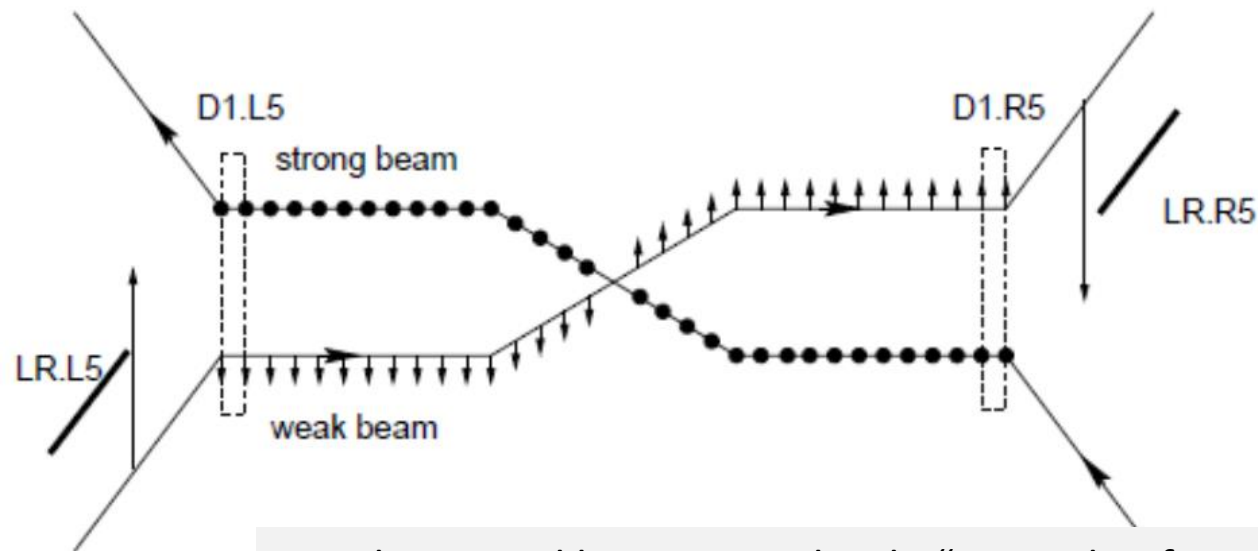


# Potential of wire compensation for (HL-)LHC & Optimal optics and hardware conditions

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Initial proposal by J.P. Koutchouk, "Principle of a Correction of the Long-Range Beam-Beam Effect in LHC Using Electromagnetic Lenses", LPN 223, 2000

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# Introduction to flat Optics and potential of wire compensation

- Flat optics (not flat beams!) means

$$\varepsilon_x \sim \varepsilon_y \sim \varepsilon \text{ but } \beta_x^* \equiv \sqrt{r} \beta^* \text{ and } \beta_y^* \equiv \beta^* / \sqrt{r} \text{ with } r \neq 1, \text{ typically 3 to 4 in LHC}$$

- The Xing plane is always the plane of largest  $\beta^*$  (i.e. smallest  $\beta$  in the triplet)
  - To preserve/gain aperture in the triplet** (smaller X-angle requested, and better matching between beam-screen and beam aspect ratio for LHC, see later)
  - To gain in luminosity** (geometric loss factor closer to unity)

$$L(r, \beta^*) = \frac{L_0}{\sqrt{1 + \frac{1}{r} \times \left( \frac{\alpha \sigma_z}{2\beta^*} \right)^2}}$$

$L_0$ : Luminosity calculated for head-on colliding round beams  
 $\frac{\alpha \sigma_z}{2\beta^*}$ : Full normalized X-angle (9-10  $\sigma$  for LHC, up to 12.5  $\sigma$  for HL-LHC with more current and longer triplet with more LR's)  
 $\sigma_z$ : r.m.s. bunch length (7.5 cm nominally but 9-10 cm in practice for various reasons)  
 $\beta^* \equiv \sqrt{\beta_x^* \times \beta_y^*}$  (30 - 40 cm for LHC, 10 - 20 cm for HL - LHC)  
 $r$  the beta\* aspect ratio (defined as  $\beta_x^* / \beta_y^* \geq 1$ )

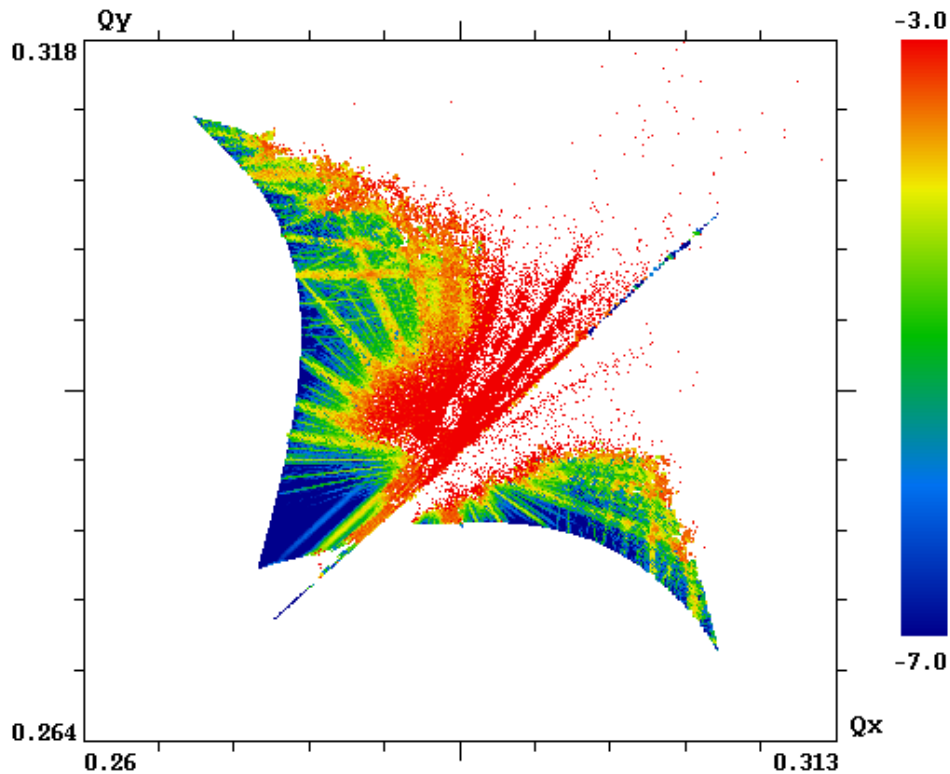
→ Increasing the beta\* aspect ratio **could in principle** rapidly mitigate the geometric luminosity loss w/o need of crab-cavities  
 → But w/o dedicated action, the **normalised X-angle should unfortunately as well increase with the beta\* aspect ratio ...**

# Introduction to flat optics and potential of wire compensation

- Flat optics example:

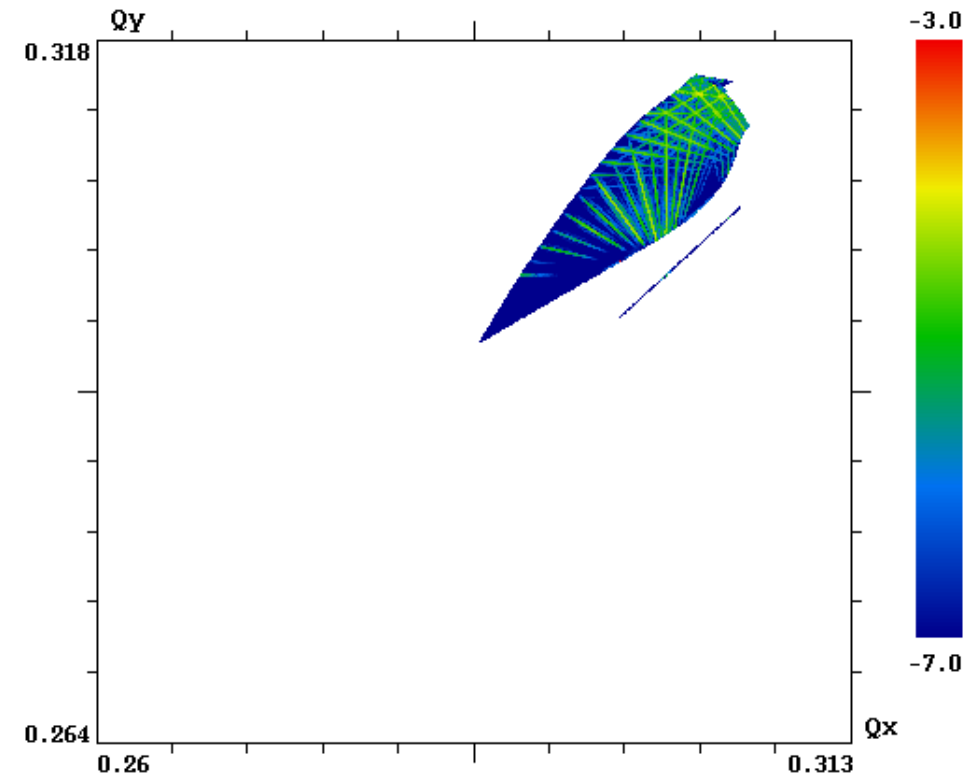
**HL-LHC plan B for  $10^{35}$  virtual luminosity w/o crab-cavities** (HL-LHC Coordination Group, May 2013, and *PRSTAB 18-121001, 2015*)

→  $\beta^* = 40/10$  cm at IP1&5 (i.e.  $r=4$ ),  $\Theta_c = 300$   $\mu$ rad, i.e. about halved vs. baseline but still  $10.5 \sigma$  at  $\beta^* = 40$  cm in the X-plane, no collision at full current in 3 IPs



A "monster" before correction  
( $\Delta Q_{ho} = 0.025$ ,  $\Delta Q_{LR} = 0.015$ )

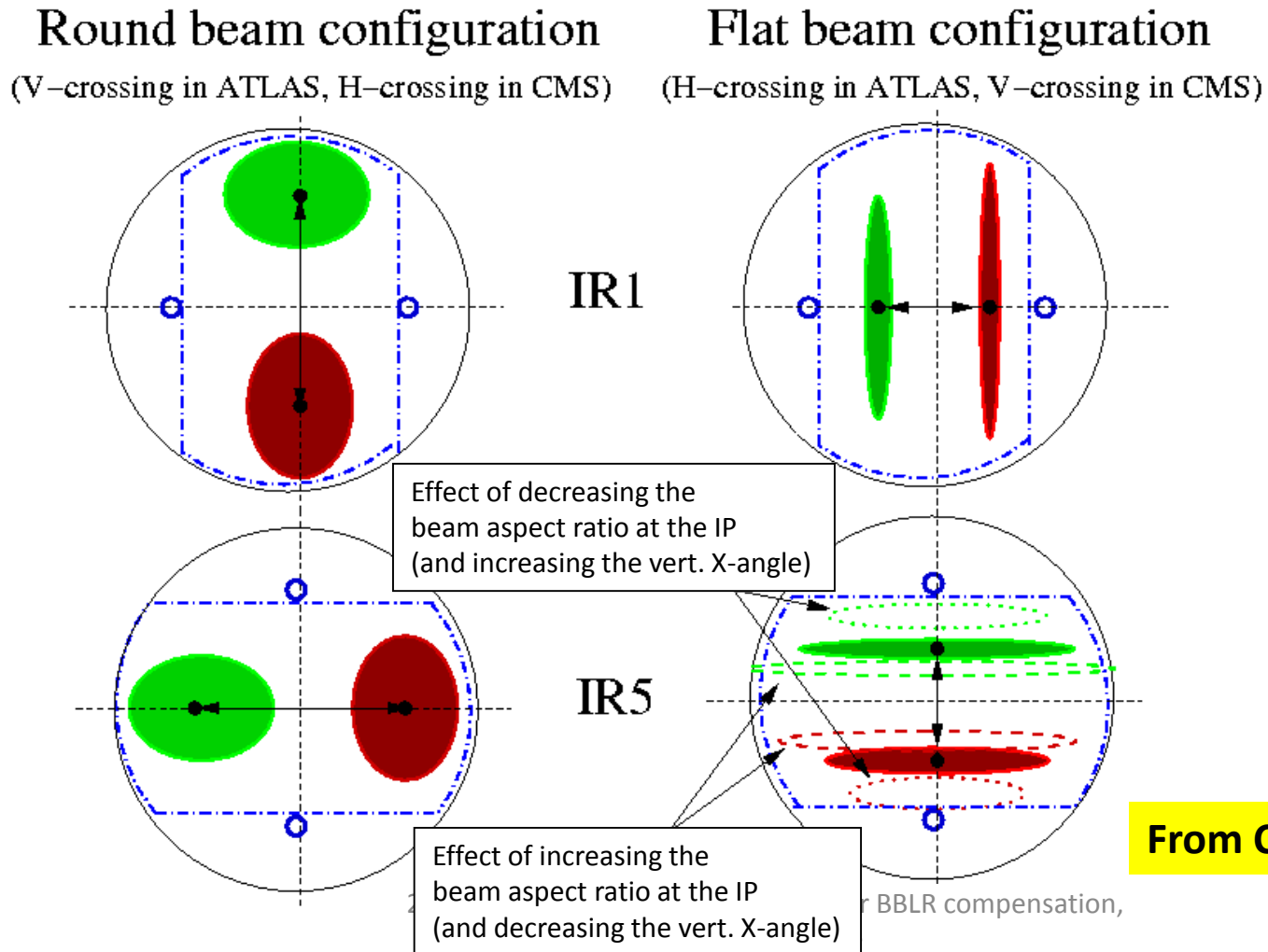
2nd Workshop on w



A regular HO footprint after correction ( $\Delta Q_{ho} = 0.025$ ,  $\Delta Q_{LR} = 0.0$ )  
with wire installed at optimal position (see later)

# Introduction to flat optics and potential of wire compensation

- **Competitive flat optics in LHC** (e.g. 80/20 instead of 40/40, or 60/15 instead of 30/30) requires to **change the crossing plane orientation** (IT aperture), hence installing **the wires in the right plane!**.. (see later possible “oval” optics)

