

Neutrino Mass Models and Lepton Flavor Violating Decays of the Higgs boson

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- Contents
- Introduction
 - Classification of Models
 - Experimental Tests
 - Summary

Based on "S. Kanemura, HS, PLB753, 161"

"S. Kanemura, K. Sakurai, HS, PLB758, 465"

"M. Aoki, S. Kanemura, K. Sakurai, HS, PLB763,352"



Neutrino oscillation

Transition prob.

$$\Delta m^2 \equiv m_2^2 - m_1^2$$

$$P(\nu_e \rightarrow \nu_{e'}) \simeq \sin^2(2\theta) \sin^2\left(\frac{\Delta m^2 L}{4E}\right)$$

Non-zero neutrino mass

cf. Massless in SM

Very tiny mass

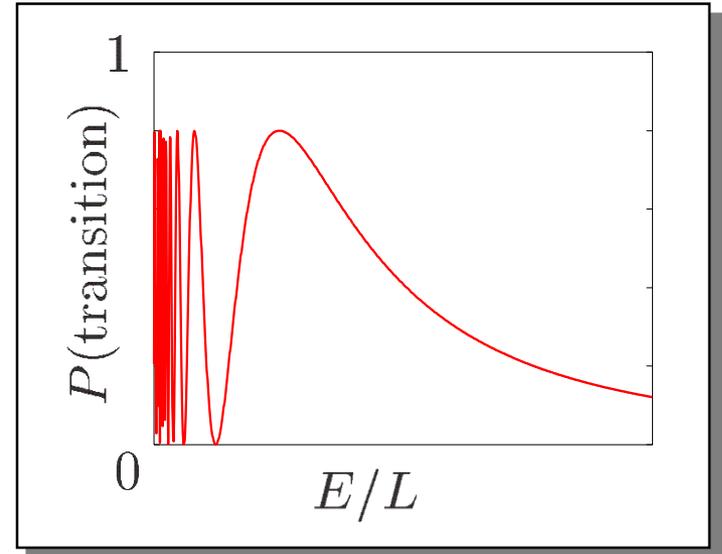
Lepton Flavor Violation (LFV)

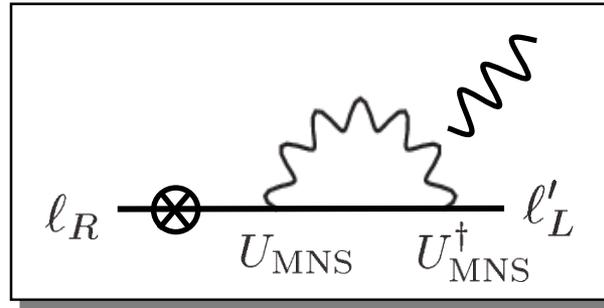
cf. Conserved in SM

Large mixings exist

$$(\theta_{23} \simeq 45^\circ, \theta_{12} \simeq 33^\circ)$$

Two new physics
beyond the standard model (SM)





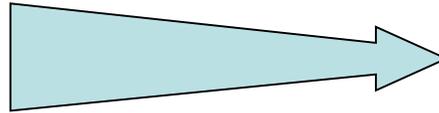
ν oscillation results

Large mixings in U_{MNS}



Potentially large LFV

Suppressed by $\frac{m_\nu^4}{m_W^4}$



LFV (other than ν osc.)

e.g., $l \rightarrow \bar{l}_1 l_2 l_3$

$l \rightarrow l' \gamma$

$h \rightarrow ll'$

New observable

Models for tiny neutrino masses

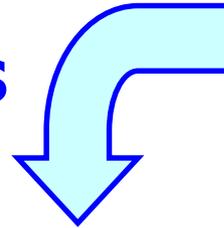
New Yukawa matrices as origin of LFV
(potentially large)



**New scalar fields
with leptonic Yukawa interactions**

**Not necessarily
suppressed**

Discrimination of models



LFV (other than ν osc.)

e.g., $l \rightarrow \bar{l}_1 l_2 l_3$

$l \rightarrow l' \gamma$

$h \rightarrow ll'$

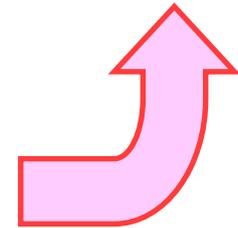
New observable

Models for tiny neutrino masses

New Yukawa matrices as origin of LFV
(potentially large)



**New scalar fields
with leptonic Yukawa interactions**



**Not necessarily
suppressed**

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Neutrino Mass in New Physics Models

{ The standard model (SM) \longrightarrow Massless
 { Neutrino oscillation \longrightarrow **Non-zero masses**



Two possible neutrino masses



Dirac mass : $m_D \bar{\nu}_L \nu_R$ (introduce ν_R)

$$y_\nu \bar{L} \epsilon \Phi^* \nu_R \implies m_D = \frac{y_\nu}{\sqrt{2}} v$$

$$(m_D \sim 0.1 \text{ eV} \implies y_\nu \sim 10^{-12})$$

Unnaturally small

Nontrivial way ?



Majorana mass : $m_L \bar{\nu}_L (\nu_L)^c$ (Lepton # violation)

$$Q_{\text{EM}} : 0 + 0 = 0$$

Specific to neutrinos \longrightarrow **How to generate ?**

Many possibilities \longrightarrow Which is the true one ?

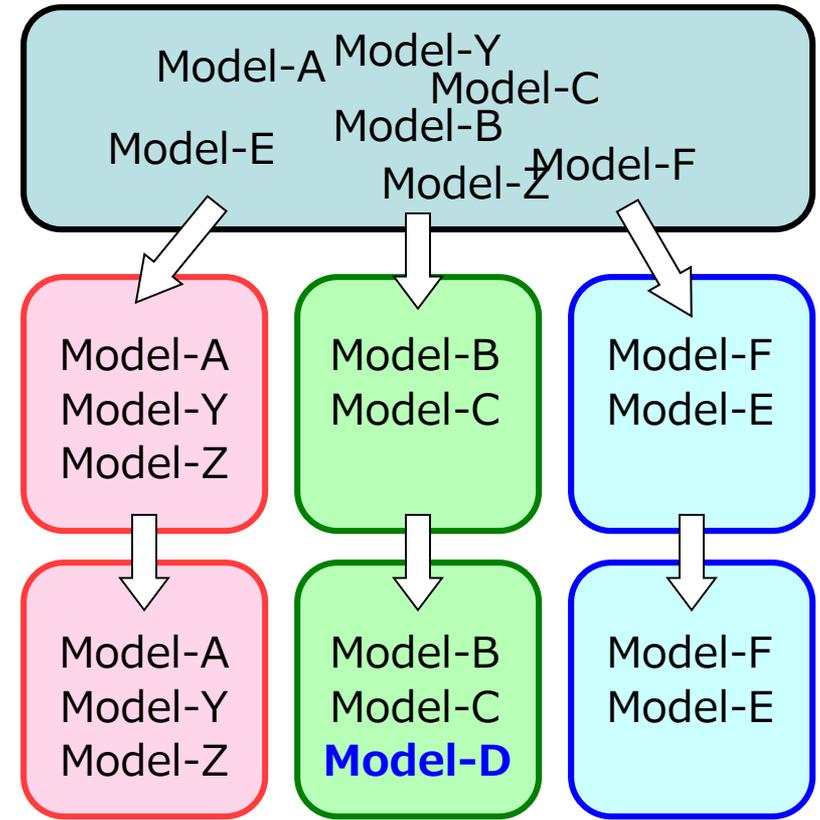
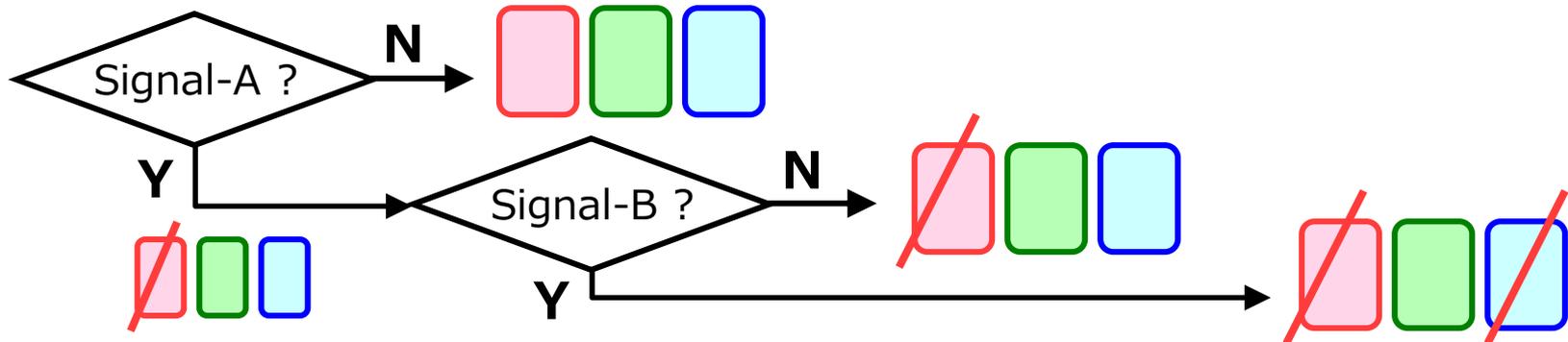
Classification of Models of Neutrino Mass

There are (too) many models.

Classification is desired.

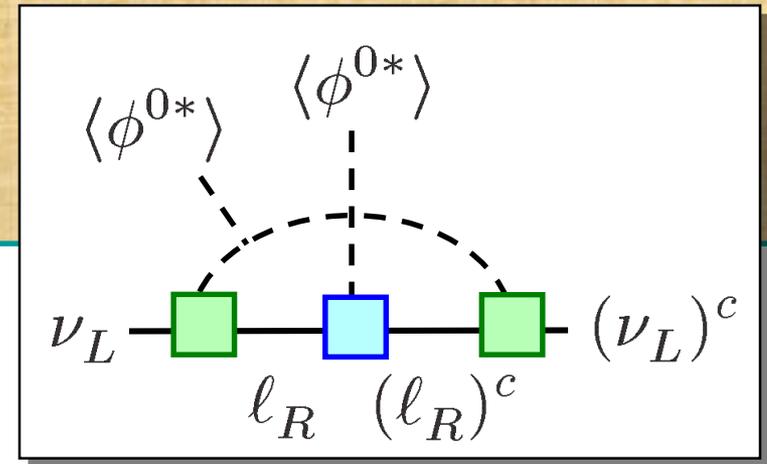
Missing models ?

Efficient tests ?



How to classify ?

Properties of neutrino mass matrix



Overall scale ← {
 New particle masses
 Topology of diagram (tree, one-loop, ...)
 Sizes of coupling constants (Yukawa, potential)

Matrix structure ← {
 Products of Yukawa matrices
 Structures of Yukawa (sym., antisym., diag.)

Only Yukawa. Not detail of models



Classification by concentrating on Yukawa int. with leptons

Setup

New scalars : Required to be introduced
 cf. No new scalars \Rightarrow Seesaw
 \Rightarrow Difficult to be tested

No lepton flavor

cf. Sleptons for SUSY
 Flavor symmetry

No color

cf. Scalar leptoquarks

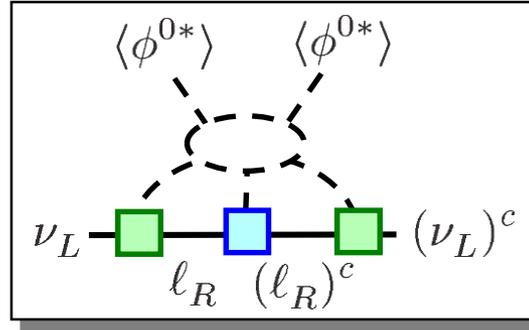
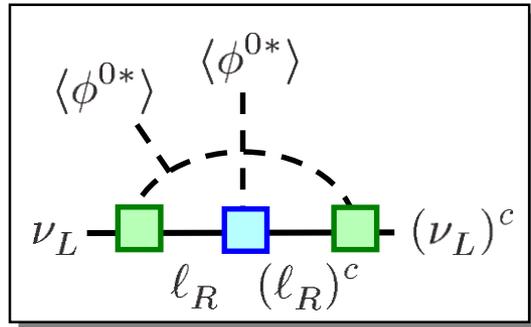
No flavor changing neutral current at tree level

New fermions : ν_R only for Dirac neutrinos (no $m_R \overline{(\nu_R)^c} \nu_R$)

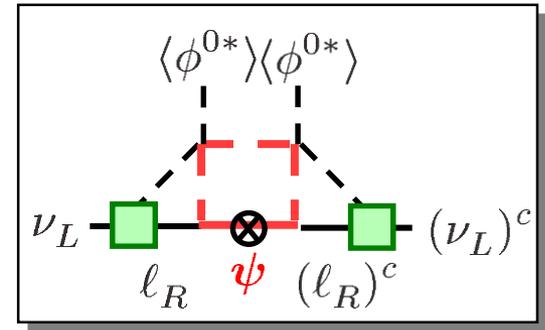
ψ_R^0 $\left\{ \begin{array}{l} \text{Gauge-singlet} \\ \mathbf{Z_2 \text{ odd}} \\ \text{Majorana fermion} \end{array} \right. \quad m_\psi \overline{(\psi_R^0)^c} \psi_R^0$

Classification according to interactions of leptons

● Models (full Lagrangian)

