Large field inflation: Recent progress and observational predictions

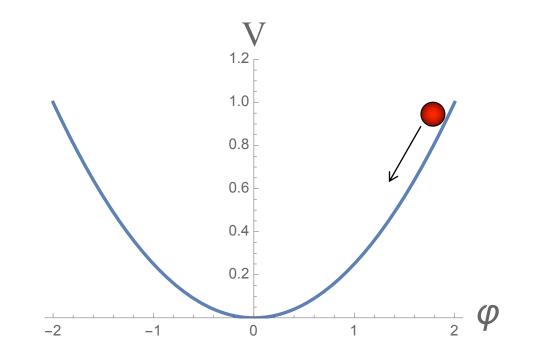
Andrei Linde

See also related talks by Kallosh, Yamada and Scalisi

Madrid, PASCOS2017

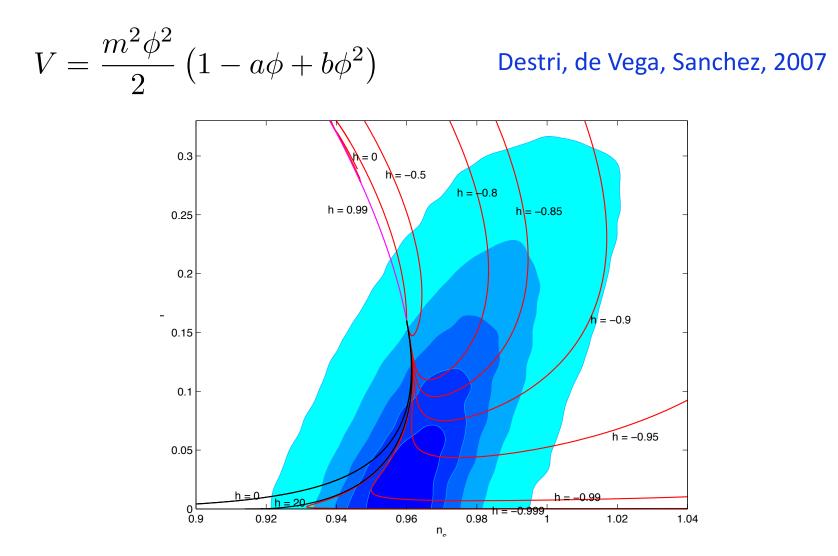
Simplest inflationary model: $V = \frac{m^2}{2}$

Inflation can start at the Planck density if there is a single Planck size domain with a potential energy V of the same order as kinetic and gradient density. This is the minimal requirement, compared to standard Big Bang, where initial homogeneity is requires across 10⁹⁰ Planck size domains.



Polynomial inflation:

Simplest quadratic model predicts too large amount of the gravitational waves. However, it can be trivially generalized to avoid this problem, while still offering the possibility of inflation beginning at the Planck density



One can fit all Planck data by a polynomial, with inflation starting at the Planck density

