

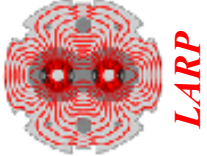
Effects of wire on tails at injection

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Acknowledgements:

S. Fartoukh, R. De Maria, G. Sterbini

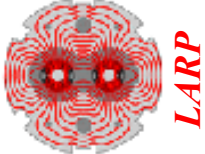


Motivation:

- halo is depleted in collision in presence of strong long range beam-beam effects
- wire mimics the long-range beam-beam force => show that halo can be depleted while core stays unchanged.

Relevant questions for halo depletion:

- What is the effect of the wire/long-range beam-beam on tail particles and the beam distribution?
- Does the wire/long-range beam-beam deplete the halo?
- If long-range beam-beam anyway depleted the halo, would we then actually still need further halo control?



Some theory ...



Multipole expansion of wire field [1]:

$$\int ds [B_y + iB_x] = \sum_{k=1}^{\infty} [B_k + iA_k] z^{k-1}$$

$$\text{with } B_k + iA_k = \frac{\mu_0 I L}{2\pi} \times \frac{1}{z_0^k}$$

z = transverse position of test particle in respect to the beam centroid

z_0 = distance between wire and beam

I = current of wire, L = length of wire

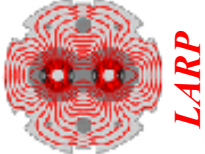
⇒ for wire in the horizontal plane ($z_0=x_0$ real) only normal multipole components ($A_k = 0$ for all k)

⇒ wire drives only resonances with

$$p \cdot Q_x + q \cdot Q_y = n, \quad n \in \mathbb{N} \text{ with}$$

$$p \in \mathbb{N}, q = 0 \text{ or } p \bmod 2 = 0, q \in \mathbb{N}$$

[1] S. Fartoukh et al., Compensation of the long-range beam-beam interactions as a path towards new configurations for the high luminosity LHC, PRSTAB 18, 121001 (2015)



Some theory ...



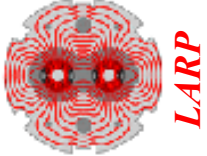
Driving terms [1]:

$$c_{p,q}^w = \sum_{k=L,R} \frac{\beta_x^{|p|/2}(s_k) \beta_y^{|q|/2}(s_k)}{d_w^{|p|+|q|}(s_k) [\text{m}]} e^{i(p\mu_x(s_k) + q\mu_y(s_k))}$$
$$\Rightarrow c_{p,q}^w \sim \sum_{k=L,R} \frac{1}{r} \frac{1}{d_w^{|p|+|q|}(s_k) [\sigma]} \quad \text{with } r = \frac{\beta_x(s_k)}{\beta_y(s_k)}$$

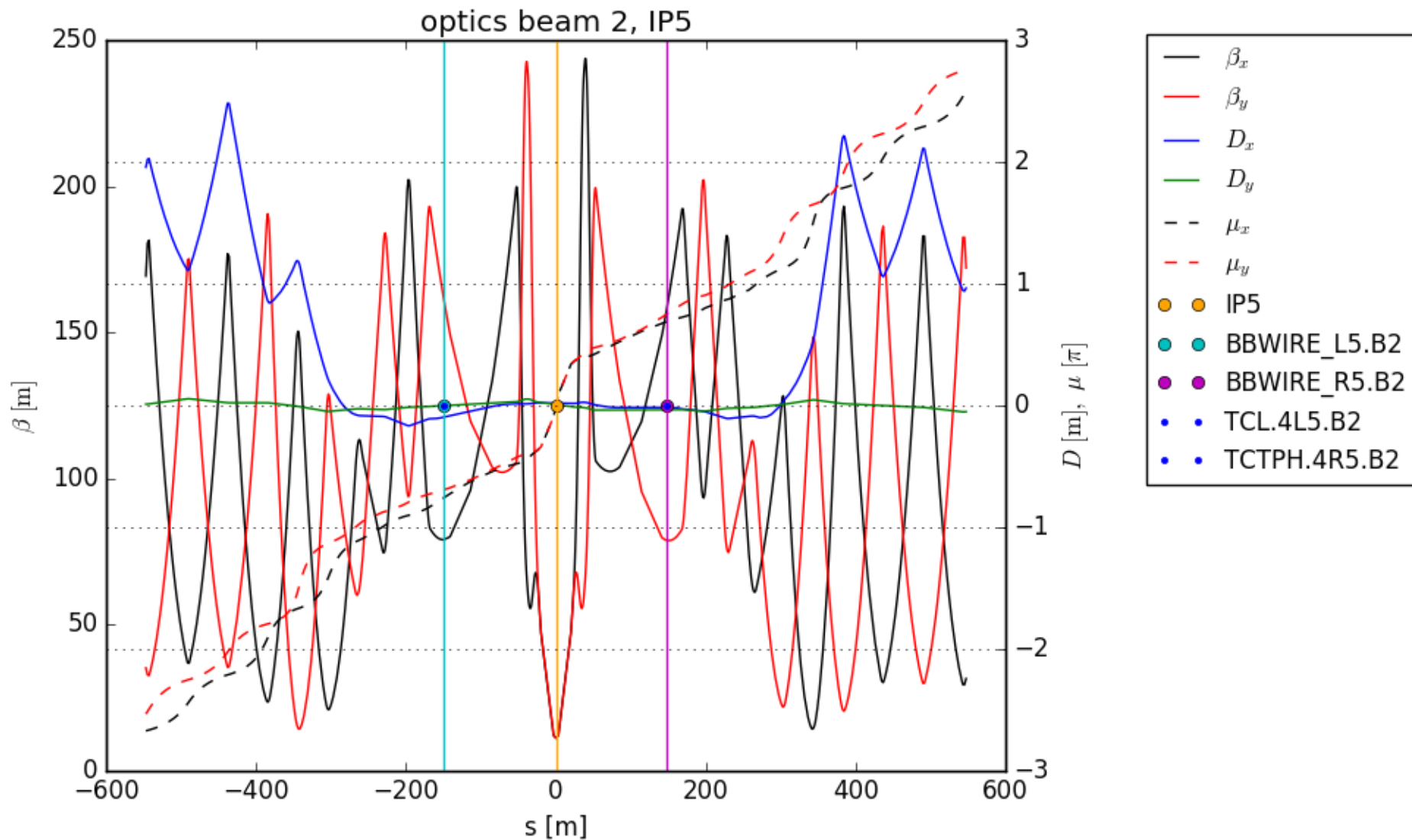
d_w = distance between wire and beam

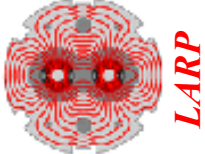
- ⇒ at injection wires on left and right can not be simply lumped together in one interaction as the phase advance between the two wires is 1.4π
- ⇒ RDTs scale with ratio of the β -function r and the distance d_w [σ] between wire and beam

[1] S. Fartoukh et al., Compensation of the long-range beam-beam interactions as a path towards new configurations for the high luminosity LHC, PRSTAB 18, 121001 (2015)



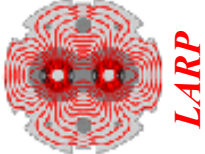
Optics @ injection



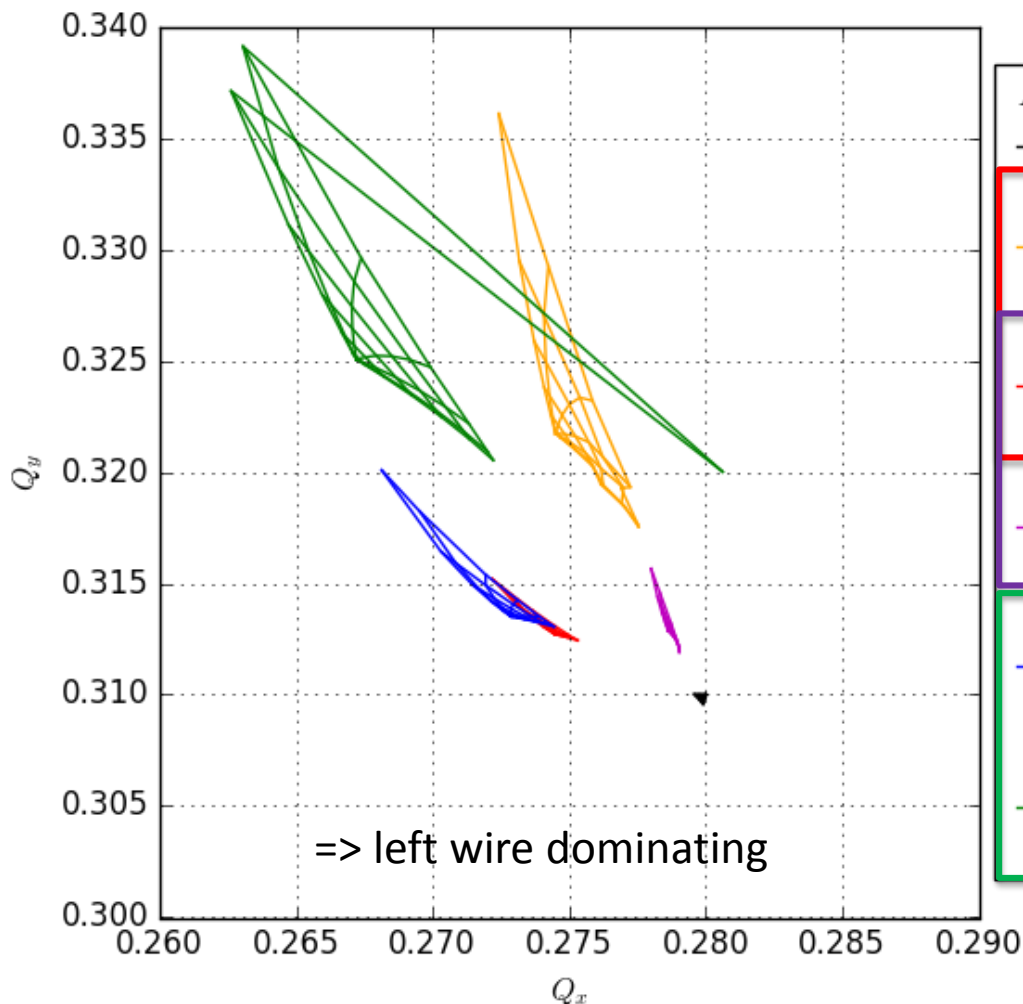


	TCL.4L5.B2	TCTPH.4R5.B2
$d_{\text{jaw} \leftrightarrow \text{wire}}$	3 mm	
β_x [m]	81.2	169.6
β_y [m]	166.5	81.3
β_x / β_y	0.5	2.1
D_x [m]	-0.1	0.1
$\Delta\mu_x(\text{TCL.4L5}, \text{TCTPH.4R5})$ [π]	1.43	
$\Delta\mu_y(\text{TCL.4L5}, \text{TCTPH.4R5})$ [π]		
$d_{\text{jaw} \leftrightarrow \text{beam}}$ [σ] for $d_{\text{wire} \leftrightarrow \text{beam}} = 9.6 \sigma$ ($\epsilon_N = 3.5 \mu\text{m}$)	5.7	6.9
$d_{\text{jaw} \leftrightarrow \text{beam}}$ [mm] for $d_{\text{wire} \leftrightarrow \text{beam}} = 9.6 \sigma$ ($\epsilon_N = 3.5 \mu\text{m}$)	6.5	9.3

⇒ larger effect for wire on left side



Tune footprints, no octupoles



$I_{\text{wire}} < 0 \Rightarrow$ long – range beam – beam compensation

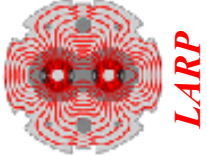
— $I_{\text{MO}} = 0 \text{ A}, I_{\text{wire}} = 0 \text{ A}$

