

Flavor violation in a SUSY GUT

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Work in progress

in collaboration with

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SUSY 2007, University of Karlsruhe, 2007-07-28

Supersymmetrizing the Standard Model

attractively

- offers a natural candidate of dark matter
 - stabilizes hierarchy between distant scales
 - helps gauge coupling unification
- ⇒ has an intimate relation with grand unification

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however

- may cause cosmological problems (gravitino, moduli)
 - introduces many potential sources of flavor and CP violations in the soft SUSY breaking terms
- ⇒ may serve as a probe of SUSY

Flavor violation as a probe of SUSY

- Down-type scalar quark mass term:

$$-\mathcal{L}_{\text{soft}} \ni \tilde{d}_{Ai}^* (M_{d,AB}^2)_{ij} \tilde{d}_{Bj}$$

$A, B = L, R$ and $i, j = 1, 2, 3$

- may lead to an interaction

$$\tilde{d}_{Bj} \dots \times \dots \tilde{d}_{Ai} = -i (M_{d,AB}^2)_{ij}$$

if M_d^2 is non-diagonal in the basis where m_d is diagonal and a $d-\tilde{d}-\tilde{g}$ vertex preserves flavor

- For almost diagonal M_d^2 , use a mass insertion parameter

$$(\delta_{ij}^d)_{AB} \equiv (\Delta_{ij}^d)_{AB} / m_d^2$$

$$(M_{d,AB}^2)_{ij} = m_d^2 \delta_{ij} + (\Delta_{ij}^d)_{AB}$$

Hadronic and leptonic flavor violations

- $K^0-\bar{K}^0$ mixing

$$\propto (\delta_{12}^d)_{BA} \times (\delta_{12}^d)_{DC}$$

- $\mu \rightarrow e\gamma$

$$\propto (\delta_{12}^l)_{LL}$$

SUSY GUT and flavor physics

- Superpotential of SUSY SU(5) model

$$W_{\text{GUT}} = (1/8) T^T \lambda_U T H + T^T \lambda_D \overline{F} \overline{H} + v_R^T \lambda_\nu \overline{F} H + (1/2) v_R^T M_R v_R$$

$$T [10] = \{Q, V_Q^\dagger \Theta_Q^\dagger \overline{U}, \Theta_L \overline{E}\}, \quad \overline{F} [5] = \{\overline{D}, \Theta_L^\dagger L\}$$

- Part of W_{GUT} in terms of MSSM fields, in a particular basis

$$W_{\text{SSM}} = Q^T [V_Q^T \widehat{Y}_U] \overline{U} H_u + Q^T [\widehat{Y}_D] \overline{D} H_d + \overline{E}^T [\widehat{Y}_D] L H_d \\ + v_R^T [\widehat{Y}_\nu V_L] L H_u + (1/2) v_R^T M_R v_R$$

- Soft scalar mass terms

$$-\mathcal{L}_{\text{soft}} \supset \widetilde{Q}^\dagger m_{10}^2 \widetilde{Q} + \widetilde{E}^\dagger \Theta_L^\dagger m_{10}^2 \Theta_L \widetilde{E} + \widetilde{U}^\dagger \Theta_Q V_{Qm_{10}^2} V_Q^\dagger \Theta_Q^\dagger \widetilde{U} \\ + \widetilde{D}^\dagger m_{\overline{5}}^2 \widetilde{D} + \widetilde{L}^\dagger \Theta_L m_{\overline{5}}^2 \Theta_L^\dagger \widetilde{L}$$

- Ignore phase factor Θ_L not relevant to $B(l_i \rightarrow l_j \gamma)$; then,

$$(\delta_{ij}^d)_{LL} = (\delta_{ij}^l)_{RR}^*, \quad (\delta_{ij}^d)_{RR} = (\delta_{ij}^l)_{LL}^* \quad \text{at } M_{\text{GUT}}$$

Grand unification of flavor violations

Ciuchini, Masiero, Silvestrini, Vempati, Vives, PRL(2004)

- Off-diagonal entries of scalar mass matrix are not renormalized very much if between M_{GUT} and M_{SUSY} is a desert

$$(\delta_{ij}^d)_{RR} = (\delta_{ij}^l)_{LL}^* \quad \text{at } M_{\text{GUT}} \quad \Longrightarrow \quad (\delta_{ij}^d)_{RR} \approx \frac{m_{\tilde{L}}^2}{m_{\tilde{d}}^2} (\delta_{ij}^l)_{LL}^* \quad \text{at } M_{\text{SUSY}}$$

