

PDFs and Low  $x$  at LHeC  
Oxford, March 20th 2017

# Status of nPDF studies

Néstor Armesto

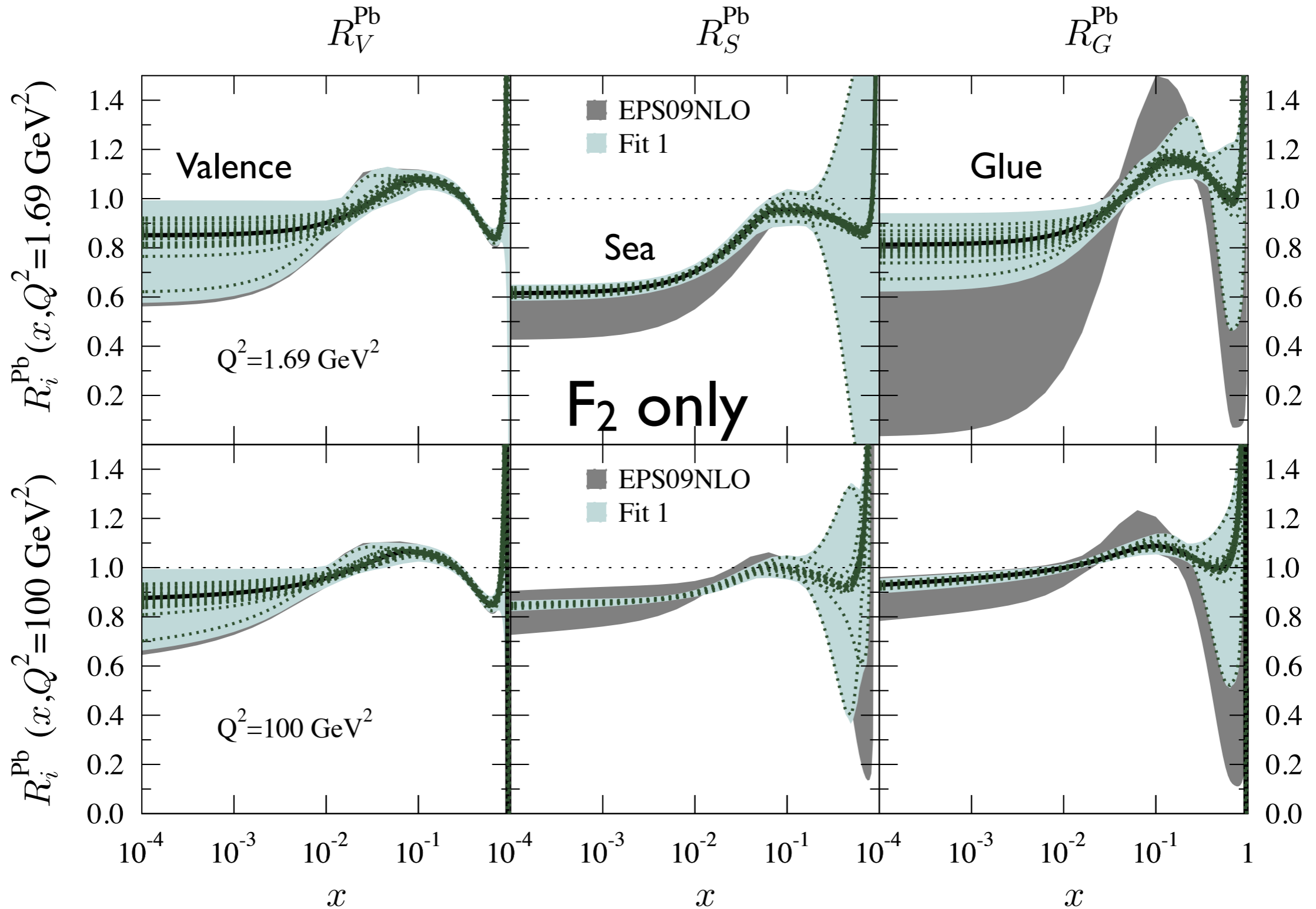
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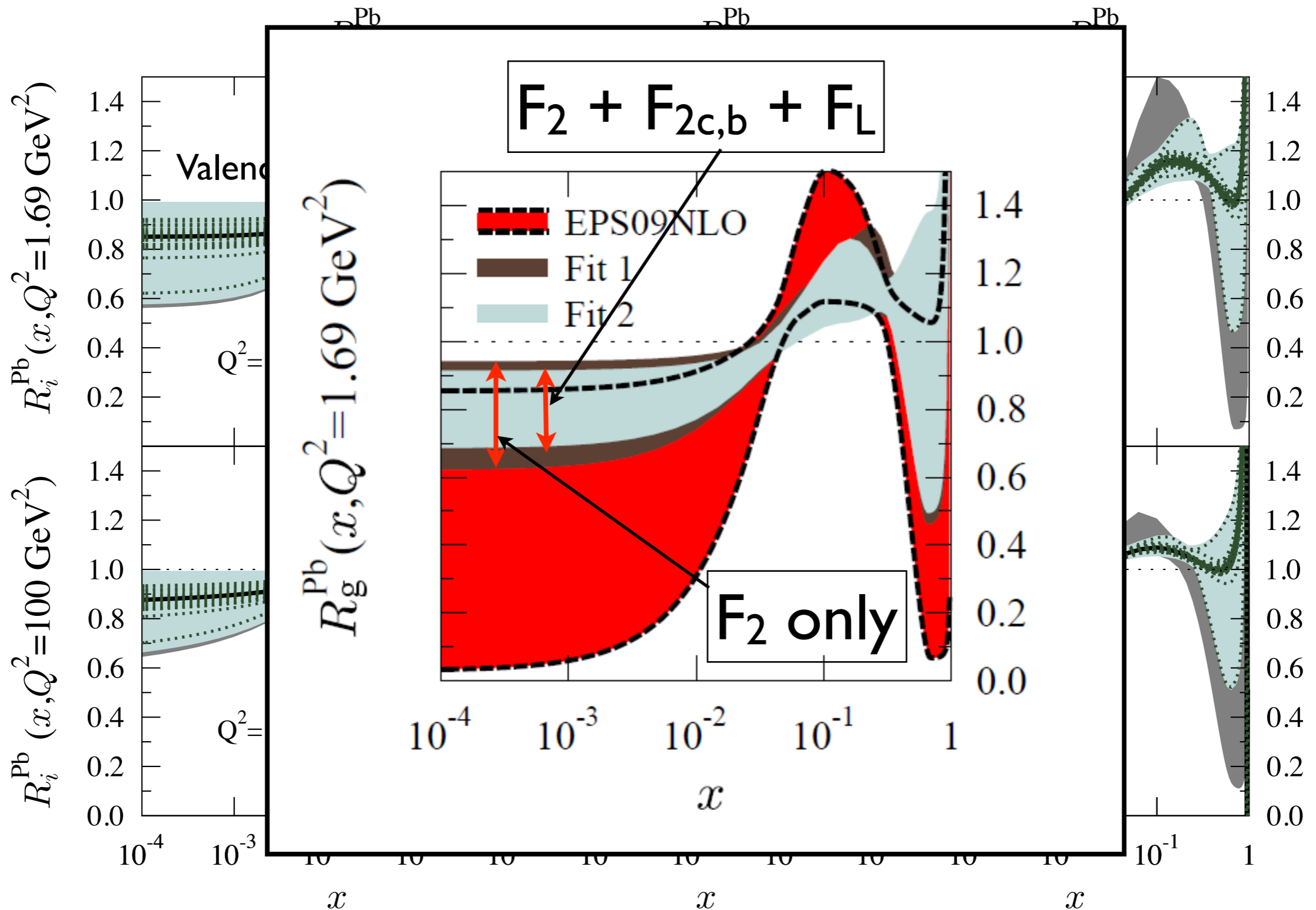
for the LHeC/FCC-eh Study Group

- $F_2$  data substantially reduce the uncertainties in DGLAP analysis; inclusion of charm, beauty (new!); and  $F_L$  (new!) also give constraints.

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## The LHeC & EIC pseudodata

- **Samples of neutral-current DIS pseudodata for reduced cross-sections**

$$\sigma_r = \frac{xQ^4}{2\pi\alpha_{\text{em}}^2 Y_+} \frac{d^2\sigma}{dx dQ^2} \quad Y_+ = 1 + (1-y)^2$$

$$\frac{d^2\sigma}{dx dQ^2} = \frac{4\pi\alpha_{\text{em}}^2}{Q^4} \frac{1}{x} \left[ xy^2 F_1 + (1-y)F_2 \pm xy\left(1 - \frac{y}{2}\right)F_3 \right]$$

was generated from using assuming:

$$\begin{array}{ll} E_{\text{lepton}} = 60 \text{ GeV}, & E_{\text{proton}} = 7000 \text{ GeV}, E_{\text{Pb}} = 2750 \text{ GeV} \\ E_{\text{lepton}} = 20 \text{ GeV}, & E_{\text{proton}} = 7000 \text{ GeV}, E_{\text{Pb}} = 2750 \text{ GeV} \\ E_{\text{lepton}} = 26.9 \text{ GeV}, & E_{\text{proton}} = 7000 \text{ GeV}, E_{\text{Pb}} = 2750 \text{ GeV} \end{array}$$

in the kinematical window:  $10^{-5} < x < 1$  &  $2 < Q^2 < 10^5 \text{ GeV}^2$

- **For comparison, the foreseen EIC capabilities**

$$\begin{array}{lll} E_{\text{lepton}} = 5 \text{ GeV}, & E_{\text{p,Au,Cu}} = 50, 75, 100 \text{ GeV} & \text{(Phase 1)} \\ E_{\text{lepton}} = 20 \text{ GeV}, & E_{\text{p,Au,Cu}} = 50, 75, 100 \text{ GeV} & \text{(Phase 2)} \end{array}$$

in the kinematical window:  $10^{-3} < x < 1$  &  $Q^2 < 500 \text{ GeV}^2$

- **Nuclear effects in cross sections “EPS09 based”**

## Framework of the pQCD analysis

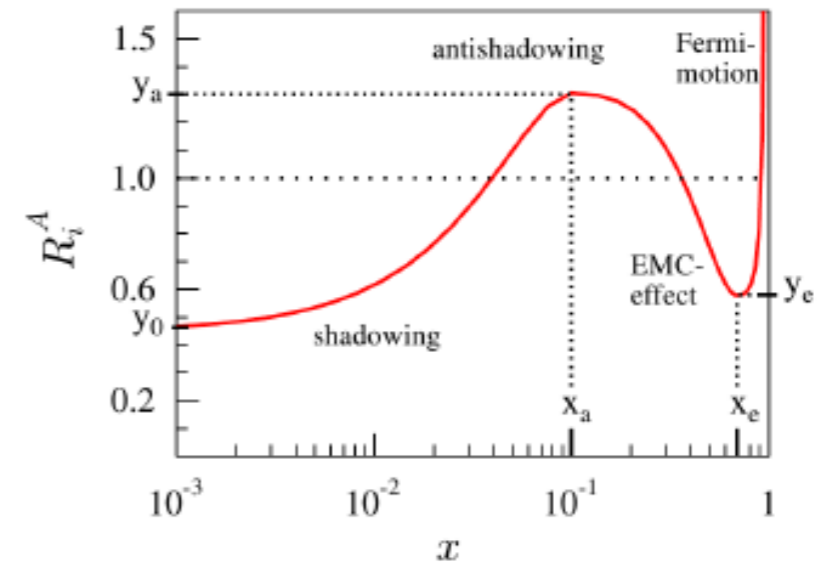
- The cross-sections are computed at NLO with the SACOT prescription for the heavy quark treatment
- Parametrize the nuclear modifications at  $Q=1.3$  GeV, CTEQ6.6 as the baseline