$$V = \frac{m^2 \phi^2}{2} \left(1 - a\phi + b\phi^2 \right)$$

3 observables: A_s, n_s, r

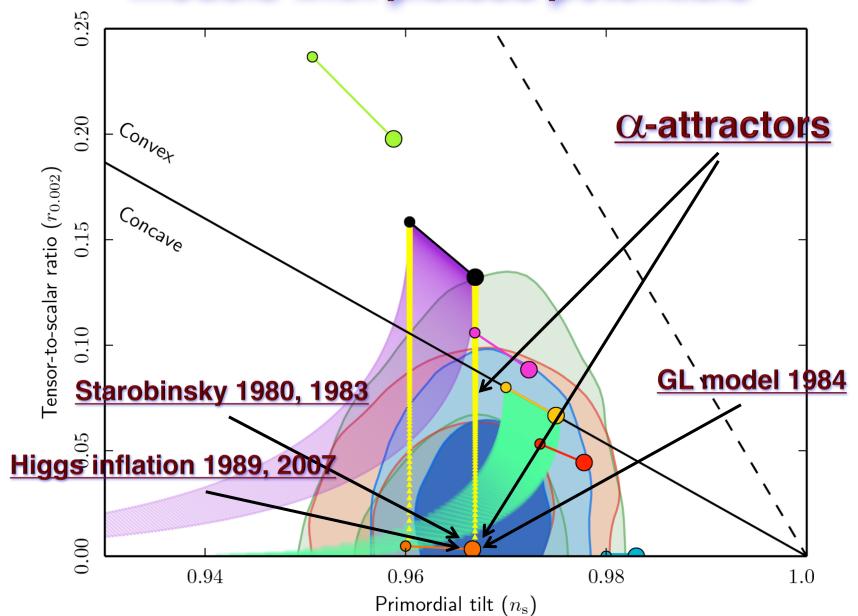
3 parameters: m, a, b

Example: m =10⁻⁵, a = 0.12, b=0.29

Destri, de Vega, Sanchez, 2007 Nakayama, Takahashi and Yanagida, 2013 Kallosh, AL, Westphal 2014 Kallosh, AL, Roest, Yamada <u>1705.09247</u>

But the best fit is provided by models with plateau potentials

The most natural fit is provided by models with plateau potentials



What is the meaning of α -attractors?

Kallosh, AL 2013; Ferrara, Kallosh, AL, Porrati, 2013; Kallosh, AL, Roest 2013; Galante, Kallosh, AL, Roest 2014

Start with the simplest chaotic inflation model

$$\frac{1}{\sqrt{-g}}\mathcal{L} = \frac{1}{2}R - \frac{1}{2}\partial\phi^2 - \frac{1}{2}m^2\phi^2$$

Modify its kinetic term

$$\frac{1}{\sqrt{-g}}\mathcal{L} = \frac{1}{2}R - \frac{1}{2}\frac{\partial\phi^2}{(1 - \frac{\phi^2}{6\alpha})^2} - \frac{1}{2}m^2\phi^2$$

Switch to canonical variables $\phi = \sqrt{6\alpha} \tanh \frac{\varphi}{\sqrt{6\alpha}}$

The potential becomes

$$V = 3\alpha \, m^2 \tanh^2 \frac{\varphi}{\sqrt{6\alpha}}$$

General chaotic inflation model

$$\frac{1}{\sqrt{-g}}\mathcal{L} = \frac{1}{2}R - \frac{1}{2}\partial\phi^2 - V(\phi)$$

Modify its kinetic term

$$\frac{1}{\sqrt{-g}}\mathcal{L} = \frac{1}{2}R - \frac{1}{2}\frac{\partial\phi^2}{(1 - \frac{\phi^2}{6\alpha})^2} - V(\phi)$$

Switch to canonical variables $\phi = \sqrt{6\alpha} \tanh \frac{\varphi}{\sqrt{6\alpha}}$

The potential becomes

$$V = V(\tanh\frac{\varphi}{\sqrt{6\alpha}})$$

This is a **plateau potential** for any nonsingular $V(\phi)$

The essence of α -attractors

Galante, Kallosh, AL, Roest 1412.3797

$$\frac{1}{2}R - \frac{3}{4}\alpha \left(\frac{\partial t}{t}\right)^2 - V(t)$$

Suppose inflation takes place near the pole at t = 0, and V(0) > 0, V'(0) > 0, and V has a minimum nearby. Then in canonical variables

$$\frac{1}{2}R - \frac{1}{2}(\partial\varphi)^2 - V_0(1 - e^{-\sqrt{\frac{2}{3\alpha}}\varphi} + ...)$$

Then in the leading approximation in 1/N, for any non-singular V

$$n_s = 1 - \frac{2}{N}, \qquad r = \alpha \frac{12}{N^2}$$

The essence of α -attractors

Galante, Kallosh, AL, Roest 1412.3797

THE BASIC RULE:

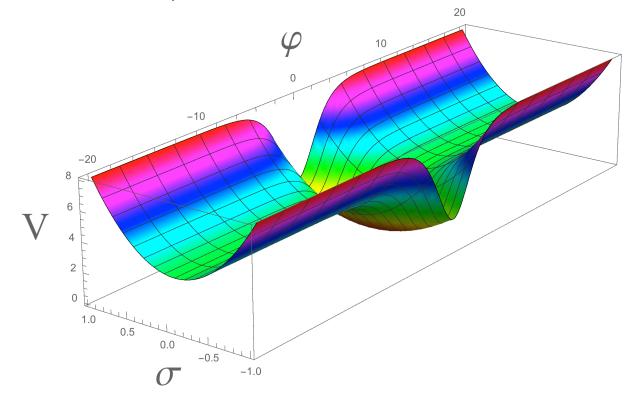
For a broad class of cosmological attractors, the spectral index **n**_s depends mostly on the <u>order of the pole</u> in the kinetic term, while the tensor-to-scalar ratio **r** depends on the <u>residue</u>. **Choice of the potential almost does not matter**, as long as it is non-singular at the pole of the kinetic term. Geometry of the moduli space, not the potential, determines much of the answer.

An often discussed concern about higher order corrections to the potential for large field inflation does not apply to these models.

What happens if we add other fields?

$$\frac{1}{\sqrt{-g}}\mathcal{L} = \frac{1}{2}R - \frac{1}{2}\frac{(\partial\phi)^2}{(1 - \frac{\phi^2}{6\alpha})^2} - \frac{1}{2}m^2\phi^2 - \frac{1}{2}(\partial\sigma)^2 - \frac{1}{2}M^2\sigma^2 - \frac{g^2}{2}\phi^2\sigma^2$$

Potential in canonical variables has a plateau at large values of the inflaton field, and it is quadratic with respect to σ .



Asymptotic freedom of the inflaton

$$\frac{1}{\sqrt{-g}}\mathcal{L} = \frac{1}{2}R - \frac{1}{2}\frac{(\partial\phi)^2}{(1 - \frac{\phi^2}{6\alpha})^2} - \frac{1}{2}(\partial\sigma)^2 - V(\phi, \sigma)$$

Kallosh, AL, 1604.00444

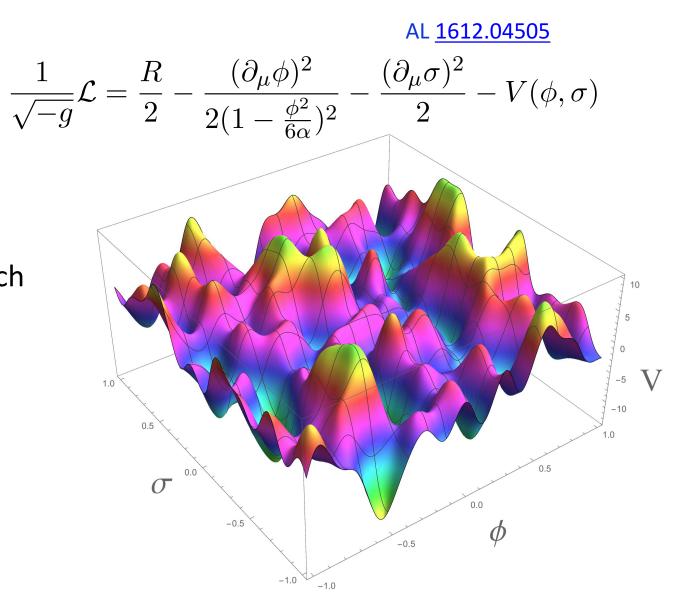
Couplings of the canonically normalized fields are determined by derivatives such as

$$\lambda_{\varphi,\sigma,\sigma} = \partial_{\varphi} \partial_{\sigma}^2 V(\phi,\sigma) = 2\sqrt{\frac{2}{3\alpha}} e^{-\sqrt{\frac{2}{3\alpha}}\varphi} \partial_{\phi} \partial_{\sigma}^2 V(\phi,\sigma)_{|_{\phi\to\sqrt{6\alpha}}}$$

As a result, **couplings of the inflaton field to all other fields are exponentially suppressed during inflation**. The asymptotic shape of the plateau potential of the inflaton is **not** affected by quantum corrections.

