

# Intrinsic Heavy Quarks

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Many thanks to my long term collaborators on heavy quark related topics:

Fred Olness, Aleksander Kusina, Florian Lyonnet,...

and to Pavel Nadolsky for providing some slides

PDF Lattice 2017, Oxford, 23/03/2017

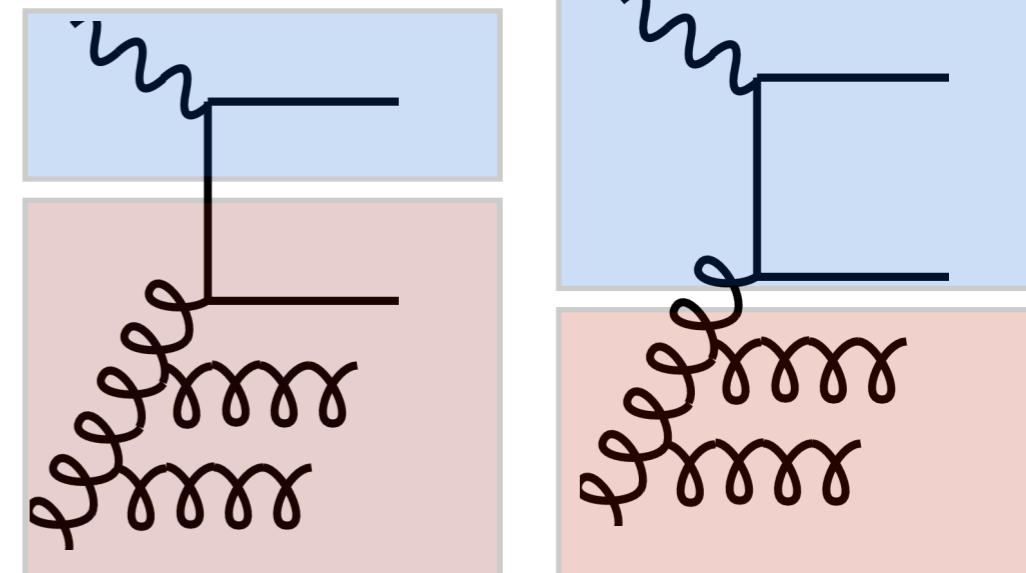
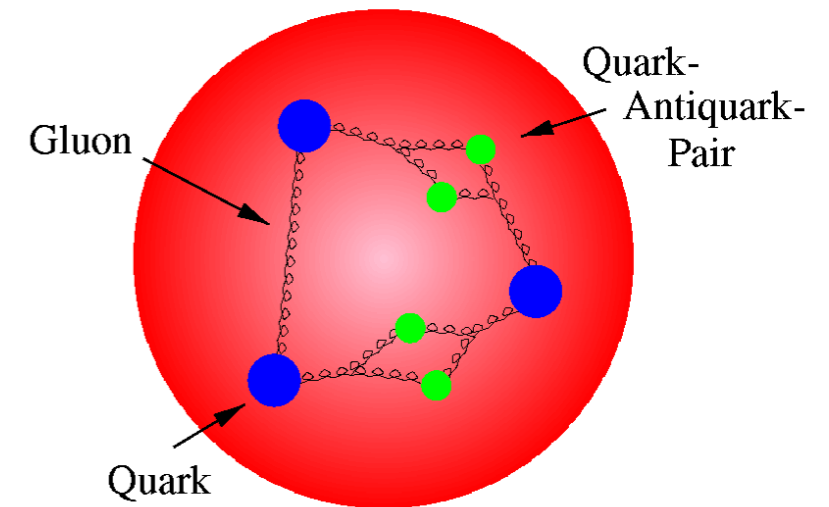
# Introduction

# Heavy Quarks

- charm, bottom, top
- $m_h \gg \Lambda_{\text{QCD}}$ , perturbative scale
- Well, charm not so heavy...
- will mostly talk about charm but also a bit about bottom

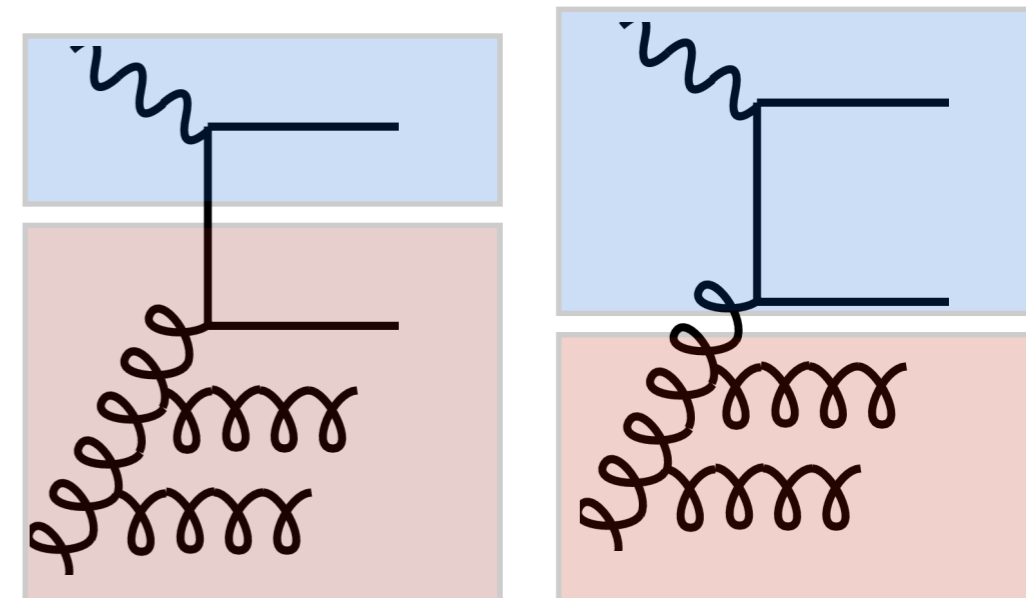
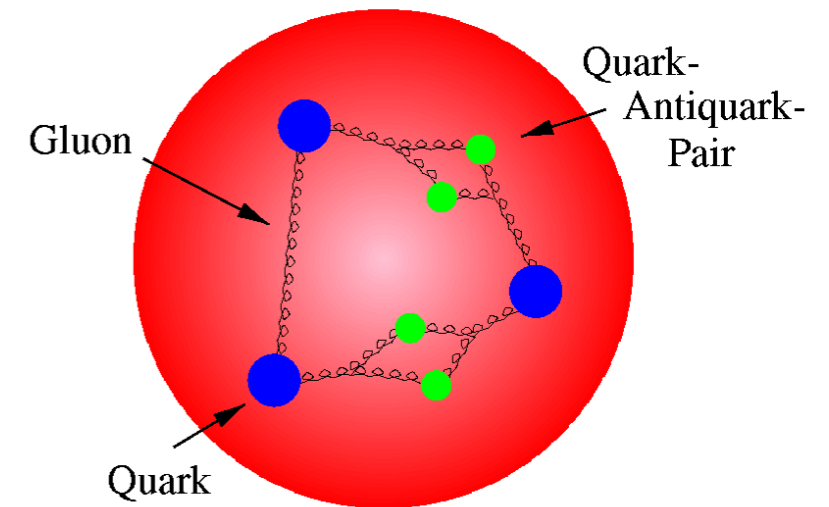
# Is there charm in the nucleon?

- Standard approach: Charm entirely perturbative
- Heavy Flavour Schemes
  - FFNS: charm not in the proton  
keep  $\log(Q/m)$  in fixed order
  - VFNS: charm PDF in the proton  
resum  $\log(Q/m)$
- Different Heavy Flavour Schemes = different ways to organize the perturbation series
- What is structure? What is interaction?  
Freedom to choose the factorization scale
- However, charm not so much heavier than  $\Lambda_{\text{QCD}}$
- There could be a **non-perturbative** intrinsic charm component (added to the VFNS or even FFNS)
- Important to test the charm PDF experimentally



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**WARNING:**  
Not sure whether there is consensus on a) whether this is true and b) how it has to be incorporated in the pQCD formalism

# Charm PDFs

- Large majority of global analyses:

Charm PDF is **calculated**,  
there is no fit parameter!

- Boundary condition for DGLAP evolution  
calculated **perturbatively**:

(matching condition when switching from  $n_f=3$  to  $n_f=4$  flavours)

$$c(x, Q=m_c) = 0 \quad @\text{NLO, MSbar}$$

# Charm PDFs

- Is there a (sizable) non-perturbative contribution to the twist-2 charm PDF?
- After all, we cannot calculate the strange PDF in perturbation theory and charm is not so heavy.
- **Answers** can come from:
  - global analysis:  
need data sensitive to charm
  - lattice calculations:  
even one or two moments would help

# Why do we care?

- **Hadron structure:** (I put it on the 1st place here!)

Models exist which predict a sizable intrinsic charm component; pheno. consequences for a number of observables;  
searches for BSpQCD (Beyond Standard pQCD) physics

- **LHC:**

Precision PDFs required as tool,  
there are observables at the LHC sensitive to charm,  
new physics may have couplings  $\sim$ quark mass!

- **Astroparticle physics:**

Calculation of neutrino fluxes in the atmosphere depend strongly on the charm PDF



# Models predicting intrinsic charm

# How to define “intrinsic”?

- So far I have only talked about “the charm PDF”
- The question was whether a perturbatively generated charm PDF is sufficient or whether one needs to determine a non-perturbative input distribution from data
- No attempt to split up the charm PDF into something “extrinsic” and “intrinsic” at the end it’s the charm PDF which is needed for collider pheno
- However, for understanding models, the literature need to say precisely what we understand under “intrinsic” and “extrinsic”

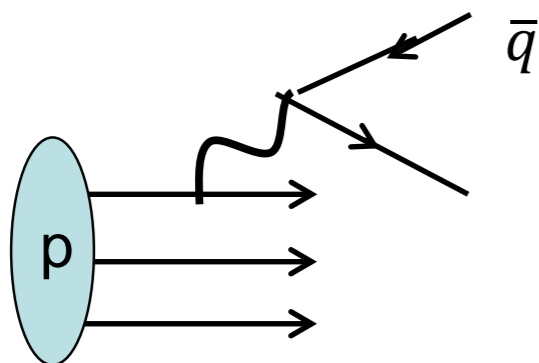
# How to define “intrinsic”?

