

# Lepton flavour violating Higgs decays involving taus

Cédric Weiland

Pitt-PACC, University of Pittsburgh

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# Charged lepton flavour violation (see Adrian's and Ana's talks)

- SM: no  $\nu$  mass term, **lepton number and lepton flavour are conserved**
- Neutrino oscillations = Neutral lepton flavour violation  
What about **charged lepton flavour violation (cLFV)** ?
- Ad-hoc SM extension (Dirac  $m_\nu + U_{\text{PMNS}}$ ): **cLFV** from loop processes  
 $\Rightarrow$  **negligible**, e.g.  $\text{Br}(\mu \rightarrow e\gamma) \sim 10^{-54}$  [Petcov, 1977]
- If cLFV observed:
  - Clear **evidence** of new Physics
  - **Probe** the origin of lepton mixing
  - **Could** tell us more about the origin of neutrino masses and mixing

- Searched for in numerous channels:

Radiative decays

$$\text{Br}(\mu \rightarrow e\gamma) < 4.2 \times 10^{-13} \text{ [MEG, 2016]}$$

3-body decays

$$\text{Br}(\tau \rightarrow 3\mu) < 2.1 \times 10^{-8} \text{ [Belle, 2010]}$$

Meson decays

$$\text{Br}(B^0 \rightarrow e\mu) < 1.0 \times 10^{-9} \text{ [LHCb, 2017]}$$

Z decays

$$\text{Br}(Z^0 \rightarrow e\mu) < 7.5 \times 10^{-7} \text{ [ATLAS, 2014]}$$

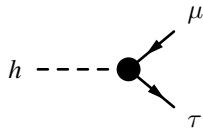
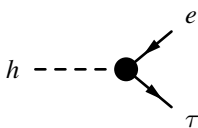
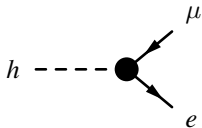
Neutrinoless muon conversion

$$\mu^-, \text{Au} \rightarrow e^-, \text{Au} < 7 \times 10^{-13} \text{ [SINDRUM II, 2006]}$$



# Many sources of cLFV Higgs decays

- Higgs discovery allows to search for cLFV in the scalar sector



- Many models give rise to cLFV Higgs decays

## Tree-level:

**general 2HDM** [Diaz-Cruz and Toscano, 2000; Han and Marfatia, 2001; Kanemura *et al.*, 2006; Dorsner *et al.*, 2015 ...]

**3HDM** [Campos *et al.*, 2015; Crivellin *et al.*, 2015; Merchand and Sher, 2017]

**Warped extra-dim / Composite Higgs** [Azatov *et al.*, 2009; de Lima *et al.*, 2015]

**RPV SUSY** [Arhrib *et al.*, 2013; Huang and Tang, 2015; ... ]

**Froggatt-Nielsen** [Huitu *et al.*, 2016; Barradas-Guevara *et al.*, 2017; ... ]

## Loop induced:

**low-scale seesaw models** [Pilaftsis, 1992; Arganda, Herrero, Marcano and CW, 2015; Herrero-Garcia *et al.*, 2016; Thao *et al.*, 2017; ...]

**MSSM** [Diaz-Cruz, 2002; Brignole and Rossi, 2003; Arana-Catania *et al.*, 2013; Aloni *et al.*, 2016; Alvarado *et al.*, 2016; Gomez *et al.*, 2017; ... ]

**SUSY seesaw** Arganda *et al.*, 2005; Diaz-Cruz *et al.*, 2009, Arganda, Herrero, Marcano and CW, 2016... ]

**Leptoquarks** [Dorsner *et al.*, 2015; de Medeiros Varzielas and Hiller, 2015; Cheung *et al.*, 2016 ...]

**Vector-like fermions** [Falkowski *et al.*, 2014; Dorsner *et al.*, 2015; Chen and Nomura, 2016 ...]

# EFT as a generic description (see Adrian's talk)

- Effects of particles heavier than the process energy scale described by effective operators, e.g. for cLFV radiative decays

$$\hat{\mathcal{O}}^{\mathcal{D}} = \frac{C^{\mathcal{D}}}{\Lambda_{\text{NP}}^2} \bar{L} H \sigma^{\mu\nu} e_R B_{\mu\nu}$$

