

# Probing the BFKL dynamics at hadronic colliders

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9th workshop on Multipartonic Interactions, Shimla, India, 11-15  
December 2017

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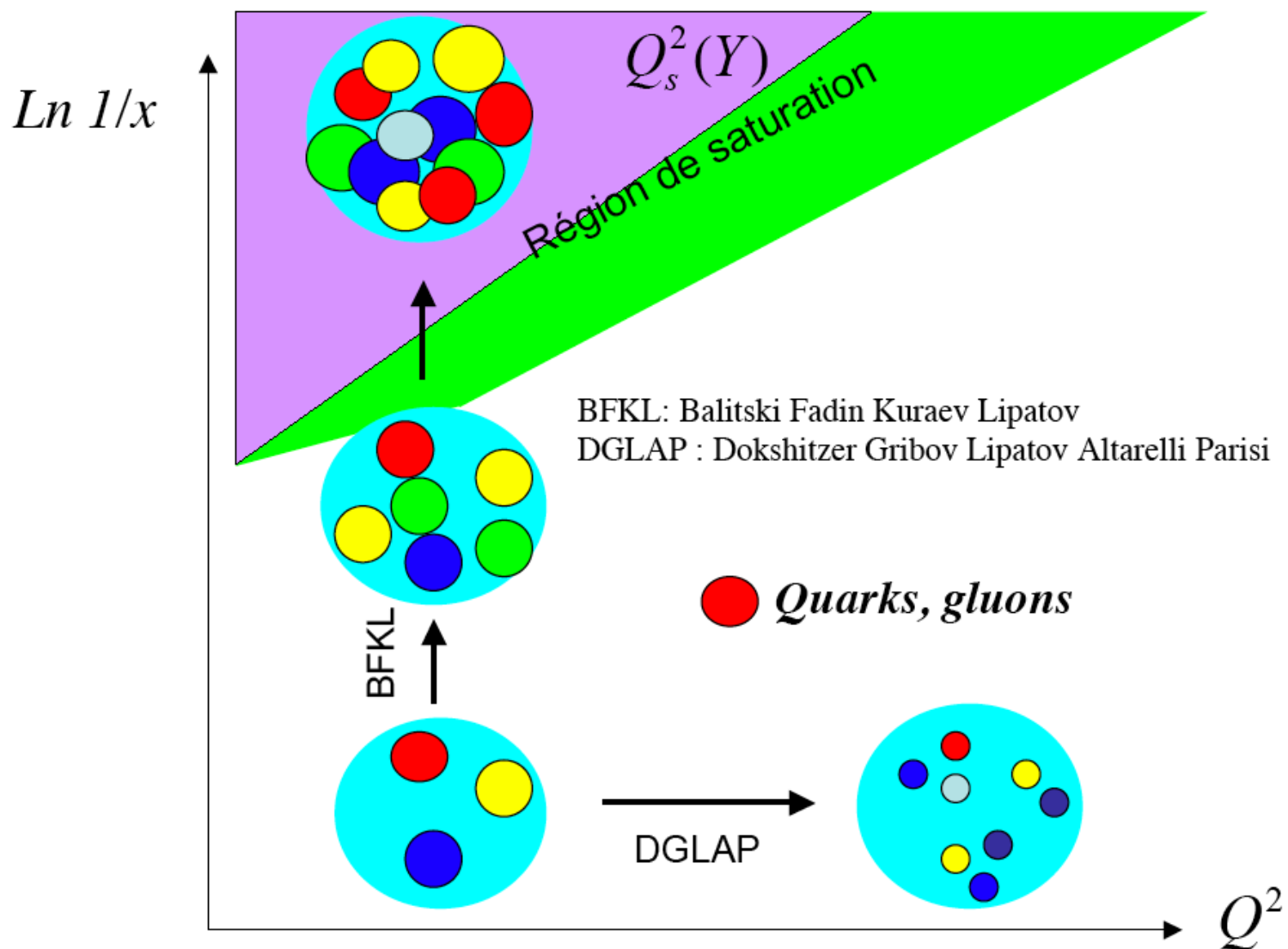
- Forward jets at HERA (short reminder)
- Mueller Navelet jet
- Jet gap jet at Tevatron, LHC
- Jet gap jet in diffraction at the LHC

Work done in collaboration with D. Werder, O. Kepka, C. Marquet, R. Peschanski, M. Trzebinski, Y. Hatta, G. Soyez, T. Ueda, R. Zlebcik,...

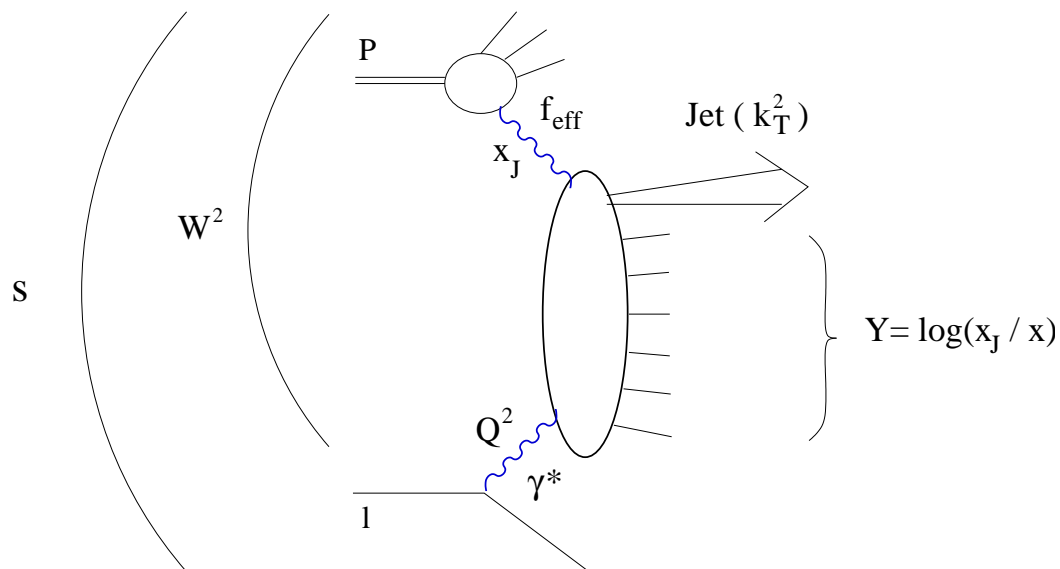
Work in progress with G. Chachamis, D. Colferai, F. Deganutti, D. Gordo, T. Raben, A. Sabio Vera, S. Schlichting

## Looking for BFKL/saturation effects

Looking for BFKL effects ( $x$ -resummation) at HERA/LHC in dedicated final states



