



# FCC-ee Requirements on Beam Polarization and Energy Calibration

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## Beam Polarization can provide two main ingredients to Physics Measurements

### 1. Transverse beam polarization provides beam energy calibration

by resonant depolarization

-- low level of polarization is required ( $\sim 10\%$  is enough)

→ at W pair threshold comes naturally

→ at Z use of wigglers at beginning of fills

since polarization time is otherwise very long.

→ could be used also at ee → H(126) (depending on exact  $M_H$ !)

→ use 'single' non-colliding bunches

not available at beam energies higher than  $\sim 90$  GeV

but for H and top can use ee → Z  $\gamma$  or ee → ZZ, WW to calibrate  $E_{CM}$  at  $\sim 5$  MeV level.

-- must be done continuously during physics fills to avoid issues encountered at LEP

→ this is possible with single bunches and Compton polarimeter (commercial laser)

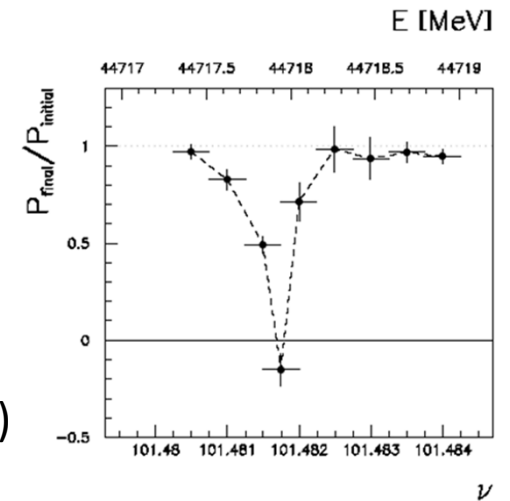
-- must be complemented by analysis of «average  $E_{beam}$ » to  $E_{CM}$  relationship

Aim: Z mass and width to  $\sim 0.1$  MeV (stat: 0.01 MeV)

W mass to  $\sim 0.5$  MeV (stat : 0.3MeV)

«EPOL» working group on polarization and beam energy:

J. Wenninger, E. Gianfelice, D. Barber, W. Hillert, A. Bogomyagkov, I. Kopp, N. Munchoi, M. Koratzinos, K. Oide, A.B., et al. see already [arXiv:1506.00933](https://arxiv.org/abs/1506.00933)





## Beam Polarization can provide two main ingredients to Physics Measurements

### 2. Longitudinal beam polarization provides chiral e+e- system

- High level of polarization is required ( $>40\%$ )
- Must compare with natural e+e- polarization due to chiral couplings of electrons (15%) or with final state polarization analysis for CC weak decays (100% polarized) (tau and top)
- Physics case for Z peak is very well studied and motivated:  
A\_LR, A\_FB^Pol(f) etc... (CERN Y.R. 88-06)  
**figure of merit is  $L.P^2$  --> must not lose more than a factor  $\sim 10$  in lumi.**  
self calibrating polarization measurement \* $\rightarrow$
- uses : enhance Higgs cross section (by 30%)  
top quark couplings? final state analysis does as well (Janot [arXiv:1503.01325](https://arxiv.org/abs/1503.01325))  
enhance signal, subtract/monitor backgrounds, for  $ee \rightarrow WW$  ,  $ee \rightarrow H$
- requires High polarization level and often both e- and e+ polarization  
 **$\rightarrow$  not interesting if loss of luminosity is too high**
- Obtaining high level of polarization in high luminosity collisions is delicate in top-up mode



**We have concluded that first priority is to achieve transverse polarization**

in a way that allows continuous beam calibration by resonant depolarization

- We believe that this is all possible
- the question of the residual systematic error requires further studies of the relationship between beam energy and center-of-mass energy

**The multi-million question is ‘do we want longitudinal polarization’?**

we will discuss this in the following.

# EXPERIMENTS ON BEAM-BEAM DEPOLARIZATION AT LEP

R. Assmann\*, A. Blondel\*, B. Dehning, A. Drees°, P. Grosse-Wiesmann, H. Grote, M. Placidi, R. Schmidt, F. Tecker†, J. Wenninger

PAC 1995

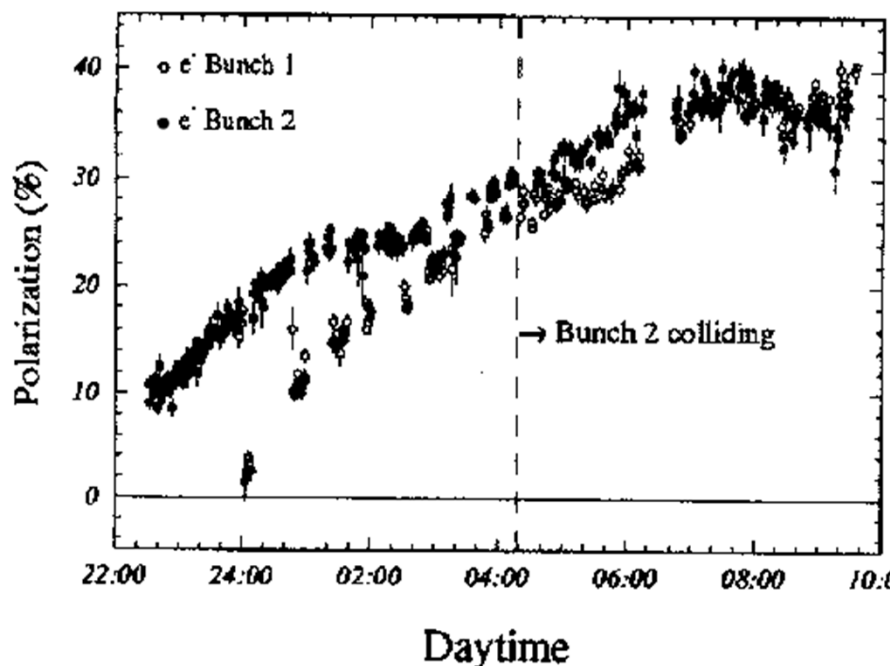


Figure. 3. Polarization level during third experiment

- With the beam colliding at one point, a polarization level of 40 % was achieved. The polarization level was about the same for one colliding and one non colliding bunch.
- It was observed that the polarization level depends critically on the synchrotron tune : when  $Q_s$  was changed by 0.005, the polarization strongly decreased.

experiment performed at an energy of 44.71 GeV the polarization level was 40 % with a linear beam-beam tune shift of about 0.04/IP. This indicates, that the beam-beam depolarization does not scale with the linear beam-beam tune shift at one crossing point. Other parameters as spin tune and synchrotron tune are also of importance.

LEP:

This was only tried 3 times!

Best result:  $P = 40\%$  ,  $\xi_y^* = 0.04$  , one IP

FCC-ee

Assuming 2 IP and  $\xi_y^* = 0.01 \rightarrow$

**reduce luminosity,  $10^{10} Z @ P \sim 30\%$**



## Reduction due to continuous injection

The colliding bunches will lose intensity continuously due to collisions.

In FCC-ee with 4 IPs,  $L = 28 \cdot 10^{34}/\text{cm}^2/\text{s}$  beam lifetime is 213 minutes

In FCC-ee with 2 IPs,  $L = 220 \cdot 10^{34}/\text{cm}^2/\text{s}$  beam life time is 55minutes

Luminosity scales inversely to beam life time.

