

# Dark Sector at CLIC

Michael Rauch | Physics at CLIC – July 18, 2017

INSTITUTE FOR THEORETICAL PHYSICS



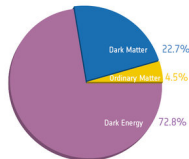
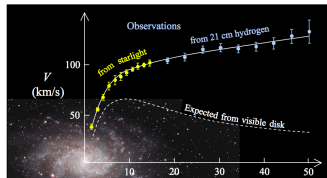
Strong indications for existence of Dark Matter (DM)

- Rotation curves of galaxies
- Galaxy clusters and gravitational lensing
- Cosmic microwave background

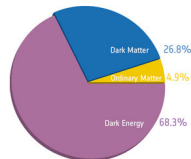
→  $\Lambda$ CDM Model

⇒ Dark sector in many BSM extensions

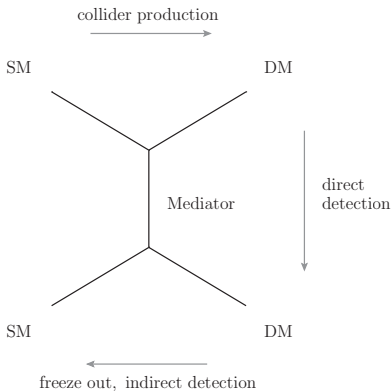
- particle(s) without electric or colour charge
- protected by global symmetries  
→ stable on astrophysical time scales
- often not completely decoupled  
↔ interacts with SM by Z boson  
or mediator exchange



Before Planck



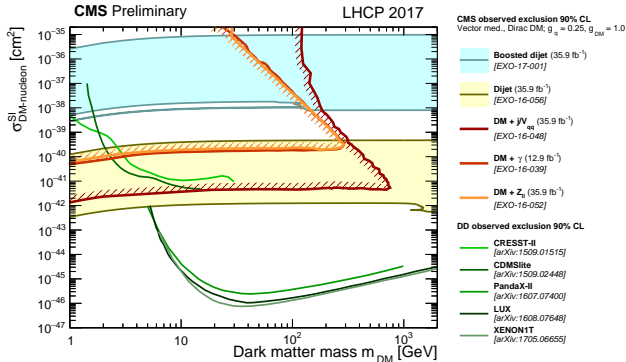
After Planck



## Collider searches: LHC

- detection in mono-jet/mono-photon searches  $pp \rightarrow j/\gamma + \cancel{E}_T$
- Sensitivity almost independent of DM mass
- $\rightarrow$  limits in low-mass region stronger than from direct detection experiments

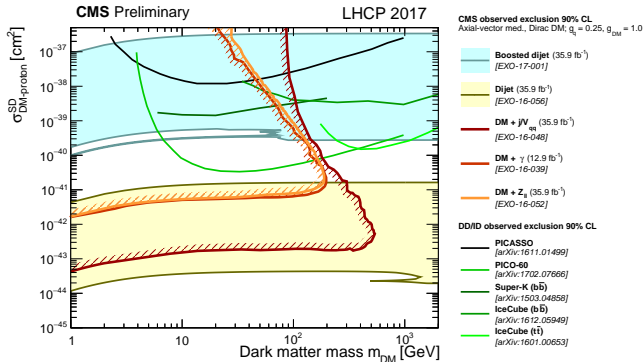
$$1\text{fb} \hat{=} 10^{-39}\text{cm}^2$$



## Collider searches: LHC

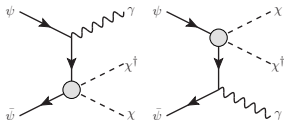
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









$$1\text{fb} \hat{=} 10^{-39}\text{cm}^2$$



[Dreiner, Huck, Krämer, Schmeier, Tattersall]

- Extensive survey of different combinations
- scalar, fermion and vector dark matter
- process  $e^+ e^- \rightarrow \gamma \chi \chi$

