

# Higgs Decays in the Complex MSSM

Karina Williams, in collaboration with Georg Weiglein

University of Durham

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# The complex Minimal Supersymmetric Standard Model

In its general form, the MSSM includes complex parameters such as

- the trilinear coupling  $A$
- the gluino mass parameter  $M_3$
- the higgsino mass parameter  $\mu$

The parameters are often taken to be real for simplicity. However, when the complex phases are included, it leads to some interesting phenomenology

- a new source of CP violation to explain the matter-antimatter asymmetry in the universe
- the possibility of a low mass for the lightest Higgs without conflicting with LEP results

# Analysis of LEP results by LEP Higgs Working Group

Two different programs were used to calculate the cMSSM Higgs sector - *FeynHiggs* and *CPH*. A point in the parameter space was said to be excluded only if the analysis with *both* programs found it excluded.

	<i>CPX</i>	<i>CPX inspired</i>
$\tan \beta$	0.6–40	0.6–17
$m_{H^\pm}(\text{GeV}/c^2)$	4–1000	110–190
$M_{\text{SUSY}}(\text{GeV})$	500	500
$\mu(\text{GeV})$	2000	2000
$M_2(\text{GeV})$	200	200
$\text{Abs}(A)(\text{GeV})$	1000(MS)	1000(on-shell)
$\text{Arg}(A)$	$90^\circ$	$90^\circ$
$\text{Abs}(M_3)(\text{GeV}/c^2)$	1000	1000
$\text{Arg}(M_3)$	$90^\circ$	$0^\circ$
$m_t(\text{GeV})$	174.3	170.9

The LEP Higgs Working Group analysis found a domain in the *CPX* scenario at  $30 \text{ GeV}/c^2 < m_{h_1} < 55 \text{ GeV}/c^2$  which was not excluded at the 95% CL. In this region, the  $h_2 \rightarrow h_1 + h_1$  branching ratio dominates. However, *FeynHiggs* does not currently have a reliable calculation for the decay width,  $\Gamma(h_2 \rightarrow h_1 + h_1)$ , so  $\Gamma(h_2 \rightarrow h_1 + h_1)$  from *CPH* was used in both analyses.

Unless otherwise stated, *CPX inspired* parameters are used in this presentation.

# The neutral Higgs masses in the complex MSSM

First, find the poles of the  $3 \times 3$  propagator matrix  $\mathbf{\Delta}(p^2)$ , which is equivalent to solving  $|p^2 \mathbb{1} - \mathbf{M}(p^2)| = 0$  where

$$\mathbf{M}(p^2) = \begin{pmatrix} m_h^2 - \hat{\Sigma}_{hh}(p^2) & -\hat{\Sigma}_{hH}(p^2) & -\hat{\Sigma}_{hA}(p^2) \\ -\hat{\Sigma}_{hH}(p^2) & m_H^2 - \hat{\Sigma}_{HH}(p^2) & -\hat{\Sigma}_{HA}(p^2) \\ -\hat{\Sigma}_{hA}(p^2) & -\hat{\Sigma}_{HA}(p^2) & m_A^2 - \hat{\Sigma}_{AA}(p^2) \end{pmatrix}$$

In general, the three solutions  $\mathcal{M}_{h_a}^2$  are complex. The physical masses,  $M_{h_a}^2 = \text{Re}\mathcal{M}_{h_a}^2$  and labelled by  $M_{h_1} \leq M_{h_2} \leq M_{h_3}$   $\hat{\Sigma}_{jk}(p^2)$  were calculated using an expansion about  $\text{Re}p^2$ .

$$\hat{\Sigma}_{jk}(p^2) = \hat{\Sigma}_{jk}(\text{Re}p^2) + i (\text{Im}p^2) \hat{\Sigma}'_{jk}(\text{Re}p^2) + \mathcal{O}(\text{Im}p^2)^2$$

The program *FeynHiggs* was used for  $\hat{\Sigma}_{jk}(\text{Re}p^2)$  and  $\hat{\Sigma}'_{jk}(\text{Re}p^2)$ . In practice, the eigenvalues of a momentum independent approximation to  $\mathbf{M}(p^2)$  was used as a starting point for iteration.

