

# High-energy vacuum birefringence in an intense laser field

LNPC'17, Yokohama

April 20, 2017

**Sergey Bragin**

Sebastian Meuren, Christoph H. Keitel, Antonino Di Piazza

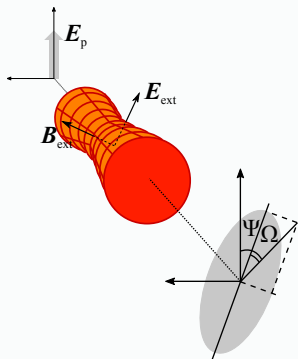
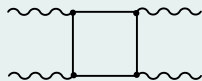
**arXiv:1704.05234**



MPI for Nuclear Physics, Heidelberg (Germany)

## Vacuum polarization

- Vacuum birefringence:  
Different refractive indices for two different polarizations.
- Vacuum dichroism (via  $e^- e^+$  pair production):  
Different absorption for two different polarizations.



### Small vacuum polarization limit (linearly polarized probe photons)

- Birefringence:  $\Omega$  (ratio of the ellipse axes).
- Dichroism:  $\Psi$  (major axis rotation).



## Vacuum magnetic birefringence

$$\Omega \sim \omega_p B^2 L \sim 10^{-11}.$$

F. Della Valle et al., Phys. Rev. D 90, 092003 (2014).

## How to improve the vacuum birefringence effect

- Increasing the field strength  $\rightarrow$  high-intensity optical lasers ( $A^\mu, k^\mu, k^0 = \omega_L, k_\mu k^\mu = 0, \omega_L \sim 1 \text{ eV}$ ).
- Increasing the probe photon energy  $\rightarrow$  gamma photons ( $q^\mu, q^0 = \omega_p, q_\mu q^\mu = 0$ ).

B. King & N. Elkina, Phys. Rev. A 94, 062102 (2016); A. Ilderton & M. Marklund, J. Plasma Phys. 82, 655820201 (2016); Y. Nakamiya et al., arXiv:1512.00636; V. Dinu et al., Phys. Rev. D 89, 125003 (2014).

## Parameters ( $\hbar = c = 1$ )

Classical intensity parameter:

$$\xi = \frac{|e|E}{m\omega_L}.$$

$$\xi \sim 100 \text{ for } I \sim 10^{23} \text{ W/cm}^2.$$

Quantum nonlinearity parameter:

$$\chi = \frac{kq}{m^2} \xi \stackrel{\text{head-on}}{=} \frac{2\omega_p \omega_L}{m^2} \xi.$$

$$\chi \sim 1 \rightarrow \text{pair production is sizable.} \\ (\omega_p \sim 1 \text{ GeV}, I \sim 10^{23} \text{ W/cm}^2)$$



- Vacuum birefringence and dichroism in a linearly polarized strong plane-wave field.
  - Radiative corrections to probe photon propagation, Dyson equation.
  - Locally constant crossed field approximation.
- Feasibility of a high-energy vacuum birefringence experiment.
  - Setup, gamma photon generation and detection.
  - General polarization of the probe photon beam: density matrix, Stokes parameters.
  - Statistical analysis and estimations.



## Dyson equation

$$\text{wavy line} = \text{wavy line} + \text{wavy line} \text{---} \text{shaded circle} \text{---} \text{wavy line} + \text{wavy line} \text{---} \text{shaded circle} \text{---} \text{shaded circle} \text{---} \text{wavy line} + \dots$$

$$= \text{wavy line} + \text{wavy line} \text{---} \text{shaded circle} \text{---} \text{wavy line}$$

$$\text{shaded circle} = \text{circle} + \text{circle with blob} + \text{circle with blob} + \text{circle with blob} + \dots$$

$$-\partial^\sigma \partial_\sigma \Phi^\mu(x) = \int d^4y P^{\mu\nu}(x, y) \Phi_\nu(y).$$

## Laser pulse

$$A^\mu(kx) = a^\mu \psi(kx).$$

$$a^2 < 0, \quad ka = 0; \quad |\psi(kx)|, |\psi'(kx)| \lesssim 1; \quad f^{\mu\nu} = k^\mu a^\nu - k^\nu a^\mu;$$

$$\{L_1^\mu, L_2^\mu\}: \quad L_1^\mu = \frac{f^{\mu\nu} q_\nu}{kq\sqrt{-a^2}}, \quad qL_i = kL_i = 0, \quad L_i^\mu L_{j\mu} = -\delta_{ij}.$$