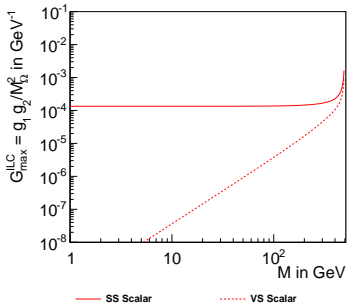


DM Med.	Diagram	$-\mathcal{L}_{UV}$ $-\mathcal{L}_{eff}$
S S		$g_s \chi^\dagger \chi \phi + \tilde{\psi} (g_s + i g_p \gamma^5) \psi \phi$ $\frac{g_s}{M_\phi^2} \chi^\dagger \chi \tilde{\psi} (g_s + i g_p \gamma^5) \psi$
S F		$\tilde{\eta} (g_s + g_p \gamma^5) \psi \chi + \tilde{\psi} (g_s - g_p \gamma^5) \eta \chi^\dagger$ $\frac{1}{M_\eta} \left[ (g_s^2 - g_p^2) \tilde{\psi} \psi \chi^\dagger \chi + \frac{i}{M_\eta} \chi^\dagger \tilde{\psi} (g_s^2 + g_p^2 - 2 g_s g_p \gamma^5) \gamma^\mu \partial_\mu (\psi \chi) \right]$
S V		$g_s (\chi^\dagger \partial_\mu \chi - \chi \partial_\mu \chi^\dagger) Z^\mu + \tilde{\psi} \gamma^\mu (g_L P_L + g_R P_R) \psi Z_\mu$ $\frac{g_s}{M_\phi^2} \tilde{\psi} \gamma^\mu (g_L P_L + g_R P_R) \psi (\phi^\dagger \partial_\mu \phi - \phi \partial_\mu \phi^\dagger)$
F S		$\tilde{\chi} (g_s + g_p \gamma^5) \chi \phi + \tilde{\psi} (g_s + g_p \gamma^5) \psi \phi$ $\frac{1}{M_\phi^2} \tilde{\chi} (g_s + i g_p \gamma^5) \chi \tilde{\psi} (g_s + i g_p \gamma^5) \psi$
F V		$\tilde{\psi} \gamma^\mu (g_L P_L + g_R P_R) \psi Z_\mu + \tilde{\chi} \gamma^\mu (g_L P_L + g_R P_R) \chi Z_\mu$ $\frac{1}{M_\phi^2} \tilde{\psi} \gamma^\mu (g_L P_L + g_R P_R) \psi \tilde{\chi} \gamma_\mu (g_L P_L + g_R P_R) \chi$
F tS		$\tilde{\chi} (g_s + g_p \gamma^5) \psi \phi + \tilde{\psi} (g_s + g_p \gamma^5) \chi \phi$ $\frac{1}{M_\eta^2} \tilde{\psi} (g_s - g_p \gamma^5) \chi \tilde{\chi} (g_s + g_p \gamma^5) \psi$
F tV		$\tilde{\psi} \gamma^\mu (g_L P_L + g_R P_R) \chi Z_\mu + \tilde{\chi} \gamma^\mu (g_L P_L + g_R P_R) \psi Z_\mu$ $\frac{1}{M_\eta^2} \tilde{\psi} \gamma^\mu (g_L P_L + g_R P_R) \chi \tilde{\chi} \gamma_\mu (g_L P_L + g_R P_R) \psi$
V S		$-\chi^\dagger \chi_\mu \phi + \tilde{\psi} (g_s + i g_p \gamma^5) \psi \phi$ $-\frac{g_s}{M_\phi^2} \chi^\dagger \chi_\mu \tilde{\psi} (g_s + i g_p \gamma^5) \psi$
V F		$-\tilde{\eta} \gamma^\mu (g_L P_L + g_R P_R) \chi_\mu + \tilde{\psi} \gamma^\mu (g_L P_L + g_R P_R) \eta \chi_\mu^\dagger$ $\frac{1}{M_\eta} \left[ g_s g_p \tilde{\psi} \gamma^\mu \psi \chi_\mu^\dagger \chi_\mu + \frac{i}{M_\eta} \chi_\mu^\dagger \tilde{\psi} \gamma^\mu \gamma^\nu \gamma^\mu (g_L^2 P_L + g_R^2 P_R) \partial_\nu (\psi \chi_\mu) + \right]$
V V		$i g_s [Z_\mu \chi_\nu^\dagger \partial^\mu \chi^\nu + Z_\mu \chi_\nu \partial^\mu \chi^{\nu\dagger} + \chi_\mu^\dagger \chi_\nu \partial^\mu Z^{\nu\mu}] + \tilde{\psi} \gamma_\mu (g_L P_L + g_R P_R) \psi$ $\frac{i g_s}{M_\phi^2} \tilde{\psi} \gamma^\mu (g_L P_L + g_R P_R) \psi \left[ \chi^\nu \partial_{\mu\nu}^\dagger - \chi^{\nu\dagger} \partial_{\mu\nu} + \partial^\nu (\chi_\mu^\dagger \chi_\nu - \chi_\mu \chi_\nu^\dagger) \right]$

