Production and evolution of axion dark matter in the early universe

Ken'ichi Saikawa (DESY)

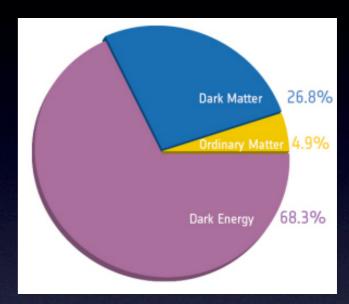


Based on

- T. Hiramatsu, M. Kawasaki, KS, T. Sekiguchi, PRD85, 105020 (2012) [1202.5851]
- T. Hiramatsu, M. Kawasaki, KS, T. Sekiguchi, JCAP01, 001 (2013) [1207.3166]
- M. Kawasaki, KS, T. Sekiguchi, PRD91, 065014 (2015) [1412.0789]
- A. Ringwald, KS, PRD93, 085031 (2016) [1512.06436]

Dark matter

- Recent astrophysical observations imply that about 27% of the total energy of the universe is occupied by unknown matter.
 - Stable in cosmological timescales
 - Collisionless ("invisible")
 - "Cold" (velocity dispersion is sufficiently small at the beginning of structure formation)



Credit: ESA and the Planck Collaboration

- Physics beyond the Standard Model
 - A well motivated candidate: axion and axion-like particles

Peccei-Quinn extension of the standard model

Solution to the strong CP problem

Strong CP problem and axion

- Strong CP problem
 - Quantum chromodynamics (QCD) allows a CP violating term:

$$\mathcal{L} \supset \frac{\alpha_s}{8\pi} \theta G^a_{\mu\nu} \tilde{G}^{a\mu\nu}$$

Physical observable: $\bar{\theta} = \theta + \arg \, \det M_q$

Non-observation of neutron electric dipole moment implies

$$|\bar{\theta}| < \mathcal{O}(10^{-11})$$
 "Why it is so small?"

- Peccei-Quinn (PQ) mechanism
 - Take $\bar{\theta}$ as a dynamical variable that explains its smallness, i.e. $\bar{\theta} \to \bar{\theta}_{\rm eff}(x) = a(x)/F_a$
 - Predicts the existence of light particle a(x) = axion .

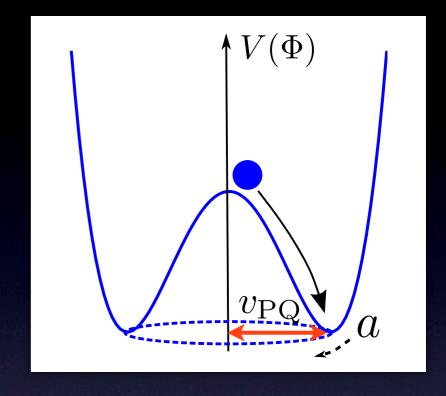
Axion as a Nambu-Goldstone boson

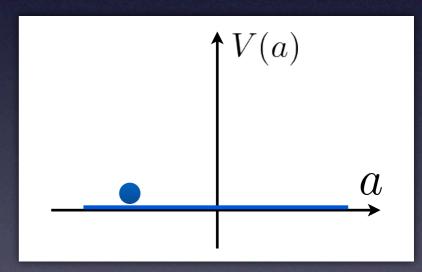
- Axions can be identified as
 Nambu-Goldstone bosons arising from breaking of global symmetry.
 (Peccei-Quinn (PQ) symmetry)
- Hidden scalar field:

$$\Phi(x) = \frac{1}{\sqrt{2}} [v_{PQ} + \rho(x)] e^{ia(x)/v_{PQ}}$$

Massive modulus, massless phase:

$$m_{\rho} \sim v_{\rm PQ}, \quad m_a = 0$$





 Interactions with standard model particles are suppressed by a large symmetry breaking scale.

$$v_{\rm PQ} \gg v_{\rm electroweak} \approx \mathcal{O}(100) \, {\rm GeV}$$

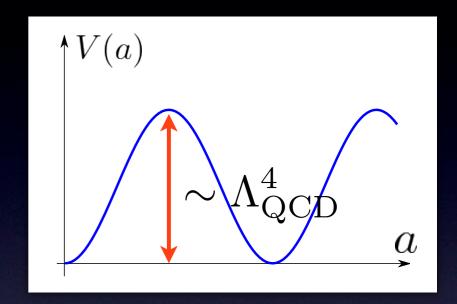
Properties of axion

Axions can couple to gluons via

$$\mathcal{L} \supset -\frac{\alpha_s}{8\pi} \frac{a}{F_a} G^a_{\mu\nu} \tilde{G}^{a\mu\nu}$$

 $F_a \propto v_{
m PQ}$: axion decay constant

• Below the QCD scale $\Lambda_{\rm QCD}\sim \mathcal{O}(100\,{
m MeV})$, topological charge fluctuations in QCD vacuum induce the potential energy:



$$V(a) \sim \Lambda_{\rm QCD}^4 \left(1 - \cos\frac{a}{F_a}\right)$$

- $\langle a \rangle = 0$ at the minimum, solving strong CP problem
- Mass of QCD axions $m_a \sim \Lambda_{\rm QCD}^2/F_a$:

$$m_a = \frac{m_{\pi} F_{\pi}}{F_a} \frac{\sqrt{z}}{1+z} \simeq 6 \,\text{meV} \left(\frac{10^9 \,\text{GeV}}{F_a}\right) \qquad z = m_u/m_d = 0.48(3)$$