<p>no tune rematch, $I_{\text{MO}} = 0 \text{ A}, I_{\text{wire,L}} = -350 \text{ A}, I_{\text{wire,R}} = 0 \text{ A},$ $d_{\text{beam} \leftrightarrow \text{jaw,L}} = 5.7\sigma$</p>
<p>no tune rematch, $I_{\text{MO}} = 0 \text{ A}, I_{\text{wire,L}} = 0 \text{ A}, I_{\text{wire,R}} = -350 \text{ A},$ $d_{\text{beam} \leftrightarrow \text{jaw,L}} = 6.85\sigma$</p>
<p>no tune rematch, $I_{\text{MO}} = 0 \text{ A}, I_{\text{wire,L}} = -87.5 \text{ A}, I_{\text{wire,R}} = 0 \text{ A},$ $d_{\text{beam} \leftrightarrow \text{jaw,L}} = 5.7\sigma$</p>
<p>no tune rematch, $I_{\text{MO}} = 0 \text{ A}, I_{\text{wire,L}} = 0 \text{ A}, I_{\text{wire,R}} = -350 \text{ A},$ $d_{\text{beam} \leftrightarrow \text{jaw,L}} = 4.53\sigma$</p>
<p>no tune rematch, $I_{\text{MO}} = -350 \text{ A}, I_{\text{wire,L}} = -350 \text{ A}, I_{\text{wire,R}} = 0 \text{ A},$ $d_{\text{beam} \leftrightarrow \text{jaw,L}} = 5.7\sigma = d_{\text{beam} \leftrightarrow \text{jaw,R}}$</p>

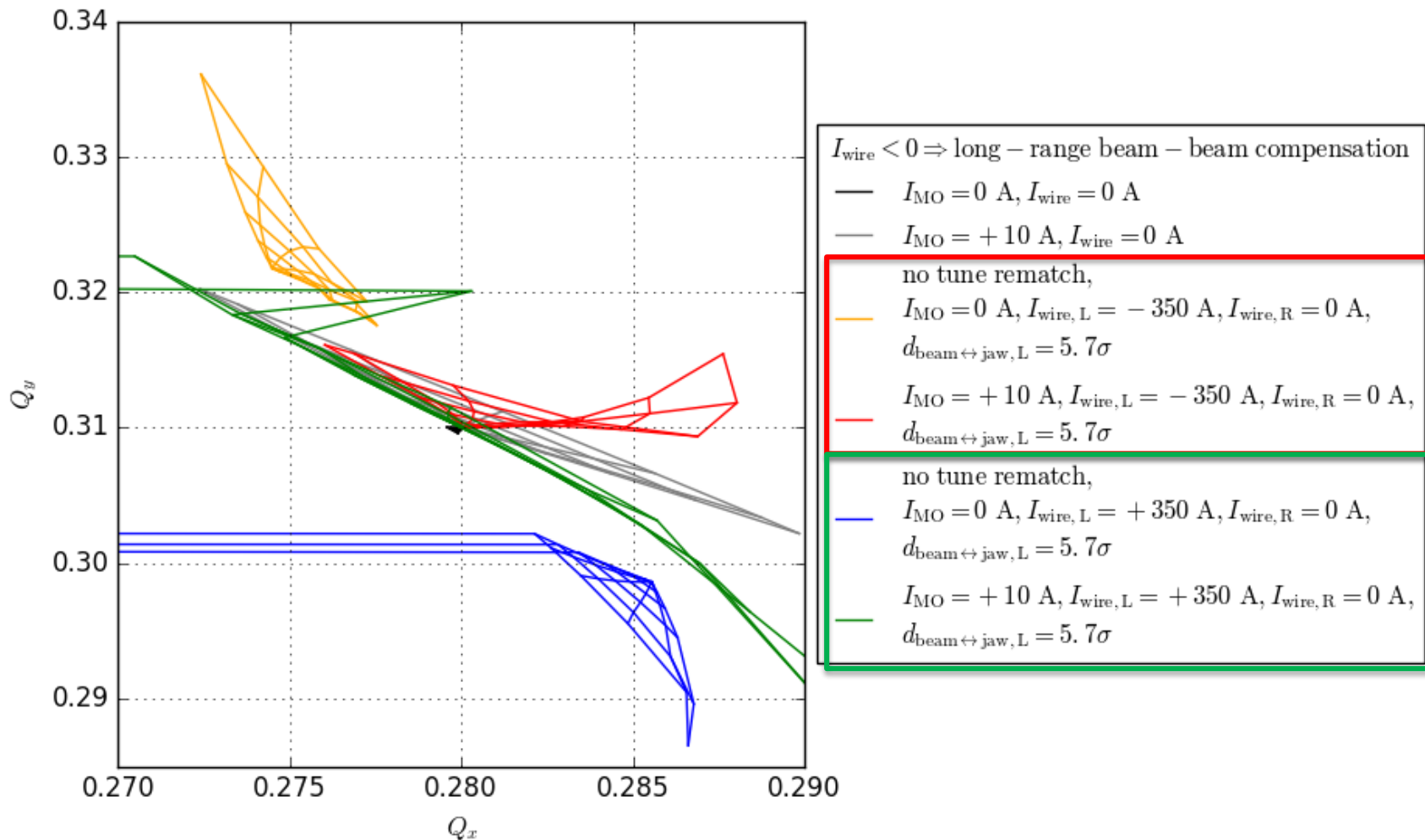
same separation and current: $I_{\text{wire,R}} = I_{\text{wire,L}}, d(\text{wire,beam})_{\text{L}} = d(\text{wire,beam})_{\text{R}}$

same tune spread: $I_{\text{wire,R}} = 4 * I_{\text{wire,L}}, d(\text{wire,beam})_{\text{L}} = d(\text{wire,beam})_{\text{R}}$

maximum current, minimal separation: $I_{\text{wire,R}} = I_{\text{wire,L}}, d(\text{jaw,beam})_{\text{L}} [\sigma] = d(\text{jaw,beam})_{\text{R}} [\sigma]$

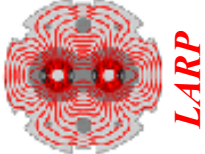


Tune footprints, with octupoles



negative current (same sign as for BBLR compensation)

positive current



Code: Lifetrac

Optics: 2016 and 2017 injection optics (changes are marginal)

Beam: beam 2, $N_b=1.1 \times 10^{11}$, $\epsilon_N=3.5 \mu\text{m}$

FMA analysis:

- turns tracked: 10^4
- quadratic grid up to 8σ

Long term tracking:

- distribution: uniform distribution in x and y within $[-5.7, 5.7] \sigma$
- turns tracked: 10^6
- single aperture in IP3 @ 5.7σ (only betatron part) -> any diffusion above this aperture doesn't matter!

Notation:

- Separation $d_{\text{wire} \leftrightarrow \text{beam}}$ is always given in terms of $d_{\text{jaw} \leftrightarrow \text{beam}}$ for the wire on the left side. The right side is then set so that $d_{\text{wire} \leftrightarrow \text{beam}, L} [\sigma] = d_{\text{wire} \leftrightarrow \text{beam}, R} [\sigma]$.
- LEFT and RIGHT wire refer to the position from the IP: LEFT = TCL.4L5, RIGHT = TCTPH.4R5

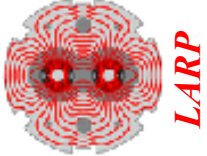
$$I_{\text{wire}} < 0$$

injection optics

injection tunes $Q_x=62.28$, $Q_y=60.31$

$$Q_x' = Q_y' = 4$$

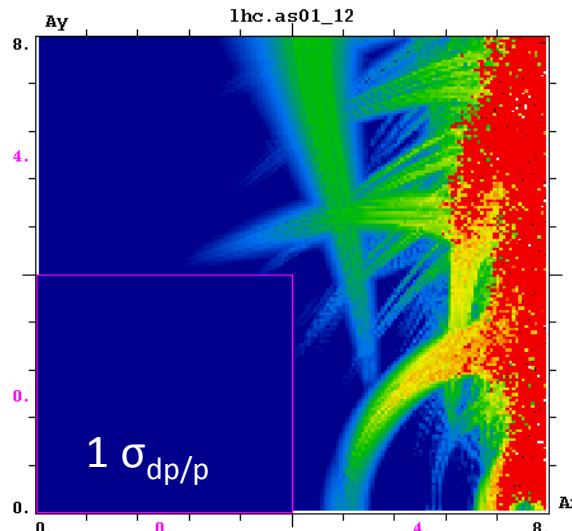
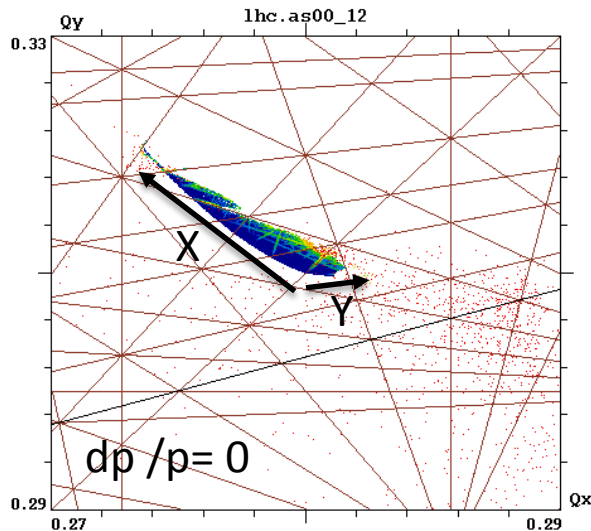
$$I_{\text{oct}} = 0 \text{ A}$$



$I_{\text{wire}} < 0$, no octupoles, wire R

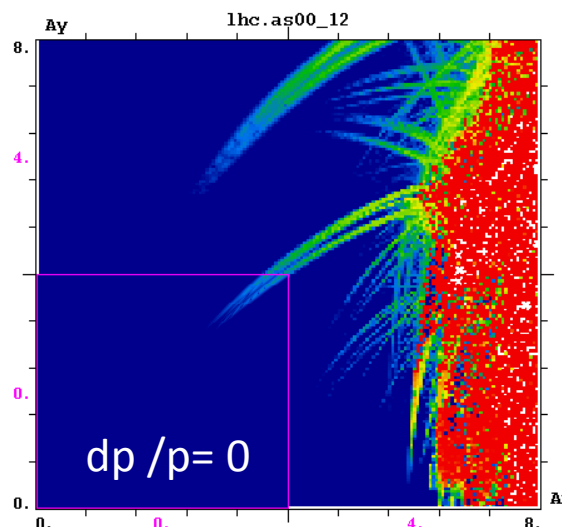
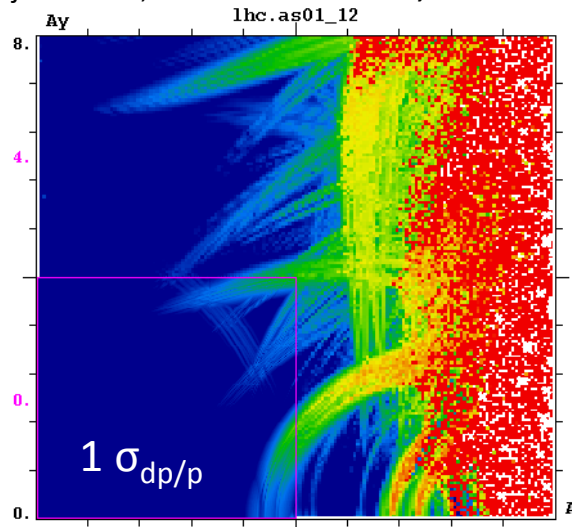
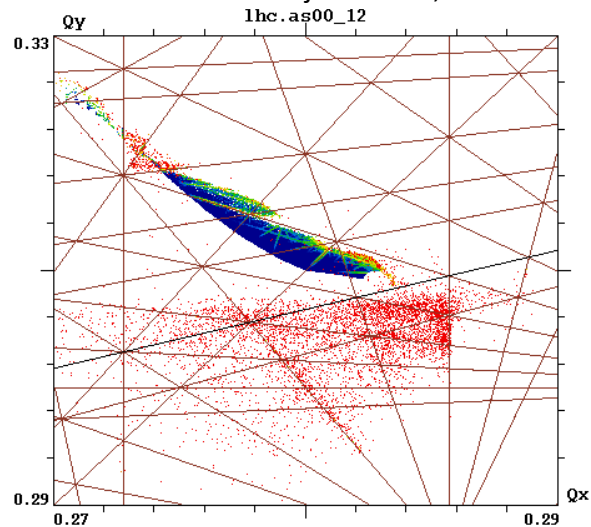