## Extrinsic and intrinsic sea PDFs

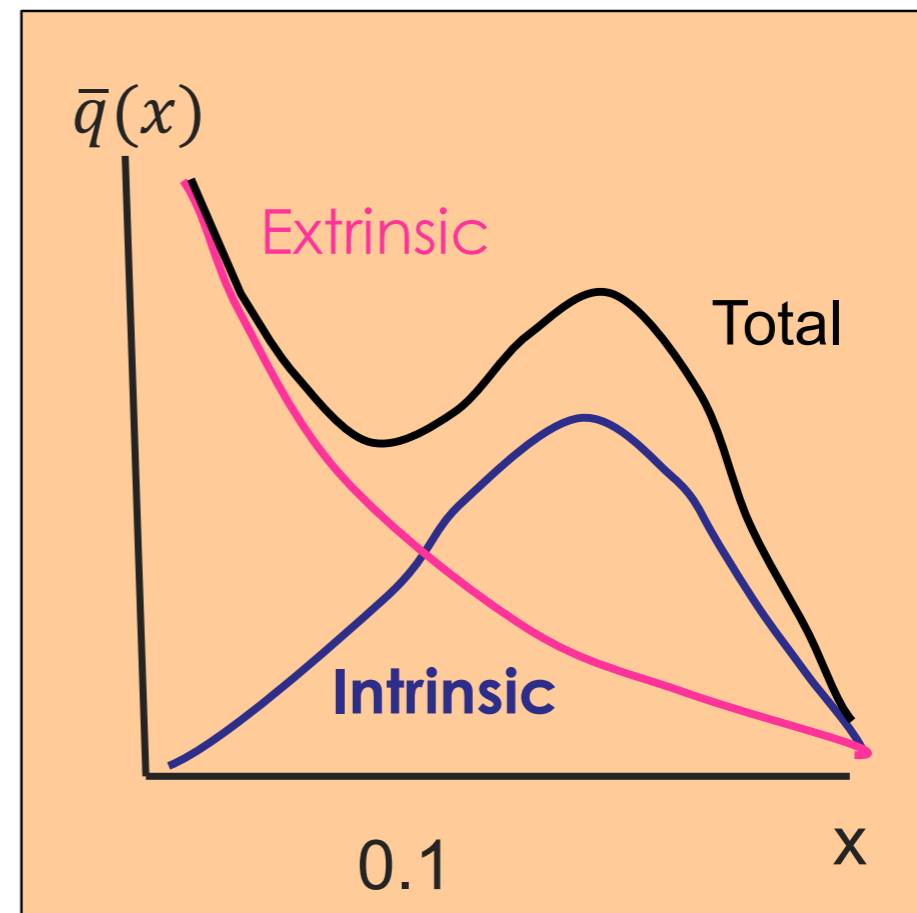
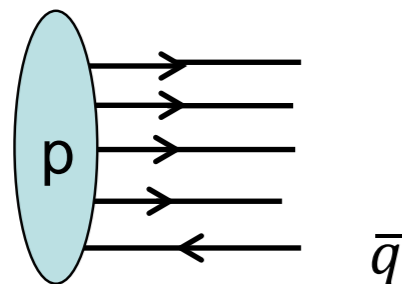
$$(\bar{q} = \bar{u}, \bar{d}, \bar{s}, \bar{c}, \bar{b})$$

### “Extrinsic” sea

(maps on disconnected diagrams of lattice QCD for both heavy and light flavors?)



“Intrinsic” sea (excited Fock nonpert. states, maps on connected diagrams of lattice QCD?)



# (Dis)connected topologies in lattice QCD

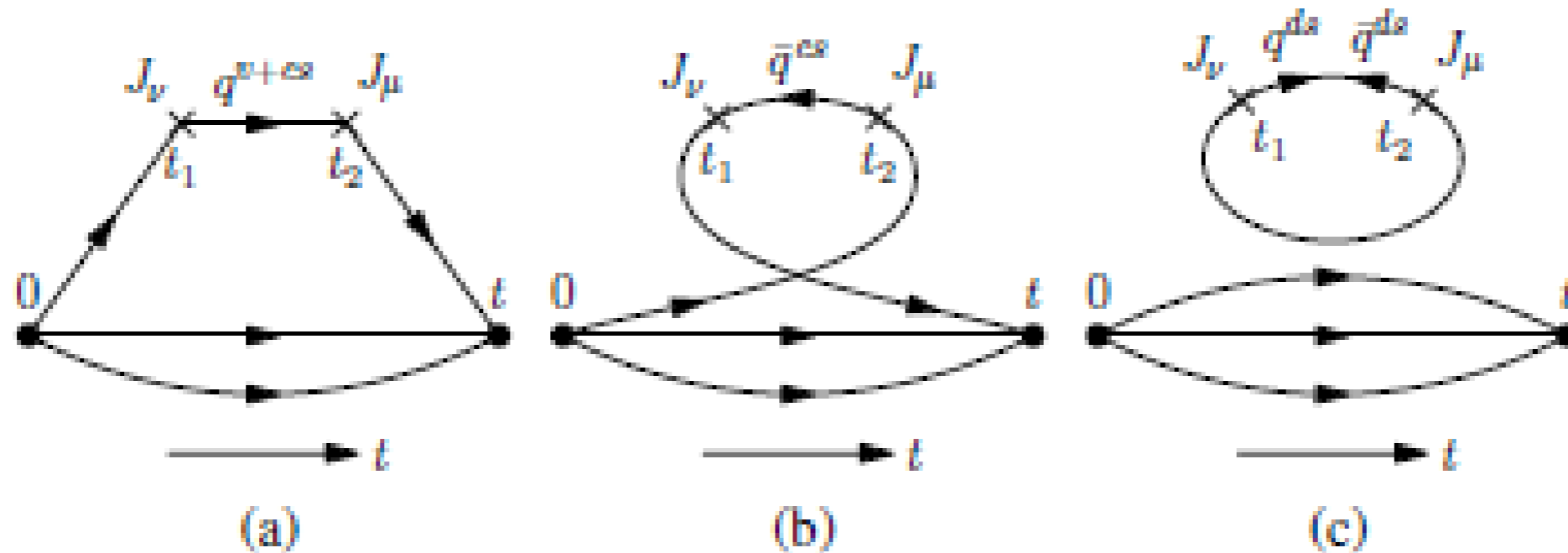


FIG. 1: Three gauge invariant and topologically distinct diagrams in the Euclidean path-integral formalism of the nucleon hadronic tensor in the large momentum frame. In between the currents at  $t_1$  and  $t_2$ , the parton degrees of freedom are (a) the valence and CS partons  $q^{v+cs}$ , (b) the CS anti-partons  $\bar{q}^{cs}$ , and (c) the DS partons  $q^{ds}$  and anti-partons  $\bar{q}^{ds}$  with  $q = u, d, s$ , and  $c$ . Only  $u$  and  $d$  are present in (a) and (b).

From Pavel's talk in case we want to discuss this

Liu, Chang, Cheng, Peng, 1206.4339

# How to define intrinsic heavy quarks?

- For light quarks both mechanisms, “extrinsic” and “intrinsic” are non-perturbative. There is no way to separate the parts, one can only access the full PDF.
- For heavy quarks, one can calculate the “extrinsic” part perturbatively and one can define the “intrinsic part by subtracting the “extrinsic” part from the full result:

$$\text{Intrinsic Charm} := \text{Charm} - \text{Extrinsic Charm}$$

- This definition is to a good accuracy independent of the scale (at least for a large-x intrinsic component) since the intrinsic part decouples from the full evolution equation
- In the following the full charm PDF will also be called “Fitted Charm”

# Models

- For a recent review see [arXiv:1504.06287](#)
- Most models are concentrated at large  $x$  and have a precise  $x$ -shape but do not predict the scale (BHPS, Meson cloud models)
- In some models  $c(x)=\bar{c}(x)$  in others not
- In global analyses also **phenomenological models** with a **sea-like charm** (broad range in  $x$ ) are analyzed

# BHPS model

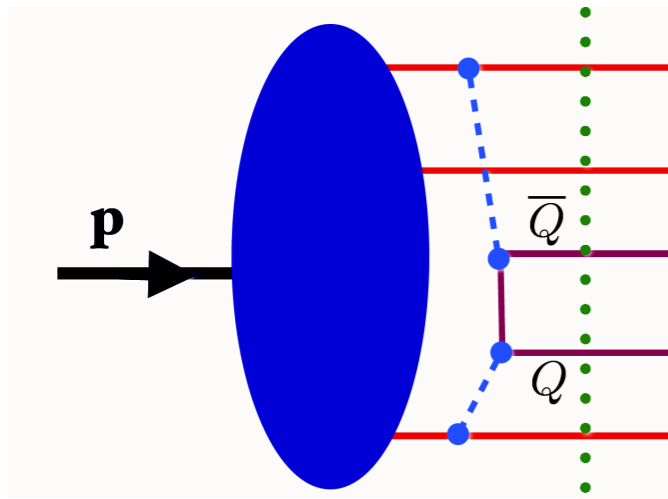


Figure 1: Five-quark Fock state  $|uudQ\bar{Q}\rangle$  of the proton and the origin of the intrinsic sea.

