

Cosmological implications of unification with D-parity

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Particles Strings and Cosmology PASCOS2017
ITF-UAM Madrid, 20 June 2017

Overview

- Seeking a GUT – the inevitability of D-parity
- Parity symmetric world at PeV scale \rightarrow SUSY L-R
- Domain wall dynamics
 - Domain wall removal
- Minimal Supersymmetric GUT – contenders with $SO(10)$
- The D-domain wall ... parametric
- Implications to cosmology

Collaborators : [Piyali Bannerjee](#), [Ila Garg](#) ... (Sasmita Mishra, Anjishnu Sarkar, Desish Borah)

What choices did *der Alte* have?

Looking beyond the SM in the light of

- Baryon asymmetry
- Neutrino masses and mixing

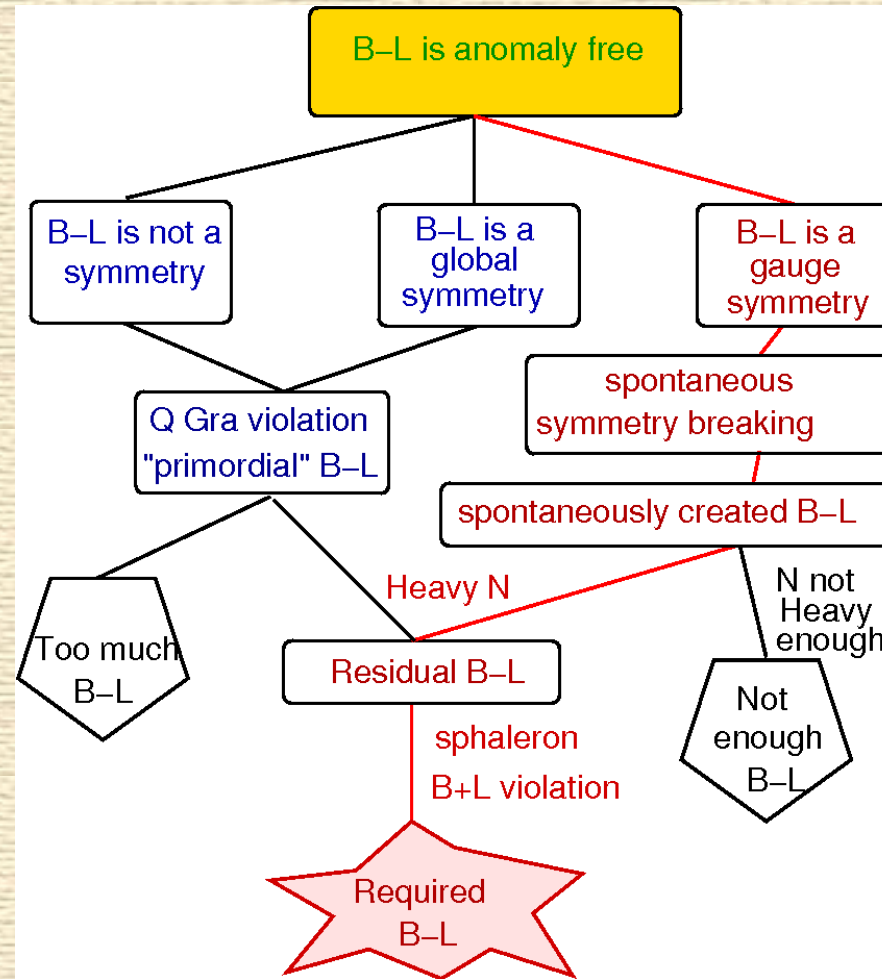
Toolkits

- Gauge principle – massless vector bosons; quantisation of charge
- Chirality – massless fermions
- Scalars – symmetry breaking and universal source of masses
 - $O(1)$ CP violation natural

Other than Dark Matter and Dark Energy, the almost massless neutrino begs inclusion within above principles ...

$B - L$ is one exact anomaly free ungauged charge

What choices did *der Alte* have?



