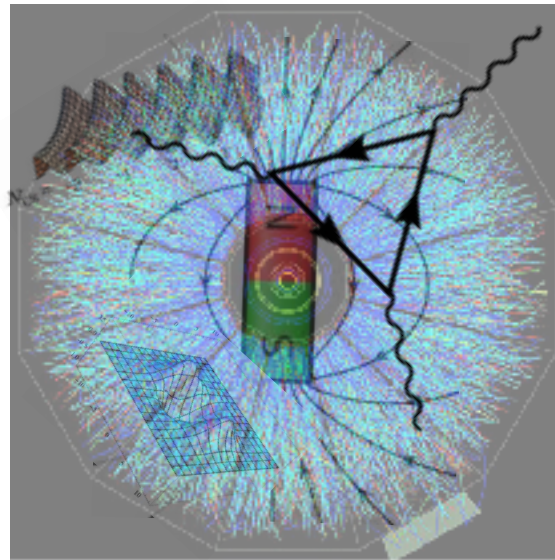


# **Magnetic Field & Fluid Rotation in Heavy Ion Collisions**



**Jinfeng Liao 廖劲峰**

Indiana University, Physics Dept. & CEEM

Central China Normal University

**Research Supported by NSF & DOE**



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# The Bigger Picture

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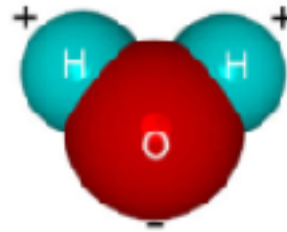
# Nuclear Matter: At the Heart of All Matter

*The physical world has a hierarchy of structures.*

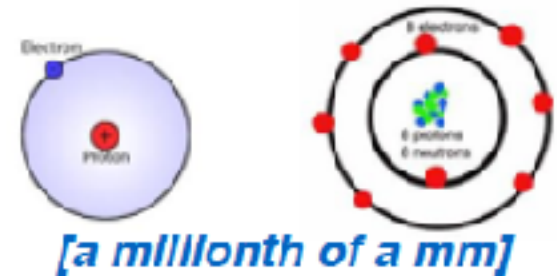
**matter**



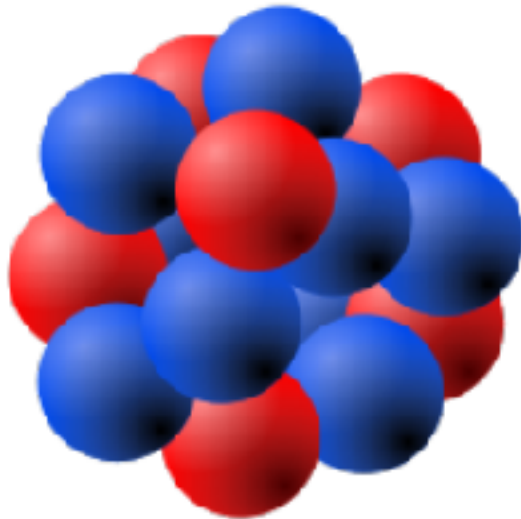
**molecule**



**atoms**

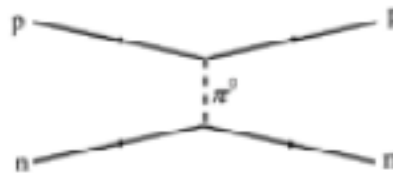


**atomic nucleus**



*[a trillionth of a mm]*

**proton**



**nuclear force**



**neutron**

**Most basic entities:  
quarks  
and  
gluons.**

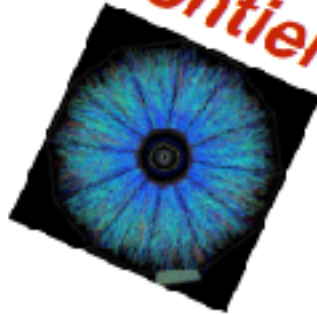
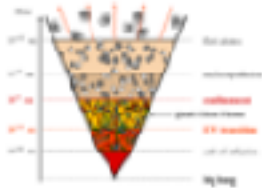


**Quantum Chromodynamics (QCD)**

# A Map of Nuclear Matter

Temperature

**“Hot Frontier”**

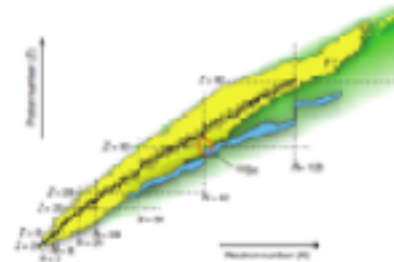


Emergent Properties  
from the same QCD!

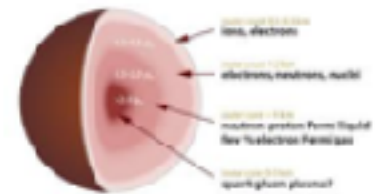
**“Force Frontier”**



Normal  
Matter



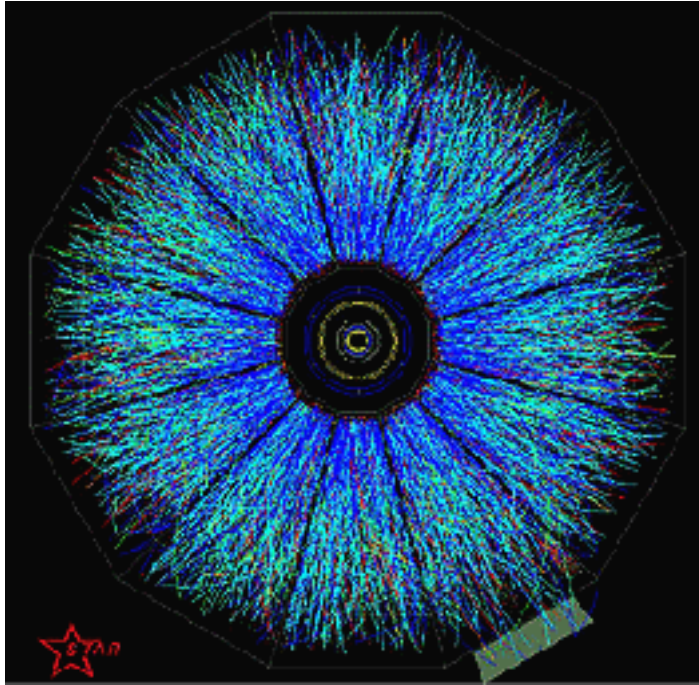
**“Dense Frontier”**



Baryon Density

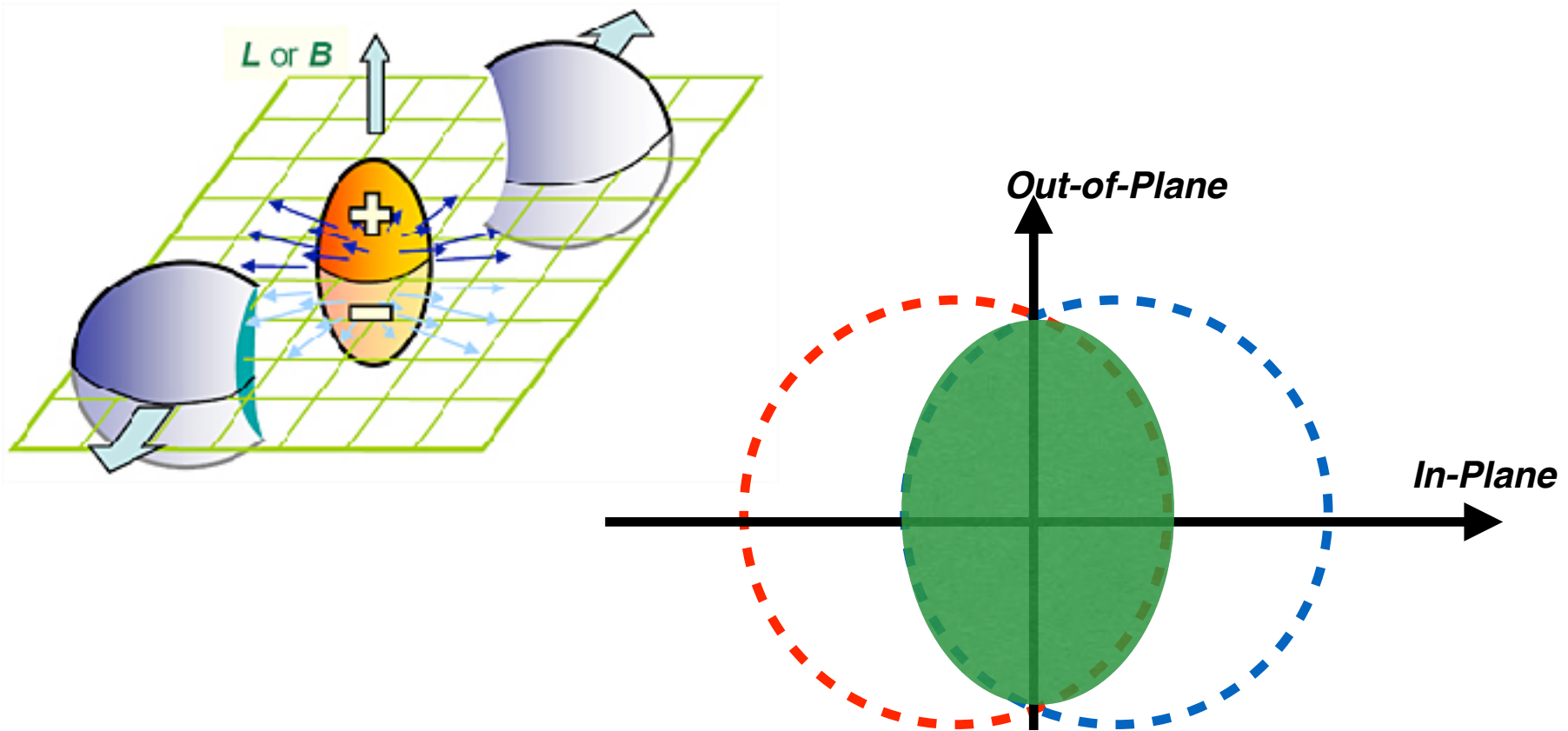
This talk will focus on the “hot frontier”.