- Light cone Fock space picture
- $|uudQ\bar{Q}\rangle$  state with heavy quarks connected to valence quarks, fundamental property of wave function
- Intrinsic contribution dominant at large  $x$  and on the order  $O(\Lambda^2/m_Q^2)$
- A finite IC contribution has been extracted from the lattice: Probability for the  $\langle N|c\bar{c}|N\rangle$  ME of 5 to 6% [MILC collab., arXiv:1204.3866]

The  $x$ -dependence predicted by the BHPS model, unknown at which scale:

$$c_1(x) = \bar{c}_1(x) \propto x^2 [6x(1+x) \ln x + (1-x)(1+10x+x^2)]$$

Typical moments;

	$\int_0^1 dx c(x)$	$\int_0^1 dx x [c(x) + \bar{c}(x)] \equiv \langle x \rangle_{c+\bar{c}}$
CTEQ6.6	0	0
CTEQ6.6c0	0.01	0.0057
CTEQ6.6c1	0.035	0.0200

# Global analyses testing intrinsic charm

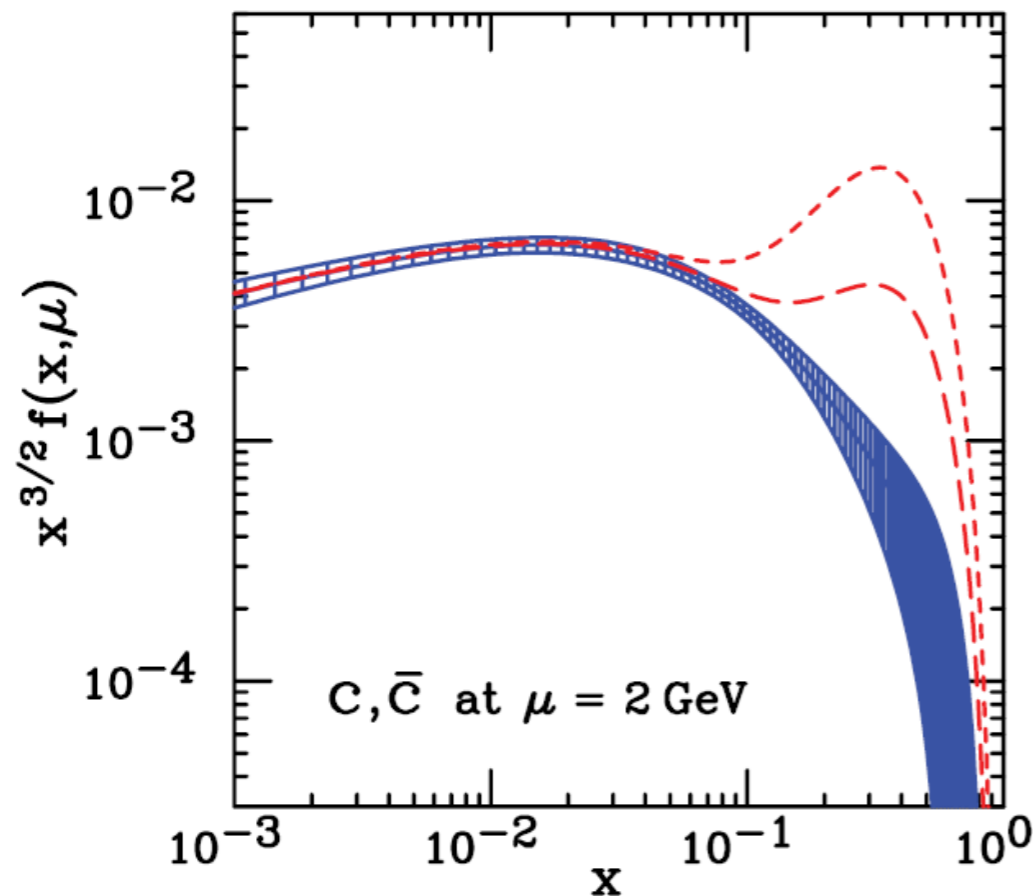


# A global fit by CTEQ to extract IC

PHYSICAL REVIEW D 75, 054029 (2007)

## Charm parton content of the nucleon

J. Pumplin,<sup>1,\*</sup> H. L. Lai,<sup>1,2,3</sup> and W. K. Tung<sup>1,2</sup>



Blue band corresponds to CTEQ6 best fit, including uncertainty

Red curves include intrinsic charm of 1% and 3% ( $\chi^2$  changes only slightly)

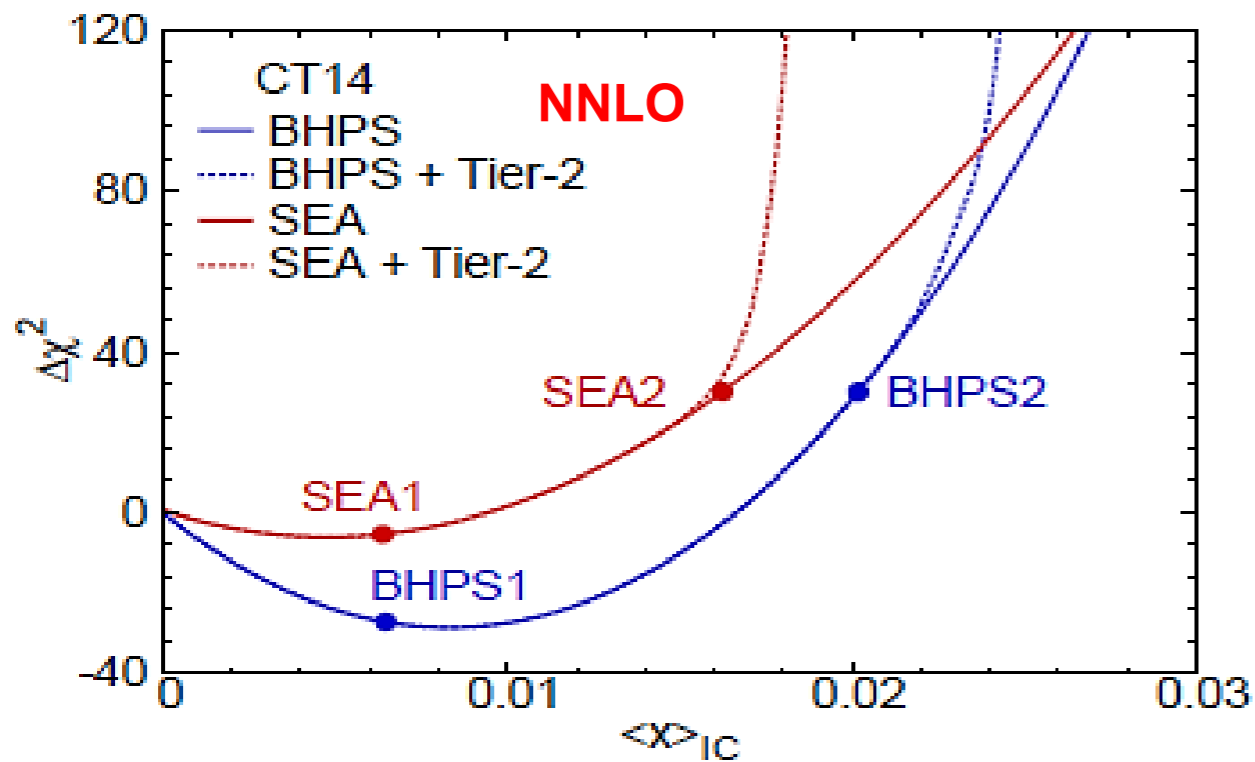
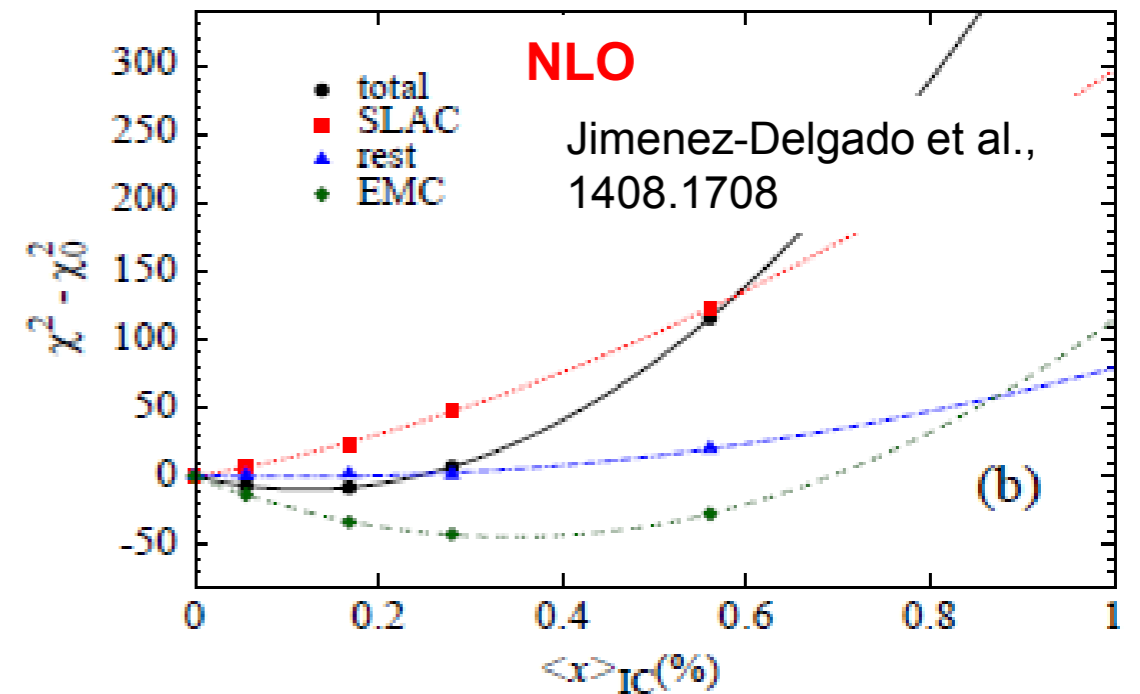
We find that the range of IC is constrained to be from zero (no IC) to a level 2–3 times larger than previous model estimates. The behaviors of typical charm distributions within this range are described, and their implications for hadron collider phenomenology are briefly discussed.

