## $\mathrm{E}_{6}\text{-extended}$ SUSY trinification

#### Jonas Wessén<sup>1</sup>

J. E. Camargo-Molina<sup>1</sup> A. P. Morais<sup>1,2</sup> A. Ordell<sup>1</sup> R. Pasechnik<sup>1</sup>

<sup>1</sup>Dept. of Astronomy and Theoretical Physics Lund University, Lund, Sweden

<sup>2</sup>Center for Research and Development in Mathematics and Applications (CIDMA) Aveiro University, Aveiro, Portugal



July 7, 2016



- Postulate a supersymmetric (SUSY) grand unified theory GUT valid at high energy scales
- $\bullet~$  Large degree of symmetry  $\Rightarrow~$  Very few parameters
- Study to what degree the Standard Model (SM) can emerge in the low energy limit
- Hope to explain seemingly arbitrary features of the SM such as the number of families, fermion mass hierarchies, the almost Cabibbo form of the CKM matrix etc.
- The model was recently introduced in Camargo-Molina, J.E., Morais, A.P., Ordell, A., Pasechnik, R., Sampaio, M., JW, Phys. Rev. D 95, 075031
- We are currently finalizing a more detailed paper that will soon appear on arXiv
- See also Camargo-Molina, J.E., Morais, A.P., Pasechnik, R., JW. J. High Energ. Phys. (2016) 2016: 129. for a non-SUSY version of the model

- Postulate a supersymmetric (SUSY) grand unified theory GUT valid at high energy scales
- Large degree of symmetry  $\Rightarrow$  Very few parameters
- Study to what degree the Standard Model (SM) can emerge in the low energy limit
- Hope to explain seemingly arbitrary features of the SM such as the number of families, fermion mass hierarchies, the almost Cabibbo form of the CKM matrix etc.
- The model was recently introduced in Camargo-Molina, J.E., Morais, A.P., Ordell, A., Pasechnik, R., Sampaio, M., JW, Phys. Rev. D 95, 075031
- We are currently finalizing a more detailed paper that will soon appear on arXiv
- See also Camargo-Molina, J.E., Morais, A.P., Pasechnik, R., JW. J. High Energ. Phys. (2016) 2016: 129. for a non-SUSY version of the model

- Postulate a supersymmetric (SUSY) grand unified theory GUT valid at high energy scales
- Large degree of symmetry  $\Rightarrow$  Very few parameters
- Study to what degree the Standard Model (SM) can emerge in the low energy limit
- Hope to explain seemingly arbitrary features of the SM such as the number of families, fermion mass hierarchies, the almost Cabibbo form of the CKM matrix etc.
- The model was recently introduced in Camargo-Molina, J.E., Morais, A.P., Ordell, A., Pasechnik, R., Sampaio, M., JW, Phys. Rev. D 95, 075031
- We are currently finalizing a more detailed paper that will soon appear on arXiv
- See also Camargo-Molina, J.E., Morais, A.P., Pasechnik, R., JW. J. High Energ. Phys. (2016) 2016: 129. for a non-SUSY version of the model

- Postulate a supersymmetric (SUSY) grand unified theory GUT valid at high energy scales
- Large degree of symmetry  $\Rightarrow$  Very few parameters
- Study to what degree the Standard Model (SM) can emerge in the low energy limit
- Hope to explain seemingly arbitrary features of the SM such as the number of families, fermion mass hierarchies, the almost Cabibbo form of the CKM matrix etc.
- The model was recently introduced in Camargo-Molina, J.E., Morais, A.P., Ordell, A., Pasechnik, R., Sampaio, M., JW, Phys. Rev. D 95, 075031
- We are currently finalizing a more detailed paper that will soon appear on arXiv
- See also Camargo-Molina, J.E., Morais, A.P., Pasechnik, R., JW. J. High Energ. Phys. (2016) 2016: 129. for a non-SUSY version of the model

- Postulate a supersymmetric (SUSY) grand unified theory GUT valid at high energy scales
- Large degree of symmetry  $\Rightarrow$  Very few parameters
- Study to what degree the Standard Model (SM) can emerge in the low energy limit
- Hope to explain seemingly arbitrary features of the SM such as the number of families, fermion mass hierarchies, the almost Cabibbo form of the CKM matrix etc.
- The model was recently introduced in Camargo-Molina, J.E., Morais, A.P., Ordell, A., Pasechnik, R., Sampaio, M., JW, Phys. Rev. D 95, 075031
- We are currently finalizing a more detailed paper that will soon appear on arXiv
- See also Camargo-Molina, J.E., Morais, A.P., Pasechnik, R., JW. J. High Energ. Phys. (2016) 2016: 129. for a non-SUSY version of the model

- Postulate a supersymmetric (SUSY) grand unified theory GUT valid at high energy scales
- Large degree of symmetry  $\Rightarrow$  Very few parameters
- Study to what degree the Standard Model (SM) can emerge in the low energy limit
- Hope to explain seemingly arbitrary features of the SM such as the number of families, fermion mass hierarchies, the almost Cabibbo form of the CKM matrix etc.
- The model was recently introduced in Camargo-Molina, J.E., Morais, A.P., Ordell, A., Pasechnik, R., Sampaio, M., JW, Phys. Rev. D 95, 075031
- We are currently finalizing a more detailed paper that will soon appear on arXiv
- See also Camargo-Molina, J.E., Morais, A.P., Pasechnik, R., JW. J. High Energ. Phys. (2016) 2016: 129. for a non-SUSY version of the model

- Postulate a supersymmetric (SUSY) grand unified theory GUT valid at high energy scales
- Large degree of symmetry  $\Rightarrow$  Very few parameters
- Study to what degree the Standard Model (SM) can emerge in the low energy limit
- Hope to explain seemingly arbitrary features of the SM such as the number of families, fermion mass hierarchies, the almost Cabibbo form of the CKM matrix etc.
- The model was recently introduced in Camargo-Molina, J.E., Morais, A.P., Ordell, A., Pasechnik, R., Sampaio, M., JW, Phys. Rev. D 95, 075031
- We are currently finalizing a more detailed paper that will soon appear on arXiv
- See also Camargo-Molina, J.E., Morais, A.P., Pasechnik, R., JW. J. High Energ. Phys. (2016) 2016: 129. for a non-SUSY version of the model

$$\begin{split} [\mathrm{SU}(3)_\mathrm{L} \times \mathrm{SU}(3)_\mathrm{R} \times \mathrm{SU}(3)_\mathrm{C}] \rtimes \mathbb{Z}_3^{(\mathrm{LRC})} \\ \downarrow \\ \mathrm{SU}(3)_\mathrm{C} \times \mathrm{SU}(2)_\mathrm{L} \times \mathrm{SU}(2)_\mathrm{R} \times \mathrm{U}(1)_{\mathrm{L+R}} \\ \downarrow \\ \mathrm{SU}(3)_\mathrm{C} \times \mathrm{SU}(2)_\mathrm{L} \times \mathrm{U}(1)_\mathrm{Y} \end{split}$$