# “Little Bang” in High Energy Nuclear Collision



- \* Quark-gluon plasma (QGP) is created in such collisions.*
- \* It is PRIMORDIALLY HOT ~ trillion degrees ~ early universe.*

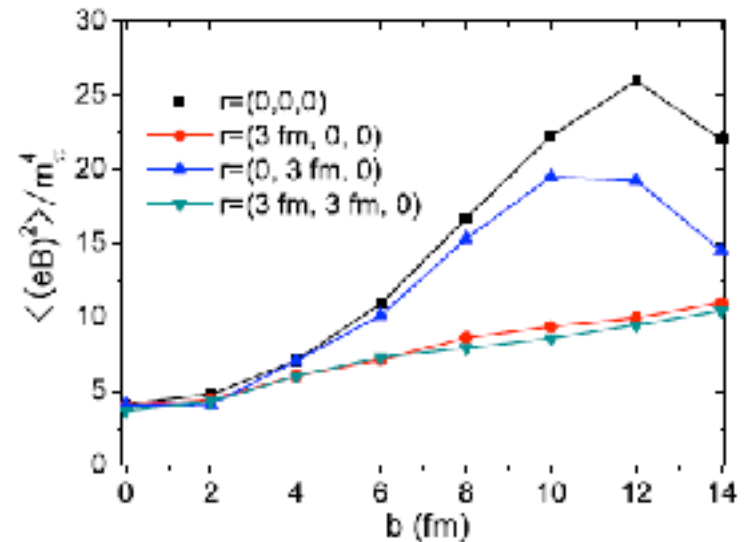
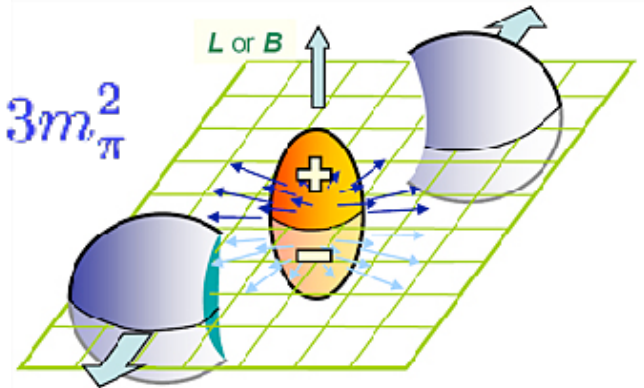
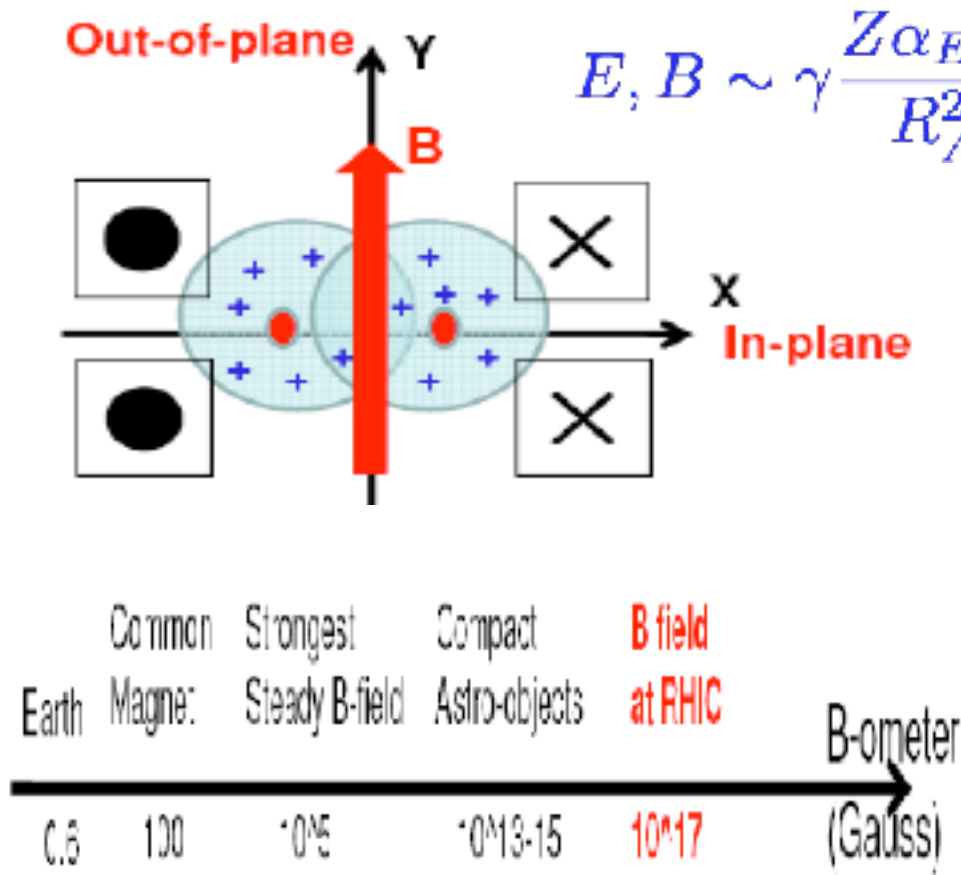
# New Phase & New Extreme Conditions



*The quark-gluon plasma is a type of CHIRAL MATTER, with (approximately) chiral quarks.*

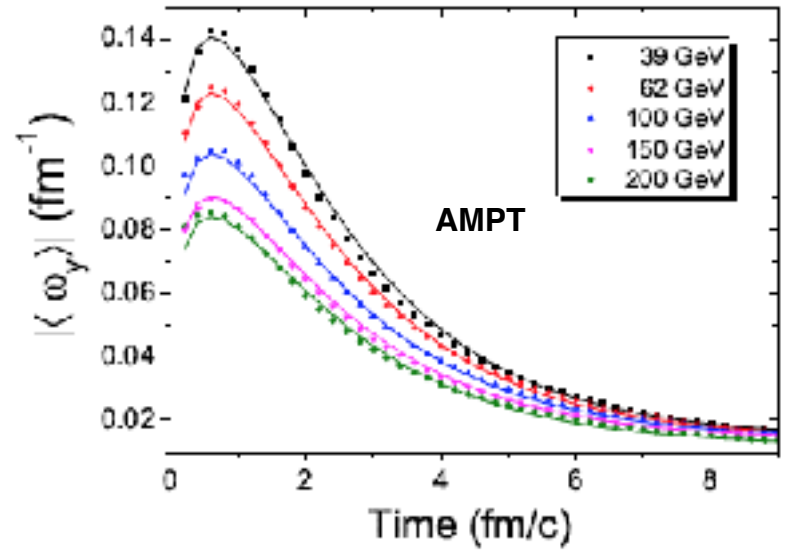
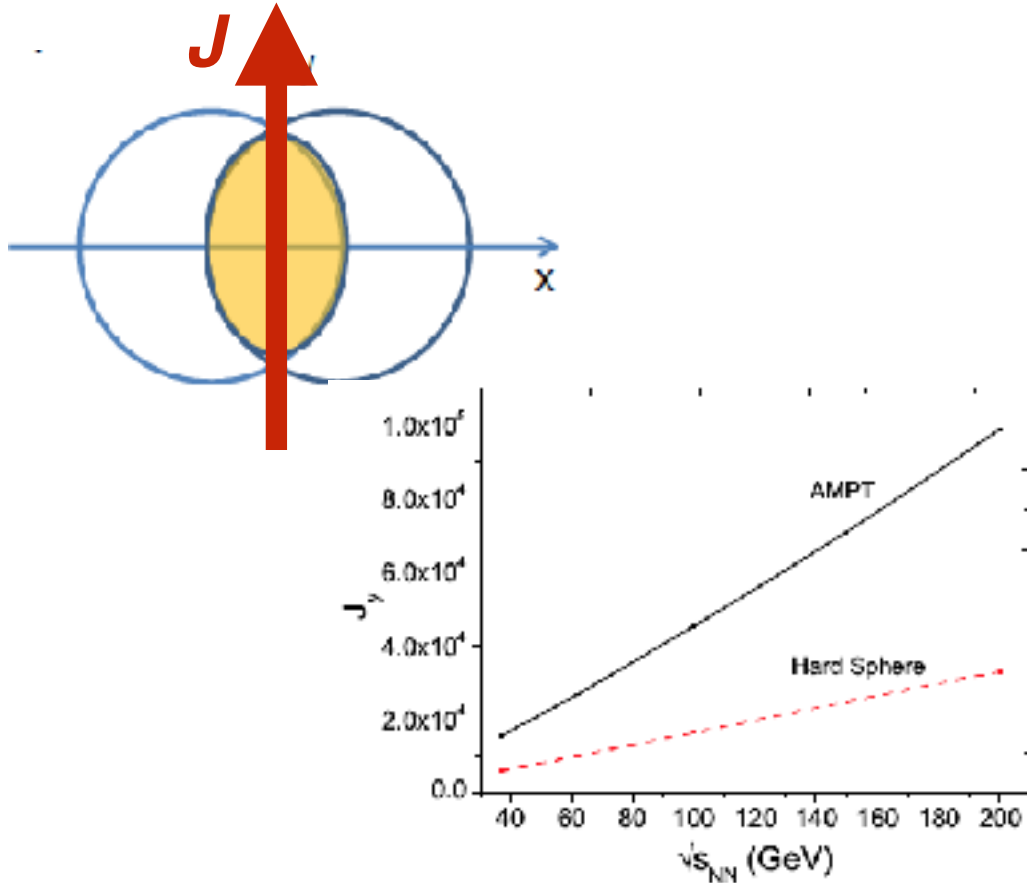
*Heavy ion collision environment:  
extremely strong magnetic field and fluid rotation!*