The injected  $e^+$  and  $e^-$  are not polarized  $\rightarrow$  asymptotic polarization is reduced.

Assume here that machine has been well corrected and beams (no collisions, no injection) can be polarized to nearly maximum.

*(Eliana Gianfelice in Rome talk)*

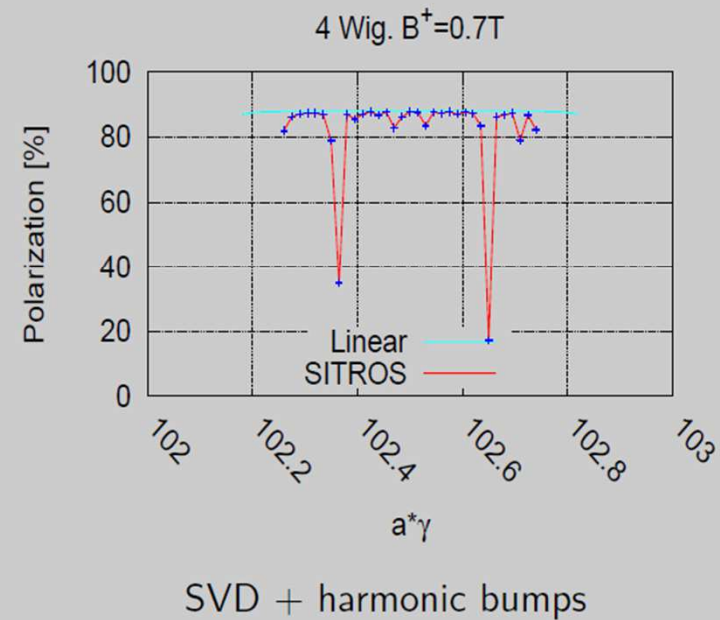
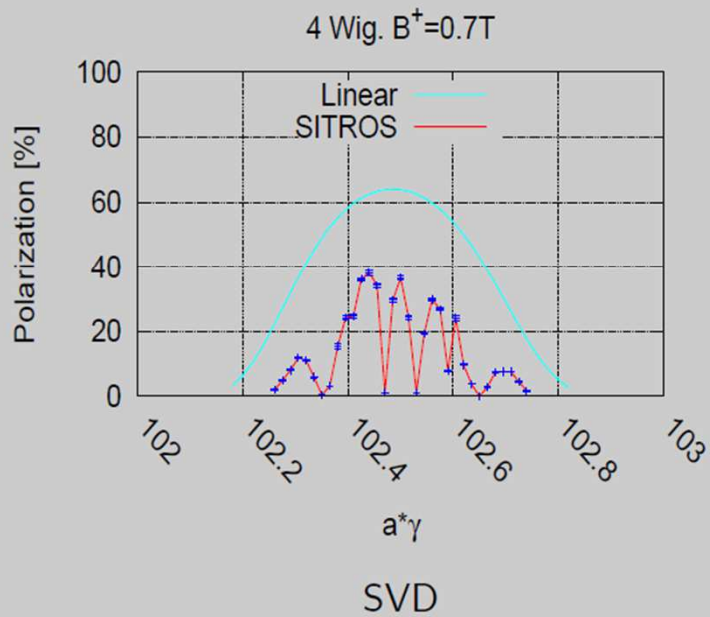
- 45 GeV
  - limit  $\Delta E = 50$  MeV (extrapolating from LEP)
  - 4 wigglers with  $B^+ = 0.7$  T
  - 10% polarization in 2.9 h for energy calibration

(polarization time is 26h)



- $\delta_y^Q = 200 \mu\text{m}$
- BPMs errors
  - $\delta_y^M = 200 \mu\text{m}$
  - 10% calibration errors

	$y_{rms}$ (mm)	$\delta\hat{n}_{0,rms}$ (mrad)
	8.	26.4
SVD	0.8	3.9
+Harmonic bumps	0.9	2.0



Mike Koratzinos and AB have simulated the simultaneous effect of

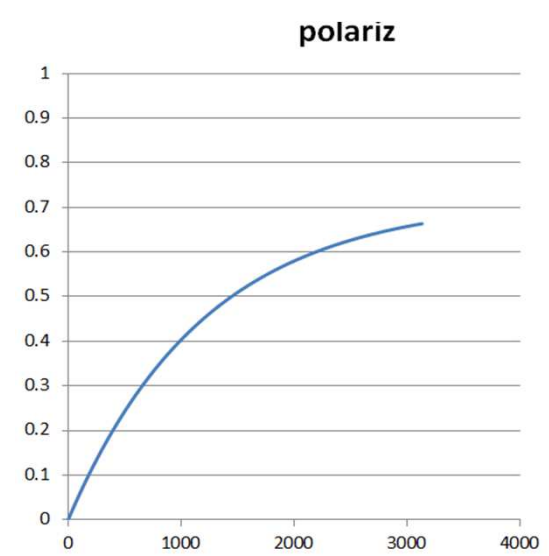
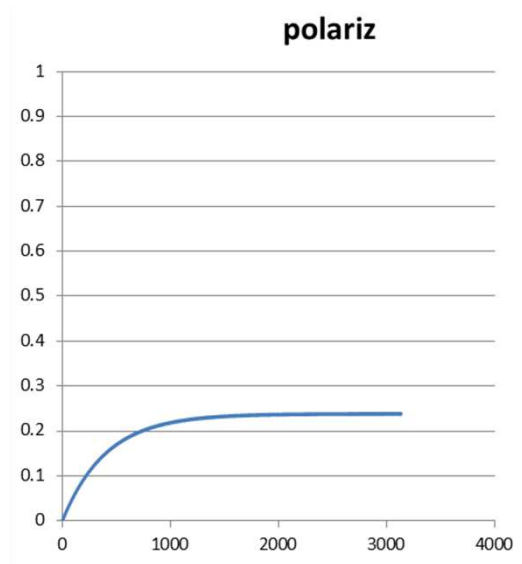
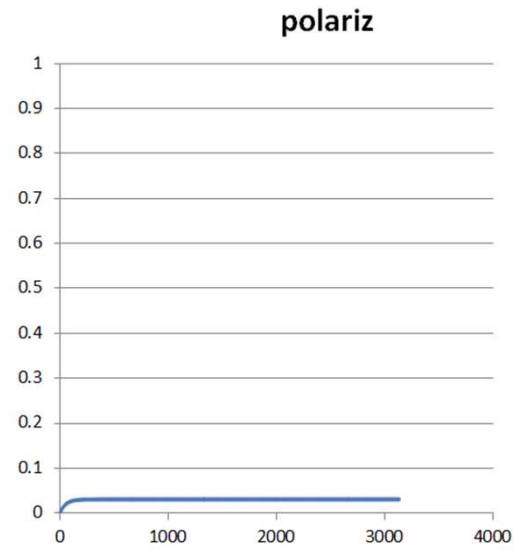
- natural polarization
- beam consumption by e+e- interactions
- replenishment with unpolarized beams