- Subgroup of  $\mathrm{E}_6 \supset [\mathrm{SU}(3)]^3$
- SM fields sit in chiral superfields that are bi-fundamental representations of the gauge group: L  $\sim$  (3, 3, 1), Q<sub>L</sub>  $\sim$  (3, 1, 3), and Q<sub>R</sub>  $\sim$  (1, 3, 3):

$$\begin{pmatrix} \boldsymbol{\mathsf{L}}^i \end{pmatrix}_r^i = \begin{pmatrix} \boldsymbol{\mathsf{H}}_{11} & \boldsymbol{\mathsf{H}}_{12} & \boldsymbol{\nu}_{\mathrm{L}} \\ \boldsymbol{\mathsf{H}}_{21} & \boldsymbol{\mathsf{H}}_{22} & \boldsymbol{\mathsf{e}}_{\mathrm{L}} \\ \boldsymbol{\nu}_{\mathrm{R}}^c & \boldsymbol{\mathsf{e}}_{\mathrm{R}}^c & \boldsymbol{\varphi} \end{pmatrix}^i, \begin{pmatrix} \boldsymbol{\mathsf{Q}}_{\mathrm{L}}^i \end{pmatrix}_r^x = \begin{pmatrix} \boldsymbol{\mathsf{u}}_{\mathrm{L}}^x & \boldsymbol{\mathsf{d}}_{\mathrm{L}}^x & \boldsymbol{\mathsf{D}}_{\mathrm{L}}^x \end{pmatrix}^i, \\ \begin{pmatrix} \boldsymbol{\mathsf{Q}}_{\mathrm{R}}^i \end{pmatrix}_r^r = \begin{pmatrix} \boldsymbol{\mathsf{u}}_{\mathrm{R}}^x & \boldsymbol{\mathsf{d}}_{\mathrm{R}}^c & \boldsymbol{\mathsf{D}}_{\mathrm{R}}^c \end{pmatrix}^{\top i}, \end{cases}$$

 $\bullet$  Each family can be arranged into an  $\mathrm{E}_{6}$  27-plet:

$$\mathbf{27}^{i} = \left(\mathbf{3}, \mathbf{\bar{3}}, \mathbf{1}\right)^{i} \otimes \left(\mathbf{1}, \mathbf{3}, \mathbf{\bar{3}}\right)^{i} \otimes \left(\mathbf{\bar{3}}, \mathbf{1}, \mathbf{3}\right)^{i}$$

$$\begin{split} [\mathrm{SU}(3)_\mathrm{L} \times \mathrm{SU}(3)_\mathrm{R} \times \mathrm{SU}(3)_\mathrm{C}] \rtimes \mathbb{Z}_3^{(\mathrm{LRC})} \\ \downarrow \\ \mathrm{SU}(3)_\mathrm{C} \times \mathrm{SU}(2)_\mathrm{L} \times \mathrm{SU}(2)_\mathrm{R} \times \mathrm{U}(1)_{\mathrm{L+R}} \\ \downarrow \\ \mathrm{SU}(3)_\mathrm{C} \times \mathrm{SU}(2)_\mathrm{L} \times \mathrm{U}(1)_\mathrm{Y} \end{split}$$

- $\bullet~\mbox{Subgroup}$  of  ${\rm E}_6 \supset [{\rm SU}(3)]^3$
- SM fields sit in chiral superfields that are bi-fundamental representations of the gauge group: L  $\sim$  (3, 3, 1), Q<sub>L</sub>  $\sim$  (3, 1, 3), and Q<sub>R</sub>  $\sim$  (1, 3, 3):

$$\begin{pmatrix} \boldsymbol{\mathsf{L}}^i \end{pmatrix}_r^i = \begin{pmatrix} \boldsymbol{\mathsf{H}}_{11} & \boldsymbol{\mathsf{H}}_{12} & \boldsymbol{\nu}_{\mathrm{L}} \\ \boldsymbol{\mathsf{H}}_{21} & \boldsymbol{\mathsf{H}}_{22} & \boldsymbol{\mathsf{e}}_{\mathrm{L}} \\ \boldsymbol{\nu}_{\mathrm{R}}^c & \boldsymbol{\mathsf{e}}_{\mathrm{R}}^c & \boldsymbol{\varphi} \end{pmatrix}^i, \begin{pmatrix} \boldsymbol{\mathsf{Q}}_{\mathrm{L}}^i \end{pmatrix}_r^x = \begin{pmatrix} \boldsymbol{\mathsf{u}}_{\mathrm{L}}^x & \boldsymbol{\mathsf{d}}_{\mathrm{L}}^x & \boldsymbol{\mathsf{D}}_{\mathrm{L}}^x \end{pmatrix}^i, \\ \begin{pmatrix} \boldsymbol{\mathsf{Q}}_{\mathrm{R}}^i \end{pmatrix}_r^r = \begin{pmatrix} \boldsymbol{\mathsf{u}}_{\mathrm{R}}^x & \boldsymbol{\mathsf{d}}_{\mathrm{R}}^c & \boldsymbol{\mathsf{D}}_{\mathrm{R}}^c \end{pmatrix}^{\top i}, \end{cases}$$

 $\bullet$  Each family can be arranged into an  $\mathrm{E}_{6}$  27-plet:

$$\mathbf{27}^{i}=\left(\mathbf{3},\mathbf{ar{3}},\mathbf{1}
ight)^{i}\otimes\left(\mathbf{1},\mathbf{3},\mathbf{ar{3}}
ight)^{i}\otimes\left(\mathbf{ar{3}},\mathbf{1},\mathbf{3}
ight)^{i}$$

$$\begin{split} [\mathrm{SU}(3)_\mathrm{L} \times \mathrm{SU}(3)_\mathrm{R} \times \mathrm{SU}(3)_\mathrm{C}] \rtimes \mathbb{Z}_3^{(\mathrm{LRC})} \\ \downarrow \\ \mathrm{SU}(3)_\mathrm{C} \times \mathrm{SU}(2)_\mathrm{L} \times \mathrm{SU}(2)_\mathrm{R} \times \mathrm{U}(1)_{\mathrm{L+R}} \\ \downarrow \\ \mathrm{SU}(3)_\mathrm{C} \times \mathrm{SU}(2)_\mathrm{L} \times \mathrm{U}(1)_\mathrm{Y} \end{split}$$