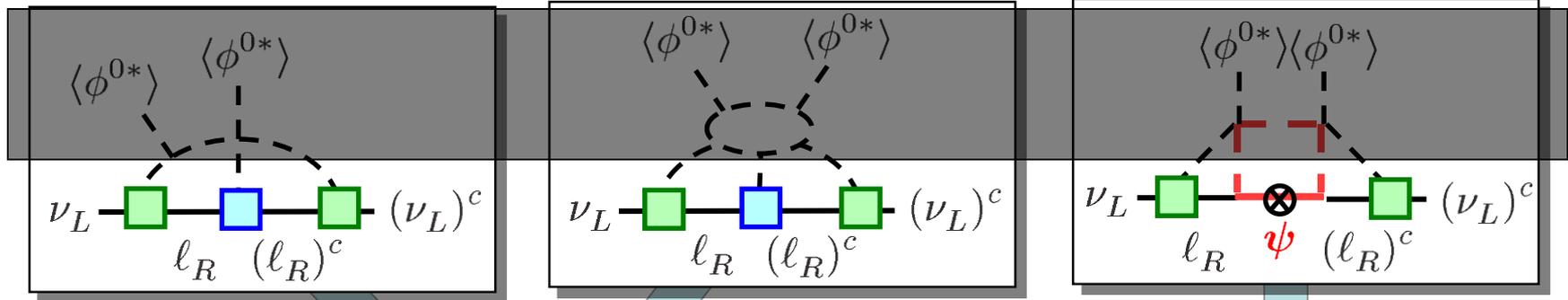


Red lines : Z_2 - odd

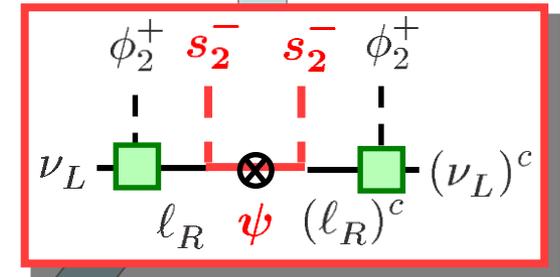
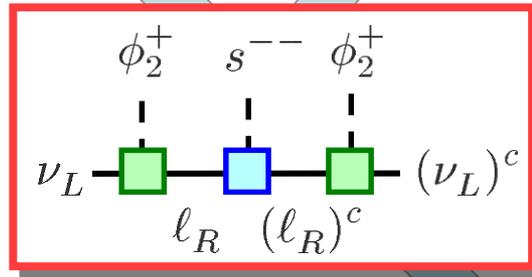


Classification according to interactions of leptons

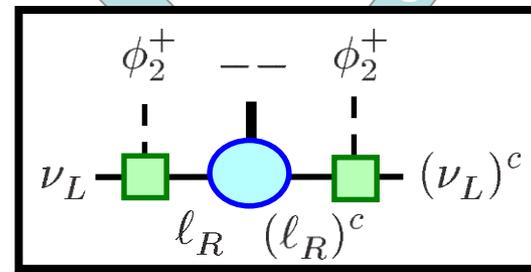
- Models (full Lagrangian)



- Concentrating on **Yukawa int.**



- Concentrating on interactions **between two leptons** (effective)



Scalars with Leptonic Yukawa Int.



Majorana

	SU(2) _L	U(1) _Y	L#	Z' ₂	Yukawa int.	Note
						Sym.
s_L^+	<u>1</u>	1	-2	+	$(Y_A^s)_{\ell\ell'} [\overline{L}_\ell \in L_{\ell'}^c, s_L^-]$	Antisym.
s^{++}	<u>1</u>	2	-2	+	$(Y_S^s)_{\ell\ell'} [\overline{(\ell_R)^c} \ell'_R s^{++}]$	Sym.
$\Phi_2 = \begin{pmatrix} \phi_2^+ & \phi_2^0 \end{pmatrix}^T$	<u>2</u>	1/2	0	+	$y_\ell [\overline{L}_\ell \Phi_2 \ell_R]$	Diag.
$\Delta = \begin{pmatrix} \Delta^+/\sqrt{2} & \Delta^{++} \\ \Delta^0 & -\Delta^+/\sqrt{2} \end{pmatrix}$	<u>3</u>	1	-2	+	$(Y_S^\Delta)_{\ell\ell'} [\overline{L}_\ell \Delta^\dagger \in L_{\ell'}^c]$	Sym.
s_2^+ Z₂ odd	<u>1</u>	1	-1	+	$(Y_\psi^+)_{li} [\overline{(\ell_R)^c} \psi_{iR}^0 s_2^+]$	ψ_R^0
$\eta = (\eta^+ \ \eta^0)^T$ Z₂ odd	<u>2</u>	1/2	-1	+	$(Y_\psi^\eta)_{li} [\overline{L}_\ell \in \eta^* \psi_{iR}^0]$	ψ_R^0

For Majorana ν masses ($m_L \bar{\nu}_L (\nu_L)^c$)

	Scalar with leptonic Yukawa int.					
					Z_2 -odd	
	s_L^+	s^{++}	Φ_2	Δ	s_2^+	η
$SU(2)_L$	<u>1</u>	<u>1</u>	<u>2</u>	<u>3</u>	<u>1</u>	<u>2</u>
$U(1)_Y$	1	2	1/2	1	1	1/2
Unbroken Z_2	+	+	+	+	-	-
M1	✓	✓				
M2		✓	✓			
M3		✓				
M4				✓		
M5	✓				✓	
M6			✓		✓	
M7					✓	
M8						✓

8 combinations



Dirac

Lepton number
(conserved)forbid $y_\nu \bar{L} \in \Phi^* \nu_R$ at tree level
+ + -

	$SU(2)_L$	$U(1)_Y$	L#	Z'_2	Yukawa int.	Note
s^0	<u>1</u>	0	-2	+	$(Y_S^0)_{ij} \left[(\nu_{iR})^c \nu_{jR} s^0 \right]$	Sym.
s_L^+	<u>1</u>	1	-2	+	$(Y_A^s)_{\ell\ell'} \left[\bar{L}_\ell \in L_{\ell'}^c s_L^- \right]$	Antisym.
s_R^+	<u>1</u>	1	-2	-	$(Y^s)_{\ell i} \left[(\ell_R)^c \nu_{iR} s_R^+ \right]$	ν_R
s^{++}	<u>1</u>	2	-2	+	$(Y_S^s)_{\ell\ell'} \left[(\ell_R)^c \ell' s^{++} \right]$	Sym.
$\Phi_\nu = \begin{pmatrix} \phi_\nu^+ & \phi_\nu^0 \end{pmatrix} T$	<u>2</u>	1/2	0	-	$(Y_\nu)_{\ell i} \left[\bar{L}_\ell \in \Phi_\nu^* \nu_{iR} \right]$	ν_R
$\Phi_2 = \begin{pmatrix} \phi_2^+ & \phi_2^0 \end{pmatrix} T$	<u>2</u>	1/2	0	+	$y_\ell \left[\bar{L}_\ell \Phi_2 \ell_R \right]$	Diag.
$\Delta = \begin{pmatrix} \Delta^+/\sqrt{2} & \Delta^{++} \\ \Delta^0 & -\Delta^+/\sqrt{2} \end{pmatrix}$	<u>3</u>	1	-2	+	$(Y_S^\Delta)_{\ell\ell'} \left[\bar{L}_\ell \Delta^\dagger \in L_{\ell'}^c \right]$	Sym.
s_2^0 Z_2 odd	<u>1</u>	0	-1	-	$(Y_\psi^0)_{ij} \left[(\nu_{iR})^c \psi_{jR}^0 s_2^0 \right]$	ν_R ψ_R^0
s_2^+ Z_2 odd	<u>1</u>	1	-1	+	$(Y_\psi^+)_{\ell i} \left[(\ell_R)^c \psi_{iR}^0 s_2^+ \right]$	ψ_R^0
$\eta = (\eta^+ \ \eta^0)^T$ Z_2 odd	<u>2</u>	1/2	-1	+	$(Y_\psi^\eta)_{\ell i} \left[\bar{L}_\ell \in \eta^* \psi_{iR}^0 \right]$	ψ_R^0

For Dirac ν masses (without DM)

	Scalar with leptonic Yukawa int.									
								Z_2 -odd		
	s^0	s_L^+	s_R^+	s^{++}	Φ_ν	Φ_2	Δ	s_2^0	s_2^+	η
$SU(2)_L$	<u>1</u>	<u>1</u>	<u>1</u>	<u>1</u>	<u>2</u>	<u>2</u>	<u>3</u>	<u>1</u>	<u>1</u>	<u>2</u>
$U(1)_Y$	0	1	1	2	1/2	1/2	1	0	1	1/2
L#	-2	-2	-2	-2	0	0	-2	-1	-1	-1
Z'_2	+	+	-	+	-	+	+	-	+	+
D1		✓	✓							
D2			✓				✓			
D3			✓	✓		✓				
D4			✓	✓						
D5	✓		✓			✓				
D6	✓		✓							
D7					✓					

S. Kanemura, K. Sakurai, HS, PLB**758**, 465 (2016)

For Dirac ν masses (with DM)

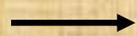
	Scalar with leptonic Yukawa int.									
								Z ₂ -odd		
	s^0	s_L^+	s_R^+	s^{++}	Φ_ν	Φ_2	Δ	s_2^0	s_2^+	η
SU(2) _L	<u>1</u>	<u>1</u>	<u>1</u>	<u>1</u>	<u>2</u>	<u>2</u>	<u>3</u>	<u>1</u>	<u>1</u>	<u>2</u>
U(1) _Y	0	1	1	2	1/2	1/2	1	0	1	1/2
L#	-2	-2	-2	-2	0	0	-2	-1	-1	-1
Z' ₂	+	+	-	+	-	+	+	-	+	+
D8		✓						✓	✓	
D9							✓	✓	✓	
D10			✓							✓
D11			✓			✓			✓	
D12			✓						✓	
D13			✓			✓		✓		
D14			✓					✓		
D15						✓		✓	✓	
D16								✓	✓	
D17			✓						✓	✓
D18								✓		✓

18 combinations

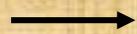
Combinations of Yukawa int. (or scalar fields)

For Majorana mass : **8 combinations**

For Dirac mass : **18 combinations**



How can we **test them ?**



Concentrating on Yukawa \Rightarrow **Flavor experiments**

$$l \rightarrow \bar{l}_1 l_2 l_3$$

$$l \rightarrow l' \nu \bar{\nu}$$

$$l \rightarrow l' \gamma$$

$$h \rightarrow ll'$$

- 
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LFV Decay of the Higgs Boson

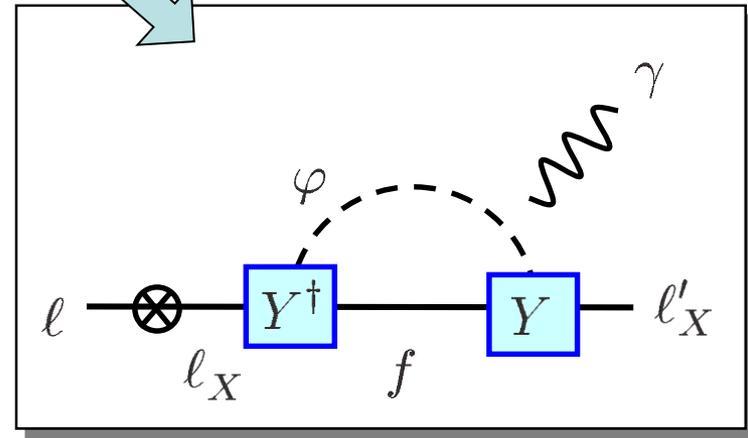
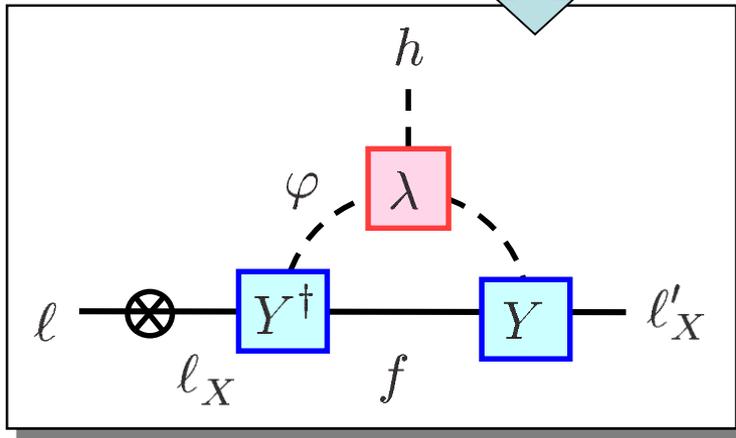
$$\text{BR}(h \rightarrow \ell\ell') \equiv \text{BR}(h \rightarrow \bar{\ell}\ell') + \text{BR}(h \rightarrow \ell\bar{\ell}')$$

		ATLAS arXiv:1604.07730 (8 TeV, 20.3 fb ⁻¹)	CMS [1] PLB 763 , 472 (2016) [2] PLB 749 , 337 (2015) [3] CMS PAS HIG-16-005 (13 TeV, 2.3 fb ⁻¹)
$h \rightarrow \mu e$	Limit		$< 3.5 \times 10^{-4}$ [1]
	Best fit		
$h \rightarrow \tau e$	Limit	$< 1.04 \times 10^{-2}$	$< 6.9 \times 10^{-3}$ [1]
	Best fit	$-3.4^{+6.4}_{-6.6} \times 10^{-3}$	
$h \rightarrow \tau \mu$	Limit	$< 1.43 \times 10^{-2}$	$< 1.51 \times 10^{-2}$ [2] $< 1.20 \times 10^{-2}$ [3]
	Best fit	$5.3^{+5.1}_{-5.1} \times 10^{-3}$	$\left\{ \begin{array}{l} 8.4^{+3.9}_{-3.7} \times 10^{-3} (2.4 \sigma) \text{ [2]} \\ -7.6^{+8.1}_{-8.4} \times 10^{-3} \text{ [3]} \end{array} \right.$