## Dyson equation ( $\xi \gg 1$ , $\chi \lesssim 1$ )

$$-\partial^\sigma \partial_\sigma \Phi^\mu(x) = P^{\mu\nu}(kx, \chi) \Phi_\nu(y),$$

$$P^{\mu\nu}(kx, \chi) = -[p_1(kx, \chi) L_1^\mu L_1^\nu + p_2(kx, \chi) L_2^\mu L_2^\nu],$$

$$p_1(kx, \chi) = \frac{\alpha m^2}{3\pi} \int_{-1}^1 dv (w-1) \frac{f'(u)}{u}, \quad p_2(kx, \chi) = \frac{\alpha m^2}{3\pi} \int_{-1}^1 dv (w+2) \frac{f'(u)}{u},$$

$$w = 4/(1-v^2), \quad u = [w/\chi |\psi'(kx)|]^{2/3}, \quad f(u) = \pi [\text{Gi}(u) + i \text{Ai}(u)].$$

## Solution

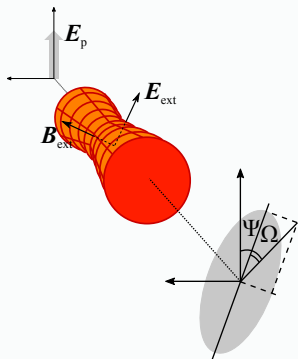
$$\Phi^{(0)\mu}(x) = \epsilon^{(0)\mu} e^{-iqx} = \sum_{i=1,2} b_i^{(0)} L_i^\mu e^{-iqx} \rightarrow \Phi^\mu(x) = \sum_{i=1,2} b_i^{(0)} e^{i\phi_i} e^{-\lambda_i} L_i^\mu e^{-iqx}.$$

$$\phi_i = -\frac{1}{2kq} \int_{-\infty}^{\infty} d\phi \text{Re}[p_i(\phi, \chi)], \quad \lambda_i = -\frac{1}{2kq} \int_{-\infty}^{\infty} d\phi \text{Im}[p_i(\phi, \chi)].$$

## Difference of the two components

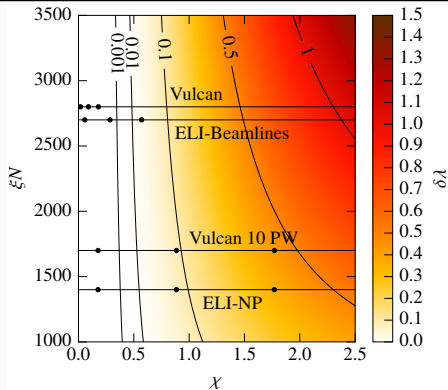
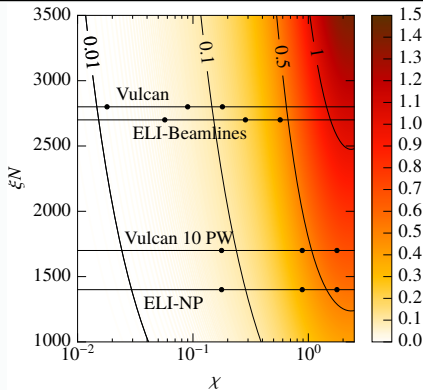
$$\delta\phi = \phi_2 - \phi_1 = -\frac{1}{2kq} \int_{-\infty}^{\infty} d\phi \operatorname{Re} [p_2(\phi, \chi) - p_1(\phi, \chi)],$$

$$\delta\lambda = \lambda_2 - \lambda_1 = -\frac{1}{2kq} \int_{-\infty}^{\infty} d\phi \operatorname{Im} [p_2(\phi, \chi) - p_1(\phi, \chi)].$$



## Small vacuum polarization limit (linearly polarized probe photons)

- Birefringence:  $\Omega \propto \delta\phi$ .
- Dichroism:  $\Psi \propto \delta\lambda$ .