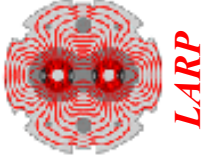
WIRE RIGHT, $d_{\text{jaw-beam,L}} = 5.7 \sigma$ ($d_{\text{jaw-beam,R}} = 6.9 \sigma$): $I_{\text{wire,L}} = 0 \text{ A}$, $I_{\text{wire,R}} = -350 \text{ A}$, $I_{\text{oct}} = 0 \text{ A}$



- cleaning only in the horizontal plane
- cleaning only for high amplitudes
- also for the minimal distance $d_{\text{jaw-beam,R}} = 5.7 \sigma$ the wire only cleans for amplitudes above $\sim 6.5 \sigma$

WIRE RIGHT, $d_{\text{jaw-beam,L}} = 4.5 \sigma$ ($d_{\text{jaw-beam,R}} = 5.7 \sigma$): $I_{\text{wire,L}} = 0 \text{ A}$, $I_{\text{wire,R}} = -350 \text{ A}$, $I_{\text{oct}} = 0 \text{ A}$

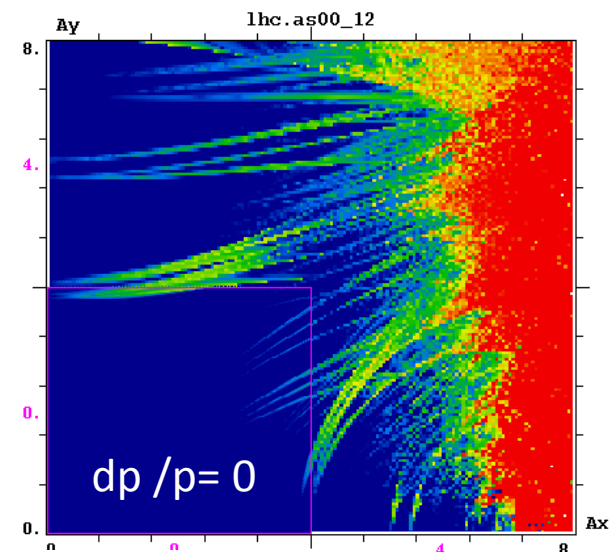
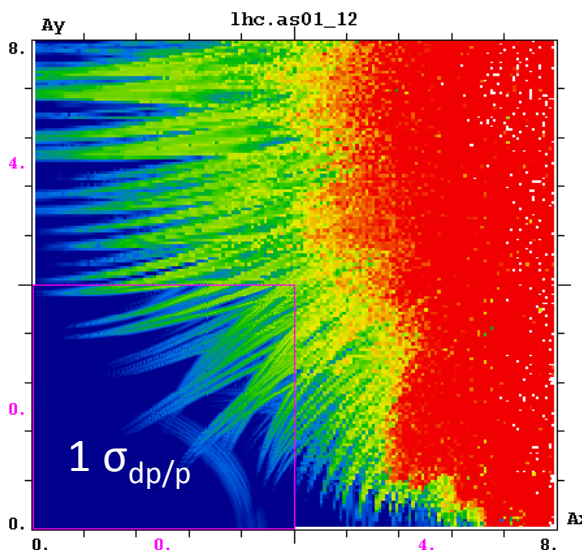
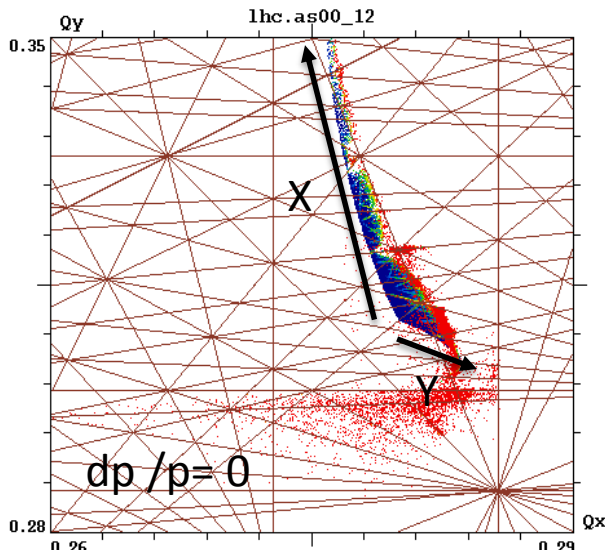




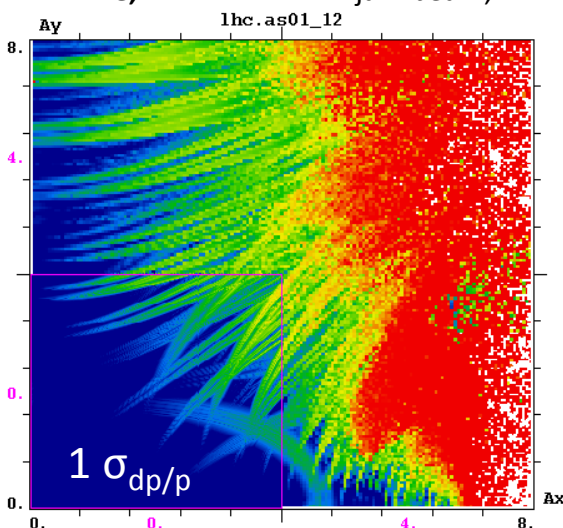
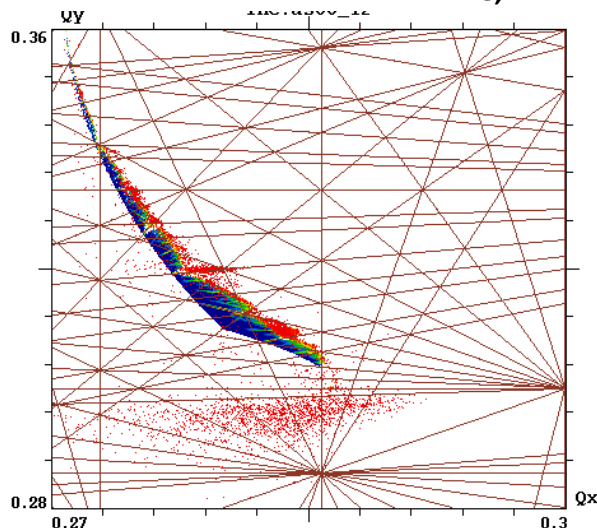
$I_{\text{wire}} < 0$, no octupoles, wire L, wire L+R



WIRE LEFT: $I_{\text{wire,L}} = -350$ A, $I_{\text{wire,R}} = 0$ A, $d_{\text{jaw-beam,L}} = 5.7 \sigma$, $I_{\text{oct}} = 0$ A



WIRE LEFT+RIGHT: $I_{\text{wire,L}} = -350$ A, $I_{\text{wire,R}} = -350$ A, $d_{\text{jaw-beam,L}} = 5.7 \sigma$, $I_{\text{oct}} = 0$ A



- WIRE LEFT more efficient than WIRE RIGHT
- cleaning only in the horizontal plane
- on-momentum: clear cleaning above $\sim 6 \sigma$
- off-momentum: cleaning down to $\sim 4 \sigma$
- adding wire on right appears to decrease diffusion

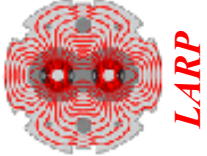
$$I_{\text{wire}} < 0$$

injection optics

injection tunes $Q_x=62.28$, $Q_y=60.31$

$$Q_x' = Q_y' = 4$$

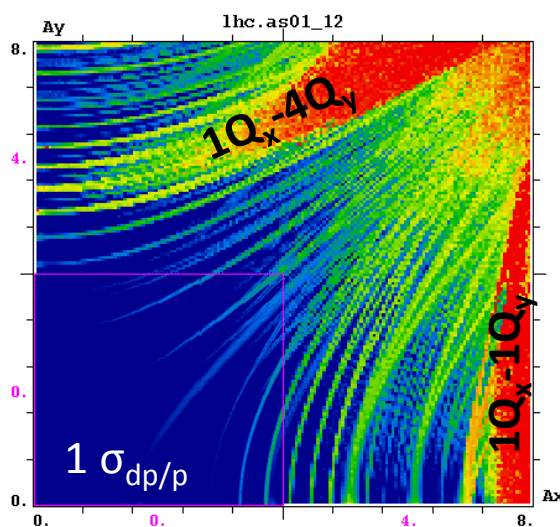
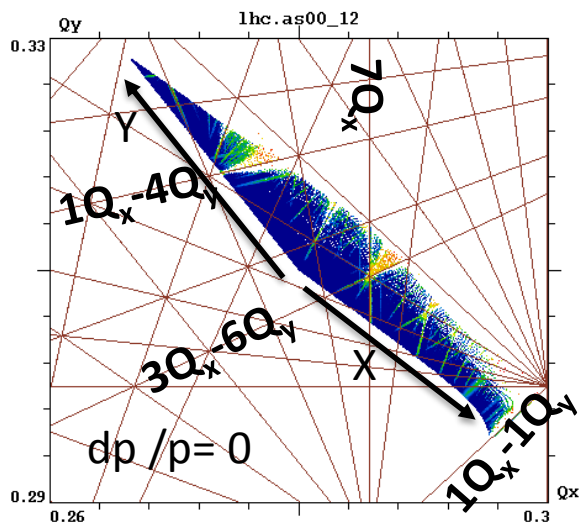
$$I_{\text{oct}} = +10 \text{ A}$$



$I_{\text{wire}} < 0$, $I_{\text{oct}} = +10 \text{ A}$, no wire, wire L

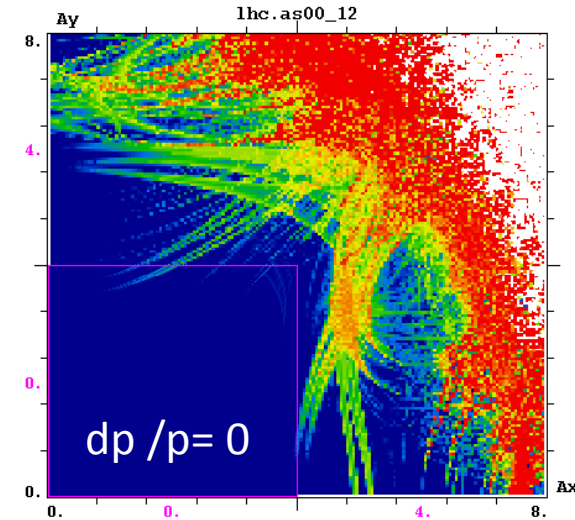
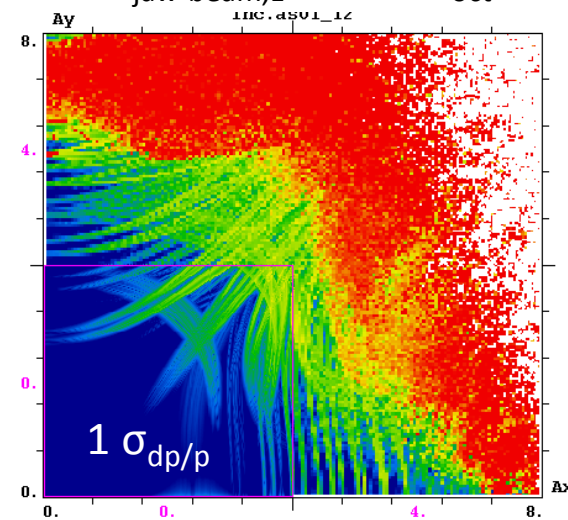
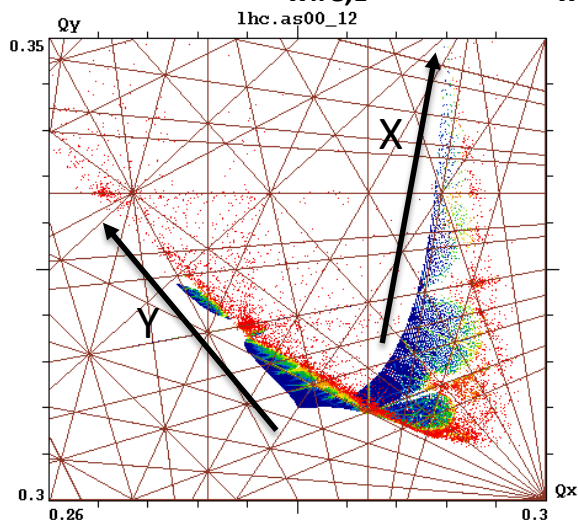


