

MASSIVE NEUTRINOS CIRCA 2017

Concha Gonzalez-Garcia

(*YITP Stony Brook & ICREA U. Barcelona*)

PASCOS, June 19th, 2017



<http://www.nu-fit.org>



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Neutrino Flavour Transition: Data and Interpretation

Some comments on Status of :

Leptonic CP violation

Determination of mass Ordering

Degeneracies with NC-NSI

Light Sterile neutrinos

Mass scale

Neutrinos in the Standard Model

The SM is a gauge theory based on the symmetry group

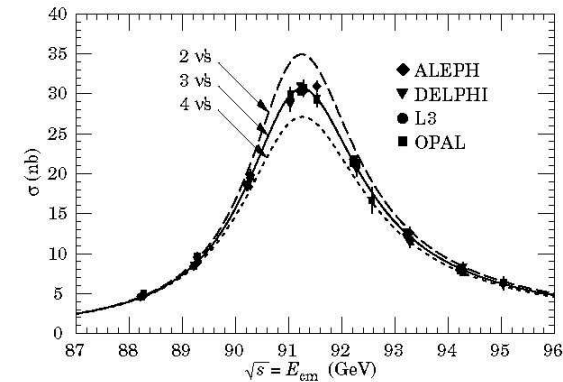
$$SU(3)_C \times SU(2)_L \times U(1)_Y \Rightarrow SU(3)_C \times U(1)_{EM}$$

With three generation of fermions

$(1, 2)_{-\frac{1}{2}}$	$(3, 2)_{\frac{1}{6}}$	$(1, 1)_{-1}$	$(3, 1)_{\frac{2}{3}}$	$(3, 1)_{-\frac{1}{3}}$
$\begin{pmatrix} \nu_e \\ e \end{pmatrix}_L$	$\begin{pmatrix} u^i \\ d^i \end{pmatrix}_L$	e_R	u^i_R	d^i_R
$\begin{pmatrix} \nu_\mu \\ \mu \end{pmatrix}_L$	$\begin{pmatrix} c^i \\ s^i \end{pmatrix}_L$	μ_R	c^i_R	s^i_R
$\begin{pmatrix} \nu_\tau \\ \tau \end{pmatrix}_L$	$\begin{pmatrix} t^i \\ b^i \end{pmatrix}_L$	τ_R	t^i_R	b^i_R

There is no ν_R

Three and only three



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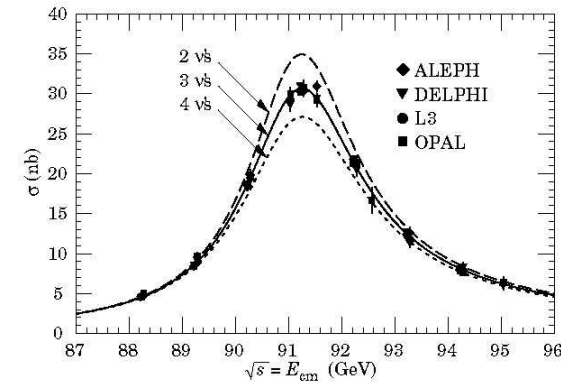


Accidental global symmetry: $B \times L_e \times L_\mu \times L_\tau$ (hence $L = L_e + L_\mu + L_\tau$)



ν strictly massless

Three and only three



- By 2017 we have observed with high (or good) precision:
 - * Atmospheric ν_μ & $\bar{\nu}_\mu$ disappear most likely to ν_τ (**SK, MINOS, ICECUBE**)
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All this implies that L_α are violated

and There is Physics Beyond SM

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- The *starting* path:

Precise determination of the low energy parametrization

The New Minimal Standard Model

- Minimal Extension to allow for LFV \Rightarrow give Mass to the Neutrino

* Introduce ν_R AND impose L conservation \Rightarrow Dirac $\nu \neq \nu^c$:

$$\mathcal{L} = \mathcal{L}_{SM} - M_\nu \overline{\nu}_L \nu_R + h.c.$$

* NOT impose L conservation \Rightarrow Majorana $\nu = \nu^c$

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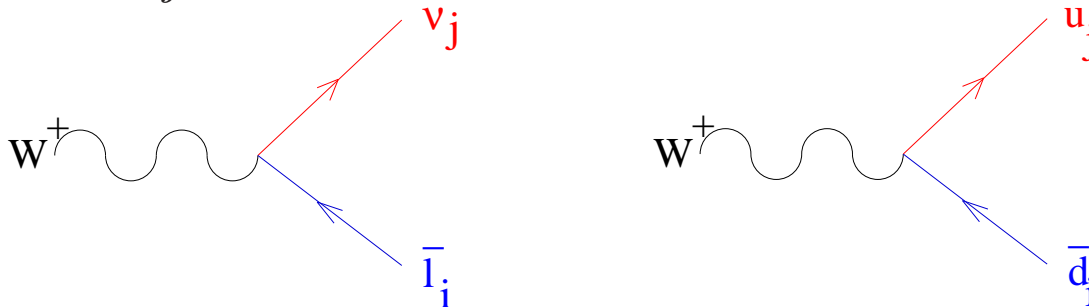
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- The charged current interactions of leptons are not diagonal (same as quarks)

$$\frac{g}{\sqrt{2}} W_\mu^+ \sum_{ij} (U_{LEP}^{ij} \bar{\ell}^i \gamma^\mu L \nu^j + U_{CKM}^{ij} \bar{U}^i \gamma^\mu L D^j) + h.c.$$



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- In general for $N = 3 + s$ massive neutrinos U_{LEP} is $3 \times N$ matrix

$$U_{\text{LEP}} U_{\text{LEP}}^\dagger = I_{3 \times 3} \quad \text{but in general} \quad U_{\text{LEP}}^\dagger U_{\text{LEP}} \neq I_{N \times N}$$

- U_{LEP} : $3 + 3s$ angles + $2s + 1$ Dirac phases + $s + 2$ Majorana phases

- If neutrinos have mass, a weak eigenstate $|\nu_\alpha\rangle$ produced in $l_\alpha + N \rightarrow \nu_\alpha + N'$

is a linear combination of the mass eigenstates ($|\nu_i\rangle$): $|\nu_\alpha\rangle = \sum_{i=1}^n U_{\alpha i} |\nu_i\rangle$

- After a distance L it can be detected with flavour β with probability

$$P_{\alpha\beta} = \delta_{\alpha\beta} - 4 \sum_{j \neq i}^n \text{Re}[U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*] \sin^2 \left(\frac{\Delta_{ij}}{2} \right) + 2 \sum_{j \neq i} \text{Im}[U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*] \sin(\Delta_{ij})$$

$$\frac{\Delta_{ij}}{2} = \frac{(E_i - E_j)L}{2} = 1.27 \frac{(m_i^2 - m_j^2)}{\text{eV}^2} \frac{L/E}{\text{Km/GeV}}$$

No information on ν mass scale nor Majorana versus Dirac

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- When osc between 2- ν dominates:

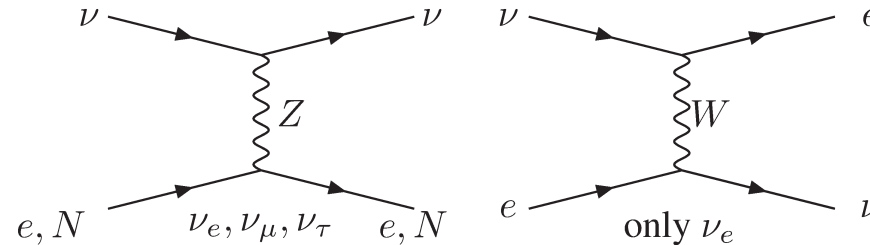
$$P_{\alpha\alpha} = 1 - P_{osc} \quad \text{Disappear}$$

$$P_{osc} = \sin^2(2\theta) \sin^2 \left(1.27 \frac{\Delta m^2 L}{E} \right) \quad \text{Appear}$$

Matter Effects

- If ν cross **matter** regions (Sun, Earth...) it interacts *coherently*

- But **Different flavours** have **different interactions** :



\Rightarrow Effective potential in ν evolution : $V_e \neq V_{\mu, \tau} \Rightarrow \Delta V^\nu = -\Delta V^{\bar{\nu}} = \sqrt{2}G_F N_e$

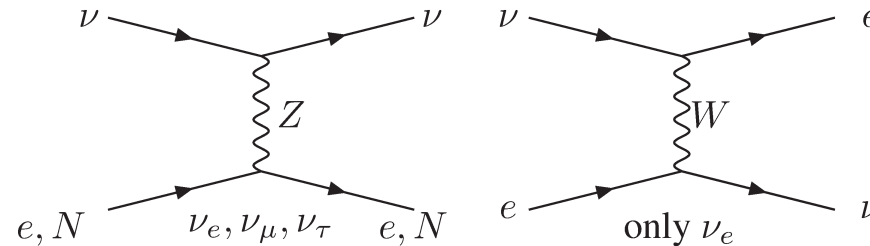
$$-i \frac{\partial}{\partial x} \begin{pmatrix} \nu_e \\ \nu_X \end{pmatrix} = \left[- \begin{pmatrix} V_e - V_X - \frac{\Delta m^2}{4E} \cos 2\theta & \frac{\Delta m^2}{4E} \sin 2\theta \\ \frac{\Delta m^2}{4E} \sin 2\theta & \frac{\Delta m^2}{4E} \cos 2\theta \end{pmatrix} \right] \begin{pmatrix} \nu_e \\ \nu_X \end{pmatrix}$$

\Rightarrow **Modification of mixing angle and oscillation wavelength (MSW)**

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⇒ **Modification of mixing angle and oscillation wavelength** (MSW)

- Mass difference and mixing in matter:

$$\Delta m_m^2 = \sqrt{(\Delta m^2 \cos 2\theta - 2E\Delta V)^2 + (\Delta m^2 \sin 2\theta)^2}$$

$$\sin(2\theta_m) = \frac{\Delta m^2 \sin(2\theta)}{\Delta m_{mat}^2}$$

⇒ For solar ν 's in adiabatic regime

$$P_{ee} = \frac{1}{2} [1 + \cos(2\theta_m) \cos(2\theta)]$$

Dependence on θ octant

⇒ In LBL terrestrial experiments

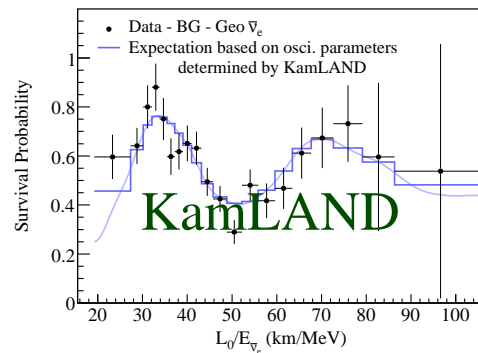
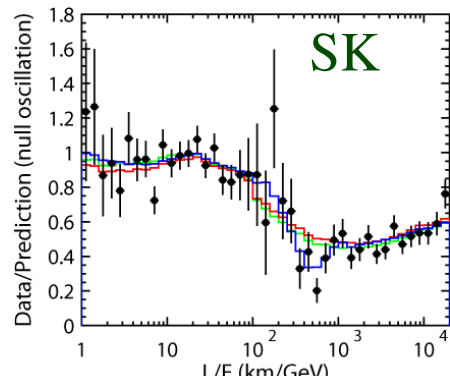
Dependence on **sign of Δm^2**

and θ octant

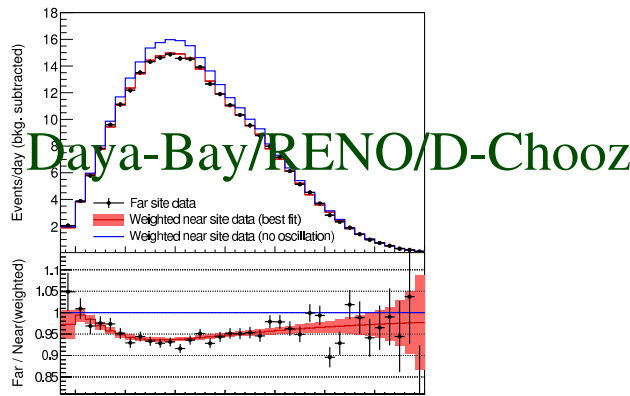
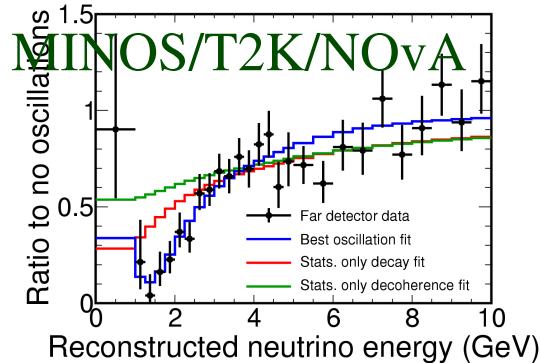
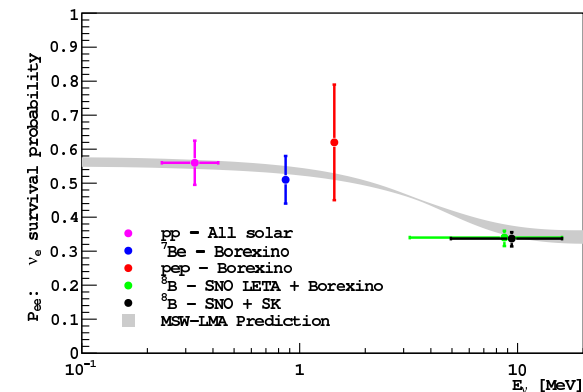
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● Confirmed: Vacuum oscillation L/E pattern with 2 frequencies



MSW conversion in Sun

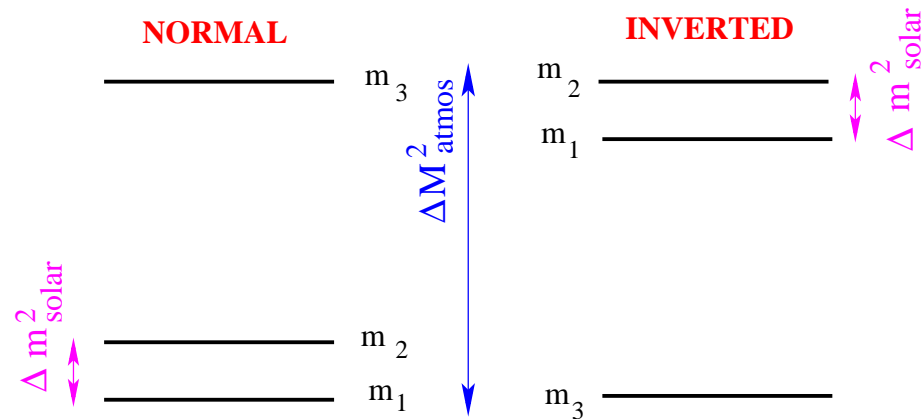


3ν Flavour Parameters

- For for 3 ν's : 3 Mixing angles + 1 Dirac Phase + 2 Majorana Phases

$$U_{\text{LEP}} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{i\delta_{\text{CP}}} \\ 0 & 1 & 0 \\ -s_{13}e^{-i\delta_{\text{CP}}} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{21} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} e^{i\eta_1} & 0 & 0 \\ 0 & e^{i\eta_2} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