- Large couplings and large mixing in Y_V may modify the relation at M_{SUSY} ; still, a footprint of the GUT relation remains
- Naturally expected correlations among flavor transitions

| Transitions of L | | Transitions of \bar{D} |
|------------------------|-------------------|--------------------------|
| $\mu \rightarrow e$ | \leftrightarrow | $s \rightarrow d$ |
| $\tau \rightarrow e$ | \leftrightarrow | $b \rightarrow d$ |
| $\tau \rightarrow \mu$ | \leftrightarrow | $b \rightarrow s$ |

Caveat: $Y_D \neq Y_E^T$ at M_{GUT}

- Fermion mass relations from W_{GUT} ,

$$\bar{m}_e = \bar{m}_d, \quad \bar{m}_\mu = \bar{m}_s, \quad \bar{m}_\tau = \bar{m}_b \quad \text{at } M_{\text{GUT}},$$

are inconsistent with data

- Solutions: add non-renormalizable terms or **45** Higgs
- In the basis where Y_D is diagonal,

$$Y_U = V_Q^T \hat{Y}_U U_Q^*, \quad Y_D = \hat{Y}_D, \quad Y_E = U_L^T \hat{Y}_E U_R^*, \quad Y_N = U_L^T V_L^T \hat{Y}_N$$

- GUT relations are modified to

$$\delta_{LL}^l = U_L \delta_{RR}^{d*} U_L^\dagger, \quad \delta_{RR}^l = U_R \delta_{LL}^{d*} U_R^\dagger$$

- Suppose $U_L = U_R = \mathbf{1}$ for numerical analysis
(a general case is discussed later)

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- Or, how do they interplay?

For recent analyses, see e.g.
Cheung, Kang, Kim, Lee, hep-ph/0702050
Ciuchini, Masiero, Paradisi, Silvestrini, Vempati, Vives, hep-ph/0702144

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- This talk deals with cases with **more than one mass insertions**.

Consider $(\delta_{23}^d)_{RR}$ [= $(\delta_{23}^l)_{LL}^*$ at M_{GUT}]

- Well motivated from large neutrino mixing within SUSY GUT + ν_R with $O(1)$ neutrino Yukawa couplings

\Leftarrow GUT partner of $(\delta_{23}^l)_{LL}^*$

Moroi, JHEP(2000)

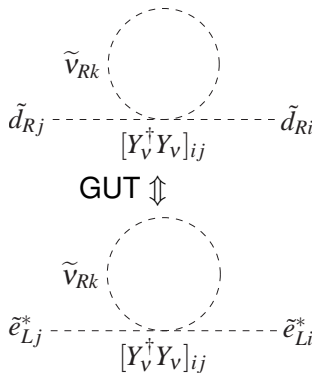
Baek, Goto, Okada, Okumura, PRD(2001)

- Recently has attracted interests regarding $b \rightarrow s$ transitions such as $B \rightarrow \phi K$ and B_s mixing

With Kane, Ko, Kolda, Wang $\times 2$
Hisano, Shimizu

With Ko, Masiero, PRD(2005)

Endo, Mishima, PLB(2006)



Constraints on $(\delta_{23}^d)_{RR}$ in SUSY GUT

- Linked to $\tau \rightarrow \mu \gamma$

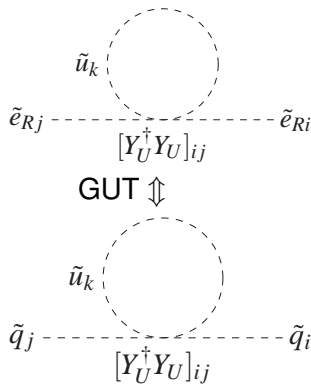
Hisano, Shimizu, PLB(2003)

Constraints on $(\delta_{23}^d)_{RR}$ in SUSY GUT

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- Radiatively generated $(\delta_{13}^l)_{RR}$ included,