**No conclusive evidence for intrinsic-charm**

# Recent PDFs with fitted charm

Several studies conclude that IC may carry no more than 1% of the proton's momentum

Constraints depend on data selection (e.g., on whether the EMC  $F_2^C$  data are included) and methodology (CTEQ vs. NNPDF)



NNPDF3 NLO Fitted Charm,  $Q=1.65$  GeV

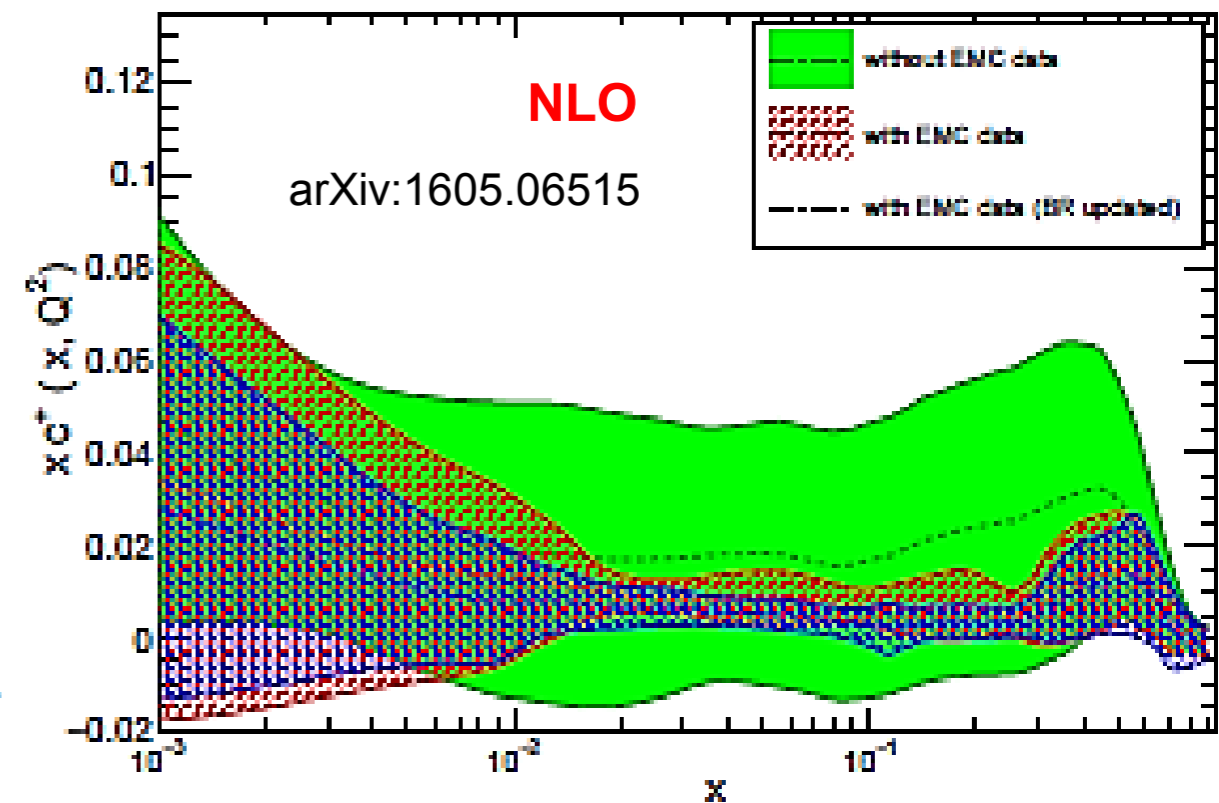
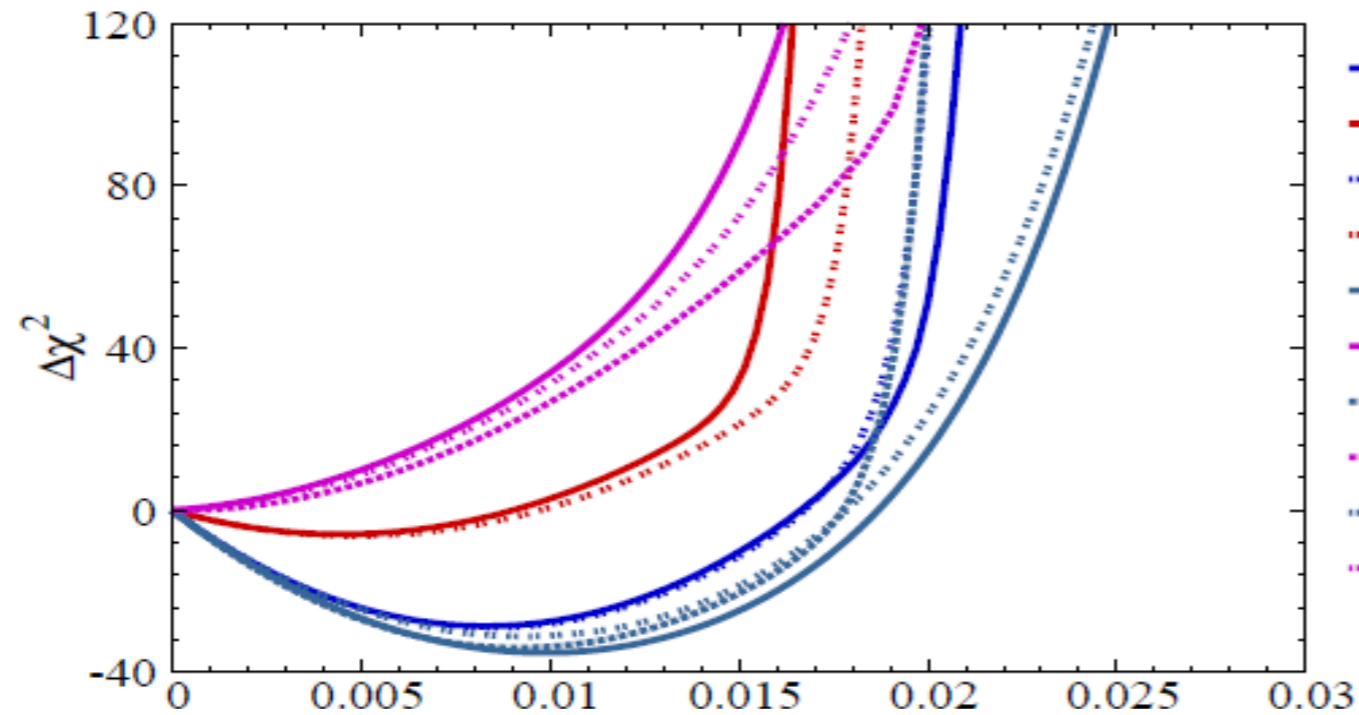


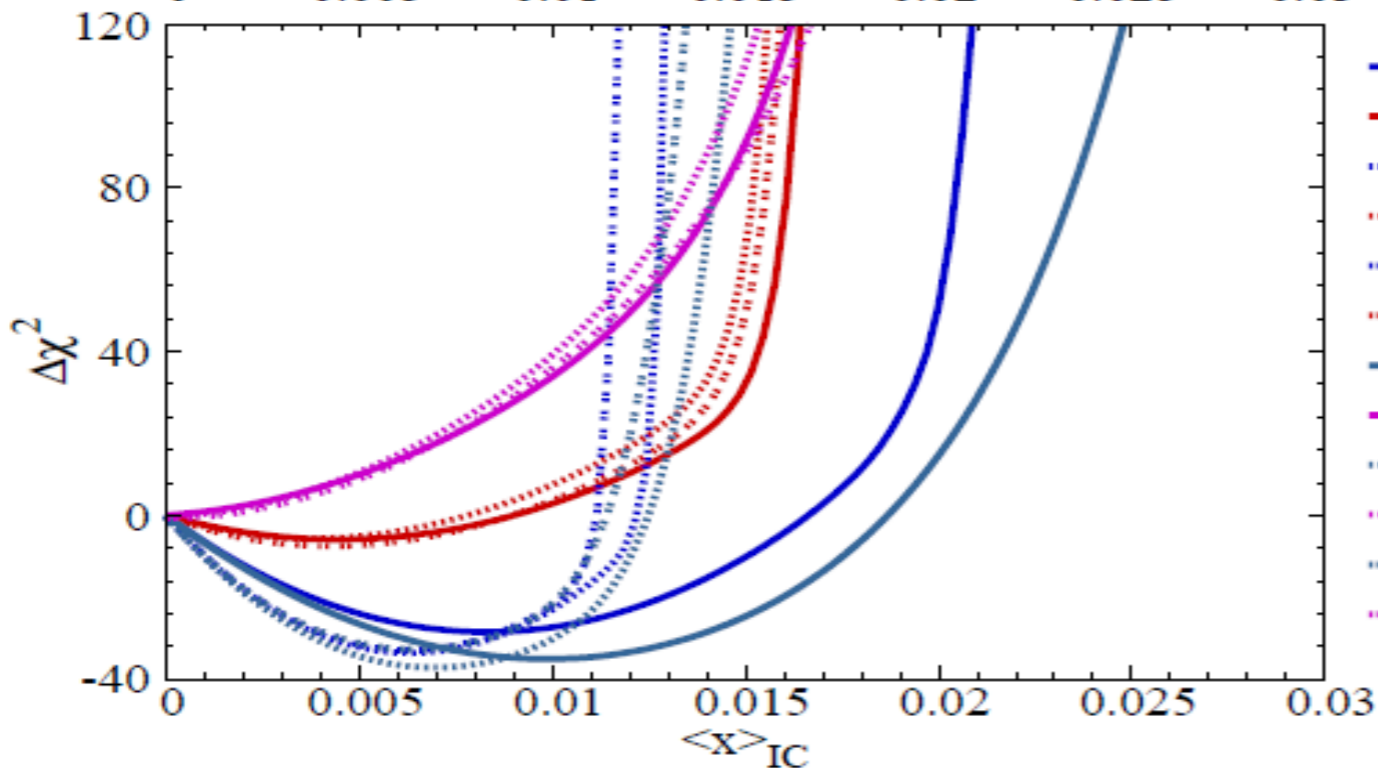
Figure 1: The  $\Delta\chi^2$  versus the momentum fraction of charm  $\langle x \rangle_{IC}$ . PoS DIS2015 (2015) 166

# CT14 IC fits



- CT14 BHPS  $M_C = 1.3$  GeV
- CT14 SEA  $M_C = 1.3$  GeV
- ⋯ CT14(11849) BHPS  $M_C = 1.3$  GeV
- ⋯ CT14(11849) SEA  $M_C = 1.3$  GeV
- CT14HERA2 BHPS  $M_C = 1.3$  GeV
- CT14HERA2 SEA  $M_C = 1.3$  GeV
- ⋯ CT14HERA2 BHPS  $M_C = 1.4$  GeV
- ⋯ CT14HERA2 SEA  $M_C = 1.4$  GeV
- ⋯ CT14HERA2(11849) BHPS  $M_C = 1.3$  GeV
- ⋯ CT14HERA2(11849) SEA  $M_C = 1.3$  GeV

11849:  $Q_0 = 1$  GeV,  
MMHT-like  $g(x, Q_0)$



- CT14 BHPS
- CT14 SEA
- ⋯ CT14, BHPS, w/ EMC
- ⋯ CT14, SEA, w/ EMC
- ⋯ CT14(11849), BHPS, w/ EMC
- ⋯ CT14(11849), SEA, w/ EMC
- CT14HERA2, BHPS
- CT14HERA2, SEA
- ⋯ CT14HERA2, BHPS, w/ EMC
- ⋯ CT14HERA2, SEA, w/ EMC
- ⋯ CT14HERA2(11849), BHPS, w/ EMC
- ⋯ CT14HERA2(11849), SEA, w/ EMC

