

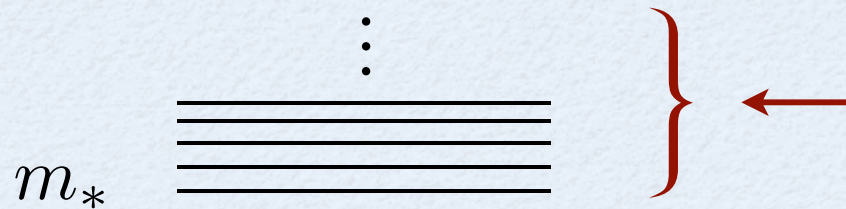
WARPED/COMPOSITE PHENOMENOLOGY SIMPLIFIED

Roberto Contino

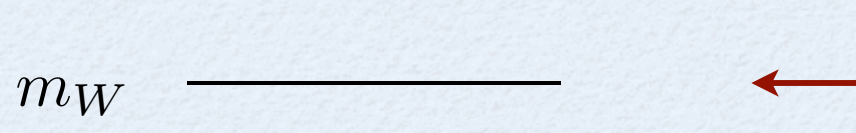
CERN - TH

R.C. , T. Kramer, M. Son, R. Sundrum, *JHEP* 0705:074 (2007)

THE CASE FOR A COMPOSITE HIGGS

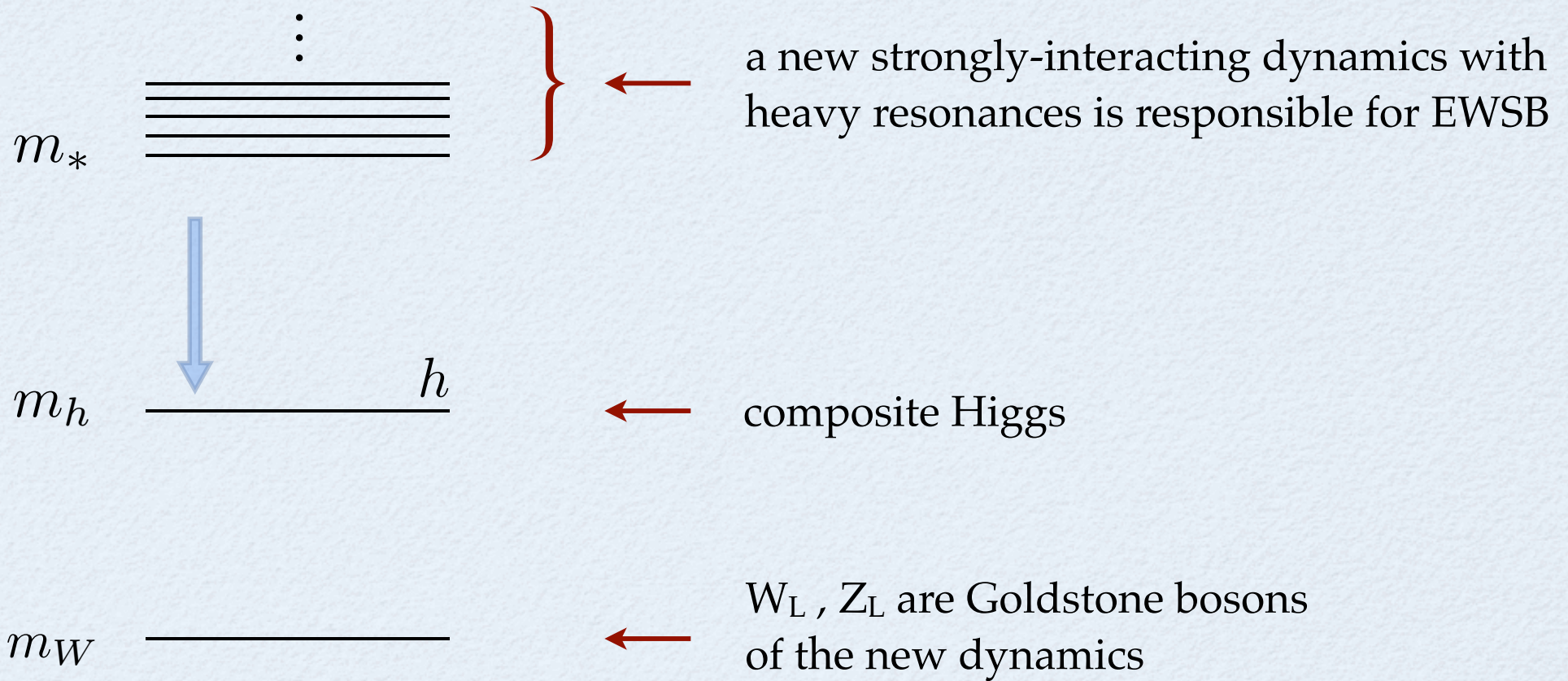


a new strongly-interacting dynamics with heavy resonances is responsible for EWSB



W_L, Z_L are Goldstone bosons of the new dynamics

THE CASE FOR A COMPOSITE HIGGS



 Can the composite Higgs be naturally light ?

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 yes, if it is a (pseudo) Goldstone boson [Georgi & Kaplan, '80s]

