

Susy QCD corrections in Higgs boson production via gluon fusion

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Outline

NLO SUSY-QCD corrections to $gg \rightarrow h$ (in progress...)

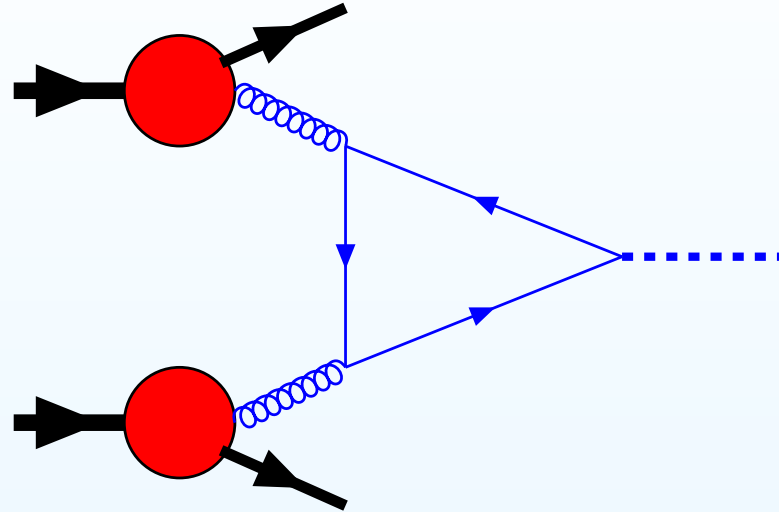
in collaboration with Stefan Beerli, Stefan Bucherer, Alejandro Daleo and Zoltan Kunszt

- introduction
- quark and scalar-quark two-loop amplitudes
- diagrams with gluinos and squarks (the method only - no results)
- summary

NNLO QCD corrections for $gg \rightarrow h \rightarrow W^+W^- \rightarrow l^+l^-\nu\nu$ (full calculation with all experimental cuts at the parton level)

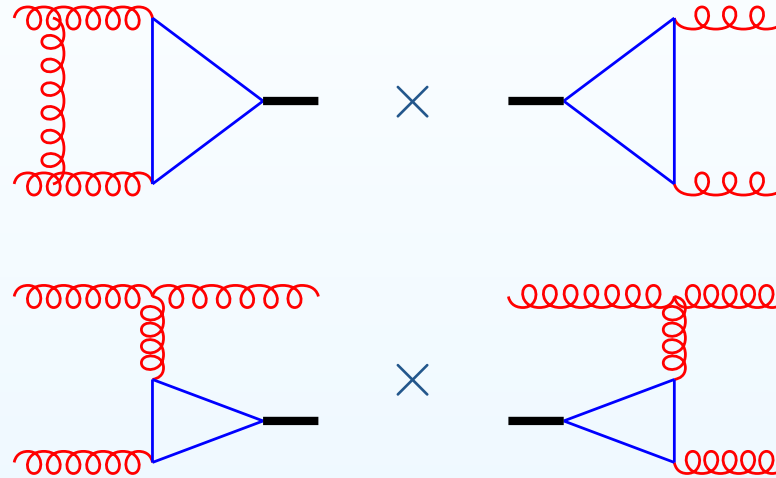
in collaboration with Günther Dissertori and Fabian Stöckli

The gluon-gluon fusion channel in the Standard Model



- Higgs boson couples to gluons at the one-loop level, through (heavy) quarks
- Recall the large gluon density at $x \sim 10^{-4} - 10^{-2}, Q \sim 100\text{GeV}$
- Large Born cross-section at the LHC ($\sim \mathcal{O}(20)pb$)
- But not precise - scale uncertainty $\sim 40\%$

