

Physics Beyond the Standard Model II: Supersymmetry

David E Kaplan
HCP Summer School 2007
CERN

Natural EWSB

The Higgs is very sensitive to new mass scales in the theory.

The Higgs needs a symmetry.

Options

- electron mass multiplicatively renormalized:
chiral symmetry
- photon mass not generated by quantum effects: gauge invariance
- pion mass naturally small compared to the rho mass: goldstone's theorem

Symmetries Relating Spins

Spin $1/2$

Chiral Symmetry

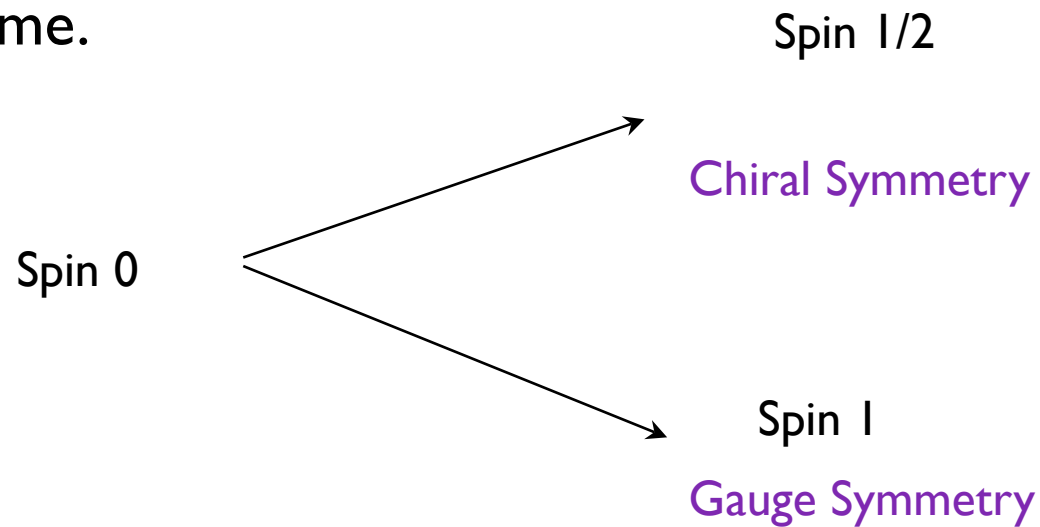
Spin 0

Spin 1

Gauge Symmetry

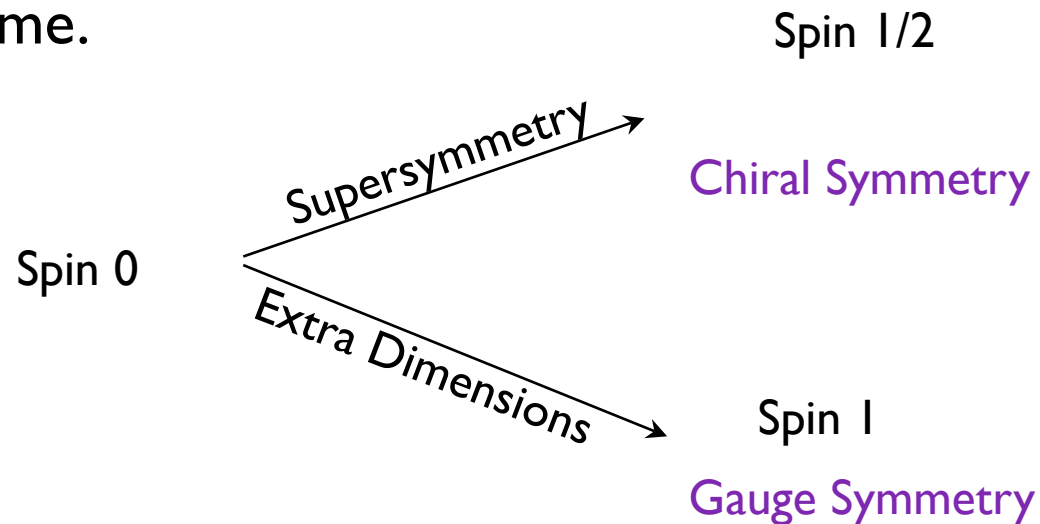
Symmetries Relating Spins

Masses and scattering cross sections
would be the same.



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Supersymmetry

Definitely the more exotic of the two

Fermionic (or purely quantum mechanical) extra dimensions

Mixes with symmetries of relativity -
extends the Poincare group

Simple Example

$$\mathcal{L} = -|\partial\phi|^2 - i\psi^\dagger \bar{\sigma} \cdot \partial\psi - |m\phi|^2 - \frac{1}{2}(m\psi\psi + \text{h.c.})$$

Invariant under:

$$\delta\phi = \epsilon\psi \quad \delta\psi_\alpha = i(\sigma^\mu \epsilon^\dagger)_\alpha \partial_\mu\phi$$

Simple Example

$$\begin{aligned}\mathcal{L} = & -|\partial\phi|^2 - i\psi^\dagger\bar{\sigma}\cdot\partial\psi - |m\phi|^2 \\ & -\frac{1}{2}(m+y\phi)\psi\psi - \text{h.c.} - \frac{1}{2}m^*y|\phi|^2\phi - \text{h.c.} + \frac{1}{4}|y\phi^2|^2\end{aligned}$$

Invariant under:

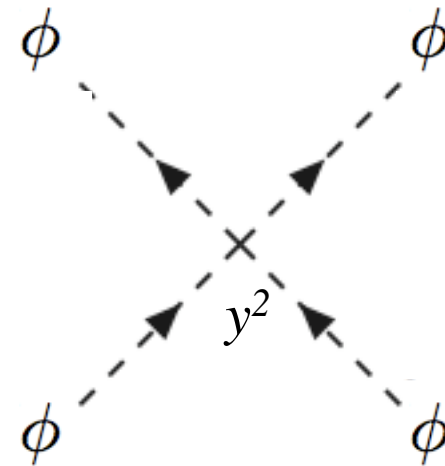
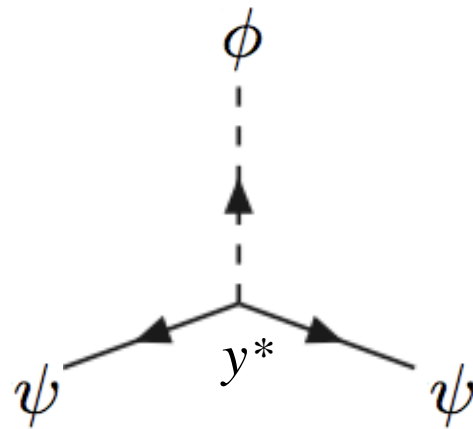
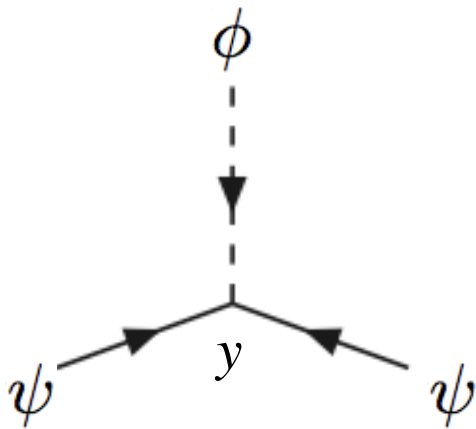
$$\delta\phi = \epsilon\psi \qquad \delta\psi_\alpha = i(\sigma^\mu\epsilon^\dagger)_\alpha\partial_\mu\phi$$

Implications

ϕ complex - two bosons, spin 0

ψ Weyl spinor - two fermions, spin 1/2

All particles of mass m - degenerate



couplings related

Canceling Contributions

The diagram illustrates the cancellation of contributions at zero momentum. It consists of three terms arranged in two rows, separated by plus signs and an equals sign.

The first row contains two terms:

- The first term is a solid circle labeled ψ . It has two external dashed lines: one on the left labeled ϕ with momentum y entering, and one on the right labeled ϕ with momentum y^* exiting.
- The second term is a dashed circle labeled ϕ . It has two external dashed lines: one on the left labeled ϕ with momentum y^*m entering, and one on the right labeled ϕ with momentum ym^* exiting.

The second row contains one term:

- A dashed circle labeled ϕ . It has two external dashed lines: one on the left labeled ϕ with momentum y^2 entering, and one on the right labeled ϕ with momentum y^2 exiting.

The entire expression is set equal to zero, with the text "(at zero momentum)" in parentheses to the right of the equals sign.

$$\begin{aligned} & \phi \text{---} y \text{---} \psi \text{---} y^* \text{---} \phi + \phi \text{---} y^*m \text{---} \phi \text{---} ym^* \text{---} \phi \\ & + \phi \text{---} y^2 \text{---} \phi = 0 \quad (\text{at zero momentum}) \end{aligned}$$

The Superpotential

$$W = \frac{1}{2}m\phi^2 + \frac{1}{6}y\phi^3$$

$$\frac{\partial W}{\partial \phi} = m\phi + \frac{1}{2}y\phi^2$$

$$\frac{\partial^2 W}{\partial \phi^2} = m + y\phi$$

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fermion
partner
of phi

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General Superpotential

You pick a superpotential W , generate the potential V using the rules below, and you have a supersymmetric theory.

$$W = \frac{1}{2}M^{ij}\phi_i\phi_j + \frac{1}{6}y^{ijk}\phi_i\phi_j\phi_k$$

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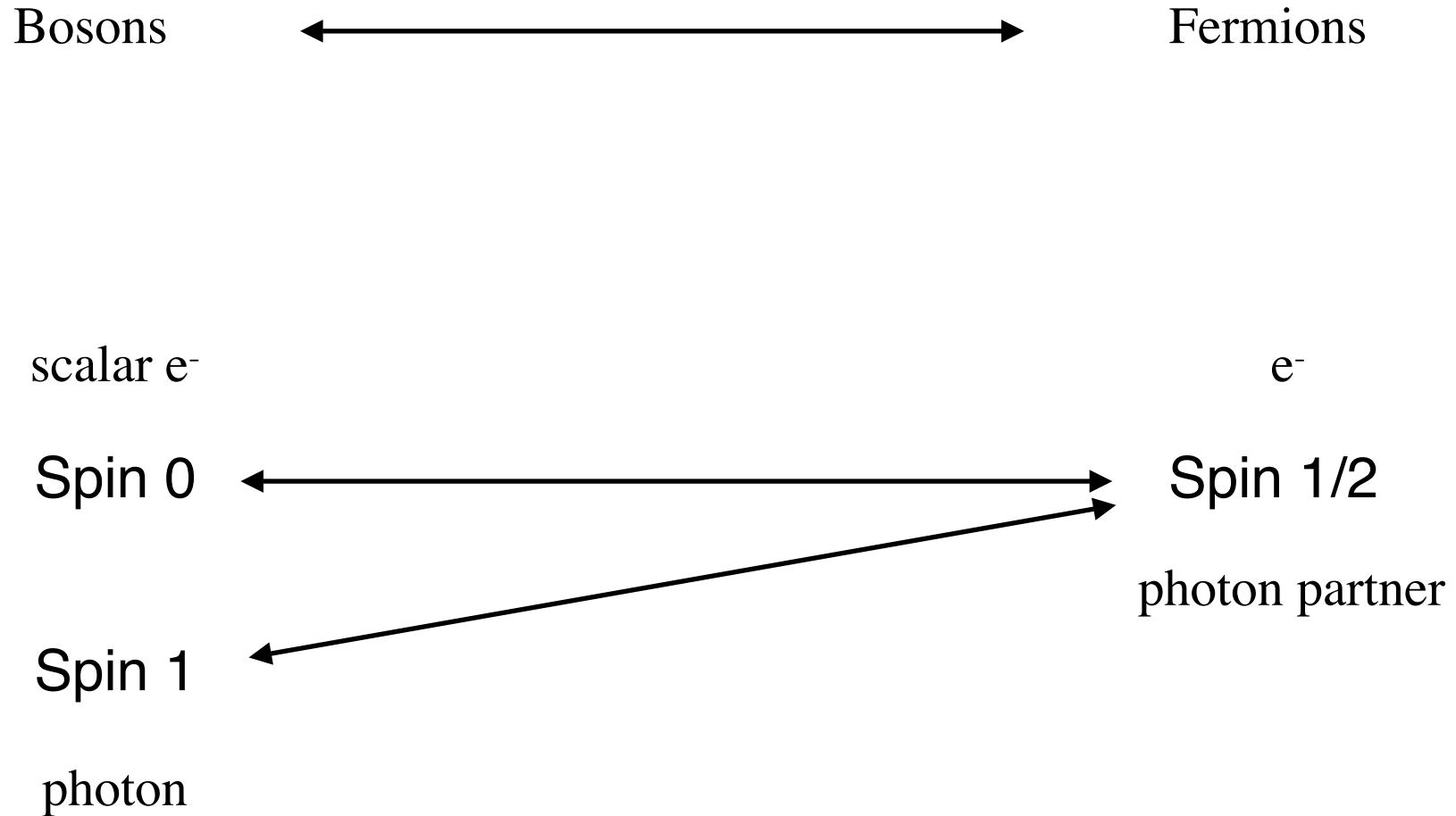
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$$W^{ij} = \frac{\delta^2}{\delta \phi_i \delta \phi_j} W \qquad W^i = \frac{\delta W}{\delta \phi_i}$$

Additional Partners



Additional Potential

$$V = +\frac{1}{2}g^2 \left(\sum_k \phi_k^* t^a \phi_k \right)^2 - \sqrt{2}g (\phi^* \lambda^{aT} t^a c\psi - \psi^\dagger c\lambda^{a*} t^a \phi)$$

SU(3): t^a - Gellman matrices

SU(2): t^a - Pauli matrices

U(1): t^a - hypercharges

Supersymmetrize the SM

e^-

γ

q

W

h

Supersymmetrize the SM

$$e^- \rightarrow e^-$$

$$\gamma \rightarrow \gamma$$

$$q \rightarrow q$$

$$W \rightarrow W$$

$$h \rightarrow h$$

Supersymmetrize the SM

$$e^- \rightarrow \tilde{e}^-$$

$$\gamma \rightarrow \overset{\sim}{\gamma}$$

$$q \rightarrow \tilde{q}$$

$$W \rightarrow \tilde{W}$$

$$h \rightarrow \tilde{h}$$

Supersymmetrize the SM

$$W = H QD^c + H QU^c$$

Need two Higgses.

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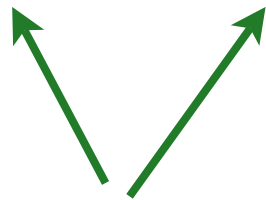
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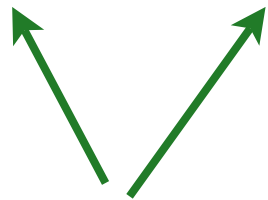
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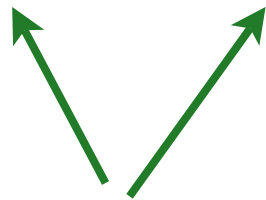
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$$H_1 = H_d = H \quad H_2 = H_u = \bar{H} = H^c$$

$$\tan \beta = \langle H_2 \rangle / \langle H_1 \rangle$$

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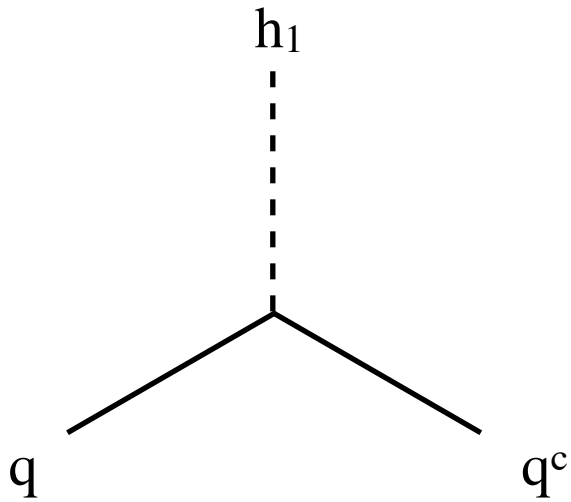
Another reason: require
two higgsinos for
anomaly cancelation.

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MSSM

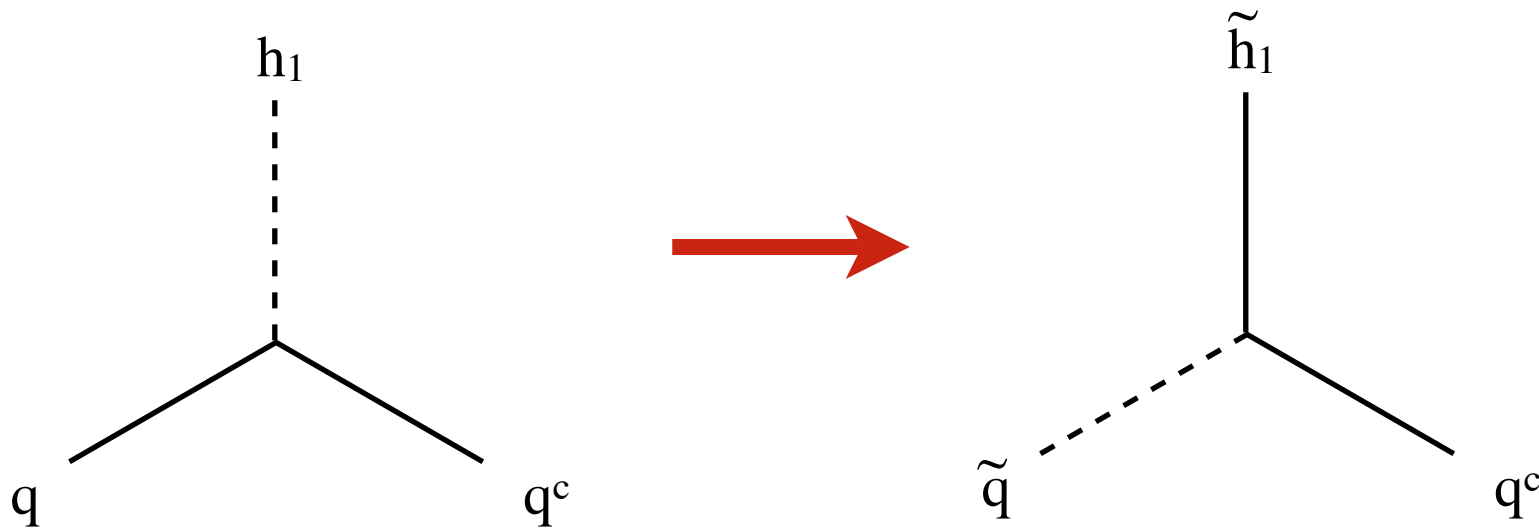
$$W = H_1 Q D^c + H_2 Q U^c + H_1 L E^c + \mu H_1 H_2$$



Take any SM diagram and switch the spins of two lines.

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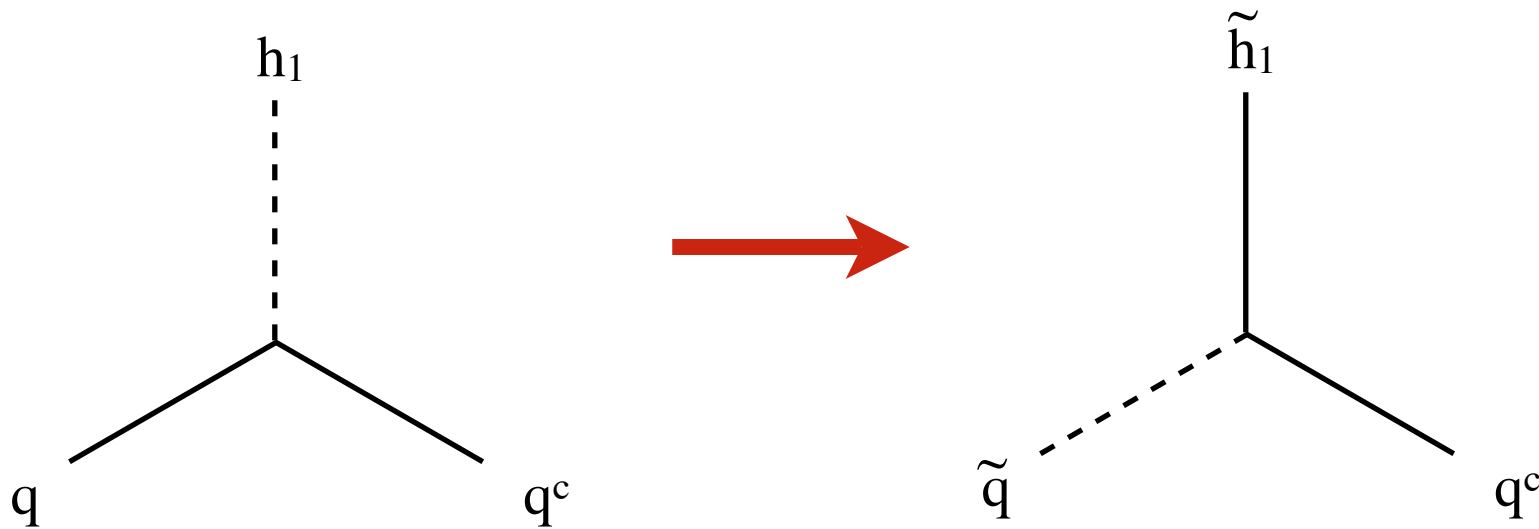
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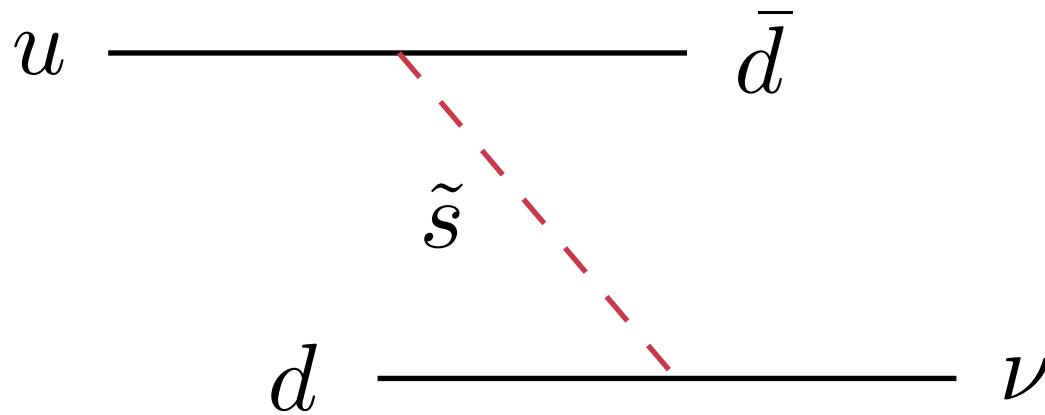
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Dimension 4 Operators

$$W = H_1 Q D^c + H_2 Q U^c + H_1 L E^c + \mu H_1 H_2 \\ + L Q D^c + U^c D^c D^c + L L E^c + \mu_L L H_2$$

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$$p \rightarrow \pi^+ \nu \quad \sim 1 \text{ hour}$$

Dimension 4 Operators

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Introduce a parity symmetry

$$\begin{array}{ll} Q \rightarrow -Q & \text{Equivalent to:} \\ H \rightarrow +H & \end{array} \quad \begin{array}{l} \phi_{SM} \rightarrow +\phi_{SM} \\ \tilde{\phi}_{SP} \rightarrow -\tilde{\phi}_{SP} \end{array}$$

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R Parity

Consequences of R_p

- Reduce effect on Electroweak Precision observables
- Must pair produce superpartners
- Missing E_T if the LSP is neutral
- Dark Matter candidate

MSSM

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There are no observed superpartners with the same masses as standard model particles.