- $\bullet \ \mbox{Subgroup of } {\rm E}_6 \supset \left[ {\rm SU}(3) \right]^3$
- SM fields sit in chiral superfields that are bi-fundamental representations of the gauge group: L  $\sim$  (3, 3, 1), Q<sub>L</sub>  $\sim$  (3, 1, 3), and Q<sub>R</sub>  $\sim$  (1, 3, 3):

$$\begin{pmatrix} \mathbf{L}^{i} \end{pmatrix}_{r}^{\prime} = \begin{pmatrix} \mathbf{H}_{11} & \mathbf{H}_{12} & \nu_{\mathrm{L}} \\ \mathbf{H}_{21} & \mathbf{H}_{22} & \mathbf{e}_{\mathrm{L}} \\ \nu_{\mathrm{R}}^{c} & \mathbf{e}_{\mathrm{R}}^{c} & \phi \end{pmatrix}^{i}, \\ \begin{pmatrix} \mathbf{Q}_{\mathrm{L}}^{i} \end{pmatrix}_{r}^{\prime} = \begin{pmatrix} \mathbf{u}_{\mathrm{L}}^{x} & \mathbf{d}_{\mathrm{L}}^{x} & \mathbf{D}_{\mathrm{L}}^{x} \end{pmatrix}^{i}, \\ \begin{pmatrix} \mathbf{Q}_{\mathrm{R}}^{i} \end{pmatrix}_{r}^{\prime} = \begin{pmatrix} \mathbf{u}_{\mathrm{R}}^{c} & \mathbf{d}_{\mathrm{R}}^{c} & \mathbf{D}_{\mathrm{R}}^{c} \end{pmatrix}^{\top i},$$

 $\bullet$  Each family can be arranged into an  $\mathrm{E}_{6}$  27-plet:

$$\mathbf{27}^{i}=\left(\mathbf{3},\mathbf{ar{3}},\mathbf{1}
ight)^{i}\otimes\left(\mathbf{1},\mathbf{3},\mathbf{ar{3}}
ight)^{i}\otimes\left(\mathbf{ar{3}},\mathbf{1},\mathbf{3}
ight)^{i}$$

$$\begin{split} [\mathrm{SU}(3)_\mathrm{L} \times \mathrm{SU}(3)_\mathrm{R} \times \mathrm{SU}(3)_\mathrm{C}] \rtimes \mathbb{Z}_3^{(\mathrm{LRC})} \\ \downarrow \\ \mathrm{SU}(3)_\mathrm{C} \times \mathrm{SU}(2)_\mathrm{L} \times \mathrm{SU}(2)_\mathrm{R} \times \mathrm{U}(1)_{\mathrm{L+R}} \\ \downarrow \\ \mathrm{SU}(3)_\mathrm{C} \times \mathrm{SU}(2)_\mathrm{L} \times \mathrm{U}(1)_\mathrm{Y} \end{split}$$

- $\bullet \ \mbox{Subgroup of } {\rm E}_6 \supset \left[ {\rm SU}(3) \right]^3$
- SM fields sit in chiral superfields that are bi-fundamental representations of the gauge group: L  $\sim$  (3, 3, 1), Q<sub>L</sub>  $\sim$  (3, 1, 3), and Q<sub>R</sub>  $\sim$  (1, 3, 3):

$$\begin{pmatrix} \mathbf{L}^{i} \end{pmatrix}_{r}^{i} = \begin{pmatrix} \mathbf{H}_{11} & \mathbf{H}_{12} & \nu_{\mathrm{L}} \\ \mathbf{H}_{21} & \mathbf{H}_{22} & \mathbf{e}_{\mathrm{L}} \\ \nu_{\mathrm{R}}^{c} & \mathbf{e}_{\mathrm{R}}^{c} & \phi \end{pmatrix}^{i}, \begin{pmatrix} \left( \mathbf{Q}_{\mathrm{L}}^{i} \right)_{r}^{x} = \left( \mathbf{u}_{\mathrm{L}}^{x} & \mathbf{d}_{\mathrm{L}}^{x} & \mathbf{D}_{\mathrm{L}}^{x} \right)^{i}, \\ \left( \left( \mathbf{Q}_{\mathrm{R}}^{i} \right)_{r}^{r} = \left( \mathbf{u}_{\mathrm{R}x}^{c} & \mathbf{d}_{\mathrm{R}x}^{c} & \mathbf{D}_{\mathrm{R}x}^{c} \right)^{\top i},$$

• Each family can be arranged into an  $E_6$  27-plet:

$$\mathbf{27}^{i} = \left(\mathbf{3}, \mathbf{\bar{3}}, \mathbf{1}\right)^{i} \otimes \left(\mathbf{1}, \mathbf{3}, \mathbf{\bar{3}}\right)^{i} \otimes \left(\mathbf{\bar{3}}, \mathbf{1}, \mathbf{3}\right)^{i}$$

- The model can accomodate any quark and lepton masses and mixing angles (Sayre et al. 2006)
- Naturally light neutrinos via radiative see-saw with split-SUSY (Cauet et al. 2011)
- Gauge symmetry preserves baryon number  $\Rightarrow$  No gauge-mediated proton decay (Achiman and Stech, 1978) (Glashow and Kang 1984)
- Well motivated as low energy versions of  $E_8 \times E_8$  heterotic string theory (Gross et al. 1985),  $E_6$  orbifold (Braam et al. 2010) or N = 8 supergravity (Cremmer et al. 1979).