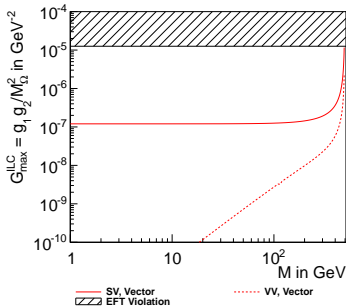
# Exclusion Limits

Setup:  $\sqrt{s} = 1 \text{ TeV}$ ,  $\mathcal{L} = 500 \text{ fb}^{-1}$

scalar mediator



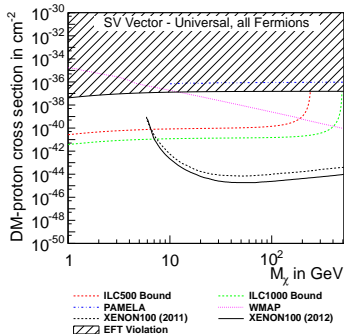
vector mediator



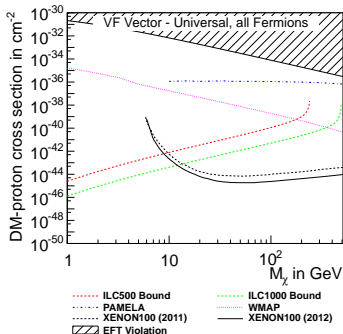
coupling reach ( $G = \frac{g_1 g_2}{M_{\text{Mediator}}}$ ):  $10^{-4} \text{ GeV} / 10^{-7} \text{ GeV}^2$

fairly independent of mass up to kinematic threshold  
except vector DM: much stronger limit for small DM mass

scalar DM, vector mediator



vector DM, fermion mediator



low-mass range ( $\lesssim 10$  GeV): competitive with astrophysical bounds in many models

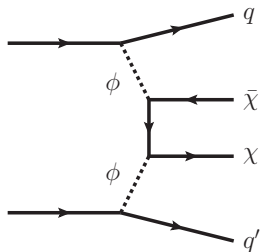
high-mass range ( $\gtrsim 100$  GeV): difficult to push into unexcluded regions



- Mono-jet / Mono-photon searches:  
WIMP recoils against high- $p_T$  jet/photon
- $\Rightarrow$  Only total amount of  $\cancel{E}_T$  can be measured,  
i.e. differential c.s. for one observable
- $\rightarrow$  Limited tool for determining properties

$\Rightarrow$  Test other processes

## Vector-Boson Fusion



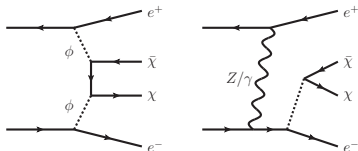
( $\phi$ : mediator,  
 $\chi$ : DSP (dark sector particle))