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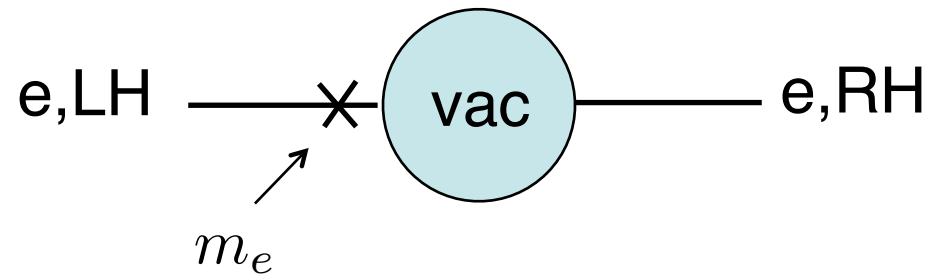
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Give Masses to SP's

Remember the electron:

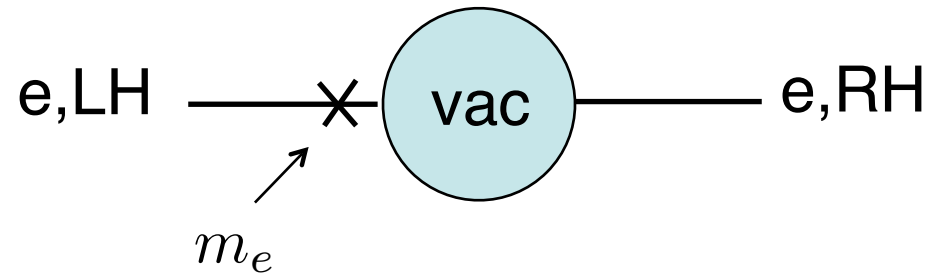
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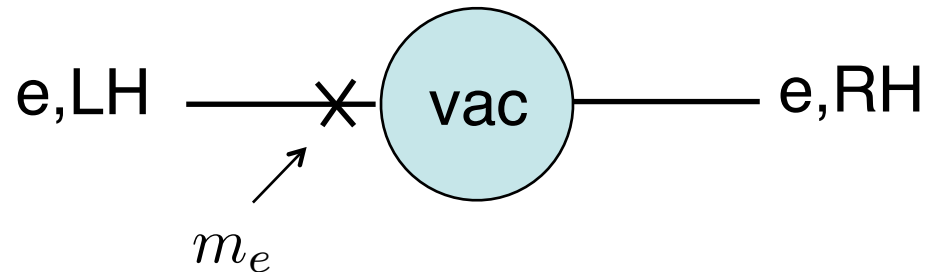
Remember the electron:



$$\delta m_e \sim \epsilon m_e \ln \Lambda \quad (\text{dimensional analysis})$$

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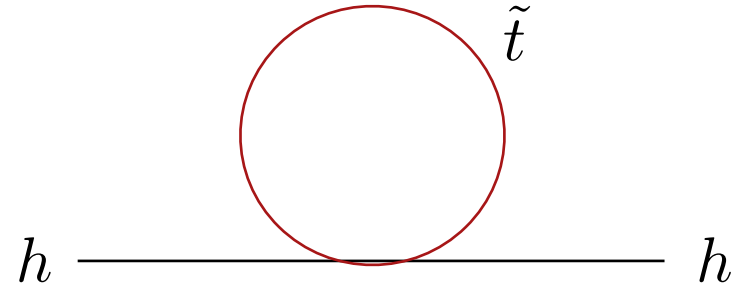
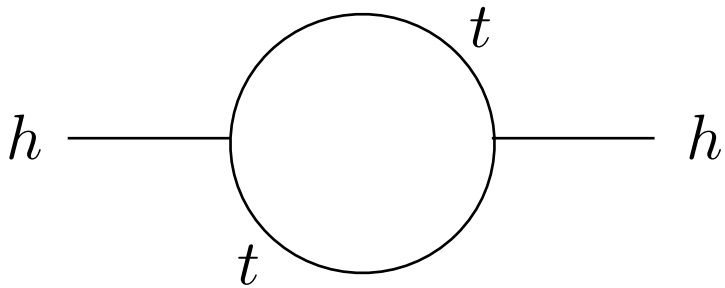


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Similarly, contributions to the Higgs mass will be proportional to the mass of superpartners (the 'mass' of supersymmetry breaking).

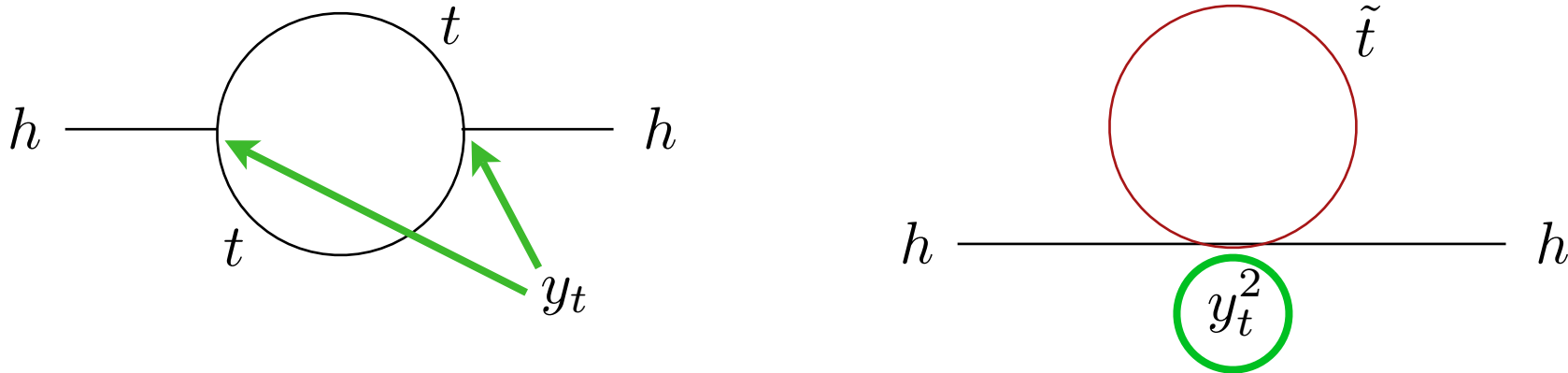
Supersymmetry could be an approximate symmetry and still stabilize the Higgs mass scale (solve the hierarchy problem).

Top Loop Cancellation



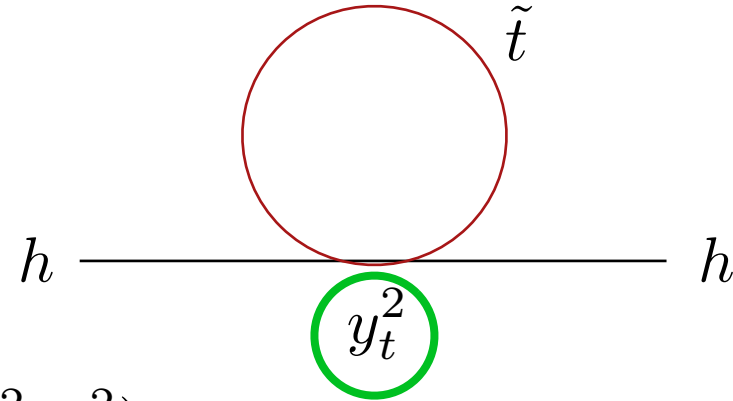
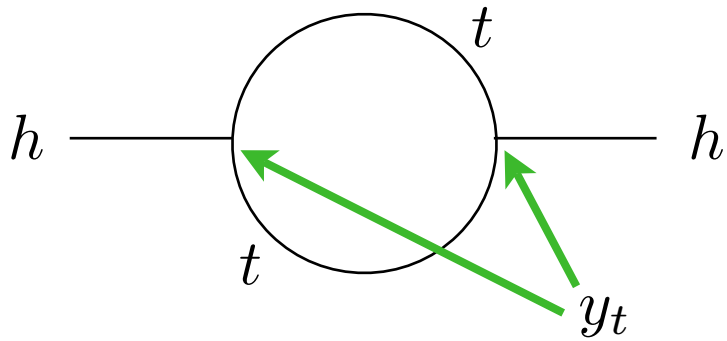
Exact supersymmetry - cancellation exact (up to w.f. ren.)

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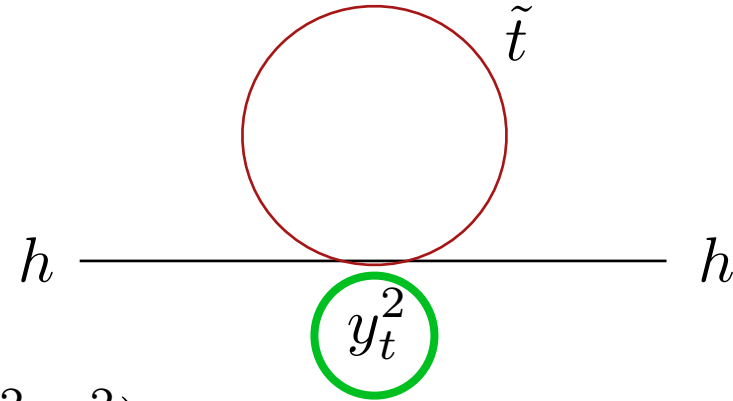
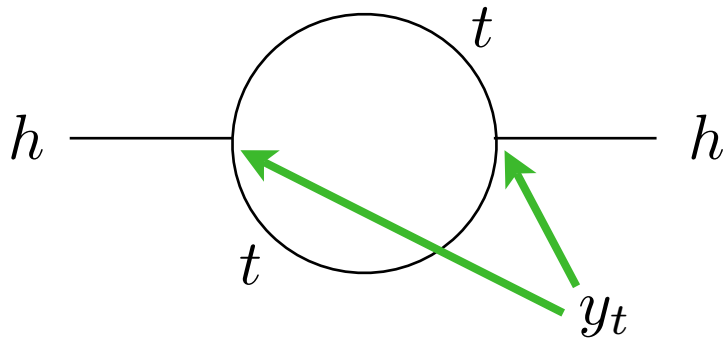
Top Loop Cancellation



Broken SUSY

$$\delta m_h^2 = f(m_t^2, m_{\tilde{t}}^2, y_t^2)$$

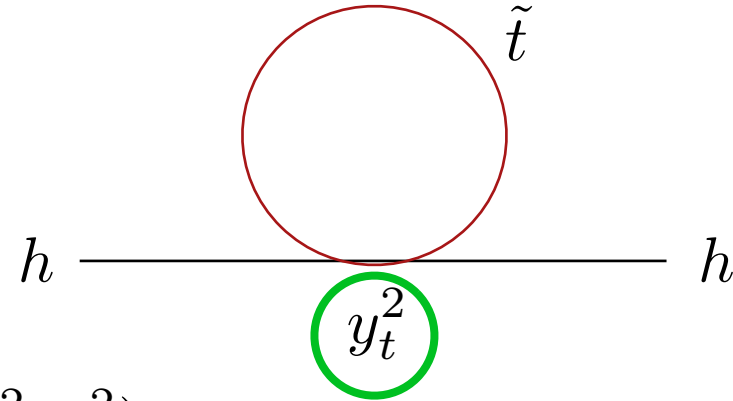
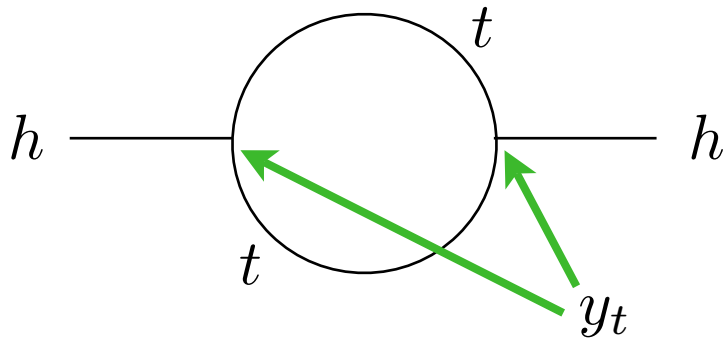
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$$m_{\tilde{t}}^2 \neq m_t^2 \rightarrow \delta m_h^2 \propto (m_{\tilde{t}}^2 - m_t^2) \ln \Lambda \quad \text{Soft breaking}$$

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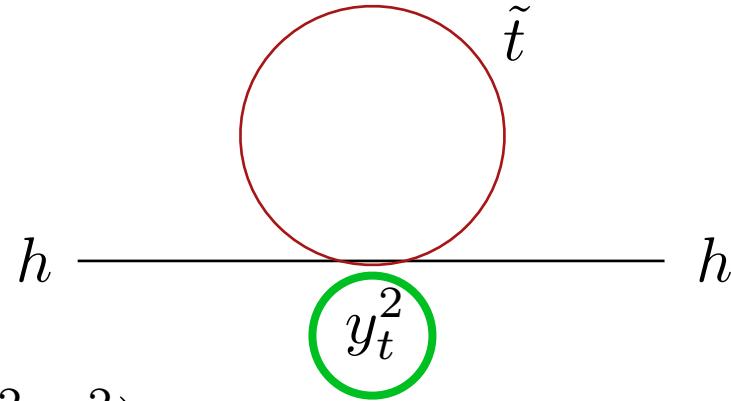
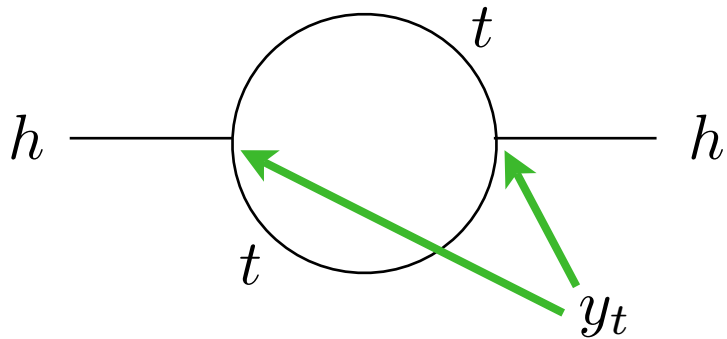


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remove the scalar top (“stop”) Hard breaking

Number of Parameters

Masses for everybody.

- Scalar partners of LH fermions
- Scalar partners of RH fermions
- L-R masses after the Higgs gets a vev (A terms)
- Higgs mass parameters

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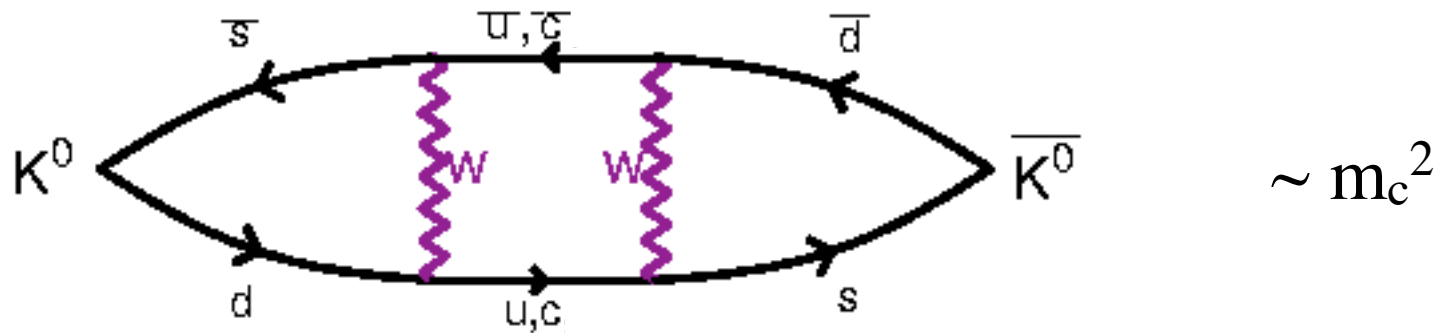
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108 New Parameters (minus 1)

Parameters: Soft Masses

$$\begin{aligned}\mathcal{L}_{\text{soft}}^{\text{MSSM}} = & -\frac{1}{2} \left(M_3 \tilde{g}\tilde{g} + M_2 \tilde{W}\tilde{W} + M_1 \tilde{B}\tilde{B} + \text{c.c.} \right) \\ & - \left(\tilde{u} \mathbf{a}_u \tilde{Q} H_u - \tilde{d} \mathbf{a}_d \tilde{Q} H_d - \tilde{e} \mathbf{a}_e \tilde{L} H_d + \text{c.c.} \right) \\ & - \tilde{Q}^\dagger \mathbf{m}_Q^2 \tilde{Q} - \tilde{L}^\dagger \mathbf{m}_L^2 \tilde{L} - \tilde{u} \mathbf{m}_u^2 \tilde{u}^\dagger - \tilde{d} \mathbf{m}_d^2 \tilde{d}^\dagger - \tilde{e} \mathbf{m}_e^2 \tilde{e}^\dagger \\ & - m_{H_u}^2 H_u^* H_u - m_{H_d}^2 H_d^* H_d - (b H_u H_d + \text{c.c.}) .\end{aligned}$$

Flavor Constraints



Small in the standard model because the CKM matrix is unitary

$$V_{ud}^* V_{us} + V_{cd}^* V_{cs} + V_{td}^* V_{ts} = 0$$

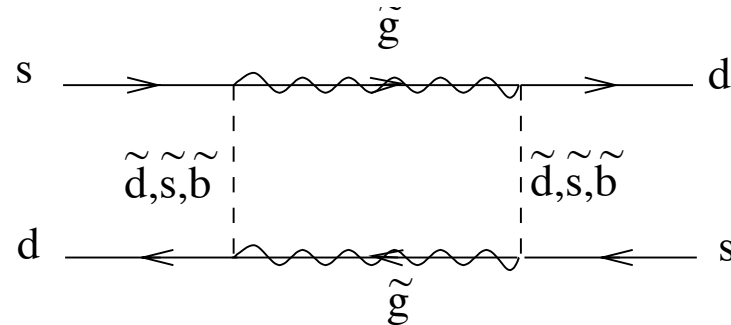
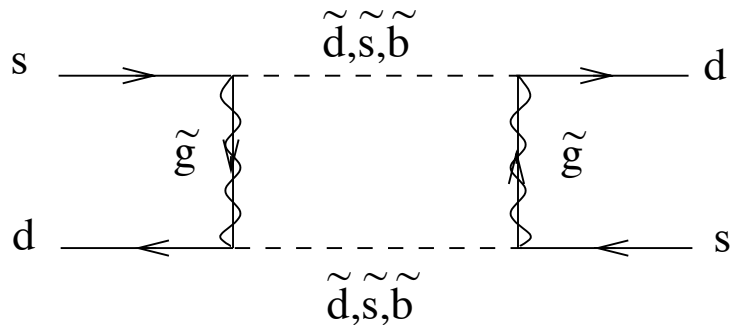
Soft Masses and Flavor

$$\begin{pmatrix} \tilde{d} & \tilde{s} & \tilde{b} \end{pmatrix}^* \cdot \begin{pmatrix} \tilde{m}_{dd}^2 & \tilde{m}_{ds}^2 & \tilde{m}_{db}^2 \\ \tilde{m}_{sd}^2 & \tilde{m}_{ss}^2 & \tilde{m}_{sb}^2 \\ \tilde{m}_{bd}^2 & \tilde{m}_{bs}^2 & \tilde{m}_{bb}^2 \end{pmatrix} \cdot \begin{pmatrix} \tilde{d} \\ \tilde{s} \\ \tilde{b} \end{pmatrix}$$

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$$\frac{m_{\tilde{d}\tilde{s}}^2}{m_{\tilde{s}\tilde{s}}^2} < \text{few} \times 10^{-4} \quad \text{for} \quad m_{\tilde{q}}^2 = 500 \text{ GeV}$$

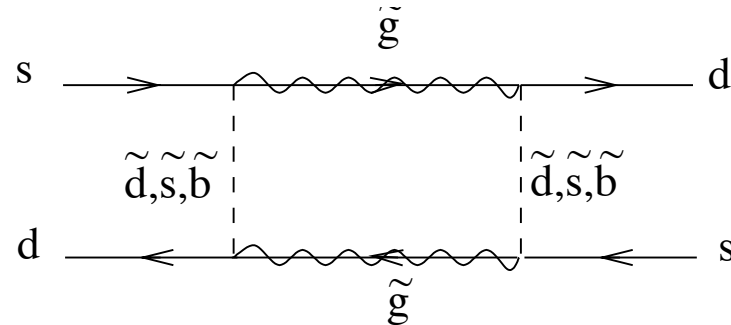
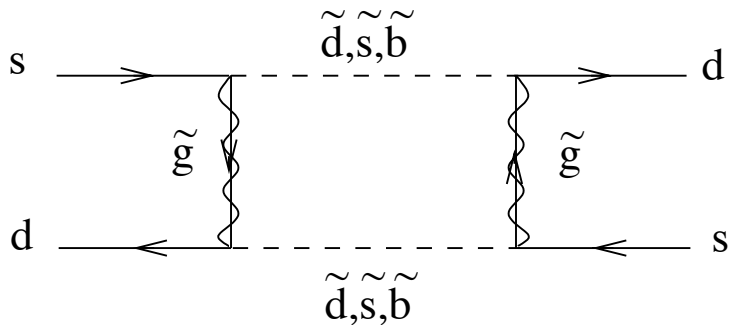


Soft Masses and Flavor

Important because standard model process is also a loop

The problem goes away if the scalar masses are degenerate.

