

# Top Quark Physics in ep Scattering

**Christian Schwanenberger**

**Deutsches Elektronensynchrotron (DESY)**  
on behalf of top/BSM LHeC/FCC–he study group



**2<sup>nd</sup> FCC Physics Workshop**  
**18 January 2018**

# Outline

**Introduction**  
**CC Top Production**  
**NC Top Production**  
**BSM Top Production**  
**Conclusions**

# Outline

## Introduction

CC Top Production

NC Top Production

BSM Top Production

Conclusions

# Linac–Ring Collider, LHeC and FCC–eh

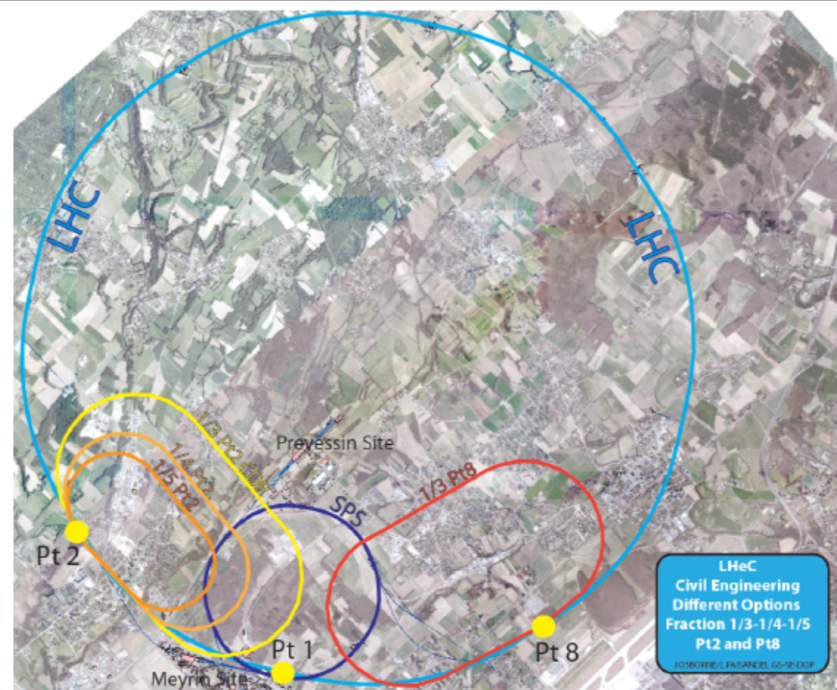
## Energy Recovering Linac

$e^\pm$  beam: 60 GeV

studied here:

$L_{int}$  up to  $1 \text{ ab}^{-1}$

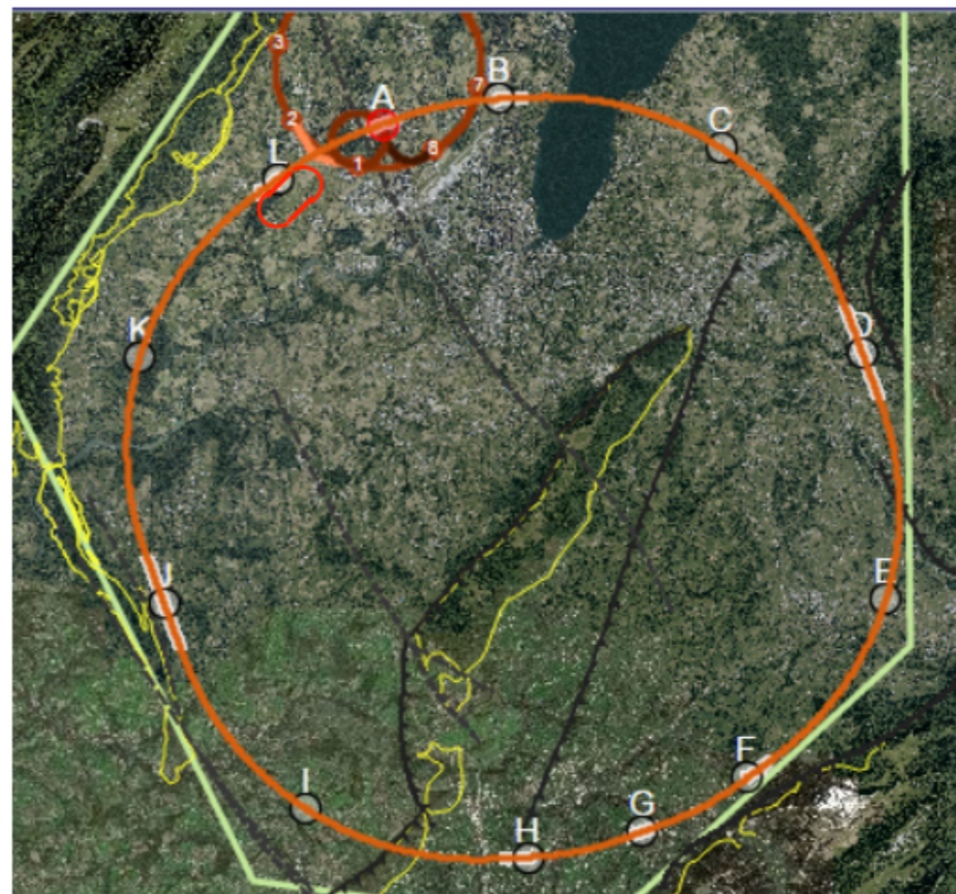
FCC–ep



LHeC

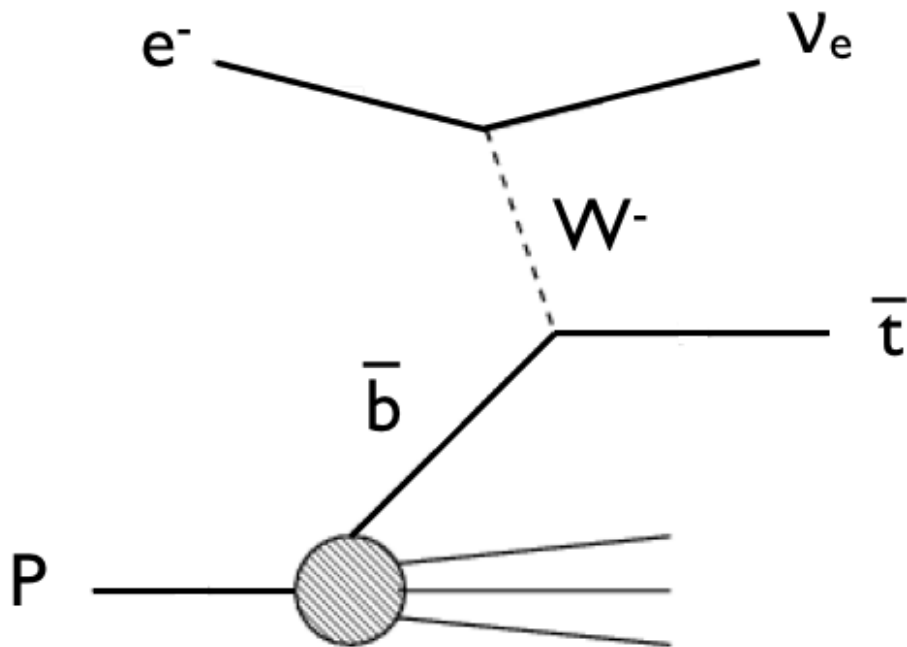
operated **synchronously**

- with HL–LHC:  
p beam: 7 TeV,  $\sqrt{s}=1.3 \text{ TeV}$
- with HE–LHC:  
p beam: 13.5 TeV,  $\sqrt{s}=1.8 \text{ TeV}$
- or later with FCC–hh:  
p beam: 50 TeV,  $\sqrt{s}=3.5 \text{ TeV}$



# SM Top Quark Production

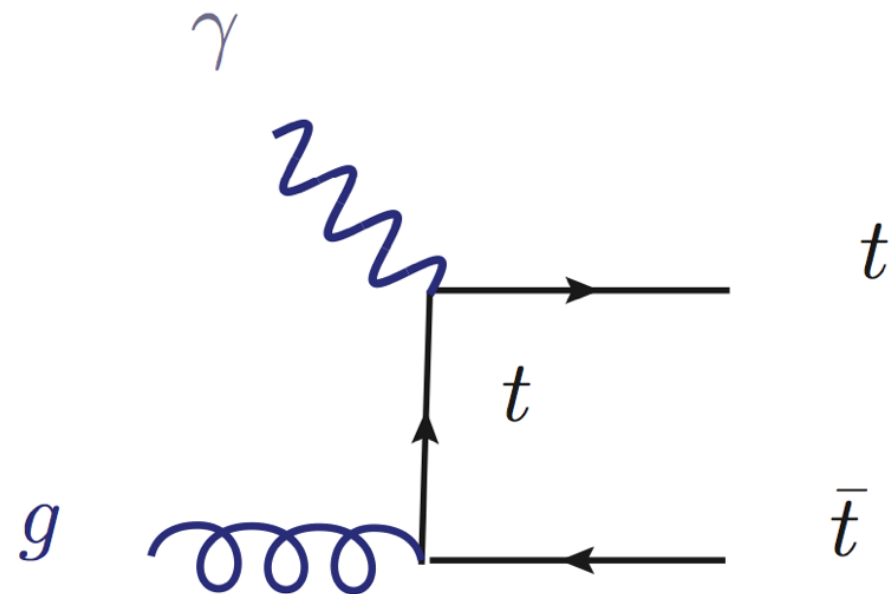
## CC DIS top production



$$\sigma = 1.73 \text{ pb @ LHeC}$$

$$\sigma = 15.3 \text{ pb @ FCC-ep}$$

## NC top photoproduction



$$\sigma = 0.05 \text{ pb @ LHeC}$$

$$\sigma = 1.14 \text{ pb @ FCC-ep}$$

$E_e = 60 \text{ GeV}$

→ future ep collider is **ideal to study EWK interactions of the top quark**

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**BSM Top Production**

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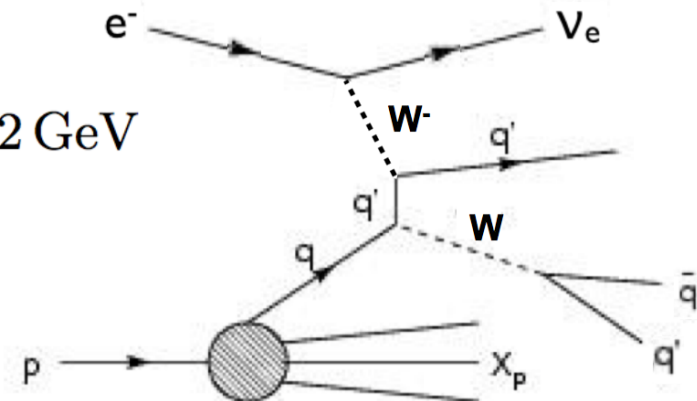
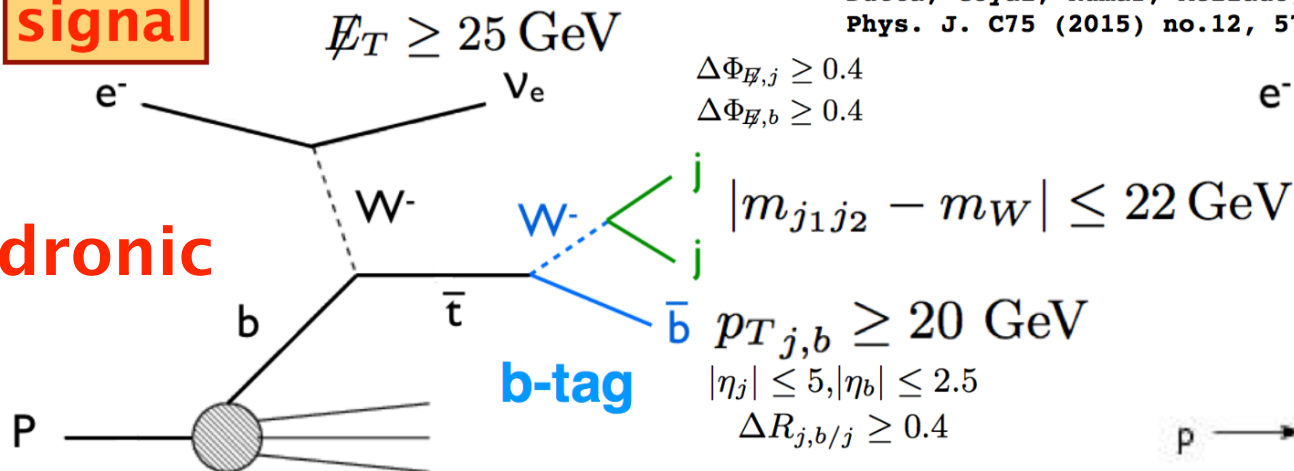
# Signal and Backgrounds

Dutta, Goyal, Kumar, Mellado, Eur. Phys. J. C75 (2015) no.12, 577

**signal**

**background**

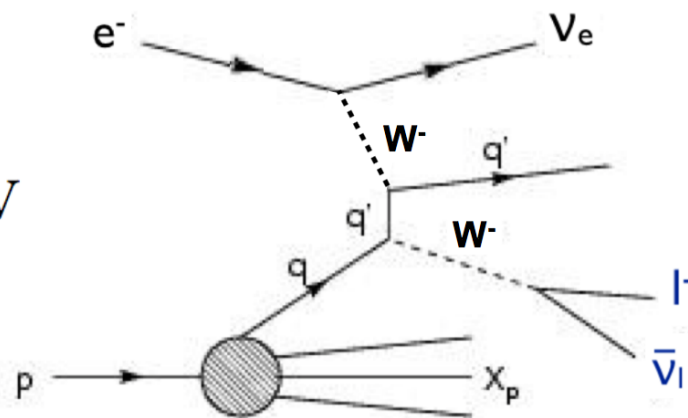
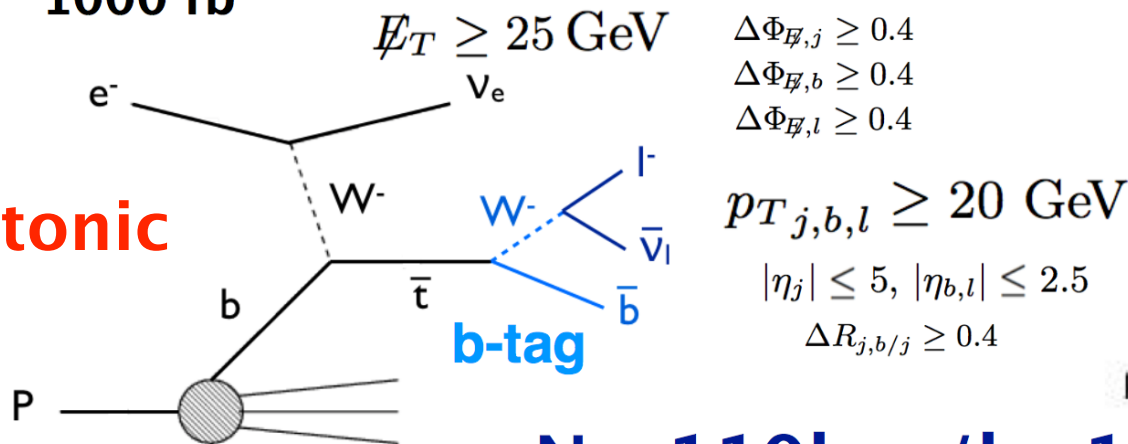
**hadronic**



**$N_t = 220k, s/b = 1.2$**

e beam: 60 GeV  
1000 fb<sup>-1</sup>

**leptonic**



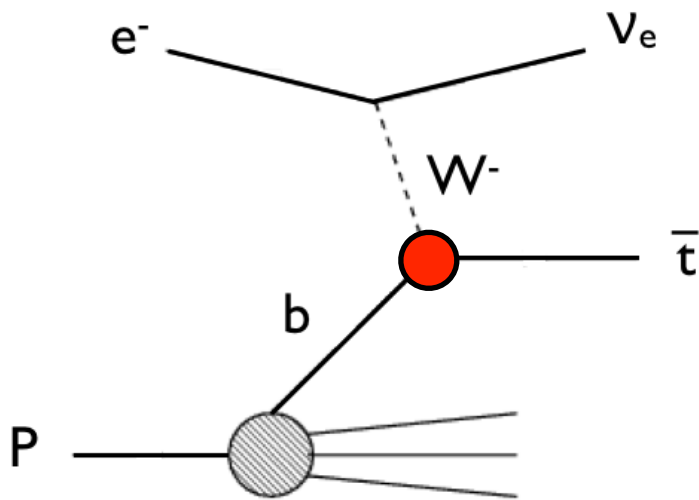
**$N_t = 110k, s/b = 11$**

→ top quark factory (with low backgrounds)

# Limits on Anomalous $Wtb$ Couplings

= 1 in SM

$$L = -\frac{g}{\sqrt{2}} \bar{b} \gamma^\mu V_{tb} (f_V^L P_L + f_V^R P_R) t W_\mu^- - \frac{g}{\sqrt{2}} \bar{b} \frac{i\sigma^{\mu\nu} q_\nu}{M_W} (f_T^L P_L + f_T^R P_R) t W_\mu^- + h.c.$$



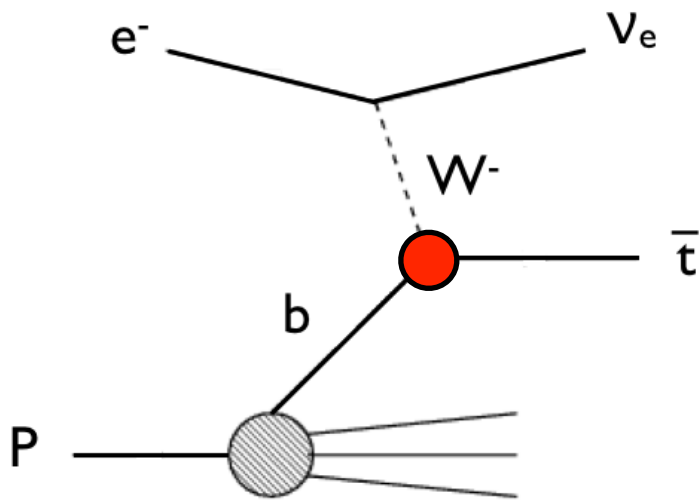
$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & \mathbf{V_{tb}} \end{pmatrix}$$



# Limits on Anomalous $Wtb$ Couplings

= 1 in SM

$$L = -\frac{g}{\sqrt{2}} \bar{b} \gamma^\mu V_{tb} (f_V^L P_L + f_V^R P_R) t W_\mu^- - \frac{g}{\sqrt{2}} \bar{b} \frac{i\sigma^{\mu\nu} q_\nu}{M_W} (f_T^L P_L + f_T^R P_R) t W_\mu^- + h.c.$$



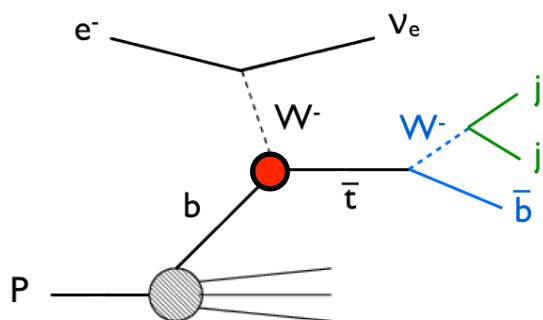
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# Limits on Anomalous $Wtb$ Couplings

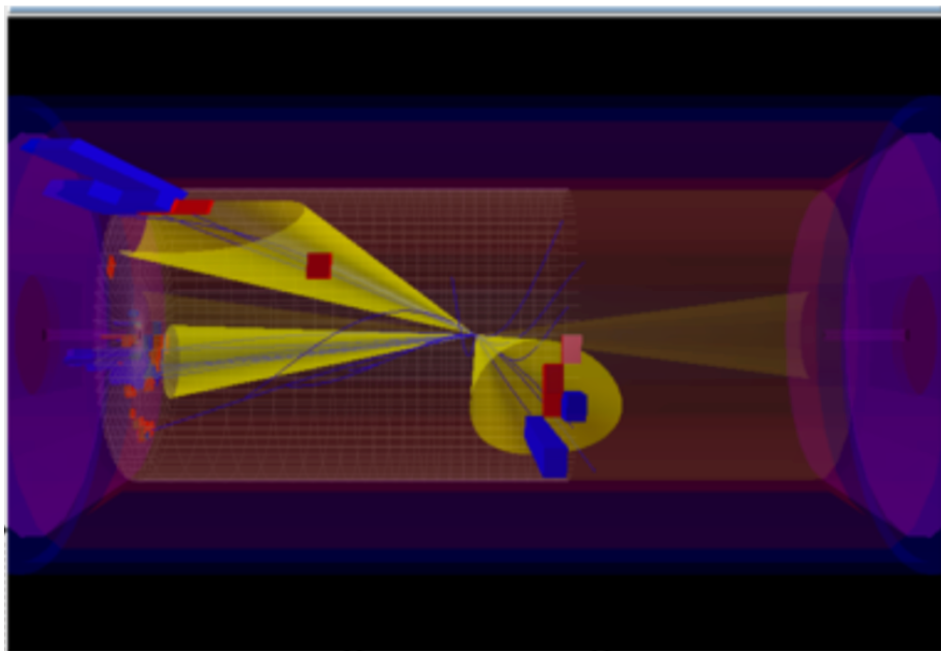
= 1 in SM

$$L = -\frac{g}{\sqrt{2}} \bar{b} \gamma^\mu V_{tb} (f_V^L P_L - f_V^R P_R) t W_\mu^- - \frac{g}{\sqrt{2}} \bar{b} \frac{i\sigma^{\mu\nu} q_\nu}{M_W} (f_T^L P_L - f_T^R P_R) t W_\mu^- + h.c.$$

Dutta, Goyal, Kumar, Mellado, Eur. Phys. J. C75 (2015) no.12, 577  
Kumar, Ruan, to be publ.



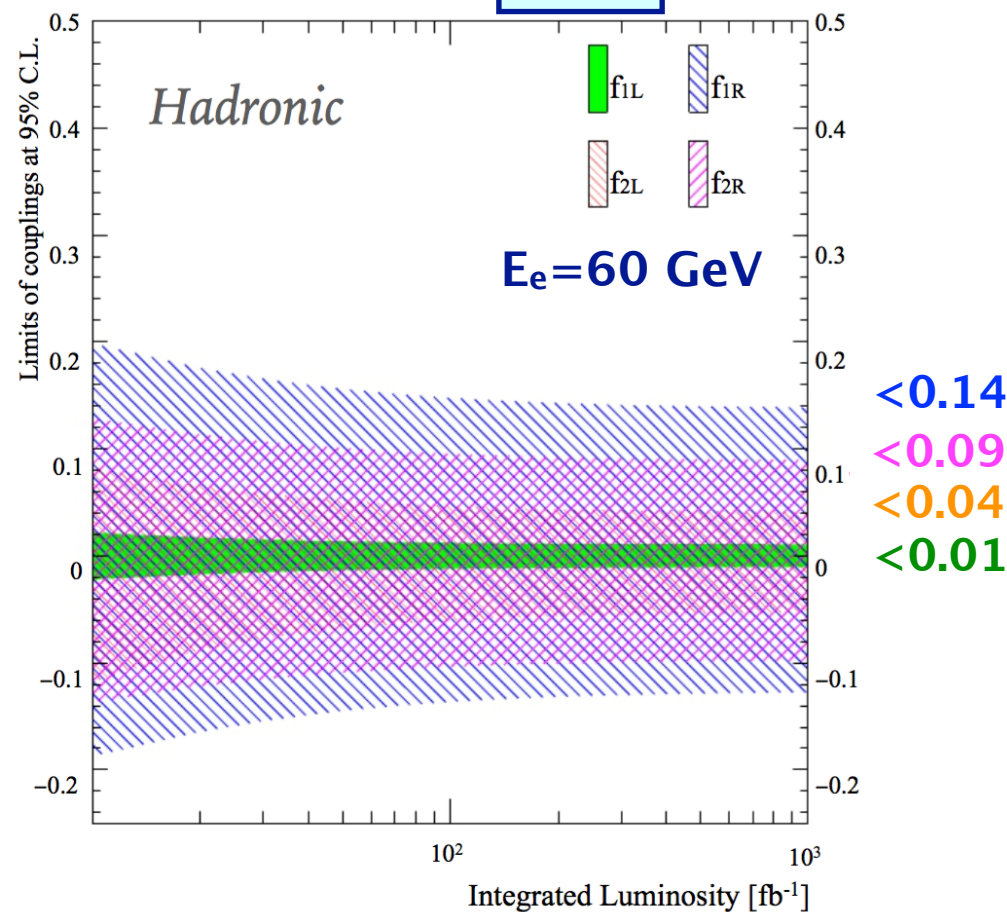
DELPHES



including detector simulation (Delphes)

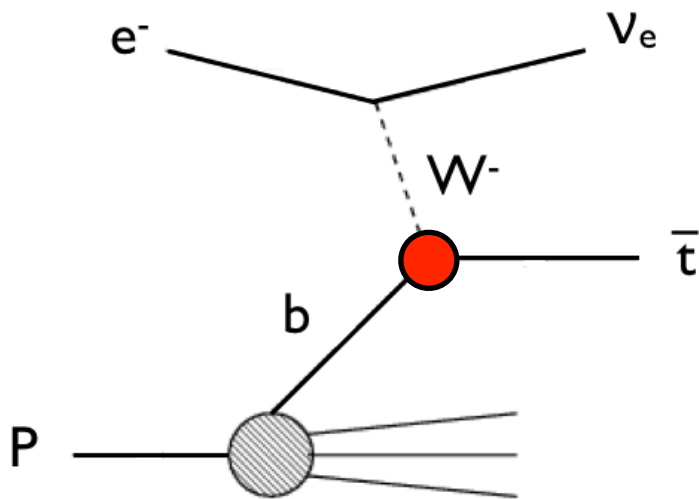
LHeC

95% C.L.

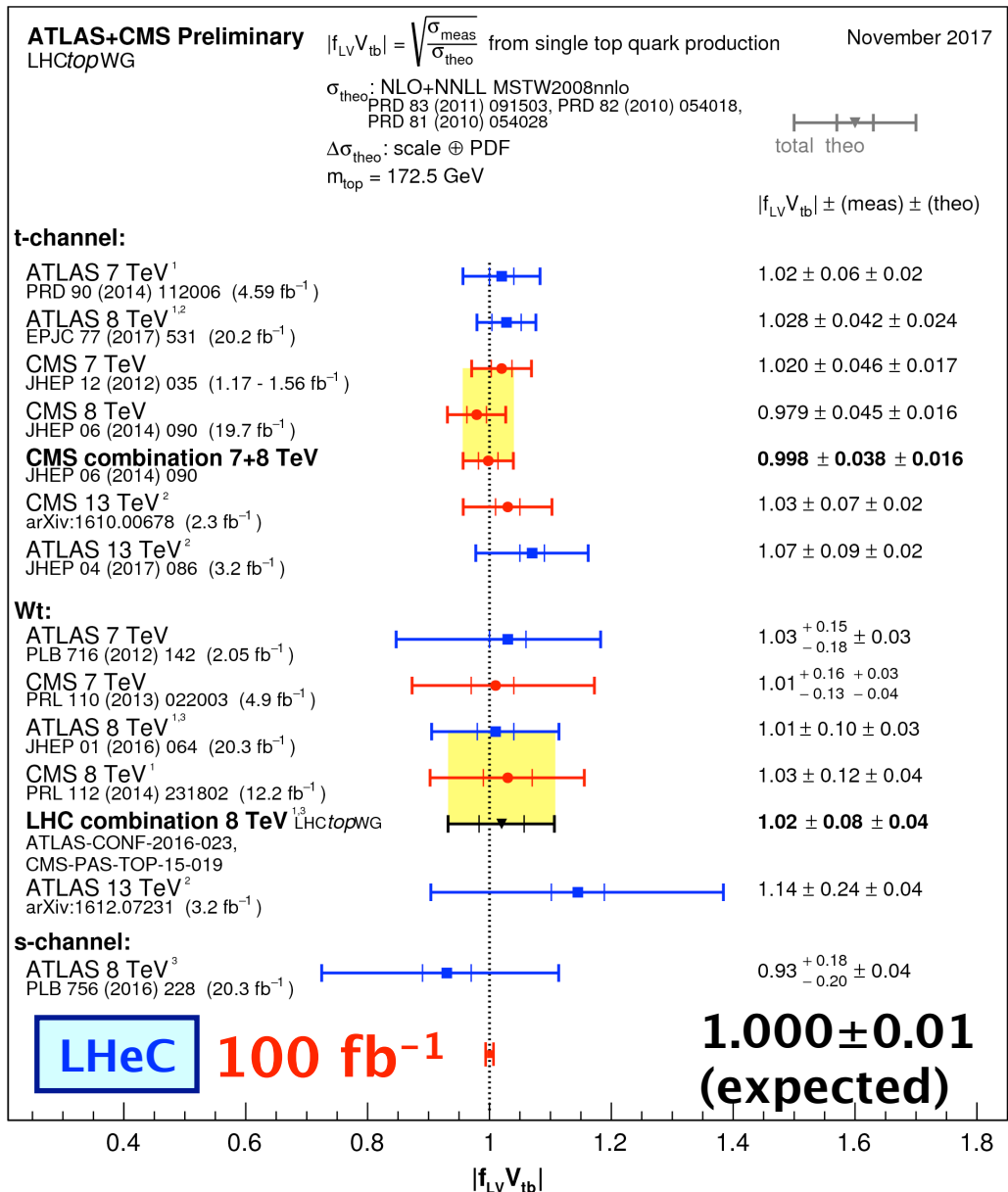


# Direct Measurement of $|V_{tb}|$

- <sup>1</sup> including top-quark mass uncertainty
- <sup>2</sup>  $\sigma_{\text{theo}}$ : NLO PDF4LHC11
- <sup>3</sup> NPPS205 (2010) 10, CPC191 (2015) 74 including beam energy uncertainty

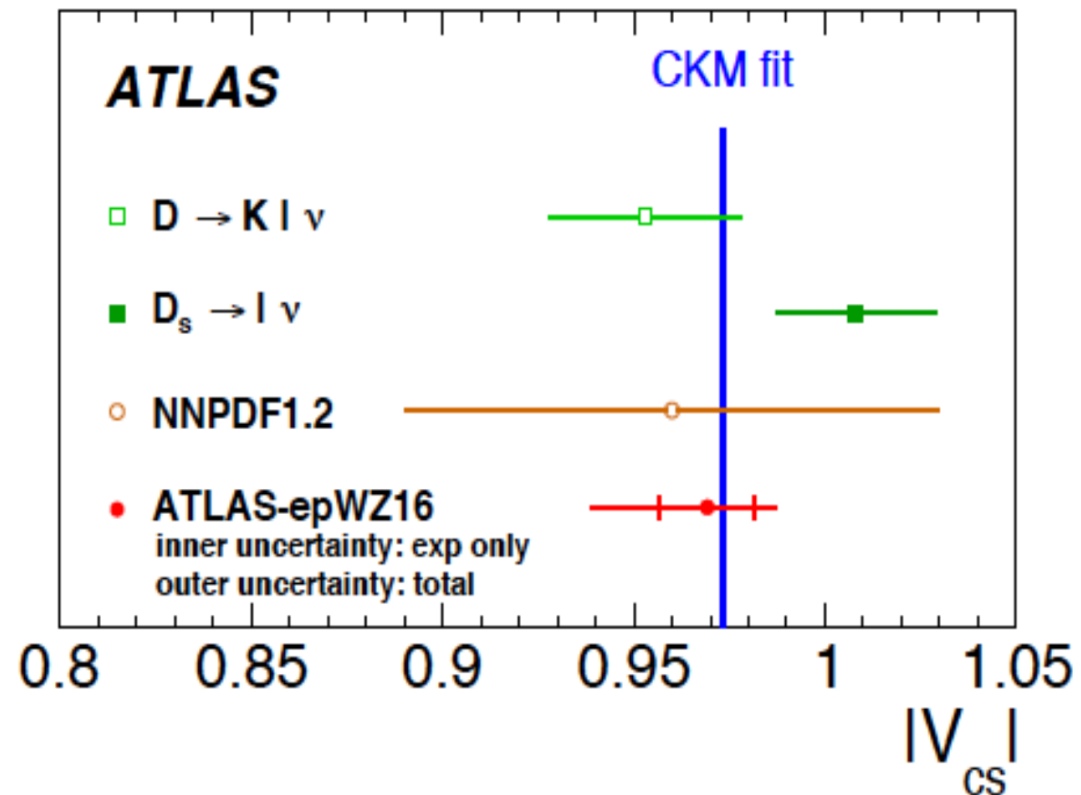


$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$



# Measurement of $|V_{cs}|$

$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$



HERA+ATLAS  $\rightarrow V_{cs}$

Expect LHeC+HL LHC to be 10 x better  
from +2-3% to surely 0.5% or below  
(work in progress)

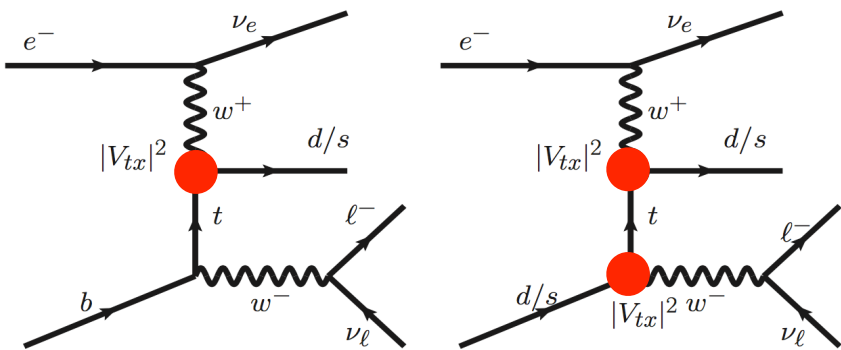
**$\rightarrow$  heavy flavour factory**

# Measurement of $|V_{td}|$

$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ \color{red}{V_{td}} & V_{ts} & V_{tb} \end{pmatrix}$$

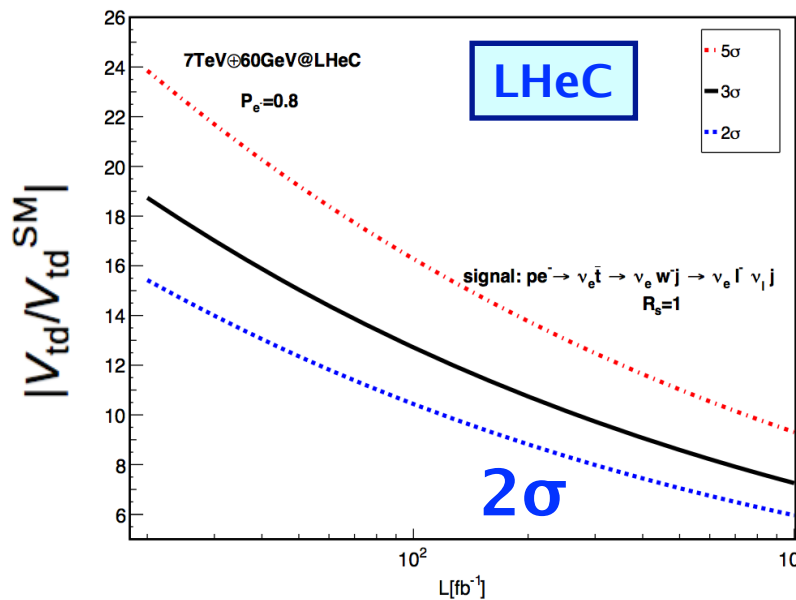
similar

$$|V_{td}^{SM}| = 8.575_{-0.098}^{+0.076} \times 10^{-3}$$



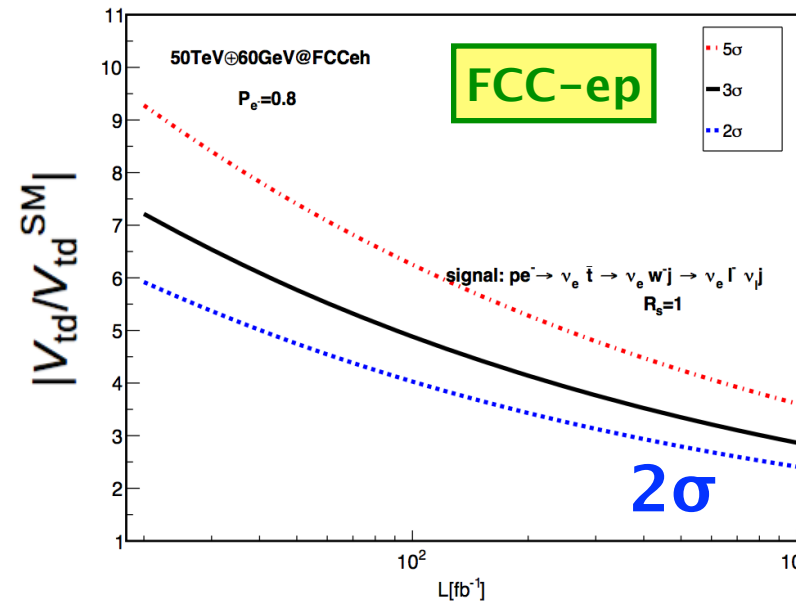
DELPHES

Hao Sun to be publ.