“Just” Beyond the SM ?

The see-saw and the GUT scale

- Tentative possibility ... or
- False start about high scale?

GUT naturalness of gauge coupling unification \longrightarrow see-saw M_N was expected to fit in.

But note that

$$\begin{aligned} m_N &\approx \frac{m_D^2}{m_\nu} \\ &\approx 10^{14} \text{GeV} \left(\frac{0.1 \text{eV}}{m_\nu} \right) \left(\frac{m_D}{100 \text{GeV}} \right)^2 \\ &\approx 10^4 \text{GeV} \left(\frac{0.1 \text{eV}}{m_\nu} \right) \left(\frac{m_D}{1 \text{MeV}} \right)^2 \end{aligned}$$

So in the absence of any suggestive high scale, may as well explore the PeV scale.
(Narendra Sahu and UAY PRD 2005)

Minimal SUSY L-R Model – MSLRM

Just Beyond the Standard Model ... $SU(2)_L \otimes SU(2)_R \otimes U(1)_X$

$$Q = \tau_L^3 + \tau_R^3 + \frac{1}{2}X$$

- In praise of $B - L$... the only conserved charge of SM which is not gauged! \rightarrow Hereby it gains the status of being gauged

The minimal set of Higgs superfields required is,

$$\begin{aligned}\Phi_i &= (1, 2, 2, 0), & i &= 1, 2, \\ \Delta &= (1, 3, 1, 2), & \bar{\Delta} &= (1, 3, 1, -2), \\ \Delta_c &= (1, 1, 3, -2), & \bar{\Delta}_c &= (1, 1, 3, 2), \\ \Omega &= (1, 3, 1, 0), & \Omega_c &= (1, 1, 3, 0)\end{aligned}$$

where the bidoublet is doubled so that the model has non-vanishing Cabibbo-Kobayashi-Maskawa matrix. The number of triplets is doubled to have anomaly cancellation.

Under discrete parity symmetry the fields are prescribed to transform as,

$$\begin{aligned} Q &\leftrightarrow Q_c^*, & L &\leftrightarrow L_c^*, & \Phi_i &\leftrightarrow \Phi_i^\dagger, \\ \Delta &\leftrightarrow \Delta_c^*, & \bar{\Delta} &\leftrightarrow \bar{\Delta}_c^*, & \Omega &\leftrightarrow \Omega_c^*. \end{aligned} \quad (1)$$

The F-flatness and D-flatness conditions lead to the following set of vev's for the Higgs fields as one of the possibilities,

$$\langle \Omega_c \rangle = \begin{pmatrix} \omega_c & 0 \\ 0 & -\omega_c \end{pmatrix}, \quad \langle \Delta_c \rangle = \begin{pmatrix} 0 & 0 \\ d_c & 0 \end{pmatrix}, \quad \langle \Phi_i \rangle = \begin{pmatrix} \kappa_i & 0 \\ 0 & \kappa_i' \end{pmatrix} \quad (2)$$

This ensures spontaneous parity violation [Aulakh, Bajc, Melfo, Rasin, Senjanovic (1998 ...)] Mass scale see-saw

- An R symmetry ensures Ω mass terms in superpotential are vanishing, no new spurious mass scale
- Leads naturally to a see-saw relation

$$M_{B-L}^2 = M_{EW} M_R$$

- Leptogenesis postponed to an energy scale closer to M_{EW} not a high scale like $10^9 - 10^{14}$ GeV

The D-degeneracy of vacua

A $U(1)_D$ path connecting $SU(2)_L$ and $SU(2)_R$ like vacua :

$$W_L = m_\Delta \cos^2 \frac{\theta}{2} d^2 + 2 m_\Omega \cos^2 \frac{\theta}{2} w^2 + a \cos^3 \frac{\theta}{2} d^2 w$$

$$W_R = m_\Delta \sin^2 \frac{\theta}{2} d^2 + 2 m_\Omega \sin^2 \frac{\theta}{2} w^2 + a \sin^3 \frac{\theta}{2} d^2 w$$