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Soft Masses

$$\begin{aligned}
 \mathcal{L}_{\text{soft}}^{\text{MSSM}} = & -\frac{1}{2} \left(M_3 \tilde{g} \tilde{g} + M_2 \tilde{W} \tilde{W} + M_1 \tilde{B} \tilde{B} + \text{c.c.} \right) \\
 & - \left(\tilde{u} \mathbf{a}_u \tilde{Q} H_u - \tilde{d} \mathbf{a}_d \tilde{Q} H_d - \tilde{e} \mathbf{a}_e \tilde{L} H_d + \text{c.c.} \right) \\
 & - \tilde{Q}^\dagger \mathbf{m}_Q^2 \tilde{Q} - \tilde{L}^\dagger \mathbf{m}_L^2 \tilde{L} - \tilde{u} \mathbf{m}_u^2 \tilde{u}^\dagger - \tilde{d} \mathbf{m}_d^2 \tilde{d}^\dagger - \tilde{e} \mathbf{m}_e^2 \tilde{e}^\dagger \\
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 \end{aligned}$$

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 \mathcal{L}_{\text{soft}}^{\text{MSSM}} = & -\frac{1}{2} \left(M_3 \tilde{g} \tilde{g} + M_2 \tilde{W} \tilde{W} + M_1 \tilde{B} \tilde{B} + \text{c.c.} \right) \\
 & - \left(\tilde{u} \mathbf{a}_u \tilde{Q} H_u - \tilde{d} \mathbf{a}_d \tilde{Q} H_d - \tilde{e} \mathbf{a}_e \tilde{L} H_d + \text{c.c.} \right) \\
 & - \tilde{Q}^\dagger \mathbf{m}_Q^2 \tilde{Q} - \tilde{L}^\dagger \mathbf{m}_L^2 \tilde{L} - \tilde{u} \mathbf{m}_u^2 \tilde{u}^\dagger - \tilde{d} \mathbf{m}_d^2 \tilde{d}^\dagger - \tilde{e} \mathbf{m}_e^2 \tilde{e}^\dagger \\
 & - m_{H_u}^2 H_u^* H_u - m_{H_d}^2 H_d^* H_d - (b H_u H_d + \text{c.c.}) .
 \end{aligned}$$

single
parameters
times the
identity
matrix

Soft Masses

proportional
to Yukawa
couplings

$$\begin{aligned}
 \mathcal{L}_{\text{soft}}^{\text{MSSM}} = & -\frac{1}{2} \left(M_3 \tilde{g} \tilde{g} + M_2 \tilde{W} \tilde{W} + M_1 \tilde{B} \tilde{B} + \text{c.c.} \right) \\
 & - \left(\tilde{u} \mathbf{a}_u \tilde{Q} H_u - \tilde{d} \mathbf{a}_d \tilde{Q} H_d - \tilde{e} \mathbf{a}_e \tilde{L} H_d + \text{c.c.} \right) \\
 & - \tilde{Q}^\dagger \mathbf{m}_Q^2 \tilde{Q} - \tilde{L}^\dagger \mathbf{m}_L^2 \tilde{L} - \tilde{u} \mathbf{m}_u^2 \tilde{u}^\dagger - \tilde{d} \mathbf{m}_d^2 \tilde{d}^\dagger - \tilde{e} \mathbf{m}_e^2 \tilde{e}^\dagger \\
 & - m_{H_u}^2 H_u^* H_u - m_{H_d}^2 H_d^* H_d - (b H_u H_d + \text{c.c.}) .
 \end{aligned}$$

single
parameters
times the
identity
matrix

$$\mathbf{a}_u = \mathbf{y}_u A_u$$

Simplified Parameter Space

gaugino masses: $M_{1,2,3}$

squarks and sleptons: $m_{q,u,d,l,e}$

scalar³ : $A_{u,d,l}$

higgs masses: $m_{1,2}$ & b

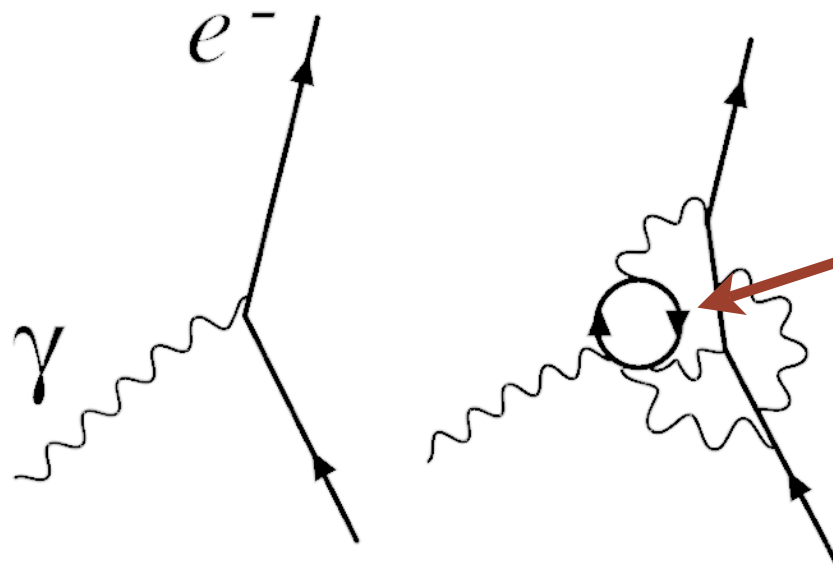
All real: 14 parameters (μ is exchanged for the Z-mass)

b can be exchanged for $\tan \beta$

Sign of μ remains

Interlude: Unification

Renormalizing Couplings

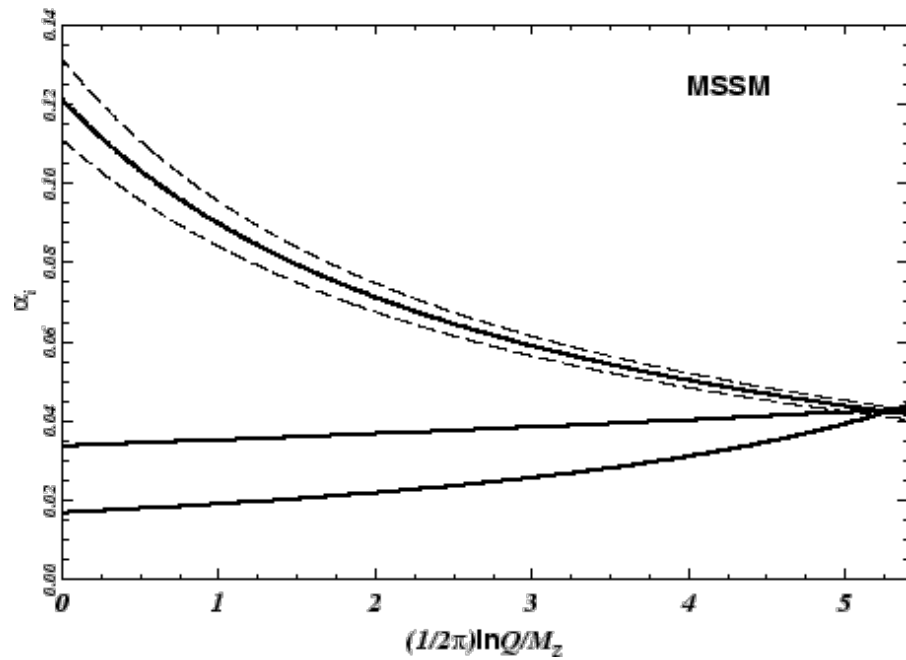


new particles could run in this loop if they were lighter than the Z boson

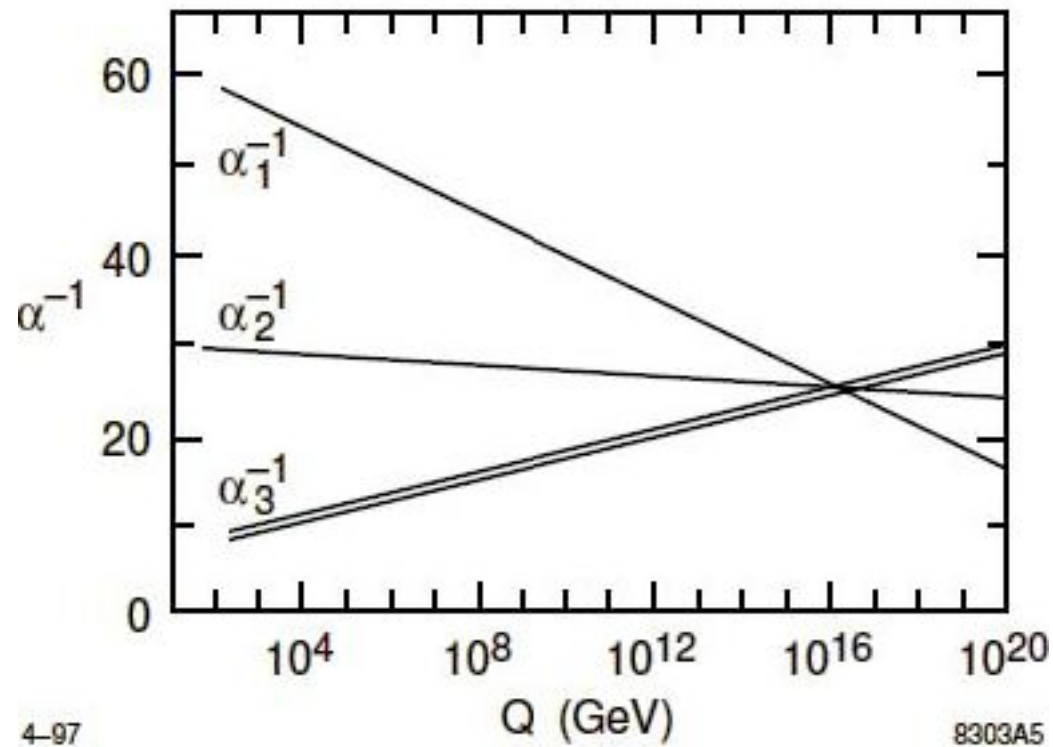
$$\alpha(1 \text{ eV}) \simeq \frac{1}{137}$$

$$\alpha(M_Z) \simeq \frac{1}{128}$$

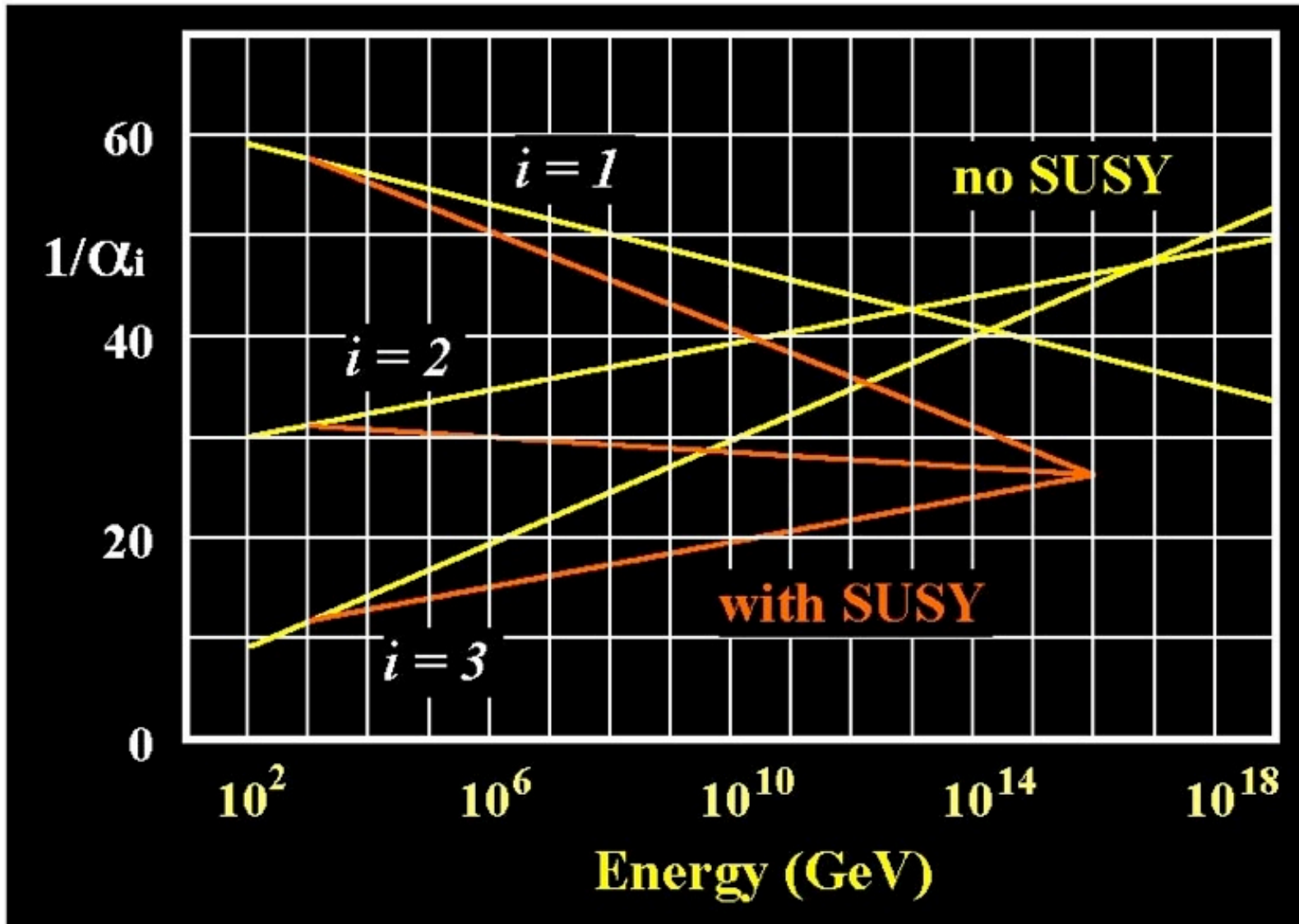
Running Gauge Couplings



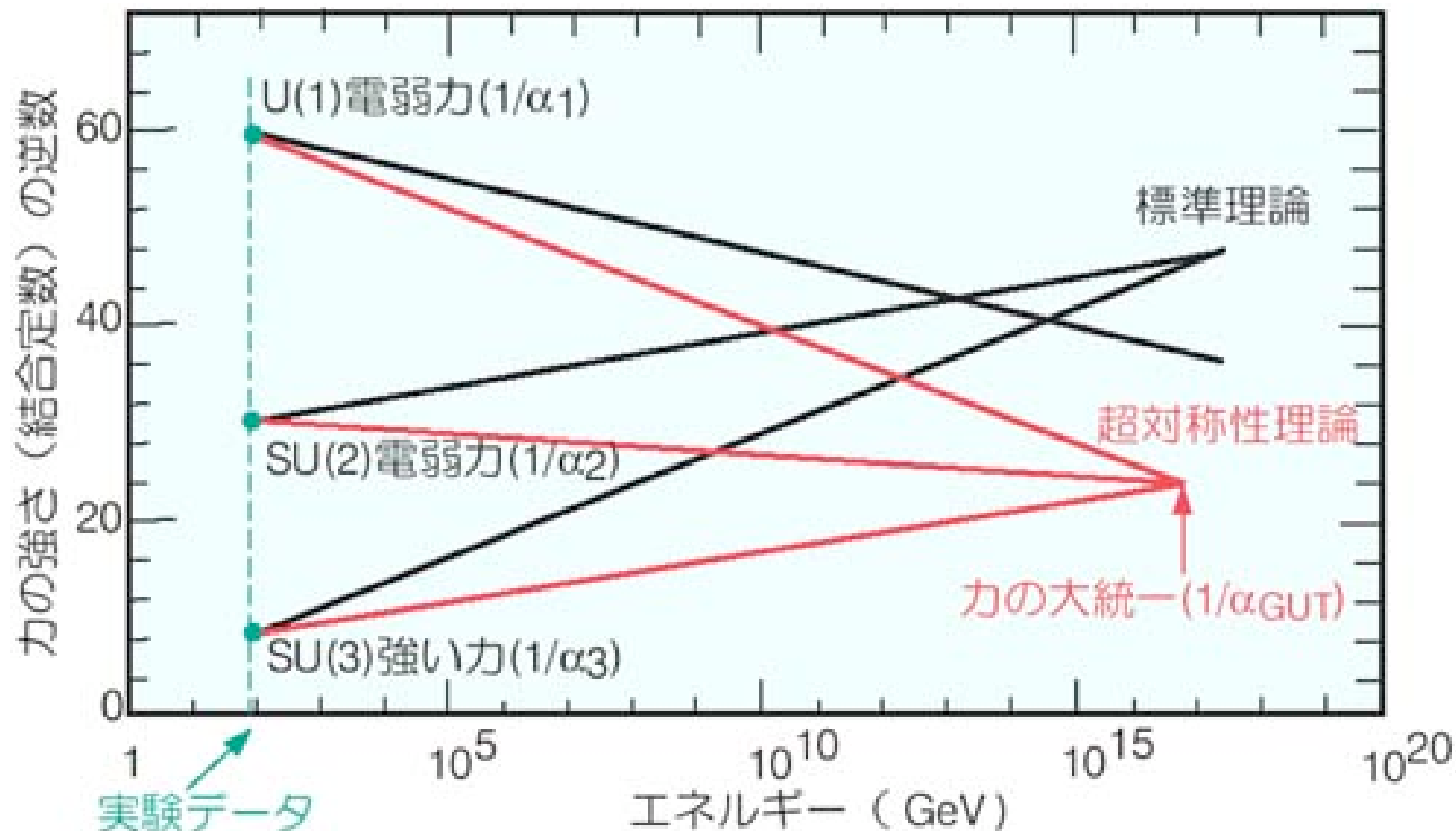
Running Gauge Couplings



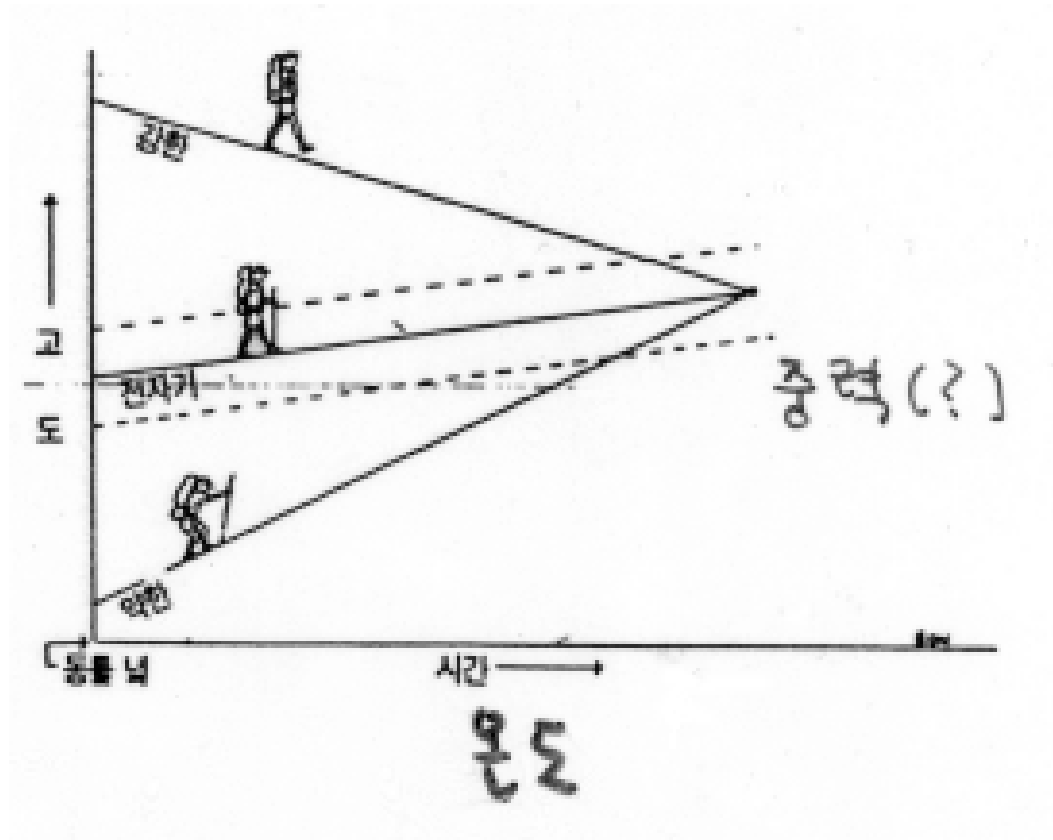
Running Gauge Couplings



Running Gauge Couplings



Running Gauge Couplings



Simplification or Model

Pick a universal mass for all scalar partners, and another for all gauginos.

mSUGRA

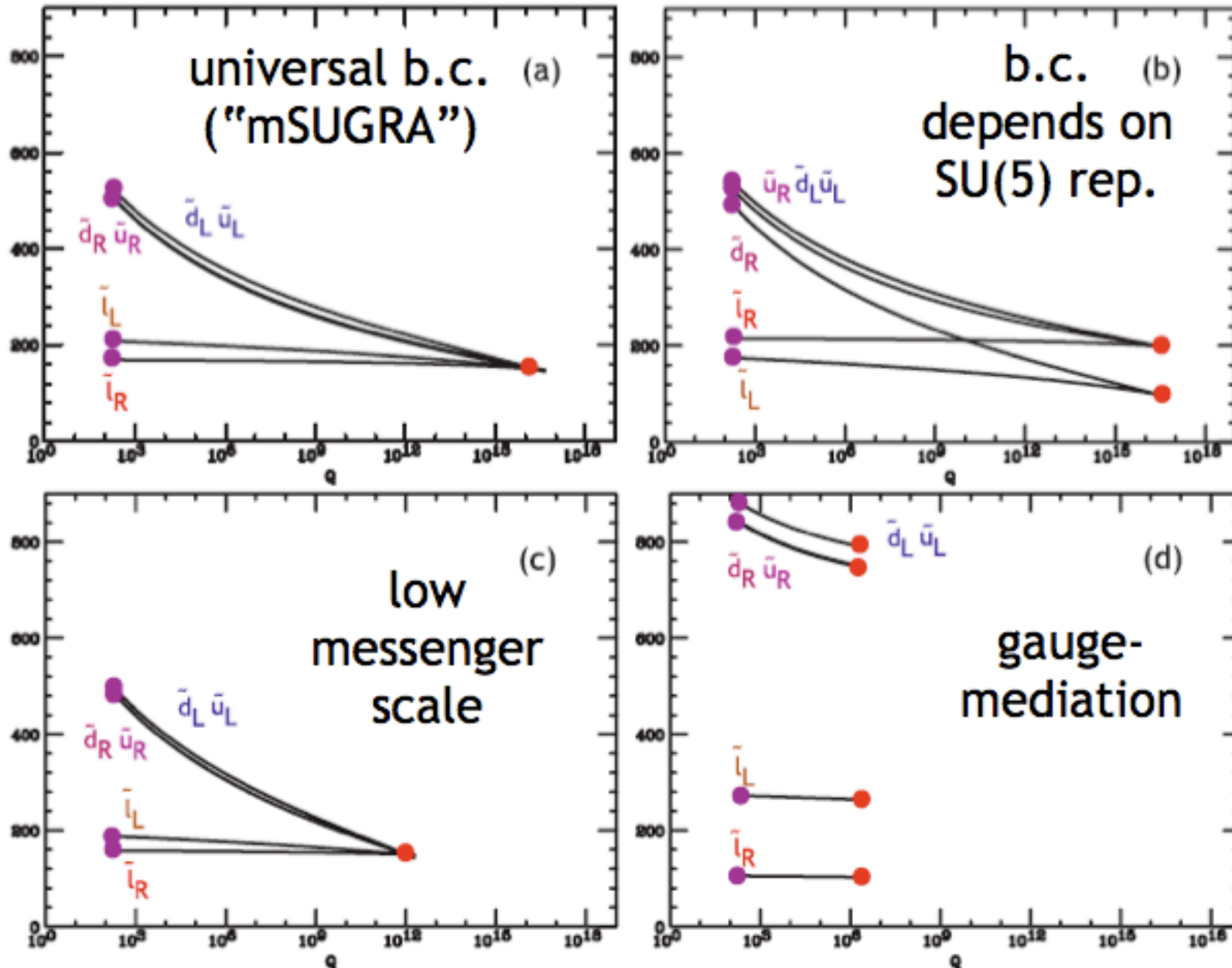
$m_0, M_{1/2}, A, \tan \beta, \text{sgn}(\mu)$

Models that automatically solve the flavor problem

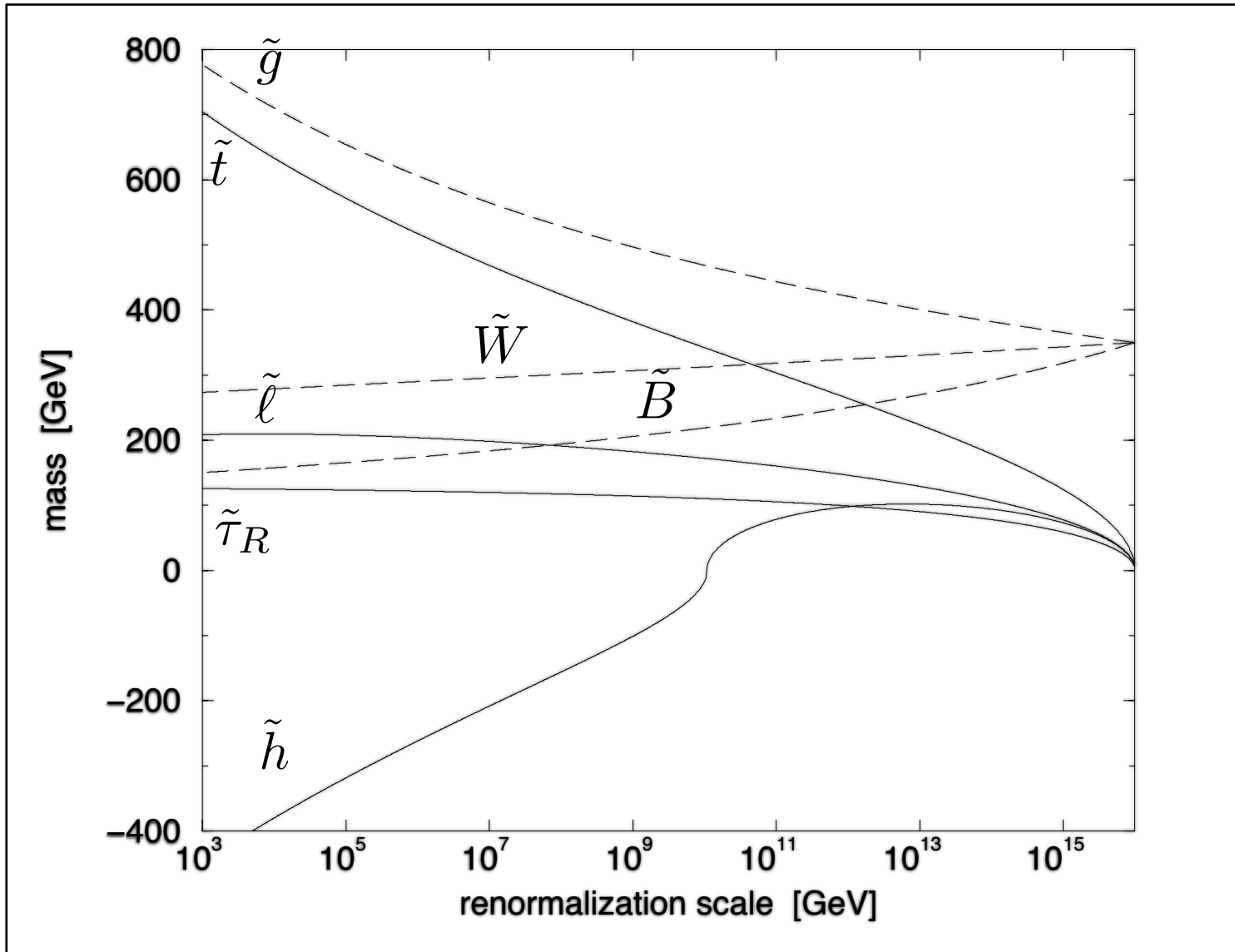
- Gauge Mediation: 3.5
- Anomaly Mediation: 2.5-5.5
- Gaugino Mediation: 1.5-4.5
- ...