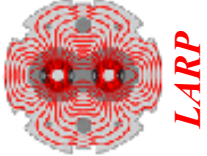
NO WIRE: $I_{\text{oct}} = +10 \text{ A}$



- resonances from octupoles enhanced with wire
- $1Q_x-4Q_y$ resonances results in cleaning also in vertical plane
- on-momentum: clear cleaning above $\sim 6 \sigma$
- off-momentum: cleaning down to $\sim 4 \sigma$

WIRE LEFT: $I_{\text{wire,L}} = -350 \text{ A}$, $I_{\text{wire,R}} = 0 \text{ A}$, $d_{\text{jaw-beam,L}} = 5.7 \sigma$, $I_{\text{oct}} = +10 \text{ A}$

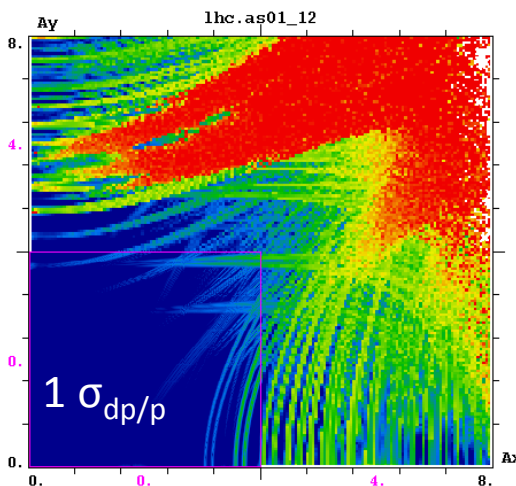
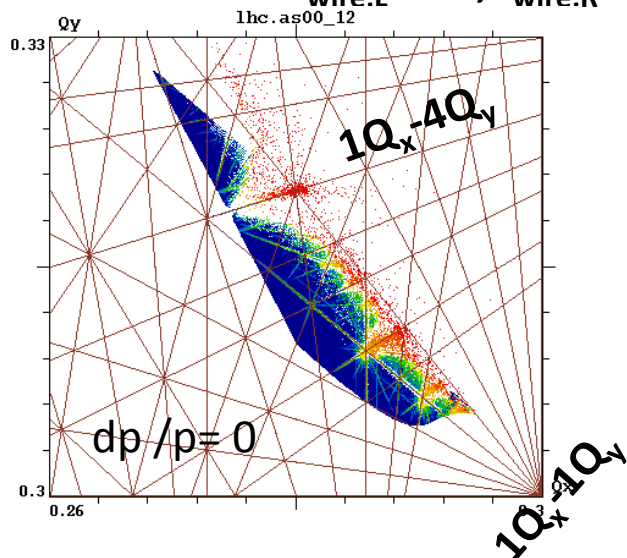




$I_{\text{wire}} < 0, I_{\text{oct}} = +10 \text{ A, wire R, wire L+R}$

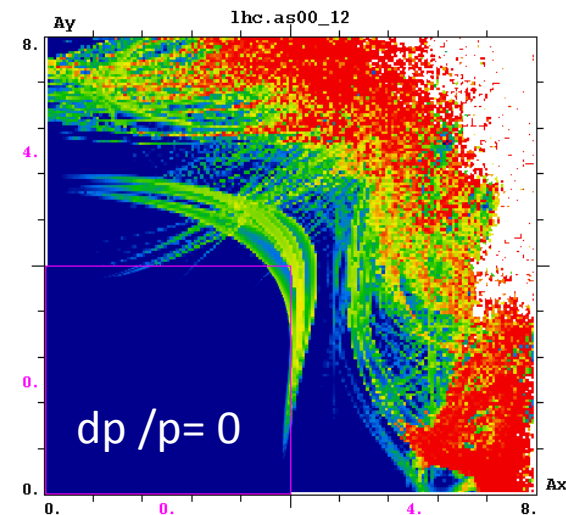
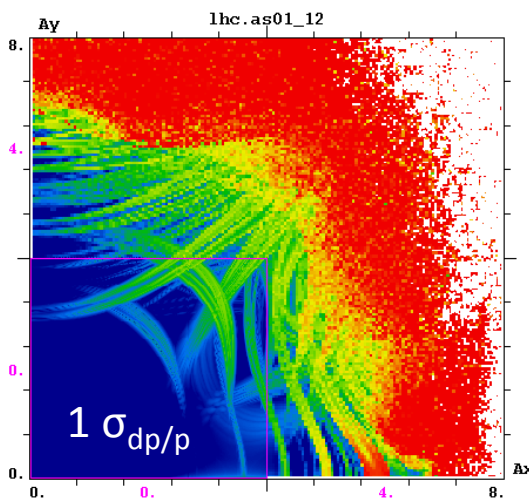
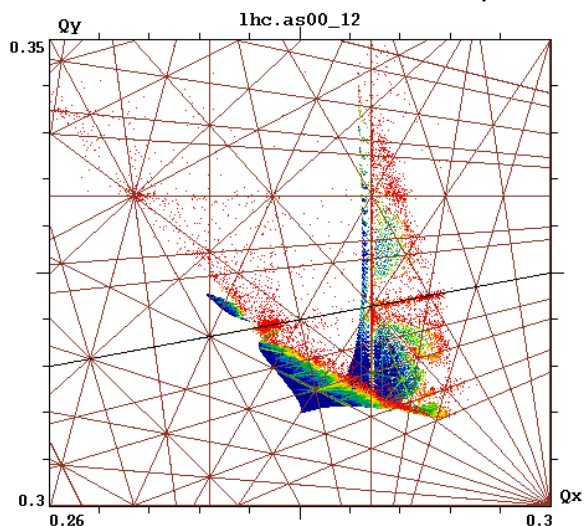


WIRE RIGHT: $I_{\text{wire,L}} = 0 \text{ A, } I_{\text{wire,R}} = -350 \text{ A, } d_{\text{jaw-beam,L}} = 5.7 \sigma, I_{\text{oct}} = +10 \text{ A}$



- WIRE RIGHT: small effect, octupolar resonances are enhanced
- WIRE LEFT+RIGHT: additional wire on right does not have a considerable effect

WIRE LEFT+RIGHT: $I_{\text{wire,L}} = -350 \text{ A, } I_{\text{wire,R}} = -350 \text{ A, } d_{\text{jaw-beam,L}} = 5.7 \sigma, I_{\text{oct}} = +10 \text{ A}$



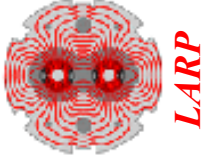
$$I_{\text{wire}} > 0$$

injection optics

injection tunes $Q_x=62.28$, $Q_y=60.31$

$$Q_x' = Q_y' = 4$$

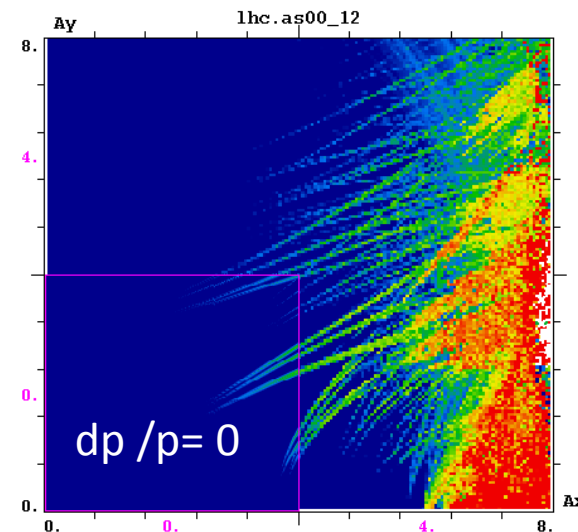
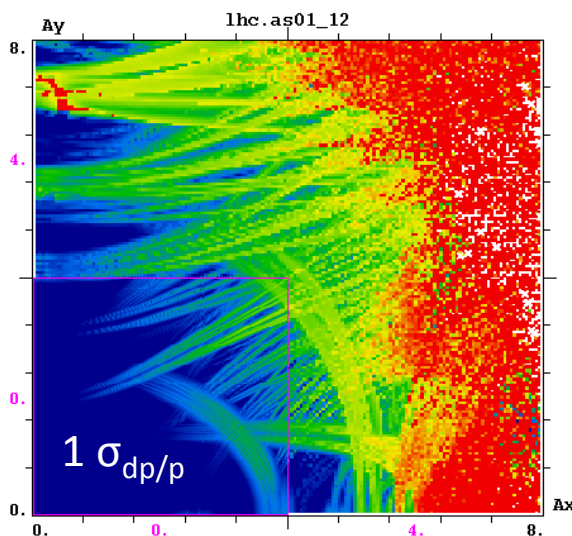
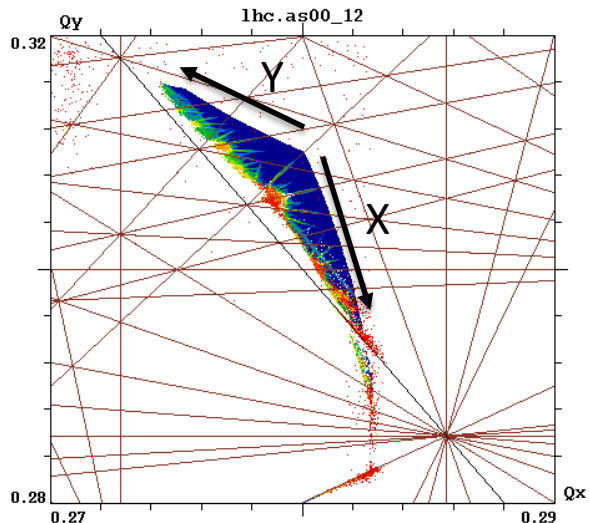
$$I_{\text{oct}} = +10 \text{ A}$$



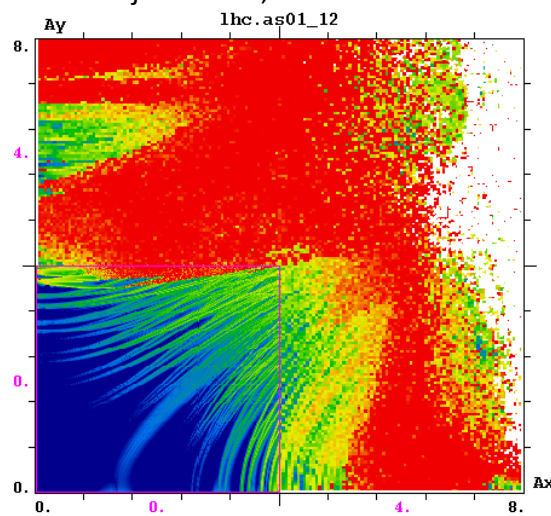
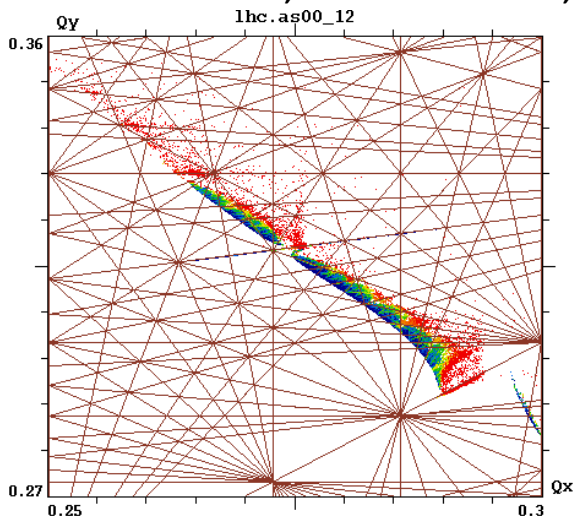
$I_{\text{wire}} > 0, \text{wire L}$



WIRE LEFT: $I_{\text{wire,L}} = +350 \text{ A}$, $I_{\text{wire,R}} = 0 \text{ A}$, $d_{\text{jaw-beam,L}} = 5.7 \sigma$, $I_{\text{oct}} = 0 \text{ A}$



WIRE LEFT: $I_{\text{wire,L}} = +350 \text{ A}$, $I_{\text{wire,R}} = 0 \text{ A}$, $d_{\text{jaw-beam,L}} = 5.7 \sigma$, $I_{\text{oct}} = +10 \text{ A}$



- without octupoles cleaning down to $\sim 6 \sigma$
- with octupoles cleaning down to small amplitudes in both planes, even better than for $I_{\text{wire}} < 0$
- tune footprint collapses to thin line with octupoles -> beam stability?