For the Brodsky-Hoyer-Peterson-Sakai (BHPS) parametrization,

a **marginally** better  $\chi^2$  for IC with  $\langle x \rangle_{IC} \approx 1\%$

For SEA parametrization, IC with  $\langle x \rangle_{IC} \approx 1.5\%$  is allowed within uncertainty

# On the scale evolution of intrinsic heavy quarks

# Full set of coupled evolution equations

Q is the heavy quark

$$\begin{aligned}\dot{g} &= P_{gg} \otimes g + P_{gq} \otimes q + P_{gQ} \otimes Q, \\ \dot{q} &= P_{qg} \otimes g + P_{qq} \otimes q + P_{qQ} \otimes Q, \\ \dot{Q} &= P_{Qg} \otimes g + P_{Qq} \otimes q + P_{QQ} \otimes Q.\end{aligned}$$

Writing:  $Q(x,\mu) = Q_0(x,\mu) + Q_1(x,\mu)$  where  $Q_0$  is the perturbative piece and  $Q_1$  an intrinsic component with support at large  $x$

$$\begin{aligned}\dot{g} &= P_{gg} \otimes g + P_{gq} \otimes q + P_{gQ} \otimes Q_0 + \cancel{P_{gQ} \otimes Q_1}, \\ \dot{q} &= P_{qg} \otimes g + P_{qq} \otimes q + P_{qQ} \otimes Q_0 + \cancel{P_{qQ} \otimes Q_1}, \\ \dot{Q}_0 + \dot{Q}_1 &= P_{Qg} \otimes g + P_{Qq} \otimes q + P_{QQ} \otimes Q_0 + P_{QQ} \otimes Q_1.\end{aligned}$$

# Evolution equation for intrinsic heavy quark

Standard coupled evolution equation without intrinsic heavy quark:

$$\dot{g} = P_{gg} \otimes g + P_{gq} \otimes q + P_{gQ} \otimes Q_0 ,$$

$$\dot{q} = P_{qg} \otimes g + P_{qq} \otimes q + P_{qQ} \otimes Q_0 ,$$

$$\dot{Q}_0 = P_{Qg} \otimes g + P_{Qq} \otimes q + P_{QQ} \otimes Q_0 .$$

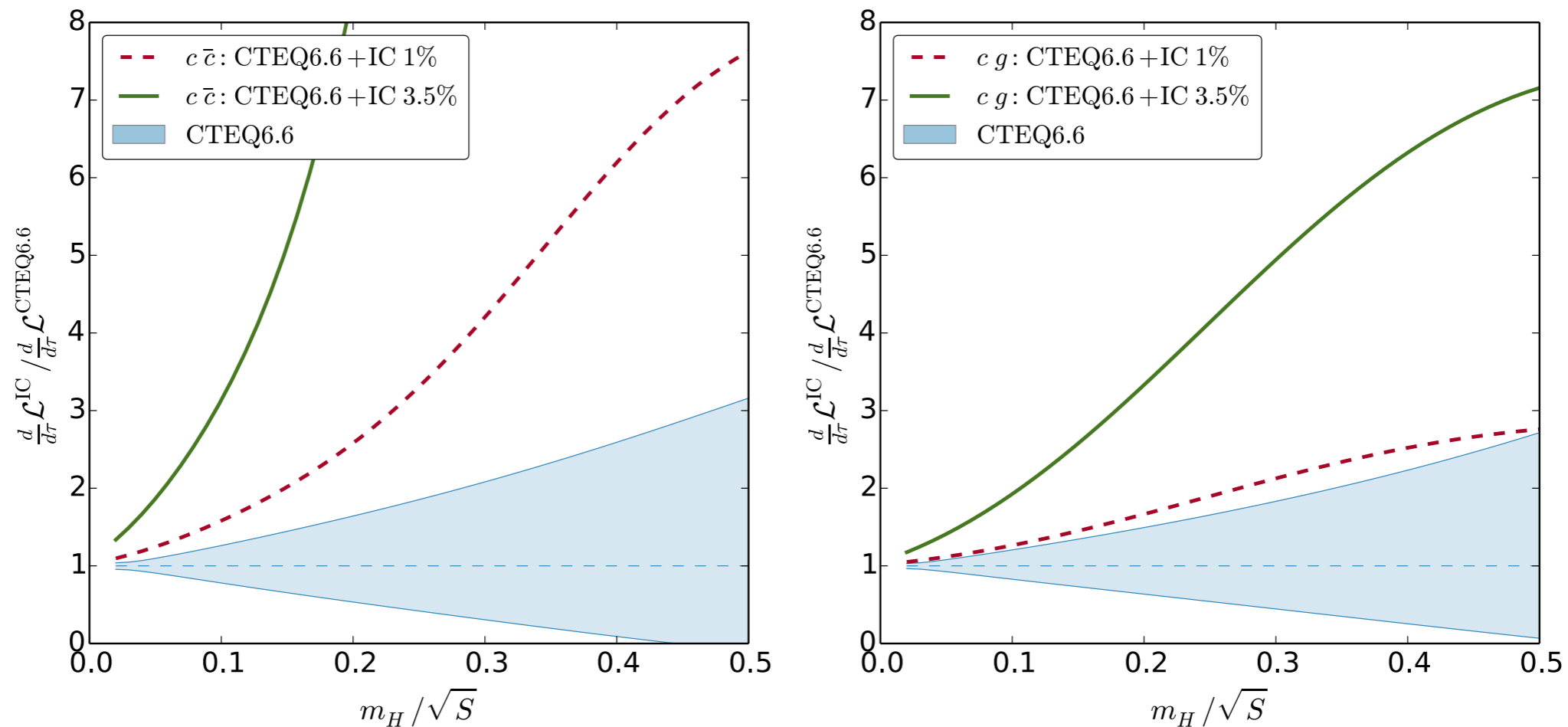
Decoupled non-singlet evolution equation for intrinsic component

$$\dot{Q}_1 = P_{QQ} \otimes Q_1 .$$

Procedure valid up to small violation of momentum sum rule!  
Useful for understanding and phenomenological applications

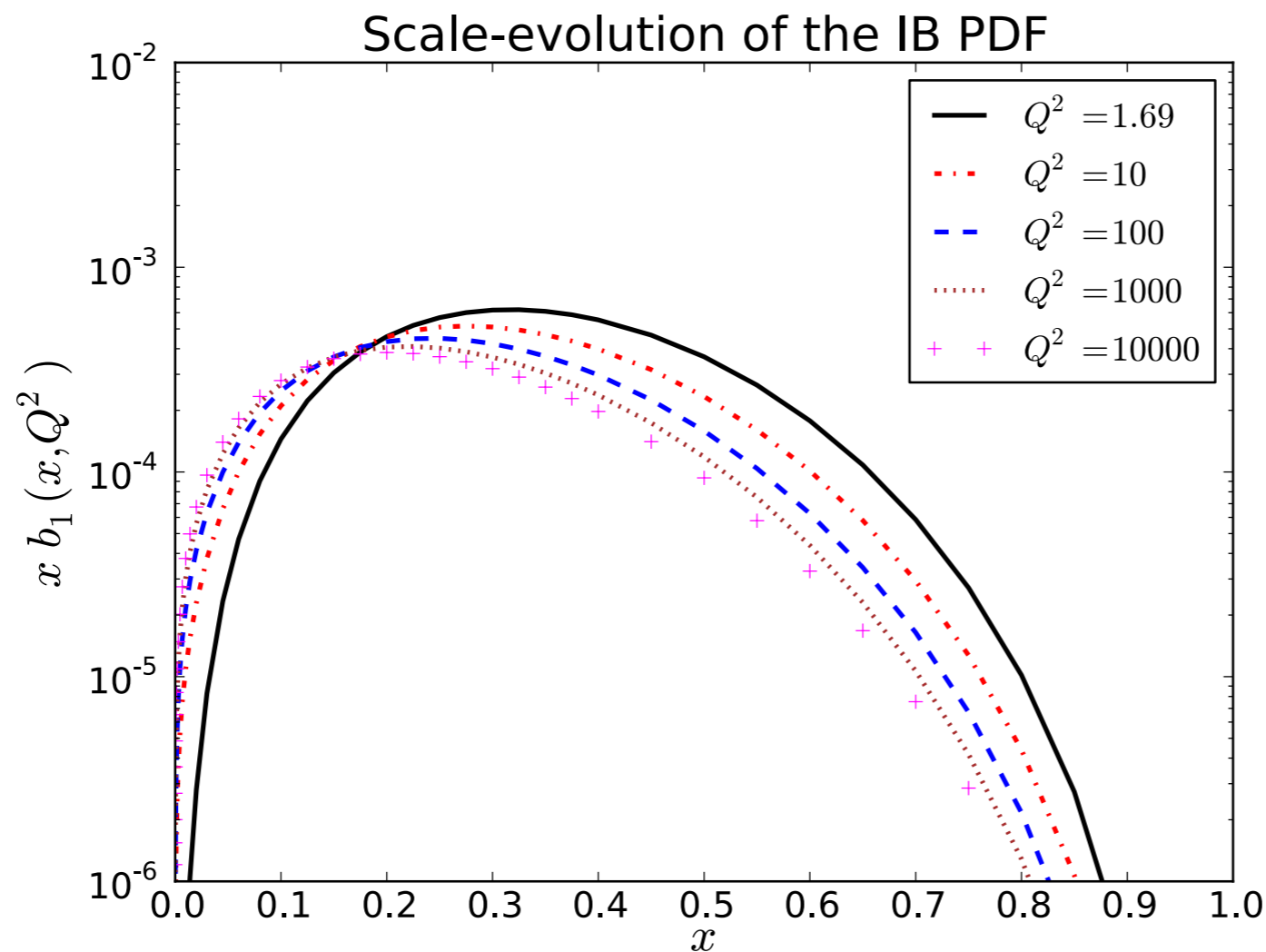
arXiv:1507.08935

# Parton-Parton Luminosities: Charm



**Figure 10.** Ratio of  $c\bar{c}$  luminosities (left) and  $cg$  luminosities (right) at the LHC14 for charm-quark PDF sets with and without an intrinsic component as a function of  $\sqrt{\tau} = m_H/\sqrt{S}$ . The ratio for the  $c\bar{c}$  luminosity (solid, green line) in the left figure reaches values of 50 at  $\sqrt{\tau} = 0.5$ . In addition to the curves with 1% normalization (red, dashed lines) we include the results for the 3.5% normalization (green, solid lines) which was found to be still compatible with the current data [25].