My naïve calc. $\rightarrow (5.6 \pm 3.5) \times 10^{-3} (1.6 \sigma)$

$$h \rightarrow ll' \text{ and } l \rightarrow l'\gamma$$

Toy model : $\mathcal{L} = Y_{ae} \left[\overline{f_a} l_X \varphi \right] - \lambda |\Phi|^2 |\varphi|^2 + \dots$
 $X = L, R$



$$\text{BR}(h \rightarrow ll'_X) \sim 0.1 \frac{\lambda^2}{(2 - 3Q_\varphi)^2} \text{BR}(l \rightarrow l'_X \gamma)$$

Too small $\text{BR}(h \rightarrow ll')$
to be observed.
If observed,
the toy model is excluded.



$$\left\{ \begin{array}{l} \text{BR}(\mu \rightarrow e\gamma) < 4.2 \times 10^{-13} \\ \text{MEG collab., EPJC76, no.8, 434} \\ \text{BR}(\tau \rightarrow e\gamma) < 3.3 \times 10^{-8} \\ \text{BR}(\tau \rightarrow \mu\gamma) < 4.4 \times 10^{-8} \\ \text{Babar collab., PRL104, 021802} \end{array} \right.$$

If $h \rightarrow \ell\ell'$ is Observed

M. Aoki, S. Kanemura, K. Sakurai, HS,
PLB763, 352 (2016)

"Mechanisms" for Majorana ν mass

	Scalar with leptonic Yukawa int.						$\ell \rightarrow \ell'\gamma$	
	s_L^+	s^{++}	Φ_2	Δ	s_2^+	η	ℓ'_L	ℓ'_R
SU(2) _L	<u>1</u>	<u>1</u>	<u>2</u>	<u>3</u>	<u>1</u>	<u>2</u>		
U(1) _Y	1	2	1/2	1	1	1/2		
Unbroken Z ₂	+	+	+	+	-	-		
M1	✓	✓					✓	✓
M2		✓	✓					✓
M3		✓						✓
M4				✓			✓	
M5	✓				✓		✓	✓
M6			✓		✓			✓
M7					✓			✓
M8						✓	✓	✓

$h \rightarrow \ell\ell'$ signal \Rightarrow BR($\ell \rightarrow \ell'\gamma$) is too large \Rightarrow **Excluded**

If $h \rightarrow \ell\ell'$ is Observed

M. Aoki, S. Kanemura, K. Sakurai, HS,
PLB763, 352 (2016)

"Mechanisms" for Majorana ν mass

	Scalar with leptonic Yukawa int.						$\ell \rightarrow \ell'\gamma$	
	s_L^+	s^{++}	Φ_2	Δ	Z_2 -odd		ℓ'_L	ℓ'_R
					s_2^+	η		
$SU(2)_L$	<u>1</u>	<u>1</u>	<u>2</u>	<u>3</u>	<u>1</u>	<u>2</u>		
$U(1)_Y$	1	2	1/2	1	1	1/2		
Unbroken Z_2	+	+	+	+	-	-		
M1	✓	✓					✓	✓
M2		✓	✓					✓
M3		✓						✓
M4				✓			✓	
M5	✓				✓		✓	✓
M6			✓		✓			✓
M7					✓			✓
M8						✓	✓	

All excluded for Majorana neutrinos !

“Mechanisms” for Dirac ν mass (without DM)

	Scalar with leptonic Yukawa int.										$l \rightarrow l' \gamma$	
								Z ₂ -odd				
	s^0	s_L^+	s_R^+	s^{++}	Φ_ν	Φ_2	Δ	s_2^0	s_2^+	η		
SU(2) _L	<u>1</u>	<u>1</u>	<u>1</u>	<u>1</u>	<u>2</u>	<u>2</u>	<u>3</u>	<u>1</u>	<u>1</u>	<u>2</u>		
U(1) _Y	0	1	1	2	1/2	1/2	1	0	1	1/2		
L#	-2	-2	-2	-2	0	0	-2	-1	-1	-1		
Z' ₂	+	+	-	+	-	+	+	-	+	+		
D1		✓	✓								✓	✓
D2			✓			✓					✓	✓
D3			✓	✓		✓					✓✓	✓✓
D4			✓	✓							✓✓	✓✓
D5	✓		✓								✓	✓
D6	✓		✓								✓	✓
D7					✓						✓	✓

D3 and D4 survive

$$\text{BR}(l \rightarrow l' \gamma) \propto \left| \frac{(Y^{s\dagger} Y^s)_{\ell\ell'}}{m_{s_R^+}^2} + \frac{(Y_S^{s\dagger} Y_S^s)_{\ell\ell'}}{m_{s^{++}}^2} \right|^2 \ll \left| \frac{(Y^{s\dagger} Y^s)_{\ell\ell'}}{m_{s_R^+}^2} \right|^2$$

Cancellation is possible

“Mechanisms” for Dirac ν mass (with DM)

Scalar with leptonic Yukawa int.

	Scalar with leptonic Yukawa int.									$l \rightarrow l' \gamma$		
								Z_2 -odd			l'_L	l'_R
	s^0	s_L^+	s_R^+	s^{++}	Φ_ν	Φ_2	Δ	s_2^0	s_2^+	η		
$SU(2)_L$	<u>1</u>	<u>1</u>	<u>1</u>	<u>1</u>	<u>2</u>	<u>2</u>	<u>3</u>	<u>1</u>	<u>1</u>	<u>2</u>		
$U(1)_Y$	0	1	1	2	1/2	1/2	1	0	1	1/2		
LN	-2	-2	-2	-2	0	0	-2	-1	-1	-1		
Z'_2	+	+	-	+	-	+	+	-	+	+		
D8		✓						✓	✓		✓	✓
D9							✓	✓	✓		✓	✓
D10			✓							✓	✓	✓
D11			✓			✓			✓			✓✓
D12			✓						✓			✓✓
D13			✓			✓		✓				✓
D14			✓					✓				✓
D15										✓		✓
D16								✓	✓			✓
D17			✓						✓	✓	✓	✓✓
D18								✓		✓	✓	✓

D11, D12, and D17 survive

“Mechanisms” for Dirac ν mass

	Scalar with leptonic Yukawa int.										$l \rightarrow l' \gamma$	
								Z_2 -odd			l'_L	l'_R
	s^0	s_L^+	s_R^+	s^{++}	Φ_ν	Φ_2	Δ	s_2^0	s_2^+	η		
$SU(2)_L$	<u>1</u>	<u>1</u>	<u>1</u>	<u>1</u>	<u>2</u>	<u>2</u>	<u>3</u>	<u>1</u>	<u>1</u>	<u>2</u>		
$U(1)_Y$	0	1	1	2	1/2	1/2	1	0	1	1/2		
LN	-2	-2	-2	-2	0	0	-2	-1	-1	-1		
Z'_2	+	+	-	+	-	+	+	-	+	+		
D3			✓	✓		✓						✓✓
D4			✓	✓								✓✓
D11			✓			✓			✓			✓✓
D12			✓						✓			✓✓
D17			✓						✓	✓	✓	✓✓

These mechanisms for generating masses of **Dirac neutrinos**

can **survive** after discovery of $h \rightarrow ll'$

Summary



Simple models to generate **Majorana** ν masses can be classified into **8 combinations** of Yukawa int. (New scalars)

Simple models to generate **Dirac** ν masses can be classified into **18 combinations** of Yukawa int. (New scalars)



$h \rightarrow \ell\ell'$



Simple models for **Majorana** ν masses are **excluded**

Some simple models for **Dirac** ν masses can **survive**

Backup

$$\theta_{23} \simeq 45^\circ$$

$$\theta_{13} \simeq 9^\circ$$

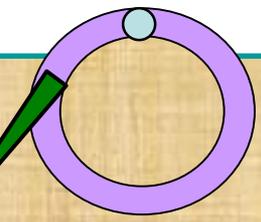
$$\delta ?$$

$$\theta_{12} \simeq 33^\circ$$

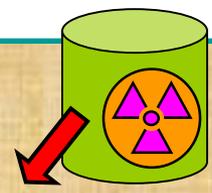
$$U_{MNS} \simeq \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0.71 & 0.71 \\ 0 & -0.71 & 0.71 \end{pmatrix} \begin{pmatrix} 0.99 & 0 & 0.15 \\ 0 & 1 & 0 \\ 0.15 & 0 & 0.99 \end{pmatrix} \begin{pmatrix} 0.83 & 0.55 & 0 \\ -0.55 & 0.83 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$



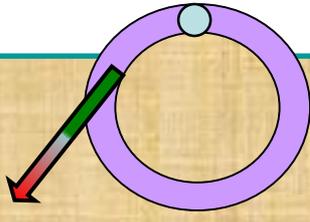
Atmospheric



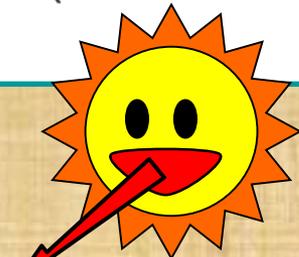
Accelerator



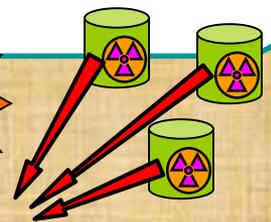
Reactor



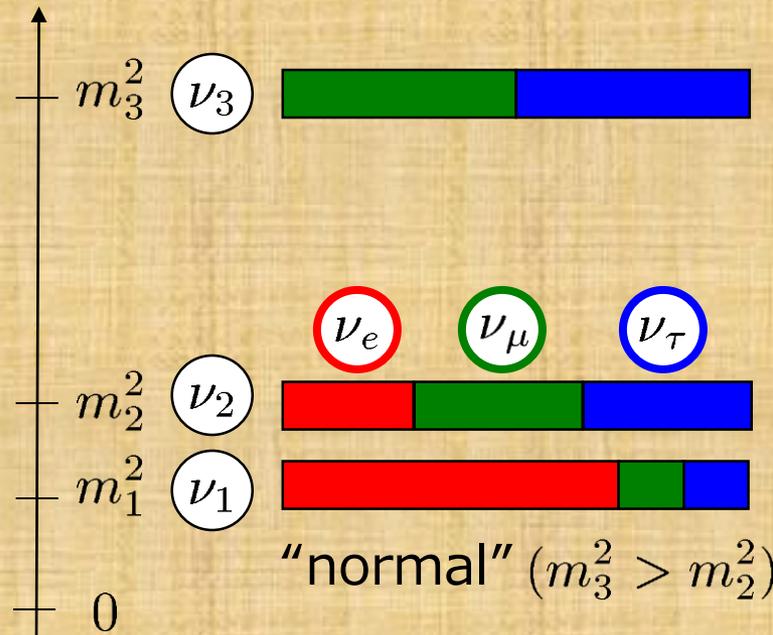
T2K



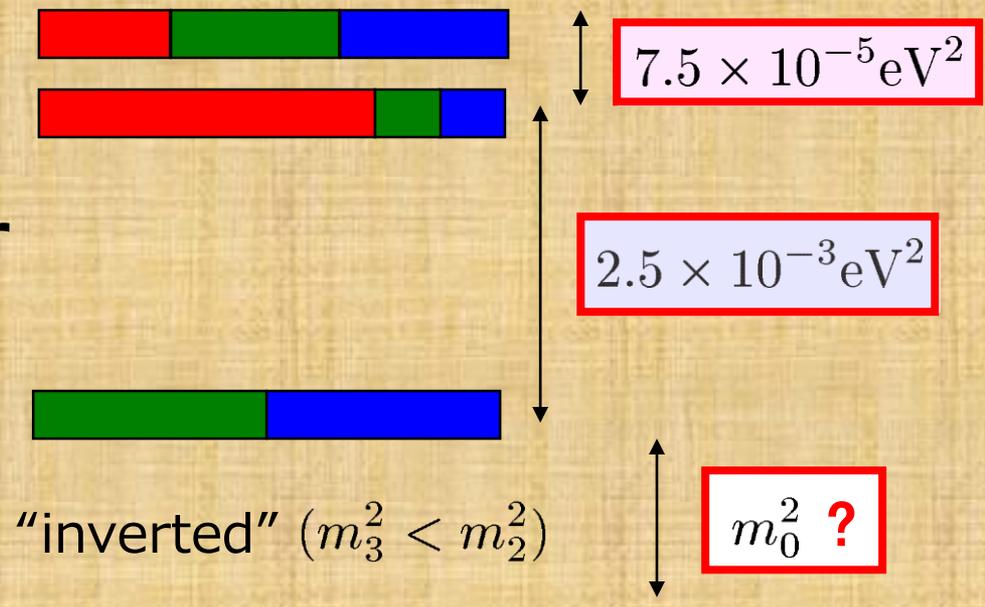
Solar



KamLAND



or



Oscillation Data

$$m_\nu = U_{\text{MNS}}^* \text{diag}(m_1 e^{i\alpha_{12}}, m_2, m_3 e^{i\alpha_{32}}) U_{\text{MNS}}^\dagger$$

$$U_{\text{MNS}} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13} e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13} e^{i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$c_{ij} \equiv \cos \theta_{ij} \quad s_{ij} \equiv \sin \theta_{ij}$$

$$\text{T2K : } \begin{cases} \sin^2 \theta_{23} = 0.514_{-0.056}^{+0.055}, & \Delta m_{32}^2 = (2.51 \pm 0.10) \times 10^{-3} \text{ eV}^2 \\ \sin^2 \theta_{23} = 0.511_{-0.055}^{+0.055}, & \Delta m_{23}^2 = (2.48 \pm 0.10) \times 10^{-3} \text{ eV}^2 \end{cases}$$