- Tiny coupling with matter + non-thermal production
 - → good candidate of cold dark matter

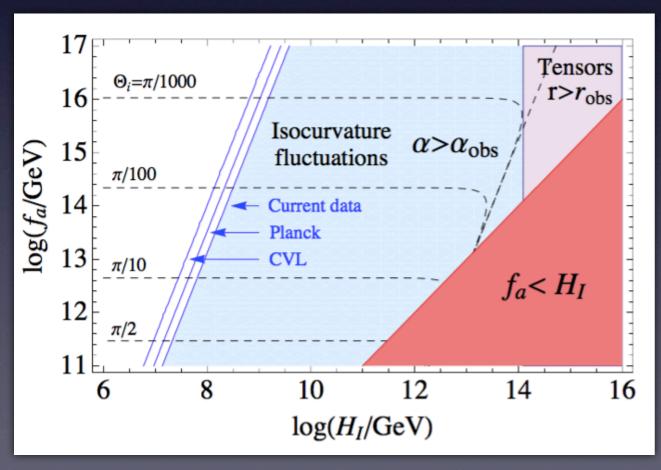
How axions are produced?

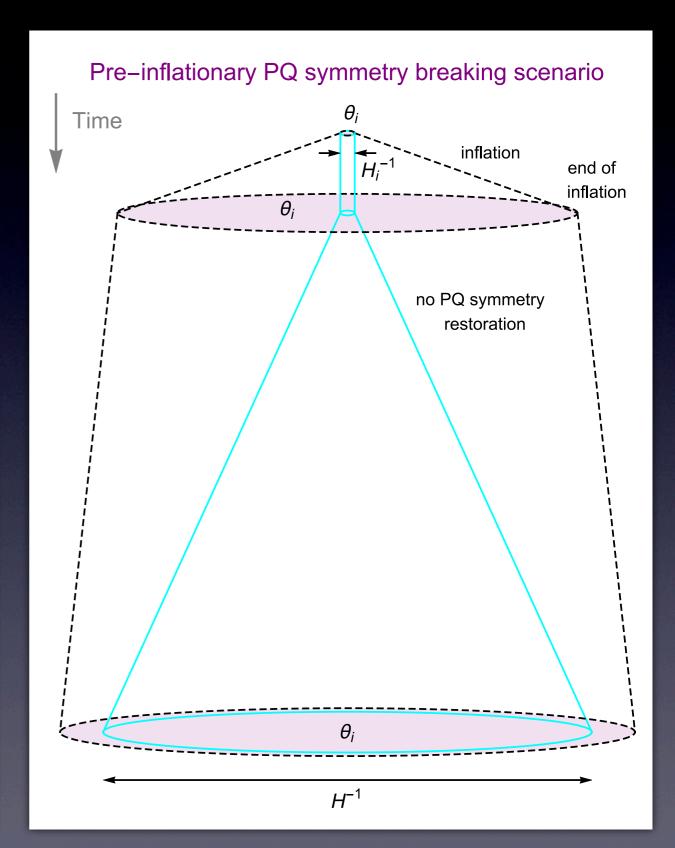
$$\Omega_a = \Omega_a(F_a), \quad m_a \simeq 6 \,\mathrm{meV} \left(\frac{10^9 \,\mathrm{GeV}}{F_a} \right)$$

- What is the "typical mass" of the axion
 (or the "typical value" for the axion decay constant),
 if axions explain 100% of CDM abundance?
- Predictions strongly depend on the early history of the universe.
- Two possibilities:
 - PQ symmetry is never restored after inflation
 - PQ symmetry is restored during/after inflation

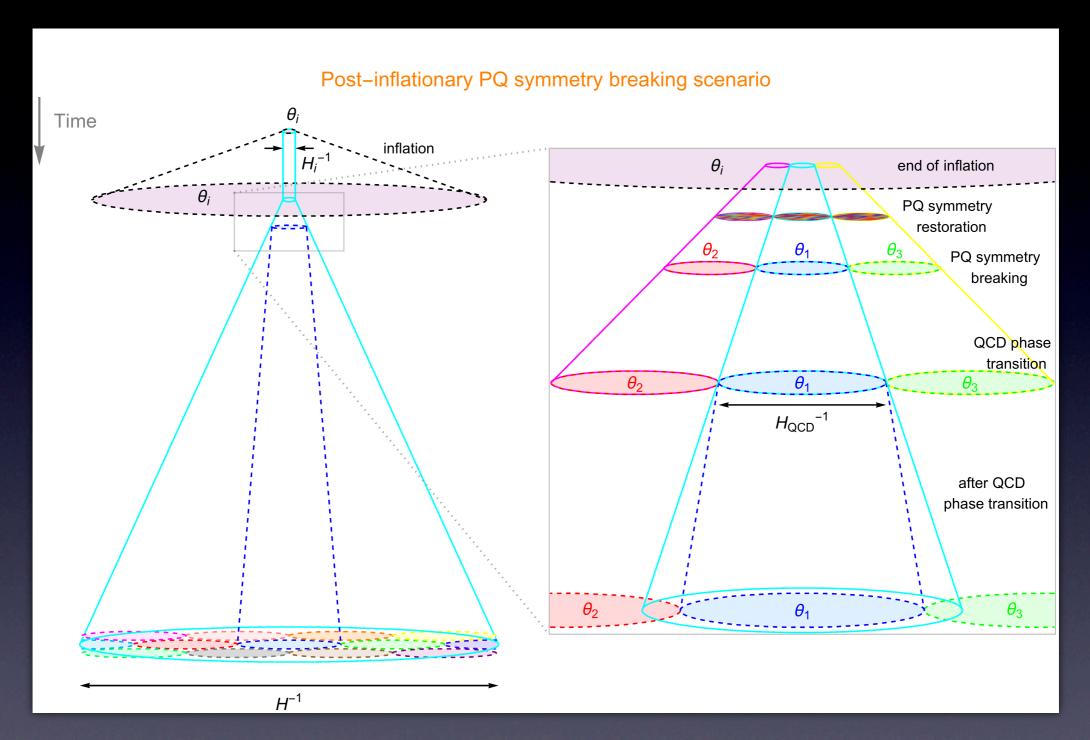
Pre-inflationary PQ symmetry breaking scenario