So when $\theta=0$, we have left like vacuum and for $\theta = \pi$, right like. Now

$$\frac{\partial V}{\partial \theta} = 2 \text{Re} \sum_i \frac{\delta W}{\delta \phi_i} \frac{\partial}{\partial \theta} \left(\frac{\delta W}{\delta \phi_i} \right)$$

Using $w = \frac{-m_\Delta}{a}$ and $d = \left(\frac{2m_\Delta m_\Omega}{a^2} \right)^{\frac{1}{2}}$ whihc gives usual vacua,

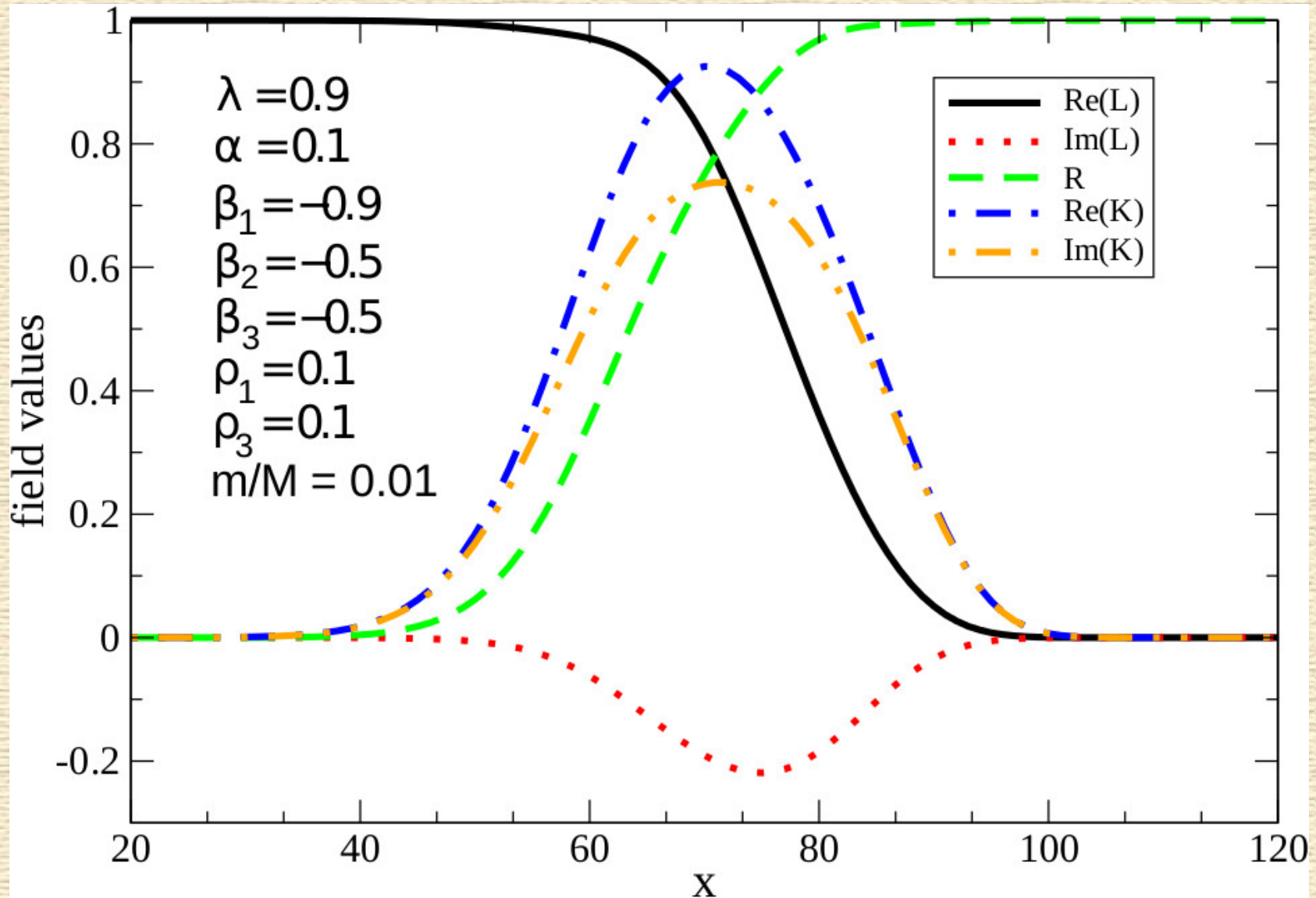
$$\frac{\delta V_{total}}{\delta \theta} = \sin \theta \left(-d^2 \cos \theta \left(w^2 + \frac{a^2}{4} \right) + a d^2 \left(\sin \frac{\theta}{2} - \cos \frac{\theta}{2} \right) (2w^2 - d^2) \right)$$