# External Higgs Bosons

Diagrams with external Higgs bosons need finite wave function renormalisation factors, contained in the  $3 \times 3$  matrix  $\hat{\mathbf{Z}}$ .

$$\lim_{p^2 \rightarrow \mathcal{M}_{h_1}^2} -\frac{i}{p^2 - \mathcal{M}_{h_1}^2} \left( \hat{\mathbf{Z}} \cdot \hat{\mathbf{r}}_2 \cdot \hat{\mathbf{Z}}^T \right)_{hh} = 1$$

$$\lim_{p^2 \rightarrow \mathcal{M}_{h_2}^2} -\frac{i}{p^2 - \mathcal{M}_{h_2}^2} \left( \hat{\mathbf{Z}} \cdot \hat{\mathbf{r}}_2 \cdot \hat{\mathbf{Z}}^T \right)_{HH} = 1$$

$$\lim_{p^2 \rightarrow \mathcal{M}_{h_3}^2} -\frac{i}{p^2 - \mathcal{M}_{h_3}^2} \left( \hat{\mathbf{Z}} \cdot \hat{\mathbf{r}}_2 \cdot \hat{\mathbf{Z}}^T \right)_{AA} = 1$$

with

$$\hat{\mathbf{Z}} = \begin{pmatrix} \sqrt{Z_h} & \sqrt{Z_h} Z_{hH} & \sqrt{Z_h} Z_{hA} \\ \sqrt{Z_H} Z_{Hh} & \sqrt{Z_H} & \sqrt{Z_H} Z_{HA} \\ \sqrt{Z_A} Z_{Ah} & \sqrt{Z_A} Z_{AH} & \sqrt{Z_A} \end{pmatrix}$$

$-\hat{\mathbf{r}}_2(p^2)$  is the inverse of the propagator matrix  $\mathbf{\Delta}(p^2)$ .

# External Higgs Bosons

The components of  $\hat{\mathbf{Z}}$  are found using,

$$Z_h^{-1} = \left. \frac{\partial}{\partial p^2} \left( \frac{i}{\Delta_{hh}(p^2)} \right) \right|_{p^2 = \mathcal{M}_{h_1}^2}$$

note

$$Z_H^{-1} = \left. \frac{\partial}{\partial p^2} \left( \frac{i}{\Delta_{HH}(p^2)} \right) \right|_{p^2 = \mathcal{M}_{h_2}^2}$$

$$\Delta_{ii}(p^2) = \frac{i}{p^2 - m_i^2 + \hat{\Sigma}_{ii}^{\text{eff}}(p^2)}$$

$$Z_A^{-1} = \left. \frac{\partial}{\partial p^2} \left( \frac{i}{\Delta_{AA}(p^2)} \right) \right|_{p^2 = \mathcal{M}_{h_3}^2}$$

$$Z_{hH} = \left. \frac{\Delta_{hH}}{\Delta_{hh}} \right|_{p^2 = \mathcal{M}_{h_1}^2}$$

$$Z_{Hh} = \left. \frac{\Delta_{Hh}}{\Delta_{HH}} \right|_{p^2 = \mathcal{M}_{h_2}^2}$$

$$Z_{Ah} = \left. \frac{\Delta_{hA}}{\Delta_{AA}} \right|_{p^2 = \mathcal{M}_{h_3}^2}$$

$$Z_{hA} = \left. \frac{\Delta_{hA}}{\Delta_{hh}} \right|_{p^2 = \mathcal{M}_{h_1}^2}$$

$$Z_{HA} = \left. \frac{\Delta_{HA}}{\Delta_{HH}} \right|_{p^2 = \mathcal{M}_{h_2}^2}$$

$$Z_{AH} = \left. \frac{\Delta_{HA}}{\Delta_{AA}} \right|_{p^2 = \mathcal{M}_{h_3}^2}$$

where  $\Delta_{ij}$  are components of the  $3 \times 3$  propagator matrix  $\mathbf{\Delta}(p^2)$ .

