Driving Questions:

- **LSST Techniques**
  - Which combinations of techniques will ensure that the LSST results are as precise and robust as possible? What type of external data would be particularly beneficial to include?

- **Clusters in Multiple Bands**
  - Cluster data in **optical**, **X-ray**, and **microwave**
  - What are the strengths and weaknesses of these three techniques? How are they complementary? How should we combine them to obtain the best dark energy constraints possible from galaxy clusters in the 2020s?

- **Post-LSST Surveys**
  - What ground based survey project do you propose should be carried out after LSST? Consider telescope size, location, observing wavelength, instrumentation and anticipated cost alongside the expected science payoffs.
Large Synoptic Survey Telescope (LSST)

Most ambitious optical survey to date:

- 8.4 m primary mirror with a **3.5 deg** field of view
- 3.2 gigapixel camera in **6 bands** (ugrizy)
- **18,000 deg²** coverage of southern sky
  - Full footprint imaged every ~3 days
- Estimated 40 billion objects (20 billion galaxies) to be imaged over 10 years
  - For the expected 800 visits, that is **32 trillion observations**
LSST Science Goals

“Massively parallel astrophysics”

- A Comprehensive Survey of the Solar System
- Structure and Stellar Content of the Milky Way
- The Variable Universe
- The Evolution of Galaxies
- Cosmological Models, and the Nature of Dark Energy and Dark Matter

From LSST Science Book: https://arxiv.org/abs/0912.0201
LSST Dark Energy Probes

LSST will be able to distinguish between different models of dark energy by using a number of cosmological probes sensitive to cosmic **growth** and **geometry**; largely independent from one another.

- **Weak Gravitational Lensing**: Growth; Geometry
- **Strong Gravitational Lensing**: Geometry
- **Supernovae**: Geometry
- **Baryonic Acoustic Oscillations (BAO)**: Geometry
- **Galaxy Clusters**: Growth; geometry

These different probes can also be used as cross checks to understand and **calibrate systematic errors**.
LSST Dark Energy Probes

LSST will be able to distinguish between different models of dark energy by using a number of cosmological probes sensitive to cosmic growth and geometry; largely independent from one another.

- **Weak Gravitational Lensing**: Cluster mass calibrations, shear correlations, halo-mass function
- **Strong Gravitational Lensing**: Time delays, $10^3$-$10^4$ SL AGN
- **Supernovae**: SN peculiar velocities, ~100 strongly lensed SN, color calibration
- **Baryonic Acoustic Oscillations (BAO)**: Better statistics in angular matter power spectrum
- **Galaxy Clusters**: Evolution of mass function, Cluster density at high $z$

These different probes can also be used as cross checks to understand and calibrate systematic errors.
Robustness: Breaking Degeneracies and Consistency

As we only get one realization of the universe, it is important to have numerous **cross-checks** and **independent measures** of cosmological parameters.

Individual probes are only sensitive to some params, but independent probes can help break degeneracies in parameter space.

As all of these probes come from the same experiment, it is easier to calibrate systematics and maximize consistency of comparison (same cosmic volume).

Further enhanced by the survey’s excellent uniformity and completeness.
Complementary Probes: BAO and Weak Lensing

Constraints from WL are sensitive to photo-z errors, but not the shear power spectrum itself

- Galaxy # density correlation in cross-bin galaxy power spectra *calibrates photo-z’s!*

Galaxy clustering bias degenerate for angular BAO measurements

- $gg, g\gamma, \gamma\gamma$ power spectra sensitive to different powers of galaxy bias; *calibrates bias* for BAO

These probes *mutually calibrate systematics* and strengthen parameter constraints with information *not captured in either technique alone*
Angular power spectrum

Cross-bin power spectrum

Priors on photo-z bias

Priors on photo-z RMS

(LSST Science Book)
Robustness of LSST Approach: **“Wide, Deep, Fast”**

‘By simultaneously measuring the redshift/distance relation and the growth of cosmic structure, LSST data can test whether the recent acceleration is due to dark energy or modified gravity. Because of its wide area coverage, LSST will be uniquely capable of constraining more general models of dark energy. LSST’s redshift coverage will bracket the epoch at which dark energy began to dominate the cosmic expansion. Much of the power of the LSST will come from the fact that all the different measurements will be obtained from the same basic set of observations, using a facility that is optimized for this purpose. The wide-deep LSST survey will allow a unique probe of the isotropy and homogeneity of dark energy by mapping it over the sky, using weak lensing, supernovae and BAO, especially when normalized by Planck observations.’ - *Science Book Introduction*
LSST Robustness: Shapes and Photo-z Calibration

Some of the worst errors in imaging surveys are photo-z estimation and galaxy shape noise.

If the distribution of photo-z’s to ‘real’ spectroscopic z’s isn’t well calibrated, can lead to catastrophic redshift errors for many probes.