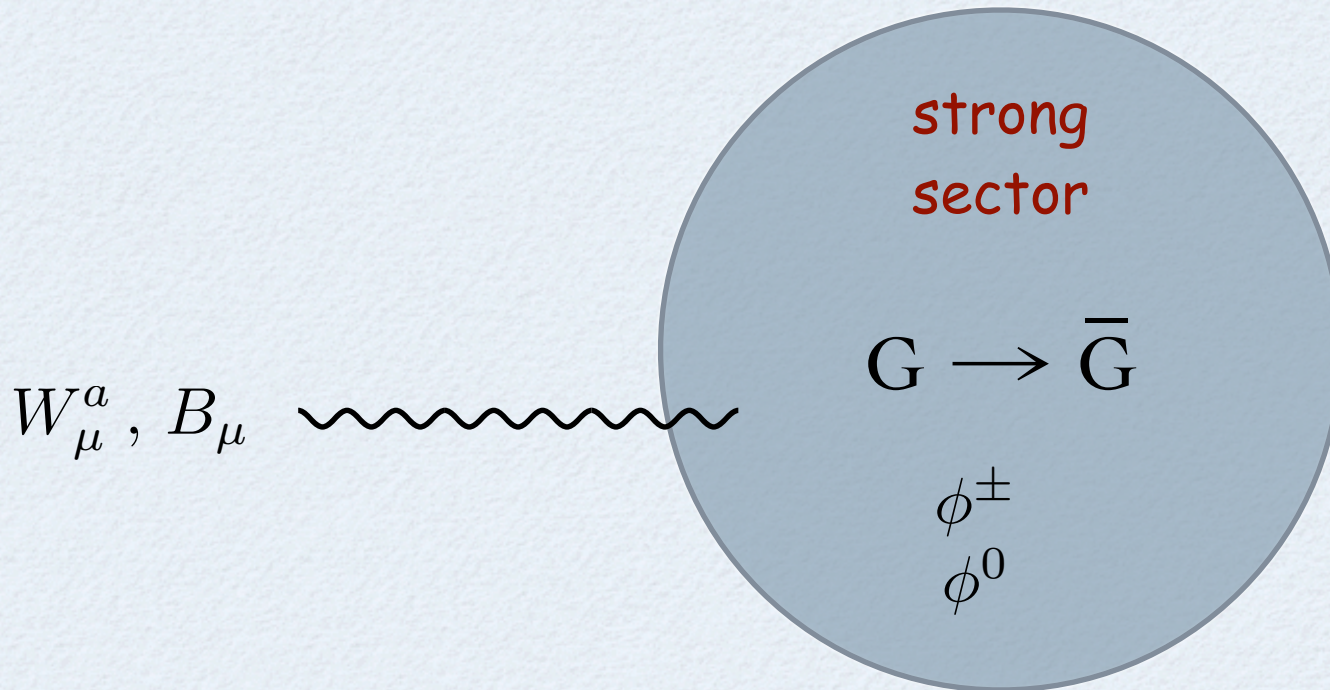


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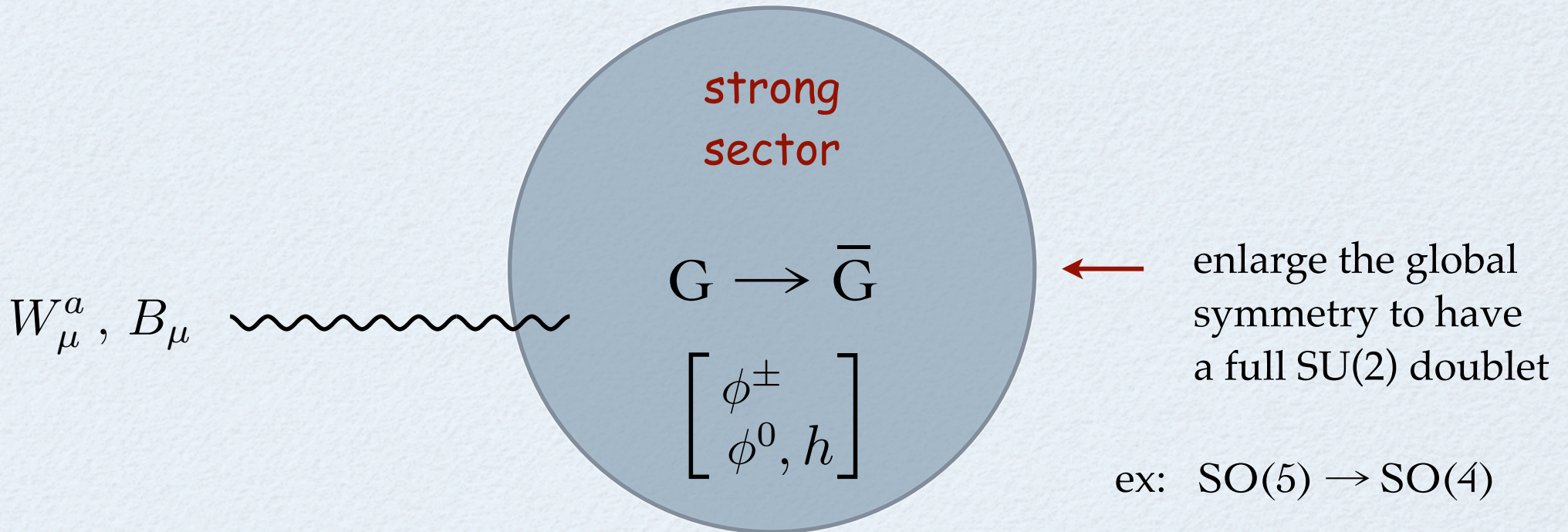
[Georgi & Kaplan, '80s]



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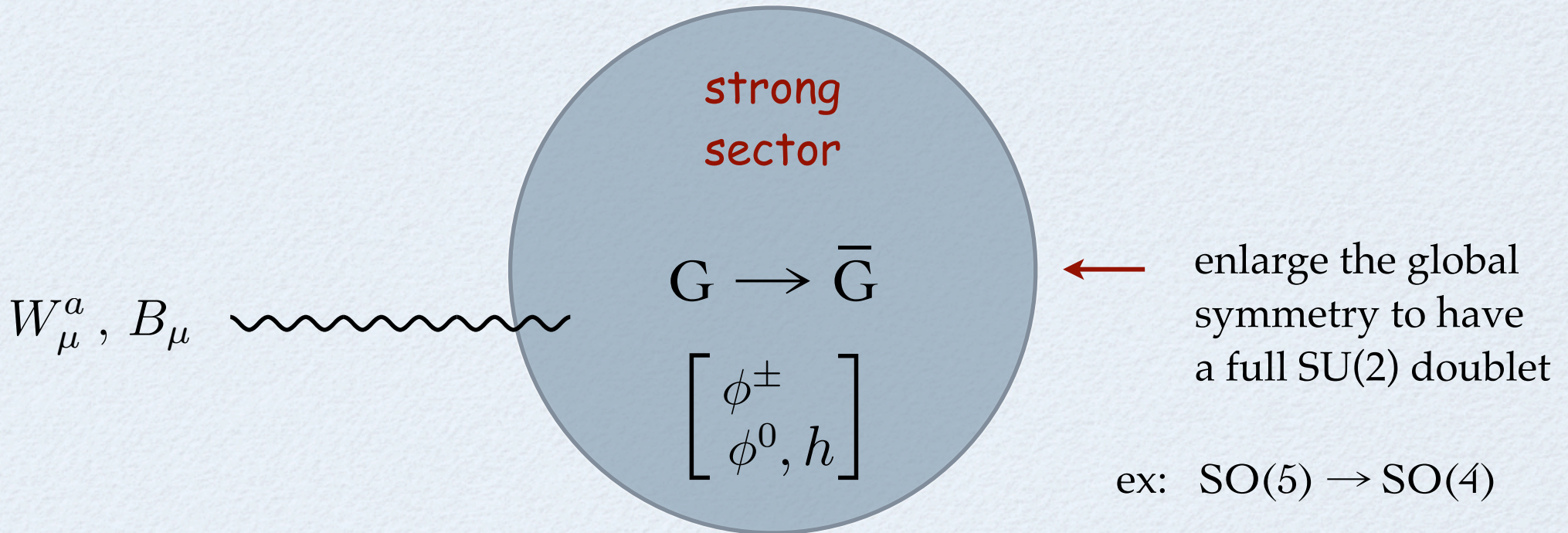
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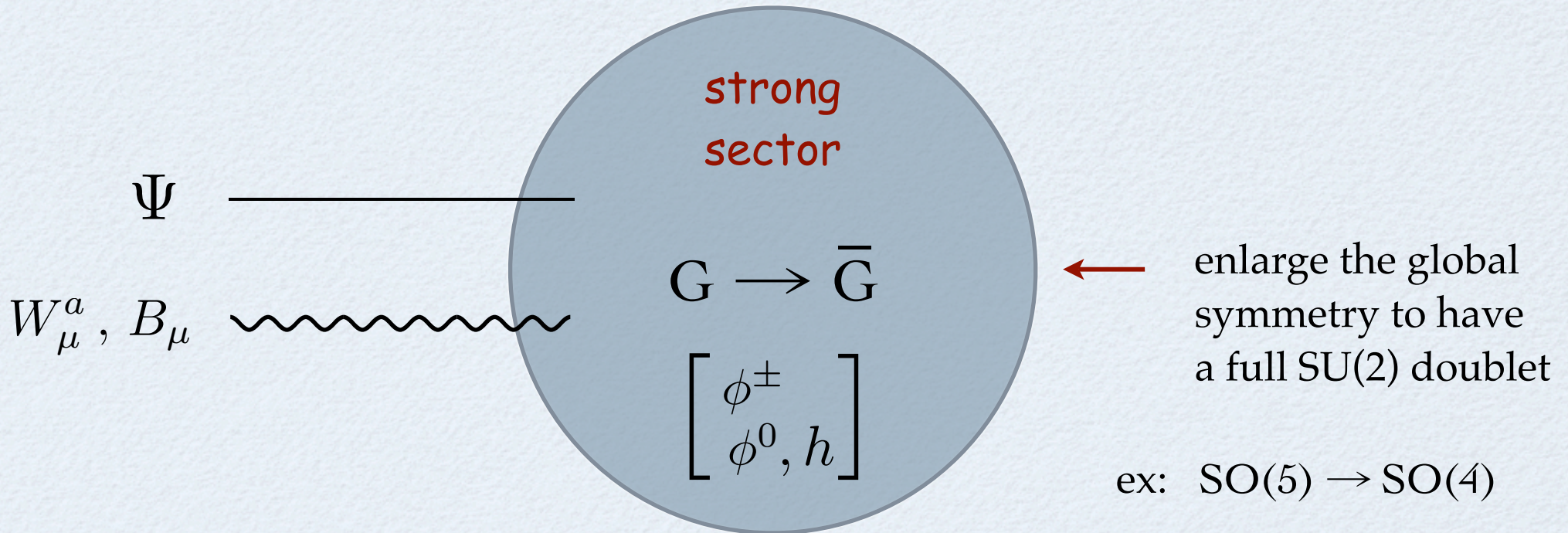
the explicit breaking of the global symmetry by a weak interaction leads to a light Higgs

$$m_h^2 \sim \frac{\lambda^2}{16\pi^2} m_*^2$$

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A new fundamental parameter:

being a Goldstone, the composite Higgs behaves like an “angle” :

$$V(h) = F_\pi^2 m_*^2 \frac{\lambda^2}{16\pi^2} g(h/F_\pi)$$

F_π = scale at which $G \rightarrow \bar{G}$

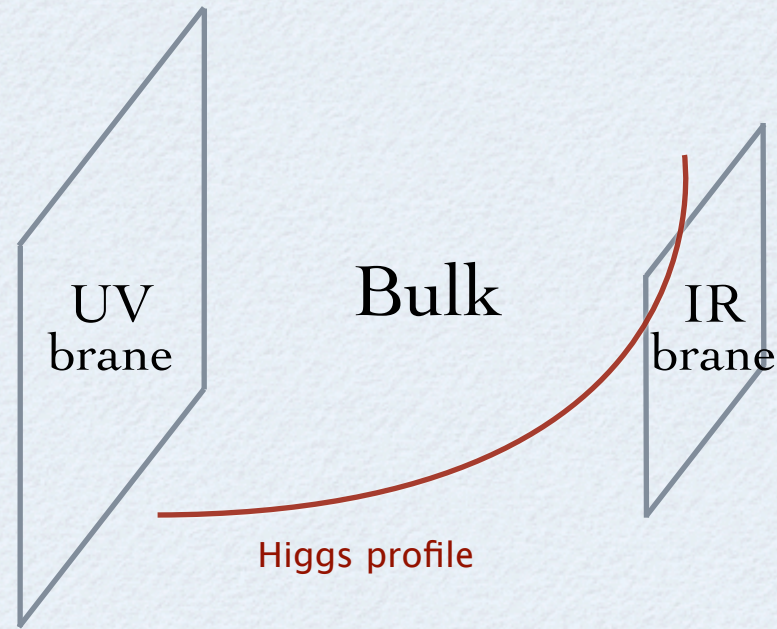
$g(x)$ = periodic function

new parameter:

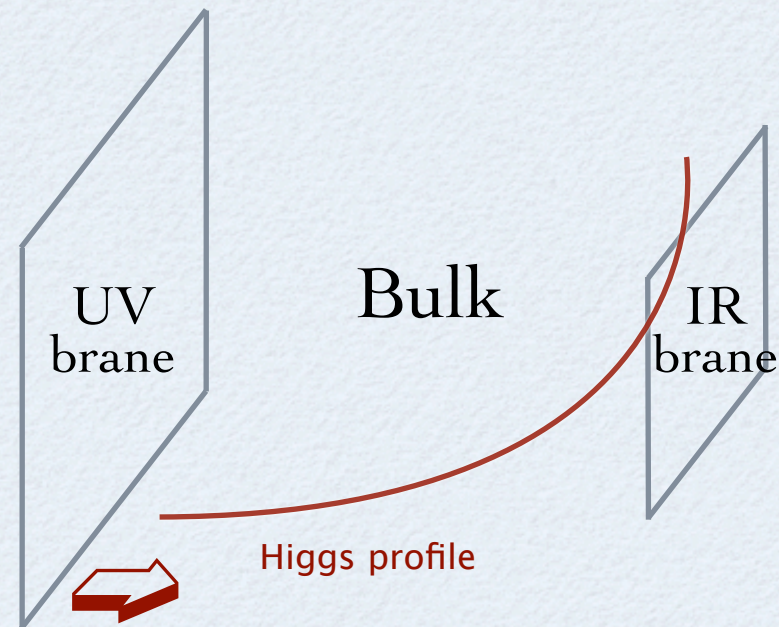
$$\epsilon = \frac{v}{F_\pi}$$

$$0 \leq \epsilon \leq 1$$

Composite Higgs from an extra warped dimension



Composite Higgs from an extra warped dimension



the Higgs structure along the extra dimension
appears like a form factor
for an observer on the UV brane



... ok, suppose we discover the Higgs:
how can we tell it is composite ?



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①

Measuring its couplings

shifts expected at $\mathcal{O}(\epsilon^2)$



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②

Probing its strong interaction
in the WW scattering

the composite Higgs alone fails to fully
unitarize WW scattering at high energy

$$\mathcal{A}(s, t) = \frac{s}{v^2} \epsilon^2 - \frac{s m_h^2}{s - m_h^2} (1 - \epsilon^2) + (s \leftrightarrow t)$$

see: Giudice, Grojean, Pomarol, Rattazzi, JHEP 0706:045 (2007)

These signals would give **direct evidence**
for the Higgs compositeness

- theoretically clean
- experimentally challenging

required: full control of the detector and of background
large integrated luminosity

Indirect evidence can come from the production of the new resonances of the strong sector

- experimentally easier
- more model dependent

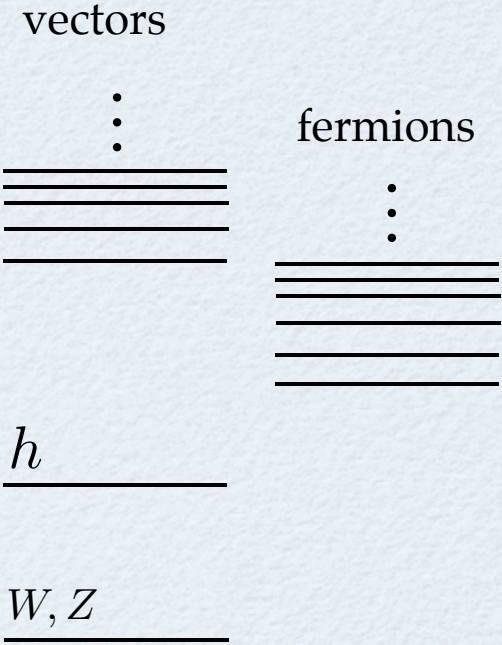
Partners of the top
(resonances that cut off the loop of the top)

✓ Naturalness requires these new states to be light(er)

ex: $m_h = 200 \text{ GeV}$
 and NO tuning $\longrightarrow m_* \sim 700 \text{ GeV}$

✓ These states are colored fermions (no SUSY)

expected to be strongly coupled to t, b, W_L, Z_L



Need a low-energy effective description
of the lowest-lying resonances
to study their phenomenology

we focus on the class of models with

✦ no T-parity

✦ linear couplings between composite
and elementary sector

✓ Flavor

✓ Fermion masses

this includes extra-dimensional warped
(Randall-Sundrum) theories

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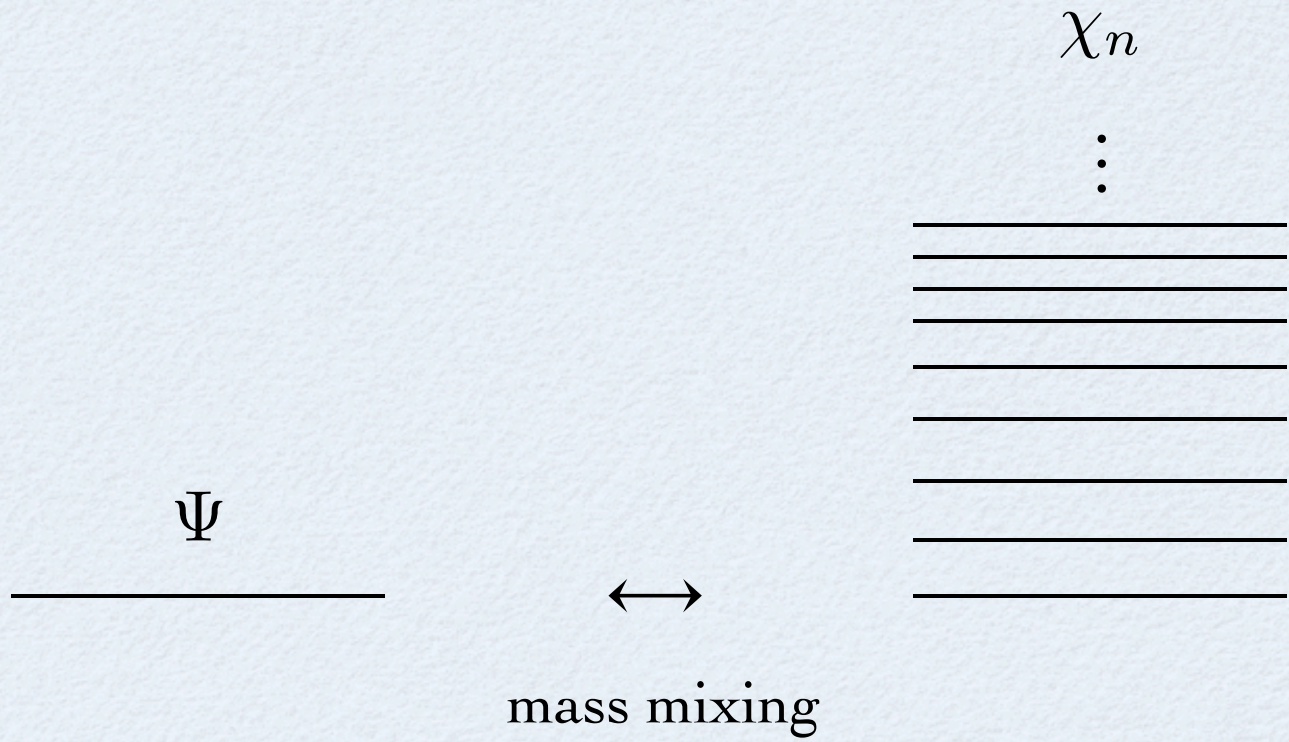
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effective description of the
lowest-lying resonances
given by a

Two-site
model

RULES

- Elementary sector: $\{SM - Higgs\}$
inter-elementary coupling: $g_{el} \sim 1$
- Composite sector: $\{\rho, \chi + Higgs\}$
[\supset excited massive copy of the SM]
inter-composite coupling: $4\pi \gg g_* \gg 1$
- Mixing: only mass mixings allowed
- Higgs: H couples only to ρ and χ