assuming **optimistically** a maximal 90% asymptotic polarization

Running at full luminosity  
 $P_{\text{max}}=0.03!$   $P_{\text{eff}}=0.03$

Running at 10% Lumi  
 $P_{\text{max}}=0.24$ ,  $P_{\text{eff}}=0.21$

Running at 1% Lumi  
 $P_{\text{max}}=0.66$ ,  $P_{\text{eff}}=0.5$





$\Delta A_{LR}$  scales as  $1/\sqrt{(P^2L)}$



Lumi loss factor	L.10 <sup>34</sup>	Figure of merit: sum(P <sup>2</sup> L)	effpol	Pmax
1	220	0.195	0.03	0.03
2	110	0.367	0.059	0.06
4	55	0.627	0.1078	0.11
6	37	0.805	0.149	0.16
8	27.5	0.924	0.184	0.2
10	22	1.003	0.214	0.24
12	18	1.053	0.24	0.27
15	14.7	1.09	0.27	0.32
<b>18</b>	<b>12.2</b>	<b>1.101</b>	<b>0.3</b>	<b>0.35</b>
22	10	1.088	0.33	0.4
26	8.5	1.059	0.354	0.43
30	7.3	1.023	0.37	0.46
40	5.5	0.92	0.41	0.52

Since one can see that there is an optimum around a reduction of luminosity by a factor 18.

This is still a luminosity of  $>10^{35}$  per IP... and the effective polarization is 30%. This is equivalent to a 100% polarization expt with luminosity reduced by 180.



# Longitudinal polarization at FCC-Z?

Main interest: measure EW couplings at the Z peak most of which provide measurements of  $\sin^2\theta_w^{lept} = e^2/g^2 (m_z)$

(-- not to be confused with --  $\sin^2\theta_w = 1 - m_w^2/m_z^2$ )

Useful references from the past:

«polarization at LEP» CERN Yellow Report 88-02

Precision Electroweak Measurements on the Z Resonance

Phys.Rept.427:257-454,2006

<http://arxiv.org/abs/hep-ex/0509008v3>

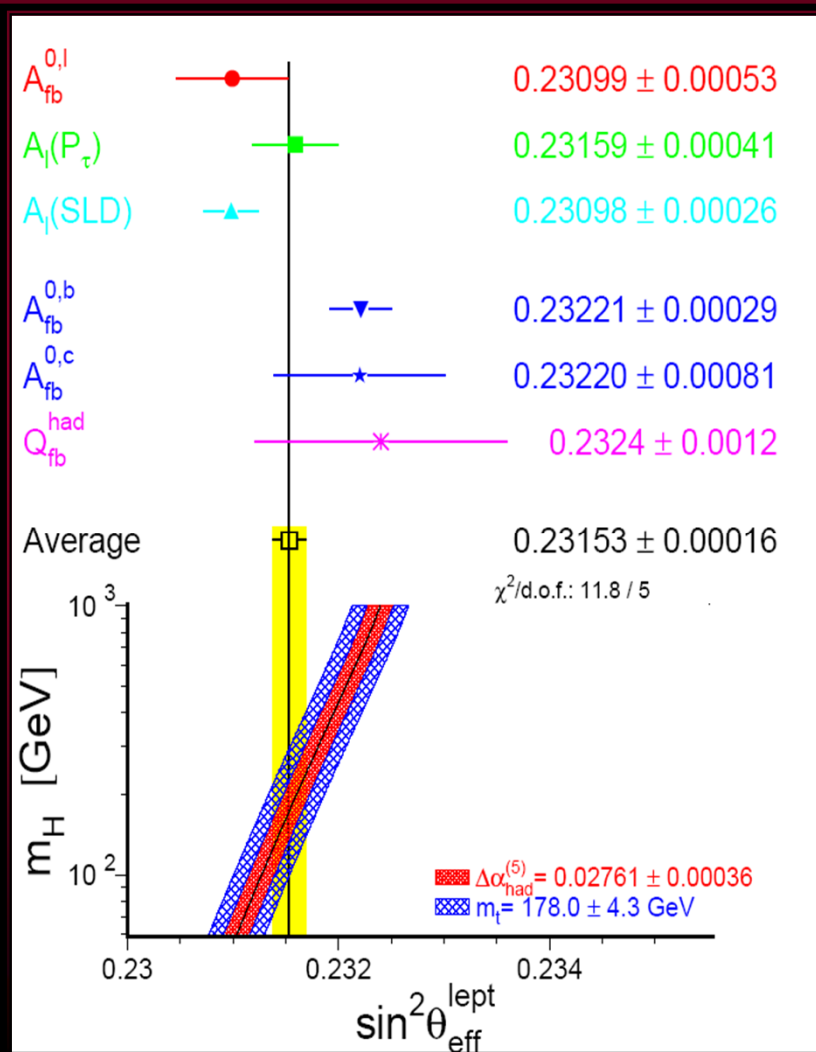
GigaZ @ ILC by K. Moenig

# Measuring $\sin^2\theta_W^{\text{eff}} (m_Z)$

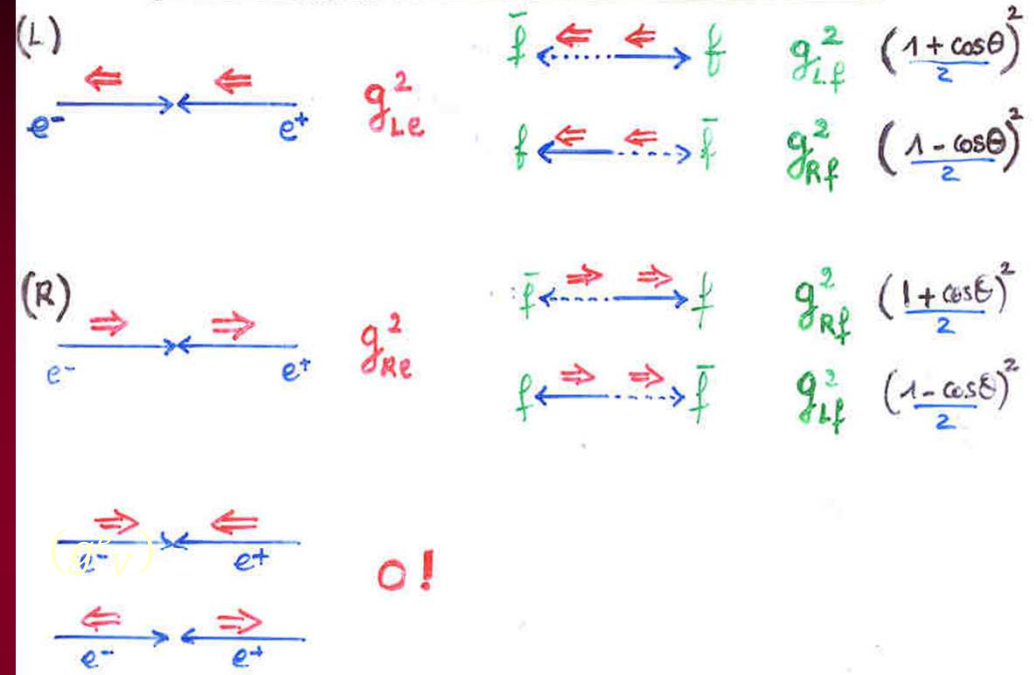
$$\sin^2\theta_W^{\text{eff}} \equiv \frac{1}{4} (1 - g_V/g_A)$$

