

# Marginal Events

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# Summary

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- ❖ Expected events for “golden” analysis
- ❖ Expected events for minimum bias analysis
- ❖ Significance evaluation:
  - $P^*$  method
  - Likelihood
- ❖  $\Delta m^2_{23}$  measurement
- ❖ Absolute  $\nu_\tau$  cross-section measurement
- ❖ BDT Analysis + Significance evaluation (in progress)
- ❖ Lepton number measurement

# “Golden” and “Minimum Bias” selections

Variable	$\tau \rightarrow 1h$		$\tau \rightarrow 3h$		$\tau \rightarrow \mu$		$\tau \rightarrow e$	
	OLD	NEW	OLD	NEW	OLD	NEW	OLD	NEW
$z_{dec}$ ( $\mu m$ )	[44, 2600]	<2600		<2600	[44, 2600]	<2600		<2600
$\theta_{kink}$ ( $rad$ )		>0.02		<0.5	>0.02			>0.02
$p_{2ry}$ ( $GeV/c$ )		>2		>1	>3	>1	[1, 15]	[1, 15] >1
$p_{2ry}^T$ ( $GeV/c$ )	>0.6 (0.3)*	>0.15		/			>0.25	>0.1
$p_{miss}^T$ ( $GeV/c$ )	< 1*	/	< 1*	/			/	/
$\phi_{lH}$ ( $rad$ )		> $\pi/2$ *		/	> $\pi/2$ *	/		/
$m, m_{min}$ ( $GeV/c^2$ )		/		[0.5, 2]	/		/	/

Cuts marked with \* are not applied for Quasi-Elastic event

\*  $p_{2ry}^T$  cut is 0.3 in the presence of  $\gamma$  particles associated to the decay vertex

# Expected events for “golden” analysis

- Efficiencies of 5<sup>th</sup>  $\tau$  paper updated with  $\Delta m^2_{23} = 0.0025 \text{ eV}^2$  and final statistics (see back-up slides)

Channel	Expected Background				Total	Expected Signal	Observed
	Charm	Had. re-interaction	Large $\mu$ -scat.				
$\tau \rightarrow 1h$	0.02	0.023	—		0.04	0.57	3
$\tau \rightarrow 3h$	0.18	0.003	—		0.18	0.80	1
$\tau \rightarrow \mu$	0.004	—	0.0002		0.004	0.66	1
$\tau \rightarrow e$	0.03	—	—		0.03	0.85	0
<b>Total</b>	<b>0.23</b>	<b>0.03</b>	<b>0.0002</b>		<b><math>0.26 \pm 0.05</math></b>	<b><math>2.9 \pm 0.6</math></b>	<b>5</b>

- Efficiencies evaluated by myself (larger “new” MC production, different OpRelease version) also for  $\nu_\mu$ ,  $\Delta m^2_{23} = 0.0025 \text{ eV}^2$ , final statistics (see back-up slides)

Channel	Expected Background				Total	Expected Signal	Observed
	Charm	Had. re-interaction	Large $\mu$ -scat.				
$\tau \rightarrow 1h$	0.02	0.024	—		0.05	0.57	3
$\tau \rightarrow 3h$	0.20	0.003	—		0.21	1.09	1
$\tau \rightarrow \mu$	0.003	—	0.0002		0.003	0.55	1
$\tau \rightarrow e$	0.03	—	—		0.03	0.75	0
<b>Total</b>	<b>0.27</b>	<b>0.03</b>	<b>0.0002</b>		<b><math>0.29 \pm 0.06</math></b>	<b><math>3.0 \pm 0.6</math></b>	<b>5</b>

# Expected events for minimum bias analysis

Channel	Expected Background				Total	Expected Signal	Observed
	Charm	Had. re-interaction	Large $\mu$ -scat.				
$\tau \rightarrow 1h$	0.15	1.28	—	—	1.43	2.82	6
$\tau \rightarrow 3h$	0.44	0.09	—	—	0.52	1.75	3
$\tau \rightarrow \mu$	0.008	—	0.02	—	0.03	1.09	1
$\tau \rightarrow e$	0.035	—	—	—	0.03	0.80	0
<b>Total</b>	<b>0.63</b>	<b>1.37</b>	<b>0.02</b>	<b><math>2.0 \pm 0.5</math></b>		<b><math>6.5 \pm 1.3</math></b>	<b>10</b>

# Significance (I): $P^*$ method

[http://operaweb.lngs.infn.it/Opera/publicnotes/OPERA\\_note\\_173.pdf](http://operaweb.lngs.infn.it/Opera/publicnotes/OPERA_note_173.pdf)

*channels*

$$P^* = \prod_{i=1} \mathcal{P}(n_i, b_i)$$

- ❖ Min bias Analysis → 14803 events over 1410065408 have  $P > P^*$ .  
 $P_{\text{val}} = 1.05 \cdot 10^{-5} \rightarrow 4.25\sigma$
- ❖ Min bias Analysis 8 channels: 4 “golden”+4 “silver” (table in back-up) → 32 events over 1410065408 have  $P > P^*$ .  
 $P_{\text{val}} = 2.27 \cdot 10^{-8} \rightarrow 5.47\sigma$

# Significance (II): Likelihood

Roofit - Profile likelihood ratio one sided  
Asymptotic calculator

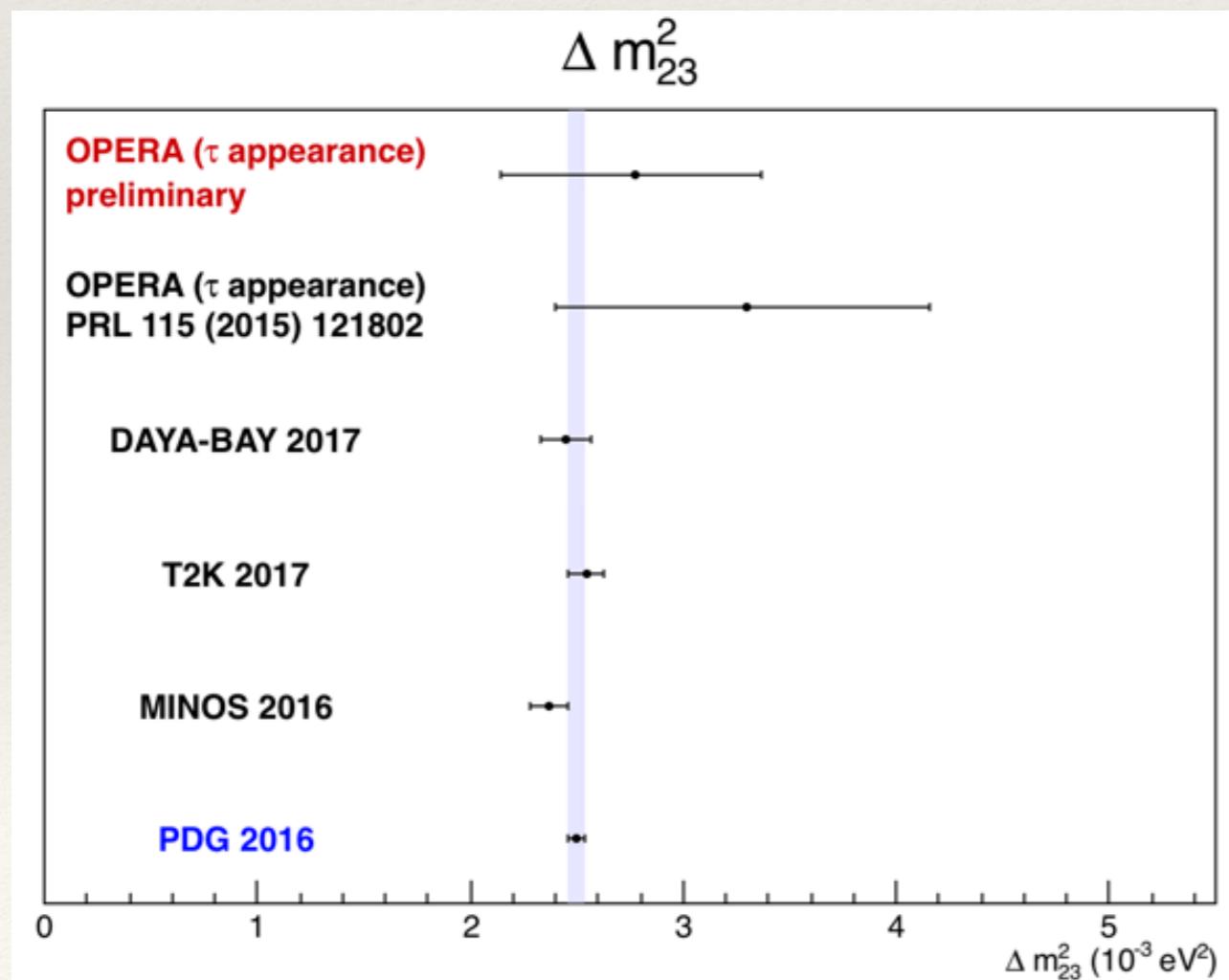
- ❖ Min bias Analysis →  $P_{\text{val}} = 2.41 \cdot 10^{-5} \rightarrow 4.1\sigma$
- ❖ Min bias Analysis 8 channels: 4 “golden” + 4 “marginal” (table in back-up) →  $P_{\text{val}} = 5.90 \cdot 10^{-9} \rightarrow 5.7\sigma$

TO DO: Frequentist calculator. Crash after about 100M MC toy experiments to be solved

# $\Delta m^2_{23}$ measurement

	Expected Signal	Expected Background	Observed $\nu_\tau$	$\Delta m^2_{23}$ ( $10^{-3}$ eV $^2$ ) (68% C.L)	$\Delta m^2_{23}$ ( $10^{-3}$ eV $^2$ ) (90% C.L)
PRL 115 (2015) 121802 $\Delta m^2_{23} = 2.44 \cdot (10^{-3}$ eV $^2$ )	2.56	0.25	5	$3.3^{+0.86}_{-0.90}$	[2.0; 5.0]
<u>Preliminary</u> $\Delta m^2_{23} = 2.5 \cdot (10^{-3}$ eV $^2$ )	6.5	2.0	10	$2.8 \pm 0.6$	[1.84; 3.73]

Assuming maximal mixing and standard  $\sigma_{\nu\tau}$



Agreement with *PDG 2016*  
value within  $1\sigma$

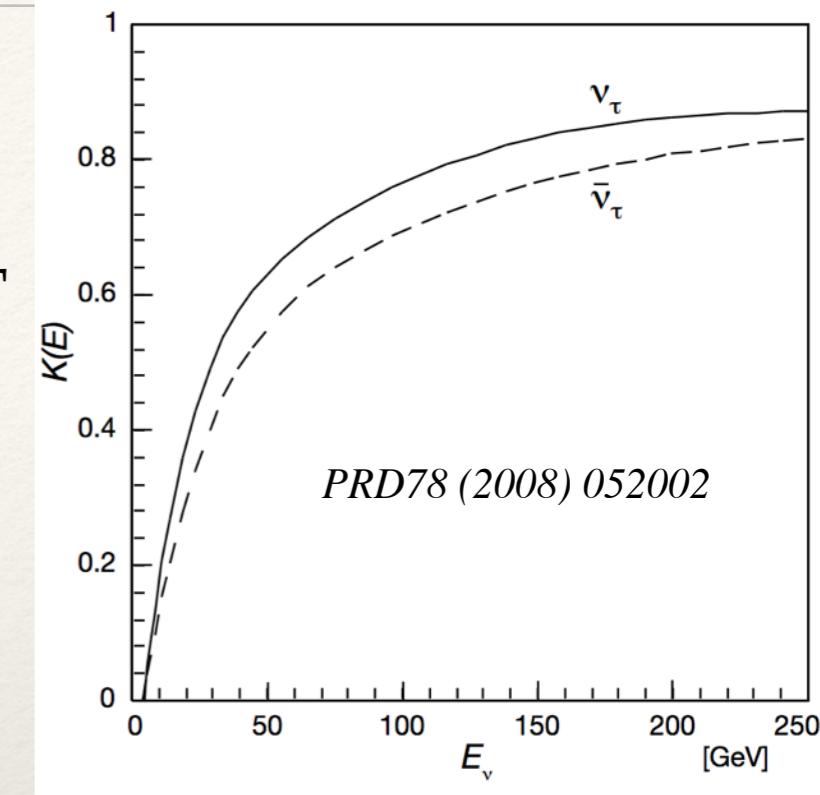
Latest (13/03/2017) global fit on  
 $\Delta m^2_{23} = 2.52 \cdot 10^{-3}$  eV $^2$   
 (see: <https://arxiv.org/pdf/1703.04471.pdf>)