First order QCD radiative corrections



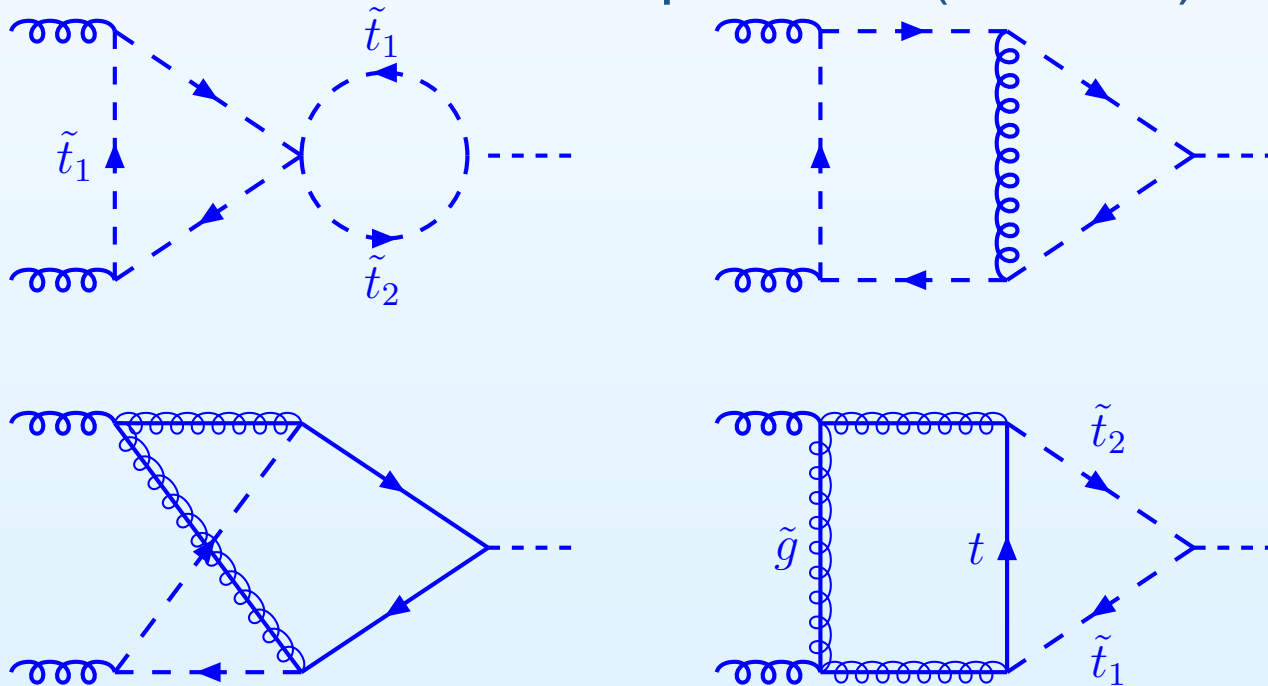
- a two-loop calculation, **Spira, Djouadi, Graudenz, Zerwas**
- large scale uncertainty $\sim 25\%$
- a very big correction ($\sim 70\%$) **Dawson; Spira et. al.**

Gluon fusion: sensitive to BSM physics

- Anything that couples to gluons and the Higgs boson can circulate inside the production loop!
- There is a lot of room in the model building world to change the cross-section significantly
- For example, an additional quark in a Left-Right symmetric Randall-Sundrum model could alter the Higgs cross-section from -50% to $+400\%$ without any conflict with electroweak precision data. **Djouadi, Moreau**
- The interpretation of the nature of the Higgs boson will also rely on the magnitude of the cross-section in various BSM models.

Two-loop corrections in BSM

- The LO cross-section is uncertain in the SM. It is the same (or worse) uncertain in BSM. Can we compute the NLO cross-section scanning a multitude of models?
- For the MSSM only, we need two loop three point diagrams with up to four different internal particles (masses)



Effective theory approach

- Heavy Quark Effective Theory is very successful for the SM Higgs boson. It will be successful in many other scenaria too. Still a formidable computation!
- NLO Wilson coefficient for heavy quarks+squarks+gluinos is known **Harlander, Steinhauser**
- It should be a very good approximation for a light MSSM Higgs boson
- ET hierarchies are not always satisfied. E.g. heavy Higgs boson? Other BSM than MSSM?