## Forward jet measurement at HERA



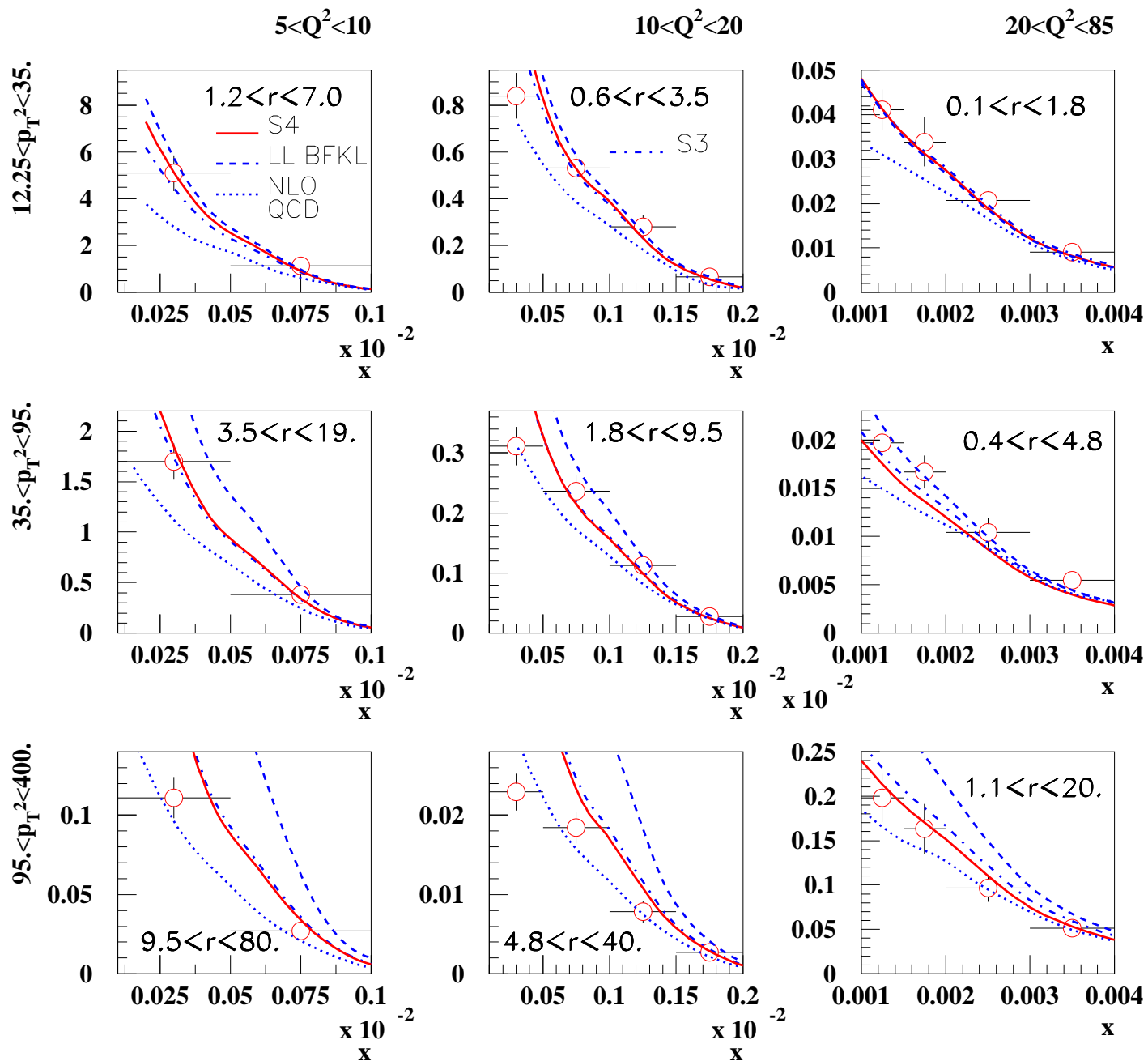
- Full BFKL NLL calculation used for the BFKL kernel, available in S3 and S4 resummation schemes to remove the spurious singularities (modulo the impact factors taken at LL)
- Equation:

$$\frac{d\sigma_{T,L}^{\gamma^* p \rightarrow JX}}{dx_J dk_T^2} = \frac{\alpha_s(k_T^2)\alpha_s(Q^2)}{k_T^2 Q^2} f_{\text{eff}}(x_J, k_T^2) \int \frac{d\gamma}{2i\pi} \left(\frac{Q^2}{k_T^2}\right)^\gamma \phi_{T,L}^\gamma(\gamma) e^{\bar{\alpha}(k_T Q)\chi_{\text{eff}}[\gamma, \bar{\alpha}(k_T Q)]Y}$$

- Implicit equation:  $\chi_{\text{eff}}(\gamma, \alpha) = \chi_{\text{NLL}}(\gamma, \alpha, \chi_{\text{eff}}(\gamma, \alpha))$  solved numerically (Nucl. Phys. B 739 (2006) 131; Phys. Lett. B 655 (2007) 236; Eur. Phys. J. C55 (2008) 259)

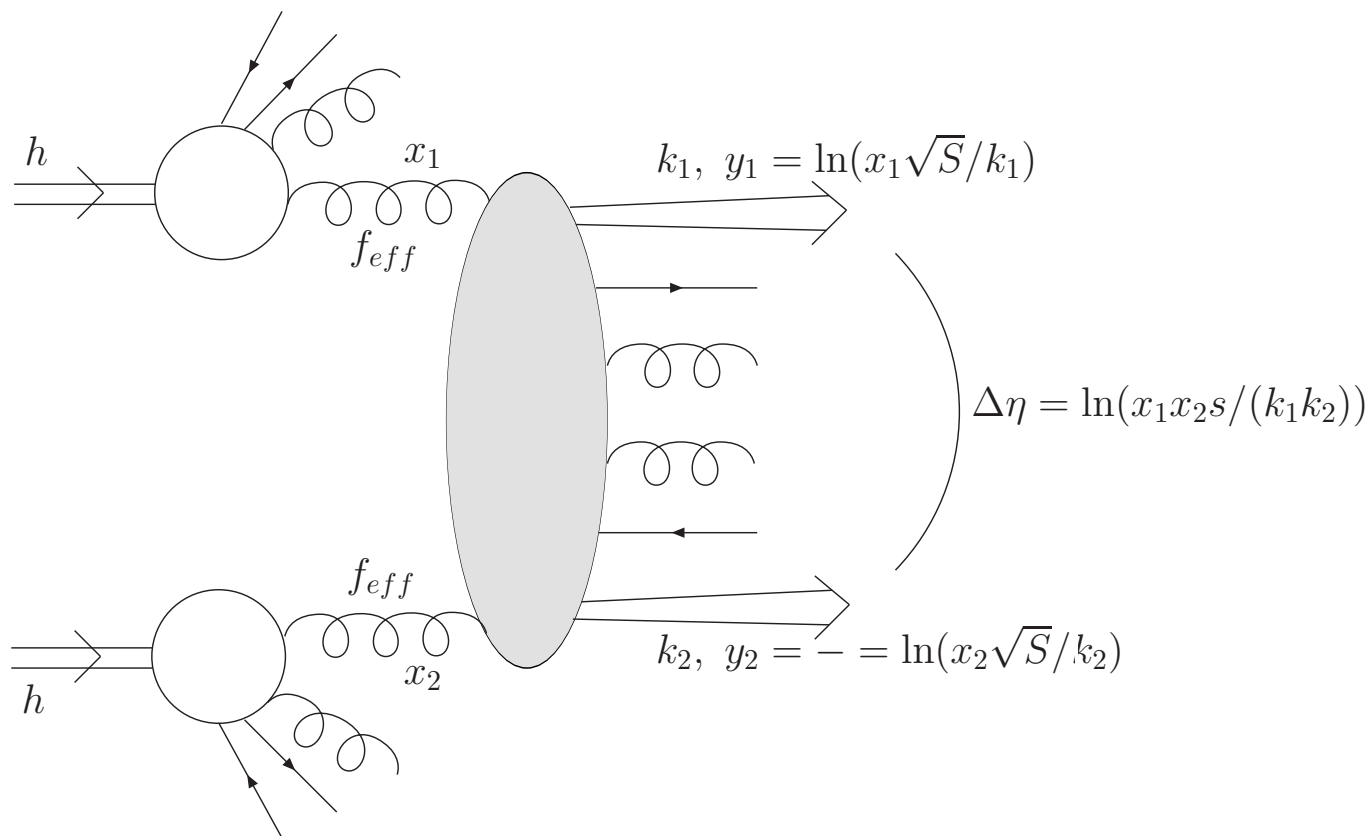
# Comparison with H1 triple differential data

$d\sigma/dx dp_T^2 dQ^2$  - H1 DATA



## Mueller Navelet jets

Same kind of processes at the Tevatron and the LHC



- Same kind of processes at the Tevatron and the LHC: Mueller Navelet jets
- Study the  $\Delta\Phi$  between jets dependence of the cross section:
- See papers by Papa, Murdaca, Wallon, Szymanowski, Ducloue, Sabio-Vera, Chachamis...