- The most general superpotential contains a large number of free parameters ⇒ Calculations become messy beyond tree-level!
- $\bullet$  We introduce global  ${\rm SU}(3)_{\rm F}$  symmetry
- With  $L^i,~Q^i_{\rm L}$  and  $Q^i_{\rm R}$  being  ${\rm SU}(3)_{\rm F}$  triplets, the superpotential becomes extraordinarily simple:

$$W_{27} = \lambda_{27} \epsilon_{ijk} \mathsf{L}^{i} \mathsf{Q}_{\mathrm{L}}^{j} \mathsf{Q}_{\mathrm{R}}^{k}$$

- Only two free parameters in total:  $\lambda_{27}$  and the unified gauge coupling  $g_{\rm U}$ .
- ${\rm SU}(3)_{\rm F}$  also fits neatly into an  ${\rm E}_8 \subset {\rm E}_6 \times {\rm SU}(3)_{\rm F}$  embedding.

- The most general superpotential contains a large number of free parameters ⇒ Calculations become messy beyond tree-level!
- $\bullet$  We introduce global  ${\rm SU}(3)_{\rm F}$  symmetry
- With  $L^i,~Q^i_{\rm L}$  and  $Q^i_{\rm R}$  being  ${\rm SU}(3)_{\rm F}$  triplets, the superpotential becomes extraordinarily simple:

$$W_{27} = \lambda_{27} \epsilon_{ijk} \mathsf{L}^{i} \mathsf{Q}_{\mathrm{L}}^{j} \mathsf{Q}_{\mathrm{R}}^{k}$$

- Only two free parameters in total:  $\lambda_{27}$  and the unified gauge coupling  $g_{\rm U}$ .
- ${\rm SU}(3)_{\rm F}$  also fits neatly into an  ${\rm E}_8 \subset {\rm E}_6 \times {\rm SU}(3)_{\rm F}$  embedding.

- The most general superpotential contains a large number of free parameters ⇒ Calculations become messy beyond tree-level!
- $\bullet$  We introduce global  ${\rm SU}(3)_{\rm F}$  symmetry
- With  $L^i$ ,  $Q_L^i$  and  $Q_R^i$  being  $SU(3)_F$  triplets, the superpotential becomes extraordinarily simple:

$$W_{27} = \lambda_{27} \epsilon_{ijk} \mathbf{L}^i \mathbf{Q}_{\mathrm{L}}^j \mathbf{Q}_{\mathrm{R}}^k$$

- Only two free parameters in total:  $\lambda_{27}$  and the unified gauge coupling  $g_{\rm U}$ .
- $SU(3)_F$  also fits neatly into an  $E_8 \subset E_6 \times SU(3)_F$  embedding.

- The most general superpotential contains a large number of free parameters ⇒ Calculations become messy beyond tree-level!
- $\bullet$  We introduce global  ${\rm SU}(3)_{\rm F}$  symmetry
- With  $L^i$ ,  $Q_L^i$  and  $Q_R^i$  being  $SU(3)_F$  triplets, the superpotential becomes extraordinarily simple:

$$W_{27} = \lambda_{27} \epsilon_{ijk} \mathbf{L}^i \mathbf{Q}_{\mathrm{L}}^j \mathbf{Q}_{\mathrm{R}}^k$$

- Only two free parameters in total:  $\lambda_{27}$  and the unified gauge coupling  $g_{\rm U}$ .
- ${\rm SU}(3)_{\rm F}$  also fits neatly into an  ${\rm E}_8 \subset {\rm E}_6 \times {\rm SU}(3)_{\rm F}$  embedding.

- The most general superpotential contains a large number of free parameters ⇒ Calculations become messy beyond tree-level!
- $\bullet$  We introduce global  ${\rm SU}(3)_{\rm F}$  symmetry
- With  $L^i$ ,  $Q_L^i$  and  $Q_R^i$  being  $SU(3)_F$  triplets, the superpotential becomes extraordinarily simple:

$$W_{27} = \lambda_{27} \epsilon_{ijk} \mathbf{L}^i \mathbf{Q}_{\mathrm{L}}^j \mathbf{Q}_{\mathrm{R}}^k$$

- Only two free parameters in total:  $\lambda_{27}$  and the unified gauge coupling  $g_{\mathrm{U}}$ .
- $SU(3)_F$  also fits neatly into an  $E_8 \subset E_6 \times SU(3)_F$  embedding.

$$W_{27} = \lambda_{27} \epsilon_{ijk} \mathsf{L}^i \mathsf{Q}^j_{\mathrm{L}} \mathsf{Q}^k_{\mathrm{R}}$$

- $U(1)_A \times U(1)_B$ , where  $U(1)_B$  gives a conserved baryon number.
- Left-Right parity! I.e. spatial inversion + swapping  ${\rm SU}(3)_{\rm L}\leftrightarrow {\rm SU}(3)_{\rm R}$  representations:

$$\begin{split} (t,\vec{x}) &\stackrel{\mathbb{P}}{\to} (t,-\vec{x}), \quad \theta^{\alpha} \stackrel{\mathbb{P}}{\to} -\mathrm{i}\theta^{\dagger}_{\dot{\alpha}} \\ (\mathsf{L}^{i})^{a}{}_{b} \stackrel{\mathbb{P}}{\to} -(\mathsf{L}^{*}_{i})^{a}{}_{b}, \quad (\mathbb{Q}^{i}_{\mathrm{L}})^{c}{}_{a} \stackrel{\mathbb{P}}{\leftrightarrow} (\mathbb{Q}^{*}_{\mathrm{R}i})^{c}{}_{a} \quad \text{(chiral superfields)} \\ & \mathsf{V}_{\mathrm{L,R,C}} \stackrel{\mathbb{P}}{\to} -\mathsf{V}_{\mathrm{R,L,C}} \quad \text{(vector superfields)} \end{split}$$

- $(\theta\theta \stackrel{\mathbb{P}}{\leftrightarrow} \theta^{\dagger}\theta^{\dagger}$  means that  $W \stackrel{\mathbb{P}}{\leftrightarrow} W^*$  for  $\theta^{\dagger}\theta^{\dagger}W + \theta\theta W^*$  to be parity invariant)
- Parity exists at the SU(3) level, contrary to common LR-symmetric constructions in which parity means  $SU(2)_L \stackrel{\mathbb{P}}{\leftrightarrow} SU(2)_R$
- $\bullet$  There are also Colour-Left and Right-Colour parity transformations (due to  $\mathbb{Z}_3^{(\mathrm{LRC})})$

$$W_{27} = \lambda_{27} \epsilon_{ijk} \mathbf{L}^i \mathbf{Q}_{\mathrm{L}}^j \mathbf{Q}_{\mathrm{R}}^k$$