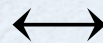


$$\mathcal{L}_{mix} = \sum_n \Delta_n \bar{\Psi} \chi_n + h.c.$$

elementary



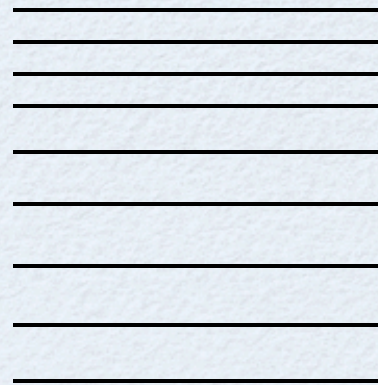
Ψ



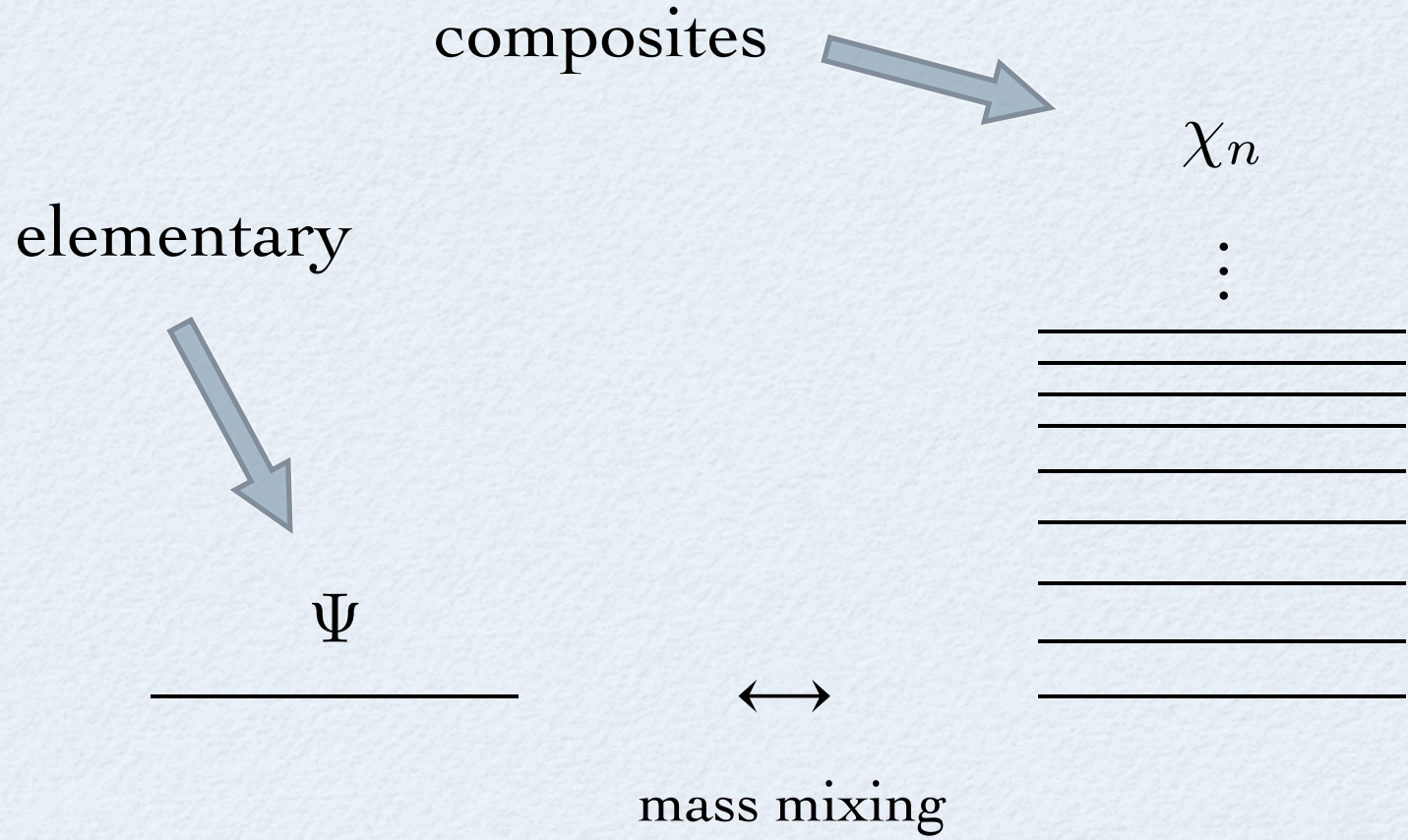
mass mixing

χ_n

\vdots

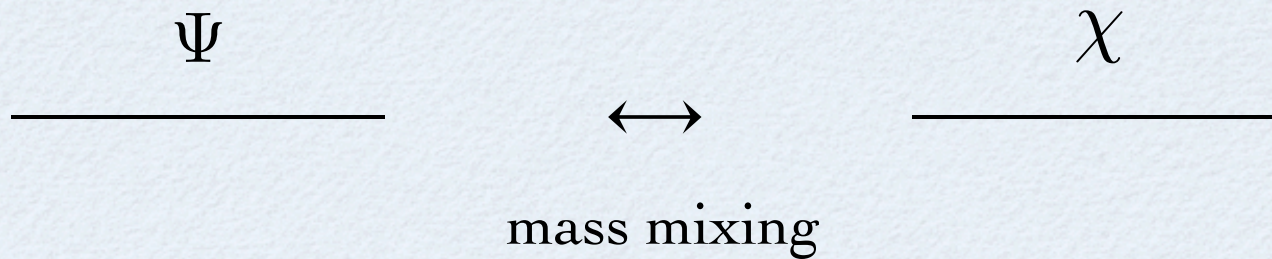


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☞ Keep only the first resonance of each tower



$$\mathcal{L}_{mix} = \Delta \bar{\Psi} \chi + h.c.$$

example:



A simple Two-Site $SO(5)/SO(4)$ model

$$SO(5) \times U(1)_X \rightarrow SO(4) \times U(1)_X$$

$$\Sigma_0 = (0, 0, 0, 0, 1)$$

$$SO(4) \sim SU(2)_L \times SU(2)_R$$

$$Y = T_{3R} + X$$

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$$\Sigma = \Sigma_0 e^{T^{\hat{a}} h^{\hat{a}} / F_\pi}$$

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1 Heavy composite
fermion multiplet

$$\chi = \begin{bmatrix} (Q') \\ Q \\ \tilde{T} \end{bmatrix}$$

$\mathbf{5}_{2/3}$ of $\text{SO}(5) \times \text{U}(1)_X$

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composite sector

$$\chi = \begin{bmatrix} (Q') \\ Q \\ \tilde{T} \end{bmatrix}$$

$$[\mathbf{5} = (\mathbf{2}, \mathbf{2}) \oplus (\mathbf{1}, \mathbf{1})]$$

$$Q = \begin{bmatrix} T \\ B \end{bmatrix}$$

$$Q' = \begin{bmatrix} T_{5/3} \\ T_{2/3} \end{bmatrix}$$

$$Y[Q] = 1/6$$

$$Y[Q'] = 7/6$$

$$\begin{aligned}
\mathcal{L} = & \bar{\chi} (i\partial - m) \chi - m_{\Sigma} \bar{\chi}_i \Sigma_i \Sigma_j \chi_j \\
& + \bar{q}_L i\partial q_L + \bar{t}_R i\partial t_R \\
& + \Delta_q \bar{q}_L Q_R + \Delta_{t_R} \bar{t}_R \tilde{T}_L + h.c.
\end{aligned}$$

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source of explicit
SO(5) breaking

$$\longrightarrow \left[\begin{array}{l} + \bar{q}_L i\partial q_L + \bar{t}_R i\partial t_R \\ + \Delta_q \bar{q}_L Q_R + \Delta_{t_R} \bar{t}_R \tilde{T}_L + h.c. \end{array} \right.$$

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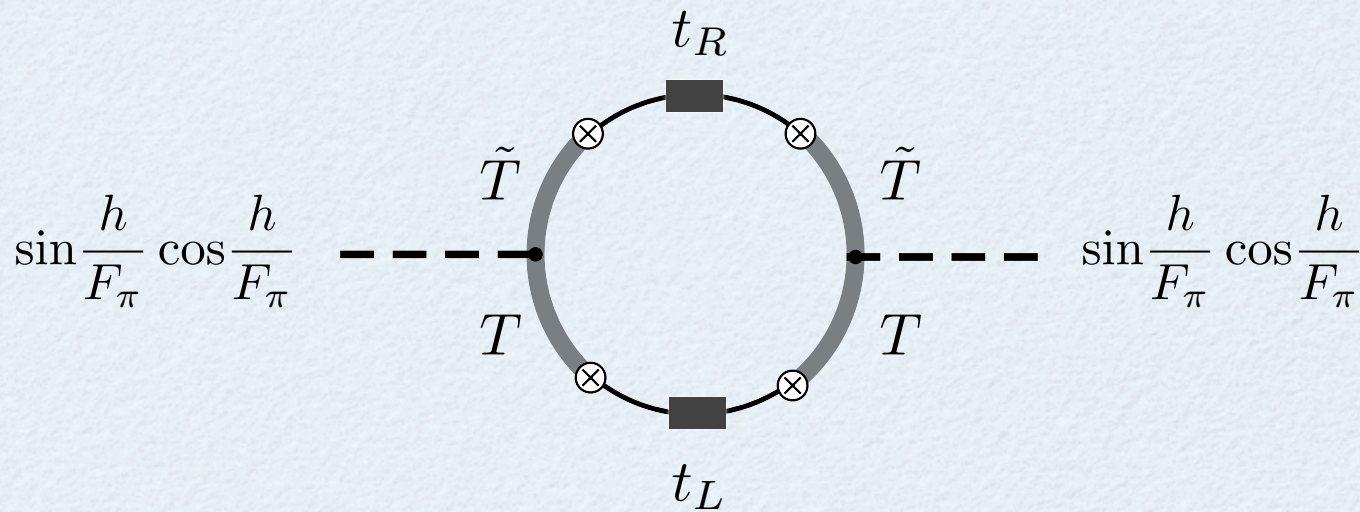
$$\begin{aligned} \mathcal{L} = & + \bar{Q} \left(i\partial - m - m_\Sigma \frac{s^2}{2} \hat{H} \hat{H}^\dagger \right) Q + \bar{Q}' \left(i\partial - m - m_\Sigma \frac{s^2}{2} \hat{H}^c \hat{H}^{c\dagger} \right) Q' \\ & + \tilde{T} (i\partial - \tilde{m} + m_\Sigma s^2) \tilde{T} - m_\Sigma \frac{s^2}{2} \bar{Q}' \hat{H} \hat{H}^{c\dagger} Q + h.c. \\ & - m_\Sigma \frac{sc}{\sqrt{2}} \left(\bar{Q} \hat{H}^c \tilde{T} + \bar{Q}' \hat{H} \tilde{T} + h.c. \right) \\ & + \bar{q}_L i\partial q_L + \bar{t}_R i\partial t_R + \Delta_q \bar{q}_L Q_R + \Delta_{t_R} \bar{t}_R \tilde{T}_L + h.c. \end{aligned}$$

