

What is the Magnetic Weak Gravity Conjecture for Axions?

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based on work with Arthur Hebecker & Lukas Witkowski [[1701.06553](#)]

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Motivation

Axions are inflaton candidates in models of **large-field inflation**.

[Freese, Friemann, Olinto; 1990]

For these models to work one needs a **super-Planckian axion decay constant f** .

(See, however, [Kim, Nilles, Peloso; 2005 / Dimopoulos, Kachru, McGreevy, Wacker; 2008 / ...] for attempts to evade this requirement.)

The magnetic **Weak Gravity Conjecture (WGC)** for axions naively gives a strong constraint on f .

This talk is about the interpretation of the WGC. For recent attempts towards a 'derivation' see for example [Cottrell, Shiu, Soler; 2016 / Hebecker, Soler; 2017].

Electric Weak Gravity Conjecture

Question: Which consistent low energy effective field theories are also consistent with quantum gravity?

Part of the answer might be provided by the WGC: [Arkani-Hamed, Motl, Nicolis, Vafa; 2007]

Consider a U(1) gauge theory with charged particles (1-form theory):

$$S = \frac{1}{2g_e^2} \int F_2 \wedge \star F_2 + m \int_{\text{WL}} dl + q \int_{\text{WL}} A_1.$$

The **electric WGC** requires the existence of a particle with

$$m < qM_{\text{P}}.$$

Magnetic Weak Gravity Conjecture

The **magnetic WGC** requires the minimally charged magnetic monopole to not be a black hole.

This is equivalent to the statement

Schwarzschild radius < monopole radius.

If we associate a cutoff Λ with the monopole radius, this implies

$$\frac{\Lambda}{M_{\text{P}}} \lesssim g_{\text{e}}.$$

In a weakly coupled theory ($g_{\text{e}} < 1$) this implies an unexpected low cutoff!

Weak Gravity Conjecture for p -form theories

It is possible to generalize the WGC to theories with a p -form gauge potential in d space-time dimensions:

$$S = \frac{1}{2g_e^2} \int F_{p+1} \wedge \star F_{p+1} + m \int_{\text{WS}} dV + q \int_{\text{WS}} A_p.$$

The gauge potential A_p couples to a $(p-1)$ -brane, which has a p -dimensional worldsheet (WS).

The magnetic object equivalent to the monopole is a $(d-p-3)$ -brane.

According to the magnetic WGC this should not be a black brane:

$$\frac{\Lambda}{M_{\text{P}}} \lesssim \left(g_e M_{\text{P}}^{d/2-p-1} \right)^{1/p}.$$

Magnetic Weak Gravity Conjecture for axions

For $p = 0$ the gauge potential A_0 is just a scalar and we obtain the action of an axion $\phi = A_0$ coupled to instantons.

By comparing with the kinetic term of an axion with decay constant f ,

$$\frac{1}{2g_e^2} d\phi \wedge \star d\phi = \frac{f^2}{2} d\phi \wedge \star d\phi,$$

we can identify $g_e = 1/f$.

With this the WGC bound in 4 space-time dimensions reads

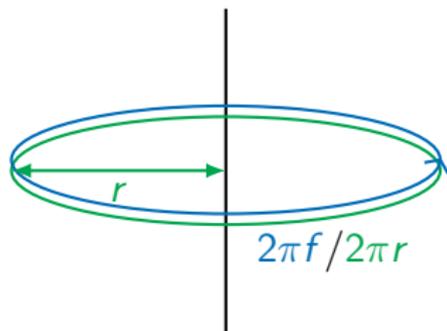
$$\frac{\Lambda}{M_{\text{P}}} \lesssim \lim_{p \rightarrow 0} \left(\frac{M_{\text{P}}}{f} \right)^{1/p},$$

which is zero for $f > M_{\text{P}}$.

Axionic strings

The naive interpretation of a vanishing cutoff is that the theory with $f > M_{\text{P}}$ is forbidden.

We want to check this naive conclusion by analyzing the object dual to instantons: An axionic string.



The **axion winds** around the string with **periodicity $2\pi f$** .

Hence, the (gradient) **energy density** is $\sim f^2/r^2$.

The **tension** of such a string **diverges logarithmically** (in flat space).

Axionic strings and gravitational backreaction

The **static spacetime** of an axionic string has a **physical singularity** in the center of the string and at a finite distance from the string!

[Cohen, Kaplan; 1988]

One can get rid of these singularities by having a non-static spacetime. [Gregory; 1996 / Gregory, Santos; 2003]

This spacetime expands in the direction of the string but, however, this solution fails to be valid for $f \gtrsim M_{\text{P}}$.

For $f \gtrsim M_{\text{P}}$ the spacetime becomes **highly non-static** and expands in all directions. This is known as **topological inflation** and provides a (unconventional) UV-completion of the string.

[Linde; 1994 / Vilenkin; 1994]

Recent numerical work on this was done in [Dolan, Draper, Kozaczuk, Patel; 2017].

Interpretation of results

Now we have an **interpretation problem**. Although we have not found any black string solutions, we had to allow for non-static spacetimes in order to get a proper string solution (Note that this is true even for $f < M_{\text{P}}$!). We are therefore essentially left with two options:

- 1) **We do not accept a non-static object** as a proper magnetic string required by the WGC. In this case $f \gtrsim M_{\text{P}}$ is forbidden.
- 2) **We do accept topological inflation** as a proper magnetic string and hence, $f \gtrsim M_{\text{P}}$ is allowed.

The meaning and relevance of non-static magnetic objects remains unclear...