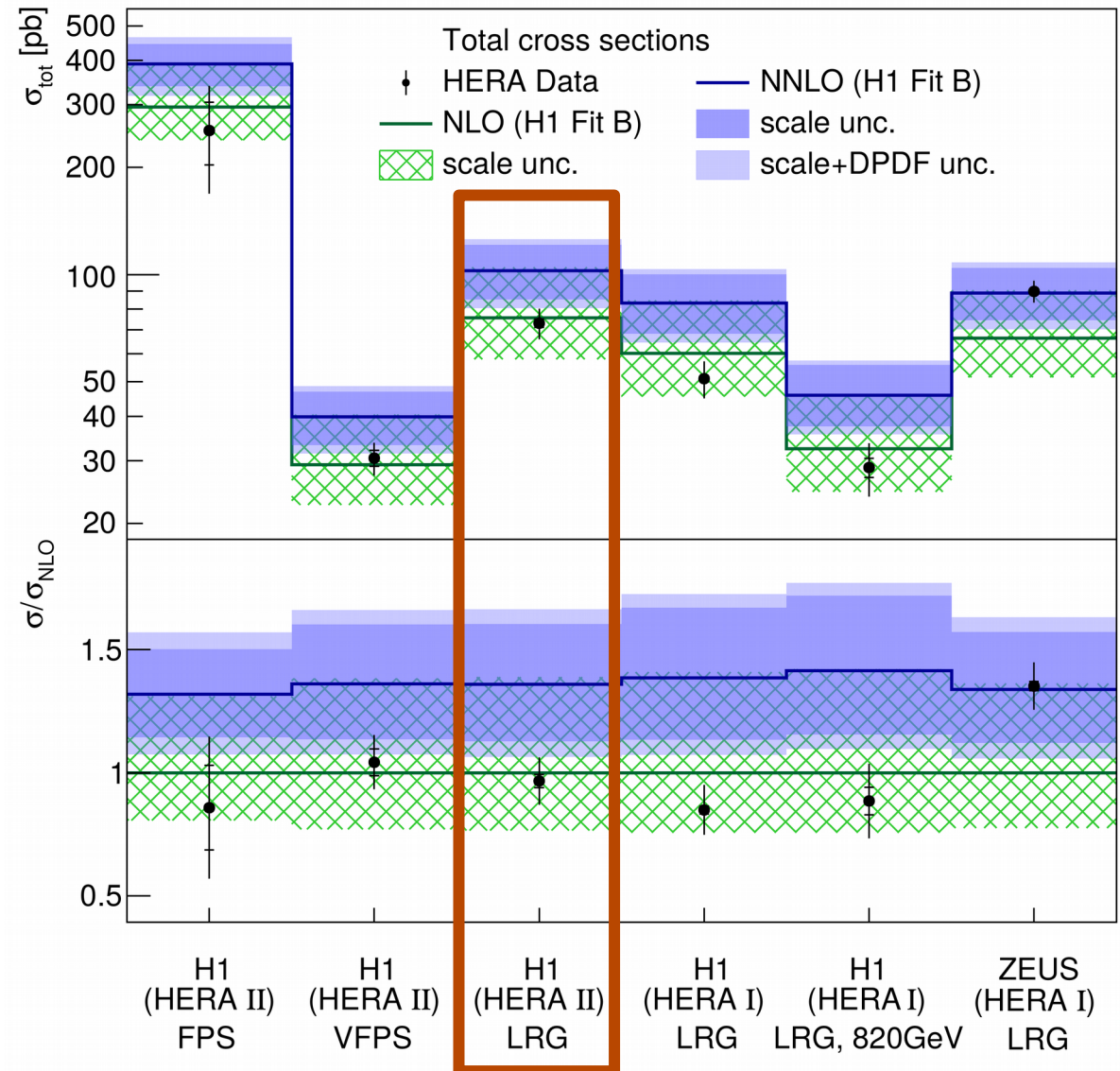
$$\mu_R^2 = \mu_F^2 = Q^2 + \langle p_T^{*\text{jets}} \rangle^2$$