## Mueller Navelet jets: $\Delta\Phi$ dependence

- Study the  $\Delta\Phi$  dependence of the relative cross section
- Relevant variables:

$$\begin{aligned}\Delta\eta &= y_1 - y_2 \\ y &= (y_1 + y_2)/2 \\ Q &= \sqrt{k_1 k_2} \\ R &= k_2/k_1\end{aligned}$$

- Azimuthal correlation of dijets:

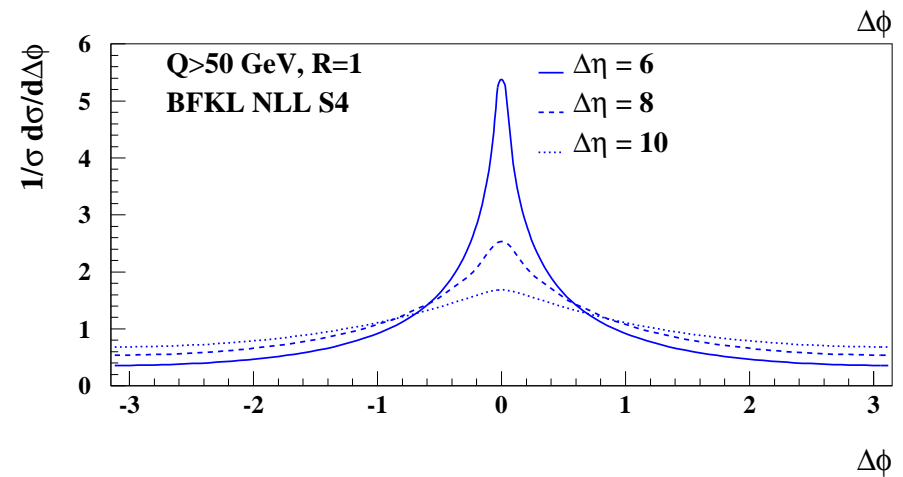
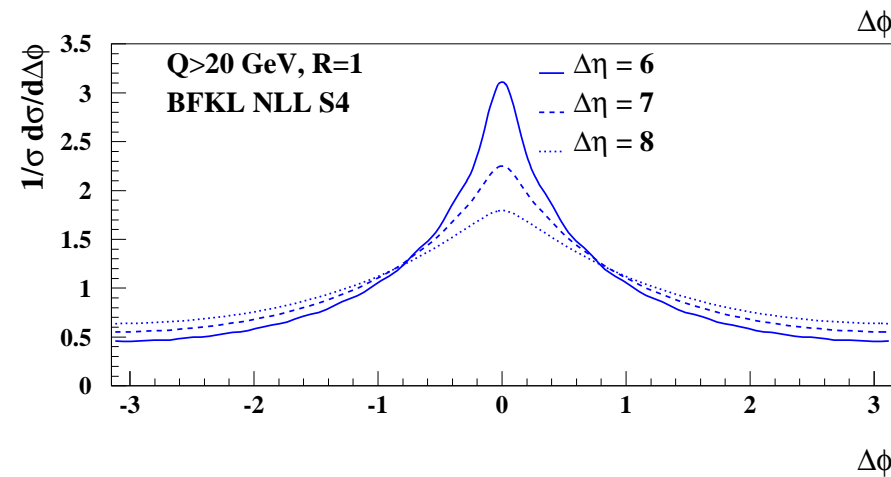
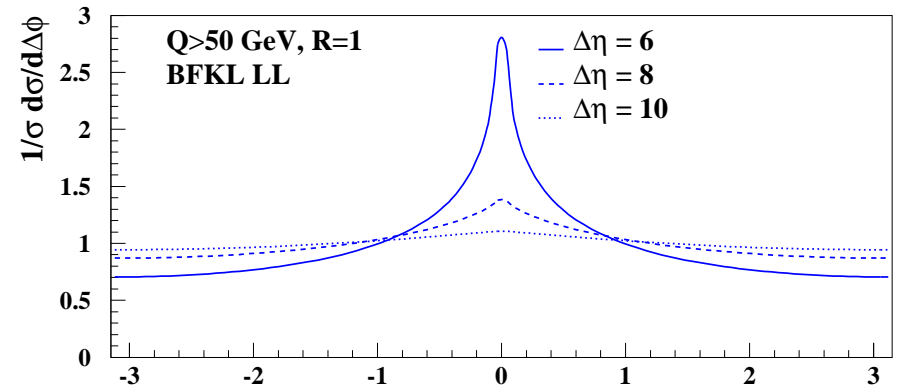
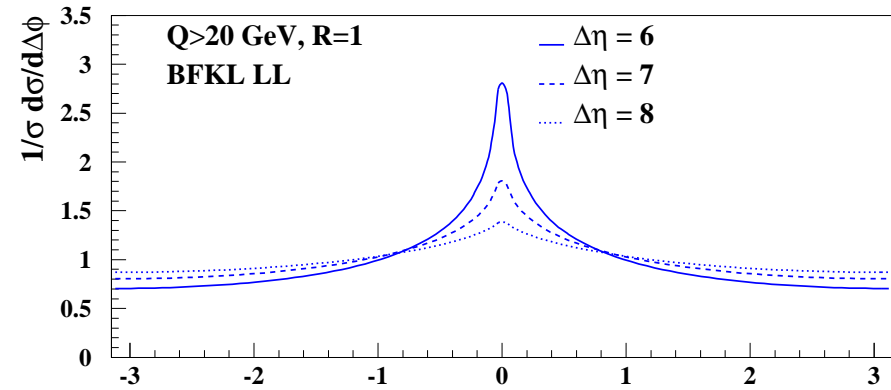
$$\begin{aligned}2\pi \frac{d\sigma}{d\Delta\eta dR d\Delta\Phi} \Big/ \frac{d\sigma}{d\Delta\eta dR} &= 1 + \\ \frac{2}{\sigma_0(\Delta\eta, R)} \sum_{p=1}^{\infty} \sigma_p(\Delta\eta, R) \cos(p\Delta\Phi)\end{aligned}$$

where

$$\begin{aligned}\sigma_p &= \int_{E_T}^{\infty} \frac{dQ}{Q^3} \alpha_s(Q^2/R) \alpha_s(Q^2 R) \\ &\left( \int_{y_<}^{y_>} dy x_1 f_{eff}(x_1, Q^2/R) x_2 f_{eff}(x_2, Q^2 R) \right) \\ &\int_{1/2-\infty}^{1/2+\infty} \frac{d\gamma}{2i\pi} R^{-2\gamma} e^{\bar{\alpha}(Q^2) \chi_{eff}(p) \Delta\eta}\end{aligned}$$

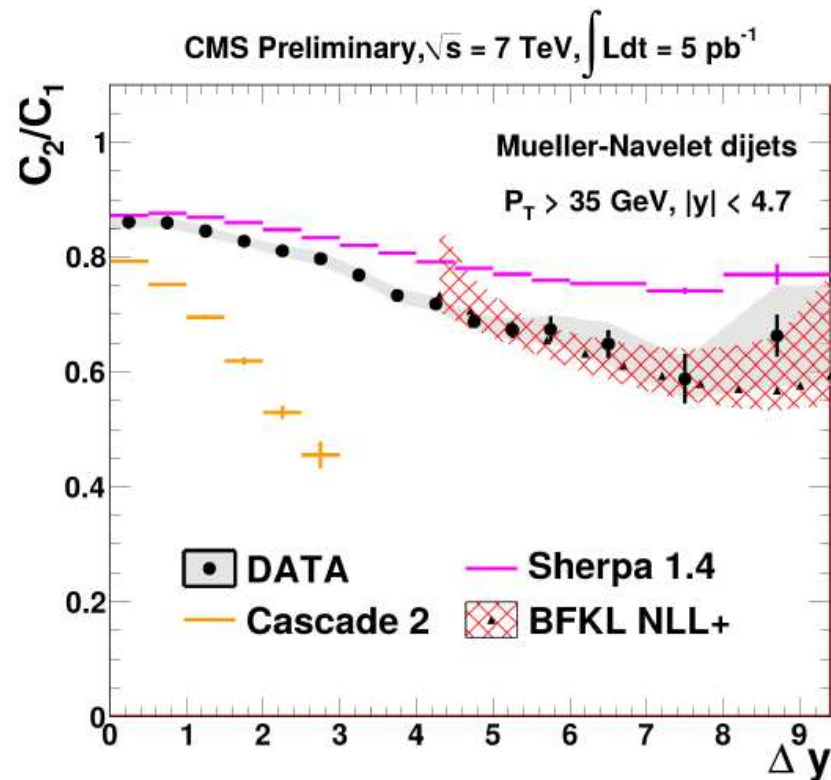
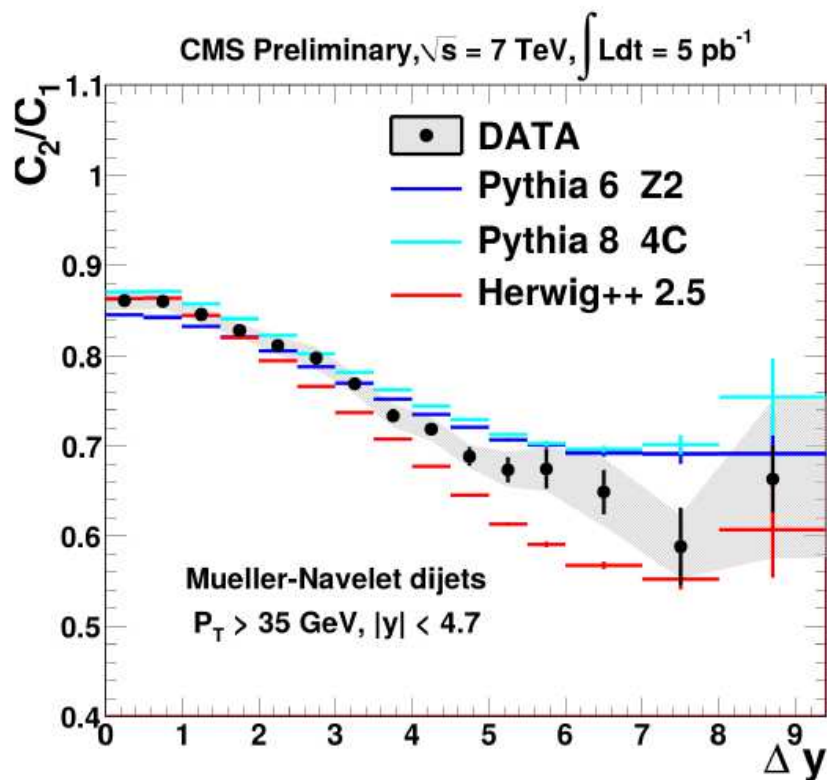
## Mueller Navelet jets: $\Delta\Phi$ dependence