- Relic axion CDM abundance depends on F_a and initial misalignment angle θ_i
- Severe constraints from isocurvature fluctuations if inflationary scale is sufficiently high.





Post-inflationary PQ symmetry breaking scenario

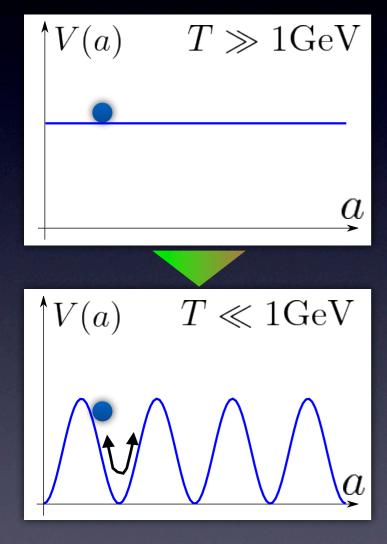


- ullet Present observable universe contains many different patches with different values of $heta_i$.
- Topological defects (strings and domain walls) are formed.
- Relic axion density should be estimated by summing over all possible field configurations.

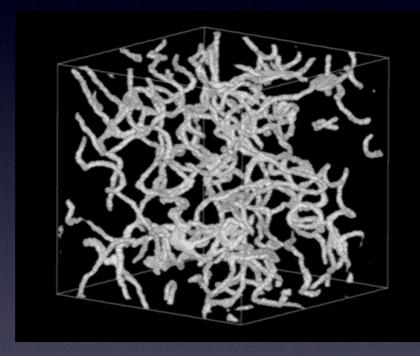
How axions are produced?

If PQ symmetry is broken after inflation, there are three contributions:

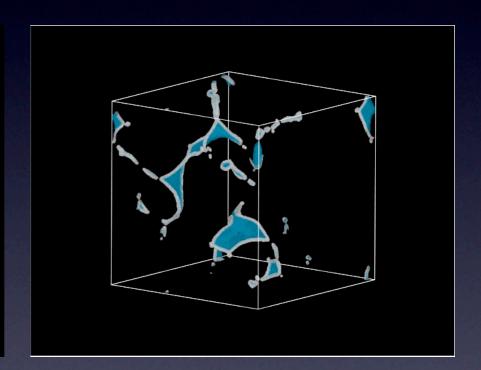
(I) Re-alignment mechanism



(2) Radiation from strings



(3) Collapse of string-wall systems



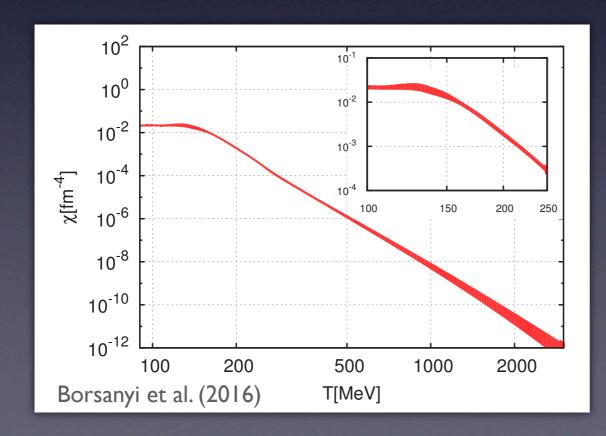
- Total abundance is sum of all these contributions.
- All these effects have to be quantitatively taken into account.