K. Abe *et al.*, PRL**112**, 181801 (2014)

$$\text{Daya Bay : } \sin^2 2\theta_{13} = 0.090_{-0.009}^{+0.008} \quad \text{R.P. An *et al.*, PRL**112**, 061801 (2014)}$$

$$\sin^2 2\theta_{13} = 0.084 \pm 0.005 \quad \text{R.P. An *et al.*, PRL**115**, 111802 (2015)}$$

$$\text{SNO : } \tan^2 \theta_{12} = 0.427_{-0.024}^{+0.027}, \quad \Delta m_{21}^2 = 7.46_{-0.19}^{+0.20} \times 10^{-5} \text{ eV}^2$$

B. Aharmim *et al.*, PRC**88**, 025501 (2013)

Absolute Mass Scale

$$\mathbf{I}) m_\nu \propto Y_A y_\ell X_{SR} y_\ell Y_A^T$$

$$\mathbf{I}') m_D \propto Y_A^s y_\ell X^s$$

$$(Y_A)_{\ell\ell'} \left[\overline{L}_\ell \in L_{\ell'}^c s^- \right]$$

$$\text{Det}(m_\nu) \propto \text{Det}(Y_A) = 0$$

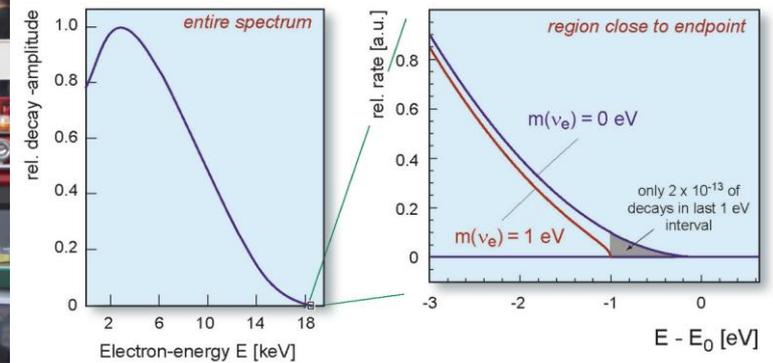
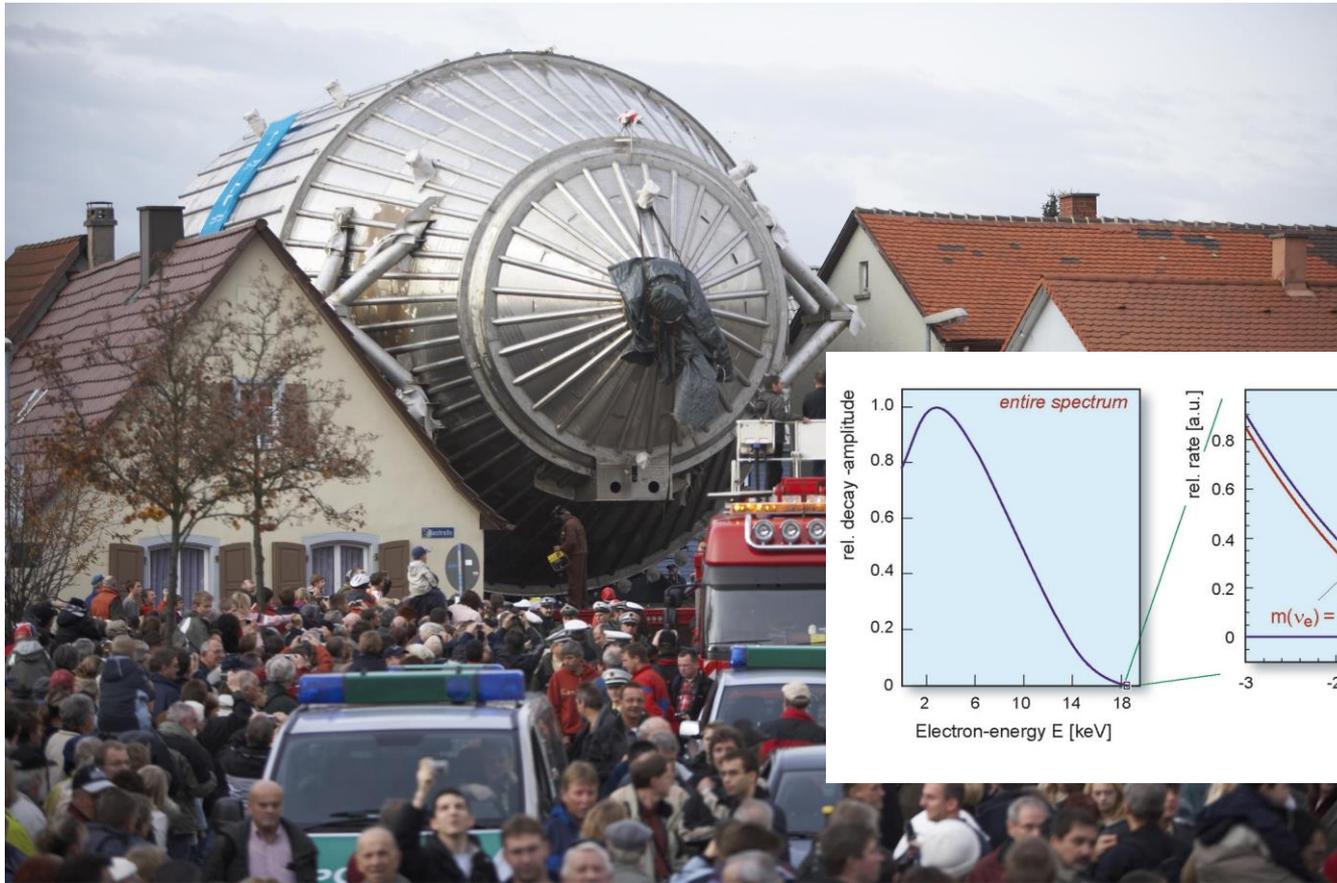
\longrightarrow $m_1 = 0$ or $m_3 = 0$ m_i : Neutrino mass eigenvalues
 ($m_2 \neq 0$ due to solar ν osc.)

\longrightarrow If $\min(m_i) \neq 0$ experimentally \Rightarrow **Excluded**

Direct (${}^3\text{H}$ β -decay): $m_\nu \simeq 0.35$ eV (5σ sensitivity)

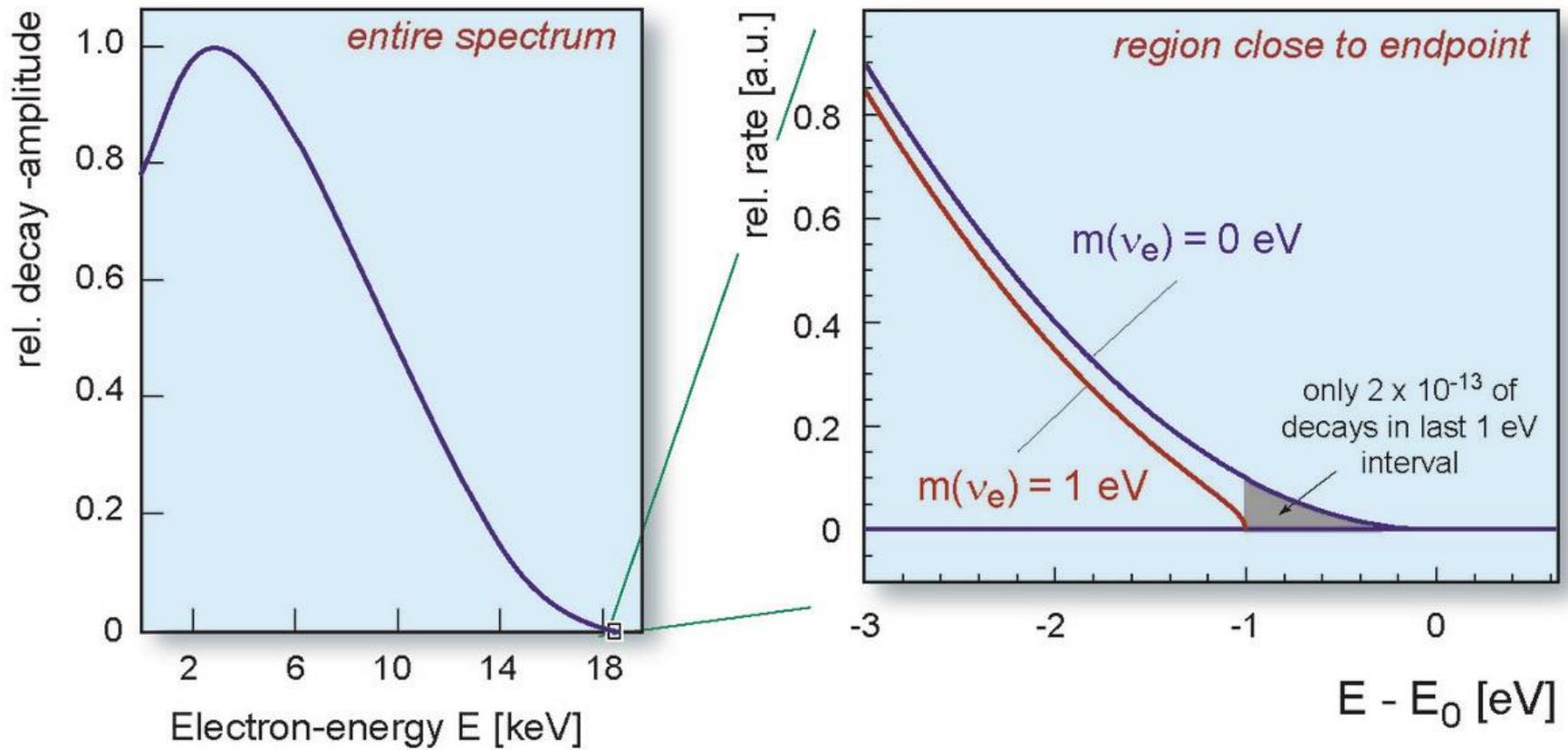
Indirect (Cosmology): $\Sigma m_i = \mathcal{O}(0.01)$ eV (95% CL sens.)

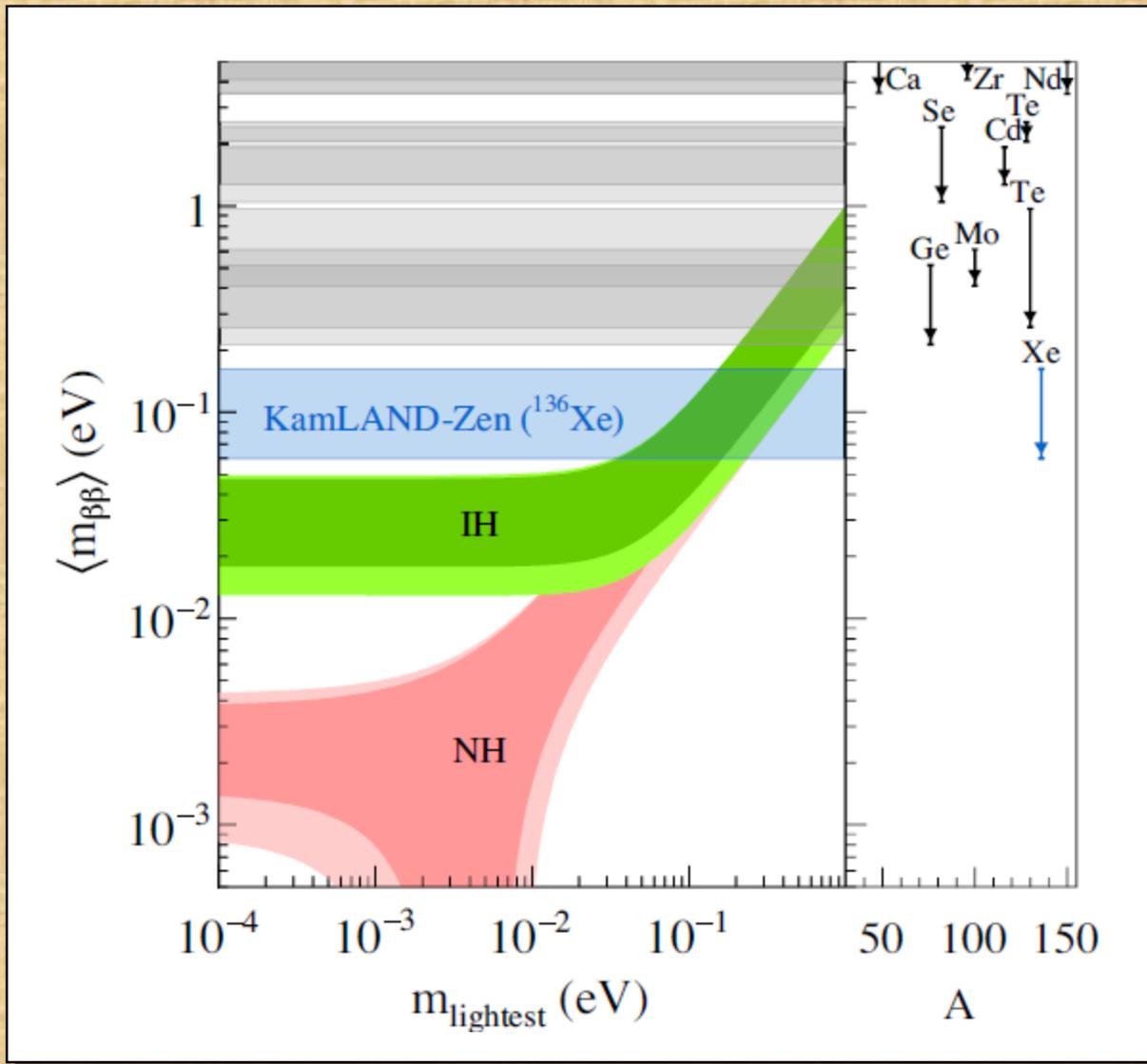
Not for a model but **for all models belong to Group-I and I'**
 (e.g. ZB model, KNT model, NM model)