$$s \equiv \sin \frac{h}{F_\pi}, \quad c \equiv \cos \frac{h}{F_\pi}$$

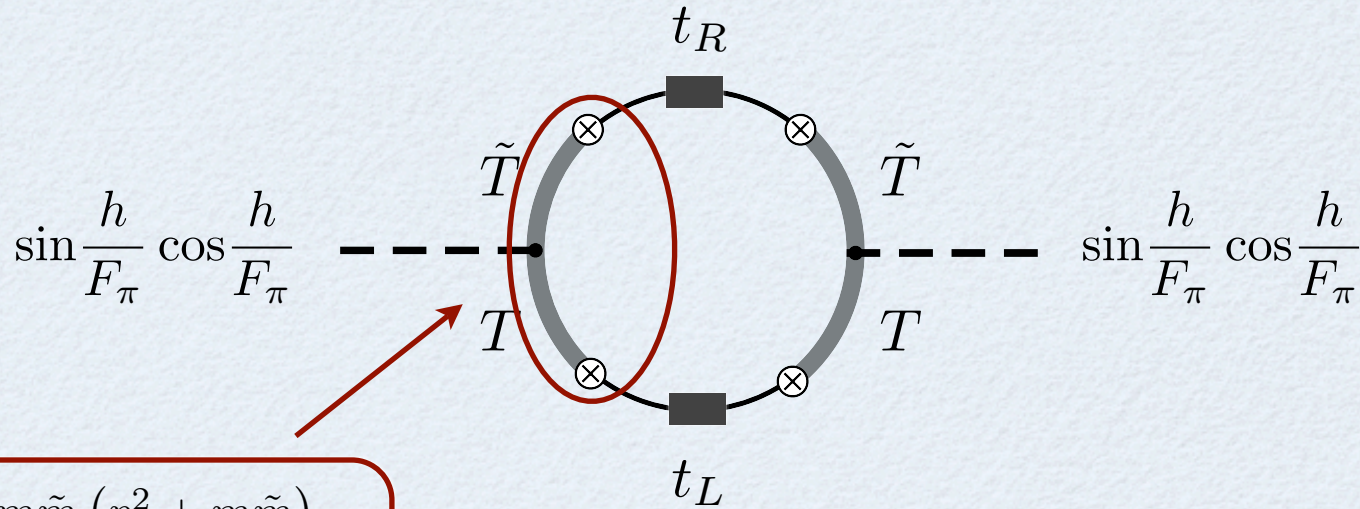
$$\hat{H} \equiv \frac{1}{h} H = \frac{1}{h} \begin{bmatrix} h^1 - ih^2 \\ h^3 - ih^4 \end{bmatrix} \quad h = \sqrt{h^{\hat{a}} h^{\hat{a}}}$$

$$\tilde{m} = m + m_\Sigma$$

Higgs potential

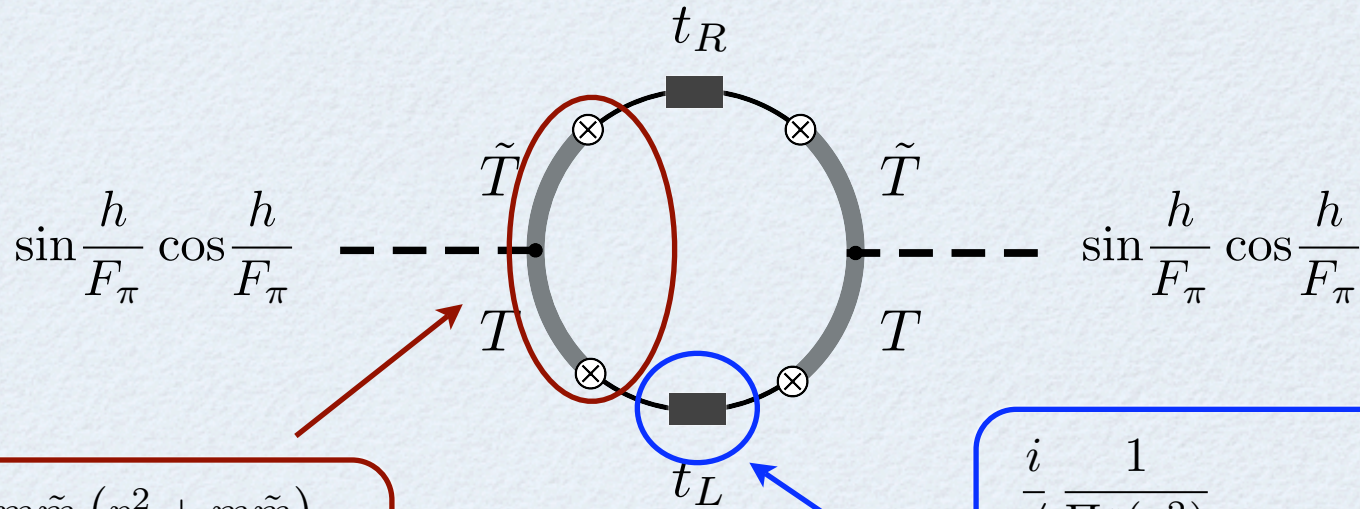


Higgs potential



$$F(p^2) = y_t \frac{m\tilde{m} (p^2 + m\tilde{m})}{(p^2 - m^2)(p^2 - \tilde{m}^2)}$$

Higgs potential

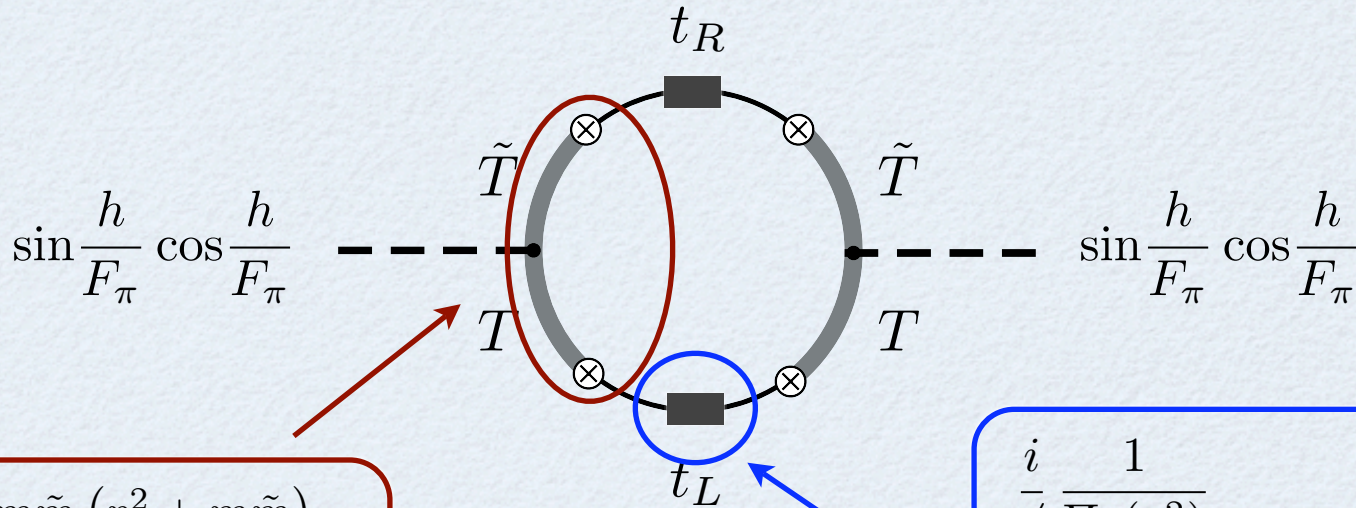


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$$\frac{i}{\not{p}} \frac{1}{\Pi^q(p^2)}$$

$$\Pi^q(p^2) = \frac{1 + p^2 (m^2 + \Delta_q^2)^{-1}}{1 + p^2 m^{-2}}$$

Higgs potential



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$$\Delta V(h) = -\frac{2N_c}{8\pi^2} F_\pi^2 \int_0^\infty dp p \frac{F^2(-p^2)}{\Pi^q(-p^2)\Pi^{t_R}(-p^2)} \sin^2 \frac{h}{F_\pi} \cos^2 \frac{h}{F_\pi}$$

$$\simeq -\frac{2N_c}{8\pi^2} y_t^2 \frac{m^2}{6} F_\pi^2 \sin^2 \frac{h}{F_\pi} \cos^2 \frac{h}{F_\pi}$$