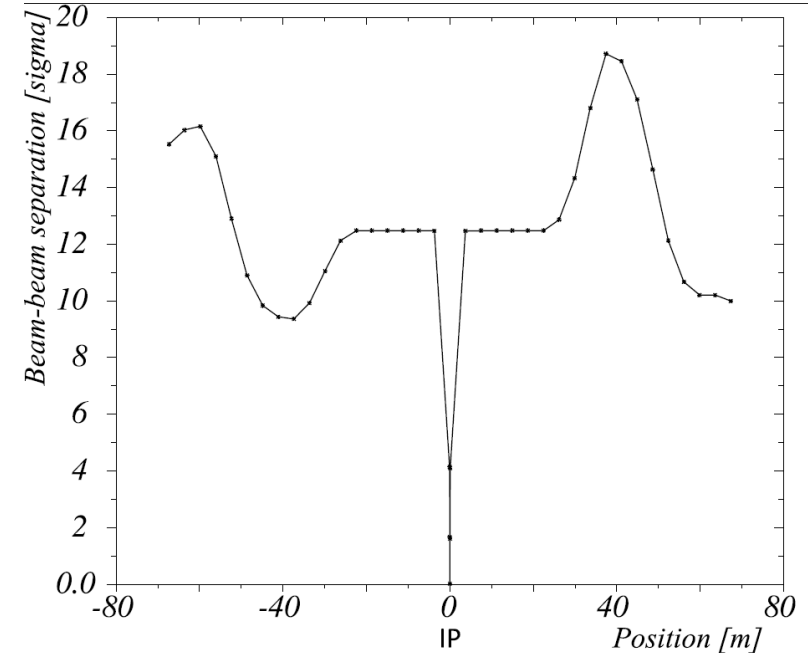


From CERN MAC, 2006

# Principle of the wire correction and wire specification

- **Many questions with non-obvious answers**

- 1) With only 2 wires left/right the IP, can we properly compensate 15-20 LR encounters taking place at **non uniform normalized beam-beam separation**?
- 2) If yes, can we build an **automatic tool for setting generation** (transverse position and current) working for arbitrary optics (flat or round) and crossing angle ?
- 3) Are there any preferences (based on beam dynamics criteria) where to install the wire, i.e. at **which  $\beta$ -function aspect ratio** ? Is an aspect ratio of 1 really the optimal choice as thought in the initial proposal?



**HL-LHC: Normalized beam-beam separation for 590  $\mu$ rad full crossing angle ( $12.5 \sigma$ ) at  $\beta^*=15$  cm (7 TeV,  $\gamma\epsilon=2.5$  mrad)**

# Principle of the wire correction and wire specification

- **Beam-beam long-range multipole expansion**

Working in complex coordinates is the right thing to do:

$z \equiv x + i y$  : transverse coordinate of the test particle wrt the centroid of the weak beam

$z_0 \equiv x_0 + i y_0$ : relative centroid position of the strong beam wrt the weak beam

... And assuming  $|z| \ll |z_0|$

$$\int ds [B_y + i B_x]_{\text{eq}} = - \frac{\mu_0 \overbrace{(\widehat{Qc})}^{\equiv [IL]_{\text{eq}}}}{2\pi} \times \frac{1}{z-z_0} \rightarrow B_k + i A_k = \frac{\mu_0 [IL]_{\text{eq}}}{2\pi} \times \frac{1}{z_0^k}$$
$$\equiv \sum_{k=1}^{\infty} [B_k + i A_k] z^{k-1}$$

$$[IL]_{\text{eq}} = 10.56 \text{ A.m / LR for the HL-LHC beam (2.2E11)}$$

$$[IL]_{\text{eq}} = 5.76 \text{ A.m /LR for the LHC BCMS beam (1.2E11)}$$

**90 A.m would have been fully OK for LHC (15 LRs/IP side), about 200 A.m for HL-LHC (18-19 LRs/IP side) ... The TCTW has been designed for 350 A ??**

# Principle of the wire correction and wire specification

$$B_k + i A_k = \frac{\mu_0 [IL]_{eq}}{2\pi} \times \frac{1}{z_0^k}$$

1. H crossing ( $z_0 = x_0$  real) induces only normal harmonics ( $A_k=0$ ).
2. V crossing ( $z_0 = iy_0$  purely imaginary) induces both skewed harmonics when  $k$  is odd ( $B_{2k+1}=0$ ) and normal harmonic when  $k$  is even ( $A_{2k}=0$ ).
3. An **alternated HV Xing scheme in 2 low- $\beta$  IRs with identical round optics** compensates all  $(4n + 2)$ -pole tune shift and tune spread ( $B_2, B_6, \dots$ ) but combine additively the  $(4n)$ -pole tune spread ( $B_4, B_8, \dots$ ). ...That is why the LR tune spread is close to that of a **pure octupole in the LHC**, and was easy to compensate with octupole magnets, at least at 4 TeV ....
4. The compensation is only **partial for alternated HV Xing in 2 low- $\beta$  IR's with flat optics of aspect ratio  $r$  and  $1/r$**



# Principle of the wire correction and wire specification

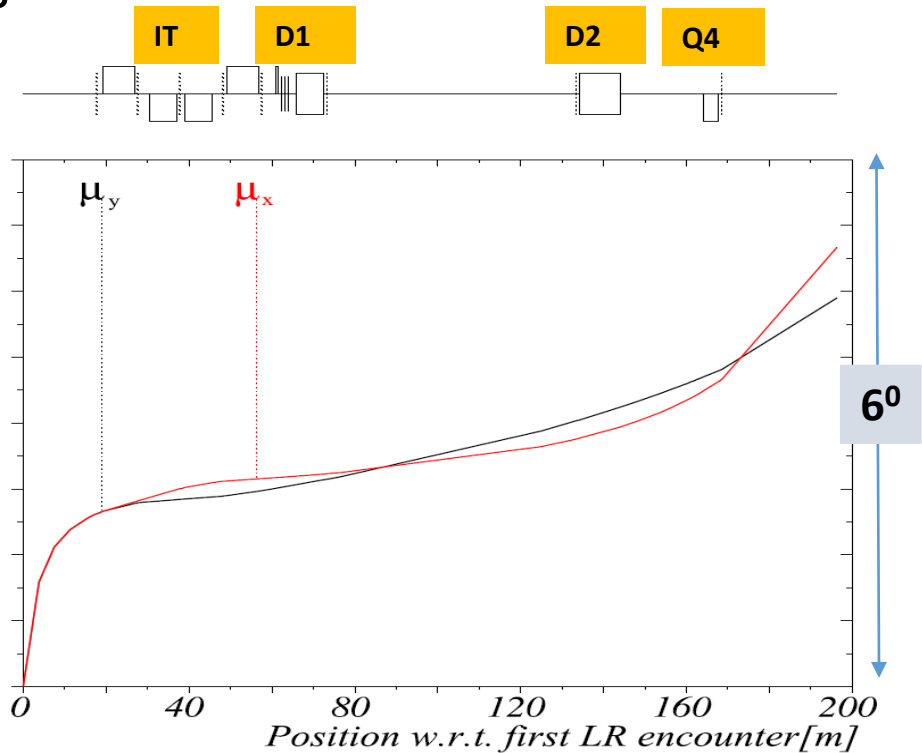
- Resonance Driving Terms (RDT) from the LR interactions in H or V crossing**

... neglecting the small phase shift between wires and LRs

$$C_{pq}^{LR} \propto \sum_{k \in LR} \frac{\beta_{x,k}^{|p|/2} \beta_{y,k}^{|q|/2}}{d_{bb,k}^{|p|+|q|}}$$

with p (resp. q) even for H (resp. V) crossing, and  $d_{bb,k}$  the (non-normalized) beam-beam distance (taken positive) at the  $k^{\text{th}}$  encounter.

→ The detuning terms (footprint) are non-zero only when both p and q are even, and are equal to the corresponding driving terms.