$$g_V = g_L + g_R$$

$$g_A = g_L - g_R$$



## Helicity effects in $e^+e^- \rightarrow f\bar{f}$



Red BEAM  $\Rightarrow$

$$A_{LR} = \frac{\sigma_L^{\text{tot}} - \sigma_R^{\text{tot}}}{\sigma_L^{\text{tot}} + \sigma_R^{\text{tot}}} = \frac{g_{Le}^2 - g_{Re}^2}{g_{Le}^2 + g_{Re}^2} \equiv A_e = \frac{2g_V g_A}{g_V^2 + g_A^2}$$

$$A_{FB}^{\text{pol}f} = \frac{\sigma_L^{Ff} - \sigma_L^{Bf} - (\sigma_R^{Ff} - \sigma_R^{Bf})}{\sigma_L^{Ff} + \sigma_L^{Bf} + \sigma_R^{Ff} + \sigma_R^{Bf}} = \frac{3}{4} A_e A_f$$

no Pol available:

$$A_{FB} = \frac{\sigma_U^{Ff} - \sigma_U^{Bf}}{\sigma_U^{Ff} + \sigma_U^{Bf}} = \frac{3}{4} A_e A_f$$

Pol<sup>n</sup> analyses:

$$\langle P_f \rangle = \frac{\sigma_U^R - \sigma_U^L}{\sigma_U^R + \sigma_U^L} = -A_f$$

$$A_{FB}^{\text{pol}} = \frac{\sigma_U^{RF} - \sigma_U^{LF} - (\sigma_U^{RB} - \sigma_U^{LB})}{\sigma_U^{RF} + \sigma_U^{LF} + \sigma_U^{RB} + \sigma_U^{LB}} = -\frac{3}{4} A_e$$

$$\Delta\rho: \Gamma_l = (1 + \Delta\rho) \frac{G_F m_Z^3}{24\pi\sqrt{2}} \left( 1 + \left( \frac{g_{Vl}}{g_{Al}} \right)^2 \right) \left( 1 + \frac{3}{4} \frac{\alpha}{\pi} \right)$$

$$\varepsilon_3 \sin^2\theta_w^{\text{eff}} \cos^2\theta_w^{\text{eff}} = \frac{\pi\alpha(M_Z^2)}{\sqrt{2} G_F m_Z^2} \frac{1}{1 + \Delta\rho} \frac{1}{1 - \frac{\varepsilon_3}{\cos^2\theta_w}}$$

$$\delta_{vb} \Gamma_b = (1 + \delta_{vb}) \Gamma_d \left( 1 - \frac{\text{mass corrections}}{\alpha m_b^2/M_Z^2} \right)$$

$$\varepsilon_2 M_W^2 = \frac{\pi\alpha(M_Z^2)}{\sqrt{2} G_F \sin^2\theta_w^{\text{eff}}} \cdot \frac{1}{(1 - \varepsilon_3 + \varepsilon_2)}$$

$\sin^2\theta_w^{\text{eff}}$  is defined from

$$\sin^2\theta_w^{\text{eff}} = \frac{1}{4} \left( 1 - \frac{g_{Vl}}{g_{Al}} \right) = \sin^2\theta_w^{\text{opt}}$$

obtained from asymmetries at the Z.

also

$\Delta\alpha$

$$M_W^2 = \frac{\pi\alpha}{\sqrt{2} G_F} \cdot \frac{1}{\left( 1 - \frac{M_W^2}{M_Z^2} \right)} \frac{1}{(1 - \Delta\alpha)}$$

$$\Delta\alpha = \Delta\alpha - \frac{\cos^2\theta_w}{\sin^2\theta_w} \Delta\rho + 2 \frac{G^2\theta_w}{\sin^2\theta_w} \varepsilon_3 + \frac{C^2 - S^2}{S^2} \varepsilon_2$$

# EWRCs

relations to the well measured

$$G_F m_Z \propto_{\text{QED}}$$

at first order:

$$\Delta\rho = \alpha/\pi (m_{\text{top}}/m_Z)^2 - \alpha/4\pi \log(m_h/m_Z)^2$$

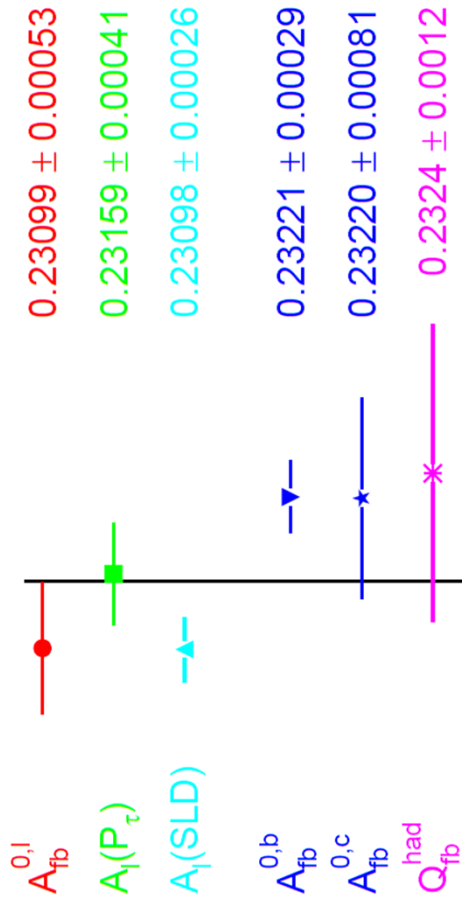
$$\varepsilon_3 = \cos^2\theta_w \alpha/9\pi \log(m_h/m_Z)^2$$

$$\delta_{vb} = 20/13 \alpha/\pi (m_{\text{top}}/m_Z)^2$$

complete formulae at 2d order including strong corrections are available in fitting codes

e.g. ZFITTER, GFITTER





## A Sample of Essential Quantities:

<b>X</b>	<b>Physics</b>	<b>Present precision</b>		<b>TLEP stat Syst Precision</b>	<b>TLEP key</b>	<b>Challenge</b>
<b>M<sub>Z</sub></b> MeV/c <sup>2</sup>	<b>Input</b>	91187.5 <b>±2.1</b>	Z Line shape scan	<b>0.005 MeV</b> <b>&lt;±0.1 MeV</b>	E_cal	QED corrections
<b>Γ<sub>Z</sub></b> MeV/c <sup>2</sup>	<b>Δρ (T)</b> <b>(no Δα!)</b>	2495.2 <b>±2.3</b>	Z Line shape scan	<b>0.008 MeV</b> <b>&lt;±0.1 MeV</b>	E_cal	QED corrections
<b>R<sub>ℓ</sub></b>	<b>α<sub>s</sub>, δ<sub>b</sub></b>	20.767 <b>± 0.025</b>	Z Peak	<b>0.0001</b> <b>± 0.002</b> <b>- 0.0002</b>	Statistics	QED corrections
<b>N<sub>ν</sub></b>	<b>Unitarity of PMNS, sterile ν's</b>	2.984 <b>±0.008</b>	Z Peak Z+γ(161 GeV)	<b>0.00008</b> <b>±0.004</b> <b>0.001</b>	->lumi meast Statistics	<b>QED corrections to Bhabha scat.</b>
<b>R<sub>b</sub></b>	<b>δ<sub>b</sub></b>	0.21629 <b>±0.00066</b>	Z Peak	<b>0.000003</b> <b>±0.000020 - 60</b>	Statistics, small IP	Hemisphere correlations
<b>A<sub>LR</sub></b>	<b>Δρ, ε<sub>3</sub>, Δα (T, S)</b>	0.1514 <b>±0.0022</b>	Z peak, polarized	<b>±0.000015</b>	4 bunch scheme	Design experiment
<b>M<sub>W</sub></b> MeV/c <sup>2</sup>	<b>Δρ, ε<sub>3</sub>, ε<sub>2</sub>, Δα (T, S, U)</b>	80385 <b>± 15</b>	Threshold (161 GeV)	<b>0.3 MeV</b> <b>&lt;0.5 MeV</b>	E_cal & Statistics	QED corections
<b>m<sub>top</sub></b> MeV/c <sup>2</sup>	<b>Input</b>	173200 <b>± 900</b>	Threshold scan	<b>10 MeV</b>	E_cal & Statistics	Theory limit at 100 MeV?