$$f_k^{\text{proton},A}(x, Q^2) = R_k^A(x, Q^2) f_k^{\text{proton}}(x, Q^2)$$

$R_V^A(x, Q_0^2)$  for all valence quarks

$R_S^A(x, Q_0^2)$  for all sea quarks

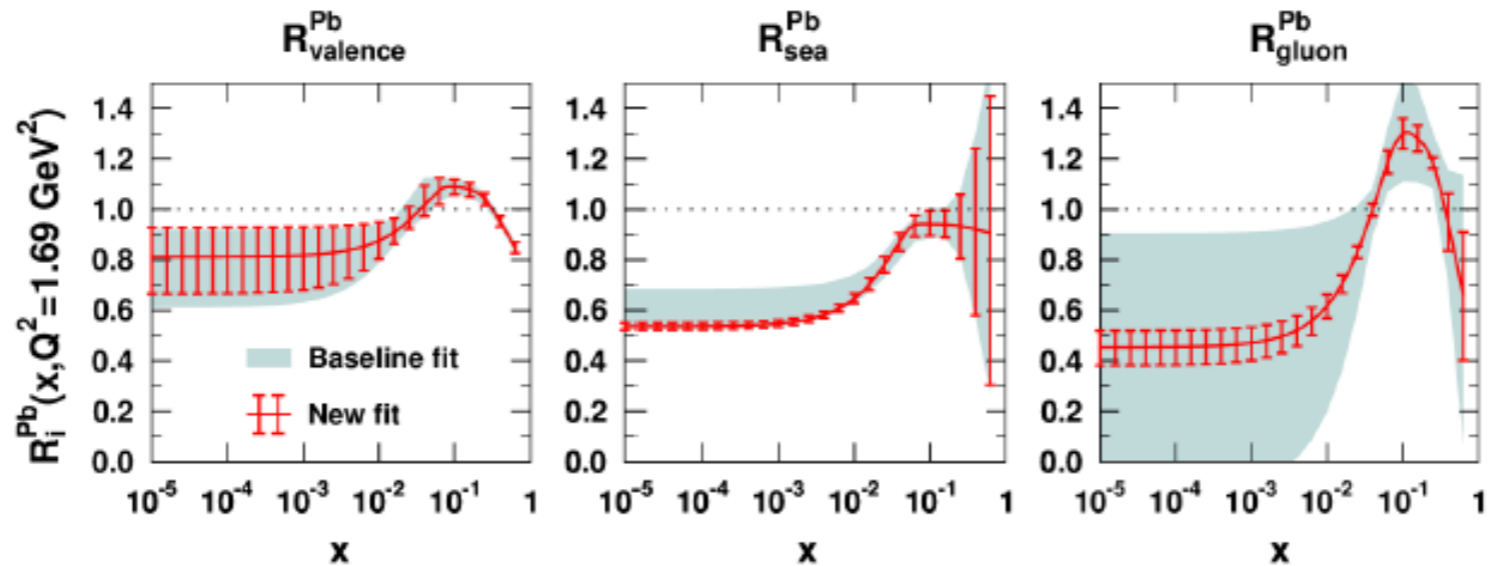
$R_G^A(x, Q_0^2)$  for gluons



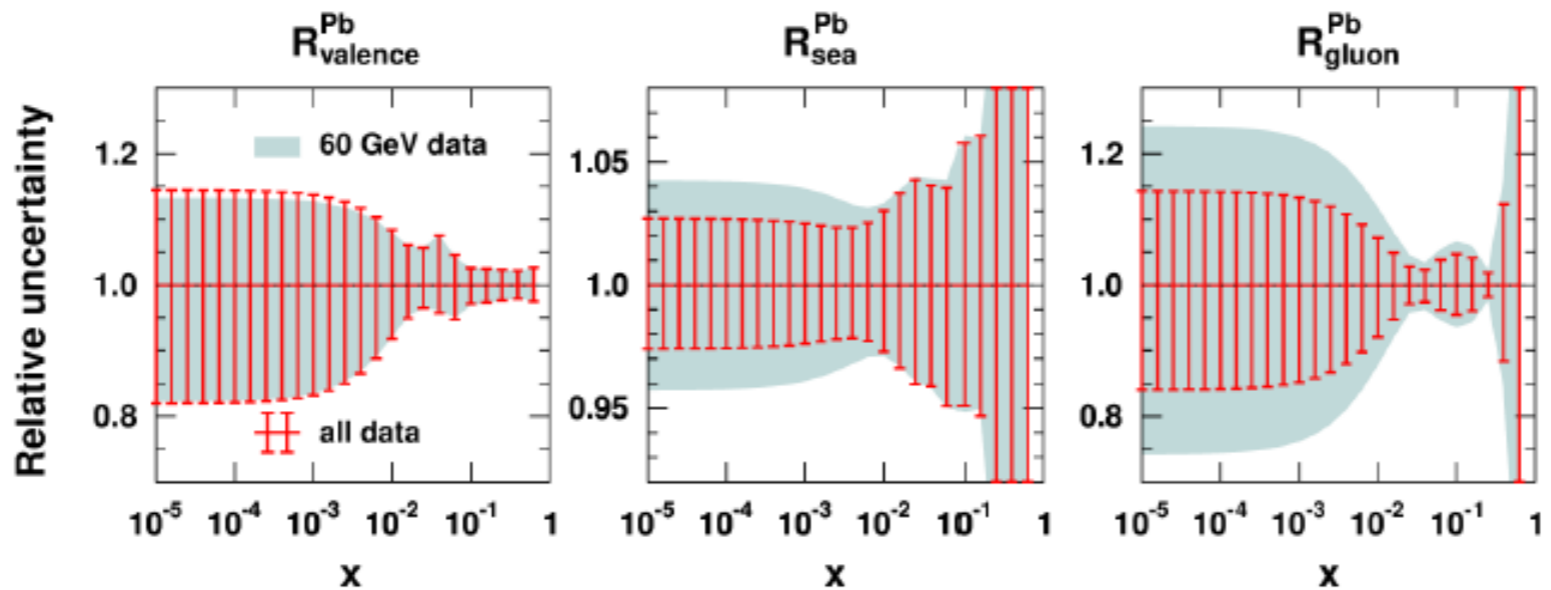
- The LHeC/EIC pseudodata are added on top of all other DIS, Drell-Yan, and inclusive pion data, that were included in EPS09.
- Standard  $\chi^2$ -fit with Hessian error analysis with  $\Delta\chi^2 = 25$

## Inclusion of the low-energy data

- Include also the data from the  $E_{\text{lepton}} = 20\text{GeV}$  and  $E_{\text{lepton}} = 26.9\text{GeV}$  runs



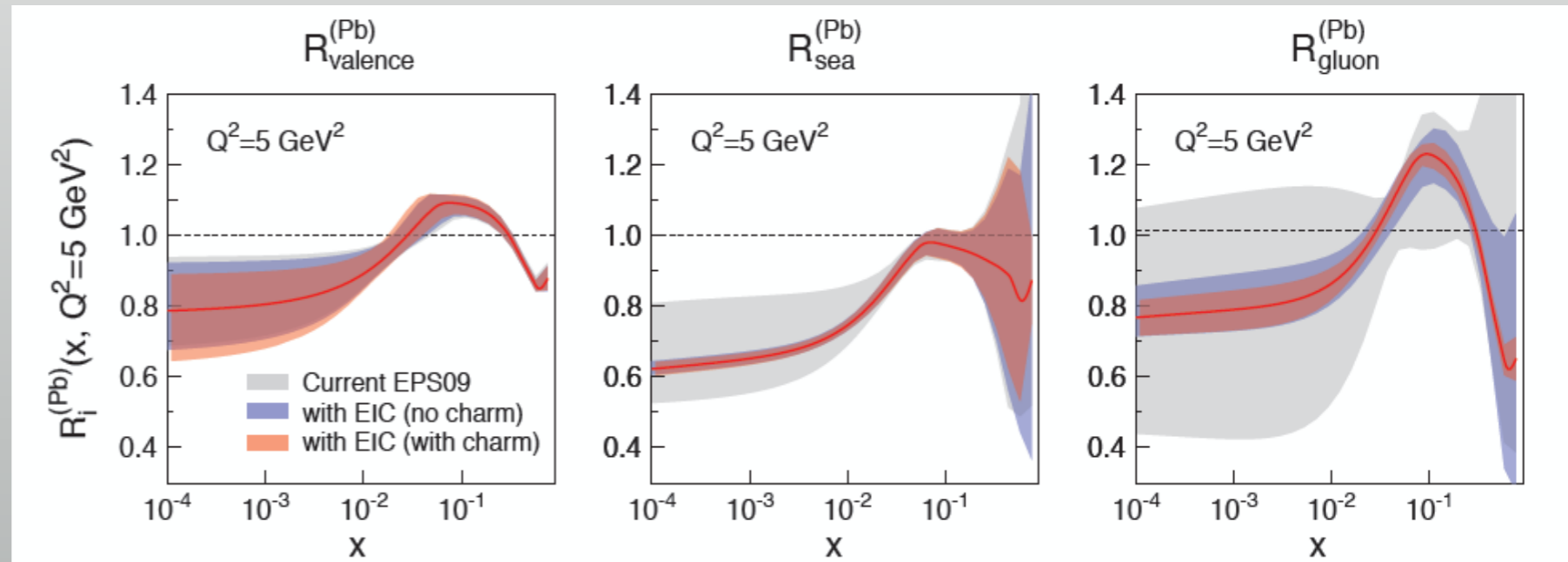
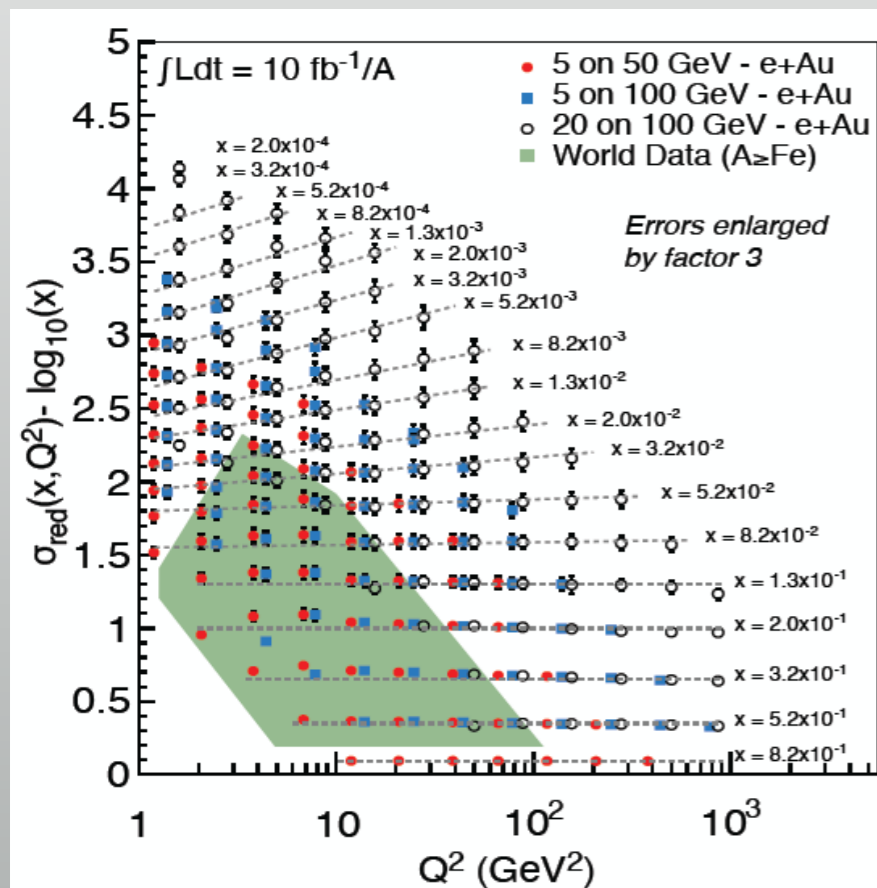
- Relative uncertainties compared to the case with  $E_{\text{lepton}} = 60\text{GeV}$  data only



- Even larger reduction in the small-x uncertainties – though not dramatic

# Parametrisation bias:

- Sensitivity to the mathematical form of the initial conditions is a well-known issue in proton PDFs: NNPDF, PDF4LHC recommendation of comparing different sets, HERAPDF2.0 studies, ...
- In our case: determination of nPDFs beyond (pseudo)data...



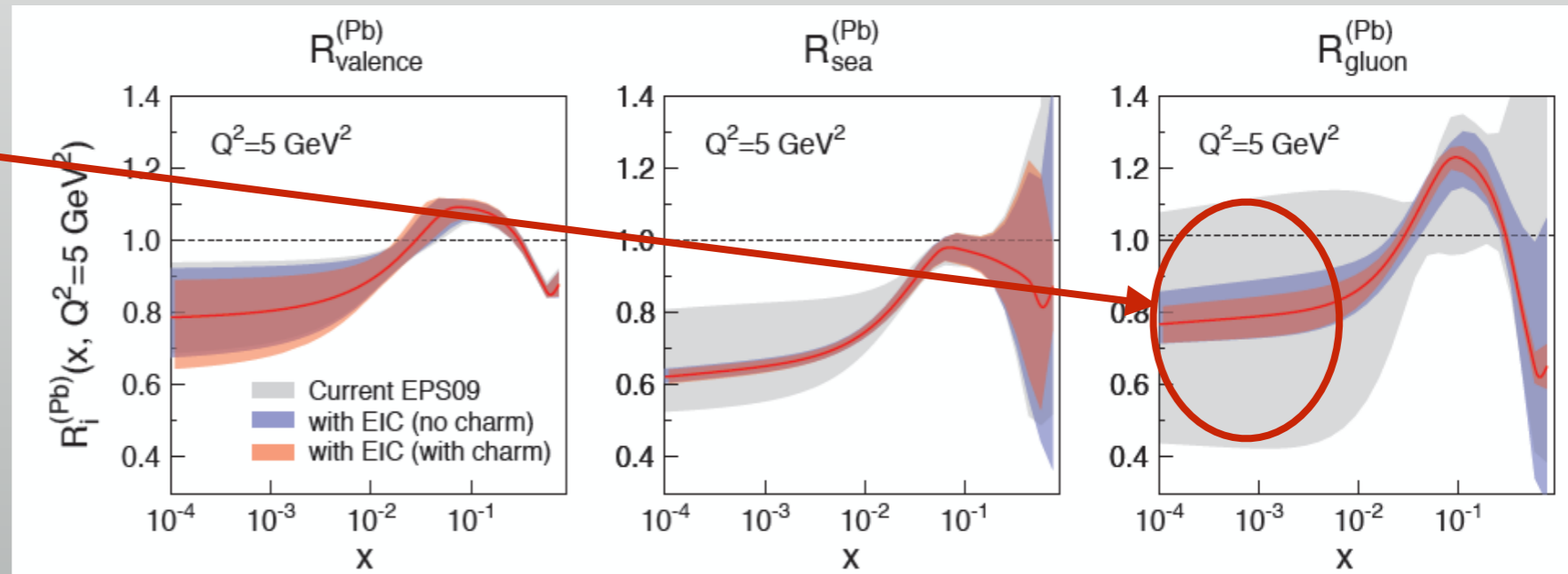
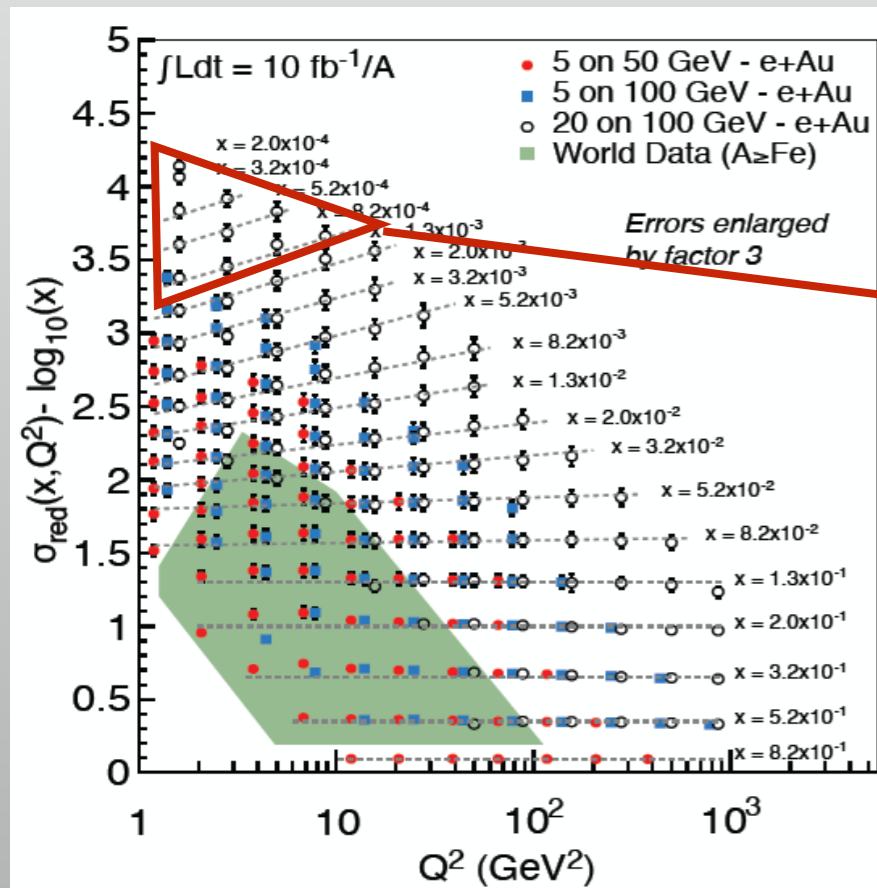
EIC example