- proven as great tool already in Higgs phenomenology
- Predominant background:  
 $pp \rightarrow Zjj \rightarrow \nu\bar{\nu}jj$   
(both QCD and VBF-EW)
- couplings very constrained from mono-jet searches
- $\leftrightarrow \mathcal{O}$ (electro-weak coupling) required for useful phenomenology

[see also An, Wang, Zhang]

# Moving to $e^+e^-$ colliders

→ Try same topology at  $e^+e^-$  collider

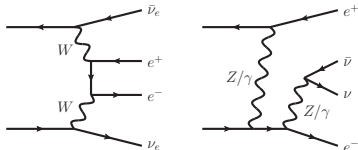


Signature:  $e^+e^-$  pair +  $\cancel{E}_T$

$e^+e^-$  collider clean environment:

- almost no exp. systematics
- smaller theory uncertainties
- $\Rightarrow$  mostly statistics limited

Main backgrounds:



## Simple effective model used for study:

- DSP  $\chi$ : Dirac fermion
- Mediator  $\phi$ : scalar or vector

Mediator couples to electrons only (results for leptons-only basically identical)

→ Interaction terms appearing in the Lagrangian:

	scalar	vector
e	$i g_{ee\phi,S} \bar{e} e \phi_S$	$i g_{ee\phi,V} \bar{e} \gamma_\mu e \phi_V^\mu$
$\chi$	$i g_{\chi\chi\phi,S} \bar{\chi} \chi \phi_S$	$i g_{\chi\chi\phi,V} \bar{\chi} \gamma_\mu \chi \phi_V^\mu$

Define effective mass:

$$M_* = \frac{M_\phi}{\sqrt{g_{ee\phi} g_{\chi\chi\phi}}}$$

Heavy mediator can be integrated out:

$$g_{ee\phi} \frac{1}{q^2 - M_\phi^2} g_{\chi\chi\phi} \stackrel{q^2 \ll M_\phi^2}{=} g_{ee\phi} \frac{1}{-M_\phi^2} g_{\chi\chi\phi} = -\frac{1}{M_*^2}$$

→ effective dimension-6 operators:  $\bar{e} e \bar{\chi} \chi$ ,  $\bar{e} \gamma_\mu e \bar{\chi} \gamma^\mu \chi$

Benchmark points for study:

model	mediator mass	mediator spin	DSP mass	$M_*$
LSL	8 GeV	0 (scalar)	5 GeV	30 GeV
LVL	8 GeV	1 (vector)	5 GeV	30 GeV
LSH	8 GeV	0 (scalar)	120 GeV	27.4 GeV
LVH	8 GeV	1 (vector)	120 GeV	21 GeV
HSL	200 GeV	0 (scalar)	5 GeV	1250 GeV
HVL	200 GeV	1 (vector)	5 GeV	1250 GeV
HSH	200 GeV	0 (scalar)	120 GeV	332.4 GeV
HVH	200 GeV	1 (vector)	120 GeV	511.8 GeV

→ light mediator

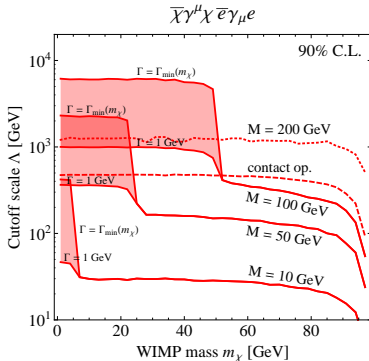
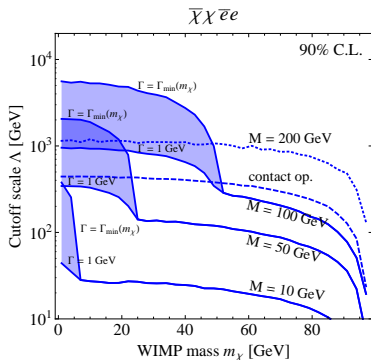
⇒ full momentum dependence in propagator required

→  $M_*$  used as effective coupling constant

Technical setup:

- Event Simulation: MadGraph/MadEvent 4.5.1
- Mediator width: BRIDGE  
(width small:  $< 1$  GeV)