- $1/\sigma d\sigma/d\Delta\Phi$  spectrum for BFKL LL and BFKL NLL as a function of  $\Delta\Phi$  for different values of  $\Delta\eta$ , scale dependence:  $\sim 20\%$



- C. Marquet, C.R., Phys. Rev. D79 (2009) 034028
- Mueller Navelet jets at NLL and saturation effects: Study in progress with F. Deganutti, T. Raben, S. Schlichting

## CMS measurement of MN jets



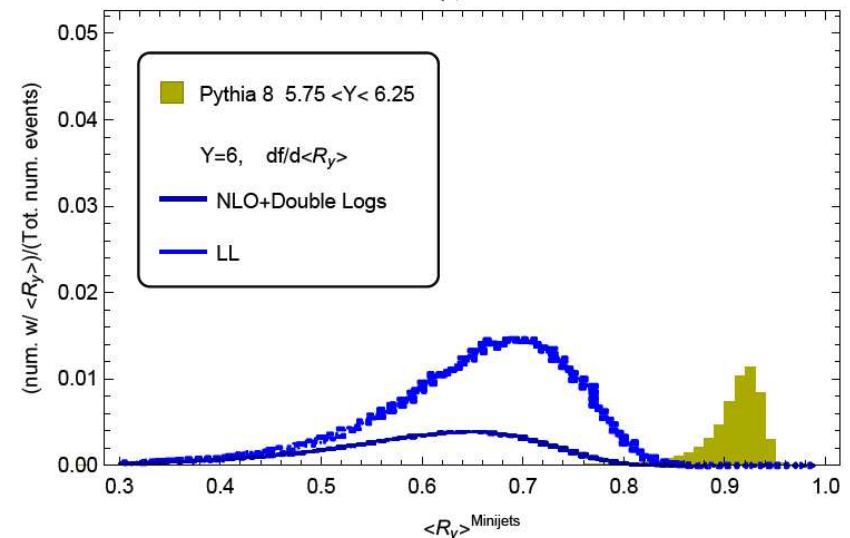
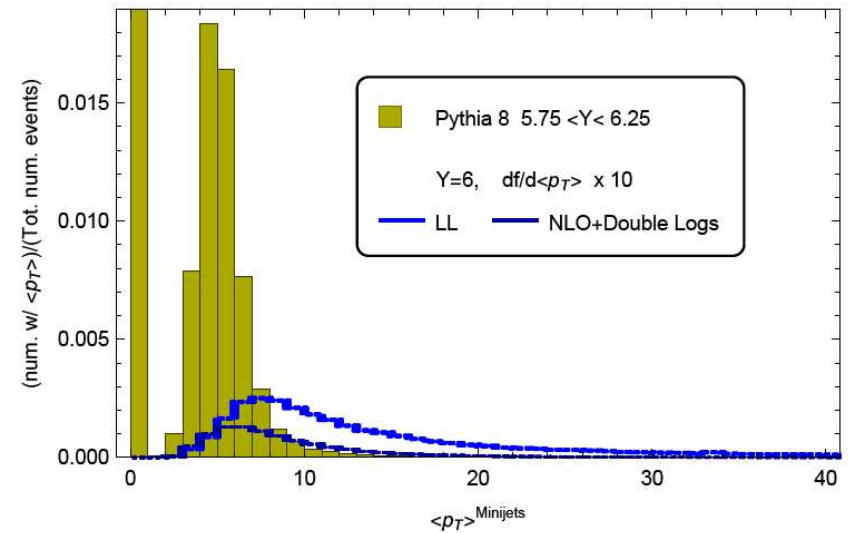
- Test of BFKL predictions at 7 TeV for  $C_m/C_0 = \langle \cos(m(\Phi_{J_1} - \Phi_{J_2} - \pi)) \rangle$
- no clear difference between BFKL and DGLAP dynamics



## BFKL dynamics: looking for less inclusive variables

$$\langle p_T \rangle = \frac{1}{N} \sum_{i=1}^N |p_{Ti}|$$

$$\langle R_y \rangle = \frac{1}{N+1} \sum_{i=1}^{N+1} \frac{y_i}{y_{i-1}}$$



- Looking for multiple gluon emission along ladder characteristic of BFKL: number,  $p_T$ , rapidity distributions of “minijets”
- Comparison between BFKL-ex MC and pythia/herwig to find best variables: collaboration with A. Sabio Vera, D. Gordo, G. Chachamis, F. Deganutti, T. Raben

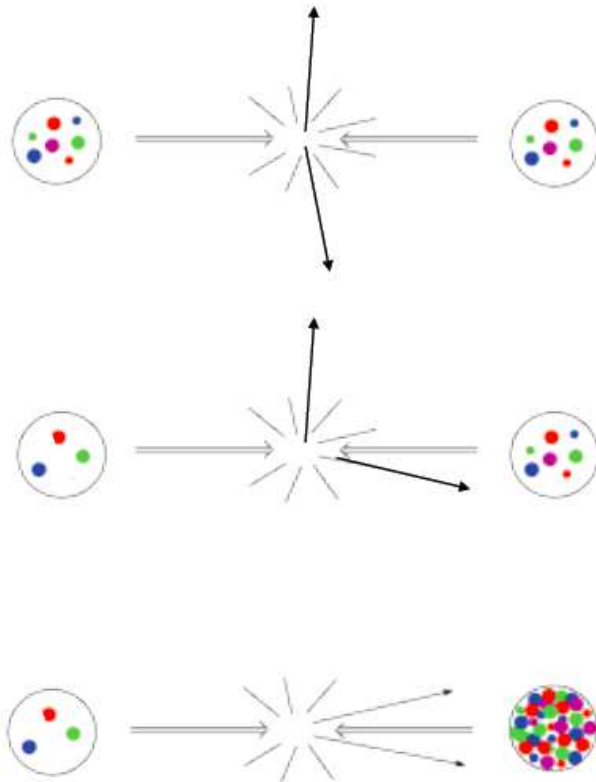
## Saturation effects at the LHC: Use pA data