# Scale evolution of IB



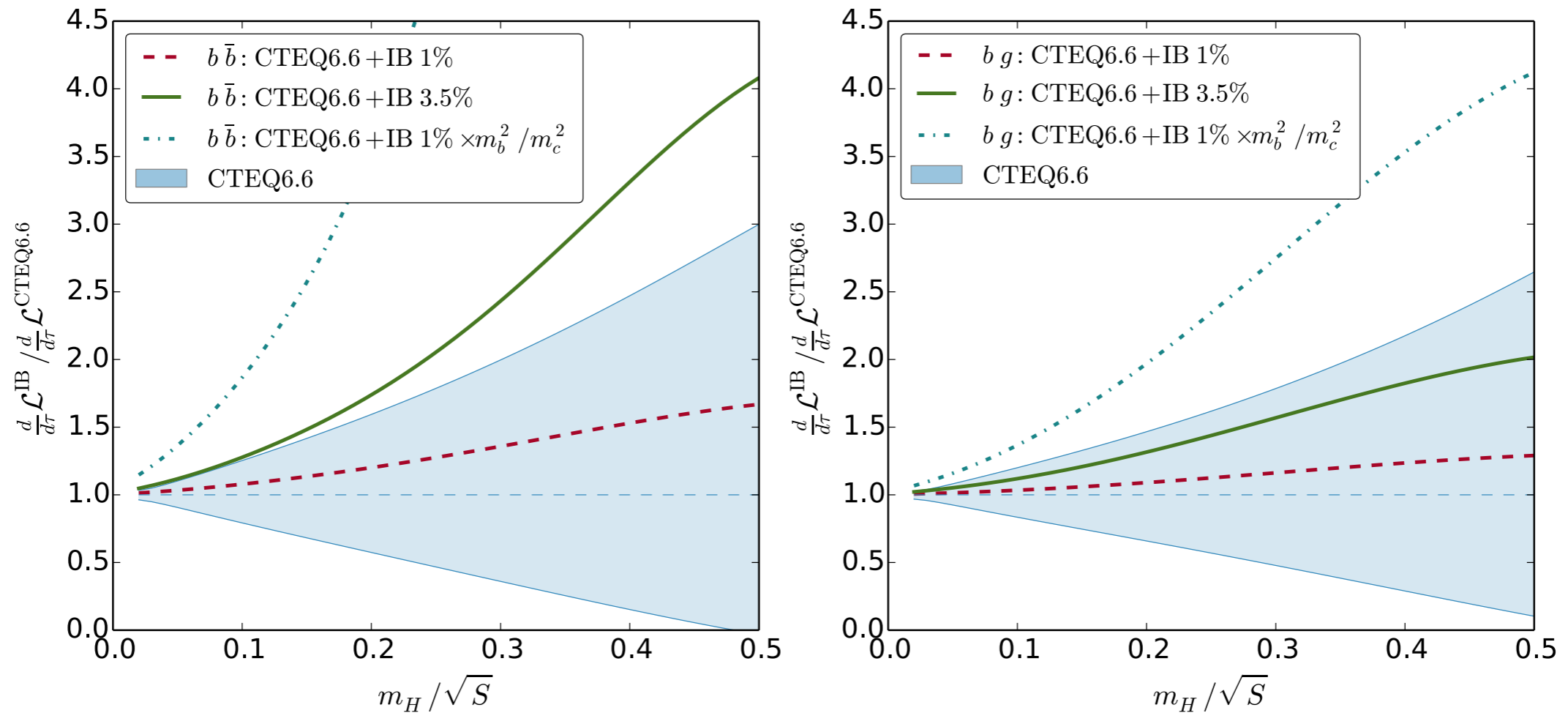
**Black solid line:  
BHPS shape**

Can add the intrinsic  $b_1$  PDF to the radiatively generated  $b_0$  PDF:  
 $b(x) = b_0(x) + b_1(x)$

Allows to estimate the effect of IB

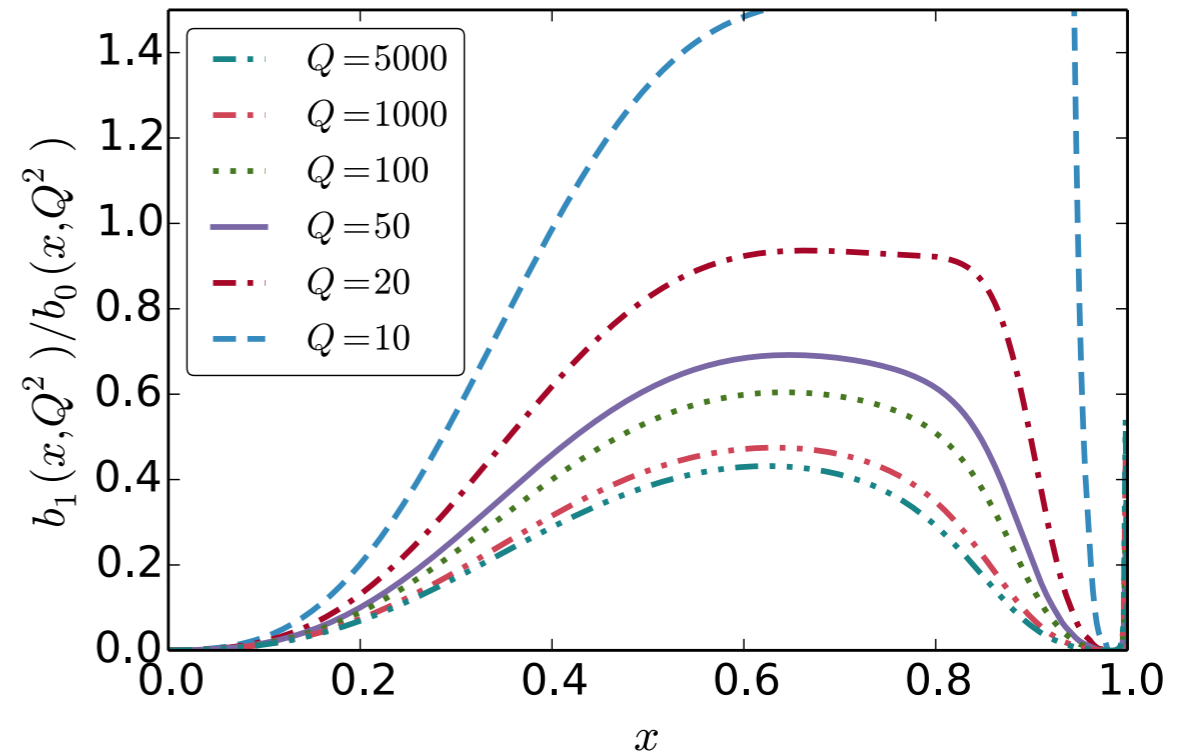
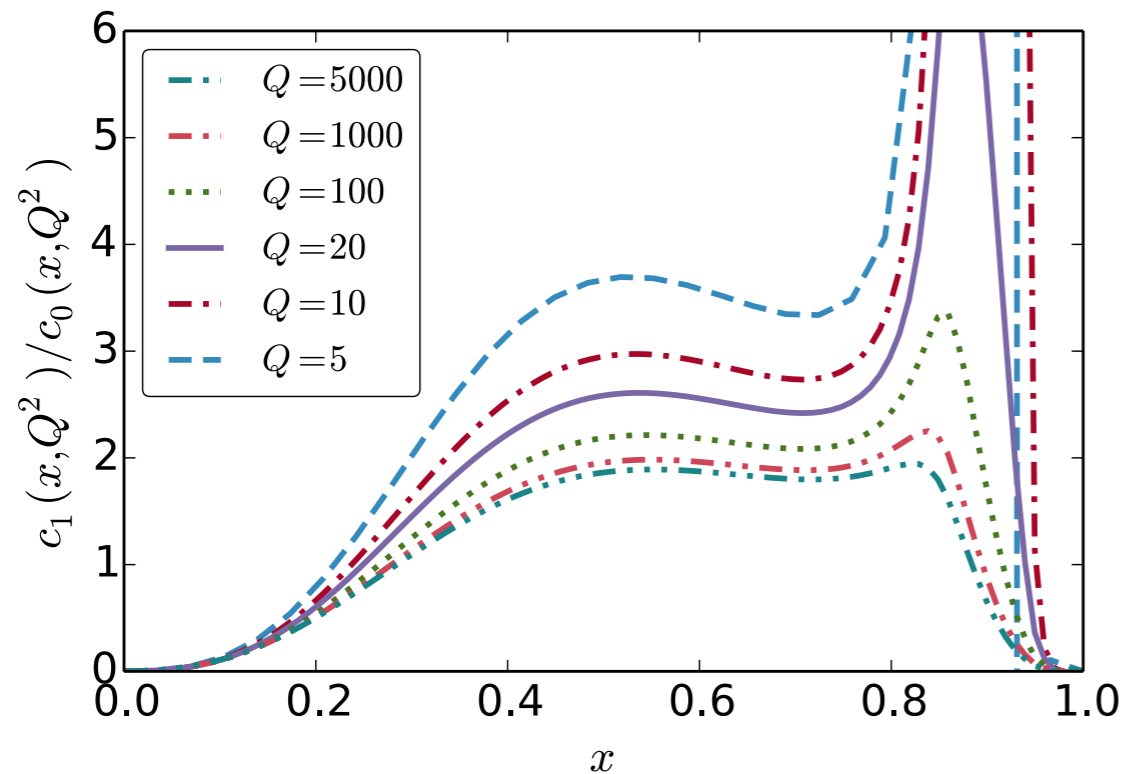


# Parton-Parton Luminosities: Bottom



**Figure 11.** Ratio of luminosities at the LHC14 for bottom-quark PDF sets with different normalizations of the intrinsic bottom component. The plot has been truncated, and the  $b\bar{b}$  luminosity in the extreme scenario reaches about 17 at  $\sqrt{\tau} = 0.5$ .

# IC vs IB



- Clearly,  $b_1/b_0 \ll c_1/c_0$  (for the model used)
- Questions:

What would be the ratio “intrinsic/extrinsic” for the strange sea or the light quark sea at large- $x$ ?

If there is a “bump” due to IC, one can also expect “bumps” for the light sea?