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How?: mainly dictated by the shape of ICs



EIC example

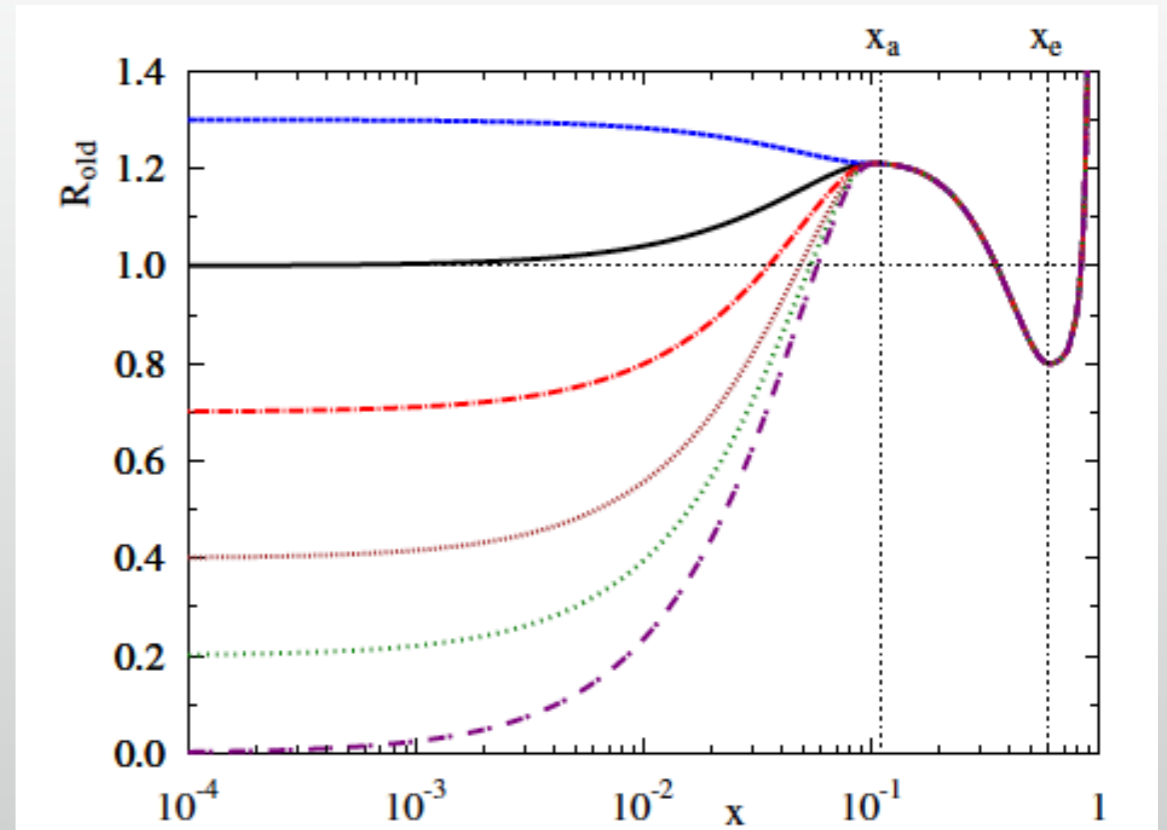
$$\frac{\partial R_{F_2}^A(x, Q^2)}{\partial \log Q^2} \approx \frac{10\alpha_s}{27\pi} \frac{xg(2x, Q^2)}{\frac{1}{2}F_2^D(x, Q^2)} \left\{ R_g^A(2x, Q^2) - R_{F_2}^A(x, Q^2) \right\}$$

hep-ph/0201256

# Parametrisation bias:

- An idea to deal with it in the EPS09 framework:

$$R_{\text{old}}(x) = \begin{cases} a_0 + (a_1 + a_2x)(e^{-x} - e^{-x_a}) & x \leq x_a \\ b_0 + b_1x + b_2x^2 + b_3x^3 & x_a \leq x \leq x_e \\ c_0 + (c_1 - c_2x)(1-x)^{-\beta} & x_e \leq x \leq 1, \end{cases}$$



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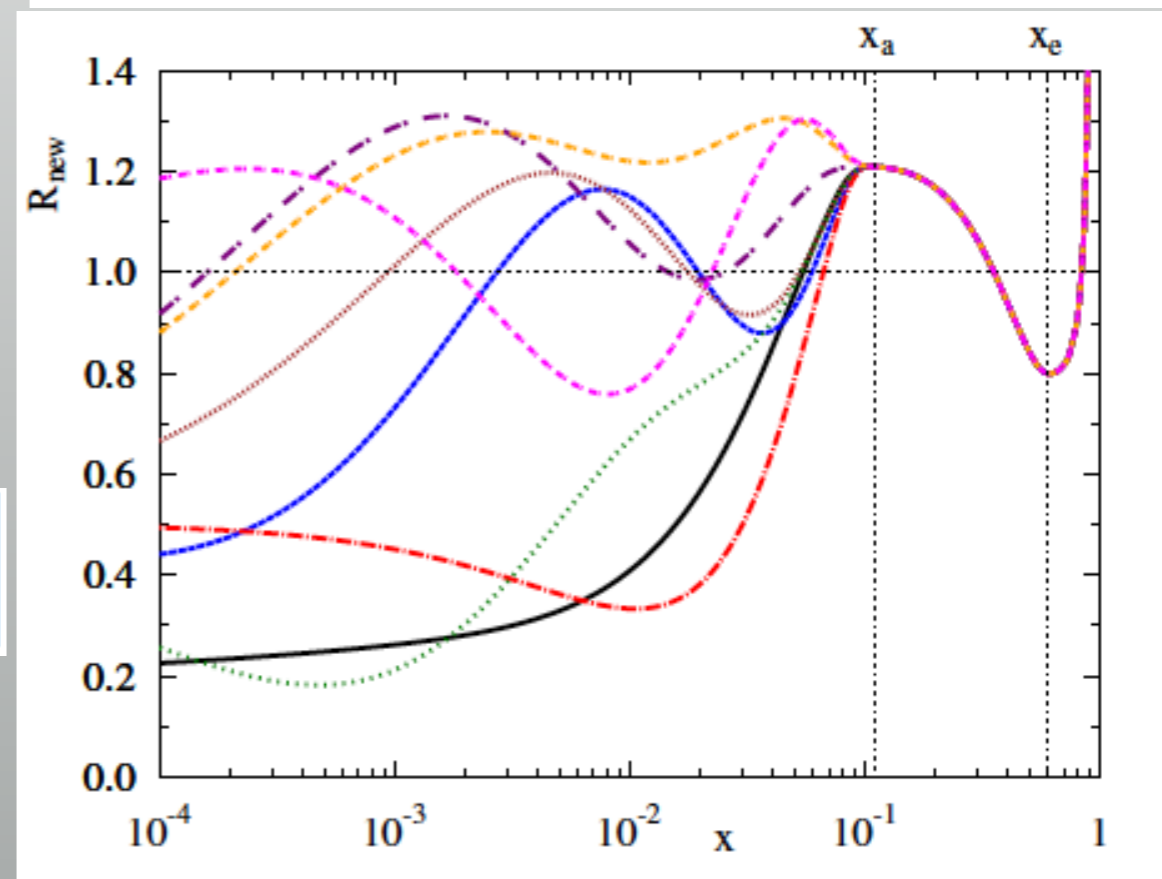
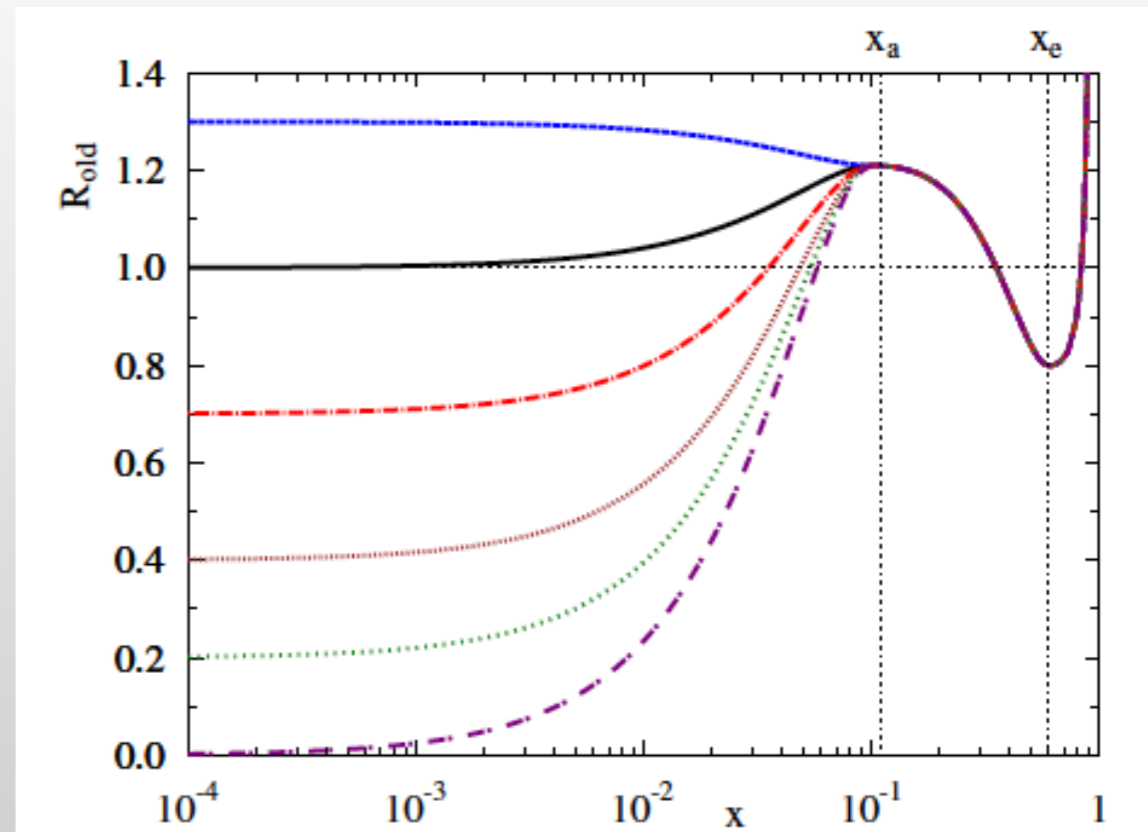
$$R_{\text{old}}(x) = \begin{cases} a_0 + (a_1 + a_2x)(e^{-x} - e^{-x_a}) & x \leq x_a \\ b_0 + b_1x + b_2x^2 + b_3x^3 & x_a \leq x \leq x_e \\ c_0 + (c_1 - c_2x)(1-x)^{-\beta} & x_e \leq x \leq 1, \end{cases}$$



3 for LHeC

$$R(x \leq x_a) = a_0 + a_1(x - x_a)^2 + x(x_a - x) \left[ \sum_{k=1}^4 a_{k+2} \log \left( \frac{x}{x_a} \right)^k \right]$$

- 15 (orig.) → 19 (new) parameters.



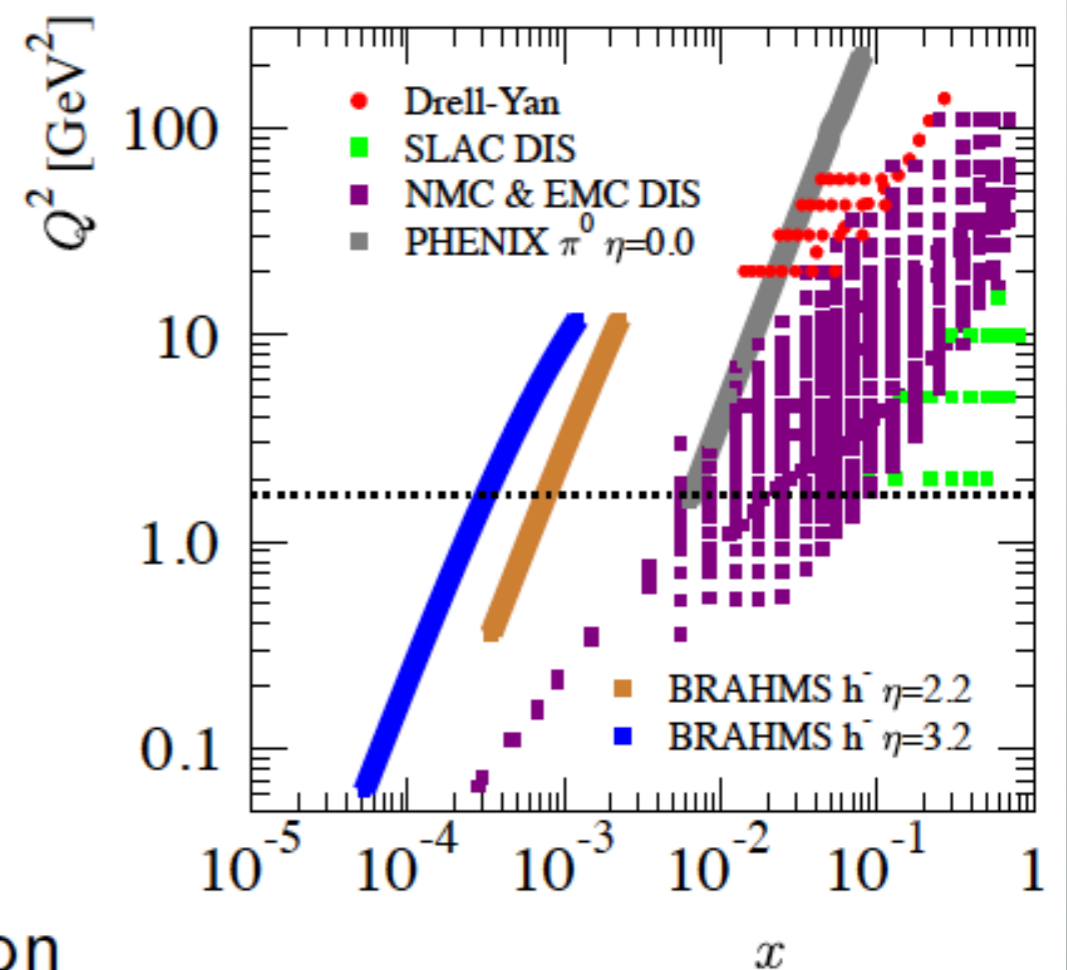
- Include the same data (DIS, Drell-Yan, inclusive  $\pi^0$ ) as in EPS09 (no LHC data yet) plus LHeC (neutral current) pseudo data.
- CTEQ6.6 as baseline (doesn't really matter which one)
- Flavour-independent nuclear modifications at  $Q_0 = 1.3 \text{ GeV}$