- $U(1)_A \times U(1)_B$ , where  $U(1)_B$  gives a conserved baryon number.
- Left-Right parity! I.e. spatial inversion + swapping  ${\rm SU}(3)_{\rm L}\leftrightarrow {\rm SU}(3)_{\rm R}$  representations:

$$\begin{split} (t,\vec{x}) &\stackrel{\mathbb{P}}{\to} (t,-\vec{x}), \quad \theta^{\alpha} \stackrel{\mathbb{P}}{\to} -\mathrm{i}\theta^{\dagger}_{\dot{\alpha}} \\ (\mathsf{L}^{i})_{\ b}^{\ a} \stackrel{\mathbb{P}}{\to} -(\mathsf{L}^{*}_{i})_{b}^{\ a}, \quad (\mathsf{Q}^{i}_{\mathrm{L}})_{\ a}^{\ c} \stackrel{\mathbb{P}}{\to} (\mathsf{Q}^{*}_{\mathrm{R}i})_{a}^{\ c} \quad \text{(chiral superfields)} \\ \mathbf{V}_{\mathrm{L,R,C}} \stackrel{\mathbb{P}}{\to} -\mathbf{V}_{\mathrm{R,L,C}} \quad \text{(vector superfields)} \end{split}$$

- $(\theta\theta \stackrel{\mathbb{P}}{\leftrightarrow} \theta^{\dagger}\theta^{\dagger}$  means that  $W \stackrel{\mathbb{P}}{\leftrightarrow} W^*$  for  $\theta^{\dagger}\theta^{\dagger}W + \theta\theta W^*$  to be parity invariant)
- Parity exists at the SU(3) level, contrary to common LR-symmetric constructions in which parity means  $SU(2)_L \stackrel{\mathbb{P}}{\leftrightarrow} SU(2)_R$
- $\bullet$  There are also Colour-Left and Right-Colour parity transformations (due to  $\mathbb{Z}_3^{(\mathrm{LRC})})$

$$W_{27} = \lambda_{27} \epsilon_{ijk} \mathbf{L}^i \mathbf{Q}_{\mathrm{L}}^j \mathbf{Q}_{\mathrm{R}}^k$$

- $U(1)_A \times U(1)_B$ , where  $U(1)_B$  gives a conserved baryon number.
- Left-Right parity! I.e. spatial inversion + swapping  ${\rm SU}(3)_{\rm L}\leftrightarrow {\rm SU}(3)_{\rm R}$  representations:

$$\begin{split} (t,\vec{x}) &\stackrel{\mathbb{P}}{\to} (t,-\vec{x}), \quad \theta^{\alpha} \stackrel{\mathbb{P}}{\to} -\mathrm{i}\theta^{\dagger}_{\dot{\alpha}} \\ (\mathsf{L}^{i})^{\mathfrak{s}}_{b} \stackrel{\mathbb{P}}{\to} -(\mathsf{L}^{*}_{i})^{\mathfrak{s}}_{b}, \quad (\mathsf{Q}^{i}_{\mathrm{L}})^{\mathfrak{c}}_{a} \stackrel{\mathbb{P}}{\leftrightarrow} (\mathsf{Q}^{*}_{\mathrm{R}i})^{\mathfrak{c}}_{a} \quad \text{(chiral superfields)} \\ \mathbf{V}_{\mathrm{L,R,C}} \stackrel{\mathbb{P}}{\to} -\mathbf{V}_{\mathrm{R,L,C}} \quad \text{(vector superfields)} \end{split}$$

- $(\theta\theta \stackrel{\mathbb{P}}{\leftrightarrow} \theta^{\dagger}\theta^{\dagger}$  means that  $W \stackrel{\mathbb{P}}{\leftrightarrow} W^*$  for  $\theta^{\dagger}\theta^{\dagger}W + \theta\theta W^*$  to be parity invariant)
- Parity exists at the SU(3) level, contrary to common LR-symmetric constructions in which parity means  $SU(2)_L \stackrel{\mathbb{P}}{\leftrightarrow} SU(2)_R$
- $\bullet$  There are also Colour-Left and Right-Colour parity transformations (due to  $\mathbb{Z}_3^{(\mathrm{LRC})})$

$$W_{27} = \lambda_{27} \epsilon_{ijk} \mathbf{L}^i \mathbf{Q}_{\mathrm{L}}^j \mathbf{Q}_{\mathrm{R}}^k$$

- $U(1)_A \times U(1)_B$ , where  $U(1)_B$  gives a conserved baryon number.
- Left-Right parity! I.e. spatial inversion + swapping  ${\rm SU}(3)_{\rm L}\leftrightarrow {\rm SU}(3)_{\rm R}$  representations:

$$\begin{split} (t,\vec{x}) &\stackrel{\mathbb{P}}{\to} (t,-\vec{x}), \quad \theta^{\alpha} \stackrel{\mathbb{P}}{\to} -\mathrm{i}\theta^{\dagger}_{\dot{\alpha}} \\ (\mathsf{L}^{i})^{\mathfrak{s}}_{b} \stackrel{\mathbb{P}}{\to} -(\mathsf{L}^{*}_{i})^{\mathfrak{s}}_{b}, \quad (\mathsf{Q}^{i}_{\mathrm{L}})^{\mathfrak{c}}_{a} \stackrel{\mathbb{P}}{\leftrightarrow} (\mathsf{Q}^{*}_{\mathrm{R}i})^{\mathfrak{c}}_{a} \quad \text{(chiral superfields)} \\ \mathbf{V}_{\mathrm{L,R,C}} \stackrel{\mathbb{P}}{\to} -\mathbf{V}_{\mathrm{R,L,C}} \quad \text{(vector superfields)} \end{split}$$

- $(\theta\theta \stackrel{\mathbb{P}}{\leftrightarrow} \theta^{\dagger}\theta^{\dagger}$  means that  $W \stackrel{\mathbb{P}}{\leftrightarrow} W^*$  for  $\theta^{\dagger}\theta^{\dagger}W + \theta\theta W^*$  to be parity invariant)
- Parity exists at the SU(3) level, contrary to common LR-symmetric constructions in which parity means  $SU(2)_L \stackrel{\mathbb{P}}{\leftrightarrow} SU(2)_R$
- There are also Colour-Left and Right-Colour parity transformations (due to  $\mathbb{Z}_3^{(\mathrm{LRC})})$

$$W_{27} = \lambda_{27} \epsilon_{ijk} \mathbf{L}^i \mathbf{Q}_{\mathrm{L}}^j \mathbf{Q}_{\mathrm{R}}^k$$