- Two Possible Orderings

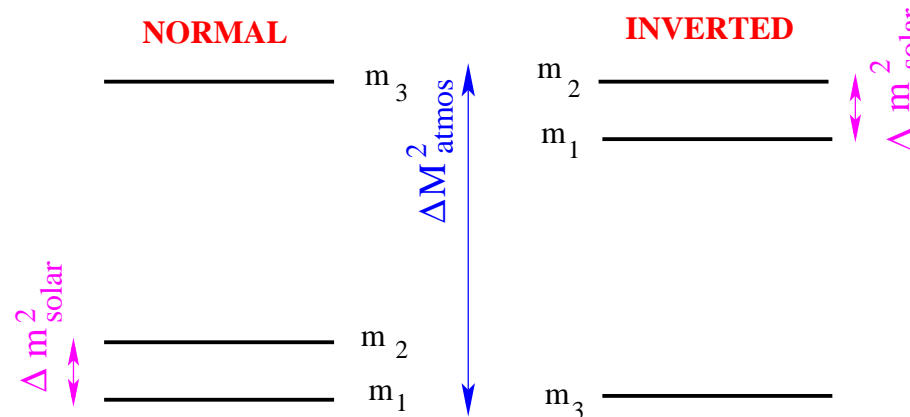


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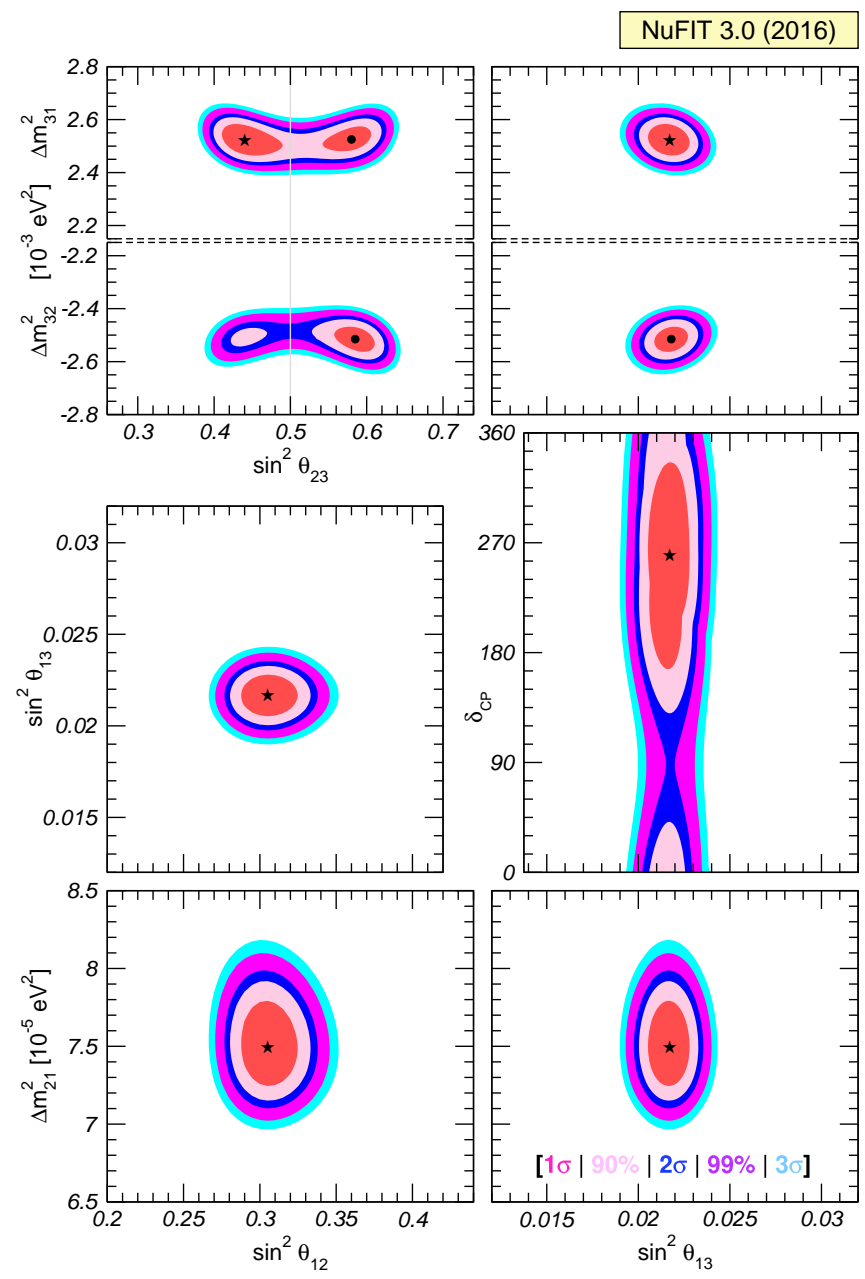
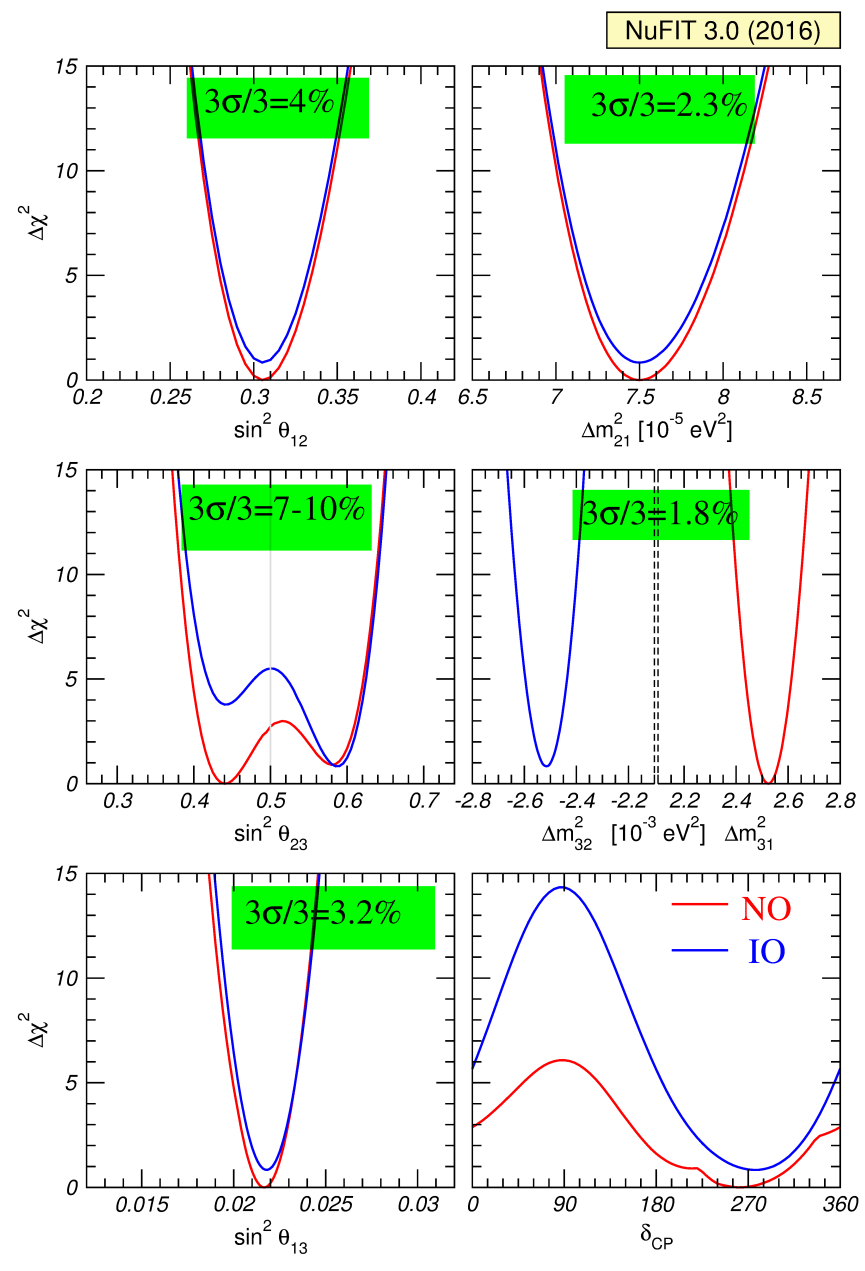


Experiment	Dominant Dependence	Important Dependence
Solar Experiments	$\rightarrow \theta_{12}$	$\Delta m_{21}^2, \theta_{13}$
Reactor LBL (KamLAND)	$\rightarrow \Delta m_{21}^2$	θ_{12}, θ_{13}
Reactor MBL (Daya Bay, Reno, D-Chooz)	$\rightarrow \theta_{13}$	Δm_{atm}^2
Atmospheric Experiments	$\rightarrow \theta_{23}$	$\Delta m_{\text{atm}}^2, \theta_{13}, \delta_{\text{CP}}$
Acc LBL ν_μ Disapp (Minos, T2K, NOvA)	$\rightarrow \Delta m_{\text{atm}}^2$	θ_{23}
Acc LBL ν_e App (Minos, T2K, NOvA)	$\rightarrow \theta_{13}$	$\delta_{\text{CP}}, \theta_{23}$

3 ν Flavour Parameters: Status in 6/2017

Global 6-parameter fit <http://www.nu-fit.org>

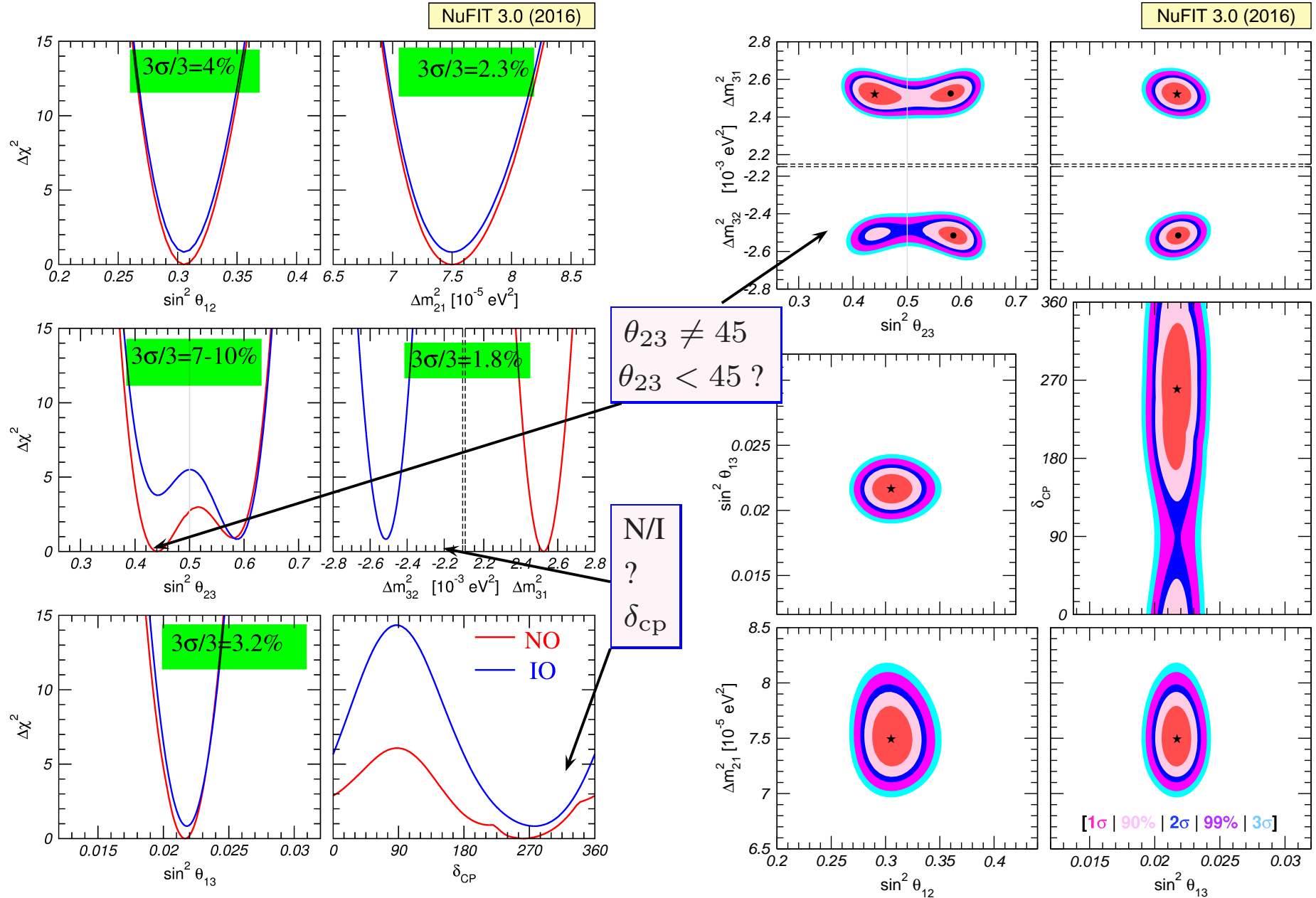
Esteban, Maltoni, Martinez-Soler, Schwetz, MCG-G ArXiv:1611:01514



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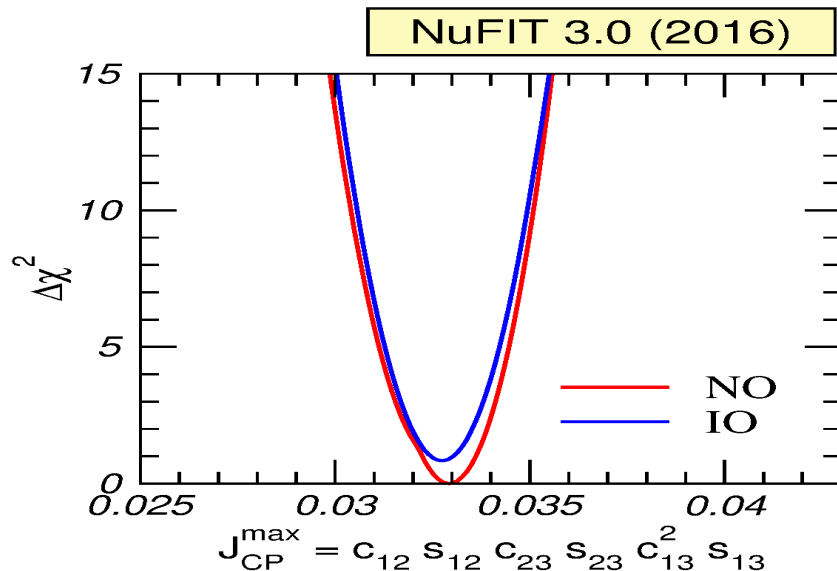


- Leptonic CP $\Rightarrow P_{\nu_\alpha \rightarrow \nu_\beta} \neq P_{\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta}$:

$$P_{\nu_\alpha \rightarrow \nu_\beta} - P_{\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta} \propto J = \text{Im}(U_{\alpha 1} U_{\alpha 2}^* U_{\beta 2} U_{\beta 1}^*) = J_{\text{LEP,CP}}^{\text{max}} \sin \delta_{\text{CP}}$$

$$J_{\text{LEP,CP}}^{\text{max}} = \frac{1}{8} c_{13} \sin^2 2\theta_{13} \sin^2 2\theta_{23} \sin^2 2\theta_{12}$$

- Maximum Allowed Leptonic CPV:



$$J_{\text{LEP,CP}}^{\text{max}} = (3.29 \pm 0.07) \times 10^{-2}$$

to compare with

$$J_{\text{CKM,CP}} = (3.04 \pm 0.21) \times 10^{-5}$$

\Rightarrow Leptonic CPV may be largest CPV

in New Minimal SM

if $\sin \delta_{\text{CP}}$ not too small

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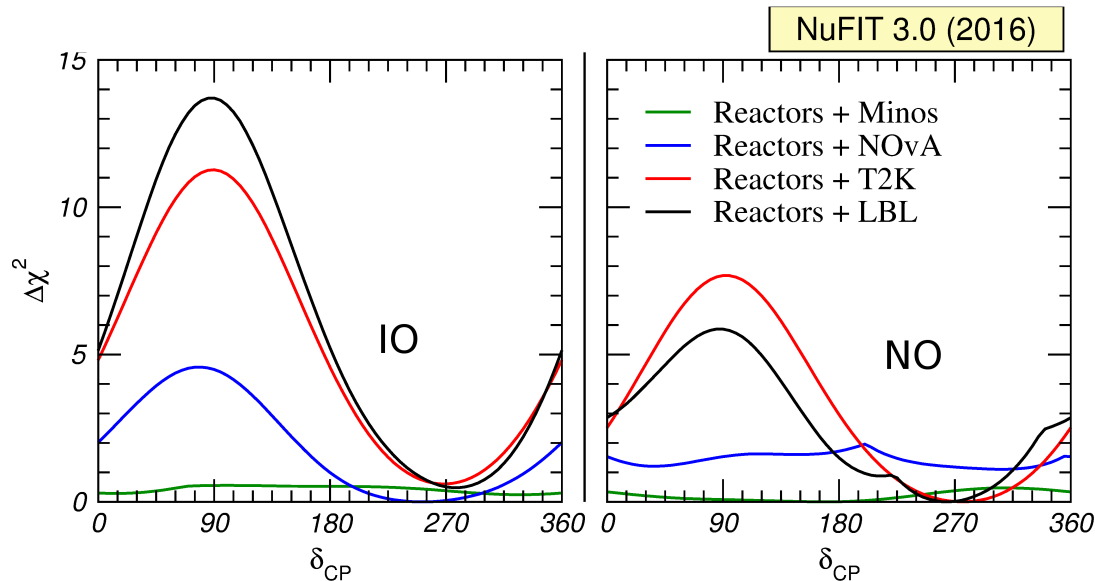
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- Leptonic CPV Phase: Mainly from $\nu_\mu \rightarrow \nu_e$ in LBL (complicated by matter effects)

$$P_{\mu e} \simeq s_{23}^2 \sin^2 2\theta_{13} \left(\frac{\Delta_{31}}{B_\mp}\right)^2 \sin^2\left(\frac{B_\mp L}{2}\right) + 8 J_{\text{LEP,CP}}^{\text{max}} \frac{\Delta_{12}}{V_E} \frac{\Delta_{31}}{B_\mp} \sin\left(\frac{V_E L}{2}\right) \sin\left(\frac{B_\mp L}{2}\right) \cos\left(\frac{\Delta_{31} L}{2} \pm \delta_{\text{CP}}\right)$$

$$\Delta_{ij} = \frac{\Delta m_{ij}^2}{2E} \quad B_\pm = \Delta_{31} \pm V_E \quad J_{\text{LEP,CP}}^{\text{max}} = \frac{1}{8} c_{13} \sin^2 2\theta_{13} \sin^2 2\theta_{23} \sin^2 2\theta_{12}$$

- Best fit $\delta_{\text{CP}} \sim 270^\circ$
- CP conservation at 70% (NO), 97% (IO)
- Driven by “fluctuation” in T2K



Mass hierarchy	ν_e		$\bar{\nu}_e$	
	Normal	Inverted	Normal	Inverted
$\delta_{\text{CP}} = -\pi/2$	28.8	25.5	6.0	6.5
$\delta_{\text{CP}} = 0$	24.2	21.2	6.9	7.4
$\delta_{\text{CP}} = \pi/2$	19.7	17.2	7.7	8.4
$\delta_{\text{CP}} = \pm\pi$	24.2	21.6	6.8	7.4
Data	32		4	

\Rightarrow Significance may not grow soon

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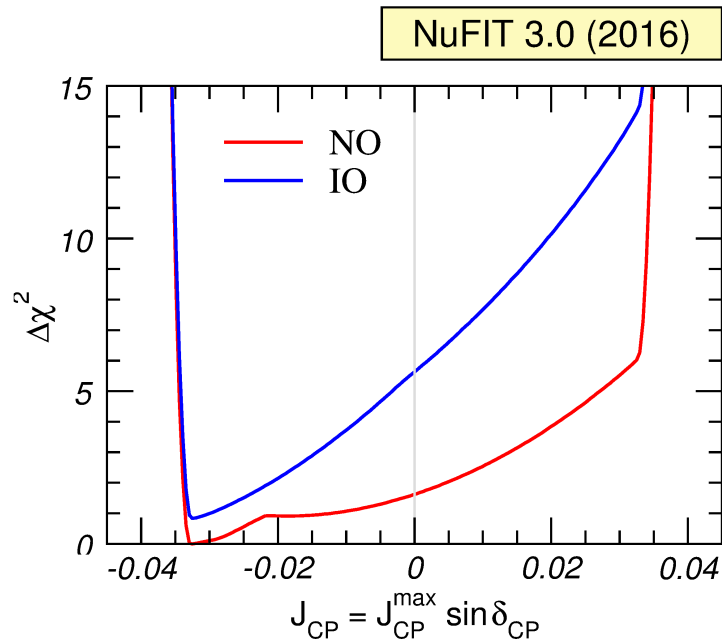
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$$\Delta_{ij} = \frac{\Delta m_{ij}^2}{2E} \quad B_\pm = \Delta_{31} \pm V_E \quad J_{\text{LEP,CP}}^{\text{max}} = \frac{1}{8} c_{13} \sin^2 2\theta_{13} \sin^2 2\theta_{23} \sin^2 2\theta_{12}$$

- Leptonic Jarlskog Invariant



Best fit $J_{\text{LEP,CP}} = -0.033$

Redundancy: Δm_{23}^2 in LBL vs Reactors

- At LBL determined in ν_μ and $\bar{\nu}_\mu$ disappearance spectrum

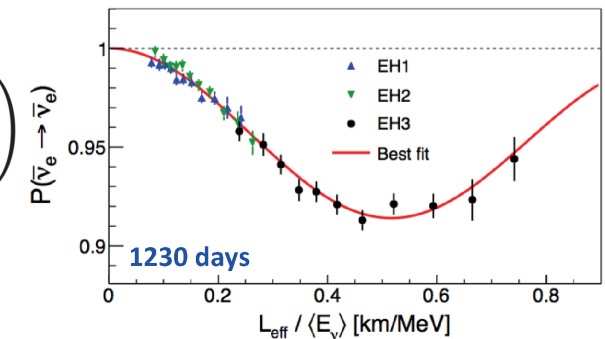
$$P_{\mu\mu} \simeq 1 - (c_{13}^4 \sin^2 2\theta_{23} + s_{23}^2 \sin^2 2\theta_{13}) \sin^2 \left(\frac{\Delta m_{31}^2 L}{4E} \right) + \mathcal{O}(\Delta m_{21}^2)$$