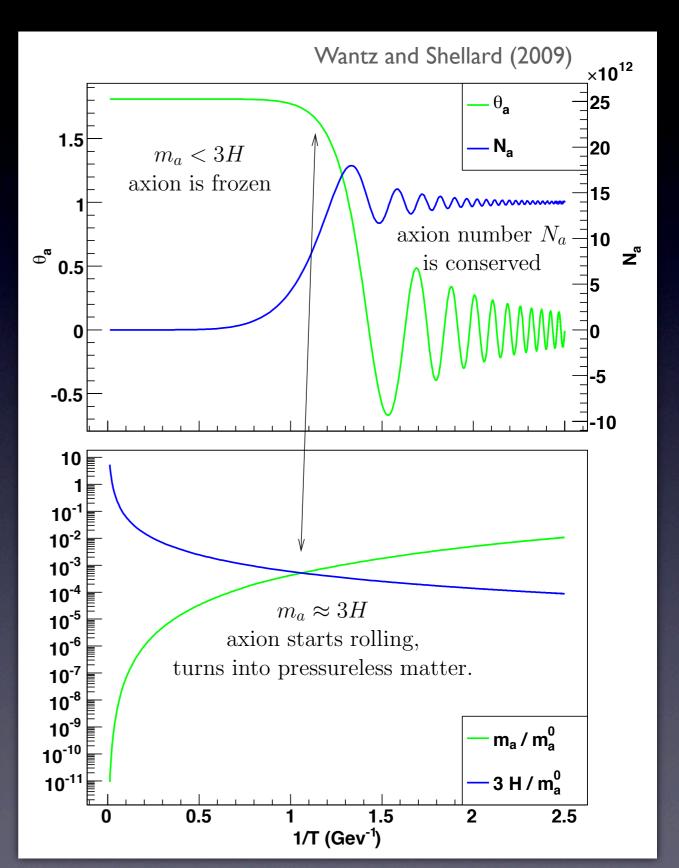
Re-alignment mechanism

- Axion field starts to oscillate at $m_a(T_{
 m osc}) pprox 3H(T_{
 m osc})$
- Temperature dependence of axion mass is important.

$$m_a(T)F_a = \sqrt{\chi(T)}$$

• Recently, the lattice calculations of χ in full QCD became available.





Axionic string and axionic domain wall

Peccei-Quinn field (complex scalar field)

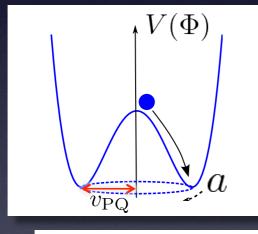
$$\Phi = |\Phi| e^{ia(x)/v_{\rm PQ}} \quad a(x) : {\rm axion \ field}$$

String formation $T \lesssim F_a$

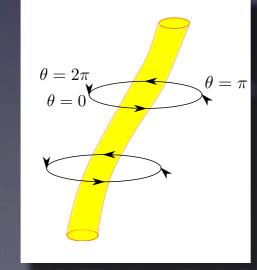
Spontaneous breaking of U(1)PQ

$$V(\Phi) = \lambda \left(|\Phi|^2 - \frac{v_{PQ}^2}{2} \right)^2$$

field space



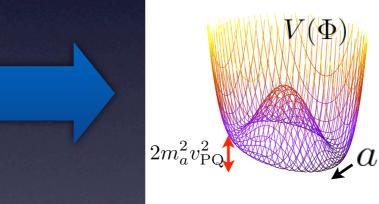
coordinate space

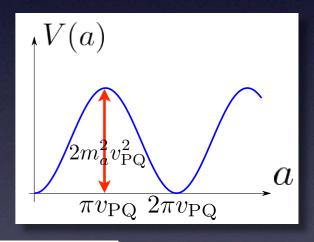


Domain wall formation $T \lesssim 1 { m GeV}$

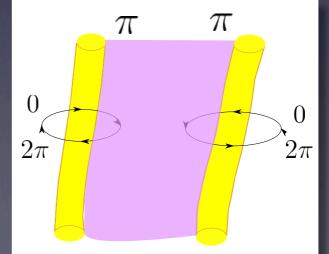
QCD effect

$$V(\Phi) = \lambda \left(|\Phi|^2 - \frac{v_{PQ}^2}{2} \right)^2 + m_a^2 v_{PQ}^2 (1 - \cos(a/v_{PQ}))$$









strings attached by domain walls

Domain wall problem

- Domain wall number N_{DW}
 - N_{DW} degenerate vacua

$$V(a) = \frac{m_a^2 v_{PQ}^2}{N_{DW}^2} \left(1 - \cos \left(N_{DW} \frac{a}{v_{PQ}} \right) \right)$$

 $N_{
m DW}$: integer determined by QCD anomaly

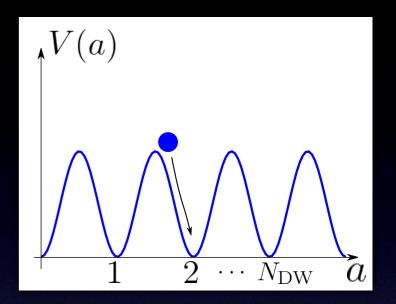


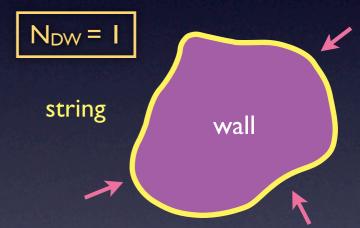
- They collapse soon after the formation.
- If N_{DW} > I, string-wall systems are stable.
 - coming to overclose the universe.