**Betatron phases  $[2\pi]$  w.r.t. the first LR encounter**  
**For Typical optics at  $\beta^*=15$  cm (HL-LHC)**  
 → A few degrees till Q4  
 → But rapid degradation of the situation for  $\beta^* > 50$  cm-1 m

# Principle of the wire correction and wire specification

## • RDTs from the wire

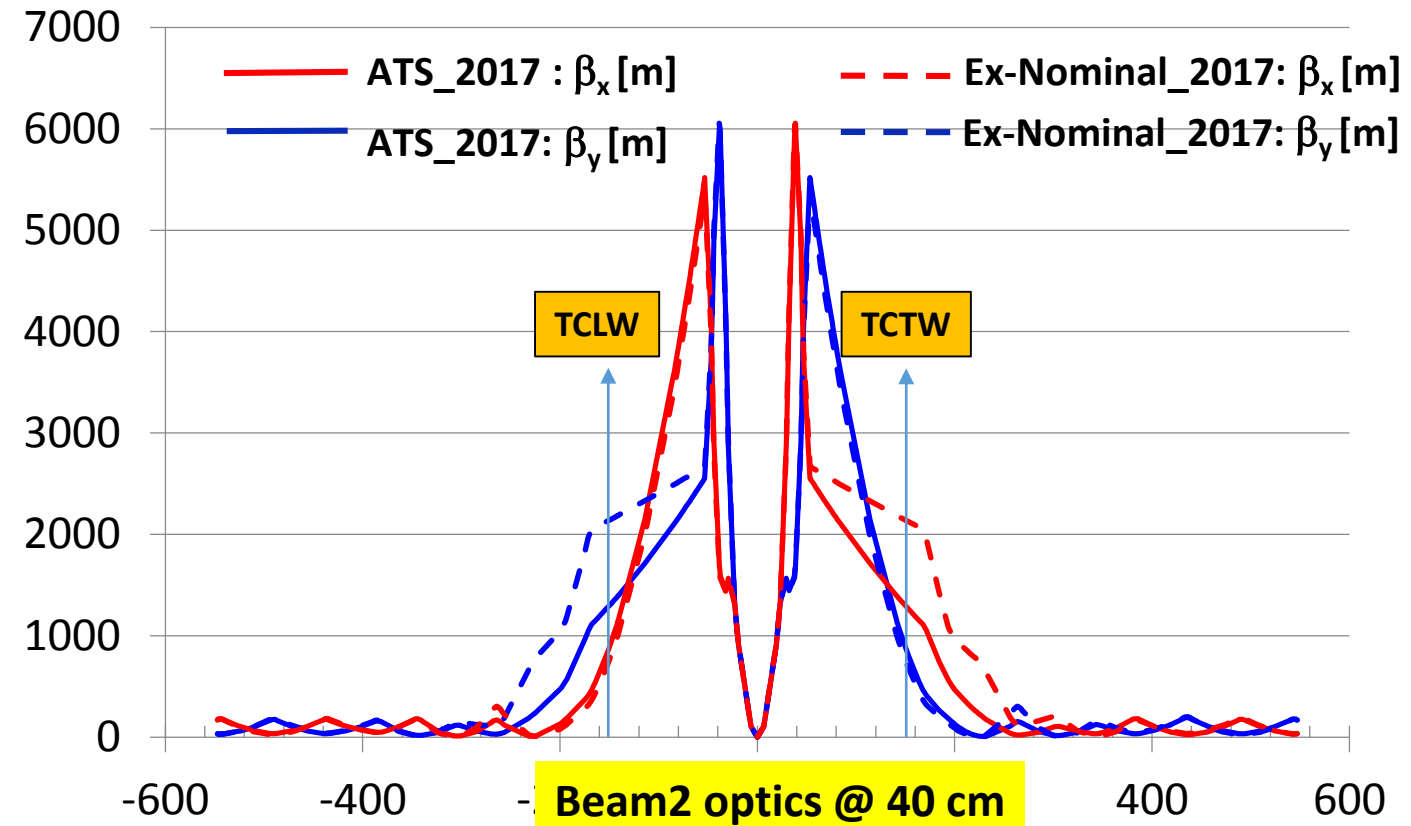
$$c_{pq}^w \propto N_w \times \frac{\frac{|p|-|q|}{r_w^4}}{\left(d_w / \sqrt[4]{\beta_{x,w}\beta_{y,w}}\right)^{|p|+|q|}}$$

$d_w$  : (non-normalized) distance of the wire  
w.r.t. the weak beam

$N_w$  : integrated current expressed in terms  
of equivalent number of LR encounters

$r_w$  :  **$\beta$ -function aspect ratio at the wire ( $\beta_x/\beta_y$ )**

→ The actual product of the  $\beta$ 's at the wire is not relevant (can be absorbed in rescaling  $d_w$ ), **only the  $\beta$  aspect ratio is important, which can be eventually (re-)adjusted with the triplet settings**



Optics type @ 40 cm	ATS 2016	Nominal 2016	ATS 2017 (new nominal 2017)	“ex-Nominal 2017”
$\beta_{x(y)}$ [m] at TCT (TCL)	1654 (1645)	2149 (2144)	<b>1314 (1302)</b>	2149 (2144)
$\beta_{y(x)}$ [m] at TCT (TCL)	966 (935)	800 (772)	<b>932 (901)</b>	800 (772)
$r_w$ at TCT (TCL)	<b>1.71 (1.76)</b>	2.68 (2.78)	<b>1.41 (1.44)</b>	2.68 (2.78)

# Principle of the wire correction and wire specification

- Correction algorithm:

With 2 knobs (1 wire/beam/ IP-side assumed to be symmetric w.r.t. the IP), only 2 or 4 RDT's can be a priori fully corrected:

→  $(c_{p_1 q_1}^{LR}, c_{p_2 q_2}^{LR})$  and  $(c_{q_1 p_1}^{LR}, c_{q_2 p_2}^{LR})$  by symmetry with left & right wires at the same physical transverse distance w.r.t. the beam and at the same current

For round optics

$$\left\{ \begin{aligned} d_{w.L} = d_{w.R} = d_w &\equiv \sqrt{\beta_{eq}^w} \times \left[ \frac{c_{p_1 q_1}^{LR} \frac{p_2 - q_2}{r_w^4} + \frac{q_2 - p_2}{r_w^4}}{c_{p_2 q_2}^{LR} \frac{p_1 - q_1}{r_w^4} + \frac{q_1 - p_1}{r_w^4}} \right]^{\frac{1}{p_2 + q_2 - p_1 - q_1}} \\ N_{w.L} = N_{w.R} = N_w &\equiv \frac{\left( c_{p_1 q_1}^{LR} \right)^{p_2 + q_2} \left( \frac{p_2 - q_2}{r_w^4} + \frac{q_2 - p_2}{r_w^4} \right)^{p_1 + q_1}}{\left( c_{p_2 q_2}^{LR} \right)^{p_1 + q_1} \left( \frac{p_1 - q_1}{r_w^4} + \frac{q_1 - p_1}{r_w^4} \right)^{p_2 + q_2}} \cdot \frac{1}{p_2 + q_2 - p_1 - q_1} \end{aligned} \right.$$

...which is independent of  $\beta^*$  !

For flat optics of sufficiently small  $\beta^*$  in both planes, these settings are still optimal for the 2 RDT's considered, but the residuals of the other RDT's remains in general optics dependent.