$R_V(x, Q_0)$  for both valence quarks

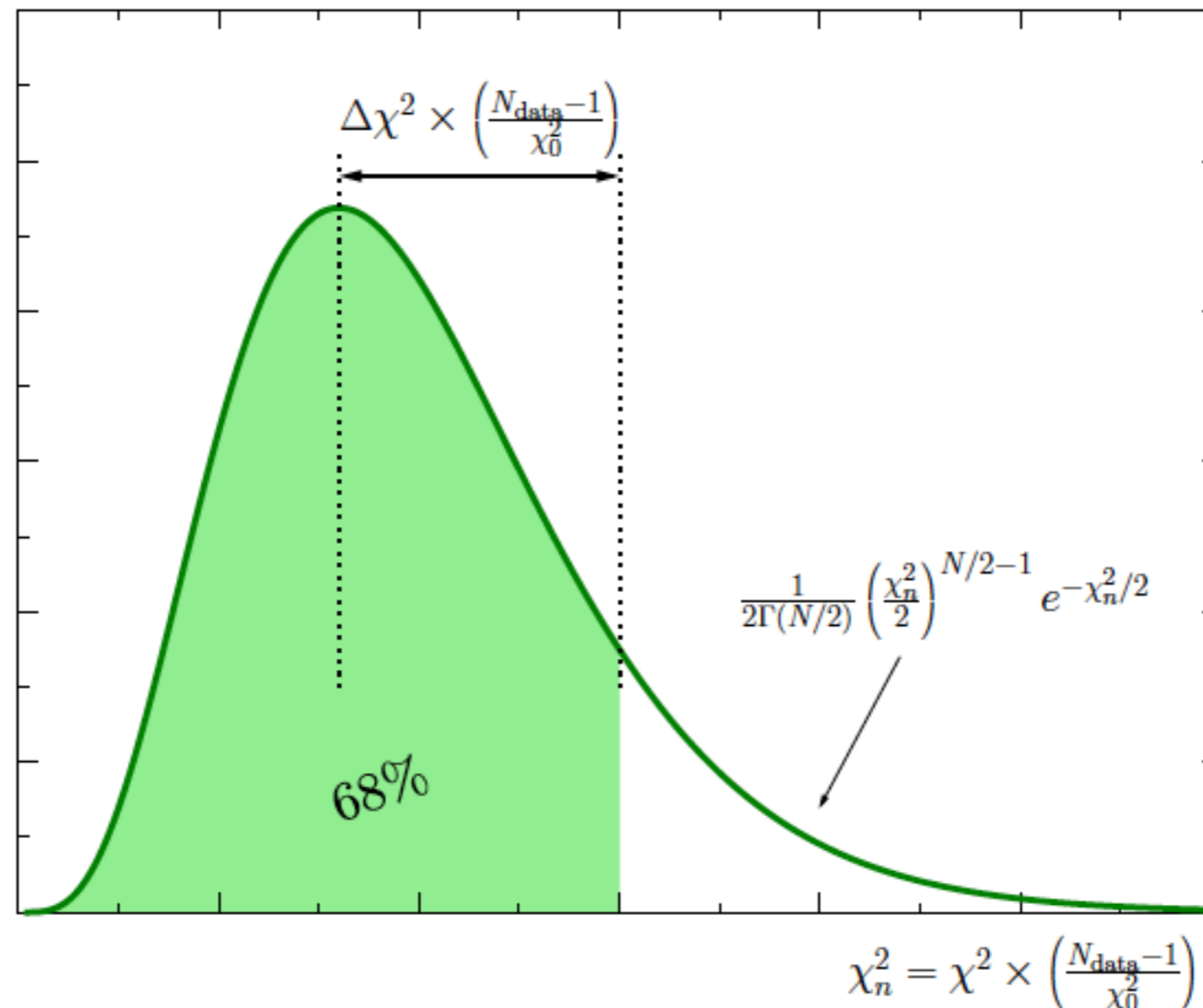
$R_S(x, Q_0)$  for light sea quarks

$R_G(x, Q_0)$  for gluons

- Charged-current data will be added later on to study the flavour dependence
- Cross-sections at NLO in the SACOT heavy-quark scheme (as CTEQ6.6)
- Robust Levenberg-Marquardt minimization method

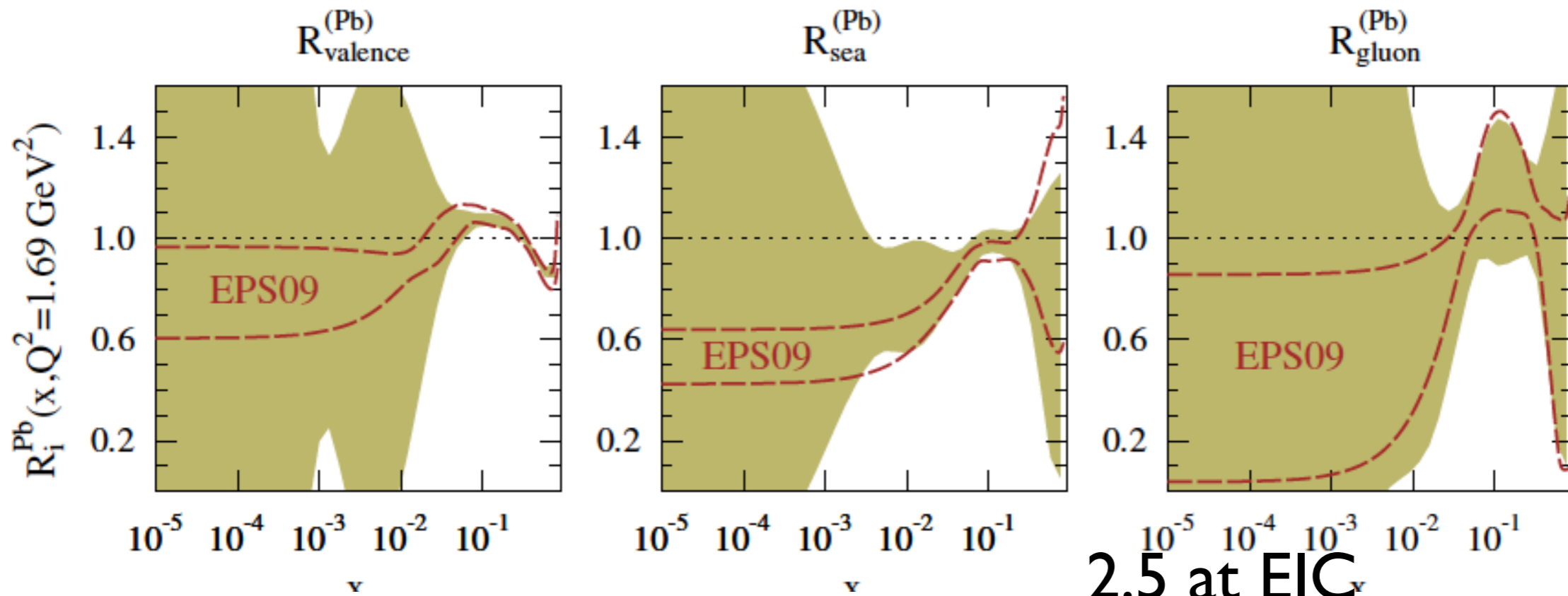


Standard Hessian uncertainty analysis (a la CTEQ, MSTW,...) with  $\Delta\chi^2$  determined from the expected behaviour of probability distribution for the global  $\chi^2$



Gives  $\Delta\chi^2 \approx 17$  (without or with the pseudodata)

The baseline fit using the new fit functions: no control over small  $x$ !



2.5 at EIC<sub>x</sub>

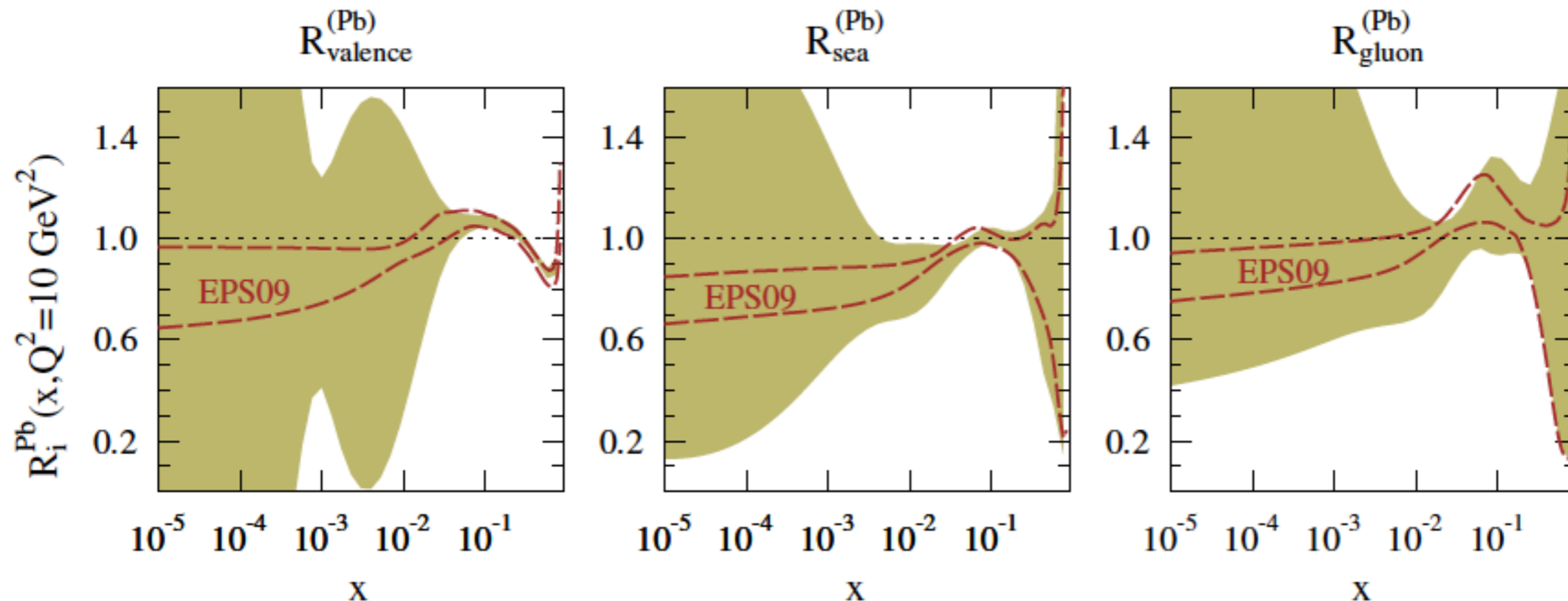
The lower bound restricted here by  $F_L(Q^2 = 2 \text{ GeV}^2, x > 10^{-5}) > 0$

Maybe against “physical intuition” (small- $x$  theory predicts shadowing,  $R_i < 1$ ), but consistent with the data.

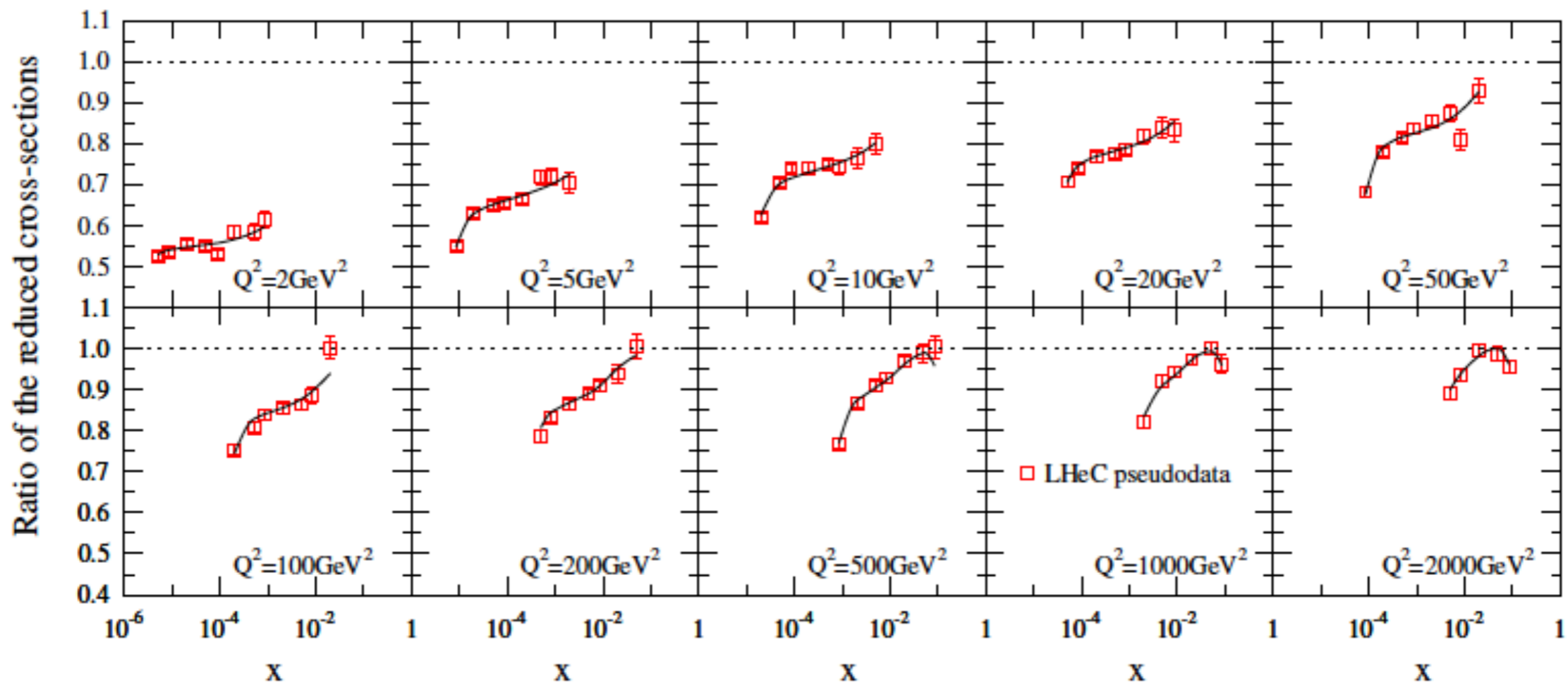
E.g. in EPS09, small- $x$  shadowing was essentially built in

The baseline fit using the new fit functions: no control over small  $x$ !