- Saturation effects: need to go to low  $x$ , jets as forward as possible on the same side
- Compare pp and pA runs in order to remove many systematics

final state :  $k_1, y_1$     $k_2, y_2$

$$x_p = \frac{k_1 e^{y_1} + k_2 e^{y_2}}{\sqrt{s}} \quad x_A = \frac{k_1 e^{-y_1} + k_2 e^{-y_2}}{\sqrt{s}}$$

scanning the wave functions:



$$x_p \sim x_A < 1$$

central rapidities probe moderate  $x$

$$x_p \text{ increases} \quad x_A \sim \text{unchanged}$$

$$x_p \sim 1, x_A < 1$$

forward/central doesn't probe much smaller  $x$

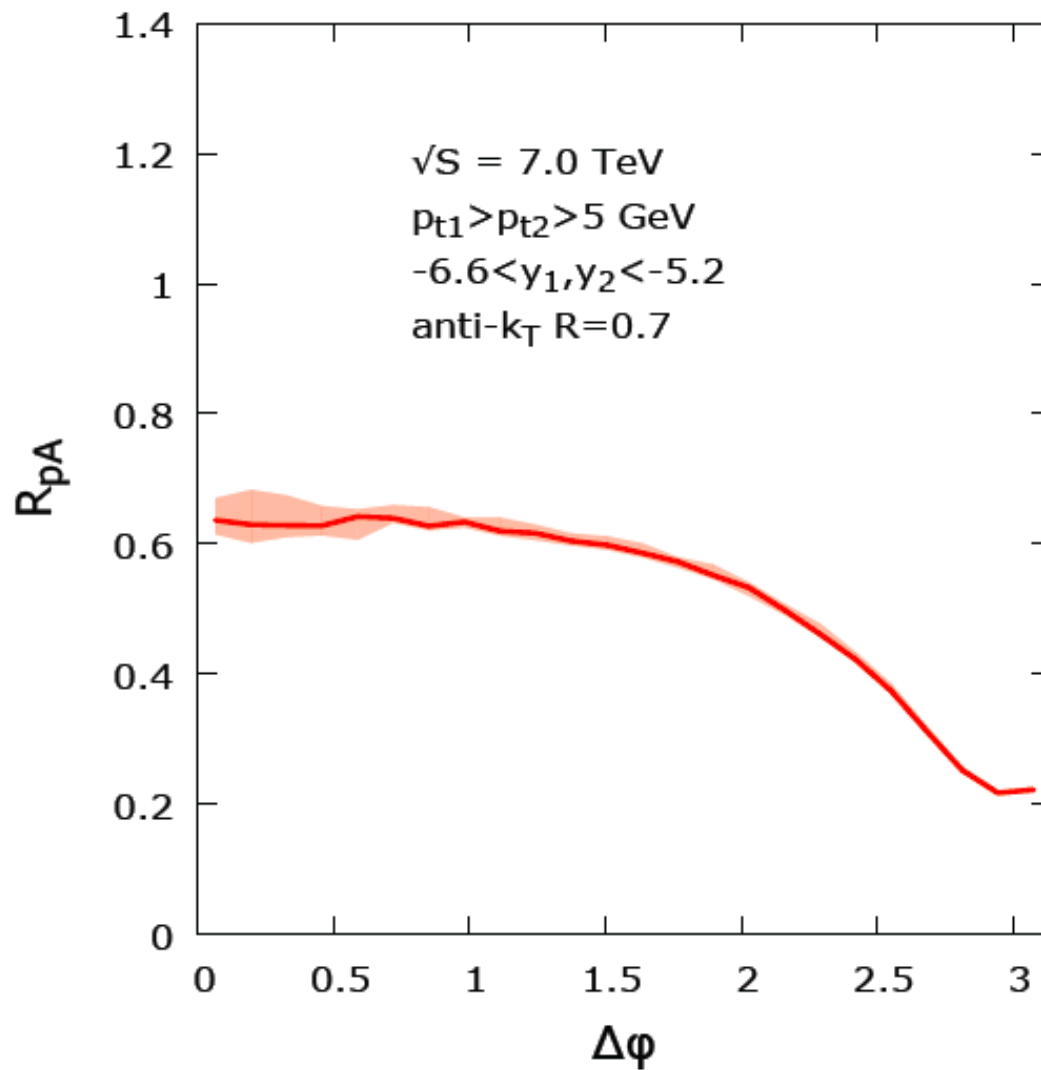
$$x_p \sim \text{unchanged} \quad x_A \text{ decreases}$$

$$x_p \sim 1, x_A \ll 1$$

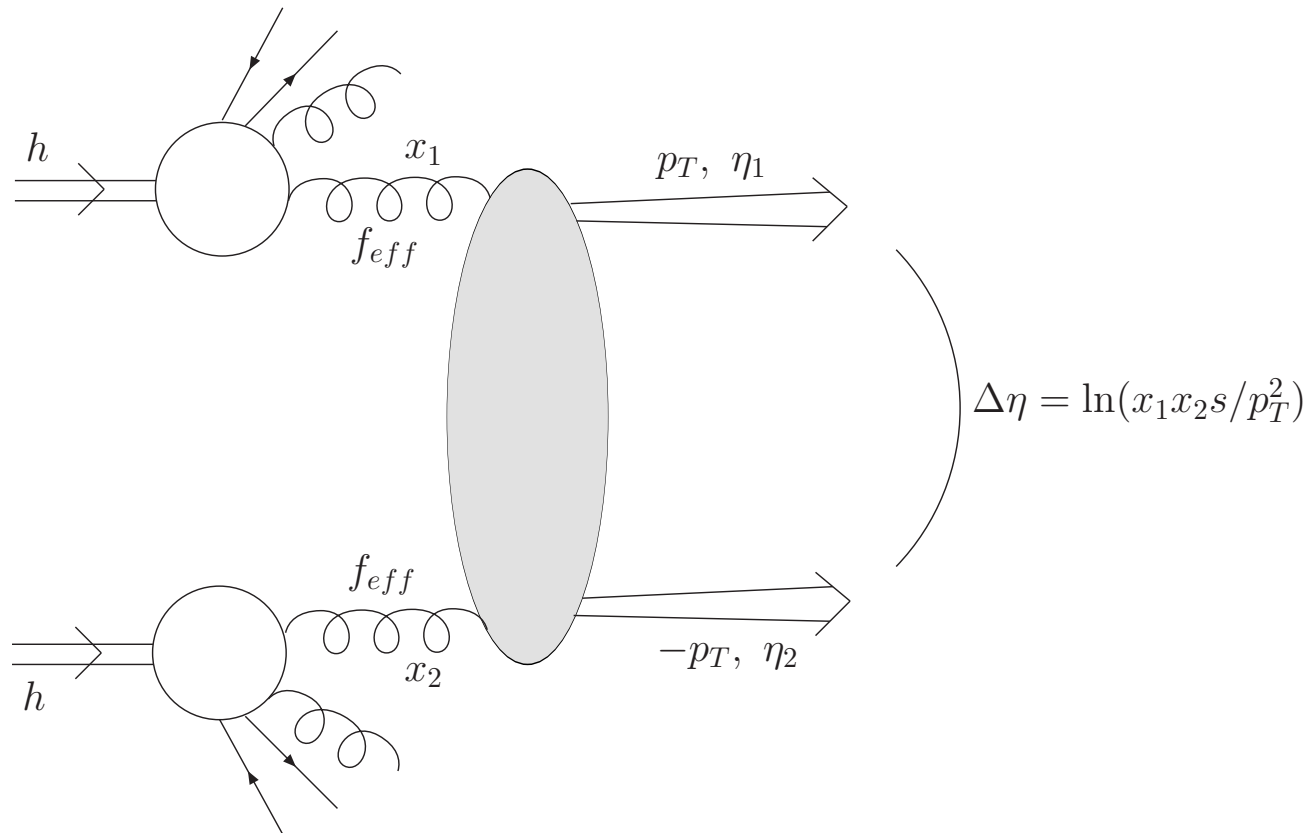
forward rapidities probe small  $x$

## Saturation effects at the LHC

- Suppression factor between pp and pA runs: estimated to be 1/2 in CASTOR acceptance
- Important to get CASTOR in pA and low lumi pp data
- Study performed by Cyrille Marquet et al.



