

Role of  $h \rightarrow \eta\eta$  in the search of  
intermediate-mass Higgs boson at the LHC

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hep-ph/0611294 (PRD): with Jeonghyeon Song

## Outline

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- Motivations of the  $h \rightarrow \eta\eta$  decay mode
- Possibility in the NMSSM (this talk)
- Possibility in the simplest little Higgs model (Song's talk)
- Detection at the LHC

## SM Higgs boson searches

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- For  $m_h$  upto about 130 GeV,  $h \rightarrow b\bar{b}$  dominates. But due to QCD background only associated production  $Wh, Zh, t\bar{t}h$  are considered.
- $h \rightarrow \gamma\gamma$  is one of the important channel for the discovery of intermediate Higgs boson.
- For  $m_h \gtrsim 160$  GeV the mode  $h \rightarrow WW^* \rightarrow (l\nu)(l\nu)$  becomes important.
- For even heavier Higgs  $h \rightarrow ZZ \rightarrow (l\bar{l}l\bar{l})$  is the golden mode.

## Current limits on Higgs boson mass

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- Search at LEP I and II:

$$Z \rightarrow f\bar{f}h, \quad e^+e^- \rightarrow Zh \rightarrow (\ell^+\ell^-, b\bar{b}, \nu\bar{\nu}, q\bar{q}) (b\bar{b}, \tau^+\tau^-)$$

Negative results put  $m_h > 114.4$  GeV

- Search at the Tevatron:

$$p\bar{p} \rightarrow W^\pm h \rightarrow (\ell\nu, q\bar{q}) (b\bar{b}, \tau^+\tau^-)$$

Negative results

- One of the scientific programs for the LHC is search for the Higgs boson.

$$h \rightarrow \gamma\gamma, \quad h \rightarrow ZZ \rightarrow \ell^+\ell^-\ell^+\ell^-$$

## Little hierarchy problem in SUSY

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Higgs boson mass  $m_H > 115$  GeV. From the radiative corrections to  $m_H^2$ :

$$m_H^2 \leq m_Z^2 + \frac{3}{4\pi^2} y_t^2 m_t^2 \ln \left( \frac{m_{\tilde{t}}^2}{m_t^2} \right)$$

we require  $m_{\tilde{t}} \gtrsim 1000$  GeV.

RGE effect from  $M_{\text{GUT}}$  to  $M_{\text{weak}}$ :

$$\Delta m_{H_u}^2 \approx -\frac{3}{4\pi^2} y_t^2 m_t^2 \ln \left( \frac{M_{\text{GUT}}}{M_{\text{weak}}} \right) \approx -m_{\tilde{t}}^2$$

We need to obtain

$$O(100^2 \text{ GeV}^2) = (1000 \text{ GeV})^2 - (990 \text{ GeV})^2$$

a fine tuning of  $O(10^{-2})$ .

## Motivations for the $h \rightarrow \eta\eta$ decay mode

- Besides the little hierarchy problem, to some extent, the Higgs bound is contradictory to the EW precision data.
- To evade the LEP2 bound by reducing
  1. the  $h \rightarrow b\bar{b}$  branching ratio, and/or
  2. the  $ZZh$  coupling.
 such that  $e^+e^- \rightarrow Zh \rightarrow Z(b\bar{b})$  is reduced.
- Singlet extensions of the MSSM have additional pseudoscalar bosons that the Higgs can decay into. E.g. NMSSM.
- The simplest little Higgs model also has a pseudoscalar  $\eta$  that the Higgs can decay into, and  $g_{ZZh}$  is substantially reduced.
- MSSM with CP violation in the Higgs sector can allow a large BR for  $h_2 \rightarrow h_1h_1$ .
- This unconventional Higgs decay mode

$$h \rightarrow \eta\eta \quad (\eta = a_1, \eta, h_1)$$

relieves the little Hierarchy problem.

## Effects on the standard search modes

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- The new mode  $h \rightarrow \eta\eta$  for  $m_h$  around 100 – 140 GeV affects significantly  $h \rightarrow \gamma\gamma$  mode and  $h \rightarrow b\bar{b}$  mode.

- So that

$$gg \rightarrow h \rightarrow \gamma\gamma$$

$$q\bar{q}' \rightarrow Wh/Zh \rightarrow (\ell\nu)/(\ell\ell) + b\bar{b}$$

are significantly worsen.