New techniques for analytic two-loop computations

- Automated reduction to master integrals

Gehrmann, Remiddi; Laporta; CA, Lazopoulos

- Differential Equations Kotikov; Gehrmann, Remiddi

- Mellin-Barnes method

Smirnov; Tausk

Two-loop diagrams with one quark or squark

Complete analytic calculation

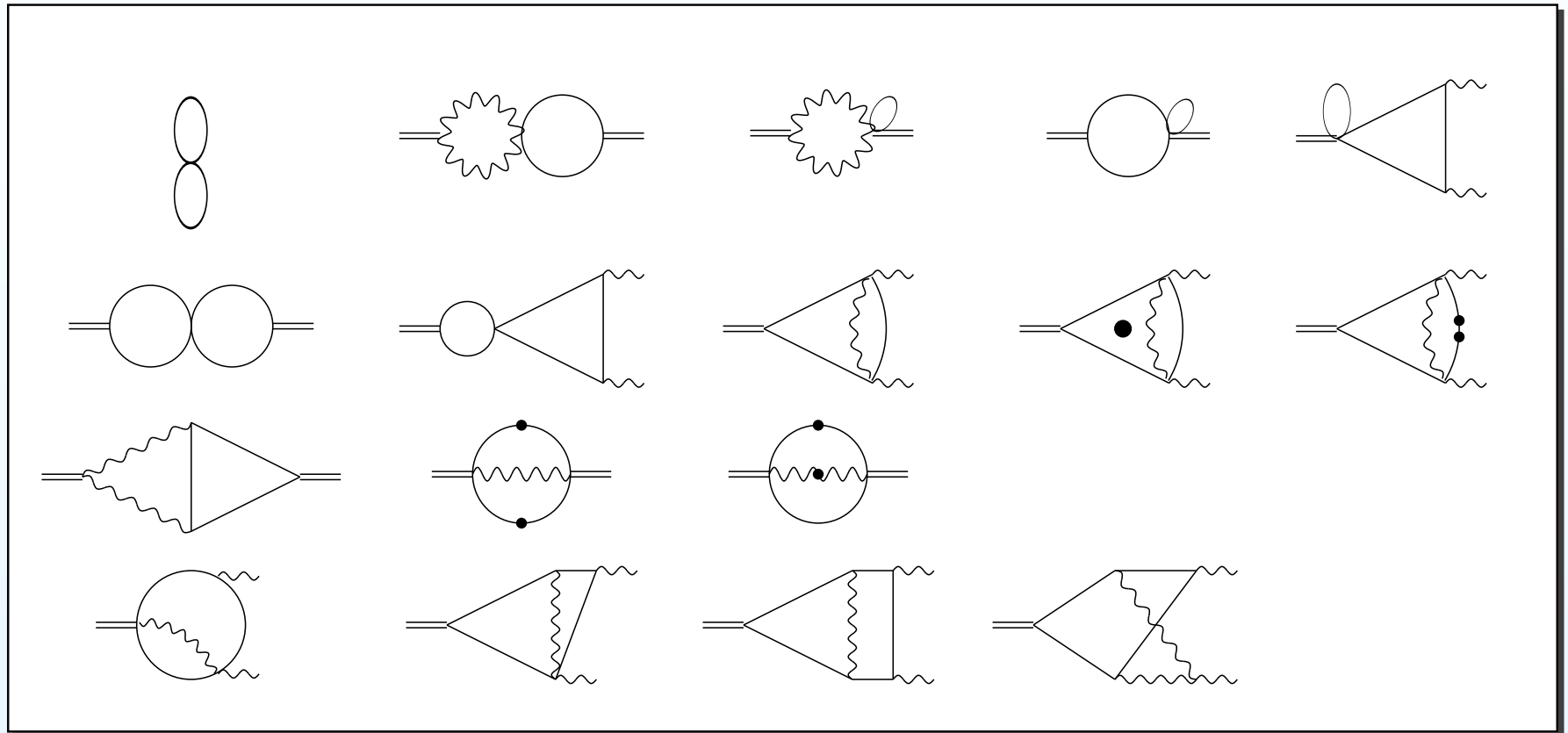
- reduced to linear combinations of master integrals using Laporta's algorithm
- complete set of master integrals computed with the method of differential equations (most were already known in the literature)
- analytic continuation of the master integrals above threshold

Contributions mediated by a heavy quark agree with the results of Spira *et al.* in the analytic form derived by Harlander and Kant

First results for the scalar quark contributions, simultaneous with

Aglietti *et al.* and Mühlleitner and Spira

Master Integrals



All computed in terms of logs and polylogs or equivalent functions
valid in all kinematic regions.