Simplified parameter spaces

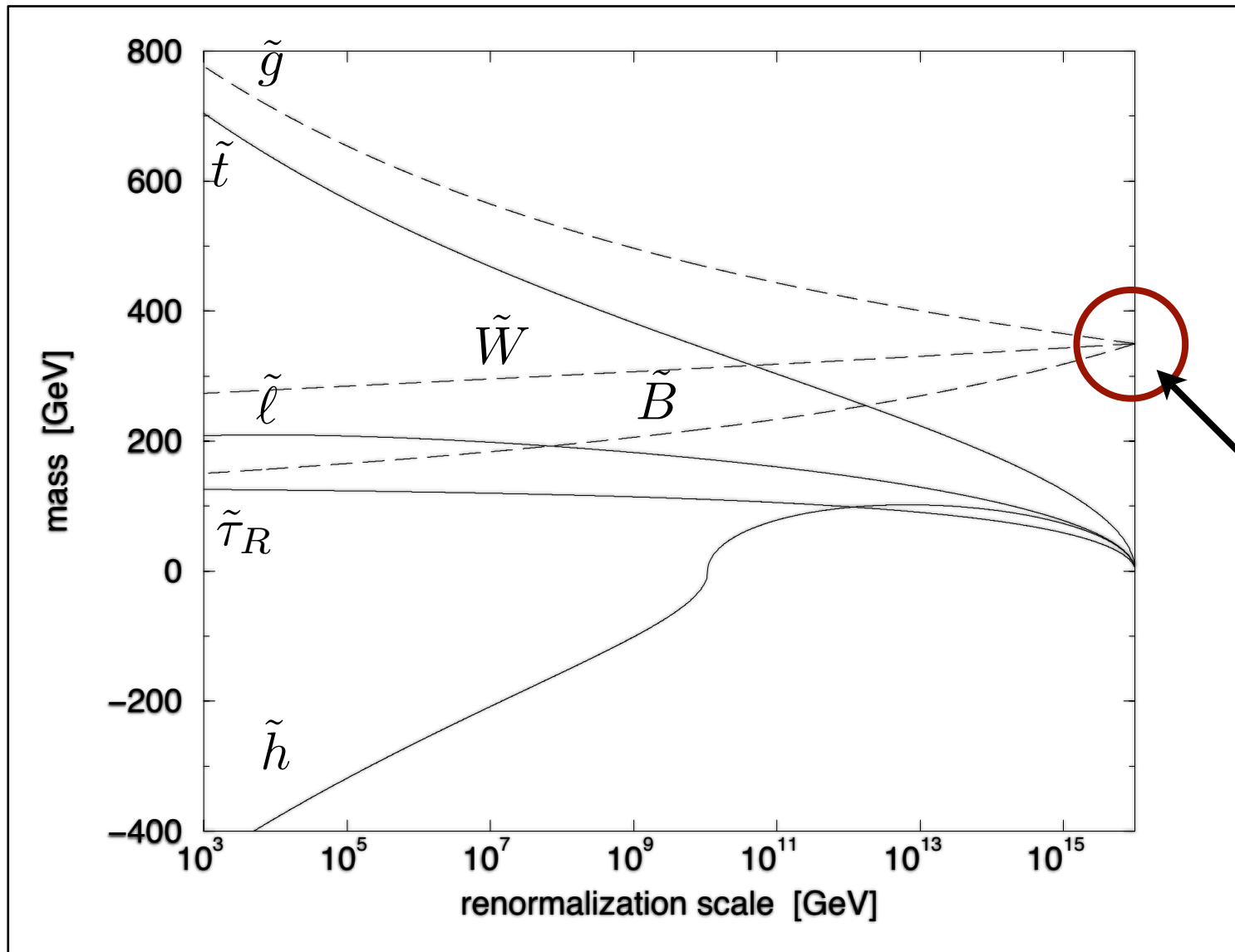
Typical Spectra



Scalars Driven by Gauginos



Scalars Driven by Gauginos



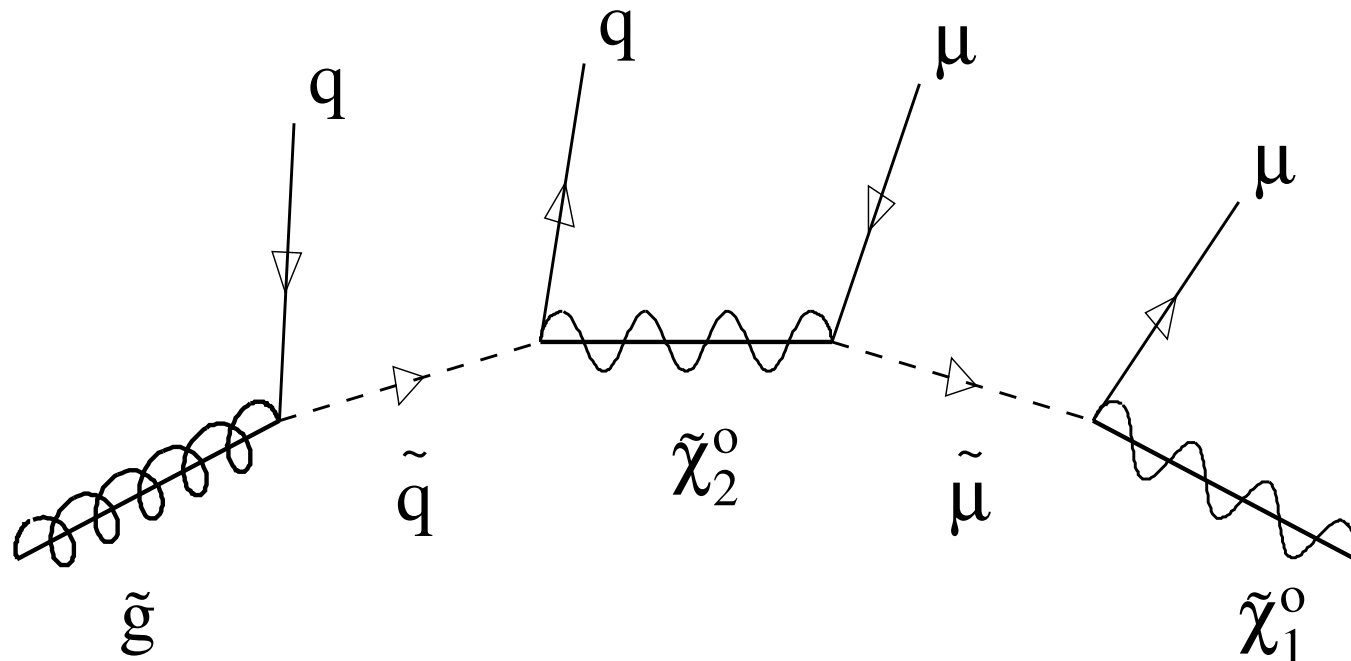
assume
unified

Cascades

Goal: SUSY spectra via cascade decay kinematics

e.g. $\tilde{g} \rightarrow \tilde{q}\bar{q} \rightarrow \chi_2^0 q\bar{q} \rightarrow \mu^+ \mu^- q\bar{q} \chi_1^0$

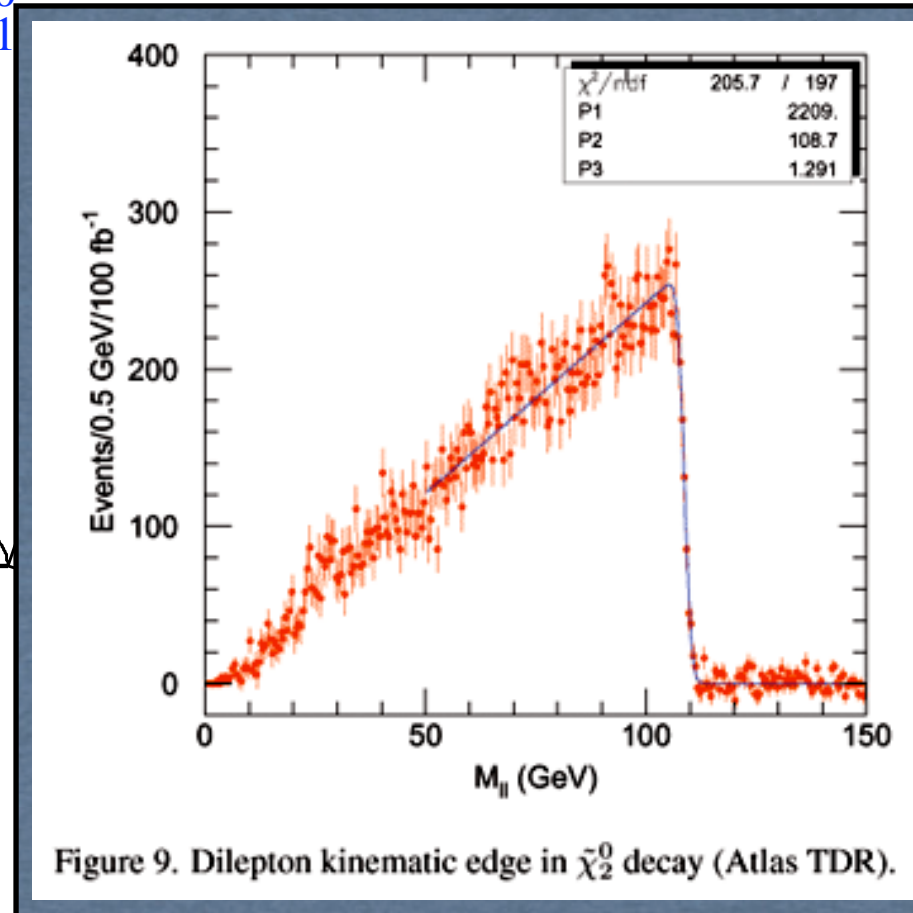
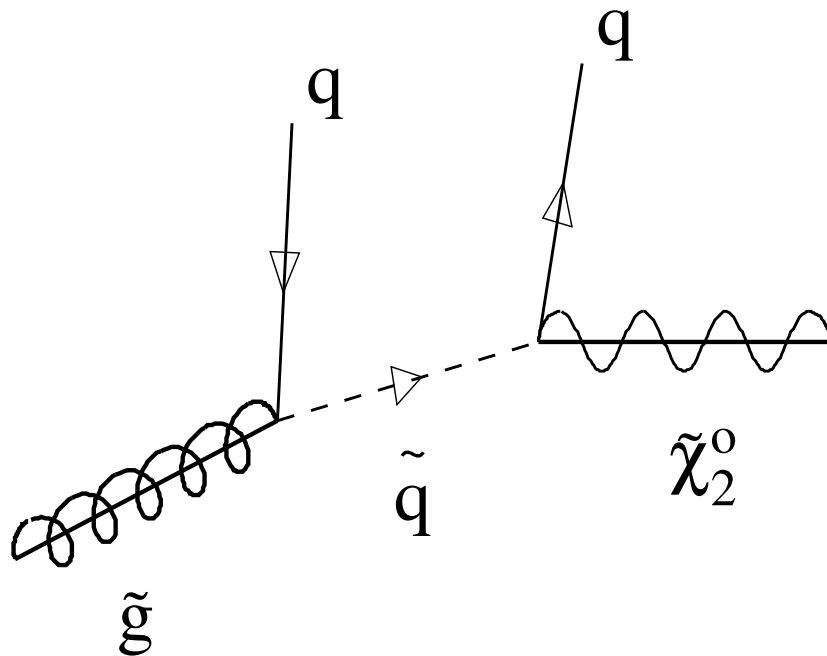
for $m_{\tilde{g}} > m_{\tilde{q}}$



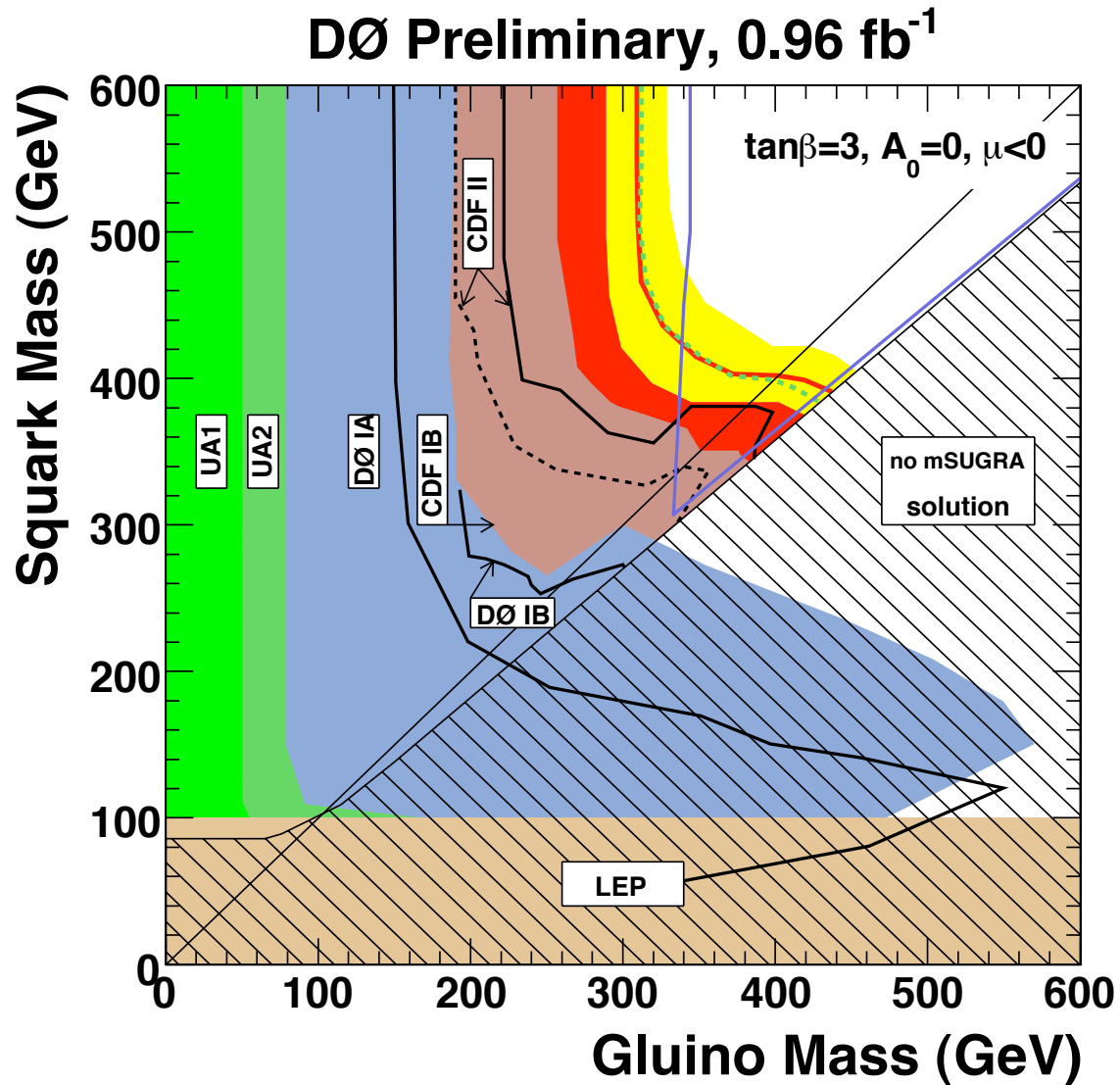
Cascades

Goal: SUSY spectra via cascade decay kinematics

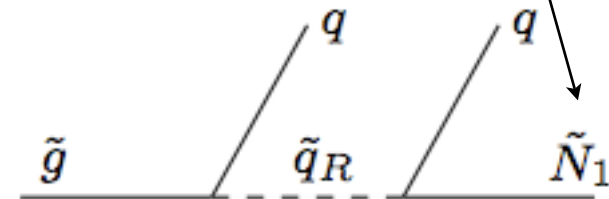
e.g. $\tilde{g} \rightarrow \tilde{q}\bar{q} \rightarrow \chi_2^0 q\bar{q} \rightarrow \mu^+ \mu^- q\bar{q} \chi_1^0$
 for $m_{\tilde{g}} > m_{\tilde{q}}$



Squarks/Gluinos

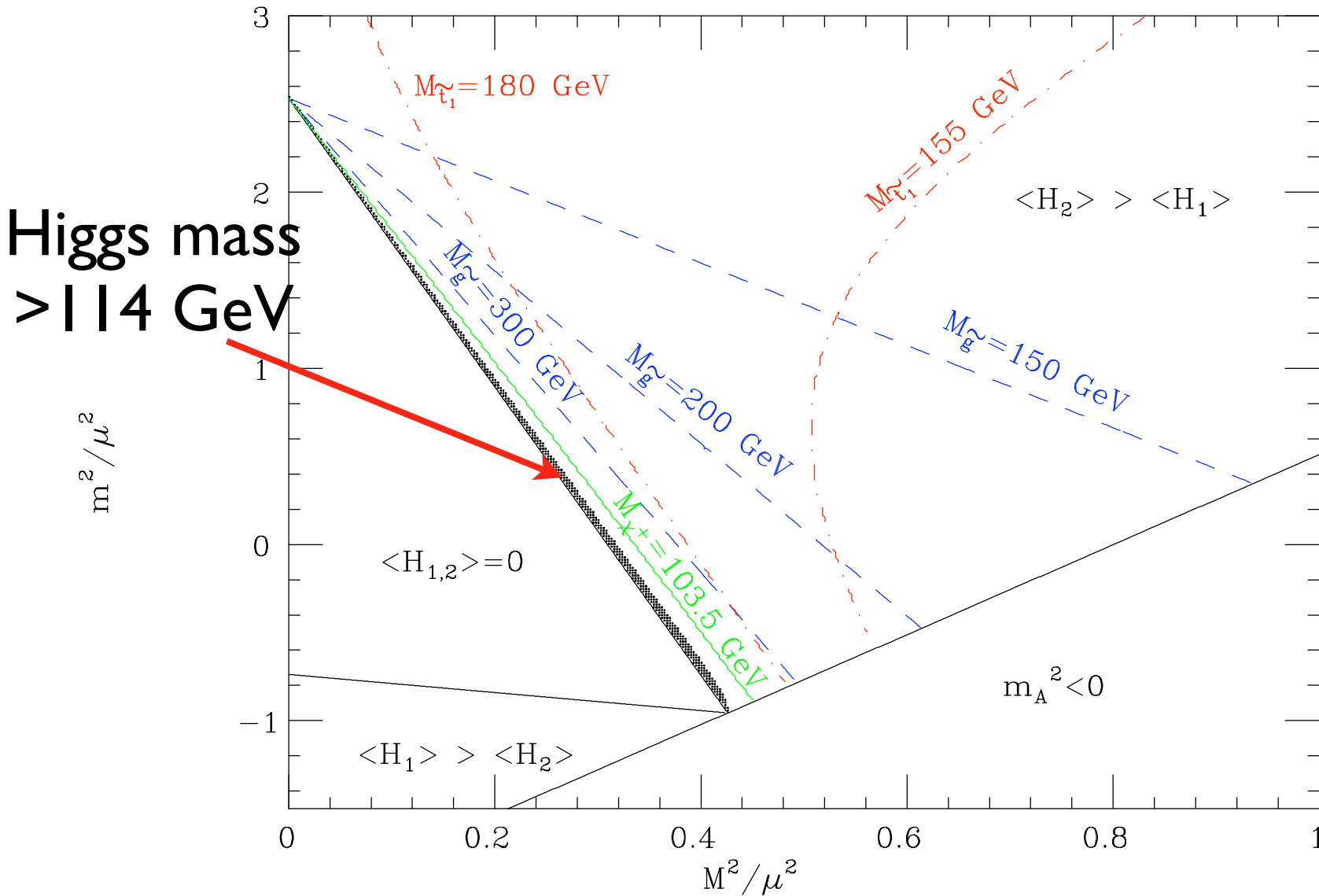


Jets + missing E_T



Unfortunately, mSUGRA
is a bit unNatural

State of mSUGRA



Giudice, Rattazzi '06

Problem with Higgs

$$\lambda|h|^4 \rightarrow \frac{g^2}{8} [|H_1|^2 - |H_2|^2]^2 \quad m_h = M_Z | \cos 2\beta |$$

$$(m_h^2)_{tree} + \delta m_h^2 > (114 \text{ GeV})^2$$

(Big Susy-breaking in top sector)