$M_*$  values for light DSP from [Fox, Harnik, Kopp, Tsai] ( $\Lambda \equiv M_*$ )



for heavy DSP strong constraints from direct detection experiments

→  $e^+e^-$  cross sections too small

↔ DSP stable on collider time scales, but not on astrophysical ones

→ for simplicity: similar c.s. as in light DSP case

- Cuts:  $p_{T,e} > 10 \text{ GeV}$ ,  $|\eta_e| < 2.5$ ,  $p_T > 50 \text{ GeV}$
- Integrated cross sections for ILC,  $\sqrt{s} = 500 \text{ GeV}$ :

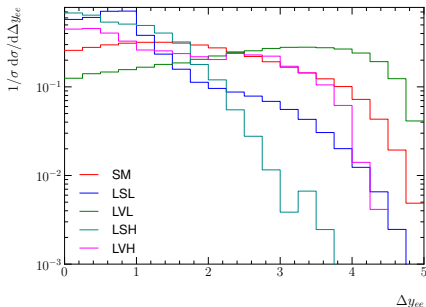
model	cross section in fb		
	unpolarized	++-polarized	+--polarized
SM	115.8	49.1	36.4
LSL	1.60	1.79	1.40
LVL	15.07	12.80	17.02
LSH	1.45	1.80	1.10
LVH	10.00	7.64	12.33
HSL	1.17	1.43	0.92
HVL	0.85	0.71	0.89
HSH	1.18	1.45	0.90
HVH	0.85	0.64	0.98

- Linear collider setup allows beams to be polarized:  
80% for  $e^-$  beam (first index)  
30% for  $e^+$  beam (second index)
- $\rightarrow$  significant background reduction possible  
 $-+$  and  $--$  combinations lead to background enhancement  $\Rightarrow$  not considered
- $\leftrightarrow$  opposite polarization than required for Higgs

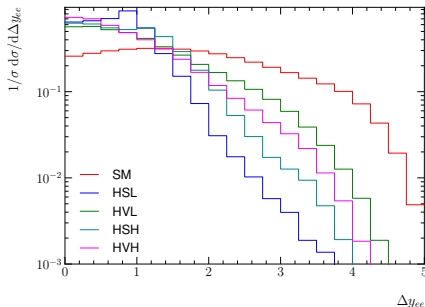
Rapidity difference of the two leptons  $\Delta y_{ee}$

[Andersen, MR, Spannowsky]

Light mediator



Heavy mediator



Clearly distinct shape between different contributions

→ Explanation?

- (non-relativistic part) developed by T. Regge in 1957
- analytic behaviour of scattering amplitudes as function of angular momentum
- angular momentum can be any complex value

$$A(z) \propto z^{\ell(E^2)} \quad z \gg 1$$

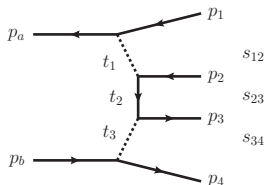
- relativistic:  $z \gg 1 \rightarrow$  large momentum transfer  $t$
- apply to crossed channel  $s \leftrightarrow t$

[Mandelstam]

$$A \propto s^{\ell(t)} \quad s \gg |t|$$

- Theory of strong interactions in 1960's
- $\rightarrow$  largely replaced by QCD nowadays
  
- $\rightarrow$  phenomenological tool for large-energy scattering





Multi-Regge kinematic limit:

invariant mass between final-state particles large compared to propagating momentum and masses

$$s_{ij} \gg |t_i|, m_{\phi, \chi}$$

⇒ VBF cuts

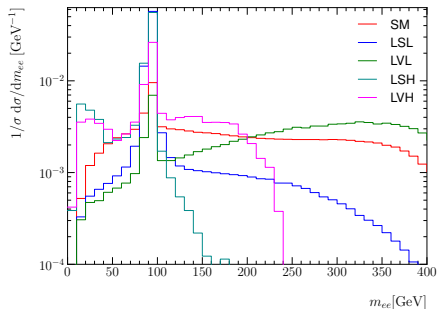
$$\mathcal{M}^{p_a p_b \rightarrow p_1 p_2 p_3 p_4} \rightarrow s_{12}^{\alpha_1(t_1)} s_{23}^{\alpha_2(t_2)} s_{34}^{\alpha_3(t_3)} \gamma$$