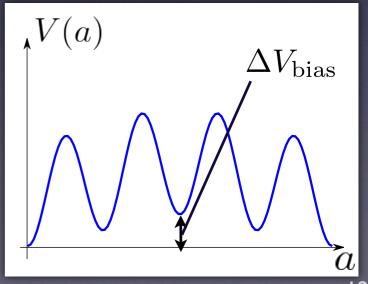
Zel'dovich, Kobzarev and Okun (1975)

 We may avoid this problem by introducing an energy bias (walls become unstable). Sikivie (1982)

$$V(a) = \frac{m_a^2 v_{\rm PQ}^2}{N_{\rm DW}^2} \left(1 - \cos\left(\frac{N_{\rm DW}a}{v_{\rm PQ}}\right)\right) + \underline{\Delta V_{\rm bias}}$$
 lifts degenerate vacua







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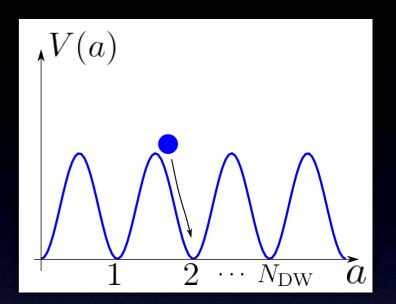


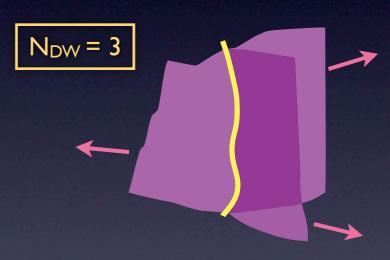
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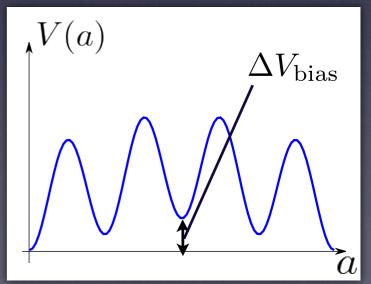
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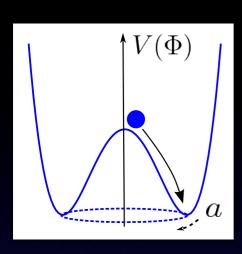






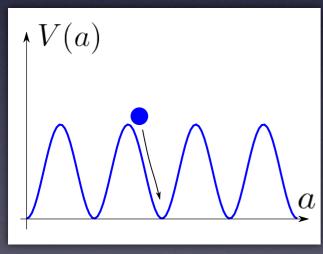
Production of axions in the early universe

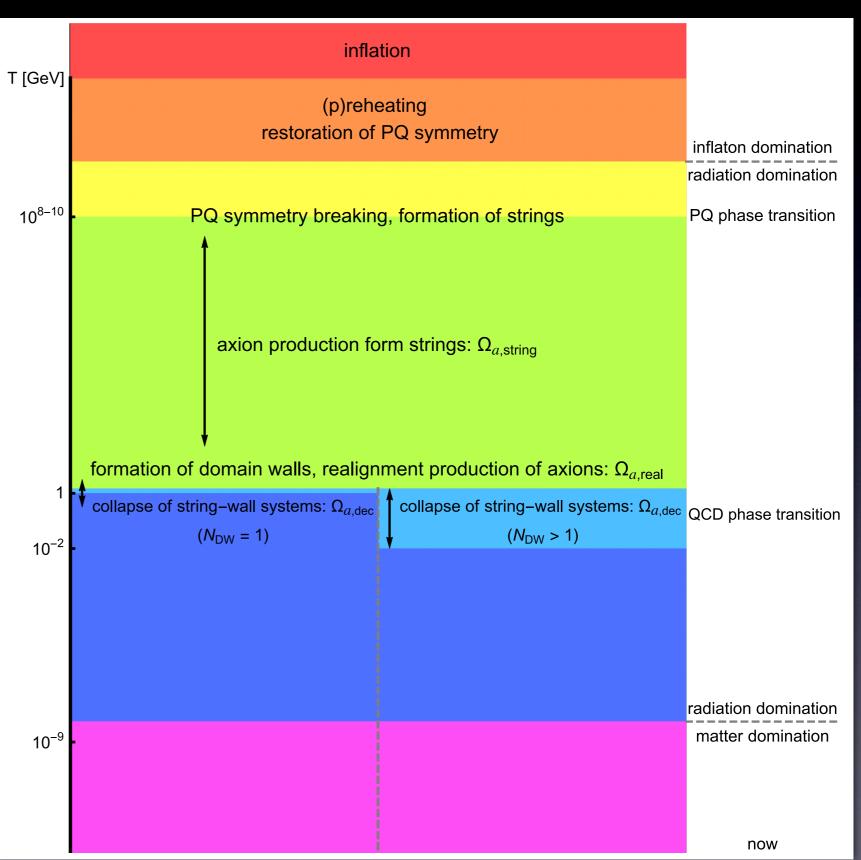
(post-inflationary PQ symmetry breaking scenario)