Squark contributions at two loops

$$\begin{aligned}
& \frac{4x C_F}{(1-x)^2} \left\{ 5 + \frac{3x^2}{(1-x)(1+x)} H(0, x) - 3H(1, x) + \frac{4x \zeta_2}{(1-x)^2} H(0, x) + \frac{8x(1+x^2)\zeta_2}{(1-x)^3(1+x)} H(0, 0, x) + \frac{36x(1+x^2)\zeta_2^2}{5(1-x)^3(1+x)} + \frac{12x\zeta_3}{(1-x)^2} \right. \\
& + \frac{16x(1+x^2)\zeta_3}{(1-x)^3(1+x)} H(0, x) - \frac{3x(1+5x)}{(1-x)^2(1+x)} H(0, 0, x) + \frac{6x}{(1-x)(1+x)} H(0, 1, x) + \frac{6x}{(1-x)(1+x)} H(1, 0, x) \\
& + \frac{16x}{(1-x)^2} H(0, -1, 0, x) - \frac{x(-13+7x)}{(1-x)^3} H(0, 0, 0, x) + \frac{12x}{(1-x)^2} H(0, 0, 1, x) + \frac{8x}{(1-x)^2} H(0, 1, 0, x) \\
& + \frac{16x}{(1-x)^2} H(1, 0, 0, x) - \frac{16x(1+x^2)}{(1-x)^3(1+x)} H(0, -1, 0, 0, x) + \frac{32x(1+x^2)}{(1-x)^3(1+x)} H(0, 0, -1, 0, x) \\
& \left. + \frac{2x(1+x^2)}{(1-x)^3(1+x)} H(0, 0, 0, 0, x) - \frac{8x(1+x^2)}{(1-x)^3(1+x)} H(0, 0, 1, 0, x) + \frac{28x(1+x^2)}{(1-x)^3(1+x)} H(0, 1, 0, 0, x) \right\} \\
& \frac{4x C_A}{(1-x)^2} \left\{ 3 - \frac{32x\zeta_2^2}{5(1-x)^2} - \frac{16x\zeta_3}{(1-x)^2} - \frac{12x\zeta_3}{(1-x)^2} H(0, x) - \frac{24x\zeta_3}{(1-x)^2} H(1, x) - \frac{2x}{(1-x)^2} H(0, 0, x) + \frac{2(1-7x)x}{(1-x)^3} H(0, 0, 0, x) \right. \\
& + \frac{16x}{(1-x)^2} H(1, 0, 0, x) - \frac{4x\zeta_2}{(1-x)^2} H(0, 0, x) - \frac{8x\zeta_2}{(1-x)^2} H(1, 0, x) - \frac{8x}{(1-x)^2} H(0, 0, -1, 0, x) - \frac{2x}{(1-x)^2} H(0, 0, 0, 0, x) \\
& \left. - \frac{16x}{(1-x)^2} H(1, 0, -1, 0, x) + \frac{8x}{(1-x)^2} H(1, 0, 0, 0, x) \right\}
\end{aligned}$$

Many massive particle in the loops

- Analytic computations are not easy any more!
Mass-thresholds and singularities in $D = 4$ dimensions.
- Could be attacked numerically; e.g. methods of Passarino and Uccirati or Spira et al.
- These methods operate on a case by case basis and may be limited in applications.
- Do we have an algorithm which can treat generic mutli-loop integrals with infrared, ultraviolet, and all types of threshold singularities?

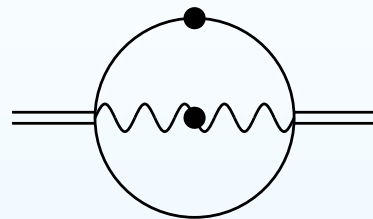
Automated numerical methods

Two general and fully automated methods to deal with multiloop integrals in a numerical way

- sector decomposition Binoth, Heinrich
 - extended to fully differential NNLO cross section calculations CA, Melnikov, Petriello
 - not possible to handle thresholds automatically
- numerical integration of Mellin-Barnes representations CA, Daleo; Czakon
 - works fine both in Euclidean and physical regions
 - has problems in most loop integrals with internal masses
 - most probably cannot deal with thresholds