- However, new search modes are stimulated:

$$h \rightarrow \eta\eta \rightarrow (4b, 2b2\tau, 4\tau)$$

- We look at

$$pp \rightarrow Wh/Zh \rightarrow W/Z + \eta\eta \rightarrow (\ell\nu)/(\ell\ell) + 4b$$

# Scenario in NMSSM



## The NMSSM Superpotential

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Superpotential:

$$W = \mathbf{h}_u \hat{Q} \hat{H}_u \hat{U}^c - \mathbf{h}_d \hat{Q} \hat{H}_d \hat{D}^c - \mathbf{h}_e \hat{L} \hat{H}_d \hat{E}^c + \lambda \hat{S} \hat{H}_u \hat{H}_d + \frac{1}{3} \kappa \hat{S}^3.$$

When the scalar field  $S$  develops a VEV  $\langle S \rangle = v_s / \sqrt{2}$ , the  $\mu$  term is generated

$$\mu_{\text{eff}} = \lambda \frac{v_s}{\sqrt{2}}$$

It was motivated by the  $\mu$  problem.

## Higgs Sector

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Higgs fields:

$$H_u = \begin{pmatrix} H_u^+ \\ H_u^0 \end{pmatrix}, \quad H_d = \begin{pmatrix} H_d^0 \\ H_d^- \end{pmatrix}, \quad S.$$

Tree-level Higgs potential:  $V = V_F + V_D + V_{\text{soft}}$ :

$$V_F = |\lambda S|^2 (|H_u|^2 + |H_d|^2) + |\lambda H_u H_d + \kappa S^2|^2$$

$$V_D = \frac{1}{8}(g^2 + g'^2)(|H_d|^2 - |H_u|^2)^2 + \frac{1}{2}g^2 |H_u^\dagger H_d|^2$$

$$V_{\text{soft}} = m_{H_u}^2 |H_u|^2 + m_{H_d}^2 |H_d|^2 + m_S^2 |S|^2 + [\lambda A_\lambda S H_u H_d + \frac{1}{3} \kappa A_\kappa S^3 + \text{h.c.}]$$

Minimization of the Higgs potential links  $M_{H_u}^2$ ,  $M_{H_d}^2$ ,  $M_S^2$  with VEV's of  $H_u$ ,  $H_d$ ,  $S$ .

In the electroweak symmetry, the Higgs fields take on VEV:

$$\langle H_d \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} v_d \\ 0 \end{pmatrix}, \quad \langle H_u \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v_u \end{pmatrix}, \quad \langle S \rangle = \frac{1}{\sqrt{2}} v_s$$

Then the mass terms for the Higgs fields are:

$$\begin{aligned} V &= \begin{pmatrix} H_d^+ & H_u^+ \end{pmatrix} \mathcal{M}_{\text{charged}}^2 \begin{pmatrix} H_d^- \\ H_u^- \end{pmatrix} \\ &+ \frac{1}{2} \begin{pmatrix} \Im m H_d^0 & \Im m H_u^0 & \Im m S \end{pmatrix} \mathcal{M}_{\text{pseudo}}^2 \begin{pmatrix} \Im m H_d^0 \\ \Im m H_u^0 \\ \Im m S \end{pmatrix} \\ &+ \frac{1}{2} \begin{pmatrix} \Re H_d^0 & \Re H_u^0 & \Re S \end{pmatrix} \mathcal{M}_{\text{scalar}}^2 \begin{pmatrix} \Re H_d^0 \\ \Re H_u^0 \\ \Re S \end{pmatrix} \end{aligned}$$

We rotate the charged fields and the scalar fields by the angle  $\beta$  to project out the Goldstone modes. We are left with

$$V_{\text{mass}} = m_{H^\pm}^2 H^+ H^- + \frac{1}{2} (P_1 \ P_2) \mathcal{M}_P^2 \begin{pmatrix} P_1 \\ P_2 \end{pmatrix} + \frac{1}{2} (S_1 \ S_2 \ S_3) \mathcal{M}_S^2 \begin{pmatrix} S_1 \\ S_2 \\ S_3 \end{pmatrix}$$

where

$$\begin{aligned} \mathcal{M}_{P_{11}}^2 &= M_A^2, \\ \mathcal{M}_{P_{12}}^2 &= \mathcal{M}_{P_{21}}^2 = \frac{1}{2} \cot \beta_s \left( M_A^2 \sin 2\beta - 3\lambda\kappa v_s^2 \right), \\ \mathcal{M}_{P_{22}}^2 &= \frac{1}{4} \sin 2\beta \cot^2 \beta_s \left( M_A^2 \sin 2\beta + 3\lambda\kappa v_s^2 \right) - \frac{3}{\sqrt{2}} \kappa A_\kappa v_s, \end{aligned}$$

with

$$M_A^2 = \frac{\lambda v_s}{\sin 2\beta} \left( \sqrt{2} A_\lambda + \kappa v_s \right)$$