- $U(1)_A \times U(1)_B$ , where  $U(1)_B$  gives a conserved baryon number.
- Left-Right parity! I.e. spatial inversion + swapping  ${\rm SU}(3)_{\rm L}\leftrightarrow {\rm SU}(3)_{\rm R}$  representations:

$$\begin{split} (t,\vec{x}) &\stackrel{\mathbb{P}}{\to} (t,-\vec{x}), \quad \theta^{\alpha} \stackrel{\mathbb{P}}{\to} -\mathrm{i}\theta^{\dagger}_{\dot{\alpha}} \\ (\mathsf{L}^{i})^{\mathfrak{s}}_{b} \stackrel{\mathbb{P}}{\to} -(\mathsf{L}^{*}_{i})^{\mathfrak{s}}_{b}, \quad (\mathsf{Q}^{i}_{\mathrm{L}})^{\mathfrak{c}}_{a} \stackrel{\mathbb{P}}{\leftrightarrow} (\mathsf{Q}^{*}_{\mathrm{R}i})^{\mathfrak{c}}_{a} \quad \text{(chiral superfields)} \\ \mathbf{V}_{\mathrm{L,R,C}} \stackrel{\mathbb{P}}{\to} -\mathbf{V}_{\mathrm{R,L,C}} \quad \text{(vector superfields)} \end{split}$$

- $(\theta\theta \stackrel{\mathbb{P}}{\leftrightarrow} \theta^{\dagger}\theta^{\dagger}$  means that  $W \stackrel{\mathbb{P}}{\leftrightarrow} W^*$  for  $\theta^{\dagger}\theta^{\dagger}W + \theta\theta W^*$  to be parity invariant)
- Parity exists at the SU(3) level, contrary to common LR-symmetric constructions in which parity means  $SU(2)_L \stackrel{\mathbb{P}}{\leftrightarrow} SU(2)_R$
- $\bullet$  There are also Colour-Left and Right-Colour parity transformations (due to  $\mathbb{Z}_3^{(\mathrm{LRC})})$

- This is all nice... but does it look anything like the SM at lower energies? No!
- W has SU(3)<sub>C</sub> breaking flat directions, and no  $[SU(3)]^3 \rightarrow SU(3)_C \times SU(2)_L \times SU(2)_R \times U(1)_{L+R}$  VEV in  $\tilde{L}$  is possible.
- Our solution: Add gauge adjoint chiral superfields  $\Delta_{\rm L,R,C}$  (transforming as the 8 under  $\rm SU(3)_{L,R,C}$  respectively)
- Does not complicate the superpotential much that now has a minimum where  $\langle \tilde{\Delta}^8_{\rm L} \rangle = \langle \tilde{\Delta}^8_{\rm R} \rangle \neq 0.$
- $\bullet~Breaks~{\rm SU}(3)_{\rm L,R}\to {\rm SU}(2)_{\rm L,R}\times {\rm U}(1)_{\rm L,R}$  but leaves both SUSY and parity unbroken
- See our paper for more on this!

- This is all nice... but does it look anything like the SM at lower energies? No!
- W has  $\mathrm{SU}(3)_{\mathrm{C}}$  breaking flat directions, and no  $[\mathrm{SU}(3)]^3 \to \mathrm{SU}(3)_{\mathrm{C}} \times \mathrm{SU}(2)_{\mathrm{L}} \times \mathrm{SU}(2)_{\mathrm{R}} \times \mathrm{U}(1)_{\mathrm{L+R}}$  VEV in  $\tilde{\mathcal{L}}$  is possible.
- Our solution: Add gauge adjoint chiral superfields  $\Delta_{\rm L,R,C}$  (transforming as the 8 under  $\rm SU(3)_{L,R,C}$  respectively)
- Does not complicate the superpotential much that now has a minimum where  $\langle \tilde{\Delta}^8_{\rm L} \rangle = \langle \tilde{\Delta}^8_{\rm R} \rangle \neq 0.$
- $\bullet~Breaks~{\rm SU}(3)_{\rm L,R}\to {\rm SU}(2)_{\rm L,R}\times {\rm U}(1)_{\rm L,R}$  but leaves both SUSY and parity unbroken
- See our paper for more on this!

- This is all nice... but does it look anything like the SM at lower energies? No!
- W has  $\mathrm{SU}(3)_{\mathrm{C}}$  breaking flat directions, and no  $[\mathrm{SU}(3)]^3 \to \mathrm{SU}(3)_{\mathrm{C}} \times \mathrm{SU}(2)_{\mathrm{L}} \times \mathrm{SU}(2)_{\mathrm{R}} \times \mathrm{U}(1)_{\mathrm{L+R}}$  VEV in  $\tilde{\mathcal{L}}$  is possible.
- Our solution: Add gauge adjoint chiral superfields  $\Delta_{\rm L,R,C}$  (transforming as the 8 under  $\rm SU(3)_{L,R,C}$  respectively)
- Does not complicate the superpotential much that now has a minimum where  $\langle \tilde{\Delta}^8_{\rm L} \rangle = \langle \tilde{\Delta}^8_{\rm R} \rangle \neq 0.$
- $\bullet$  Breaks  ${\rm SU}(3)_{\rm L,R}\to {\rm SU}(2)_{\rm L,R}\times {\rm U}(1)_{\rm L,R}$  but leaves both SUSY and parity unbroken
- See our paper for more on this!

- This is all nice... but does it look anything like the SM at lower energies? No!
- W has  $\mathrm{SU}(3)_{\mathrm{C}}$  breaking flat directions, and no  $[\mathrm{SU}(3)]^3 \to \mathrm{SU}(3)_{\mathrm{C}} \times \mathrm{SU}(2)_{\mathrm{L}} \times \mathrm{SU}(2)_{\mathrm{R}} \times \mathrm{U}(1)_{\mathrm{L+R}}$  VEV in  $\tilde{\mathcal{L}}$  is possible.
- Our solution: Add gauge adjoint chiral superfields  $\Delta_{\rm L,R,C}$  (transforming as the 8 under  $\rm SU(3)_{L,R,C}$  respectively)
- Does not complicate the superpotential much that now has a minimum where  $\langle \tilde{\Delta}^8_{\rm L} \rangle = \langle \tilde{\Delta}^8_{\rm R} \rangle \neq 0.$
- $\bullet$  Breaks  ${\rm SU}(3)_{\rm L,R}\to {\rm SU}(2)_{\rm L,R}\times {\rm U}(1)_{\rm L,R}$  but leaves both SUSY and parity unbroken
- See our paper for more on this!