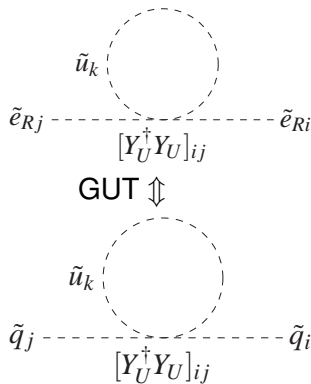
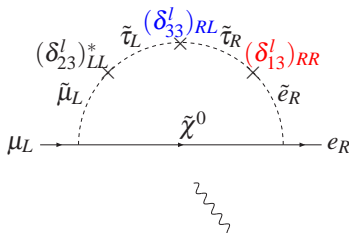


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also related to $\mu \rightarrow e \gamma$

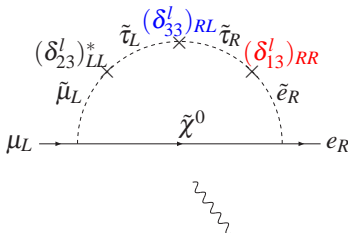


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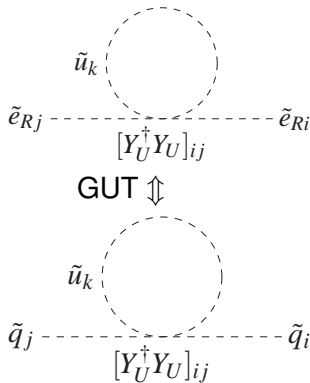
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Enhanced by a factor m_τ/m_μ

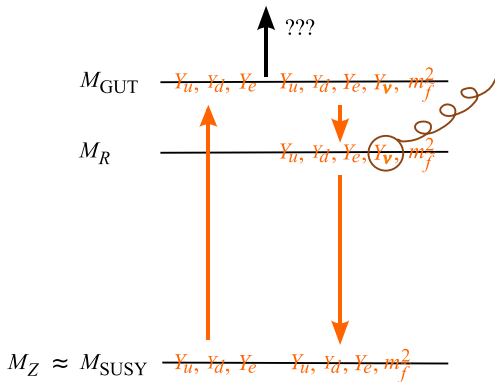
Hisano, Moroi, Tobe, Yamaguchi, PRD(1996)

Baek, Goto, Okada, Okumura, PRD(2001)



Procedure of numerical analysis

- 1 Run Y_u, Y_d, Y_e from M_Z to M_{GUT}
- 2 Go to the basis where Y_d and Y_e are diagonal
- 3 Set Y_ν, m_f^2 at M_{GUT} **by hand** regarding $(\delta_{23}^d)_{RR}$ and $(\delta_{13}^d)_{LL}$ as **free parameters**
 $A(M_{\text{GUT}}) = 0$
- 4 Run down to M_R
- 5 Remove ν_R
- 6 Run down to M_Z
- 7 Calculate μ from EWSB condition
- 8 Compute flavor violations



Mixings and constraints

- Scan over $(\delta_{23}^d)_{RR} = (\delta_{23}^l)_{LL}^*$ and $(\delta_{13}^d)_{LL} = (\delta_{13}^l)_{RR}^*$
- Leptonic constraints

| Process | Present upper bound | Future upper bound |
|---------------------------------|-----------------------|---------------------|
| $B(\mu \rightarrow e\gamma)$ | 1.2×10^{-11} | 1×10^{-13} |
| $B(\tau \rightarrow e\gamma)$ | 3.1×10^{-7} | 1×10^{-8} |
| $B(\tau \rightarrow \mu\gamma)$ | 6.8×10^{-8} | 1×10^{-8} |

- Hadronic constraints

| Observable | Range | Note |
|-------------------------------|------------------------------|------------------------------|
| ΔM_s | $[12.5, 23] \text{ ps}^{-1}$ | CDF central value $\pm 30\%$ |
| $B(B \rightarrow X_s \gamma)$ | $[2.0, 4.5] \times 10^{-4}$ | NLO uncertainty |
| $B(B \rightarrow X_d \gamma)$ | $[1, 10] \times 10^{-6}$ | |

Also, ΔM_d , $\sin 2\beta$, $\cos 2\beta$, ϕ_s , $S_{\phi K}$, ϵ_K , ϵ'/ϵ_K , d_n