The charged Higgs mass:

$$M_{H^\pm}^2 = M_A^2 + M_W^2 - \frac{1}{2} \lambda^2 v^2$$

## Pseudoscalar Higgs bosons

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The pseudoscalar fields,  $P_i$  ( $i = 1, 2$ ), is further rotated to mass basis  $A_1$  and  $A_2$ , through a mixing angle:

$$\begin{pmatrix} A_2 \\ A_1 \end{pmatrix} = \begin{pmatrix} \cos \theta_A & \sin \theta_A \\ -\sin \theta_A & \cos \theta_A \end{pmatrix} \begin{pmatrix} P_1 \\ P_2 \end{pmatrix}$$

with

$$\tan \theta_A = \frac{\mathcal{M}_{P_{12}}^2}{\mathcal{M}_{P_{11}}^2 - m_{A_1}^2} = \frac{1}{2} \cot \beta_s \frac{M_A^2 \sin 2\beta - 3\lambda \kappa v_s^2}{M_A^2 - m_{A_1}^2}$$

In large  $\tan \beta$  and large  $M_A$ , the tree-level pseudoscalar masses become

$$\begin{aligned} m_{A_2}^2 &\approx M_A^2 \left(1 + \frac{1}{4} \cot^2 \beta_s \sin^2 2\beta\right), \\ m_{A_1}^2 &\approx -\frac{3}{\sqrt{2}} \kappa v_s A_\kappa \end{aligned}$$

$$\text{Small } 2m_{A_1} < m_{h_1}$$

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A very light  $m_{A_1}$  is possible if

$$\kappa \rightarrow 0 \quad \text{and/or} \quad A_\kappa \rightarrow 0$$

while keeping  $v_s$  large enough. It is made possible by a PQ-type symmetry.

## Parameters of NMSSM: NMHDECAY

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Additional parameters other than the usual MSSM's

$$\lambda, \kappa, A_\lambda, A_\kappa, \mu_{\text{eff}}$$

Constraints inside the NMHDECAY (Ellwanger, Gunion, Hugonie):

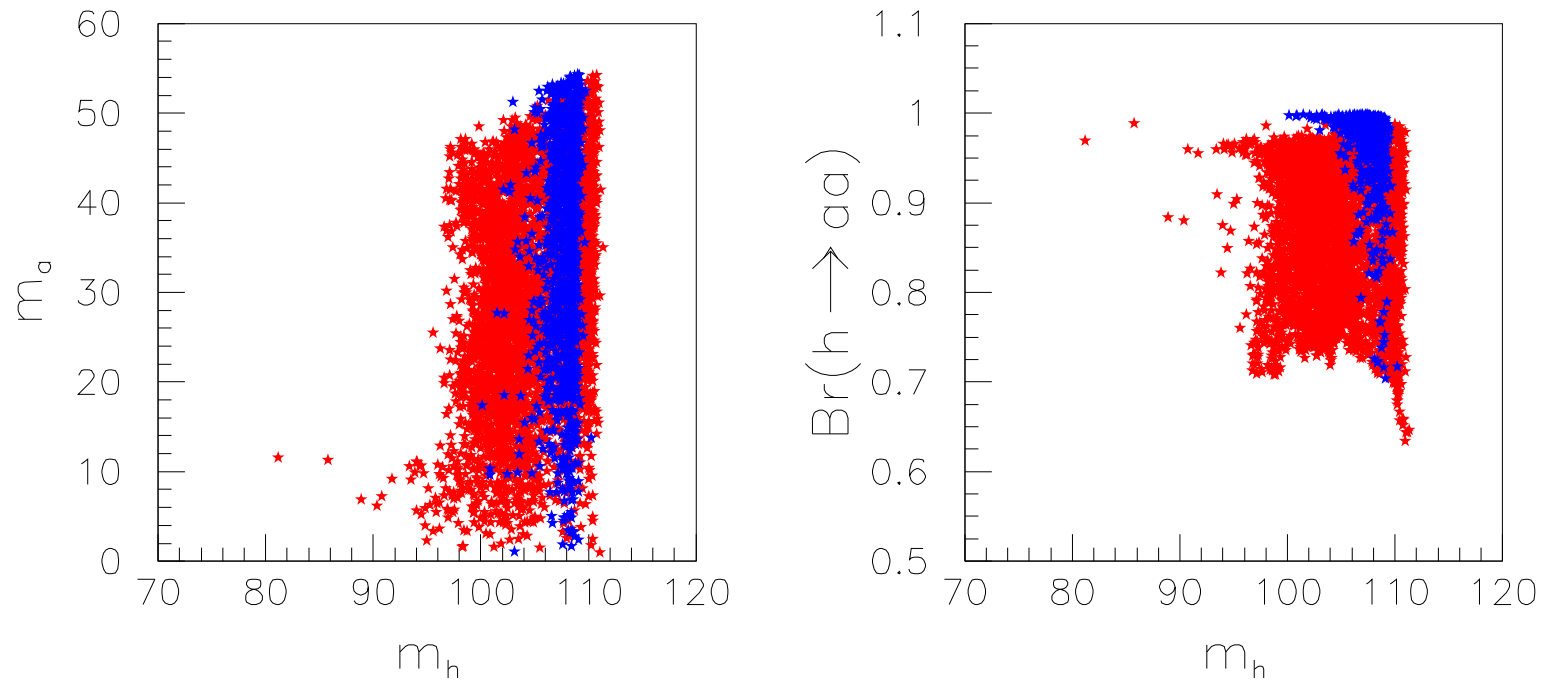
- One-loop radiative corrections to Higgs potential
- $b \rightarrow s\gamma$  constraint
- Dark matter relic density constraint: [0.095, 0.112]
- LEP2 bounds