- At MBL Reactors (Daya-Bay, Reno, D-Chooz) determined in $\bar{\nu}_e$ disapp spectrum

$$P_{ee} \simeq 1 - \sin^2 2\theta_{13} \sin^2 \left(\frac{\Delta m_{ee}^2 L}{4E} \right) - c_{13}^4 \sin^2 2\theta_{12} \sin^2 \left(\frac{\Delta m_{21}^2 L}{4E} \right)$$

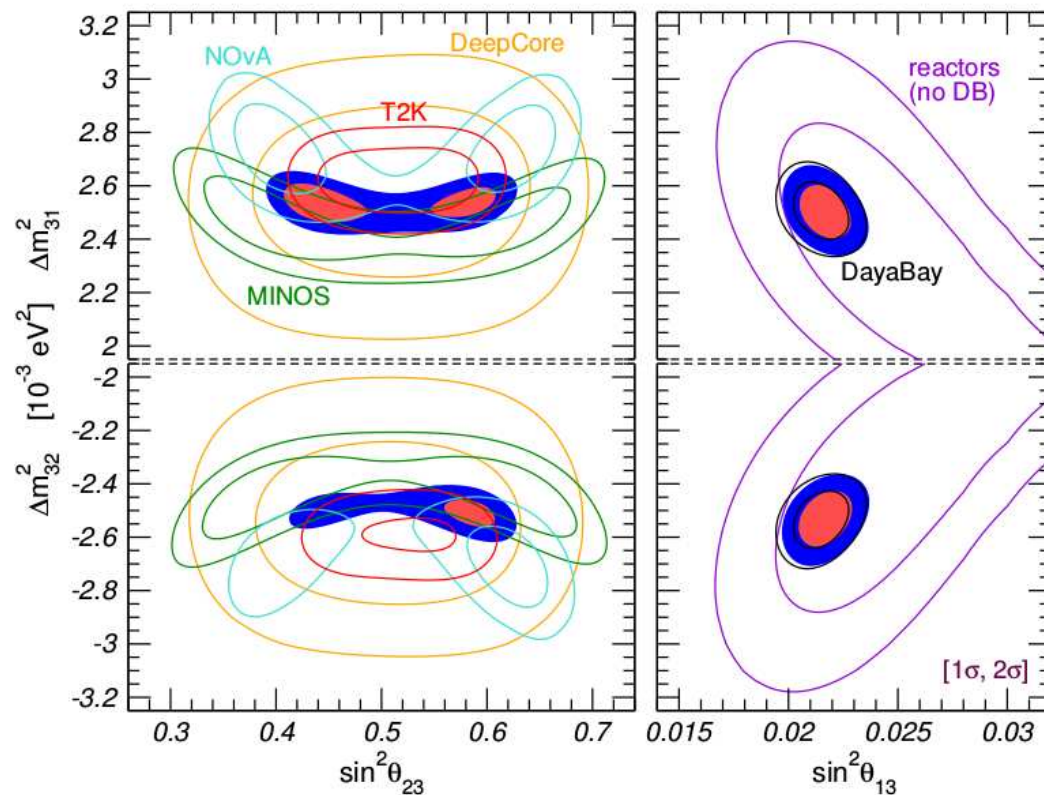
$$\Delta m_{ee}^2 \simeq |\Delta m_{32}^2| \pm c_{12}^2 \Delta m_{21}^2 \simeq |\Delta m_{32}^2| \pm 0.05 \times 10^{-3} \text{ eV}^2$$

Nunokawa, Parke, Zukanovich (2005)



Δm_{23}^2 in LBL vs Reactors: Consistency

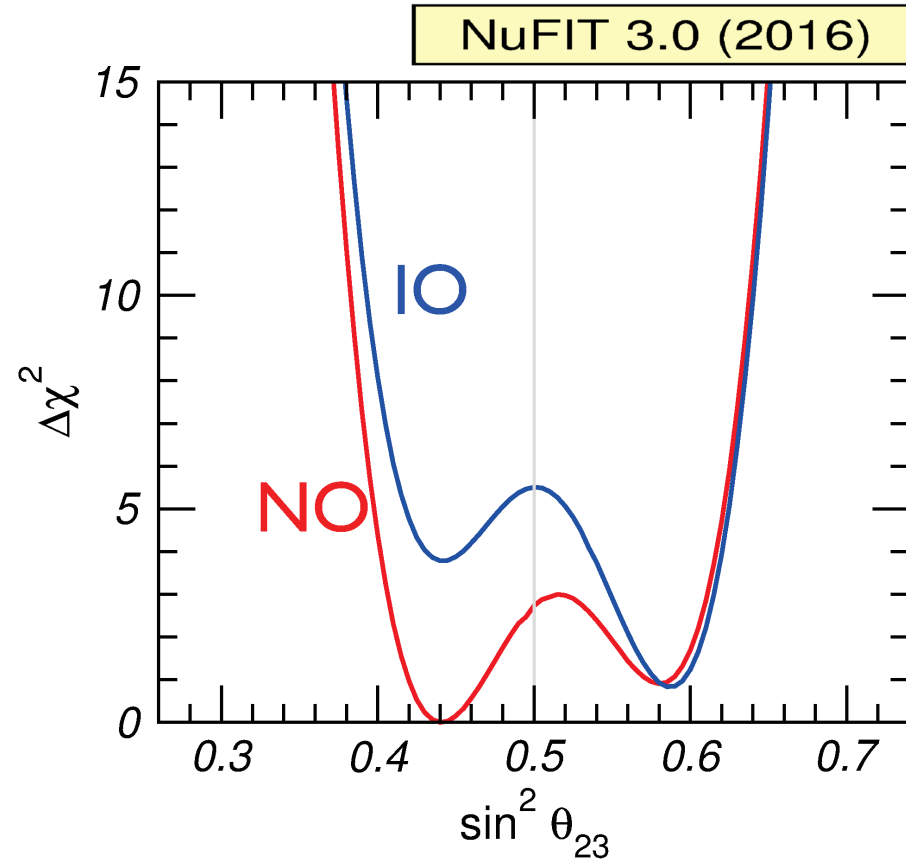
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LBL ν_μ disappearanceREAC ν_e disappearance

– Consistent determination of $|\Delta m_{32}^2|$

– Hint for non-maximal θ_{23} driven by NO ν A and MINOS

Ordering and θ_{23}



- No significance preference Normal vs Inverted Ordering: $\Delta\chi^2 \sim 1$
- Favoured Octant of θ_{23} depends on ordering
- CL of maximal mixing at 91%(NO) or 98% (IO)

Near Future for CP and Ordering: Strategies

- $\nu/\bar{\nu}$ comparison with or without Earth matter effects in $\nu_\mu \rightarrow \nu_e$ & $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ at LBL: DUNE (wide band beam, L=1300 km), HK (narrow band beam, L=300 km)

$$P_{\mu e} \simeq s_{23}^2 \sin^2 2\theta_{13} \left(\frac{\Delta_{31}}{\Delta_{31} \pm V} \right)^2 \sin^2 \left(\frac{\Delta_{31} \pm V L}{2} \right) + 8 J_{CP}^{\max} \frac{\Delta_{12}}{V} \frac{\Delta_{31}}{\Delta_{31} \pm V} \sin \left(\frac{V L}{2} \right) \sin \left(\frac{\Delta_{31} \pm V L}{2} \right) \cos \left(\frac{\Delta_{31} L}{2} \pm \delta_{CP} \right)$$

$$J_{CP}^{\max} = c_{13}^2 s_{13} c_{23} s_{23} c_{12} s_{12}$$

- Challenge: Parameter degeneracies, Normalization uncertainty, E_ν reconstruction
- Earth matter effects in large statistics ATM ν_μ disapp : HK,INO, PINGU,ORCA ...
 - Challenge: ATM flux contains both ν_μ and $\bar{\nu}_\mu$, ATM flux uncertainties
- Reactor experiment at $L \sim 60$ km (vacuum) able to observe the difference between oscillations with Δm_{31}^2 and Δm_{32}^2 : JUNO, RENO-50

$$P_{\nu_e, \nu_e} = 1 - c_{13}^4 \sin^2 2\theta_{12} \sin^2 \left(\frac{\Delta m_{21}^2 L}{4E} \right) - \sin^2 2\theta_{13} \left[c_{12}^2 \sin^2 \left(\frac{\Delta m_{31}^2 L}{4E} \right) + s_{12}^2 \sin^2 \left(\frac{\Delta m_{32}^2 L}{4E} \right) \right]$$

- Challenge: Energy resolution

Confirmed Low Energy Picture and MY List of Q&A

- At least **two** neutrinos **are massive** \Rightarrow **There is NP**
- **Three mixing angles** are non-zero (and relatively **large**) \Rightarrow very **different from CKM**
- **Leptonic CP**: Best fit $J_{\text{Lep,CP}} = -0.033$. CP conservation at 70% CL
Significance likely to grow slowly with present experiments
- **Ordering**: No significant preference in our global fit
Requires new oscillation experiments
- **Other NP at play?**

Alternative Oscillation Mechanisms

- Oscillations are due to:

- Misalignment between CC-int and propagation states: **Mixing** \Rightarrow **Amplitude**

- Difference phases of propagation states \Rightarrow **Wavelength**.

For Δm^2 -OSC $\lambda = \frac{4\pi E}{\Delta m^2}$

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- ν masses are not the only mechanism for oscillations

Violation of Equivalence Principle (VEP): Gasperini 88, Halprin, Leung 01

Non universal coupling of neutrinos $\gamma_1 \neq \gamma_2$ to gravitational potential ϕ

$$\lambda = \frac{\pi}{E|\phi|\delta\gamma}$$

Violation of Lorentz Invariance (VLI): Coleman, Glashow 97

Non universal asymptotic velocity of neutrinos $c_1 \neq c_2 \Rightarrow E_i = \frac{m_i^2}{2p} + c_i p$

$$\lambda = \frac{2\pi}{E\Delta c}$$

Interactions with space-time torsion: Sabbata, Gasperini 81

Non universal couplings of neutrinos $k_1 \neq k_2$ to torsion strength Q

$$\lambda = \frac{2\pi}{Q\Delta k}$$

Violation of Lorentz Invariance (VLI) Colladay, Kostelecky 97; Coleman, Glashow 99

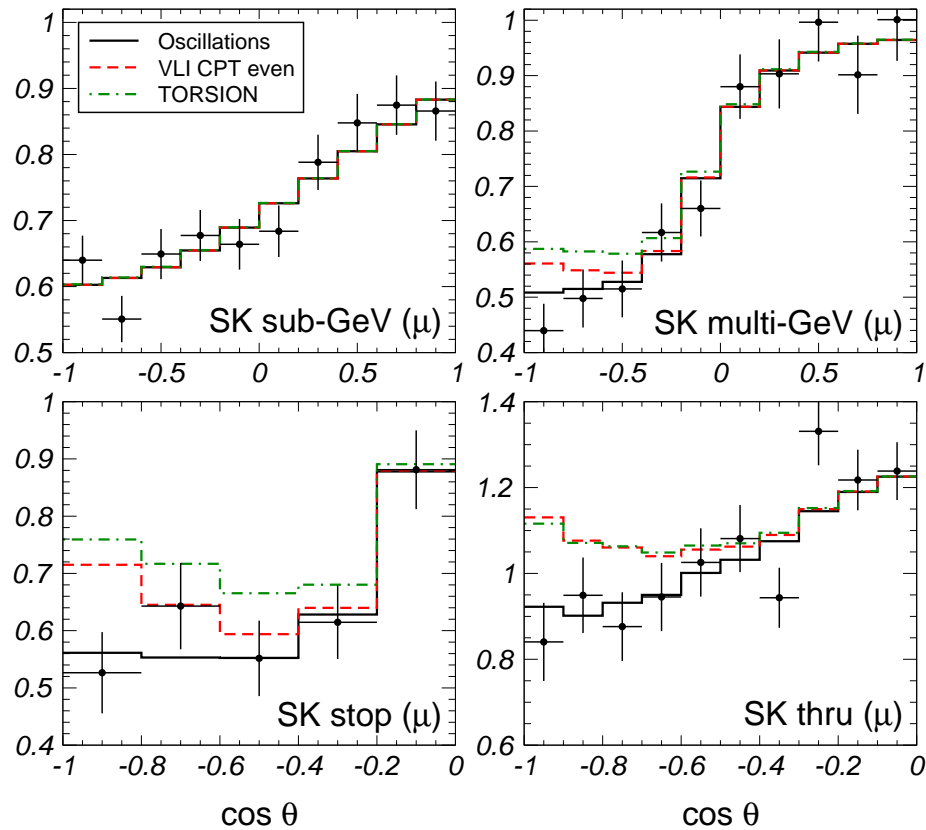
due to CPT violating terms: $\bar{\nu}_L^\alpha b_\mu^{\alpha\beta} \gamma_\mu \nu_L^\beta \Rightarrow E_i = \frac{m_i^2}{2p} \pm b_i$

$$\lambda = \pm \frac{2\pi}{\Delta b}$$

ATM ν 's: Subdominant NP Effects

- Using atmospheric neutrino data these effects can be constrained

MCG-G, M. Maltoni hepp-ph,0404085,0704.1800



At 90% CL:

$$\frac{|\Delta c|}{c} \leq 1.2 \times 10^{-24}$$

$$|\phi \Delta \gamma| \leq 5.9 \times 10^{-25}$$

$$|Q \Delta k| \leq 4.8 \times 10^{-23} \text{ GeV}$$

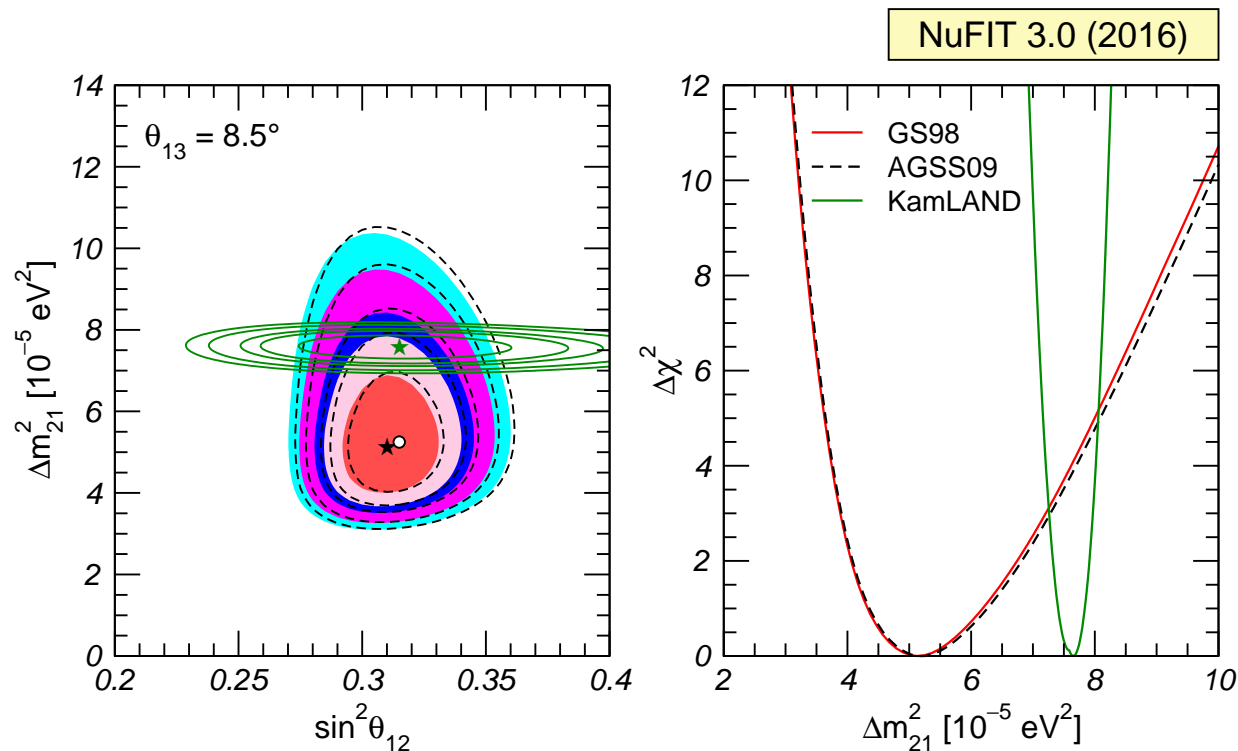
$$|\Delta b| \leq 3.0 \times 10^{-23} \text{ GeV}$$

Issues in 3 ν Analysis: Δm_{21}^2 KamLAND vs SOLAR

- $\Delta m_{13}^2 \gg E/L \Rightarrow P_{ee}^{3\nu} = c_{13}^4 P_{2\nu} + s_{13}^4$

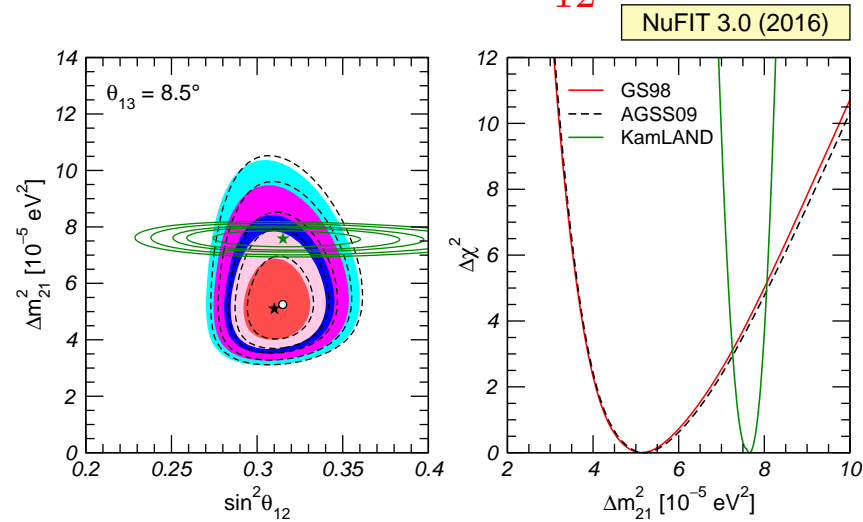
$$i \frac{d}{dt} \begin{pmatrix} \nu_e \\ \nu_a \end{pmatrix} = \left[\frac{\Delta m_{21}^2}{4E} \begin{pmatrix} -\cos 2\theta_{12} & \sin 2\theta_{12} \\ \sin 2\theta_{12} & \cos 2\theta_{12} \end{pmatrix} \pm \sqrt{2} G_F N_e \begin{pmatrix} c_{13}^2 & 0 \\ 0 & 0 \end{pmatrix} \right] \begin{pmatrix} \nu_e \\ \nu_a \end{pmatrix}$$

- With $\theta_{13} \simeq 9^\circ$ θ_{12} OK. But $\sim 2\sigma$ tension on Δm_{12}^2

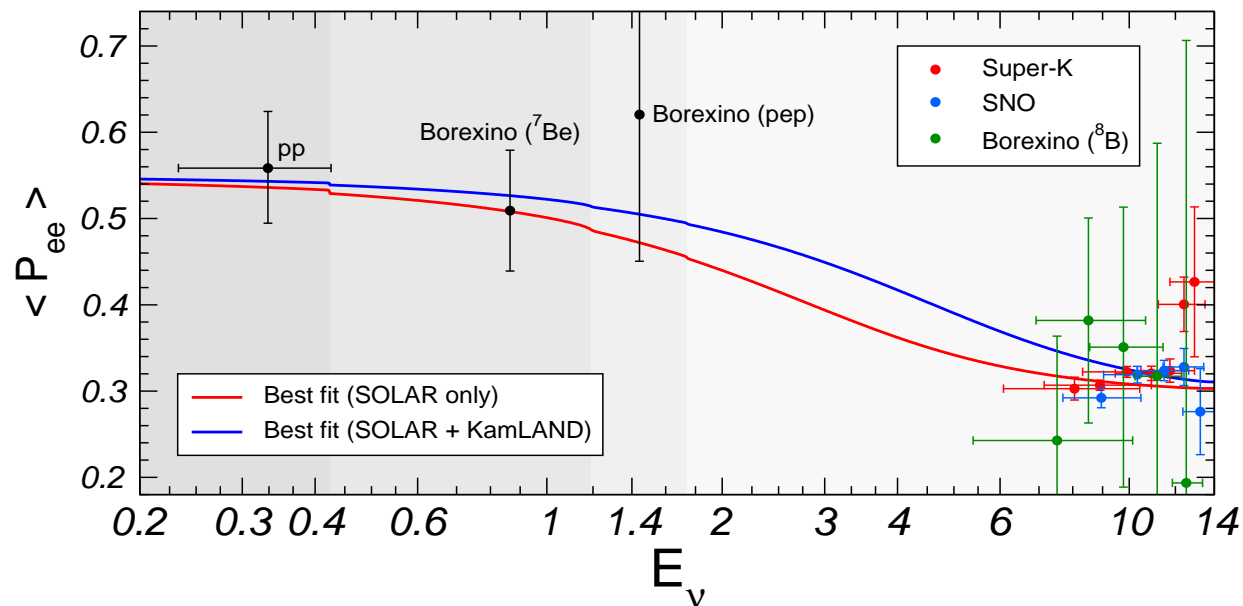


Ma Issues in 3 ν Analysis: Δm_{21}^2 KamLAND vs SOLAR rcia

For $\theta_{13} \simeq 9^\circ$ θ_{12} OK. But $\sim 2\sigma$ tension on Δm_{12}^2



Tension related to: a) “too large” of Day/Night at SK



b) smaller-than-expected low-E turn up from MSW at best global fit

Modified matter potential?