Constraints on $[(\delta_{13}^d)_{LL}, (\delta_{23}^d)_{RR}]$ plane

- Parameters

$$\mu > 0, \quad \tan \beta = 3$$

$$m_0(M_{\text{GUT}}) = 210 \text{ GeV}$$

$$M_2(M_Z) = 150 \text{ GeV}$$

$$[m_{\tilde{d}}(M_Z) = M_3(M_Z) = 500 \text{ GeV}]$$

$$[(\delta_{23}^d)_{LL}](M_{\text{GUT}}) = 0.014$$

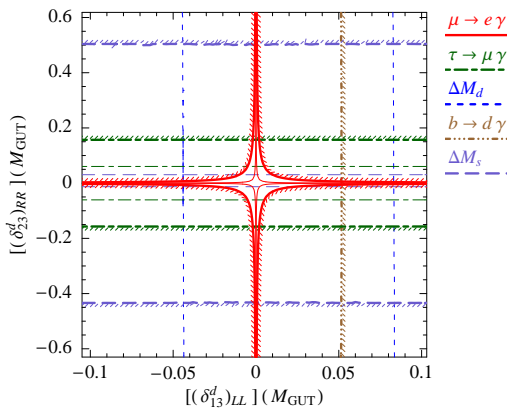
No ν_R below M_{GUT}

- Effective constraints

$$(\delta_{13}^d)_{LL} : B \rightarrow X_d \gamma$$

$$(\delta_{23}^d)_{RR} : \Delta M_s, \tau \rightarrow \mu \gamma$$

$$(\delta_{13}^d)_{LL} \times (\delta_{23}^d)_{RR} : \mu \rightarrow e \gamma$$



Constraints on $[(\delta_{13}^d)_{LL}, (\delta_{23}^d)_{RR}]$ plane

$(\delta_{13}^d)_{LL}$ from RGE between M_* and M_{GUT} \longrightarrow

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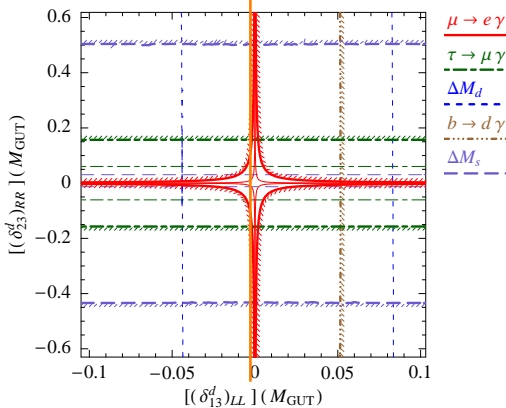
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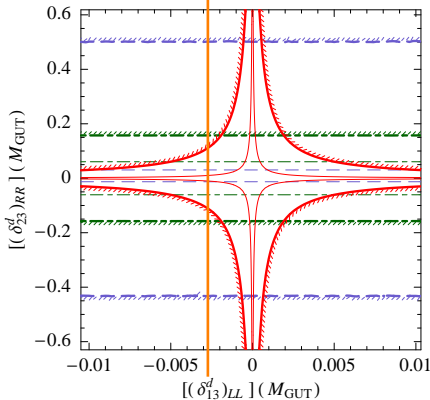
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Constraints on $[\text{Re}(\delta_{23}^d)_{RR}, \text{Im}(\delta_{23}^d)_{RR}]$ plane

Parameters

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$$m_0(M_{\text{GUT}}) = 210 \text{ GeV}$$

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$$[(\delta_{13}^d)_{LL}](M_{\text{GUT}}) = 0.0028$$

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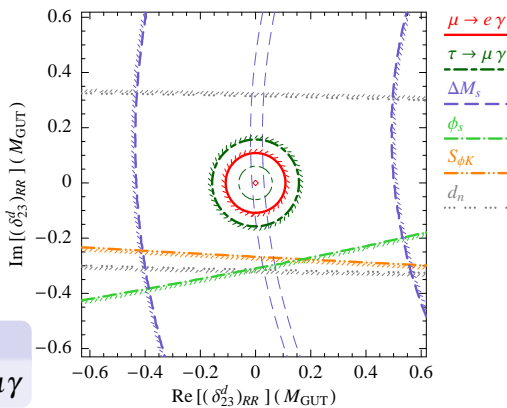
Constraints