Rectangular pulse envelope:

$$\psi'(kx) = \begin{cases} \sin(kx), & kx \in [-N\pi, N\pi], \\ 0 & \text{otherwise.} \end{cases}$$

## Optimal regime

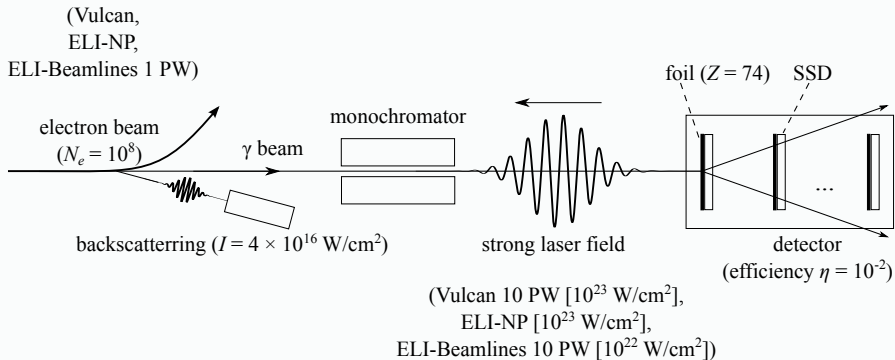
$$\chi \sim 0.1, \delta\phi \sim 0.1 \\ (\omega_p \sim 10^2 \text{ MeV for 10 PW}).$$

$$\delta\phi = \frac{\xi N}{m^2 \chi} \int_0^\pi d\phi \operatorname{Re} [p_1(\phi, \chi) - p_2(\phi, \chi)],$$

$$\delta\lambda = \frac{\xi N}{m^2 \chi} \int_0^\pi d\phi \operatorname{Im} [p_1(\phi, \chi) - p_2(\phi, \chi)],$$

$$\psi'(\phi) = \sin(\phi).$$





Gaussian pulse envelope:  $\psi'(kx) = e^{-(kx)^2/\Delta\phi^2} \sin(kx)$ .

See also: B. King & N. Elkina, Phys. Rev. A 94, 062102 (2016); A. Ilderton & M. Marklund, J. Plasma Phys. 82, 655820201 (2016); Y. Nakamiya et al., arXiv:1512.00636.



## Calculation of an observable

$$W \propto |M|^2 = M_\mu M_\nu^* \epsilon^\mu \epsilon^{*\nu}.$$

## Density matrix

$$\epsilon^\mu \epsilon^{*\nu} \rightarrow \rho^{\mu\nu} = \sum_a w_a \epsilon_a^\mu \epsilon_a^{*\nu} = \sum_{i,j=1,2} \rho_{ij} \Lambda_i^\mu \Lambda_j^\nu.$$

$$\{\Lambda_1^\mu, \Lambda_2^\mu\} : \quad q\Lambda_i = k\Lambda_i = 0, \quad \Lambda_i^\mu \Lambda_{j\mu} = -\delta_{ij}.$$

$$\begin{pmatrix} L_1^\mu \\ L_2^\mu \end{pmatrix} = R(\varphi_L) \cdot \begin{pmatrix} \Lambda_1^\mu \\ \Lambda_2^\mu \end{pmatrix}, \quad R(\varphi_L) = \begin{pmatrix} \cos \varphi_L & \sin \varphi_L \\ -\sin \varphi_L & \cos \varphi_L \end{pmatrix}.$$

## Stokes parameters

$$\rho = \frac{1}{2} (S_0 \mathbf{I} + \mathbf{S} \cdot \boldsymbol{\sigma}),$$

$\boldsymbol{\sigma} = (\sigma_1, \sigma_2, \sigma_3)$  - the Pauli matrices,

$S = \{S_0, \mathbf{S}\}$  [ $\mathbf{S} = (S_1, S_2, S_3)$ ] - the Stokes vector.



## Connection between the Stokes parameters

$$\rho = T \rho^{(0)} T^\dagger,$$

$$T = R^{-1}(\varphi_L) \begin{pmatrix} e^{i\phi_1 - \lambda_1} & 0 \\ 0 & e^{i\phi_2 - \lambda_2} \end{pmatrix} R(\varphi_L).$$

## Pair production cross section

$$d\sigma_{\text{PP}} = \frac{d\varphi}{2\pi} \left\{ S_0 \sigma^{(0)} + [S_1 \sin(2\varphi) + S_3 \cos(2\varphi)] \sigma^{(1)} \right\},$$

$\varphi$  — azimuth angle for the created pair,

$\sigma^{(0)}$  — cross section for an unpolarized beam,  $\sigma^{(1)} \sim 0.1\sigma^{(0)}$ .