# The Strongest EM Fields in Heavy Ion Collisions



- **Strongest** B field (and strong E field as well) naturally arises!  
[Kharzeev, McLerran, Warringa; Skokov, et al; Bzdak-Skokov; Deng-Huang; Błoczyński-Huang-Zhang-Liao; Skokov-McLerran; Tuchin; ...]
- “Out-of-plane” orientation (approximately)

# The Most Vortical Fluid in Heavy Ion Collisions



Yin Jiang, Zi-Wei Lin, JL,  
arXiv:1602.06580[hep-ph]

***The fluid created in heavy ion collisions carries extremely large angular momentum and local vorticity.***



# Properties of Matter under New Conditions

**Very strong magnetic field**  
—> **Magnetic Polarization!**

**Very strong global rotation**  
—> **Rotational Polarization!**

**Nontrivial interplay between external conditions & internal degrees of freedom (spin/momentum/angular momentum)**

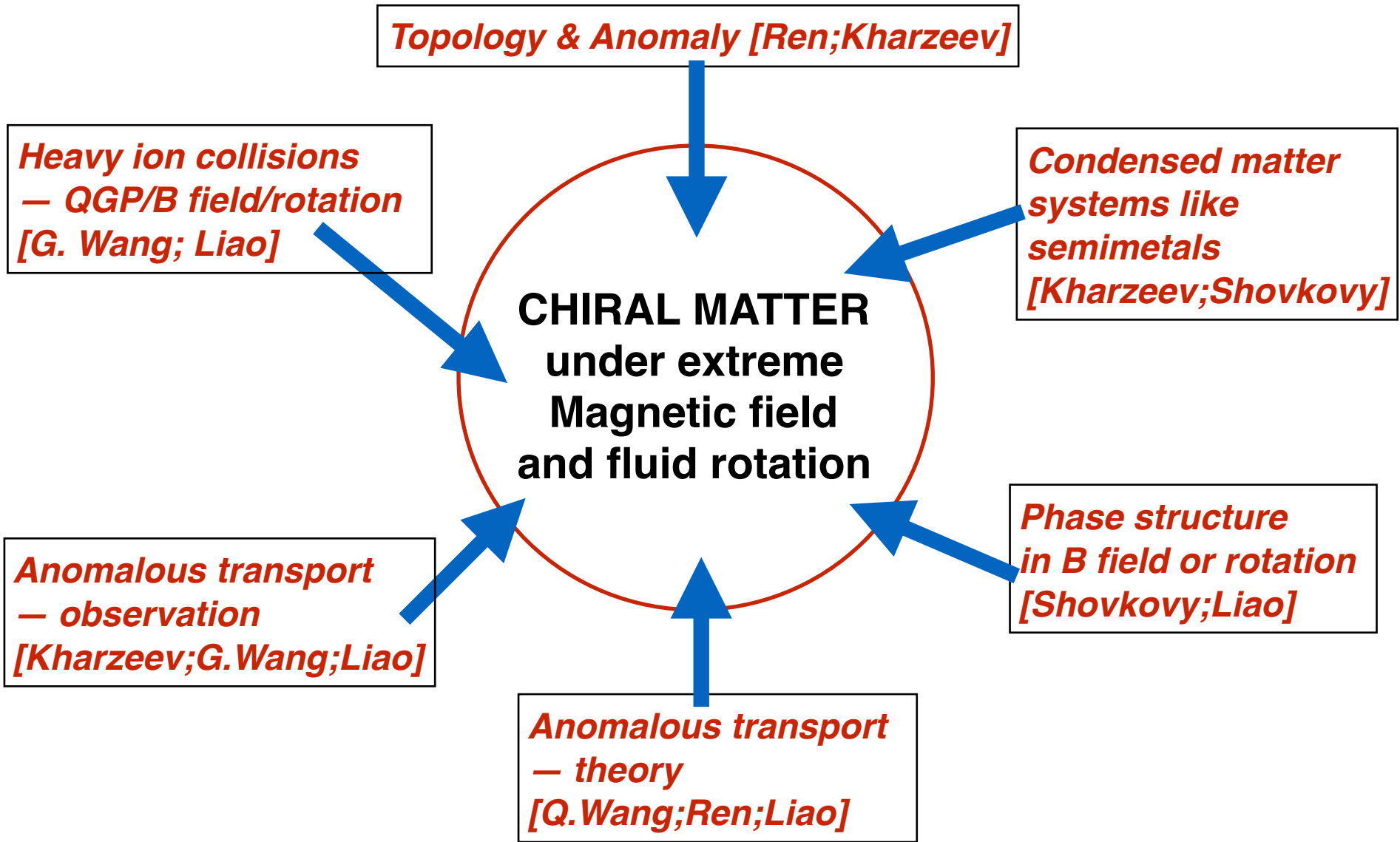
**Thermodynamic properties of matter:**

- \* **Equation of State**
- \* **Phase Structure**
- \* **Macroscopic Polarization**
- \* .....

**Transport properties of matter:**

- \* **Transport coefficients**
- \* **Anomalous transport effects**
- \* .....

# An Overall Look at the Present Summer School



# Quantifying External Conditions in H.I.C.

*In the first three lectures,  
I will give you  
a hands-on tutorial  
on how to compute  
such new external conditions as  
magnetic field and fluid rotation  
in heavy ion collisions.*

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# Computing Magnetic Fields in Heavy Ion Collisions

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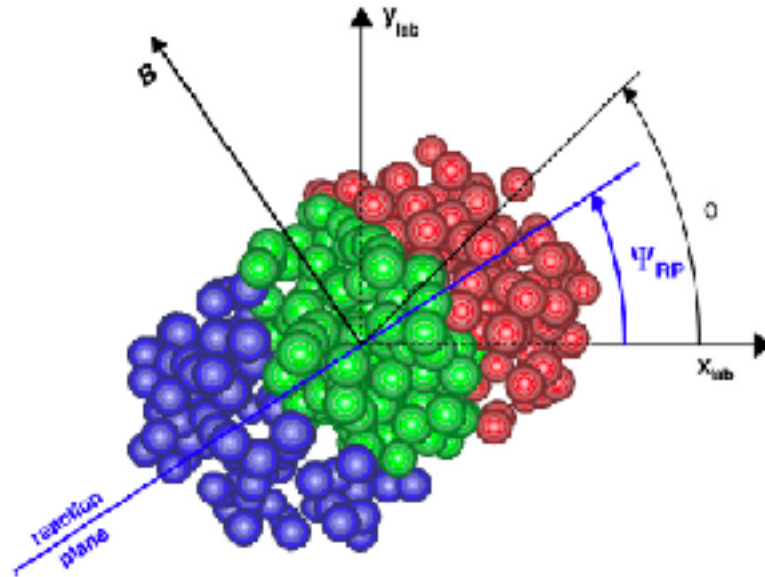
**A (very incomplete!) list of recent references on computation of magnetic fields**

- \* Deng, Huang, arXiv:1201.5108 ; \* Bzak, Skokov, arXiv:1111.1949**
- \* Blocynski, Huang, Zhang, Liao, 1209.6594**
- \* McLerran, Skokov, arXiv:1305.0774; \* Tuichin, arXiv:1305.5806**
- \* Li, Sheng, Q. Wang, 1602.02223**
- \* Inghirami, Zanna, Beraudo, Moghaddam, Becattinni, Bleicher, arXiv:1609.03042**
- \* .....**

# Magnetic Field in Heavy Ion Collisions

***Blackboard***

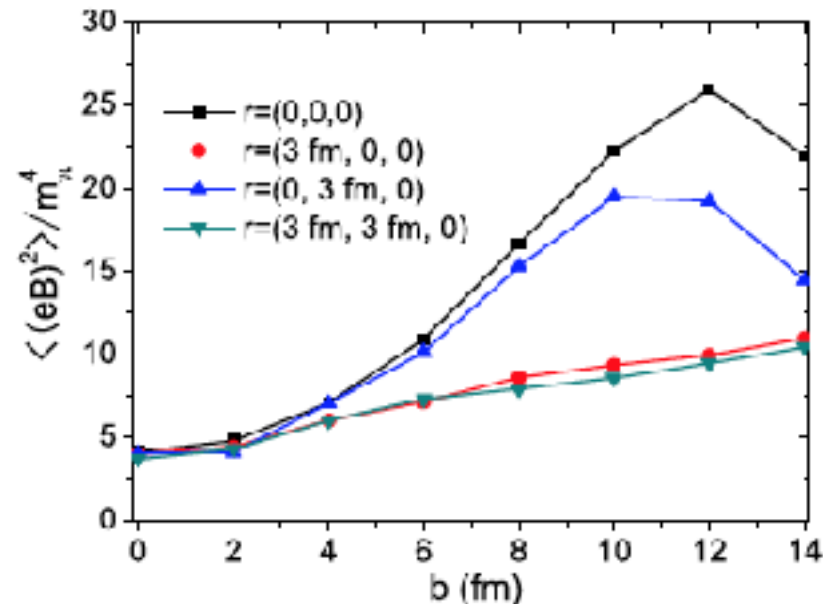
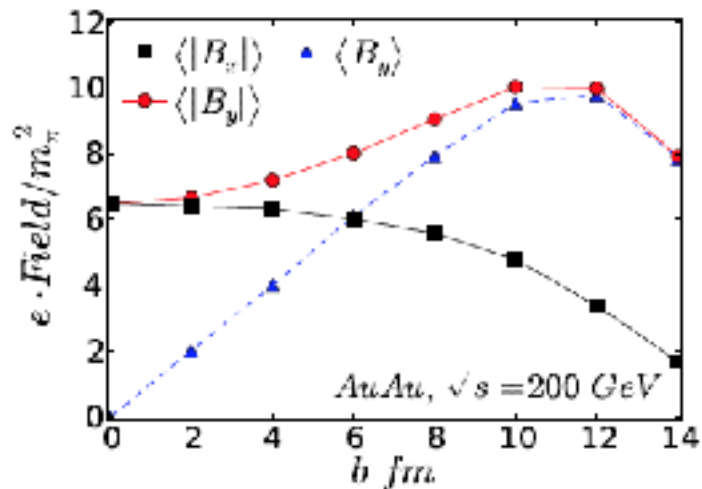
# More Realistic Computations