Present

$\mu \rightarrow e\gamma$ comparable to $\tau \rightarrow \mu\gamma$

Future

$\mu \rightarrow e\gamma$ stronger than $\tau \rightarrow \mu\gamma$



Constraints on $[\text{Re}(\delta_{23}^d)_{RR}, \text{Im}(\delta_{23}^d)_{RR}]$ plane

Parameters

$$\mu > 0, \quad \tan \beta = 3$$

$$m_0(M_{\text{GUT}}) = 400 \text{ GeV}$$

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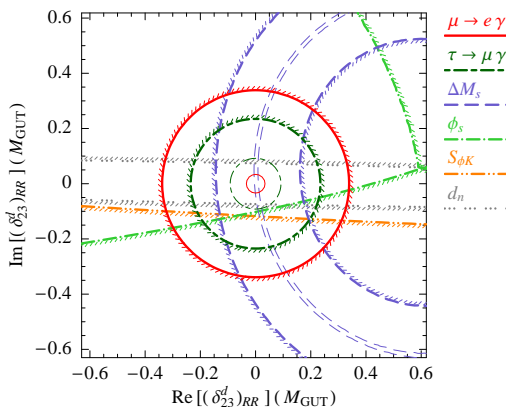
Constraints

LFV

got weaker

ΔM_s

got stronger



Same exercise on $[\text{Re}(\delta_{13}^d)_{RR}, \text{Im}(\delta_{13}^d)_{RR}]$ plane

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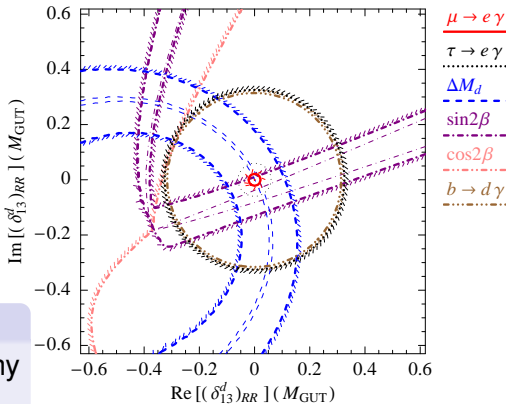
● Constraints

Present

$\mu \rightarrow e\gamma$ stronger than any other constraint

Future

$\mu \rightarrow e\gamma$ even stronger



Same exercise on $[\text{Re}(\delta_{13}^d)_{RR}, \text{Im}(\delta_{13}^d)_{RR}]$ plane

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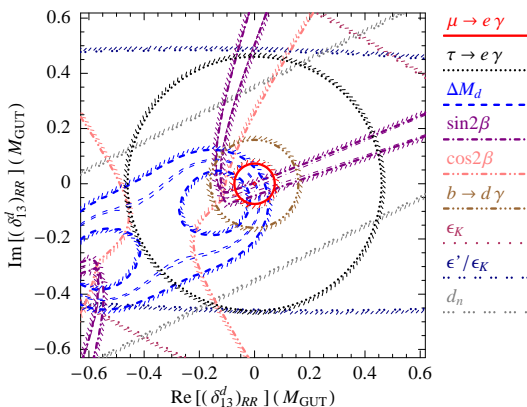
● Constraints

LFV

got weaker

hadronic

got stronger



Effects of non-renormalizable terms on an RR mixing

- Key equation

$$(\delta_{a3}^l)_{LL} = [U_L]_{ab} (\delta_{b3}^d)_{RR}^* [U_L]_{33}^* + \mathcal{O}(\cos^2 \beta \delta_{RR}^d), \quad a, b = 1, 2$$

- A tau decay is dominated by chargino loop

$$\begin{aligned} B(\tau \rightarrow (e + \mu)\gamma) &\propto |(\delta_{13}^l)_{LL}|^2 + |(\delta_{23}^l)_{LL}|^2 \\ &\approx |(\delta_{13}^d)_{RR}|^2 + |(\delta_{23}^d)_{RR}|^2 + \mathcal{O}[\cos^2 \beta (\delta_{RR}^d)^2] \end{aligned}$$