Total Cross Sections - NLO vs NNLO

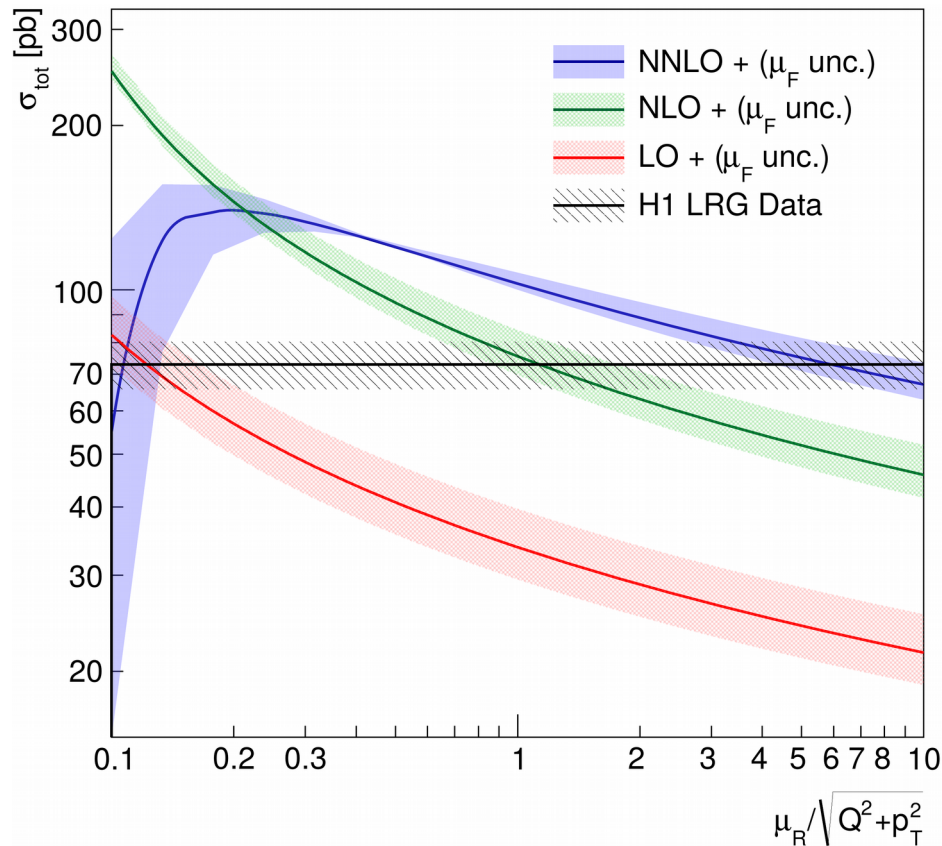
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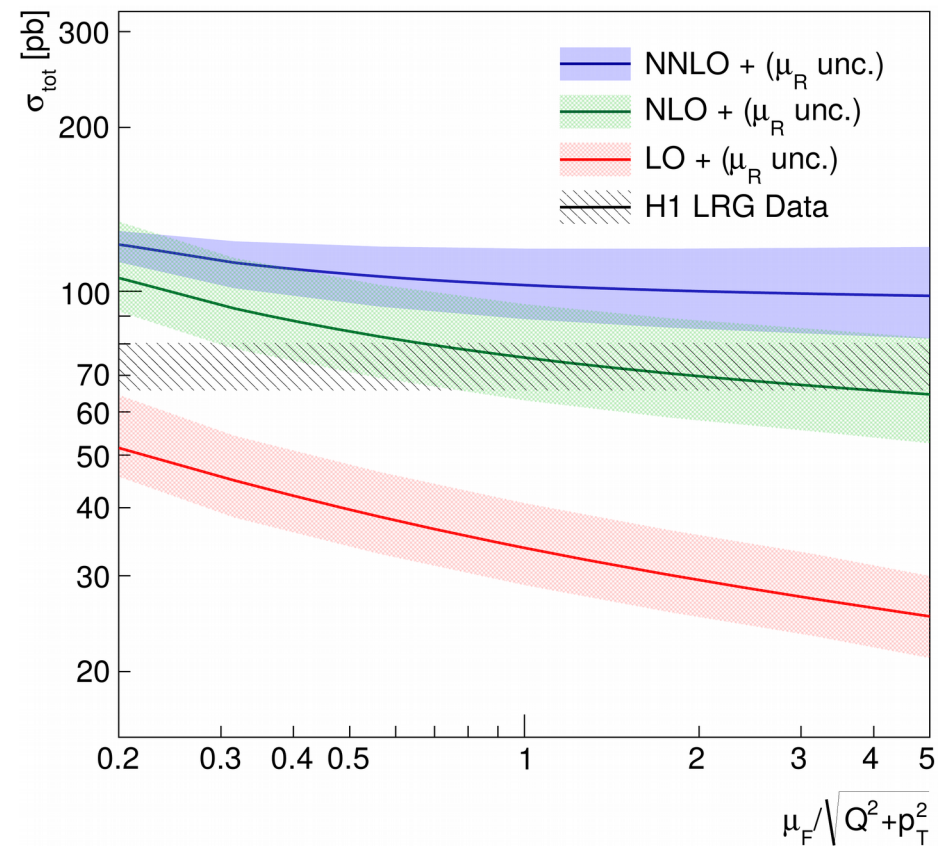
Total Cross Sections - Scale dependence

Renormalization scale dependence



- Comparable NLO and LO renormalization scale dependences (characteristic for gluon-dominated processes)
- NNLO has smaller renormalization scale dependence

Factorization scale dependence



- Factorization scale dependence lower with every order

Total Cross Sections - Scale dependence

- Four functional form of scales studied, everytime assumed:

$$\mu^2 = \mu_R^2 = \mu_F^2$$

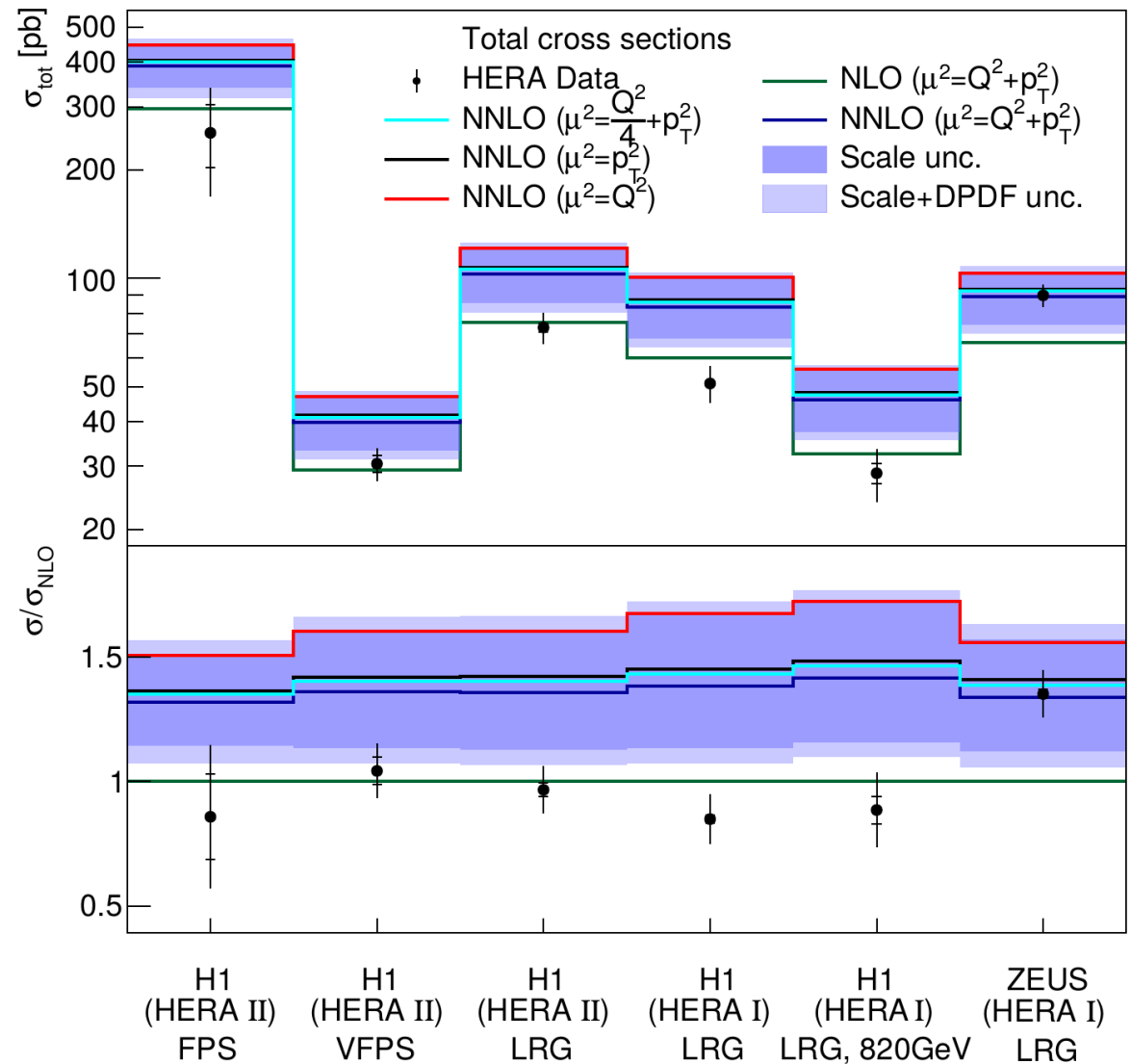
- Alternative parameterizations:

$$\mu^2 = Q^2 + \langle p_T^{*jets} \rangle^2$$

$$\mu^2 = \frac{Q^2}{4} + \langle p_T^{*jets} \rangle^2$$

$$\mu^2 = \langle p_T^{*jets} \rangle^2$$

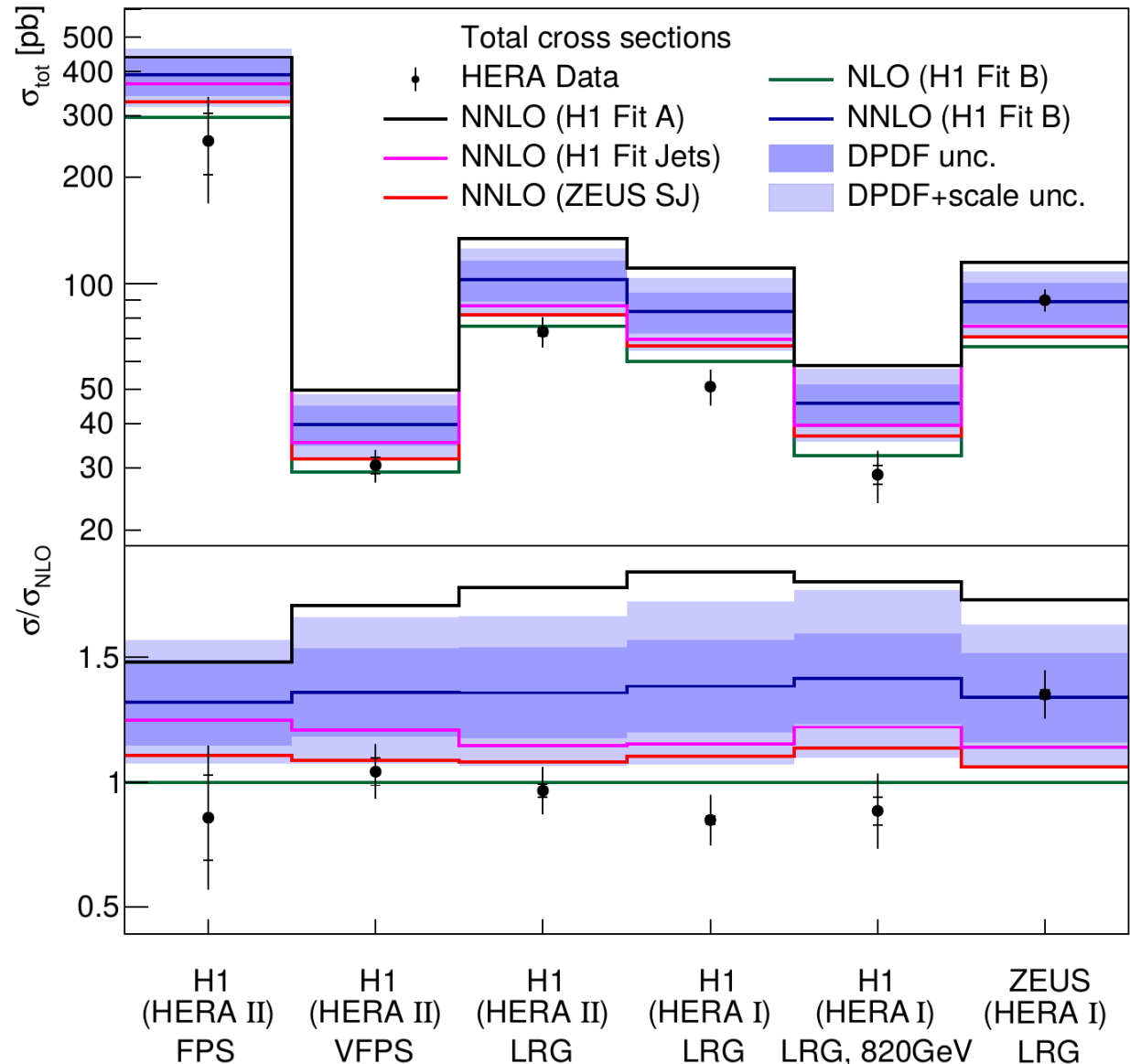
$$\mu^2 = Q^2$$



The p_T is the dominant term, if removed
the cross sections substantially higher

Total Cross Sections - DPDF dependence

- Inner bar represents the DPDF uncertainty, the outer includes scale uncertainties
- Combined fits of inclusive + dijet data
H1 Fitj Jets
ZEUS SJ
 perform best
- Inclusive data fits
H1 Fit A
H1 Fit B
 very different
 although for inclusive data had similar chi2