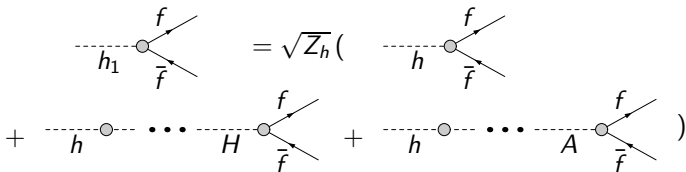
# External Higgs Bosons

For a vertex function involving 1,2,3 external Higgs  $\hat{\Gamma}_{h_a}, \hat{\Gamma}_{h_a h_b}, \hat{\Gamma}_{h_a h_b h_c}$  respectively,

$$\begin{aligned}\hat{\Gamma}_{h_a} &= \hat{\mathbf{Z}}_{ai} \hat{\Gamma}_i \\ \hat{\Gamma}_{h_a h_b} &= \hat{\mathbf{Z}}_{bj} \hat{\mathbf{Z}}_{ai} \hat{\Gamma}_{ij} \\ \hat{\Gamma}_{h_a h_b h_c} &= \hat{\mathbf{Z}}_{ck} \hat{\mathbf{Z}}_{bj} \hat{\mathbf{Z}}_{ai} \hat{\Gamma}_{ijk}\end{aligned}$$

For example,

$$\hat{\Gamma}_{h_1 f \bar{f}} = \sqrt{Z_h} \left( \hat{\Gamma}_{h f \bar{f}} + Z_{hH} \hat{\Gamma}_{H f \bar{f}} + Z_{hA} \hat{\Gamma}_{A f \bar{f}} \right)$$



## Internal Higgs Bosons

For an effective coupling involving internal Higgs bosons, can use the  $3 \times 3$  unitary rotation matrix  $\mathbf{U}$ , which diagonalises a real, momentum independent approximation to  $\mathbf{M}$  where

$$\begin{aligned}\hat{\Sigma}_{kk}(p^2) &\rightarrow \text{Re} \left[ \hat{\Sigma}_{kk}(m_k^2) \right] \\ \hat{\Sigma}_{jk}(p^2) &\rightarrow \text{Re} \left[ \hat{\Sigma}_{jk} \left( \frac{1}{2}(m_j^2 + m_k^2) \right) \right]\end{aligned}$$

so that  $\mathbf{U}$  diagonalises  $\mathbf{M}_U$

$$\begin{pmatrix} M_{h_1,U}^2 & 0 & 0 \\ 0 & M_{h_2,U}^2 & 0 \\ 0 & 0 & M_{h_3,U}^2 \end{pmatrix} = \mathbf{U} \cdot \mathbf{M}_U \cdot \mathbf{U}^\dagger$$

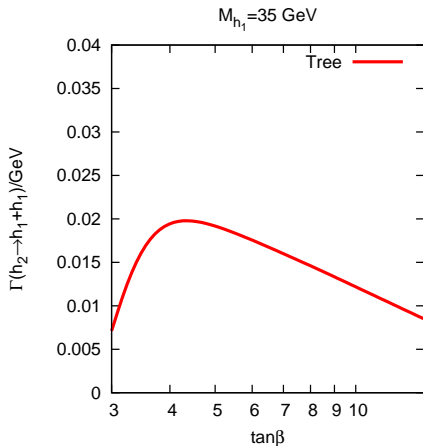
For example, the  $h_a$ -Z-Z coupling is given by a combination of  $g_{hZZ}$ ,  $g_{HZZ}$ ,  $g_{AZZ}$  using

$$g_{h_a ZZ} = \mathbf{U}_{ak} g_{kZZ}$$

which gives  $g_{h_1 ZZ}^2 + g_{h_2 ZZ}^2 + g_{h_3 ZZ}^2 = 1$  as required.



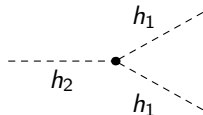
# $h_2 \rightarrow h_1 + h_1$ Decay Width



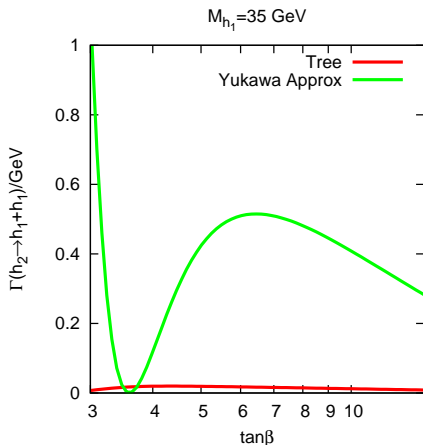
## Tree level vertex

- Finite wave function renormalisation factors are included by

$$\Gamma_{h_2 h_1 h_1} = \hat{Z}_{1k} \hat{Z}_{1j} \hat{Z}_{2i} \Gamma_{ijk}^{\text{tree}}$$