# Extracting physics from $\sin^2\theta_W^{lept}$

## 1. Direct comparison with $m_Z$

$$\sin^2\theta_W^{eff} \cos^2\theta_W^{eff} = \frac{\pi\alpha(M_Z^2)}{\sqrt{2} GF M_Z^2} \frac{1}{1+\Delta\rho} \frac{1}{1-\frac{\epsilon_3}{\cos^2\theta_W}}$$

Uncertainties in  $m_{top}$ ,  $\Delta\alpha(m_Z)$ ,  $m_H$ , etc....

$$\Delta\sin^2\theta_W^{lept} \sim \Delta\alpha(m_Z)/3 = 10^{-5} \text{ if we can reduce } \Delta\alpha(m_Z) \text{ (see P. Janot)}$$

## 2. Comparison with $m_W/m_Z$

Compare above formula with similar one:

$$\sin^2\theta_W \cos^2\theta_W = \frac{\pi\alpha(M_Z^2)}{\sqrt{2} GF M_Z^2} \frac{1}{1 - \left( -\frac{\cos^2\theta_W}{\sin^2\theta_W} \Delta\rho + 2\frac{G_F^2\theta_W}{\sin^2\theta_W} \epsilon_3 + \frac{C^2-S^2}{S^2} \epsilon_2 \right)}$$

Where it can be seen that  $\Delta\alpha(m_Z)$  cancels in the relation.

The limiting error is the error on  $m_W$ .

For  $\Delta m_W = 0.5 \text{ MeV}$  this corresponds to  $\Delta\sin^2\theta_W^{lept} = 10^{-5}$

## Assume for now ONE experiment at ECM=91.2

Luminosity «baseline» with  $\beta^*=1\text{mm}$  :  $2.1 \cdot 10^{36}/\text{cm}^2/\text{s} = 2 \text{ pb}^{-1}/\text{s}$ ,  
Sigma\_had =  $31 \cdot 10^{-33}\text{cm}^2 \rightarrow 6.5 \cdot 10^{11} \text{ qq events}/10^7 \text{ year/exp.}$

Consider 3 years of  $10^7 \text{ s}$

$2 \cdot 10^{12} \text{ Z} \rightarrow \bar{q}q$  events (typical exp at LEP was  $4 \cdot 10^6$ )

$4 \cdot 10^{11} \text{ Z} \rightarrow \bar{b}b$

$10^{11} \text{ Z} \rightarrow \mu\mu, \tau\tau$  each



**Will consider today the contribution of the Center-of-mass energy systematic errors**

**Today: step I, compare**

ILC measurement of  $A_{LR}$  with  $10^9 Z$  and  $P_{e^-} = 80\%$ ,  $P_{e^+} = 30\%$

FCC-ee measurement of  $A_{FB}^{\mu\mu}$  and  $A_{FB}^{Pol}(\tau)$  with  $2 \cdot 10^{12} Z$

## Comparing $A_{LR}$ (P) and $A_{FB}(\mu\mu)$

Both measure the weak mixing angle as **defined** by the relation  $A_\ell = \frac{(g^e_L)^2 - (g^e_R)^2}{(g^e_L)^2 + (g^e_R)^2}$   
 with  $(g^e_L) = \frac{1}{2} - \sin^2\theta_{W}^{lept}$  and  $(g^e_R) = -\sin^2\theta_{W}^{lept}$   $A_\ell \approx 8(1/4 - \sin^2\theta_{W}^{lept})$

$$A_{LR} = A_e$$

$$A_{FB}^{\mu\mu} = \frac{3}{4} A_e A_\mu = \frac{3}{4} A_\ell^2$$

- $A_{FB}^{\mu\mu}$  is measured using muon pairs (5% of visible Z decays) and unpolarized beams
- $A_{LR}$  is measured using all statistics of visible Z decays with beams of alternating longitudinal polarization both with very small experimental systematics

-- **parametric sensitivity**  $\frac{dA_{FB}^{\mu\mu}}{d\sin^2\theta_{W}^{lept}} = 1.73$  vs  $\frac{dA_{LR}}{d\sin^2\theta_{W}^{lept}} = 7.9$

- **sensitivity to center-of-mass energy** (w.r.t.  $m_Z$ ) is larger for  $A_{FB}^{\mu\mu}$

$$\frac{\partial A_{FB}^{\mu\mu}}{\partial \sqrt{s}} = 0.09/\text{GeV} \text{ vs } \frac{\partial A_{LR}}{\partial \sqrt{s}} = 0.019/\text{GeV}$$

“an 80 MeV uncertainty in  $E_{cm}$  corresponds to a 1% error on  $A_{LR}$ ” (relative error)

But of course  $A_{FB}^{\mu\mu}$  benefits from much larger statistics and  $E_{cm}$  precision of circular collider

## Measurement of $A_{LR}$

electron bunches	1←	2	3	4←
positron bunches	1	2⇒	3	4⇒
cross sections	$\sigma_1$	$\sigma_2$	$\sigma_3$	$\sigma_4$
event numbers	$N_1$	$N_2$	$N_3$	$N_4$

$$\sigma_1 = \sigma_u (1 - P_e^- \Lambda_{LR})$$

$$\sigma_2 = \sigma_u (1 + P_e^+ \Lambda_{LR})$$

$$\sigma_3 = \sigma_u$$

$$\sigma_4 = \sigma_u [1 - P_e^+ P_e^- + (P_e^+ - P_e^-) \Lambda_{LR}]$$

**Verifies polarimeter with experimentally measured cross-section ratios**

statistics

$$\Delta A_{LR} = 0.0025 \text{ with about } 10^6 \text{ } Z^0 \text{ events,}$$

$$\Delta A_{LR} = 0.000045 \text{ with } 5 \cdot 10^{10} \text{ } Z \text{ and 30\% polarization in collisions.}$$

$$\Delta \sin^2 \theta_w^{\text{eff}} (\text{stat}) = O(2 \cdot 10^{-6})$$

## Will consider two sources of errors

-- statistics

-- uncertainty on center-of-mass energy (relative to the Z mass)