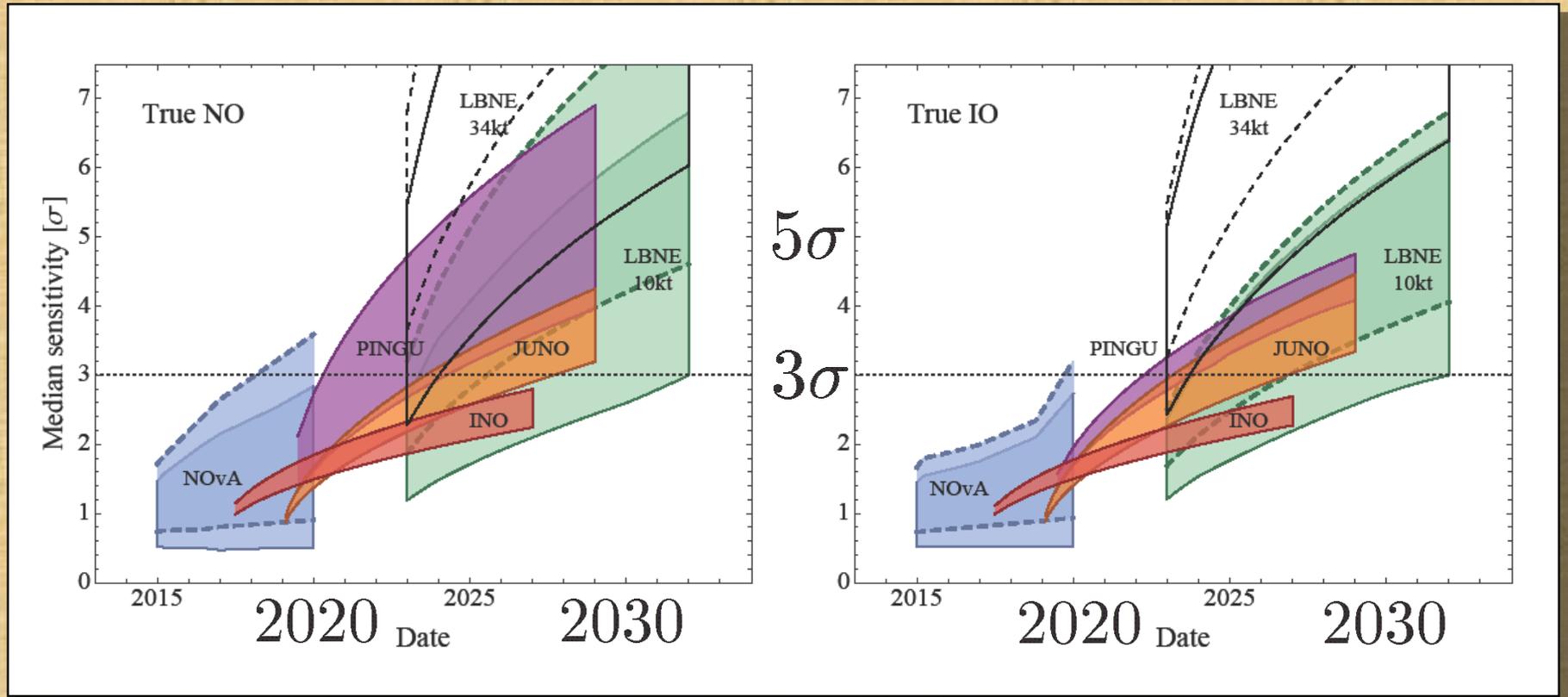
<https://www.katrin.kit.edu/213.php>

Main spectrometer of KATRIN experiment
 Transport through Leopoldshafen in Germany





KamLAND-ZEN collab., arXiv:1605.02889



M. Blennow *et al.*, JHEP1403, 028 (2014)

LFV Decay of the Higgs Boson

$$\text{BR}(h \rightarrow \ell\ell') \equiv \text{BR}(h \rightarrow \bar{\ell}\ell') + \text{BR}(h \rightarrow \ell\bar{\ell}')$$

		ATLAS arXiv:1604.07730 (8 TeV, 20.3 fb ⁻¹)	CMS [1] arXiv:1607.03561 [2] PLB 749 , 337 (2015) [3] CMS PAS HIG-16-005 (13 TeV, 2.3 fb ⁻¹)
$h \rightarrow \mu e$	Limit		$< 3.5 \times 10^{-4}$ [1]
	Best fit		
$h \rightarrow \tau e$	Limit	$< 1.04 \times 10^{-2}$	$< 6.9 \times 10^{-3}$ [1]
	Best fit	$-3.4^{+6.4}_{-6.6} \times 10^{-3}$	
$h \rightarrow \tau \mu$	Limit	$< 1.43 \times 10^{-2}$	$< 1.51 \times 10^{-2}$ [2] $< 1.20 \times 10^{-2}$ [3]
	Best fit	$5.3^{+5.1}_{-5.1} \times 10^{-3}$	$\left\{ \begin{array}{l} 8.4^{+3.9}_{-3.7} \times 10^{-3} \text{ (2.4 } \sigma) \text{ [2]} \\ -7.6^{+8.1}_{-8.4} \times 10^{-3} \text{ [3]} \end{array} \right.$

My naïve calc. $\rightarrow (5.6 \pm 3.5) \times 10^{-3} \text{ (1.6 } \sigma)$

$h \rightarrow \ell\ell'$ at the loop level

Dim.-4 operator

$$\mathcal{L} = \mathbf{Y}_4 \left[\bar{L} \Phi \ell'_R \right]$$

$$\text{Mass : } \frac{v}{\sqrt{2}} \mathbf{Y}_4 \left[\bar{\ell}_L \ell'_R \right] \xrightarrow{\text{Diagonalize}} m_\ell \left[\bar{\ell}_L \ell_R \right]$$

$$\text{Int. : } \frac{1}{\sqrt{2}} \mathbf{Y}_4 \left[\bar{\ell}_L \ell'_R h \right] \dashrightarrow \frac{m_\ell}{v} \left[\bar{\ell}_L \ell_R h \right] \quad \text{no LFV}$$

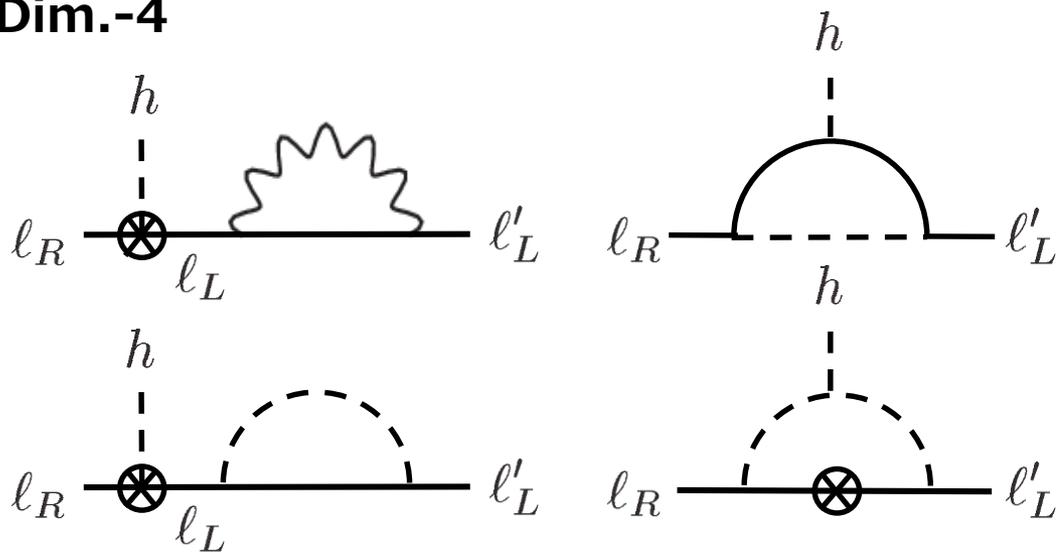
Dim.-6 operator

$$\mathcal{L} = \mathbf{Y}_4 \left[\bar{L} \Phi \ell'_R \right] + \frac{\mathbf{Y}_6}{\Lambda^2} \left[\bar{L} \Phi \ell'_R (\Phi^\dagger \Phi) \right]$$

$$\text{Mass : } v \left(\frac{1}{\sqrt{2}} \mathbf{Y}_4 + \frac{v^2}{2\Lambda^2} \mathbf{Y}_6 \right) \left[\bar{\ell}_L \ell'_R \right] \xrightarrow{\text{Diag.}} m_\ell \left[\bar{\ell}_L \ell_R \right] \quad \text{LFV}$$

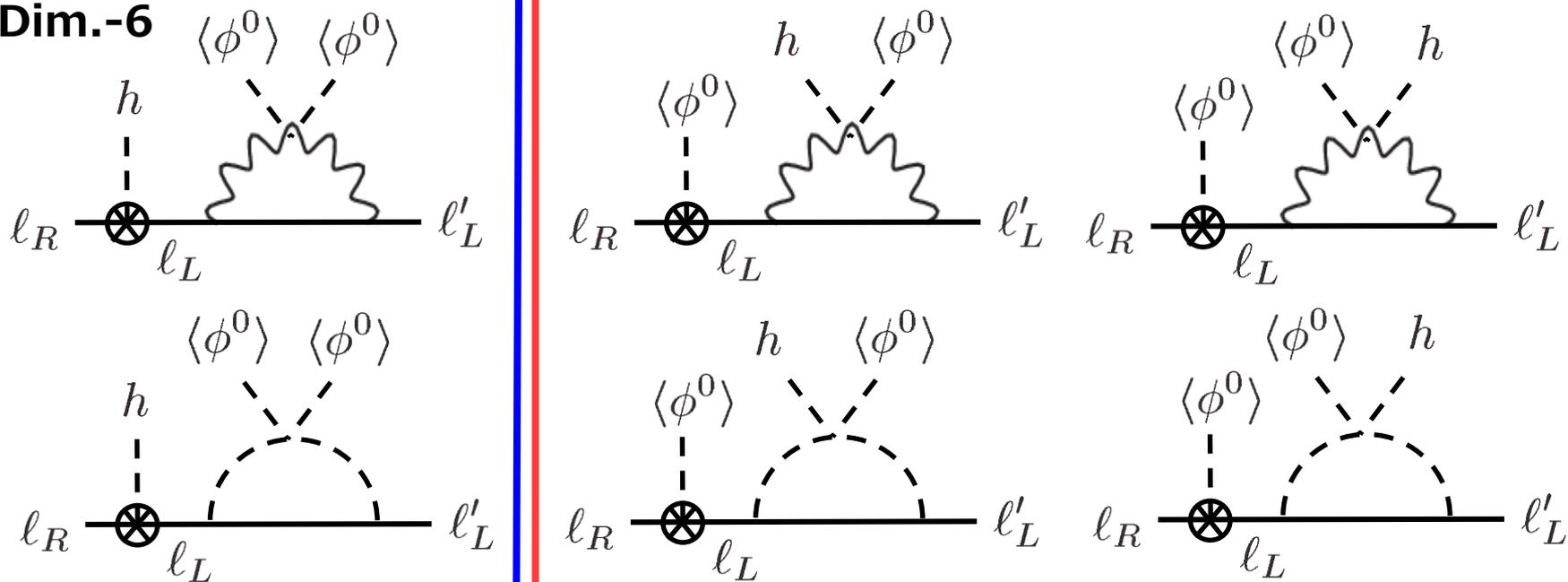
$$\text{Int. : } \left(\frac{1}{\sqrt{2}} \mathbf{Y}_4 + \frac{3v^2}{2\Lambda^2} \mathbf{Y}_6 \right) \left[\bar{\ell}_L \ell'_R h \right] \dashrightarrow \left(\frac{m_\ell}{v} \delta_{\ell\ell'} + \frac{v^2}{\Lambda^2} \mathbf{Y}_6 \right) \left[\bar{\ell}_L \ell'_R h \right]$$

Dim.-4

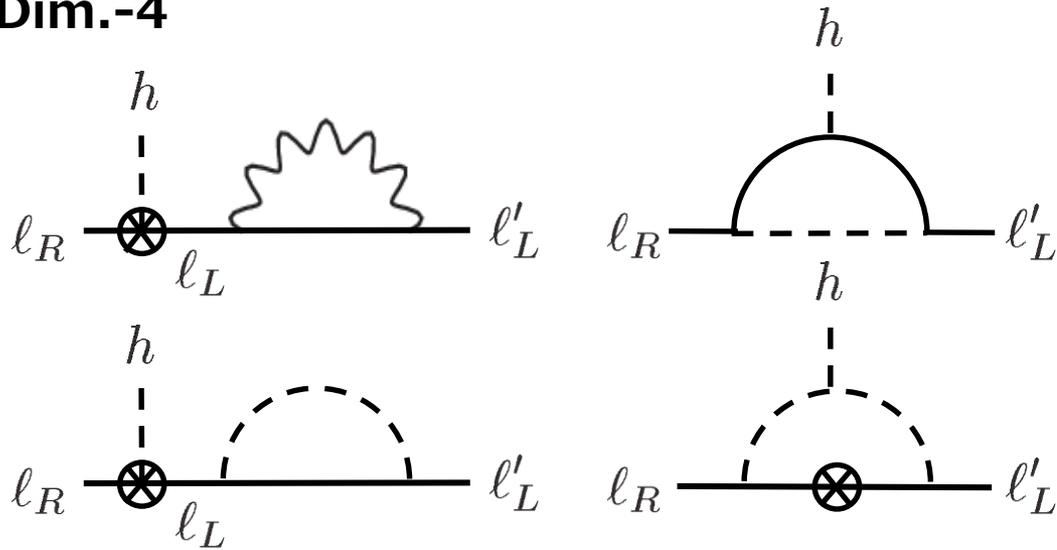


$$\left(\frac{m_l}{v} \delta_{ll'} + \frac{v^2}{\Lambda^2} \mathbf{Y}_6 \right) [\overline{l'_L} l_R h]$$