## Jet gap jet cross sections



- **Test of BFKL evolution:** jet gap jet events, large  $\Delta\eta$ , same  $p_T$  for both jets in BFKL calculation
- **Principle:** Implementation of BFKL NLL formalism in HERWIG Monte Carlo (Measurement sensitive to jet structure and size, gap size smaller than  $\Delta\eta$  between jets)

## BFKL formalism

- **BFKL jet gap jet cross section:** integration over  $\xi$ ,  $p_T$  performed in Herwig event generation

$$\frac{d\sigma^{pp \rightarrow XJJY}}{dx_1 dx_2 dp_T^2} = S \frac{f_{eff}(x_1, p_T^2) f_{eff}(x_2, p_T^2)}{16\pi} |A(\Delta\eta, p_T^2)|^2$$

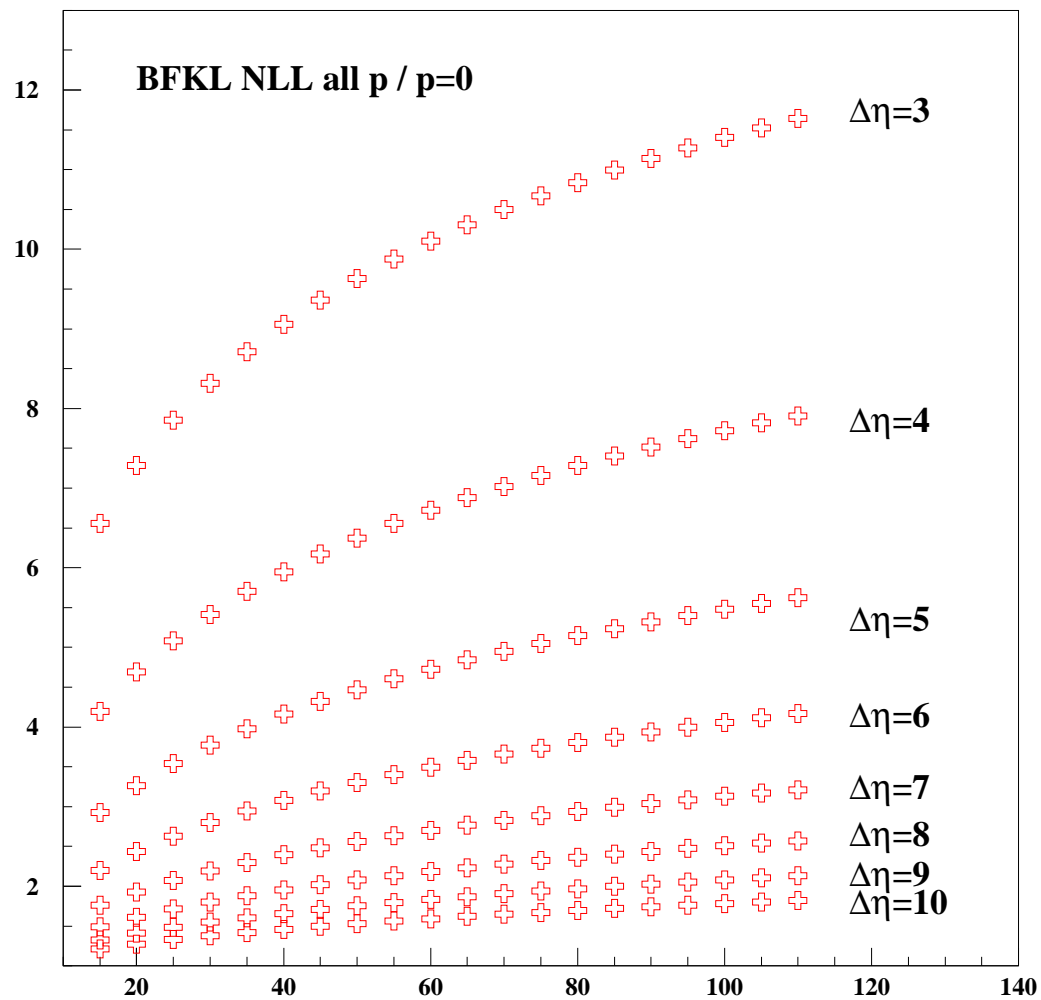
where  $S$  is the survival probability (0.1 at Tevatron, 0.03 at LHC)

$$A(\Delta\eta, p_T^2) = \frac{16N_c\pi\alpha_s^2}{C_F p_T^2} \sum_{p=-\infty}^{\infty} \int \frac{d\gamma}{2i\pi} \frac{[p^2 - (\gamma - 1/2)^2]}{[(\gamma - 1/2)^2 - (p - 1/2)^2]} \frac{\exp\left\{\frac{\alpha_s N_c}{\pi} \chi_{eff} \Delta\eta\right\}}{[(\gamma - 1/2)^2 - (p + 1/2)^2]}$$

- $\alpha_s$ : 0.17 at LL (constant), running using RGE at NLL
- **BFKL effective kernel  $\chi_{eff}$ :** determined numerically, solving the implicit equation:  $\chi_{eff} = \chi_{NLL}(\gamma, \bar{\alpha} \chi_{eff})$
- **S4 resummation scheme used** to remove spurious singularities in BFKL NLL kernel
- **Implementation in Herwig Monte Carlo:** needed to take into account jet size and at parton level the gap size is equal to  $\Delta\eta$  between jets
- **Herwig MC:** Parametrised distribution of  $d\sigma/dp_T^2$  fitted to BFKL NLL cross section (2200 points fitted between  $10 < p_T < 120$  GeV,  $0.1 < \Delta\eta < 10$  with a  $\chi^2 \sim 0.1$ )

## BFKL formalism: resummation over conformal spins

- Study of the ratio  $\frac{d\sigma/dp_T(\text{all } p)}{d\sigma/dp_T(p=0)}$
- Resummation over  $p$  needed: modifies the  $p_T$  and  $\Delta\eta$  dependences...

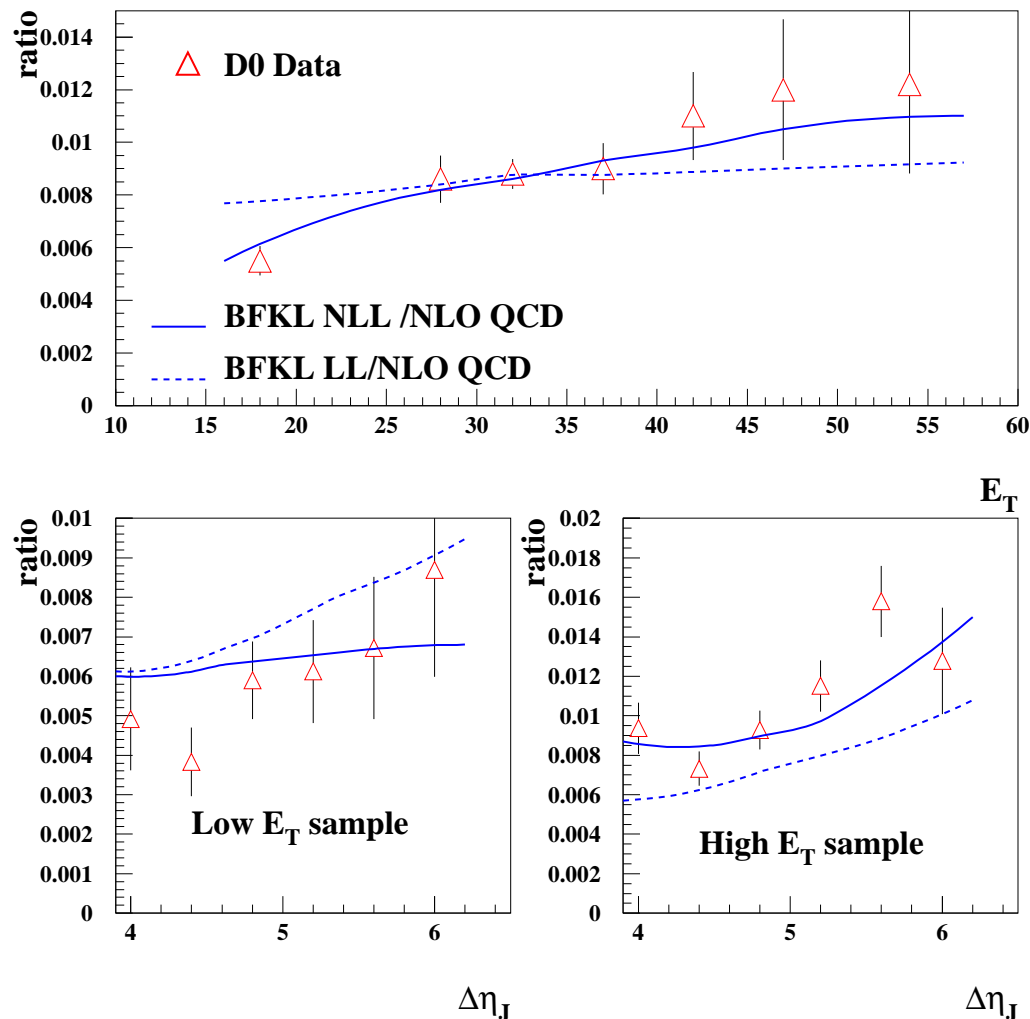


## Comparison with D0 data

- **D0 measurement:** Jet gap jet cross section ratios as a function of second highest  $E_T$  jet, or  $\Delta\eta$  for the low and high  $E_T$  samples, the gap between jets being between -1 and 1 in rapidity
- **Comparison with BFKL formalism:**