# Disclaimer

The following does not treat the **compromise case of only one driving term compensated**, as e.g. the octupolar term, where the wire can be at any distance from the beam, provided enough current is available

→ **See talk by A. Valishev** (for the very promising results already obtained in this case)

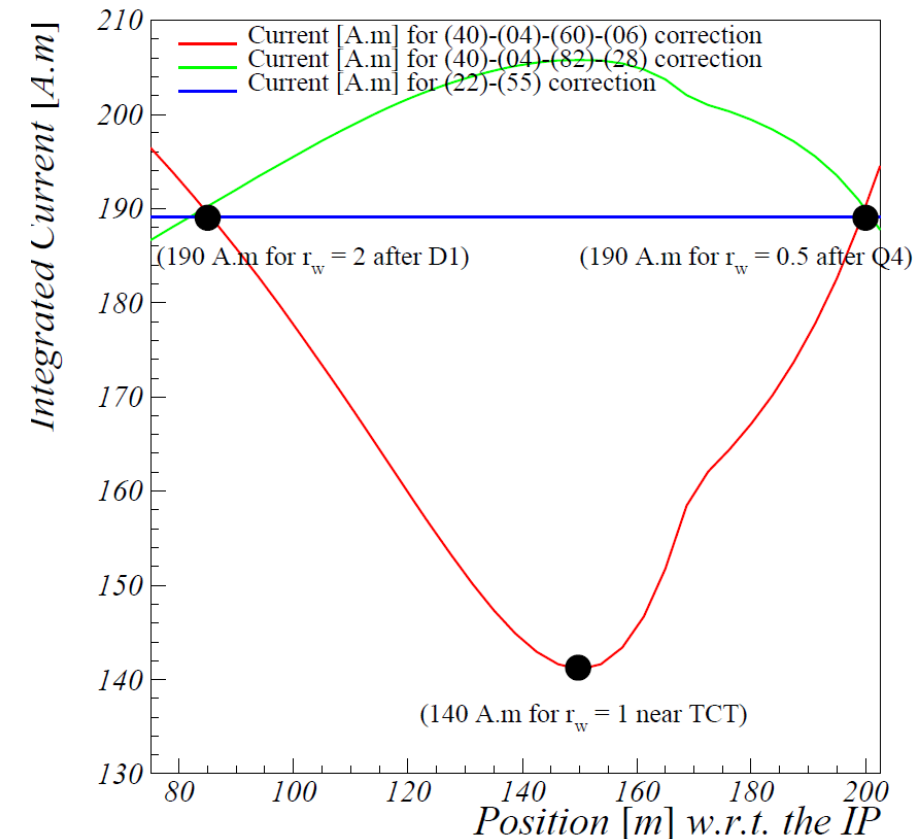
# Principle of the wire correction and wire specification

- Integrated current vs. wire positioning (HL-LHC simulations)

→ 3 correction types tested

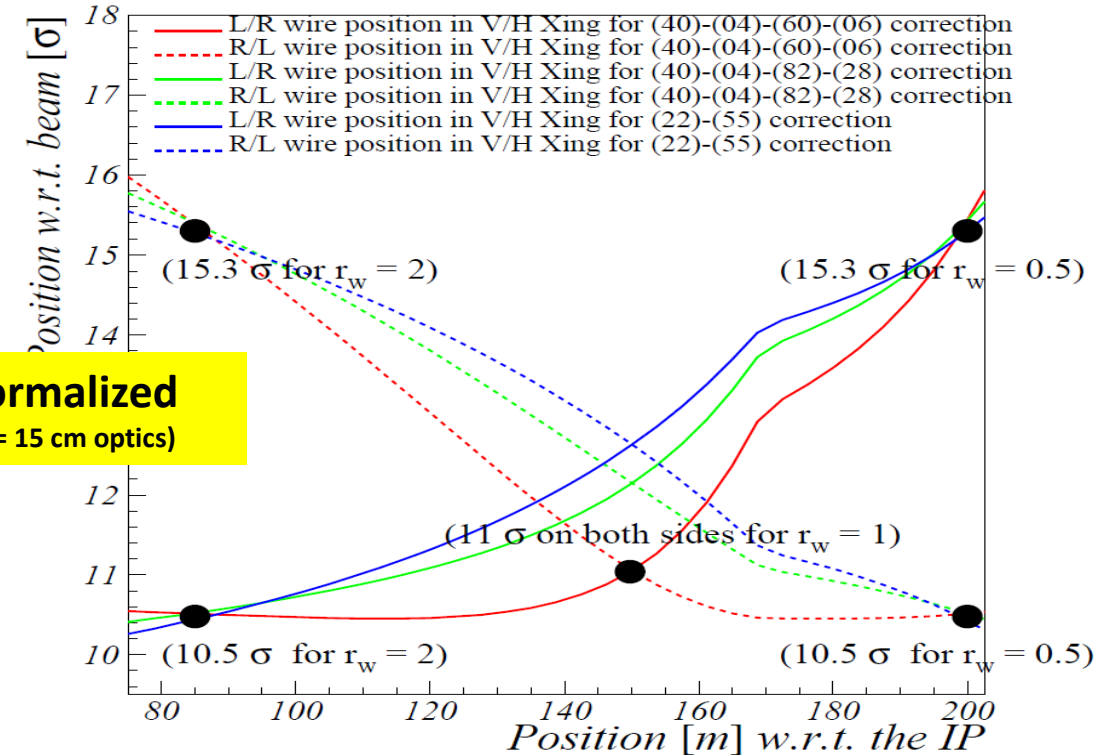
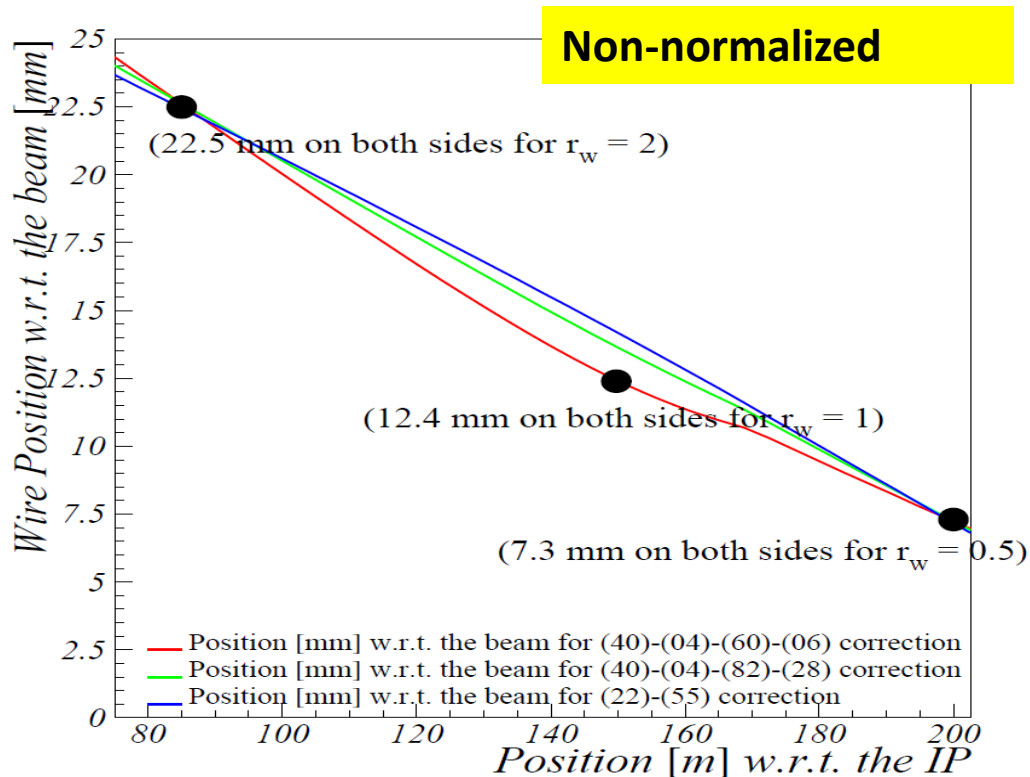
→  $r_w = 1$  can mitigate the current needed but is always worst for the quality of the correction (see later)