Inflation in Random Potentials and Cosmological Attractors

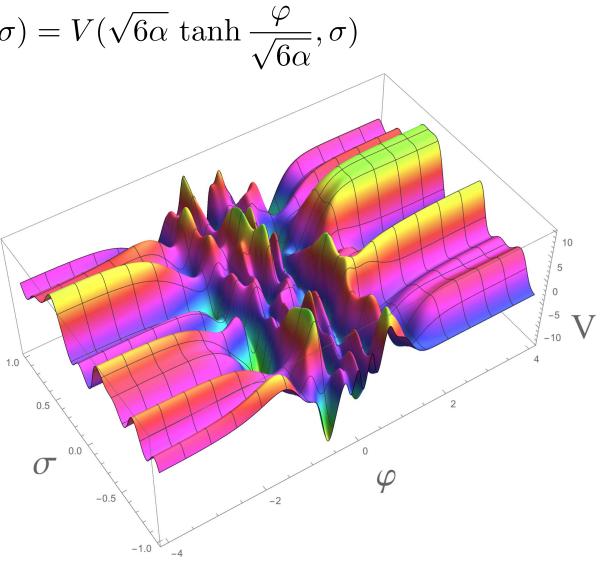
Can we have inflation in such potentials?



In terms of canonical fields φ with the kinetic term $\frac{(\partial_{\mu}\varphi)^2}{2}$, the potential is

$$V(\varphi,\sigma) = V(\sqrt{6\alpha} \tanh \frac{\varphi}{\sqrt{6\alpha}},\sigma)$$

Many inflationary valleys representing alpha-attractors



Double Attractors

$$\frac{1}{\sqrt{-g}}\mathcal{L} = \frac{R}{2} - \frac{(\partial_{\mu}\phi)^2}{2(1-\frac{\phi^2}{6\alpha})^2} - \frac{(\partial_{\mu}\sigma)^2}{2(1-\frac{\sigma^2}{6\beta})^2} - V(\phi,\sigma)$$

In terms of canonical fields

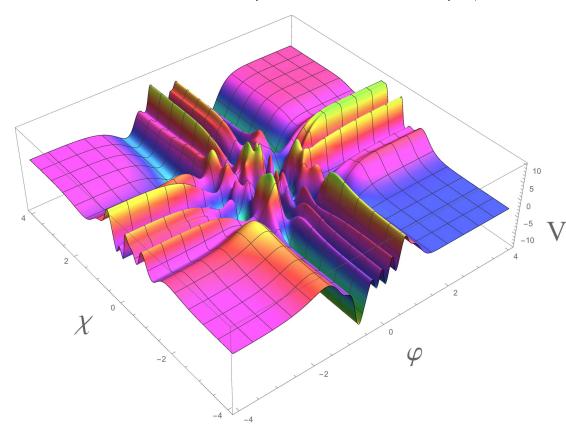
$$V(\varphi, \chi) = V(\sqrt{6\alpha} \tanh \frac{\varphi}{\sqrt{6\alpha}}, \sqrt{6\beta} \tanh \frac{\chi}{\sqrt{6\beta}})$$

Two families of attractors, related to the valleys along the two different inflaton directions:

$$1 - n_s \approx \frac{2}{N}$$
, $r \approx \frac{12\alpha}{N^2}$.

or

$$1 - n_s \approx \frac{2}{N}, \qquad r \approx \frac{12\beta}{N^2}$$



Up to now, we discussed bosonic models of cosmological attractors, but most of them have supergravity versions.

Construction of models of SUGRA inflation is especially simple now, using the new methods described in the talk by Kallosh, see also talks by Scalisi, and Yamada today. These methods allow to provide SUGRA versions of any bosonic inflationary potential, and describe arbitrary values of the cosmological constant and the gravitino mass.

What if interaction between attractors is very strong?

Kallosh, AL, Wrase, Yamada 1704.04829, Kallosh, AL, Roest, Yamada 1705.09247

We will study it in SUGRA, by methods described in the talk by Kallosh

$$\mathcal{G} = \log W_0^2 - \frac{1}{2} \sum_{i=1}^2 \log \frac{(1 - Z_i \overline{Z}_i)^2}{(1 - Z_i^2)(1 - \overline{Z}_i^2)} + S + \overline{S} + g_{S\overline{S}}S\overline{S},$$
$$g^{S\overline{S}} = \frac{1}{W_0^2} \left(|F_S|^2 + \frac{m^2}{2} (|Z_1|^2 + |Z_2|^2) + \frac{M^2}{4} \left((Z_1 + \overline{Z}_1) - (Z_2 + \overline{Z}_2) \right)^2 \right)$$