- For cLFV Higgs decays, **dominant contribution from** [Herrero-Garcia et al., 2016]

$$\hat{\mathcal{O}}^{\mathcal{Y}} = \frac{C^{\mathcal{Y}}}{\Lambda_{\text{NP}}^2} \bar{L} H e_R (H^\dagger H)$$

giving after EWSB non-diagonal Higgs interactions

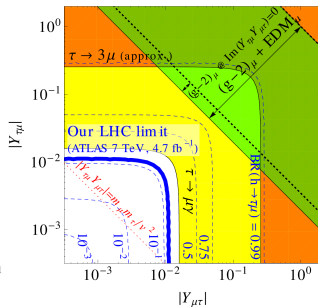
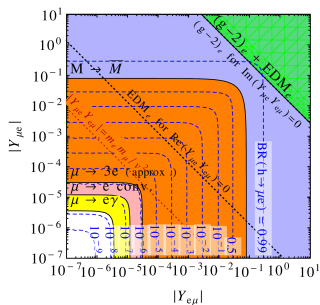
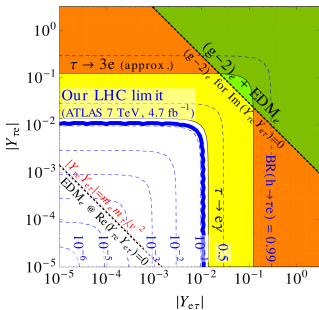
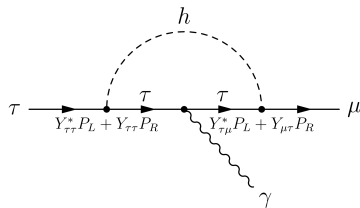
$$-\mathcal{L}^{\mathcal{Y}} = m_i \bar{\ell}_L^i \ell_R^i + Y_{ij} \bar{\ell}_L^i \ell_R^j h + \text{h.c.} \quad \rightarrow \quad Y_{ij} = \frac{m_i}{v} \delta_{ij} + \frac{v^2}{\sqrt{2} \Lambda_{\text{NP}}^2} C_{ij}^{\mathcal{Y}}$$

- **cLFV Higgs decays** governed by the effective Yukawa coupling  $Y_{ij}$



# Indirect constraints on $Y_{ij}$

- $Y_{ij}$  contributes to [Harnik et al., 2013]
  - cLFV lepton decays
  - electron EDM
  - electron and muon g-2



- Good prospects for direct searches of cLFV Higgs decays into  $\tau$   
(See talks by Brian Le and Jian Wang for recent experimental results)

# Future sensitivities

- Current upper limits at 95% C.L [Aad et al., 2017, Sirunyan et al., 2018]

	ATLAS	CMS
$\text{Br}(h \rightarrow \tau\mu)$	1.41% (8 TeV)	0.25% (13 TeV)
$\text{Br}(h \rightarrow \tau e)$	1.04% (8 TeV)	0.61% (13 TeV)

- HL-LHC sensitivities with  $3 \text{ ab}^{-1}$ , 10% systematics, at 95% C.L [Banerjee et al., 2016]

	$e\mu + \cancel{E}_T$
$\text{Br}(h \rightarrow \tau\mu)$	0.76%
$\text{Br}(h \rightarrow \tau e)$	0.61%

- ILC sensitivities at 95% C.L,  $HZ$  and  $VBF$  production channels [Banerjee et al., 2016]

	250 GeV, $250 \text{ fb}^{-1}$	1 TeV, $1 \text{ ab}^{-1}$
$\text{Br}(h \rightarrow \tau e)$	0.38%	0.22%

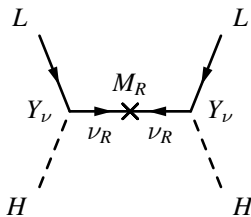
Expect similar results for  $h \rightarrow \tau\mu$

- ILC sensitivity, assuming negligible background,  $HZ$  and  $VBF$  production channels, polarized beams (-0.8,0.3) [Chakraborty et al., 2016]:

	250 GeV, $1350 \text{ fb}^{-1}$
$\text{Br}(h \rightarrow \tau\mu)$	0.0041%



## 2 examples based on low-scale seesaw models



- Taking  $M_R \gg m_D$  gives the “vanilla” type 1 seesaw

$$m_\nu = -m_D M_R^{-1} m_D^T, \text{ where } m_D = Y_\nu v$$

$$m_\nu \sim 0.1 \text{ eV} \Rightarrow \begin{cases} Y_\nu \sim 1 & \text{and } M_R \sim 10^{14} \text{ GeV} \\ Y_\nu \sim 10^{-6} & \text{and } M_R \sim 10^2 \text{ GeV} \end{cases}$$

- $m_\nu$  suppressed by small active-sterile mixing  $m_D/M_R$
- Problem:  $m_D/M_R$  also controls the heavy neutrinos phenomenology  
Solution: **Cancellation** in matrix product to get large  $m_D/M_R$
- Theorem:  $m_\nu = 0 \Leftrightarrow$  **Conserved lepton number L**  
[Kersten and Smirnov, 2007; Moffat, Pascoli, CW, 2017]  
Consequence: Large  $m_D/M_R$  in presence of nearly conserved L symmetry
- Examples: the inverse seesaw and its SUSY realisation



# An example: the inverse seesaw model

- Lower seesaw scale from approximately conserved lepton number
- Add **fermionic gauge singlets**  $\nu_R$  ( $L = +1$ ) and  $X$  ( $L = -1$ )

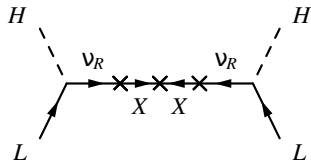
[Mohapatra and Valle, 1986, Bernabéu et al., 1987]

$$\mathcal{L}_{inverse} = -Y_\nu \bar{L} \tilde{\phi} \nu_R - M_R \bar{\nu}_R^c X - \frac{1}{2} \mu_X \bar{X}^c X + \text{h.c.}$$

$$\text{with } m_D = Y_\nu v, M^V = \begin{pmatrix} 0 & m_D & 0 \\ m_D^T & 0 & M_R \\ 0 & M_R^T & \mu_X \end{pmatrix}$$

$$m_\nu \approx \frac{m_D^2}{M_R^2} \mu_X$$

$$m_{N_1, N_2} \approx \mp M_R + \frac{\mu_X}{2}$$



2 scales:  $\mu_X$  and  $M_R$

- **Decouple** neutrino mass generation from active-sterile mixing
- Inverse seesaw:  $Y_\nu \sim \mathcal{O}(1)$  and  $M_R \sim 1 \text{ TeV}$   
 $\Rightarrow$  **within reach of the LHC and low energy experiments**

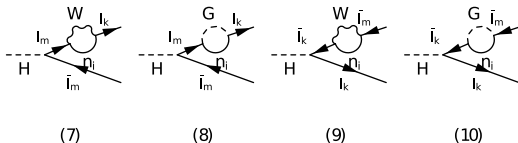
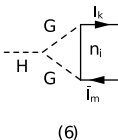
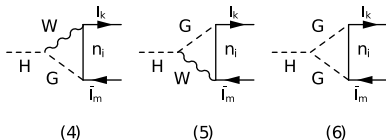
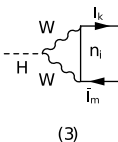
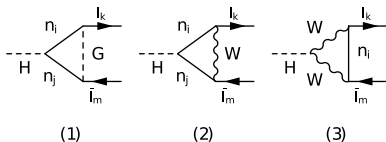




## Diagrams for the ISS

(PRD91(2015)015001)

- In the Feynman-'t Hooft gauge,  
same as type I seesaw [Arganda et al., 2005]:



- Formulas adapted from [Arganda et al., 2005]
- Diagrams 1, 8, 10 **dominate** at large  $M_R$
- Enhancement** from:
  - $-\mathcal{O}(1) Y_\nu$  couplings
  - TeV scale  $n_i$