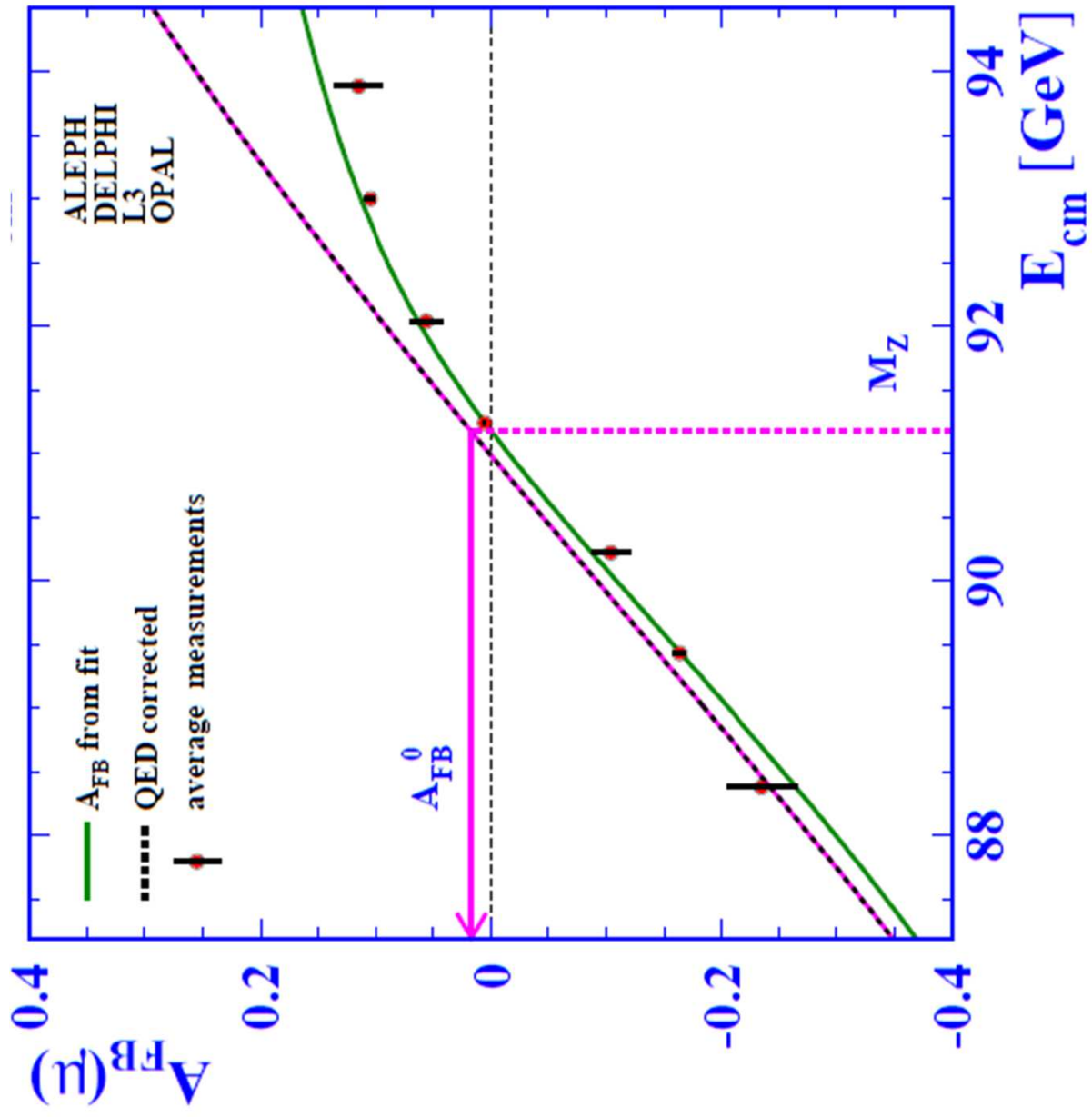
main inputs taken from

[arXiv:hep-ex/0509008v3](https://arxiv.org/abs/hep-ex/0509008v3) precision measurements on the Z resonance

Phys. Rep. 427:257-454,2006

there are other uncertainties but they are very small for  $A_{FB}$

This is a lower limit estimate for  $A_{LR}$  ; the systematics related to knowledge of the beam polarization (80% for e-, 30% for e+) should also be taken into account



	$A_{FB}^{\mu\mu}$ @ FCC-ee		$A_{LR}$ @ ILC	$A_{LR}$ @ FCC-ee
visible Z decays	$10^{12}$	visible Z decays	$10^9$	$5 \cdot 10^{10}$
muon pairs	$10^{11}$	beam polarization	90%	30%
$\Delta A_{FB}^{\mu\mu}$ (stat)	$3 \cdot 10^{-6}$	$\Delta A_{LR}$ (stat)	$4.2 \cdot 10^{-5}$	$4.5 \cdot 10^{-5}$
$\Delta E_{cm}$ (MeV)	0.1		2.2	?
$\Delta A_{FB}^{\mu\mu}$ ( $E_{CM}$ )	$9.2 \cdot 10^{-6}$	$\Delta A_{LR}$ ( $E_{CM}$ )	$4.1 \cdot 10^{-5}$	
$\Delta A_{FB}^{\mu\mu}$	$1.0 \cdot 10^{-5}$	$\Delta A_{LR}$	$5.9 \cdot 10^{-5}$	
$\Delta \sin^2 \theta_{W}^{lept}$	$5.9 \cdot 10^{-6}$		$7.5 \cdot 10^{-6}$	$6 \cdot 10^{-6} + ?$

All exceeds the theoretical precision from  $\Delta\alpha(m_Z)$  ( $3 \cdot 10^{-5}$ ) or the comparison with  $m_W$  (500keV)

**But this precision on  $\Delta \sin^2 \theta_{W}^{lept}$  can only be exploited at FCC-ee!**

The forward backward tau polarization asymmetry is very clean.  
 Dependence on  $E_{CM}$  same as  $A_{LR}$  negl.  
 At FCC-ee

ALEPH data  $160 \text{ pb}^{-1}$  (80 s @ FCC-ee !)