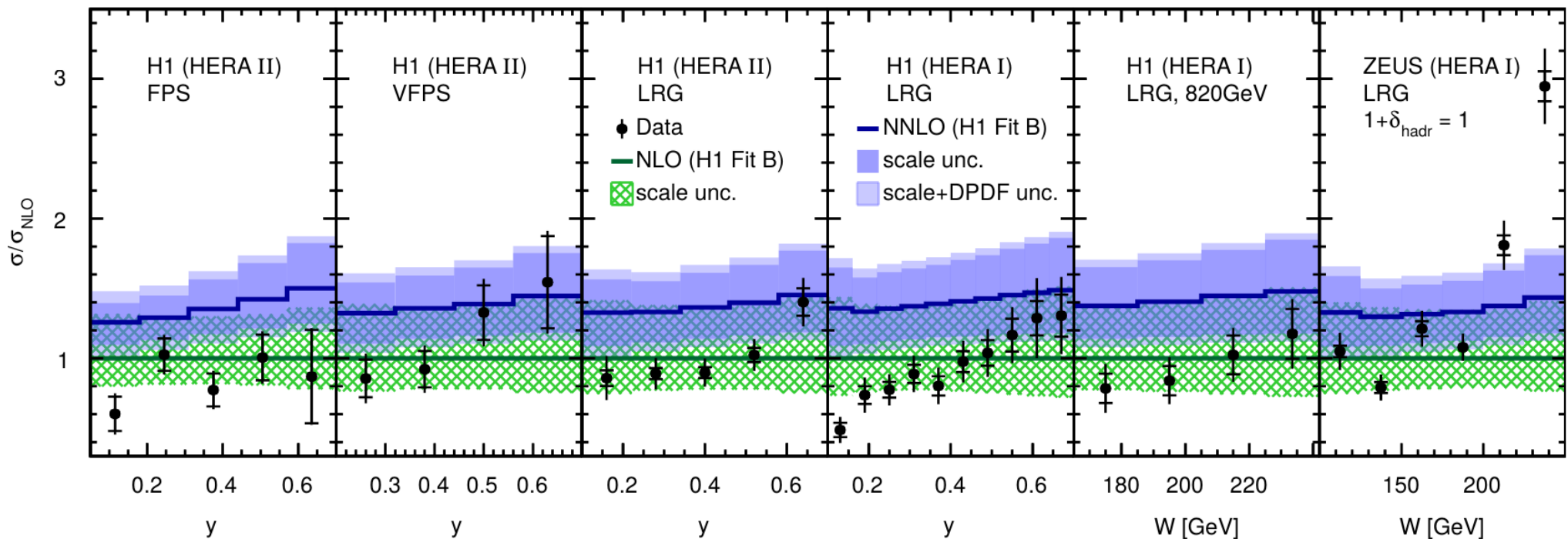
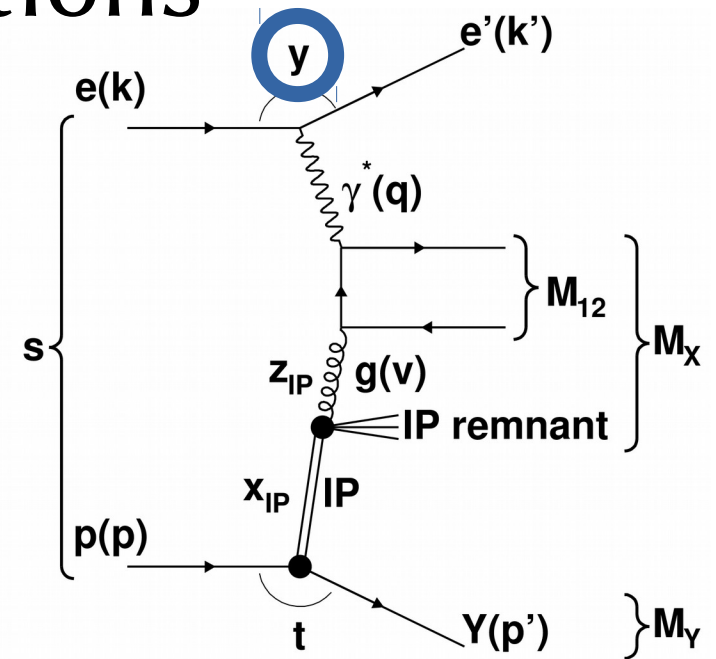


Studied differential distributions

Histogram	H1 HERA-II FPS	H1 HERA-II VFPS	H1 HERA-II LRG	H1 HERA-I LRG	H1 820 GeV LRG	ZEUS HERA-I LRG
Q^2	✓	✓	✓		✓	✓
$y [W]^*$	✓	✓	✓	✓	*	*
$p_{\text{T}}^{*,\text{jet1}} [p_{\text{T}}^{*,\text{jet}}]^*$	✓	✓	✓	✓	✓	*
$p_{\text{T}}^{*,\text{jet2}}$			✓			
$\langle p_{\text{T}} \rangle$			✓			
$\langle \eta_{\text{lab}}^{\text{jet}} \rangle [\eta_{\text{jet}}^*]^*$		✓			✓	*
$\Delta \eta_{\text{lab}}^{\text{jet}} [\Delta \eta^*]^*$	*	✓	*	*	*	
M_{X}^2		✓				✓
x_{IP}	✓	✓	✓	✓	✓	✓
z_{IP}	✓	✓	✓	✓		✓
$ t [\beta)]^*$	✓					*
x_{γ}						*
$(Q^2; p_{\text{T}}^{*,\text{jet1}})$			✓			
$(Q^2; z_{\text{IP}})$			✓			✓
$(Q^2 + (p_{\text{T}}^{*,\text{jet1}})^2; z_{\text{IP}})$				✓		
$(p_{\text{T}}^{*,\text{jet1}}; z_{\text{IP}})$						✓