- This is all nice... but does it look anything like the SM at lower energies? No!
- W has  $\mathrm{SU}(3)_{\mathrm{C}}$  breaking flat directions, and no  $[\mathrm{SU}(3)]^3 \to \mathrm{SU}(3)_{\mathrm{C}} \times \mathrm{SU}(2)_{\mathrm{L}} \times \mathrm{SU}(2)_{\mathrm{R}} \times \mathrm{U}(1)_{\mathrm{L+R}}$  VEV in  $\tilde{\mathcal{L}}$  is possible.
- Our solution: Add gauge adjoint chiral superfields  $\Delta_{\rm L,R,C}$  (transforming as the 8 under  $\rm SU(3)_{L,R,C}$  respectively)
- Does not complicate the superpotential much that now has a minimum where  $\langle \tilde{\Delta}_{\rm L}^8 \rangle = \langle \tilde{\Delta}_{\rm R}^8 \rangle \neq 0.$
- Breaks  ${\rm SU}(3)_{\rm L,R}\to {\rm SU}(2)_{\rm L,R}\times {\rm U}(1)_{\rm L,R}$  but leaves both SUSY and parity unbroken
- See our paper for more on this!

- This is all nice... but does it look anything like the SM at lower energies? No!
- W has  $\mathrm{SU}(3)_{\mathrm{C}}$  breaking flat directions, and no  $[\mathrm{SU}(3)]^3 \to \mathrm{SU}(3)_{\mathrm{C}} \times \mathrm{SU}(2)_{\mathrm{L}} \times \mathrm{SU}(2)_{\mathrm{R}} \times \mathrm{U}(1)_{\mathrm{L+R}}$  VEV in  $\tilde{\mathcal{L}}$  is possible.
- Our solution: Add gauge adjoint chiral superfields  $\Delta_{\rm L,R,C}$  (transforming as the 8 under  $\rm SU(3)_{L,R,C}$  respectively)
- Does not complicate the superpotential much that now has a minimum where  $\langle \tilde{\Delta}_{\rm L}^8 \rangle = \langle \tilde{\Delta}_{\rm R}^8 \rangle \neq 0.$
- Breaks  ${\rm SU}(3)_{\rm L,R}\to {\rm SU}(2)_{\rm L,R}\times {\rm U}(1)_{\rm L,R}$  but leaves both SUSY and parity unbroken
- See our paper for more on this!

# 

• All components of  $\pmb{\Delta}_{\rm L,R,C}$  receive  $\mathcal{O}({\sf GUT} \text{ scale})$  masses and are integrated out.

#### • We can break SUSY softly by adding soft SUSY breaking (SSB) terms

- The SSB terms induce VEVs  $\langle (\tilde{L}^3)^3_3 \rangle \equiv \langle \tilde{\phi}^3 \rangle$  and  $\langle (\tilde{L}^i)^3_1 \rangle \equiv \langle \tilde{\nu}_{\rm R}^{\rm c \ i} \rangle$  that further breaks the symmetry (including parity).
- $\bullet\,$  These VEVs are protected by SUSY from  $\mathcal{O}({\rm GUT\,\, scale})$  radiative corrections

- We can break SUSY softly by adding soft SUSY breaking (SSB) terms
- The SSB terms induce VEVs  $\langle (\tilde{L}^3)^3_3 \rangle \equiv \langle \tilde{\phi}^3 \rangle$  and  $\langle (\tilde{L}^i)^3_1 \rangle \equiv \langle \tilde{\nu}_{\rm R}^{\rm c \ i} \rangle$  that further breaks the symmetry (including parity).
- These VEVs are protected by SUSY from  $\mathcal{O}(\text{GUT scale})$  radiative corrections

- We can break SUSY softly by adding soft SUSY breaking (SSB) terms
- The SSB terms induce VEVs  $\langle (\tilde{L}^3)^3_3 \rangle \equiv \langle \tilde{\phi}^3 \rangle$  and  $\langle (\tilde{L}^i)^3_1 \rangle \equiv \langle \tilde{\nu}_{\rm R}^{\rm c \ i} \rangle$  that further breaks the symmetry (including parity).
- $\bullet\,$  These VEVs are protected by SUSY from  $\mathcal{O}({\rm GUT\,\, scale})$  radiative corrections

#### Gauge Global

$$\begin{split} [\mathrm{SU}(3)_{\mathrm{L}} \times \mathrm{SU}(3)_{\mathrm{R}} \times \mathrm{SU}(3)_{\mathrm{C}}] \rtimes \mathbb{Z}_{3} \times \{ \mathrm{SU}(3)_{\mathrm{F}} \times \mathrm{U}(1)_{\mathrm{A}} \times \mathrm{U}(1)_{\mathrm{B}} \} \\ \downarrow \quad \langle \tilde{\Delta}_{\mathrm{L,R}}^{8} \rangle, \mbox{ GUT scale} \\ \mathrm{SU}(3)_{\mathrm{C}} \times \mathrm{SU}(2)_{\mathrm{L}} \times \mathrm{SU}(2)_{\mathrm{R}} \times \mathrm{U}(1)_{\mathrm{L}} \times \mathrm{U}(1)_{\mathrm{R}} \times \{ \mathrm{SU}(3)_{\mathrm{F}} \times \mathrm{U}(1)_{\mathrm{A}} \times \mathrm{U}(1)_{\mathrm{B}} \} \\ \downarrow \quad \langle \tilde{\phi}^{3} \rangle, \mbox{ SSB scale} \\ \mathrm{SU}(3)_{\mathrm{C}} \times \mathrm{SU}(2)_{\mathrm{L}} \times \mathrm{SU}(2)_{\mathrm{R}} \times \mathrm{U}(1)_{\mathrm{L+R}} \times \{ \mathrm{SU}(2)_{\mathrm{F}} \times \mathrm{U}(1)_{\mathrm{X}} \times \mathrm{U}(1)_{\mathrm{Z}} \times \mathrm{U}(1)_{\mathrm{B}} \} \\ \downarrow \quad \langle \tilde{\nu}_{\mathrm{R}}^{c\,i} \rangle, \mbox{ SSB scale (tree-level / radiative?)} \\ \mathrm{SU}(3)_{\mathrm{C}} \times \mathrm{SU}(2)_{\mathrm{L}} \times \mathrm{U}(1)_{\mathrm{Y}} \times \{ (?) \times \mathrm{U}(1)_{\mathrm{B}} \} \\ \downarrow \quad (\mathrm{radiative?}) \\ \mathrm{SU}(3)_{\mathrm{C}} \times \mathrm{U}(1)_{\mathrm{E,M}} \times \{ (?) \times \mathrm{U}(1)_{\mathrm{B}} \} \end{split}$$

All symmetry breaking scales (including the elecro-weak) except  $v_{GUT}$  are controlled by SSB parameters  $\Rightarrow$  No  $\mu$ -problem!