# Absolute $\nu_\tau$ cross-section measurement

$$\sigma_{\nu_\tau} = \sigma_{\nu_\tau}^{const} E K(E)$$

Until now,  $\nu_\tau$  cross section measured only by DONuT  
DONuT could not distinguish  $\nu_\tau$  from anti- $\nu_\tau$

► OPERA: First measurement with  $\nu_\tau$  only

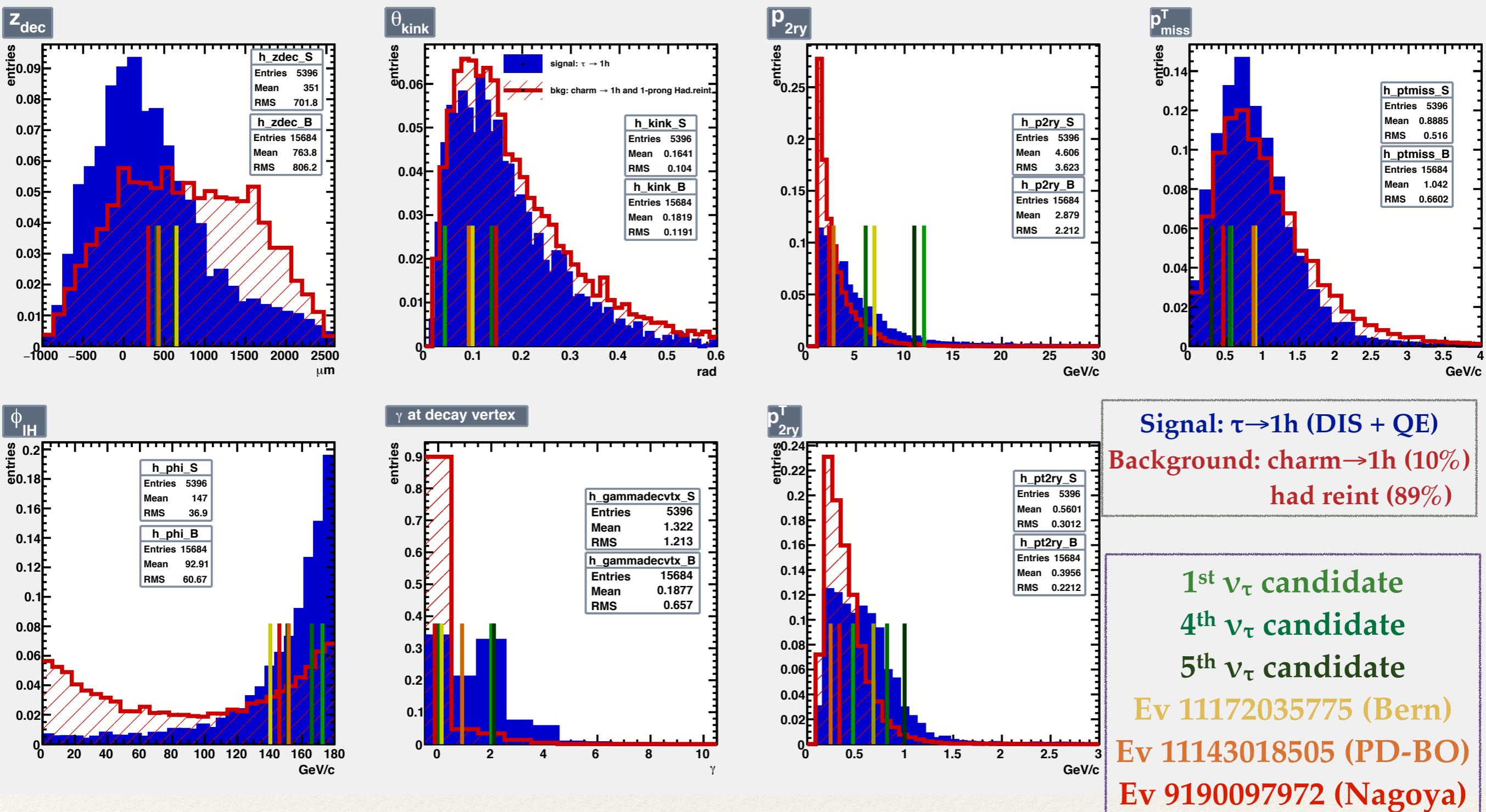


	Expected Signal	Expected Background	Observed $\nu_\tau$	$\sigma_{\nu_\tau}^{const}$ ( $10^{-38} \text{cm}^2 \text{GeV}^{-1}$ ) (68% C.L)      (90% C.L)
<u>Preliminary</u> $\Delta m_{23}^2 = 2.5 \cdot (10^{-3} \text{ eV}^2)$	6.5	2.0	10	$0.8^{+0.4}_{-0.3}$ [0.36 – 1.49]

Assuming maximal mixing and PDG2016  $\Delta m_{23}^2$

Agreement with SM value  $0.67 \cdot 10^{-38} \text{cm}^2 \text{GeV}^{-1}$   
within  $1\sigma$

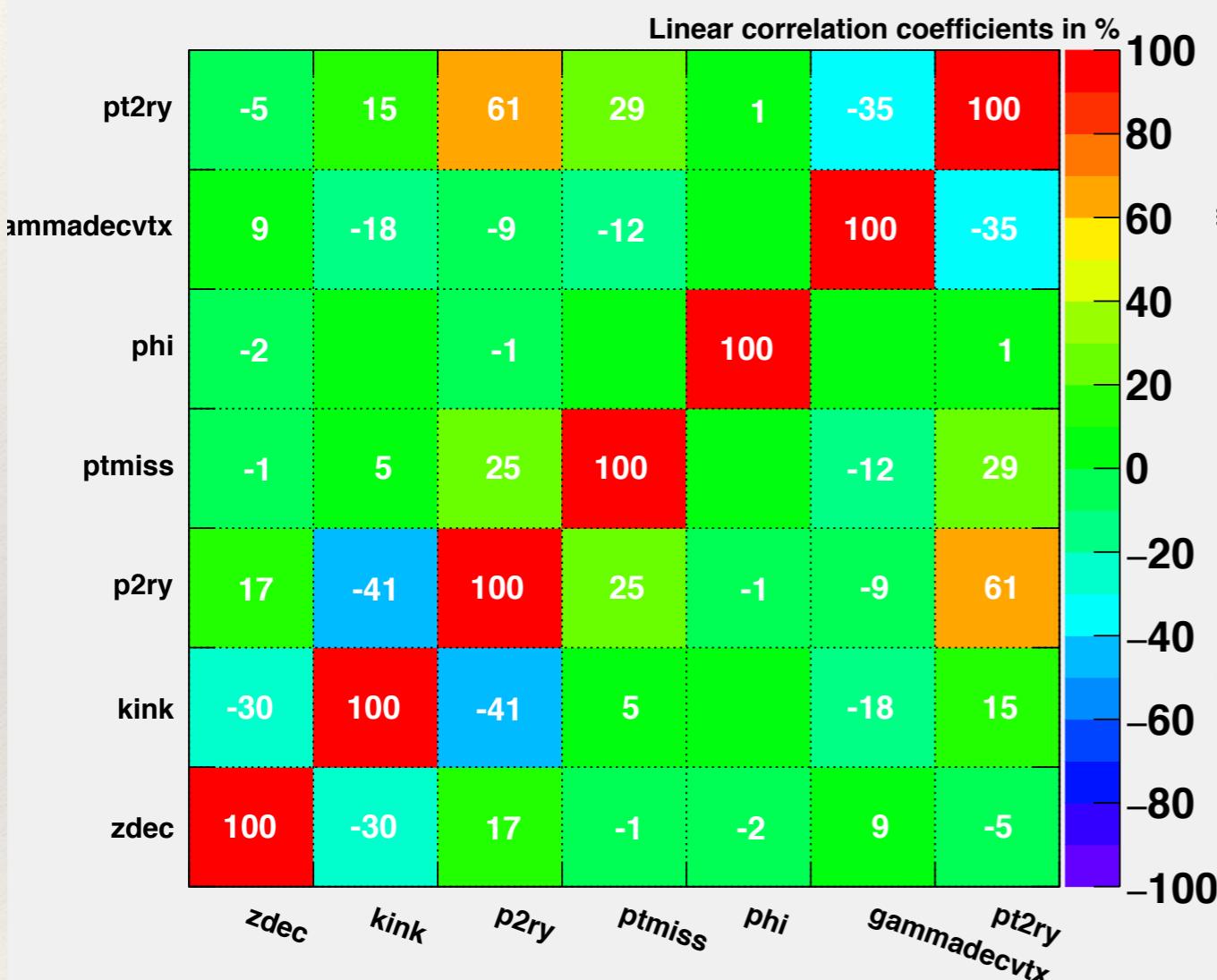
# $\tau \rightarrow 1h$ Kinematical variables



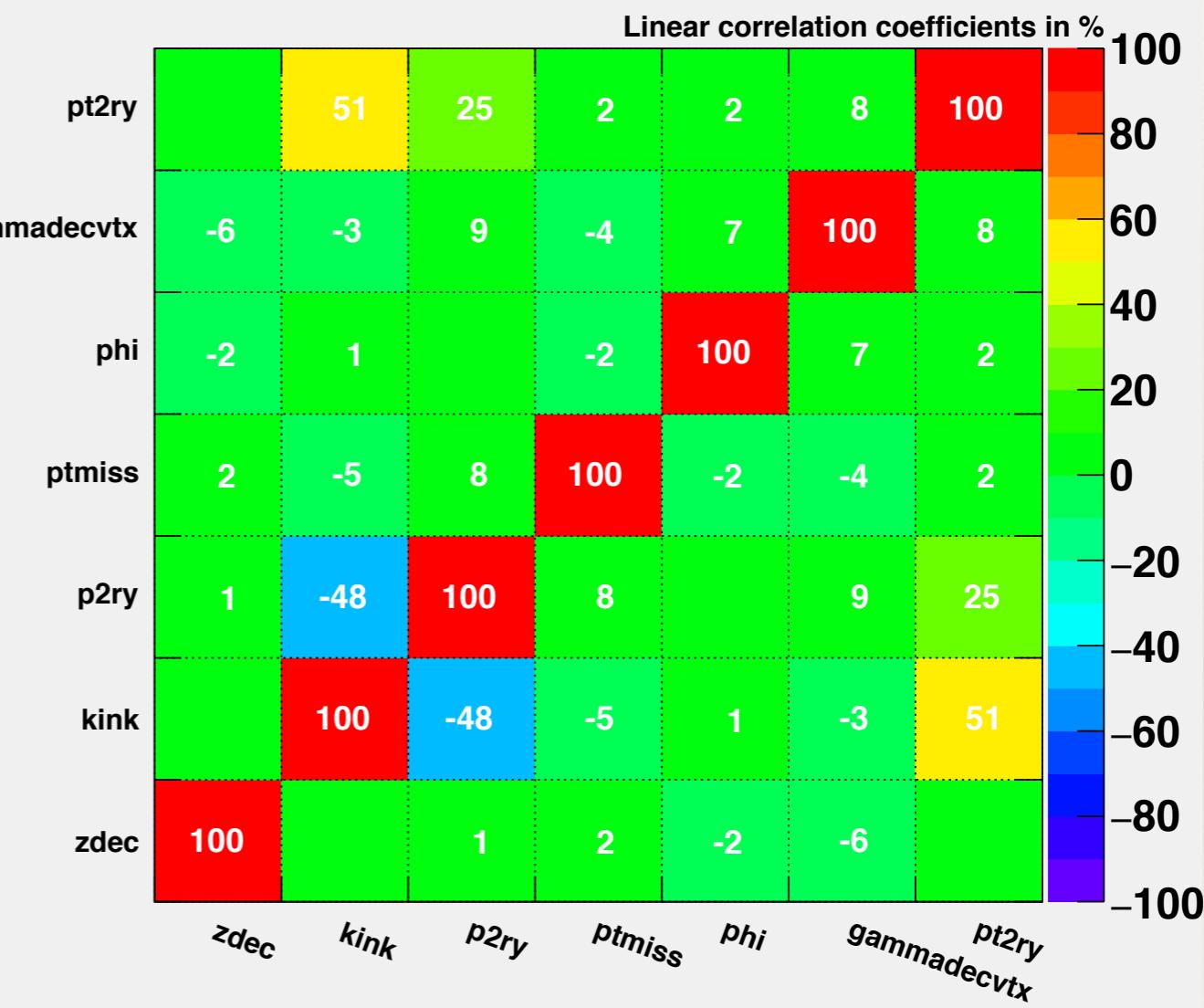
- $\tau$  distribution weighted for oscillation Probability
- charm distribution weighted for charm production Probability