# Most relevant constraints

- Neutrino data → Use **specific parametrization** (modified Casas-Ibarra (C-I) [Casas and Ibarra, 2001] or  $\mu_X$  parametrization)

$$\nu Y_\nu^T = V^\dagger \text{diag}(\sqrt{M_1}, \sqrt{M_2}, \sqrt{M_3}) R \text{diag}(\sqrt{m_1}, \sqrt{m_2}, \sqrt{m_3}) U_{PMNS}^\dagger$$

$$M = M_R \mu_X^{-1} M_R^T$$

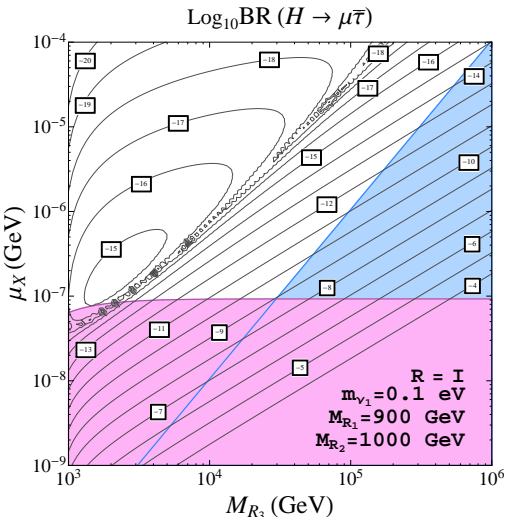
or

$$\mu_X = M_R^T Y_\nu^{-1} U_{PMNS}^* \text{diag}(\sqrt{m_1}, \sqrt{m_2}, \sqrt{m_3}) U_{PMNS}^\dagger Y_\nu^{T-1} M_R \nu^2$$

- Charged lepton flavour violation  
→ For example:  $\text{Br}(\mu \rightarrow e\gamma) < 4.2 \times 10^{-13}$  [MEG, 2016]
- Lepton universality violation: less constraining than  $\mu \rightarrow e\gamma$
- Electric dipole moment: **0** with **real** PMNS and mass matrices
- Invisible Higgs decays:  $M_R > m_H$ , **does not apply**
- Yukawa perturbativity:  $|\frac{y_\nu^2}{4\pi}| < 1.5$



# Predictions using the modified C-I parametrization



- Grows with  $M_{R_3}$  and  $\mu_X^{-1}$  due to  $Y_\nu$  growth in C-I parametrization
- Different dependence on parameters for cLFV Higgs decays and cLFV radiative decays
- Similar behaviour with degenerate heavy neutrinos
- Excluded by  $\mu \rightarrow e\gamma$   
Non-perturbative  $Y_\nu$
- $\text{Br}(H \rightarrow \bar{\tau}\mu) \leq 10^{-9}$



# Large cLFV Higgs decay rates from textures

- Possibility to evade the  $\mu \rightarrow e\gamma$  constraint ?
- Approximate formulas for large  $Y_\nu$ :

$$\text{Br}_{\mu \rightarrow e\gamma}^{\text{approx}} = 8 \times 10^{-17} \text{GeV}^{-4} \frac{m_\mu^5}{\Gamma_\mu} \left| \frac{v^2}{2M_R^2} (Y_\nu Y_\nu^\dagger)_{12} \right|^2$$

$$\text{Br}_{H \rightarrow \mu\bar{\tau}}^{\text{approx}} = 10^{-7} \frac{v^4}{M_R^4} \left| (Y_\nu Y_\nu^\dagger)_{23} - 5.7 (Y_\nu Y_\nu^\dagger Y_\nu Y_\nu^\dagger)_{23} \right|^2$$

$$\stackrel{(Y_\nu Y_\nu^\dagger)_{12}=0}{=} 10^{-7} \frac{v^4}{M_R^4} \left| 1 - 5.7 [(Y_\nu Y_\nu^\dagger)_{22} + (Y_\nu Y_\nu^\dagger)_{33}] \right|^2 |(Y_\nu Y_\nu^\dagger)_{23}|^2$$

→ **Different dependence** on the seesaw parameters

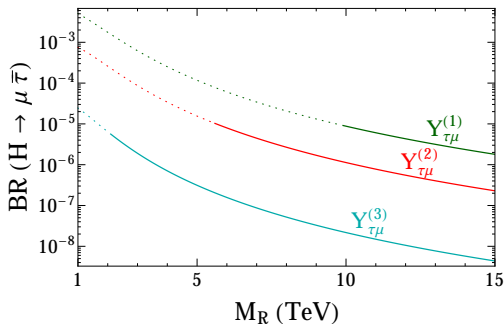
- Solution: **Textures with  $(Y_\nu Y_\nu^\dagger)_{12} = 0$**  and  $\frac{|Y_\nu^{ij}|^2}{4\pi} < 1.5$