#### $\bullet$ SUSY trinification GUT with global ${\rm SU}(3)_{\rm F}$ family symmetry.

- Few free parameters, full unification of Yukawa couplings in the fundamental sector
- Also enjoys baryon number conservation and symmetry under parity at the SU(3) level.
- $\bullet\,$  Gauge adjoints  $\Delta_{\rm L,R,C}$  are needed to initiate the first symmetry breaking
- $\bullet$  All other scales are controlled by SSB parameters  $\Rightarrow$  naturally a hierarchy between the electro-weak scale and the GUT scale
- Future work: Run the parameters of the effective Left-Right symmetric theory towards lower energies using the renormalization group, to see if radiative symmetry breaking occur (i.e. if  $m_{\tilde{\nu}_{\rm R}}^2, m_{H_i}^2$  turn negative at lower energies)

- $\bullet$  SUSY trinification GUT with global  ${\rm SU}(3)_{\rm F}$  family symmetry.
- Few free parameters, full unification of Yukawa couplings in the fundamental sector
- Also enjoys baryon number conservation and symmetry under parity at the SU(3) level.
- $\bullet\,$  Gauge adjoints  $\Delta_{\rm L,R,C}$  are needed to initiate the first symmetry breaking
- $\bullet$  All other scales are controlled by SSB parameters  $\Rightarrow$  naturally a hierarchy between the electro-weak scale and the GUT scale
- Future work: Run the parameters of the effective Left-Right symmetric theory towards lower energies using the renormalization group, to see if radiative symmetry breaking occur (i.e. if  $m_{\tilde{\nu}_{\rm R}}^2, m_{H_i}^2$  turn negative at lower energies)

- SUSY trinification GUT with global  $\mathrm{SU}(3)_{\mathrm{F}}$  family symmetry.
- Few free parameters, full unification of Yukawa couplings in the fundamental sector
- Also enjoys baryon number conservation and symmetry under parity at the SU(3) level.
- $\bullet\,$  Gauge adjoints  $\Delta_{\rm L,R,C}$  are needed to initiate the first symmetry breaking
- $\bullet$  All other scales are controlled by SSB parameters  $\Rightarrow$  naturally a hierarchy between the electro-weak scale and the GUT scale
- Future work: Run the parameters of the effective Left-Right symmetric theory towards lower energies using the renormalization group, to see if radiative symmetry breaking occur (i.e. if  $m_{\tilde{\nu}_{\rm R}}^2, m_{H_i}^2$  turn negative at lower energies)

- SUSY trinification GUT with global  $SU(3)_F$  family symmetry.
- Few free parameters, full unification of Yukawa couplings in the fundamental sector
- Also enjoys baryon number conservation and symmetry under parity at the SU(3) level.
- $\bullet\,$  Gauge adjoints  $\pmb{\Delta}_{\rm L,R,C}$  are needed to initiate the first symmetry breaking
- $\bullet$  All other scales are controlled by SSB parameters  $\Rightarrow$  naturally a hierarchy between the electro-weak scale and the GUT scale
- Future work: Run the parameters of the effective Left-Right symmetric theory towards lower energies using the renormalization group, to see if radiative symmetry breaking occur (i.e. if  $m_{\tilde{\nu}_{\rm R}}^2, m_{H_i}^2$  turn negative at lower energies)

- SUSY trinification GUT with global  $SU(3)_F$  family symmetry.
- Few free parameters, full unification of Yukawa couplings in the fundamental sector
- Also enjoys baryon number conservation and symmetry under parity at the SU(3) level.
- $\bullet\,$  Gauge adjoints  $\pmb{\Delta}_{\rm L,R,C}$  are needed to initiate the first symmetry breaking
- All other scales are controlled by SSB parameters  $\Rightarrow$  naturally a hierarchy between the electro-weak scale and the GUT scale
- Future work: Run the parameters of the effective Left-Right symmetric theory towards lower energies using the renormalization group, to see if radiative symmetry breaking occur (i.e. if  $m_{\tilde{\nu}_{\rm R}}^2, m_{H_i}^2$  turn negative at lower energies)

- SUSY trinification GUT with global  $\mathrm{SU}(3)_{\mathrm{F}}$  family symmetry.
- Few free parameters, full unification of Yukawa couplings in the fundamental sector
- Also enjoys baryon number conservation and symmetry under parity at the SU(3) level.
- $\bullet\,$  Gauge adjoints  $\pmb{\Delta}_{\rm L,R,C}$  are needed to initiate the first symmetry breaking
- All other scales are controlled by SSB parameters  $\Rightarrow$  naturally a hierarchy between the electro-weak scale and the GUT scale
- Future work: Run the parameters of the effective Left-Right symmetric theory towards lower energies using the renormalization group, to see if radiative symmetry breaking occur (i.e. if  $m_{\tilde{\nu}_{\rm R}}^2, m_{H_i}^2$  turn negative at lower energies)

- SUSY trinification GUT with global  $SU(3)_F$  family symmetry.
- Few free parameters, full unification of Yukawa couplings in the fundamental sector
- Also enjoys baryon number conservation and symmetry under parity at the SU(3) level.
- $\bullet\,$  Gauge adjoints  $\Delta_{\rm L,R,C}$  are needed to initiate the first symmetry breaking
- $\bullet$  All other scales are controlled by SSB parameters  $\Rightarrow$  naturally a hierarchy between the electro-weak scale and the GUT scale
- Future work: Run the parameters of the effective Left-Right symmetric theory towards lower energies using the renormalization group, to see if radiative symmetry breaking occur (i.e. if  $m_{\tilde{\nu}_{\rm R}}^2, m_{H_i}^2$  turn negative at lower energies)

#### Thank you for your attention!