## Two bench-mark points in NMSSM

NMSSM (A)	NMSSM (B)
$\lambda = 0.18, \kappa = -0.43$	$\lambda = 0.26, \kappa = 0.51$
$\tan \beta = 29$	$\tan \beta = 23$
$A_\lambda = -437 \text{ GeV}$	$A_\lambda = -222 \text{ GeV}$
$A_\kappa = -4 \text{ GeV}$	$A_\kappa = -13 \text{ GeV}$
$\mu_{\text{eff}} = -143 \text{ GeV}$	$\mu_{\text{eff}} = 144 \text{ GeV}$
$m_{h_1} = 110 \text{ GeV}$	$m_{h_1} = 109 \text{ GeV}$
$m_{a_1} = 30 \text{ GeV}$	$m_{a_1} = 39 \text{ GeV}$
$B(h_1 \rightarrow a_1 a_1) = 0.92$	$B(h_1 \rightarrow a_1 a_1) = 0.99$
$B(a_1 \rightarrow b\bar{b}) = 0.93$	$B(a_1 \rightarrow b\bar{b}) = 0.92$
$g_{VVh_1}/g_{VVh}^{\text{SM}} = 0.99$	$g_{VVh_1}/g_{VVh}^{\text{SM}} = -0.99$
$g_{tth_1}/g_{tth}^{\text{SM}} = 0.99$	$g_{tth_1}/g_{tth}^{\text{SM}} = -0.99$
$g_{tta_1}/g_{tth}^{\text{SM}} = -2.4 \times 10^{-3}$	$g_{tta_1}/g_{tth}^{\text{SM}} = -1.2 \times 10^{-2}$
$C_{4b}^2 = 0.80$	$C_{4b}^2 = 0.83$

$$C_{4b}^2 \equiv \left( \frac{g_{ZZh}}{g_{ZZh}^{\text{SM}}} \right)^2 \times B(h \rightarrow a_1 a_1) \times B^2(a_1 \rightarrow b\bar{b})$$





★: bench-mark point A-like

★: bench-mark point B-like

All evade the Higgs mass bound

## Further decay in $h \rightarrow a_1 a_1$

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Further decay of  $a_1$  includes