→ The current does not depend on the correction type for an aspect ratio of  $r_w \approx 0.5$  or  $r_w \approx 2$ !  
At this aspect ratio, the wire current corresponds to the strict additive contribution of each LR



# Principle of the wire correction and wire specification

- Transverse distance w.r.t. beam vs. wire positioning in **HL-LHC** for a full X-angle of  $590 \mu\text{rad}$  ( $12.5 \sigma$  at  $\beta^*=15 \text{ cm}$ )

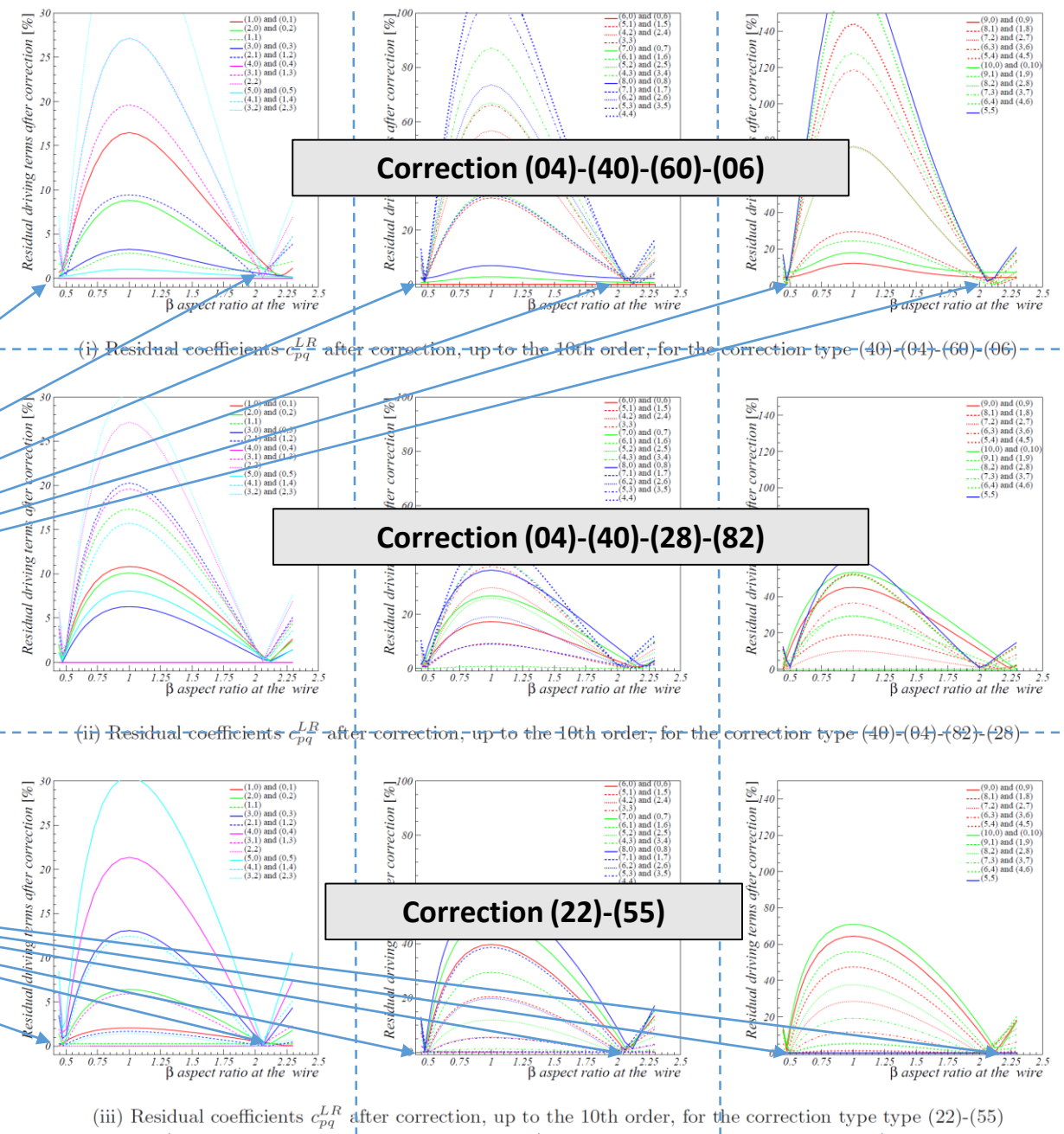


- Again the results does not depend on the correction type for  $r_w \approx 0.5$  or  $r_w \approx 2$  !?
- At this optimal aspect ratio, the normalized wire position is about:

$$d_w \sim 2^{1/4} \times \text{normalised X-angle on the side of the smallest } \beta$$

$$d_w \sim 2^{-1/4} \times \text{normalised X-angle on the side of the largest } \beta$$

• Other RDT's after correction vs.  $r_w$   
 in HL-LHC (residuals in % neglecting  
 the small phases wire/LR)

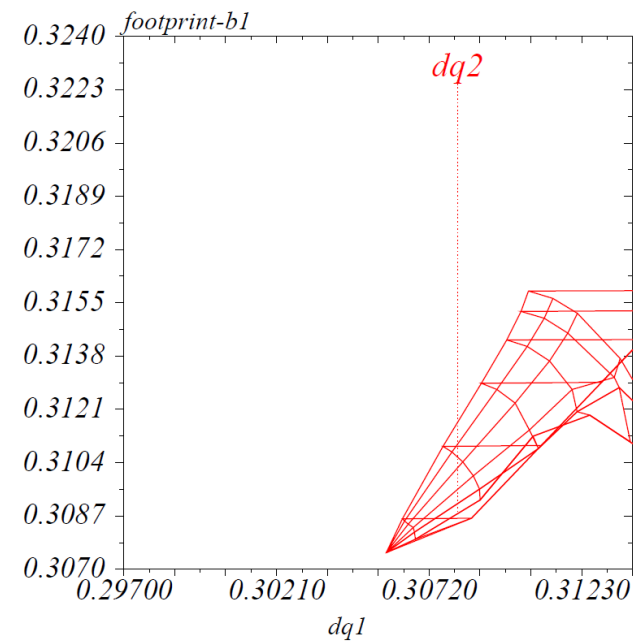
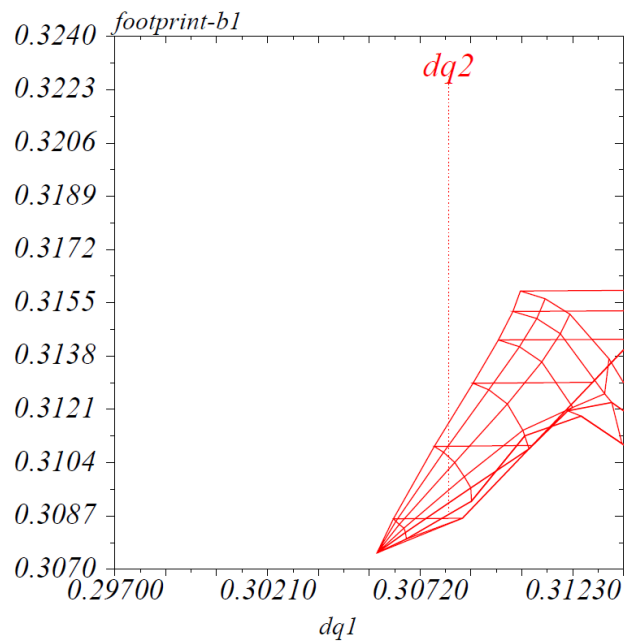
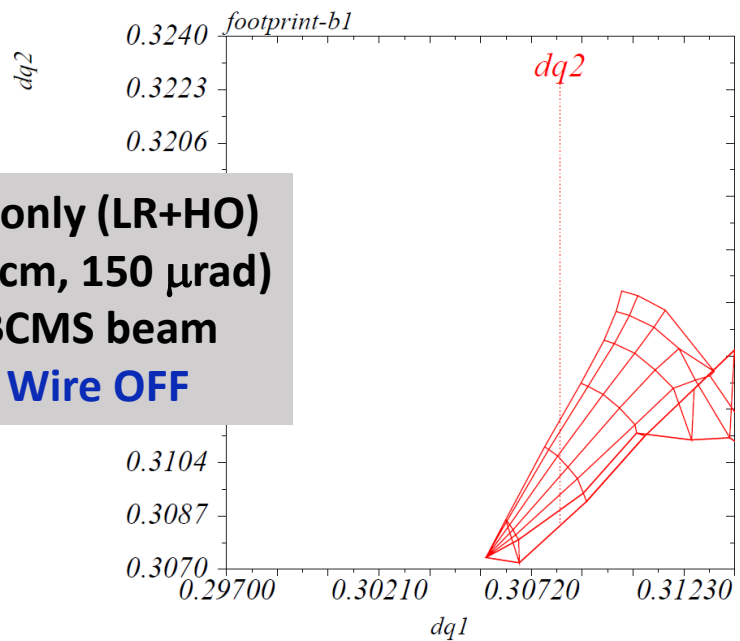