# $\tau \rightarrow 1h$ Correlation Matrices

Correlation Matrix (signal)

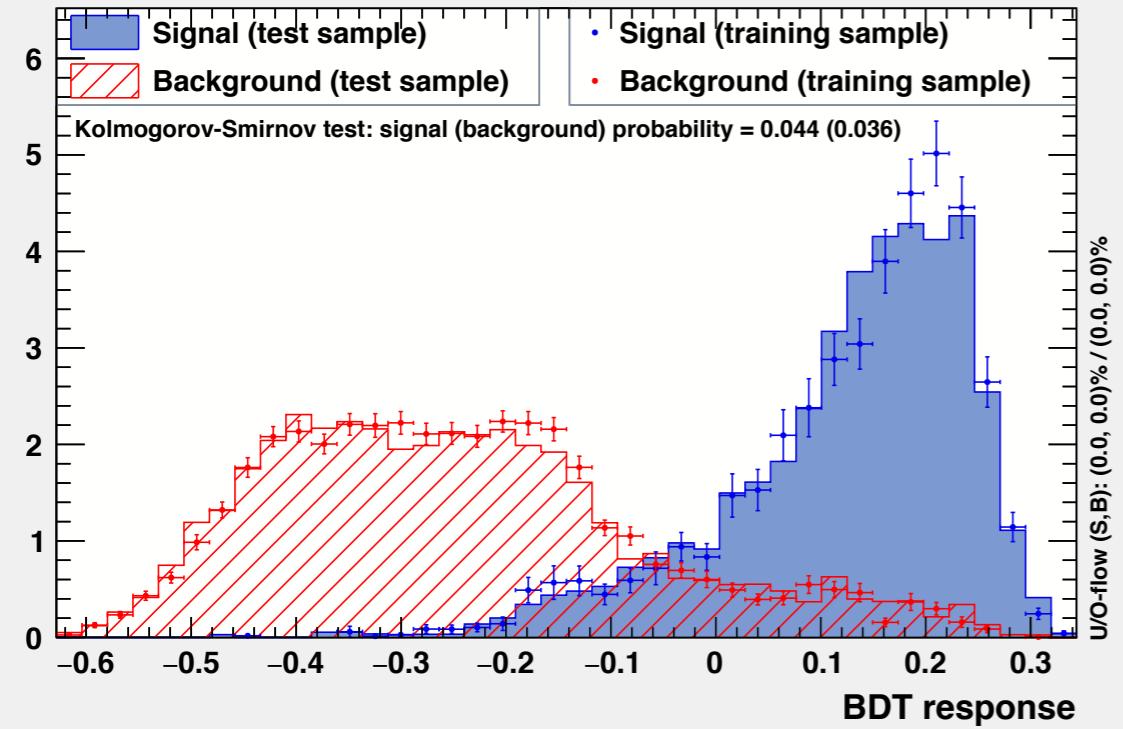


Correlation Matrix (background)



# $\tau \rightarrow 1h$ RESULTS

TMVA overtraining check for classifier: BDT

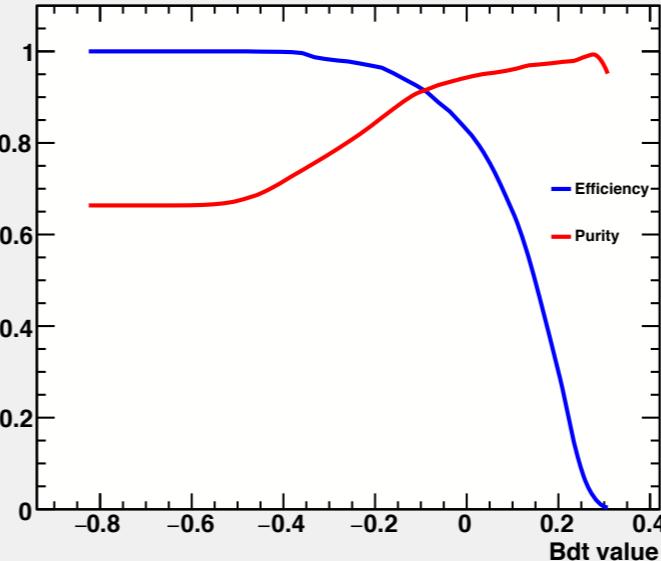


Signal & Bkg normalized for the number of expected events

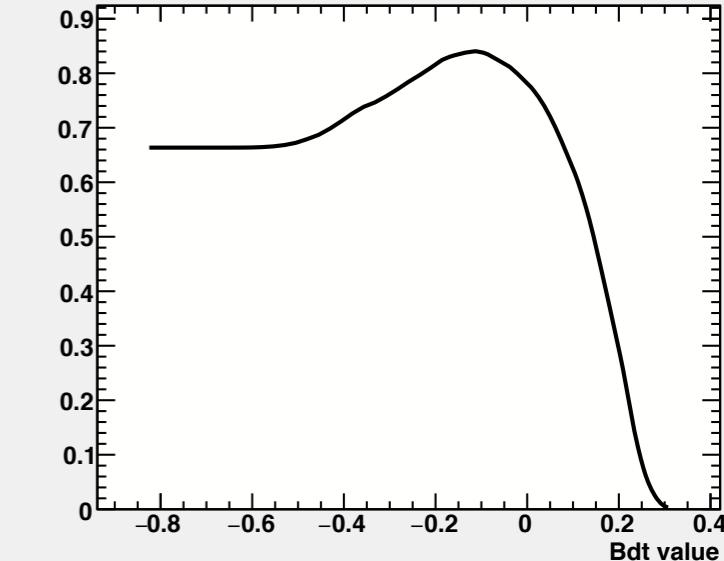
signal = 93%  
bkg = 19%

1.4 expected event of bkg for  $\tau \rightarrow 1h \Rightarrow$   
1 event classified as bkg:  
*good understanding of background*