None of these two can do $gg \rightarrow h$ at two loops

Loop Singularities


$$\sim \int dx dy \frac{\dots}{x^{1+\epsilon} (M_t^2(x+y) - M_h^2 xy - i\delta)^{1+\epsilon}}$$

- (Overlapping) singularities at the edges of the integration region. Regulated by ϵ

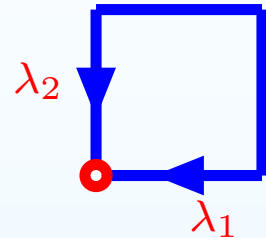
$$x = y = 0$$

- Threshold singularities $\rightsquigarrow i\pi$ terms

$$M_t^2(x+y) = M_h^2 xy$$

Overlapping singularities can be factorized

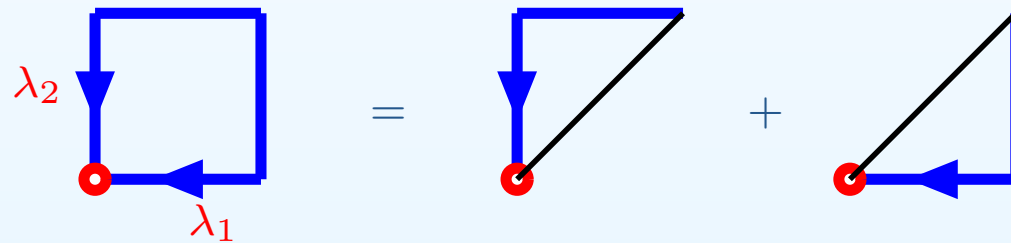
- Singularity when two (or more) variables reach the same corner



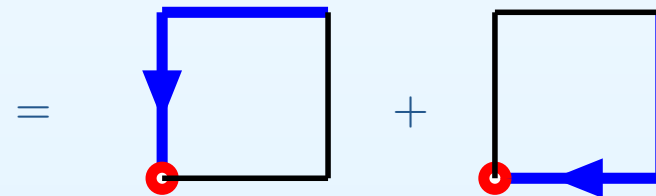
$$: \frac{\lambda_1^\epsilon \lambda_2^\epsilon}{(\lambda_1 + \lambda_2)^2} f(\lambda_1, \lambda_2)$$

- Split into sectors

Binoth, Heinrich; Denner, Roth; Hepp

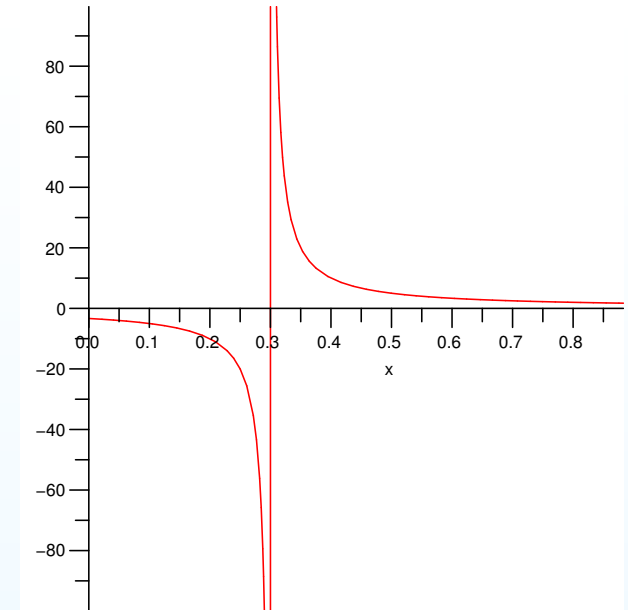


- map each sector to $[0, 1]$



$$= \int_0^1 d\lambda_1 d\lambda_2 \frac{1}{\lambda_1^{-1+\epsilon}} \frac{f(\lambda_1, \lambda_2 \lambda_1)}{(1 + \lambda_2)^2} + \int_0^1 d\lambda_1 d\lambda_2 \frac{1}{\lambda_2^{-1+\epsilon}} \frac{f(\lambda_1 \lambda_2, \lambda_2)}{(1 + \lambda_1)^2}$$