Regardless of the correction type  
**all the RDTs are vanishing at**  
 $r_w \approx 2$  or  $r_w \approx 0.5$

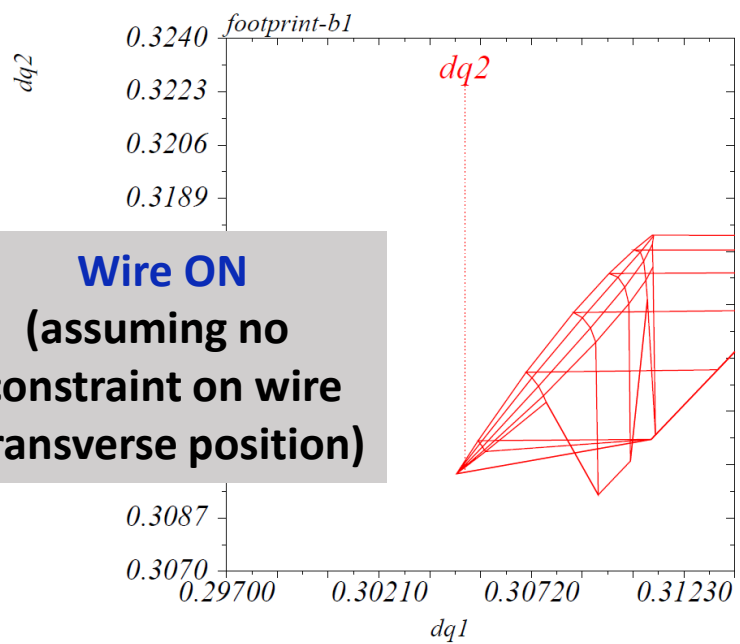
The same feature is observed for **the existing IT**, the minima is just slightly shifted at  $r_w \approx 1.8$  and  $0.55$

From 1st to 3rd order      From 4th to 8th order      From 9th to 10th order

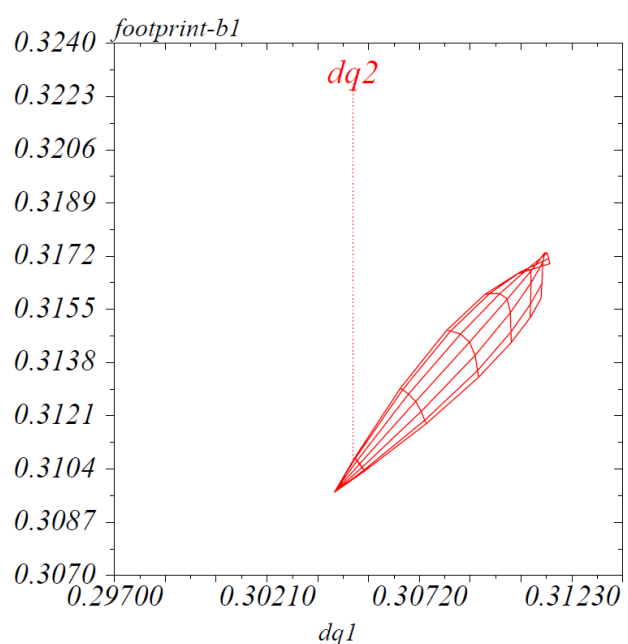
**IR5 only (LR+HO)**  
**(40 cm, 150  $\mu$ rad)**  
**BCMS beam**  
**Wire OFF**



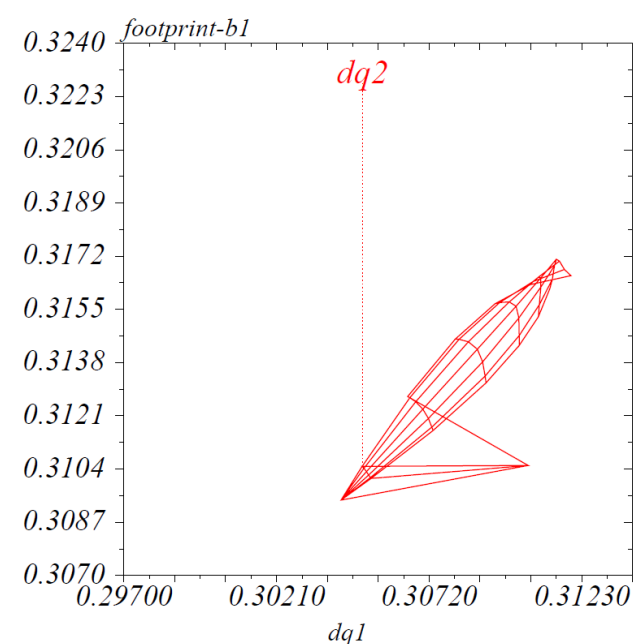
**Wire ON**  
**(assuming no**  
**constraint on wire**  
**transverse position)**



**Nominal optics-2016 ( $r_w \sim 2.7$ )**



**AT-2016 ( $r_w \sim 1.7$ )**



**AT-2017( $r_w \sim 1.4$ )**



# Optimal optics and HW conditions

- **Some optimal rules for HL-LHC (and LHC)**

**Rule # 1 (plane):** 2 wires /beam/IR installed in the X-plane .. e.g. H in IR1 and V in IR5 for “HL-LHC-like flat optics”