The  $Q^2$  dependence partly smooths out the differences in gluons



- **Simulation:** NC(+CC+c,b not yet used) with systematic uncertainties from a complete simulation.



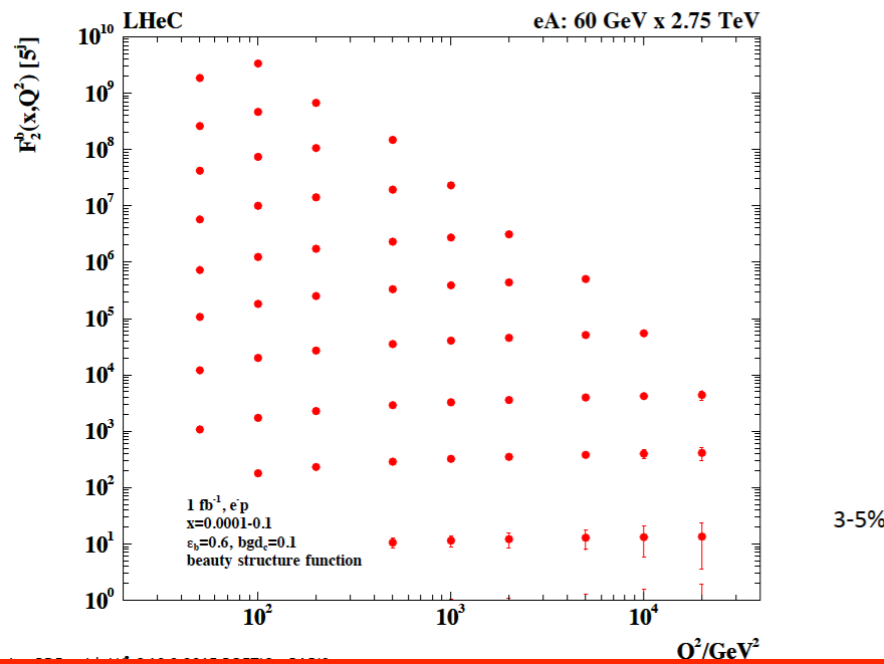
Checked that  $\chi^2/N_{\text{data}}$  to the underlying truth (=EPS09 ;) ) fluctuates about unity depending on the random numbers that got chosen



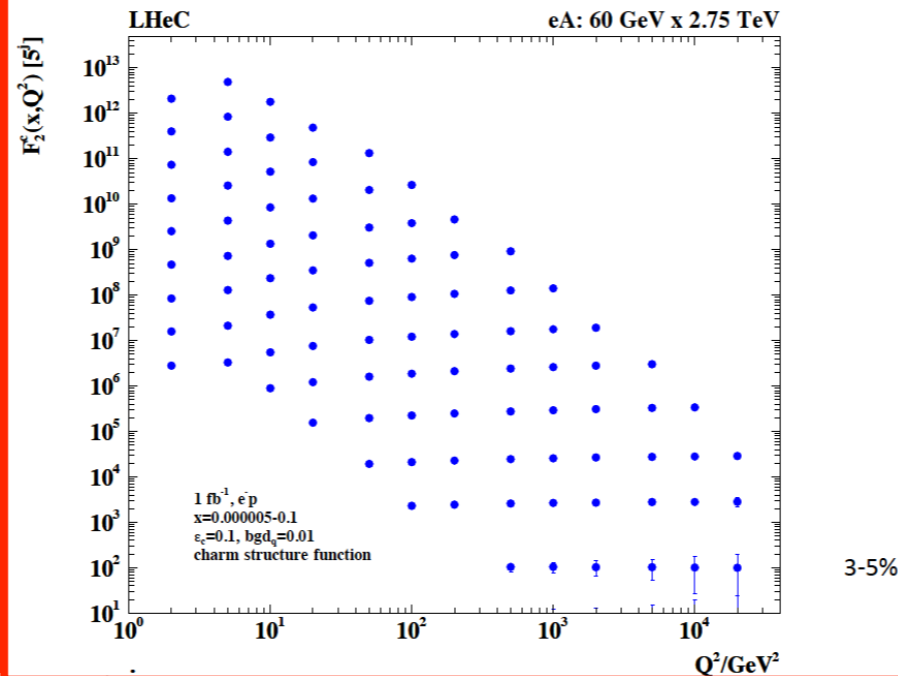
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1.1

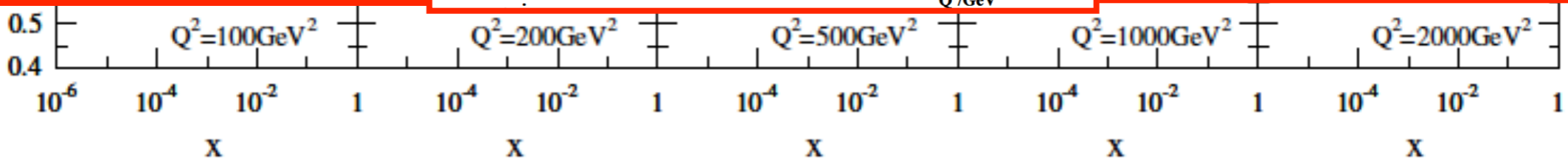
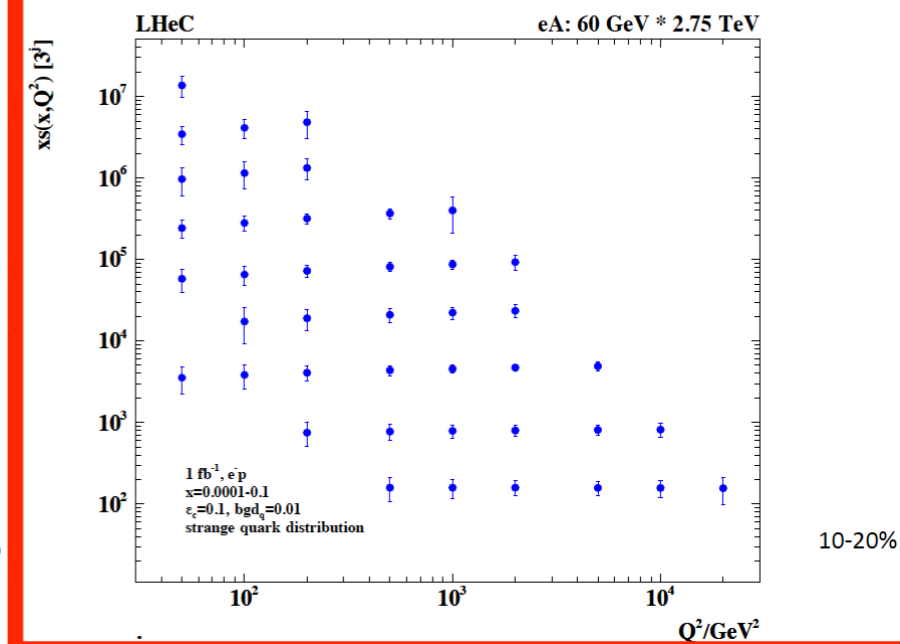
Heavy Flavour – Beauty in ePb - from NC



Heavy Flavour – Charm in eA - from NC

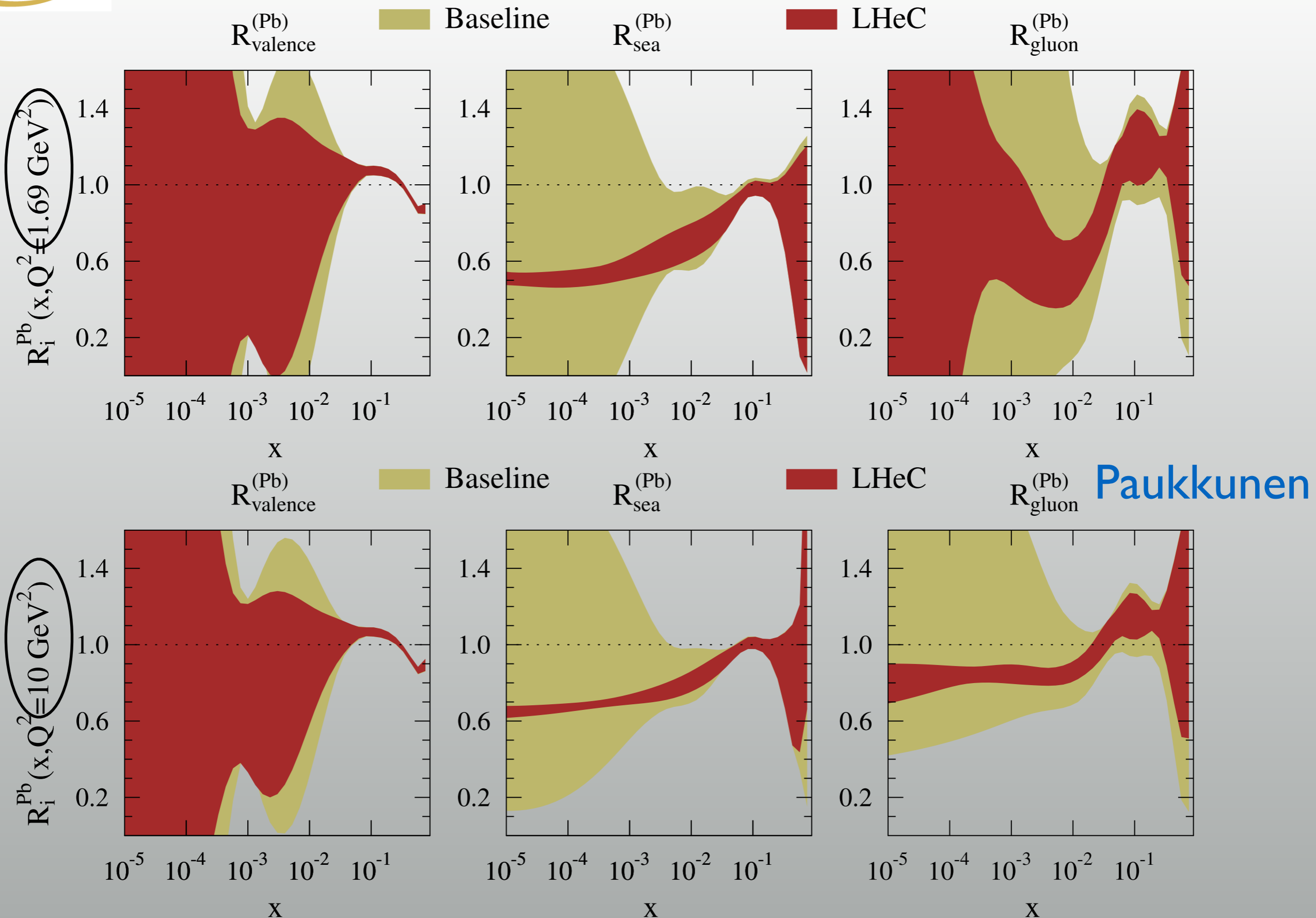


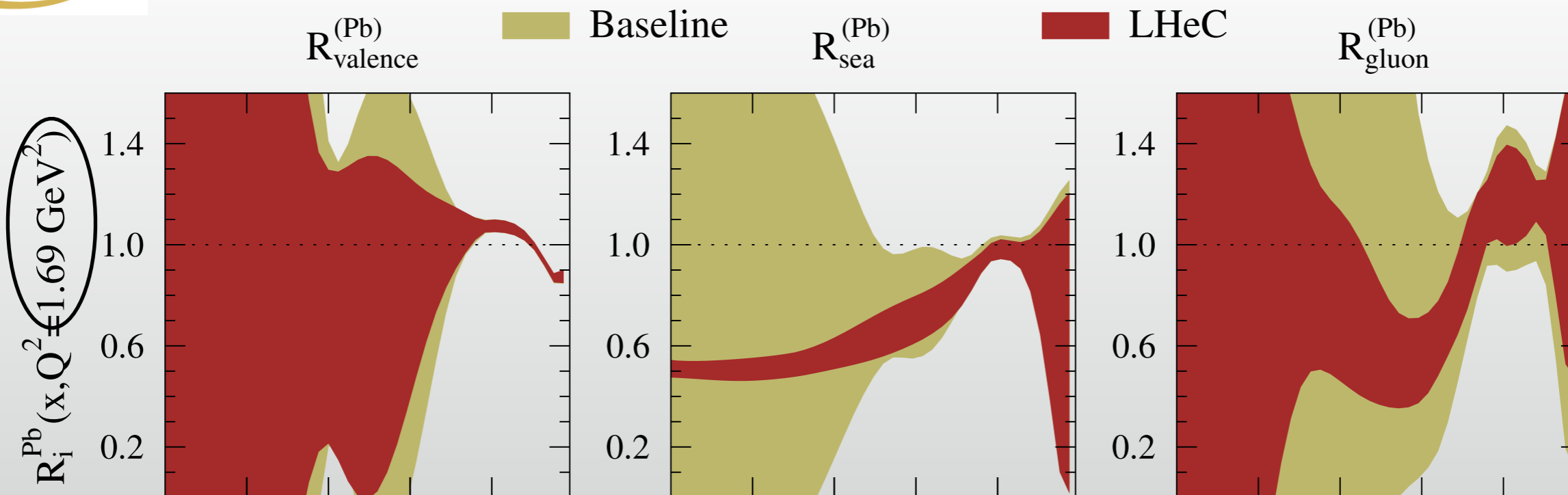
Heavy Flavour – Strange in ePb - from CC