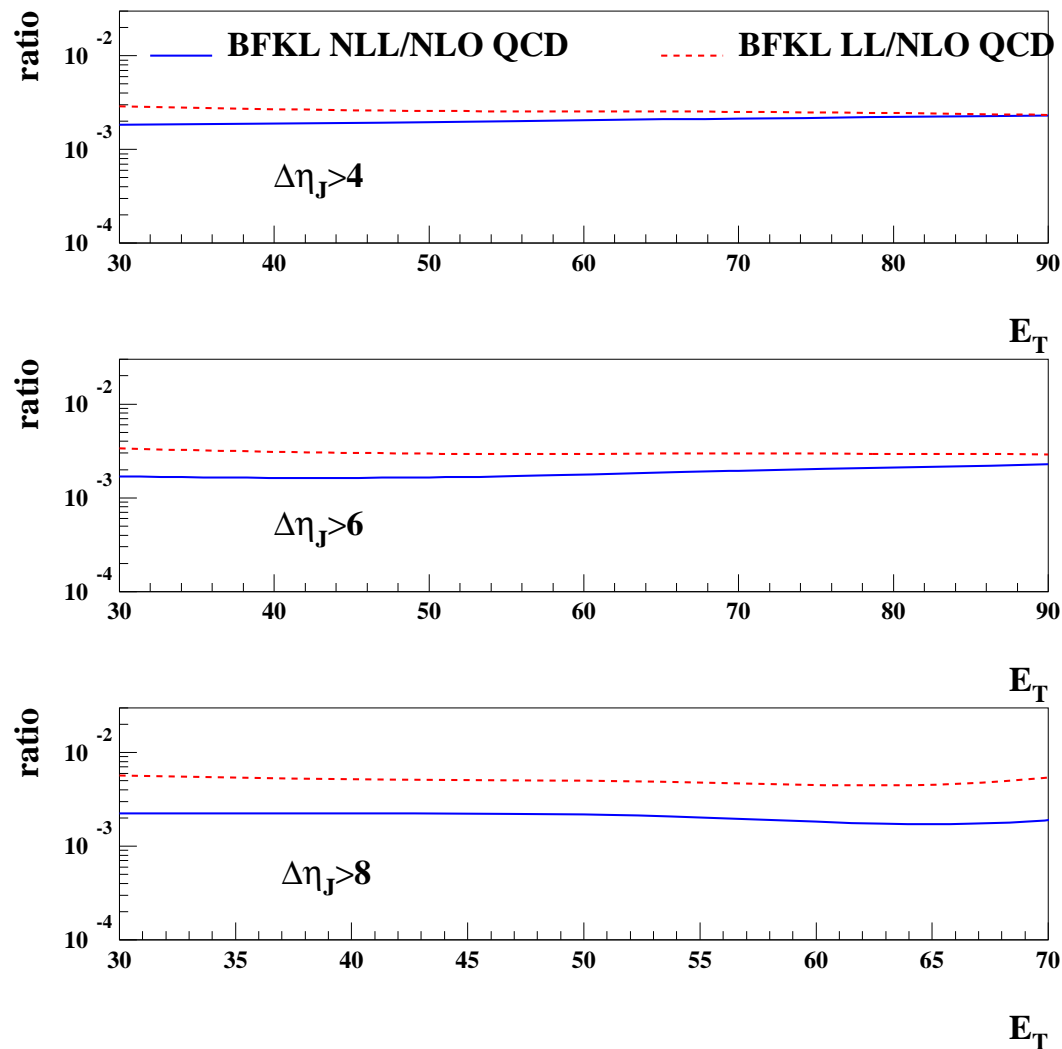
$$\text{Ratio} = \frac{\text{BFKL NLL Herwig}}{\text{Dijet Herwig}} \times \frac{\text{LO QCD NLOJet}++}{\text{NLO QCD NLOJet}++}$$

- Reasonable description using BFKL NLL formalism



## Predictions for the LHC

- Weak  $E_T$  and  $\Delta\eta$  dependence
- Large differences in normalisation between BFKL LL and NLL predictions

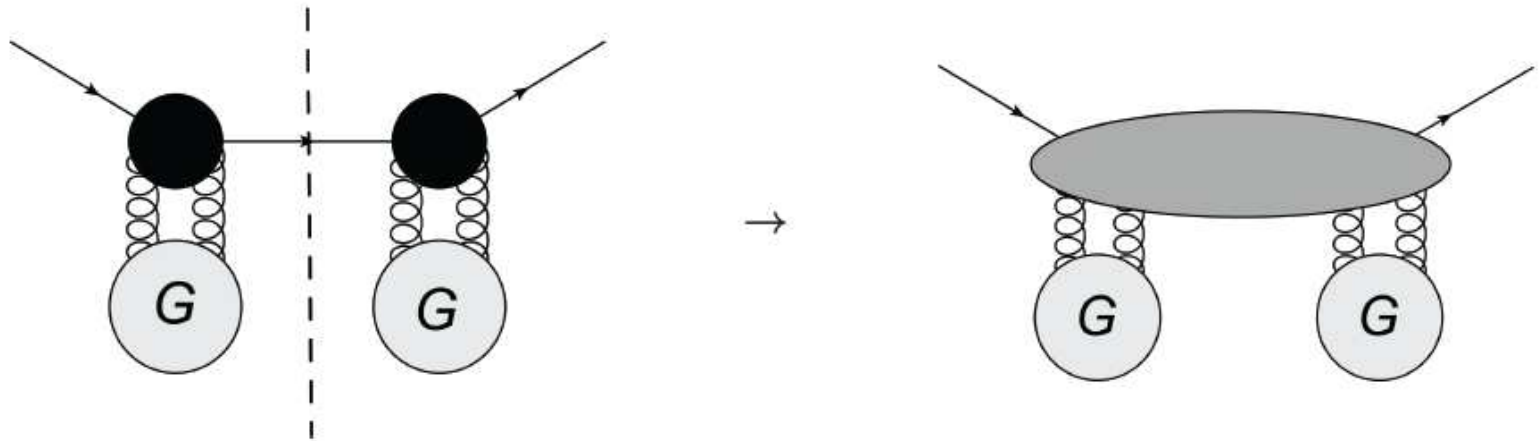


- Implementation of BFKL NLL formalism including NLO impact factors
- Work done in collaboration with D. Colferai, F. Deganutti, T. Raben



## Full NLL calculation (in progress)

- Combine NLL kernel with NLO impact factors (Hentschinski, Madrigal, Murdaca, Sabio Vera 2014)
- At NLO, impact factors are much more complicated!