When $\theta = \frac{\pi}{2}$, we have a another minima and potential energy at that minima is given by,

$$V_{DW} = d^2 w^2 \left(-a + \frac{1}{\sqrt{2}} \right)^2 + d^2 (-a d + w)^2$$

D-parity domain wall and CP violation

Example of simulated domain walls in a Left-Right symmetric model



(Cline, Rabikumar and UAY; Anjishnu Sarkar, UAY)

- The left-right symmetric model has domain walls, with sufficient CP violation provided by the scalar condensates to produce lepton number at a low scale.
- **Open question** : relating the dynamical $O(1)$ CP phase to static phases in EDM etc.

Domain wall dynamics

Domain wall dynamics in radiation dominated phase

(Kibble; Vilenkin)

The dynamics of the walls is determined by two quantities :

- Tension force $f_T \sim \sigma / R$, where σ is energy per unit area and R is the average scale of radius of curvature
- Friction force $f_F \sim \beta T^4$ for walls moving with speed β in a medium of temperature T

The two get balanced at time $t_R \sim R / \beta$ being the time scale by which the wall portions that started with radius of curvature scale R straighten out. From this we get required energy density difference

$$\delta \rho \geq G \sigma^2 \approx \frac{M_R^6}{M_{Pl}^2} \sim M_R^4 \frac{M_R^2}{M_{Pl}^2} \quad (3)$$

Domain wall dynamics in a matter dominated phase

Kawasaki and Takahashi(2004), Anjishnu Sarkar and UAY(2006)

Assume the initial wall complex relaxes to roughly one wall per horizon at a Hubble value H_i with the initial energy density in the wall complex $\rho_W^{(in)} \sim \sigma H_i$

Let the temperature at which the domain walls are formed be $T \sim \sigma^{1/3}$. So

$$H_i^2 = \frac{8\pi}{3} G \sigma^{\frac{4}{3}} \sim \frac{\sigma^{\frac{4}{3}}}{M_{Pl}^2} \quad (4)$$

From Eq.(?) we get,

$$T_D^4 \sim \frac{\sigma^{11/6}}{M_{Pl}^{3/2}} \sim \frac{M_R^{11/2}}{M_{Pl}^{3/2}} \sim M_R^4 \left(\frac{M_R}{M_{Pl}} \right)^{3/2} \quad (5)$$

Now requiring $\delta\rho > T_D^4$ we get,

$$\delta\rho > M_R^4 \left(\frac{M_R}{M_{Pl}} \right)^{3/2} \quad (6)$$

This quantifies the extent of effective potential difference across the walls for them to disappear.