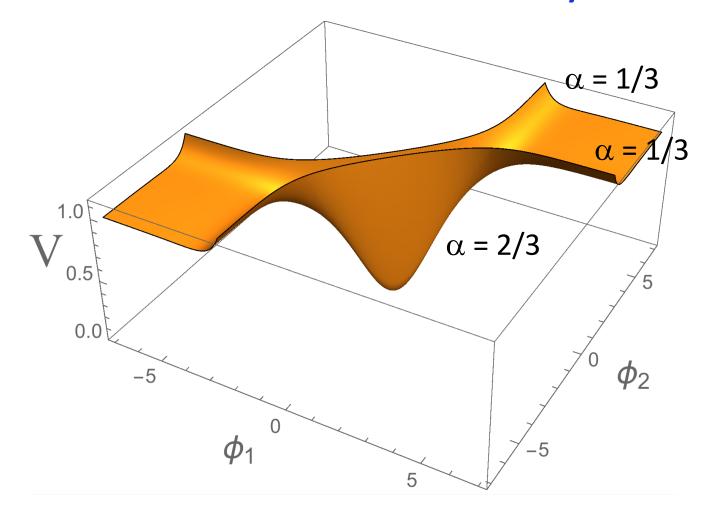
The scalar potential

$$\mathbf{V} = \Lambda + \frac{m^2}{2} (|Z_1|^2 + |Z_2|^2) + \frac{M^2}{4} \left((Z_1 + \overline{Z}_1) - (Z_2 + \overline{Z}_2) \right)^2$$
$$Z_i = \tanh \frac{\phi_i + i\theta_i}{\sqrt{2}}$$

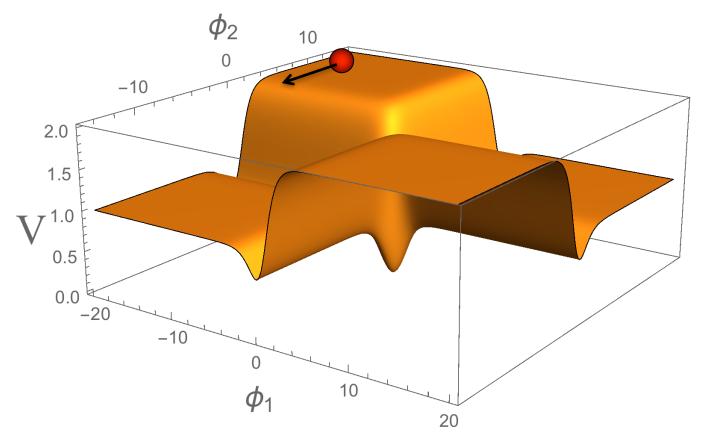
For M >> m, the last term in the potential forces the inflaton fields to coincide,

$$\phi_1 = \phi_2$$

Two strongly interacting attractors with $\alpha = 1/3$ merge into one attractor with $\alpha = 2/3$.



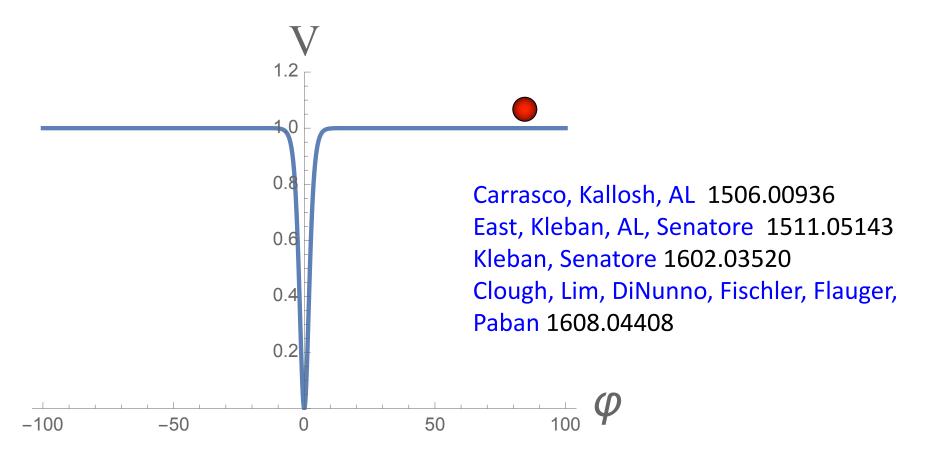
This figure shows only the lower part of the potential, cutting the upper part. Now look at the full potential