**Rule # 2 (layout):** Left/right symmetric w.r.t the IP

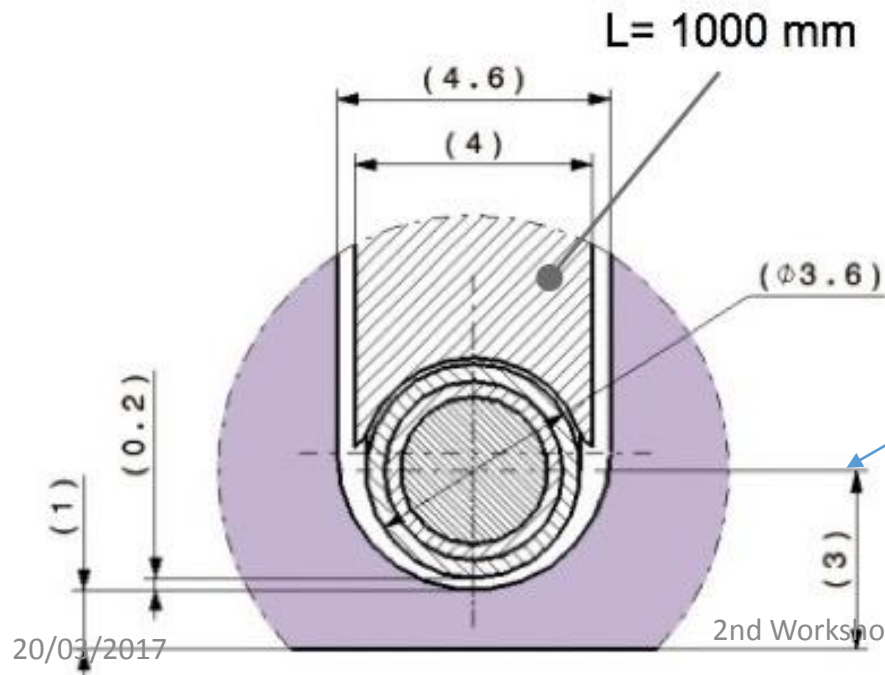
**Rule # 3 (optics):** At an optimal beta aspect ratio of about 2 (1.8 for LHC). In case, the LHC optics is flexible enough to be changed accordingly (mitigating possible constraints from the forward physics experiments)

**Rule # 4 (current):** With a current of about 200 A (100 A for LHC), same current left and right

**Rule # 5 (transverse setting):** At the same physical distance w.r.t. the beam for the left and right wires, corresponding to a normalized distance which is 15-20% larger (resp. smaller) than the crossing angle for the wire on the side of the smallest (resp. largest) beta.

# Optimal optics and HW conditions

- **Where are we with the present HW and which consequence?**
- ☺: Two wires at the TCT & TCL almost symmetric w.r.t. the IP
- ☺:  $\beta$ -aspect ratio at the wires not ideal but much better for ATS2017 than for the 2016 optics
- ☹: Wire in the H plane which rules out flat optics with very small (15-20 cm) horizontal  $\beta^*$ , not too large vertical  $\beta^*$  ( $\sim 60$  cm) and V crossing, as imposed by the IT aperture
- ☹: By far enough current ( $\times 4$  compared to LHC needs), **but which drove a specific HW solution with (too) many beam sigma's lost between wire and TCT edge** (see also next slide)



**Round optics:** 3 mm means already  $\sim 5 \sigma$  @  $\gamma\varepsilon = 2.5 \mu\text{m}$  and  $\beta^* = 40$  cm ( $\beta \sim 900$  m at the TCLW)

**“Oval” optics:** H crossing kept in CMS,  $\beta^*$  limited to  $\sim 35$ -40 cm in the V plane (parallel separation plane), and  $\beta^* \sim 1$  m in the X-plane to keep a “decent” sizeable aspect ratio

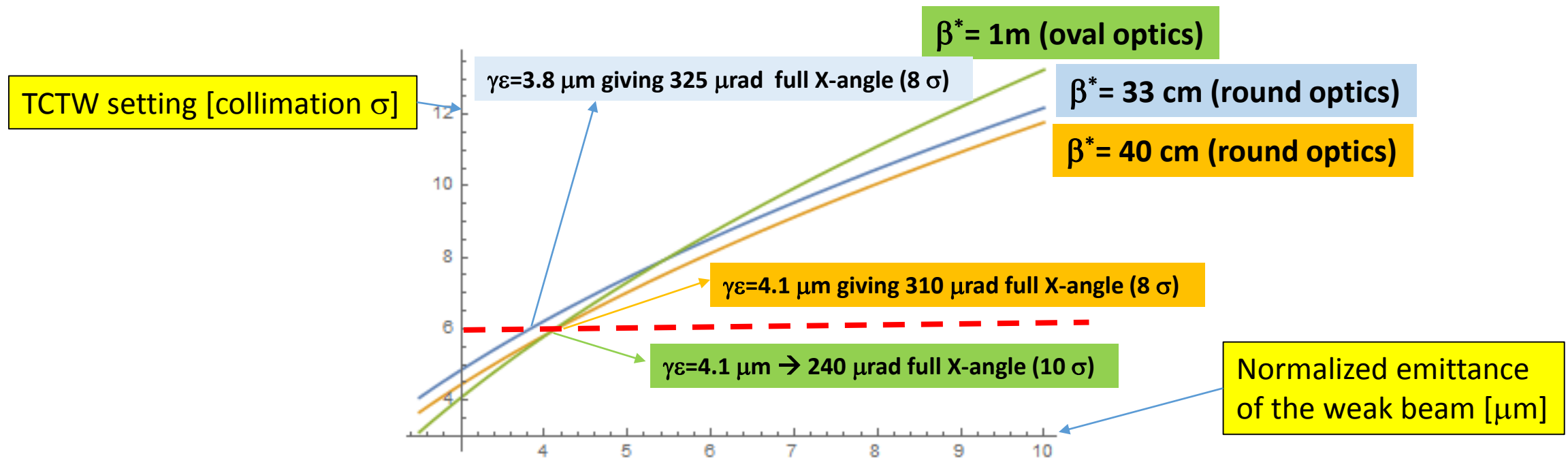
**3 mm becomes  $\sim 8 \sigma$  at  $\beta^* = 1$  m ...** ( $\beta$  shrinks to  $\sim 360$  m at the TCLW)

**→ Definitely the emittance of the weak beam has to be blown up.**

# Can we find any configuration for 2017 to test the full correction?

.. Assuming

- (i) Minimum allowed TCTW gap of 6 collimation  $\sigma$  (i.e. calculated for  $\gamma\varepsilon=3.5 \mu\text{m}$ )
- (ii) Targeting a X-angle of 8 (10) beam  $\sigma$  in round (oval) optics to see convincing life time drops (.. and recovery), i.e.  $\sim 10$  (12) beam  $\sigma$  for the wire at the smallest  $\beta$ .
- (iii) Trying  $\beta^*=33 - 40$  cm for round optics,  $\beta^*=1$  m in the X-plane for “oval” optics



It looks really tricky in all cases, and round optics still seems to be the most promising (easy) way to go

# Conclusions & Outlook

- The present HW configuration (H-plane, 5-8  $\sigma$  lost for wire integration in TCT jaw) makes the full test of the HL-LHC Plan B rather challenging
- **Testing the octupole compensation is however still perfectly within reach and potentially very beneficial, at least with round optics**
  - See Sasha's talk
- Something however still deserves work and a particular attention, which is an attempt for **global correction (all RDTs)**, re-phasing appropriately the optics, with the aim
  - (i) to use the **TCTW/TCLW in IR5 to compensate IR1 with “true” flat optics & H crossing** for the demonstration with beam
  - (ii) then, to **envisage installing wires in TCP7 or TCSG7** (existing or additional ones?), with the right current rating (..), and make the technique fully operational (i.e. w/o gymnastic needed with emittance growth and/or non-nominal collimator settings ..)