\Rightarrow Constraint on δ_{RR}^d roughly independent of U_L

- $\mu \rightarrow e\gamma$ is dominated by neutralino loop

$$\begin{aligned} B(\mu \rightarrow e\gamma) &\propto |(\delta_{13}^l)_{RR}(\delta_{32}^l)_{LL}|^2 + |(\delta_{13}^l)_{LL}(\delta_{32}^l)_{RR}|^2 \\ &\approx |(\delta_{13}^l)_{RR}|^2 \times |[U_L]_{21}(\delta_{13}^d)_{RR}^* + [U_L]_{22}(\delta_{23}^d)_{RR}^*|^2 \\ &\quad + |(\delta_{23}^l)_{RR}|^2 \times |[U_L]_{11}(\delta_{13}^d)_{RR}^* + [U_L]_{12}(\delta_{23}^d)_{RR}^*|^2 \\ &\quad + \mathcal{O}[\cos^2 \beta (\delta_{RR}^l)^2 (\delta_{RR}^d)^2] \end{aligned}$$

\Rightarrow Constraint on δ_{RR}^d generically remains strong

Summary

[δ 's at M_{GUT} ; $\tan\beta = 3$, $m_0 = 210$ GeV, $M_2 = 150$ GeV by default]

Constraints on $(\delta_{23}^d)_{RR}$, with fixed $(\delta_{13}^d)_{LL} = 0.0028$

- At present, $\mu \rightarrow e\gamma \sim \tau \rightarrow \mu\gamma$ stronger than ΔM_s
- In future, $\mu \rightarrow e\gamma$ stronger than $\tau \rightarrow \mu\gamma$ stronger than ΔM_s , unless hadronic uncertainty is reduced

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- At present, $\mu \rightarrow e\gamma$ very strong
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In either case

- For higher $\tan\beta$, LFV constraints become stronger
- For $m_0 = 400$ GeV, LFV constraints become weaker, hadronic constraints become stronger

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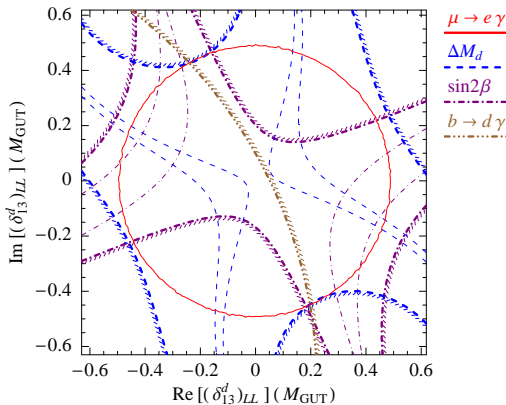
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No ν_R below M_{GUT}



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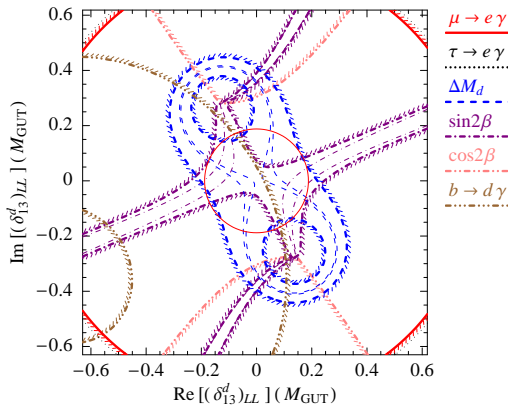
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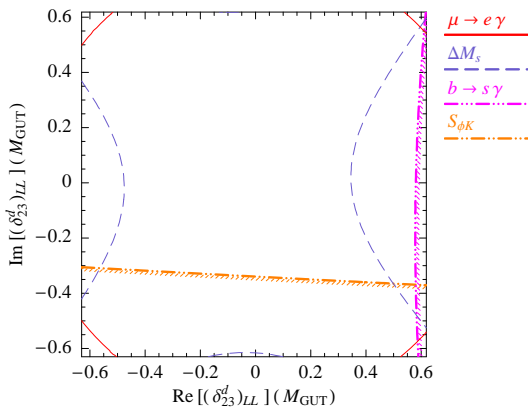
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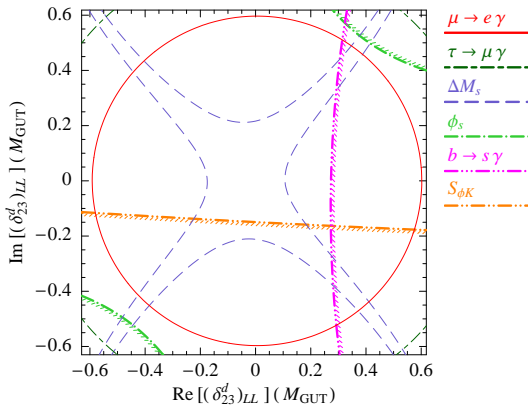
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'Mass insertion' parameter at M_{GUT}