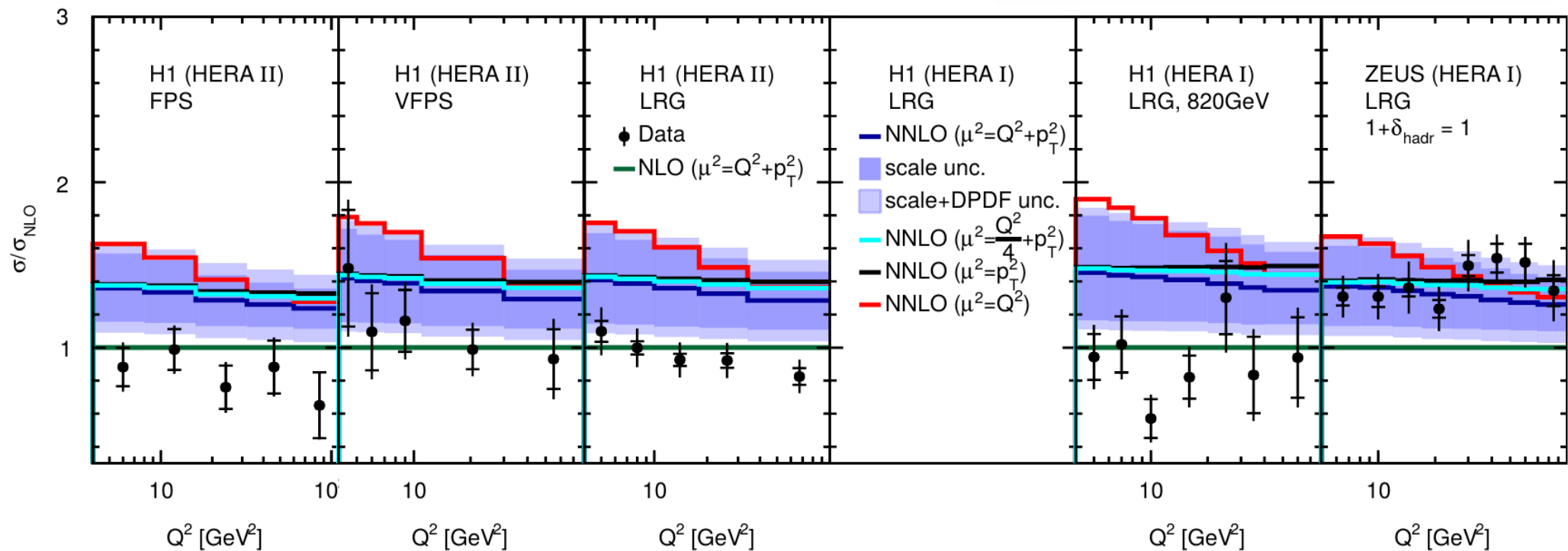
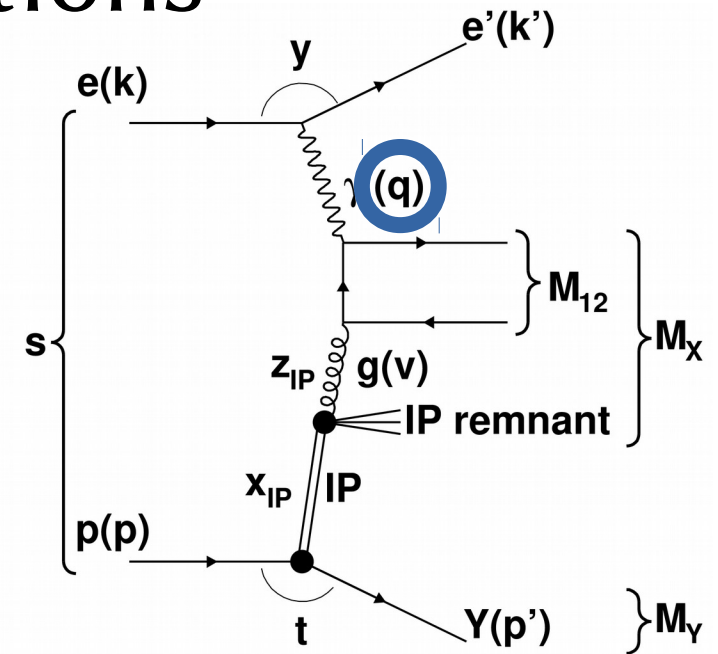
Differential x-sections

- The same or similar distributions from various analyses grouped into one plot, as shown bellow. In total **57 differential distributions** analyzed
- For inelasticity y NNLO higher for higher y
similar trend in data, note $W = \sqrt{ys}$



Differential x-sections

- The scale with **Q^2 term only** predict steeper Q^2 distribution
- Only small difference between other scale prescriptions
- No systematic trend in data