- Including non-standard neutrino NC interactions with fermion f

$$\mathcal{L}_{\text{NSI}} = -2\sqrt{2}G_F \varepsilon_{\alpha\beta}^{fP} (\bar{\nu}_\alpha \gamma^\mu L \nu_\beta) (\bar{f} \gamma_\mu P f), \quad P = L, R$$

- In flavour basis $\vec{\nu} = (\nu_e, \nu_\mu, \nu_\tau)^T$ the neutrino evolution eq.:

$$i \frac{d}{dx} \vec{\nu} = H^\nu \vec{\nu} \quad \text{with} \quad H^\nu = H_{\text{vac}} + H_{\text{mat}} \quad \text{and} \quad H^{\bar{\nu}} = (H_{\text{vac}} - H_{\text{mat}})^*$$

- The **most general matter potential** can be parametrized

$$H_{\text{mat}} = \sqrt{2}G_F N_e(r) \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} + \sqrt{2}G_F \sum_{f=e,u,d} N_f(r) \begin{pmatrix} \varepsilon_{ee}^f & \varepsilon_{e\mu}^f & \varepsilon_{e\tau}^f \\ \varepsilon_{e\mu}^{f*} & \varepsilon_{\mu\mu}^f & \varepsilon_{\mu\tau}^f \\ \varepsilon_{e\tau}^{f*} & \varepsilon_{\mu\tau}^{f*} & \varepsilon_{\tau\tau}^f \end{pmatrix}$$

Deviations from $H_{\text{mat}}^{\text{SM}} = \sqrt{2}G_F N_e(r) \text{diag}(1, 0, 0)$ induced by **NSI**

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Deviations from $H_{\text{mat}}^{\text{SM}} = \sqrt{2}G_F N_e(r) \text{diag}(1, 0, 0)$ induced by **NSI**

- The 3ν evolution depends on **6** (vac) + **8 per f** (mat)

\Rightarrow Parameters degeneracies (some well-known but being rediscovered lately ...)

In particular CPT \Rightarrow invariance under simultaneously:

$$\begin{aligned} \theta_{12} &\leftrightarrow \frac{\pi}{2} - \theta_{12}, & (\varepsilon_{ee} - \varepsilon_{\mu\mu}) &\rightarrow -(\varepsilon_{ee} - \varepsilon_{\mu\mu}) - 2, \\ \Delta m_{31}^2 &\rightarrow -\Delta m_{32}^2, & (\varepsilon_{\tau\tau} - \varepsilon_{\mu\mu}) &\rightarrow -(\varepsilon_{\tau\tau} - \varepsilon_{\mu\mu}), \\ \delta &\rightarrow \pi - \delta, & \varepsilon_{\alpha\beta} &\rightarrow -\varepsilon_{\alpha\beta}^* \quad (\alpha \neq \beta), \end{aligned}$$

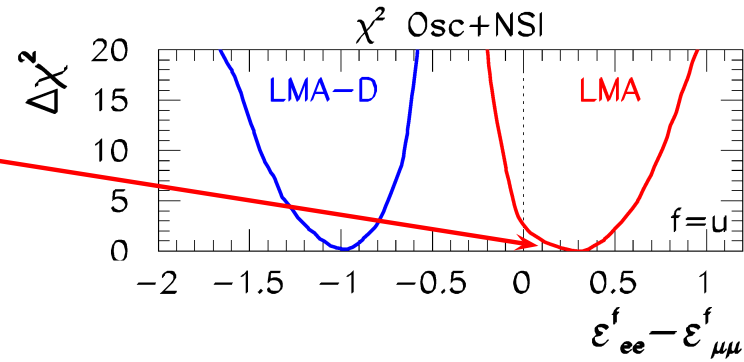
NSI: Bounds from Oscillation data

Param.	best-fit	90% CL	
		LMA	LMA \oplus LMA - D
$\varepsilon_{ee}^u - \varepsilon_{\mu\mu}^u$	+0.298	[+0.00, +0.51]	\oplus [-1.19, -0.81]
$\varepsilon_{\tau\tau}^u - \varepsilon_{\mu\mu}^u$	+0.001	[-0.01, +0.03]	[-0.03, +0.03]
$\varepsilon_{e\mu}^u$	-0.021	[-0.09, +0.04]	[-0.09, +0.10]
$\varepsilon_{e\tau}^u$	+0.021	[-0.14, +0.14]	[-0.15, +0.14]
$\varepsilon_{\mu\tau}^u$	-0.001	[-0.01, +0.01]	[-0.01, +0.01]

- Bounds $\mathcal{O}(1 - 10\%)$
- Except $\varepsilon_{ee} - \varepsilon_{\mu\mu}$

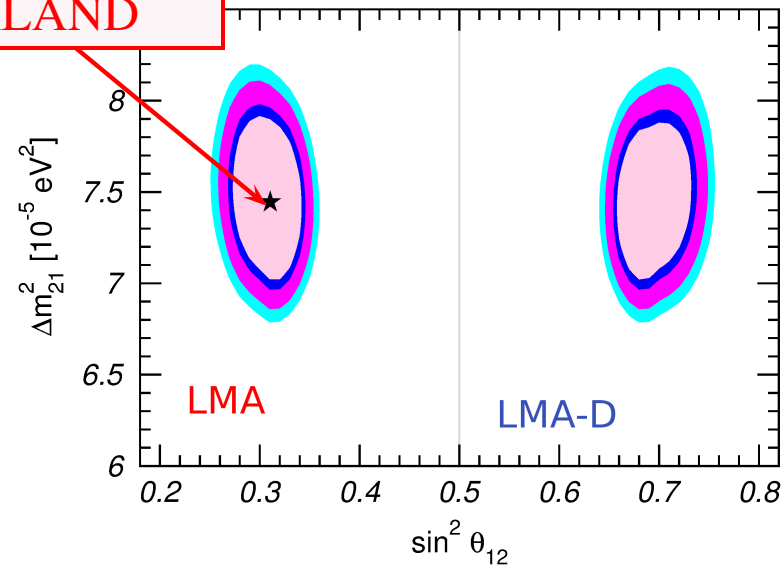
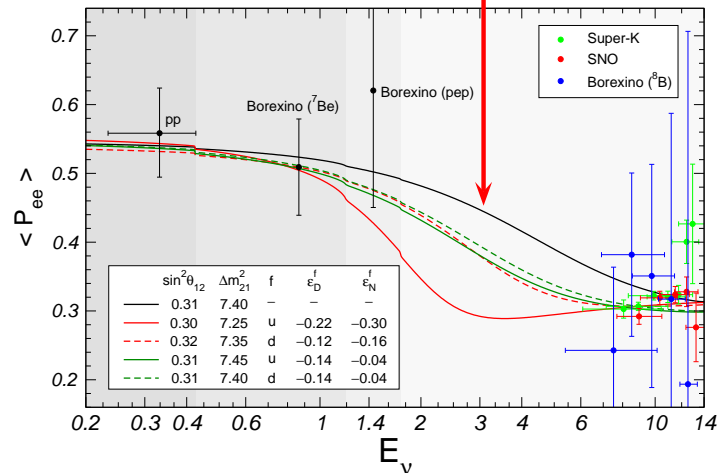
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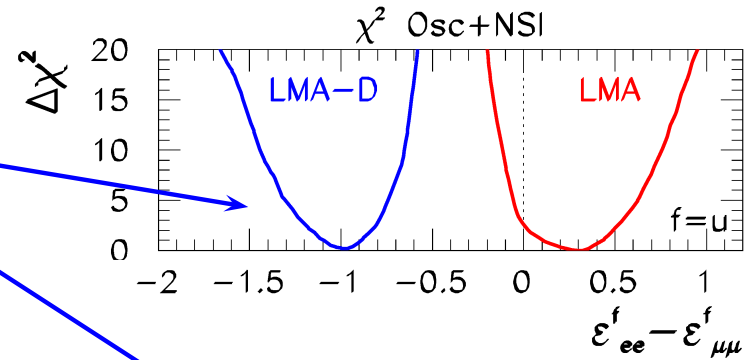
- Bounds $\mathcal{O}(1 - 10\%)$
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LMA: Improved fit to Solar+KamLAND



NSI: Bounds from Oscillation data

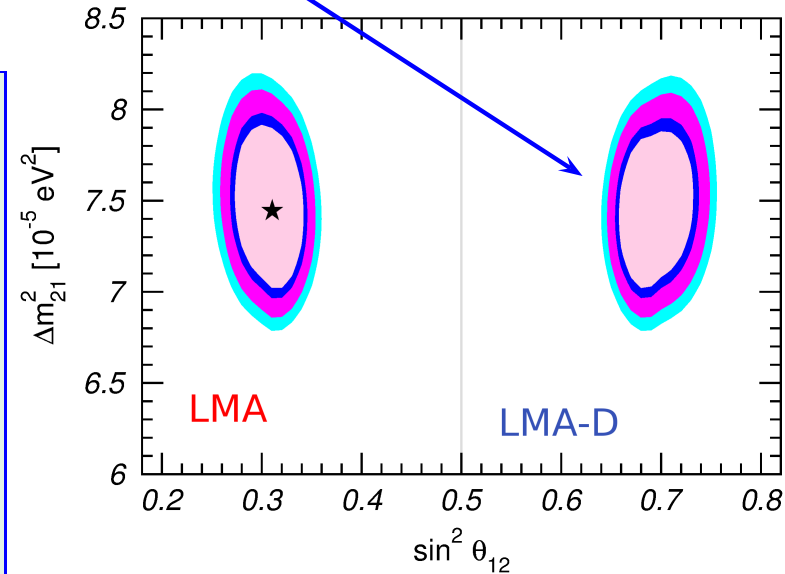
Param.	best-fit	90% CL	
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- Bounds $\mathcal{O}(1 - 10\%)$

Except $\epsilon_{ee}^u - \epsilon_{\mu\mu}^u$

Degenerate solution LMA-D ($\theta_{12} > 45^\circ$)
 Miranda, Tortola, Valle, hep-ph/0406280
 Cannot be resolved with osc-experiments
 Requires NC scattering experiments
 Coloma et al 1701.04828
 Requires NSI $\sim G_F$ (light mediators?)
 Farzan 1505.06906, and Shoemaker 1512.09147



Confirmed Low Energy Picture and MY List of Q&A

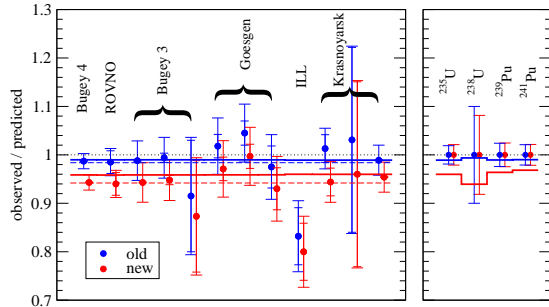
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But challenging model building
- **Only three light states?**

Beyond 3ν's: Light Sterile Neutrinos

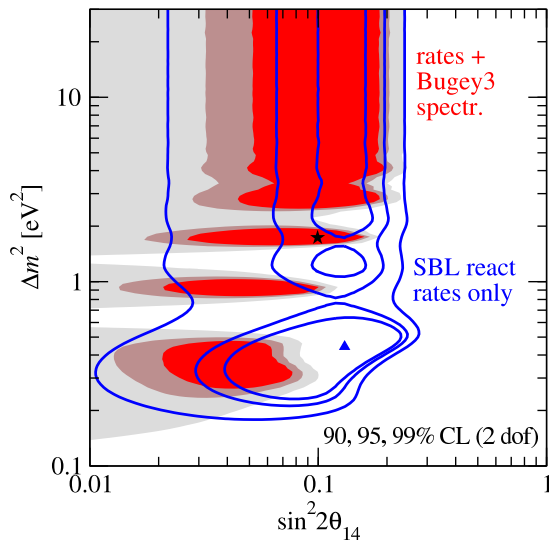
- Several Observations which can be Interpreted as Oscillations with $\Delta m^2 \sim eV^2$

Reactor Anomaly

New reactor flux calculation
 \Rightarrow Deficit in data at $L \lesssim 100$ m



Explained as ν_e disappearance

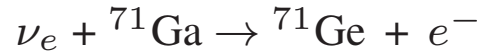


Kopp etal, ArXiv 1303.3011

Gallium Anomaly

Acero, Giunti, Laveder, 0711.4222
 Giunti, Laveder, 1006.3244

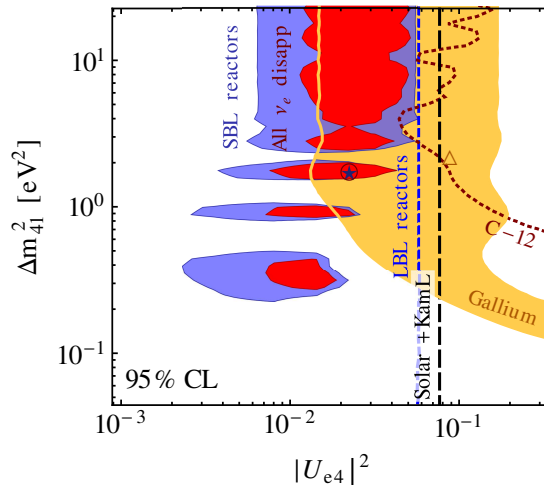
Radioactive Sources (^{51}Cr , ^{37}Ar)
 in calibration of Ga Solar Exp;



Give a rate lower than expected

$$R = \frac{N_{\text{obs}}}{N_{\text{Bahc}}^{\text{th}}} = 0.86 \pm 0.05 \quad (2.8\sigma)$$

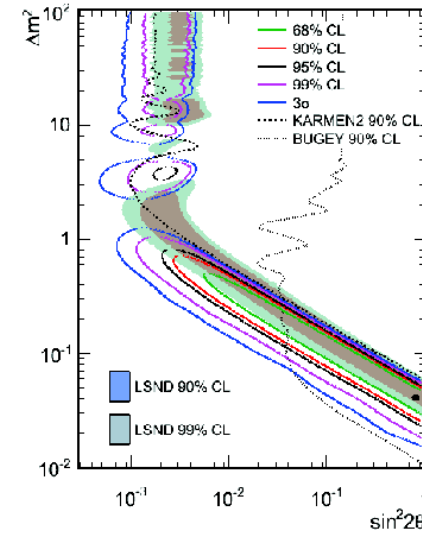
Explained as ν_e disappearance



Kopp etal, ArXiv 1303.3011

LSND, MiniBoone

$\nu_\mu \rightarrow \nu_e$ and $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$



Light Sterile Neutrinos

- These explanations require $3+N_s$ mass eigenstates $\rightarrow N_s$ sterile neutrinos

$\nu_e \rightarrow \nu_e$ **disapp** (REACT,Gallium,Solar, LSND/KARMEN)

- Problem: fit together $\nu_\mu \rightarrow \nu_e$ **app** (LSND,KARMEN,NOMAD,MiniBooNE,E776,ICARUS)

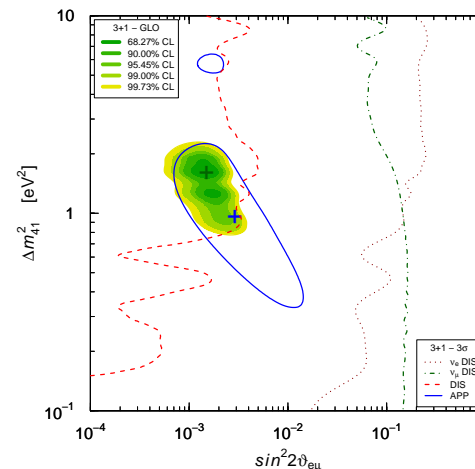
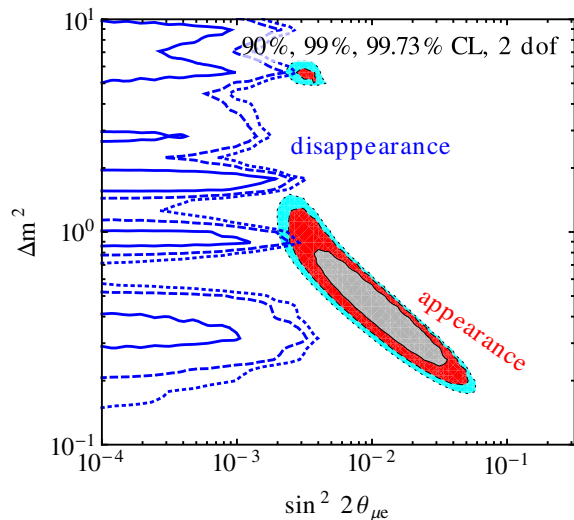
$\nu_\mu \rightarrow \nu_\mu$ **disapp** (CDHS,ATM,MINOS,ICECUBE)