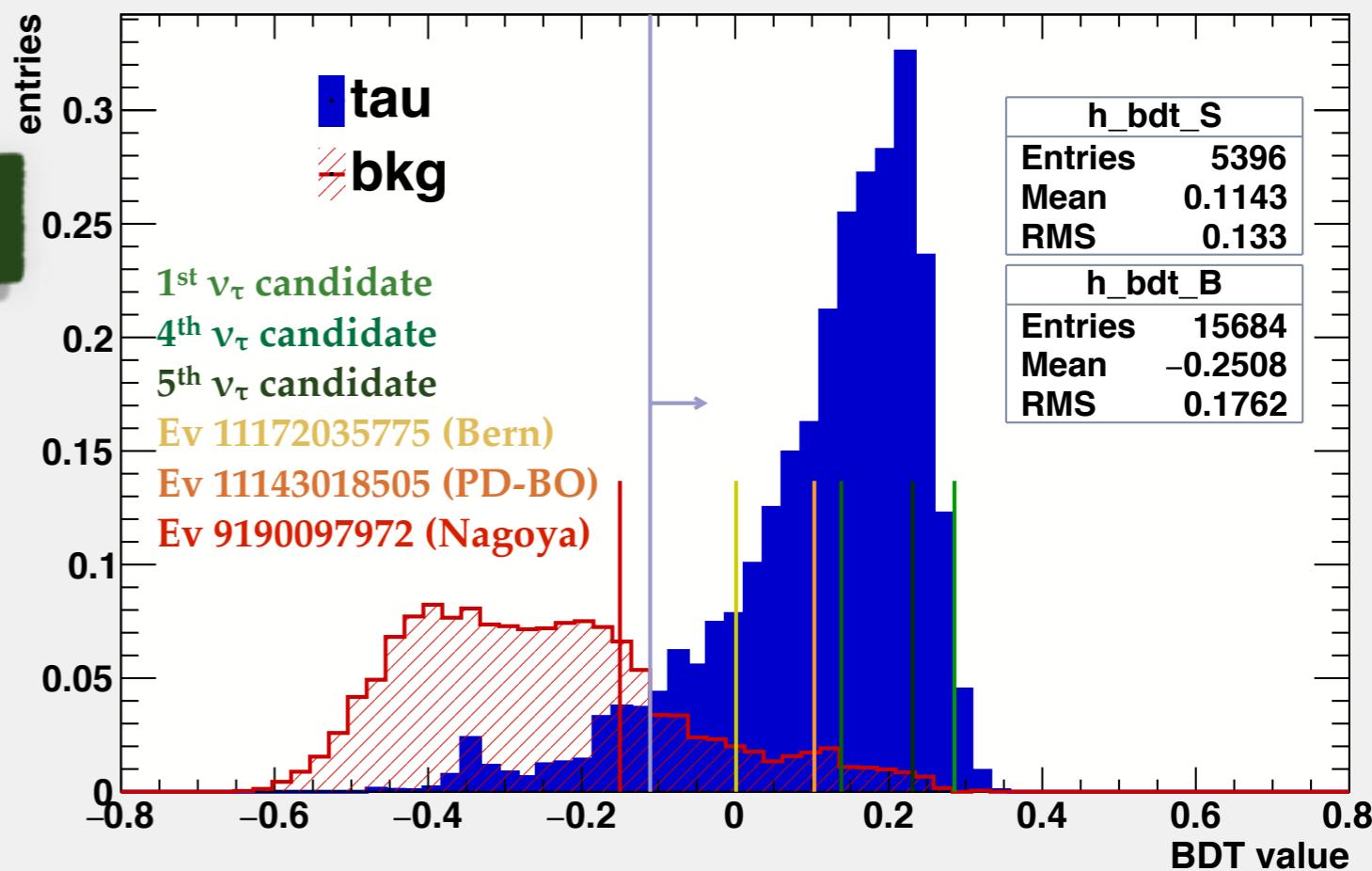
Efficiency and Purity vs cut



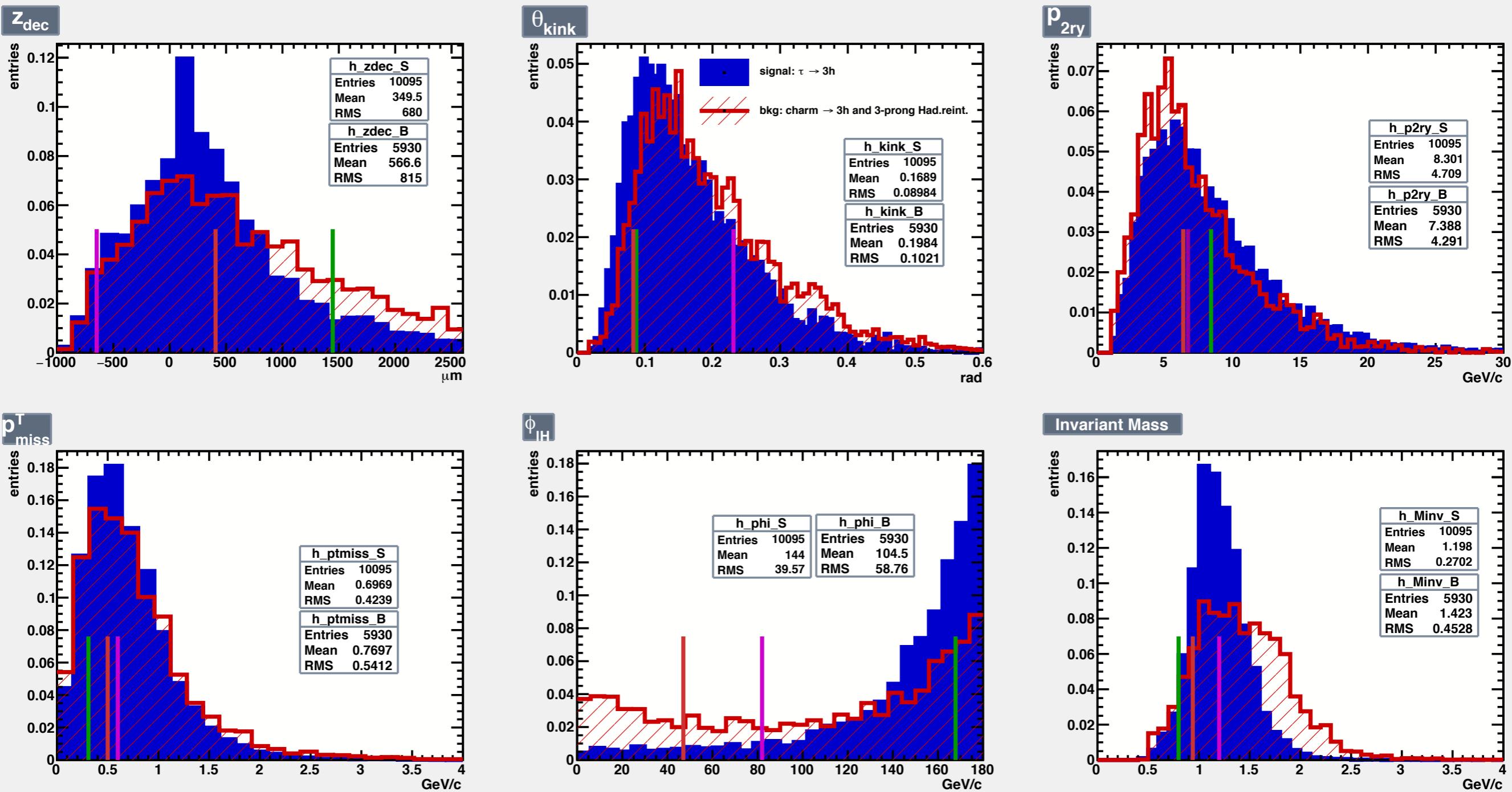
Efficiency\*Purity



BDT



# $\tau \rightarrow 3h$ Kinematical Variables



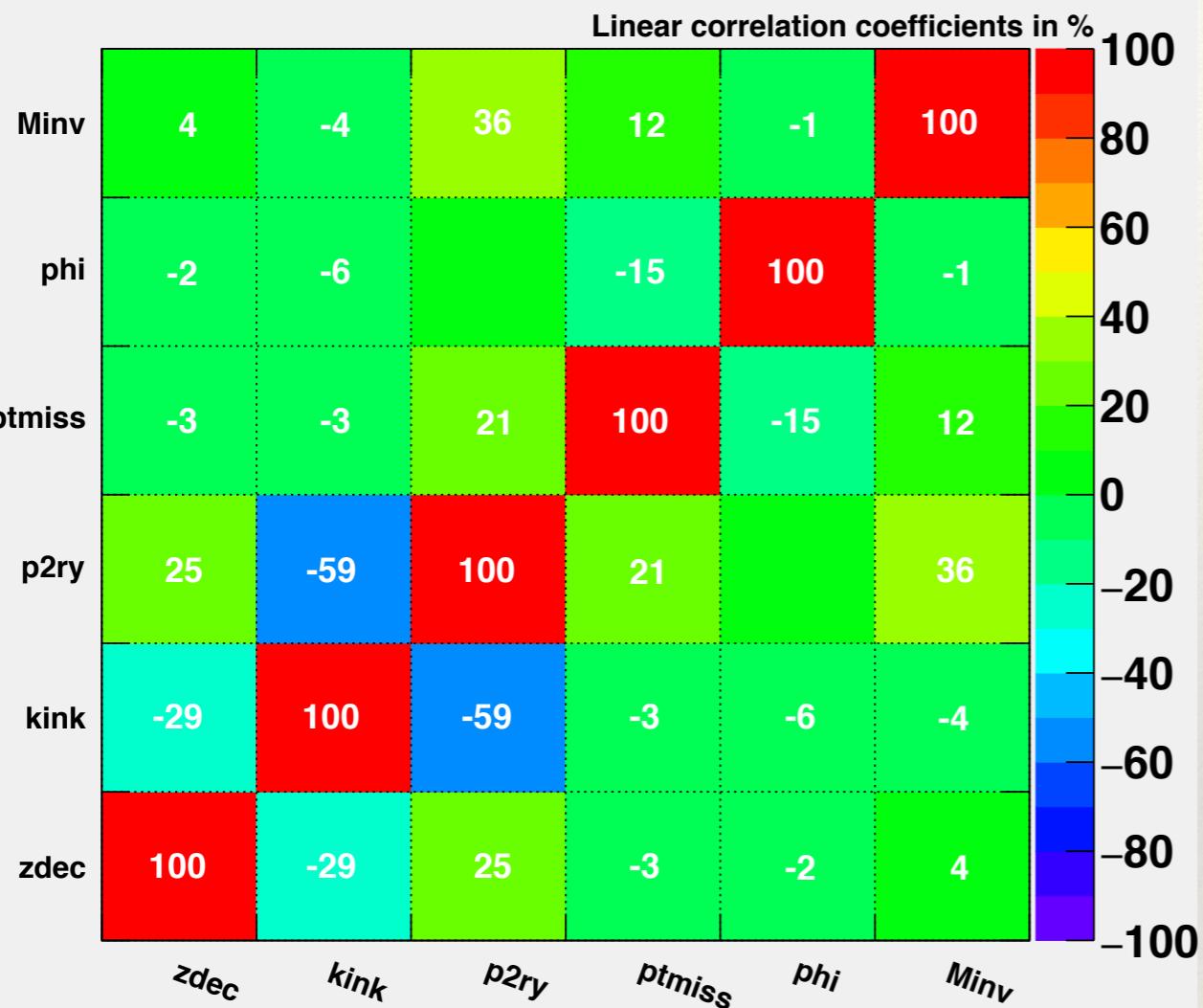
- $\tau$  distribution weighted for oscillation Probability
- charm distribution weighted for charm production Probability
- had reint weight = 1

Signal:  $\tau \rightarrow 3h$  (DIS + QE)  
 Background: charm  $\rightarrow 3h$  (83%)  
 had reint (17%)

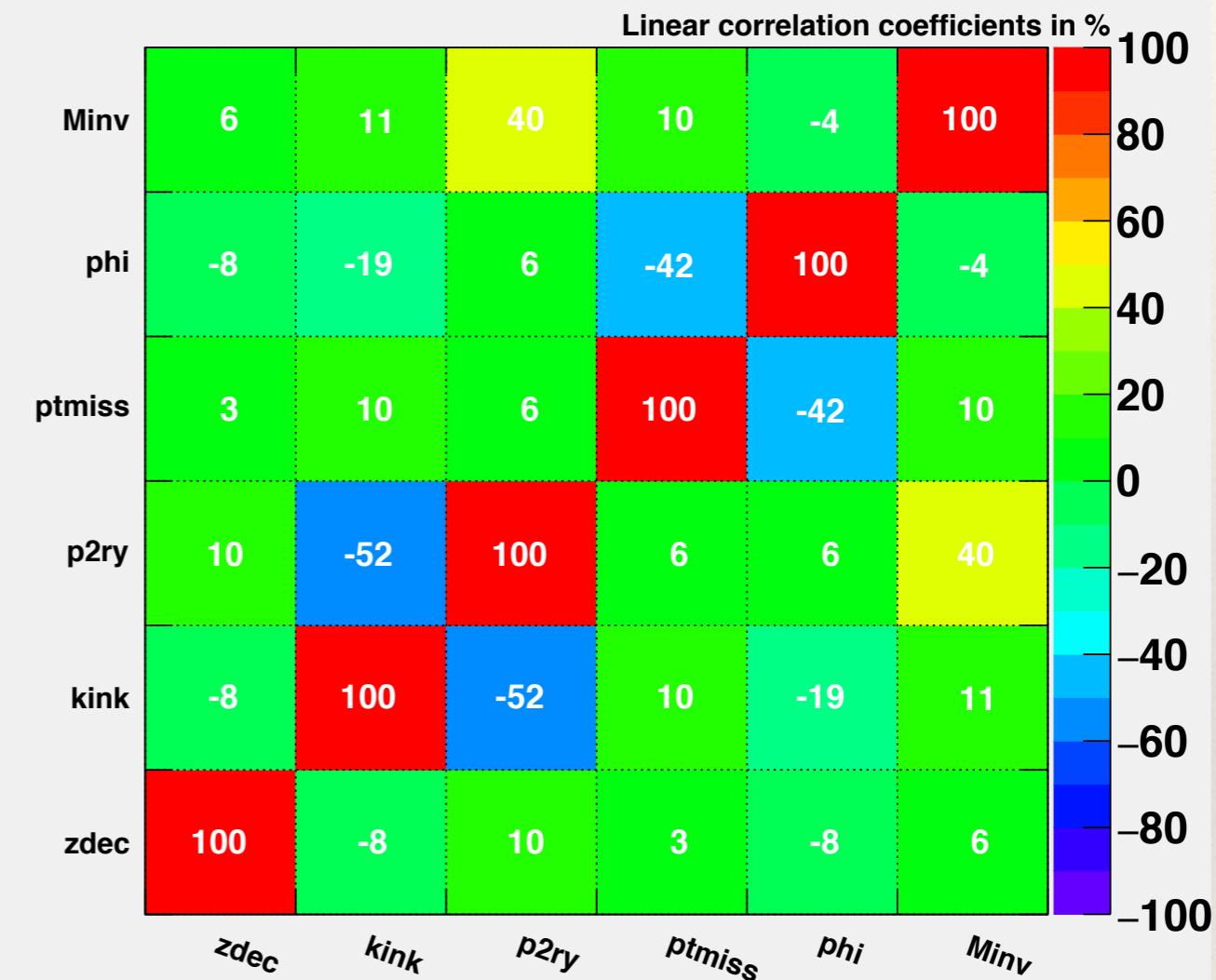
2<sup>nd</sup>  $v_\tau$  candidate  
 Ev 10123059807 (Bari)  
 Ev 11213015702 (Nagoya)

# $\tau \rightarrow 3h$ Correlation Matrices

Correlation Matrix (signal)