- Examples:

$$Y_{\tau\mu}^{(1)} = f \begin{pmatrix} 0 & 1 & -1 \\ 0.9 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix}, \quad Y_{\tau\mu}^{(2)} = f \begin{pmatrix} 0 & 1 & 1 \\ 1 & 1 & -1 \\ -1 & 1 & -1 \end{pmatrix}, \quad Y_{\tau\mu}^{(3)} = f \begin{pmatrix} 0 & -1 & 1 \\ -1 & 1 & 1 \\ 0.8 & 0.5 & 0.5 \end{pmatrix}$$



# Producing large $H \rightarrow \tau\mu$ rates



- Numerics done with the full one-loop formulas
- Dotted: excluded by  $\tau \rightarrow \mu\gamma$   
Solid: allowed by cLFV, LUV, etc
- $\text{Br}^{\max}(H \rightarrow \mu\bar{\tau}) \sim 10^{-5}$
- Same maximum branching ratio with hierarchical heavy N
- Similarly,  $\text{Br}^{\max}(H \rightarrow e\bar{\tau}) \sim 10^{-5}$  for  $Y_{\tau e}^{(i)}$  ( $=Y_{\tau\mu}^{(i)}$  with rows 1 and 2 exchanged)
- Out of LHC reach,  $\text{Br}^{\max}$  directly proportional to  $\tau \rightarrow \begin{cases} \mu\gamma \\ e\gamma \end{cases}$   
 $\Rightarrow$  Observation at the LHC could exclude inverse seesaw



# The supersymmetric inverse seesaw model

- MSSM extended by singlet chiral superfields  $\widehat{N}$  and  $\widehat{X}$  with  $L = -1$  and  $L = +1$
- Defined by the superpotential:

$$\mathcal{W} = W_{MSSM} + Y_\nu \widehat{N} \widehat{L} \widehat{H}_u + M_R \widehat{N} \widehat{X} + \frac{1}{2} \mu_X \widehat{X} \widehat{X}$$

- **New couplings**, e.g.

$$A_{Y_\nu} Y_\nu \widetilde{N} \widetilde{L} H_u + \text{h.c.}$$

- **Light** right-handed sneutrinos:

$$M_N^2 = m_N^2 + M_R^2 + Y_\nu Y_\nu^\dagger v_u^2 \sim (1\text{TeV})^2$$

⇒ **Natural Yukawa couplings with a TeV new Physics scale**



# cLFV in supersymmetric seesaw models

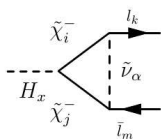
- Typically in SUSY, cLFV through RGE-induced **slepton mixing**  $(\Delta m_{\tilde{L}}^2)_{ij}$   
 [Borzumati and Masiero, 1986, Hisano et al., 1996, Hisano and Nomura, 1999]  
 $\Rightarrow (\Delta m_{\tilde{L}}^2)_{ij} \propto (Y_{\nu}^{\dagger} Y_{\nu})_{ij} \ln \frac{M_{GUT}}{M_R}$
- Contribute to **all cLFV observables**  
 → Dominant in most SUSY seesaw models
- Type I seesaw ( $Y_{\nu} \sim 1$ ,  $M_R \sim 10^{14} \text{GeV}$ ) →  $(\Delta m_{\tilde{L}}^2)_{ij} \propto 5$
- Inverse seesaw ( $Y_{\nu} \sim 1$ ,  $M_R \sim 1 \text{TeV}$ ) →  $(\Delta m_{\tilde{L}}^2)_{ij} \propto 30$   
 → **one-loop  $\tilde{N}$ -mediated processes are no longer suppressed**  
 [Deppisch and Valle, 2005, Hirsch et al., 2010, Abada et al., 2012, Ilakovac et al., 2012, Krauss et al., 2014, Abada et al., 2014]



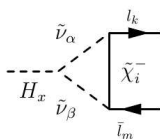
# cLFV Higgs decays from SUSY loops (PRD93(2016)055010)

- In the Feynman-'t Hooft gauge, same as SUSY type I seesaw

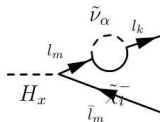
[Arganda et al., 2005]