Problem with Higgs

$$\lambda|h|^4 \rightarrow \frac{g^2}{8} [|H_1|^2 - |H_2|^2]^2 \quad m_h = M_Z | \cos 2\beta |$$

$$(m_h^2)_{tree} + \delta m_h^2 > (114 \text{ GeV})^2 \quad (\text{Big Susy-breaking in top sector})$$

New tree-level contribution requires new fields:

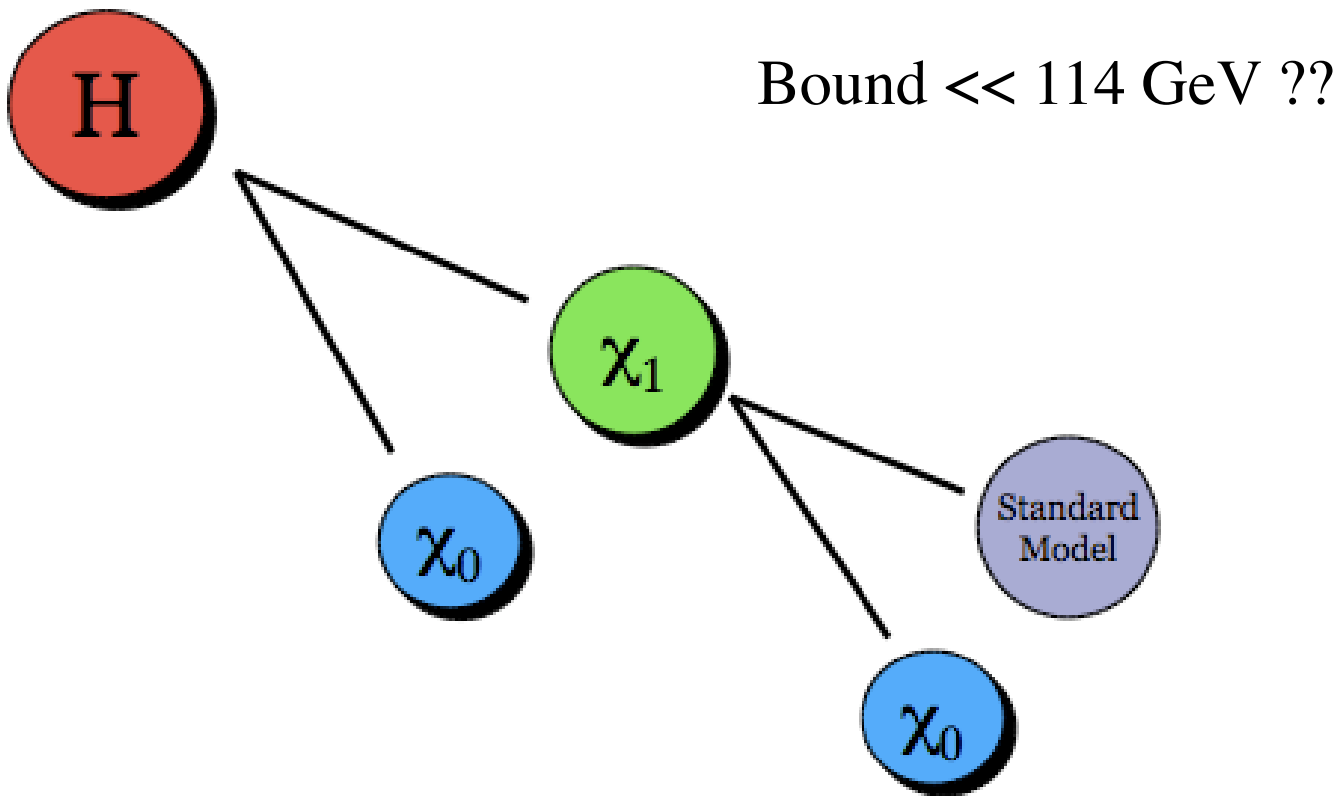
$$W = ySH_1H_2 \rightarrow y^2 |H_1H_2|^2$$

Adding a Singlet

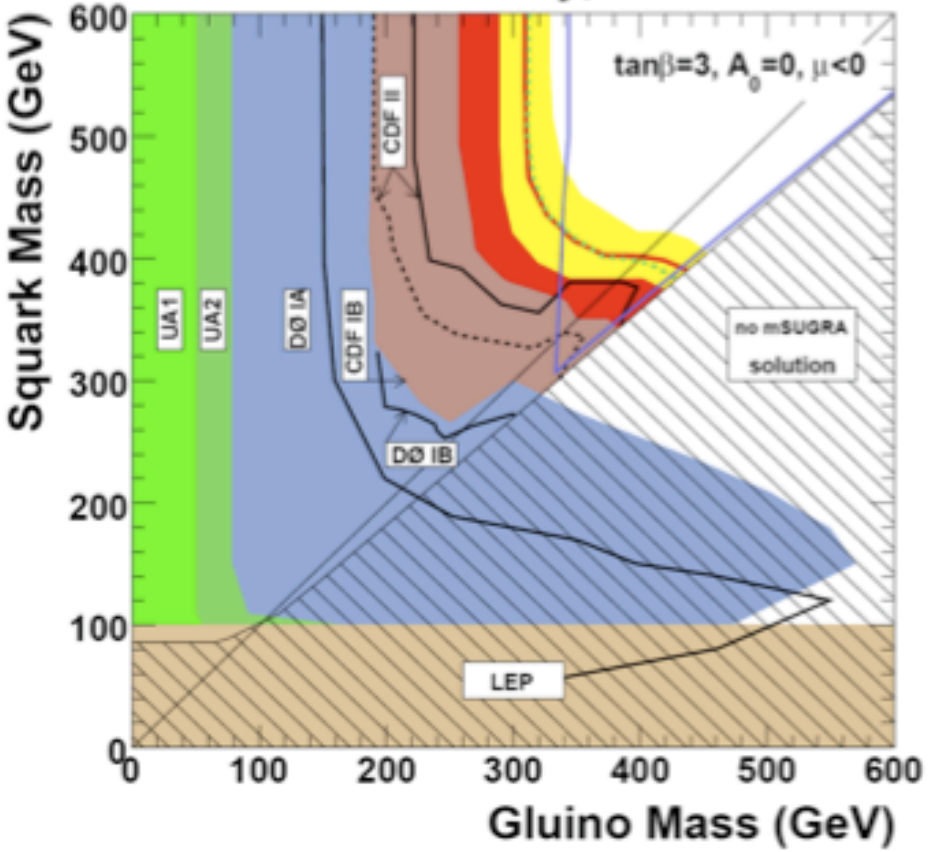
$$W = \lambda \hat{H}_u \hat{H}_d \hat{S} + \frac{\kappa}{3} \hat{S}^3$$

$$\mathbf{M}_{\tilde{N}} = \begin{pmatrix} M_1 & 0 & -g'v_d/\sqrt{2} & g'v_u/\sqrt{2} & 0 \\ 0 & M_2 & gv_d/\sqrt{2} & -gv_u/\sqrt{2} & 0 \\ -g'v_d/\sqrt{2} & gv_d/\sqrt{2} & 0 & -\lambda s & -\lambda v_u \\ g'v_u/\sqrt{2} & -gv_u/\sqrt{2} & -\lambda s & 0 & -\lambda v_d \\ 0 & 0 & -\lambda v_u & -\lambda v_d & 2\kappa s \end{pmatrix}$$

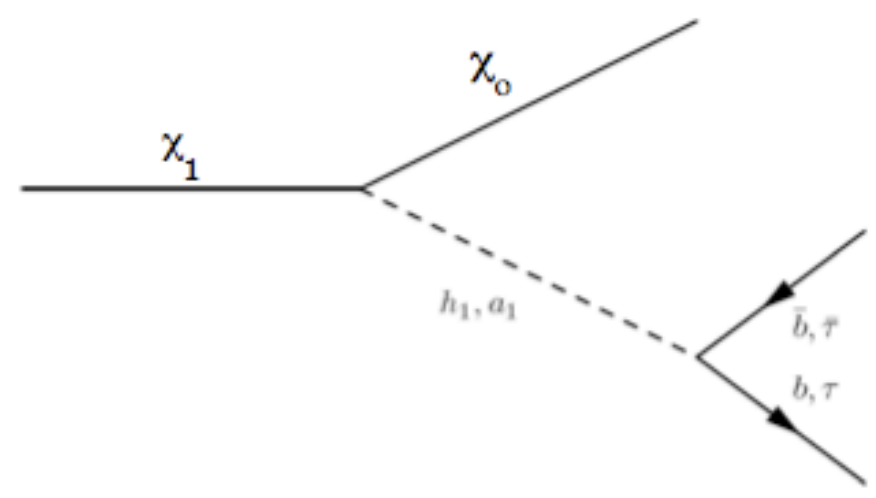
Higgs to Neutralinos



DØ Preliminary, 0.96 fb⁻¹



Missing Energy signature **suppressed**, e.g.



As m_a approaches m_{χ_1} , missing energy is reduced

Spectrum deviations

Add a light singlet and the squark
bounds reduce by ~ 100 GeV

Chang, Fox, Weiner - in progress

Change gaugino mass relations and a 70
GeV gluino may be allowed

Wacker, et al - in progress

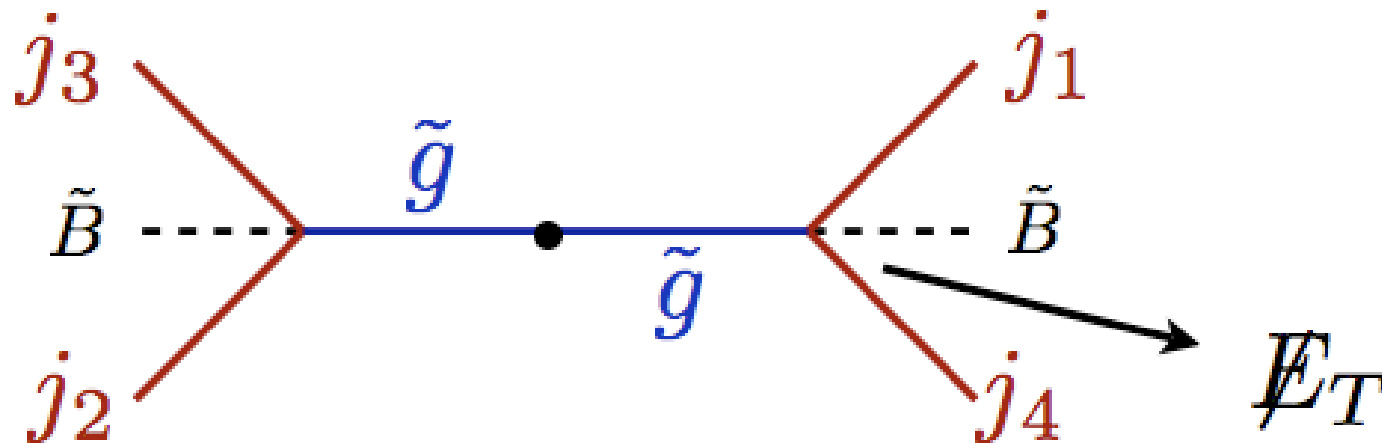
Gaugino Mass Ratio

$$M_3 : M_2 : M_1 \simeq 7 : 2 : 1$$

What if, for example, $M_2 > M_3 \gtrsim M_1$?

Generalizing the Ratio

What if, for example, $M_2 > M_3 \gtrsim M_1$?



$$Q = M_{\tilde{g}} - M_{\tilde{B}}$$

If $Q < M_{\tilde{B}}$

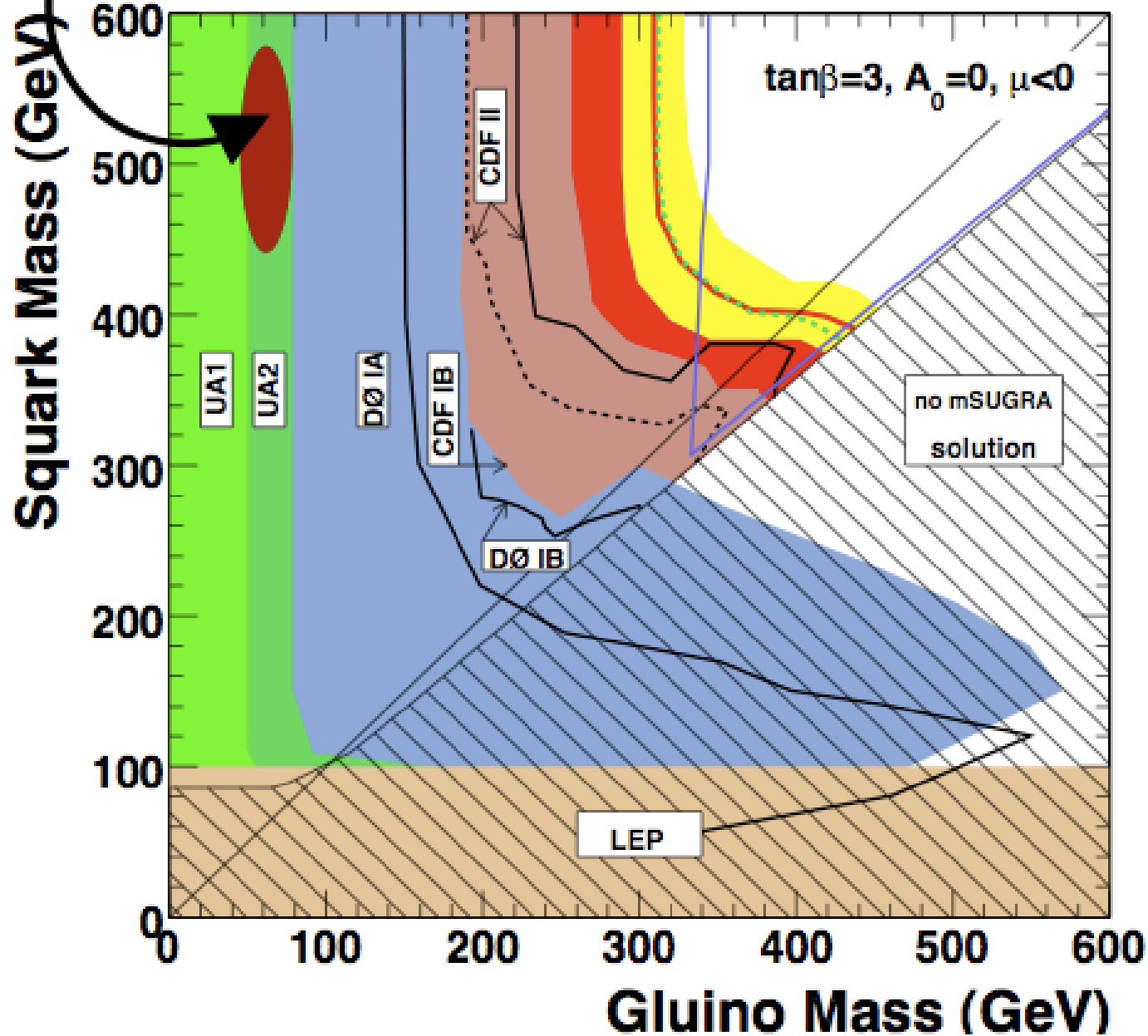
Bino carries away energy but not momentum

$$\cancel{E}_T \sim \frac{Q^2}{M_{\tilde{B}}}$$

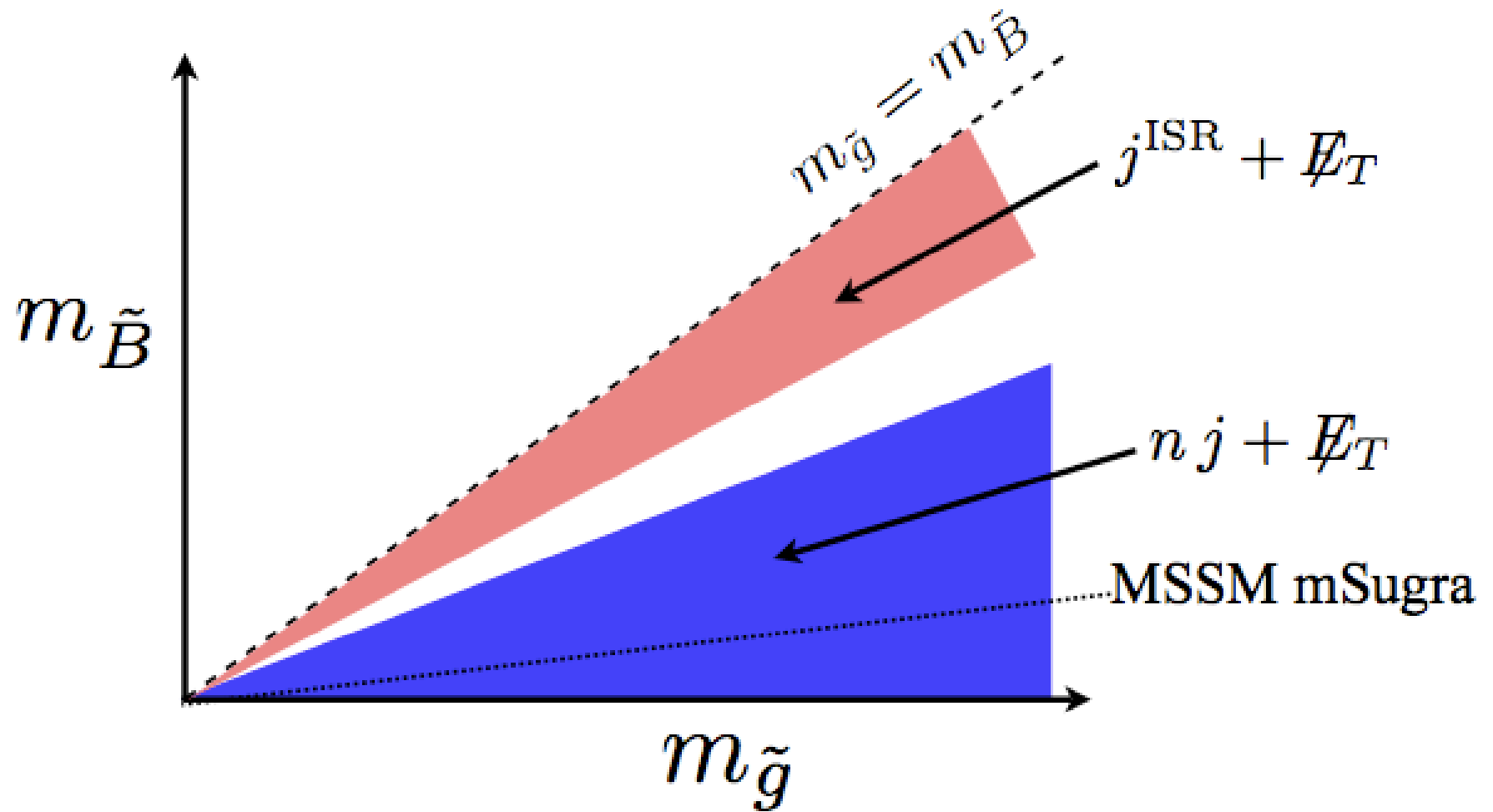
Take $M_{\tilde{B}} = 60 \text{ GeV} \dots$

70 GeV Gluinos!??

DØ Preliminary, 0.96 fb^{-1}



Preferred Bino/Gluino Plot



Wacker, et. al.

Ratio of 'ino's

$$M_3 > M_1 > M_2$$

AMSB - cascades with leptons.
LL charged particle

$$M_2 > M_3 > M_1$$

Only jets + missing E_T

$$M_1 > M_3 > M_2$$

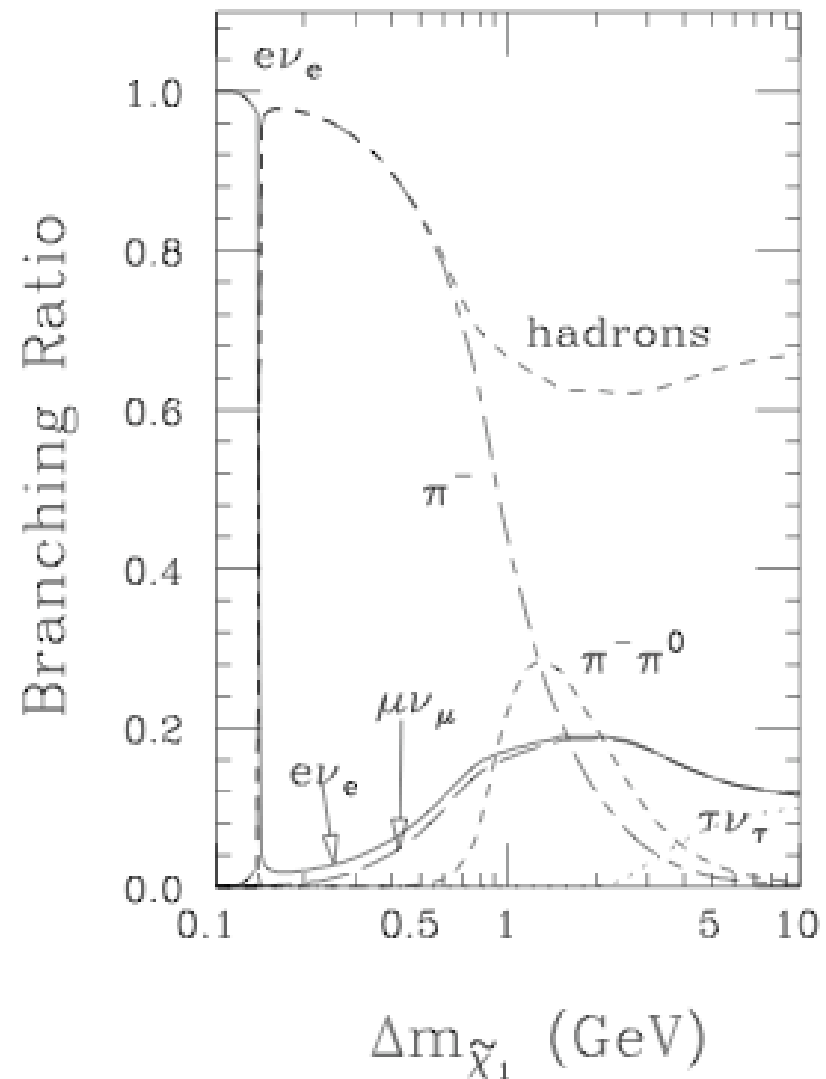
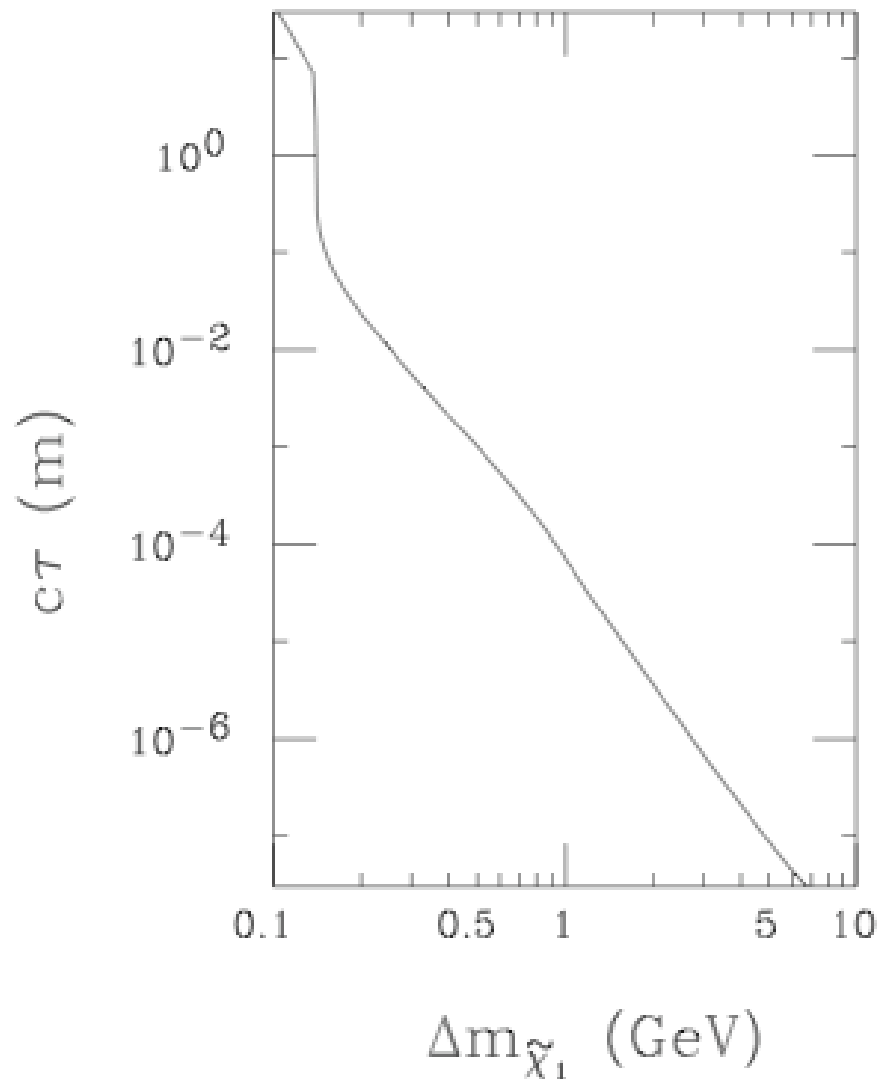
Jets plus missing E_T and/or LL
charged particle