How to rid ourselves of the domain walls

(Preskill, Srednicki, Trivedi and Wilczek)

$$\delta\rho \approx T_{\text{Decoupling}}^4 \gtrsim T_{BBN}^4$$

Soft supersymmetric terms in Left-Right model

$$\begin{aligned} \mathcal{L}_{soft}^1 = & m_1^2 \text{Tr}(\Delta \Delta^\dagger) + m_2^2 \text{Tr}(\bar{\Delta} \bar{\Delta}^\dagger) \\ & + m_3^2 \text{Tr}(\Delta_c \Delta_c^\dagger) + m_4^2 \text{Tr}(\bar{\Delta}_c \bar{\Delta}_c^\dagger) \end{aligned} \quad (7)$$

$$\begin{aligned} \mathcal{L}_{soft}^2 = & \alpha_1 \text{Tr}(\Delta \Omega \Delta^\dagger) + \alpha_2 \text{Tr}(\bar{\Delta} \Omega \bar{\Delta}^\dagger) \\ & + \alpha_3 \text{Tr}(\Delta_c \Omega_c \Delta_c^\dagger) + \alpha_4 \text{Tr}(\bar{\Delta}_c \Omega_c \bar{\Delta}_c^\dagger) \end{aligned} \quad (8)$$

$$\mathcal{L}_{soft}^3 = \beta_1 \text{Tr}(\Omega \Omega^\dagger) + \beta_2 \text{Tr}(\Omega_c \Omega_c^\dagger) \quad (9)$$

$$\mathcal{L}_{soft} = \mathcal{L}_{soft}^1 + \mathcal{L}_{soft}^2 + \mathcal{L}_{soft}^3 \quad (10)$$

- Demand that the soft parameters differ in the two possible phases $SU(2)_L \otimes U(1)_Y$ and $SU(2)_R \otimes U(1)_{\tilde{Y}}$
- Demand that the pressure difference created is enough to get rid of the domain walls well before Big Bang Nucleosynthesis

For PeV scale M_N (RH majorana neutrino mass), we get the constraints :

$T_D / \text{GeV} \sim$	10	10^2	10^3
$(m^2 - m^{2'}) / \text{GeV}^2 \sim$	10^{-4}	1	10^4
$(\beta_1 - \beta_2) / \text{GeV}^2 \sim$	10^{-8}	10^{-4}	1

Table 1. Differences in values of soft supersymmetry breaking parameters for a range of domain wall decay temperature values T_D . The differences signify the extent of parity breaking.

Open question : look for a way to generate this difference in V^{eff}
 (Sasmita Mishra, UAY PRD 2008; Sasmita Mishra, Anjishnu Sarkar, UAY PRD 2009, Sasmita Mishra, Debasish Borah JHEP 2011)

Minimal Supersymmetric SO(10) GUT

Aulakh, Bajc, Melfo, Senjanovic, Vissani 2004

The Higgs content $\mathbf{210} - \Phi_{ijkl}, \mathbf{126}(\overline{\mathbf{126}}) - \Sigma_{ijklm} (\bar{\Sigma}_{ijklm})$, (and additionally H_i)

The $\overline{\mathbf{126}}$ with $\mathbf{210}$ breaks the SO(10) \rightarrow MSSM .

The renormalizable superpotential

$$W = \frac{m_\Phi}{4!} \Phi^2 + \frac{\lambda}{4!} \Phi^3 + \frac{m_\Sigma}{5!} \Sigma \bar{\Sigma} + \frac{\eta}{4!} \Phi \Sigma \bar{\Sigma} + m_H H^2 + \frac{1}{4!} \Phi H (\gamma \Sigma + \bar{\gamma} \bar{\Sigma}).$$