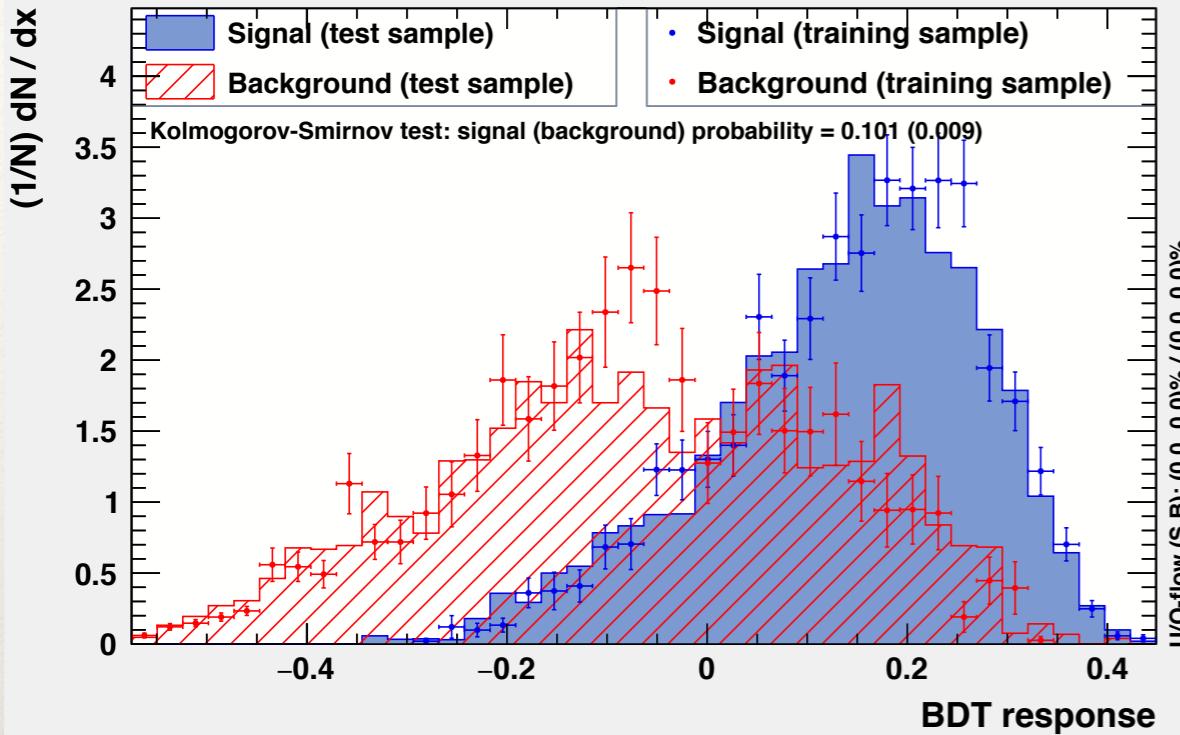
Correlation Matrix (background)



High correlation between Invariant mass and minimum invariant mass: the latter was eliminated from the analysis

# $\tau \rightarrow 3h$ RESULTS

TMVA overtraining check for classifier: BDT



PROBLEM: low statistics!!

2<sup>nd</sup>  $\nu_\tau$  candidate

Ev 10123059807 (Bari)

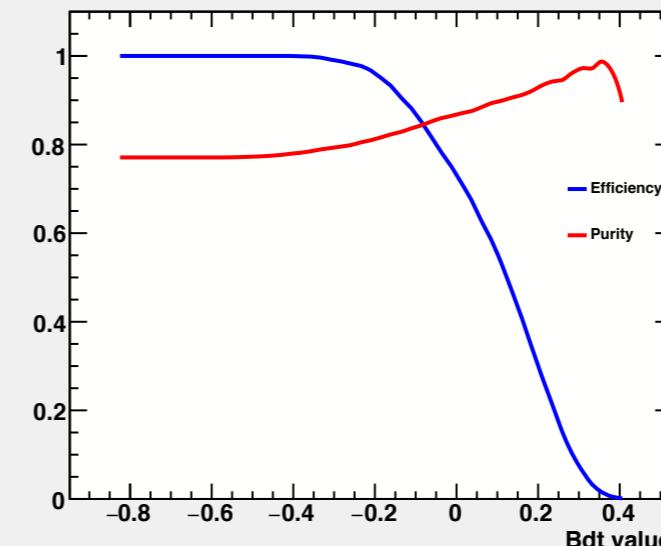
Ev 11213015702 (Nagoya)