LHC

$\rightarrow |V_{td}| < 0.05$



$\rightarrow |V_{td}| < 0.02$

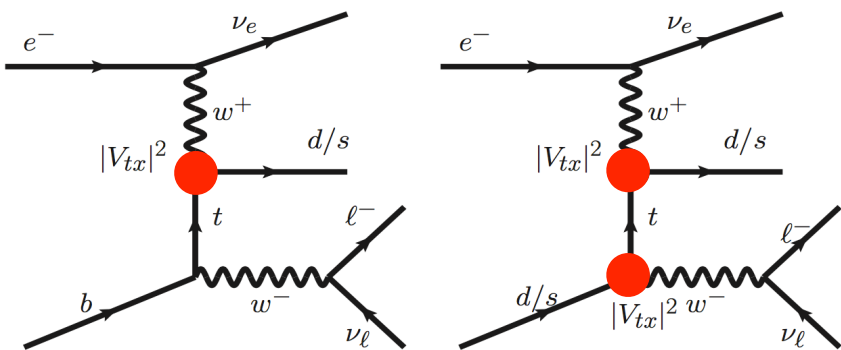
at  $2\sigma$  C.L.

# Measurement of $|V_{td}|$

$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ \color{red}{V_{td}} & V_{ts} & V_{tb} \end{pmatrix}$$

similar

$$|V_{td}^{SM}| = 8.575_{-0.098}^{+0.076} \times 10^{-3}$$

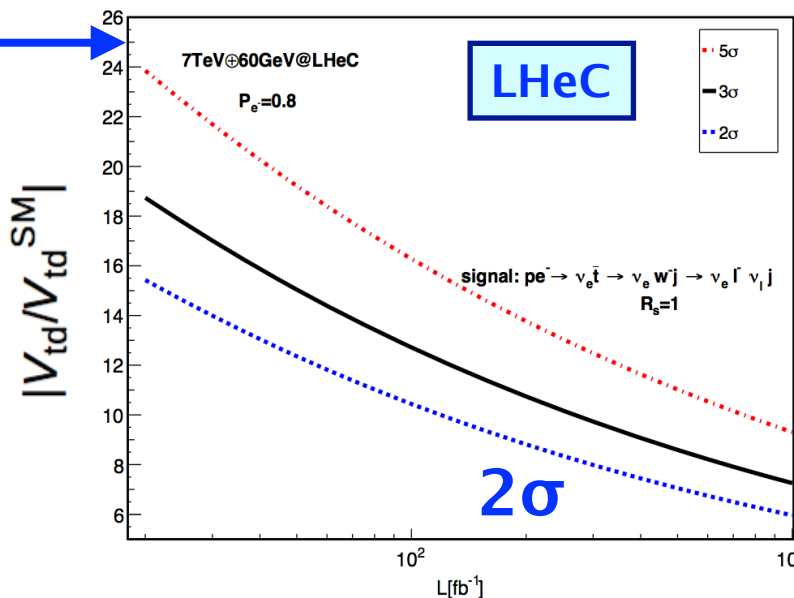


DELPHES

Hao Sun to be publ.

→ extend HL-LHC limits

LHC



LHC, 3000 fb<sup>-1</sup>@14TeV

HL-LHC

arXiv:1709.07887

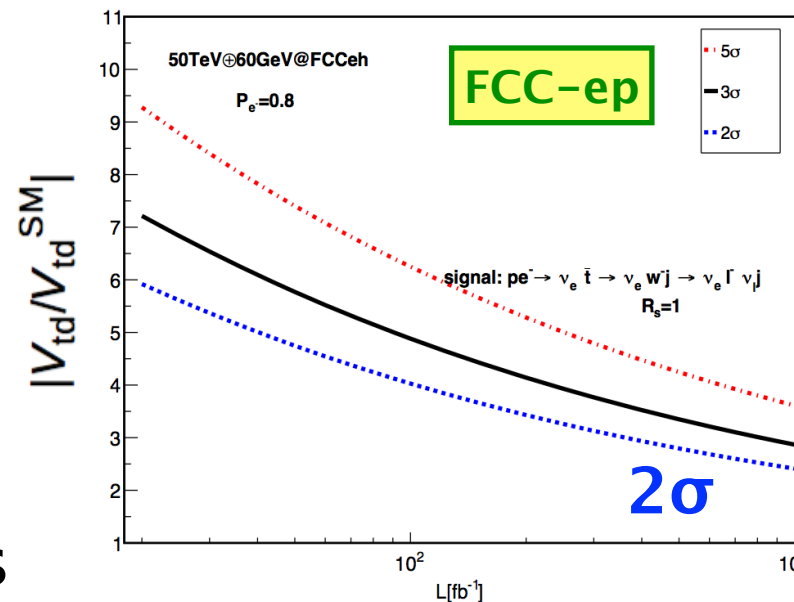
5σ

3σ

2σ

→  $|V_{td}| < 0.05$

2σ

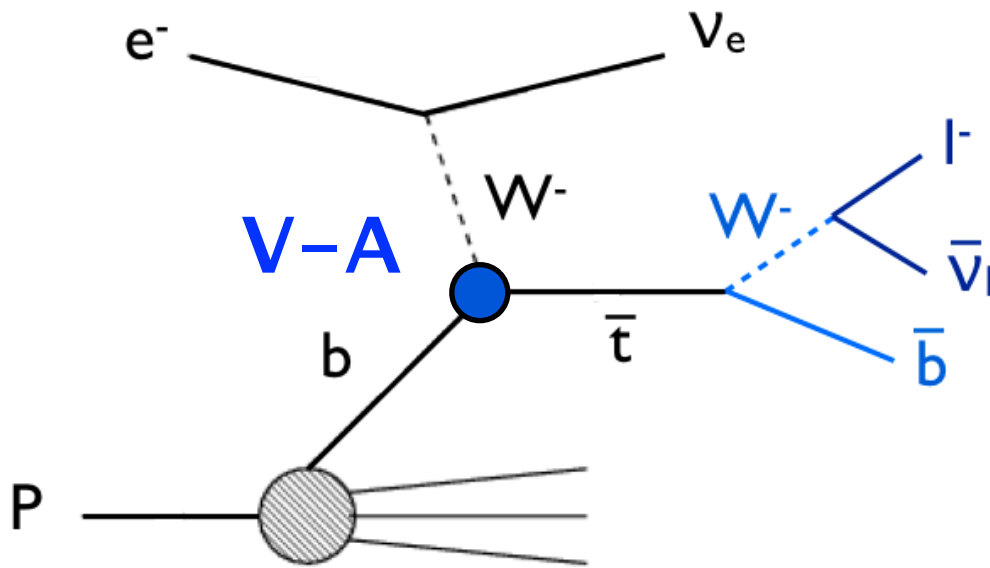


→  $|V_{td}| < 0.02$

at 2σ C.L.

# Top Quark Polarisation

Atag, Sahin,  
PRD 73, 074001 (2006)



$\cos\theta$ : angle between charged lepton and spin quantisation axis in top rest frame

$$\frac{1}{\Gamma_T} \frac{d\Gamma}{d\cos\theta} = \frac{1}{2} (1 + A_{\uparrow\downarrow} \alpha \cos\theta) \quad A_{\uparrow\downarrow} = \frac{N_{\uparrow} - N_{\downarrow}}{N_{\uparrow} + N_{\downarrow}}$$

using simply e-beam axis:  
polarisation:  $P_t = 96\%$

TESLA+HERAp:

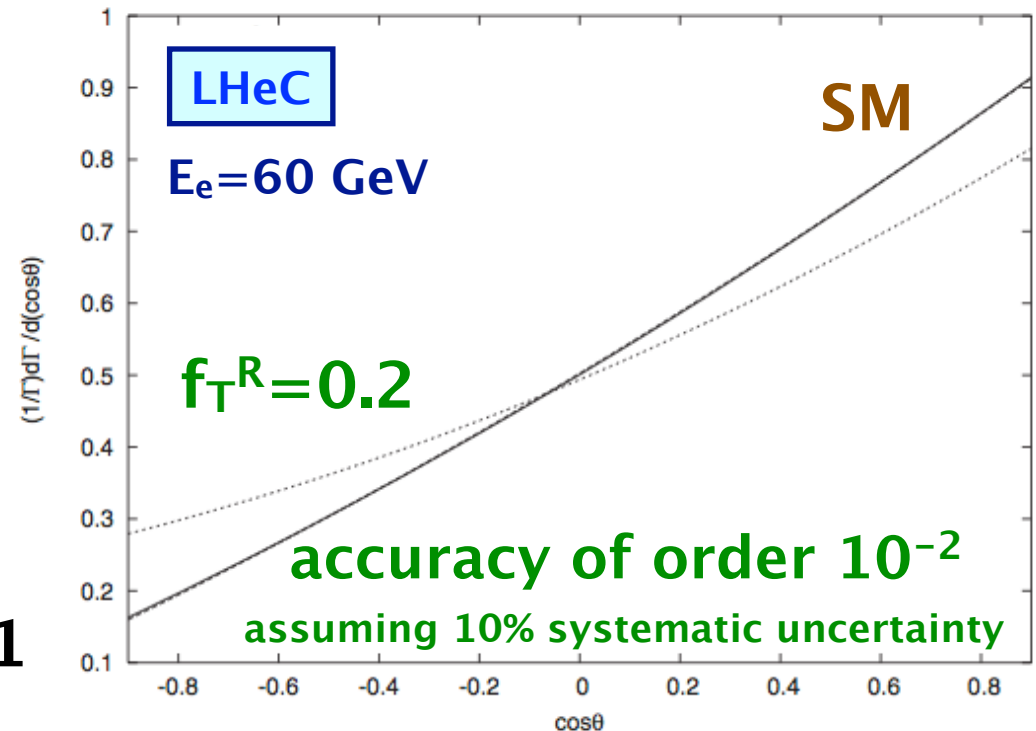
$\sqrt{s} = 1.6 \text{ TeV}$

$L_{int} = 20 \text{ fb}^{-1}$

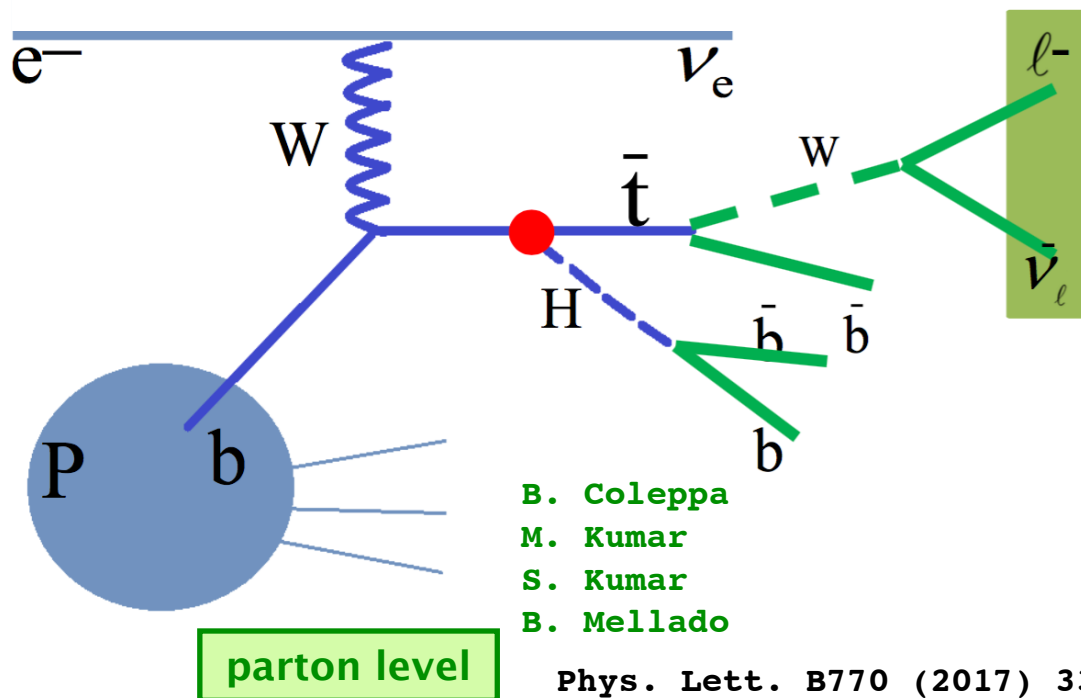


$19.7 \text{ fb}^{-1}: A_{\uparrow\downarrow} = 0.26 \pm 0.11$

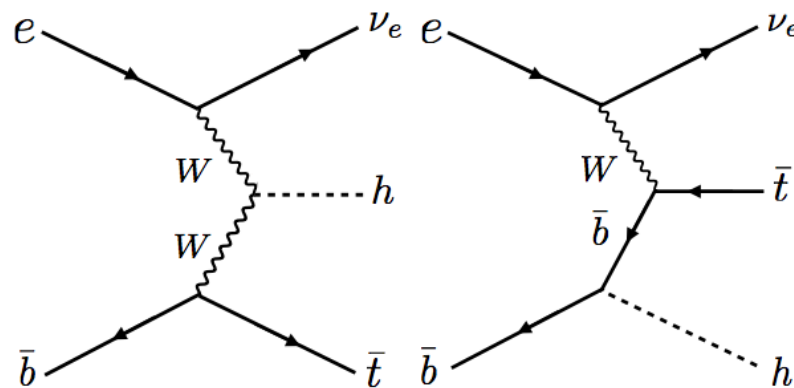
JHEP 04 (2016) 073



# CP Nature of Top-Higgs Coupling



$$\mathcal{L} = -\frac{m_t}{v} \bar{t} [\kappa \cos \zeta_t + i\gamma_5 \sin \zeta_t] t h$$

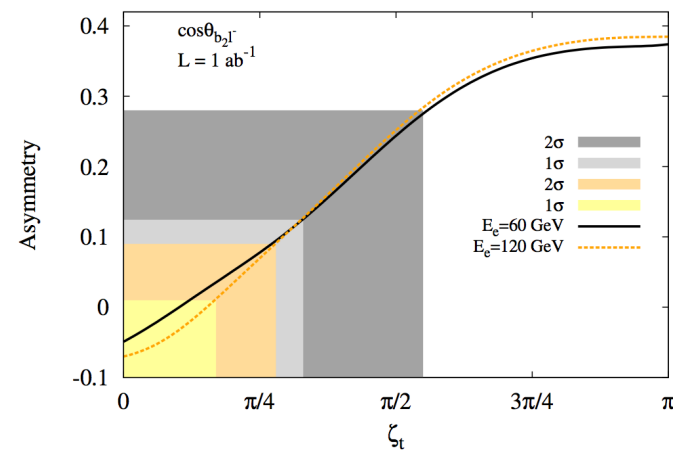
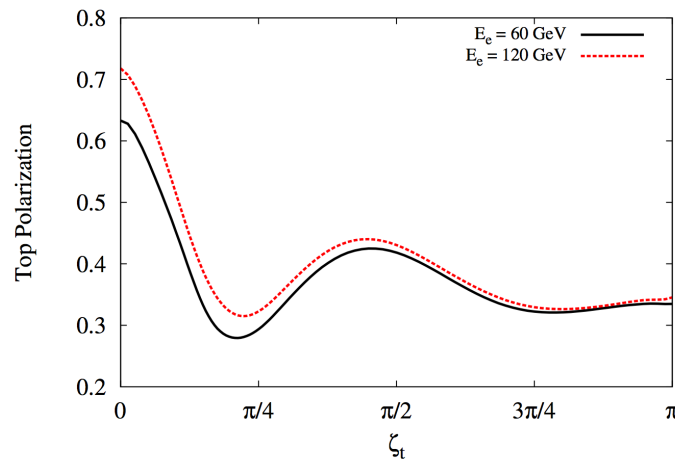
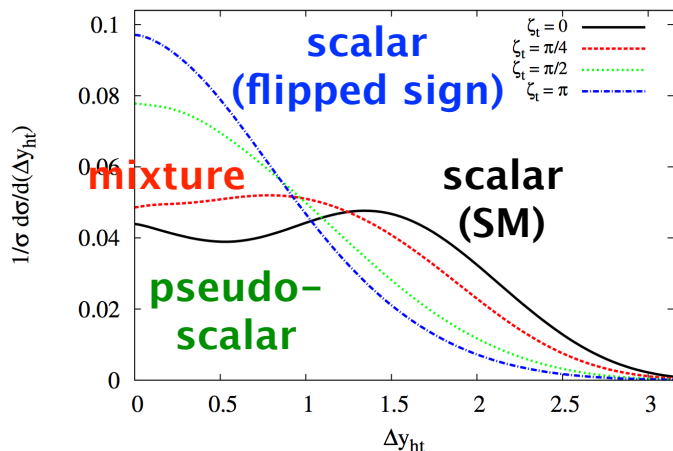


LHeC

rapidity difference (H, t-bar)

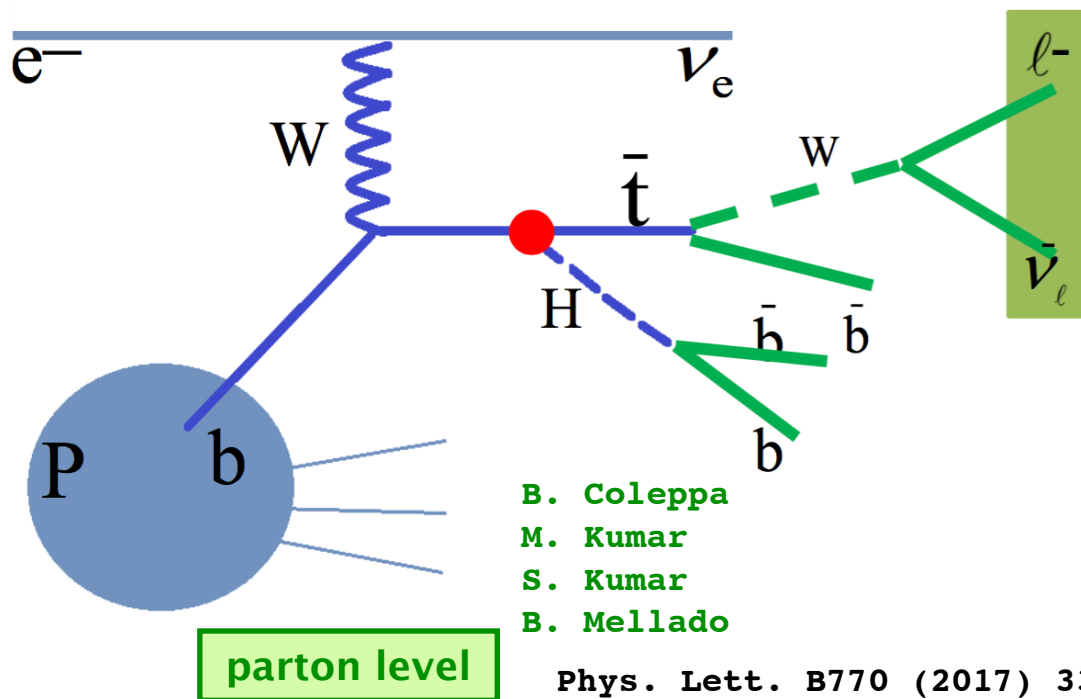
top polarisation

angular asymmetries (b2, l-)

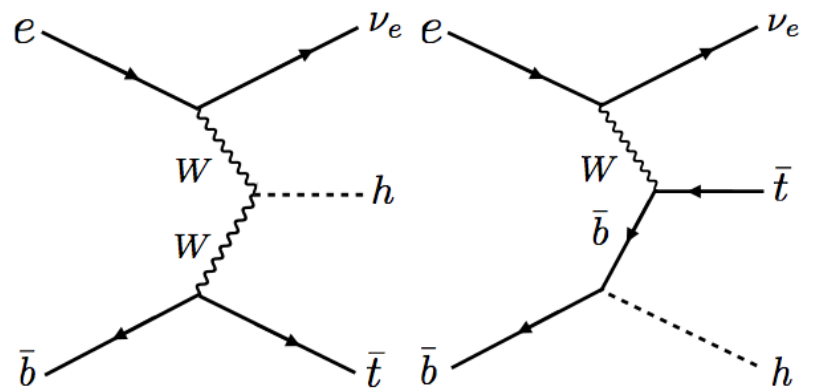




# CP Nature of Top-Higgs Coupling



$$\mathcal{L} = -\frac{m_t}{v} \bar{t} [\kappa \cos \zeta_t + i\gamma_5 \sin \zeta_t] t h$$

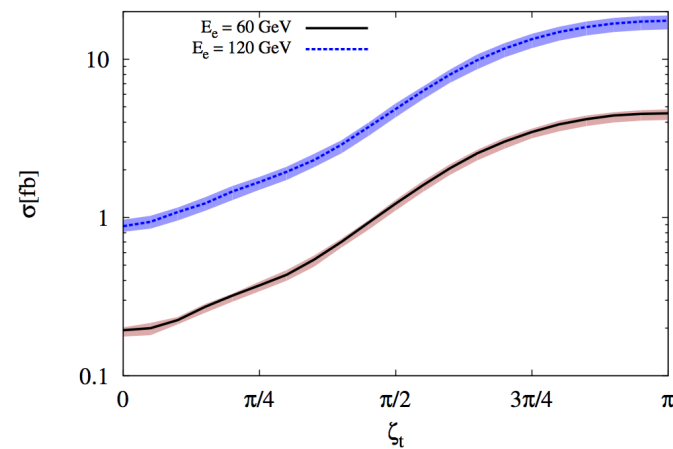
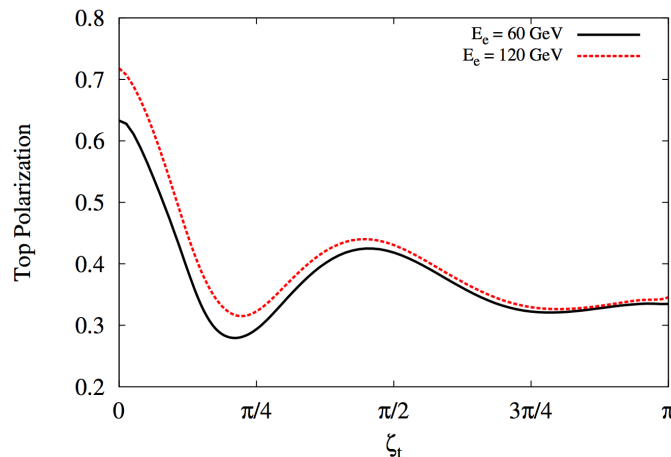
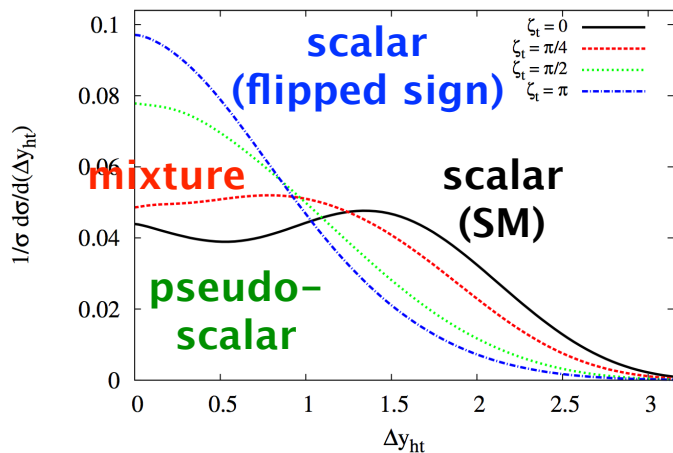


LHeC

rapidity difference (H,  $\bar{t}$ )

top polarisation

fiducial incl. cross-section



# Exclusion Contours (fiducial cross section)

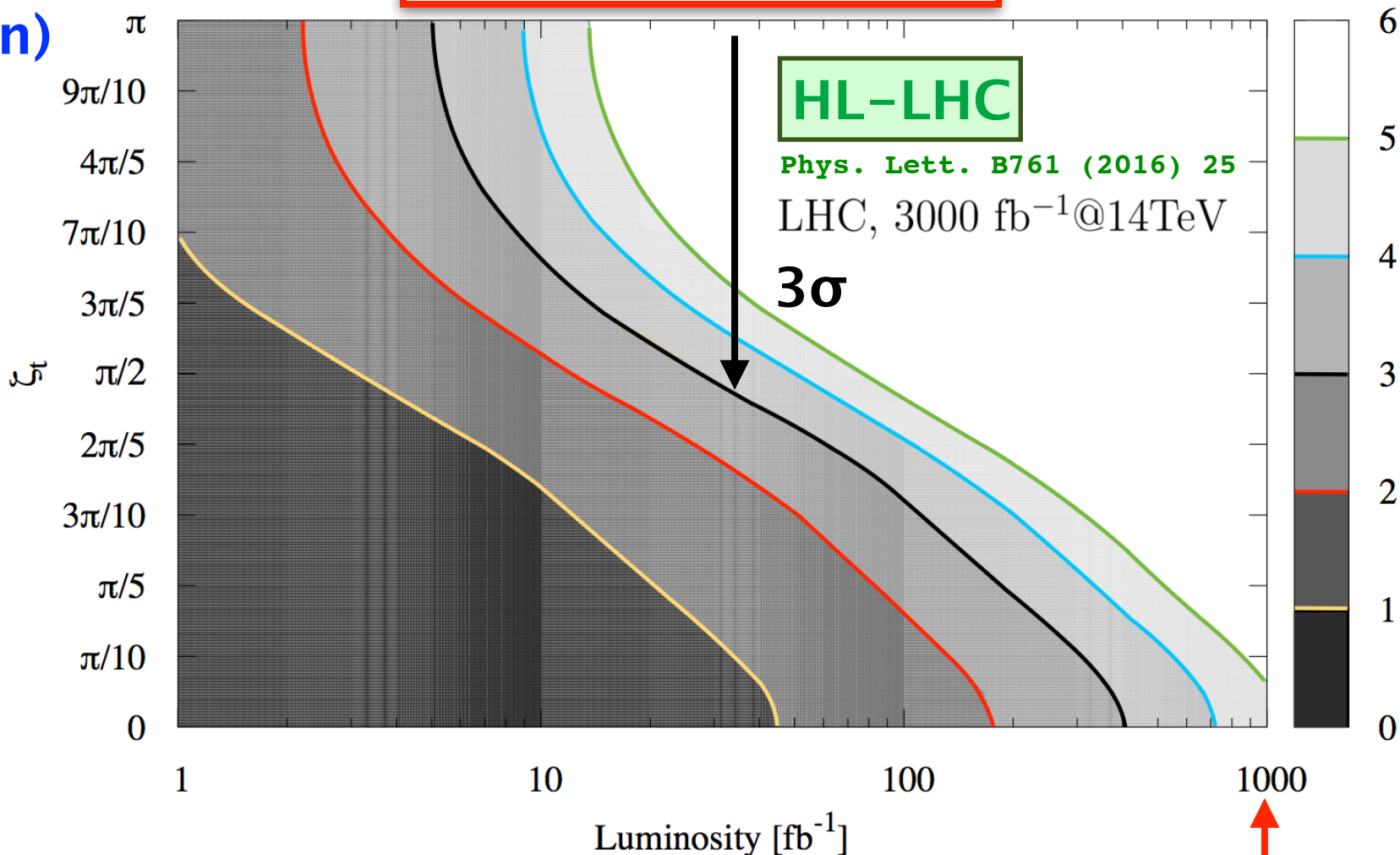
CP-even  
(flipped sign)

CP-odd

CP-even  
(SM)

$$\mathcal{L} = -\frac{m_t}{v} \bar{t} [\kappa \cos \zeta_t + i\gamma_5 \sin \zeta_t] t h$$

LHeC

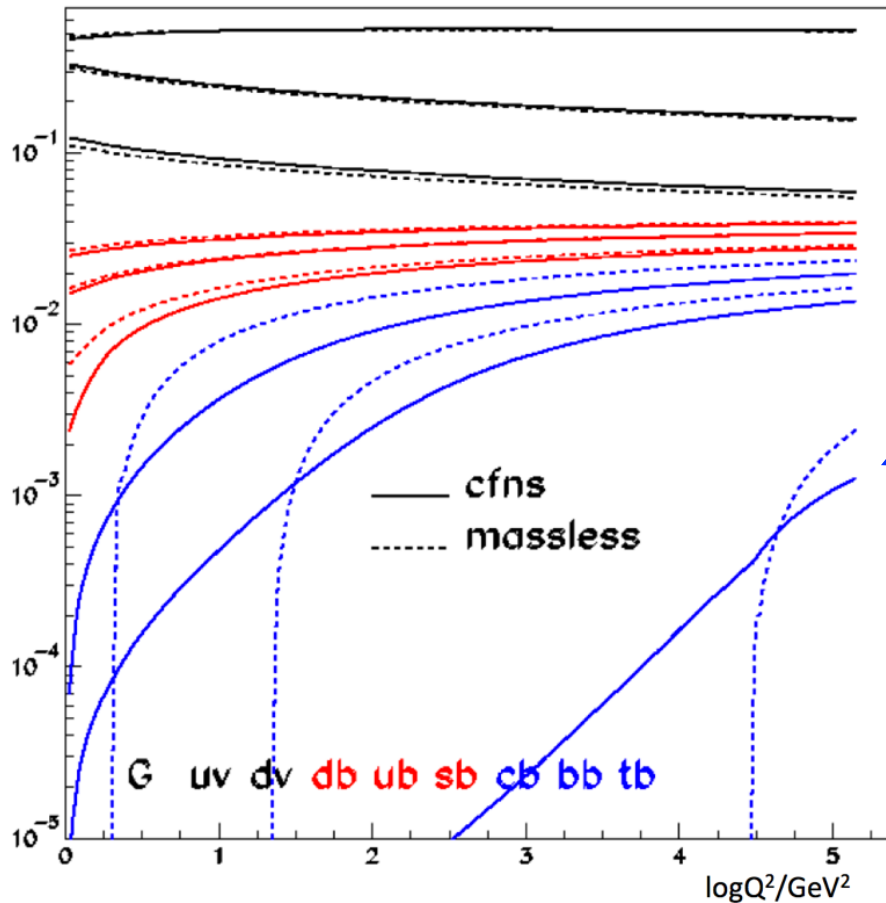


→ powerful probe  
of ttH coupling

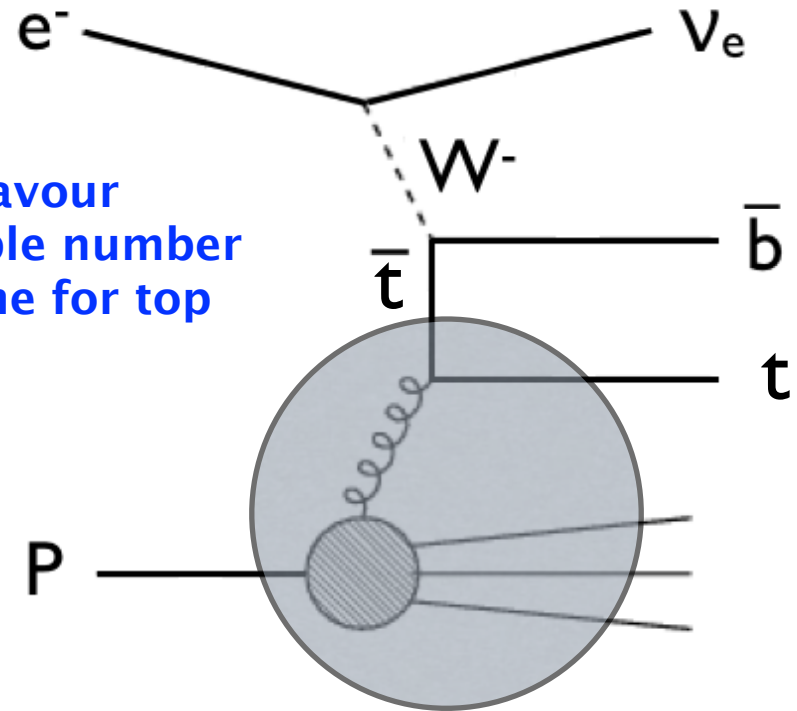
# Top Quark Parton Density Function

LHeC CDR, J.Phys. G39, 075001 (2012)

parton momentum fraction



six-flavour variable number scheme for top quark



- in 6 flavour number scheme, top receives at  $Q^2 \sim m_t^2$  certain fraction of the proton's momentum
- need to understand what a “top PDF” is in the framework of parton model

→ LHeC offers new field of research for top quark PDF

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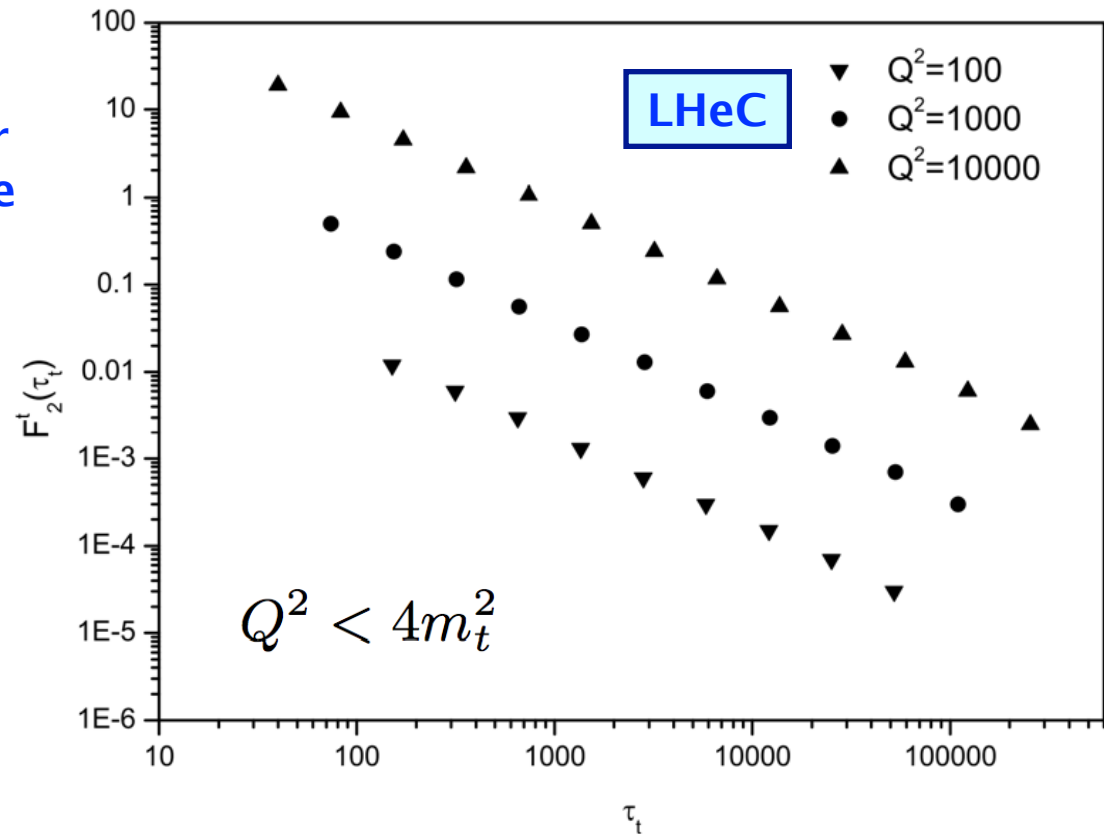
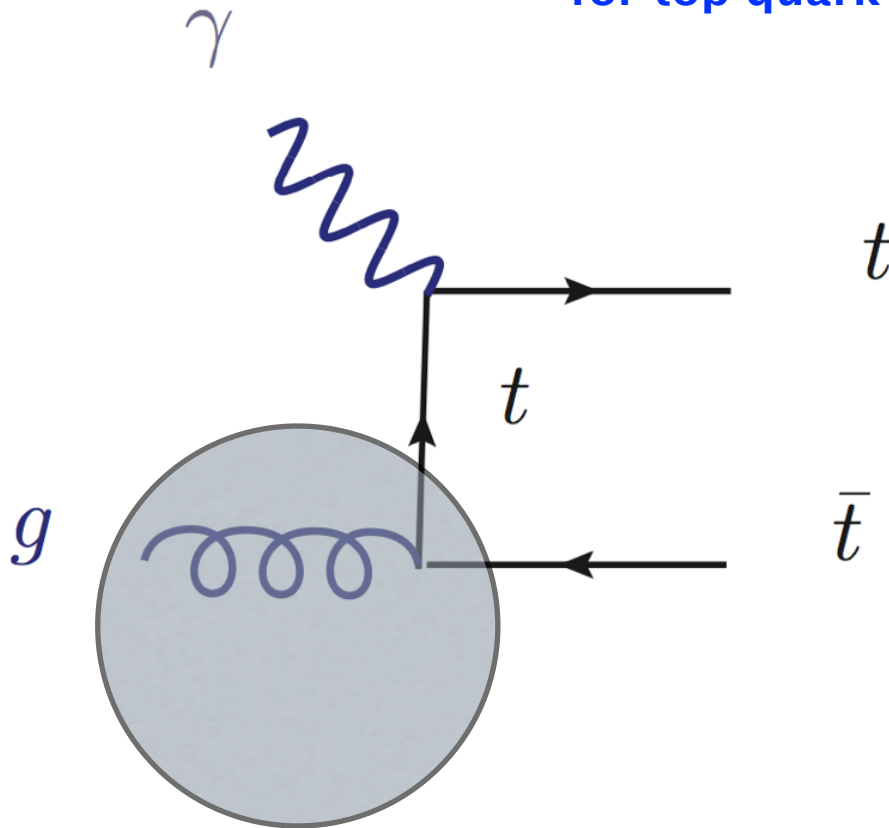
# Top Quark Structure Function