D-parity is defined as

$$D = \exp(i \pi J_{23}) \exp(i \pi J_{67}) \quad (11)$$

In terms of SO(10) vector indices the fields which acquire vev are written as

$$P = [7, 8, 9, 10]$$

$$A = [1, 2, 3, 4] + [1, 2, 5, 6] + [3, 4, 5, 6]$$

$$W_R^0 = [1, 2, 7, 8] + [3, 4, 7, 8] + [5, 6, 7, 8] + [1, 2, 9, 10] + [3, 4, 9, 10] + [5, 6, 9, 10]$$

$$\begin{aligned}
\Sigma_R^- &= -i([1, 3, 5, 7, 9] - [2, 4, 5, 7, 9] - [2, 3, 6, 7, 9] - [1, 4, 6, 7, 9] \\
&\quad -i[2, 3, 5, 7, 9] - i[1, 4, 5, 7, 9] - i[1, 3, 6, 7, 9] + i[2, 4, 6, 7, 9]) \\
&\quad - (7, 9 \rightarrow 8, 10) + i \{7, 9 \rightarrow 7, 10\} + i \{7, 9 \rightarrow 8, 9\} \\
\bar{\Sigma}_R^+ &= i([1, 3, 5, 7, 9] - [2, 4, 5, 7, 9] - [2, 3, 6, 7, 9] - [1, 4, 6, 7, 9] \\
&\quad + i[2, 3, 5, 7, 9] + i[1, 4, 5, 7, 9] + i[1, 3, 6, 7, 9] - i[2, 4, 6, 7, 9]) \\
&\quad - (7, 9 \rightarrow 8, 10) - i \{7, 9 \rightarrow 7, 10\} - i \{7, 9 \rightarrow 8, 9\} \tag{12}
\end{aligned}$$

The sign $+(-)$ in the superscript represents the T_{3R} value. Under the action of D-parity these vevs transform as

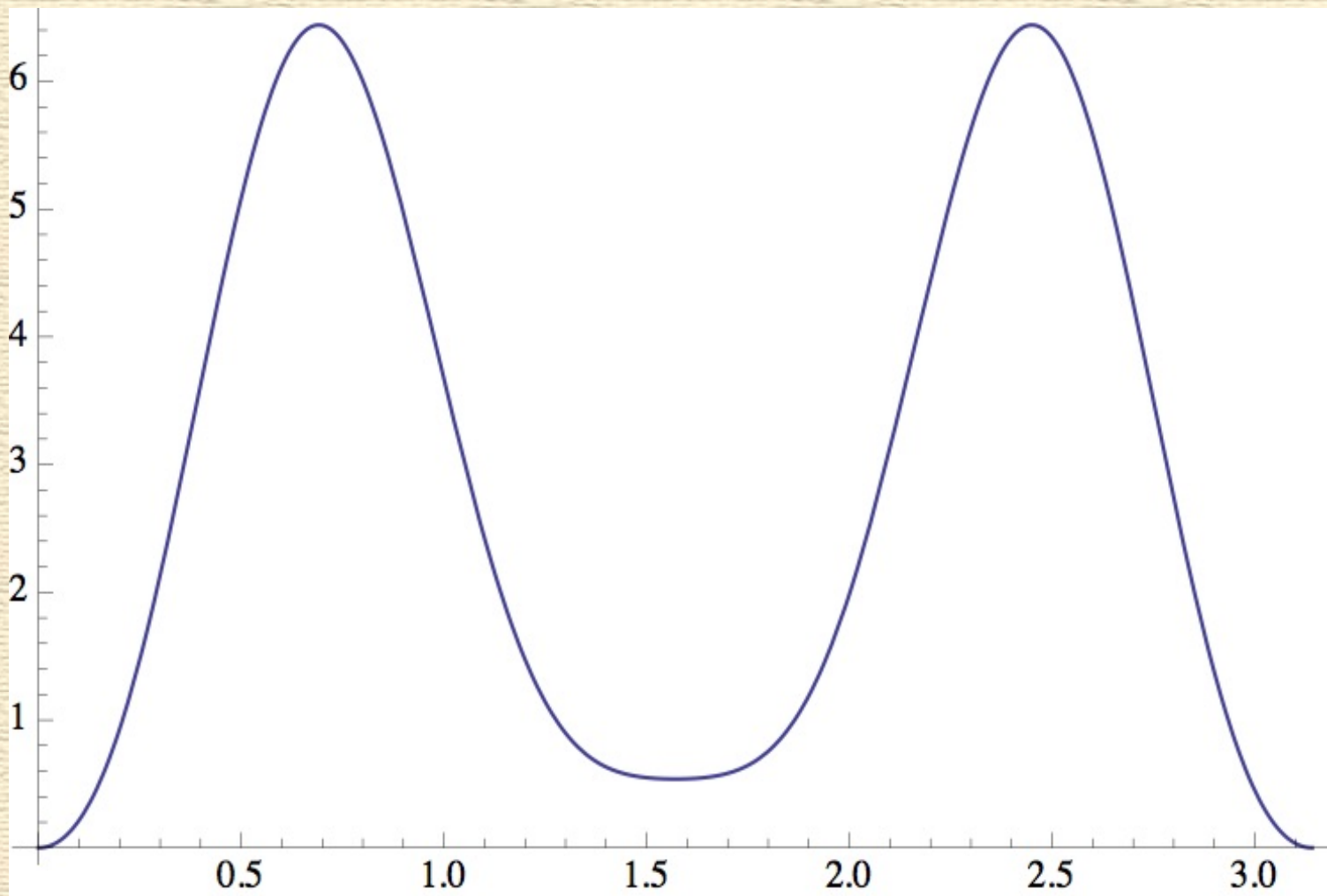
$$\begin{aligned}
P &\rightarrow -P; & A &\rightarrow A; & W_R^0 &\rightarrow W_L^0 \\
\Sigma_R^- &\rightarrow -\Sigma_L^+; & \bar{\Sigma}_R^+ &\rightarrow -\bar{\Sigma}_L^-
\end{aligned}$$