- Generically: $P(\nu_e \rightarrow \nu_\mu) \sim |U_{ei}^* U_{\mu i}|$ [i =heavier state(s)]

But $|U_{ei}|$ constrained by $P(\nu_e \rightarrow \nu_e)$ disappearance data
 And $|U_{\mu i}|$ constrained by $P(\nu_\mu \rightarrow \nu_\mu)$ disappearance data } \Rightarrow **Severe tension**

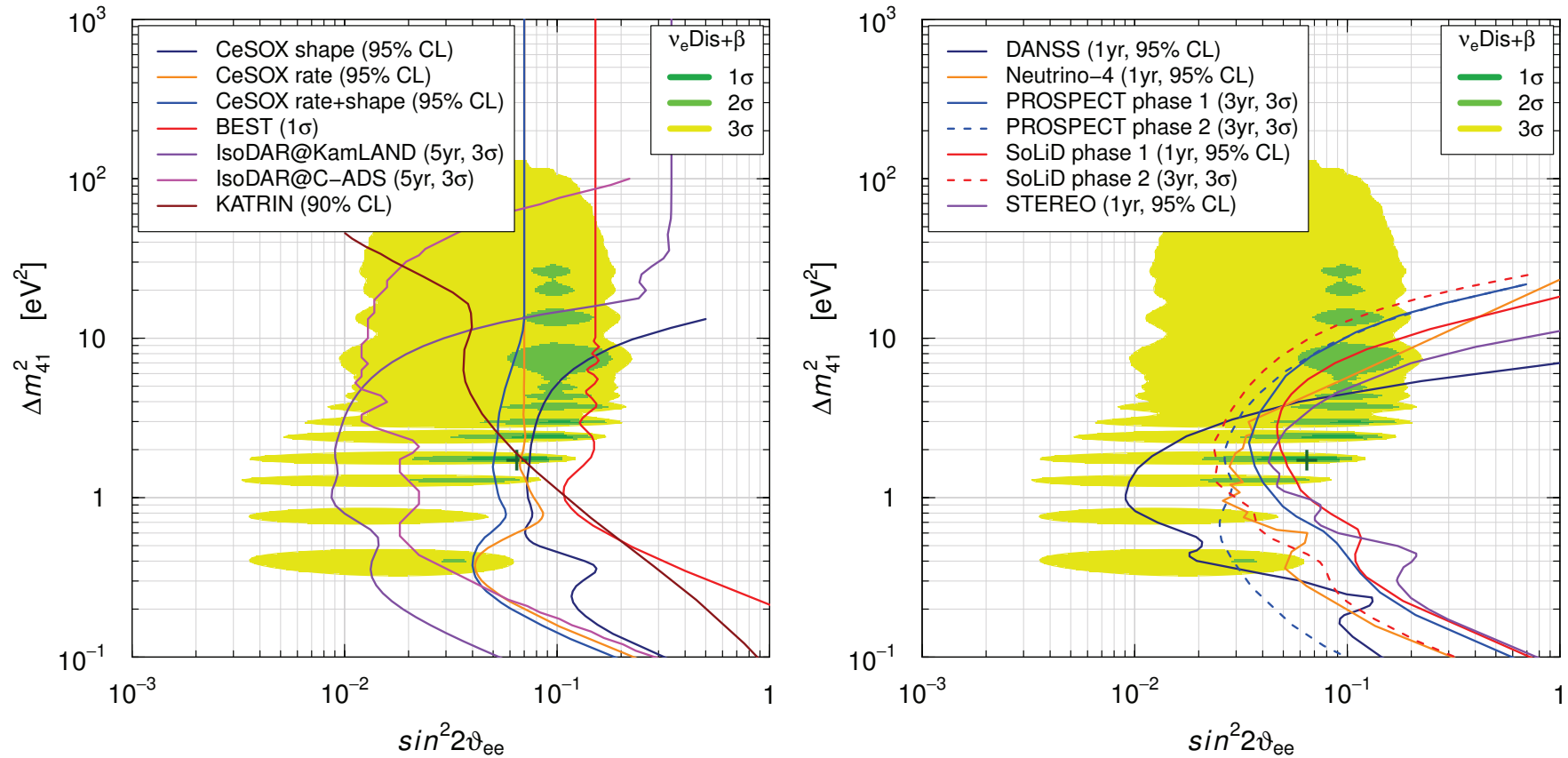
Kopp etal, ArXiv 1303.3011

Giunti etal, ArXiv 1308.5288



- New generation of ν_e disappearance experiments \Rightarrow adding to the tension

The Race for ν_e and $\bar{\nu}_e$ Disappearance



CeSOX (Gran Sasso, Italy) $^{144}\text{Ce} \rightarrow \bar{\nu}_e$
 BOREXINO: $L \simeq 5\text{-}12\text{m}$ [Vivier@TAUP2015]

BEST (Baksan, Russia) $^{51}\text{Cr} \rightarrow \nu_e$
 $L \simeq 5\text{-}12\text{m}$ [PRD 93 (2016) 073002]

IsoDAR@KamLAND (Kamioka, Japan)
 $^8\text{Li} \rightarrow \bar{\nu}_e$ $L \simeq 16\text{m}$ [arXiv:1511.05130]

IsoDAR@C-ADS (Guangdong, China)
 $^8\text{Li} \rightarrow \bar{\nu}_e$ $L \simeq 15\text{m}$ [JHEP 1601 (2016) 004]

DANSS (Kalinin, Russia) $L \simeq 10\text{-}12\text{m}$ [arXiv:1606.02896]

Neutrino-4 (RIAR, Russia) $L \simeq 6\text{-}11\text{m}$ [JETP 121 (2015) 578]

PROSPECT (ORNL, USA) $L \simeq 7\text{-}12\text{m}$ [arXiv:1512.02202]

SoLiD (SCK-CEN, Belgium) $L \simeq 5\text{-}8\text{m}$ [arXiv:1510.07835]

STEREO (ILL, France) $L \simeq 8\text{-}12\text{m}$ [arXiv:1602.00568]

KATRIN (Karlsruhe, Germany) $^3\text{H} \rightarrow \bar{\nu}_e$ [Drexlin@NOW2016]

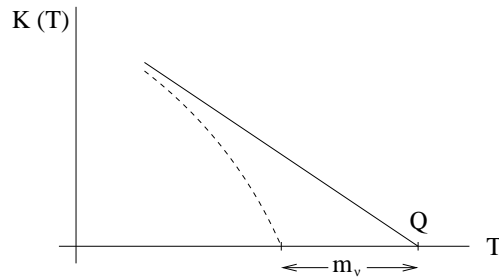
⇒ Fit with 3+N steriles severely disfavoured unless some data is dropped

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- **Other NP at play?** Large NSI interactions still allowed in ν oscillations
But challenging model building
- **Only three light states?**
Standing anomalies in app and disapp channels in severe tension with bounds
New results from ν_e disappearance further disfavour $\mathcal{O}(\text{eV}) \nu_s$ interpretation
- **Oscillations DO NOT** determine the **lightest mass**
- **Oscillations DO NOT** distinguish **Dirac/Majorana**

Neutrino Mass Scale: β Decay

Single β decay : Dirac or Majorana ν mass modify spectrum endpoint



$$m_{\nu_e}^2 = \sum m_j^2 |U_{ej}|^2 = c_{13}^2 c_{12}^2 m_1^2 + c_{13}^2 s_{12}^2 m_2^2 + s_{13}^2 m_3^2$$

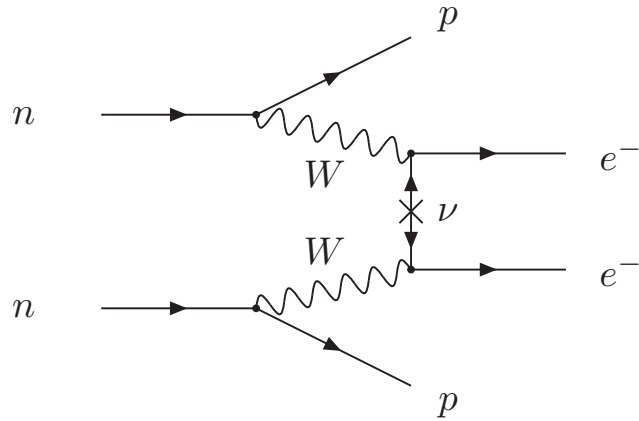
Present bound: $m_{\nu_e} \leq 2.2$ eV (at 95 % CL)

Katrin (201X????!!) Sensitivity to $m_{\nu_e} \sim 0.2$ eV

Purely kinematics \Rightarrow Only model independent probe ν -mass scale

Majorana or Dirac: $0\nu\beta\beta$ Decay

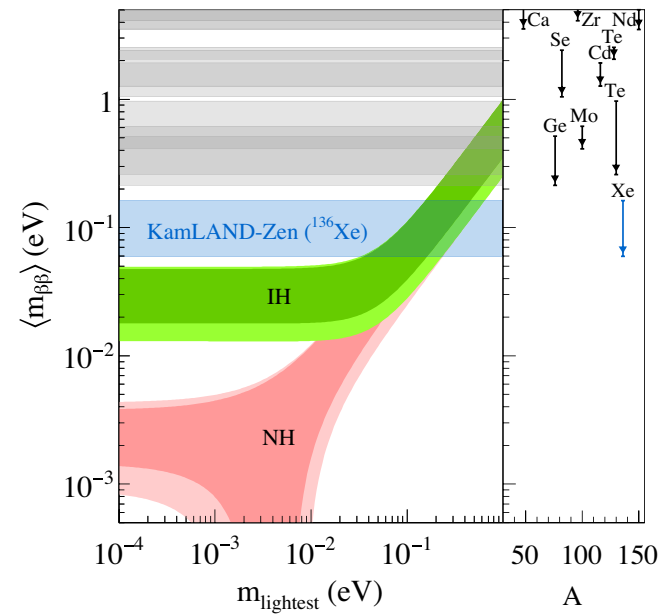
$0\nu\beta\beta \Rightarrow$ L violation \Leftrightarrow Majorana ν



If m_ν only source of ΔL

$$T_{1/2}^{0\nu} = \frac{m_e}{G_{0\nu} M_{\text{nucl}}^2 m_{ee}^2}$$

At present only bounds from ^{136}Xe (EXO and KamLAND-ZEN) ^{76}Ge (Gerda) and ^{130}Te (Cuore-0)



KamLAND-Zen Coll. ArXiv:1605.02889

$$m_{ee} \lesssim 0.061 - 0.165 \text{ (90\% CL)}$$

$$m_{ee} = \left| \sum U_{ej}^2 m_j \right|$$

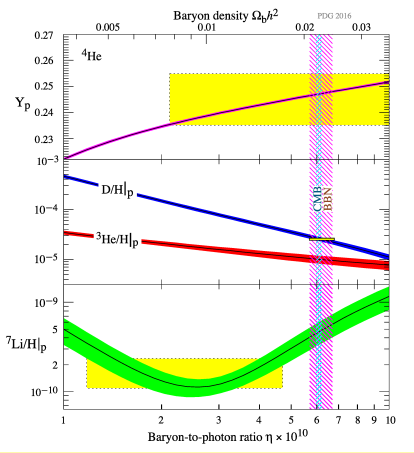
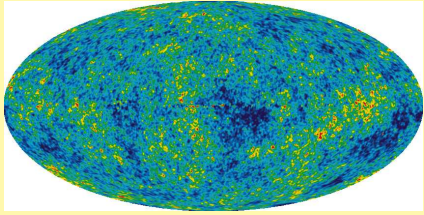
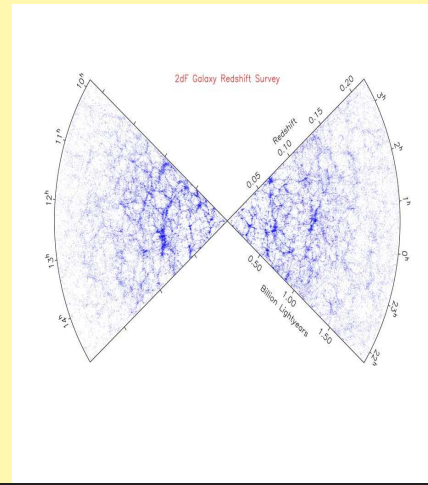
$$= \left| c_{13}^2 c_{12}^2 m_1 e^{i\eta_1} + c_{13}^2 s_{12}^2 m_2 e^{i\eta_2} + s_{13}^2 m_3 e^{-i\delta_{CP}} \right|$$

$$= f(m_\ell, \text{order, maj phases})$$

Light massive ν in Cosmology

Relic ν 's: Effects in several cosmological observations at several epochs

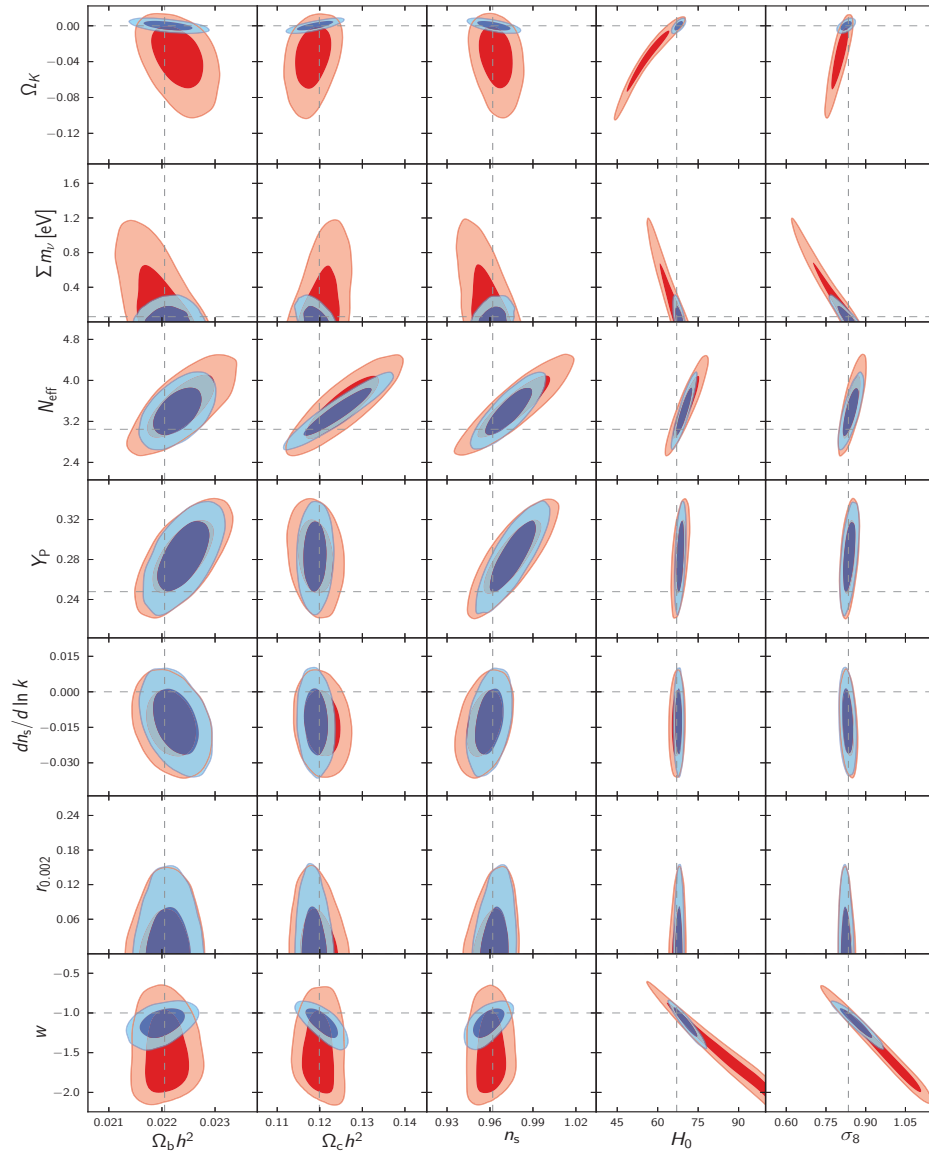
Mainly via two effects: $\rho_r = \left[1 + \frac{7}{8} \times \left(\frac{4}{11} \right)^{\frac{4}{3}} N_{\text{eff}} \right] \rho_\gamma$ and $\sum_i m_{\nu_i}$

		
<p>Primordial Nucleosynthesis BBN</p>	<p>Cosmic Microwave Background CMB</p>	<p>Large Scale Structure Formation LSS</p>
<p>$T \sim \text{MeV}$</p>	<p>$T \lesssim \text{eV}$</p>	
<p>Number of ν's (N_{eff})</p>	<p>N_{eff} and $\sum m_\nu$</p>	

BUT: Observables also depend on all other cosmo parameters (and assumptions)

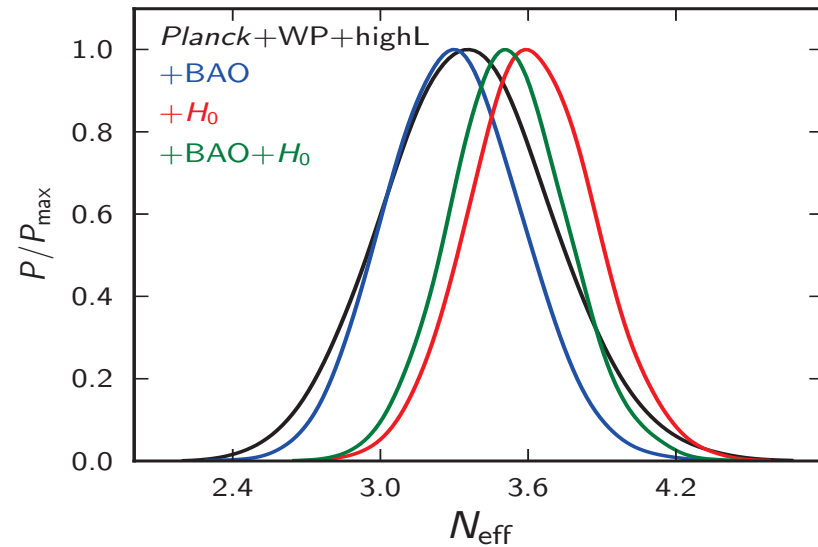
Example: Cosmological Analysis by Planck

arXiv:1502.01589

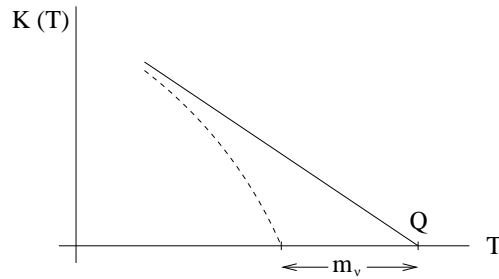


Range of Bounds in Λ CDM

Model	Observables	Σm_ν (eV) 95%
Λ CDM + m_ν	Planck TT + lowP	≤ 0.72
Λ CDM + m_ν	Planck TT + lowP + lensing	≤ 0.68
Λ CDM + m_ν	Planck TT,TE,EE + lowP+lensing	≤ 0.59
Λ CDM + m_ν	Planck TT,TE,EE + lowP	≤ 0.49
Λ CDM + m_ν	Planck TT + lowP + lensing + BAO + SN + H_0	≤ 0.23
Λ CDM + m_ν	Planck TT,TE,EE + lowP+ BAO	≤ 0.17