Signal & Bkg normalized for  
the number of expected events

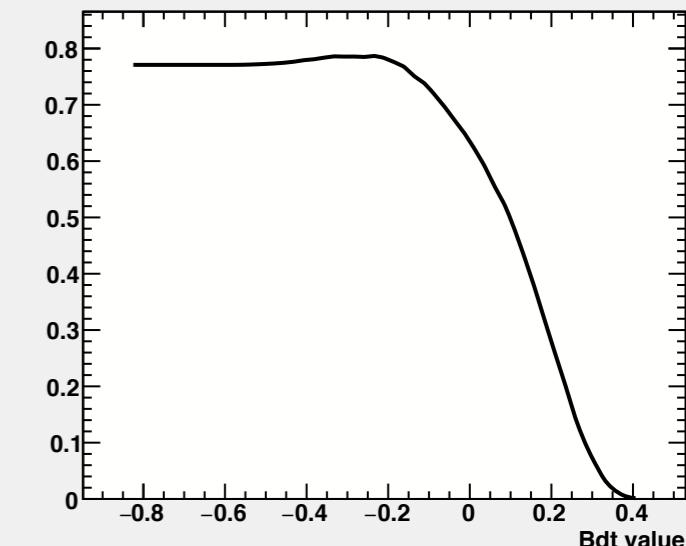
signal = 98%

bkg = 80%

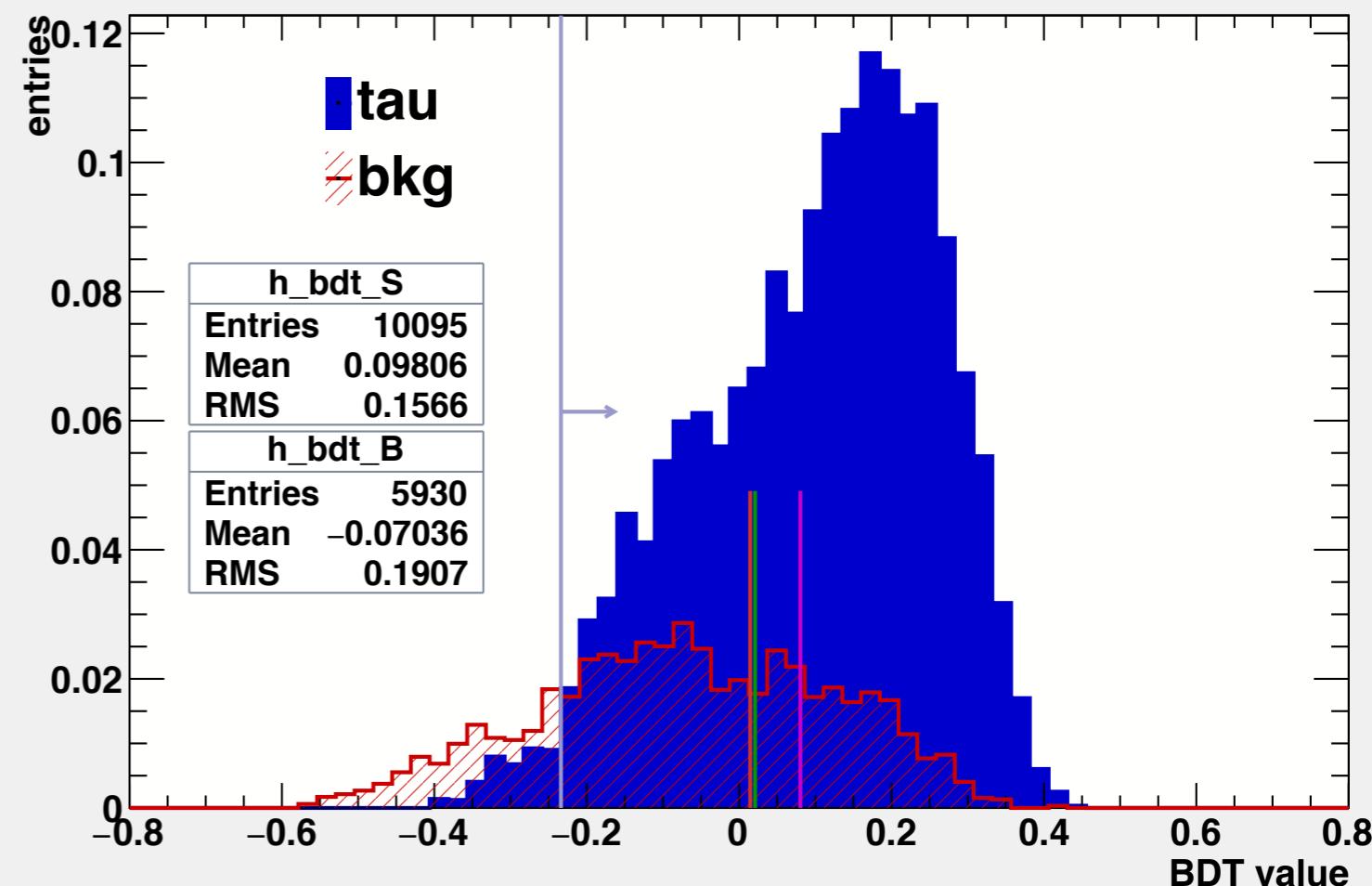
Efficiency and Purity vs cut



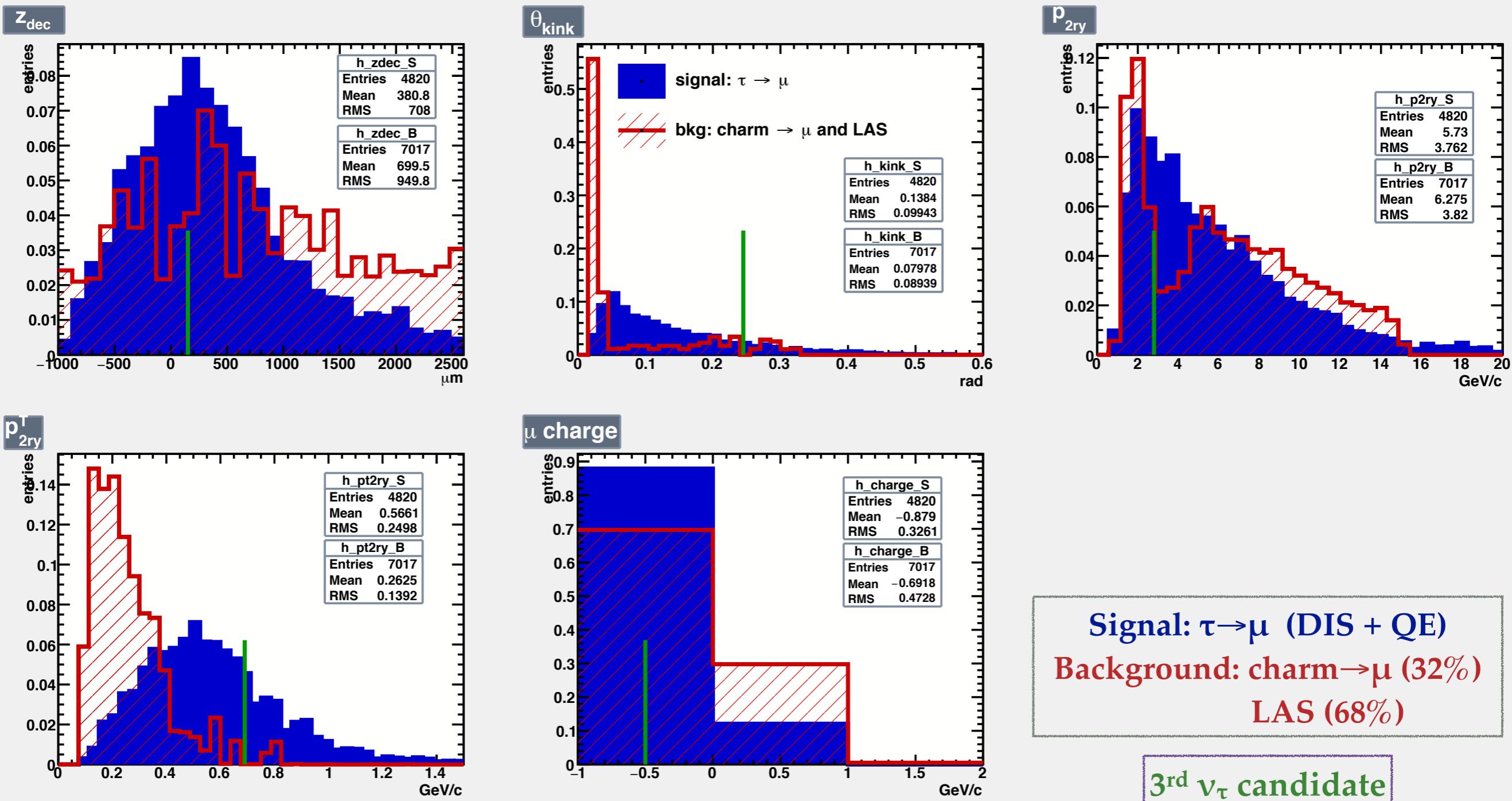
Efficiency\*Purity



BDT



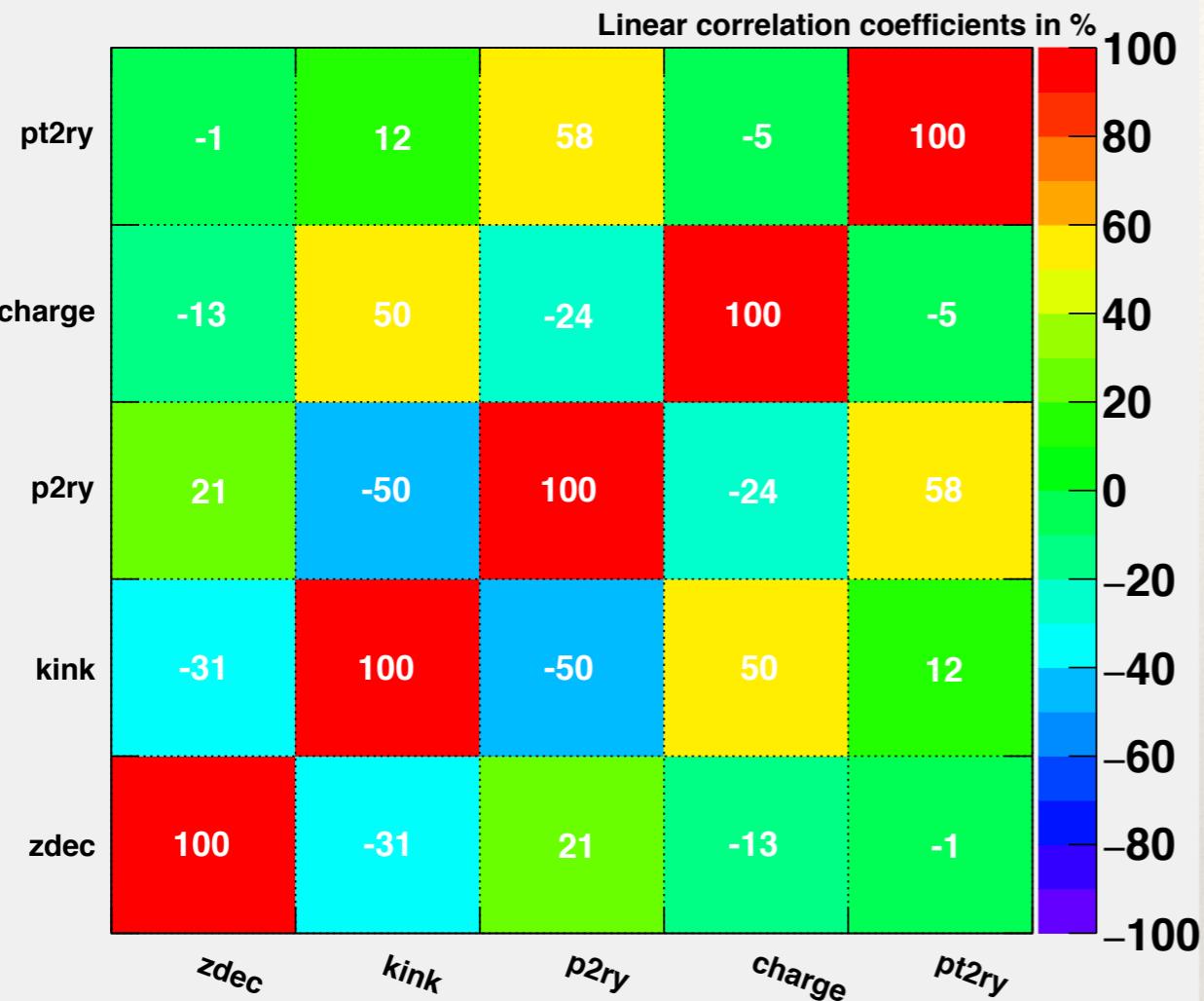
# $\tau \rightarrow \mu$ Kinematical Variables



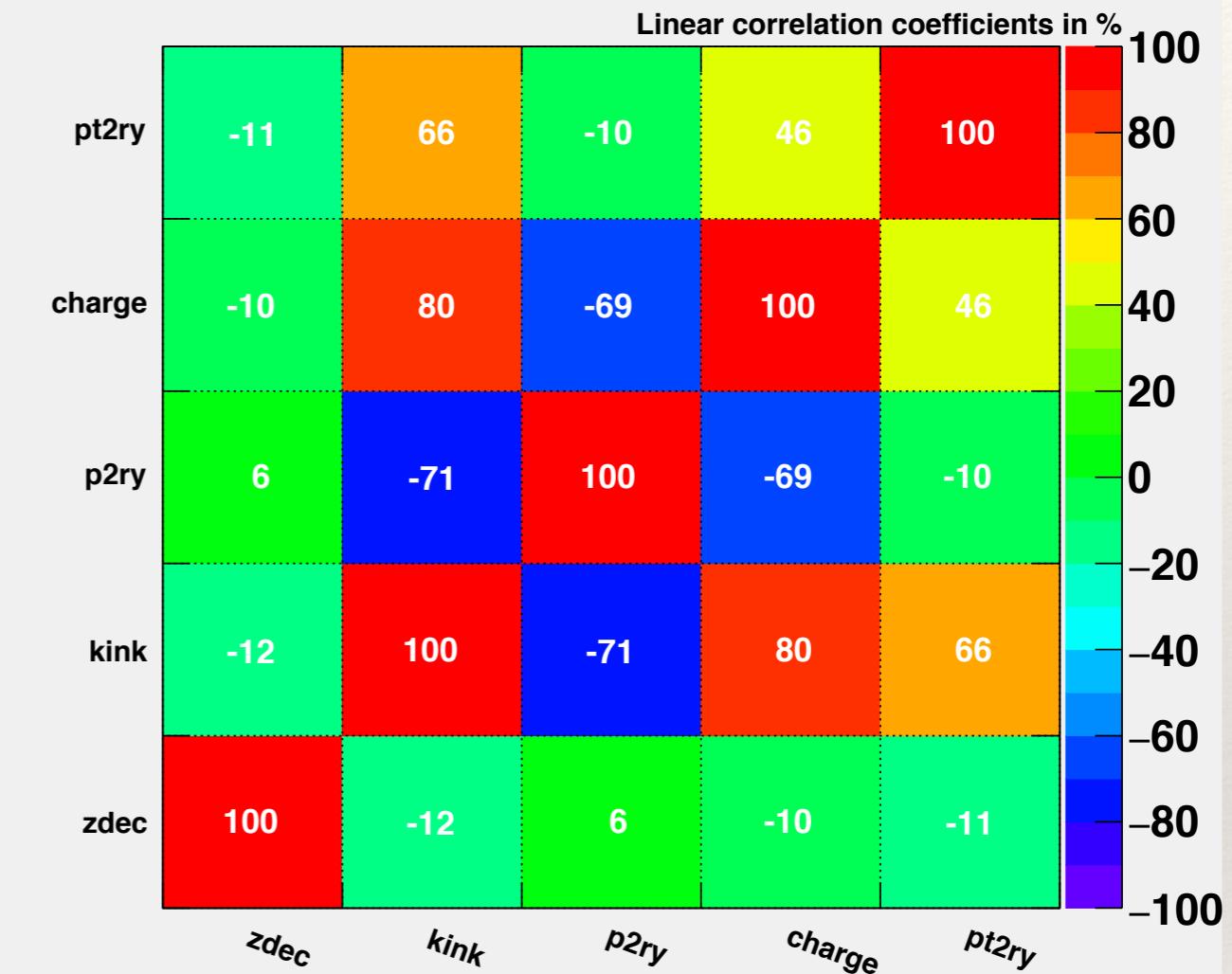
- $\tau$  distribution weighted for oscillation Probability
- charm distribution weighted for charm production Probability
- LAS weight = 1

# $\tau \rightarrow \mu$ Correlation Matrices

Correlation Matrix (signal)

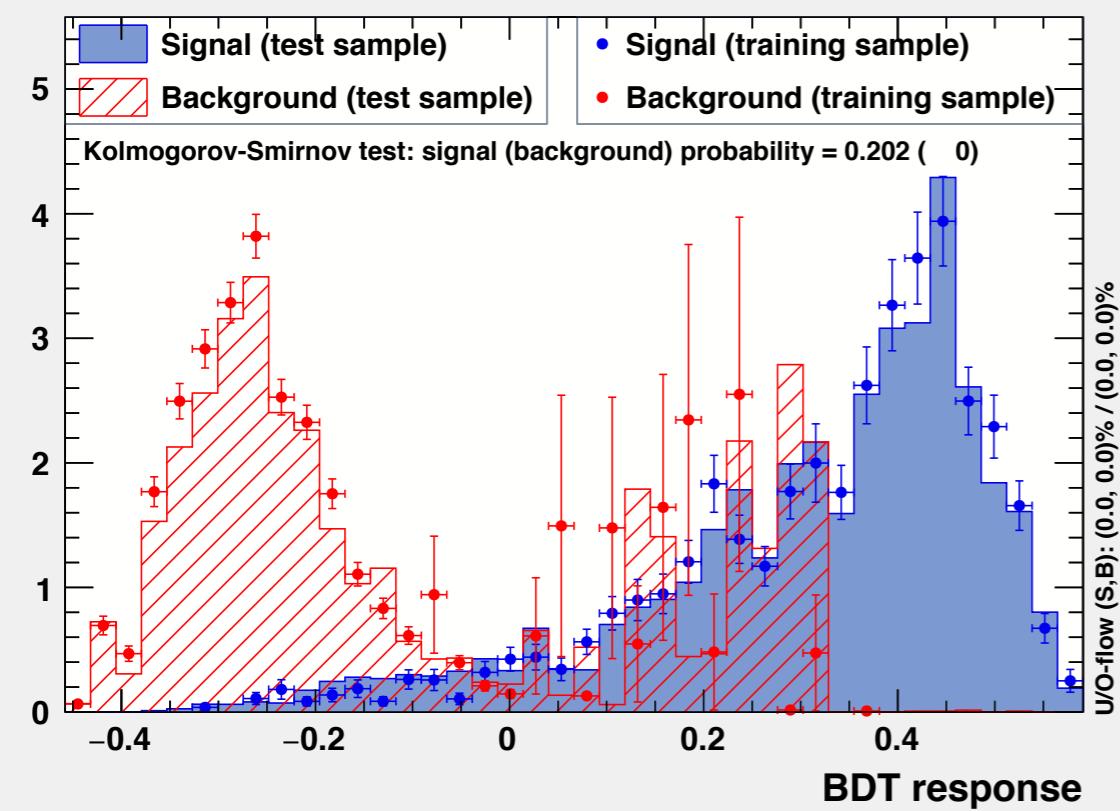


Correlation Matrix (background)



# $\tau \rightarrow \mu$ RESULTS

TMVA overtraining check for classifier: BDT

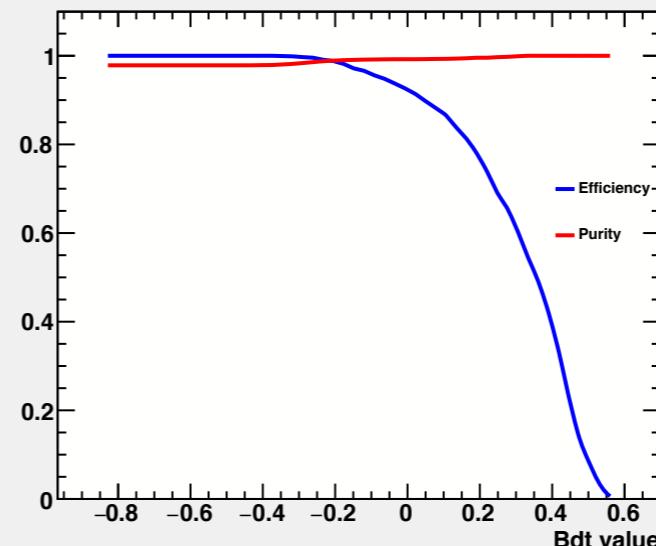


PROBLEM: low statistics, especially for charm!!