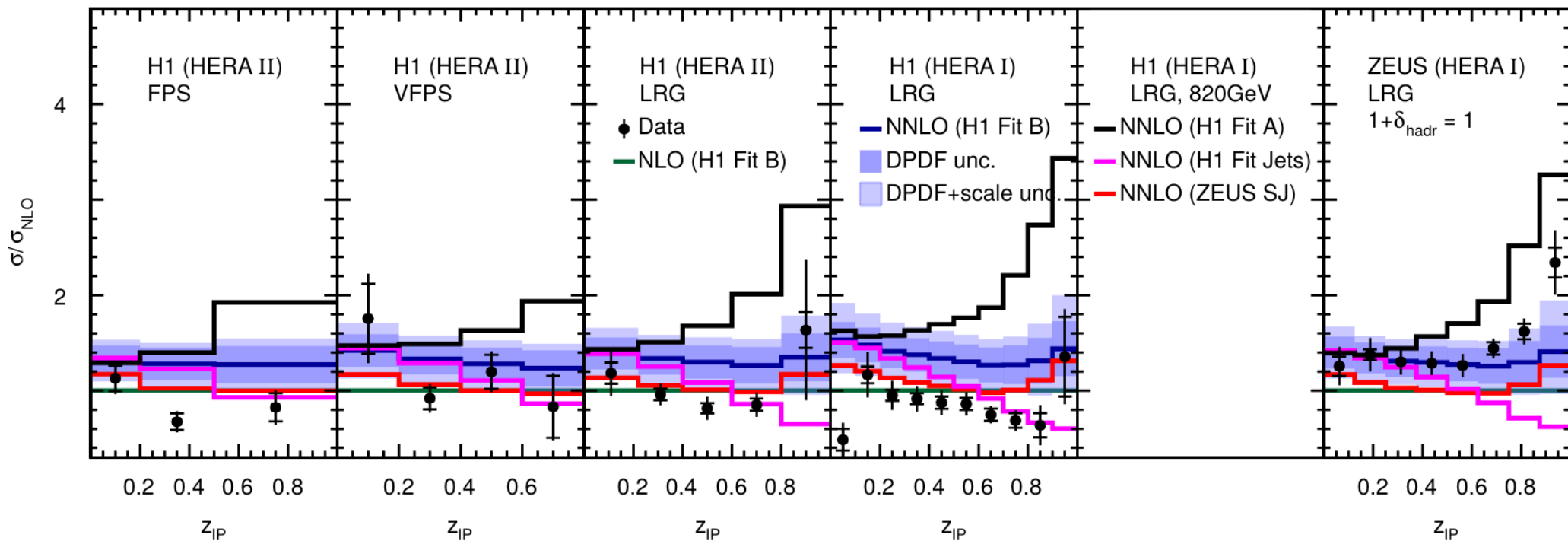
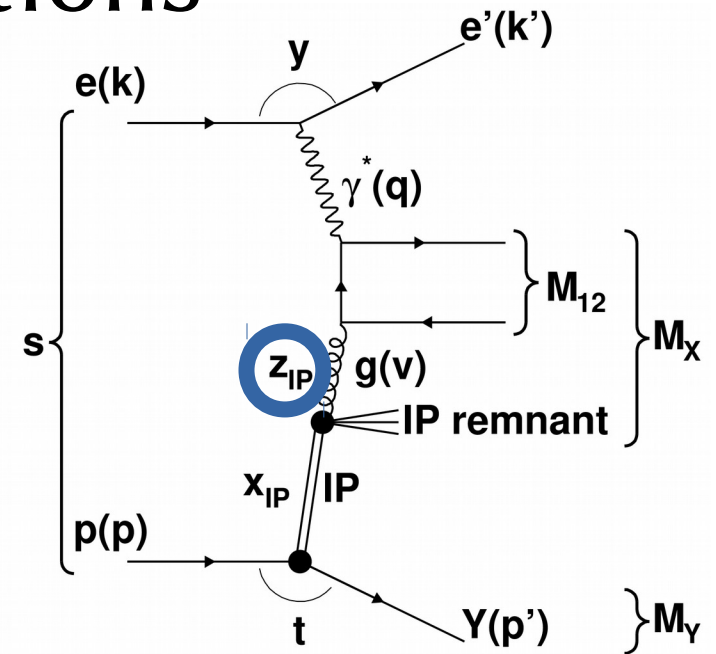


Differential x-sections

- Most sensitive variable to the partonic structure of the diffractive exchange (to DPDFs)
- NNLO predict an increase in the last bin for LRG analyses which is really seen in data

k_T -jet algorithm (R=1)

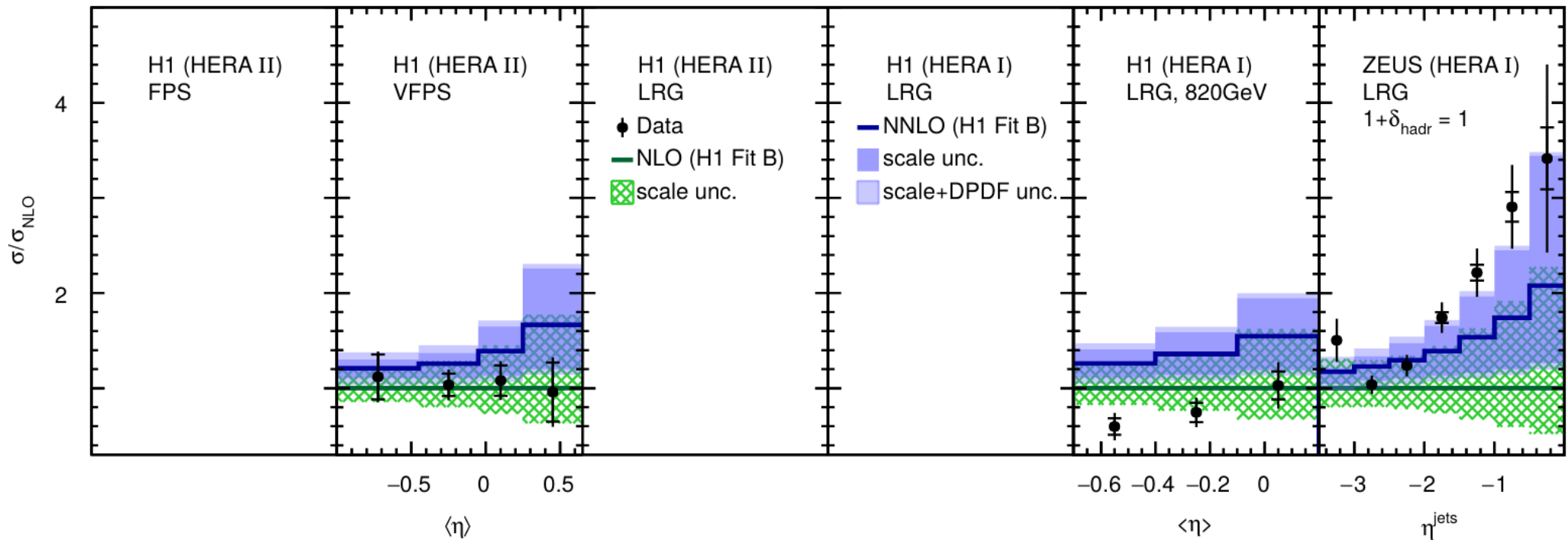
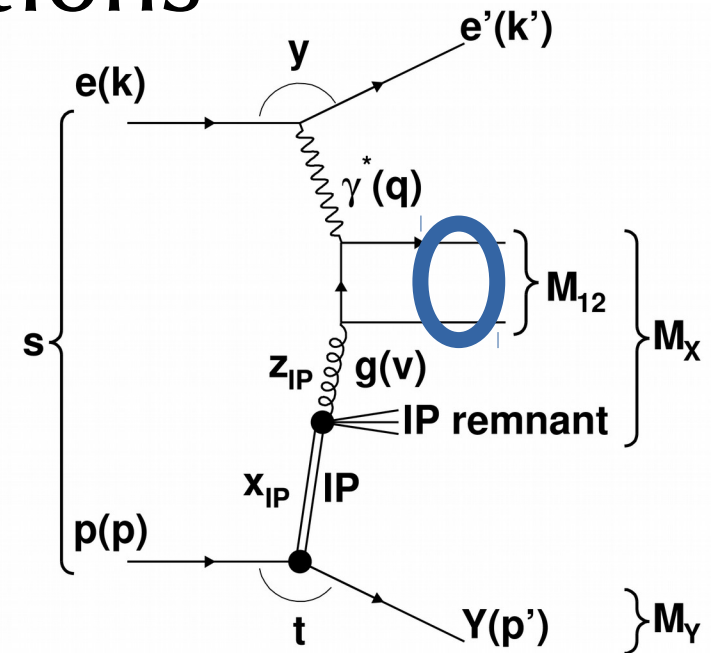
$$z_{IP} = \frac{M_{12}^2 + Q^2}{M_X^2 + Q^2}$$