$$M_2 > M_1 > M_3$$

Glino may be long lived - at
least 4-body decay

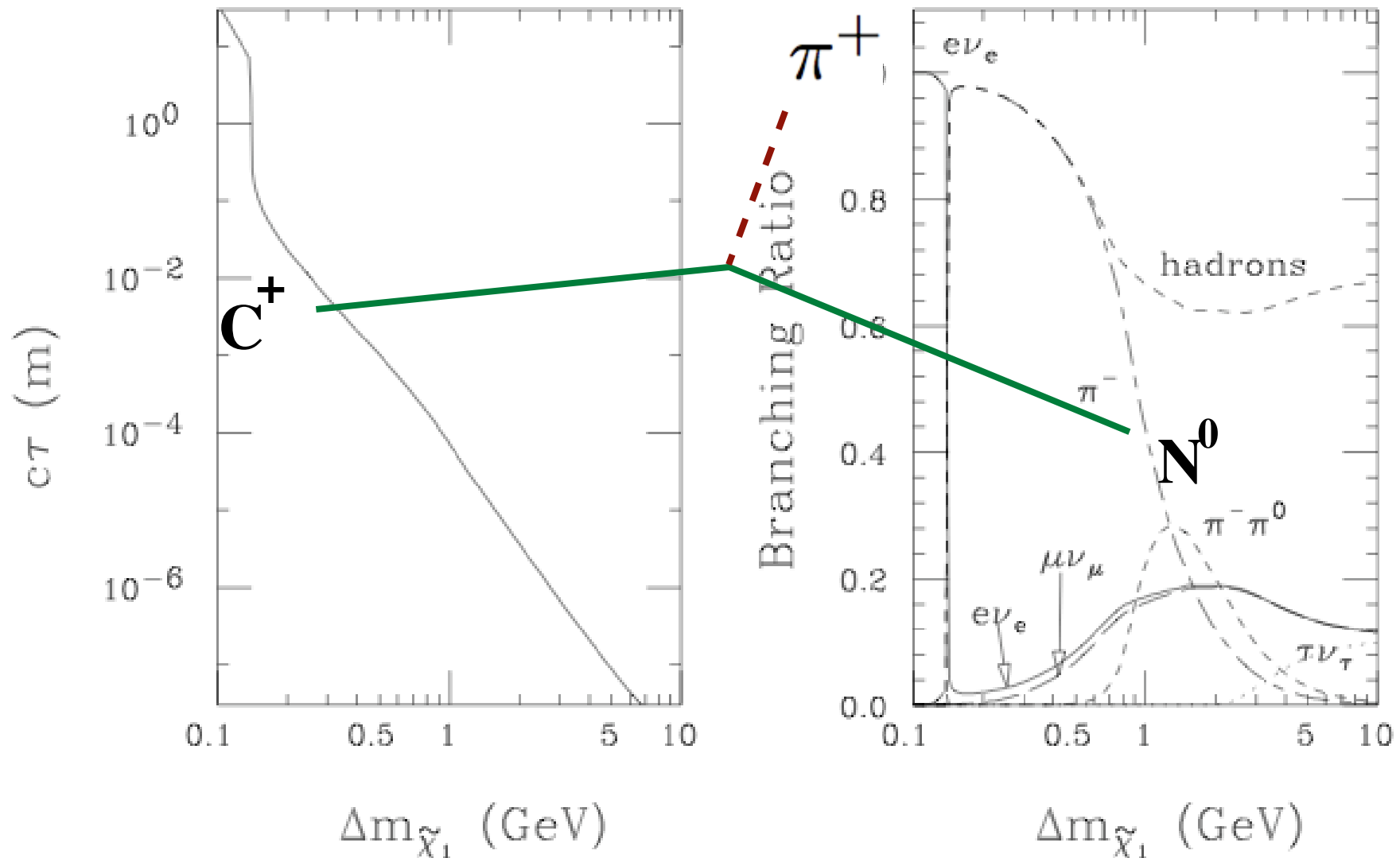
Lightest Chargino Decay

Large $|\mu|$ Limiting Case

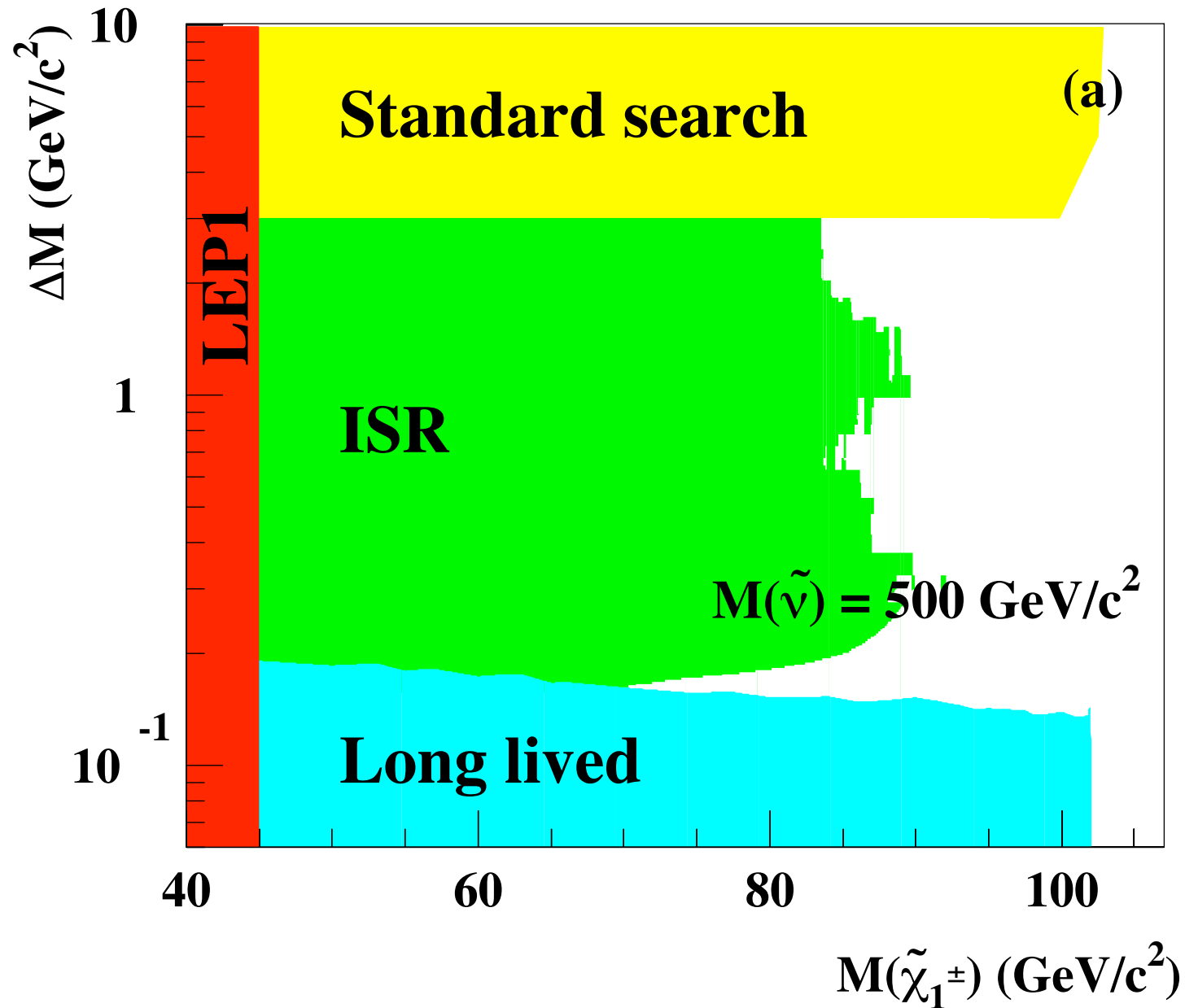


Lightest Chargino Decay

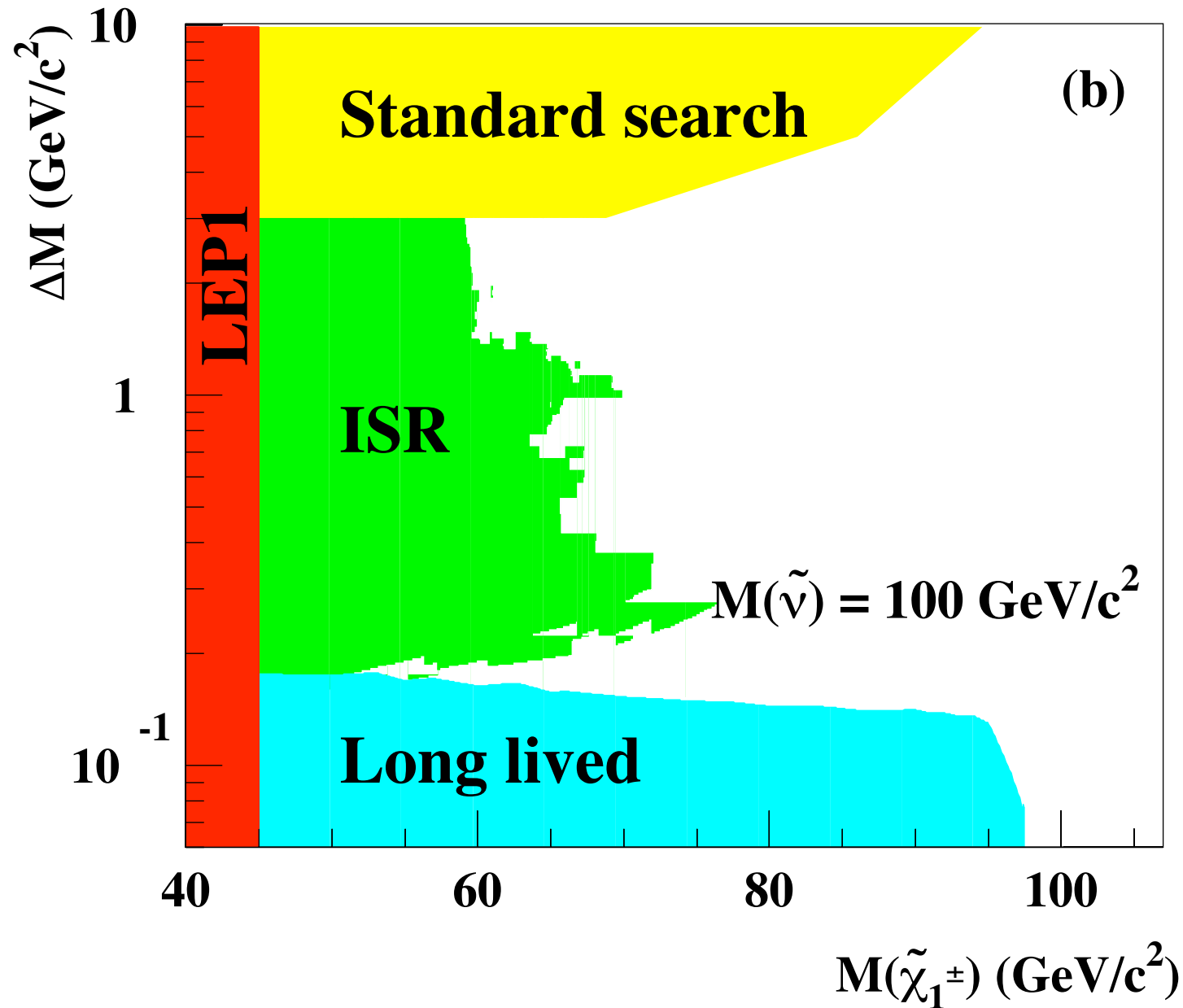
Large $|\mu|$ Limiting Case



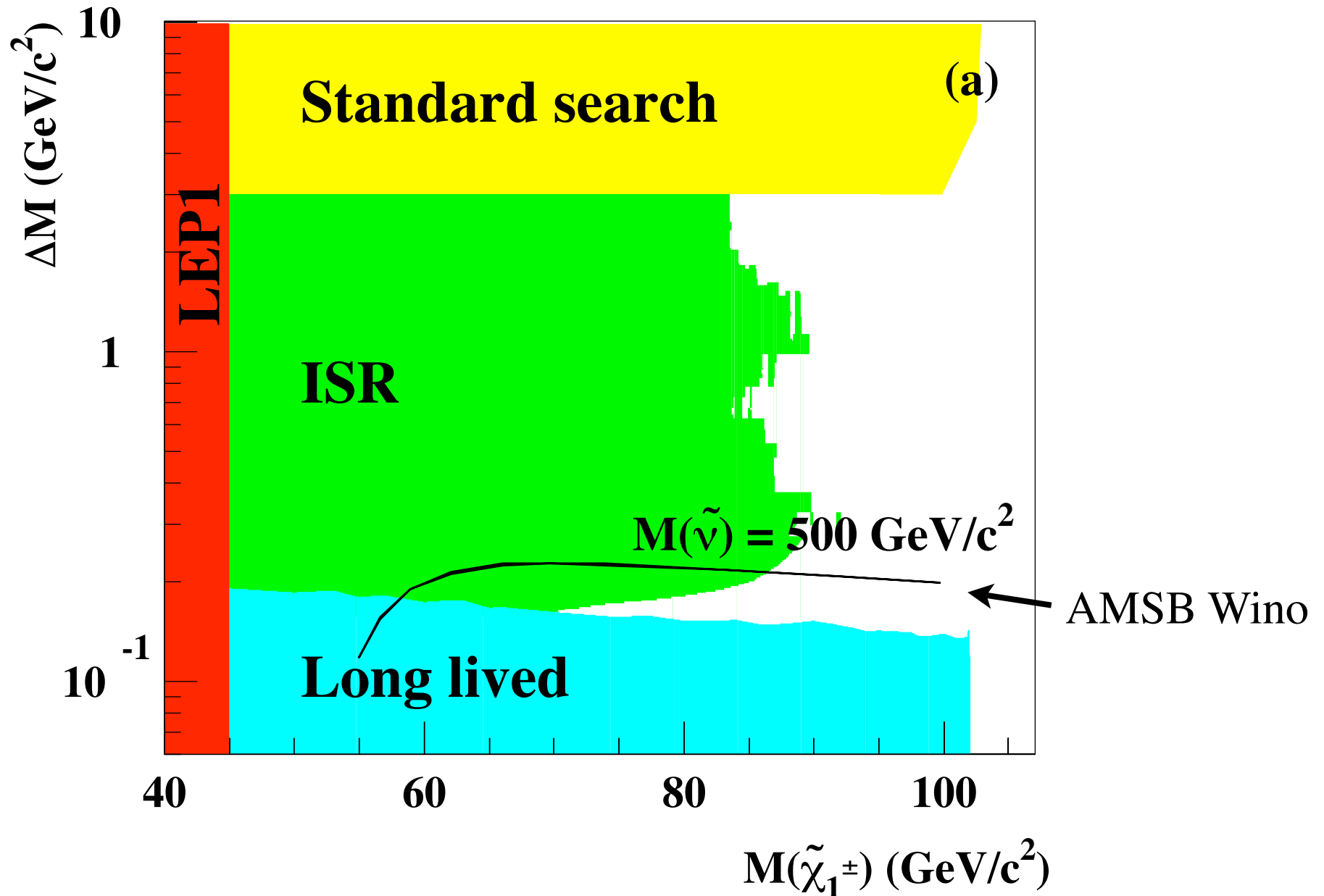
Delphi Chargino Search



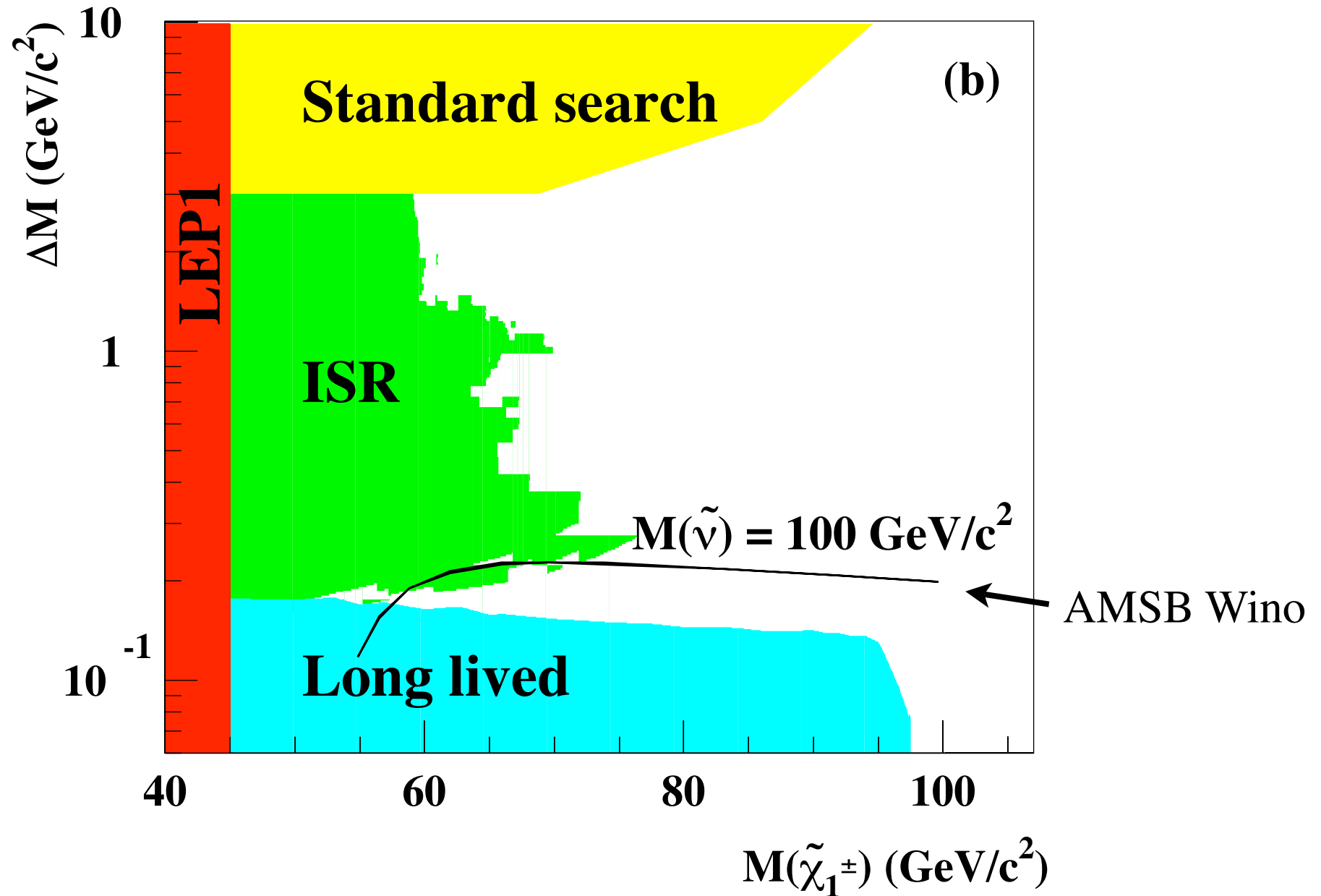
Delphi Chargino Search



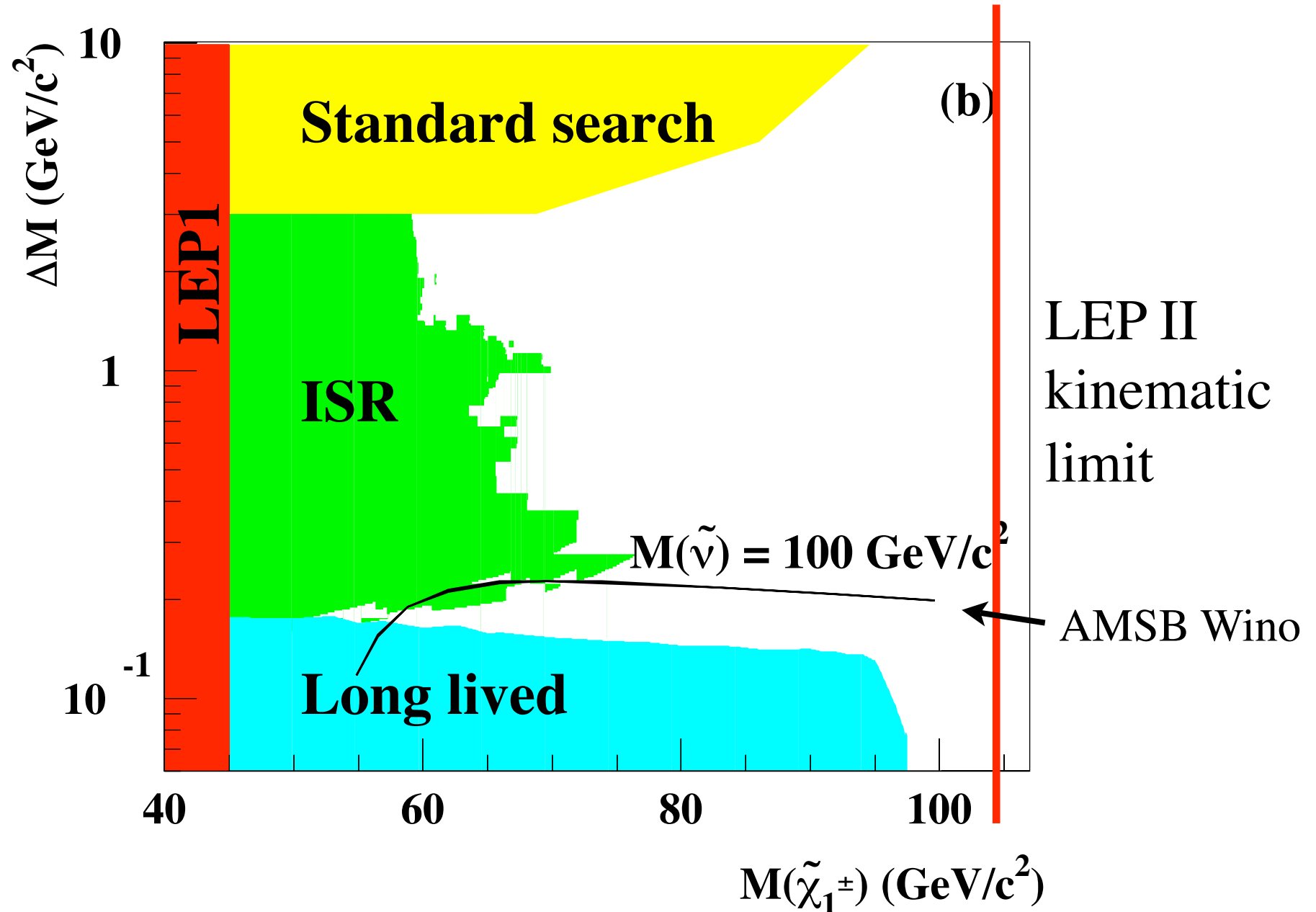
Delphi Chargino Search



Delphi Chargino Search



Delphi Chargino Search



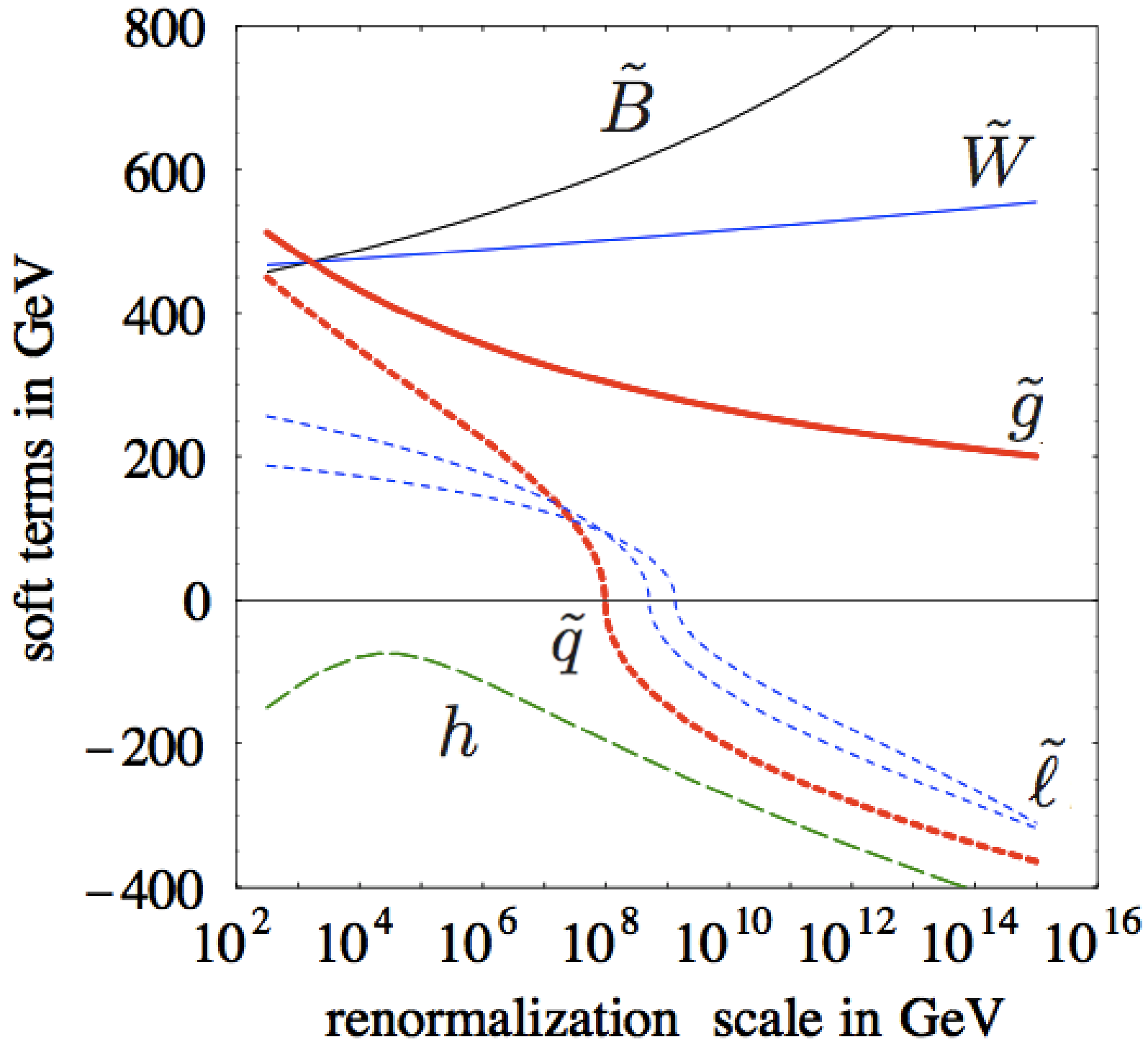
Supersymmetry Breaking with 'Squashed' Spectrum

Deflected Anomaly Mediation

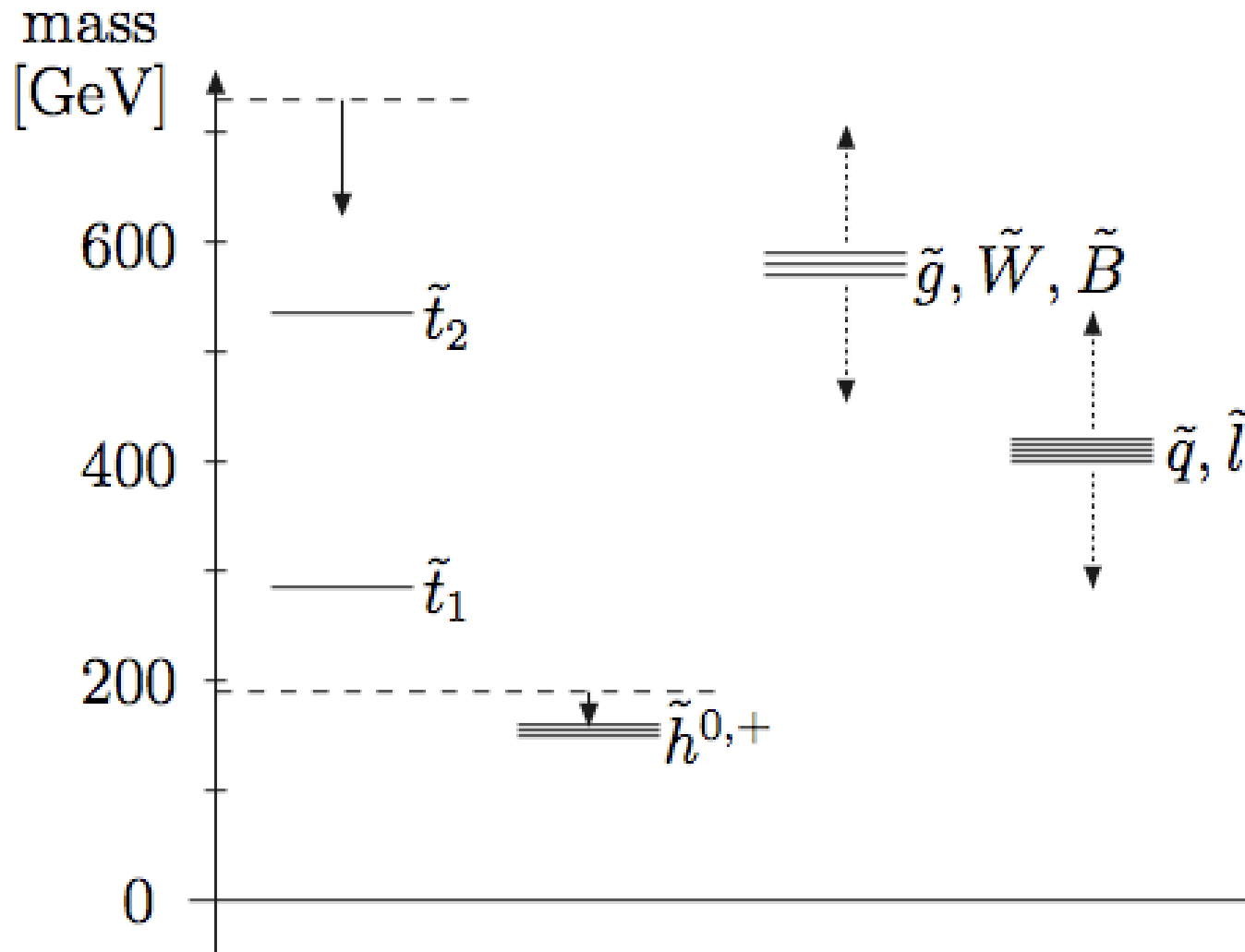
Mirage Mediation

Dirac Gauginos

DAMSB



Mirage Mediation



“New” Parameter Set At the Weak Scale

$$\begin{aligned}
 \mathcal{L}_{\text{soft}}^{\text{MSSM}} = & -\frac{1}{2} (M_3 \tilde{g}\tilde{g} + M_2 \tilde{W}\tilde{W} + M_1 \tilde{B}\tilde{B} + \text{c.c.}) \\
 & - (\tilde{u} a_u \tilde{Q} H_u - \tilde{d} a_d \tilde{Q} H_d - \tilde{e} a_e \tilde{L} H_d + \text{c.c.}) \\
 & - \tilde{Q}^\dagger m_Q^2 \tilde{Q} - \tilde{L}^\dagger m_L^2 \tilde{L} - \tilde{u} m_u^2 \tilde{u}^\dagger - \tilde{d} m_d^2 \tilde{d}^\dagger - \tilde{e} m_e^2 \tilde{e}^\dagger \\