Already syst. level of  $6 \cdot 10^{-5}$  on  $\sin^2\theta_W^{\text{eff}}$   
 much improvement possible  
 by using dedicated selection  
 e.g.  $\tau \rightarrow \pi \nu$  to avoid had. model

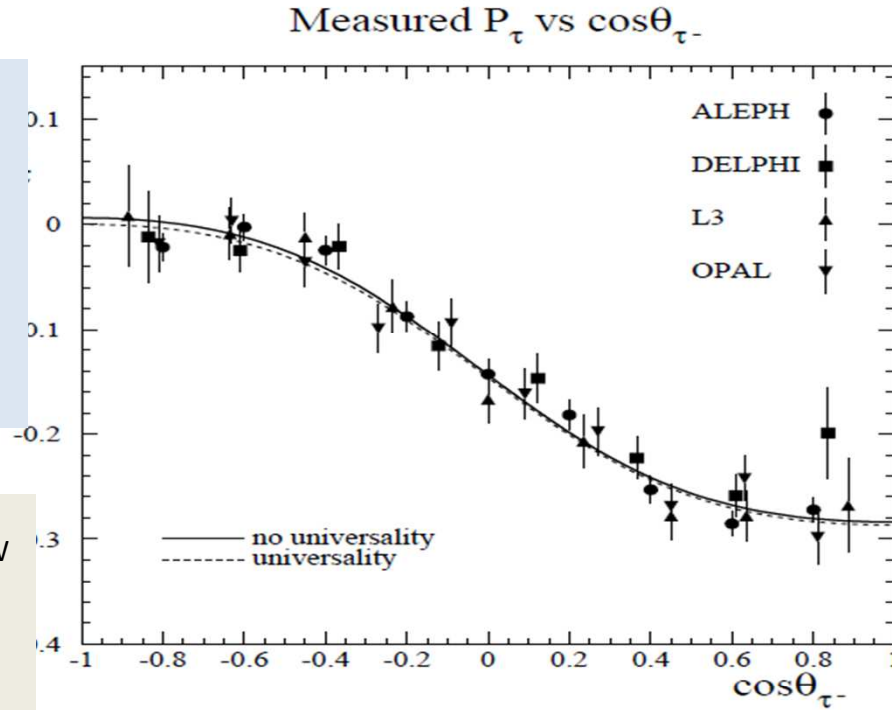


Figure 4.7: The values of  $\mathcal{P}_\tau$  as a function of  $\cos\theta_{\tau^-}$  as measured by each of the LEP experiments. Only the statistical errors are shown. The values are not corrected for radiation, interference or pure photon exchange. The solid curve overlays Equation 4.2 for the LEP values of  $\mathcal{A}_\tau$  and  $\mathcal{A}_e$ . The dashed curve overlays Equation 4.2 under the assumption of lepton universality for the LEP value of  $\mathcal{A}_e$ .

	ALEPH		DELPHI		L3		OPAL	
	$\delta\mathcal{A}_\tau$	$\delta\mathcal{A}_e$	$\delta\mathcal{A}_\tau$	$\delta\mathcal{A}_e$	$\delta\mathcal{A}_\tau$	$\delta\mathcal{A}_e$	$\delta\mathcal{A}_\tau$	$\delta\mathcal{A}_e$
ZFITTER	0.0002	0.0002	0.0002	0.0002	0.0002	0.0002	0.0002	0.0002
$\tau$ branching fractions	0.0003	0.0000	0.0016	0.0000	0.0007	0.0012	0.0011	0.0003
two-photon bg	0.0000	0.0000	0.0005	0.0000	0.0007	0.0000	0.0000	0.0000
had. decay model	0.0012	0.0008	0.0010	0.0000	0.0010	0.0001	0.0025	0.0005

Table 4.2: The magnitude of the major common systematic errors on  $\mathcal{A}_\tau$  and  $\mathcal{A}_e$  by category for each of the LEP experiments.

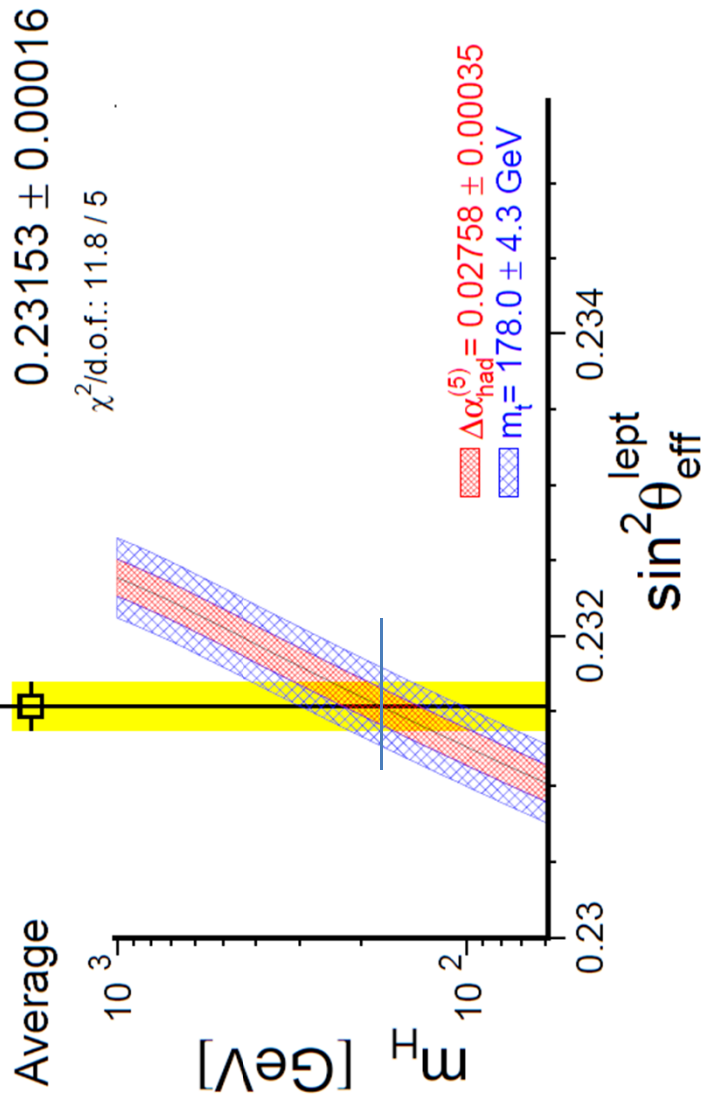
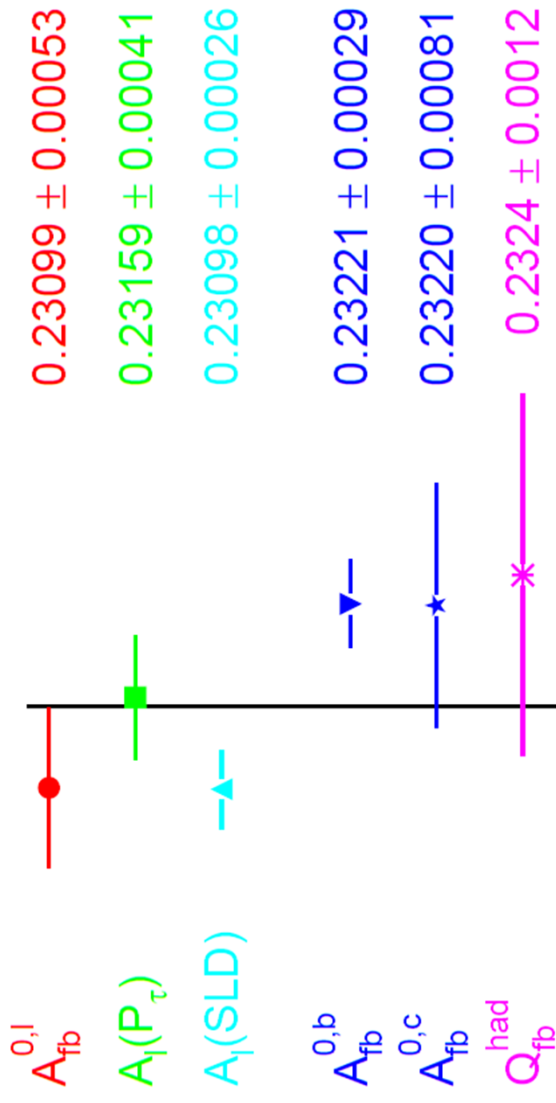
## Concluding remarks