- $p_1, \dots, p_4$  rapidity-ordered
- $\gamma = \gamma(\text{couplings}, t_i, \frac{s_{ij}}{\prod s_{kl}})$
- $\alpha_j = \text{spin } J_j \text{ of } t\text{-channel particle } i \text{ (+ radiative corrections)}$
- Remember:  $s_{ij} = 2 p_{T,i} p_{T,j} (\cosh(y_i - y_j) - \cos(\phi_i - \phi_j))$

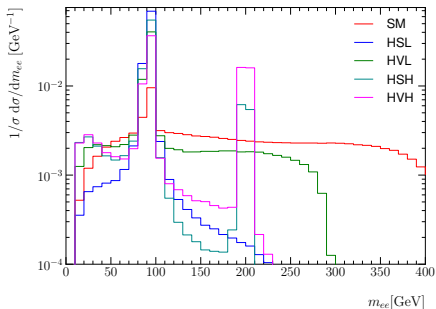
⇒ If messenger masses negligible  
distinguish messenger spin by looking at  $m_{ee}$  or  $\Delta\phi_{jj}$

## Invariant mass of the two leptons $m_{ee}$

### Light mediator



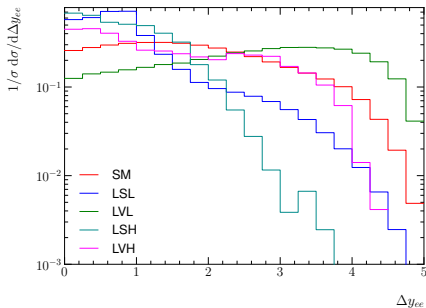
### Heavy mediator



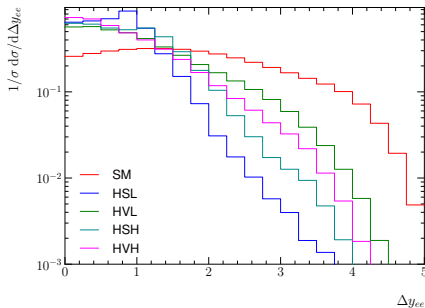
- Light mediator (L●●)  
scalar (LS●) suppressed compared to vector exchange (LV●) at large  $m_{ee}$
- Heavy mediator (H●●)  
impact of mass significant for fixed DSP mass

Rapidity difference of the two leptons  $\Delta y_{ee}$

Light mediator



Heavy mediator



- Light mediator (L●●)
    - scalar (LS●) suppressed compared to vector exchange (LV●) at large  $\Delta y_{ee}$
  - Heavy mediator (H●●)
    - vector-scalar hierarchy at large  $\Delta y_{ee}$  still holds despite heavy mass
- ⇒ Polarised beams and vector mediator: S/B  $\sim$  27% at large  $\Delta y$

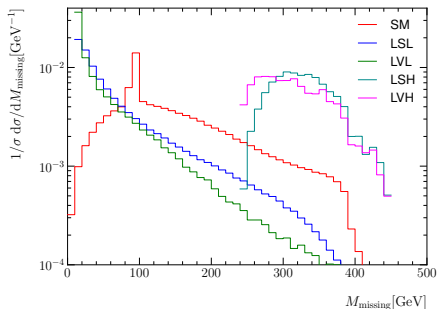
# Differential Distributions (cont.)