DIAGONALIZATION:elementary / composite \rightarrow light / heavy

$$\begin{pmatrix} q_L \\ Q_L \end{pmatrix} \rightarrow \begin{pmatrix} \cos \varphi_L & -\sin \varphi_L \\ \sin \varphi_L & \cos \varphi_L \end{pmatrix} \begin{pmatrix} q_L \\ Q_L \end{pmatrix}$$

$$\tan \varphi_L = \frac{\Delta_{q_L}}{m}$$

$$\begin{pmatrix} t_R \\ \tilde{T}_R \end{pmatrix} \rightarrow \begin{pmatrix} \cos \varphi_{t_R} & -\sin \varphi_{t_R} \\ \sin \varphi_{t_R} & \cos \varphi_{t_R} \end{pmatrix} \begin{pmatrix} t_R \\ \tilde{T}_R \end{pmatrix}$$

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$$|\text{SM}\rangle = \cos \varphi |\Psi\rangle + \sin \varphi |\chi\rangle$$

$$|\text{heavy}\rangle = -\sin \varphi |\Psi\rangle + \cos \varphi |\chi\rangle$$

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 φ parametrizes the degree of partial compositeness

$$\mathcal{L} = \bar{q}_L i \not{\partial} q_L + \bar{t}_R i \not{\partial} t_R$$

$$\begin{aligned}
& + \bar{Q} (i \not{\partial} - m_Q) Q + \bar{Q}' (i \not{\partial} - m) Q' + \bar{\tilde{T}} (i \not{\partial} - m_{\tilde{T}}) \tilde{T} \\
& - Y_* \left[(\sin \varphi_L \bar{q}_L + \cos \varphi_L \bar{Q}) H^c (\sin \varphi_{t_R} t_R + \cos \varphi_{t_R} \tilde{T}) \right. \\
& \quad \left. + \bar{Q}' H (\sin \varphi_{t_R} t_R + \cos \varphi_{t_R} \tilde{T}) + h.c. \right] + \dots
\end{aligned}$$

$$m_{\tilde{T}} = \sqrt{\tilde{m}^2 + \Delta_{t_R}^2}$$

$$m_Q = \sqrt{m^2 + \Delta_{q_L}^2}$$

$$\tilde{m} = m + m_\Sigma$$

$$Y_* = \frac{m_\Sigma}{F_\pi \sqrt{2}}$$

$$\begin{aligned}
\mathcal{L} = & \bar{q}_L i \not{\partial} q_L + \bar{t}_R i \not{\partial} t_R \\
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m_{\tilde{T}} &= \sqrt{\tilde{m}^2 + \Delta_{t_R}^2} \\
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\end{aligned}$$

$$\begin{aligned}
\tilde{m} &= m + m_\Sigma \\
Y_* &= \frac{m_\Sigma}{F_\pi \sqrt{2}}
\end{aligned}$$

induced Yukawa
coupling



$$y_t = Y_* \sin \varphi_L \sin \varphi_{t_R}$$

Heavy partners of the top

	charge
$T_{5/3}$	$+ 5/3$
$T_{2/3}$	$+ 2/3$
T	$+ 2/3$
B	$- 1/3$
\tilde{T}	$+ 2/3$

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\tilde{T}	$+ 2/3$	\leftarrow partner of t_R

Heavy partners of the top

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$T_{5/3}$	$+ 5/3$	
$T_{2/3}$	$+ 2/3$	
T	$+ 2/3$	} ← partners of q_L
B	$- 1/3$	
\tilde{T}	$+ 2/3$	← partner of t_R

Heavy partners of the top

	charge	
$T_{5/3}$	$+ 5/3$	} ← $SU(2)_R$ partners of q_L
$T_{2/3}$	$+ 2/3$	
T	$+ 2/3$	} ← partners of q_L
B	$- 1/3$	
\tilde{T}	$+ 2/3$	← partner of t_R

Heavy partners of the top

charge

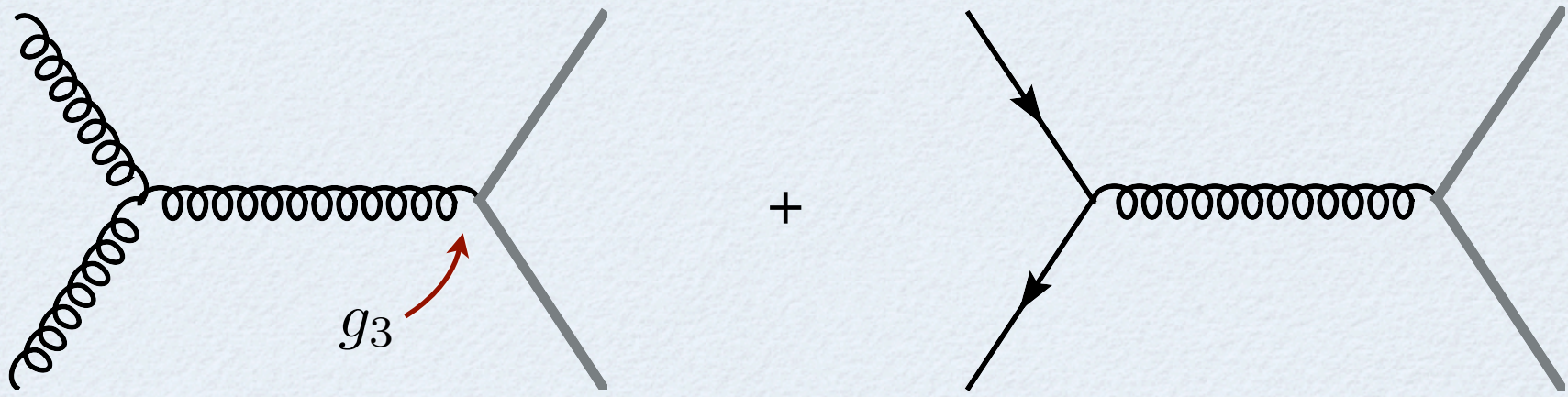
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most studies
focused on

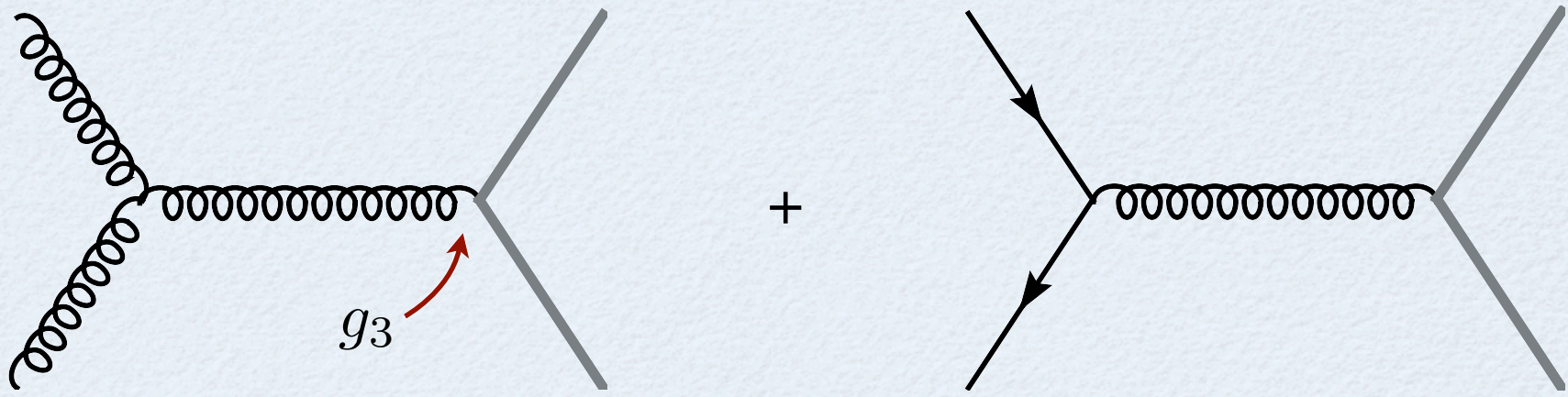


\tilde{T}	$+ 2/3$	← partner of t_R
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PAIR PRODUCTION