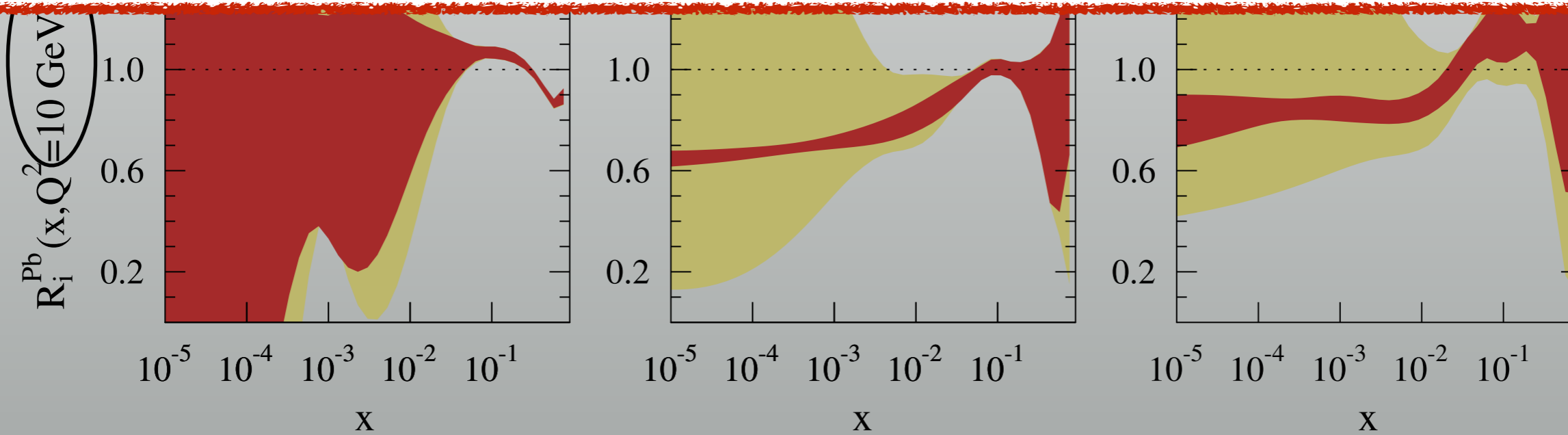
M. Klein at POETIC6

Checked that  $\chi^2/N_{\text{data}}$  to the underlying truth (=EPS09 ;) ) fluctuates about unity depending on the random numbers that got chosen



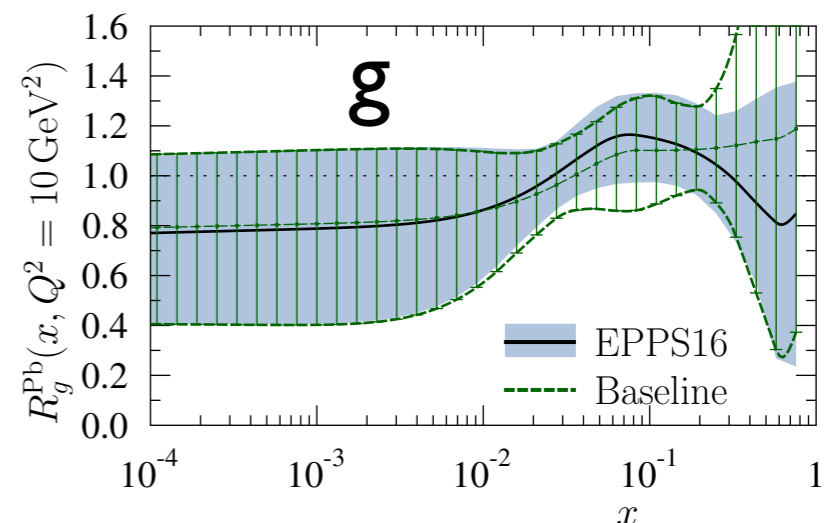
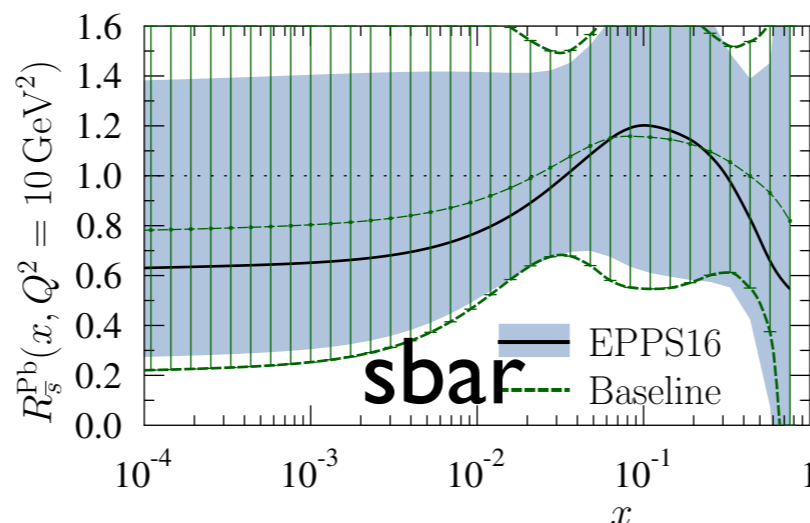
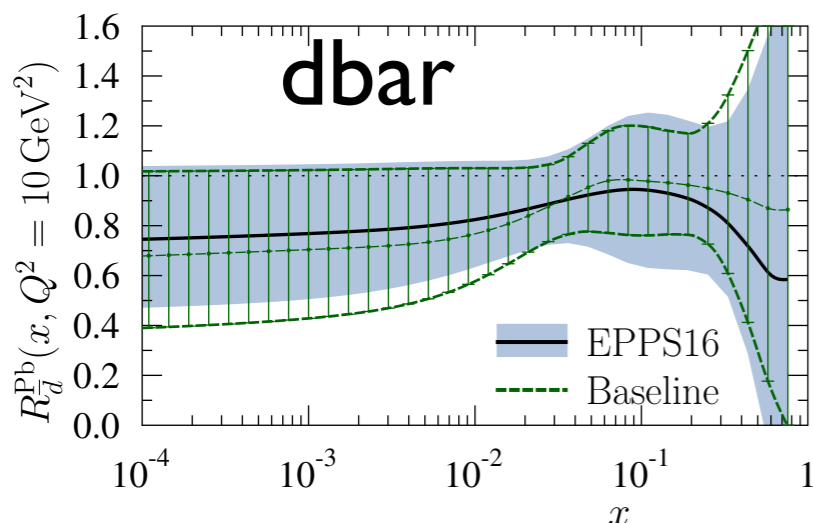
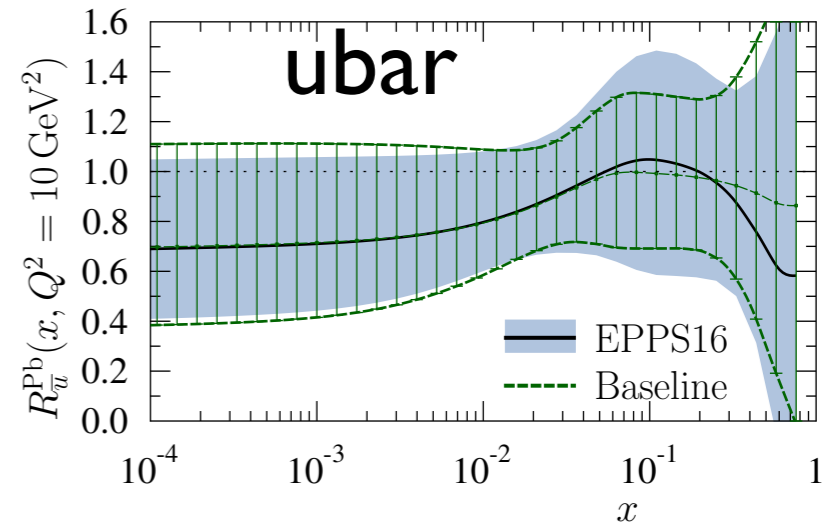
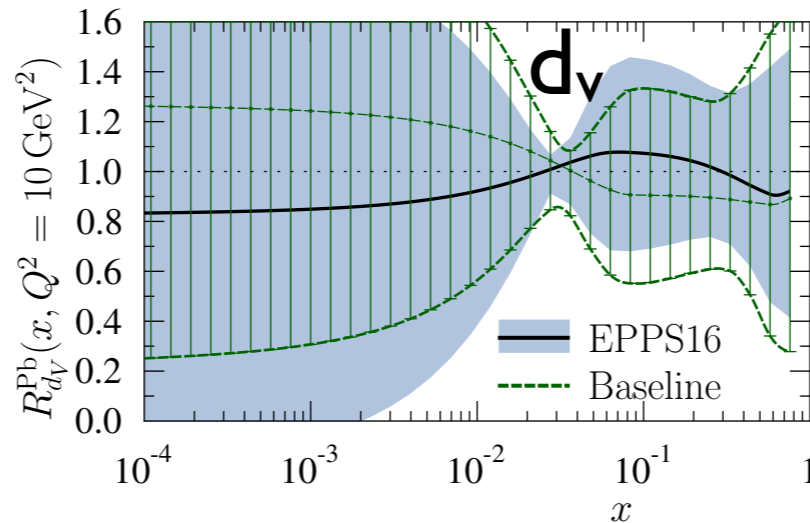
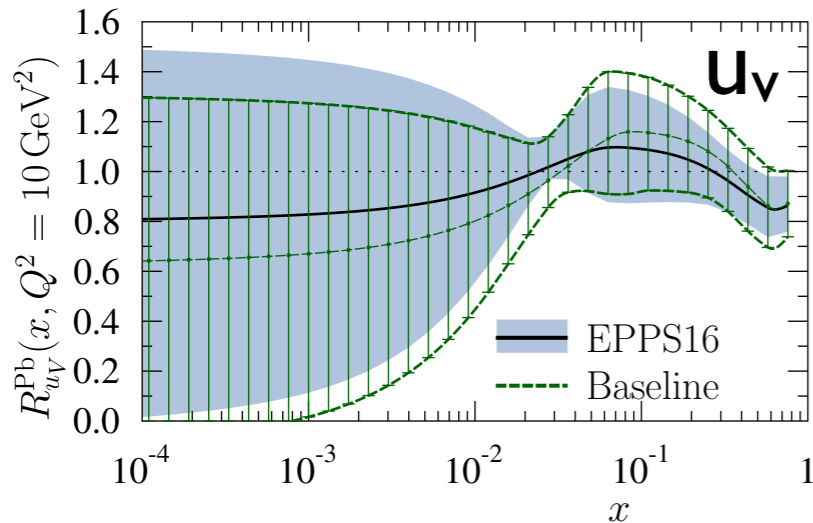
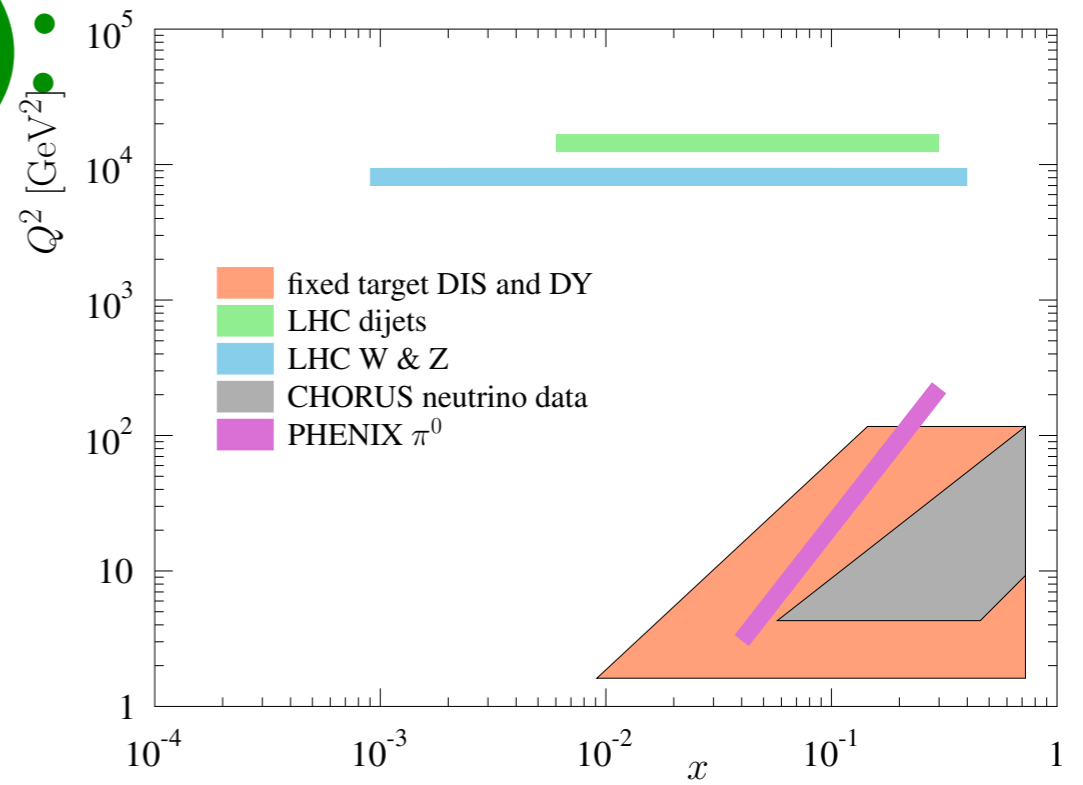


- Substantial reduction of uncertainties.
- EICs provide the nPDFs with the precision required for the heavy-ion programmes at RHIC, LHC and future colliders.