Boroun, Phys. Lett. B744, 142 (2015)

$L_{int} = 10 \text{ fb}^{-1}$

$E_e = 60 \text{ GeV}$

variable flavour  
number scheme  
for top quark



$$\tau_t = \left(1 + \frac{4m_t^2}{Q^2}\right)^{1+\lambda} \frac{Q^2}{Q_0^2} \left(\frac{x_B}{x_0}\right)^\lambda$$

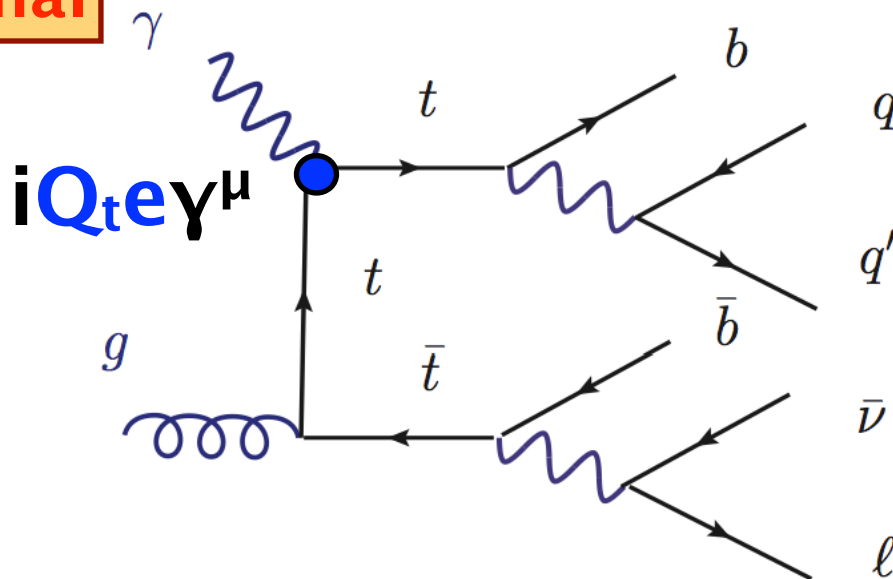
$$x = x_B \left(1 + \frac{4m_t^2}{Q^2}\right)$$

→ LHeC/FCC-ep opens up a new field of top quark PDFs and to unveil the complete flavour structure of the proton

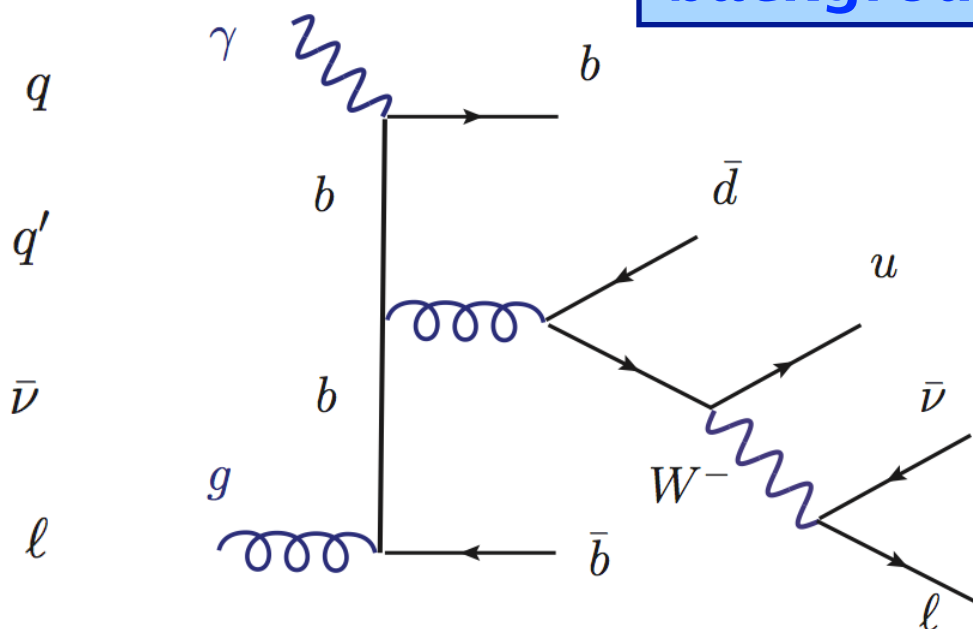
# Analysis of the $t\bar{t}\gamma$ Vertex

signal

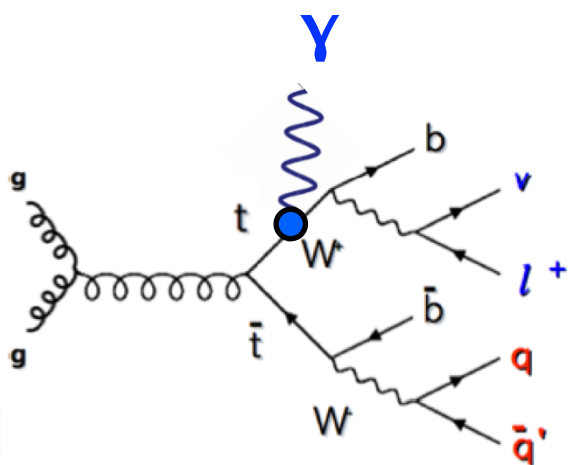
background



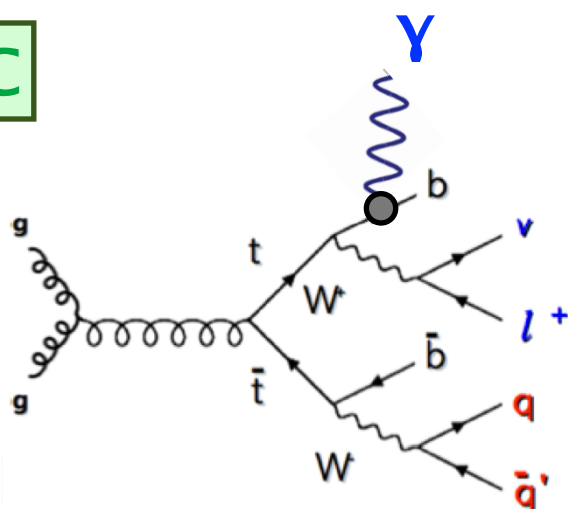
→ measure top quark charge



LHC



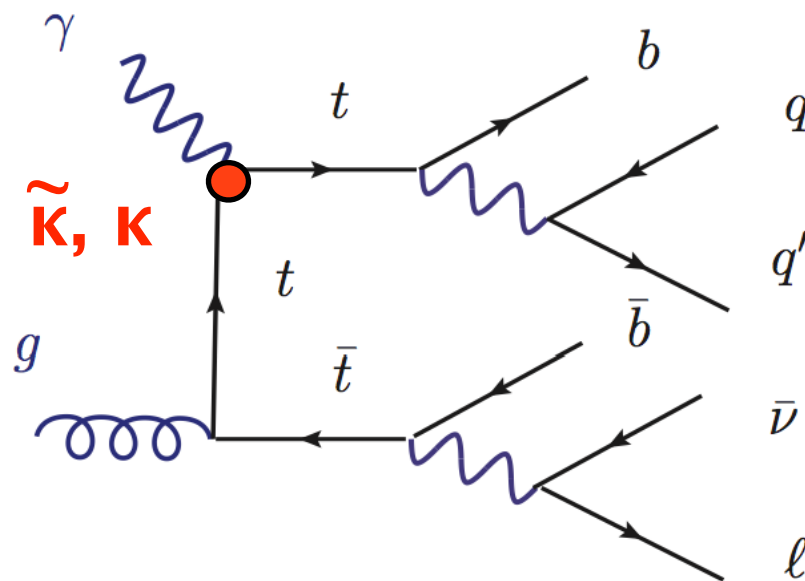
OR



?

→ not unambiguous at the LHC

# Search for Anomalous $t\bar{t}\gamma$ Couplings



LHeC

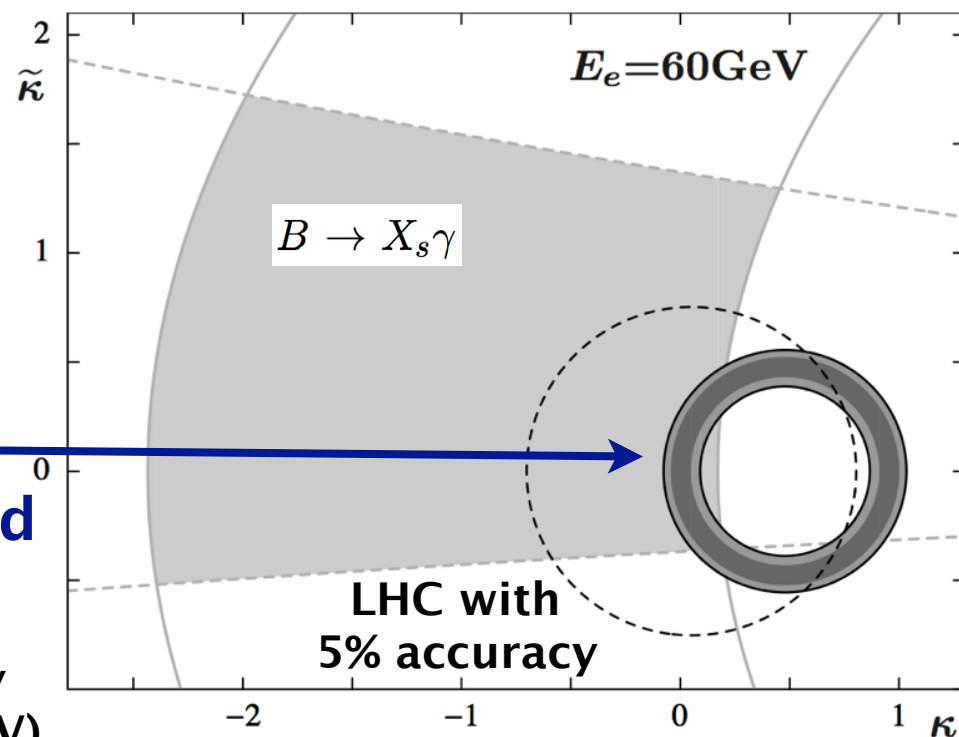
10% and 18% accuracy assumed



27% accuracy  
(4.59fb<sup>-1</sup>, 7 TeV)

$$\mathcal{L}_{t\bar{t}\gamma} = e\bar{t} \left( Q_t \gamma^\mu A_\mu + \frac{1}{4m_t} \sigma^{\mu\nu} F_{\mu\nu} (\kappa + i\tilde{\kappa}\gamma_5) \right) t$$

electric dipole moment:  $\tilde{\kappa}$

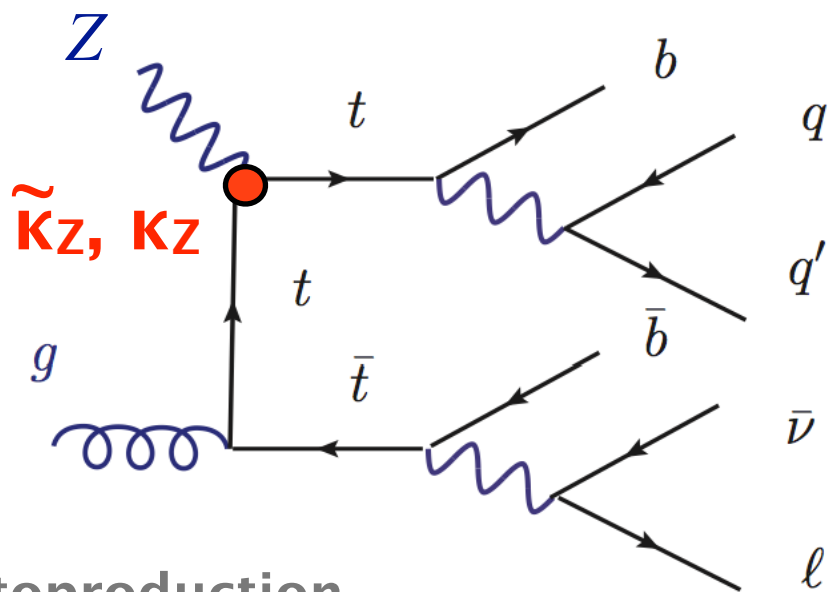


magnetic dipole moment:  $\kappa$

Bouzas, Larios,  
Physical Review D 88, 094007 (2013)

# Search for Anomalous $t\bar{t}Z$ Couplings

Bouzas, Larios,  
Physical Review D 88, 094007 (2013)

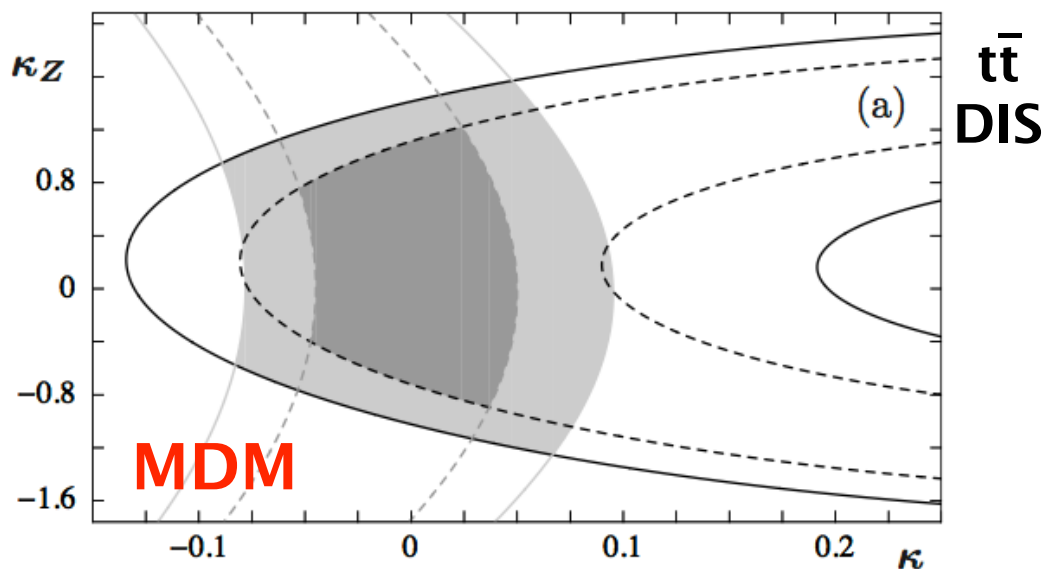


$t\bar{t}$  photoproduction

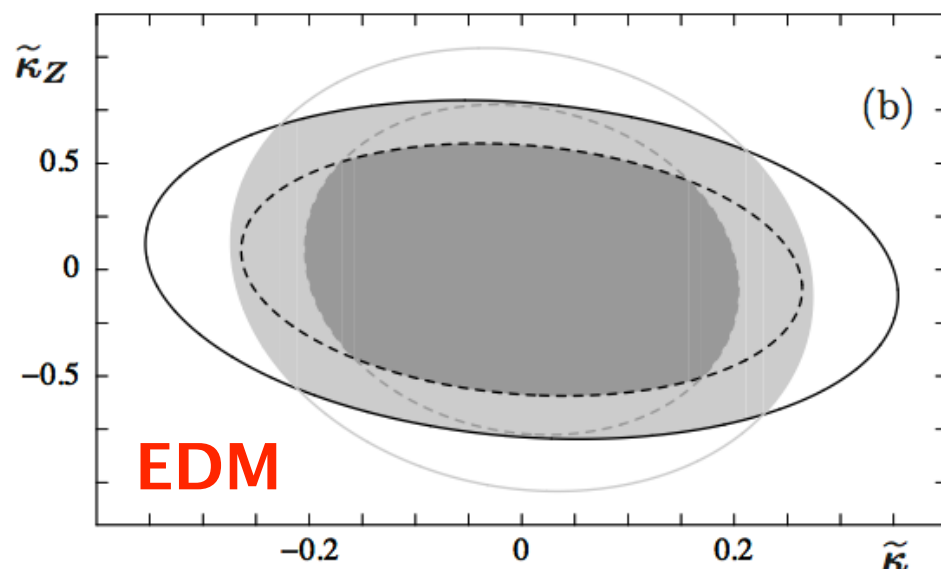
property	precision
<b>EDM:</b> $\tilde{\kappa} / \tilde{\kappa}_Z$	0.20-0.28/0.6-0.8
<b>MDM:</b> $\kappa / \kappa_Z$	0.05-0.09/0.9-1.3

**LHeC**  $E_e=60$  GeV

10% and 18% accuracy assumed



$t\bar{t}$  DIS





# Outline

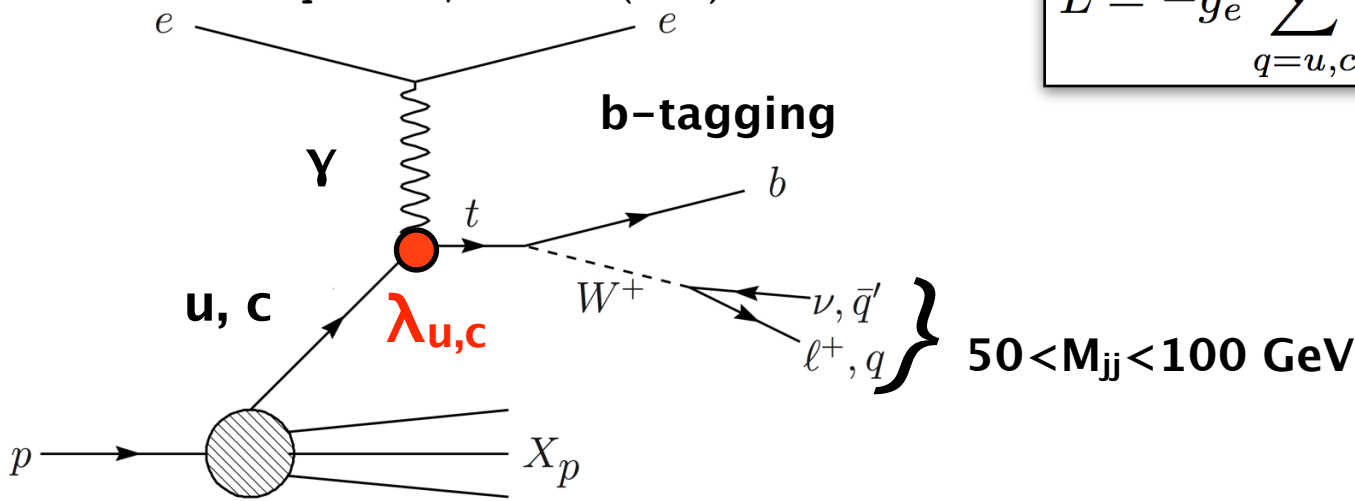
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# Search for Anomalous FCNC $t\bar{t}$ Coupling

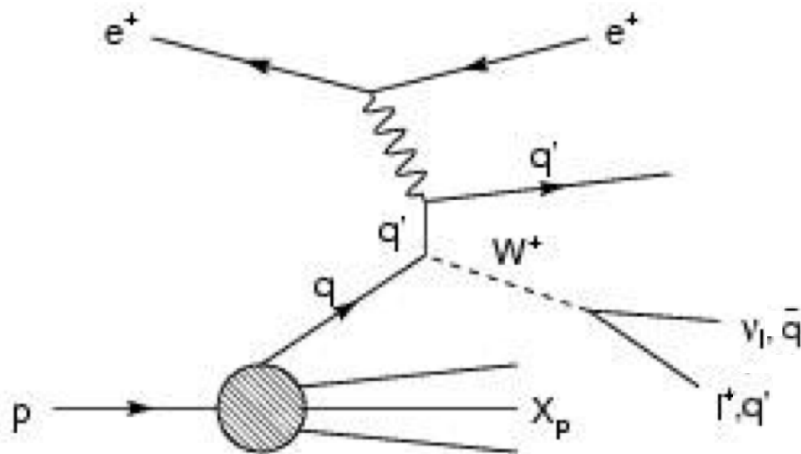
**signal**

I. Cakir, Yilmaz, Denizli, Senol,  
Karadeniz, O. Cakir, Adv. High Energy  
Phys. 2017, 1572053 (2017)

$$L = -g_e \sum_{q=u,c} Q_q \frac{\lambda^q}{\Lambda} \bar{t} \sigma^{\mu\nu} (f_q + h_q \gamma_5) q A_{\mu\nu} + h.c.$$



**background**

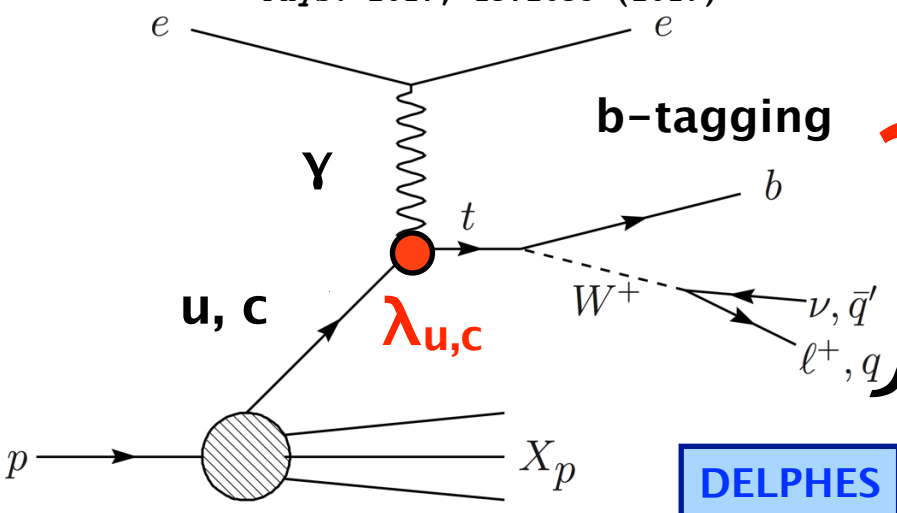


# Search for Anomalous FCNC $t\bar{u}$ Coupling

**signal**

I. Cakir, Yilmaz, Denizli, Senol,  
Karadeniz, O. Cakir, Adv. High Energy  
Phys. 2017, 1572053 (2017)

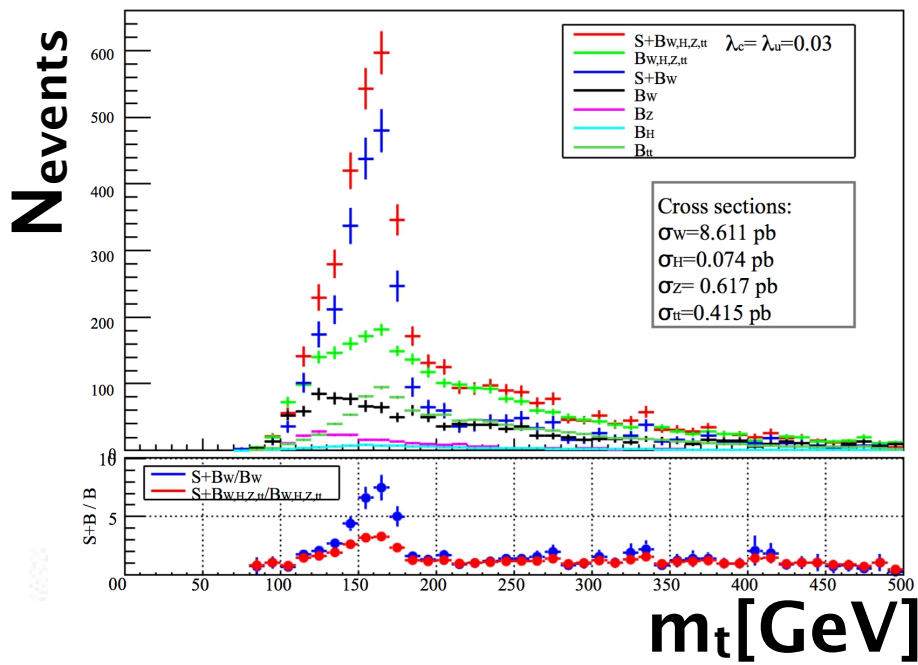
$$L = -g_e \sum_{q=u,c} Q_q \frac{\lambda_q}{\Lambda} \bar{t} \sigma^{\mu\nu} (f_q + h_q \gamma_5) q A_{\mu\nu} + h.c.$$



$130 < M_{Wb} < 190 \text{ GeV}$

$50 < M_{jj} < 100 \text{ GeV}$

**DELPHES**

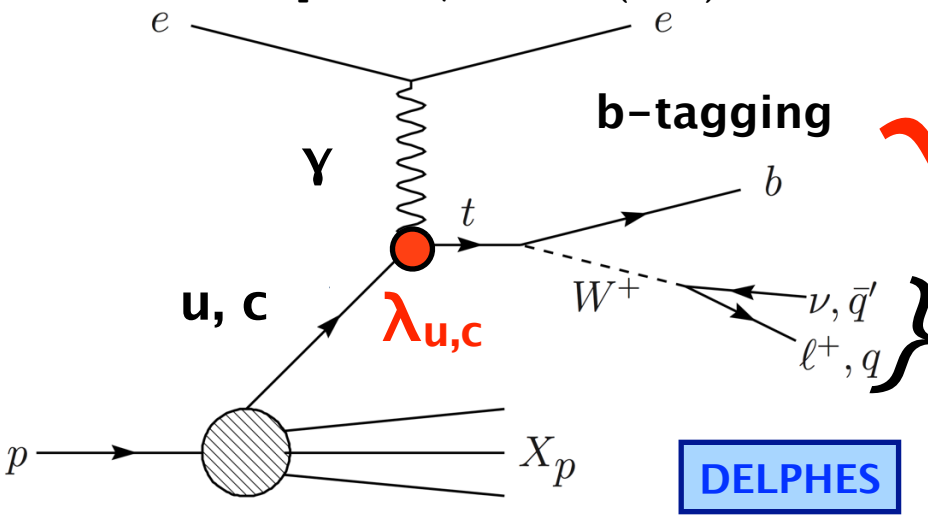


# Search for Anomalous FCNC $t\bar{u}\gamma$ Coupling

**signal**

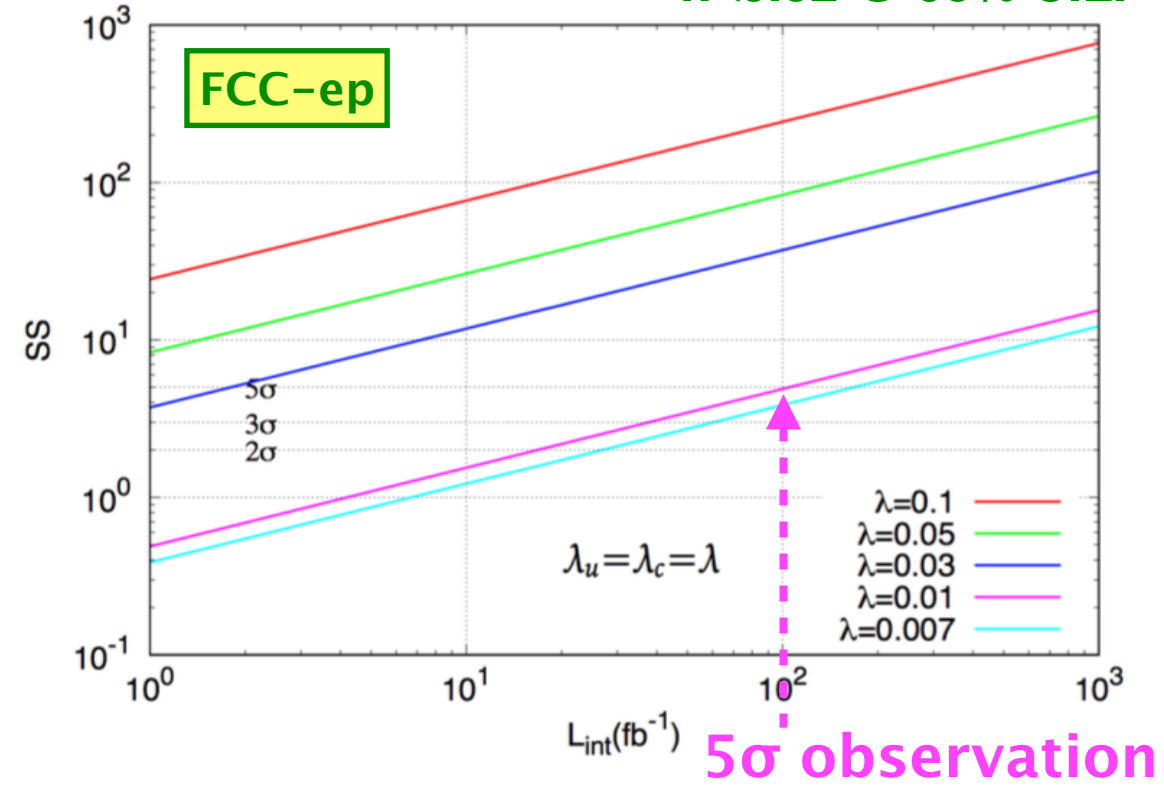
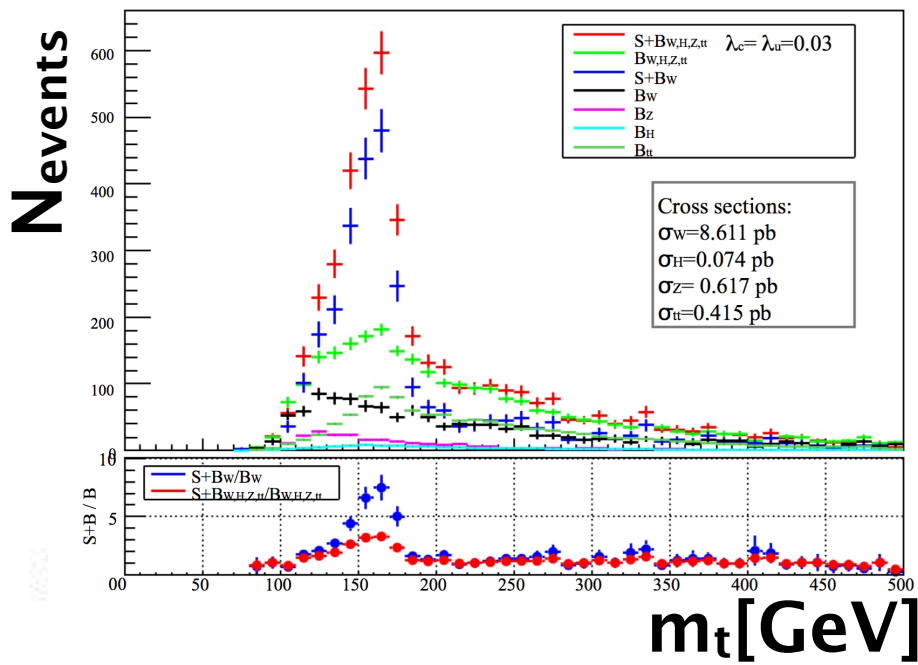
I. Cakir, Yilmaz, Denizli, Senol,  
Karadeniz, O. Cakir, Adv. High Energy  
Phys. 2017, 1572053 (2017)

$$L = -g_e \sum_{q=u,c} Q_q \frac{\lambda^q}{\Lambda} \bar{t} \sigma^{\mu\nu} (f_q + h_q \gamma_5) q A_{\mu\nu} + h.c.$$



**130 < M<sub>Wb</sub> < 190 GeV**  **300 fb<sup>-1</sup>, sqrt(s) = 14 TeV:**  
**lambda < 0.022 @ 95% C.L.**

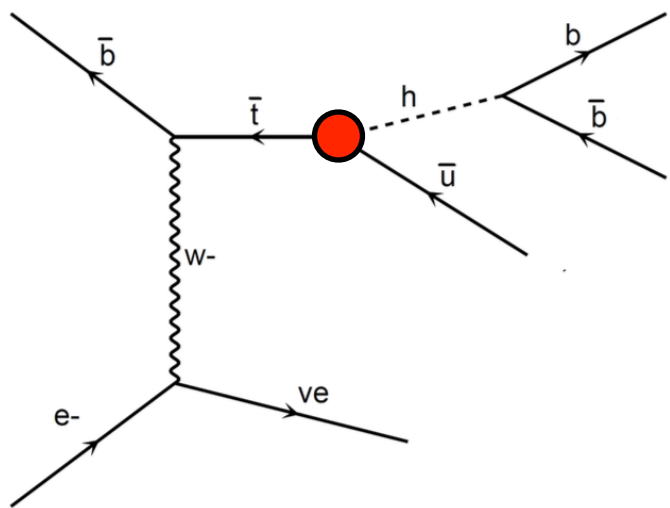
**50 < M<sub>jj</sub> < 100 GeV**  **500 fb<sup>-1</sup>, sqrt(s) = 250 GeV:**  
**lambda < 0.02 @ 95% C.L.**



# Search for Anomalous FCNC $tHu$ Coupling

signal

Sun, Wang,  
arXiv:1602.04670 [hep-ph]



$e^- p \rightarrow \nu_e \bar{t} \rightarrow \nu_e h \bar{q} \rightarrow \nu_e b \bar{b} \bar{q}, \quad q = u, c$

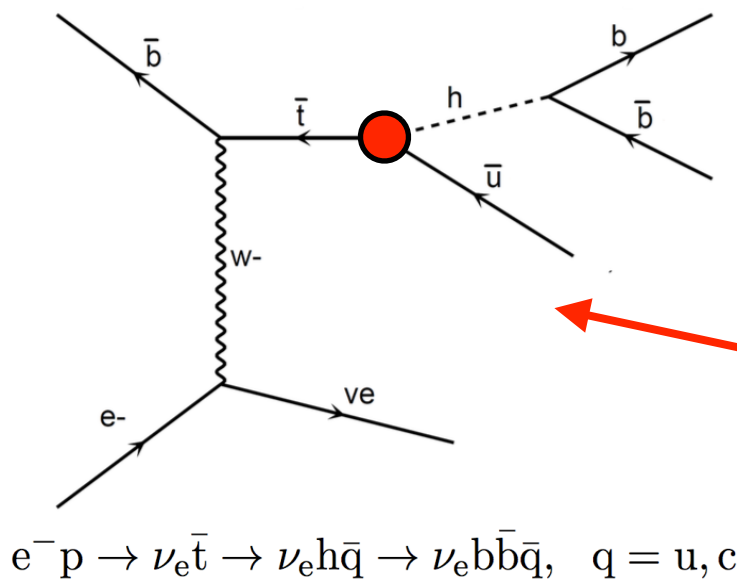
$$\mathcal{L} = \kappa_{tuh} \bar{t} u h + \kappa_{tch} \bar{t} c h + \text{h.c.}$$

# Search for Anomalous FCNC tHu Coupling

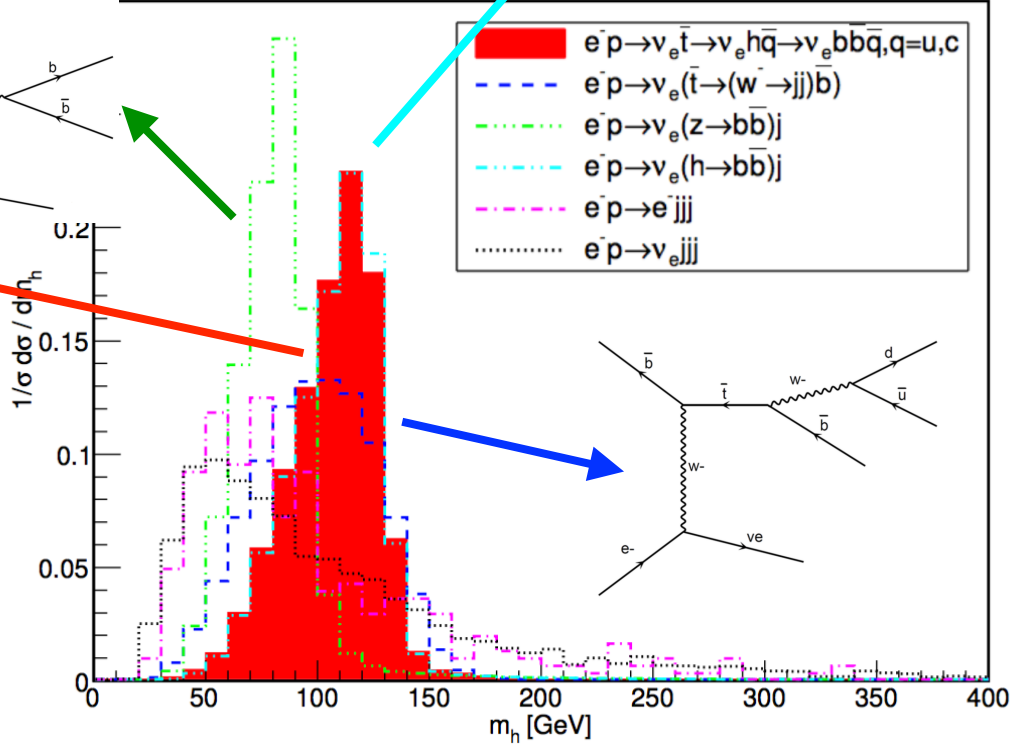
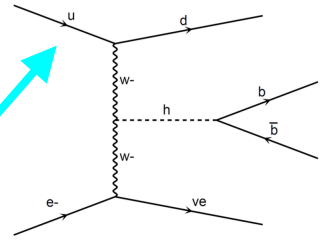
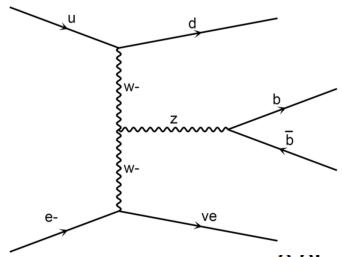
**signal**