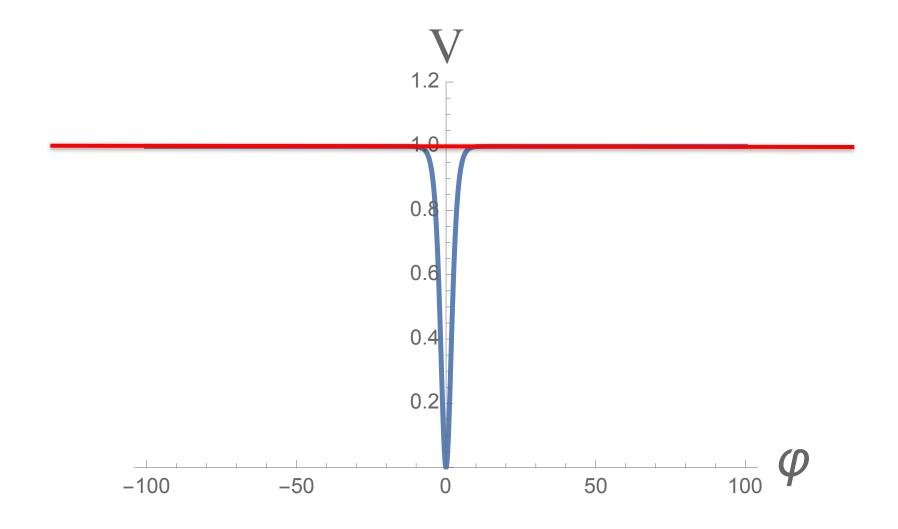
The minimum corresponds to the attractor merger shown at the previous slide. This is where inflation ends. But it begins at the infinitely long <u>upper</u> plateau of height $O(M^2)$. We will return to it shortly.

α -attractors: Initial conditions for inflation

At large fields, the α -attractor potential remains 10 orders of magnitude below Planck density. Can we have inflation with natural initial conditions here? The same question applies for the Starobinsky model and Higgs inflation.



To explain the main idea, note that this potential coincides with the cosmological constant <u>almost everywhere</u>.

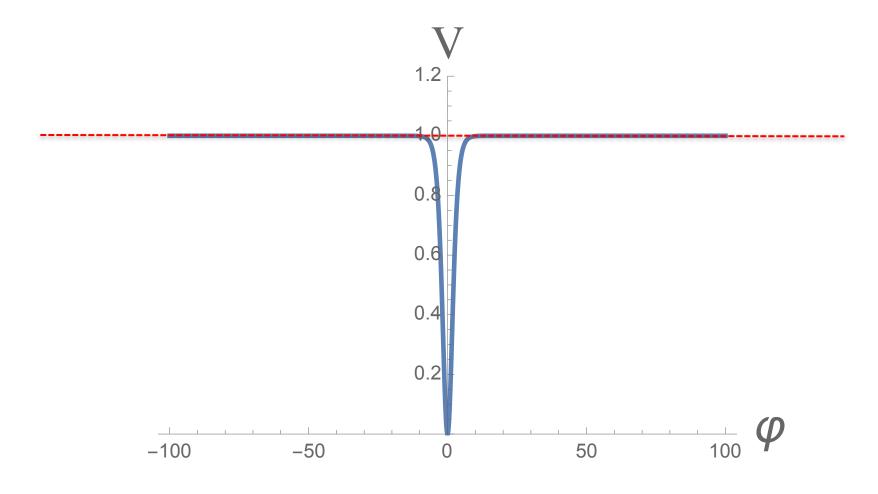


For the universe with a cosmological constant, the problem of initial conditions is nearly trivial.

Start at the Planck density, in an expanding universe dominated by inhomogeneities. The energy density of matter is diluted by the cosmological expansion as $1/t^2$. What could prevent the exponential expansion of the universe which becomes dominated by the cosmological constant Λ after the time t = $\Lambda^{-1/2}$?