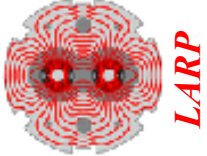
$$I_{\text{wire}} < 0$$

injection optics

change of working point

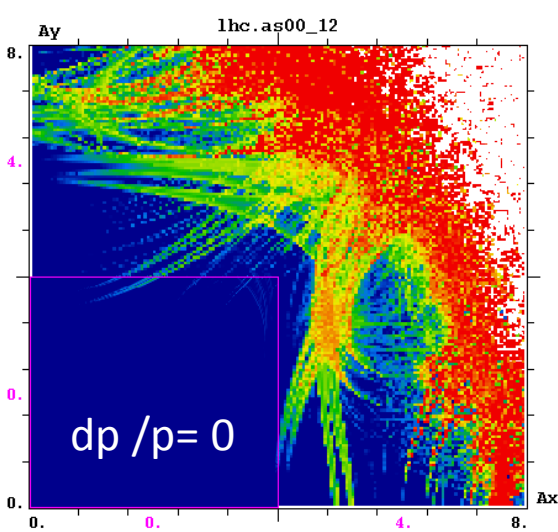
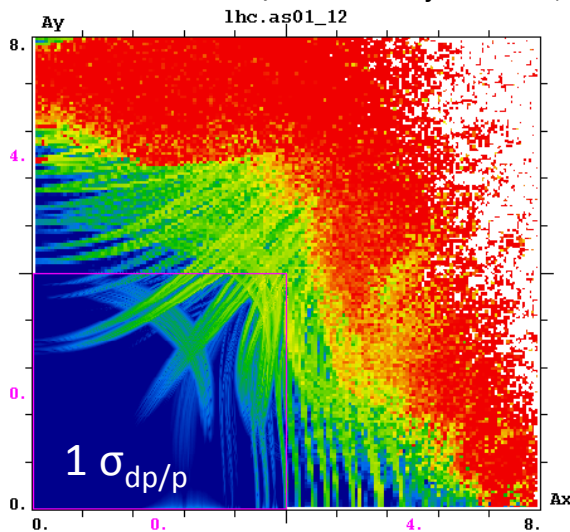
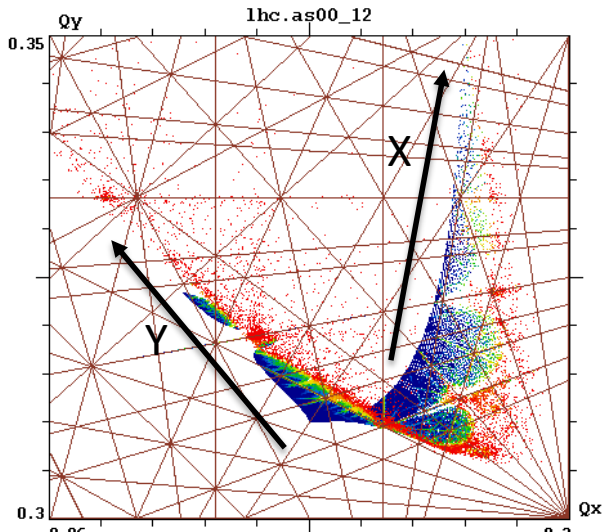
$$Q_x' = Q_y' = 4$$

$$I_{\text{oct}} = +10 \text{ A}$$

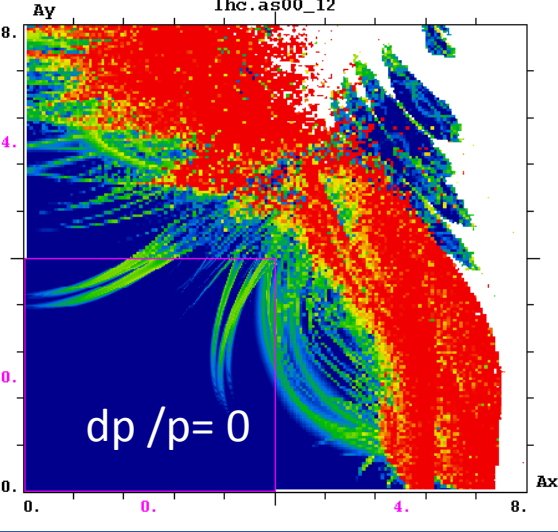
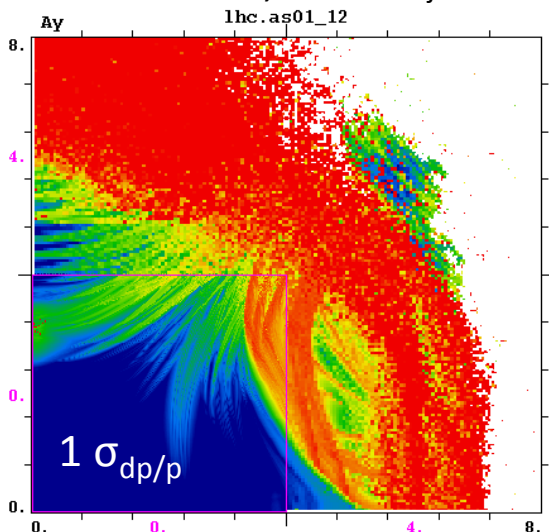
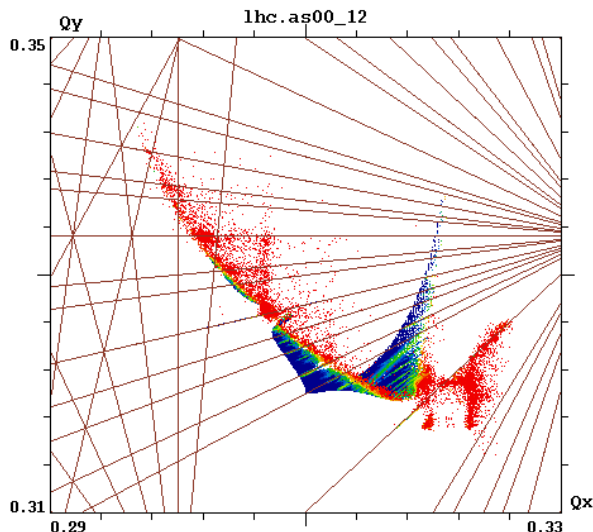


$I_{\text{wire}} < 0, I_{\text{oct}} = +10 \text{ A}, \text{wire L}$

$Q_x = .28, Q_y = .31$, WIRE LEFT: $I_{\text{wire,L}} = -350 \text{ A}, I_{\text{wire,R}} = 0 \text{ A}, d_{\text{jaw-beam,L}} = 5.7 \sigma, I_{\text{oct}} = +10 \text{ A}$



$Q_x = .31, Q_y = .32$, WIRE LEFT: $I_{\text{wire,L}} = -350 \text{ A}, I_{\text{wire,R}} = 0 \text{ A}, d_{\text{jaw-beam,L}} = 5.7 \sigma, I_{\text{oct}} = +10 \text{ A}$



$$I_{\text{wire}} < 0$$

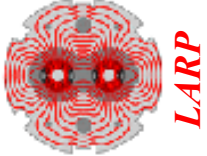
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injection tunes $Q_x=62.28$, $Q_y=60.31$

$$Q_x' = Q_y' = 4$$

$$I_{\text{oct}} = +10 \text{ A}$$

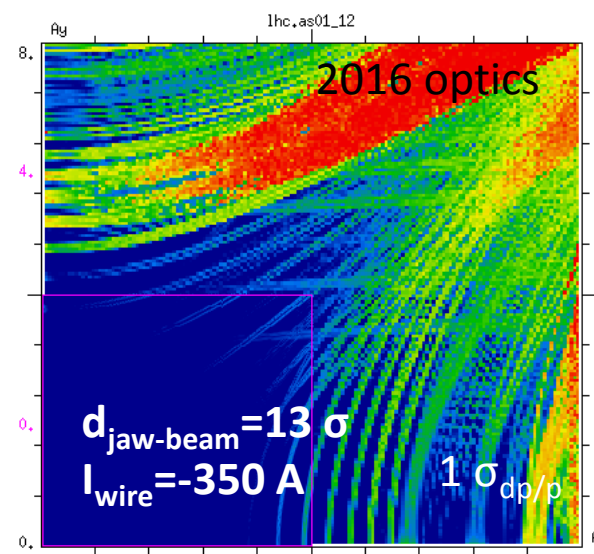
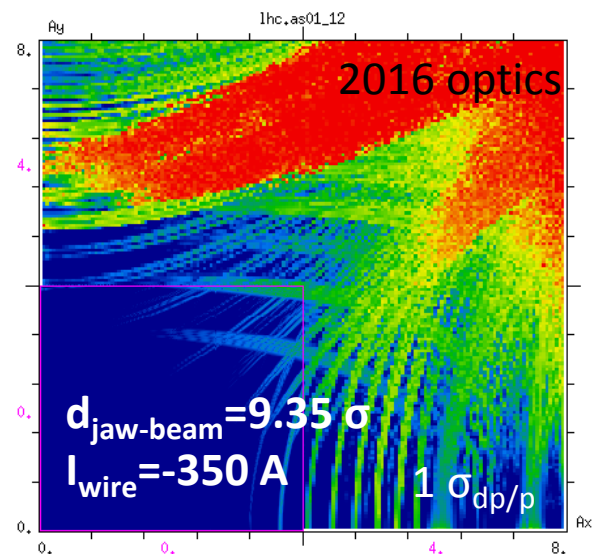
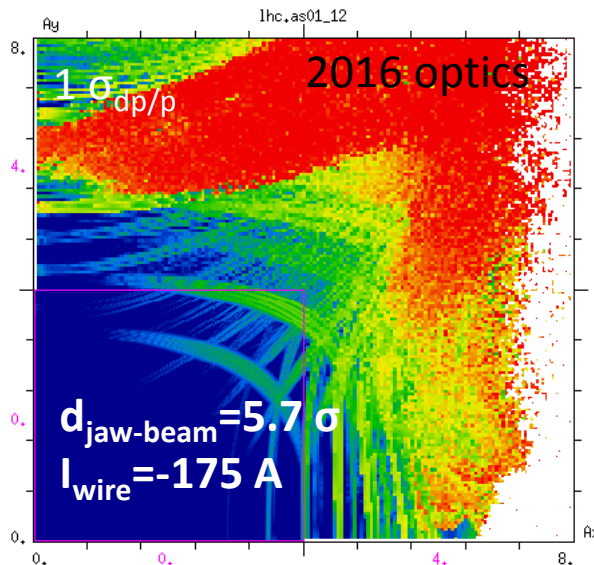
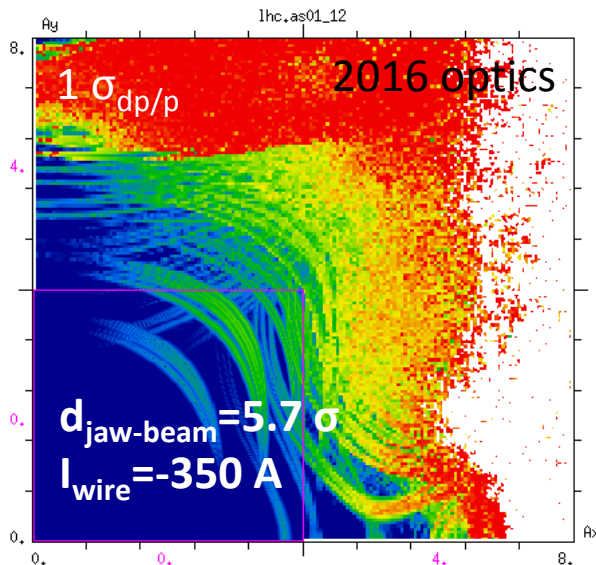
Dependence on $d_{\text{wire} \leftrightarrow \text{beam}}$ and I_{wire}