Single β decay : Dirac or Majorana ν mass modify spectrum endpoint

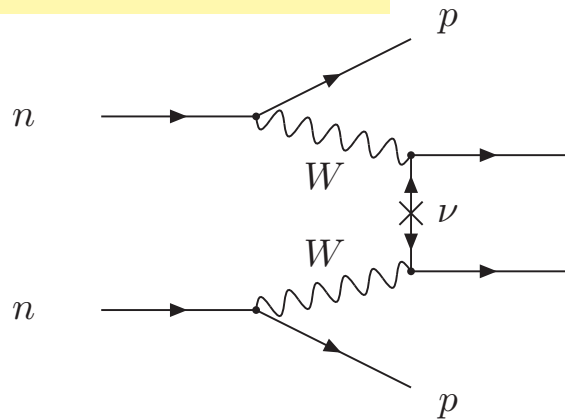


$$m_{\nu_e}^2 = \sum m_j^2 |U_{ej}|^2 = \begin{cases} \text{NO} : m_\ell^2 + \Delta m_{21}^2 c_{13}^2 s_{12}^2 + \Delta m_{31}^2 s_{13}^2 \\ \text{IO} : m_\ell^2 + \Delta m_{21}^2 c_{13}^2 s_{12}^2 - \Delta m_{31}^2 c_{13}^2 \end{cases}$$

Present bound: $m_{\nu_e} \leq 2.2 \text{ eV}$ (at 95 % CL)

Katrin (20XX???) Sensitivity to $m_{\nu_e} \sim 0.2 \text{ eV}$

ν -less Double- β decay: \Leftrightarrow Majorana ν 's



If m_ν only source of ΔL $T_{1/2}^{0\nu} = \frac{m_e}{G_{0\nu} M_{\text{nucl}}^2 m_{ee}^2}$

$$m_{ee} = \left| \sum U_{ej}^2 m_j \right|$$

$$= \left| c_{13}^2 c_{12}^2 m_1 e^{i\eta_1} + c_{13}^2 s_{12}^2 m_2 e^{i\eta_2} + s_{13}^2 m_3 e^{-i\delta_{CP}} \right|$$

$$= f(m_\ell, \text{order, maj phases})$$

Present Bounds: $m_{ee} < 0.06 - 0.76 \text{ eV}$

COSMO for Dirac or Majorana m_ν affect growth of structures

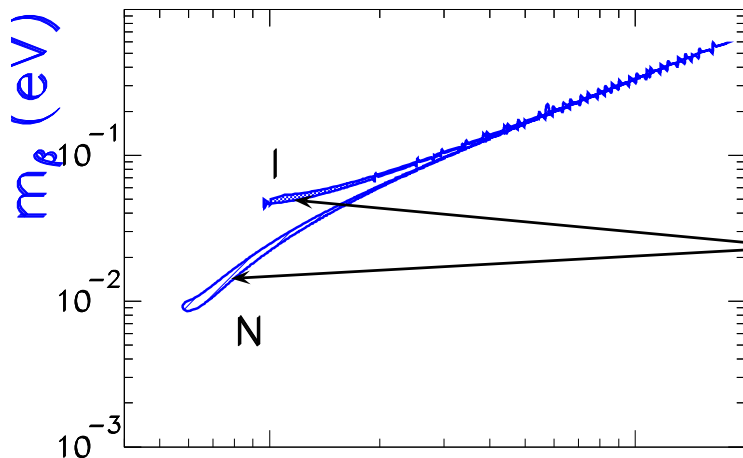
$$\sum m_i = \begin{cases} \text{NO} : \sqrt{m_\ell^2} + \sqrt{\Delta m_{21}^2 + m_\ell^2} + \sqrt{\Delta m_{31}^2 + m_\ell^2} \\ \text{IO} : \sqrt{m_\ell^2} + \sqrt{-\Delta m_{31}^2 - \Delta m_{21}^2 - m_\ell^2} + \sqrt{-\Delta m_{31}^2 - m_\ell^2} \end{cases}$$

Neutrino Mass Scale: The Cosmo-Lab Connection

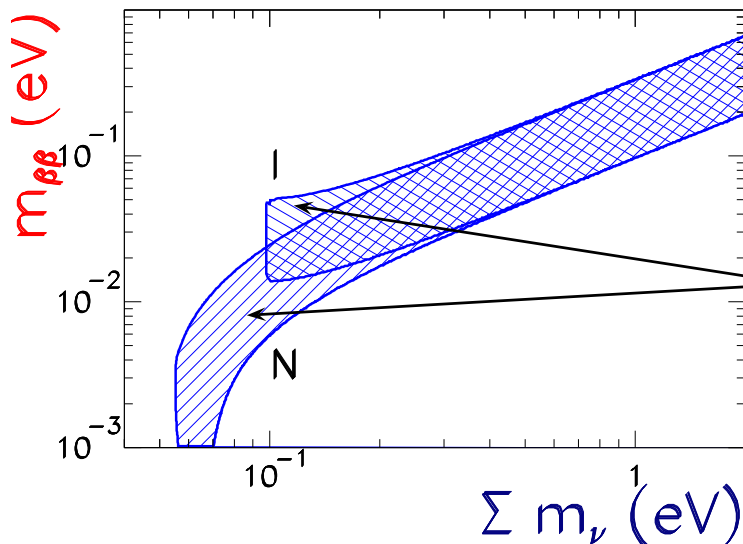
Global oscillation analysis

⇒ Correlations m_{ν_e} , m_{ee} and $\sum m_\nu$
(Fogli *et al* (04))

Nufit (95%)



Width due to range in oscillation parameters very narrow
Lower bound on $\sum m_i$ depends on ordering



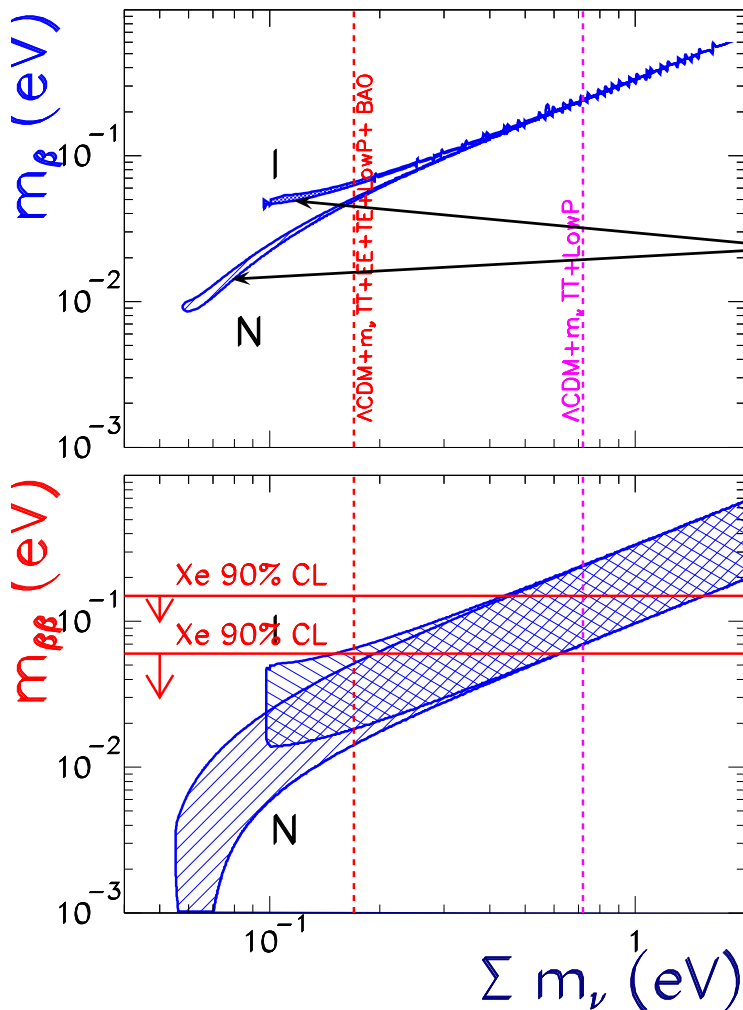
Wide band due to unknown Majorana phases ⇒
Possible Det of Maj phases?

Neutrino Mass Scale: The Cosmo-Lab Connection

Global oscillation analysis

⇒ Correlations m_{ν_e} , m_{ee} and $\sum m_i$
(Fogli *et al* (04))

Nufit (95%)



Lower bound on $\sum m_i$ depends on ordering

Precision determination/bound of $\sum m_i$ can give information on ordering ?

Hannestad, Schwetz 1606.04691, Simpson *et al* 1703.03425, Capozzi *et al* 1703.04471 ...

Or much ado about nothing?

Cosmo data will only add to N/I likelihood when accuracy on $\sum m_{\nu}$ better than 0.02 eV (to see a 2σ N/I difference between 0.06 and 0.1)

Hannestad, Schwetz 1606.04691

Confirmed Low Energy Picture and MY List of Q&A

- At least **two** neutrinos **are massive** \Rightarrow **There is NP**
- **Three mixing angles** are non-zero (and relatively **large**) \Rightarrow very **different from CKM**
- **Leptonic CP**: Best fit $J_{\text{Lep,CP}} = -0.033$. CP conservation at 70% CL
Significance likely to grow slowly with present experiments
- **Ordering**: No significant preference in our global fit
Requires new oscillation experiments
- **Other NP at play?** Large NSI interactions still allowed in ν oscillations
But challenging model building
- **Only three light states?**
Standing anomalies in app and disapp channels in severe tension with bounds
New results from ν_e disappearance further disfavour $\mathcal{O}(\text{eV}) \nu_s$ interpretation
- **Oscillations DO NOT determine the** lightest mass
Only model independent probe of m_ν **β decay**: $\sum m_i^2 |U_{ei}|^2 \leq (2.2 \text{ eV})^2$
Anxiously waiting for Katrin
- **Dirac or Majorana?**: We do not know, *anxiously* waiting for ν -less $\beta\beta$ decay
- **Cosmological effects?**: Still missing a “signal” and will we ever be convinced it is $\nu' s$?

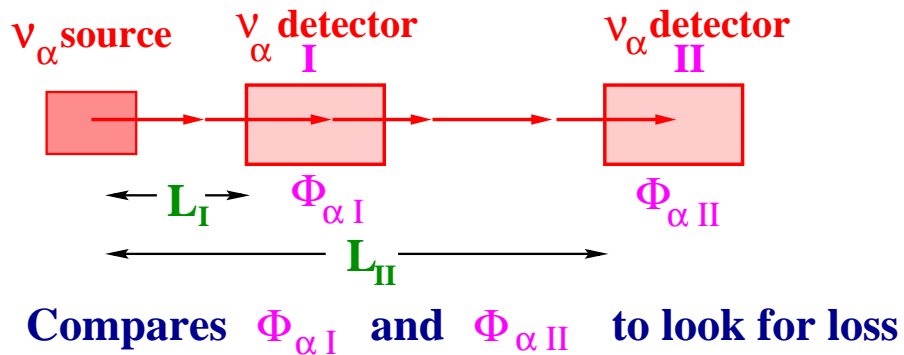
THANK YOU

Back-up Slides

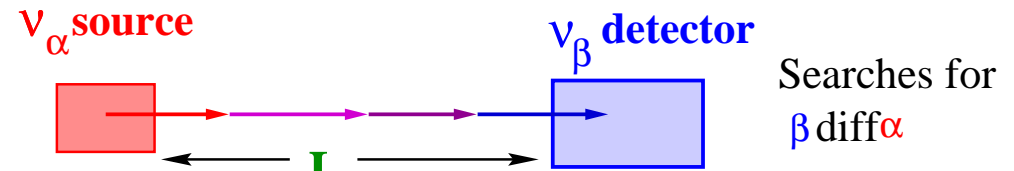
ν Oscillations: Experimental Probes

- Generically there are two types of experiments to search for ν oscillations :

Disappearance Experiment



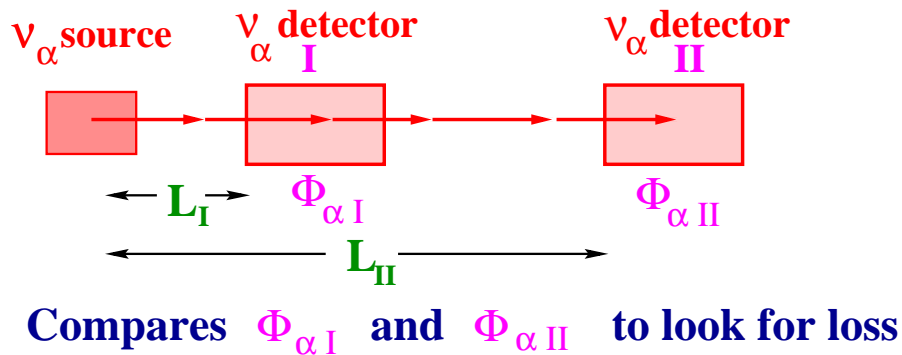
Appearance Experiment



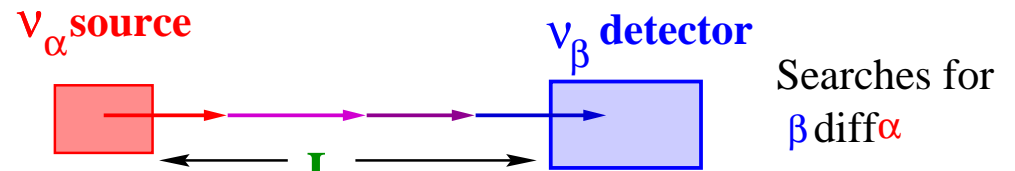
ν Oscillations: Experimental Probes

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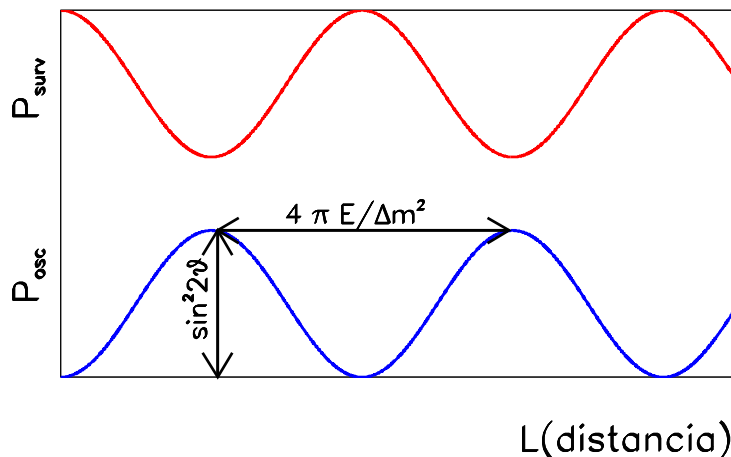
Disappearance Experiment



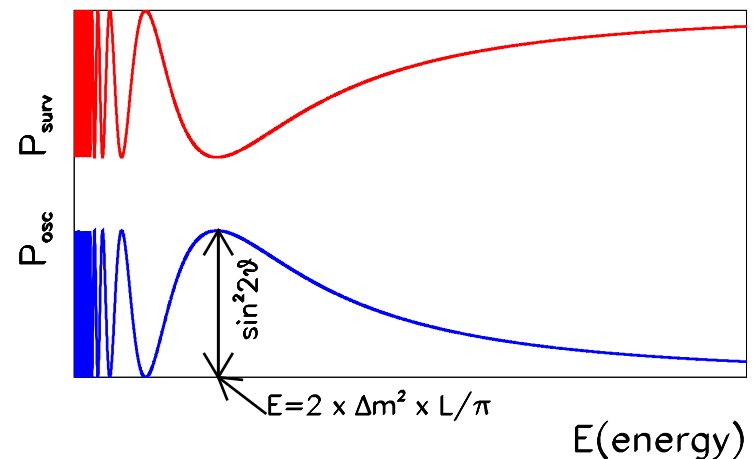
Appearance Experiment



- To detect **oscillations** we can study **the neutrino flavour** as function of the **Distance** to the source



- As function of the neutrino **Energy**



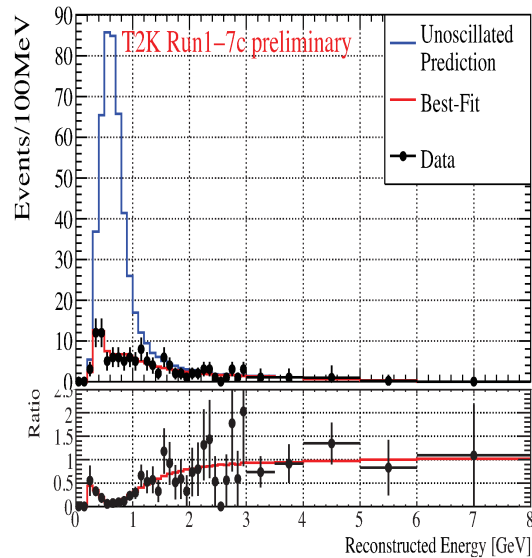
3 ν Analysis: θ_{23}

- Best determined in ν_μ and $\bar{\nu}_\mu$ disappearance in LBL

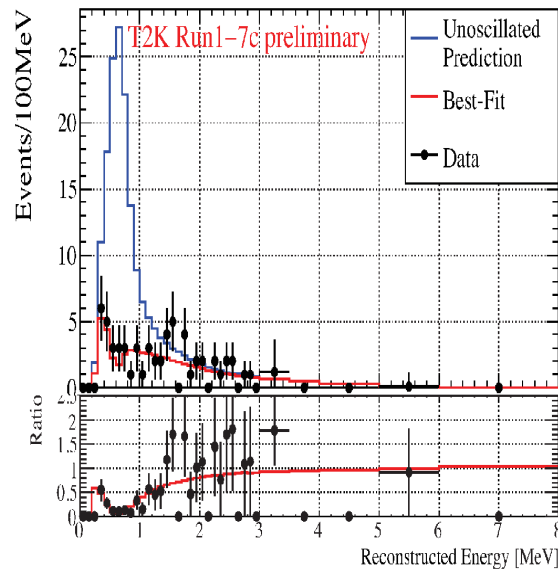
$$P_{\mu\mu} \simeq 1 - (c_{13}^4 \sin^2 2\theta_{23} + s_{23}^2 \sin^2 2\theta_{13}) \sin^2 \left(\frac{\Delta m_{31}^2 L}{4E} \right) + \mathcal{O}(\Delta m_{21}^2)$$