 & - m_{H_u}^2 H_u^* H_u - m_{H_d}^2 H_d^* H_d - (b H_u H_d + \text{c.c.}) .
 \end{aligned}$$

parameter
x identity
matrix

Use this to
fix the Z
mass.

μ sets higgsino mass

$\tan \beta$

“New” Parameter Set At the Weak Scale

$$\begin{aligned}
 \mathcal{L}_{\text{soft}}^{\text{MSSM}} = & -\frac{1}{2} (M_3 \tilde{g}\tilde{g} + M_2 \tilde{W}\tilde{W} + M_1 \tilde{B}\tilde{B} + \text{c.c.}) \\
 & - (\tilde{u} \mathbf{a}_u \tilde{Q} H_u - \tilde{d} \mathbf{a}_d \tilde{Q} H_d - \tilde{e} \mathbf{a}_e \tilde{L} H_d + \text{c.c.}) \\
 & - \tilde{Q}^\dagger m_Q^2 \tilde{Q} - \tilde{L}^\dagger m_L^2 \tilde{L} - \tilde{u} m_u^2 \tilde{u}^\dagger - \tilde{d} m_d^2 \tilde{d}^\dagger - \tilde{e} m_e^2 \tilde{e}^\dagger \\
 & - m_{H_u}^2 H_u^* H_u - m_{H_d}^2 H_d^* H_d - (\mu H_u H_d + \text{c.c.}) .
 \end{aligned}$$

$\mathbf{a}_u = \mathbf{y}_u A_u$

parameter x identity matrix

Use this to fix the Z mass.

μ sets higgsino mass

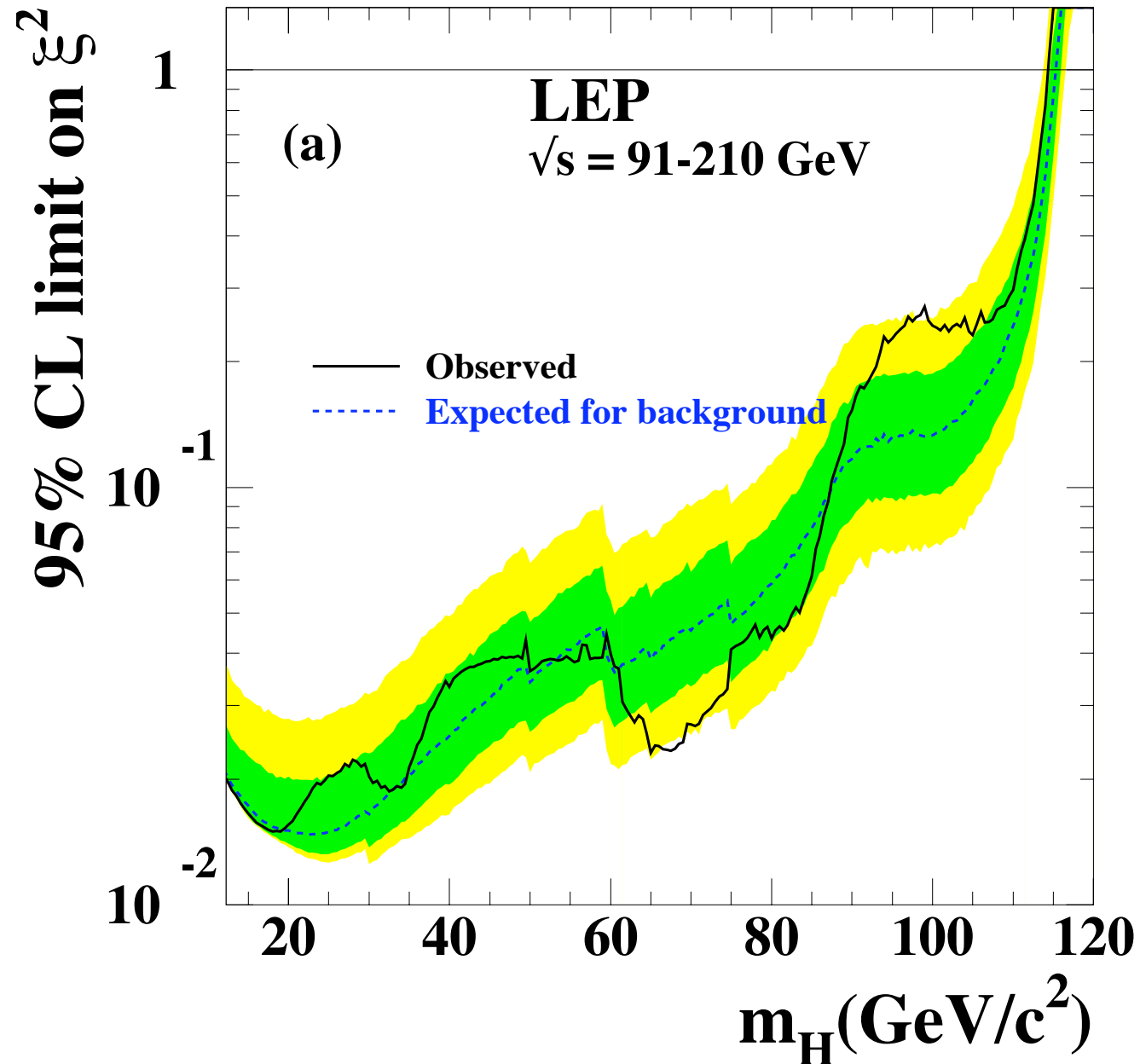
$\tan \beta$

Back to the Extra Singlet

$$h^0 \longrightarrow a^0 a^0$$

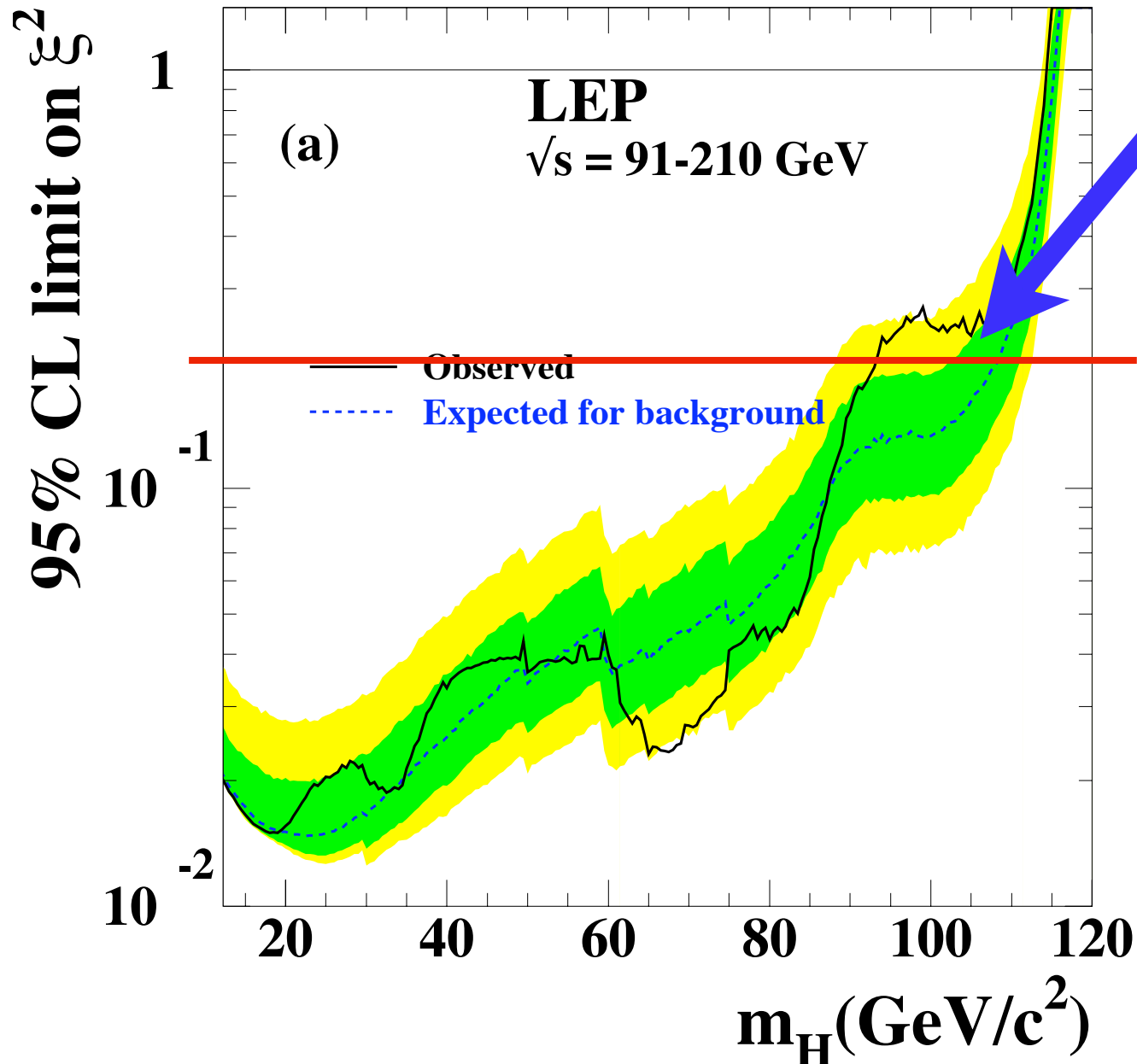
And then the pseudo-scalars decay.