$$T \lesssim F_a \simeq 10^{8-11} \, \mathrm{GeV}$$



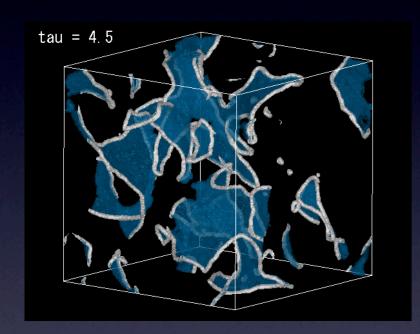


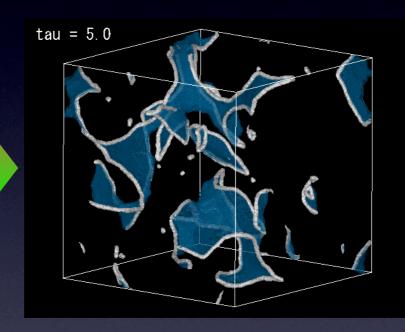


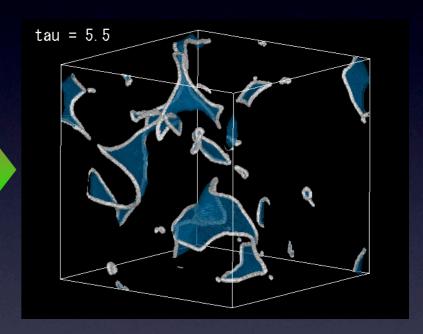
Numerical simulation : $N_{DW} = I$

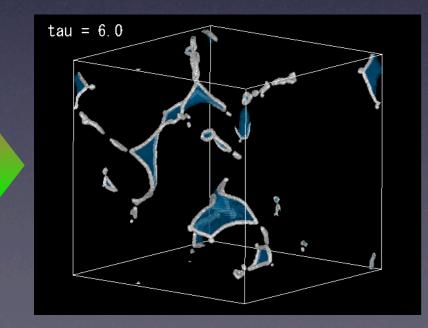
Hiramatsu, Kawasaki, KS and Sekiguchi (2012)

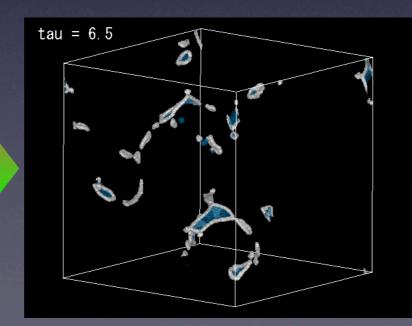
- Solving the classical field equations on lattice
- Number of grids in simulation box: $N^3 = 512^3$

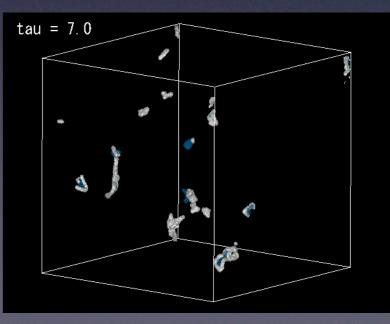






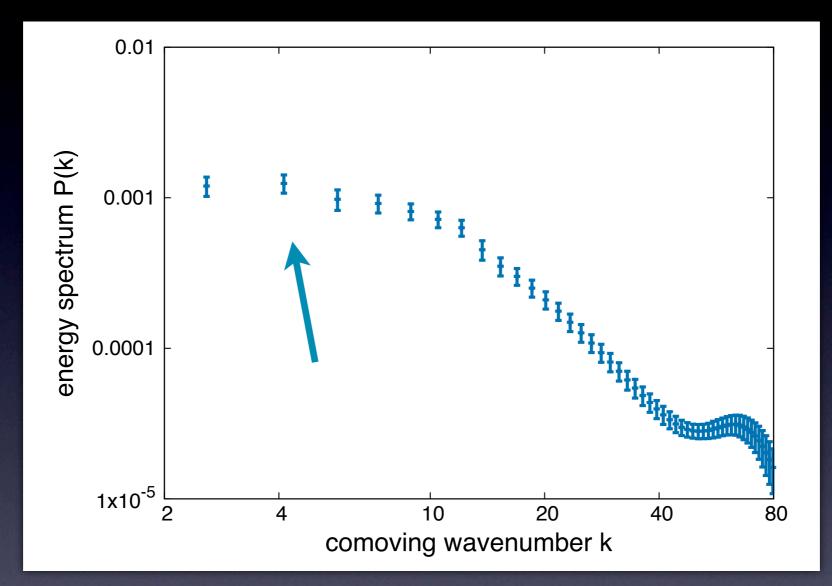






Spectrum of radiated axions

Hiramatsu, Kawasaki, KS and Sekiguchi (2012) Kawasaki, KS and Sekiguchi (2015)



Mean energy

$rac{\langle \omega_a angle}{m_a}(t_{ m decay})=3.23\pm0.18$ $\omega_a=\sqrt{m_a^2+k^2/R(t)^2}$ R(t) : scale factor of the universe

Contribution to the relic abundance

$$\rho_a(t_{\rm today}) = m_a \frac{\rho_a(t_{\rm decay})}{\langle \omega_a \rangle} \left(\frac{R(t_{\rm decay})}{R(t_{\rm today})} \right)^3$$

$$\rho_a(t_{\rm decay}) \approx \rho_{\rm defects}(t_{\rm decay})$$

Axion dark matter abundance $(N_{DW} = I)$

Re-alignment mechanism Borsanyi et al. (2016), Ballesteros, Redondo, Ringwald and Tamarit (2016)

$$\Omega_{a,\text{real}}h^2 \approx (3.8 \pm 0.6) \times 10^{-3} \left(\frac{F_a}{10^{10} \text{ GeV}}\right)^{1.165}$$

Production from string-wall systems

$$\Omega_{a,\text{string-wall}} h^2 \approx 1.2_{-0.7}^{+0.9} \times 10^{-2} \left(\frac{F_a}{10^{10} \,\text{GeV}} \right)^{1.165}$$