- An off-diagonal entry of a **soft** scalar mass matrix divided by a diagonal entry

$$m_q^2 = m_0^2 \begin{pmatrix} 1 & 0 & (\delta_{13}^d)_{LL} \\ 0 & 1 & (\delta_{23}^d)_{LL} \\ (\delta_{13}^d)_{LL}^* & (\delta_{23}^d)_{LL}^* & 1 \end{pmatrix},$$

$$m_d^2 = m_0^2 \begin{pmatrix} 1 & 0 & (\delta_{13}^d)_{RR} \\ 0 & 1 & (\delta_{23}^d)_{RR} \\ (\delta_{13}^d)_{RR}^* & (\delta_{23}^d)_{RR}^* & 1 \end{pmatrix}$$

List of hadronic constraints

| Observable | Measured value | Imposed constraint |
|-------------------------------|--|--|
| ΔM_{B_d} | $0.507 \pm 0.004 \text{ ps}^{-1}$ | $[0.355, 0.659] \text{ ps}^{-1}$ |
| $\sin 2\beta$ | 0.678 ± 0.025 | 2σ |
| $\cos 2\beta$ | > -0.4 | |
| $B(B \rightarrow X_d \gamma)$ | | $[10^{-6}, 10^{-5}]$ |
| ΔM_{B_s} | $17.77 \pm 0.12 \text{ ps}^{-1}$ | $[12.5, 23] \text{ ps}^{-1}$ |
| ϕ_{B_s} | $-0.70^{+0.47}_{-0.39}$ | $[-1.48, 0.24]$ |
| $B(B \rightarrow X_s \gamma)$ | $(355 \pm 24^{+9}_{-10} \pm 3) \times 10^{-6}$ | $[2.0, 4.5] \times 10^{-4}$ |
| S_{ϕ_K} | 0.39 ± 0.18 | 2σ |
| $ \epsilon_K $ | $(2.232 \pm 0.007) \times 10^{-3}$ | $ \epsilon_K^{\text{SUSY}} < \epsilon_K^{\text{exp}} $ |
| ϵ'/ϵ_K | $(1.66 \pm 0.26) \times 10^{-3}$ | $ (\epsilon'/\epsilon_K)^{\text{SUSY}} < (\epsilon'/\epsilon_K)^{\text{exp}} $ |
| $ d_n $ | $< 6.3 \times 10^{-26} \text{ e cm}$ | |

$B \rightarrow X_s \gamma$?

Parameters

$$\mu > 0$$

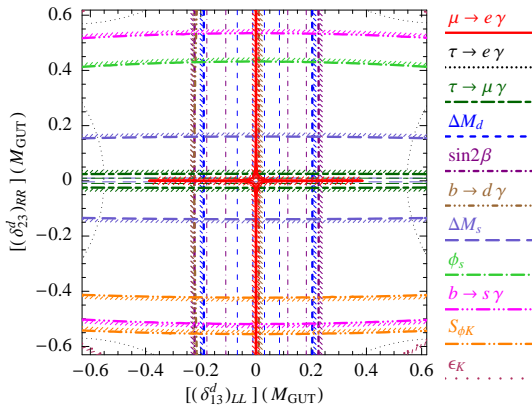
$$\tan \beta = 25$$

$$m_0 = 400 \text{ GeV}$$

$$M_2 = 150 \text{ GeV}$$

No ν_R below M_{GUT}

$$[(\delta_{23}^d)_{LL}](M_{\text{GUT}}) = 0.014$$



$\tau \rightarrow e\gamma$?