Sun, Wang,  
arXiv:1602.04670 [hep-ph]

**background**



$$\mathcal{L} = \kappa_{tuh} \bar{t} u h + \kappa_{tch} \bar{t} c h + h.c.$$

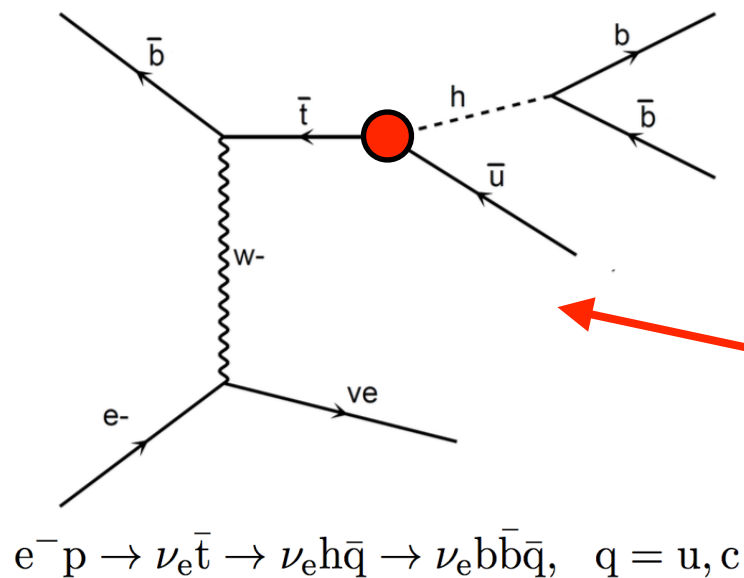


# Search for Anomalous FCNC tHu Coupling

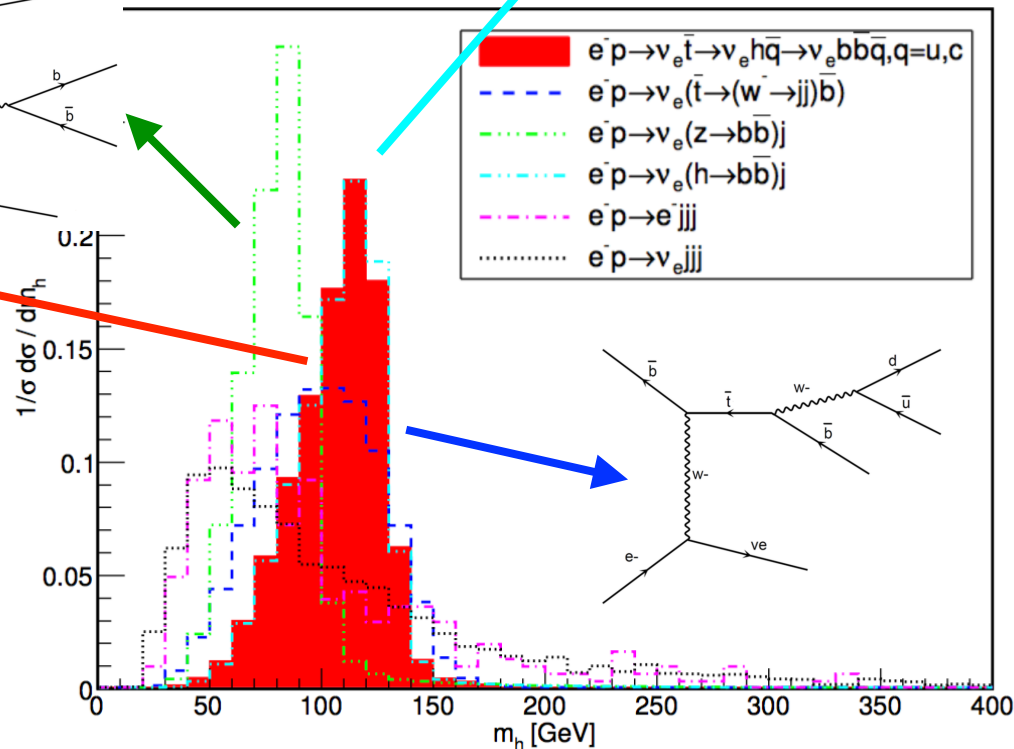
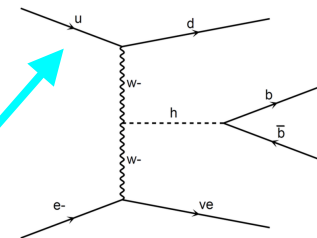
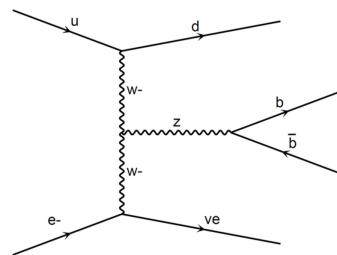
signal

Sun, Wang,  
arXiv:1602.04670 [hep-ph]

background



$$\mathcal{L} = \kappa_{tuh} \bar{t} u h + \kappa_{tch} \bar{t} c h + \text{h.c.}$$



- parametrised assumed resolutions for electrons/photons, muons, jets and unclustered energy using ATLAS values
- b-tag rate of 60%, c-jet fake rate of 10%, light-jet fake rate of 1%
- selections optimized for LHeC and FCC-ep scenarios ( $s/\sqrt{(S+B)}$ )
- cut-based and MVA-based analyses

# Upper Limit on $\text{Br}(t \rightarrow uH)$ in MVA analysis

Sun, Wang,  
arXiv:1602.04670 [hep-ph]

parametrisation

HL-LHC

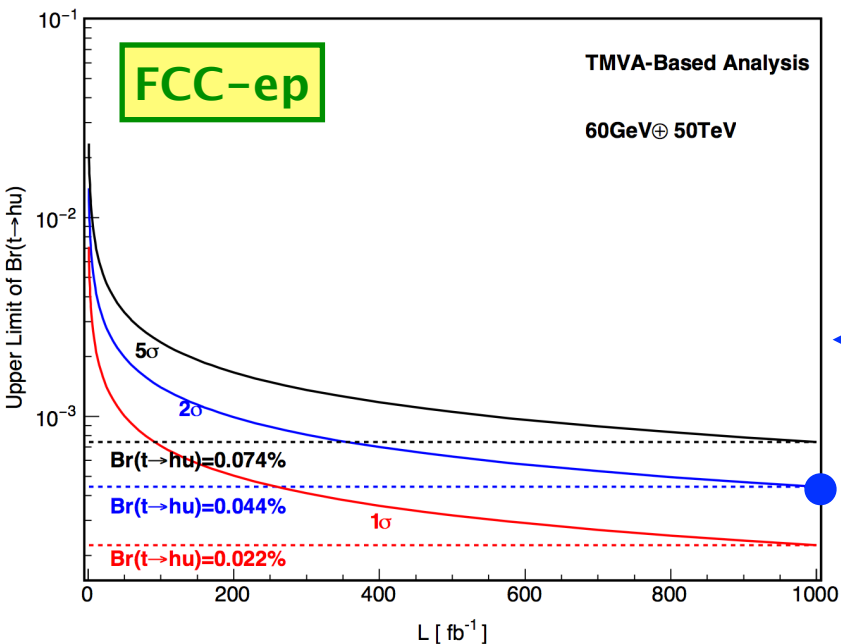
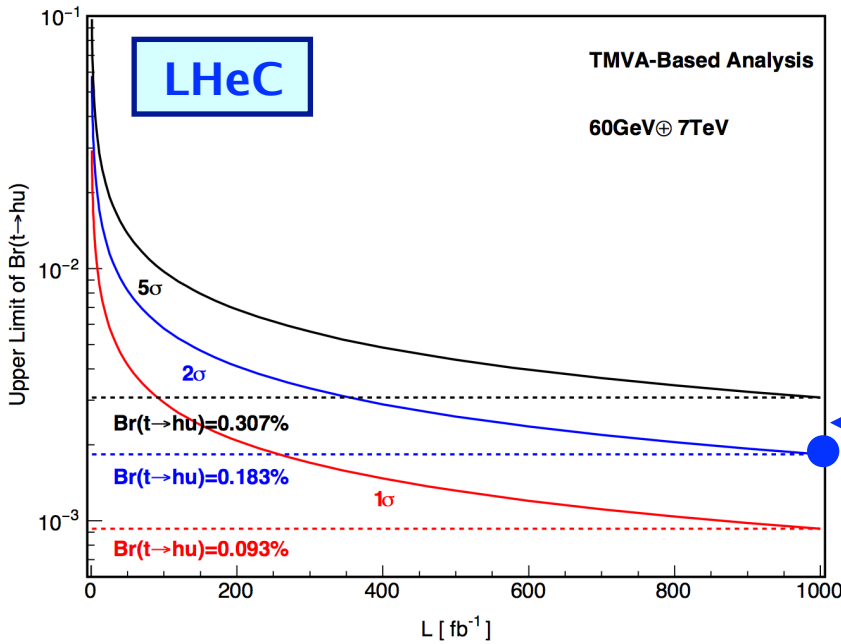
LHC,  $3000 \text{ fb}^{-1}$  @ 14 TeV

HL-LHC

LHC,  $3000 \text{ fb}^{-1}$  @ 14 TeV

--- observation

→ improves sensitivity of HL-LHC

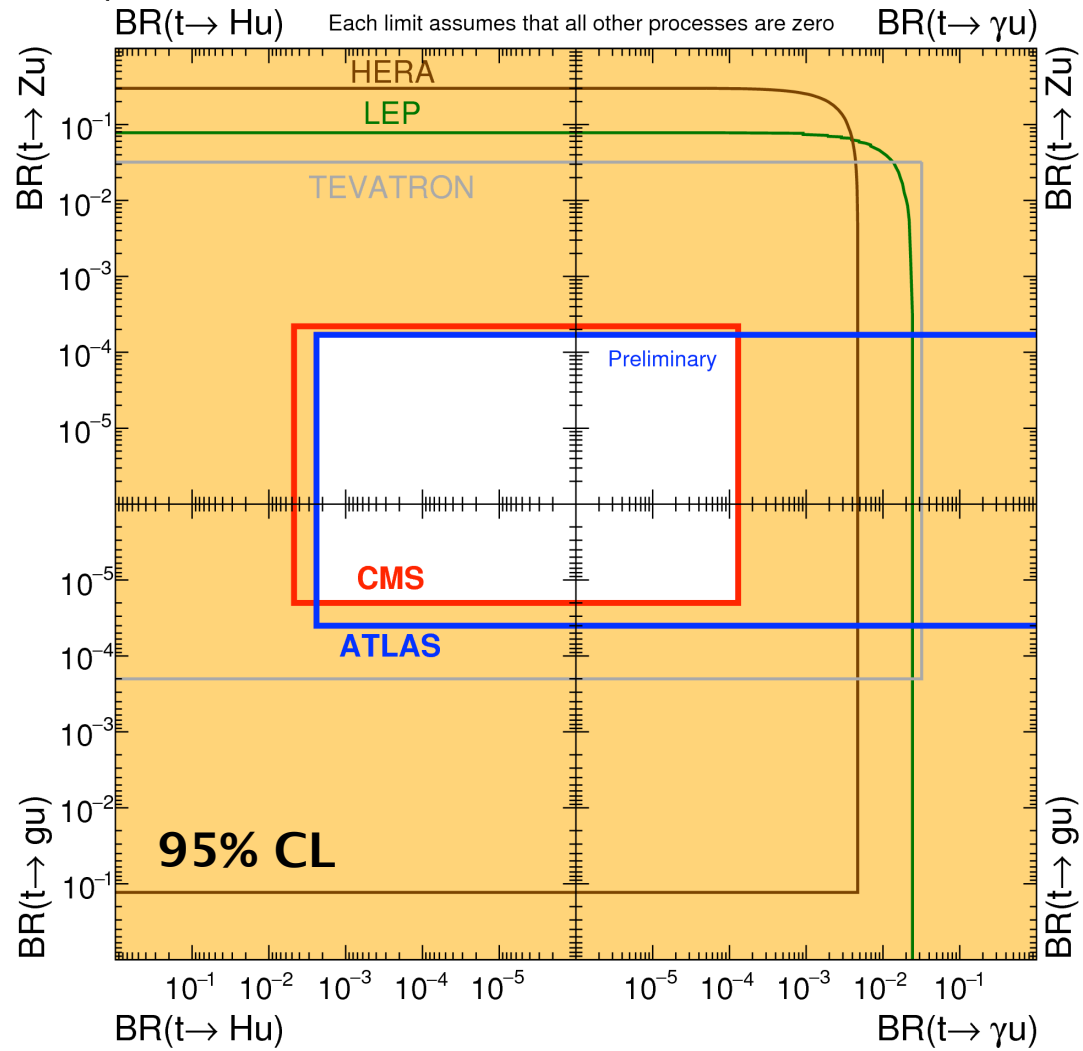




# FCNC Branching Ratios at Colliders

ATLAS+CMS Preliminary  
LHCtopWG

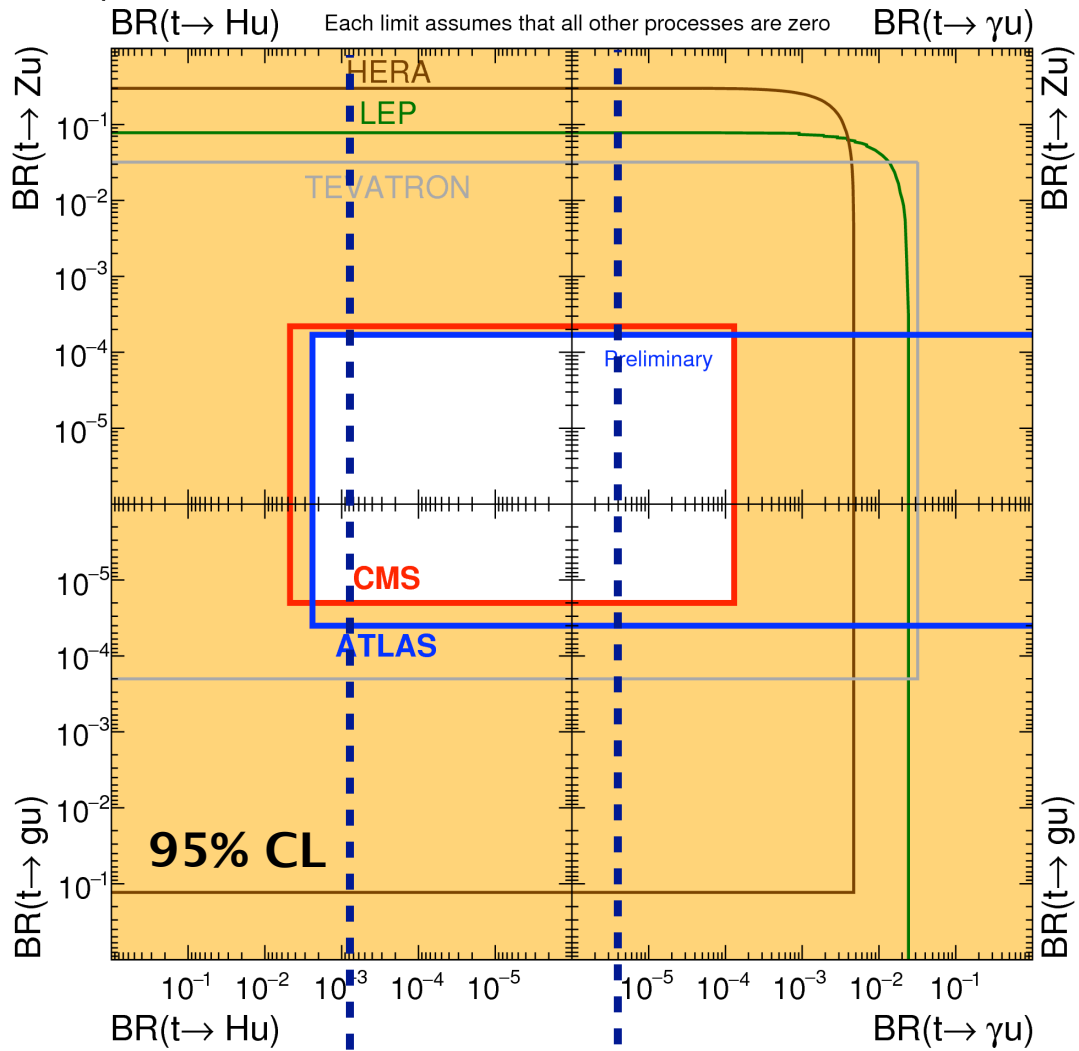
November 2017



# FCNC Branching Ratios at Colliders

ATLAS+CMS Preliminary  
LHCtopWG

November 2017



$E_e = 60 \text{ GeV}$   
 $1000 \text{ fb}^{-1}$

MVA

LHeC

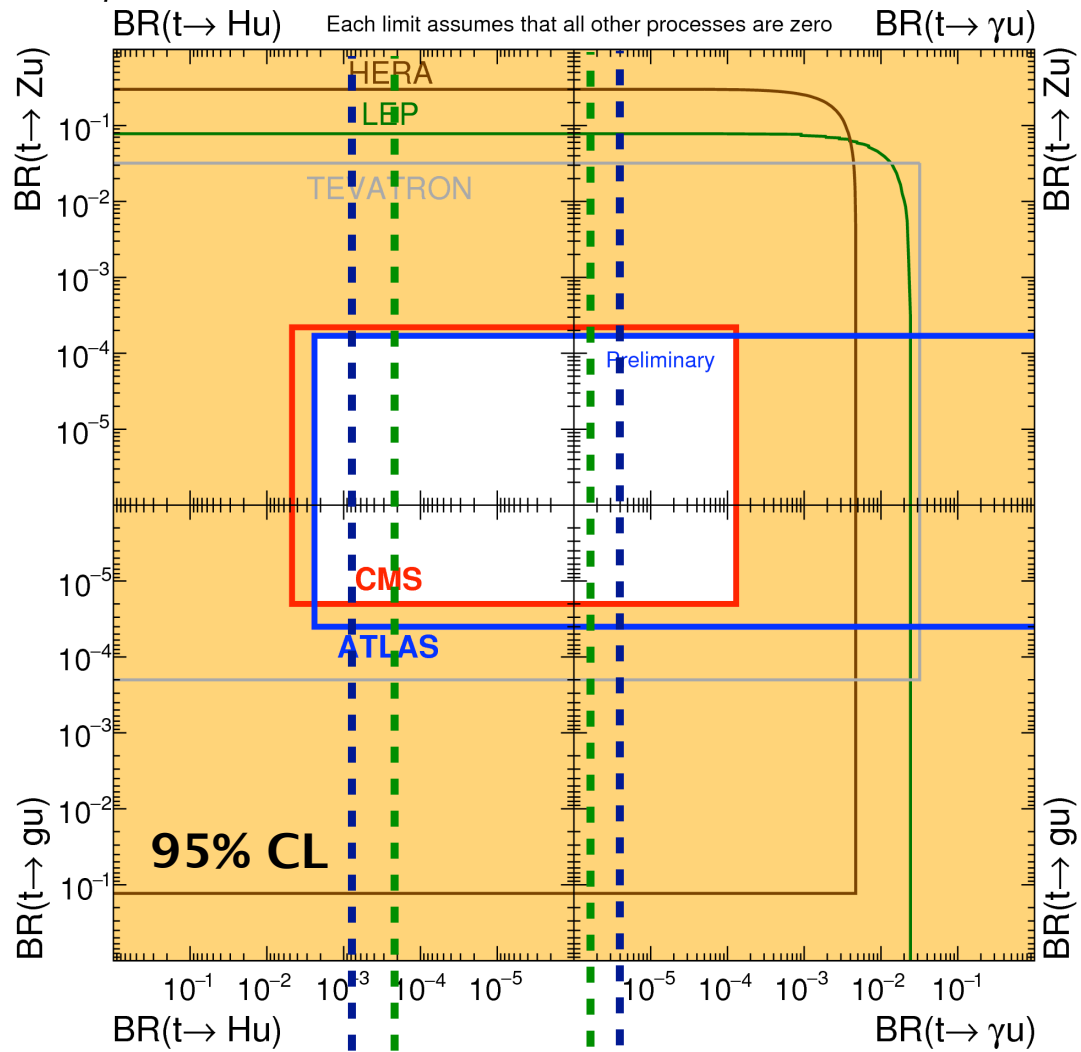
LHeC

cut-based

# FCNC Branching Ratios at Colliders

ATLAS+CMS Preliminary  
LHCtopWG

November 2017



$E_e = 60 \text{ GeV}$   
 $1000 \text{ fb}^{-1}$

MVA

LHeC

FCC-ep

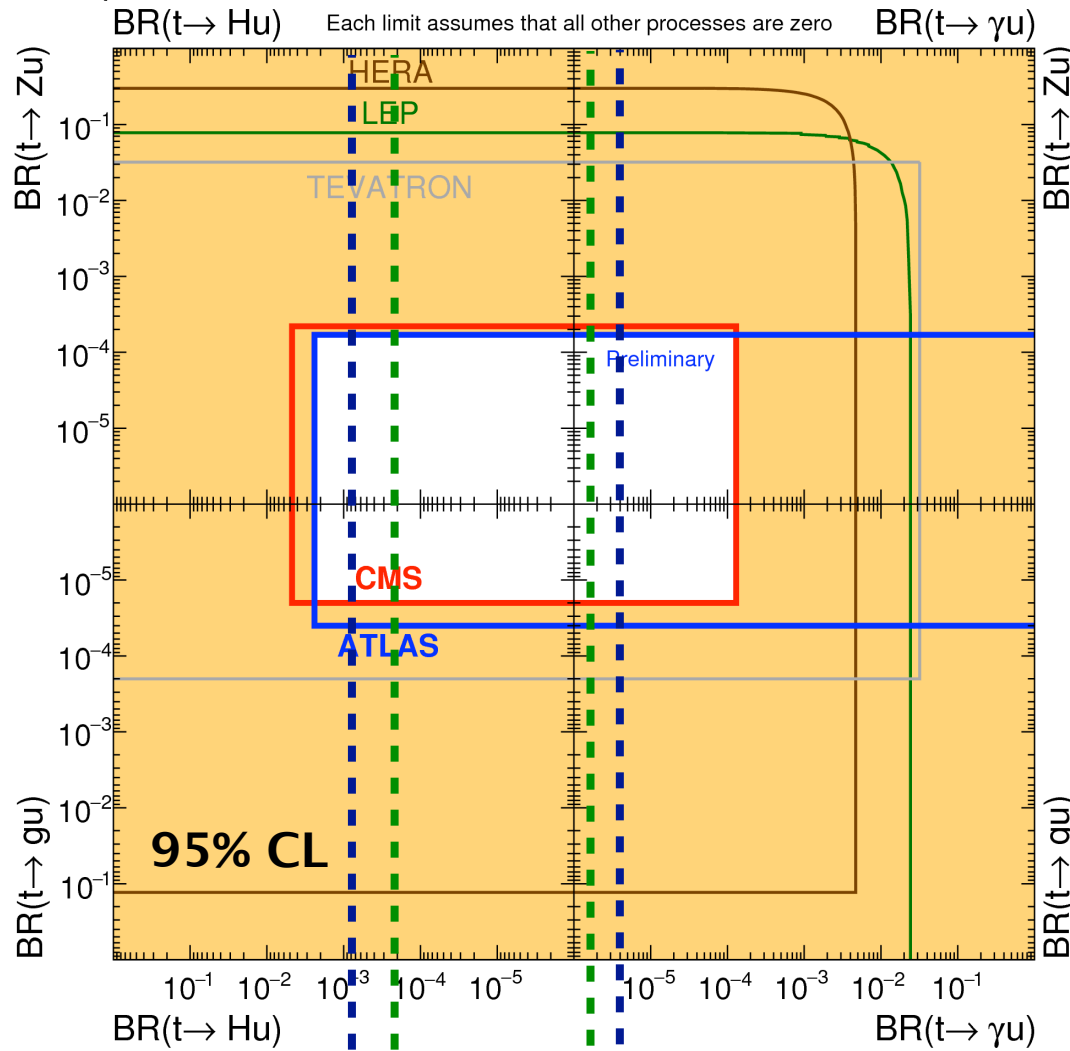
LHeC

cut-based

# FCNC Branching Ratios at Colliders

ATLAS+CMS Preliminary  
LHCtopWG

November 2017



● improve limits on BR(t → γu), BR(t → Hu) considerably

→ test SUSY, little Higgs, technicolor...

$E_e = 60 \text{ GeV}$   
 $1000 \text{ fb}^{-1}$

MVA

LHeC

FCC-ep

LHeC

cut-based

# Outline

**Introduction**  
**CC Top Production**  
**NC Top Production**  
**BSM Top Production**  
**Conclusions**

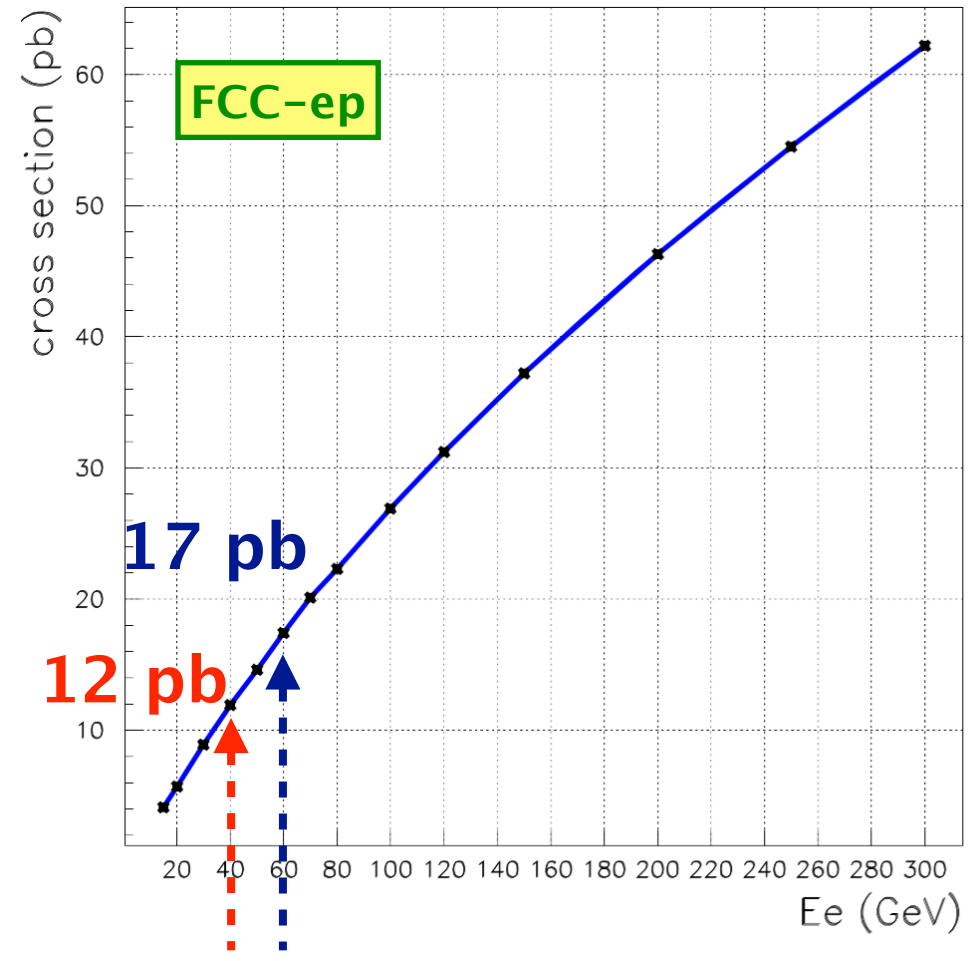
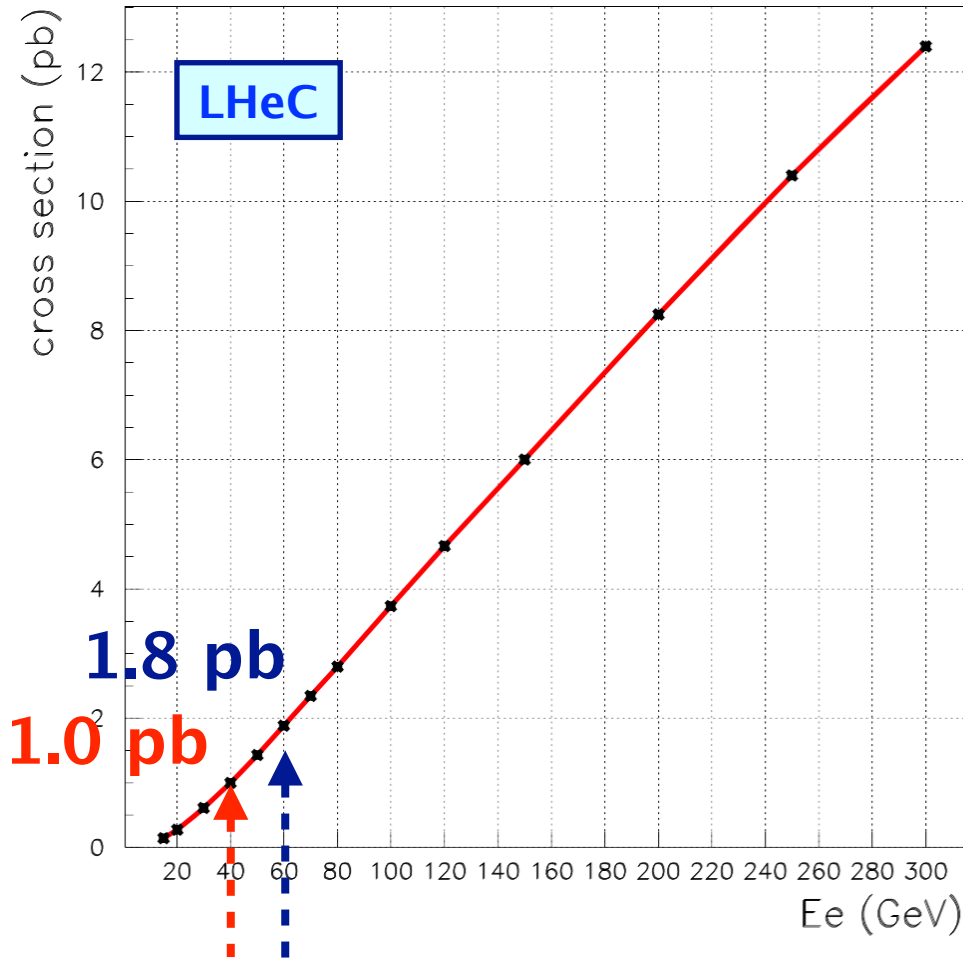
# Summary

- **future ep collider has a rich analysis programme for top quark physics**
  - **single top quark factory:  $|V_{tb}|$  ( $\sim 1\%$ )**
  - **top quark couplings to electroweak bosons (Wtb, tt $\gamma$ , ttZ, ttH, ...)**
  - **analyse top quark properties with high precision: polarisation, charge, PDFs of tops, ...**
  - **many stringent searches for new physics: anomalous couplings, FCNC, CP violation in top–Yukawa, heavy top, SUSY stops...**
- further exciting studies/updates to come for**



# Backup

# CC Single Top Quark Cross Section



40 GeV 60 GeV

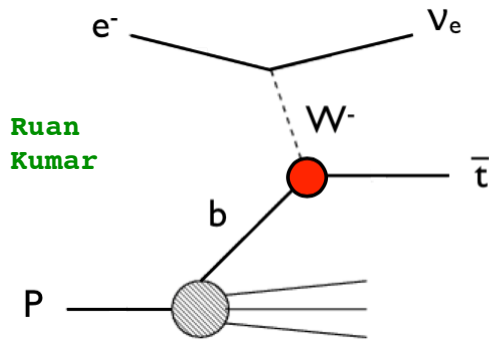
O. Behnke,  
Madgraph

40 GeV 60 GeV

→ strong rise of cross section with electron beam energy



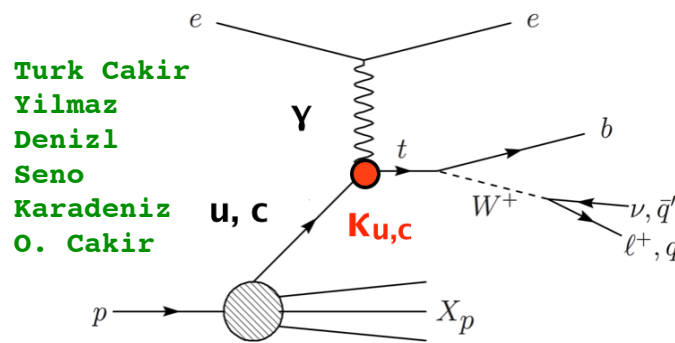
# Status: Top Quark SM+BSM



Ruan Kumar

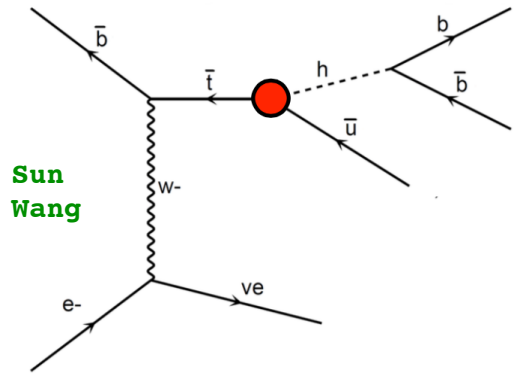
$$L = -\frac{g}{\sqrt{2}} \bar{b} \gamma^\mu V_{tb} (f_V^L P_L - f_V^R P_R) t W_\mu^- - \frac{g}{\sqrt{2}} \bar{b} i\sigma^{\mu\nu} q_\nu (f_T^L P_L - f_T^R P_R) t W_\mu^- + h.c.$$

= 1 in SM



Turk Cakir  
Yilmaz Denizl  
Seno Karadeniz  
O. Cakir

$$L = -g_e \sum_{q=u,c} Q_q \frac{\kappa_q}{\Lambda} \bar{t} \sigma^{\mu\nu} (f_q + h_q \gamma_5) q A_{\mu\nu} + h.c.$$



Sun Wang

$$\mathcal{L} = \kappa_{tuh} \bar{t} u h + \kappa_{tch} \bar{t} c h + h.c.$$

DELPHES

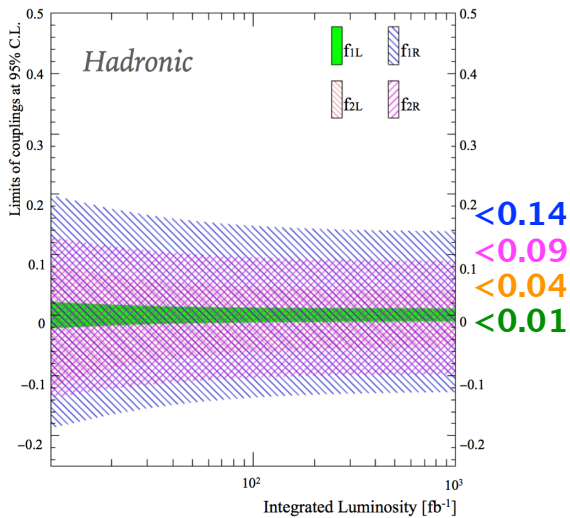
LHeC+FCC

DELPHES

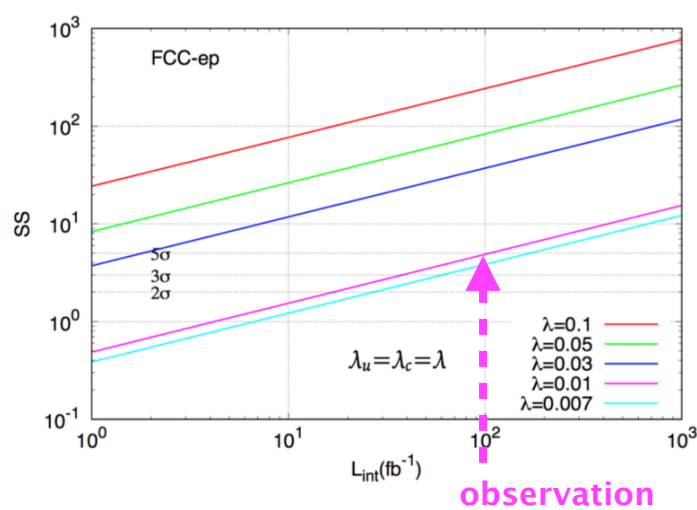
LHeC+FCC

parametrisation

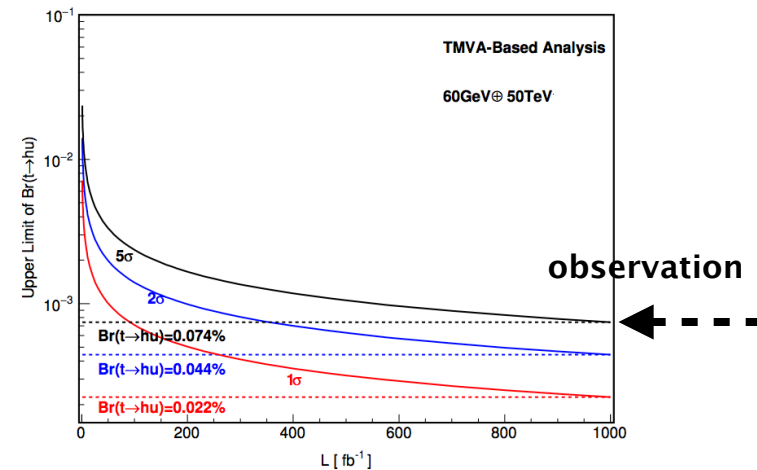
LHeC+FCC



→ to be published  
→ ask for SM cross sections



→ published: arXiv:1705.05419  
→ ask for BR(t→qγ)