- \* *Glauber model (with discrete nucleons)*
- \* *Event-by-event with Monte-Carlo*
- \* *Finite size of proton*
- \* *Azimuthal angle fluctuations*
- \* *Time evolution further in medium??????*

# Event-By-Event Magnetic Fields

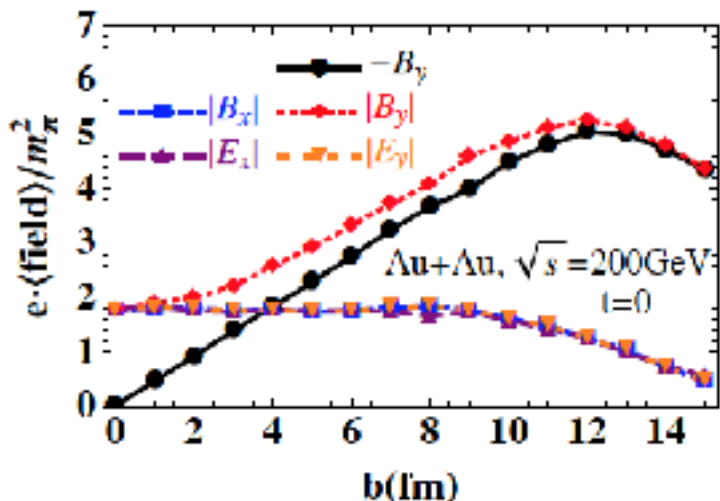
Bzdak & Skokov,  
arXiv:1111.1949



PLB 718 (2013) 1529  
[arXiv:1209.6594]

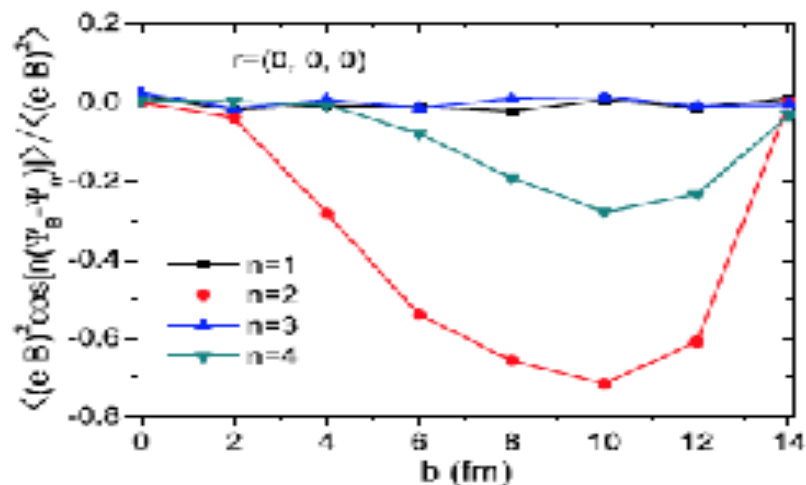
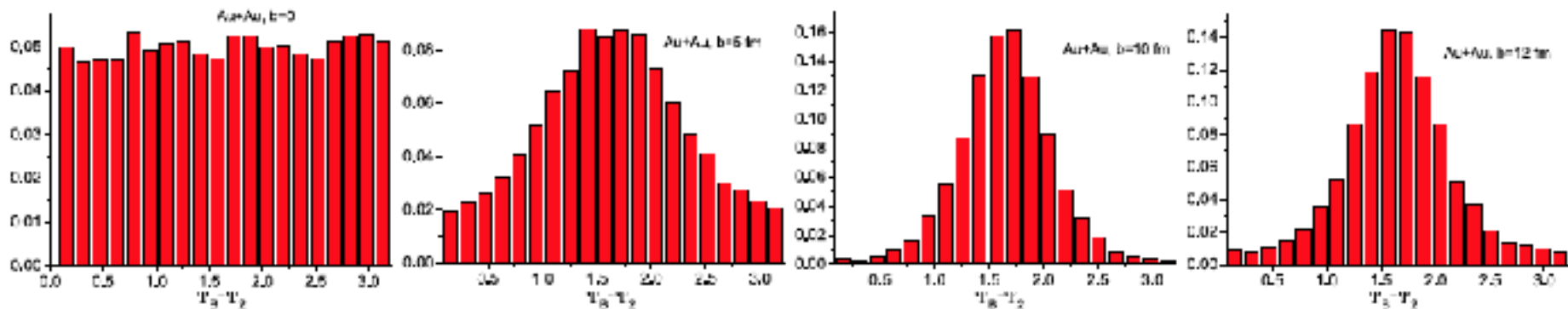
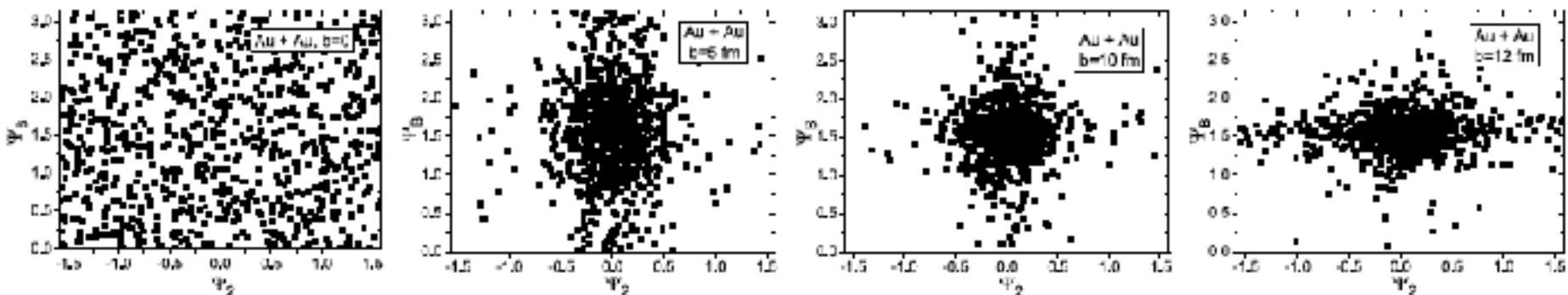


*Proton is a finite size object!*



Deng & Huang,  
arXiv:1201.5108

# Event-By-Event Magnetic Fields



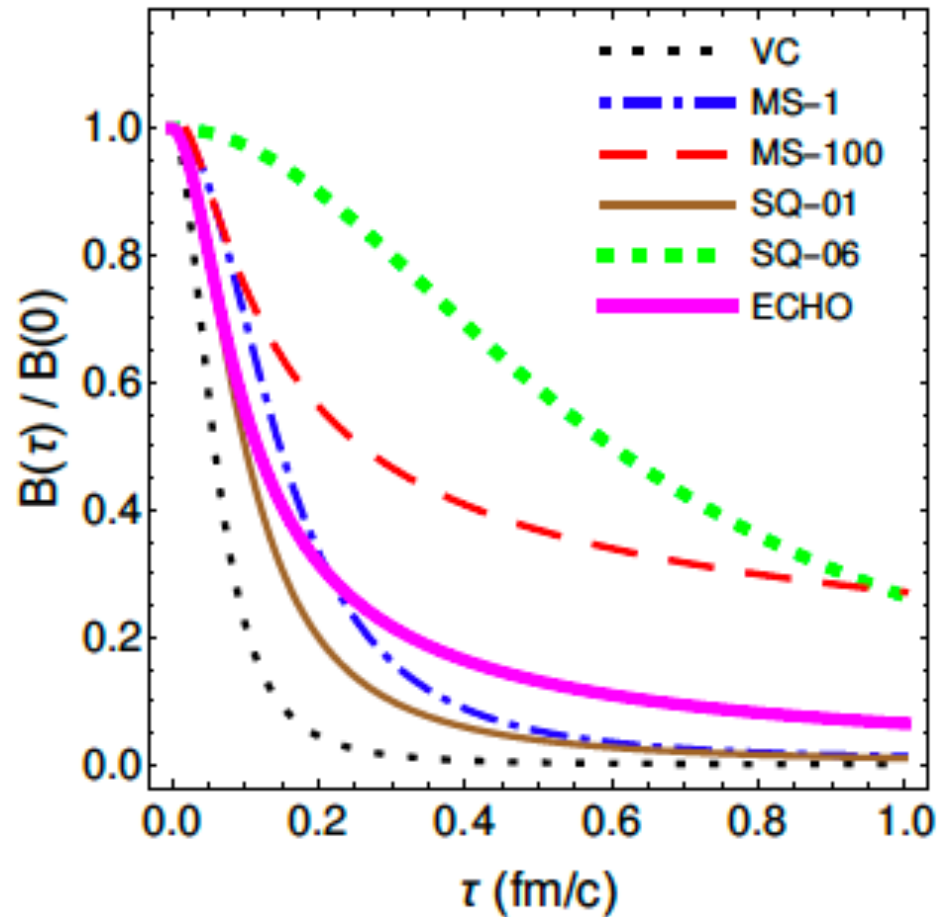
*Measurable effects (CME, CMW, photon  $v_2$ ,...) are controlled by:*