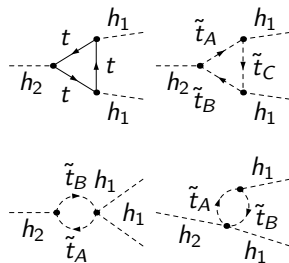


# $h_2 \rightarrow h_1 + h_1$ Decay Width



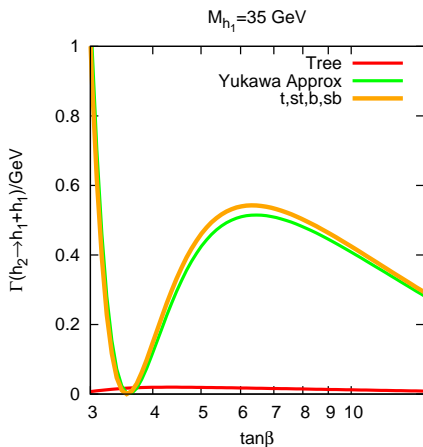
## Yukawa approximation in vertex

- $m_t^4$  terms only
- zero incoming momentum:  
 $p^2 = 0$



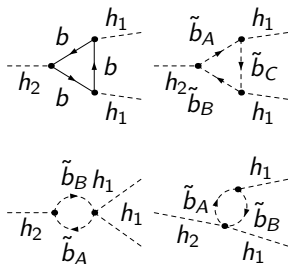
where  $\tilde{t}_A, \tilde{t}_B, \tilde{t}_C = \tilde{t}_1, \tilde{t}_2$ .

# $h_2 \rightarrow h_1 + h_1$ Decay Width



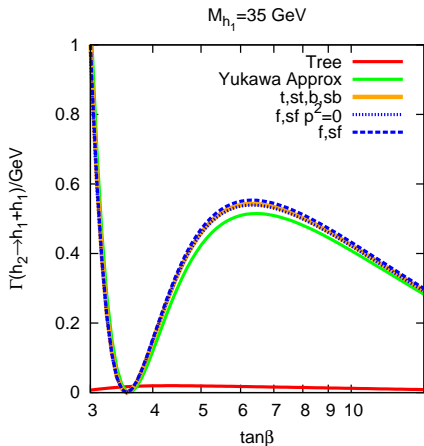
$t, \tilde{t}, b, \tilde{b}$

- loops involving  $t, \tilde{t}, b, \tilde{b}$  only
- full momentum dependence



with  $\tilde{b}_A, \tilde{b}_B, \tilde{b}_C = \tilde{b}_1, \tilde{b}_2$  and  $t, \tilde{t}$  diagrams as before.

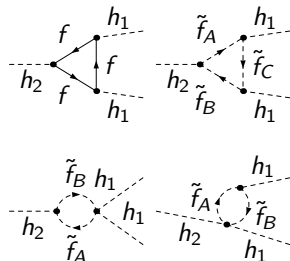
# $h_2 \rightarrow h_1 + h_1$ Decay Width



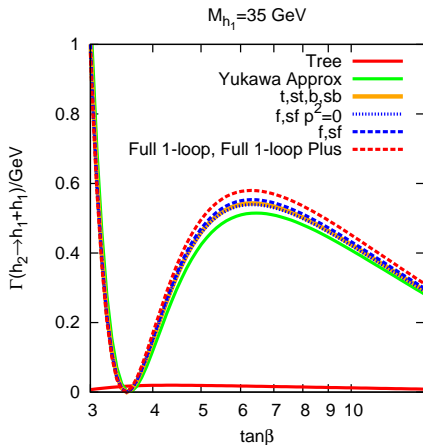
## Fermions, Sfermions

Standard model fermions and their superpartners. Two options

- $p^2 = 0$
- full momentum dependence



# $h_2 \rightarrow h_1 + h_1$ Decay Width

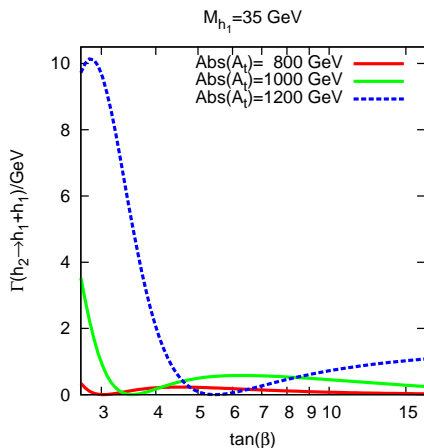


## Full 1-loop and Full 1-loop Plus

- Both options include full 1-loop corrections.
- Full 1-loop Plus has  $h_1, h_2, h_3$  inside loops instead of  $h, H, A$ . Transformations with  $\mathbf{U}$  are used to obtain the new couplings. Negligible difference to full 1-loop case.