Dim.-6

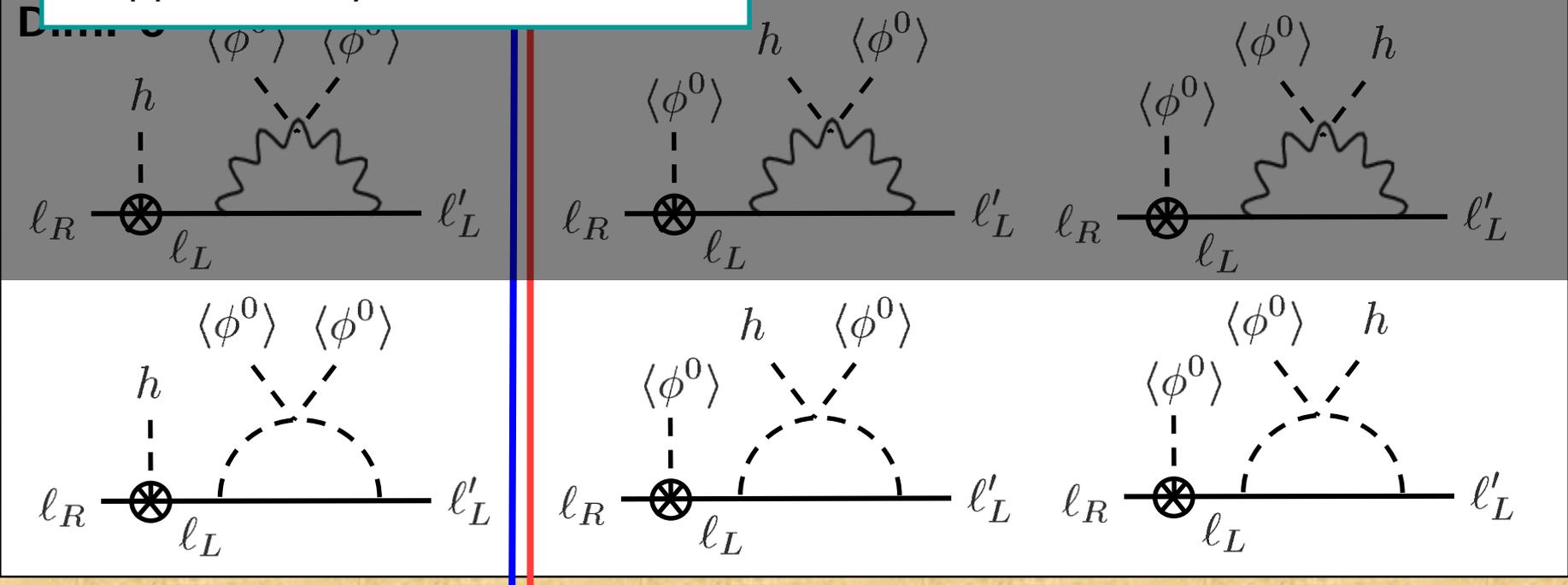


Dim.-4

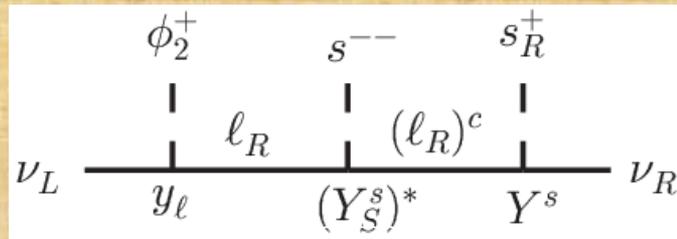


$$\left(\frac{m_l}{v} \delta_{ll'} + \frac{v^2}{\Lambda^2} \mathbf{Y}_6 \right) [\overline{l'_L} l_R h]$$

