

$\tan(\beta)$ Enhanced Yukawa Couplings for Supersymmetric Higgs Singlets at One-Loop

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Outline

- 1 SUSY Higgs Singlets
- 2 One Loop Singlet Couplings
- 3 Phenomenology
 - mnSSM Results
 - NMSSM Results
- 4 Conclusions

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The Minimal Supersymmetric Standard Model

- Before SUSY breaking, models are defined by their gauge symmetries and **Superpotential**
- The MSSM superpotential contains only the Yukawa couplings and a Higgs mass term μ

$$\mathcal{W}_{\text{MSSM}} = h_l \hat{H}_1^T i\tau_2 \hat{L} \hat{E} + h_d \hat{H}_1^T i\tau_2 \hat{Q} \hat{D} + h_u \hat{Q}^T i\tau_2 \hat{H}_2 \hat{U} - \mu \hat{H}_1^T i\tau_2 \hat{H}_2$$

- μ should naturally be of the order of the Planck scale, but successful electroweak symmetry breaking requires it to be much smaller, of the order M_{SUSY}

Effective μ Parameter

- Introduce a new Higgs field \hat{S} and replace the μ term in the superpotential with

$$\mathcal{W} = \dots + \lambda \hat{S} \hat{H}_1^T i\tau \hat{H}_2$$

- An effective μ term is then generated when \hat{S} develops a VEV v_S

$$\mu = \frac{\lambda v_S}{\sqrt{2}}$$

- The Singlet Higgs \hat{S} does not have tree level couplings to **any** SM fermions or gauge bosons

Breaking the Peccei-Quinn Symmetry

This new superpotential contains a Peccei-Quinn symmetry which must be broken.¹

- NMSSM: add term $+\frac{1}{3}\kappa\hat{S}^3$ to \mathcal{W}
- mnSSM: use non-renormalisable supergravity terms + discrete Z^5 or Z^7 R symmetry (a.k.a. nMSSM, MNSSM)
- UMSSM: additional $U(1)'$ gauge symmetry
- ...

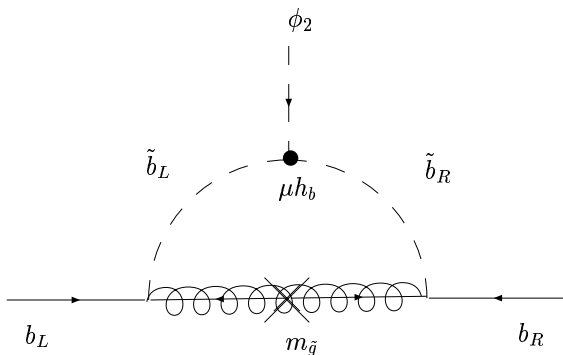
¹See E. Accomando *et al.*, arXiv: hep-ph/0608079 and references within

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Dominant 1-loop Graphs

$\tan \beta$ Enhanced MSSM coupling ²

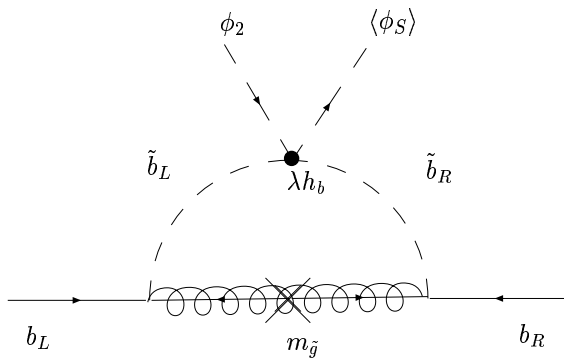


²T. Banks, Nucl. Phys. B **303** (1988) 172;