$I_{\text{wire}} < 0, I_{\text{oct}} = +10 \text{ A}, \text{wire L+R}$



WIRE LEFT+RIGHT, $d_{\text{jaw-beam,L}} = d_{\text{jaw-beam,R}} : I_{\text{wire,L}} = I_{\text{wire,R}}, I_{\text{oct}} = +10 \text{ A}$



- weak dependence on current I_{wire} compared to $d_{\text{wire} \leftrightarrow \text{beam}}$

- effect of wire rapidly decreases with $d_{\text{wire} \leftrightarrow \text{beam}}$
 -> most likely have to use minimal separation of $d_{\text{jaw} \leftrightarrow \text{beam}} = 5.7 \sigma$

$$I_{\text{wire}} < 0$$

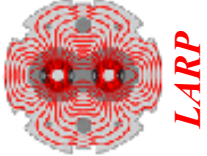
injection optics

injection tunes $Q_x=62.28$, $Q_y=60.31$

$$Q_x' = Q_y' = 4$$

$$I_{\text{oct}} = +10 \text{ A}$$

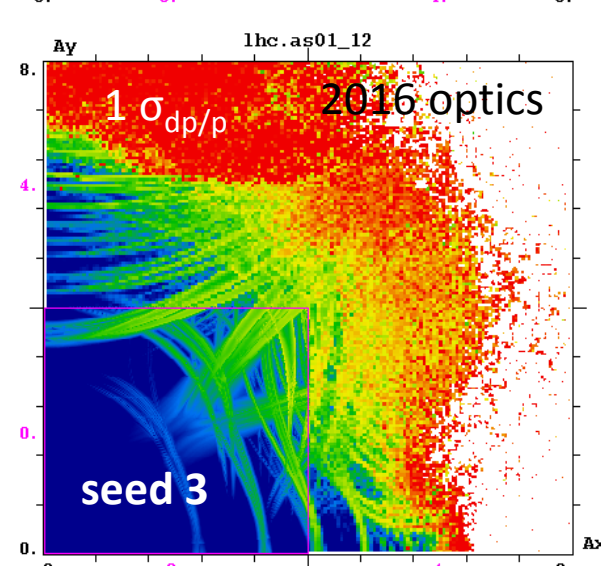
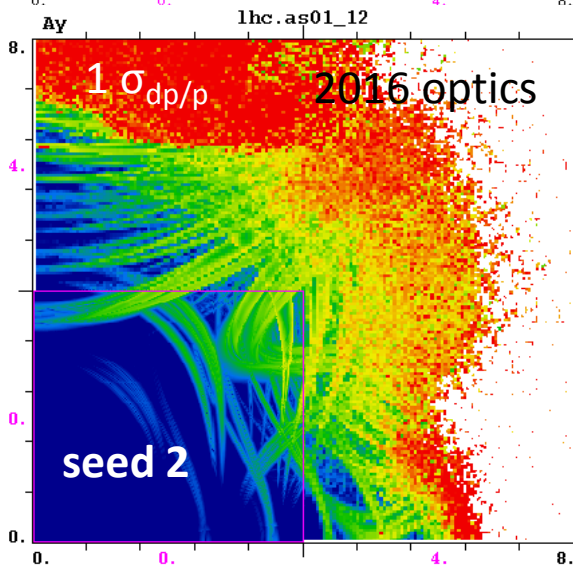
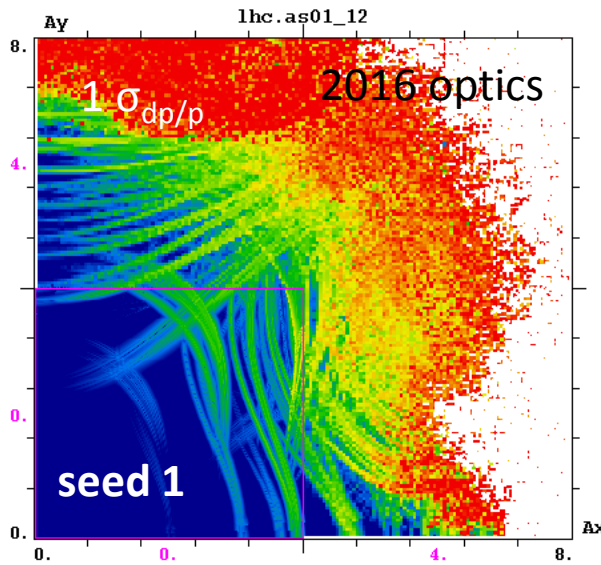
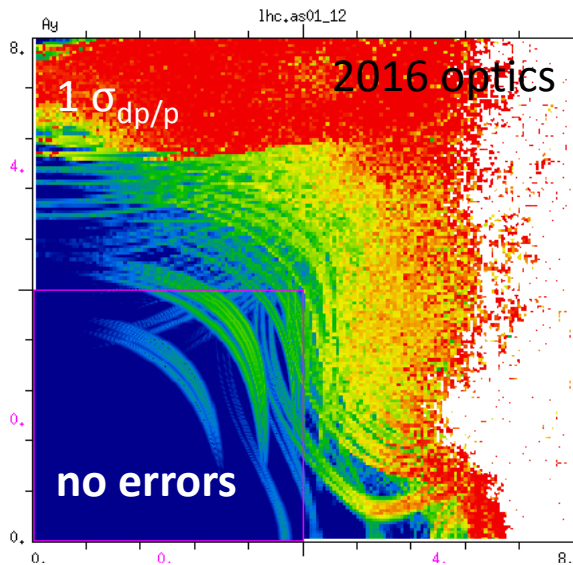
**Dependence on errors
(non-linear + b2)**



$I_{\text{wire}} < 0, I_{\text{oct}} = +10 \text{ A}, \text{wire L+R}$

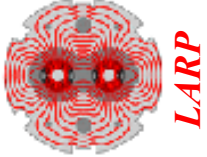


WIRE LEFT+RIGHT, $d_{\text{jaw-beam,L}} = d_{\text{jaw-beam,R}} = 5.7 \sigma, I_{\text{wire,L}} = I_{\text{wire,R}} = -350 \text{ A}, I_{\text{oct}} = +10 \text{ A}$



- small impact due to beta-beat and non-linear errors expected
- closed orbit distortions are not taken into account as collimator alignment is considered to be “good enough”.

Histograms for long term tracking (10^6 turns)



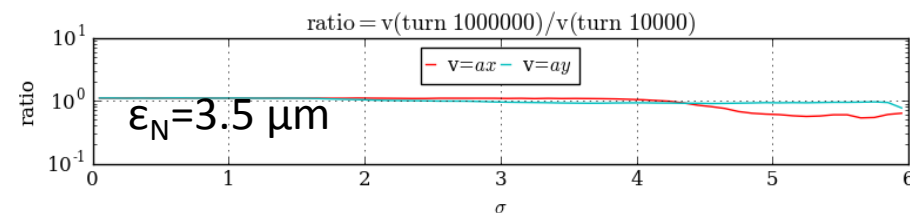
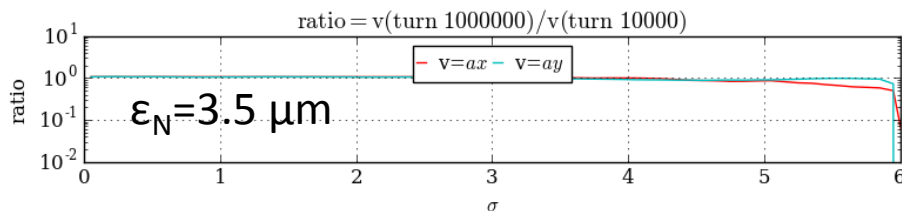
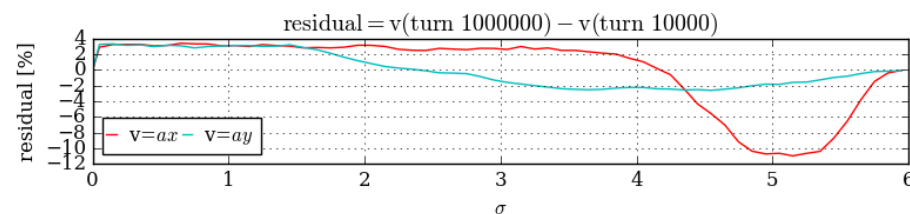
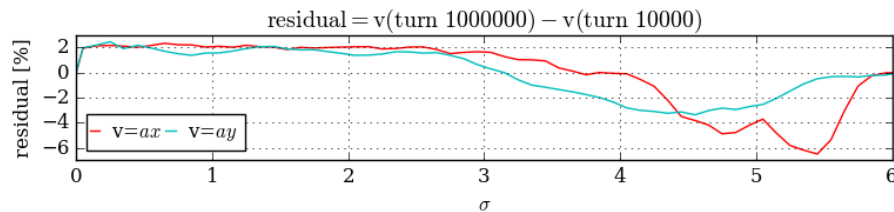
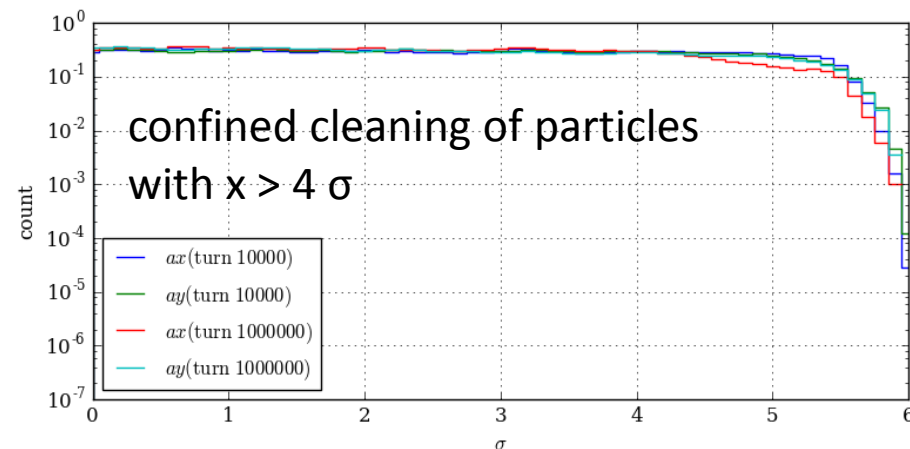
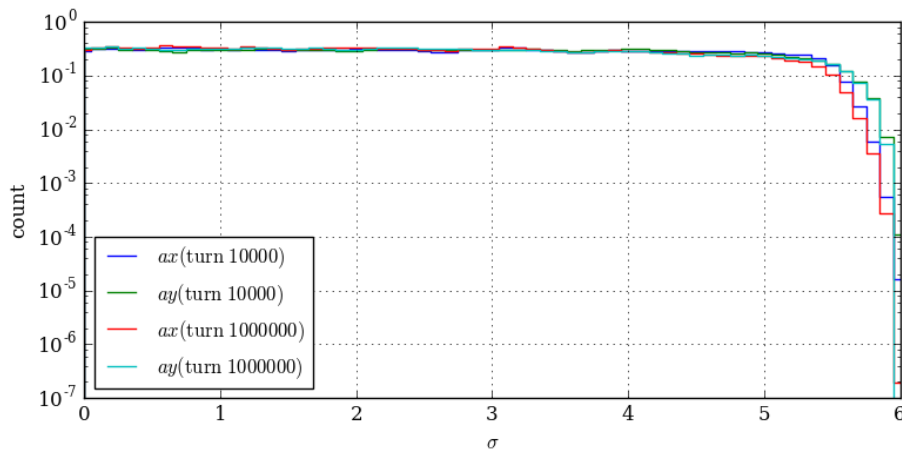
Histograms