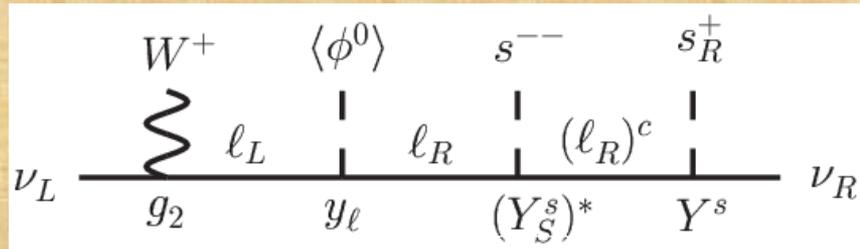
Suppressed by GIM mechanism



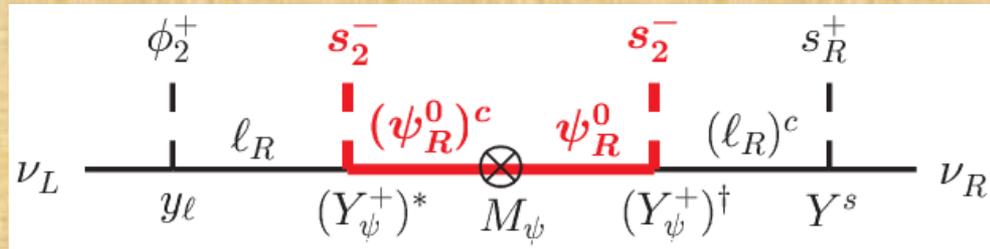
D3



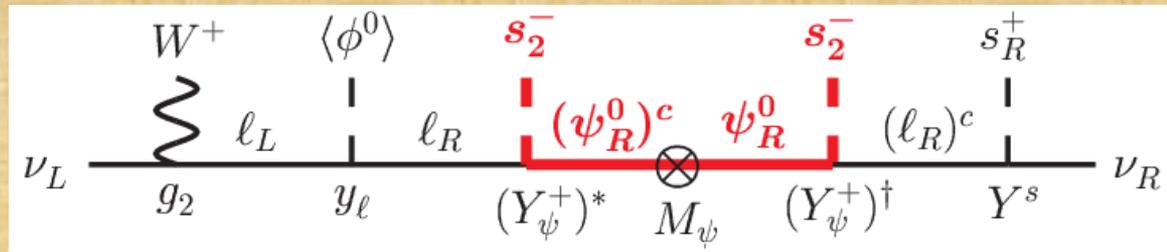
D4



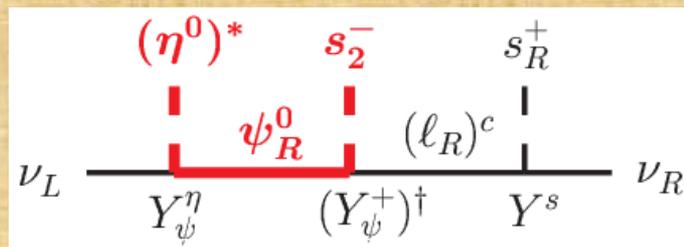
D11

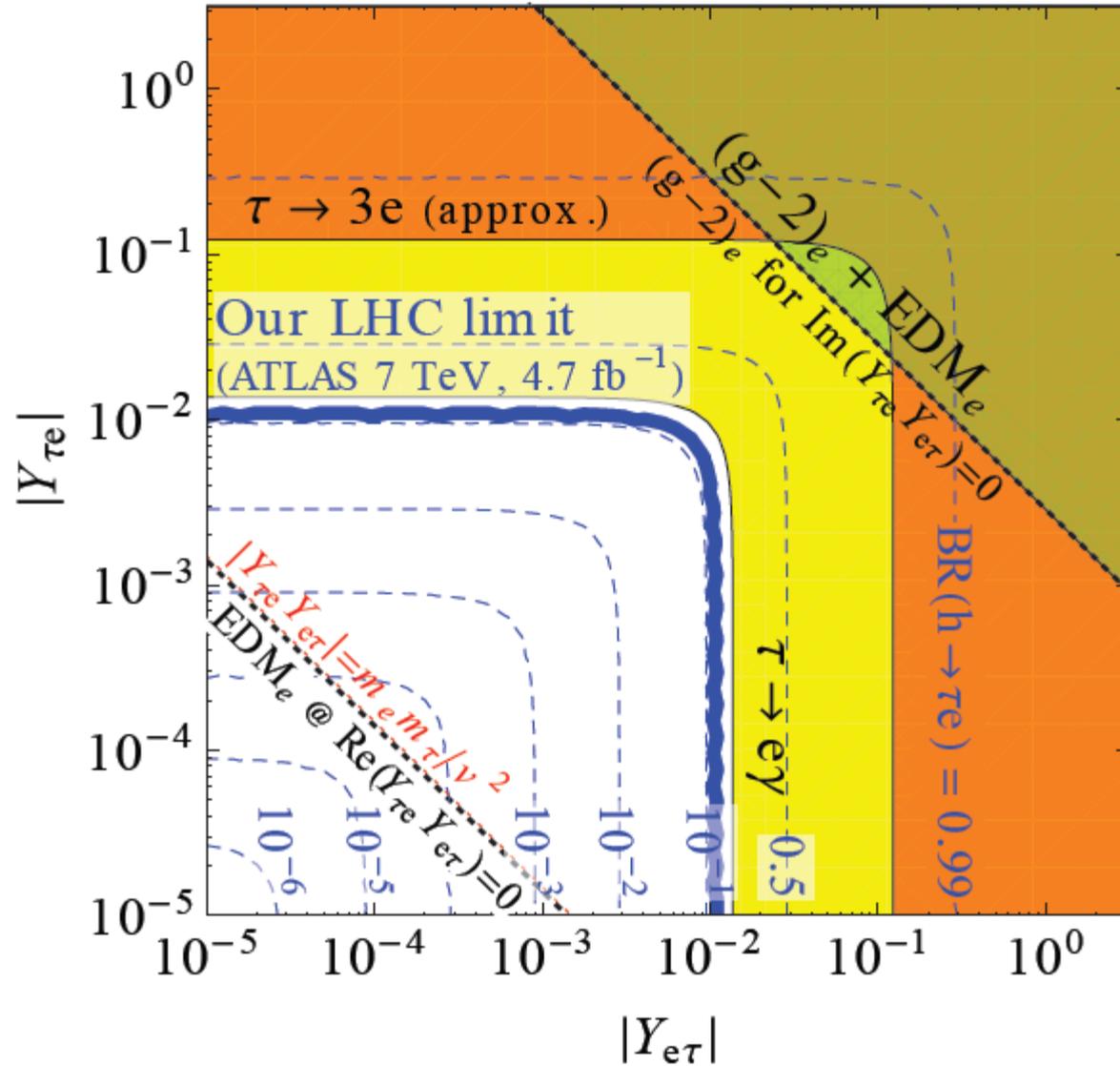


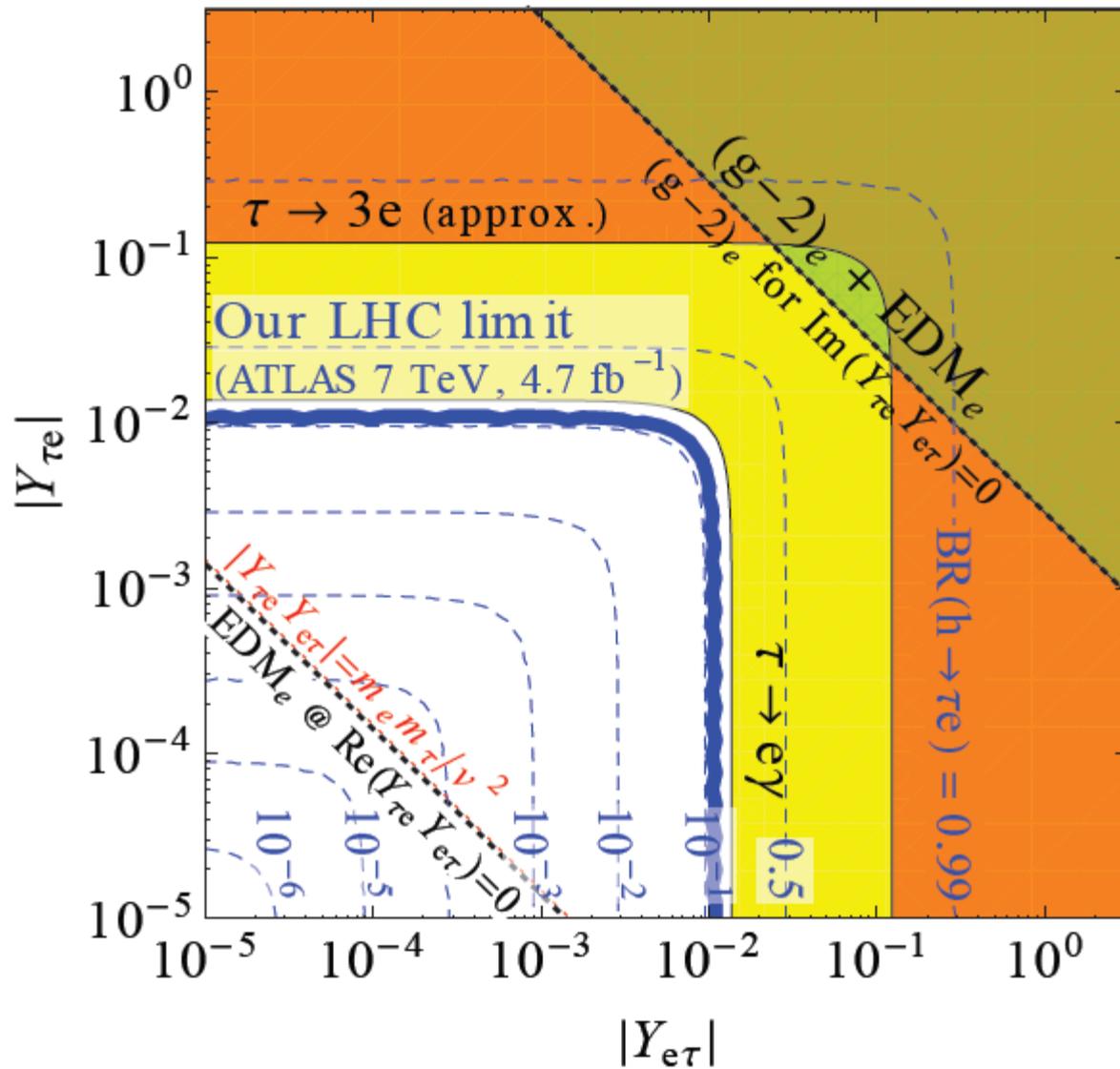
D12

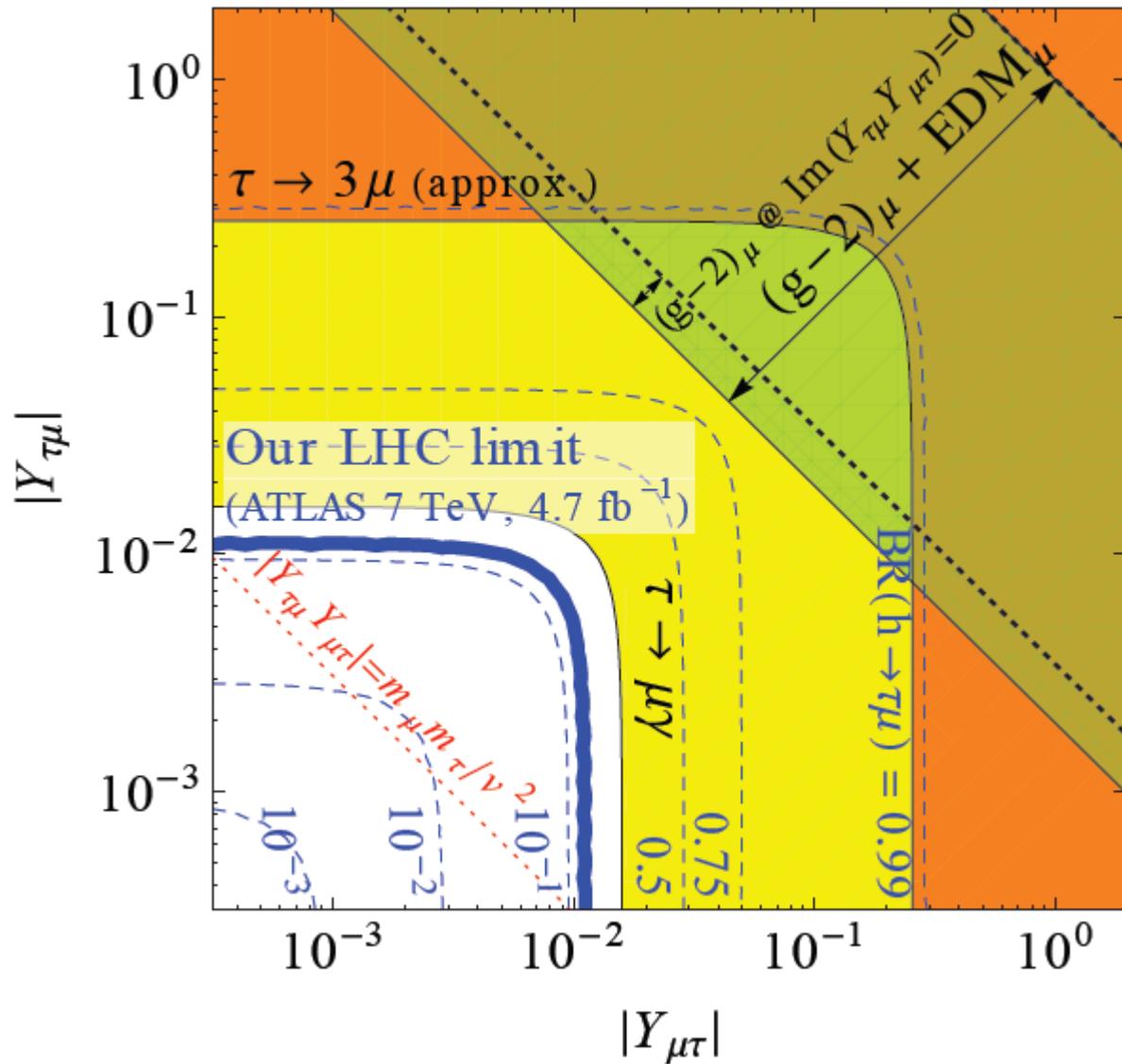


D17









$$\Phi_{LQ} = (\phi_{LQ}^{2/3}, \phi_{LQ}^{-1/3})^T \quad Y = 1/6$$

$$\begin{cases} \bar{Q} \Phi_{LQ} \nu_R \longrightarrow \bar{u}_L \nu_R \phi_{LQ}^{2/3} \\ \bar{d}_R \Phi_{LQ}^T \epsilon L \longrightarrow \bar{d}_R \ell_L \phi_{LQ}^{2/3} \end{cases}$$

$$\Phi'_{LQ} = (\phi'_{LQ}{}^{5/3}, \phi'_{LQ}{}^{2/3})^T \quad Y = 7/6$$

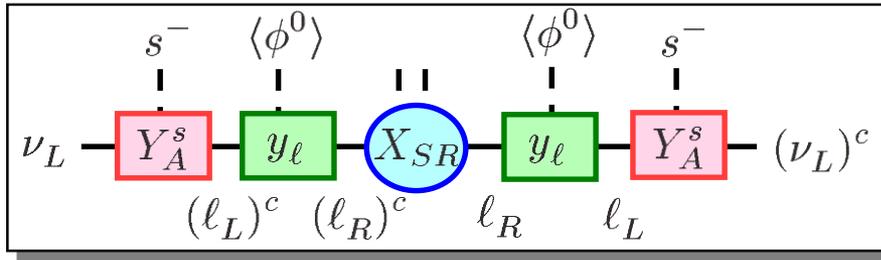
$$\begin{cases} \bar{Q} \Phi'_{LQ} \ell_R \longrightarrow \bar{d}_L \ell_R \phi'_{LQ}{}^{2/3} \\ \bar{u}_R \Phi'_{LQ}{}^T \epsilon L \longrightarrow \bar{u}_R \nu_L \phi'_{LQ}{}^{2/3} \end{cases}$$

3 Groups for Majorana ν mass

I) $m_L \propto$

$$Y_A^s y_l X_{SR} y_l Y_A^{sT}$$

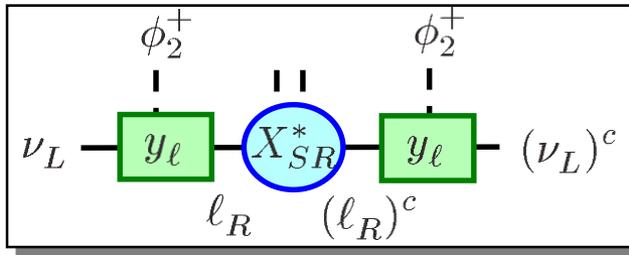
Y_A : **Antisym.** Yukawa for s^-



II) $m_L \propto$

$$y_l X_{SR}^* y_l$$

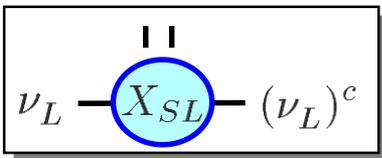
y_l : **Diagonal** Yukawa ($\propto m_\ell$) for Φ



III) $m_L \propto$

$$X_{SL}$$

$X_{SL}(X_{SR})$: **Sym.** matrix



For Dirac ν masses (without DM)

Scalar with leptonic Yukawa int.

								Z_2 -odd			
	s^0	s_L^+	s_R^+	s^{++}	Φ_ν	Φ_2	Δ	s_2^0	s_2^+	η	
$SU(2)_L$	<u>1</u>	<u>1</u>	<u>1</u>	<u>1</u>	<u>2</u>	<u>2</u>	<u>3</u>	<u>1</u>	<u>1</u>	<u>2</u>	
$U(1)_Y$	0	1	1	2	1/2	1/2	1	0	1	1/2	
L#	-2	-2	-2	-2	0	0	-2	-1	-1	-1	
Z'_2	+	+	-	+	-	+	+	-	+	+	
D1		✓	✓								→ I'
D2			✓				✓				→ IV
D3			✓	✓			✓				} V
D4			✓	✓							
D5	✓		✓				✓				} VI
D6	✓		✓								
D7					✓						→ III'

For Dirac ν masses (with DM)

Scalar with leptonic Yukawa int.

								Z_2 -odd		
	s^0	s_L^+	s_R^+	s^{++}	Φ_ν	Φ_2	Δ	s_2^0	s_2^+	η
$SU(2)_L$	<u>1</u>	<u>1</u>	<u>1</u>	<u>1</u>	<u>2</u>	<u>2</u>	<u>3</u>	<u>1</u>	<u>1</u>	<u>2</u>
$U(1)_Y$	0	1	1	2	1/2	1/2	1	0	1	1/2
L#	-2	-2	-2	-2	0	0	-2	-1	-1	-1
Z'_2	+	+	-	+	-	+	+	-	+	+
D8		✓						✓	✓	
D9							✓	✓	✓	
D10			✓							✓
D11			✓			✓			✓	
D12			✓						✓	
D13			✓			✓		✓		
D14			✓					✓		
D15						✓		✓	✓	
D16								✓	✓	
D17			✓						✓	✓
D18								✓		✓

7 Groups

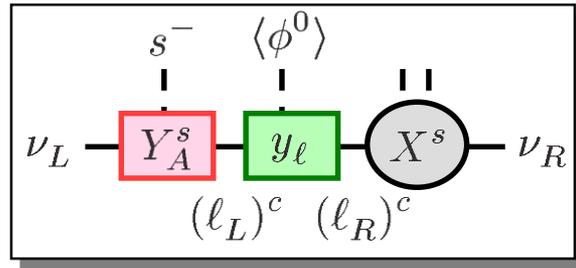
→ I'
 } IV
 } V
 } VI
 } II'
 → VII
 → III'

18 Mechanisms

7 Groups for Dirac ν mass

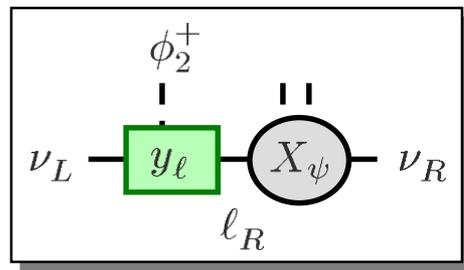
$$\mathbf{I}') m_D \propto Y_A^s y_l X^s$$

Y_A : **Antisym.** Yukawa for s^-



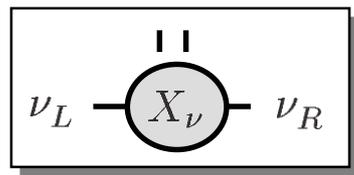
$$\mathbf{II}') m_D \propto y_l X_\psi$$

y_l : **Diagonal** Yukawa ($\propto m_\ell$) for Φ

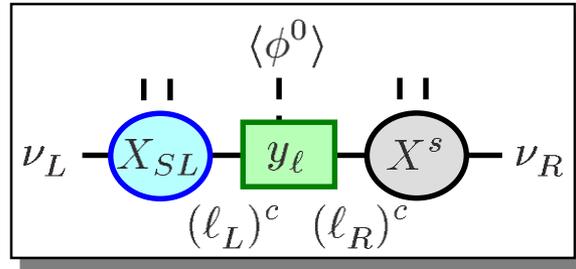


$X_\nu(X^s, X_\psi)$: Arbitrary

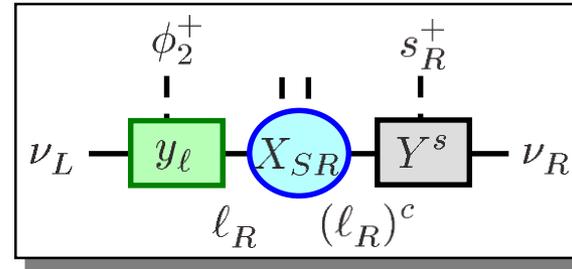
$$\mathbf{III}') m_D \propto X_\nu$$



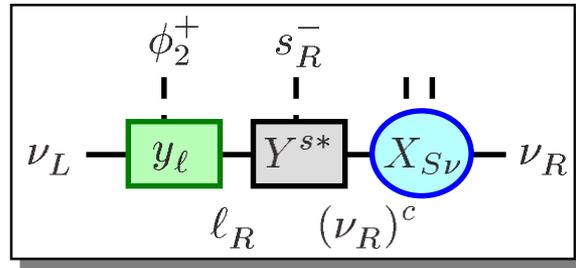
$$\text{IV) } m_D \propto X_{SL} y_l X^s$$



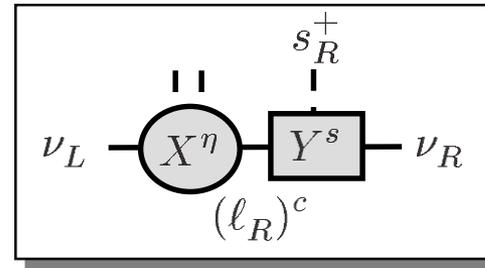
$$\text{V) } m_D \propto y_l X_{SR} Y^s$$



$$\text{VI) } m_D \propto y_l (Y^s)^* X_{S\nu}$$



$$\text{VII) } m_D \propto X^\eta Y^s$$



How can we discriminate them ?