Threshold singularities



- Singular inside the integration region; not the edges

$$I = \int_0^1 dx \frac{1}{x - a - i0},$$

- Regulator $i0$ is not good enough for a numerical evaluation.
- Choose a different contour $C : z = x - i\lambda x(1 - x)$

$$\begin{aligned} I &= \int_C dz \frac{1}{z - a} = \int_0^1 dx \frac{\partial z}{\partial x} \frac{1}{z - a} \\ &= \int_0^1 dx \left[1 + i\lambda \left(1 - \frac{x}{2} \right) \right] \frac{1}{x - a - i\lambda x(1 - x)} \end{aligned}$$

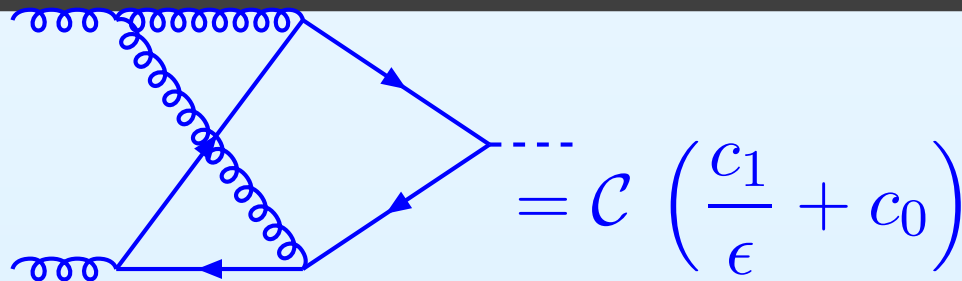
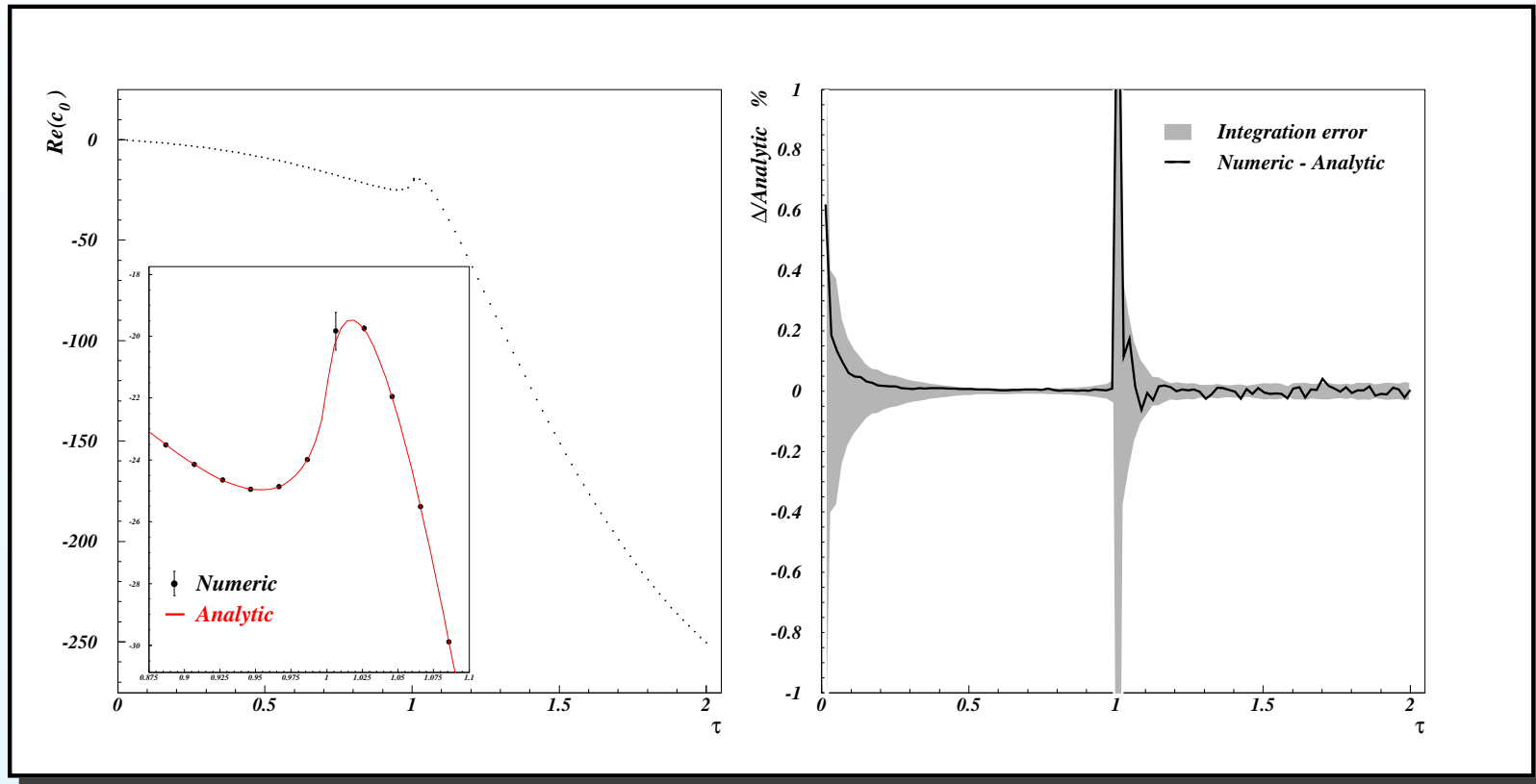
- Suitable for numerical integration!