Additionally, need to understand effects of shape distortions in combining galaxy images for accurate weak lensing results.
Simple Coadd
Simple Coadd
Simple Coadd

Introduces shape noise (bad for $wl$), high scatter in photo-z estimate.
Using all data...
Using all data...
Using all data...
Using all data...
Using all data...
Using all data...

$P(\theta)$

Multi-epoch (Fast) ~800
Using all data...

- Multi-epoch (Fast)
- Multi-band (Calibration)

\[ P(\theta) \]

~800
Using all data...

- Multi-epoch (Fast)
  - ~800
- Multi-band (Calibration)
- Multi-object (Deep, Wide)
Complementary Surveys

While LSST will be revolutionary for optical astronomy and precision cosmology, there are many complementary surveys in a variety of bands that help further break degeneracies, calibrate systematics, and allow cross-correlation studies:

- **Radio**: FAST
  - 21 cm HI, Integrated Sachs-Wolfe

- **Microwave**: Planck, SPT
  - CMB priors, cluster CMB lensing, SZ effect

- **Optical (Photometric)**: SDSS, DES
  - Combined catalogs, cross-correlations

- **Optical (Spectroscopic)**: DESI, BOSS
  - Spectroscopic z measurements, Ly-α forest, BAO, RSD

- **X-Ray**: eROSITA, ATHENA
  - Cluster ICM, Cluster Mis-centering

(DES Y1 Abbott et al. 2017)
Clusters in Optical: Weak Lensing

- Can provide the best estimates for cluster masses.
- Requires shear measurements and knowledge of the galaxy redshift distribution.
- This gives the 2D surface mass distribution.
- Additional assumptions required about halo shape to convert to the 3D distribution.
- Typically used to calibrate other observable-mass relations.
Clusters in Optical: Number Density

- We can measure a simple tracer of cluster mass, the richness, or the number of galaxies in the cluster.

- Using a low-scatter proxy, like weak lensing mass, we can convert richness to an estimate on mass.

- Finally, we can arrive at cosmology by fitting the halo mass function.
Clusters in X-ray: Miscentering

- We need to know where the centers of the clusters are to measure their 3D mass distribution.

- Optical cluster finding algorithms choose a center statistically using the Brightest Cluster Galaxy, but this is not always correct.
Clusters in Microwave: SZ Effect

- The **SZ effect** describes how CMB photons get *up-scattered* when passing through energetic gas clouds in clusters.
- LSST will provide **optical counterparts** to the SPT SZ survey and the Planck SZ survey.
- The deep imaging offered by LSST will allow for **calibration of the mass distribution function** through gravitational lensing. This will help calibrate observable mass relations in mm-wave and X-ray maps.
- Comparison with catalogs at different wavebands will also help **improve systematics and modeling** related to cluster detection.
Cross-correlation with CMB maps

The **Integrated Sachs-Wolfe (ISW)** effect describes the process in which CMB photons are gravitationally red-(or blue-)shifted upon entering a gravitational potential, and retain some of the momentum difference upon exiting the potential well due to the change in the slope of the potential caused by the expanding universe.

This effect is the primary cause of temperature fluctuations in the CMB at low multipoles.
Cross-correlation with CMB maps

- Using **stacked galaxy samples** from LSST, cross-correlation of superclusters and voids with maps of the CMB will provide greater insight into the ISW effect.
- LSST will be able to measure ISW to **7σ precision**, greater than current efforts at 4σ correlating SDSS with Planck and WMAP.
- The ISW will be able to be measured up to $z=2$, enabling us to track the **evolution of the effect over cosmic time**.
- LSST will be able to place constraints on the smoothness of the dark energy potential at the 3-5% level on scales of ~1 Gpc.
LSST / Clusters Summary

LSST cosmology constraints will be robust due to wide, deep, fast:

- Survey data will be largely uniform and complete;
- Survey strategy will allow better techniques/calibrations (e.g. photo-z’s);
- Multiple and independent cosmological probes break degeneracies in parameter space;
- LSST will be complemented by a variety of other surveys in many bands
  - FAST, SPT, DES, DESI, eROSITA, and many, many more…

Galaxy clusters are a nice case study of these advantages
Obvious ones...

- LSST in the North
Obvious ones...

- LSST in the North
- LSST in space
Obvious ones...

- LSST in the North
- LSST in space
- LSST with spectra
Obvious ones...

- LSST in the North
- LSST in space
- LSST with spectra
- LSST in space with spectra
Redshift-drift

⇒ Independent cosmological probe!
Measures *dynamics*.

Exercises

1. If the Universe contains only non-relativistic matter and vacuum energy ($\Lambda$) and is spatially flat, calculate the value of the present matter density parameter, $\Omega_{\text{mv}}$, such that the Universe today is just marginally accelerating.