$$\langle (eB)^2 \cos(2\bar{\Psi}_B) \rangle$$

**PLB 718 (2013) 1529**  
**[arXiv:1209.6594]**



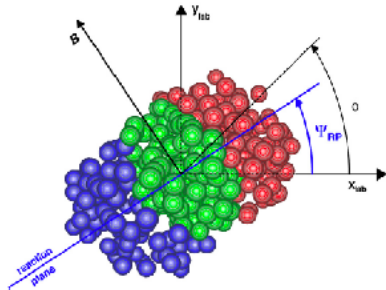
# Time Evolution of Magnetic Field



***The single biggest uncertainty in current understanding of magnetic fields in heavy ion collisions!***

# Small v.s. Large and Low v.s. High Energy

**Why we do NOT expect CME in pA collisions?**

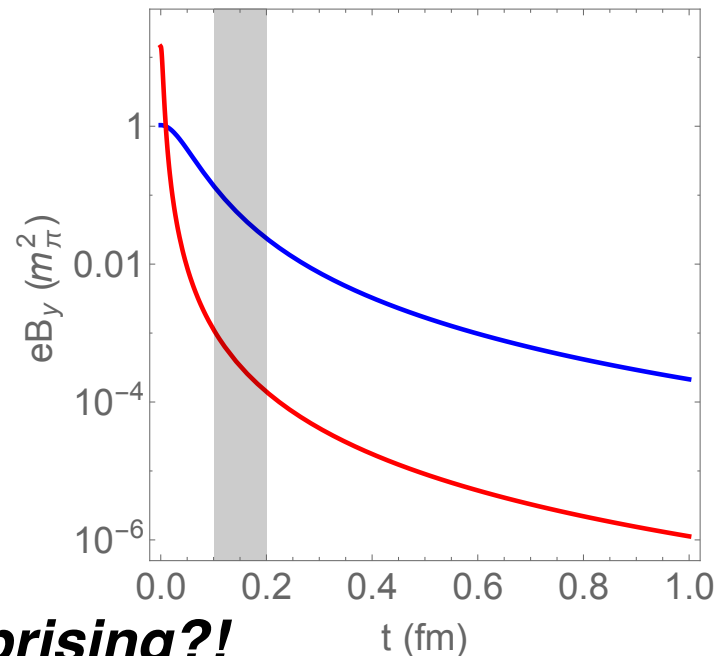
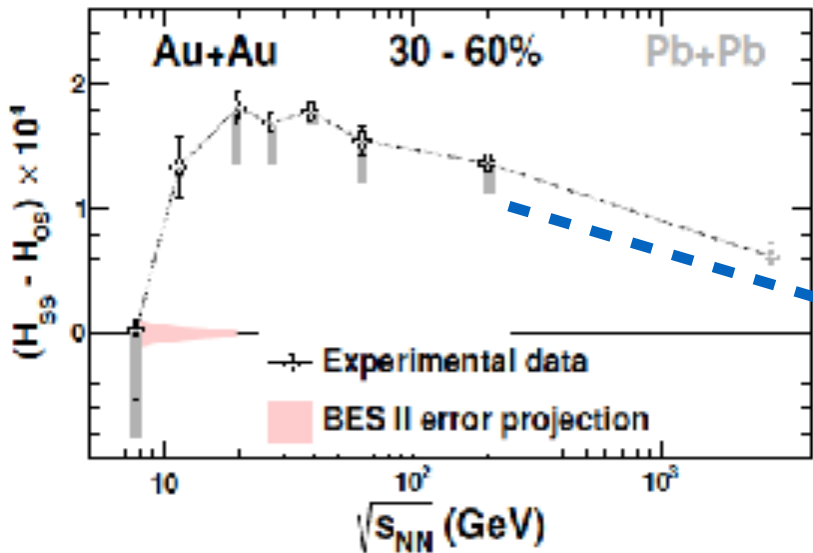


Angle de-correlation between B and event plane!!

$$\cos[2(\Psi_B - \Psi_2)]$$

CMS reported nice measurements at 5TeV.

**Why CME may be expected to disappear at 5TeV?**



**Perhaps not surprising?!**

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# Computing Fluid Rotation in Heavy Ion Collisions

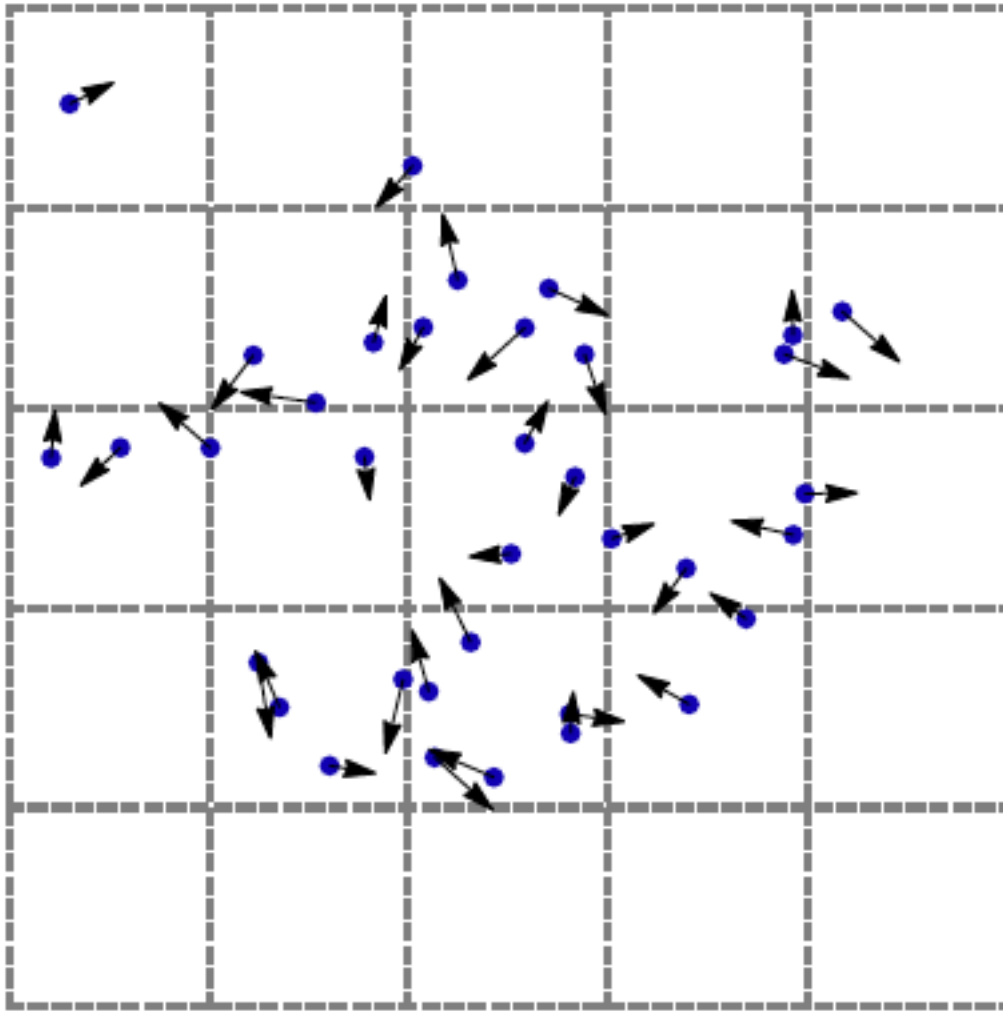
**A (very incomplete!) list of recent references on computation of fluid rotation**

- \* **Jiang, Lin, JL, arXiv:1602.06580**
- \* **Deng, Huang, arXiv:1603.06117**
- \* **Pang, Petersen, Q. Wang, X.-N. Wang, arXiv:1605.04024**
- \* **Becattinni, et al, arXiv:1501.04468**
- \* **Csernai, Magas, arXiv:1302.5310**
- \* **.....**