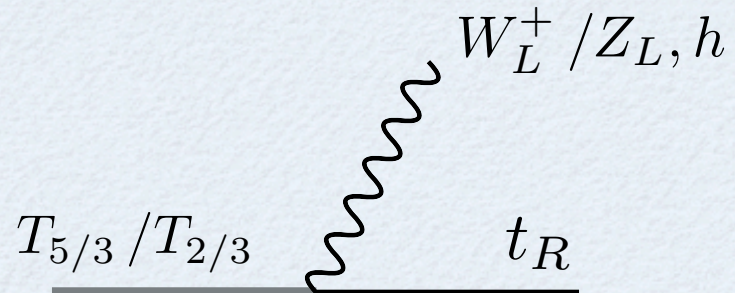


PAIR PRODUCTION

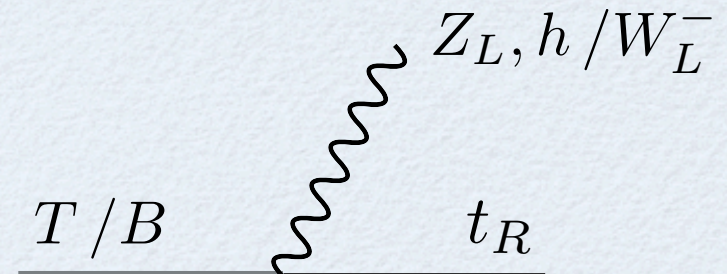


any of $T, B, T_{5/3}, T_{2/3}, \tilde{T}$

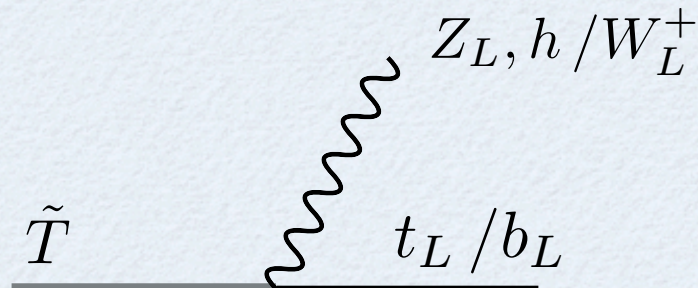
DECAYS



$$\lambda_{Q'} = Y_* \sin \varphi_{t_R}$$



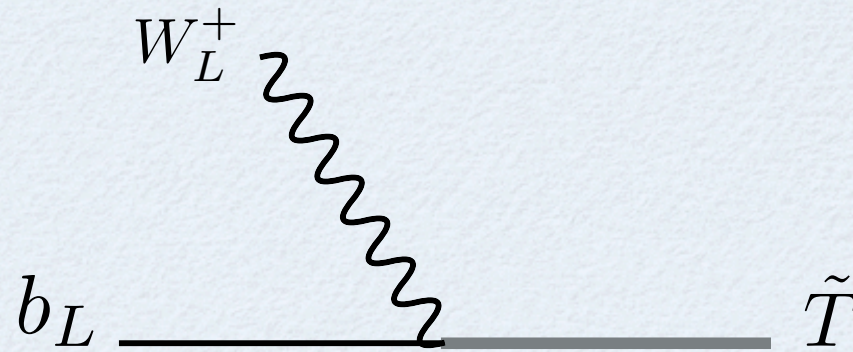
$$\lambda_Q = Y_* \sin \varphi_{t_R} \cos \varphi_L$$



$$\lambda_{\tilde{T}} = Y_* \sin \varphi_L \cos \varphi_{t_R}$$

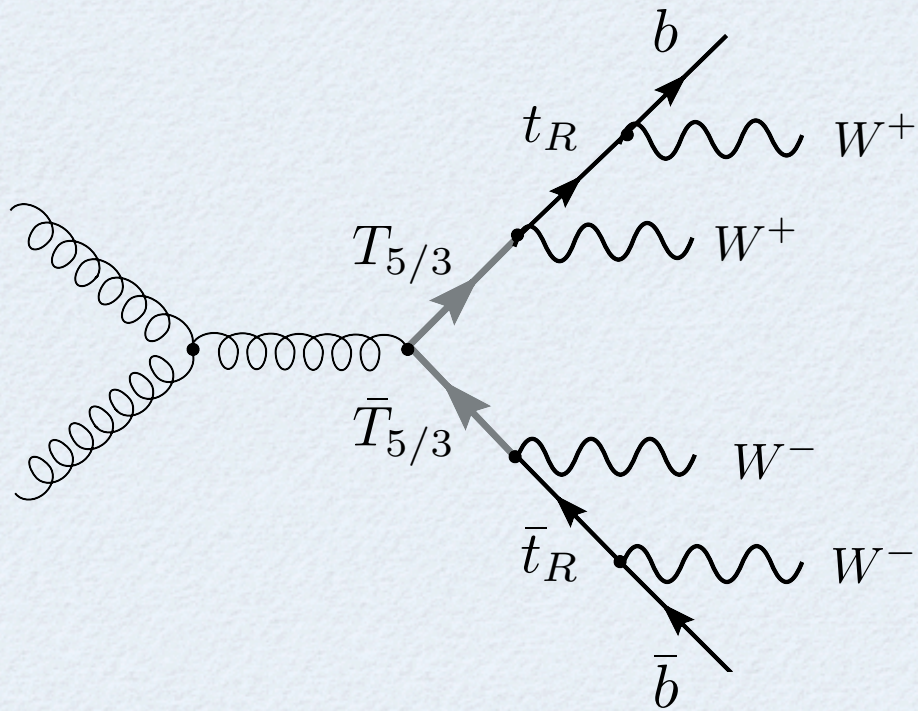
SINGLE PRODUCTION

ex:



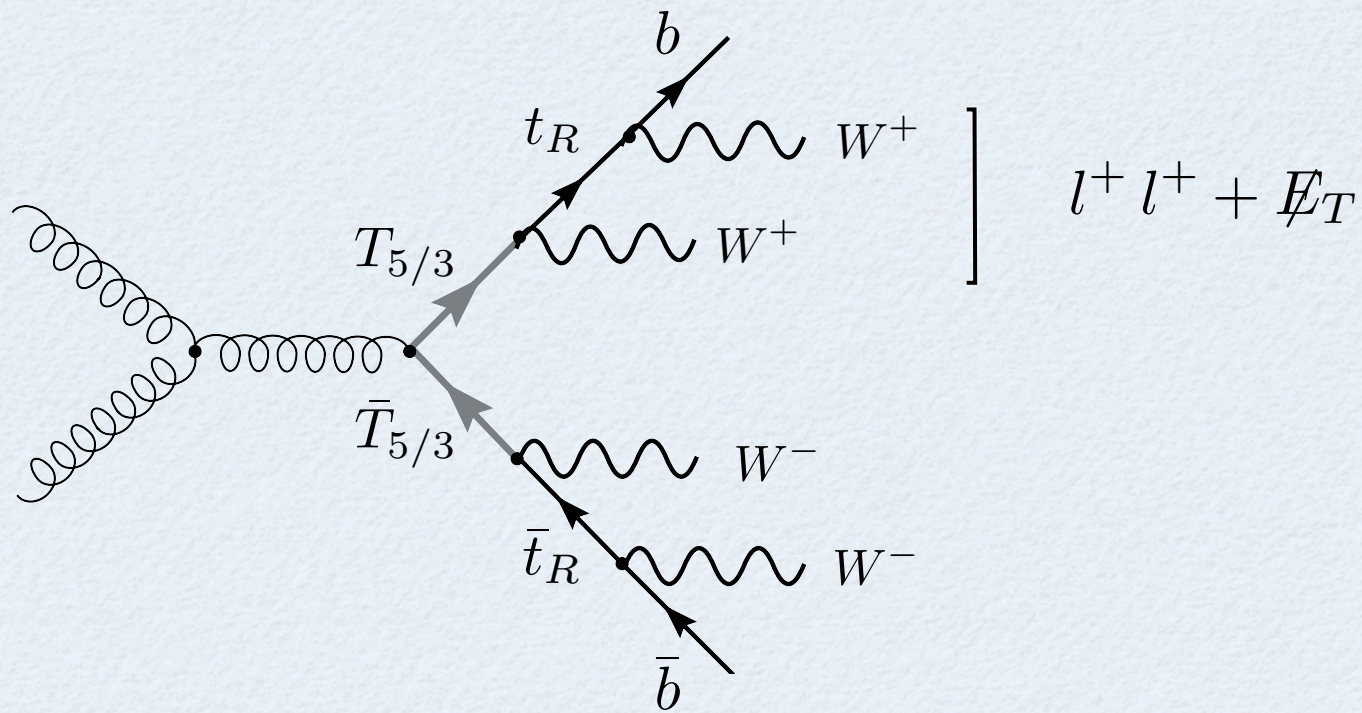
Discovering the exotic $T_{5/3}$

work in progress
with G. Servant



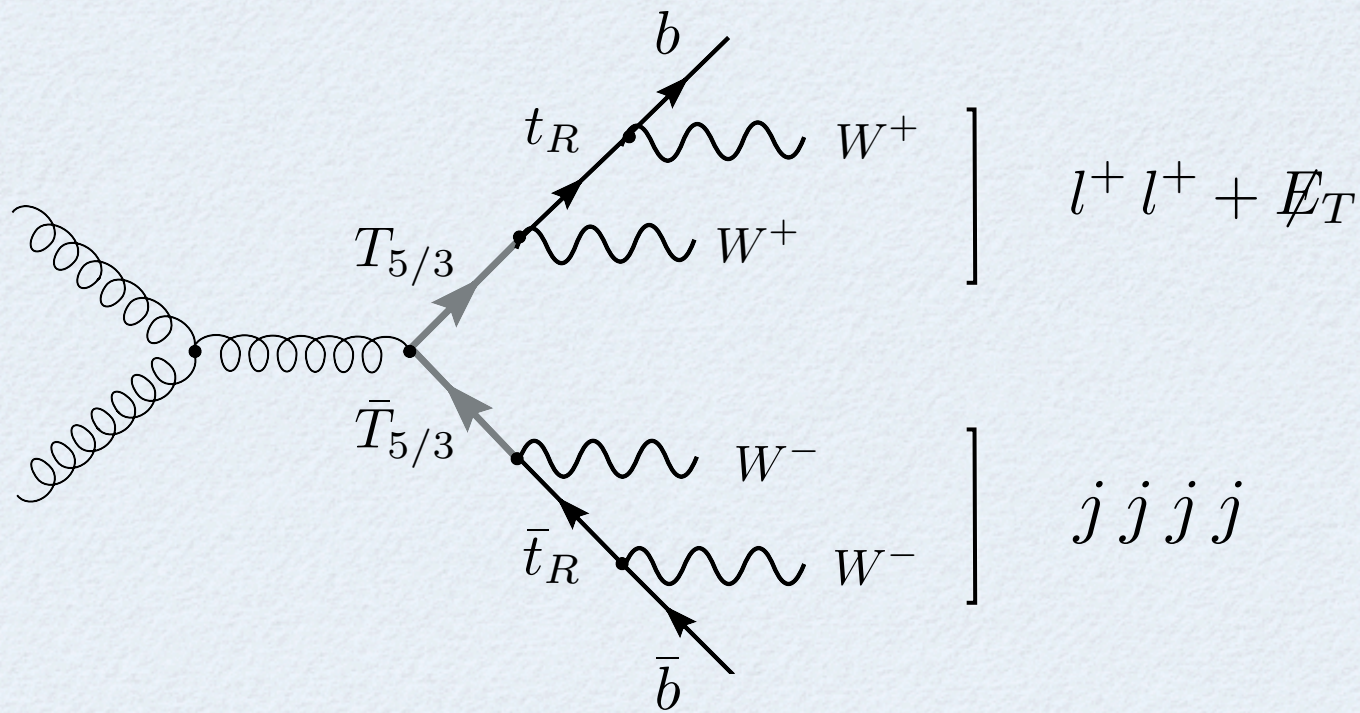
Discovering the exotic $T_{5/3}$

work in progress
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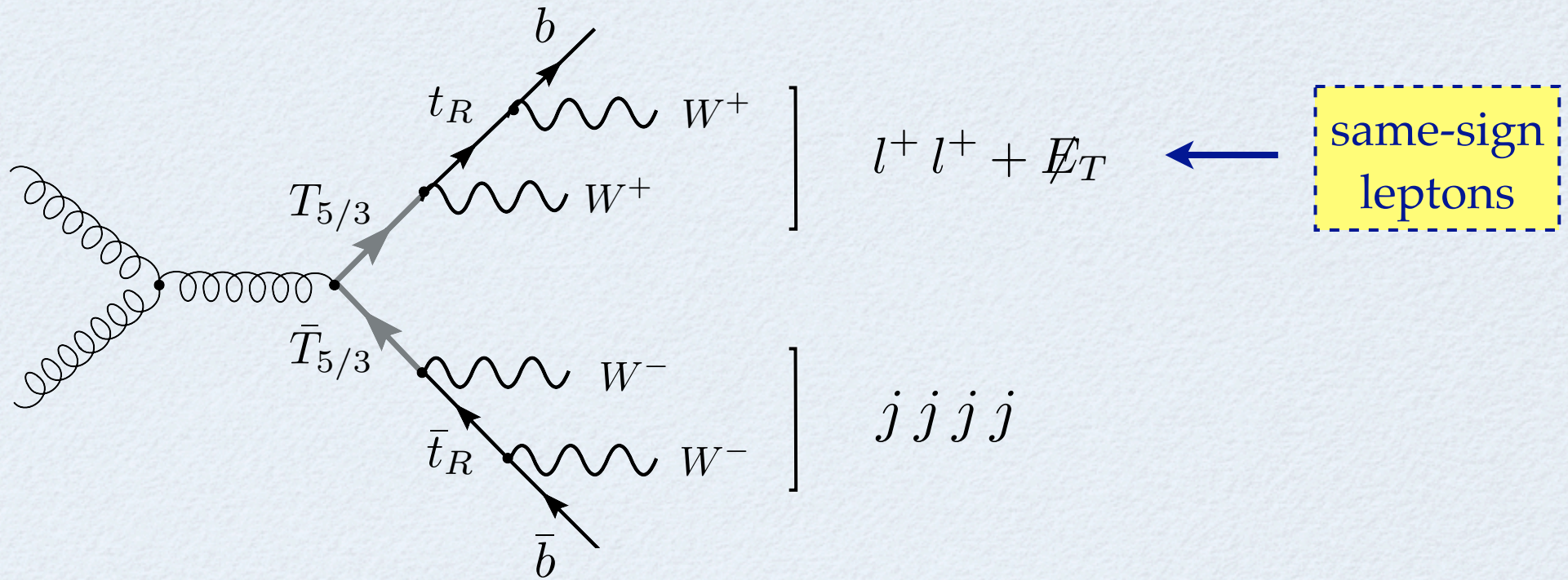
Discovering the exotic $T_{5/3}$

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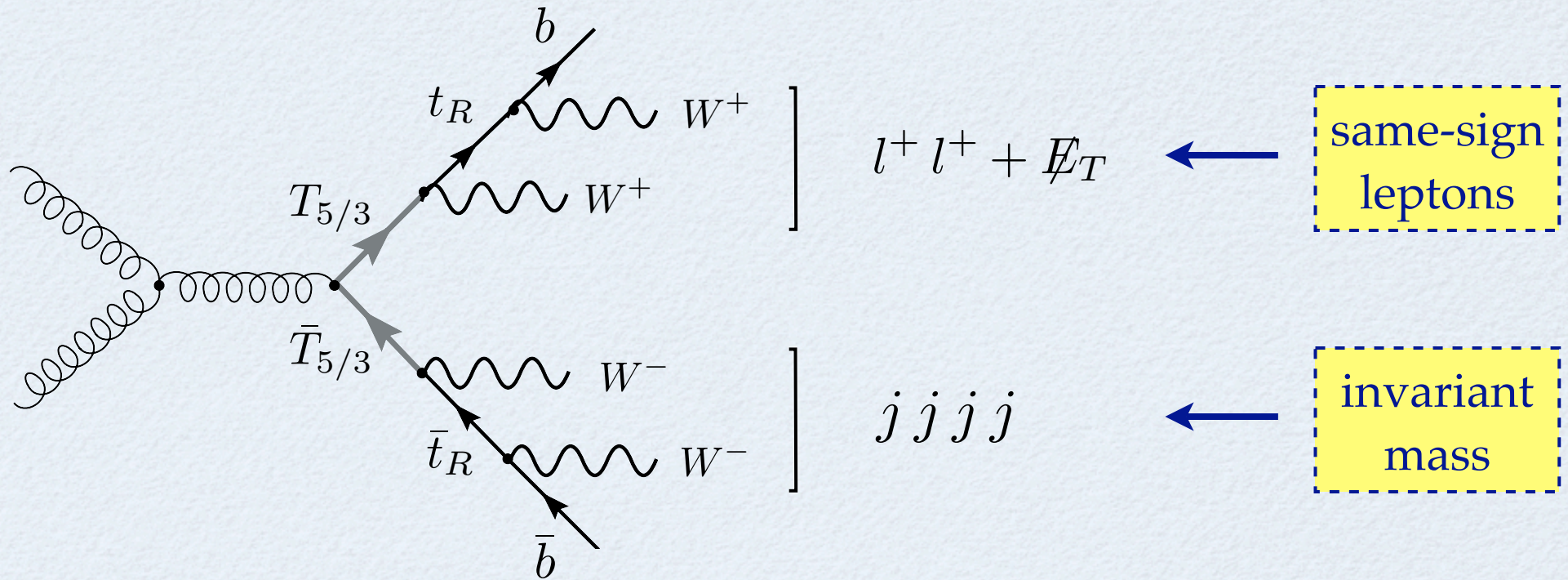
Discovering the exotic $T_{5/3}$

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Discovering the exotic $T_{5/3}$

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Conclusions



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- ★ Indirect evidence might come much earlier by producing the partners of the top