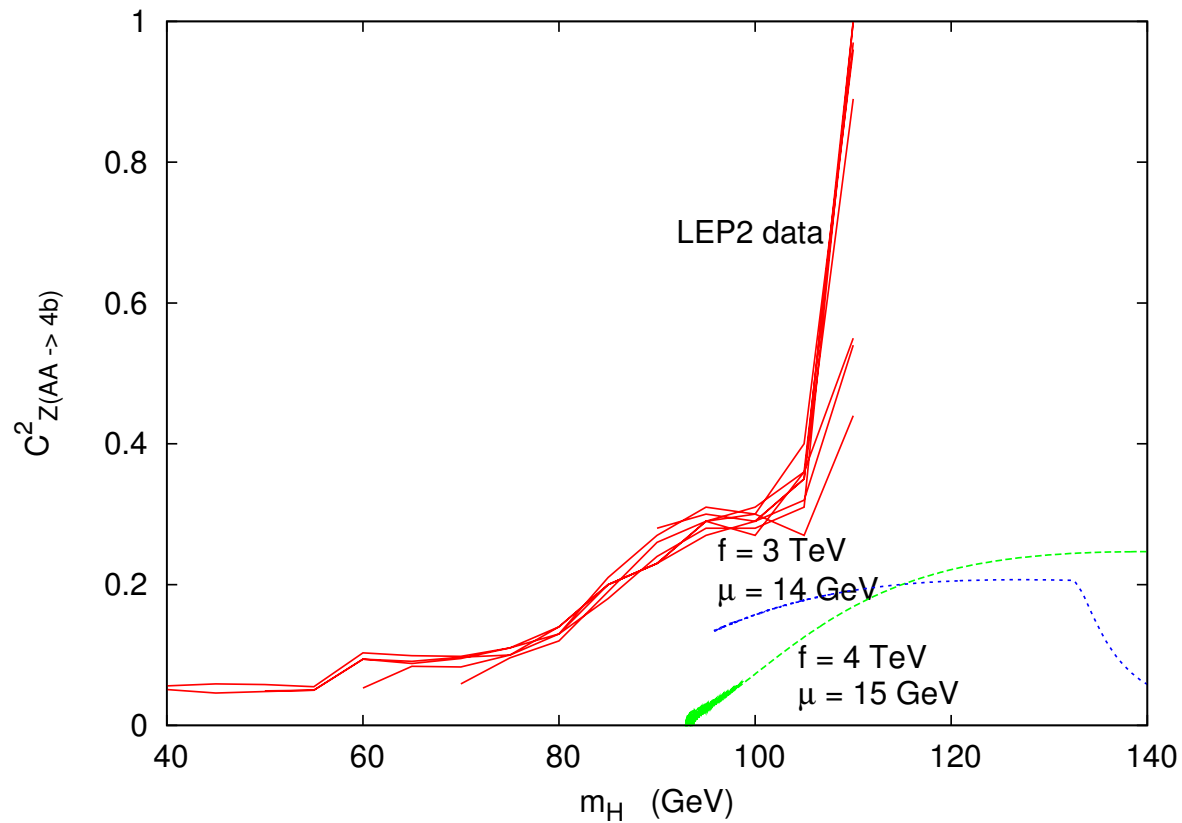
$$h \rightarrow a_1 a_1 \rightarrow (2\gamma, 2\tau, 2b, 2g) (2\gamma, 2\tau, 2b, 2g)$$

- If  $a_1$  is very light and so energetic that **the two photons are very collimated. It may be difficult to resolve them.** Effectively, like  $h \rightarrow \gamma\gamma$ .
- If the mixing angle is larger than  $10^{-3}$  and  $a_1$  is heavier than a few GeV, it can decay into  $\tau^+\tau^-$ . Thus, **4 $\tau$ s in the final state** (Graham, Pierce, Wacker 2006).
- If  $a_1$  is heavier than  $2m_b$ ,  $a_1$  will dominately decay into  **$b\bar{b}$** .
- The gluon mode suffers from QCD background.

Scenario in Little Higgs  
(see Song's talk)