Differential x-sections

- NNLO predicts more jets in the forward (=proton) direction
- The inclusive jet variable η^{*jets} filled for each jet in the event shows the biggest observed difference between NLO and NNLO - **factor 2!**

$$\langle \eta^{jets} \rangle = \frac{1}{2} (\eta^{jet1} + \eta^{jet2}) \quad \eta^{*jets} = \eta^{*jet1,2}$$



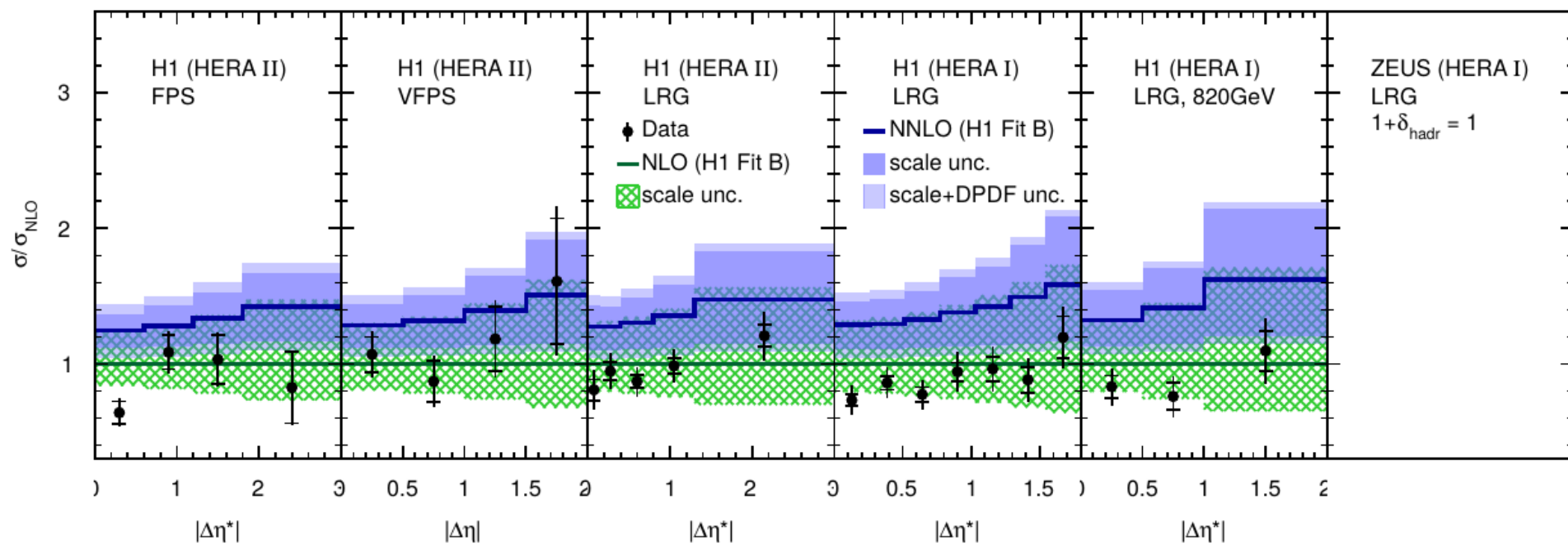
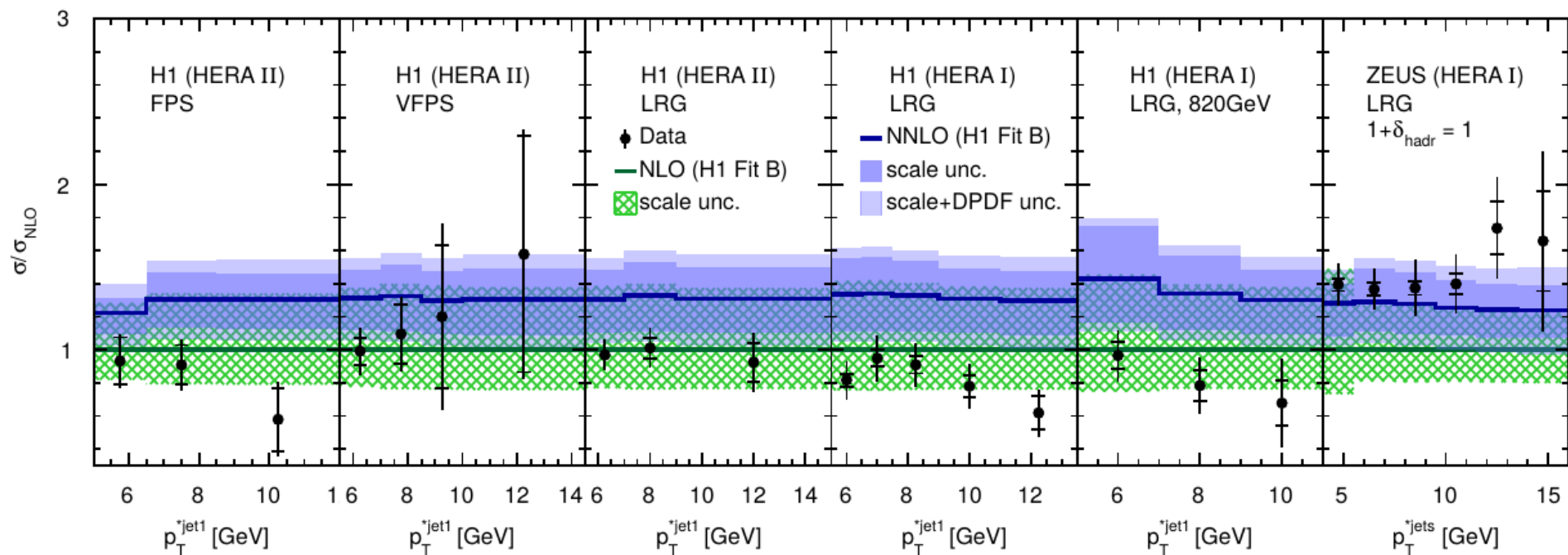
Conclusions