# Fluid Rotation in Heavy Ion Collisions

***Blackboard***

# Fluid Rotation in Heavy Ion Collisions



$$\vec{J} = \int d^3r \vec{r} \times \vec{p}(\vec{r}).$$

$$\vec{v}(\vec{r}) = \vec{p}(\vec{r}) / \epsilon(\vec{r})$$

$$\vec{\omega} = \nabla \times \vec{v}$$

***Simulations with AMPT model  
[Jiang,Lin,Liao, PRC2016]***

# Angular Momentum Carried by Fireball

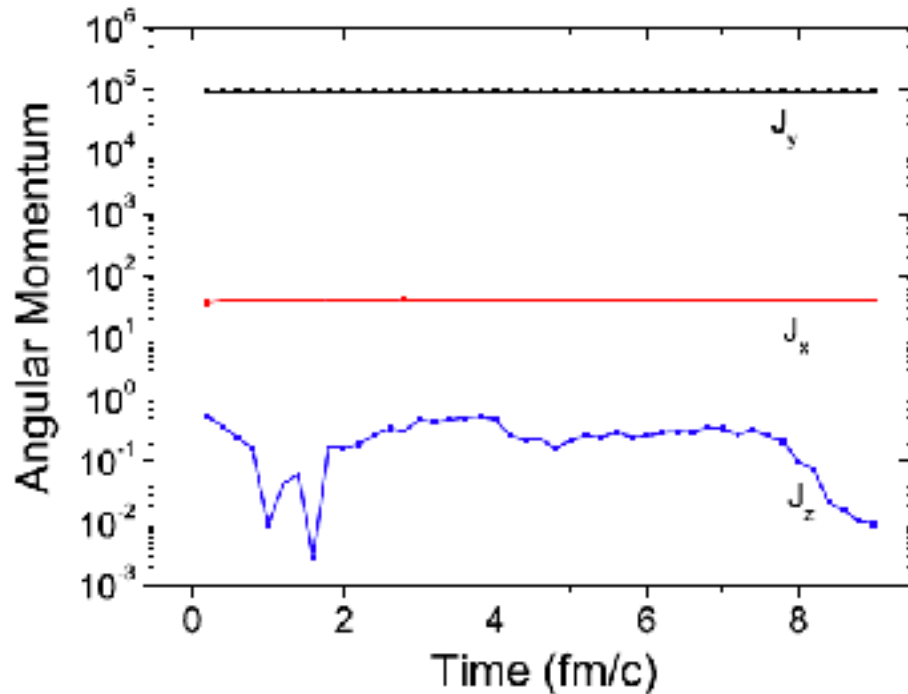
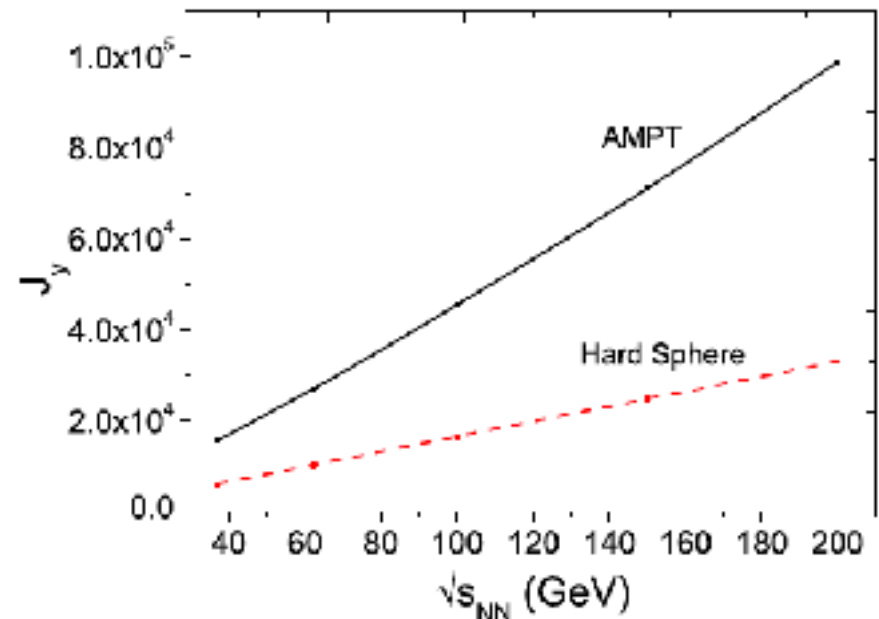
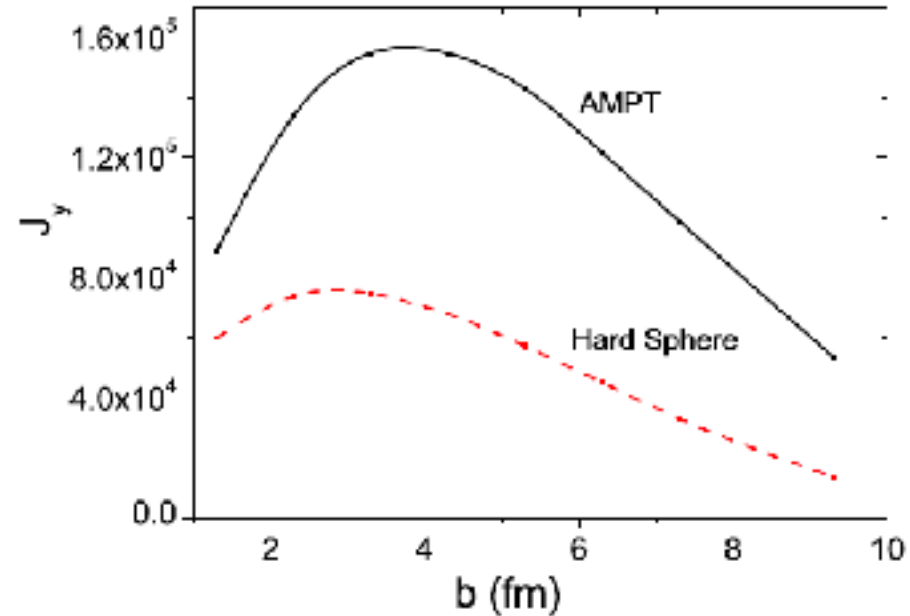


FIG. 2. Angular momentum from the AMPT model at  $b = 7$  fm and  $\sqrt{s_{NN}} = 200$  GeV.



**Simulations with AMPT model**  
**[Jiang, Lin, Liao, PRC2016]**

# Fluid Rotation in Heavy Ion Collisions

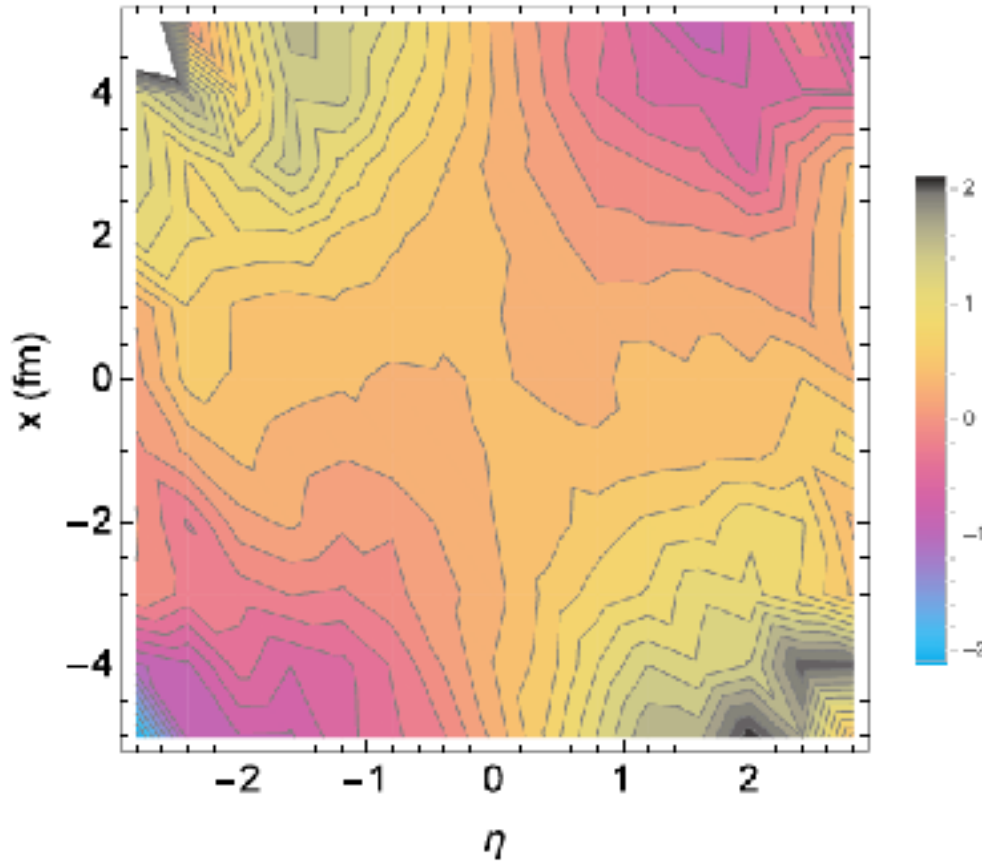


FIG. 5.  $\omega_y$  (in the unit of  $\text{fm}^{-1}$ ) profile at  $y = 0$  and  $t = 1 \text{ fm}/c$ , with  $b = 7 \text{ fm}$  and  $\sqrt{s_{NN}} = 200 \text{ GeV}$ .

**Simulations with AMPT model**  
**[Jiang, Lin, Liao, PRC2016]**

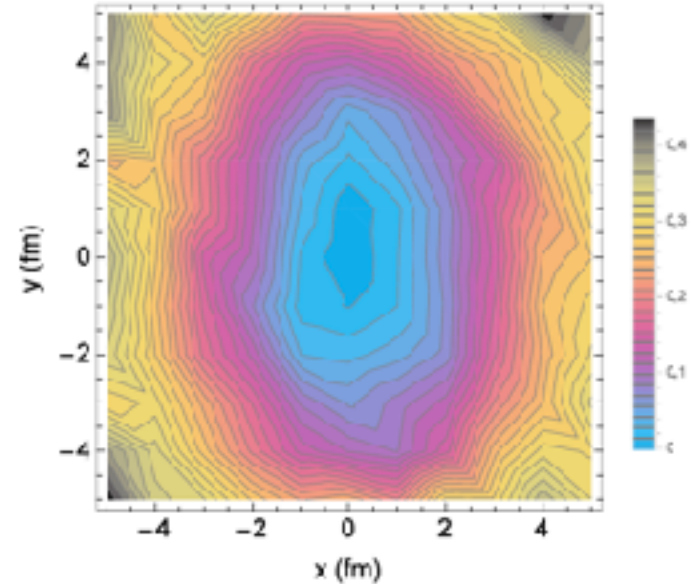


FIG. 10. Radial velocity profile at  $\eta = 1$  and  $t = 1 \text{ fm}/c$ , with  $b = 7 \text{ fm}$  and  $\sqrt{s_{NN}} = 200 \text{ GeV}$ .

$$\vec{v}(\rho, \phi, \eta) = \hat{e}_\rho v_0(\rho, \eta) [1 + 2c_2(\rho, \eta) \cos 2\phi],$$

$$\begin{aligned} \omega_y &= \frac{\partial v_\rho}{\partial z} \cos \phi \\ &= \frac{2}{t} (ch\eta)^2 \partial_\eta (v_0 + 2v_0 c_2 \cos 2\phi) \cos \phi \\ &= \frac{2}{t} (ch\eta)^2 \left(\frac{x}{\rho}\right) \partial_\eta \left[ v_0 + 2v_0 c_2 \left(2\frac{x^2}{\rho^2} - 1\right) \right]. \end{aligned}$$