SM Higgs

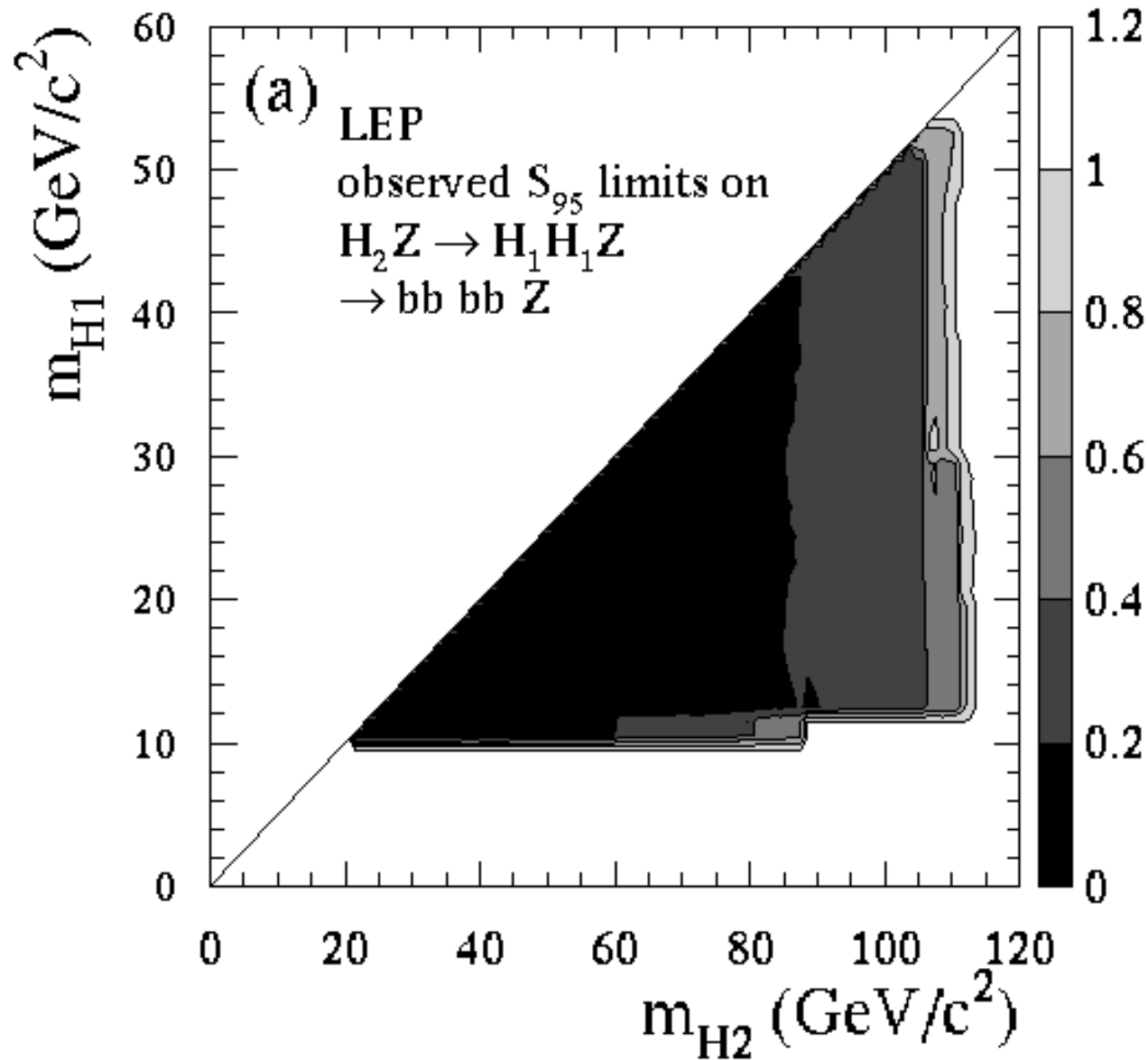


SM Higgs

Suppress cross section
or BR to standard
model modes to ~20%

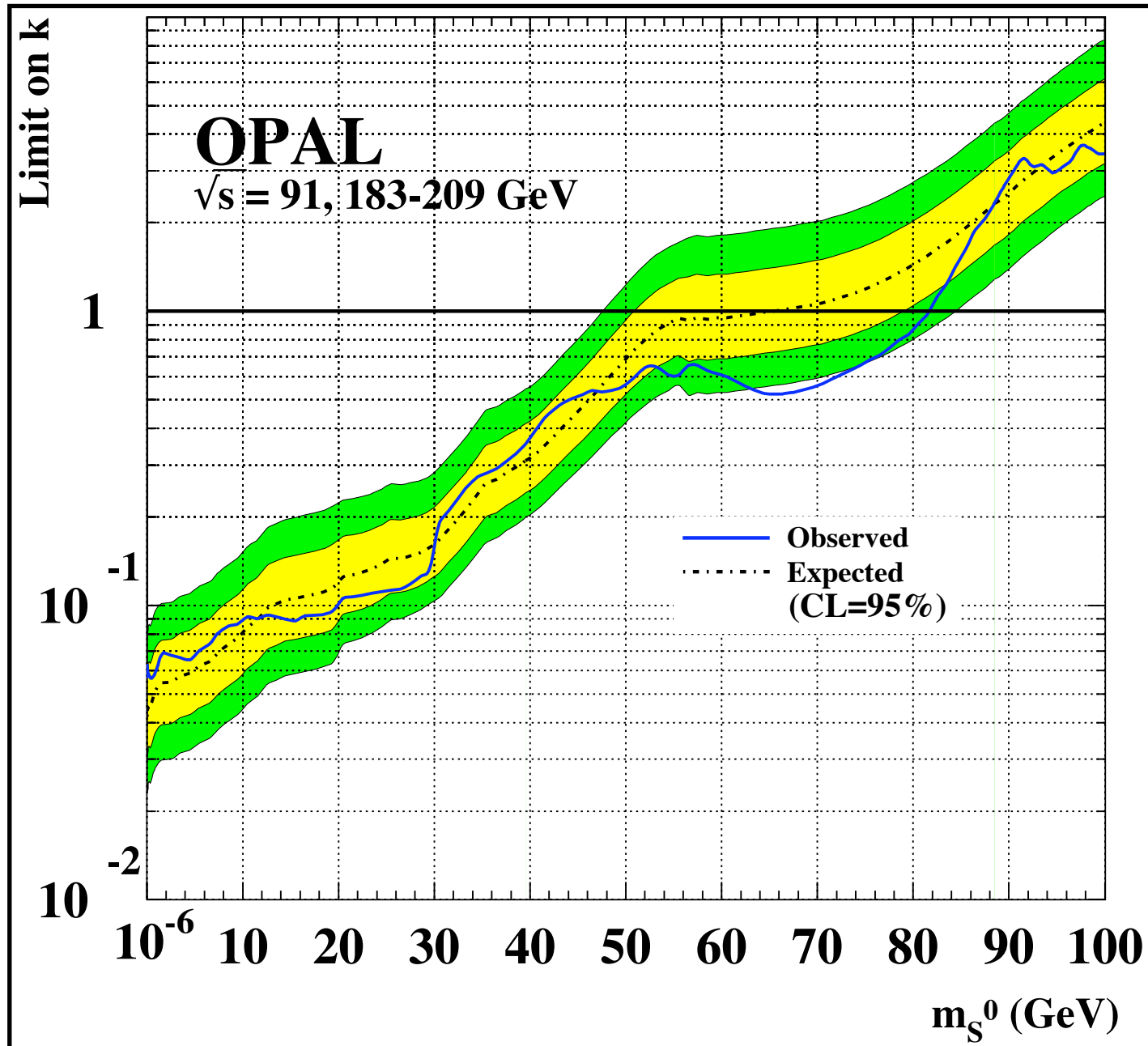


Higgs to 4b's



But NOT 4 taus!

Non-standard Decays



New Higgs Decays

LEP Bounds

$h \rightarrow aa \rightarrow \bar{b}b\bar{b}b$	$m_h > 110 \text{ GeV}$
$h \rightarrow aa \rightarrow \bar{\tau}\tau\bar{\tau}\tau$	$m_h > 86 \text{ GeV}$
$h \rightarrow aa \rightarrow gggg$	$m_h > 82 - 95 \text{ GeV ?}$
$h \rightarrow ss \rightarrow aaaa \rightarrow \bar{b}b\bar{b}b\bar{b}b$	$m_h > 82 \text{ GeV????}$

Dermisek, Gunion, Dobrescu, Matchev,
Landsberg, Chang, Fox, Weiner, Graham, Pierce,
Wacker, plus plenty of older literature.

New Higgs Decays

LEP Bounds

New analysis
on-going

$$h \rightarrow aa \rightarrow \bar{b}b\bar{b}b$$

$$m_h > 110 \text{ GeV}$$

$$h \rightarrow aa \rightarrow \bar{\tau}\tau\bar{\tau}\tau$$

$$m_h > 86 \text{ GeV}$$

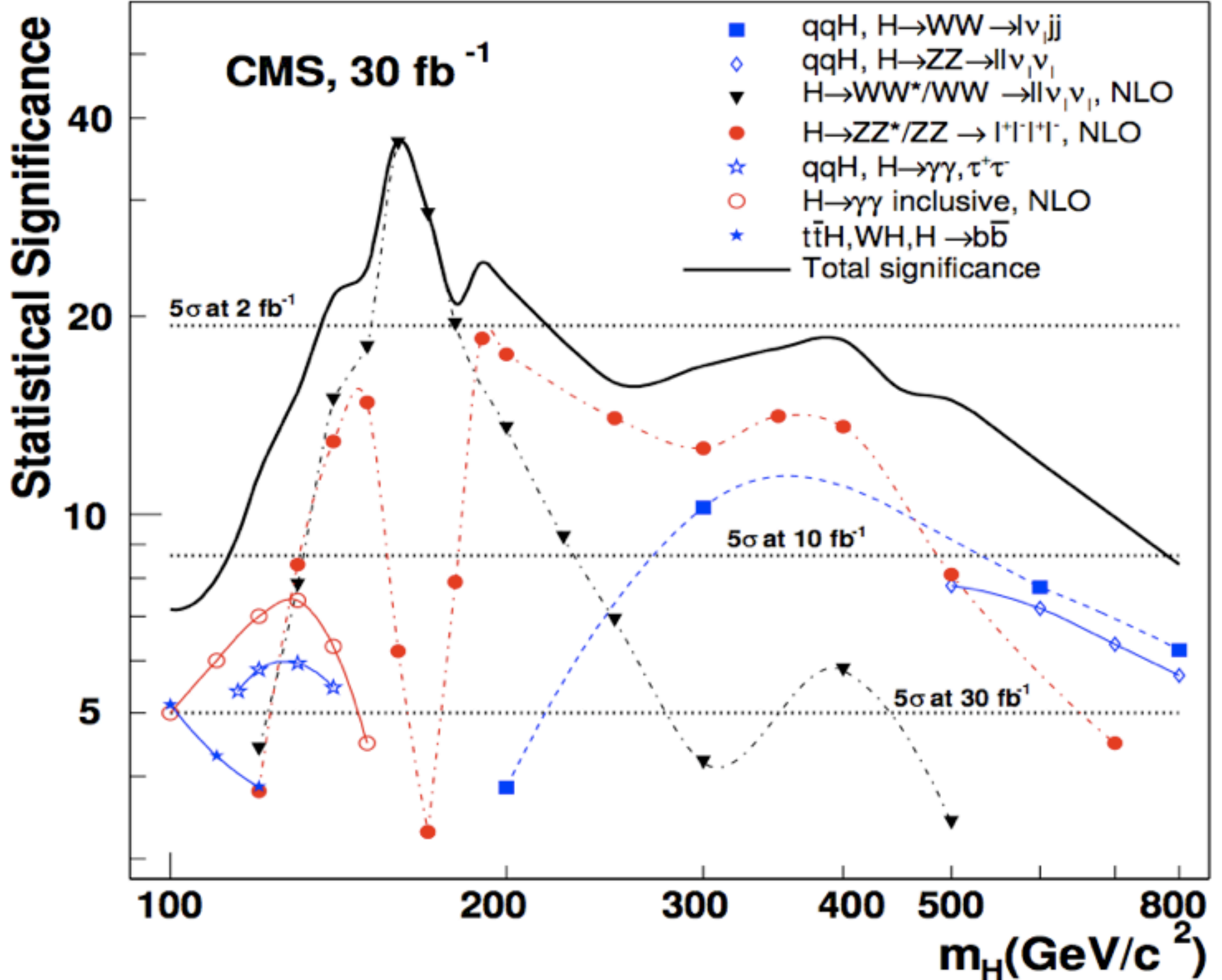
$$h \rightarrow aa \rightarrow gggg$$

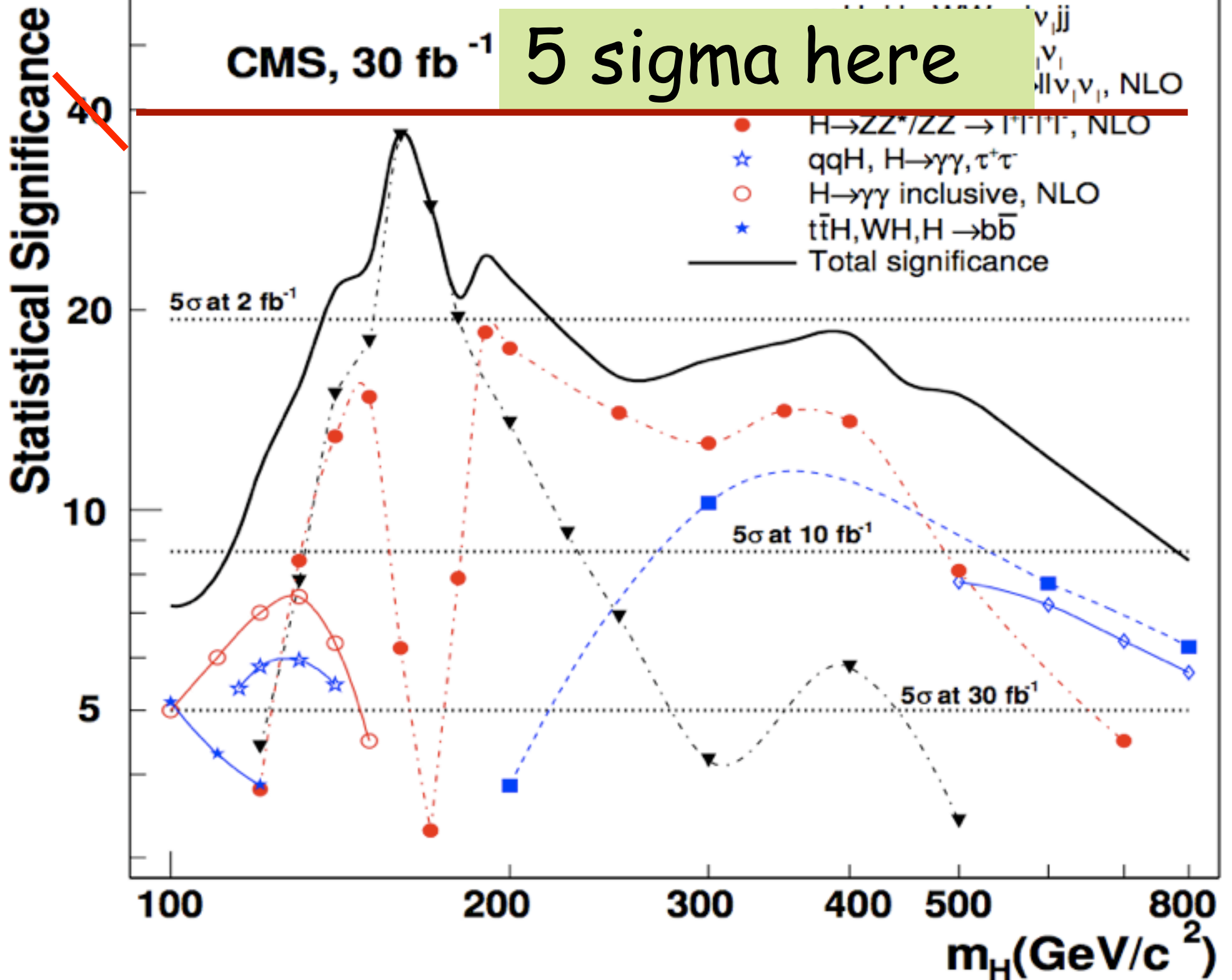
$$m_h > 82 - 95 \text{ GeV ?}$$

$$h \rightarrow ss \rightarrow aaaa \rightarrow \bar{b}b\bar{b}b\bar{b}b$$

$$m_h > 82 \text{ GeV????}$$

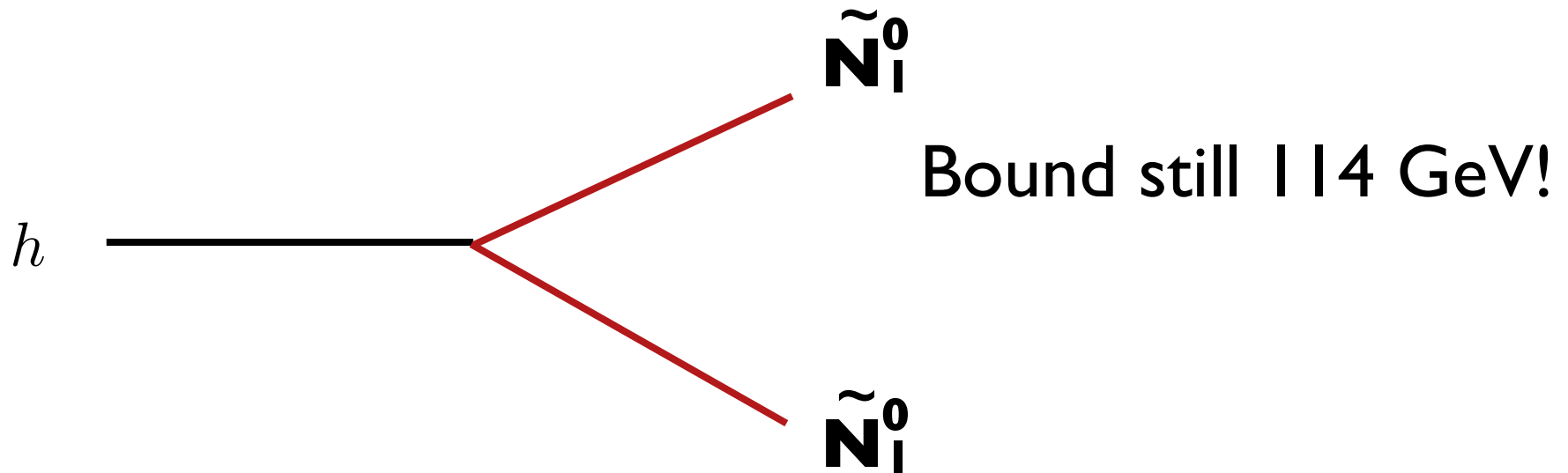
Dermisek, Gunion, Dobrescu, Matchev,
Landsberg, Chang, Fox, Weiner, Graham, Pierce,
Wacker, plus plenty of older literature.





Higgs Decays to Superpartners

Straight MSSM possibility:



Neutralinos (like neutrinos) are invisible.

Potential at LHC better via VBF

Violation of R Parity

$$W = H_1 Q D^c + H_2 Q U^c + H_1 L E^c + \mu H_1 H_2 \\ + L Q D^c + U^c D^c D^c + L L E^c + \mu_L L H_2$$

Violation of R Parity

$$W = H_1 Q D^c + H_2 Q U^c + H_1 L E^c + \mu H_1 H_2 \\ + L Q D^c + \cancel{U^c D^c D^c} + L L E^c + \mu_L L H_2$$

Could have “Baryon Parity”.

Violation of R Parity

$$W = H_1 Q D^c + H_2 Q U^c + H_1 L E^c + \mu H_1 H_2$$

$$\text{---} + L Q D^c + U^c D^c D^c + L L E^c + \mu_L L H_2 \text{---}$$

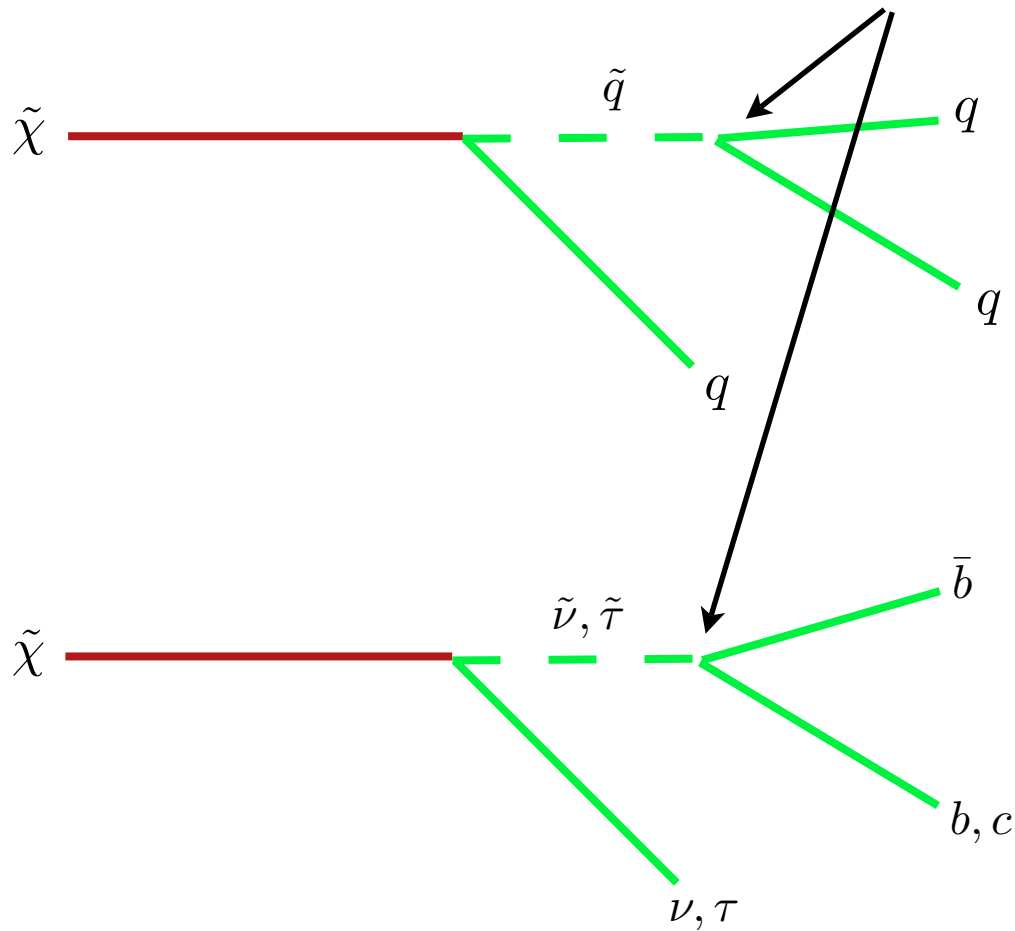
or “Lepton Parity”

$$p \not\rightarrow X$$

X must have an odd number of fermions, thus its lepton number $L = 2n + 1$. No lepton parity violation, no decay.

LSP decays

R parity violation



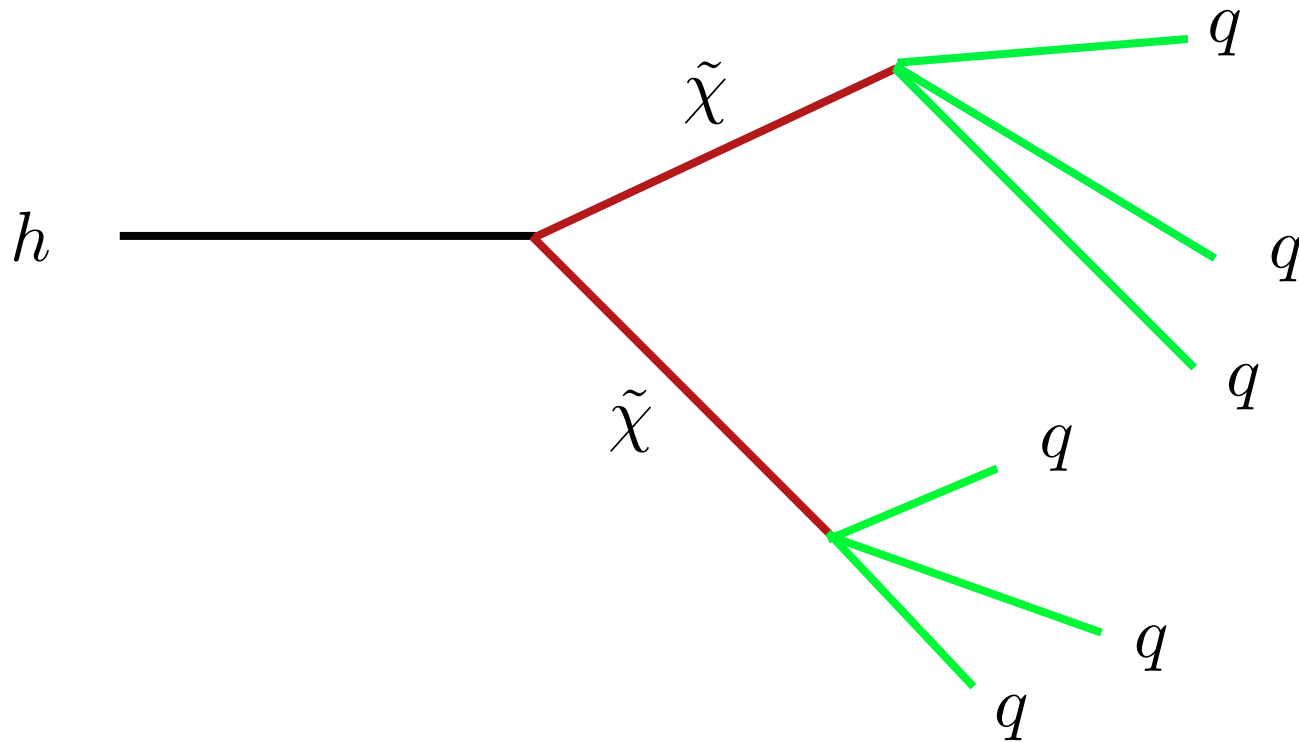
Decreases
missing E_T signal

Typical Bounds on Superpartners with B

Sleptons (R)	94,85,70 GeV (A)
Sneutrinos	88,65,65 GeV (A)
Squarks ($u_{L/R}, d_{L/R}$)	87,80,86,56 GeV (L)
Stop	77 GeV (O,D,L)
Sbottom	7.5 (>55, <30) GeV (L)
Gluino	80 GeV ? (UA2)

Only Chargino bound roughly the same
(102.5 GeV)

Higgs decays with B-violation



Higgs to 6 jets!

$m_h > 87 \text{ GeV}$

Could be a source of new
displaced vertices.

Tomorrow

Technicolor, the Higgs is a K^0 ,
and what the hell are extra dimensions?