L.J. Hall, R. Rattazzi and U. Sarid, arXiv: hep-ph/9306309

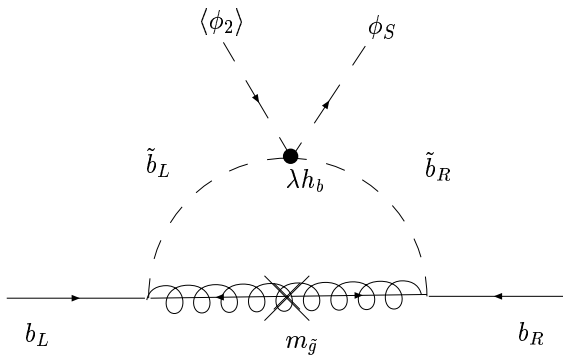
Dominant 1-loop Graphs

$\tan \beta$ enhanced MSSM+S coupling



Dominant 1-loop Graphs

$\tan \beta$ enhanced MSSM+S coupling



$Sb\bar{b}$ Coupling

- This SQCD graph gives the dominant contribution

$$\Delta_b^{\phi_S} \approx \left(\frac{2\alpha_S}{3\pi} \right) \frac{M_3\mu}{|\text{Max}(M_3, M_{\tilde{Q}})|^2} \frac{v_2}{v_S}$$

- Shows expected v/v_S scaling behaviour, though this is broken by subdominant terms
- A similar mechanism gives a coupling to $\tau^+\tau^-$
- This is dominated by a chargino exchange graph, giving a dominant contribution

$$\Delta_\tau^{\phi_S} \approx \left(\frac{\alpha_W}{4\pi} \right) \frac{\mu}{M_2} \frac{v_2}{v_S}$$

Effective Lagrangian

General interaction Lagrangian for down-type quarks and leptons

$$-\mathcal{L}_{\phi\bar{b}b} = \bar{f}_R h_f \left\{ \Phi_1^{0*} + \frac{v_1}{\sqrt{2}} \Delta_f [\Phi_1, \Phi_2, S] \right\} f_L + \text{h.c.}$$

- $\Delta_f [\Phi_1, \Phi_2, S]$ encodes all quantum corrections
- Taking the VEV gives m_f , in terms of which we express the yukawa couplings

$$h_f = \frac{g_w m_f}{\sqrt{2} M_w (1 + \langle \Delta_f \rangle)} \frac{1}{c_\beta}$$

- A Higgs Low-Energy Theorem allows us to calculate the couplings at zero momentum by taking derivatives of Δ_f

Calculating the Couplings- Higgs Low Energy Theorems

- HLET relates correlation functions which differ by the insertion of a zero momentum Higgs boson³

$$\lim_{p_H \rightarrow 0} \Gamma^{HAB}(p_H, p_A, p_B) = \frac{\partial}{\partial V} \Gamma^{AB}(p_A, -p_A)$$

- Can calculate one-loop couplings to fermions as the first derivative (w.r.t. the Higgs field) of the fermion self energy

$$\Delta_f^{\phi_i} = \frac{v c_\beta}{\sqrt{2}} \left\langle \frac{\partial \Delta_f}{\partial \phi_i} \right\rangle$$

³eg. B.A. Kniehl and M. Spira, arXiv: hep-ph/9505225 

Interaction Lagrangian

In terms of the Higgs mass eigenstates,

$$-\mathcal{L}_{\phi\bar{f}f}^{\text{eff}} = \left(\frac{g_w m_f}{\sqrt{2} M_w} \right) \sum_{i=1}^3 g_{H_i f f}^S H_i \bar{f} f + \left(\frac{g_w m_f}{\sqrt{2} M_w} \right) \sum_{j=1}^2 g_{A_j f f}^P A_j (\bar{f} i \gamma^5 f)$$

with

$$g_{H_i f f}^S = \frac{1}{(1 + \langle \Delta_f \rangle)} \left[\frac{O_{1i}^H}{c_\beta} + \Delta_f^{\phi_2} \frac{O_{2i}^H}{c_\beta} + \Delta_f^{\phi_s} \frac{O_{3i}^H}{c_\beta} \right]$$

$$g_{A_j f f}^P = \frac{1}{(1 + \langle \Delta_f \rangle)} \left[- (t_\beta + \Delta_f^{a_2}) O_{1j}^A + \Delta_f^{a_s} \frac{O_{2j}^A}{c_\beta} \right]$$