2. If $\Omega_{\text{m}}=0.3$ and $\Omega_{\Lambda}=0.7$, determine the redshift at which the Universe starts to accelerate and the redshift of matter-vacuum energy equality.

3. Suppose $H_0=70$ km/sec/Mpc and is constant in time. For a galaxy at a distance of 100 Mpc, calculate the increase in its recession speed (in km/sec) over a 10-year period. How might you nevertheless measure this “Hubble drift”, which would be a direct measurement of cosmic acceleration?
Redshift-drift is a 1 part in a billion effect

The redshift $z(t_o)$ is related to the scale factor $a(t)$ by

$$1 + z(t_o) = \frac{a(t_o)}{a(t_e)}$$

(1)

where $t_o$ is the time of observation, and $t_e$ the time of emission.

The derivative w.r.t. $t_o$ is

$$\dot{z}(t_o) = \frac{\dot{a}(t_o)}{a(t_o)} \frac{a(t_o)}{a(t_e)} - \frac{a(t_o)}{a^2(t_e)} \frac{da(t_e)}{dt_e} \frac{dt_e}{dt_o}$$

(2)

Since $H = \dot{a}/a$ and $dt_e/dt_o = 1 + z$, we get

$$\dot{z}(t_o) = (1 + z) H_0 - H(z)$$

(3)

The Hubble parameter is

$$H_0 = 100 \, h \, \text{km} \, \text{s}^{-1} \, \text{Mpc}^{-1} = 10^{-10} \, h \, \text{yr}^{-1}$$

(4)

10 years $\Rightarrow$ $\sim$ 1 part in a billion
Redshift-drift is a 1 part in a billion effect

The redshift \( z(t_o) \) is related to the scale factor \( a(t) \) by

\[
1 + z(t_o) = \frac{a(t_o)}{a(t_e)}
\]  

(1)

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\]  

(2)

Since \( H = \dot{a}/a \) and \( dt_e/dt_o = 1 + z \), we get

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\dot{z}(t_o) = (1 + z) H_0 - H(z)
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(3)

The Hubble parameter is

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H_0 = 100 \, h \, \text{km} \, \text{s}^{-1} \, \text{Mpc}^{-1} = 10^{-10} \, h \, \text{yr}^{-1}
\]  

(4)

10 years \( \Rightarrow \) \( \sim \) 1 part in a billion
Is it feasible?

- Exoplanet spectrographs: ~ 30 cm/s  (maybe 2.5 cm/s?)
- Object of choice needs to satisfy criteria (Liske et al. 2008):
  - Trace Hubble flow
  - Sharp spectral features (~30-35 km/s)
  - Large number of spectral features
  - Bright
  - Exist over a large redshift range

Use Lyman-α forest!
Lyman-α forest

1216 Å = 121.6 nm

Diffuse neutral hydrogen outside galaxies absorbs Lyman-α.
Lyman-α forest

~100-500 absorption lines per QSO
Telescope Design

See Wilken et al, doi:10.1038/nature11092
Telescope Design

Number of photons from a QSO detected by a telescope:

\[ N_{\text{photon}} = \epsilon \times N_{\text{QSO-flux}} \times A \times \Delta \lambda \times t \]

Assuming photon-noise limited, the exposure time to achieve 2.5 cm s\(^{-1}\) sensitivity for single absorption line:

\[ t = \frac{N_{\text{photon}}}{\epsilon \times N_{\text{QSO}} \times A \times \Delta \lambda} = \frac{10^{10}}{0.25 \times 5000 \text{ s}^{-1} \text{m}^{-2} \text{um}^{-1} \times \pi \times \left(\frac{D}{2}\right)^2 \times 0.25\text{nm}} \approx 4 \times \frac{10^{10}}{D^2} \text{ s m}^2 \]

E.g. \( D = 40 \text{ m} \), \( t \sim 7000 \text{ h} \); assuming \( \sim 10^2 \) lines, \( t \sim 700 \text{ h} \) (\( \sim 1 \) month).
Telescope Design

Over one decade, having a D~50m telescope that operates ¼ of the time, we will be able to have high resolution spectroscopy for ~50 QSOs.
Cosmological constraints from redshift-drift

Assuming…
… 2.5 cm/s per line
… 100 lines $2 < z < 5$
… over 10 years
… 3 parameters: $\Omega_m$, $\Omega_\Lambda$, $H_0$

Assuming…
… 1000 lines $2 < z < 5$
… 3 parameters: $\Omega_m$, $w_0$, $w_a$, $\Omega_k = 0$

Preliminary Planck + BAO
Conclusion

Redshift-drift is an independent *dynamical* probe of cosmology.

Redshift-drift is hard, but possible to detect!