(mainly **I**, **II**, **III**, **I'**, **II'**, **III'**)



Concentrating on Yukawa \Rightarrow **Flavor experiments**

$$l \rightarrow \bar{l}_1 l_2 l_3$$

$$l \rightarrow l' \nu \bar{\nu}$$

$$l \rightarrow l' \gamma \quad h \rightarrow ll'$$

$\tau \rightarrow \bar{l}_1 l_2 l_3$ for Majorana case

S. Kanemura, HS, PLB753, 161

I) $Y_A^s y_\ell X_{SR} y_\ell Y_A^{sT}$

II) $y_\ell X_{SR}^* y_\ell$

III) X_{SL}

$X_{SR} : (\ell_R)^c - \ell_R - [\text{scalars}]$

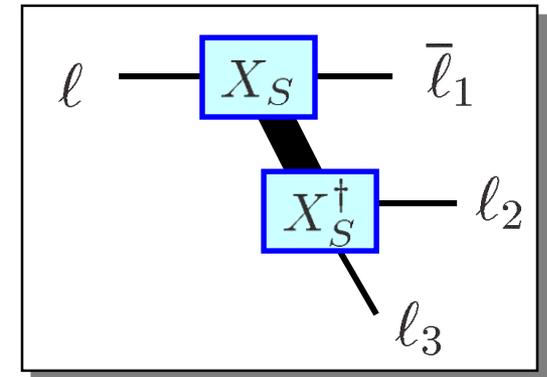
$X_{SL} : \ell_L - (\ell_L)^c - [\text{scalars}]$

X_S causes $l \rightarrow \bar{l}_1 l_2 l_3$

Stringent constraint $\text{BR}(\mu \rightarrow \bar{e} e e) < 10^{-12}$

→ Naively, no signal of $\tau \rightarrow \bar{l}_1 l_2 l_3$
 (Expected sensitivity : $\text{BR} \sim 10^{-9}$)

Belle-II collab., arXiv:1011.0352



Signal of $\tau \rightarrow \bar{l}_1 l_2 l_3 \Rightarrow (X_S)_{ee} = 0$ or $(X_S)_{e\mu} = 0$

II) III) $\Rightarrow (m_L)_{ee} = 0$ or $(m_L)_{e\mu} = 0$

\Rightarrow Prediction for flavor structure of $\tau \rightarrow \bar{l}_1 l_2 l_3$

I) has no prediction

	I)	II) $y_l X_{SR}^* y_l$			III) X_{SL}		
		$(m_\nu)_{ee} = 0$	$(m_\nu)_{e\mu} = 0$		$(m_\nu)_{ee} = 0$	$(m_\nu)_{e\mu} = 0$	
		N	N	I	N	N	I
$\tau \rightarrow \bar{e}ee$	✓	/	✓	✓	/	✓	✓
$\bar{e}e\mu$	✓	✓	/	/	/	/	/
$\bar{e}\mu\mu$	✓	✓	/	/	✓	✓	✓
$\bar{\mu}ee$	✓	/	✓	✓	/	✓	✓
$\bar{\mu}e\mu$	✓	✓	/	/	✓	/	/
$\bar{\mu}\mu\mu$	✓	/	/	/	✓	✓	✓

$\left\{ \begin{array}{l} \text{N : } m_1 < m_3 \text{ (Normal)} \\ \text{I : } m_1 > m_3 \text{ (Inverted)} \end{array} \right.$

$\left\{ \begin{array}{l} \checkmark : \text{Largest} \\ \checkmark : \text{can be observed} \end{array} \right.$

can be determined by ν osc.

	I)	II) $y_l X_{SR}^* y_l$			III) X_{SL}		
		$(m_L)_{ee}$	$X_{SR}^* \propto y_l^{-1} m_L y_l^{-1}$		$(m_L)_{ee} = 0$	$(m_L)_{e\mu} = 0$	
		N	Electron-philic		N	N	I
$\tau \rightarrow \bar{e}ee$	✓		✓	✓		✓	✓
$\bar{e}e\mu$	✓	✓					
$\bar{e}\mu\mu$	✓	✓			✓	✓	✓
$\bar{\mu}ee$	✓		✓	✓		✓	✓
$\bar{\mu}e\mu$	✓	✓			✓		
$\bar{\mu}\mu\mu$	✓				✓	✓	✓

$\left\{ \begin{array}{l} \text{N : } m_1 < m_3 \text{ (Normal)} \\ \text{I : } m_1 > m_3 \text{ (Inverted)} \end{array} \right.$

$\left\{ \begin{array}{l} \checkmark : \text{Largest} \\ \checkmark : \text{can be observed} \end{array} \right.$

can be determined by ν osc.

No $0\nu\beta\beta$ (e.g. $^{136}_{56}\text{Xe} \rightarrow ^{136}_{58}\text{Ba} + 2e^-$)

	I)	II) $y_l X_{SR}^* y_l$		III) X_{SL}		
		$(m_L)_{ee} = 0$	$(m_L)_{e\mu} = 0$	$(m_L)_{ee} = 0$	$(m_L)_{e\mu} = 0$	
		N	N	I	N	I

$\tau \rightarrow \bar{e}ee$

$\bar{e}e\mu$

$\bar{e}\mu\mu$

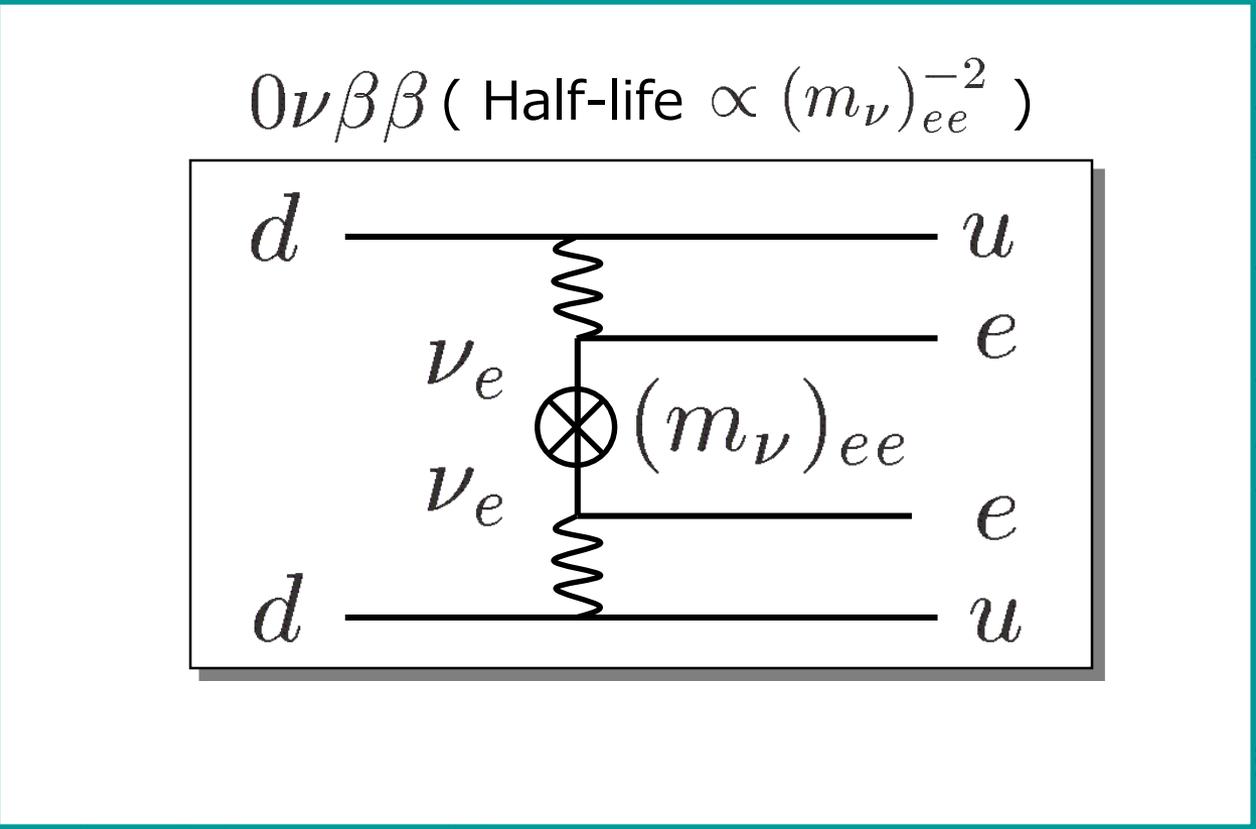
$\bar{\mu}ee$

$\bar{\mu}e\mu$

$\bar{\mu}\mu\mu$



can be determined by ν osc.



erved

	I)	II) $y_l X_{SR}^* y_l$			III) X_{SL}		
		$(m_L)_{ee} = 0$	$(m_L)_{e\mu} = 0$		$(m_L)_{ee} = 0$	$(m_L)_{e\mu} = 0$	
		N	N	I	N	N	I
$\tau \rightarrow \bar{e}ee$	✓	/	✓	✓	/	✓	✓
$\bar{e}e\mu$	✓	✓	/	/	/	/	/
$\bar{e}\mu\mu$	✓	✓			✓	✓	✓
$\bar{\mu}ee$	✓	/	✓	✓	/	✓	✓
$\bar{\mu}e\mu$	✓	✓	/	/	✓	/	/
$\bar{\mu}\mu\mu$	✓				✓	✓	✓

$\left\{ \begin{array}{l} \text{N : } m_1 < m_3 \text{ (Normal)} \\ \text{I : } m_1 > m_3 \text{ (Inverted)} \end{array} \right.$

$\left\{ \begin{array}{l} \checkmark : \text{Largest} \\ \checkmark : \text{can be observed} \end{array} \right.$

can be determined by ν osc.

	I)	II) $y_l X_{SR}^* y_l$			III) X_{SL}		
		$(m_L)_{ee} = 0$	$(m_L)_{e\mu} = 0$		$(m_L)_{ee} = 0$	$(m_L)_{e\mu} = 0$	
		N	N	I	N	N	I
$\tau \rightarrow \bar{e}ee$	✓		✓	✓		✓	✓
$\bar{e}e\mu$	✓	✓					
If observed		✓			✓	✓	✓
$\bar{\mu}ee$	✓		✓	✓		✓	✓
$\bar{\mu}e\mu$	✓	✓			✓		
$\bar{\mu}\mu\mu$	✓				✓	✓	✓

$\left\{ \begin{array}{l} \text{N : } m_1 < m_3 \text{ (Normal)} \\ \text{I : } m_1 > m_3 \text{ (Inverted)} \end{array} \right.$

$\left\{ \begin{array}{l} \checkmark : \text{Largest} \\ \checkmark : \text{can be observed} \end{array} \right.$

can be determined by ν osc.

No $0\nu\beta\beta$ (e.g. $^{136}_{56}\text{Xe} \rightarrow ^{136}_{58}\text{Ba} + 2e^-$)

	I)	II) $y_l X_{SR}^* y_l$		III) X_{SL}		
		$(m_L)_{ee} = 0$	$(m_L)_{e\mu} = 0$	$(m_L)_{ee} = 0$	$(m_L)_{e\mu} = 0$	
				N	N	I
$\tau \rightarrow \bar{e}ee$	✓		✓ ✓		✓	✓
$\bar{e}e\mu$	✓	✓				
				✓	✓	✓
$\bar{\mu}ee$	✓		✓ ✓		✓	✓
$\bar{\mu}e\mu$	✓	✓			✓	
$\bar{\mu}\mu\mu$	✓				✓	✓

If $0\nu\beta\beta$ is observed

If observed

- N : $m_1 < m_3$ (Normal)
- I : $m_1 > m_3$ (Inverted)

- ✓ : Largest
- ✓ : can be observed

can be determined by ν osc.

$\tau \rightarrow \ell \nu \bar{\nu}$ for Dirac case

S. Kanemura, K. Sakurai, HS, PLB758, 465

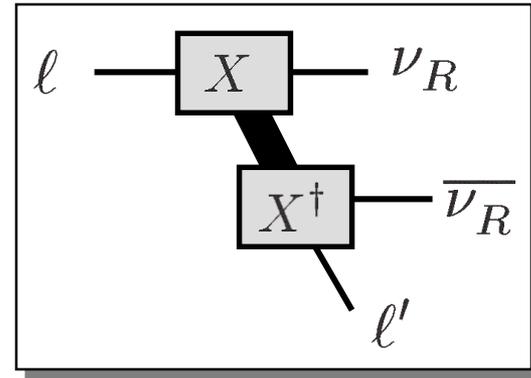
$$\text{II}') \quad m_D \propto y_\ell X_\psi$$

 $X_\psi : \ell_R - \nu_R - [\text{scalars}]$

$$\text{III}') \quad m_D \propto X_\nu$$

 $X_\nu : \ell_L - \nu_R - [\text{scalars}]$
 $\ell \rightarrow \ell' \nu_R \bar{\nu}_R$ via X

$$\left\{ \begin{array}{l} \mu \rightarrow e \nu \bar{\nu} \longrightarrow G_F^2 \\ \tau \rightarrow \ell' \nu \bar{\nu} \longrightarrow G_{\tau \ell'}^2 \end{array} \right. \begin{array}{l} \Downarrow \\ \text{Deviation} \\ \Uparrow \end{array}$$



$$\text{II}') \quad m_D \propto y_\ell X_\psi$$

$$\text{III}') \quad m_D \propto X_\nu$$

$$G_{\tau \mu}^2 \simeq G_{\tau e}^2 \lesssim G_F^2$$

$$\left\{ \begin{array}{l} G_{\tau \mu}^2 \gtrsim G_{\tau e}^2 \simeq G_F^2 \quad (m_1 < m_3) \\ G_{\tau \mu}^2 \lesssim G_{\tau e}^2 \simeq G_F^2 \quad (m_1 > m_3) \end{array} \right.$$

$$G_{\tau e}^2 / G_F^2 = 1.0029 \pm 0.0046 \quad \text{PDG}$$

$$G_{\tau \mu}^2 / G_{\tau e}^2 = 1.0036 \pm 0.0020 \quad \text{Babar collab., PRL105, 051602 (2010)}$$