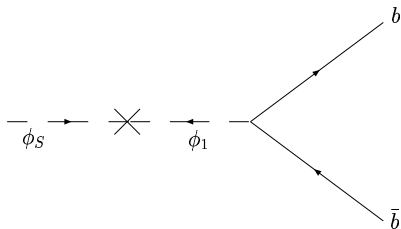
- SM-normalised effective couplings

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Higgs Scalar Mixing

- The one-loop couplings are $\tan \beta$ enhanced
- Can be comparable to SM yukawa couplings
- Tree-level couplings are also enhanced
- Mixing effects through $\phi_1(a_1)$ tend to dominate unless suppressed



General Strategy

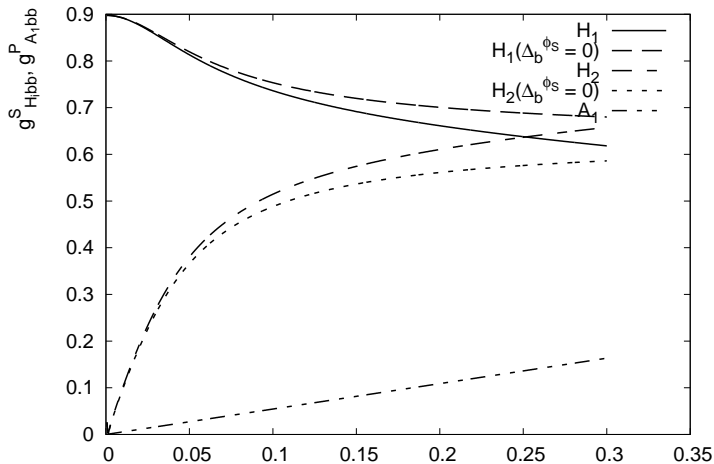
- Difficult to suppress $\phi_1 \leftrightarrow \phi_S$ and $\phi_2 \leftrightarrow \phi_S$ mixing simultaneously
(Mixing proportional to $\lambda \sim (v/v_S)$)
- Mixing effects between the pseudoscalars **can** be easily suppressed
- Concentrate on regions of parameter space where the $A_1 \sim a_S$
- Assume ϕ_1 heavy so that it approximately decouples

Benchmark Parameters

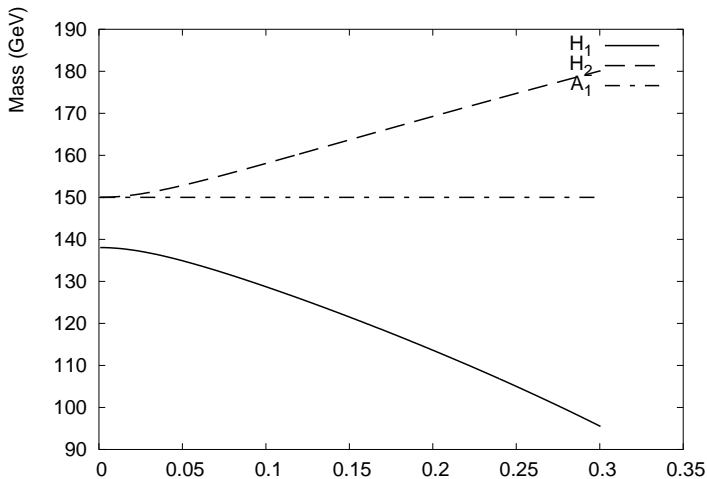
$$\begin{aligned}
 \mu &= 110 \text{ GeV}, & t_\beta &= 50, \\
 M_{\tilde{Q}} &= 300 \text{ GeV}, & M_{\tilde{L}} &= 90 \text{ GeV}, \\
 M_{\tilde{t}} &= 600 \text{ GeV}, & M_{\tilde{b}} &= 110 \text{ GeV}, & M_{\tilde{\tau}} &= 200 \text{ GeV}, \\
 A_t &= 1 \text{ TeV}, & A_b &= 1 \text{ TeV}, & A_\tau &= 1 \text{ TeV}, \\
 M_1 &= 400 \text{ GeV}, & M_2 &= 600 \text{ GeV}, & M_3 &= 400 \text{ GeV} .
 \end{aligned}$$