Redshift-drift can give competitive constraints with a single dedicated 50m telescope observing for two decades.
Useful papers


J. Liske et al, Cosmic dynamics in the era of Extremely Large Telescopes 2014

Using all data...

- Multi-epoch (Fast)
- Multi-band (Calibration)
- Multi-object (Deep, Wide)

$P(\theta)$
Error estimate

Photon noise limited

\[ \sigma_v = 2 \left( \frac{S/N}{2370} \right)^{-1} \left( \frac{N_{\text{QSO}}}{30} \right)^{-1/2} \left( \frac{1 + z_{\text{QSO}}}{5} \right)^{-1.7} \text{ cm s}^{-1} \]

R \geq 30000

\( Z_X \): zero-point in X-band

\( Z_r \): \( 8.88 \times 10^{-10} \text{ s}^{-1} \text{ m}^{-2} \text{ µm}^{-1} \)

\( m_X \): apparent magnitude

\( D, t_{\text{int}}, \epsilon \): telescope diameter, integration time, efficiency

(Eqs(15) and (26) in Liske et al)
Exercise Q3

August 18, 2017

Suppose $H_0 = 70 \text{ km/sec/Mpc}$ and is constant in time. For a galaxy at a distance of 100 Mpc, calculate the increase in its recession speed (in km/sec) over a 10-year period. How might you nevertheless measure this? Hubble drift?, which would be a direct measurement of cosmic acceleration?

\begin{equation}
H = \frac{\dot{a}}{a}
\end{equation}

\begin{equation}
d = ax
\end{equation}

where $d$ is the distance between galaxies and $x$ is the comoving distance, i.e. $\dot{x} = 0$.

Therefore,

\begin{equation}
\dot{d} = \dot{a}x = H d
\end{equation}

The change in recession speed is

\begin{equation}
\ddot{d} = H \dot{d} = H^2 d
\end{equation}

as $H$ is constant in time.

Plug in $d = 100 \text{ Mpc}$ and $H = 70 \text{ km/sec/Mpc}$.

\begin{equation}
\ddot{d} = 490,000 \frac{\text{km}^2}{\text{sec}^2 \text{Mpc}} \\
= \frac{(4.9E5)(3.24078E-20)}{3.17098E-8} \frac{\text{km}}{\text{sec yr}}
\end{equation}

\begin{equation}
= 5.0078 \times 10^{-7} \text{ km/sec/yr}
\end{equation}

So over 10 years, the recession speed increases by $5.0078 \times 10^{-6} \text{ km/sec}$, or 5mm/sec.
Redshift-drift: Sandage-Loeb test

THE CHANGE OF REDSHIFT AND APPARENT LUMINOSITY OF GALAXIES DUE TO THE DECELERATION OF SELECTED EXPANDING UNIVERSES

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(With an Appendix by G. C. McVittie, University of Illinois Observatory, Urbana)
Received February 2, 1962; revised April 13, 1962

ABSTRACT

The redshift and apparent luminosity of any given galaxy are not constant with time for most models of the expanding universe. Redshifts decrease with time because of the braking action of the gravitational field in all exploding models, except for the one where the matter density is zero. Apparent luminosities decrease with time, except for the oscillating model in the contracting phase and for galaxies with very large $\Delta \lambda/\lambda_0$ values, because the distances between galaxies are increasing. Redshifts increase with time for every galaxy in the steady-state model.

The theory and numerical results of the deceleration are presented for four selected world models. For a galaxy with redshift $z = \Delta \lambda/\lambda_0 = 0.4$ at the present epoch, the change of redshift with time is found

“Impossible with current technology”
Redshift-drift: Sandage-Loeb test

DIRECT MEASUREMENT OF COSMOLOGICAL PARAMETERS FROM THE COSMIC DECELERATION
OF EXTRAGALACTIC OBJECTS

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ABSTRACT

The redshift of all cosmological sources drifts by a systematic velocity of order a few meters per second over a century as a result of the deceleration of the universe. The specific functional dependence of the predicted velocity shift on the source redshift can be used to verify its cosmic origin and to measure directly the values of cosmological parameters, such as the density parameters of matter and vacuum, \( \Omega_m \) and \( \Omega_\Lambda \), and the Hubble constant \( H_0 \). For example, an existing spectroscopic technique, which was recently employed in planet searches, is capable of uncovering velocity shifts of this magnitude. The cosmic deceleration signal might be marginally detectable through two observations of \( \sim 10^5 \) quasars set a decade apart, with the HIRES instrument on the Keck 10 m telescope. The signal would appear as a global redshift change in the Ly\( \alpha \) forest templates imprinted on the quasar spectra by the intergalactic medium. The deceleration amplitude should be isotropic across the sky. Contamination of the cosmic signal by peculiar accelerations or local effects is likely to be negligible.

Subject heading: cosmology: theory

Measure for 100 years!