Inflation does NOT happen in the universe with the cosmological constant $\Lambda = 10^{-10}$ only if the whole universe collapses within 10^{-28} seconds after its birth.

In other words, only instant global collapse could allow the universe to avoid exponential expansion dominated by the cosmological constant. If the universe does not instantly collapse, it inflates. This optimistic conclusion related to the cosmological constant applies to α -attractors as well, because their potential coincides with the cosmological constant almost everywhere.

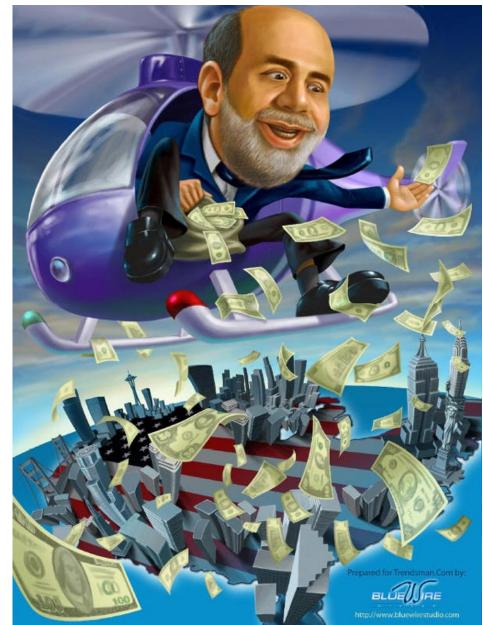


These arguments are valid for general large field inflationary models as well. Recently they have been confirmed by the same methods of numerical GR as the ones used in simulations of BH evolution and merger. The simulations show how BHs are produced from large super-horizon initial inhomogeneities, while the rest of the universe enters the stage of inflation.

East, Kleban, AL, Senatore 1511.05143

These results obtained by sophisticated calculations have a very simple interpretation in terms of inflation in economy.

It is well known that dropping money from a helicopter may lead to inflation, unless all money miss the target



A simple interpretation of our results

1.2

0

0.6

0.4

0.2

0

-50

50

100

Money dropped from a helicopter have no choice but lend on an infinitely long plateau. This inevitably leads to inflation

-100

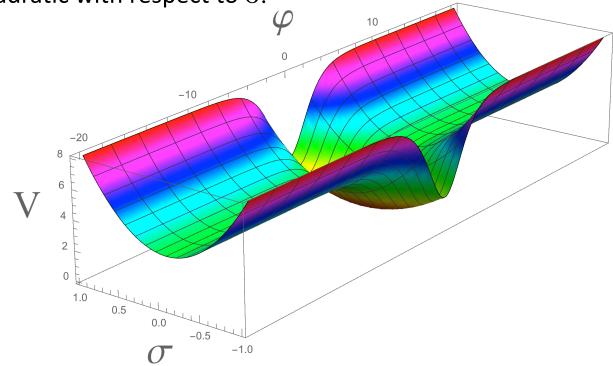
suggested by Starobinsky



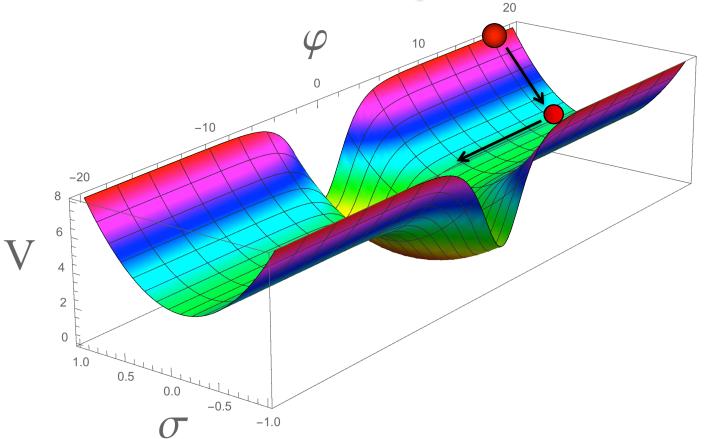
Adding other fields simplifies it even further

$$\frac{1}{\sqrt{-g}}\mathcal{L} = \frac{1}{2}R - \frac{1}{2}\frac{(\partial\phi)^2}{(1 - \frac{\phi^2}{6\alpha})^2} - \frac{1}{2}m^2\phi^2 - \frac{1}{2}(\partial\sigma)^2 - \frac{1}{2}M^2\sigma^2 - \frac{g^2}{2}\phi^2\sigma^2$$

Potential in canonical variables has a plateau at large values of the inflaton field, and it is quadratic with respect to σ .