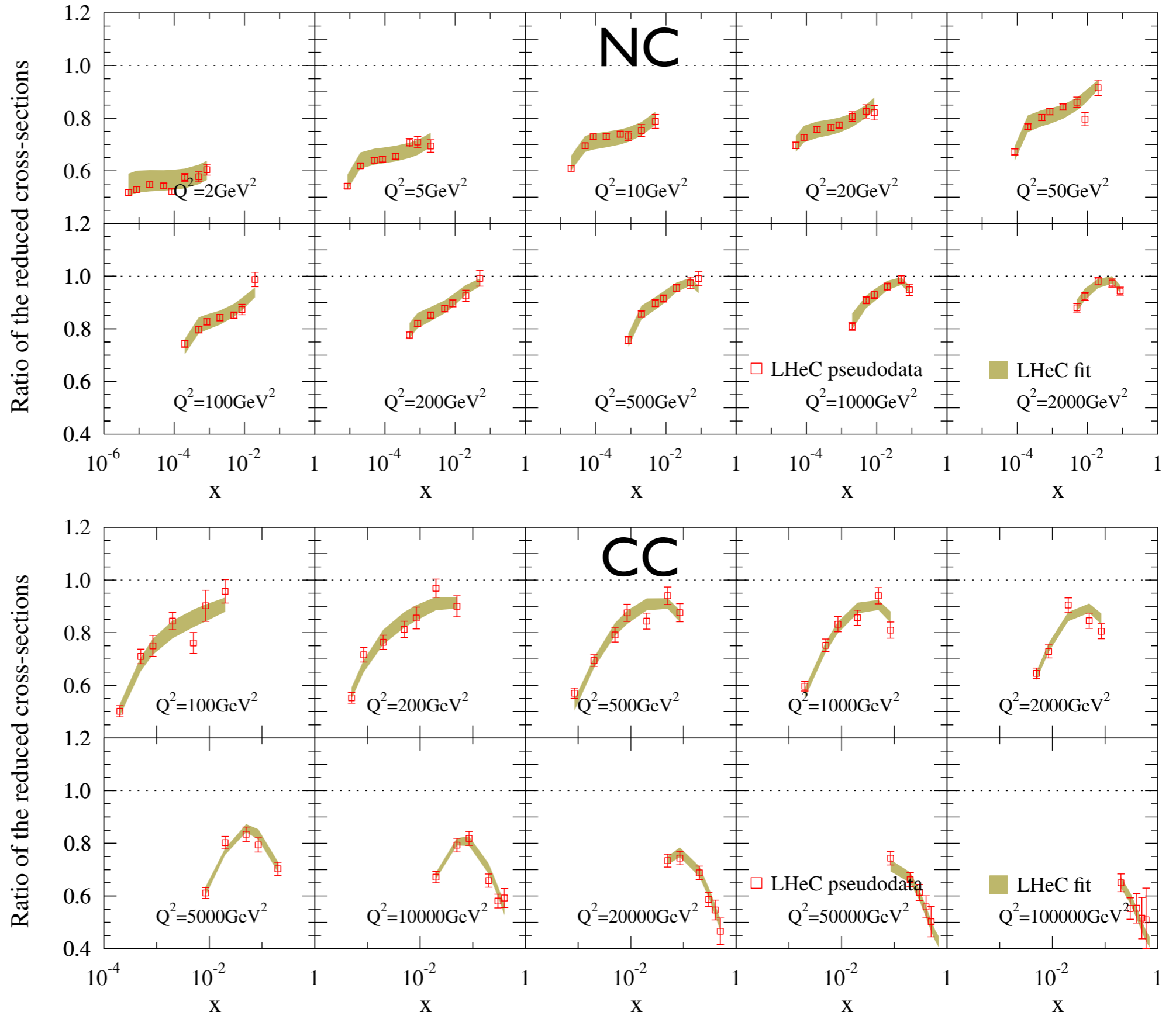


- **New setup EPPS16 [1612.05741]** including baseline (fixed target DIS, DY, RHIC) plus **neutrino and LHC (dijet, W, Z) pPb data**. More flexible parametrisation, GM-VFNS,  $R_u \neq R_d$ .

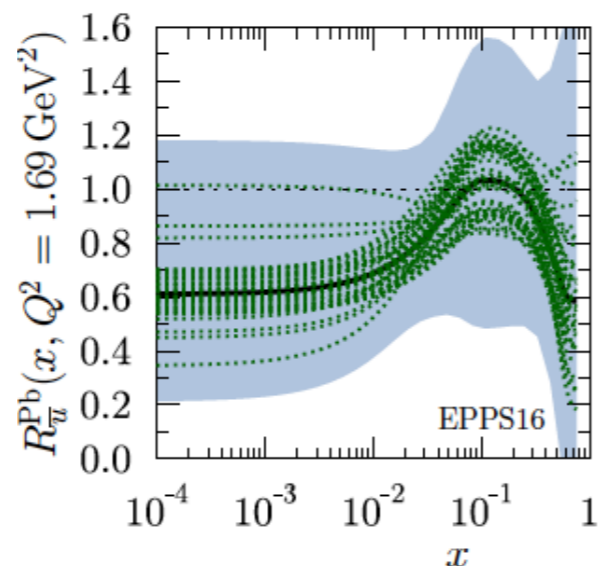
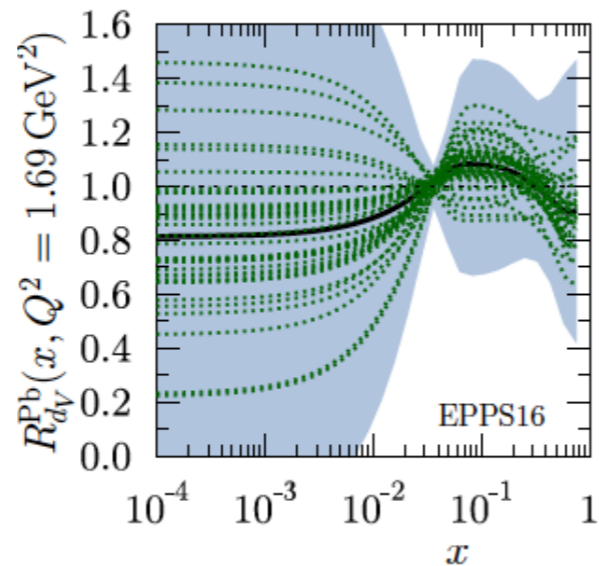
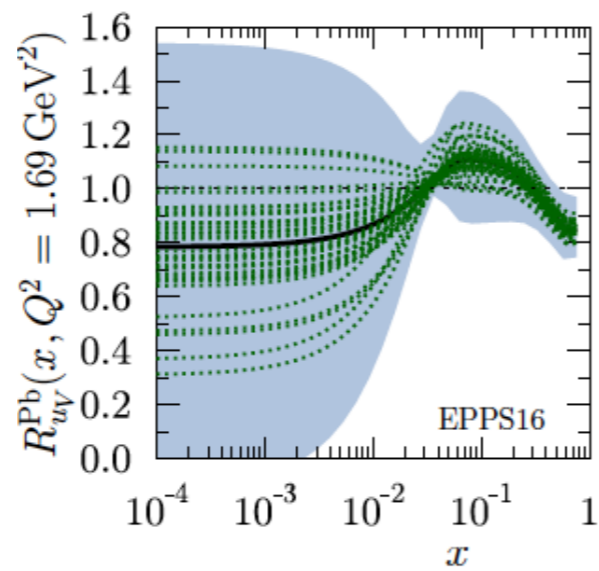
$$f_i^{P/A}(x, Q^2) = R_i^A(x, Q^2) f_i^P(x, Q^2)$$



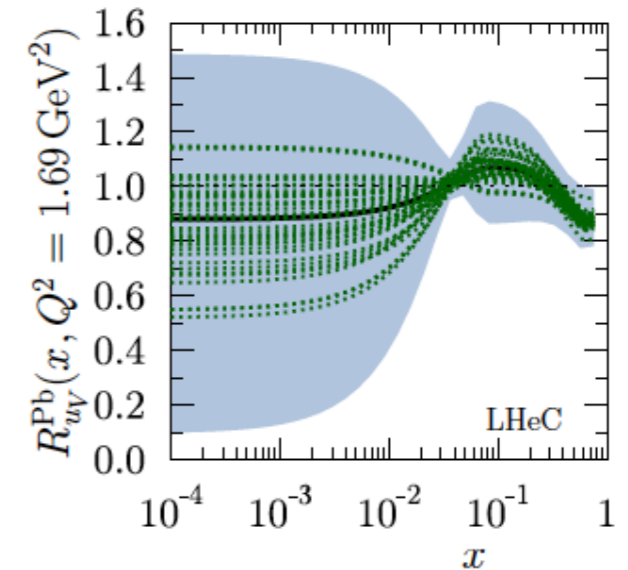
• Including eA  
 (60+2760) NC  
 and CC  
 pseudodata  
 reduces the  
 uncertainties  
 (notably on g),  
 but u,d  
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 [Paukkunen]



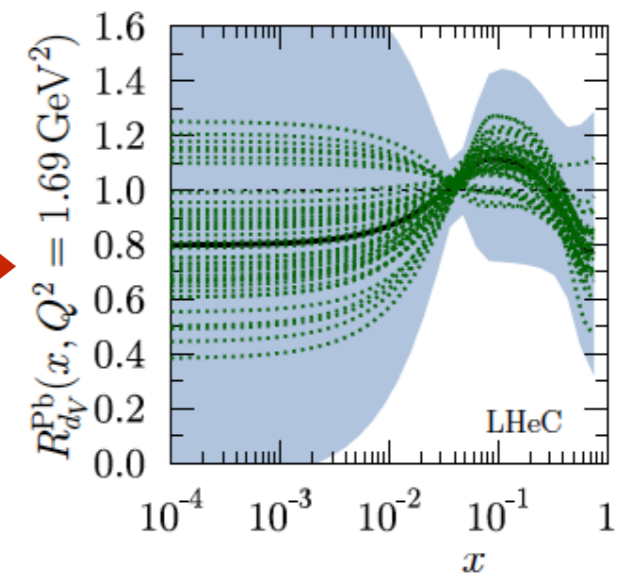
- Including eA (60+2760) NC and CC pseudodata reduces the uncertainties (notably on g), but u,d decomposition difficult (factor  $2Z/A-1$ ). [Paukkunen]



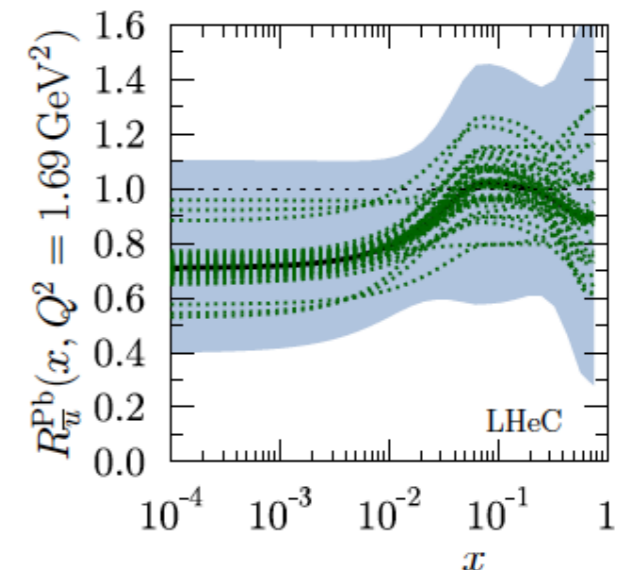
$u_v$



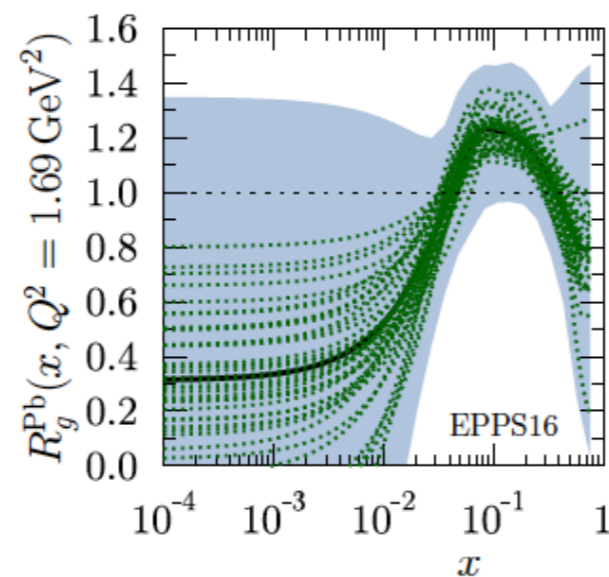
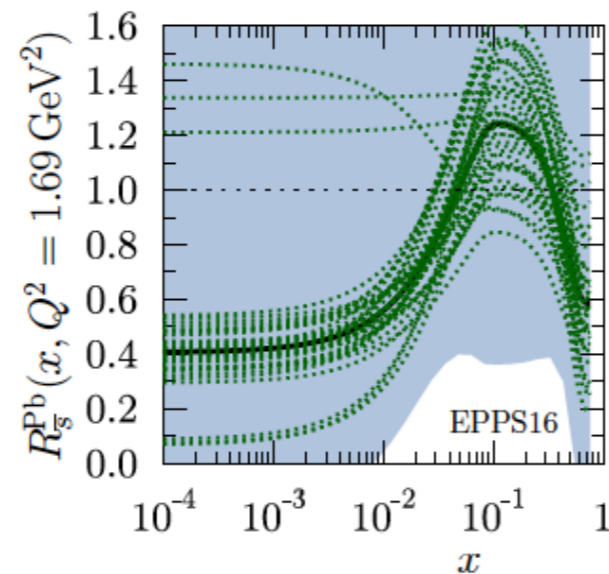
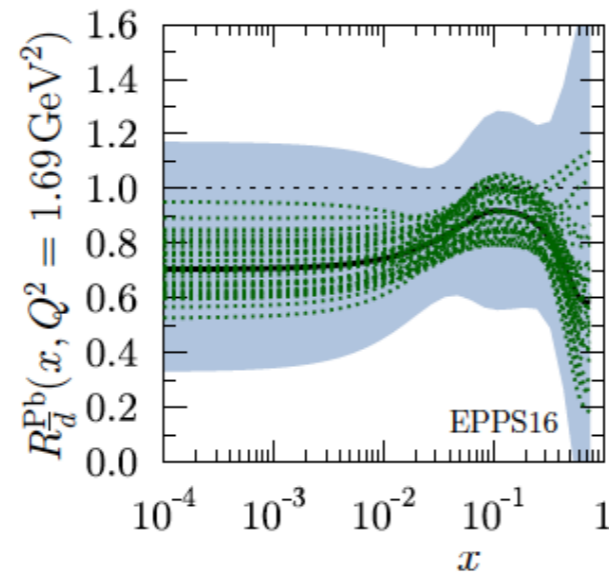
$d_v$