- At osc maximum $\sin^2 \left(\frac{\Delta m_{31}^2 L}{4E} \right) = 1 \Rightarrow P_{\mu\mu} \simeq 0$ for $\theta_{23} \simeq \frac{\pi}{4}$

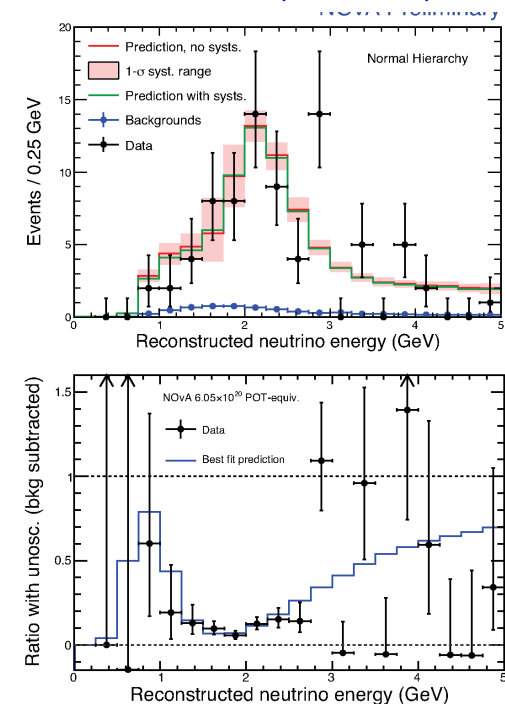
T2K $\nu_\mu \rightarrow \nu_\mu$



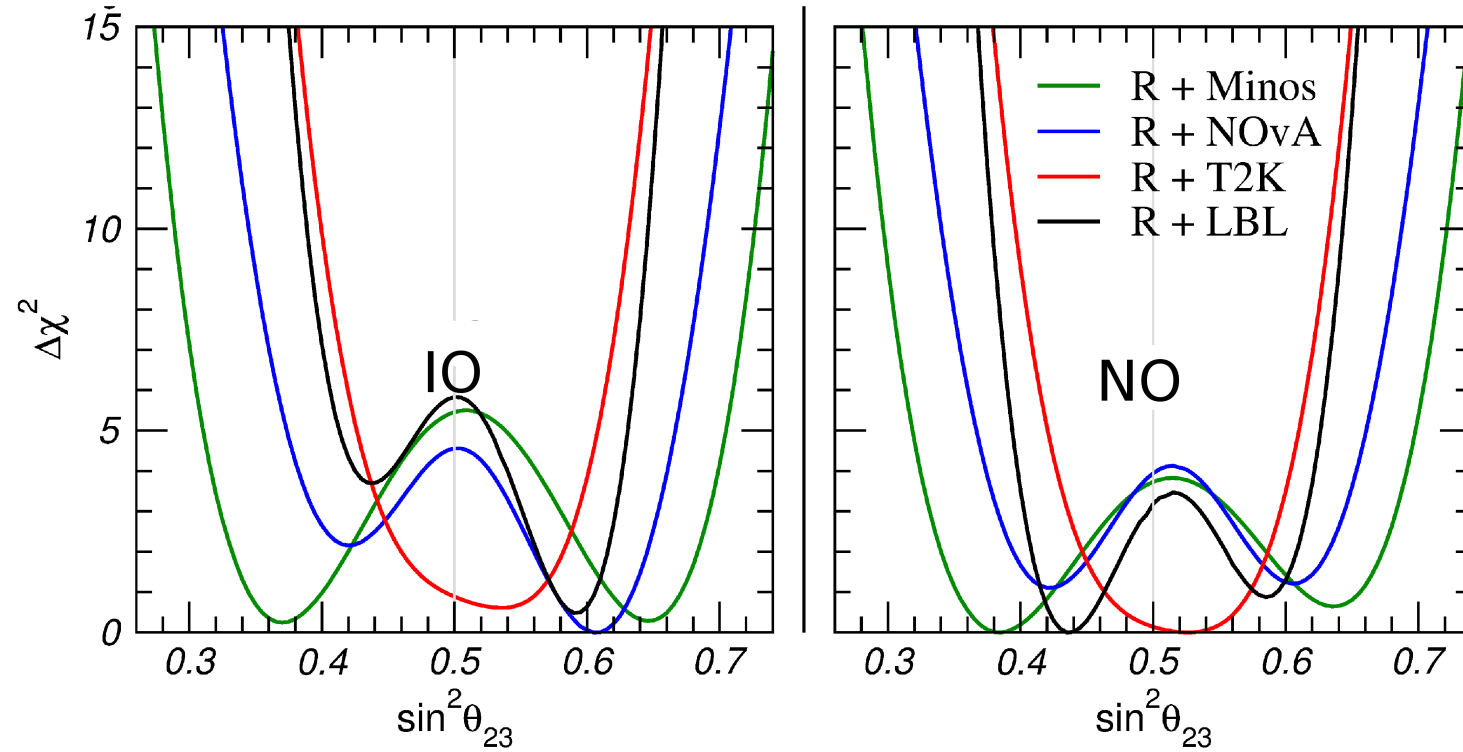
T2K $\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu$



NOvA $\nu_\mu \rightarrow \nu_\mu$



Ordering and θ_{23}



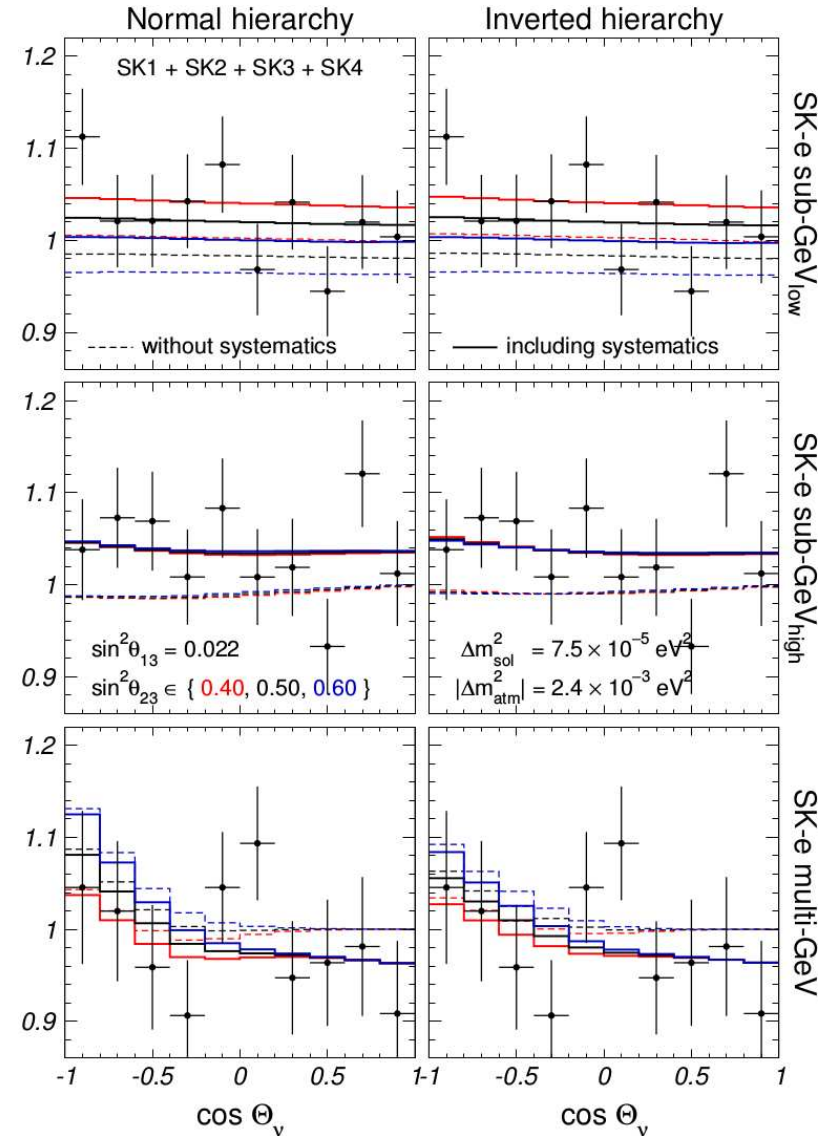
- Favoured Octant of θ_{23} depends on ordering – CL of maximal mixing at 91%(NO) 98% (IO)

3 ν Analysis: Ordering, δ_{CP} in ATM

- For $\theta_{31} \neq 0$ ATM sensitivity to octant θ_{23} & ordering & δ_{CP}

$$\begin{aligned} \frac{N_e}{N_e^0} - 1 &\simeq (\bar{r} c_{23}^2 - 1) P_{2\nu}(\Delta m_{21}^2, \theta_{12}) \quad [\Delta m_{21}^2 \text{ term}] \\ &+ (\bar{r} s_{23}^2 - 1) P_{2\nu}(\Delta m_{31}^2, \theta_{13}) \quad [\theta_{13} \text{ term}] \\ &- 2\bar{r} s_{13} s_{23} c_{23} \text{Re}(A_{ee}^* A_{\mu e}) \quad [\delta_{CP} \text{ term}] \end{aligned}$$

$$\bar{r} \equiv \Phi_\mu^0 / \Phi_e^0 \simeq 2(\text{subG}), 2.6\text{--}4.6(\text{multiG})$$

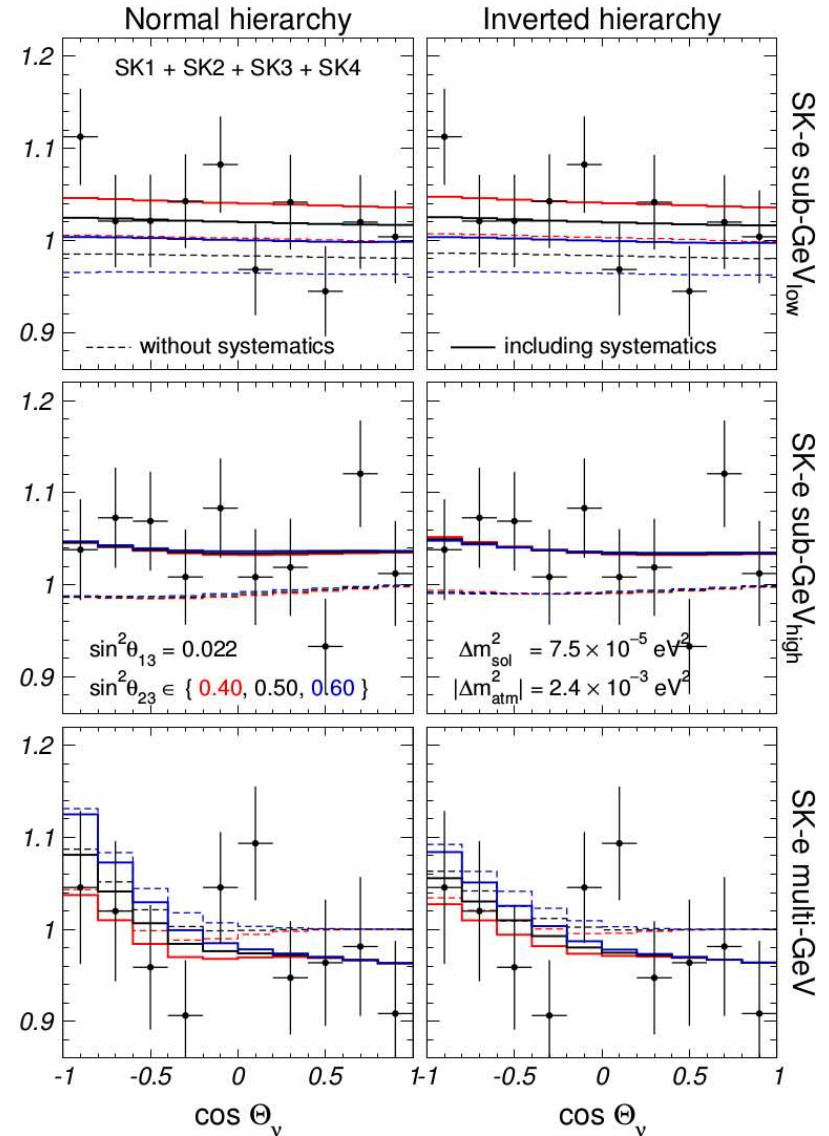
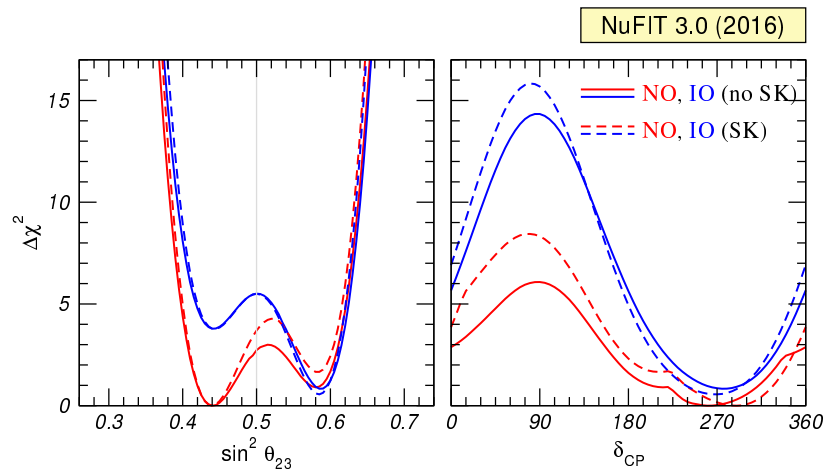


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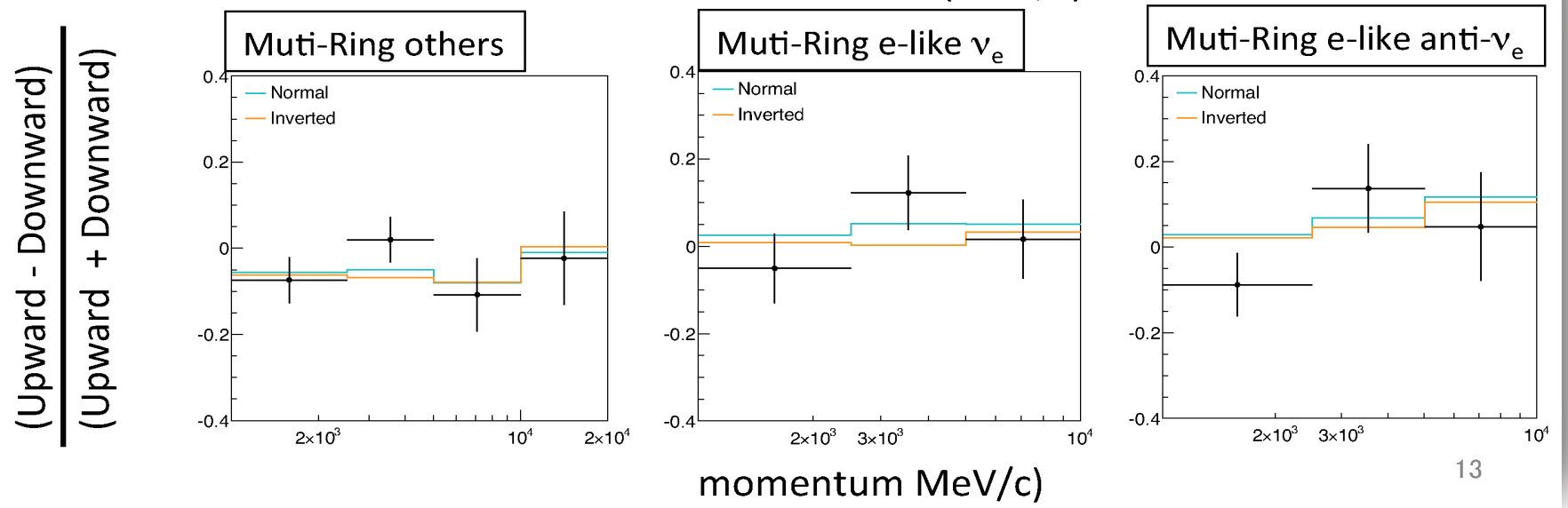
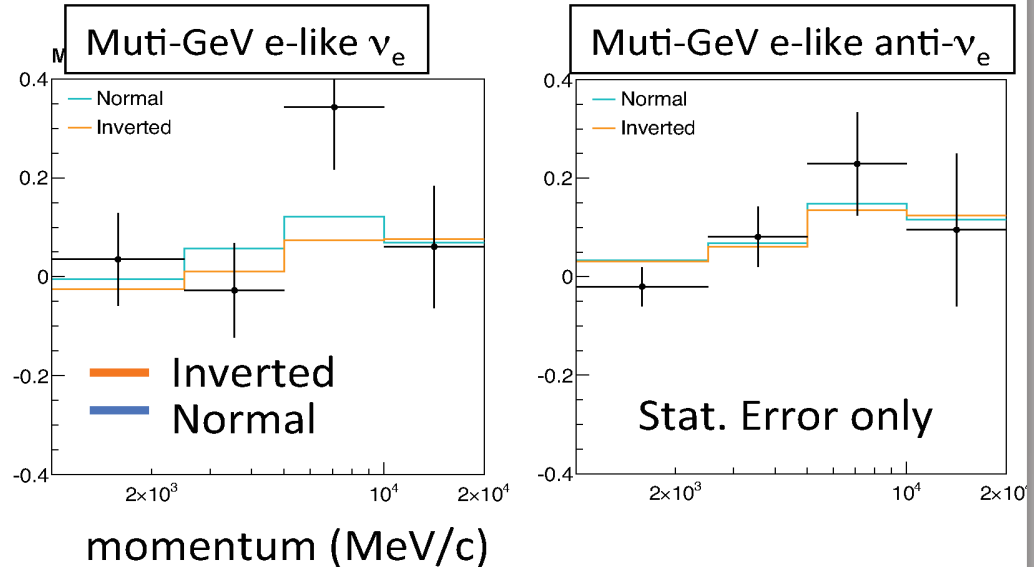
$$\begin{aligned} \frac{N_e}{N_e^0} - 1 &\simeq (\bar{r} c_{23}^2 - 1) P_{2\nu}(\Delta m_{21}^2, \theta_{12}) \quad [\Delta m_{21}^2 \text{ term}] \\ &+ (\bar{r} s_{23}^2 - 1) P_{2\nu}(\Delta m_{31}^2, \theta_{13}) \quad [\theta_{13} \text{ term}] \\ &- 2\bar{r} s_{13} s_{23} c_{23} \text{Re}(A_{ee}^* A_{\mu e}) \quad [\delta_{CP} \text{ term}] \end{aligned}$$

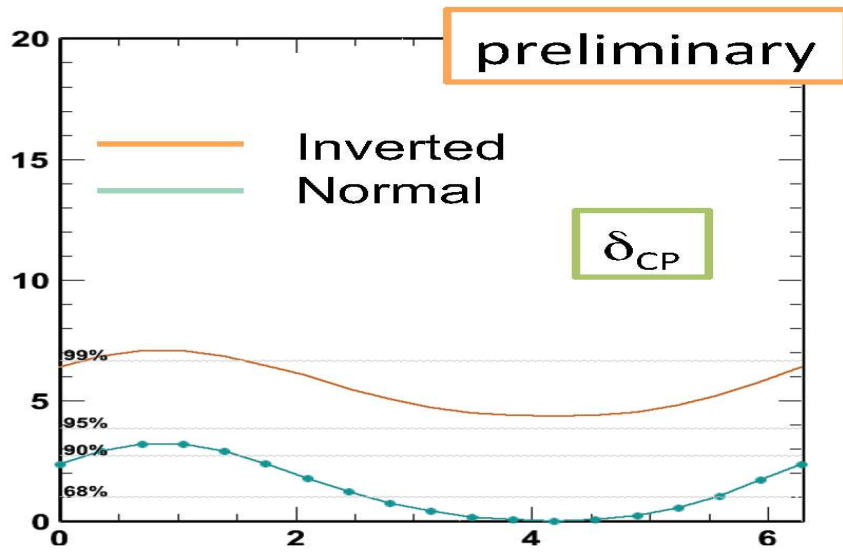
$$\bar{r} \equiv \Phi_\mu^0 / \Phi_e^0 \simeq 2(\text{subG}), 2.6\text{--}4.6(\text{multiG})$$



- **Normal** hierarchy favored at:
 - $\chi^2_{NH} - \chi^2_{IH} = -4.3$
(-3.1 expected)
- Driven by excess of **upward-going e-like events**:
 - Primarily in SK-IV data
 - consistent with the effects of θ_{13} driven ν oscillation.