Initial conditions for plateau inflation

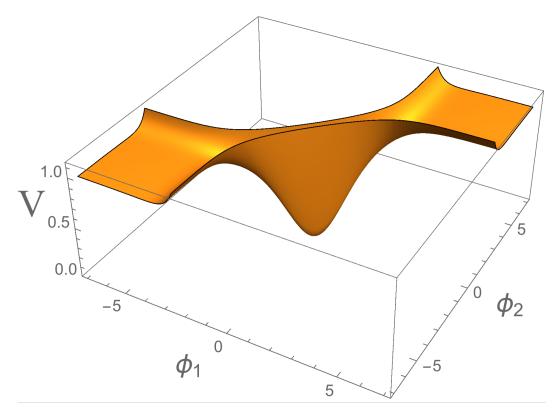


Chaotic inflation with a parabolic potential goes first, starting at nearly Planckian density. When the field down, the plateau inflation begins.

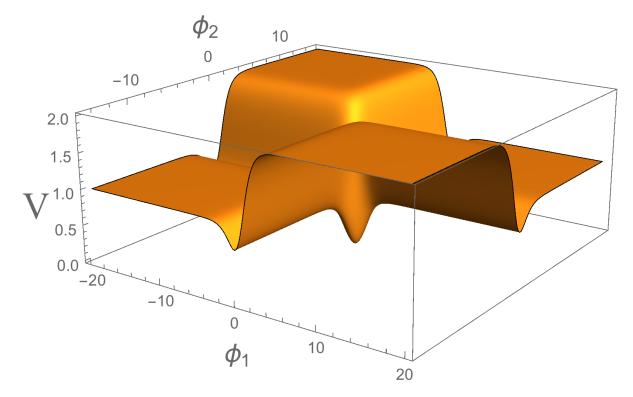
No problem with initial conditions

Kallosh, AL, Roest, Yamada 1705.09247

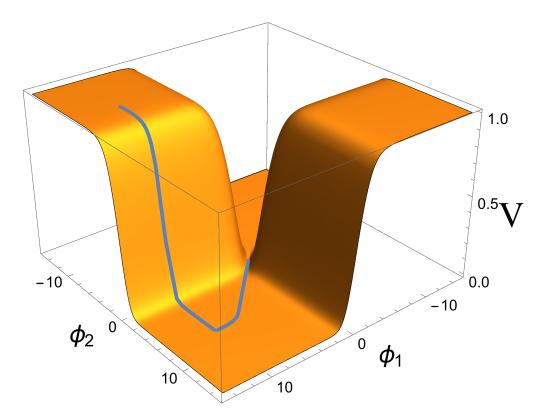
Let us return again to the two-disk merger discussed earlier:



Here we wanted to show the potential at its low values, at the end of inflation, so we cut out its upper part. Now let us restore it



The minimum corresponds to the attractor merger shown at the previous slide. This is where inflation ends. But it begins at the infinitely long <u>upper</u> <u>plateau</u> of height $O(M^2)$. For natural values of M = O(1), this plateau can have nearly Planckian height – no problem to start inflation. After that, the fields cascade down to the inflationary valleys, which later merge. Simple beginning, and last stages matching Planck data.



Inflation begins at the upper plateau of the height M², then the field waterfalls to the lower plateau of the height m², and gets captured by the gorge along the direction $\phi_1 = \phi_2$ until inflation ends. The original waterfall is described by α -attractor with α =1/3. The last stage of inflation corresponds to α =2/3. The figure shows the process for M = O(1), m<< M.

Conclusions:

Cosmological attractors allow to reconsider many usual assumptions with respect to the large field models, resolving some of their often discussed problems and offering new solutions to the problem of initial conditions in inflationary cosmology.