General multi-loop integration method

- Merge the sector decomposition algorithm with an algorithm proposed by **Nagy and Soper** to deform the contour automatically for Feynman parameters
- Very general method introduced by two groups:
 - **Lazopoulos, Melnikov, Petriello** to compute $pp \rightarrow ZZZ$ at NLO
 - **CA, Beerli, Daleo** for the two-loop SUSY QCD amplitude, re-computing numerically all diagrams with (initially) only quarks or one squark.

SUSY QCD corrections to $gg \rightarrow h$

whole amplitude, including gluinos and squark-mixing, with similar precision

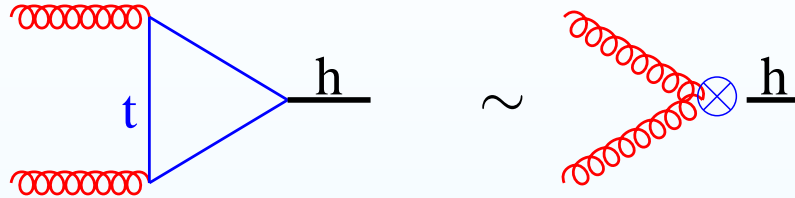


Status of the calculation

- Have computed all two-loop diagrams with quarks, squarks (and squark-mixing), gluinos.
- Renormalization + checked the infrared poles
- Performed a consistency check with our separate analytic calculation in the $m_h \rightarrow 0$ limit.
- We are checking against the computation of the Wilson coefficient of Harlander and Steinhauser
- Re-computed the real radiation $gg \rightarrow hg, \dots$ amplitudes
- Finishing checks on the two-loop amplitude
- Writing the NLO Monte-Carlo program. Results soon (sorry!)