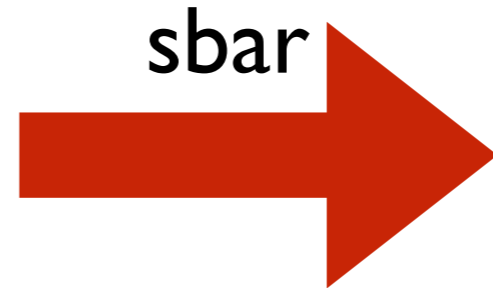
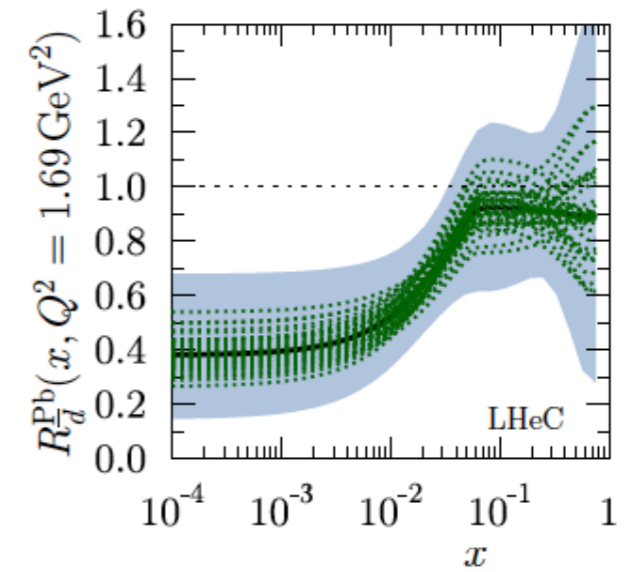
$u_{\bar{b}}$



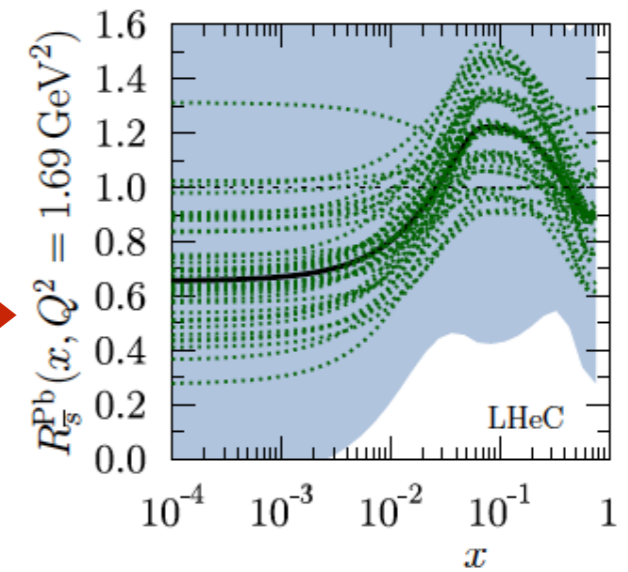
- Including eA (60+2760) NC and CC pseudodata reduces the uncertainties (notably on  $g$ ), but  $u, d$  decomposition difficult (factor  $2Z/A-1$ ). [Paukkunen]



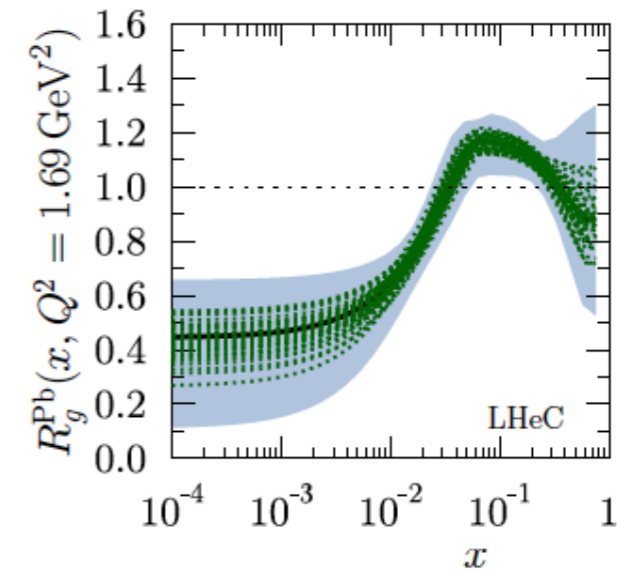
$d\bar{b}$



$s\bar{b}$



$g$



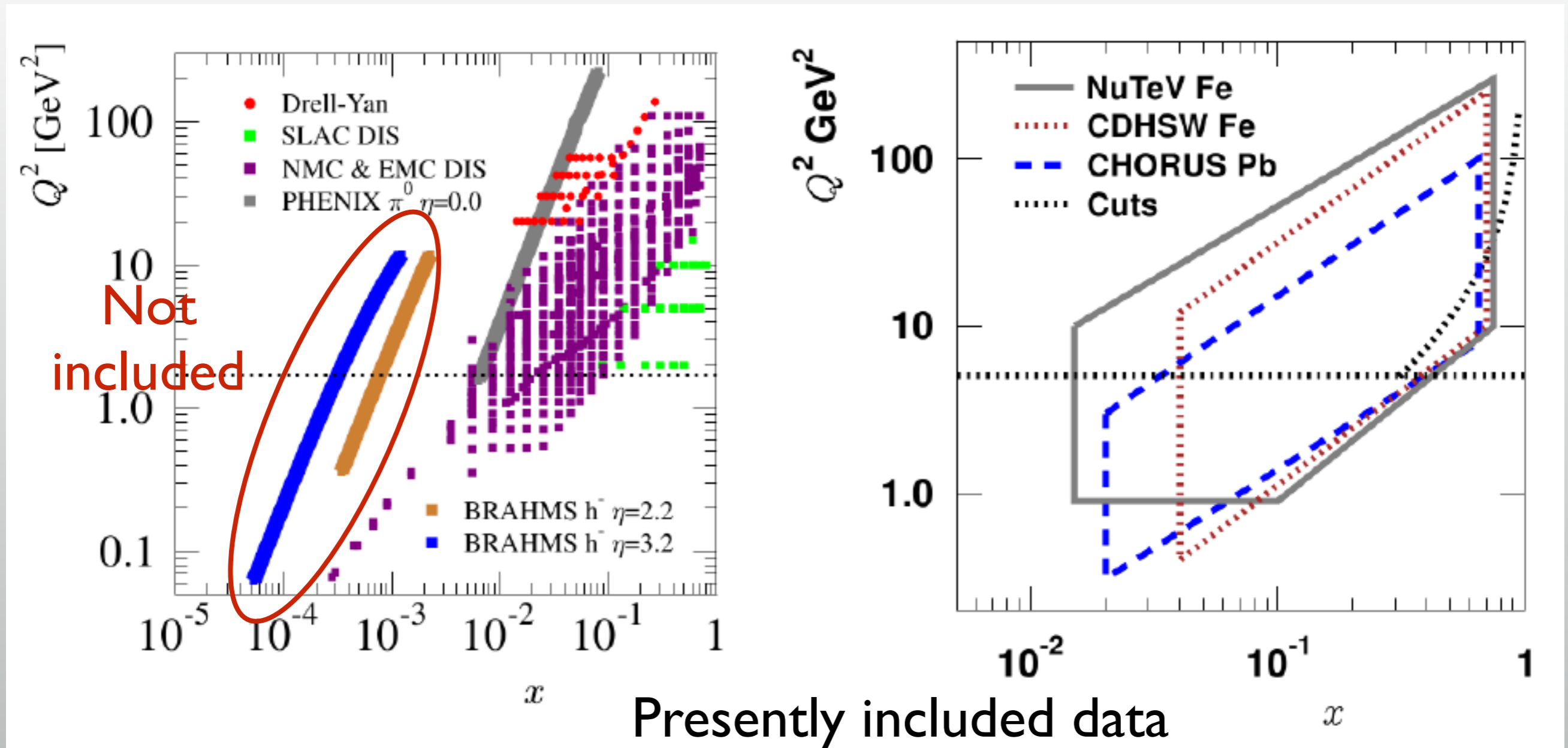
## Summary:

YEAR	BASELINE	SETS
CDR	EPS09 + 1 p., ZM-VFNS	NC $F_2 + F_L + c, b$
2014	EPS09 + 1 p., GM-VFNS (SACOT)	NC $\sigma_{\text{red}}$ , three energies, not c,b
2015	EPS09 + more flexibility at small x, GM-VFNS (SACOT)	NC $\sigma_{\text{red}}$ , top energy, not c,b
2017	EPPS16, GM-VFNS (SACOT)	NC + CC $\sigma_{\text{red}}$ , top energy, not c,b

- Done by Max, **Hannu** and me.
- Additional possibilities: Pb fit e.g. using xFitter, use (NNLO) jets for the glue (see arXiv:1703.02864).



# Available sets:



- Not enough data for any single nuclei:  $A$ -dependent parameters in either the ratios or the PDFs.
- Valence for  $x > 10^{-2}$  constrained by DIS, sea for  $x > 10^{-2}$  by DIS+DY, glue for  $x \sim 0.1$  by DIS  $Q^2$ -evolution and RHIC pions.

# Available sets:

SET	<b>HKN07</b> PRC76 (2007) 065207	<b>EPS09</b> JHEP 0904 (2009) 065	<b>DSSZ</b> PRD85 (2012) 074028	<b>nCTEQ15</b> PRD93 (2016) 085037	<b>KAI5</b> PRD93 (2016) 014036	<b>EPPS16</b> EPJC C77 (2017)163
<b>data</b>	eDIS	✓	✓	✓	✓	✓
	DY	✓	✓	✓	✓	✓
	$\pi^0$	✗	✓	✓	✓	✗
	vDIS	✗	✗	✓	✗	✗
	pPb	✗	✗	✗	✗	✗
<b># data</b>	1241	929	1579	740	1479	1811
<b>order</b>	NLO	NLO	NLO	NLO	NNLO	NLO
<b>proton PDF</b>	MRST98	CTEQ6.1	MSTW2008	~CTEQ6.1	JR09	CT14NLO
<b>mass scheme</b>	ZM-VFNS	ZM-VFNS	GM-VFNS	GM-VFNS	ZM-VFNS	GM-VFNS
<b>comments</b>	$\Delta\chi^2=13.7$ , ratios, <u>no EMC for gluons</u>	$\Delta\chi^2=50$ , ratios, <u>huge shadowing-antishadowing</u>	$\Delta\chi^2=30$ , ratios, <u>medium-modified FFs for <math>\pi^0</math></u>	$\Delta\chi^2=35$ , PDFs, <u>flavour sep., not enough sensitivity</u>	PDFs, <u>deuteron data included</u>	$\Delta\chi^2=52$ , ratios, <u>LHC pPb data</u>

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SET	<b>HKN07</b> PRC76 (2007) 065207	<b>EPS09</b> JHEP 0904 (2009) 065	<b>DSSZ</b> PRD85 (2012) 074028	<b>nCTEQ15</b> PRD93 (2016) 085037	<b>KAI5</b> PRD93 (2016) 014036	<b>EPPS16</b> EPJC C77 (2017)163
<b>data</b>	eDIS	✓	✓	✓	✓	✓
	DY	✓	✓	✓	✓	✓
	$\pi^0$	✗	✓	✓	✓	✗
	vDIS	✗	✗	✓	✗	✗
	pPb	✗	✗	✗	✗	✗
<b># data</b>	1241	929	1579	740	1479	1811
<b>order</b>	NLO	NLO	NLO	NLO	NNLO	NLO
<b>proton PDF</b>	MRST98	CTEQ6.1	MSTW2008	~CTEQ6.1	JR09	CT14NLO
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<b>comments</b>	$\Delta\chi^2=13.7$ , ratios, <u>no EMC for gluons</u>	$\Delta\chi^2=50$ , ratios, <u>huge shadowing-antishadowing</u>	$\Delta\chi^2=30$ , ratios, <u>medium-modified FFs for <math>\pi^0</math></u>	$\Delta\chi^2=35$ , PDFs, <u>flavour sep., not enough sensitivity</u>	PDFs, <u>deuteron data included</u>	$\Delta\chi^2=52$ , ratios, <u>LHC pPb data</u>

# LHeC scenarios:

config.	E(e)	E(N)	N	$\int L(e^+)$	$\int L(e^-)$	Pol	L/10 <sup>32</sup>	P/MW	years	type
<b>For F<sub>2</sub></b>										
A	20	7	p	1	1	-	1	10	1	SPL
B	50	7	p	50	50	0.4	25	30	2	RR hiQ <sup>2</sup>
C	50	7	p	1	1	0.4	1	30	1	RR lo x
D	100	7	p	5	10	0.9	2.5	40	2	LR
E	150	7	p	3	6	0.9	1.8	40	2	LR
F	50	3.5	D	1	1	--	0.5	30	1	eD
G	50	2.7	Pb	10 <sup>-4</sup>	10 <sup>-4</sup>	0.4	10 <sup>-3</sup>	30	1	ePb
H	50	1	p	--	1	--	25	30	1	lowEp
I	50	3.5	Ca	5 · 10 <sup>-4</sup>		?	5 · 10 <sup>-3</sup>	?	?	eCa

- **For F<sub>L</sub>**: 10, 25, 50 + 2750 (7000); Q<sup>2</sup> ≤ sx; Lumi=5, 10, 100 pb<sup>-1</sup> respectively; charm and beauty: same efficiencies in ep and eA.