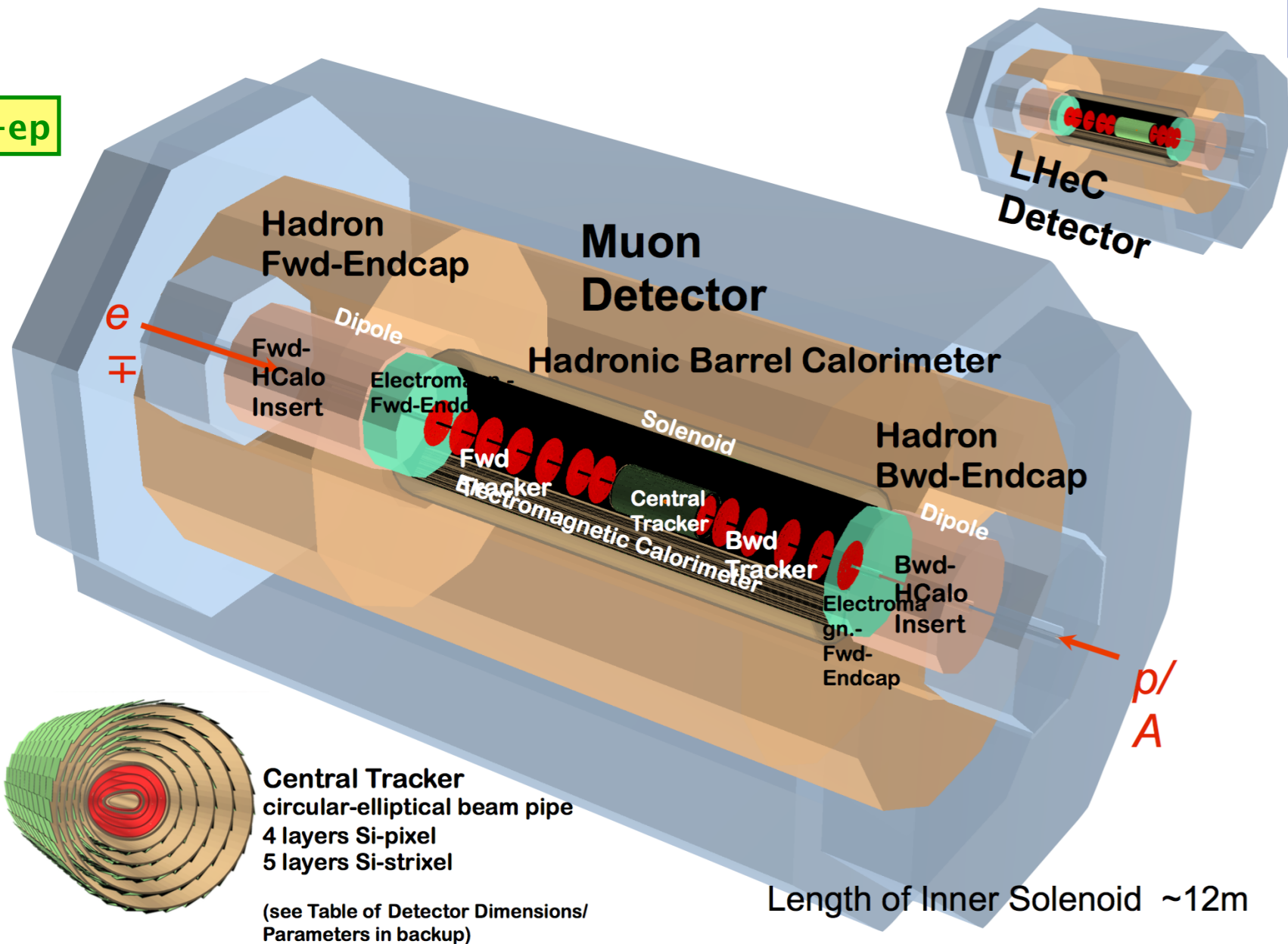


→ published: arXiv:1602.04670

# LHeC and FCC-eh Detector Layout

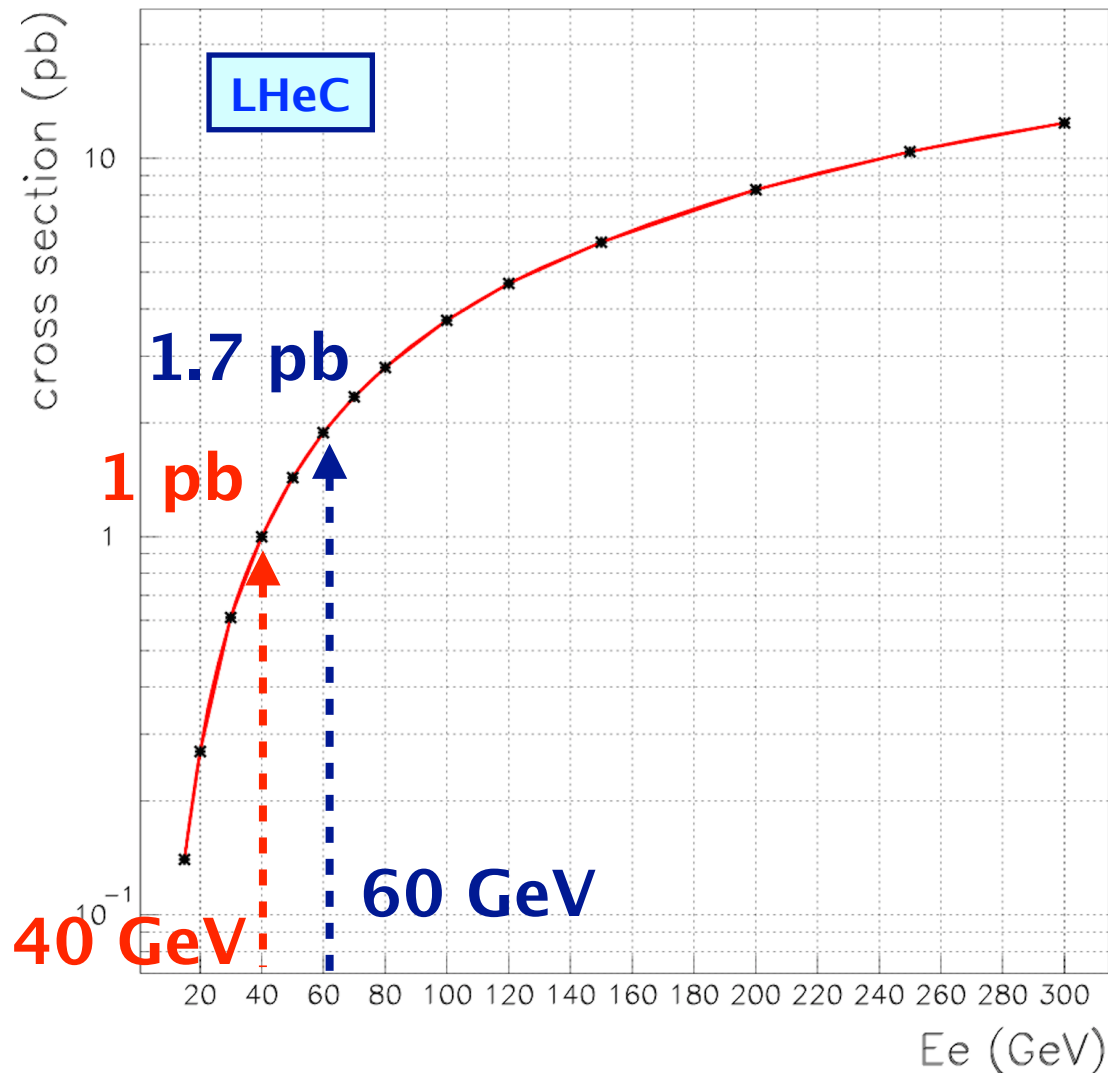
FCC-ep

LHeC



# CC Single Top Quark Cross Section

O. Behnke,  
Madgraph

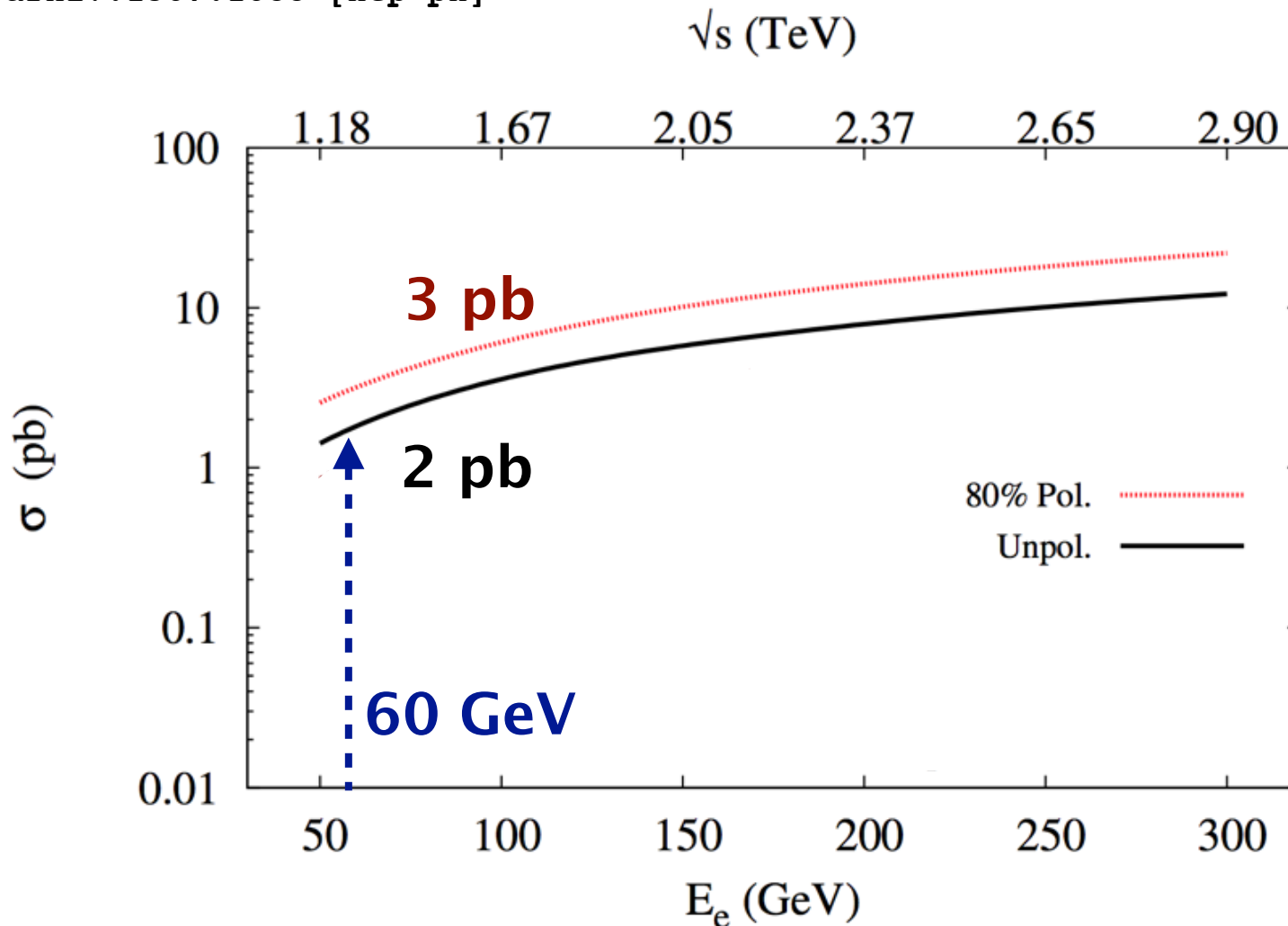


- LHeC offers excellent prospects for top quark physics
- strong rise of cross section with electron beam energy

# CC Single Top Quark Cross Section

Dutta, Goyal, Kumar, Mellado,  
arXiv:1307.1688 [hep-ph]

**100 fb<sup>-1</sup>:**  
**2 · 10<sup>5</sup> events**  
**3 · 10<sup>5</sup> events**



→ LHeC offers excellent prospects for top quark physics

# FCC-eh: tracker, calorimeters and steps

Tracker	FST <sub>pix</sub>	FST <sub>striz</sub>	CFT <sub>pix</sub>	CPT <sub>pix</sub>	CST <sub>striz</sub>	CBT <sub>pix</sub>	BST <sub>striz</sub>	BST <sub>pix</sub>
#Wheels	7		2	—	—	2	5	
#Rings/Wheel	2 <sub>inner</sub>	3 <sub>outer</sub>	3/4	—	—	3/4	3 <sub>outer</sub>	2 <sub>inner</sub>
#Layers	—	—	—	4	5	—	—	—
$\theta_{min/max}$ [°]	0.5	3.8	3.6	5.1	24/155	176.4	173.1	179.3
$\eta_{max/min}$	5.4	3.4	3.5	±3.1	±1.4	-3.5	-2.8	-5.2
Si <sub>pix/striz</sub> [m <sup>2</sup> ]	9.7	13.3	2.8	5.4	33.7	2.8	9.7	6.9
Sum-Si [m <sup>2</sup> ]	84.3 double layers taken into account							
Calo	FHC <sub>SiW</sub>	FEC <sub>SiW</sub>	EMC <sub>SciPb/LAr</sub>	HAC <sub>SciFe</sub>		BEC <sub>SiPb</sub>	BHC <sub>SiFe</sub>	
$\theta_{min/max}$ [°]	0.3	0.4	5.6/173.4	8.6/167		179.4	179.6	
$\eta_{max/min}$	6.0	5.6	3.0/-2.7	2.5/-2.2		-5.3	-5.6	
Volume [m <sup>3</sup> ]	13.2	3.1	28.8	407		1.98	7.0	
Sum-Si [m <sup>2</sup> ]	461							

Input to detector design: HERA, ATLAS/CMS+their upgrades, CALICE, LHeC (CDR and update)

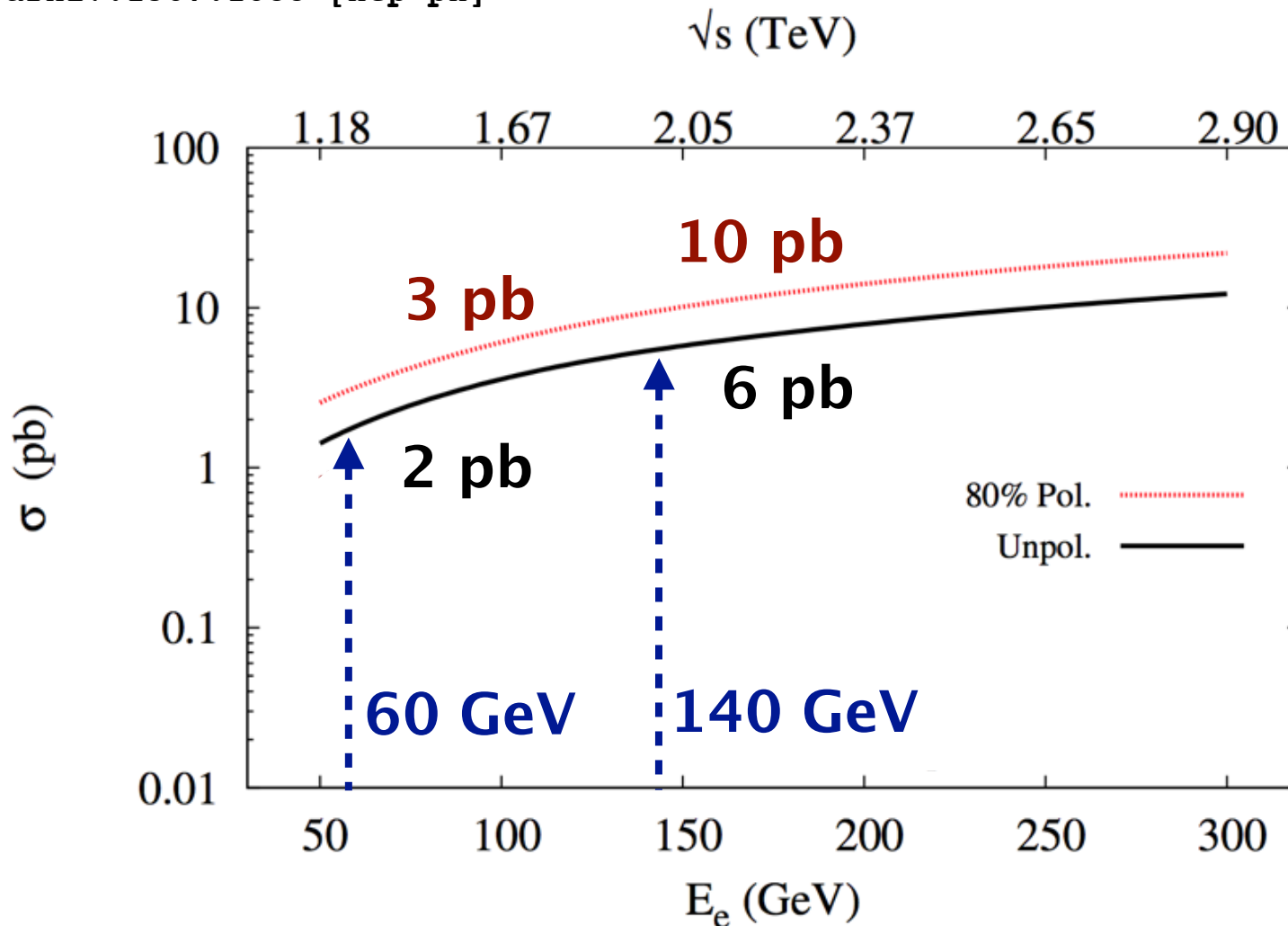
At FCC-eh unlike LHeC we think muon momentum measurement is vital (H- $\mu\mu$ )

Next steps: final choice of CDR technology, IR integration, joint eh-hh consideration, software

# CC Single Top Quark Cross Section

Dutta, Goyal, Kumar, Mellado,  
arXiv:1307.1688 [hep-ph]

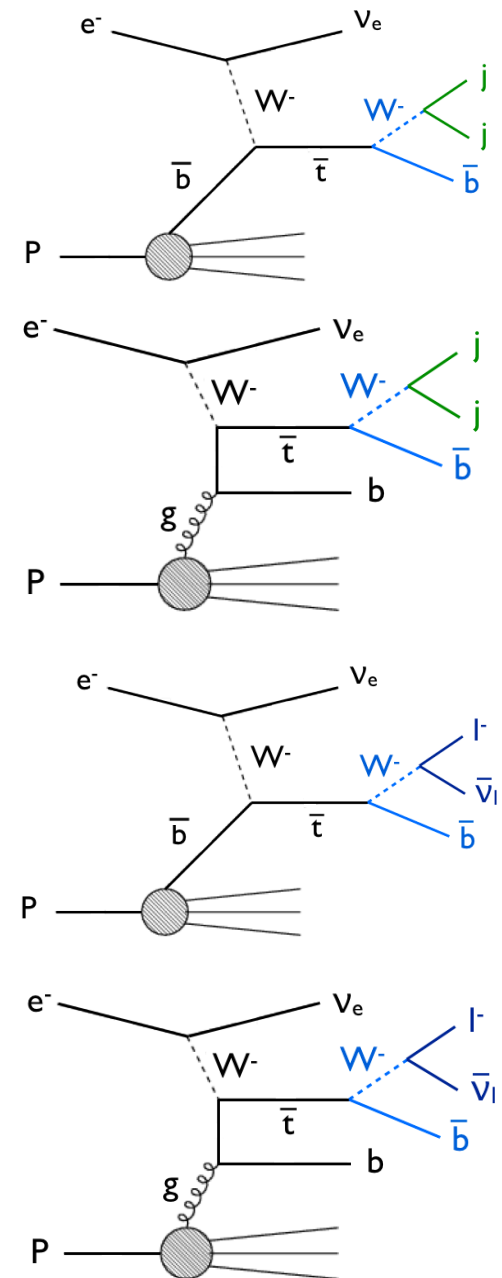
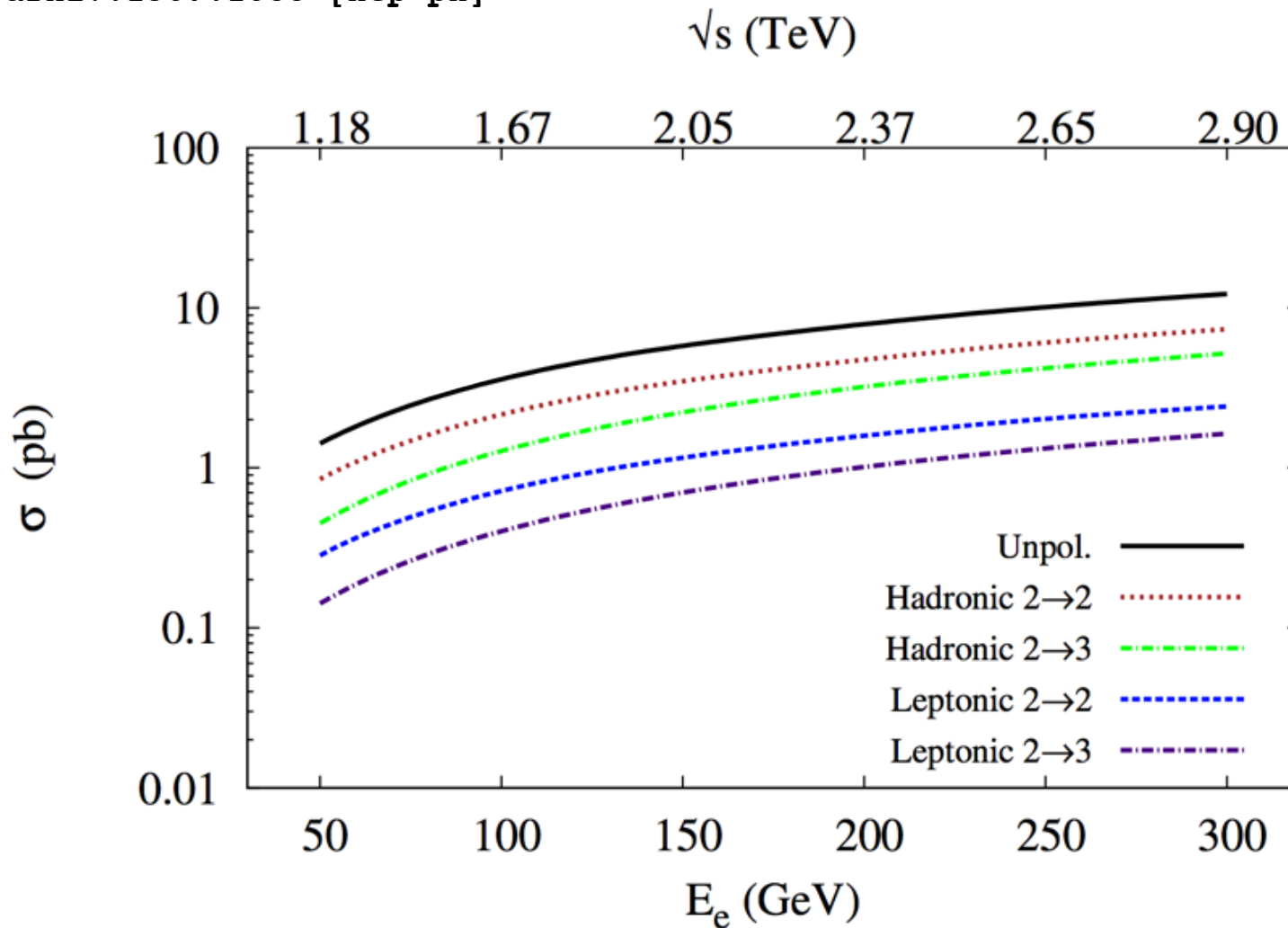
**100 fb<sup>-1</sup>:**  
**2-6 · 10<sup>5</sup> events**  
**3-10 · 10<sup>5</sup> events**



→ LHeC offers excellent prospects for top quark physics

# CC Single Top Quark Cross Section

Dutta, Goyal, Kumar, Mellado,  
arXiv:1307.1688 [hep-ph]



# Backgrounds: Hadronic Channel

No.	Background Process	$p_{T,j,b} \geq 20$ GeV $ \eta_j  \leq 5,  \eta_b  \leq 2.5$ $\Delta R_{j,b/j} \geq 0.4$ $\cancel{E}_T \geq 25$	$\Delta\Phi_{\cancel{E},j} \geq 0.4$ $\Delta\Phi_{\cancel{E},b} \geq 0.4$	$ m_{j_1j_2} - m_W  \leq 22$ GeV	$\sigma_{\text{eff.}}$
1	$e^-p \rightarrow \nu_e W^- \bar{b}$ without anti-top line	$7.5 \times 10^{-3}$	$6.8 \times 10^{-3}$	$4.5 \times 10^{-3}$	$2.7 \times 10^{-3}$
2	$e^-p \rightarrow \nu_e jjj$	$4.2 \times 10^0$	$3.6 \times 10^0$	$2.4 \times 10^0$	$7.2 \times 10^{-2}$
3	$e^-p \rightarrow \nu_e cjj$ & $e^-p \rightarrow \nu_e \bar{c}jj$	$1.5 \times 10^0$	$1.2 \times 10^0$	$8.6 \times 10^{-1}$	$8.6 \times 10^{-2}$
4	$e^-p \rightarrow \nu_e c\bar{c}j$	$5.8 \times 10^{-2}$	$5.0 \times 10^{-2}$	$3.2 \times 10^{-2}$	$6.7 \times 10^{-3}$
5	$e^-p \rightarrow \nu_e b\bar{b}j$	$2.5 \times 10^{-2}$	$2.2 \times 10^{-2}$	$5.6 \times 10^{-3}$	$1.3 \times 10^{-3}$
6	$e^-p \rightarrow \bar{c}\nu_e$ ( $\bar{c} \rightarrow W^- \bar{s}$ )	$2.5 \times 10^{-2}$	$2.2 \times 10^{-2}$	$1.5 \times 10^{-2}$	$1.5 \times 10^{-4}$

Event Selection	$p_{T,j,b} \geq 20$ GeV $ \eta_j  \leq 5,  \eta_b  \leq 2.5$ $\Delta R_{j,b/j} \geq 0.4$ $\cancel{E}_T \geq 25$	$\Delta\Phi_{\cancel{E},j} \geq 0.4$ $\Delta\Phi_{\cancel{E},b} \geq 0.4$	$ m_{j_1j_2} - m_W  \leq 22$ GeV	Fiducial Efficiency	$S/\sqrt{S+B}$
$SM$				66.7 %	–
$SM + \sum_i \text{Bkg}_i$				61.5 %	
$ V_{tb}  \Delta f_1^L = .5$				68.0 %	1.92
$f_1^R = .5$				69.7 %	1.43
$f_2^L = .5$				73.2 %	1.55
$f_2^L = -.5$				69.6 %	1.40
$f_2^R = .5$				72.3 %	1.69



# Backgrounds: Leptonic Channel

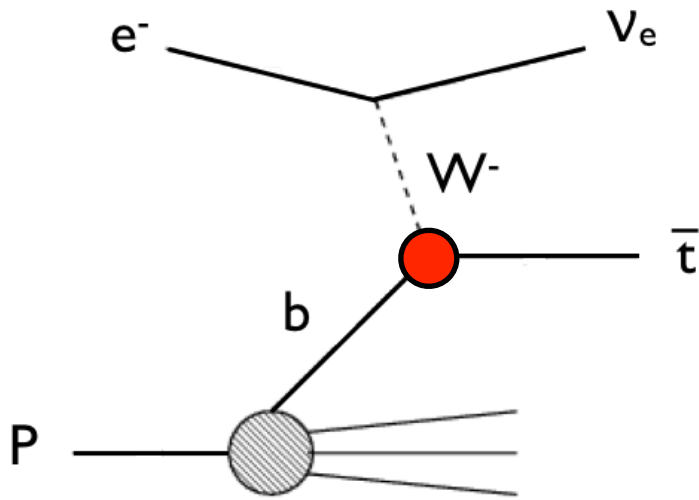
No.	Background Process	$p_{T,j,b,l} \geq 20$ GeV, $\Delta R_{j,b/j} \geq 0.4$ , $\cancel{E}_T \geq 25$ $ \eta_j  \geq 5$ , $ \eta_{b,l}  \geq 2.5$	$\Delta\Phi_{\cancel{E},j} \geq 0.4$ $\Delta\Phi_{\cancel{E},b} \geq 0.4$ $\Delta\Phi_{\cancel{E},l} \geq 0.4$	$\sigma_{\text{eff.}}$
1	$e^- p \rightarrow l^- \bar{\nu}_l \nu_e j$	$1.5 \times 10^{-1}$	$1.4 \times 10^{-1}$	$1.4 \times 10^{-3}$
2	$e^- p \rightarrow l^- \bar{\nu}_l \nu_e c$ & $e^- p \rightarrow l^- \bar{\nu}_l \nu_e \bar{c}$	$6.6 \times 10^{-3}$	$6.1 \times 10^{-3}$	$6.1 \times 10^{-4}$
3	$e^- p \rightarrow l^- \bar{\nu}_l \nu_e b$ & $e^- p \rightarrow l^- \bar{\nu}_l \nu_e \bar{b}$ Without top line	$3.6 \times 10^{-3}$	$3.2 \times 10^{-3}$	$1.9 \times 10^{-3}$
4	$e^- p \rightarrow e^- l^- \bar{\nu}_l c$	$1.5 \times 10^{-2}$	$6.9 \times 10^{-3}$	$6.9 \times 10^{-4}$
5	$e^- p \rightarrow e^- l^- \bar{\nu}_l j$	$1.2 \times 10^{-1}$	$5.5 \times 10^{-2}$	$5.5 \times 10^{-4}$

Event Selection	$p_{T,j,b} \geq 20$ GeV $ \eta_j  \leq 5,  \eta_b  \leq 2.5$ $\Delta R_{j,b/j} \geq 0.4$ $\cancel{E}_T \geq 25$	$\Delta\Phi_{\cancel{E},j} \geq 0.4$ $\Delta\Phi_{\cancel{E},b} \geq 0.4$ $\Delta\Phi_{\cancel{E},l} \geq 0.4$	Fiducial Efficiency	$S/\sqrt{S+B}$
SM	$1.2 \times 10^4$	$1.1 \times 10^4$	92.0 %	–
SM + $\sum_i \text{Bkg}_i$	$1.3 \times 10^4$	$1.2 \times 10^4$	92.0 %	–
$ V_{tb}  \Delta f_1^L = .5$	$4.5 \times 10^4$	$2.5 \times 10^4$	92.6 %	1.55
$f_1^R = .5$	$2.8 \times 10^4$	$1.6 \times 10^4$	94.1 %	1.23
$f_2^L = .5$	$3.1 \times 10^4$	$1.7 \times 10^4$	89.5 %	1.27
$f_2^L = -.5$	$1.8 \times 10^4$	$1.0 \times 10^4$	90.9 %	0.95
$f_2^R = .5$	$3.6 \times 10^4$	$2.0 \times 10^4$	90.9 %	1.38

# Direct Measurement of $|V_{tb}|$

Dutta, Goyal, Kumar, Mellado,  
arXiv:1307.1688 [hep-ph]

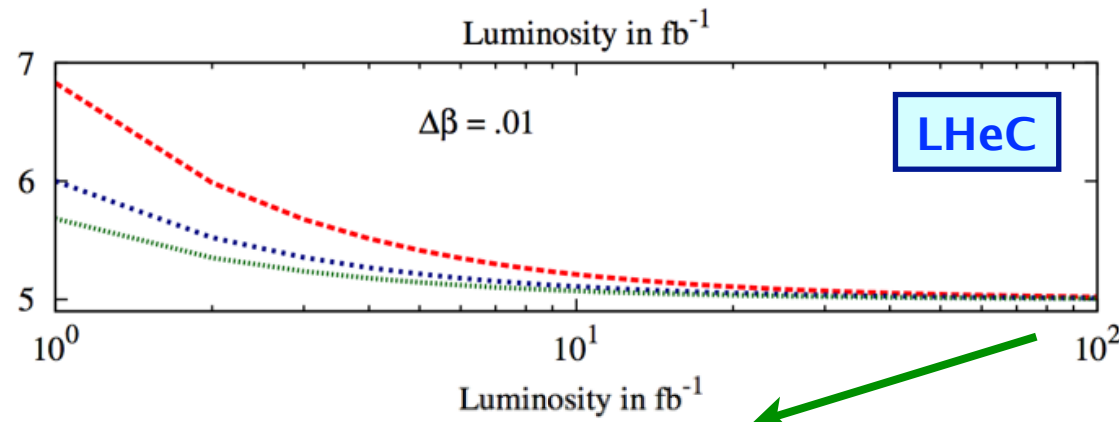
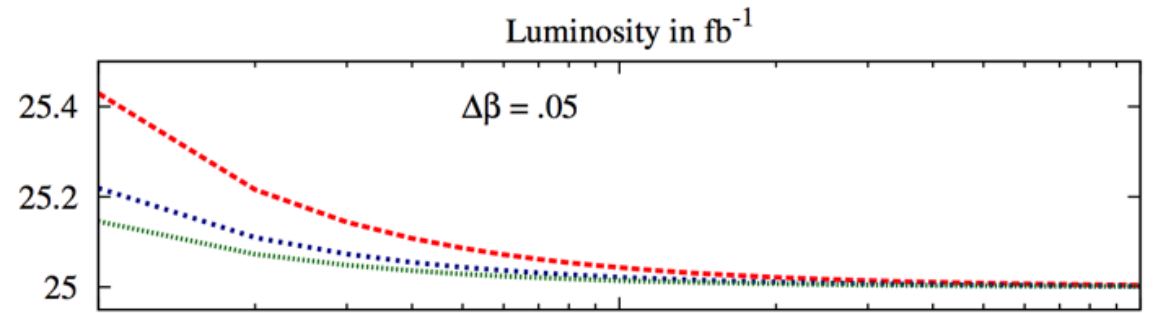
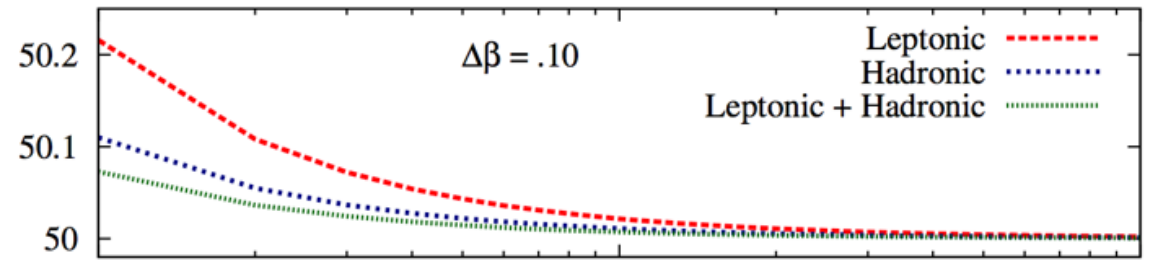
$E_e = 60 \text{ GeV}$