Invariant mass of missing momentum  $M_{\text{missing}}$

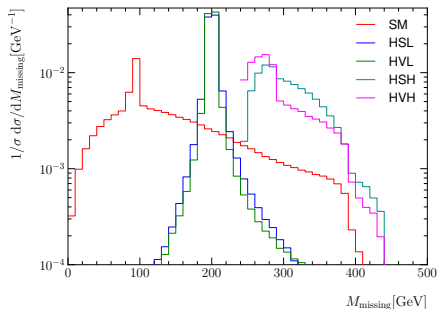
(lower bound:  $2 \cdot \text{DSP mass}$ )

[see also Chacko, Cui, Hong]

Light mediator



Heavy mediator

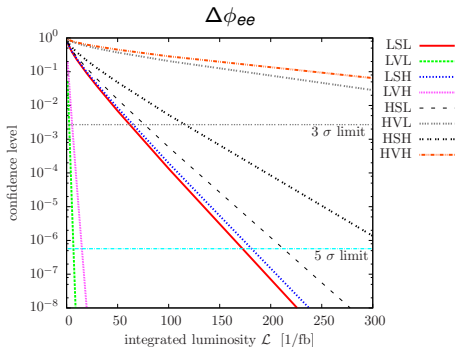
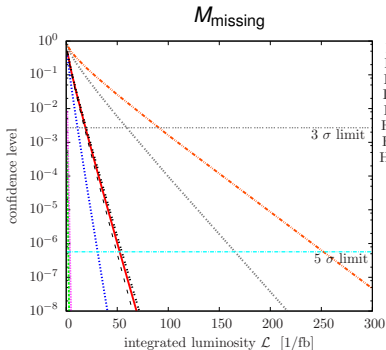


- No distinction of scalar/vector mediator
- Pronounced peak if  $m_\phi > 2m_\chi$  (H•L, on-shell mediator production)
- allows mass distinction  
→ complementary to  $m_{ee}$ ,  $\Delta y_{ee}$
- for CP-even vs. CP-odd coupling study  $\Delta\phi_{ee}$  in addition

# Excluding Models

Binned log-likelihood hypothesis test with  $CL_S$  method

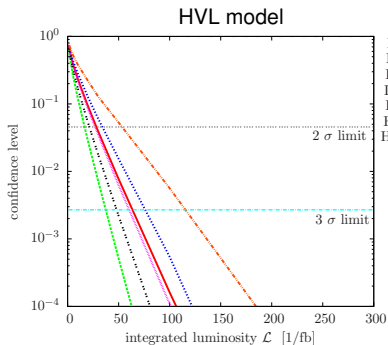
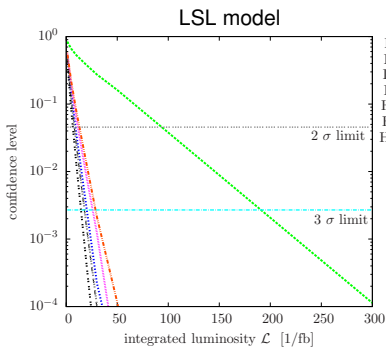
ILC,  $\sqrt{S} = 500$  GeV,  $+-$  beam polarization



- Single variable test only
- LVL, LVH large c.s.  $\rightarrow$  5 $\sigma$ -excluded with 10 fb<sup>-1</sup>
- 300 fb<sup>-1</sup> sufficient for all considered scenarios

## Binned log-likelihood hypothesis test with $CL_S$ method

ILC,  $\sqrt{S} = 500$  GeV,  $+-$  beam polarization,  $\sigma = 2.5\% \times \sigma_{SM}$  bkgd.



- Single variable test only
- Good prospects for distinguishing scenarios

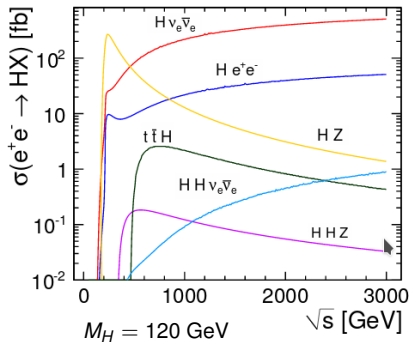
No detailed studies yet – [work for the future](#)