Connecting to the D-flipped sector

$$\begin{aligned} W = & m_{\Phi} \left((1 + \sin^2 2\theta) p^2 + ((2 + \cos 2\theta)^2 - \sin^2 2\theta) a^2 + ((-\sin\theta + \cos 2\theta + 2)^2 + (\sin 2\theta + 3\cos\theta)^2) w^2 + \right. \\ & + 2\lambda \left(\frac{1}{2} (27\cos 2\theta - \cos 6\theta + 28) a^3 + \frac{1}{2} (\sin\theta + \sin 3\theta + 2) (\sin 3\theta + 4\cos 2\theta + 5) p w^2 \right. \\ & + \frac{1}{3} (\sin 3\theta + 4\cos 2\theta + 5) (\sin\theta + \sin 3\theta + \cos\theta + 2\cos 2\theta + 3) a w^2 \\ & + \frac{m_{\Sigma}}{15} \sigma \bar{\sigma} (4\sin\theta + \sin 3\theta + 30\cos 2\theta + \cos 4\theta + 34) \\ & + \frac{\eta}{120} \sigma \bar{\sigma} (p (212\sin\theta + 224\sin 3\theta + 36\sin 5\theta + 240\cos 2\theta - 10\cos 4\theta + 290) \\ & + a (2 (116\sin\theta + 124\sin 3\theta + 20\sin 5\theta + 378\cos 2\theta + 59\cos 4\theta + 2\cos 6\theta + 341)) \\ & \left. \left. + w (2 (67\sin\theta + 93\sin 3\theta + 18\sin 5\theta + 762\cos 2\theta + 115\cos 4\theta + 2\cos 6\theta + 657))) \right) \right) \end{aligned} \quad (13)$$

Plot of potential

For representative values of the parameters



As expected we have vacua at 0 and 2π , but we see a double humped feature.
Work in progress ...

Wall removal and cosmology

- Unlike low scale model L-R, available possibilities are different
- Spontaneous formation of a hole in the wall due to cosmic string formation – dependent on Higgs content
- Planck suppressed non-renormalisable contribution

If the walls are not removed in good time,

- The dynamics may merge with that of the inflaton
- If delayed in removal, could leave CMB signature

Conclusions

- D-parity natural with right handed neutrino
 - Domain wall dominated phase inevitable in generic models
- Non-thermal leptogenesis natural through domain walls – so DW not all bad!
- Domain wall disappearance requirement constrains soft terms in low scale JBSM
- For $SO(10)$ D-parity there are implications for inflation and perhaps CMB

–> Thanks page



¡Gracias!



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