# Processes sensitive to heavy quarks

# Processes sensitive to the charm PDF

- $F_2^c$  at HERA:

charm contributes **more than 20%** to the DIS structure functions

all charm data at  $x < 0.1$

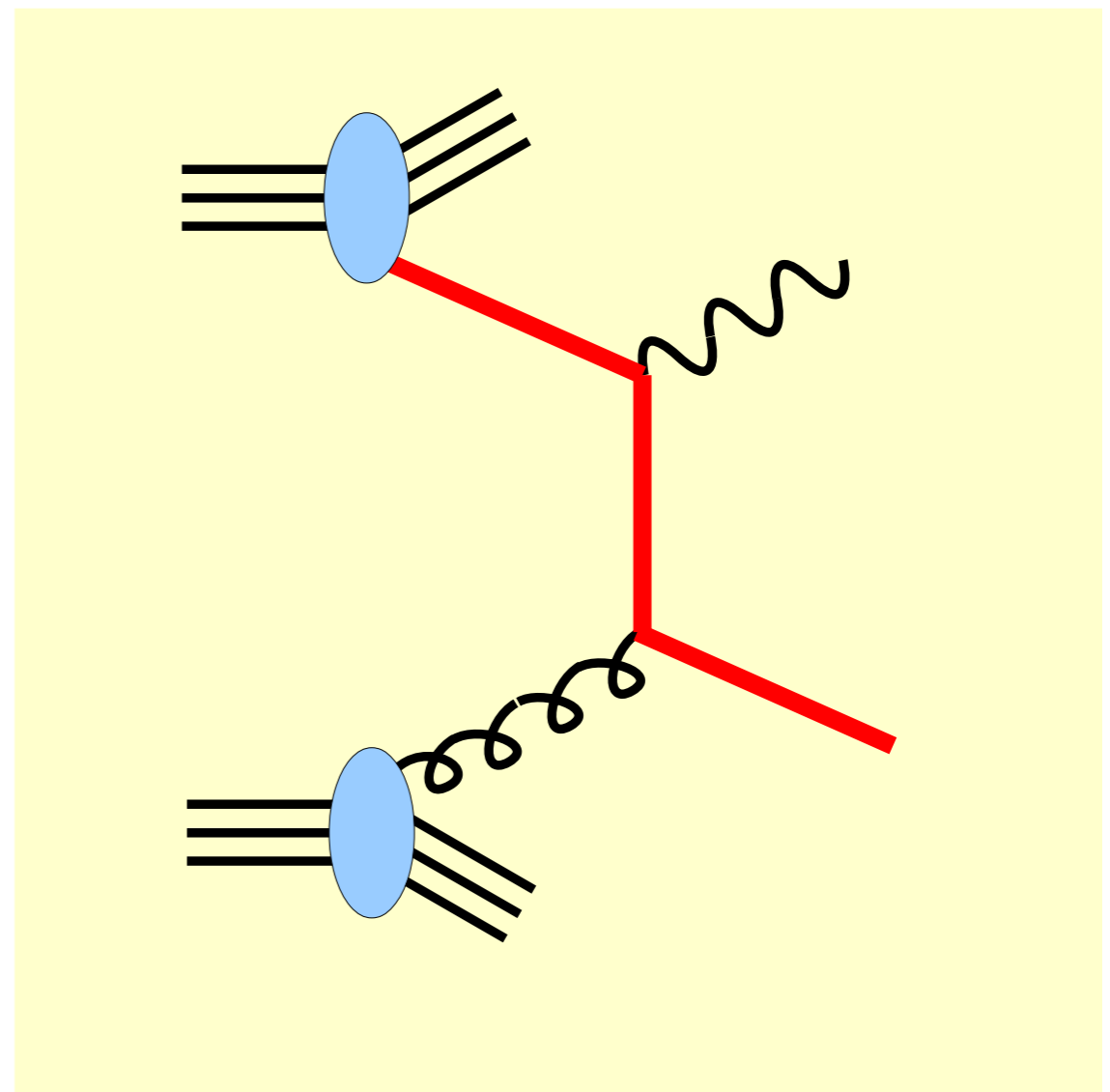
- Fixed target DIS:

the ‘controversial’ EMC data

include larger  $x$ , new progress in the understanding thanks to recent NNPDF study

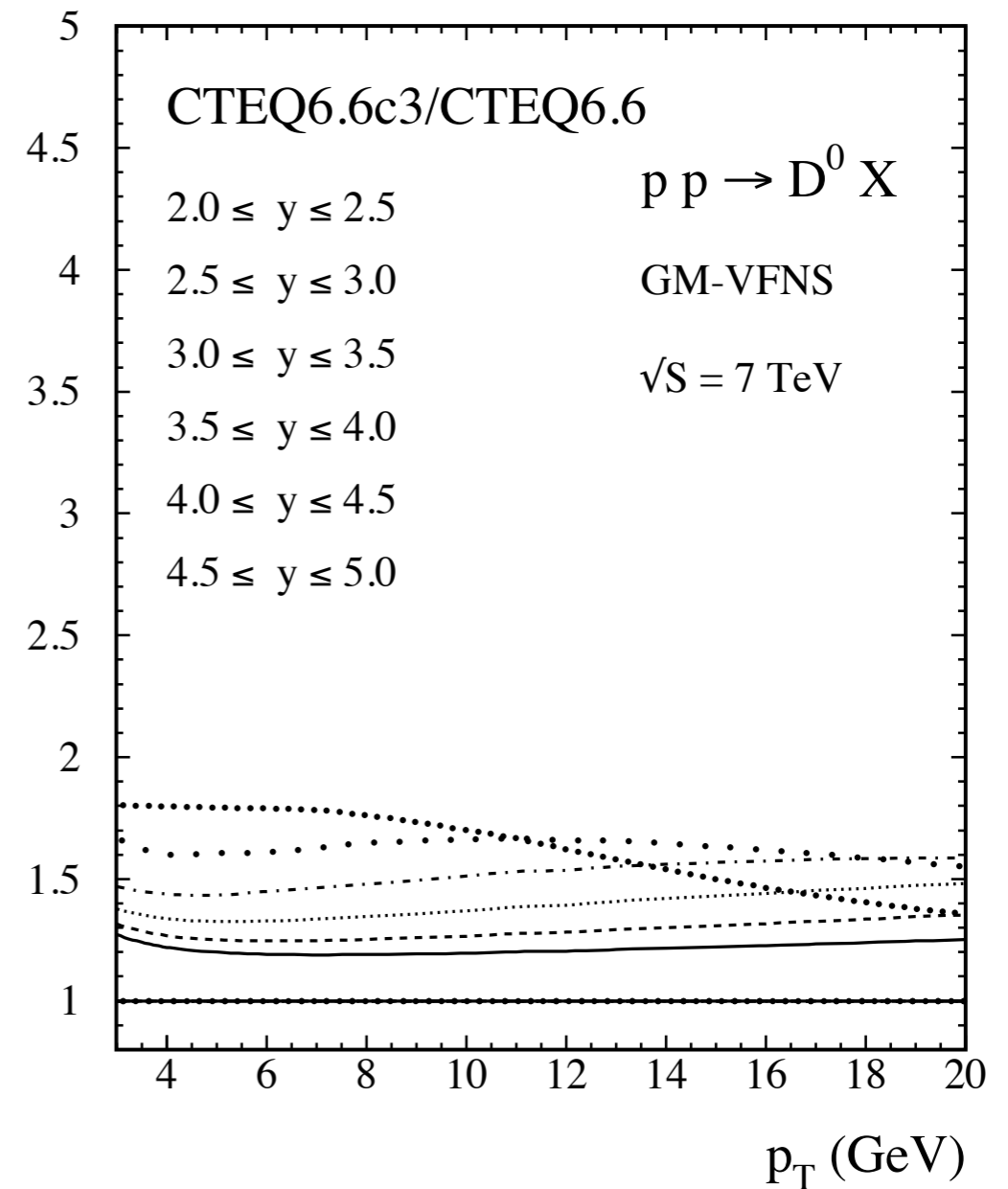
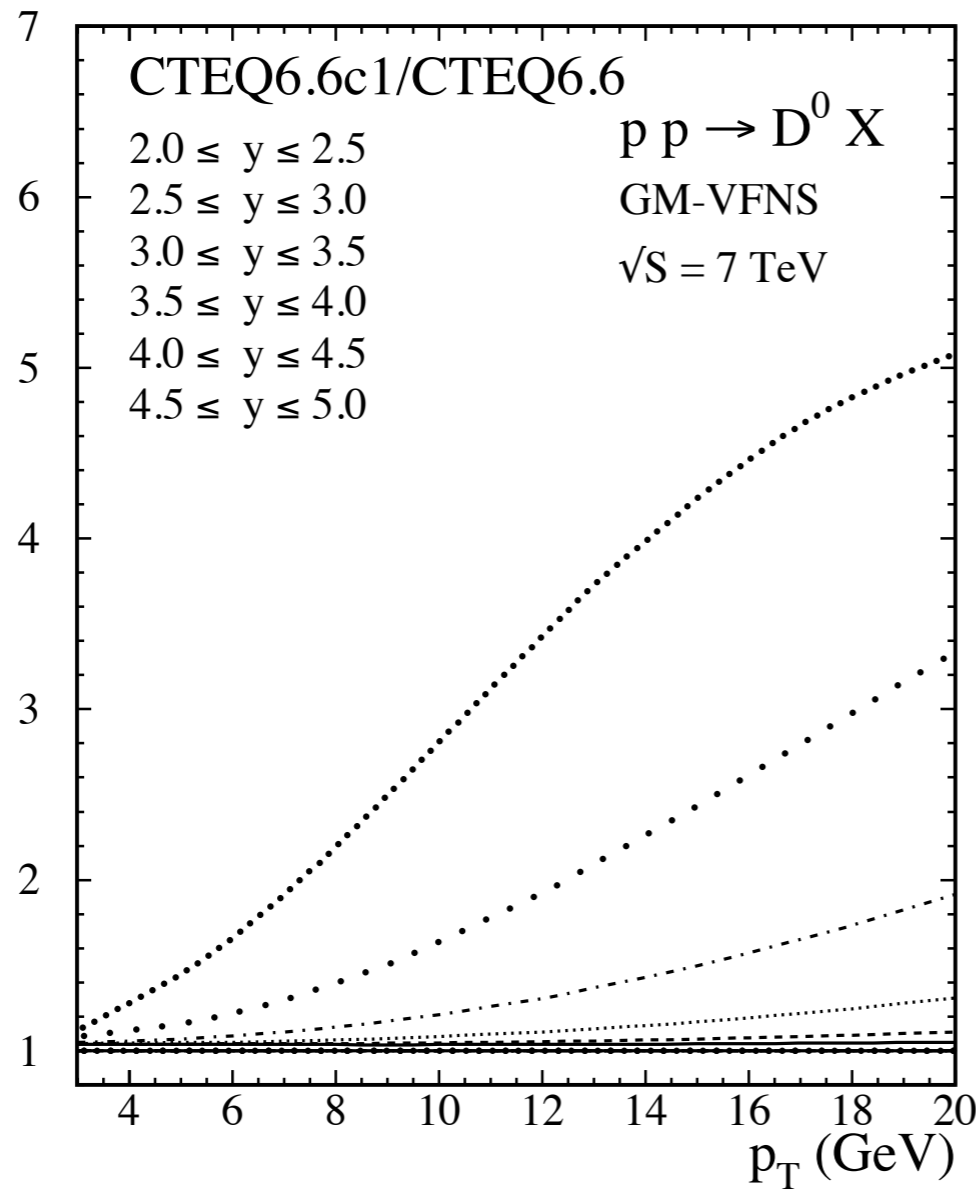
# Processes sensitive to the charm PDF