# Fluid Rotation in Heavy Ion Collisions

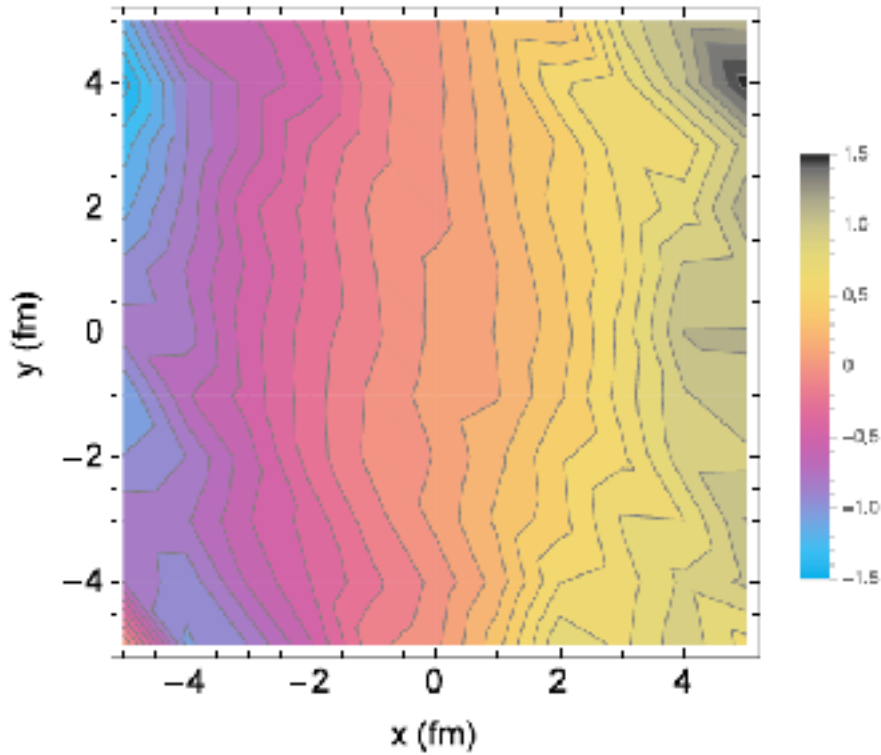


FIG. 7.  $\omega_y$  profile at  $\eta = -1$  and  $t = 1$  fm/c, with  $b = 7$  fm and  $\sqrt{s_{NN}} = 200$  GeV.

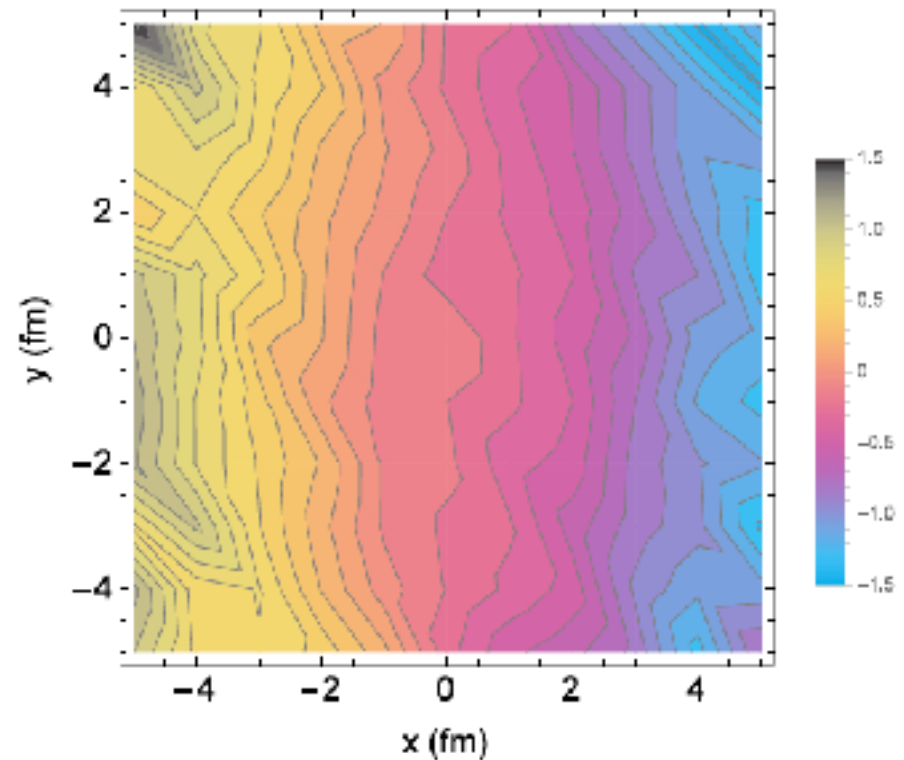
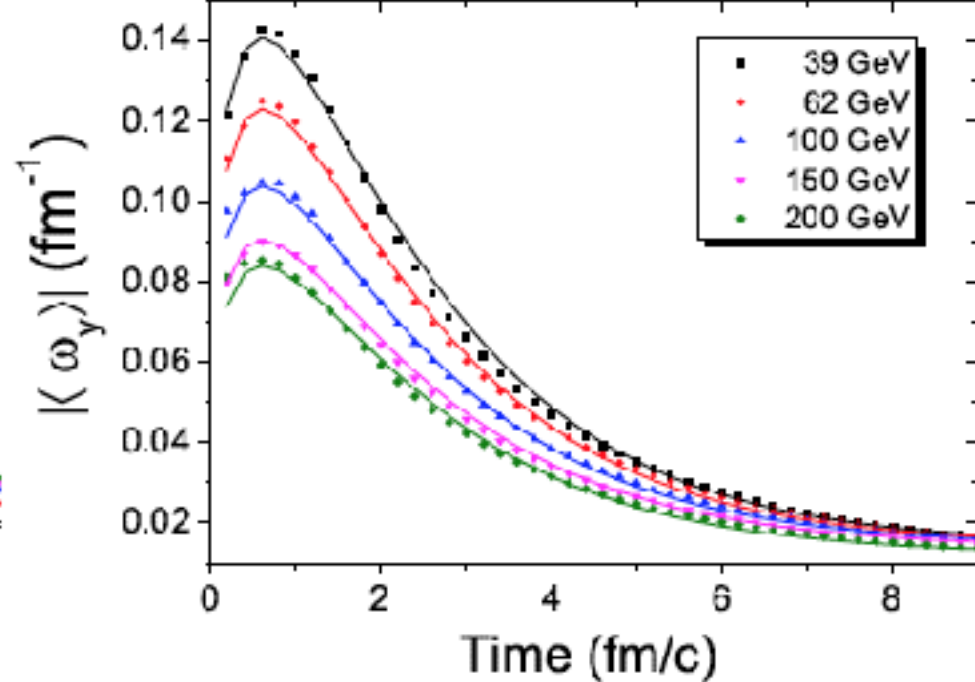
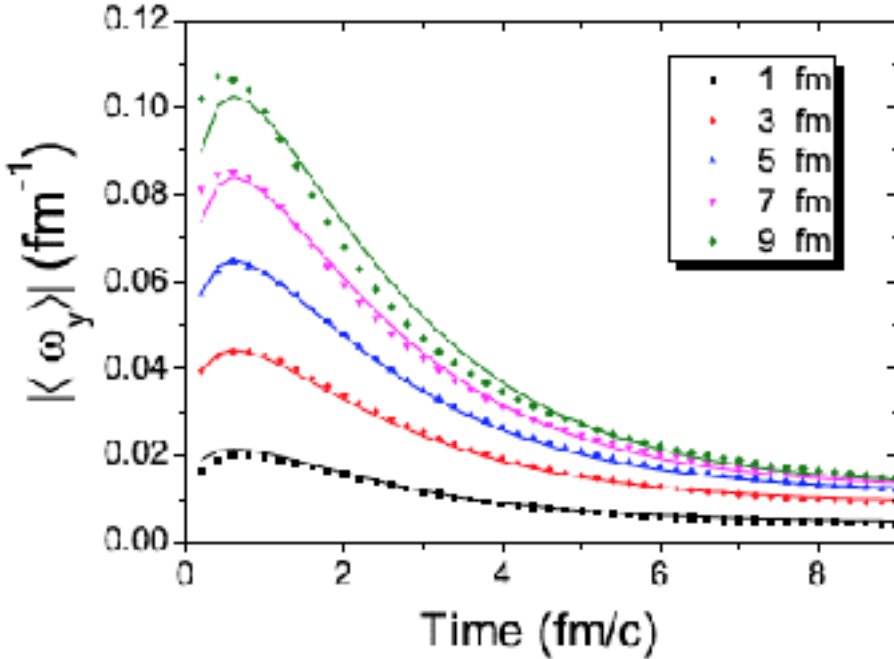


FIG. 6.  $\omega_y$  profile at  $\eta = 1$  and  $t = 1$  fm/c, with  $b = 7$  fm and  $\sqrt{s_{NN}} = 200$  GeV.