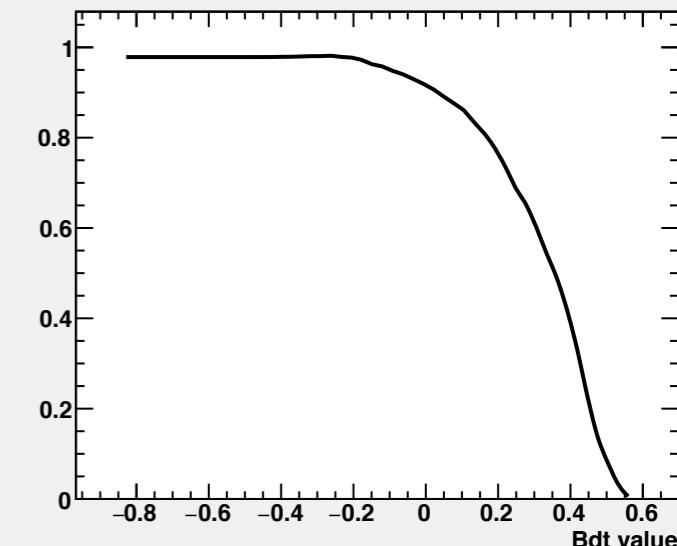
Signal & Bkg normalized for the number of expected events