Two bench-mark points of the SLH $\mu$  model

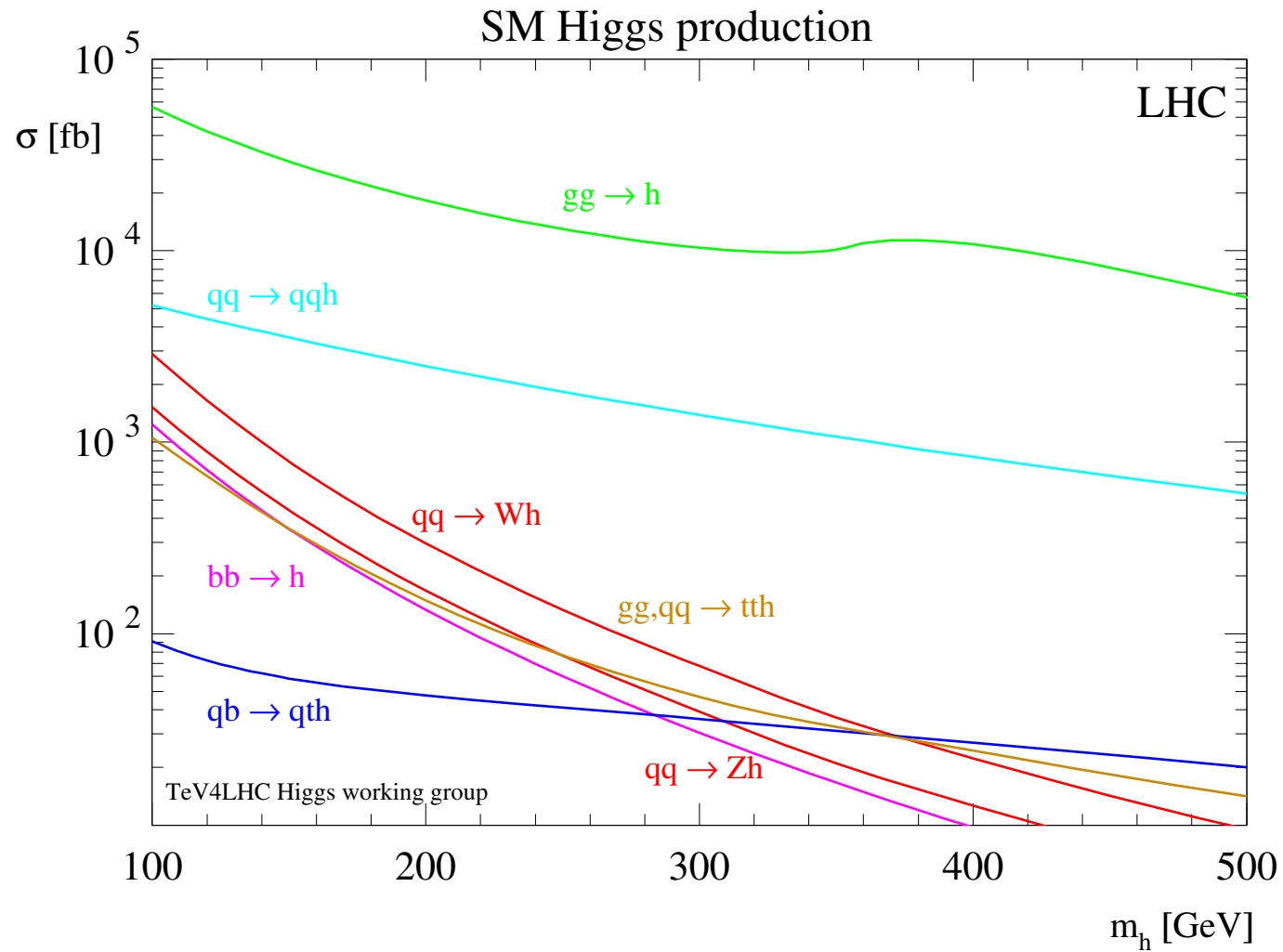
SLH $\mu$ (A)	SLH $\mu$ (B)
$f = 4 \text{ TeV}$	$f = 2 \text{ TeV}$
$\mu = 20 \text{ GeV}$	$\mu = 20 \text{ GeV}$
$x_\lambda = 5.86$	$x_\lambda = 10$
$\tan \beta = 17$	$\tan \beta = 9.47$
$m_h = 146.2 \text{ GeV}$	$m_h = 135.2 \text{ GeV}$
$m_\eta = 68.6 \text{ GeV}$	$m_\eta = 47.9 \text{ GeV}$
$B(h \rightarrow \eta\eta) = 0.65$	$B(h \rightarrow \eta\eta) = 0.75$
$B(\eta \rightarrow b\bar{b}) = 0.85$	$B(\eta \rightarrow b\bar{b}) = 0.86$
$g_{VVh}/g_{VVh}^{\text{SM}} = 0.57$	$g_{VVh}/g_{VVh}^{\text{SM}} = 0.44$
$g_{tth}/g_{tth}^{\text{SM}} = 0.79$	$g_{tth}/g_{tth}^{\text{SM}} = 0.93$
$g_{tt\eta}/g_{tt\eta}^{\text{SM}} = -0.89$	$g_{tt\eta}/g_{tt\eta}^{\text{SM}} = -1.38$
$C_{4b}^2 = 0.16$	$C_{4b}^2 = 0.11$