# $\Gamma(h_2 \rightarrow h_1 + h_1)$ - varying $\text{Abs}(A_t)$



- $\Gamma(h_2 \rightarrow h_1 + h_1)$  is strongly dependent on  $\text{Abs}(A_t)$ .
- Will be particularly relevant for transformations of parameters between on-shell and  $\overline{\text{DR}}$  scheme.

## Other Ingredients

$\text{Br}(h_a \rightarrow h_b h_c)$ ,  $\text{Br}(h_a \rightarrow b\bar{b})$ ,  $\text{Br}(h_a \rightarrow \tau^+ \tau^-)$  are needed when checking parameter points against the LEP exclusions, so two other decay widths were calculated explicitly:

$\Gamma(h_a \rightarrow b\bar{b})$ , including

- finite wave renormalisation factors in  $\hat{\mathbf{Z}}$
- SM QCD corrections
- Susy QCD corrections - resummation includes full  $M_3$  phase dependence
- full 1-loop vertex corrections (with the option of  $h_1, h_2, h_3$  in loops)
- QED corrections

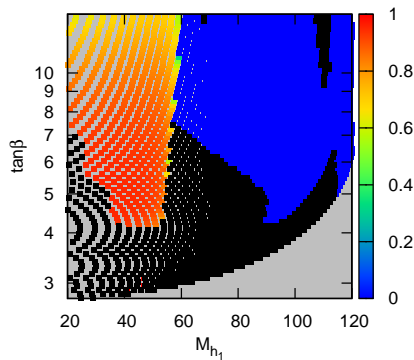
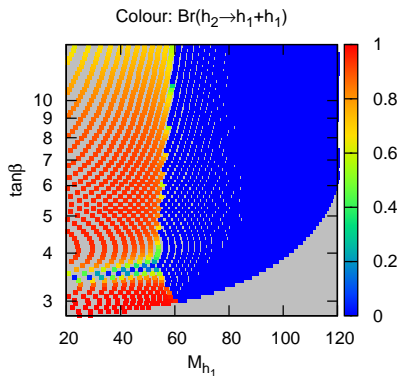
$\Gamma(h_a \rightarrow \tau^+ \tau^-)$ , including

- finite wave renormalisation factors in  $\hat{\mathbf{Z}}$
- full 1-loop vertex corrections (with the option of  $h_1, h_2, h_3$  in loops)
- QED corrections

Contribution of other neutral Higgs decay channels are taken from *FeynHiggs*



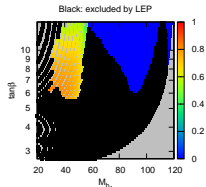
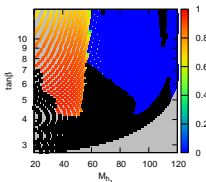
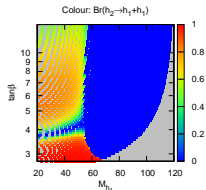
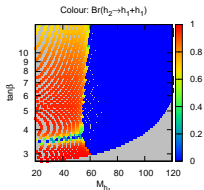
# LEP exclusions for the *CPX inspired* scenario from processes involving $h_1, h_2$



# Comparison with the program *CPsuperH*

new results (with current *FH*)

*CPsuperH*



Conversion between on-shell and  $\overline{\text{MS}}$  schemes as in hep-ph/0001002.

# Summary

- Presented new results for  $h_a \rightarrow h_b + h_c$  decay width, which include 1-loop vertex corrections.
- Concentrated on the example of  $\Gamma(h_2 \rightarrow h_1 + h_1)$  in the *CPX inspired* scenario, showed these new corrections can increase the decay width by factor of 50.
- Compared to results from momentum independent vertex approximations, which can be used for 'effective'  $h_a - h_b - h_c$  couplings, which could be very useful for probing the trilinear neutral Higgs interactions. These approximations proved very successful.
- Looked at the implications of these new corrections to constraints on the mass of the lightest Higgs mass  $M_{h_1}$  in the *CPX inspired* scenario. The results confirm the existence of a 'hole' in the LEP coverage at low  $M_{h_1} \sim 40$  and  $\tan\beta \sim 5$ .

# The End