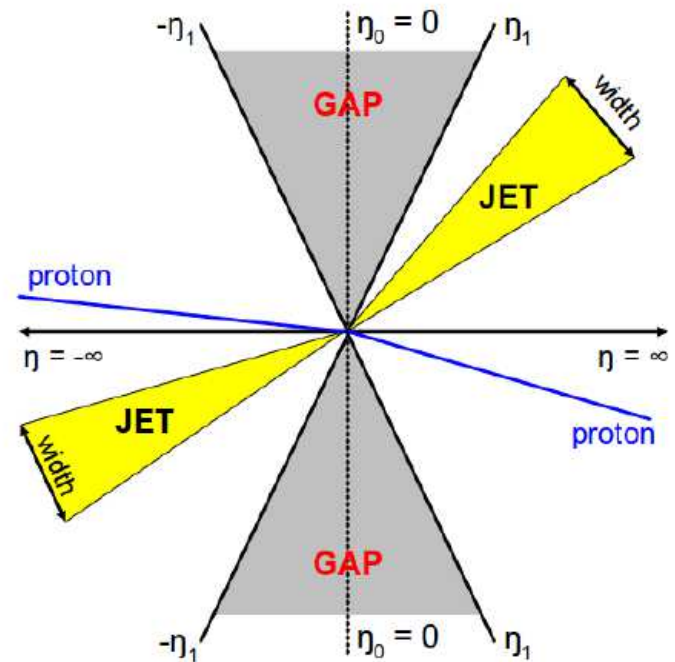
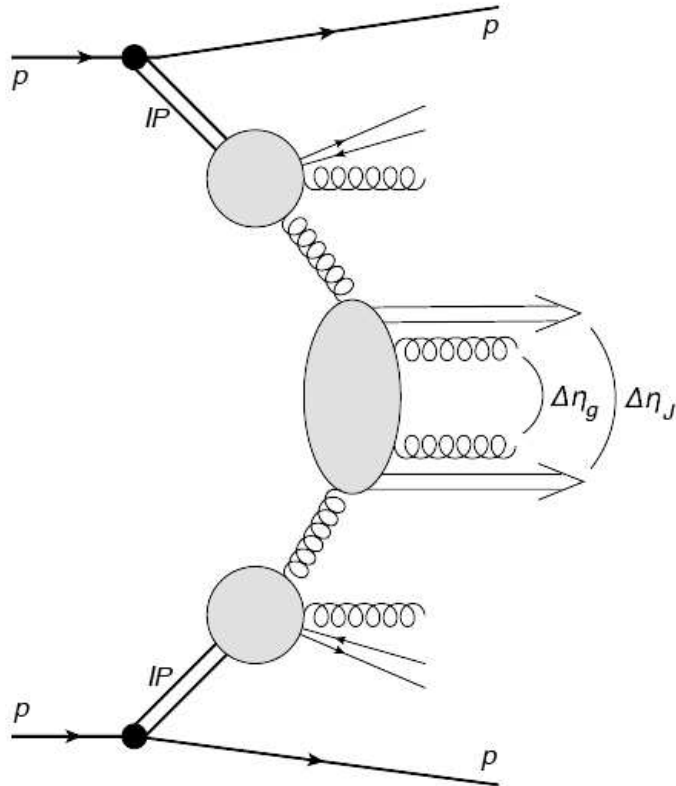
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### NLL impact factors

- Mix loop momenta (not factorized)
- Involve jet distributions with two final states
- Contain complicated non-analytic progress
- Work in progress by D. Colferai, F. Daganutti, T. Raben
- Will lead to an improved parametrisation to be implemented in HERWIG

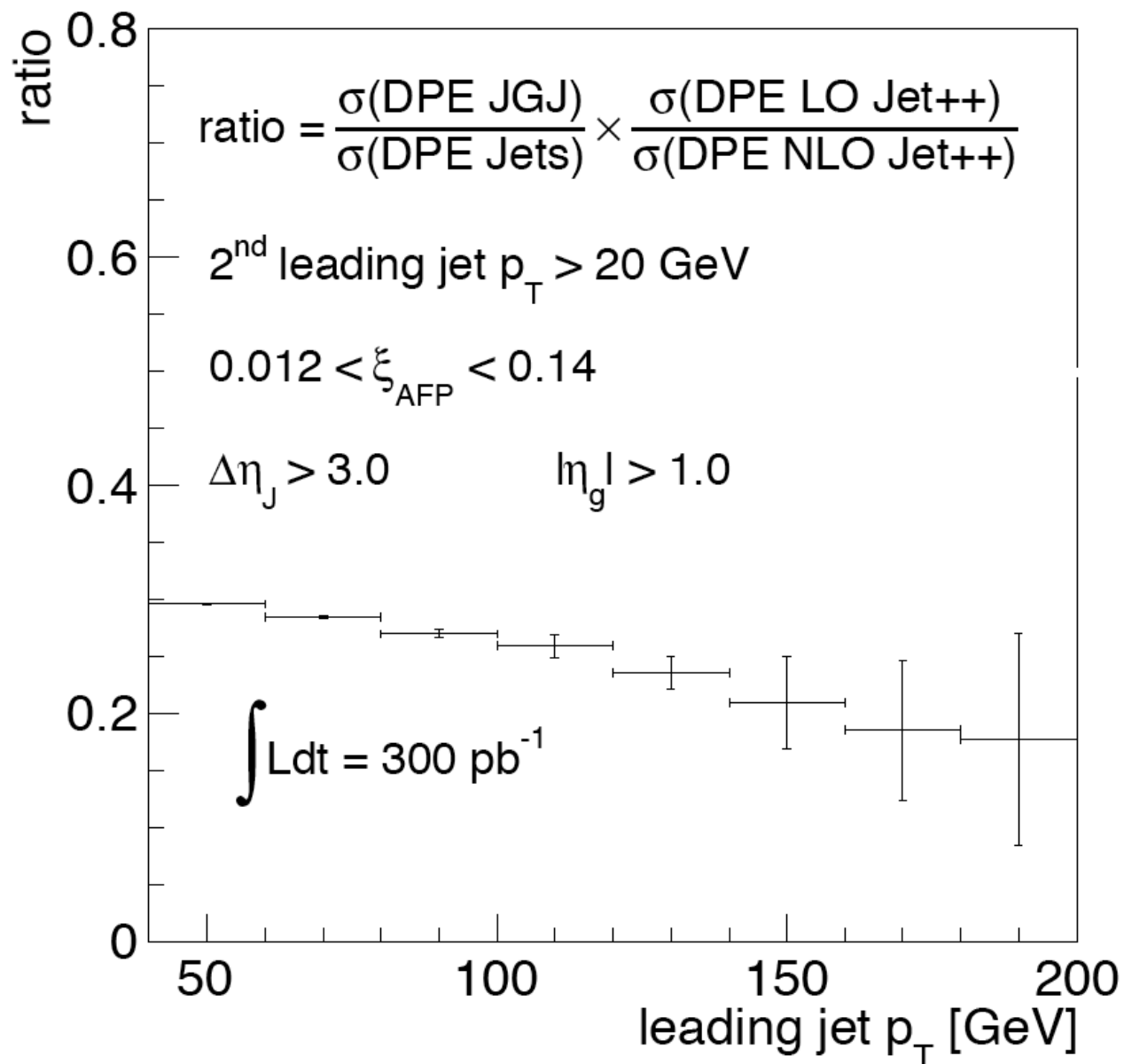
## Jet gap jet events in diffraction

- Study BFKL dynamics using jet gap jet events
- Jet gap jet events in DPE processes: clean process, allows to go to larger  $\Delta\eta$  between jets
- Reference: Gaps between jets in double-Pomeron-exchange processes at the LHC, C. Marquet, C. Royon, M. Trzebinski, R. Zlebcik, Phys. Rev. D87 (2013) 3, 034010



## Jet gap jet events in diffraction

- Measure the ratio of the jet gap jet to the dijet cross sections: sensitivity to BFKL dynamics
- As an example, study as a function of leading jet  $p_T$
- Advantage: ratio close to 10% (no survival probability), very clean events since jets not “polluted” by remnants)



## Conclusion

- Full implementation of BFKL NLL kernel for many jet processes at HERA, Tevatron and LHC
- Forward jets at HERA: DGLAP NLO fails to describe HERA data, good description of data using BFKL NLL formalism
- **Mueller Navelet jets**: Larger decorrelation expected for BFKL formalism, looking for less inclusive variables more sensitive to BFKL dynamics,, NLL BFKL with saturation in progress
- **Jet gap jets**:
  - NLL BFKL cross section implemented in HERWIG (Kernel)
  - Fair description of D0 and CDF data
  - Full NLL calculation in progress
  - Jet gap jet events in diffraction: clean tests of BFKL, modulo the survival probability (and its dependence on kinematics)