Upward/Downward asymmetry in energetic electron samples (ν_e /anti- ν_e enriched)

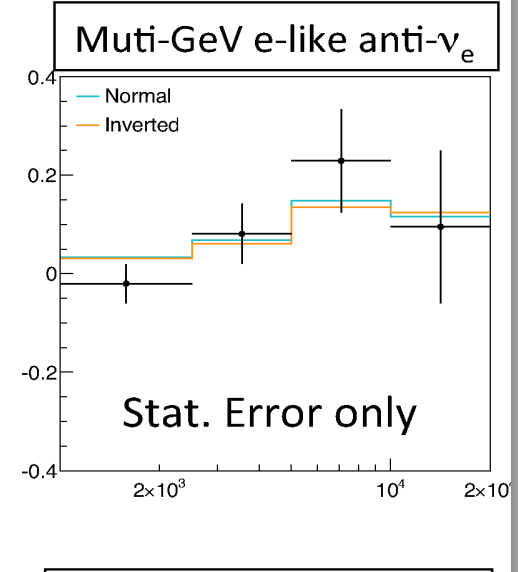
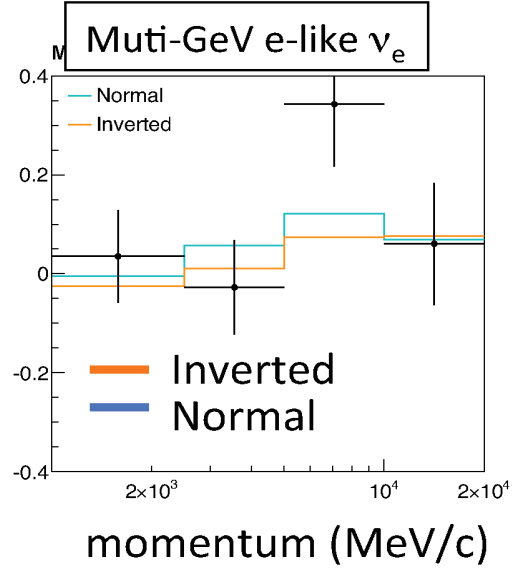




preliminary

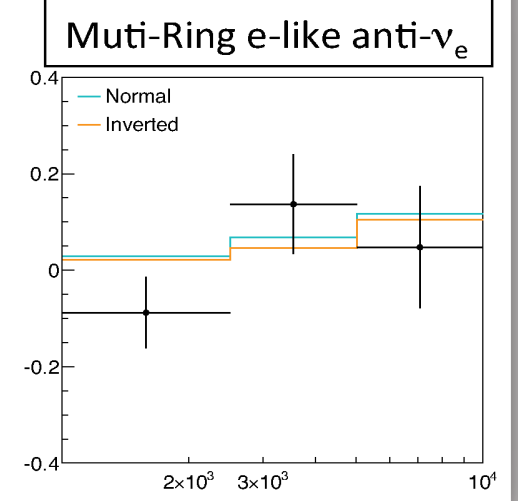
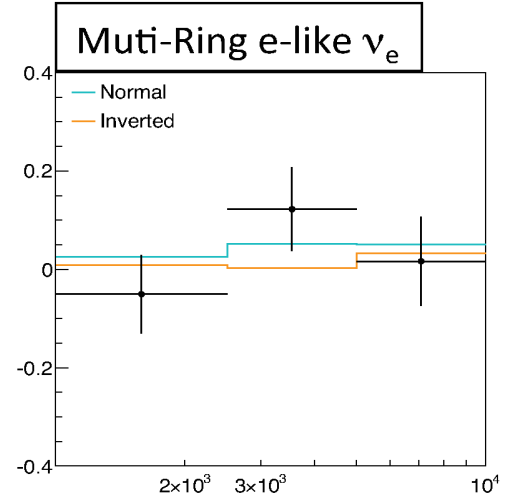
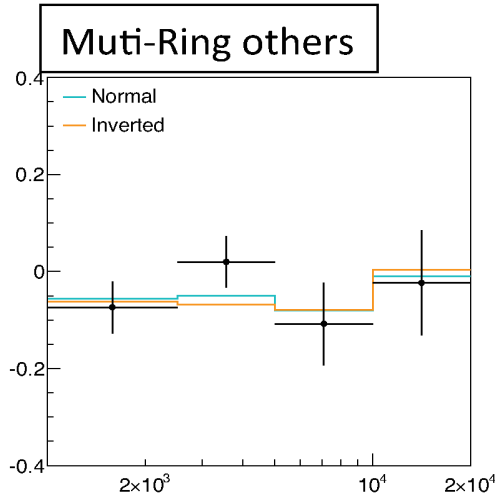
Upward/Downward asymmetry in energetic electron samples (νe/anti-νe enriched)

- consistent with the effects of θ_{13} driven ν oscillation.



Stat. Error only

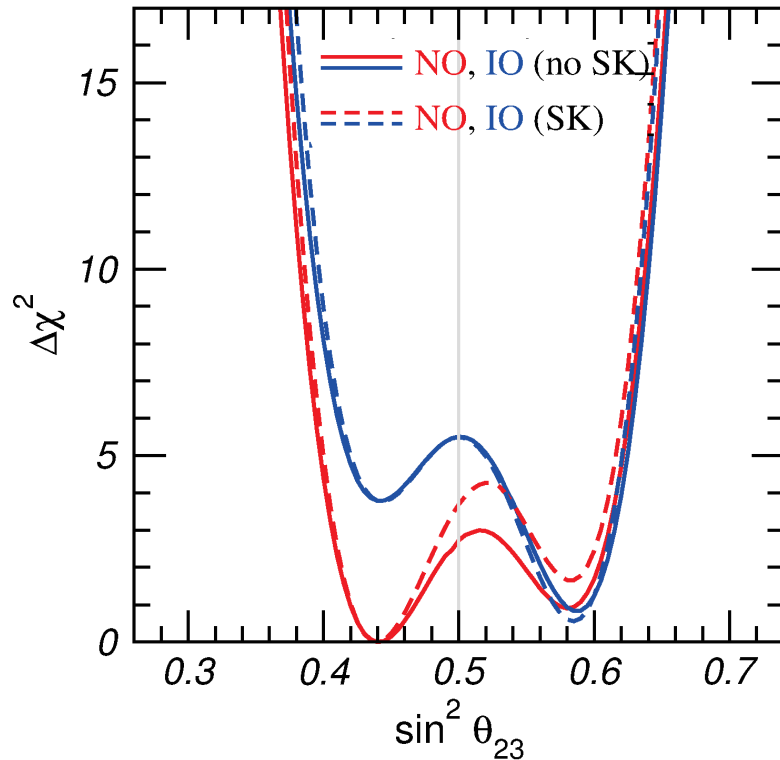
(Upward - Downward)
|
(Upward + Downward)



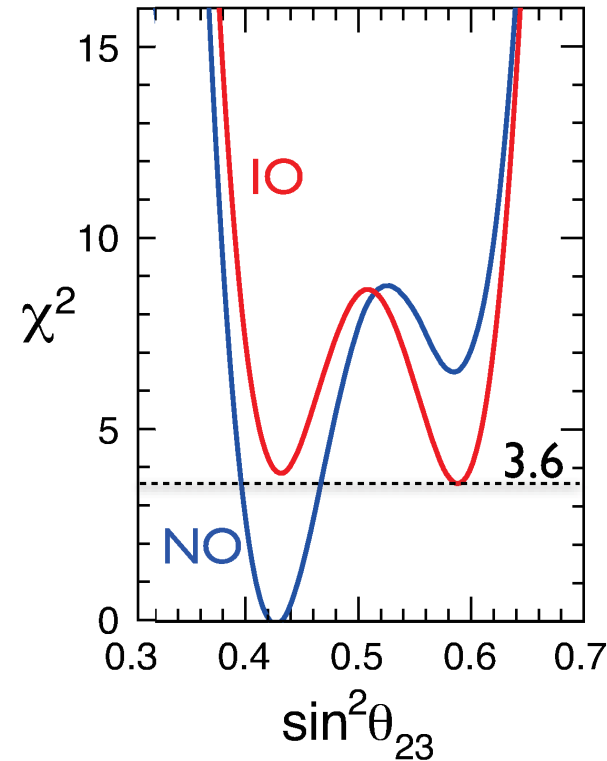
momentum MeV/c

Comparison with Bari group

NuFIT 3.0, Esteban et al., 1611.01514



Cappozzi et al., 1703.04471



Main Difference in ATM sensitivity

Both groups use the same reduced number of atm data subsamples

Using these data subsamples SK never found a $\theta_{13} \neq 0$ effect

Figure display “borrowed” from T. Schwetz Moriond 17 talk

Lepton Mixing Unitarity

- Previous results assume U_{LEP} to be unitary
- If ν_L mixed with m extra states $U_{\text{LEP}} = (K_l, K_h)$ Schechter, Valle (1980)
And $U_{\text{LEP}} U_{\text{LEP}}^\dagger = I_{3 \times 3}$ but in general $U_{\text{LEP}}^\dagger U_{\text{LEP}} \neq I_{(3+m) \times (3+m)}$
- If m states are heavy ($M \gg E_\nu$) oscillations measure K_L (not unitary)

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- If m states are heavy ($M \gg E_\nu$) oscillations measure $K_L, 3 \times 3$ (not unitary)

Flavour Changing Neutral Currents

- But this **unitarity violation** \Rightarrow Flavour Violation in Charged Lepton Processes
Universality Violation of Charge Current ...

- Constraints on these processes limit leptonic unitarity violation to

$$|K_l K_l^\dagger| = \begin{pmatrix} 0.9979 - 0.9998 & < 10^{-5} & < 0.0021 \\ < 10^{-5} & 0.9996 - 1.0 & < 0.0008 \\ < 0.0021 & < 0.0008 & 0.9947 - 1.0 \end{pmatrix}$$

Antusch *et al* ArXiv:1407.6607

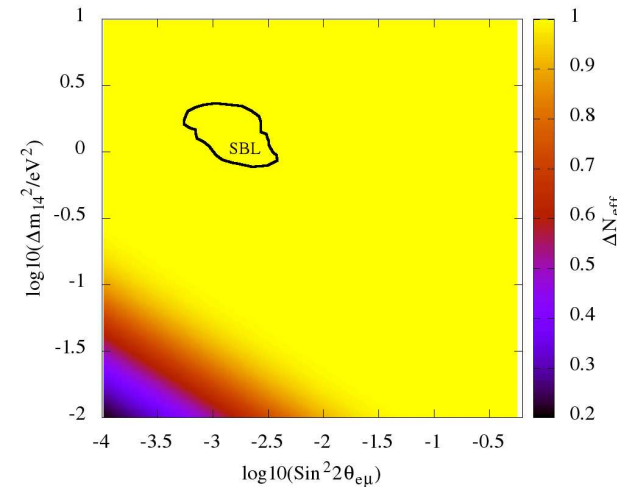
or equivalently $K_l \simeq (I + \epsilon)U(\theta_{ij}, \delta, \eta_i)$ with $|\epsilon_{\alpha j}| \leq \text{few} \times 10^{-3}$ while $K_h \sim \mathcal{O}(\epsilon)$

One light ν_s mixed with 3 ν'_a s contributes to ρ as N_{eff} .

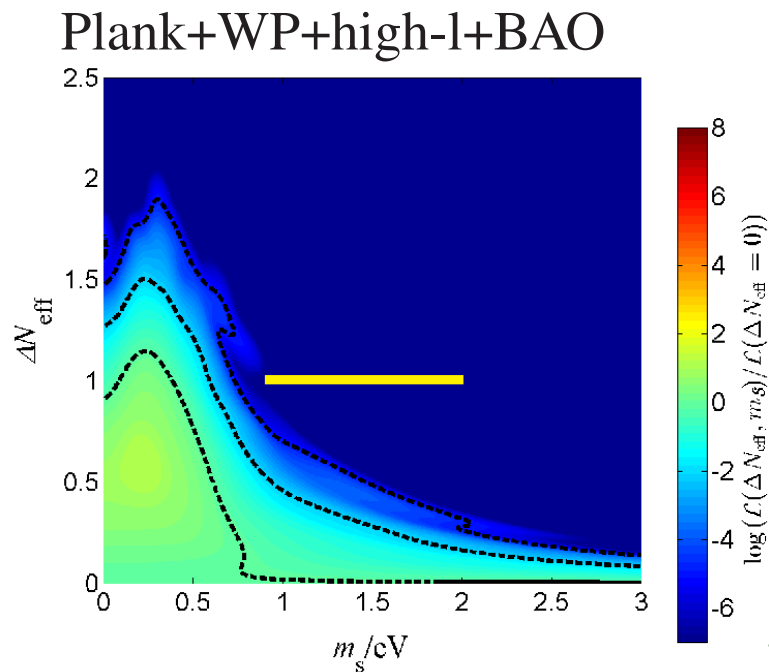
From evol eq for 3 + 1 ensemble one finds

⇒ So if “explanation” to SBL anomalies

1 ν_s contributes as much as 1 ν_a



But analysis of cosmo data in $\Lambda\text{CDM} + r + \nu_s$ tells us



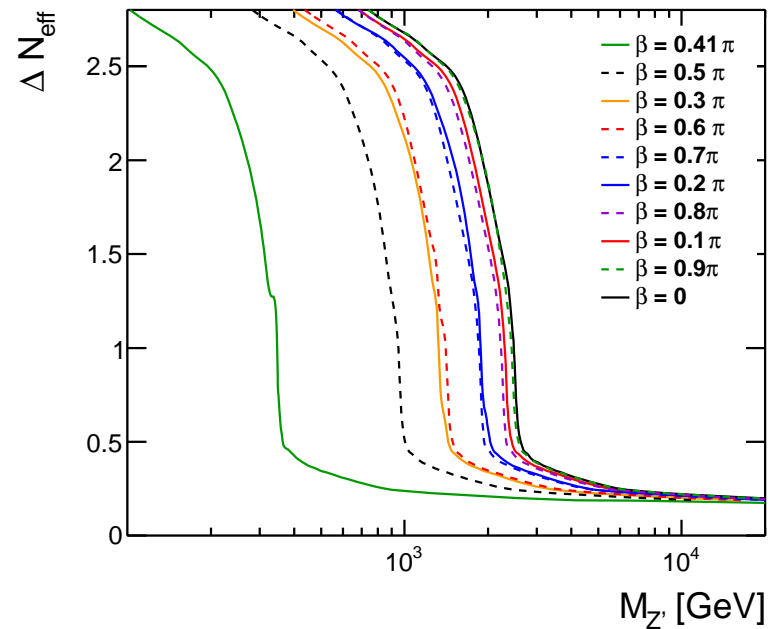
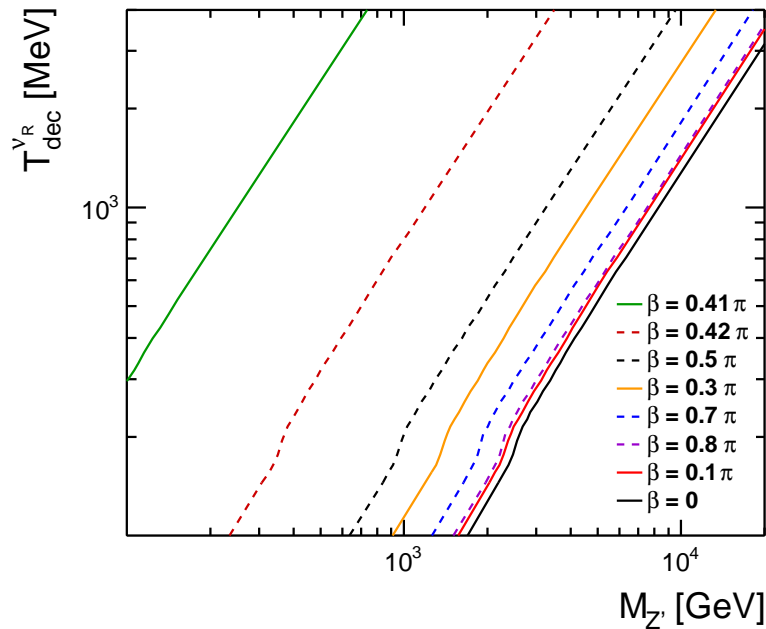
Light Sterile ν' s in Cosmology and New Interactions

- In string inspired E_6 models, 3 light ν_R 's with new interactions

$$(Z' \text{ with coupling } Y_{Z'}^{\nu_R} = \cos \beta \frac{5}{\sqrt{40}} - \frac{1}{\sqrt{24}} \sin \beta)$$

- In these scenarios $\Delta N_{\text{eff}} = 3 \times \left(\frac{T_{\nu_R}}{T_{\nu_L}} \right)^4 = 3 \times \left(\frac{g(T_{\nu_R}^{\text{dec}})}{g(T_{\nu_L}^{\text{dec}})} \right)^{\frac{4}{3}}$

Determined by $\sigma(\bar{\nu}_R \nu_R \rightarrow \bar{f} f)$ mediated by Z' (ie $M_{Z'}$ and coupling parameter β)



A. Solaguren-Beascoa, MCG-G

arXiv:1210.6350

\Rightarrow Interplay between cosmological determination of ΔN_{eff} and Z' LHC searches