Total axion abundance

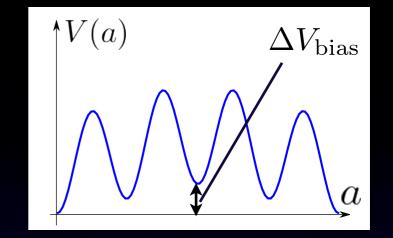
$$\Omega_{a,\text{tot}}h^2 \approx 1.6^{+1.0}_{-0.7} \times 10^{-2} \left(\frac{F_a}{10^{10} \,\text{GeV}}\right)^{1.105}$$

$$\Omega_{a,\text{tot}} \le \Omega_{\text{CDM}}$$
 $\rho_{a,\text{tot}} \le \Omega_{\text{CDM}}$
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 $\rho_{a,\text{tot}} \le 0.12$
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 $\rho_{a,\text{tot}} \le \Omega_{a,\text{tot}}$
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 Large uncertainty comes from estimation of the string density in numerical simulations.

Models with $N_{DW} > 1$: long-lived domain walls

 Domain walls are long-lived and eventually annihilated due to the energy bias.



- Origin of the bias term ?
 - U(I)_{PQ} may not be an exact symmetry:
 Global symmetry can be spoiled by gravitational effects.

Holman et al., Kamionkowski and March-Russell, Barr and Seckel, Ghigna, Lusignoli and Roncadelli, Dine (1992)

• We can assume that the PQ symmetry is not ad hoc but instead an accidental symmetry of an exact discrete Z_N symmetry (with large N).

Choi, Nilles, Ramos-Sanchez and Vaudrevange (2009)

 Planck-suppressed operators allowed by the Z_N symmetry work as the bias term.

$$\mathcal{L} \supset \frac{g}{M_{\rm Pl}^{N-4}} \Phi^N + \text{h.c.}$$

$$g = |g| e^{i\Delta}$$

$$\Delta V_{\text{bias}}(a) = -2\Xi v_{\text{PQ}}^4 \cos\left(N\frac{a}{v_{\text{PQ}}} + \Delta_D\right)$$
$$\Xi = \frac{|g|N_{\text{DW}}^{N-4}}{(\sqrt{2})^N} \left(\frac{F_a}{M_{\text{Pl}}}\right)^{N-4}, \quad \Delta_D = \Delta - N\bar{\theta}$$

Constraints

CP violation

The higher dimensional operator shifts the minimum of the potential and spoils the original Peccei-Quinn solution to the strong CP problem.

$$\frac{\langle a \rangle}{F_a} \simeq \frac{\frac{N|g|N_{\rm DW}^{N-1}}{(\sqrt{2})^{N-2}} \left(\frac{F_a}{M_{\rm Pl}}\right)^{N-2} M_{\rm Pl}^2 \sin \Delta_D}{m_a^2 + \frac{N^2|g|N_{\rm DW}^{N-2}}{(\sqrt{2})^{N-2}} \left(\frac{F_a}{M_{\rm Pl}}\right)^{N-2} M_{\rm Pl} \cos \Delta_D} < 7 \times 10^{-12}$$

→ Large N is required

Dark matter abundance

Long-lived domain walls produce too much cold axions.

Hiramatsu, Kawasaki, KS, and Sekiguchi (2013); Kawasaki, KS, and Sekiguchi (2015)

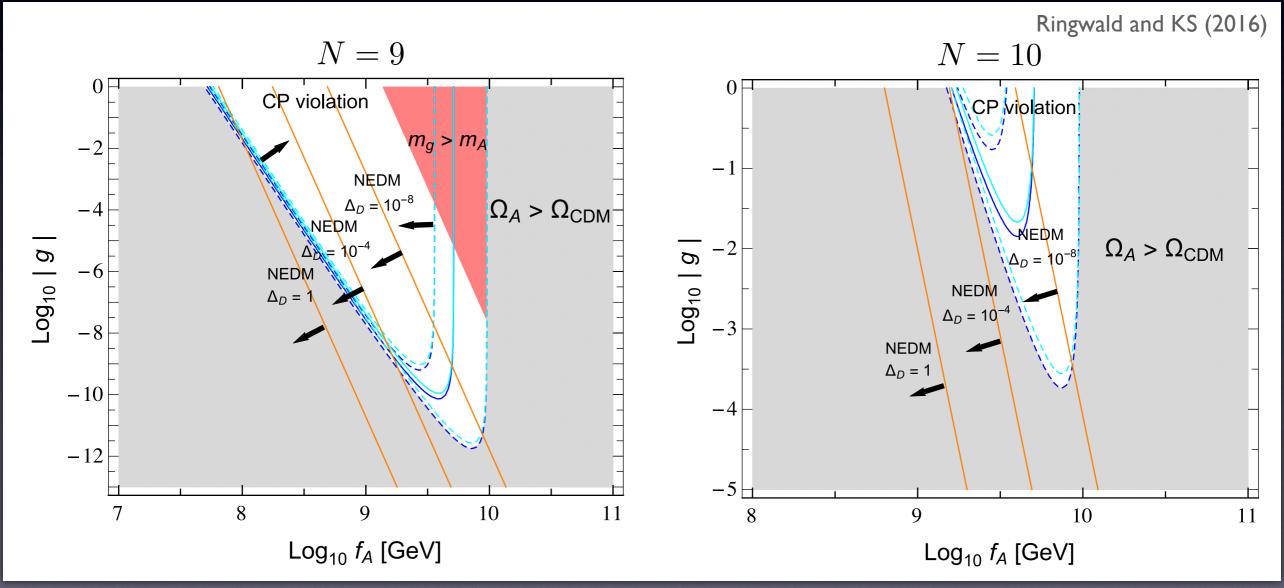
$$\Omega_a h^2 \simeq (3.4-6.2) \times N_{\mathrm{DW}}^{-2} \left(\frac{\Xi}{10^{-52}}\right)^{-1/2} \left(\frac{F_a}{10^9 \, \mathrm{GeV}}\right)^{-1/2} \quad \text{with} \quad \Xi = \frac{|g|N_{\mathrm{DW}}^{N-4}}{(\sqrt{2})^N} \left(\frac{F_a}{M_{\mathrm{Pl}}}\right)^{N-4} = \frac{1}{2} \left(\frac{1}{\sqrt{2}}\right)^N \left(\frac{F_a}{M_{\mathrm{Pl}}}\right)^{N-4} = \frac{1}{2} \left(\frac{1}{\sqrt{2}}\right)^N \left(\frac{1}{\sqrt{2}}\right)^N \left(\frac{F_a}{M_{\mathrm{Pl}}}\right)^{N-4} = \frac{1}{2} \left(\frac{1}{\sqrt{2}}\right)^N \left$$