$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

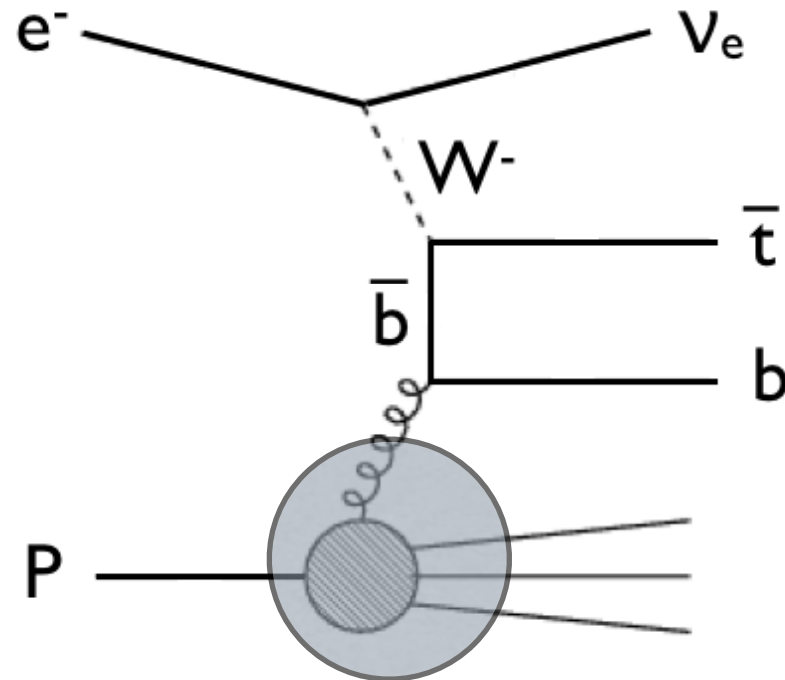
$\Delta|V_{tb}| \cdot 1000$

$\Delta\beta$ : luminosity uncertainty



**$100 \text{ fb}^{-1}: \Delta|V_{tb}| = 0.005$**

# Gluon Parton Density Function



→ measure gluon density at high  $x$

# Search for Anomalous $Wtb$ Couplings

= 1 in SM

$$L = -\frac{g}{\sqrt{2}} \bar{b} \gamma^\mu V_{tb} (f_V^L P_L + f_V^R P_R) t W_\mu^-$$
$$-\frac{g}{\sqrt{2}} \bar{b} \frac{i\sigma^{\mu\nu} q_\nu}{M_W} (f_T^L P_L + f_T^R P_R) t W_\mu^- + h.c.$$

# Search for Anomalous Wtb Couplings

= 1 in SM

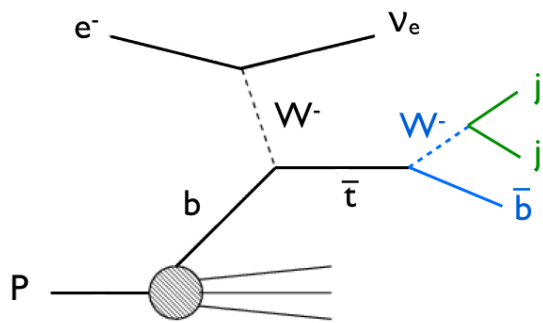
$$L = -\frac{g}{\sqrt{2}} \bar{b} \gamma^\mu V_{tb} (f_V^L P_L + f_V^R P_R) t W_\mu^- - \frac{g}{\sqrt{2}} \bar{b} \frac{i\sigma^{\mu\nu} q_\nu}{M_W} (f_T^L P_L + f_T^R P_R) t W_\mu^- + h.c.$$

# Search for Anomalous Wtb Couplings

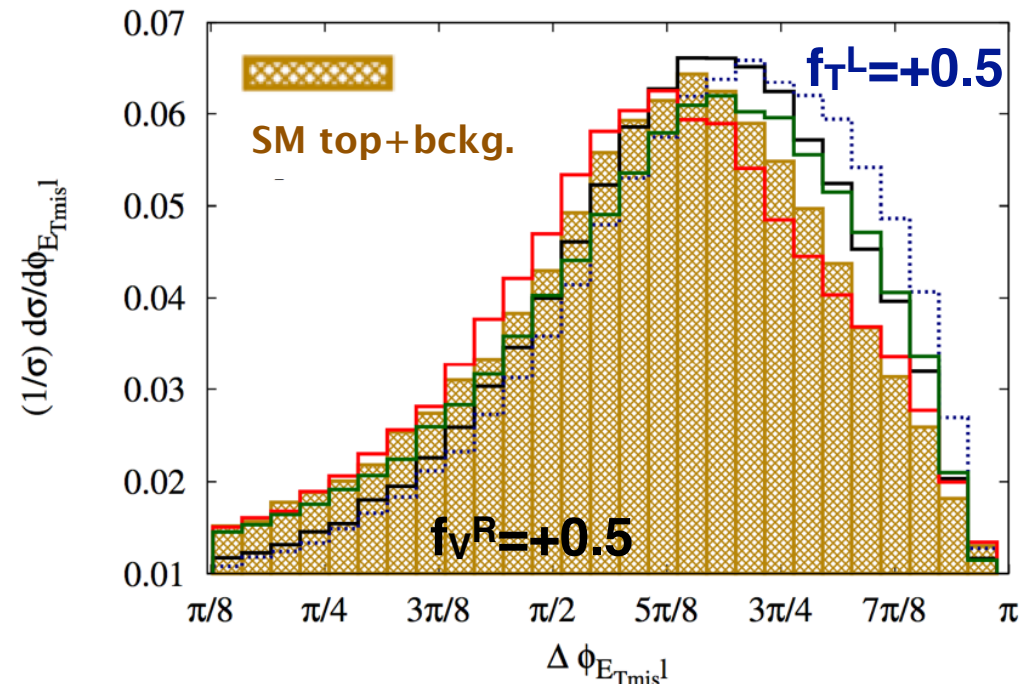
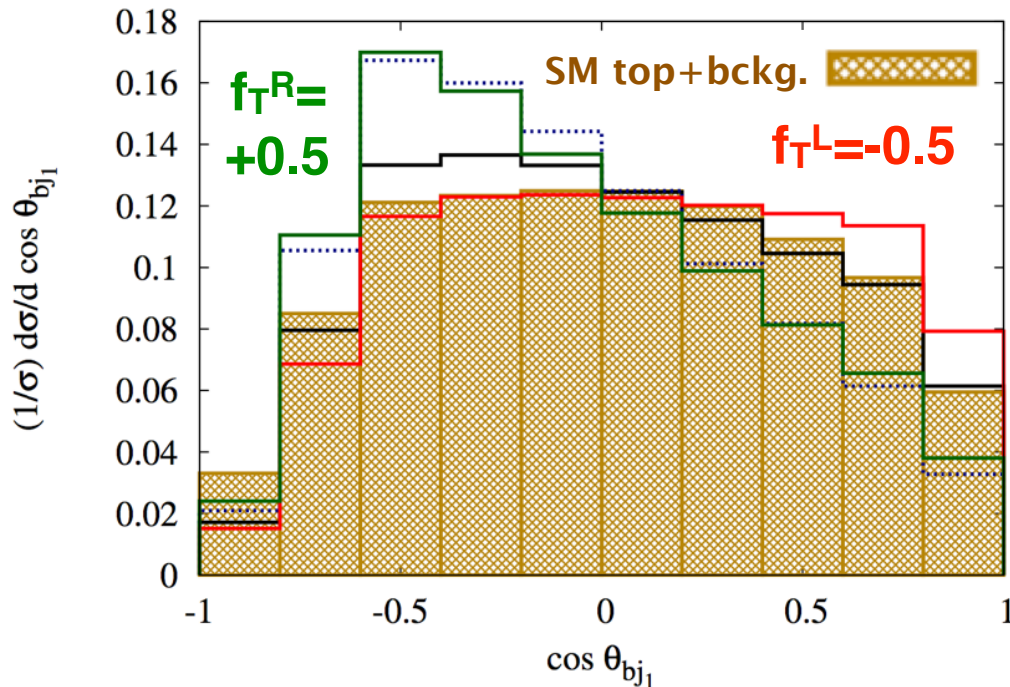
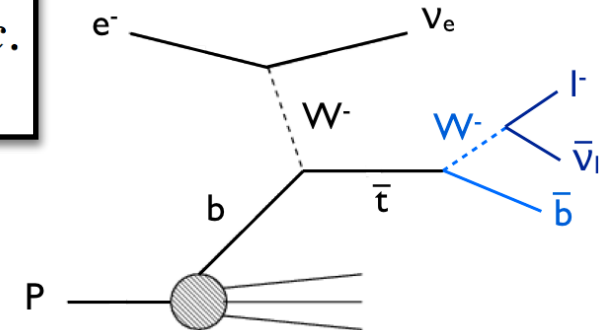
= 1 in SM

$$L = -\frac{g}{\sqrt{2}} \bar{b} \gamma^\mu V_{tb} (f_V^L P_L + f_V^R P_R) t W_\mu^- - \frac{g}{\sqrt{2}} \bar{b} \frac{i\sigma^{\mu\nu} q_\nu}{M_W} (f_T^L P_L + f_T^R P_R) t W_\mu^- + h.c.$$

Dutta, Goyal, Kumar, Mellado, arXiv:1307.1688



$L_{int} = 100 \text{ fb}^{-1}$

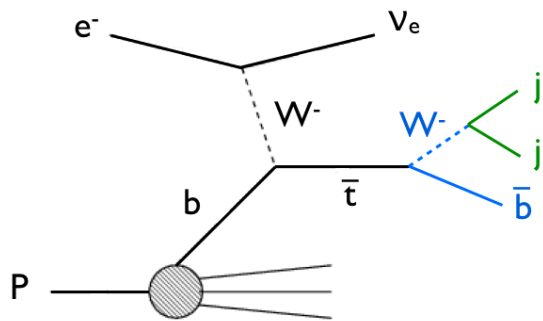


+ other variables sensitive on W helicity

# Search for Anomalous Wtb Couplings

Dutta, Goyal, Kumar,  
Mellado, arXiv:1307.1688

= 1 in SM

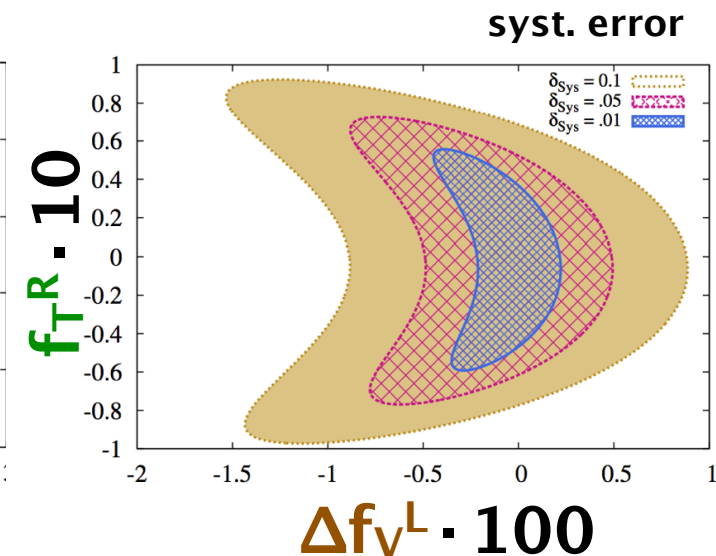
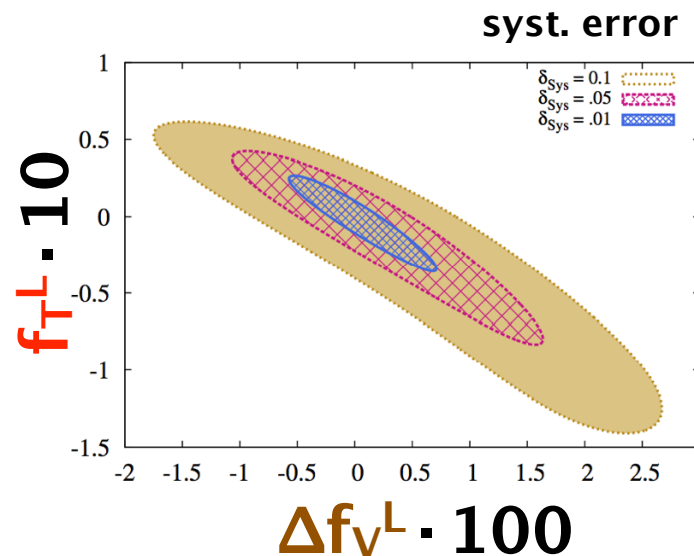
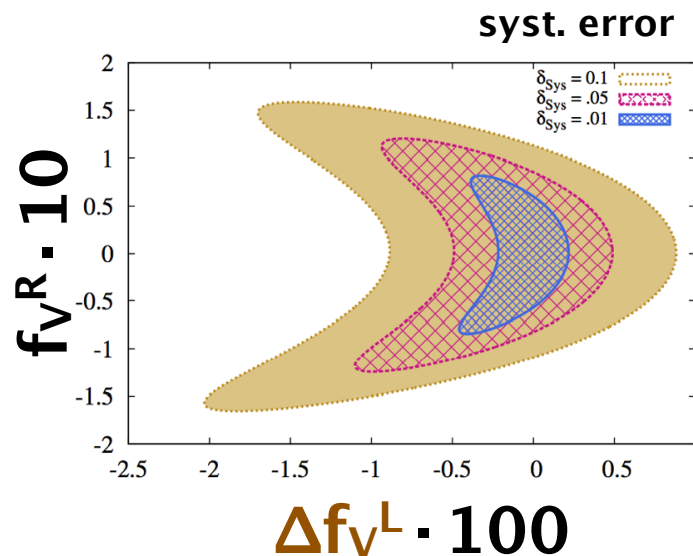


$$L = -\frac{g}{\sqrt{2}} \bar{b} \gamma^\mu V_{tb} (f_V^L P_L + f_V^R P_R) t W_\mu^-$$

$$-\frac{g}{\sqrt{2}} \bar{b} \frac{i\sigma^{\mu\nu} q_\nu}{M_W} (f_T^L P_L + f_T^R P_R) t W_\mu^- + h.c.$$

68% C.L.

property	precision
$f_V^L$	0.001-0.01
$f_V^R, f_T^L, f_T^R$	0.01-0.1

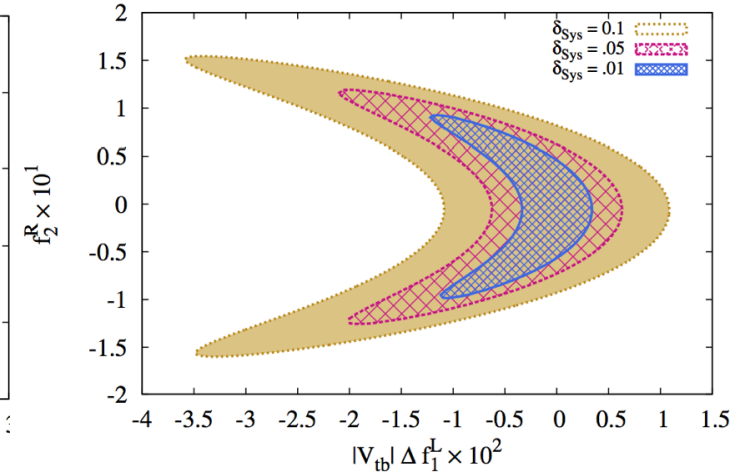
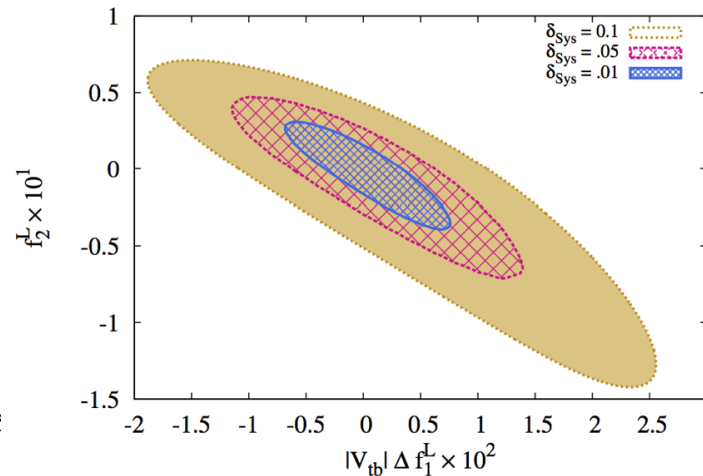
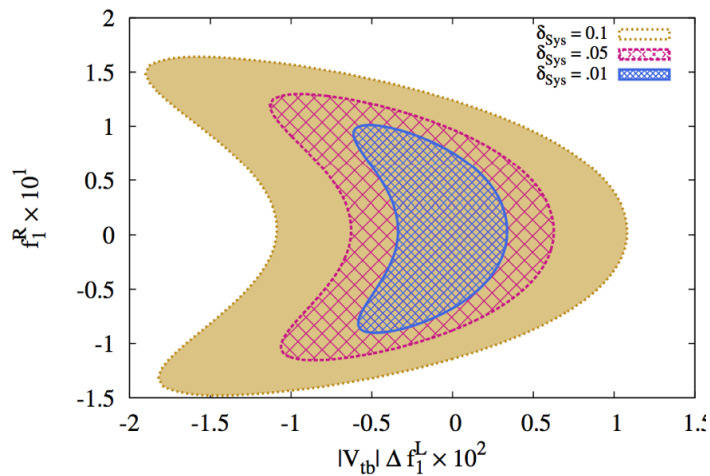
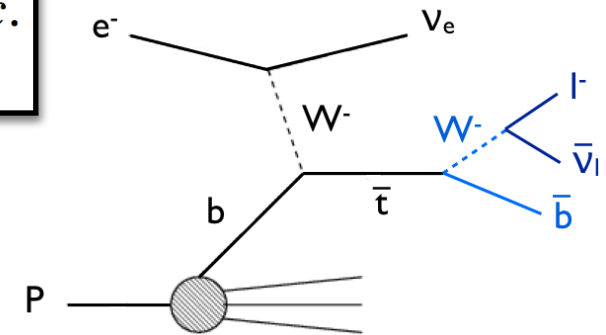


# Search for Anomalous Wtb Couplings

= 1 in SM

$$L = -\frac{g}{\sqrt{2}} \bar{b} \gamma^\mu V_{tb} (f_V^L P_L + f_V^R P_R) t W_\mu^- - \frac{g}{\sqrt{2}} \bar{b} \frac{i\sigma^{\mu\nu} q_\nu}{M_W} (f_T^L P_L + f_T^R P_R) t W_\mu^- + h.c.$$

68% C.L.

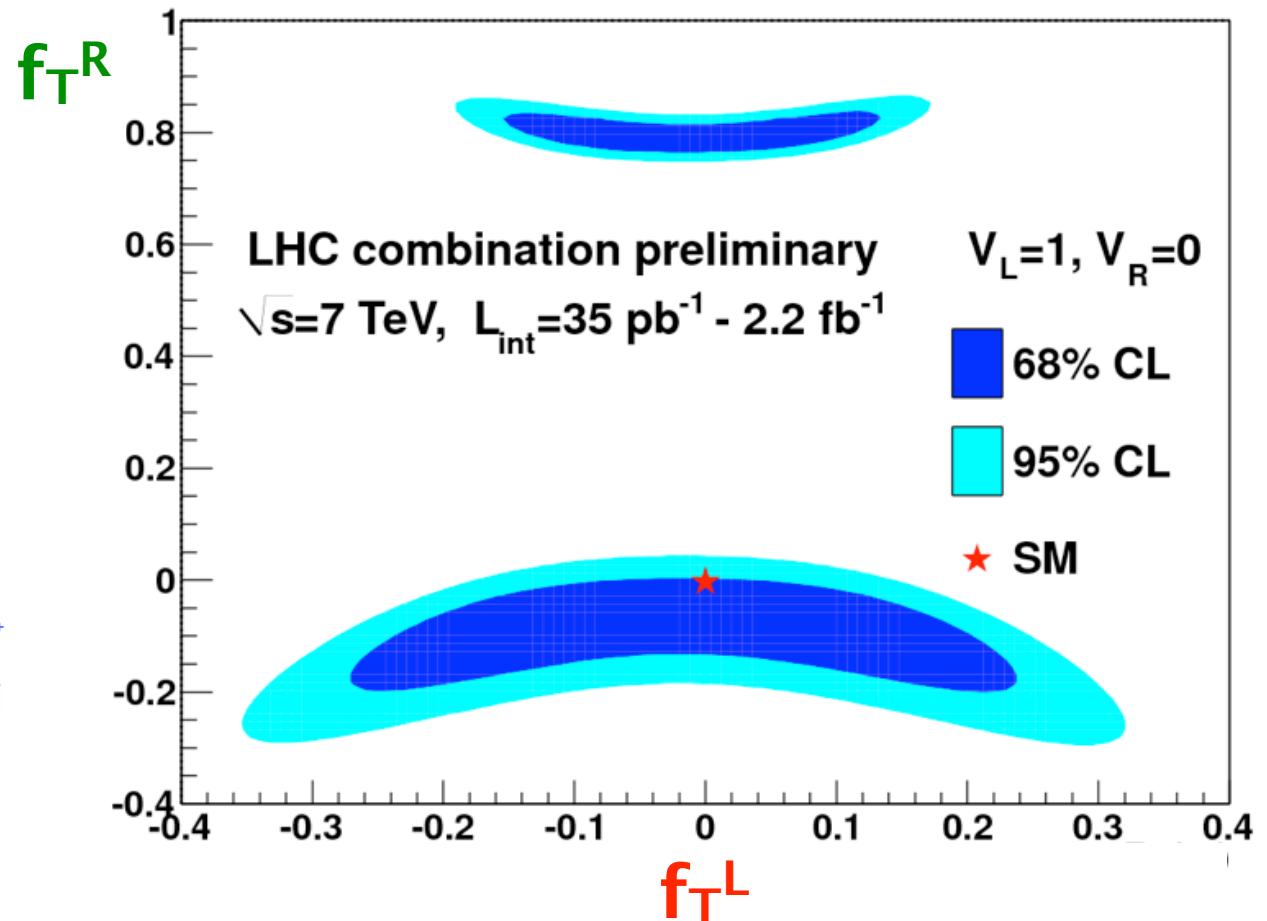
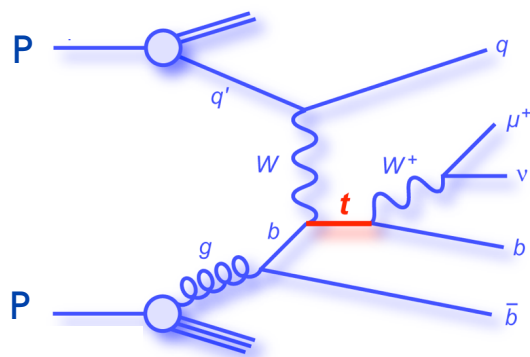




# Search for Anomalous Wtb Couplings

= 1 in SM

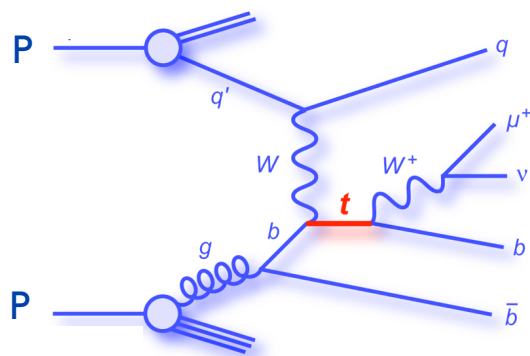
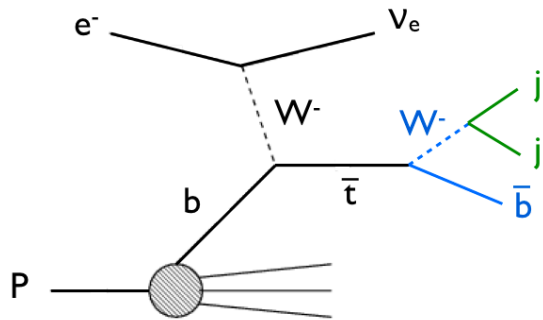
$$L = -\frac{g}{\sqrt{2}} \bar{b} \gamma^\mu V_{tb} (f_V^L P_L + f_V^R P_R) t W_\mu^- - \frac{g}{\sqrt{2}} \bar{b} \frac{i\sigma^{\mu\nu} q_\nu}{M_W} (f_T^L P_L + f_T^R P_R) t W_\mu^- + h.c.$$



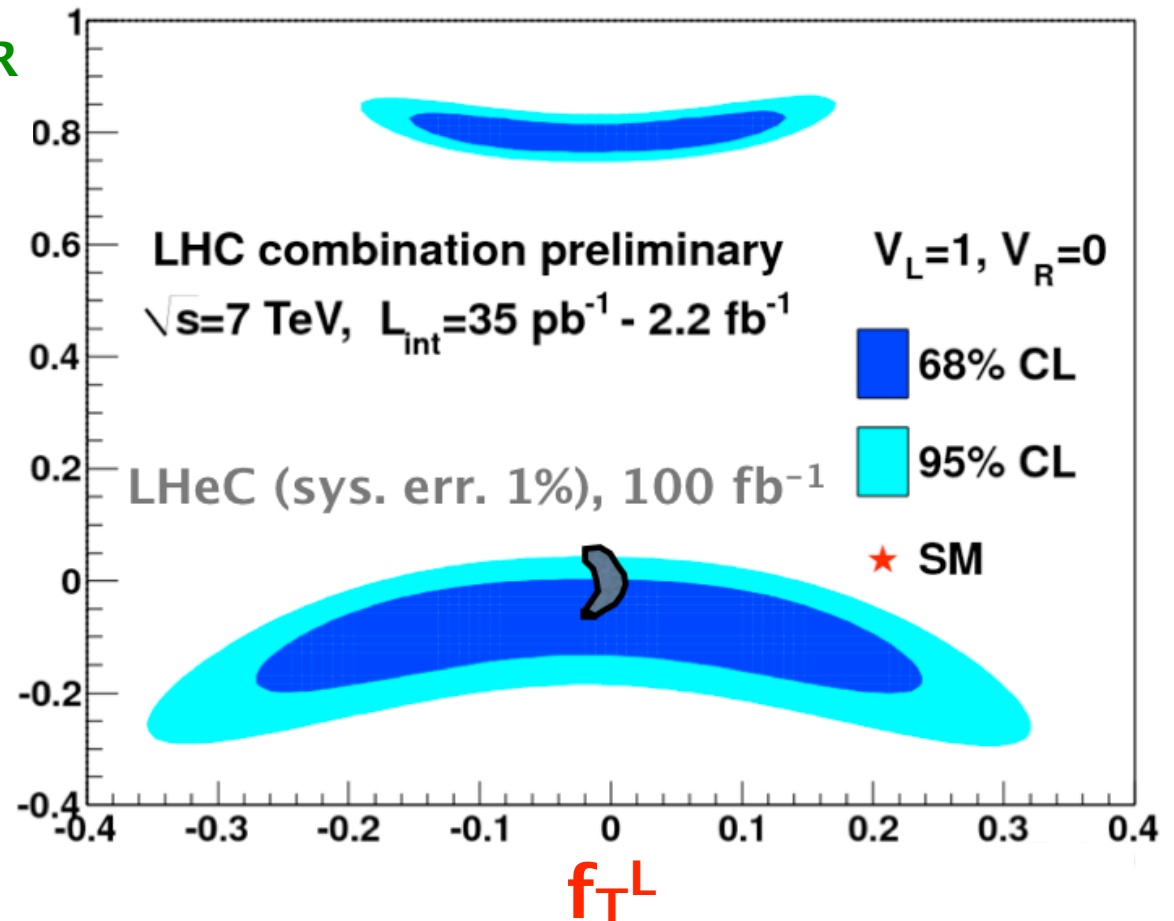
# Search for Anomalous $Wtb$ Couplings

= 1 in SM

$$L = -\frac{g}{\sqrt{2}} \bar{b} \gamma^\mu V_{tb} (f_V^L P_L + f_V^R P_R) t W_\mu^- - \frac{g}{\sqrt{2}} \bar{b} \frac{i\sigma^{\mu\nu} q_\nu}{M_W} (f_T^L P_L + f_T^R P_R) t W_\mu^- + h.c.$$



$f_T^R$

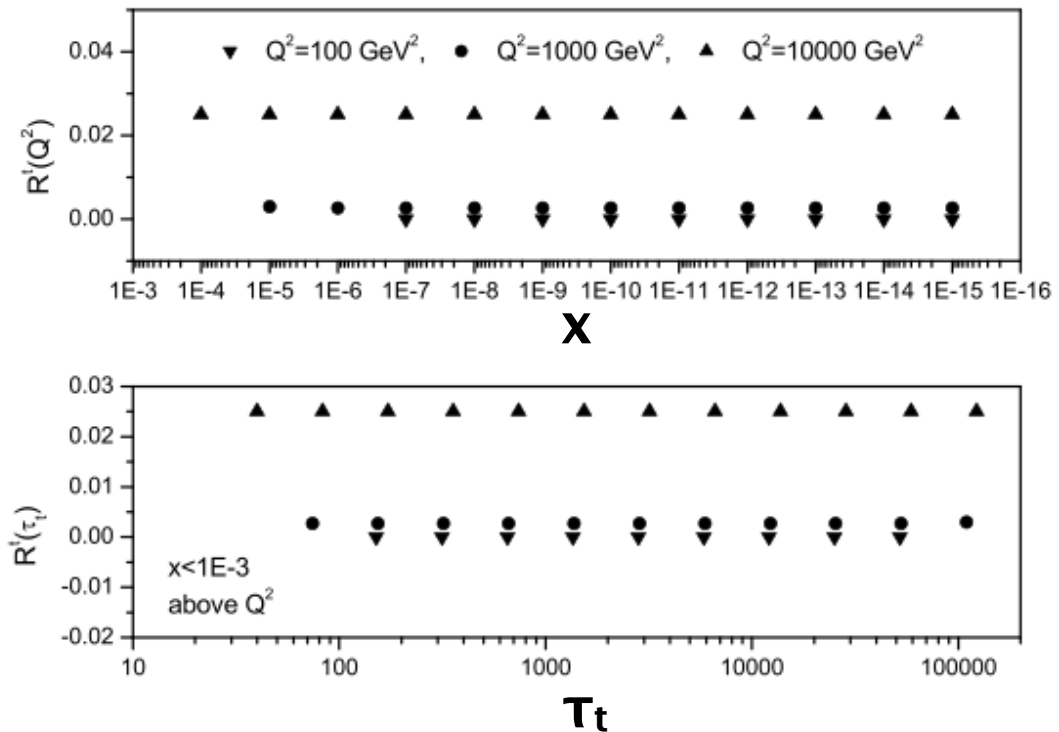
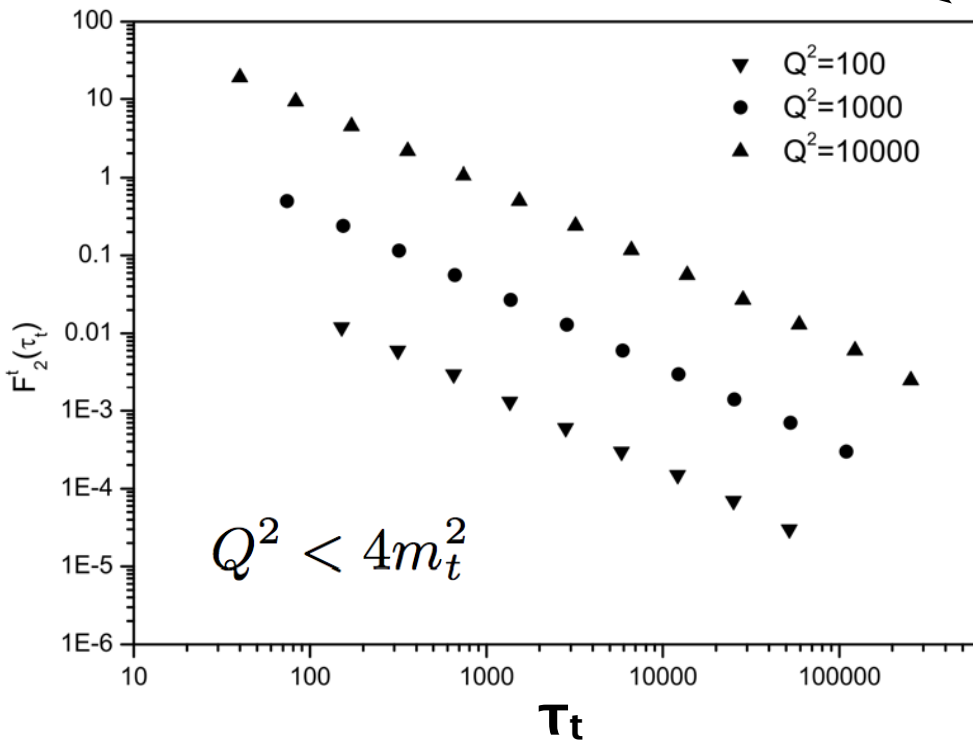


# Top Quark Structure Function

Boroun, Phys. Lett. B744, 142 (2015)

variable flavour  
number scheme  
for top quark

$$\tilde{\sigma}^{t\bar{t}}(\tau_t) \rightarrow F_2^t(\tau_t) [1 - R^t(\tau_t)]$$

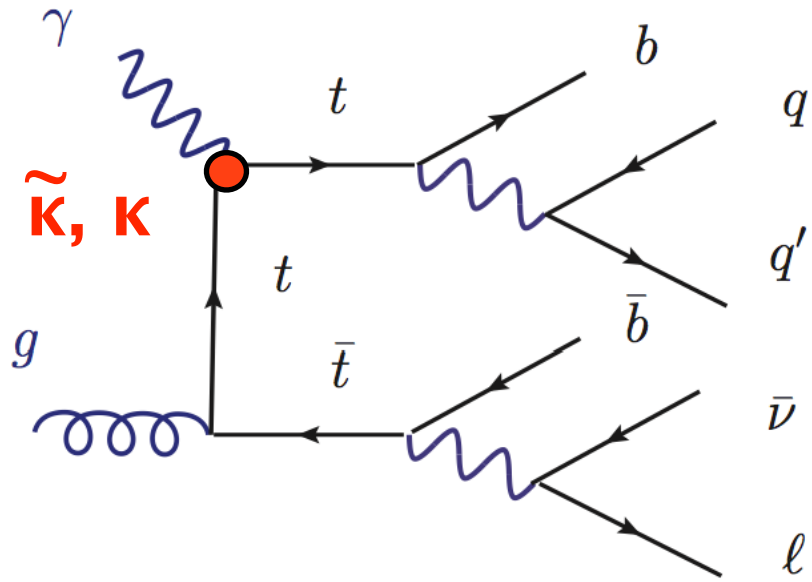


→ approximately:  $1/\tau_t$

→ independent of  $x$  and  $\tau_t$

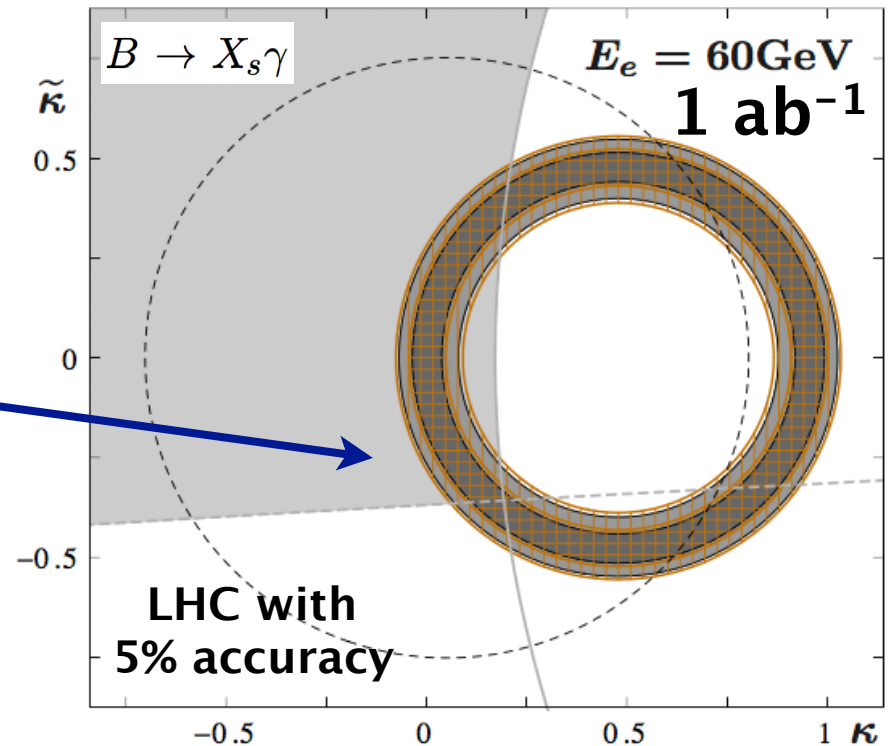
→ longitudinal top structure function component could be good to probe top quark density in proton at  $Q^2 \simeq 4m_t^2$

# Search for Anomalous $t\bar{t}\gamma$ Couplings



$$\mathcal{L}_{t\bar{t}\gamma} = e\bar{t} \left( Q_t \gamma^\mu A_\mu + \frac{1}{4m_t} \sigma^{\mu\nu} F_{\mu\nu} (\kappa + i\tilde{\kappa}\gamma_5) \right) t$$

electric dipole moment:  $\tilde{\kappa}$



LHeC

8% and 16% accuracy  
 10% 18%  
 → systematically limited



27% accuracy  
 (4.59fb<sup>-1</sup>, 7 TeV)