- Dijets in diffractive DIS calculated in **NNLO QCD for the first time**
- Differential distributions for various observables calculated
- The NNLO cross sections about $\sim 40\%$ higher than NLO
- The NNLO predictions overshoot the data for all H1 measurements and all studied DPDFs

Outlook

- Fit the inclusive and dijet diffractive DIS data at NNLO

Backup



Summary of experimental data set

Collab.	Diff. selection	\sqrt{s} [GeV]	\mathcal{L} [pb $^{-1}$]	Studied observables	DIS range	Dijet range	Diffraction range
H1 [3]	LRG	319	290 ($\sim 15000\text{ev}$)		$4 < Q^2 < 100 \text{ GeV}^2$ $0.1 < y < 0.7$	$p_{\text{T}}^{*,\text{jet}1} > 5.5 \text{ GeV}$ $p_{\text{T}}^{*,\text{jet}2} > 4.0 \text{ GeV}$ $n_{\text{jets}} \geq 2$ $-1 < \eta_{\text{lab}}^{\text{jet}} < 2$	$x_{\text{P}} < 0.03$ $ t < 1 \text{ GeV}^2$ $M_{\text{Y}} < 1.6 \text{ GeV}$
H1 [4]	VFPS	319	50 (550ev)		$4 < Q^2 < 80 \text{ GeV}^2$ $0.2 < y < 0.7$	$p_{\text{T}}^{*,\text{jet}1} > 5.5 \text{ GeV}$ $p_{\text{T}}^{*,\text{jet}2} > 4.0 \text{ GeV}$ $n_{\text{jets}} \geq 2$ $-1 < \eta_{\text{lab}}^{\text{jet}} < 2.5$	$0.010 < x_{\text{P}} < 0.024$ $ t < 0.6 \text{ GeV}^2$ $M_{\text{Y}} = m_{\text{P}}$
H1 [5]	FPS	319	156.6 (581ev)		$4 < Q^2 < 110 \text{ GeV}^2$ $0.05 < y < 0.7$	$p_{\text{T}}^{*,\text{jet}1} > 5 \text{ GeV}$ $p_{\text{T}}^{*,\text{jet}2} > 4.0 \text{ GeV}$ $n_{\text{jets}} \geq 2$ $-1 < \eta_{\text{lab}}^{\text{jet}} < 2.5$	$x_{\text{P}} < 0.1$ $ t < 1 \text{ GeV}^2$ $M_{\text{Y}} = m_{\text{P}}$
H1 [6]	LRG	319	51.5 (2723ev)		$4 < Q^2 < 80 \text{ GeV}^2$ $0.1 < y < 0.7$	$p_{\text{T}}^{*,\text{jet}1} > 5.5 \text{ GeV}$ $p_{\text{T}}^{*,\text{jet}2} > 4.0 \text{ GeV}$ $n_{\text{jets}} \geq 2$ $-3 < \eta^{*\text{jets}} < 0$	$x_{\text{P}} < 0.03$ $ t < 1 \text{ GeV}^2$ $M_{\text{Y}} < 1.6 \text{ GeV}$
H1 [7]	LRG	300	18 (322ev)		$4 < Q^2 < 80 \text{ GeV}^2$ $165 < W < 242 \text{ GeV}$	$p_{\text{T}}^{*,\text{jet}1} > 5 \text{ GeV}$ $p_{\text{T}}^{*,\text{jet}2} > 4.0 \text{ GeV}$ $n_{\text{jets}} \geq 2$ $-1 < \eta_{\text{lab}}^{\text{jet}} < 2$ $-3 < \eta^{*\text{jets}} < 0$	$x_{\text{P}} < 0.03$ $ t < 1 \text{ GeV}^2$ $M_{\text{Y}} < 1.6 \text{ GeV}$
ZEUS [8]	LRG	319	61 (5539ev)		$5 < Q^2 < 100 \text{ GeV}^2$ $100 < W < 250 \text{ GeV}$	$p_{\text{T}}^{*,\text{jet}1} > 5 \text{ GeV}$ $p_{\text{T}}^{*,\text{jet}2} > 4.0 \text{ GeV}$ $n_{\text{jets}} \geq 2$	$x_{\text{P}} < 0.03$ $ t < 1 \text{ GeV}^2$ $M_{\text{Y}} = m_{\text{P}}$