- Parameters

$$\mu > 0$$

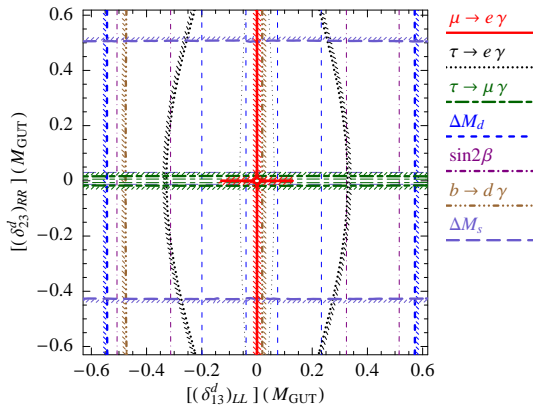
$$\tan\beta = 25$$

$$m_0 = 210 \text{ GeV}$$

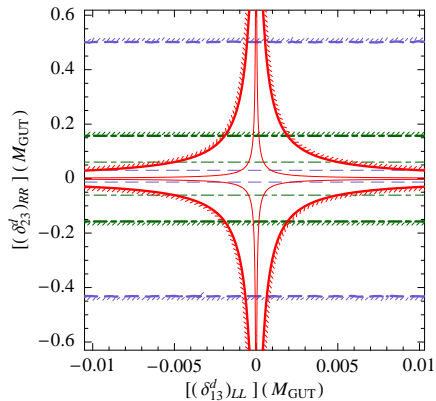
$$M_2 = 150 \text{ GeV}$$

No ν_R below M_{GUT}

$$[(\delta_{23}^d)_{LL}](M_{\text{GUT}}) = 0.014$$

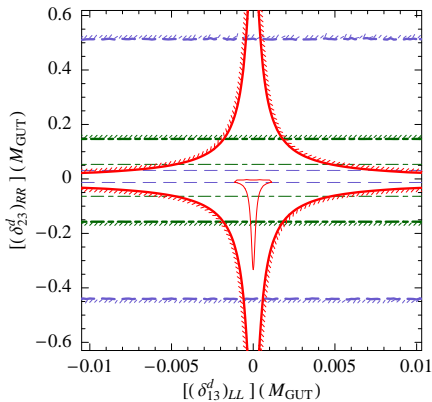


Large neutrino Yukawa couplings

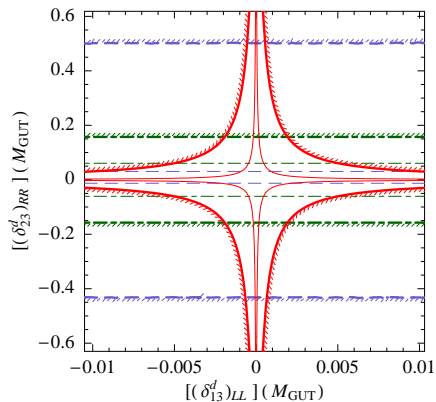


No ν_R below M_{GUT}

Large neutrino Yukawa couplings

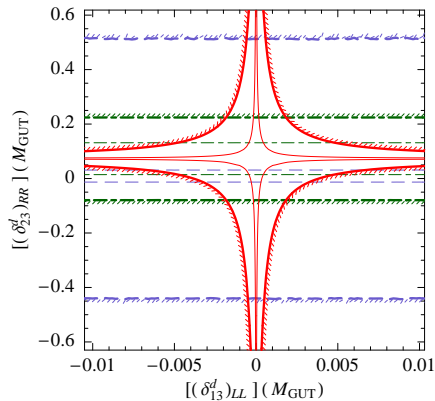
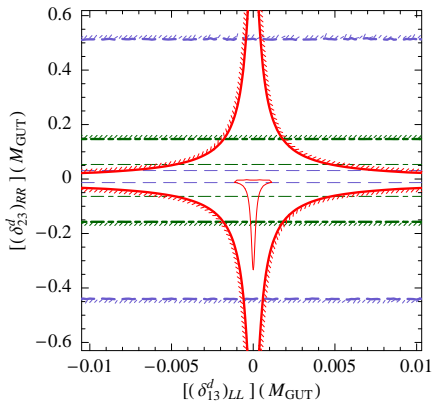


$Y_V = Y_u$ at M_{GUT} (CKM-like mixing)



No ν_R below M_{GUT}

Large neutrino Yukawa couplings



$Y_{\nu} = Y_u$ at M_{GUT} (CKM-like mixing) $Y_{\nu} = U_{\text{PMNS}}^* Y_u^{\text{diag}}$ at M_{GUT} (large mixing)