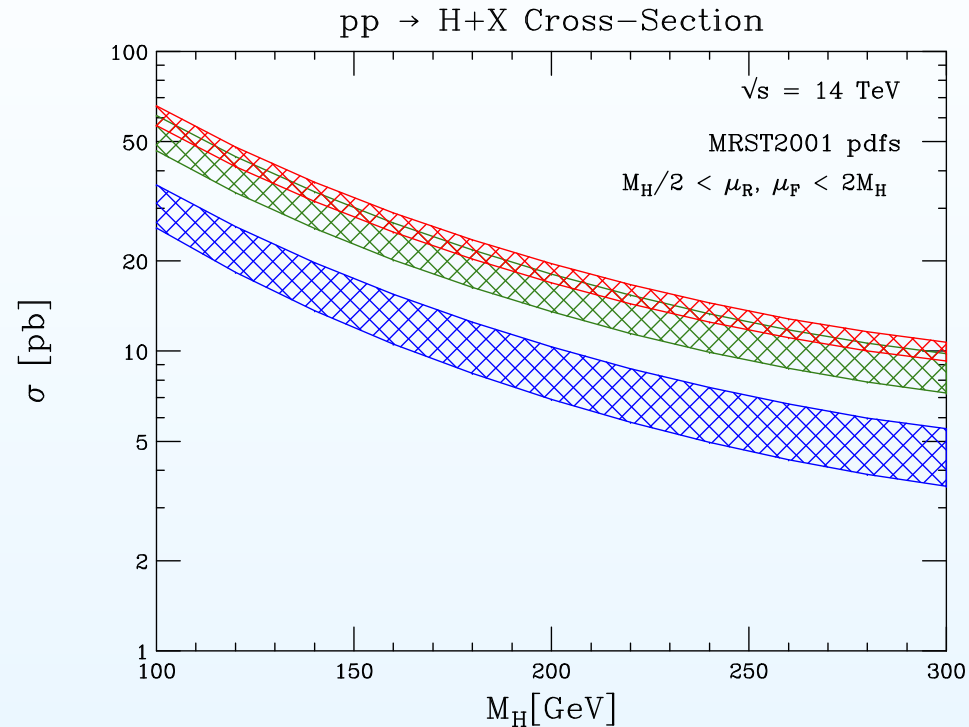
NNLO computation for SM $gg \rightarrow H \rightarrow WW \rightarrow l^+l^-\nu\nu$

Heavy top-quark approximation



- A very good approximation for a light Higgs boson
- Simplifies QCD corrections at NNLO (3 \rightarrow 2 loops).
- NNLO effective theory **Chetyrkin, Kniehl, Steinhauser**

Higgs boson total cross-section through NNLO



Harlander, Kilgore; CA, Melnikov; Ravindran, Smith, van Neerven

- Slowly **converging** perturbative series: large NLO (70%) and smaller NNLO (30%) corrections,
- Scale variation ($\sim 15\%$ at NNLO)

Effect of experimental cuts

- NNLO for fully differential cross-sections are not trivial
- $pp \rightarrow h, pp \rightarrow h \rightarrow \gamma\gamma$: First such computations for a hadron collider process
CA, Melnikov, Petriello
- Extended the NNLO calculation to $pp \rightarrow htoWW \rightarrow ll\nu\nu$
CA, Dissertori, Stöckli
- For $m_h \sim 160 - 180\text{GeV}$ almost exclusive decay to Ws .
- No narrow peak reconstruction; large backgrounds from top and W pairs.
- Aggressive cuts (jet-veto, large missing energy, small lepton angle, restricted lepton p_t) to isolate a signal.
- What is the cross-section after cuts?

Accepted cross-section

- Loose preselection cuts

$\sigma(\text{fb})$	LO	NLO	NNLO
$\mu = \frac{m_h}{2}$	71.63 ± 0.07	126.95 ± 0.13	140.73 ± 0.45

$M_{ll} < 80\text{GeV}, p_t^l > 20\text{GeV}, |\eta^l| < 2, \Delta\phi < 135^\circ, ; E_t^{\text{miss}} > 20\text{GeV}$

- Signal selection cuts

$\sigma(\text{fb})$	LO	NLO	NNLO
$\mu = \frac{m_h}{2}$	21.002 ± 0.021	22.47 ± 0.11	18.45 ± 0.54
$\mu = 2m_h$	14.529 ± 0.014	19.50 ± 0.10	19.01 ± 0.27

$12\text{GeV} < M_{ll} < 40\text{GeV}, p_t^l > 25\text{GeV}, 30\text{GeV} < p_t^{l,\text{max}} < 55\text{GeV}, |\eta^l| < 2, \Delta\phi < 45^\circ, ; E_t^{\text{miss}} > 50\text{GeV}, ; \text{isolation}, p_t^{\text{jet}} < 25\text{GeV}$

Conclusions

- Two-loop amplitude for $gg \rightarrow h$ in SUSY QCD:
 - Complete analytic and numerical calculation of single quark and squark loops
 - Last checks on the full amplitude including gluino and mixed squark diagrams
- NLO Monte-Carlo is also under completion
- A new numerical method for computing multi-loop divergent integrals with thresholds automatically
- Brief report on the NNLO cross-section for the SM $pp \rightarrow H \rightarrow WW \rightarrow ll\nu\nu$ at the LHC. Dramatic change of K-factors with cuts!