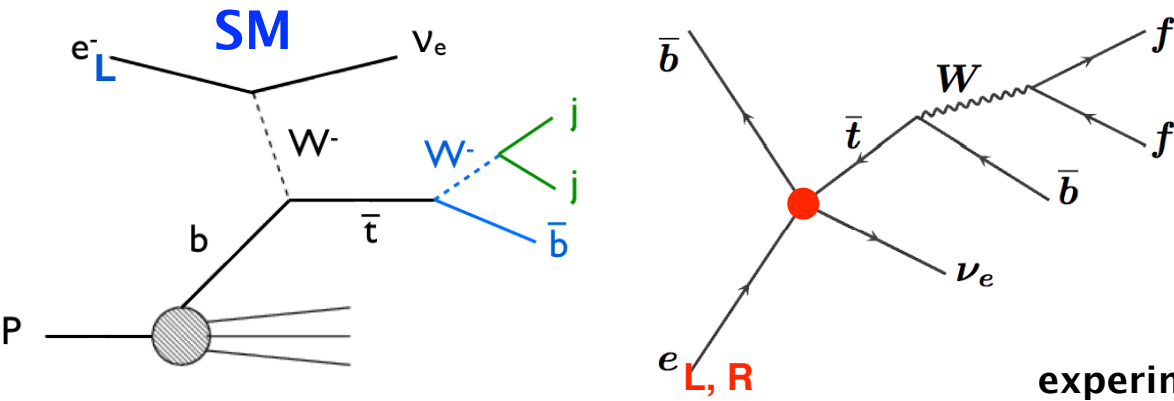
magnetic dipole moment:  $\kappa$

Bouzas, Larios,  
 Physical Review D 88, 094007 (2013)

# Top Quark Dimension 6 Operators

$$\Lambda^2 \mathcal{L}_{4f} = C_1(\bar{\nu}_L \gamma^\mu t_L \bar{b}_L \gamma_\mu e_L + h.c.) + [C_2 \bar{\nu}_L e_R \bar{b}_R t_L + C_3 \bar{b}_L e_R \bar{\nu}_L t_R + C_4 \bar{\nu}_L e_R \bar{b}_L t_R + h.c.]$$

$\Lambda=1\text{TeV}$



property	precision
$C_1$	0.50-0.85
$C_2^r$	2.2-5.0
$C_3^r$	1.4-2.9
$C_4^r$	2.2-4.9

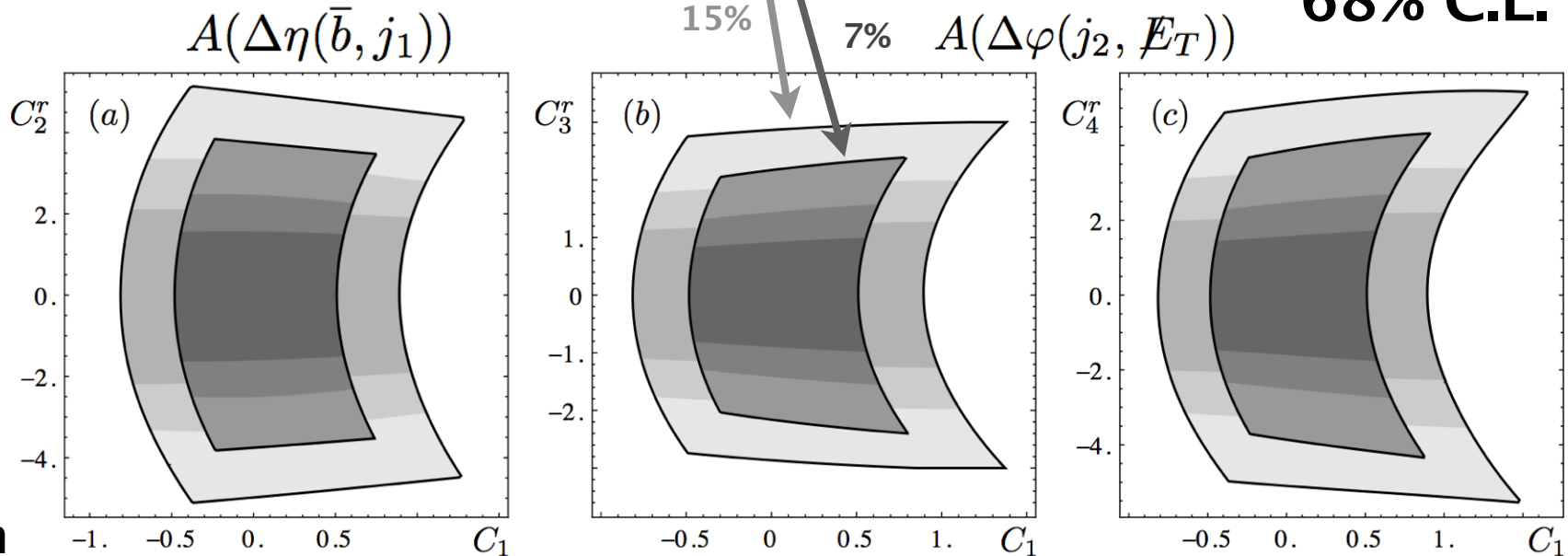
Sarmiento-Alvarado,  
Bouzas, Larios,  
arXiv:1412.6679

$$\mathcal{P}_e = 0$$

$$\mathcal{P}_e = 0.4$$

$$\mathcal{P}_e = 0.7$$

cross section



# NC Top Quark Production

Bouzas, Larios,  
Physical Review D 88, 094007 (2013)

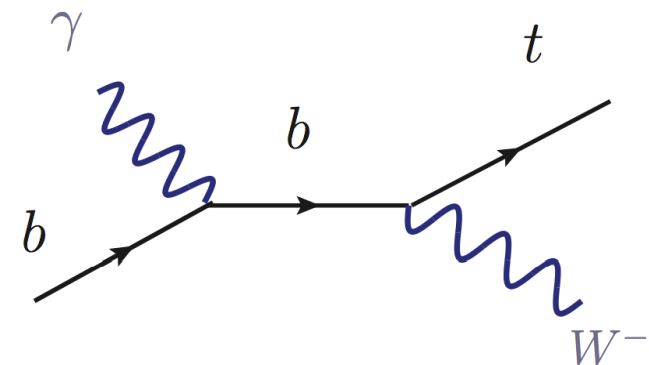
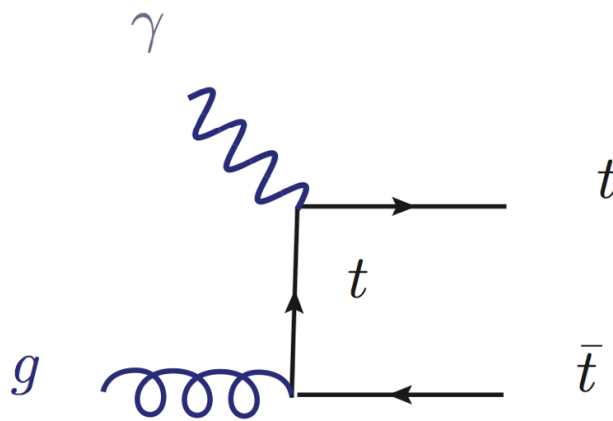
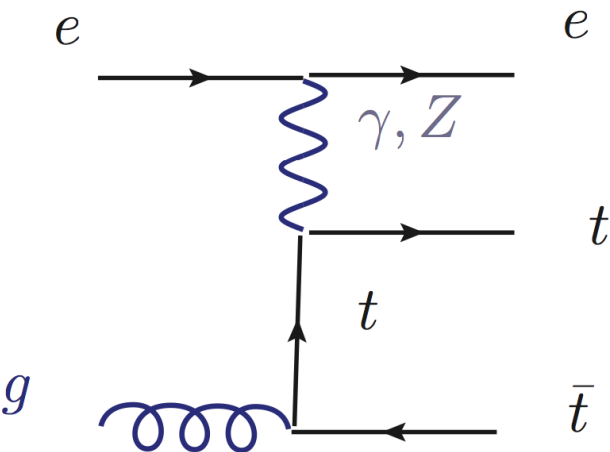
## top pair production

## single top production

DIS

photoproduction

photoproduction



e-beam 60 GeV, 1000 fb<sup>-1</sup>:

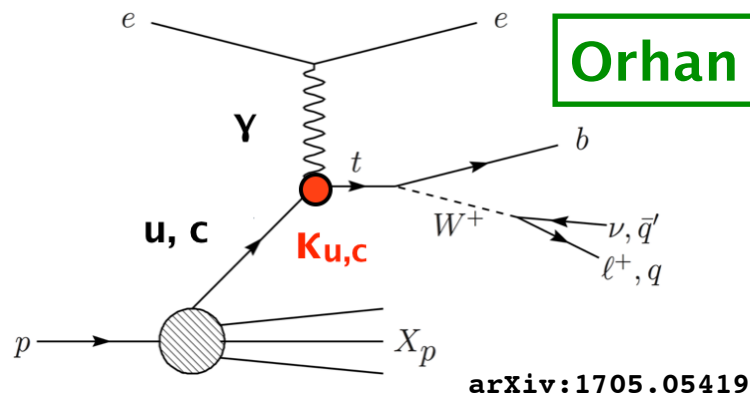
0.023 pb  
N<sub>t $\bar{t}$</sub>  = 23,000

0.70 pb  
N<sub>t $\bar{t}$</sub>  = 700,000

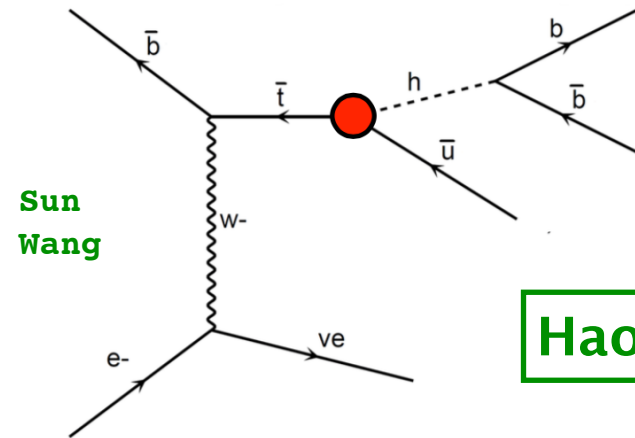
0.031 pb  
N<sub>t</sub> = 31,000

# FCNC $t\bar{u}$ and $t\bar{u}H$ Couplings

T. Cakir  
Yilmaz  
Denizl  
Seno  
Karadeniz  
O. Cakir

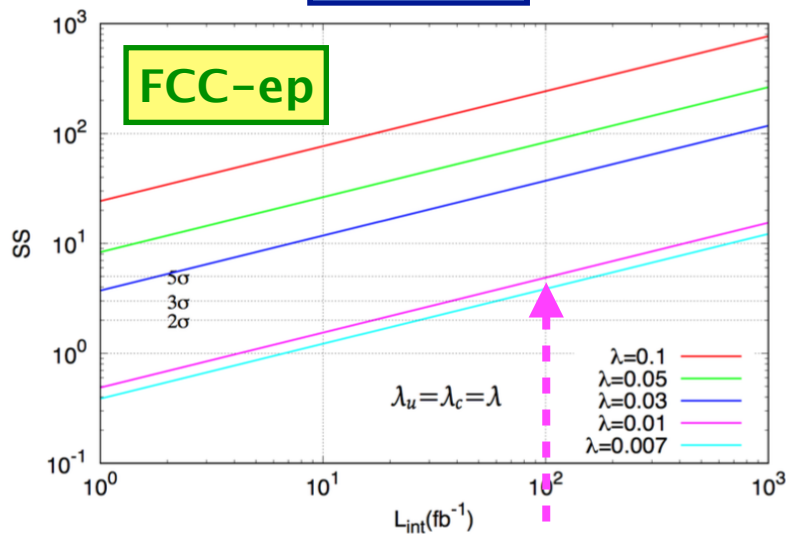


$$L = -g_e \sum_{q=u,c} Q_q \frac{\kappa_q}{\Lambda} \bar{t} \sigma^{\mu\nu} (f_q + h_q \gamma_5) q A_{\mu\nu} + h.c.$$



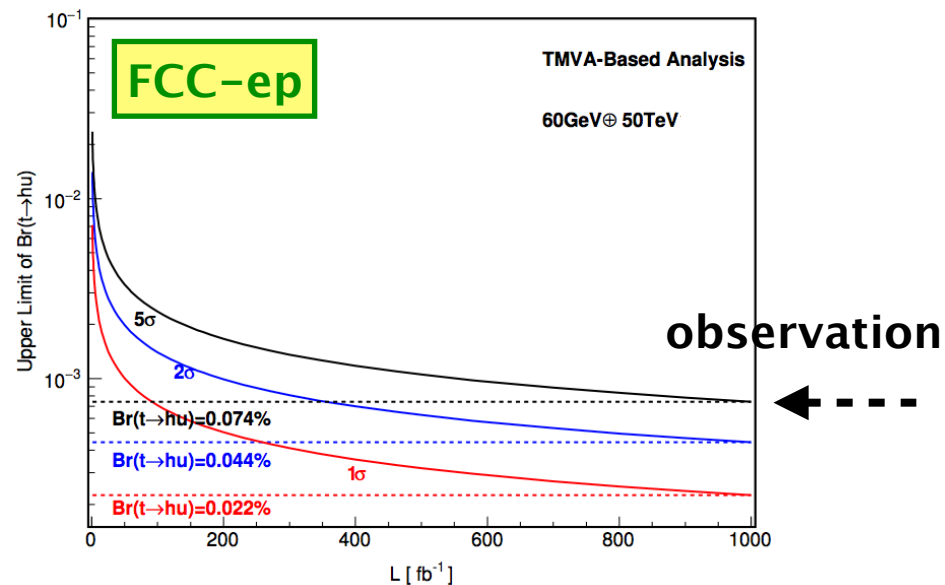
$$\mathcal{L} = \kappa_{t\bar{u}h} \bar{t} u h + \kappa_{t\bar{c}h} \bar{t} c h + h.c.$$

**DELPHES**

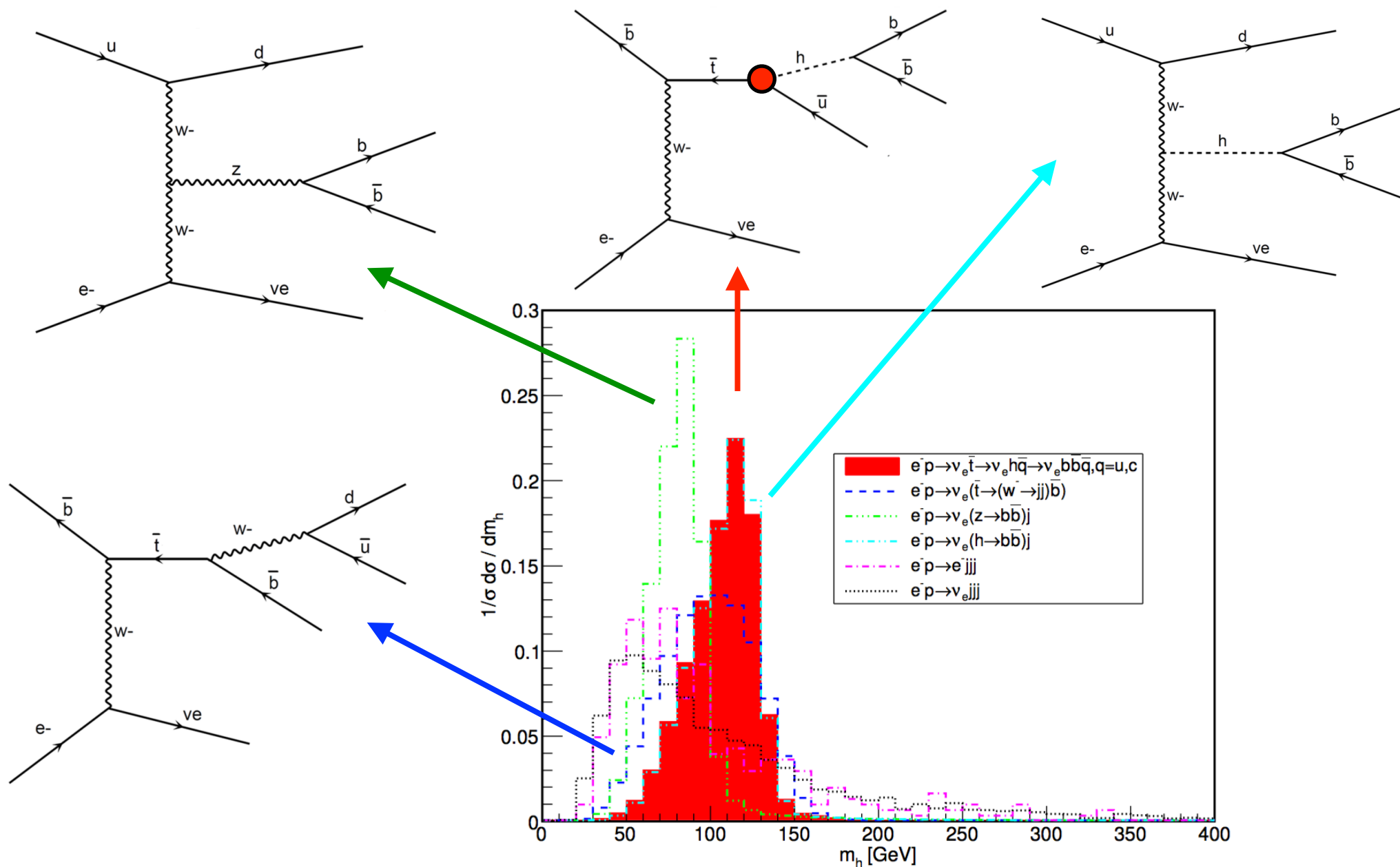


$E_e = 60$  GeV

**parametrisation**

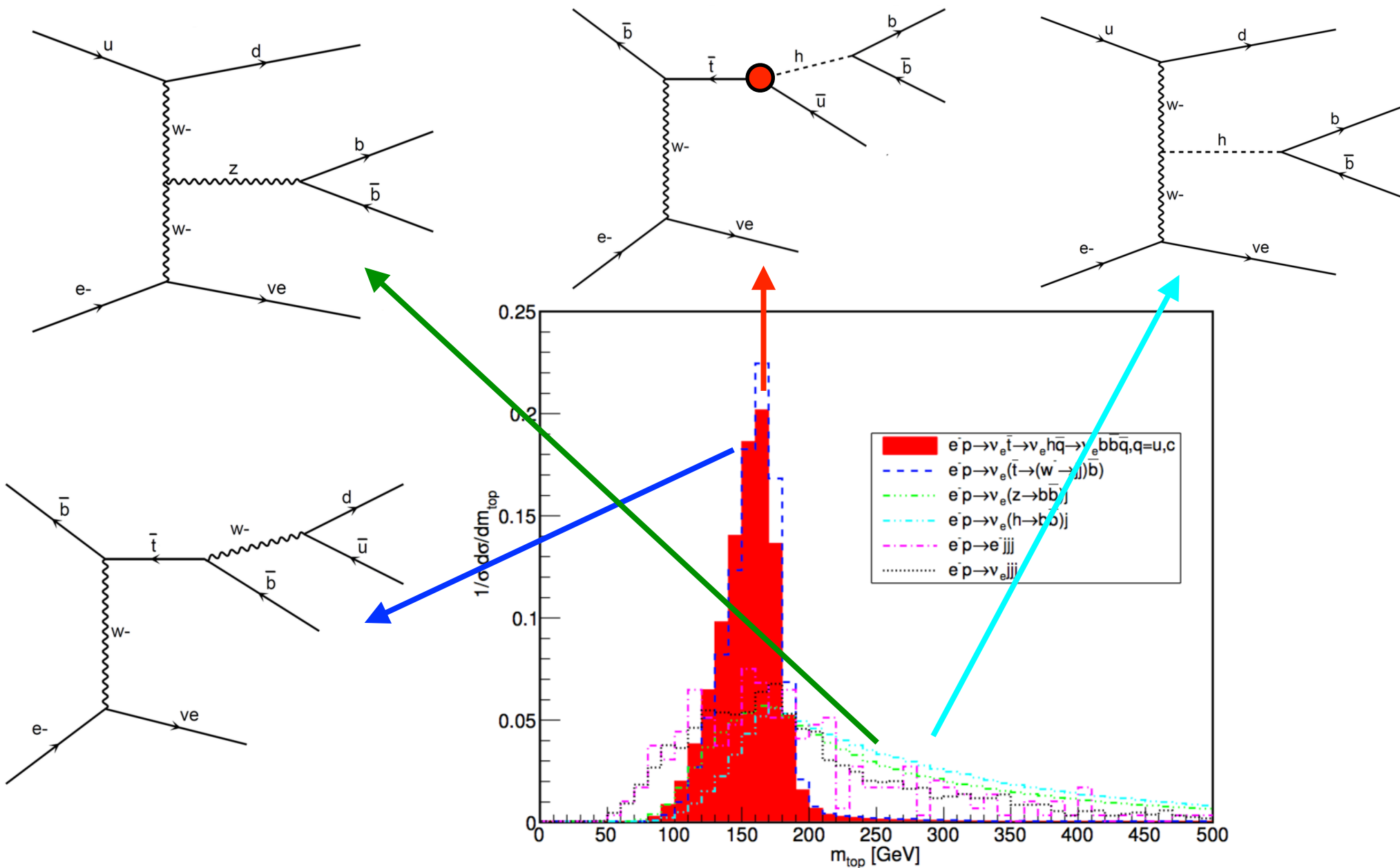


# Reconstructed Higgs mass

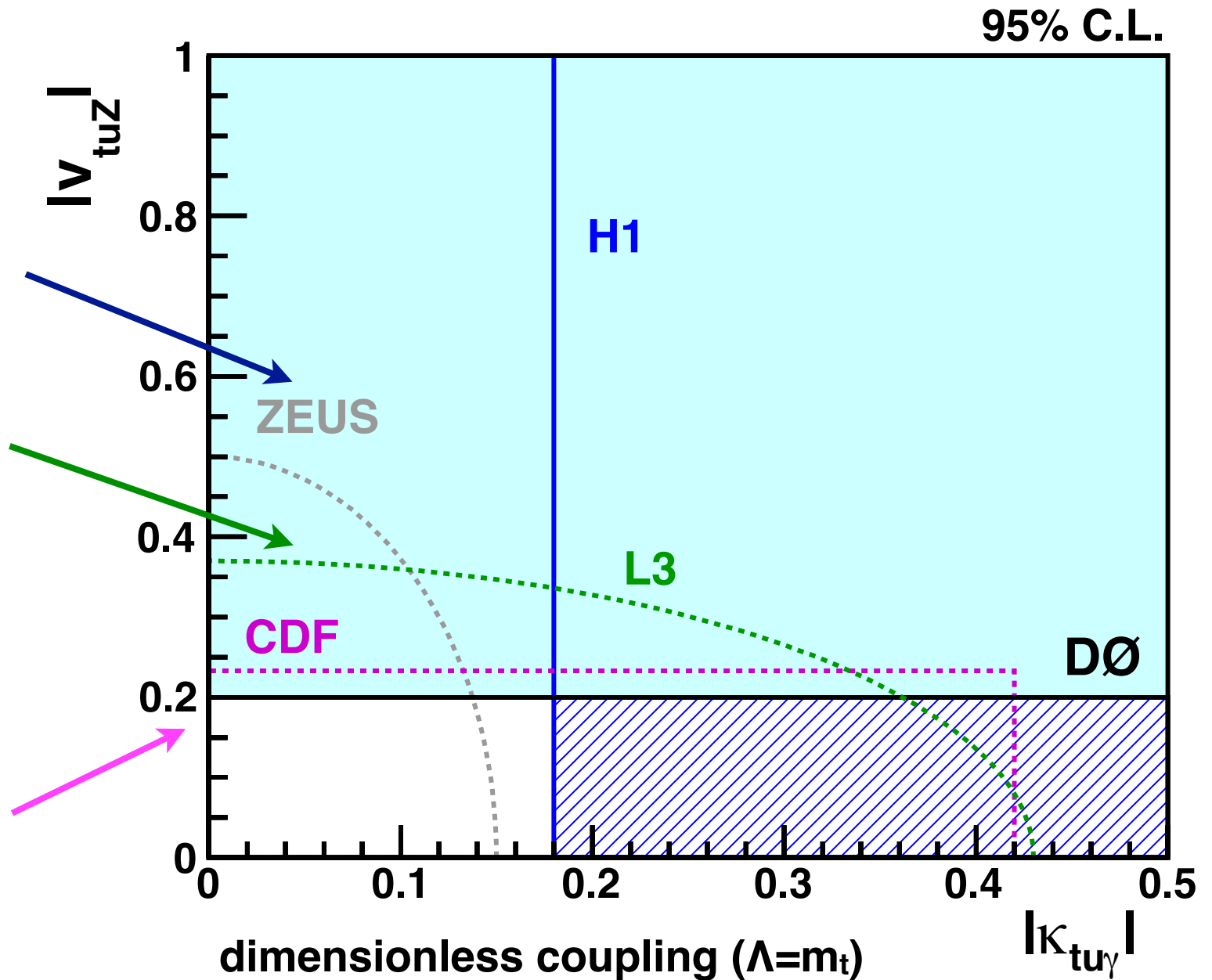
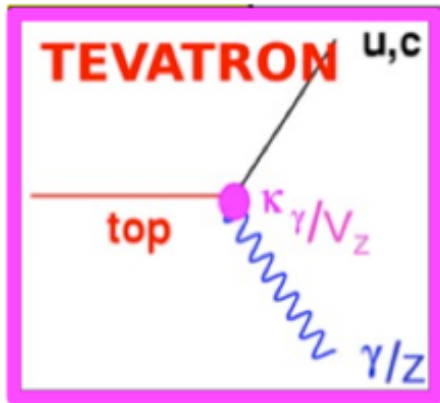
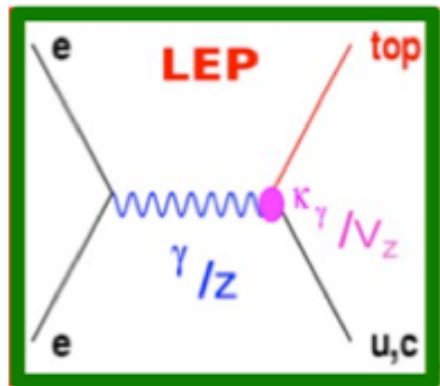
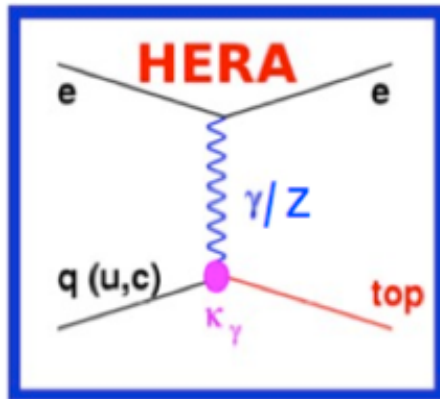




# Reconstructed top quark mass

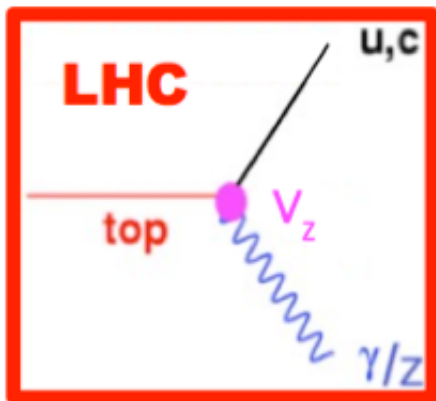
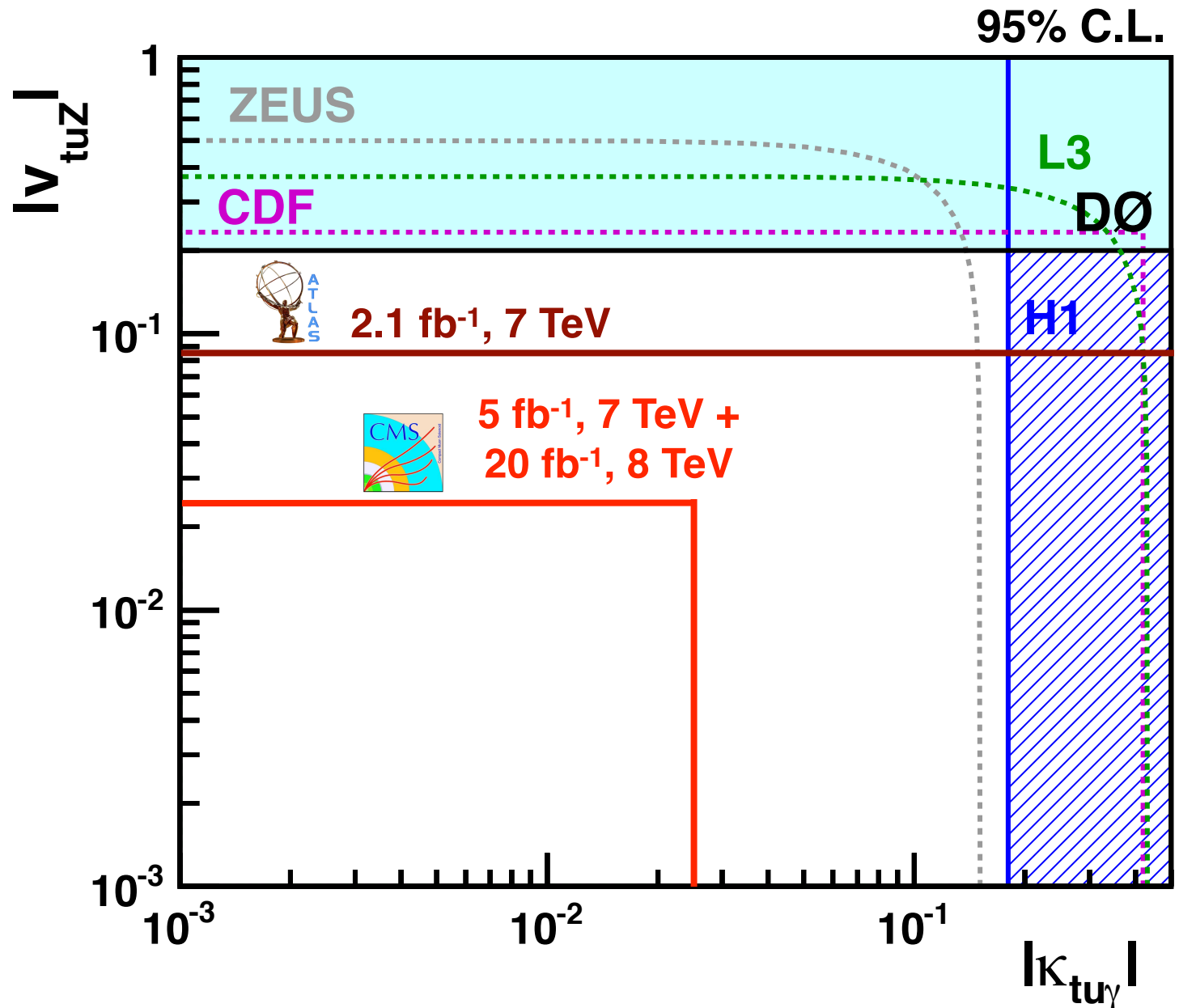


# FCNC Top Couplings at Colliders



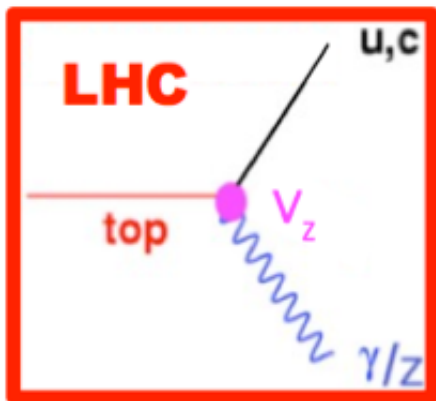
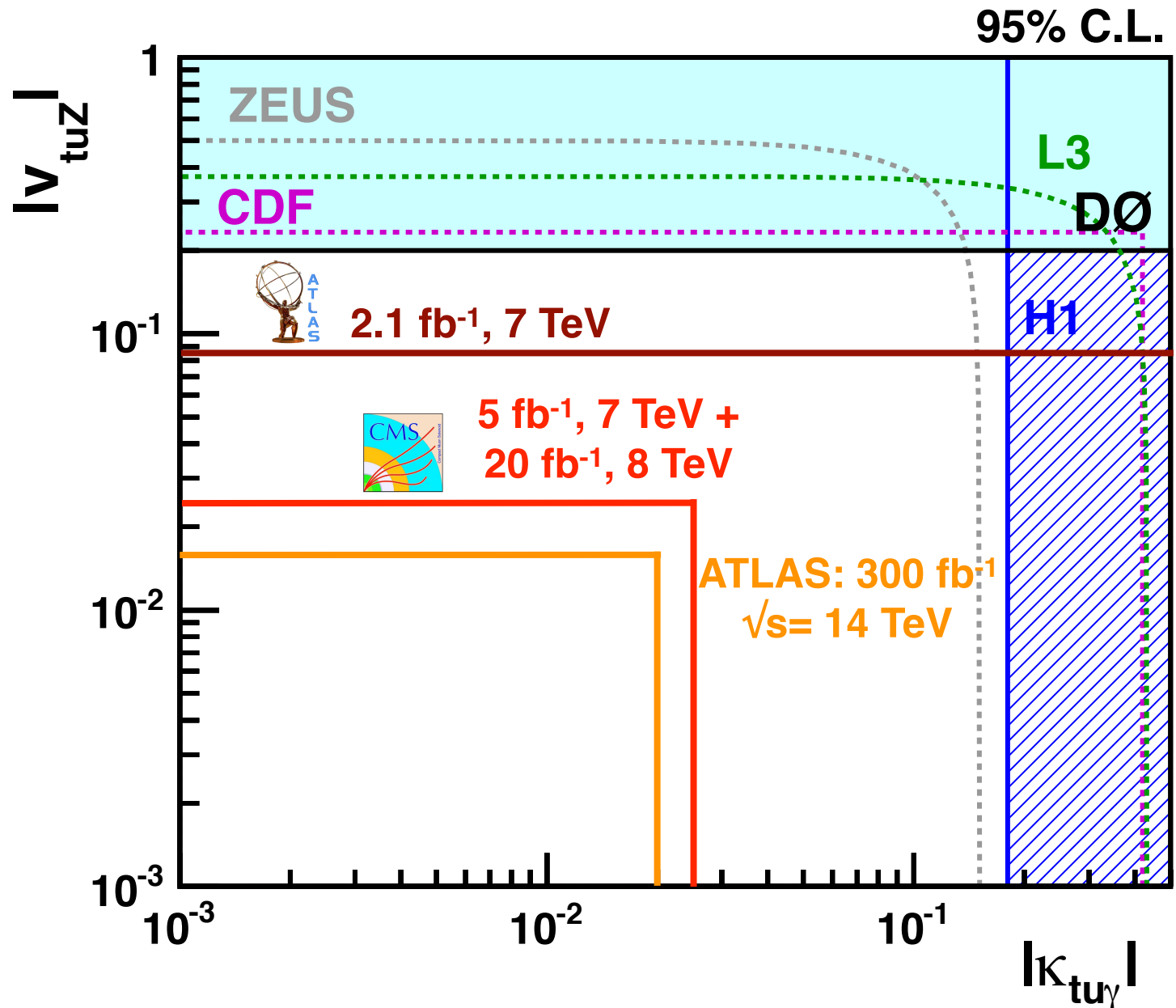
# FCNC Top Couplings at Colliders

Top Quark Working Group  
 Collaboration,  
 arXiv:1311.2028 [hep-ph]