→ Small N is required

• Constraints on the energy bias (= on the coefficient g)

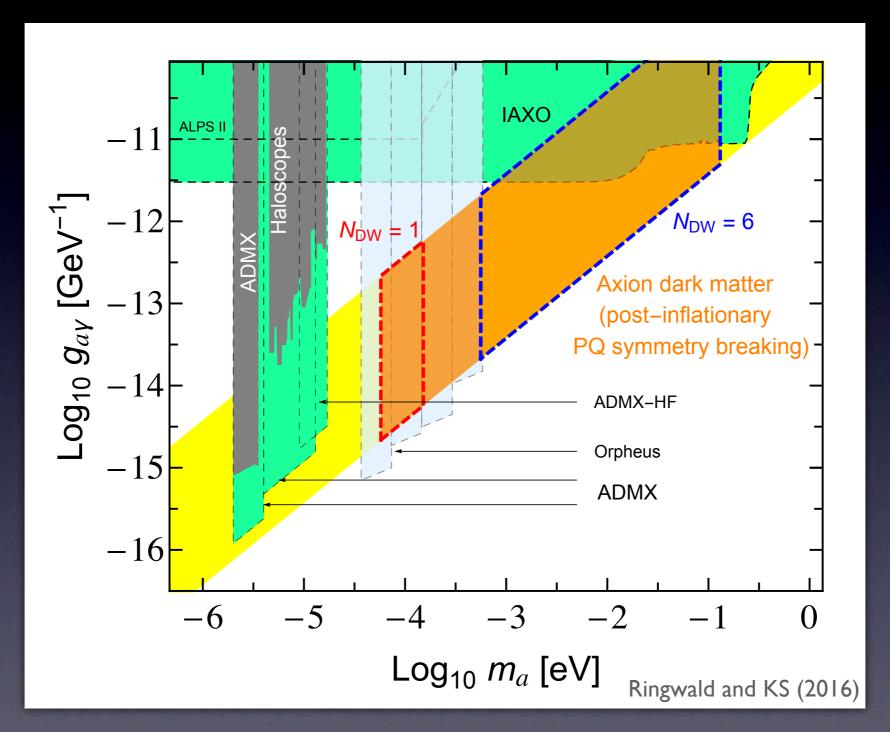
$$\Delta V_{\text{bias}}(a) = -2\Xi v_{\text{PQ}}^4 \cos\left(N\frac{a}{v_{\text{PQ}}} + \Delta_D\right) \qquad \qquad \mathcal{L} \supset \frac{g}{M_{\text{Pl}}^{N-4}}\Phi^N + \text{h.c.}$$

- Loopholes appear if the order of the discrete symmetry is N = 9 or 10, but some tuning of the phase parameter Δ_D is required.
- If we allow such a mild tuning, axions can explain total dark matter abundance in the small ${\cal F}_a$ range.



Search for axion dark matter

Search space in photon coupling $g_{a\gamma} \sim lpha/(2\pi F_a)$ vs. mass m_a



Mass ranges predicted in the post-inflationary PQ symmetry breaking scenario can be probed by various future experimental studies.

Conclusion

- Predictions for axion dark matter strongly depend on the early history of the universe.
- If the PQ symmetry is broken after inflation, string-wall systems give additional contribution to the CDM abundance.
- Axion can be dominant component of dark matter if

$$F_a \simeq (3.8 - 9.9) \times 10^{10} \, \mathrm{GeV}$$
 for N_{DW} = I $m_a \simeq (0.6 - 1.5) \times 10^{-4} \, \mathrm{eV}$

$$F_a \simeq \mathcal{O}(10^8 - 10^{10}) \, \mathrm{GeV}$$
 $m_a \simeq \mathcal{O}(10^{-4} - 10^{-2}) \, \mathrm{eV}$ for N_{DW} > I

Mass ranges can be probed in the future experiments.