- Drell-Yan production of W/Z has a relevant contribution from the cs-channel at the LHC
- Exclusive processes
  - $c+g \rightarrow c+\gamma$
  - $c+g \rightarrow c+Z$
  - $c+g \rightarrow b+W$



# Inclusive D meson production at LHCb

arXiv:1202.0439,arXiv:0901.4130



CTEQ6.6 updated:

BHPS, 3.5 % ( $c + \bar{c}$ ) at  $\mu = 1.3 \text{ GeV}$

high-strength sea-like charm

→ large effects expected at large rapidities

# Future

- $F_2^c$  at EIC:

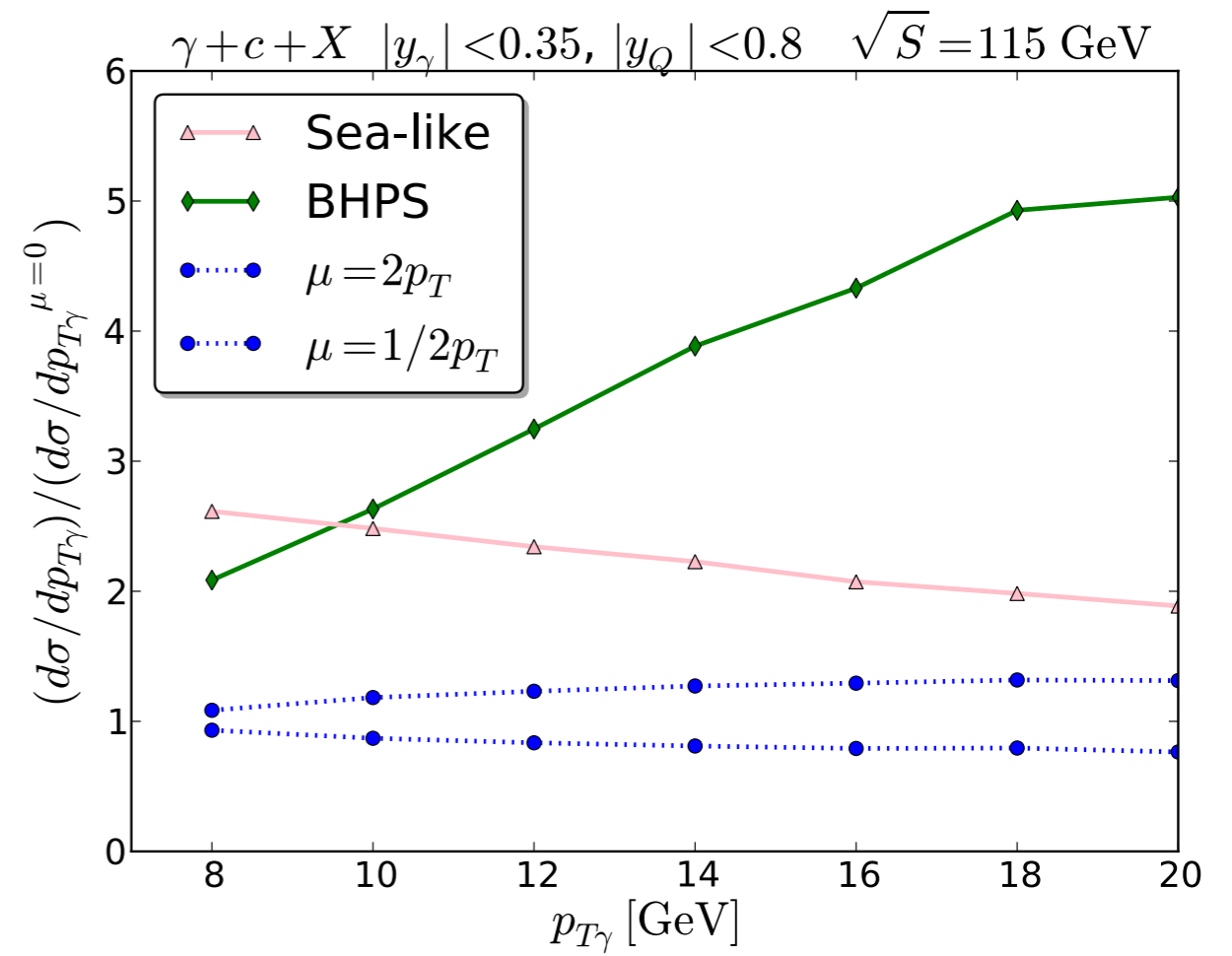
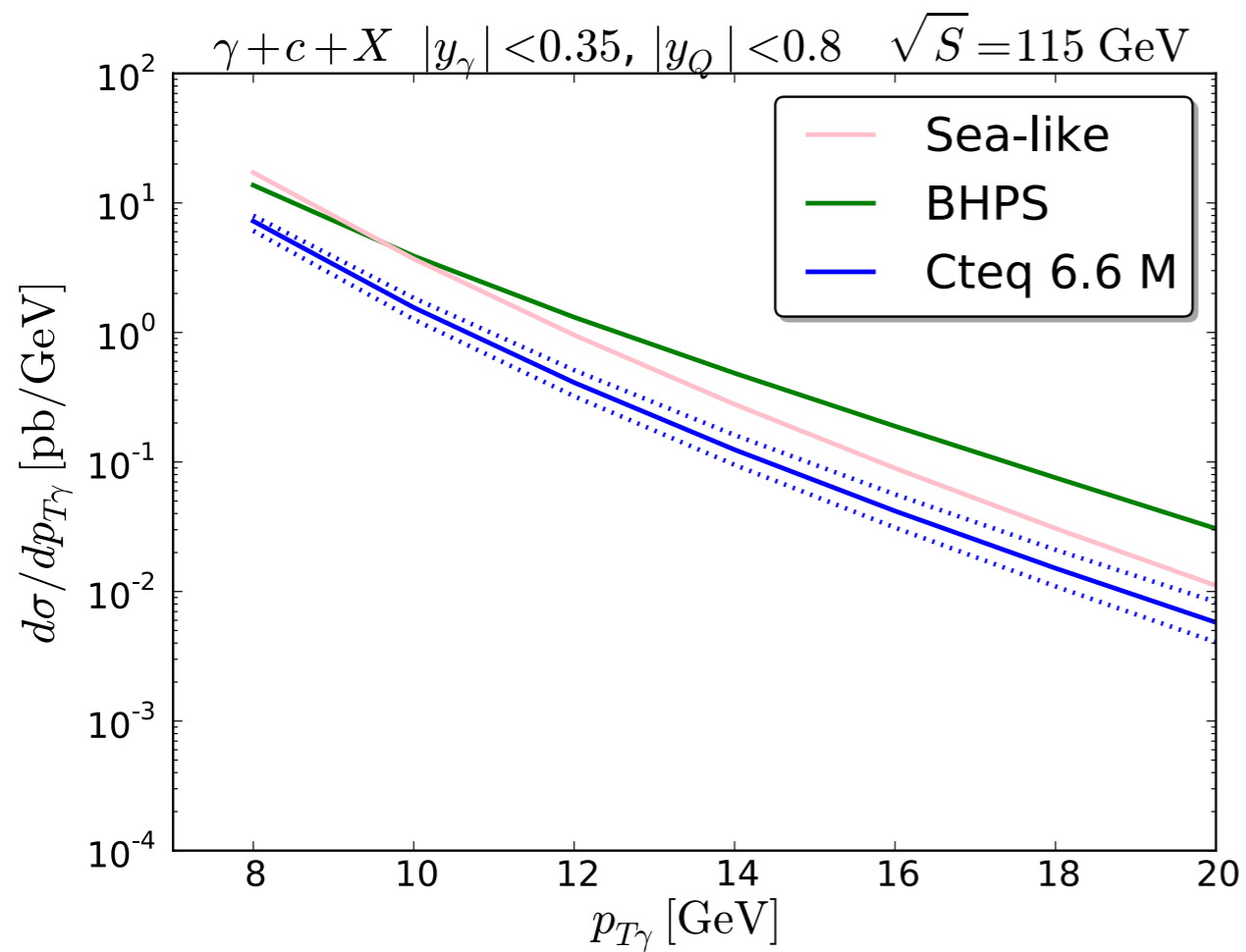
probing larger x-values ( $x \sim 0.3$ )

- Fixed target experiments using the LHC beam (AFTER@LHC):  $\sqrt{S} = 115 \text{ GeV}$

would be ideal to probe large-x IC in hadronic collisions

# Probing IC in $\gamma+Q$ production at AFTER@LHC

arXiv:1504.06287





# Conclusions

# Conclusions

- An intrinsic charm contribution is predicted by QCD.

“If QCD is right, there has to be IC”

- Open question: “How much IC is there?”  
(If you are believer)

Normalization is unclear. Typically  $\langle x \rangle_{c+cbar} \sim 0.01$

- Need more “DATA” (real or lattice)
- Is it possible to calculate, for example,  $\langle x \rangle_{c+cbar}$  on the lattice? With which precision?
- $c$  and  $cbar$  independently?