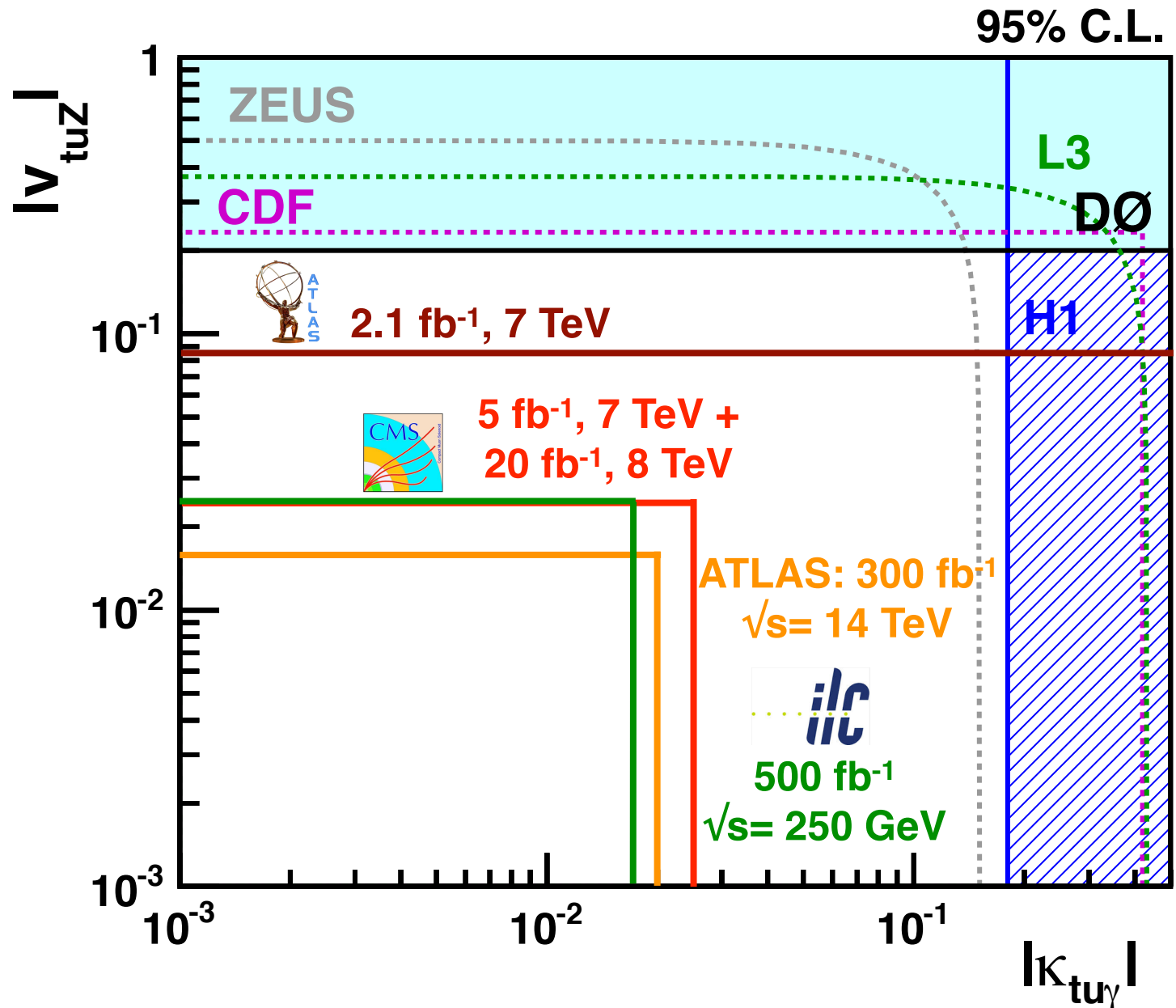
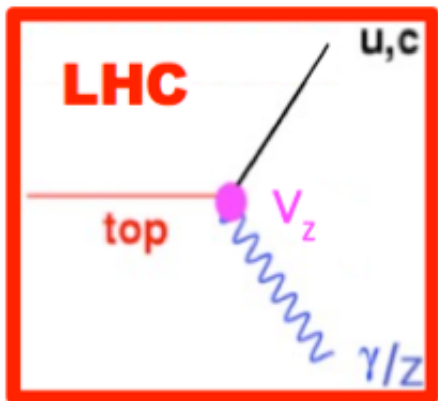
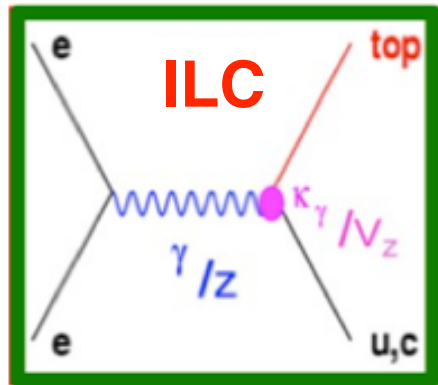
# FCNC Top Couplings at Colliders

Top Quark Working Group  
 Collaboration,  
 arXiv:1311.2028 [hep-ph]

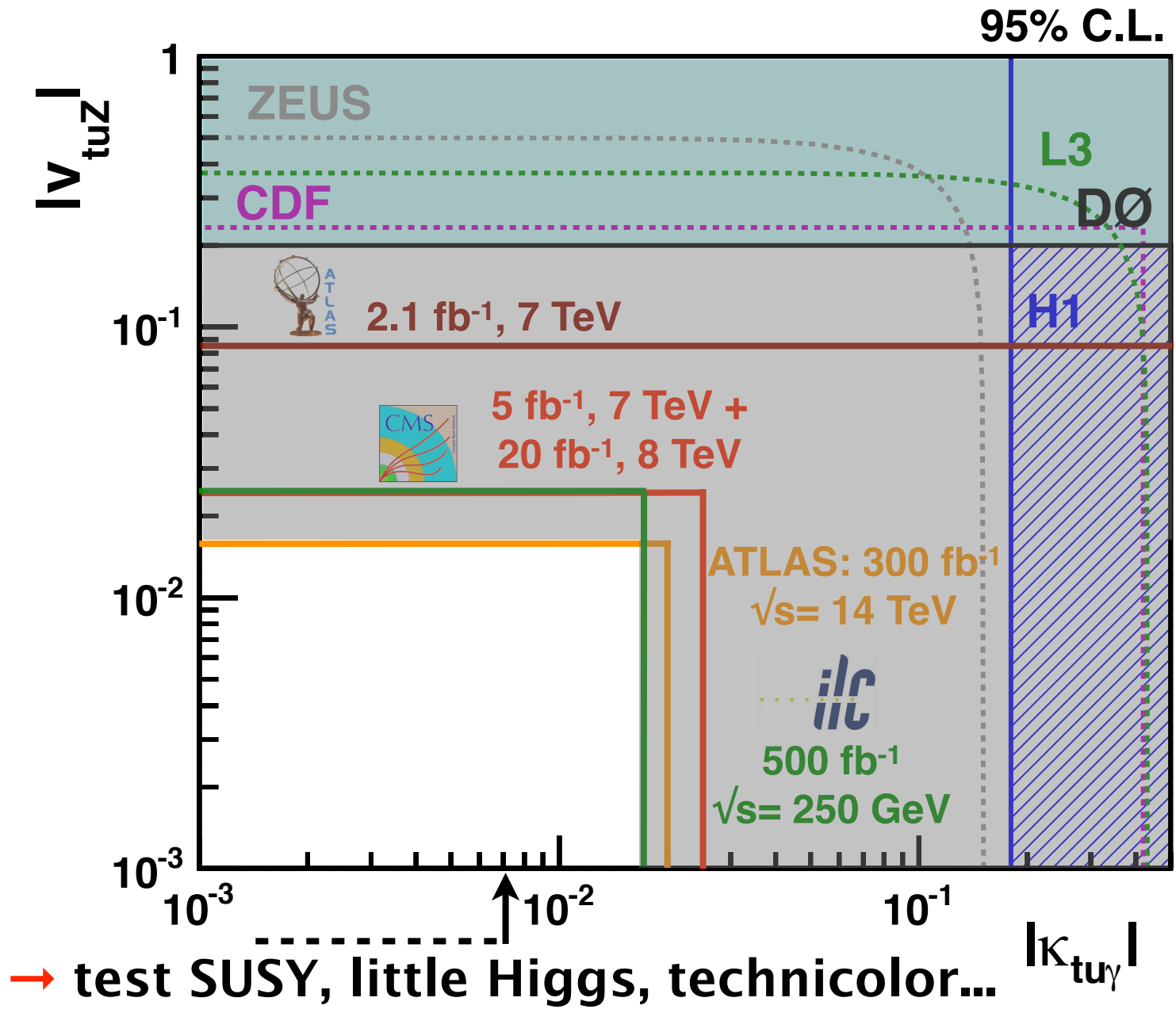
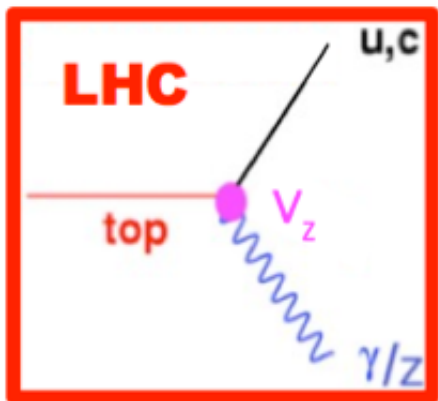
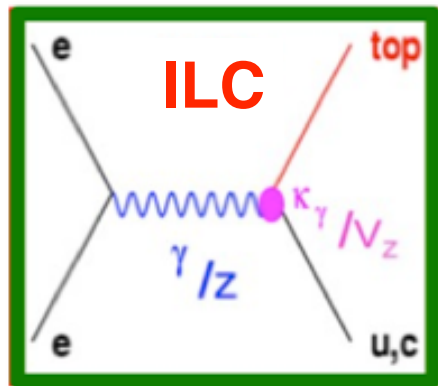


# FCNC Top Couplings at Colliders

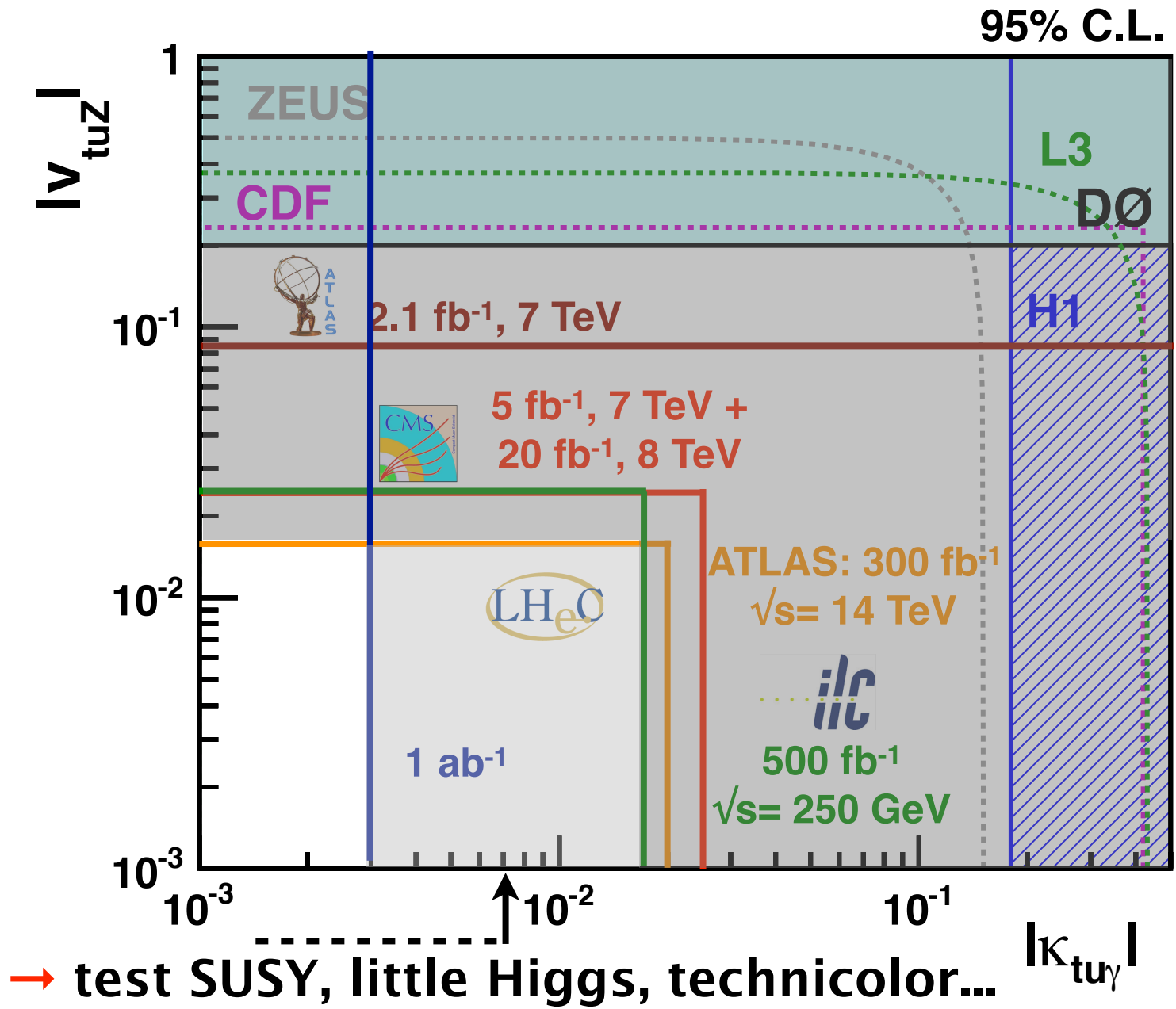
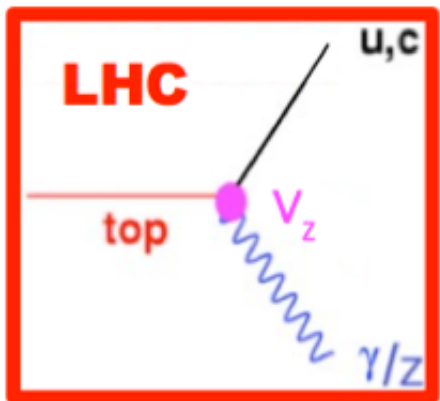
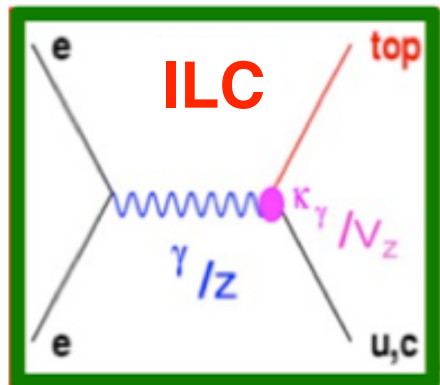
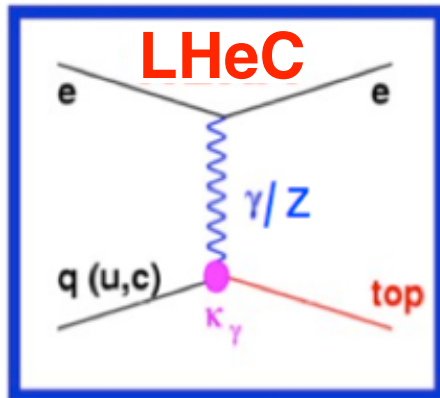
Top Quark Working Group  
 Collaboration,  
 arXiv:1311.2028 [hep-ph]



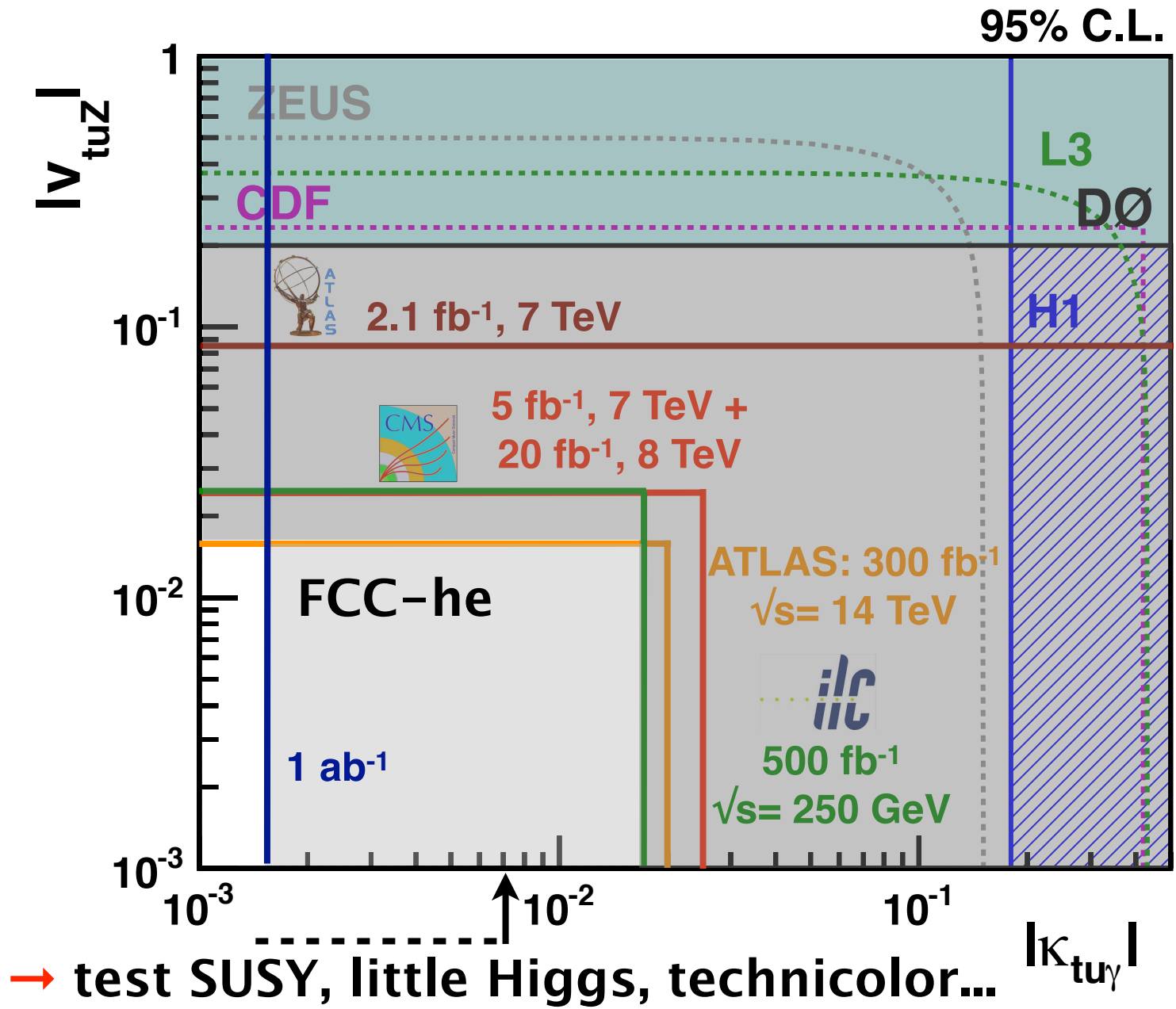
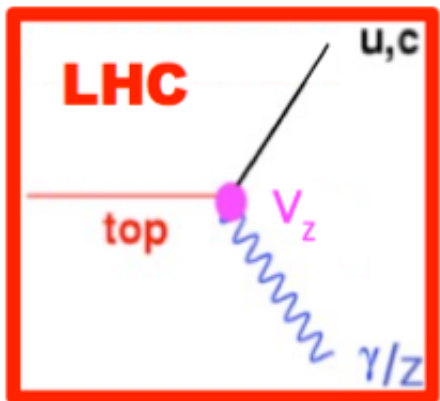
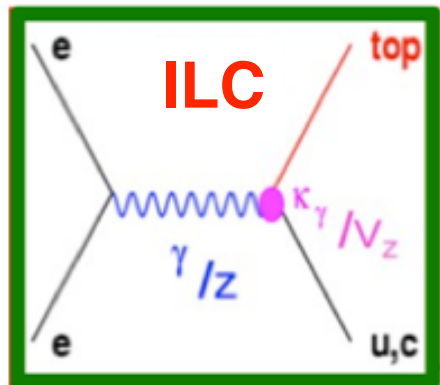
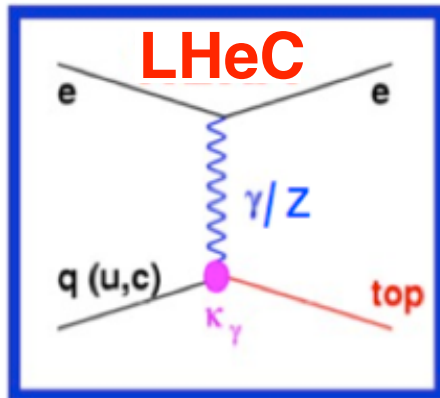
# FCNC Top Couplings at Colliders



# FCNC Top Couplings at Colliders



# FCNC Top Couplings at Colliders

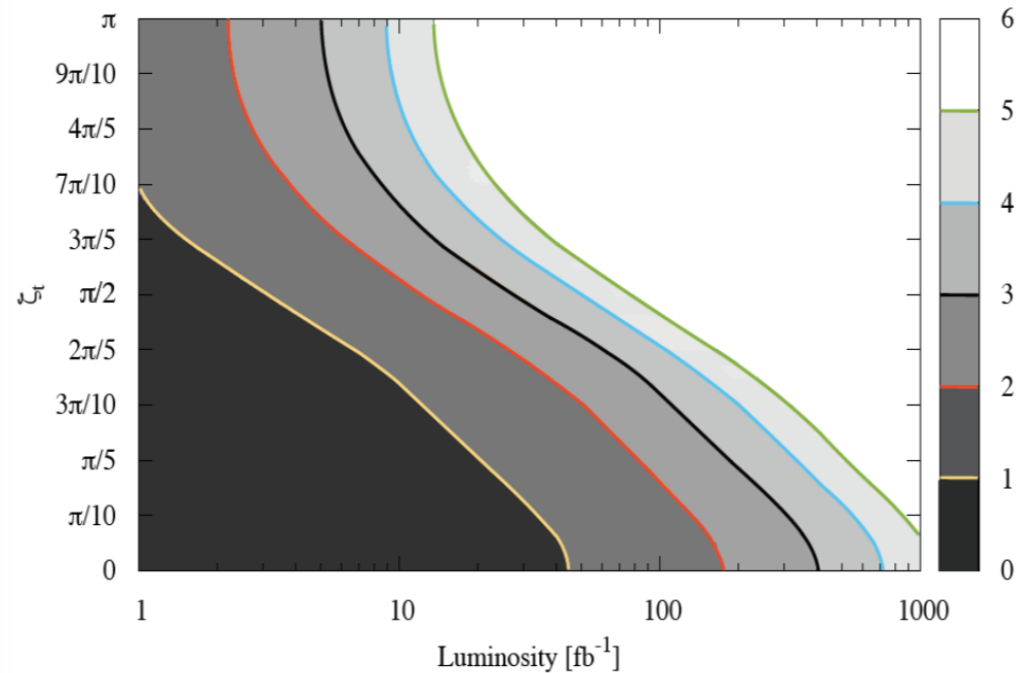
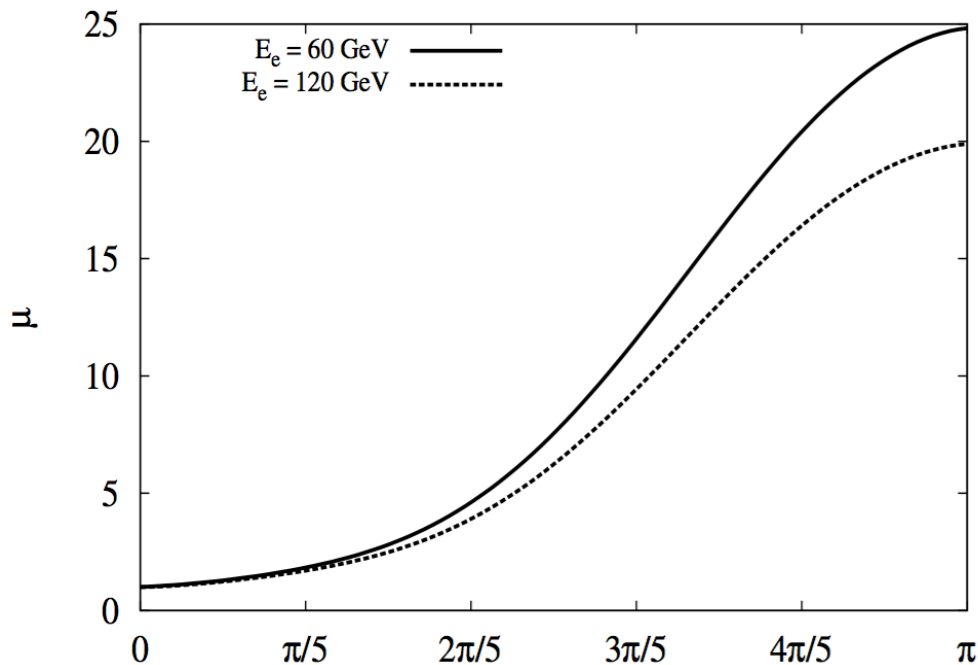




# Observation/Exclusion Contours

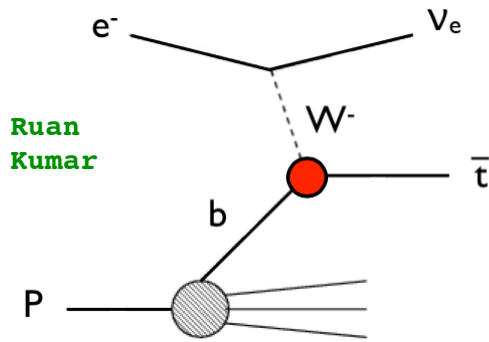
LHeC

- $\zeta_t = 0$  or  $\zeta_t = \pi$  → pure scalar state
- $\zeta_t = \pi/2$  → pure pseudo scalar state
- $0 < \zeta_t < \pi/2$  or  $\pi/2 < \zeta_t < \pi$  → mixture CP-states
- $\zeta_t = 0, \kappa = 1$  → SM case

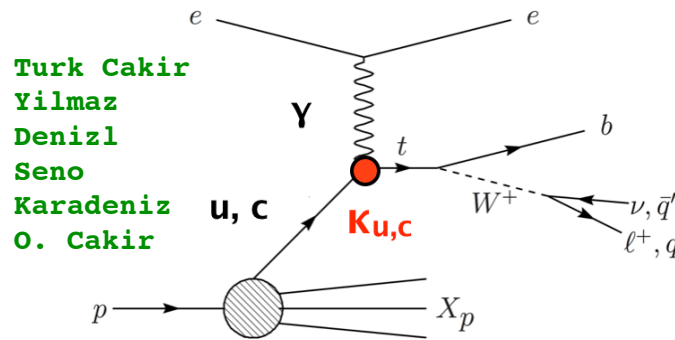


Observe/Exclude non-zero phase to better than  $4\sigma$  → With Zero Phase: Measure coupling with 17% accuracy → work ongoing on FCC-eh prospects

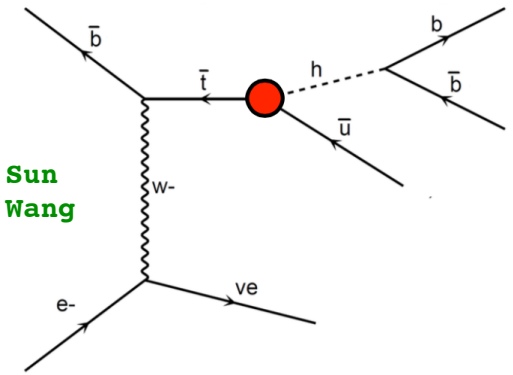
# Top Quark SM+BSM



Ruan Kumar



Turk Cakir  
Yilmaz Denizl  
Seno Karadeniz  
O. Cakir



Sun Wang

= 1 in SM

$$L = -\frac{g}{\sqrt{2}} \bar{b} \gamma^\mu V_b (f_V^L f_L + f_V^R f_R) t W_\mu^- - \frac{g}{\sqrt{2}} \bar{b} i \sigma^{\mu\nu} q_\nu (f_T^L f_L + f_T^R f_R) t W_\mu^- + h.c.$$

$$L = -g_e \sum_{q=u,c} Q_q \frac{\kappa_q}{\Lambda} \bar{t} \sigma^{\mu\nu} (f_q + h_q \gamma_5) q A_{\mu\nu} + h.c.$$

$$\mathcal{L} = \kappa_{tuh} \bar{t} u h + \kappa_{tch} \bar{t} c h + h.c.$$

DELPHES

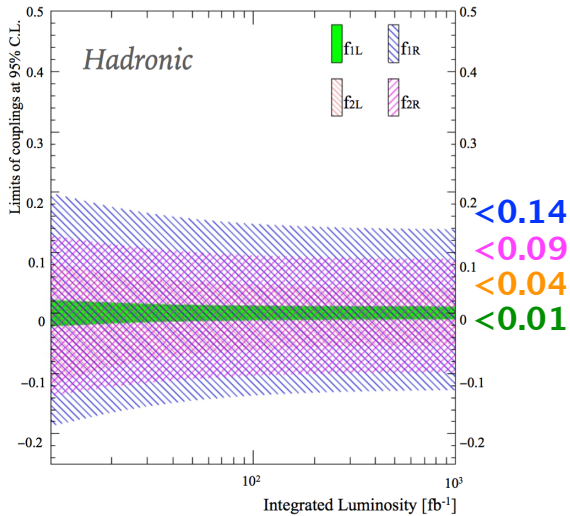
LHeC+FCC

DELPHES

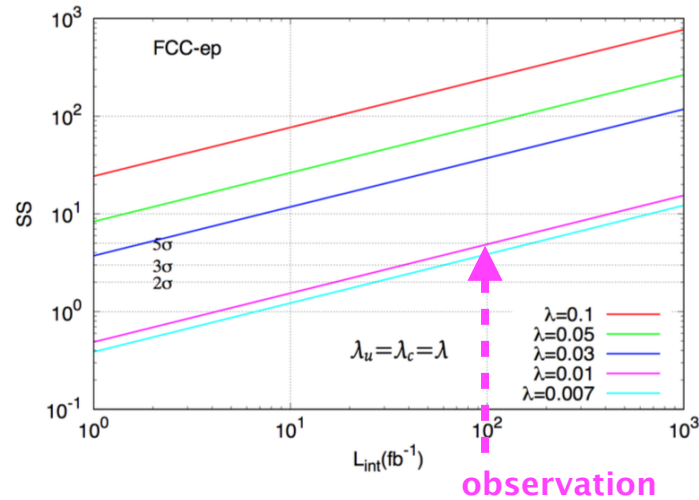
LHeC+FCC

parametrisation

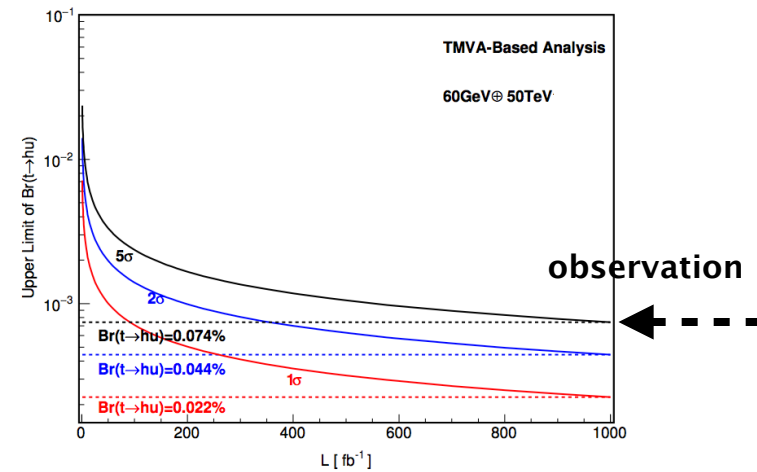
LHeC+FCC



→ to be published  
→ ask for SM cross sections



→ published: arXiv:1705.05419  
→ ask for BR(t→qγ)



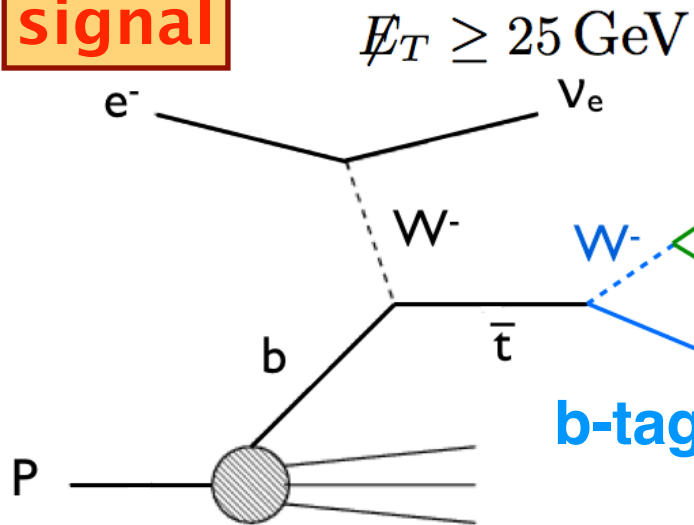
→ published: arXiv:1602.04670

# Signal and Backgrounds

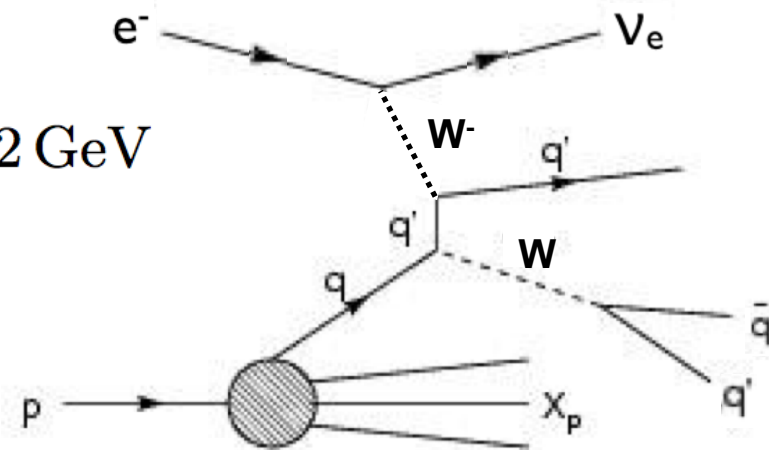
**signal**

Dutta, Goyal, Kumar, Mellado, Eur. Phys. J. C75 (2015) no.12, 577

**background**

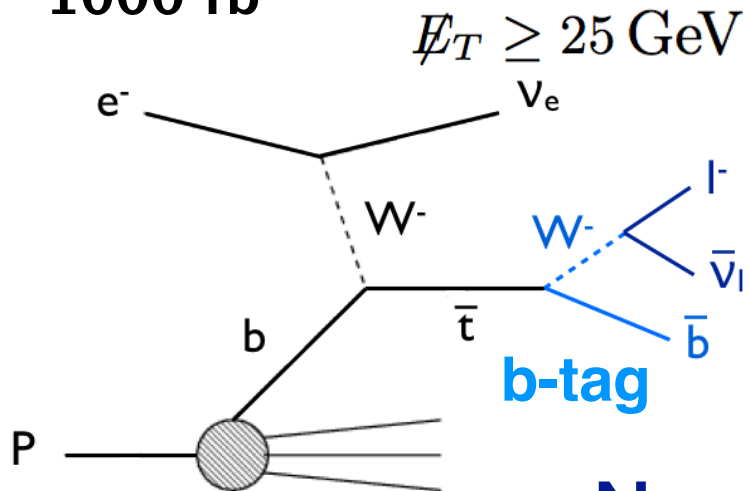


$$\begin{aligned} \Delta\Phi_{\cancel{E},j} &\geq 0.4 \\ \Delta\Phi_{\cancel{E},b} &\geq 0.4 \\ |m_{j_1 j_2} - m_W| &\leq 22 \text{ GeV} \\ p_{T,j,b} &\geq 20 \text{ GeV} \\ |\eta_j| &\leq 5, |\eta_b| \leq 2.5 \\ \Delta R_{j,b/j} &\geq 0.4 \end{aligned}$$

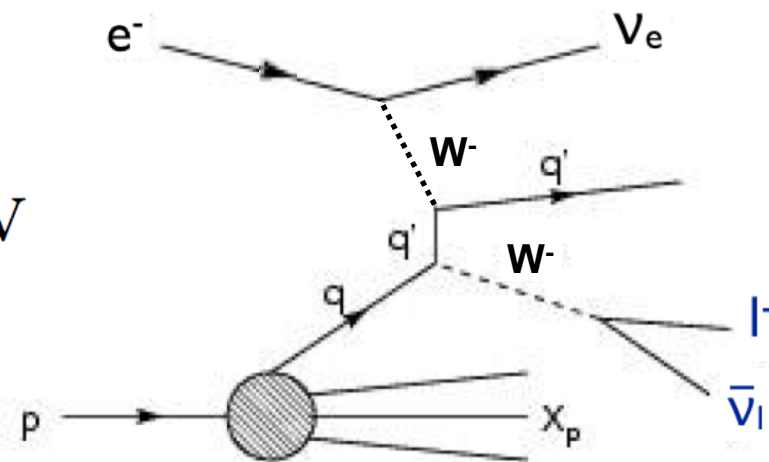


**$N_t = 220k, s/b = 1.2$**

e beam: 60 GeV  
1000 fb<sup>-1</sup>



$$\begin{aligned} \Delta\Phi_{\cancel{E},j} &\geq 0.4 \\ \Delta\Phi_{\cancel{E},b} &\geq 0.4 \\ \Delta\Phi_{\cancel{E},l} &\geq 0.4 \\ p_{T,j,b,l} &\geq 20 \text{ GeV} \\ |\eta_j| &\leq 5, |\eta_{b,l}| \leq 2.5 \\ \Delta R_{j,b/j} &\geq 0.4 \end{aligned}$$



**$N_t = 110k, s/b = 11$**