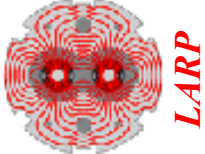


Injection tunes ($Q_x=.28, Q_y=.31$), $I_{\text{wire}} < 0$

WIRE LEFT: $I_{\text{wire,L}}=-350$ A, $I_{\text{wire,R}}=0$ A,
 $d_{\text{jaw-beam,L}}=5.7 \sigma$, $I_{\text{oct}}=0$ A

WIRE LEFT: $I_{\text{wire,L}}=-350$ A, $I_{\text{wire,R}}=0$ A,
 $d_{\text{jaw-beam,L}}=5.7 \sigma$, $I_{\text{oct}}=+10$ A

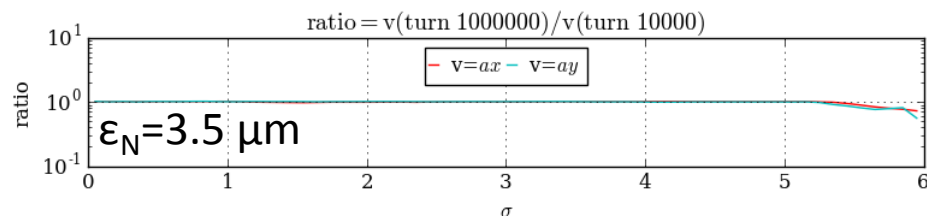
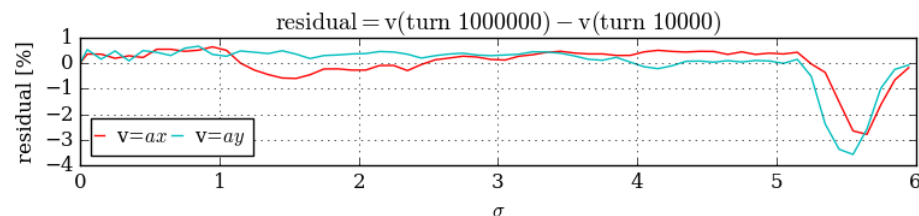
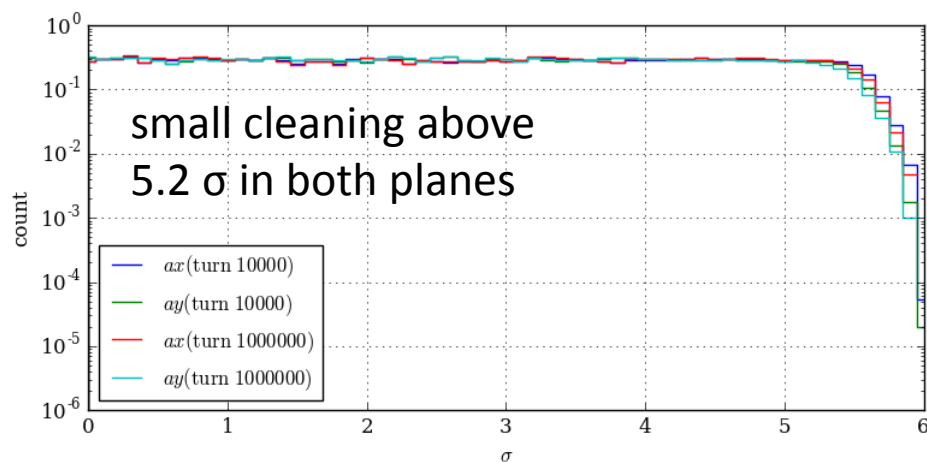


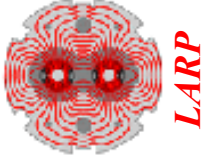


Histograms

Injection tunes ($Q_x=.28, Q_y=.31$), $I_{\text{wire}} < 0$

WIRE RIGHT: $I_{\text{wire,L}}=0$ A, $I_{\text{wire,R}}=-350$ A,
 $d_{\text{jaw-beam,L}}=5.7 \sigma$, $I_{\text{oct}}=+10$ A





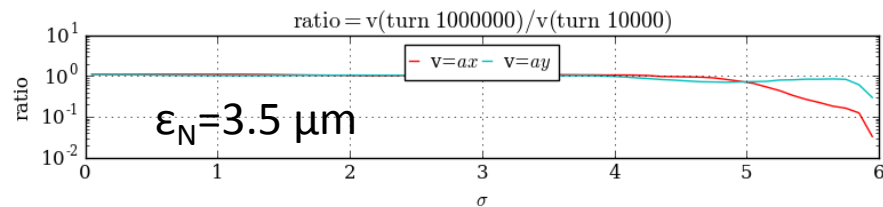
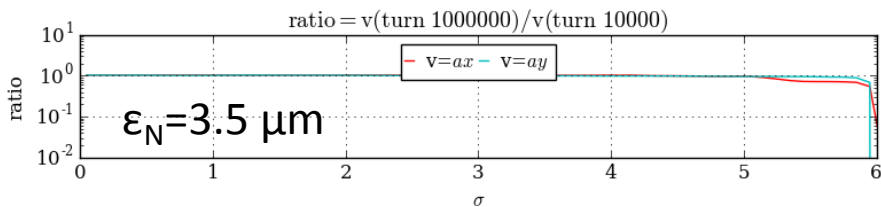
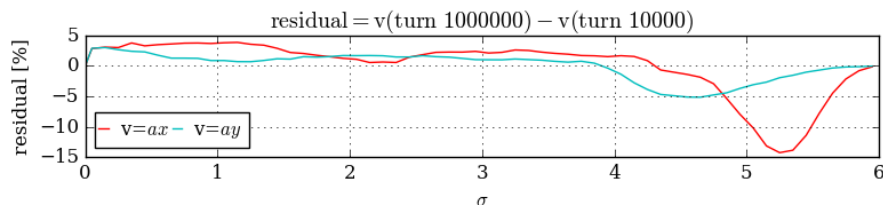
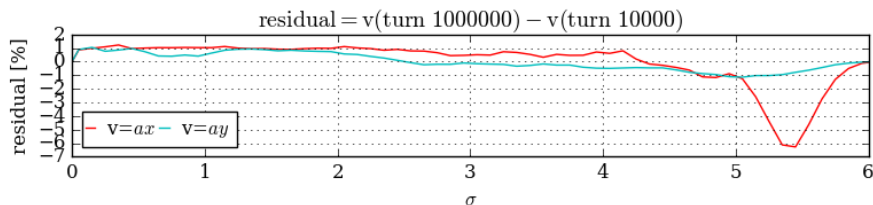
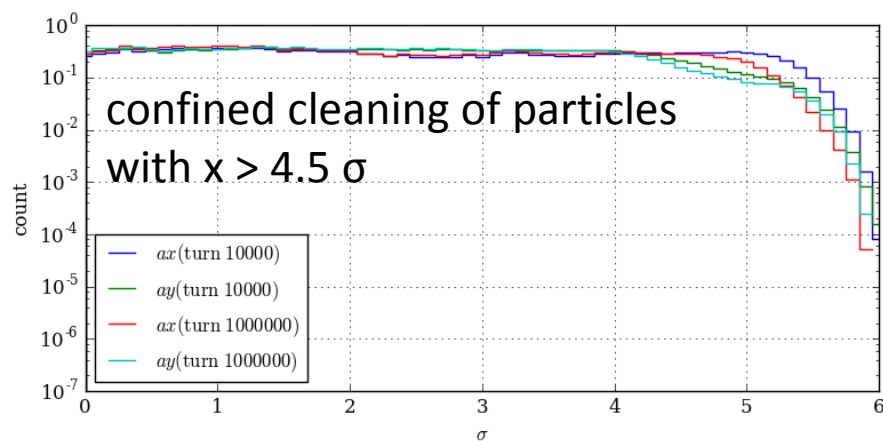
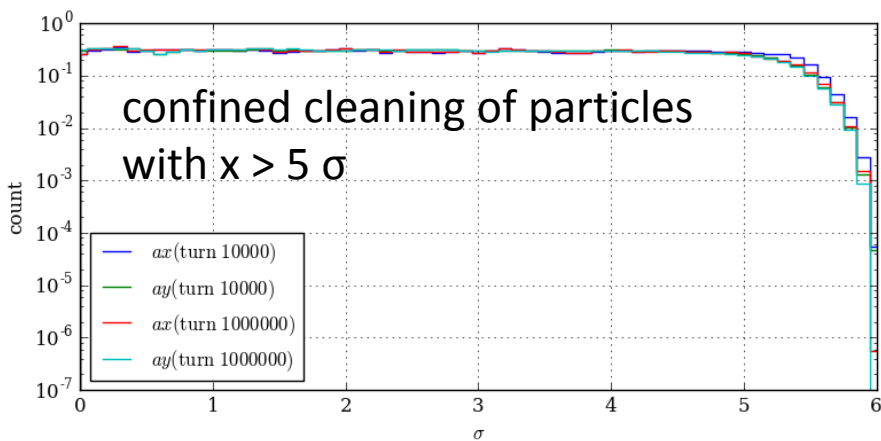
Histograms

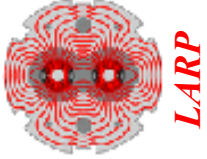


Injection tunes ($Q_x=.28, Q_y=.31$), $I_{\text{wire}} > 0$

WIRE LEFT: $I_{\text{wire,L}}=+350$ A, $I_{\text{wire,R}}=0$ A,
 $d_{\text{jaw-beam,L}}=5.7 \sigma$, $I_{\text{oct}}=0$ A

WIRE LEFT: $I_{\text{wire,L}}=-350$ A, $I_{\text{wire,R}}=0$ A,
 $d_{\text{jaw-beam,L}}=5.7 \sigma$, $I_{\text{oct}}=+10$ A



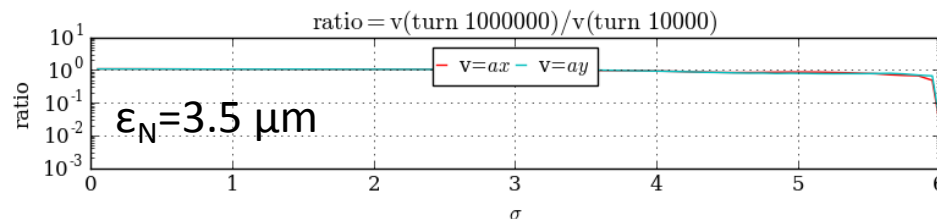
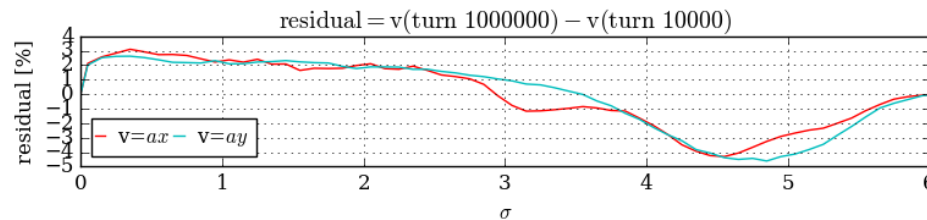
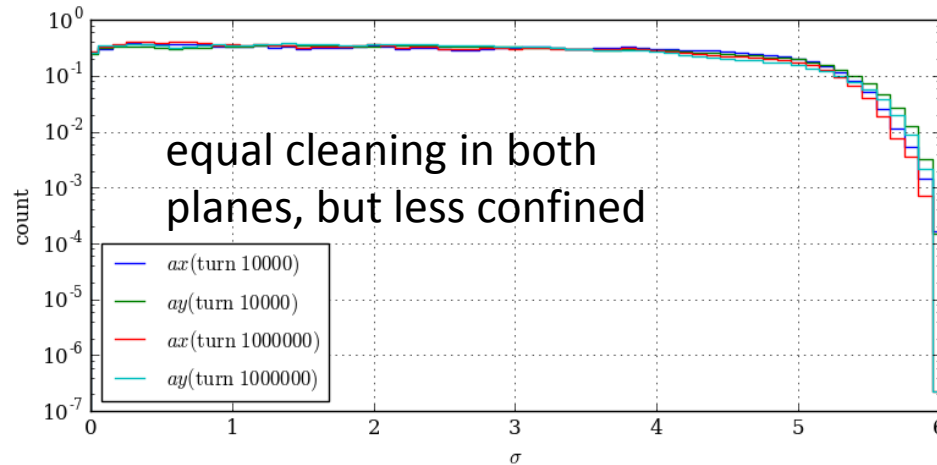