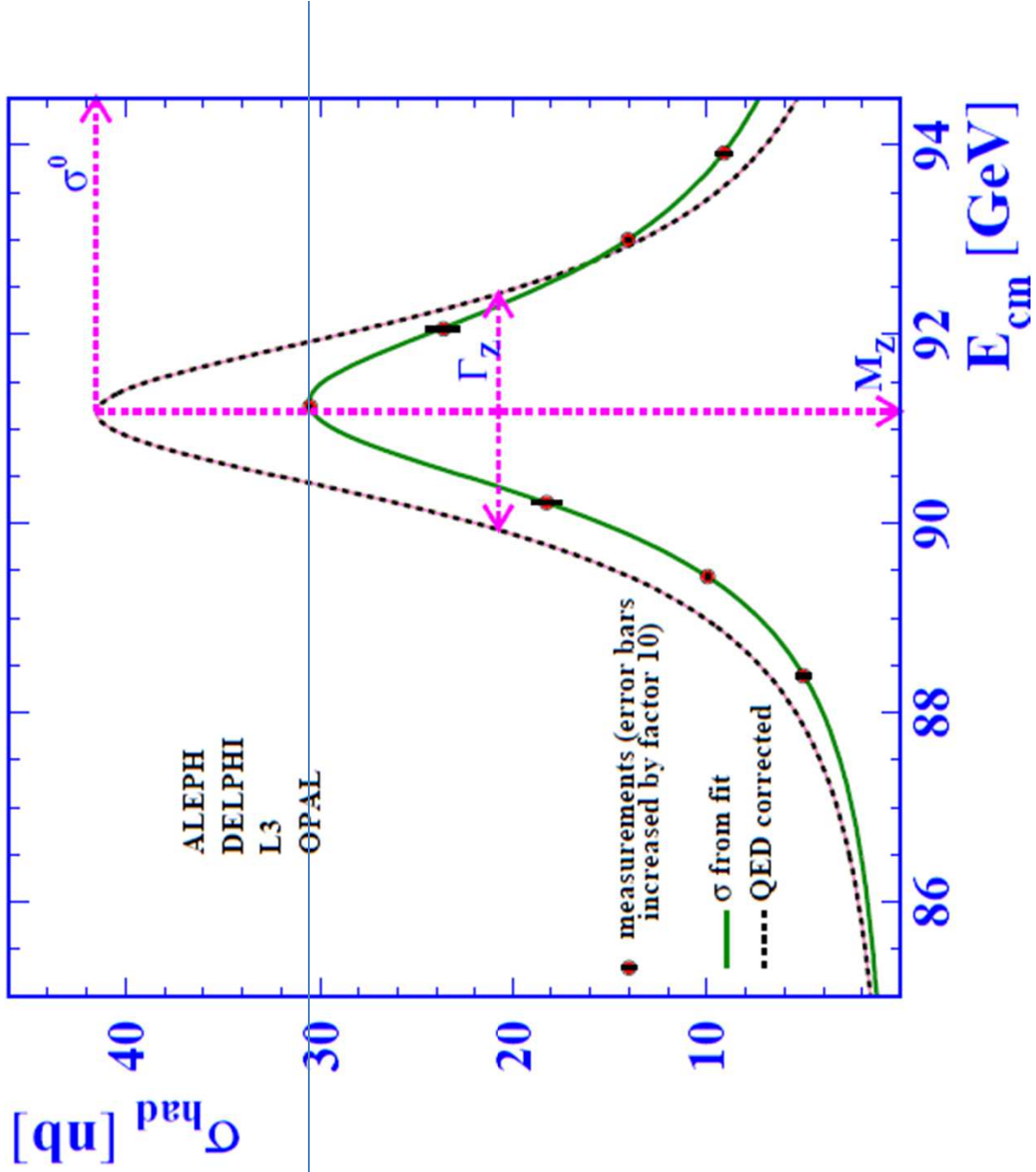
1. There are very strong arguments for precision energy calibration with transverse polarization at the Z peak.
2. Given the likely loss in luminosity, and the intrinsic uncertainties in the extraction of the weak couplings, the case for longitudinal polarization is limited.

→ **We have concluded that first priority is to achieve transverse polarization** in a way that allows continuous beam calibration by resonant depolarization

- We believe that this is all possible with a very high precision, both at the Z and the W. calibration at higher energies can be made from the data themselves at sufficient level.
- the question of the residual systematic error requires further studies of the relationship between beam energy and center-of-mass energy with the aim of achieving a precision of  $O(100 \text{ keV})$  on  $E_{\text{CM}}$







Going through the observables

the weak mixing angle as **defined** by the relation

$$A_\ell = \frac{2g_V^e g_A^e}{(g_V^e)^2 + (g_A^e)^2} = \frac{(g_L^e)^2 - (g_R^e)^2}{(g_L^e)^2 + (g_R^e)^2}$$

with  $(g_L^e) = \frac{1}{2} - \sin^2 \theta_W^{\text{lept}}$  and  $(g_R^e) = -\sin^2 \theta_W^{\text{lept}}$

$A_\ell \approx 8(1/4 - \sin^2 \theta_W^{\text{lept}})$  very sensitive to  $\sin^2 \theta_W^{\text{lept}}$  !

$A_{LR} = A_e$  measured from  $(\sigma_{\text{vis,L}} - \sigma_{\text{vis,R}}) / (\sigma_{\text{vis,L}} + \sigma_{\text{vis,R}})$

(total visible cross-section had +  $\mu\mu$  +  $\tau\tau$  (35 nb) for 100% Left Polarization

Or

$$A_{\text{FB}}^{\mu\mu} = \frac{3}{4} A_e A_\mu = \frac{3}{4} A_\ell^2$$

$$\mathcal{G}_{Vf} = \sqrt{\mathcal{R}_f} (T_3^f - 2Q_f \mathcal{K}_f \sin^2 \theta_W)$$

$$\mathcal{G}_{Af} = \sqrt{\mathcal{R}_f} T_3^f.$$

$$A_{\text{FB}}^{0,f} = \frac{3}{4} A_e A_f$$

$$A_{\text{LR}}^0 = A_e$$

$$A_{\text{LRFB}}^0 = \frac{3}{4} A_f$$

$$\langle \mathcal{P}_\tau^0 \rangle = -A_\tau$$

$$A_{\text{FB}}^{\text{pol},0} = -\frac{3}{4} A_e.$$

$$A_{\text{FB}} = \frac{\sigma_F - \sigma_B}{\sigma_F + \sigma_B}$$

$$A_{\text{LR}} = \frac{\sigma_L - \sigma_R}{\sigma_L + \sigma_R} \frac{1}{\langle |\mathcal{P}_e| \rangle}$$

$$A_{\text{LRFB}} = \frac{(\sigma_F - \sigma_B)_L - (\sigma_F - \sigma_B)_R}{(\sigma_F + \sigma_B)_L + (\sigma_F + \sigma_B)_R} \frac{1}{\langle |\mathcal{P}_e| \rangle}.$$