## ■ discovery reach

- biggest improvements from collider data for low-DM-mass regime
- → collider center-of-mass energy less relevant
- ↔ improved precision for vector DM

## ■ property determination

- from vector-boson-fusion process
- → higher energy beneficial
- → better signal-background separation
- → increased significance



[CLIC Conceptual Design Report]

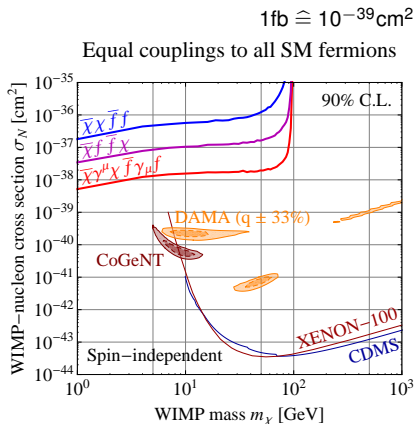
- **mono-photon** searches helpful for **discovering** dark sector
- competitive in particular in low-mass region
  
- not well suited for studying **properties**  
→ **VBF-like** topologies
- VBF cross sections grows with energy
- polarized beams help further in SM background suppression
  
- differing distributions allow distinction
  - $M_{\text{missing}}$ : mass scale and hierarchies of mediator and DSP
  - $m_{ee}$  and  $\Delta y_{ee}$ : mediator spin
- latter explained by multi-Regge kinematic limit

→ CLIC ideal collider for studying dark sector



## Collider searches: LEP

- detection in mono-photon searches  
 $e^+e^- \rightarrow \gamma + \cancel{E}_T$
- no official results  
only theorists' reinterpretation of mono-photon searches  
[Fox, Harnik, Kopp, Tsai]
- high sensitivity in low-mass region
- superseded by LHC results  
if  $\chi$  couples to all fermions
- still competitive  
if  $\chi$  couples to leptons only



Collider searches: LEP

- detection in mono-photon searches  
 $e^+e^- \rightarrow \gamma + \cancel{E}_T$

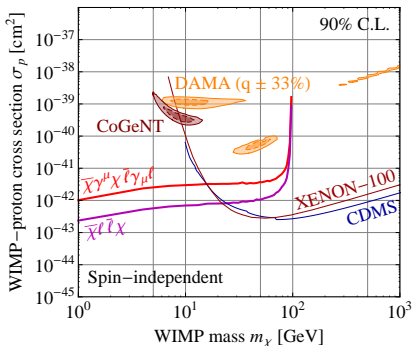
- no official results  
only theorists' reinterpretation of mono-photon searches

[Fox, Harnik, Kopp, Tsai]

- high sensitivity in low-mass region
- superseded by LHC results if  $\chi$  couples to all fermions
- still competitive if  $\chi$  couples to leptons only

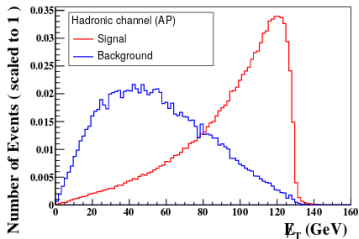
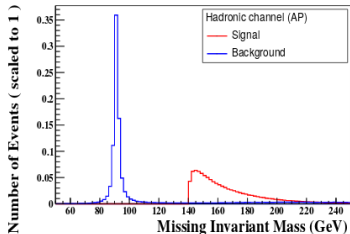
$$1\text{fb} \hat{=} 10^{-39}\text{cm}^2$$

Couplings to leptons only



# Another useful variable

[Chacko, Cui, Hong]



- studied scenario:  
Higgs portal with  $m_{DM} > m_H/2$
- here:  $m_{DM} = 70$  GeV,  $\sqrt{s} = 350$  GeV
- main channel:  
 $ZH$  associated production
- main backgrounds:  
 $ZZ$  production,  $W$ -fusion
- missing invariant mass provides good separation power
- need to know  $\sqrt{s}$   
→ only possible at  $e^+e^-$  collider