***Simulations with AMPT model  
[Jiang,Lin,Liao, PRC2016]***



# Quantifying Rotation of QGP



**Convenient parameterization:**

$$\langle \omega_y \rangle(t, b, \sqrt{s_{NN}}) = A(b, \sqrt{s_{NN}}) + B(b, \sqrt{s_{NN}}) (0.58t)^{0.35} e^{-0.58t}$$

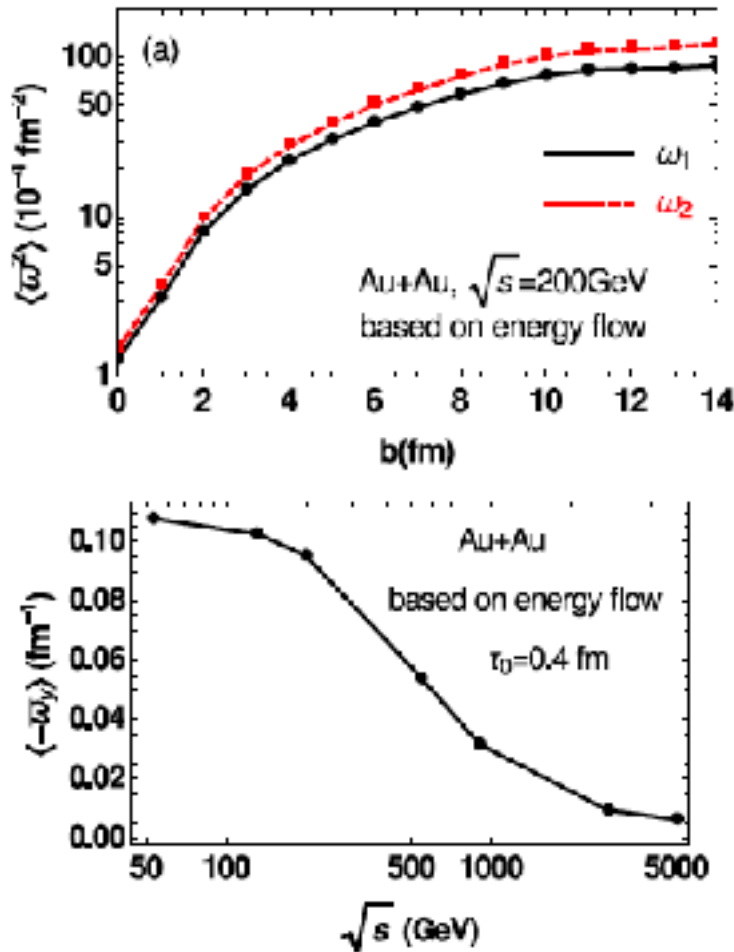
$$A = \left[ e^{-0.016b\sqrt{s_{NN}}} + 1 \right] \times \tanh(0.28b) \times [0.001775 \tanh(3 - 0.015\sqrt{s_{NN}}) + 0.0128]$$

$$B = \left[ e^{-0.016b\sqrt{s_{NN}}} + 1 \right] \times [0.02388b + 0.01203] \times [1.751 - \tanh(0.01\sqrt{s_{NN}})] .$$

**Yin Jiang, Zi-Wei Lin, JL,  
arXiv:1602.06580[hep-ph]**

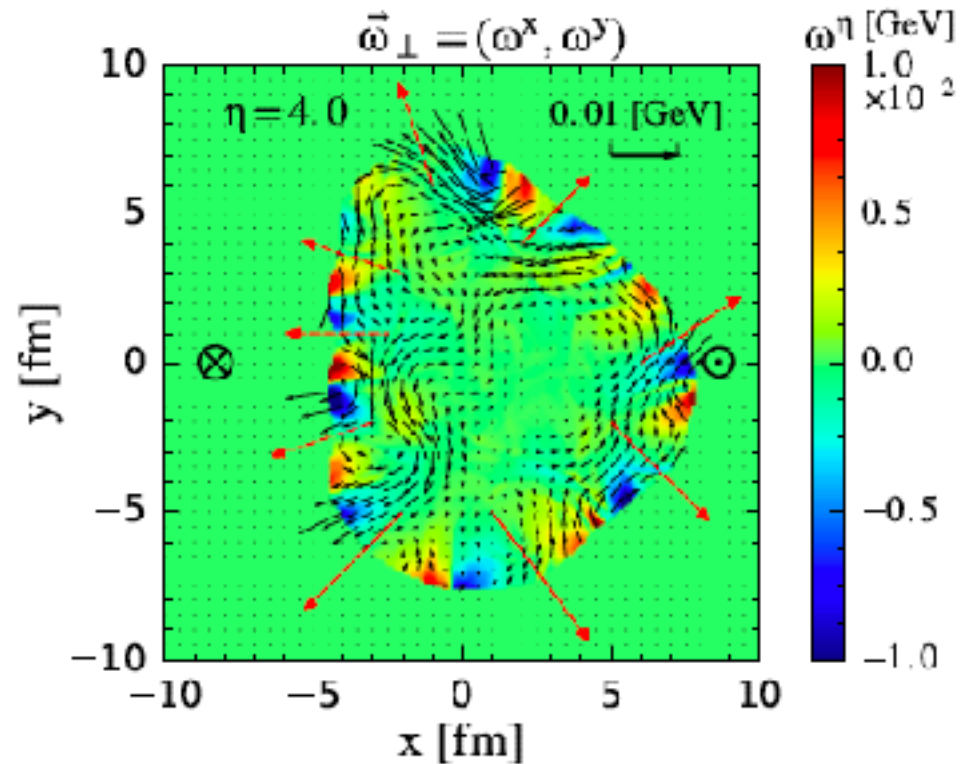
# Quantifying Rotation of QGP

*From HIJING*



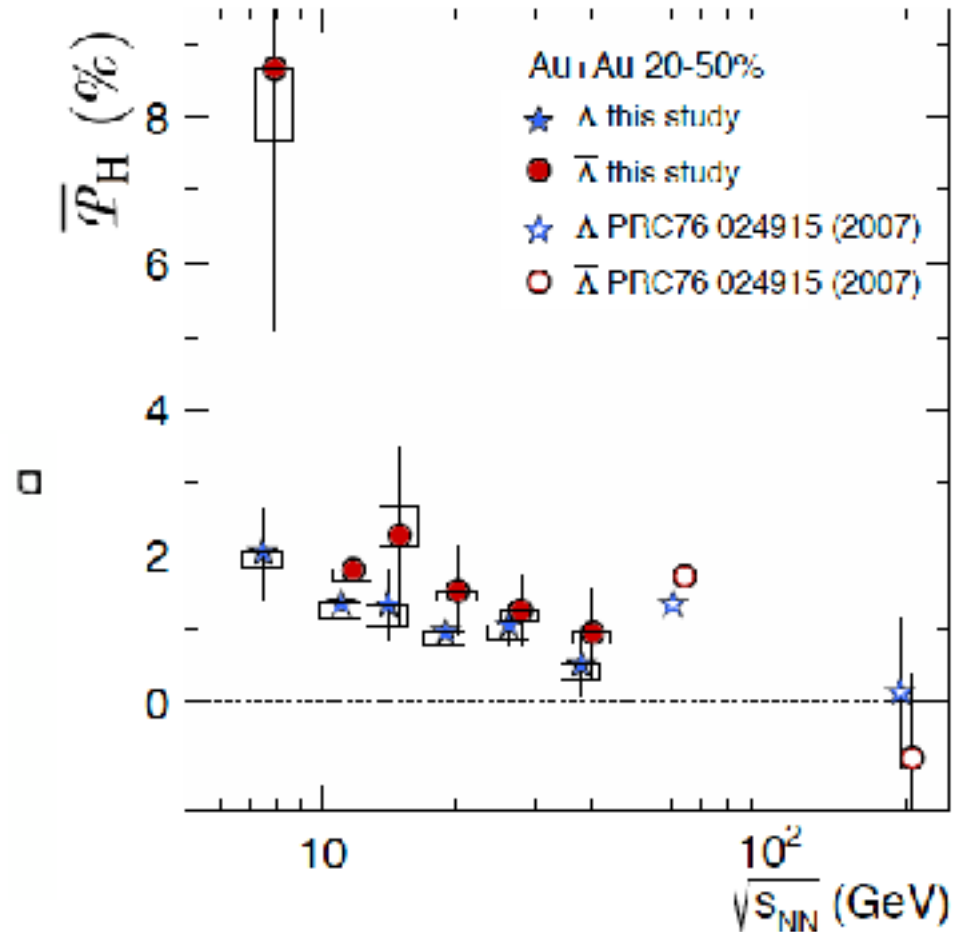
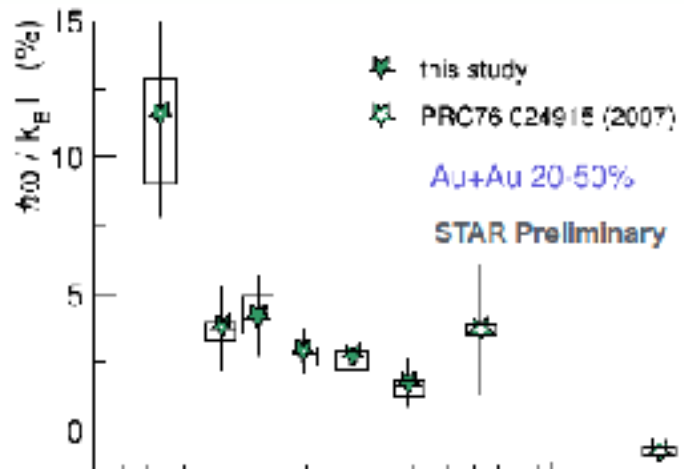
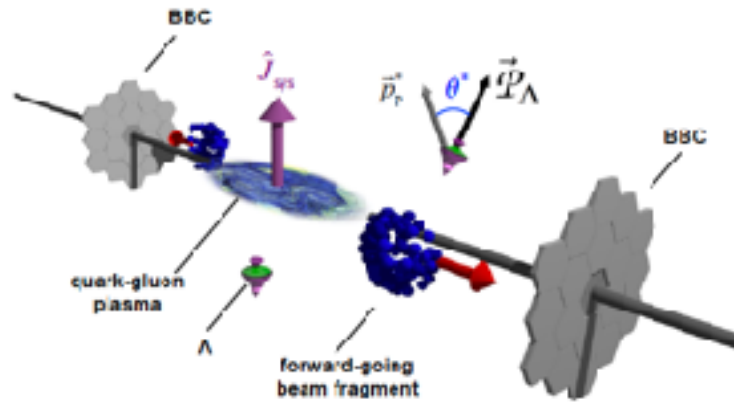
Deng, Huang,  
arXiv:1603.06117

*From 3D hydro*



Pang, Petersen, Wang, Wang  
arXiv:1605.04024

# The Most Vortical Fluid



STAR Collaboration, arXiv:1701.06657

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# Some Concluding Remarks

Q & A

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