Note: the cross section  $d\sigma_{\text{PP}}$  does not depend on  $S_2$ .

Laser polarization is rotated by  $\varphi_L = \pi/4$  with respect to the detector axes.

## Linear polarization

$$S^{(0)} = \{1, 0, 0, 1\}$$

$$S_0 = e^{-(\lambda_1 + \lambda_2)} \cosh \delta\lambda,$$

$$S_1 = e^{-(\lambda_1 + \lambda_2)} \sinh \delta\lambda,$$

$$S_2 = -e^{-(\lambda_1 + \lambda_2)} \sin \delta\phi \approx -\delta\phi,$$

$$S_3 = e^{-(\lambda_1 + \lambda_2)} \cos \delta\phi \approx 1 - (\delta\phi)^2/2.$$

## Circular polarization

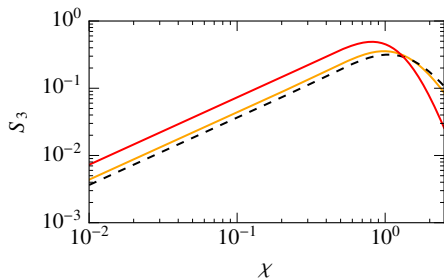
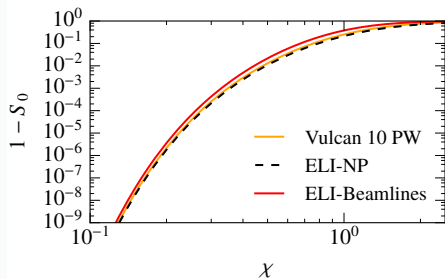
$$S^{(0)} = \{1, 0, 1, 0\}$$

$$S_0 = e^{-(\lambda_1 + \lambda_2)} \cosh \delta\lambda,$$

$$S_1 = e^{-(\lambda_1 + \lambda_2)} \sinh \delta\lambda,$$

$$S_2 = e^{-(\lambda_1 + \lambda_2)} \cos \delta\phi \approx 1 - (\delta\phi)^2/2,$$

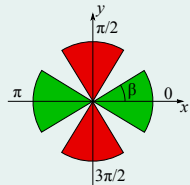
$$S_3 = e^{-(\lambda_1 + \lambda_2)} \sin \delta\phi \approx \delta\phi.$$



## Observable

$$R_B = \frac{(N_0 + N_\pi) - (N_{\pi/2} + N_{3\pi/2})}{N}.$$

$$\langle R_B \rangle = \frac{\sin(2\beta)}{2\beta} \cdot \frac{\sigma^{(1)}}{\sigma^{(0)}} \cdot \frac{S_3}{S_0} \approx \frac{\sin(2\beta)}{2\beta} \cdot \frac{\sigma^{(1)}}{\sigma^{(0)}} \cdot \delta\phi.$$



## Statistics

$N \gg 1$ :  $R_B \in \mathcal{N}(\langle R_B \rangle, 1/N)$ .

Verification/rejection at  $n\sigma$  confidence level:

$$N_\gamma^B = \frac{\pi n^2}{\eta\beta \langle R_B \rangle^2} \cdot \frac{e^{\lambda_1 + \lambda_2}}{\cosh \delta\lambda}. \quad (\beta_{\text{opt}} \approx 33^\circ)$$

## Duration of the experiment ( $3\sigma$ )

- CLF: 260 days.  $(10^{23} \text{ W/cm}^2, 30 \text{ fs}, 2 \text{ shots/hour [Vulcan]})$
- ELI-NP: 13 days.  $(10^{23} \text{ W/cm}^2, 25 \text{ fs}, 1 \text{ shot/minute})$
- ELI-Beamlines: 4 days.  $(10^{22} \text{ W/cm}^2, 150 \text{ fs}, 1 \text{ shot/minute})$



- High-energy vacuum polarization experiments in a strong laser field are promising for testing QED (and searching for physics beyond the Standard Model).
- In this regime it is important to take both vacuum birefringence and dichroism into account.
- For the high-energy vacuum birefringence experiment a significant improvement is obtained if employing circularly polarized probe photons.
- The experiment is feasible at the upcoming laser facilities (the expected duration of the experiment is a few days for the  $3\sigma$  confidence level).

**Thank you for your attention!**