LEP data (2006) for  $15 \text{ GeV} < m_a < 55 \text{ GeV}$

$$C^2_{Z(AA \rightarrow 4b)} = \left( \frac{g_{ZZH}}{g_{ZZH}^{\text{SM}}} \right)^2 \times B(H \rightarrow AA) \times B(A \rightarrow b\bar{b})^2.$$

# Detection at the LHC



(hep-ph/0612172)

## Higgs Production at the LHC

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- Gluon fusion  $gg \rightarrow h \rightarrow \eta\eta \rightarrow 4b$  suffers from huge QCD background.
- $WW$  fusion  $qq \rightarrow qqWW \rightarrow qqh \rightarrow qq(4b)$  also suffers from QCD background.
- $Wh, Zh$  associated production:

$$Wh \rightarrow (\ell\nu) + (4b), \quad Zh \rightarrow (\ell\ell) + (4b)$$

The charged lepton removes most QCD background.

- $t\bar{t}h \rightarrow (bW)(bW) + (4b)$ , combinatorial background.

Require **at least one charged lepton and 4  $b$ -tagged jets** in the final state.



## Production and decay

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- We used MADGRAPH with the effective vertex  $g_{vvh}$  to calculate the signal cross sections. Decay of the  $W/Z$  and  $h$ :

$$p_T(\ell) > 15 \text{ GeV}, \quad |\eta(\ell)| < 2.5,$$

$$p_T(b) > 15 \text{ GeV}, \quad |\eta(b)| < 2.5, \quad \Delta R(bb, b\ell) > 0.4,$$

- We employ a  $B$ -tagging efficiency of 70% for each  $B$  tag, and a probability of 5% for a light-quark jet faking a  $B$  tag.

The mis-tag probability for a  $u$ -jet is 1%, a charm-jet is 12 – 14%.

Taking into account the fact that a jet coming from  $W$  decay is much less frequently a charm-jet, the average of 5% is reasonable.

## Backgrounds

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- It is possible for the photon in  $\gamma + nj$  background to fake an electron in the EM calorimeter.
- The backgrounds from  $W + nj$  and  $Z + nj$  contribute at a very low level and are reducible as we require 4  $b$ -tagged jets in the final state.
- The background from  $WZ \rightarrow \ell\nu b\bar{b}$  is also reducible by the 4  $b$ -tagging requirement.
- $t\bar{t}$  production with one of the top decay hadronically and the other semi-leptonically. The jet from the  $W$  may fake a  $b$  jet.
- $t\bar{t}b\bar{b}$  production, irreducible.
- $W/Z + 4b$  production, irreducible.