signal = 99.6%  
bkg = 66%

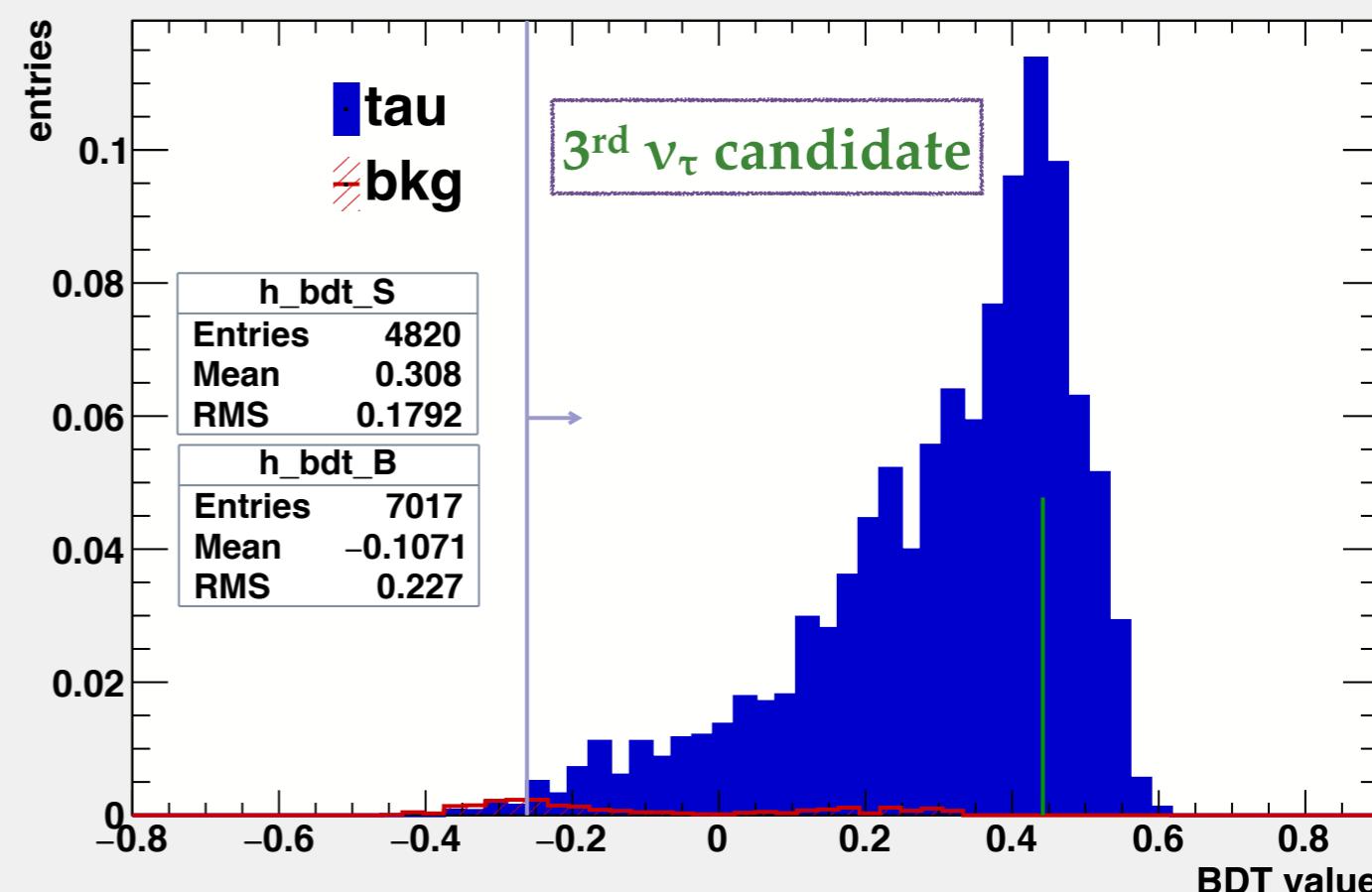
Efficiency and Purity vs cut



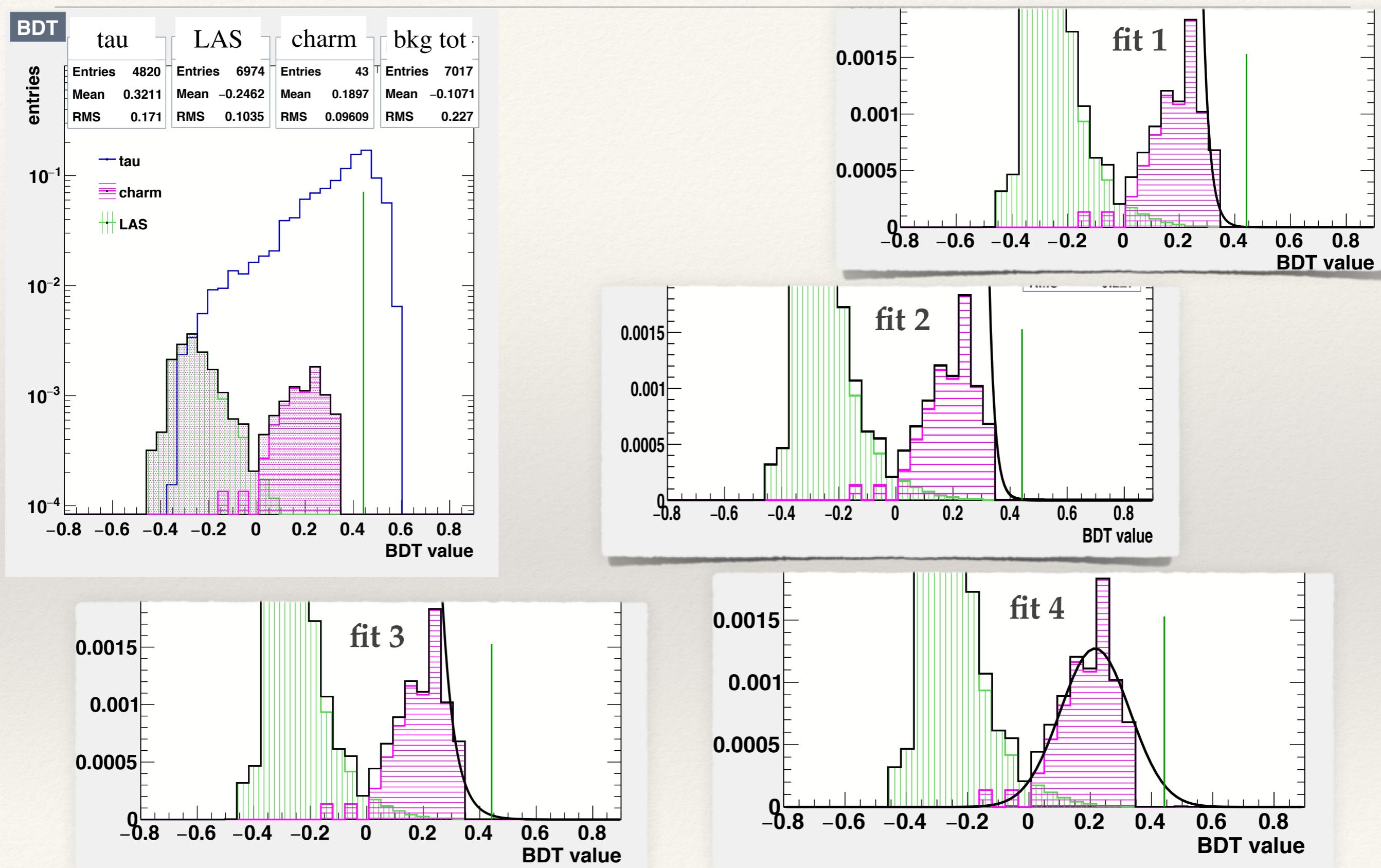
Efficiency\*Purity



BDT



# $\tau \rightarrow \mu$ RESULTS



# LEPTON NUMBER MEASUREMENT

Likelihood test for background only hypothesis:  
Poisson + BDT

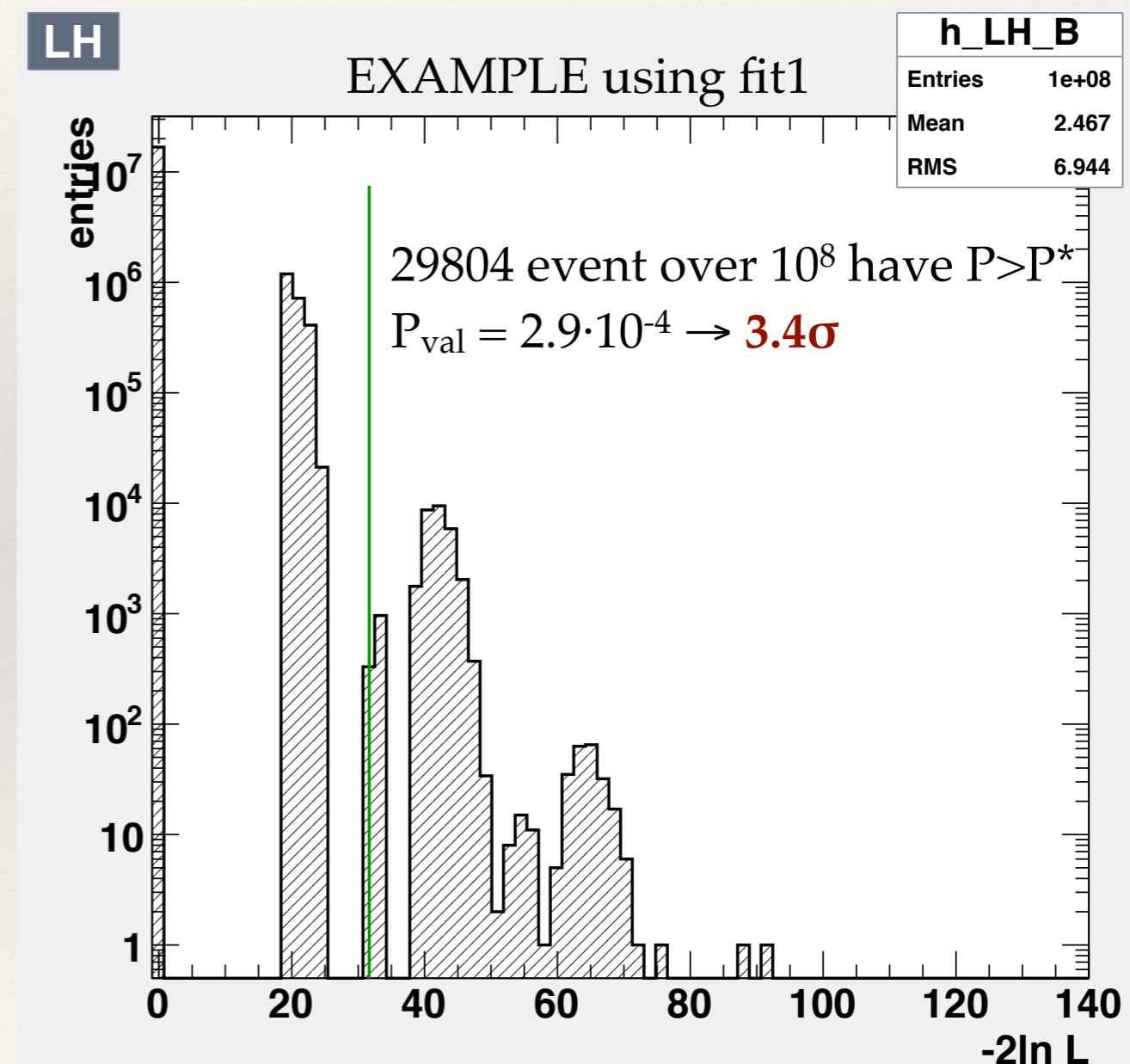
Pseudo Experiments:  $10^8$

fit	P*	P	$\sigma$
1	31.6678	2.9804E-04	3.43
2	33.0272	2.9473E-04	3.44
3	27.9158	2.9804E-04	3.43
4	24.8093	2.97748E-04	3.43

Preliminary significance: **3.4 $\sigma$**

$$\mathcal{L} = \text{Poisson}(n|b) \cdot \prod_{i=1}^n f(BDT_i)$$

(Syst. errors on  $b$  not taken into account at the moment)

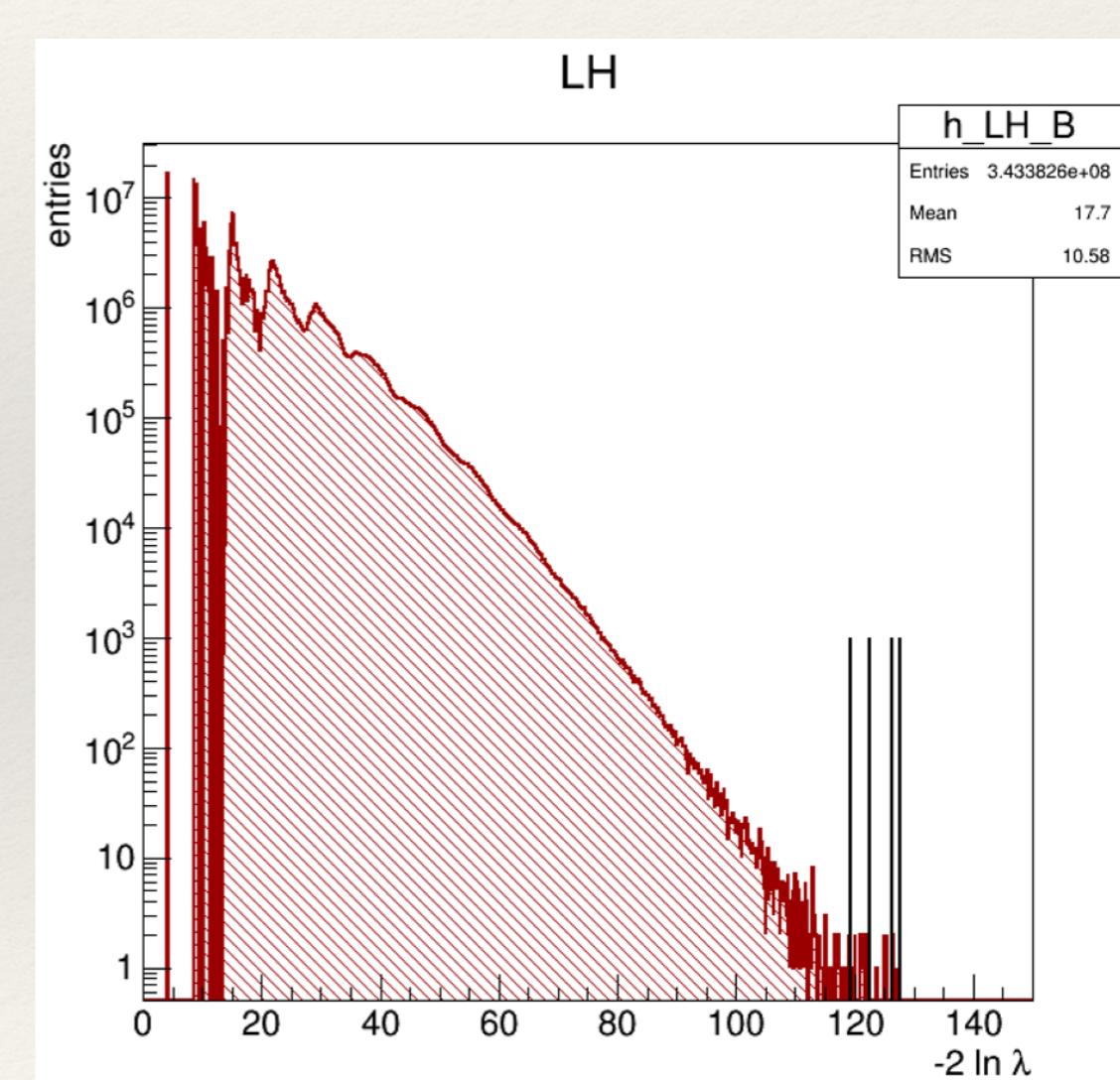


# Significance (III)

Significance obtained combining the discriminating power of the BDT analysis and Poisson with the Likelihood method:

$$\mathcal{L} = \prod_{ch=1}^4 \left( \frac{b_{ch}^{n_{ch}} e^{-b_{ch}}}{n_{ch}!} \cdot \prod_{i=1}^{n_{ch}} f(BDT_{ch_i}) \right)$$

<i>fit</i>	P*	N exp P>P*	P	$\sigma$
1	126.309	4	1.4561E-08	5.55
2	127.668	1	2.9122E-09	5.82
3	122.557	10	2.9122E-08	5.42
4	119.45	25	7.28051E-08	5.26



# Conclusions

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- ❖ Cross check with efficiencies used for tau articles performed → Good agreement reached
- ❖  $\Delta m^2_{23}$  and absolute  $\nu_\tau$  cross-section measurement: agreement with PDG2016 value / SM prediction within  $1\sigma$
- ❖ BDT analysis: more statistics is needed
- ❖ Minimum bias analysis significance  $> 5\sigma$  with  $P^*$ -method, Likelihood (8 channels mode) and BDT

# Back-up

# 8 channels

	charm	had reint	las	tot bkg	Expected signal	Observed
$\tau \rightarrow 1h$	0.02	0.024	0.00	0.05	0.57	3
$\tau \rightarrow \mu$	0.003	0.00	0.0002	0.003	0.55	1
$\tau \rightarrow 3h$	0.20	0.003	0.00	0.21	1.09	1
$\tau \rightarrow e$	0.03	0.00	0.00	0.03	0.75	0
$\tau \rightarrow 1h$	0.13	1.26	0.00	1.39	2.25	3
$\tau \rightarrow \mu$	0.005	0.00	0.02	0.02	0.54	0
$\tau \rightarrow 3h$	0.23	0.08	0.00	0.31	0.66	2
$\tau \rightarrow e$	0.00	0.00	0.00	0.00	0.04	0
<b>Total</b>	0.63	1.37	0.02	2.02	6.46	10

# Final sample

Run year	0μ DS	1μ DS
2008	150	543
2009	255	1024
2010	278	1001
2011	291	1031
2012	223	807
<b>TOTAL</b>	<b>1197</b>	<b>4406</b>

# $\nu_\mu$ efficiencies

	v	err	v	err
1 $\mu$	46.47	0.24	13.39	0.33
0 $\mu$	2.99	0.08	30.47	0.44

# Marginal Events

LAB	Event ID	Ev Class	Topo logy	zdec	DL	ptmiss	phi	P <sub>t</sub> (GeV/c)	P <sub>dau Total</sub> (GeV/c)	psum	kink	massa inv	m min inv	$\gamma$ at decvtx	TFD
1 <sup>st</sup> cand	9234119599	0 $\mu$	kink	435 $\pm$ 35	1135 $\pm$ 35	0,52 <sup>+0,32</sup> <sub>-0,17</sub>	173 $\pm$ 2	0,47 <sup>+0,24</sup> <sub>-0,12</sub>	12 <sup>+6</sup> <sub>-3</sub>	24,3 <sup>+3,9</sup> <sub>-2,7</sub>	0,041 $\pm$ 0,002	/	/	2	DONE
2 <sup>nd</sup> cand	11113019758	0 $\mu$	trident	1446 $\pm$ 10	1466 $\pm$ 10	0,31 $\pm$ 0,11	167,8 $\pm$ 1,1	/	8,4 $\pm$ 1,7	12,7 <sup>+1,7</sup> <sub>-2,3</sub>	0,0874 $\pm$ 0,0015	0,80 $\pm$ 0,12	0,96 $\pm$ 0,13	0	DONE
3 <sup>rd</sup> cand	12123032048	1 $\mu$	kink	151 $\pm$ 10	376 $\pm$ 10	/	/	0,69 $\pm$ 0,05	2,8 [2,6; 3,0]	6,8 <sup>+0,9</sup> <sub>-0,6</sub>	0,245 $\pm$ 0,005	/	/	0	DONE
4 <sup>th</sup> cand	12254000036	0 $\mu$	kink	406 $\pm$ 30	1090 $\pm$ 30	0,55 <sup>+0,3</sup> <sub>-0,2</sub>	166 <sup>+2</sup> <sub>-31</sub>	0,82 <sup>+0,3</sup> <sub>-1,6</sub>	6,0 [4,8; 8,2]	14,4 <sup>+3,9</sup> <sub>-2,7</sub>	0,137 $\pm$ 0,004	/	/	0	DONE
5 <sup>th</sup> cand	12227007334	0 $\mu$	kink	630 $\pm$ 30	960 $\pm$ 30	0,3 $\pm$ 1	151 $\pm$ 1	1 <sup>+1,1</sup> <sub>-0,4</sub>	11 <sup>+14</sup> <sub>-4</sub>	12 <sup>+14</sup> <sub>-4</sub>	0,090 $\pm$ 0,002	/	/	0	DONE
Bo-Pd	11143018505	0 $\mu$	kink	429,6	1160	0.876	151,8	0.24	2,7 [2,13; 3,70]	23.2	0.090	/	/	1	DONE
Bern	11172035775	0 $\mu$	kink	652	1100	0,90 [0,79;1,16]	140.4	0,68 [0,56; 0,90]	6,9 [5,7; 9,2]	32.2	0.098	/	/	0	NOT NEED
Nagoya	9190097972	0 $\mu$	kink	10	822	0,46	142,8	0,33	2,2 [1,6; 3,6]	9,6	0.146	/	/	0	NOT NEED
Bari	10123059807	0 $\mu$	trident	-648	140	>0,6	82	/	6,7	16,4	0.231	1,2	2	0	DONE
Nagoya	11213015702	0 $\mu$	trident	407	256	0,5	47,1	>0,40	> 6,3	>6.78	0.083	0.94	1.42	2	NOT NEED