- Light sparticles in the loops
- S enters through squark mixing, take soft trilinear couplings large
- μ small to avoid v/v_S suppression

Light Higgs Couplings in the mnSSM



Light Higgs Masses in the mnSSM



mnSSM Summary

- Mixing between the scalar bosons rules out this scenario for $\lambda \gtrsim 0.3$
- Singlet contribution suppresses the light H_1 decay rate
- Can provide the dominant decay mechanism for a light singlet pseudoscalar

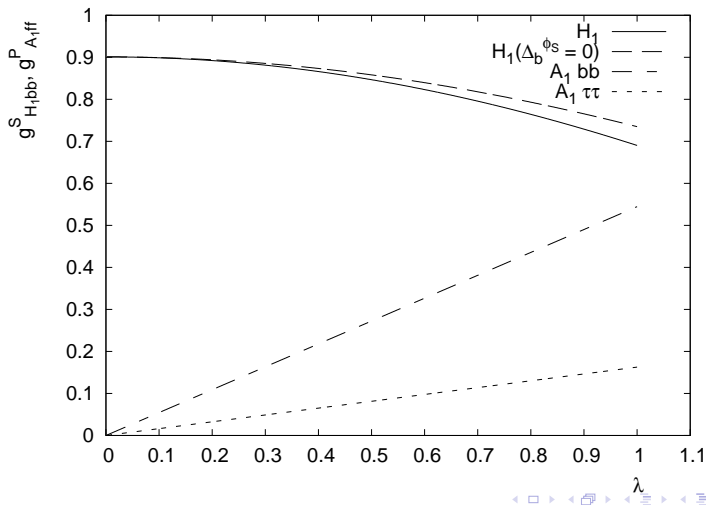
NMSSM mass spectrum

- The NMSSM allows a light pseudoscalar in the spectrum
- This scenario has attracted interest as a low fine-tuning model ⁴
- A light H_1 decays to $A_1 A_1$ pairs
- A_1 is singlet dominated (>98%) for minimum fine tuning

Requires $A_\lambda \sim O(100\text{GeV})$, $A_{\kappa} \sim O(5\text{GeV})$, which can be naturally arranged in gauge/gaugino mediated SUSY breaking.

⁴R. Dermisek and J.F. Gunion, arXiv:hep-ph/0510322

Light Higgs Couplings in the NMSSM



NMSSM summary

- In the minimally fine tuned scenario decays to $b\bar{b}$ are kinematically disallowed
- Loop corrections can provide a significant contribution to the $\tau^+\tau^-$ coupling
- Heavier pseudoscalars $m_{A_1} \sim 10\text{GeV}$ are not excluded if $m_{H_1} > 110\text{GeV}$
- Corrections to the $A_1 \rightarrow b\bar{b}$ coupling can then be comparable to the tree level (mixing) contribution previously considered

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Summary and Outlook

- The one loop singlet couplings to down-type quarks and leptons are $\tan \beta$ enhanced, which compensates for their loop suppression
- Mixing can be small between the pseudoscalars and one loop couplings can dominate a_S decay in some regions of parameter space
- In particular, this effect should be included in studies of the NMSSM with light pseudoscalars
- Analogous singlet contributions to FCNCs may also be significant as there is no tree-level competition