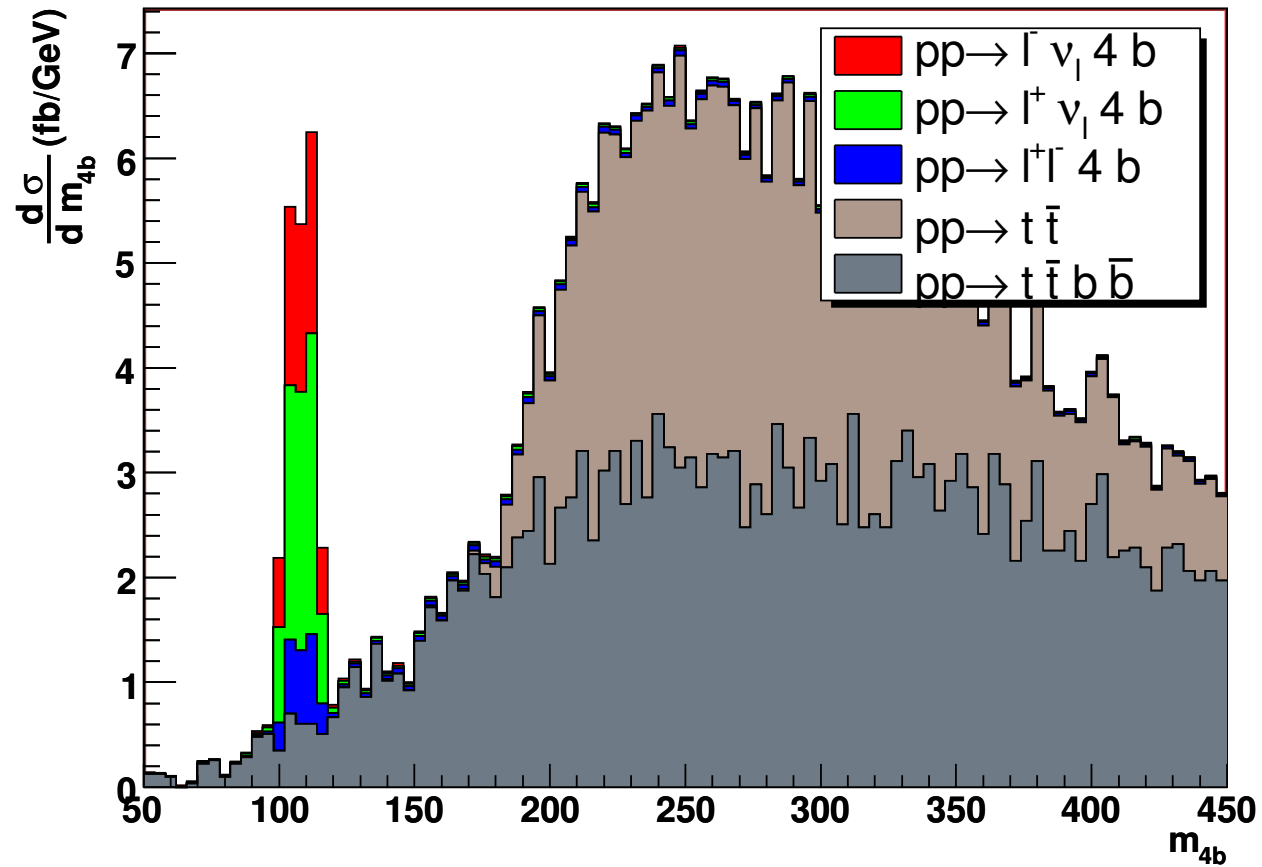
## Event rates

Channels	NMSSM (A)	NMSSM (B)	SLH $\mu$ (A)	SLH $\mu$ (B)
$W^+ h$ signal	3.13 fb	9.54 fb	1.27 fb	0.63 fb
$W^- h$ signal	2.35 fb	6.55 fb	0.87 fb	0.44 fb
$Zh$ signal	1.05 fb	2.76 fb	0.36 fb	0.18 fb

## Background

Channels	cross sections (fb)
$t\bar{t}$	172 (NMSSM & SLH $\mu$ )
$t\bar{t}b\bar{b}$	236 (NMSSM), 284 (SLH $\mu$ A), 429 (SLH $\mu$ B)
$W + 4b$	3.80 (NMSSM), 4.16 (SLH $\mu$ A), 4.63 (SLH $\mu$ B)
$Z + 4b$	3.85 (NMSSM & SLH $\mu$ )

$t\bar{t}b\bar{b}$  background is enhanced by  $t\bar{t}\eta$  production in SLH model.



Apply the invariant mass cuts:

$$m_h - 15 \text{ GeV} < M_{4b} < m_h + 15 \text{ GeV} ,$$

## Significance of the signal

Total signal and background cross sections under the signal peak:

	NMSSM (A)	NMSSM (B)	SLH $\mu$ (A)	SLH $\mu$ (B)
signal	6.53 fb	18.85 fb	2.50 fb	1.25 fb
bkgd	4.83 fb	4.77 fb	13.83 fb	22.45 fb
$S/\sqrt{B}$	29.7	86.3	6.7	2.6

$S/\sqrt{B}$  for  $L = 100 \text{ fb}^{-1}$

## Conclusions

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- In order to evade the Higgs mass bound,  $B(h \rightarrow b\bar{b})$  is substantially reduced, which can be done by additional mode,  $h \rightarrow \eta\eta$ .
- $h \rightarrow \eta\eta$  stimulates other search modes for the Higgs boson.
- We showed that  $Wh, Zh \rightarrow \ell + 4b$  is feasible at the LHC with  $4b$ -tagging.
- The  $4b$  invariant mass spectrum distinguishes the signal from  $t\bar{t}$ ,  $t\bar{t}b\bar{b}$ ,  $W/Z + 4b$  backgrounds.
- One can also reconstruct the mass bump of  $\eta$ 's.