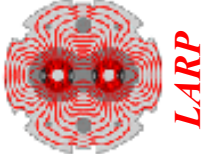
Histograms



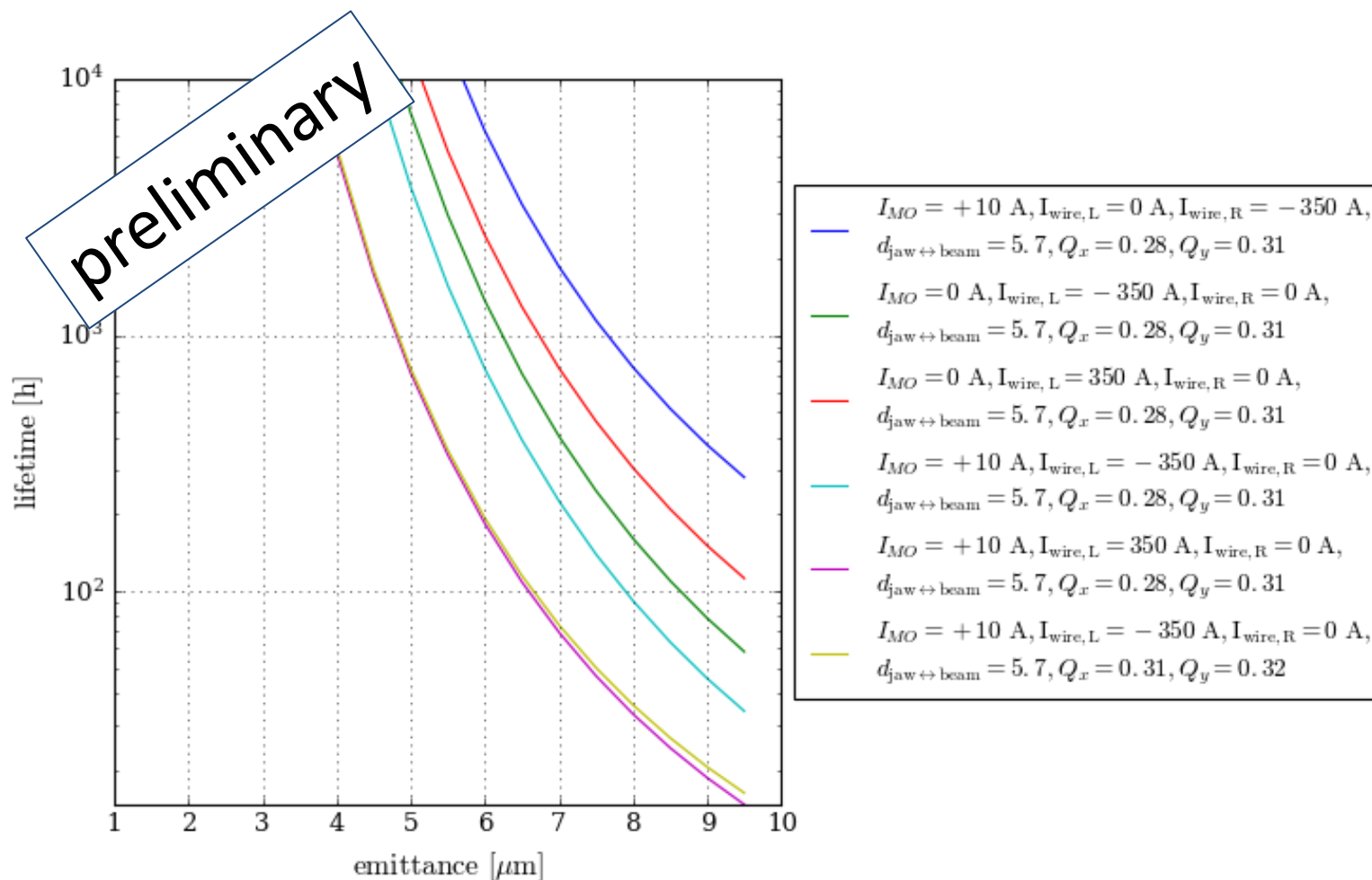
collision tunes ($Q_x=.31, Q_y=.32$)

WIRE LEFT: $I_{\text{wire,L}}=-350 \text{ A}, I_{\text{wire,R}}=0 \text{ A},$
 $d_{\text{jaw-beam,L}}=5.7 \sigma, I_{\text{oct}}=+10\text{A}$



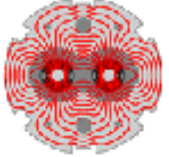


Expected lifetimes

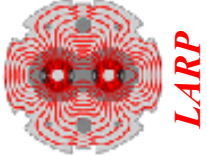


- Gaussian distribution assumed for lifetime calculation. Lifetime obtained from uniform distribution in x and y.
- from 100 – 700 of 10 000 are lost -> still small statistics?

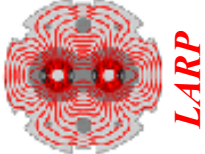
Conclusion



- effect of wire on lifetime is small at injection even at minimal separation of $d_{\text{jaw} \leftrightarrow \text{beam}} = 5.7 \sigma$ and current of $I_{\text{wire}} = 350 \text{ A}$
 - effect of WIRE RIGHT is small compared to WIRE LEFT due to different ratio in beta function
 - wire contributes considerably to the tune spread
- ⇒ tune spread generated by octupoles might be compensated by wire (e.g. thin line for $I_{\text{wire}} > 0$)
- without octupoles, wire cleans in horizontal plane ($1/r$ potential)
 - with octupoles, the effect of the wire on the tail particles depends on:
 - the non-linearities present
 - the working point
- ⇒ effect of wire on tail particles depends strongly on machine configuration (mainly tune and octupoles)
- ⇒ **wire does not necessarily deplete particles uniformly in x and y**



Backup



Crossing scheme



Calculation of $d_{\text{jaw-beam}}$:

1. use sigma of ideal beam optics to calculate the opening of the distance between the beam and the jaw $d_{\text{jaw-beam}}$

2. add the distance between collimator and wire with $d_{\text{jaw-wire}} = 3 \text{ mm}$

$$d_{\text{beam-wire}} = d_{\text{jaw-beam}} + d_{\text{jaw-wire}} = n \sigma_{\text{col}} + 3 \text{ mm}$$

3. calculate displacement of wire:

a. assume that collimator will be perfectly aligned around orbit -> calculate orbit at wire at the end (after bb, error assignment, tune adjustment etc.)

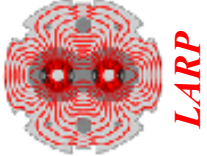
b. assume that wire is at inner jaw between the two beams (see x-scheme)

$$x_{\text{wire,left}} = -(d_{\text{jaw-beam}} + d_{\text{jaw-wire}}) + x_{\text{closed orbit}}$$

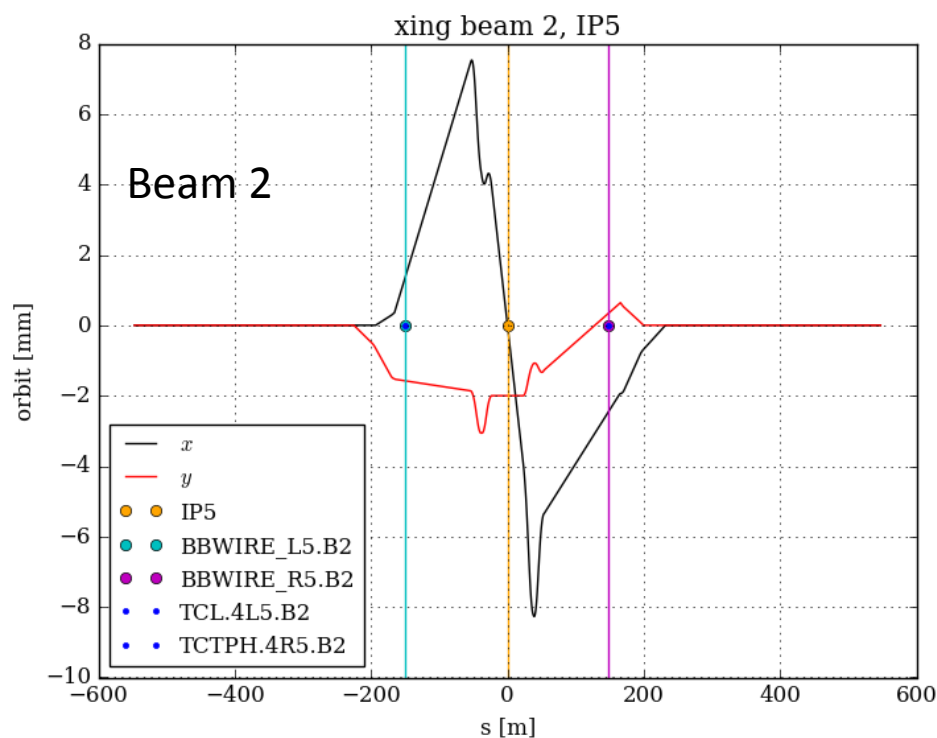
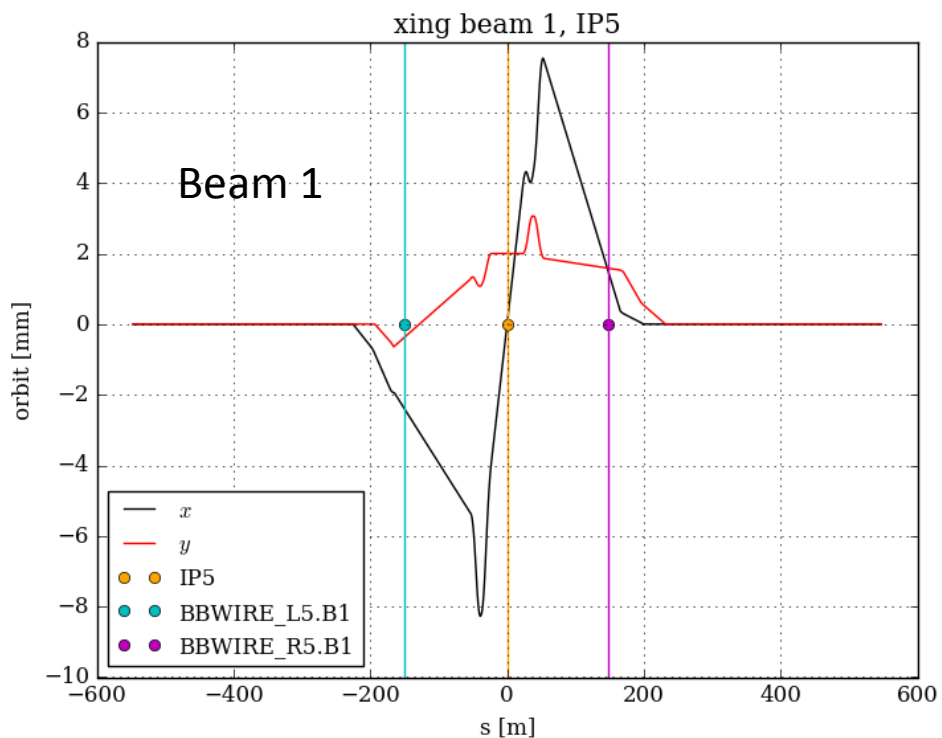
$$x_{\text{wire,right}} = (d_{\text{jaw-beam}} + d_{\text{jaw-wire}}) + x_{\text{closed orbit}}$$

$$y_{\text{wire,left}} = y_{\text{closed orbit}}$$

$$y_{\text{wire,right}} = y_{\text{closed orbit}}$$



Crossing scheme



wire placed between both beams in H, on orbit in V:

BBWIRE_L5: $x < 0, y < 0$

BBWIRE_L5: $x > 0, y > 0$