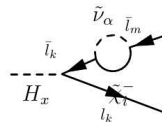
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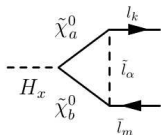
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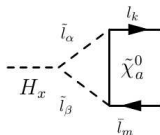
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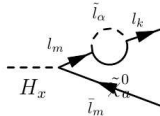
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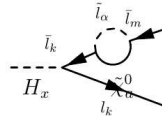
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(6)



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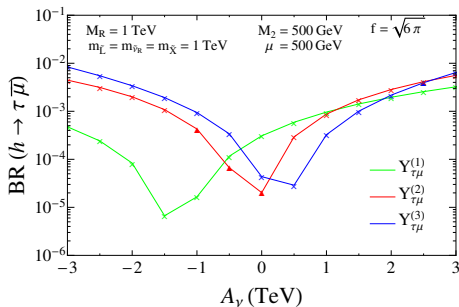
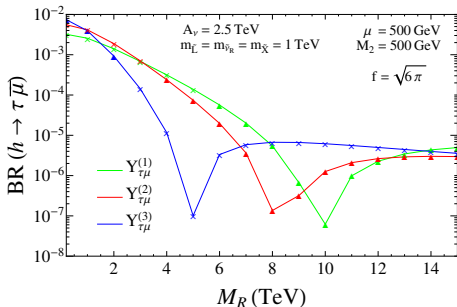
(8)

- Formulas adapted from [Arganda et al., 2005]
- Enhancement** from:  $-\mathcal{O}(1) Y_\nu$  couplings  
-TeV scale  $\tilde{\nu}$





## Results in SUSY ISS



- $M_R$  degenerate and real,  $m_A = 800 \text{ GeV}$ , squark parameters safe from LHC (direct searches, Higgs mass)
- $\blacktriangle$ : allowed by cLFV radiative decays,  $\times$ : excluded
- At low  $M_R$ : dominated by chargino-sneutrino loops  
At large  $M_R$  / small  $f$ : dominated by neutralino-slepton loops
- Can adjust other parameters ( $A_\nu$ ,  $m_{\tilde{\nu}_R}$ ) to reach  $\text{Br}(h \rightarrow \tau \bar{\mu}) \sim 1\%$   
(Dips in  $\text{BR}(h \rightarrow \tau \bar{\mu})$  and  $\text{BR}(\tau \rightarrow \mu \gamma)$  do not exactly coincide)



# Conclusion

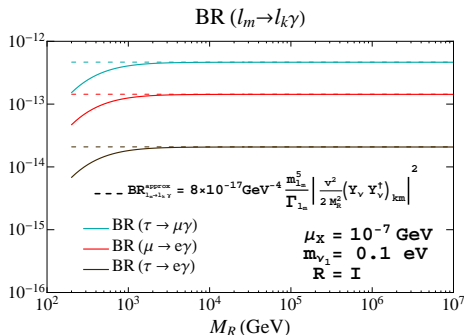
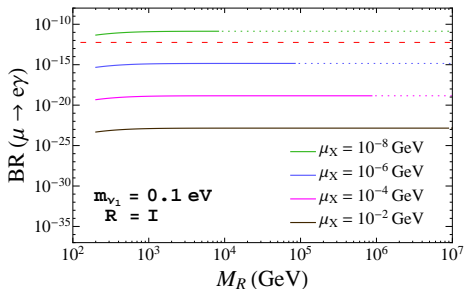
- Observation of cLFV would be a **clear signal of new Physics**
- cLFV Higgs decays: **complementary** to other cLFV searches
- **LHC searches** of cLFV Higgs decays already give the **best constraints in the  $\tau$  sector**
- Many models are **predicting rates within LHC reach**, e.g. general 2HDM, SUSY seesaw, 3HDM, Froggatt-Nielsen, leptoquarks



# Backup slides



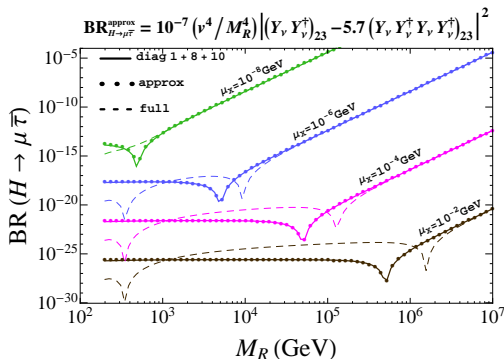
# Constraints: focus on $\mu \rightarrow e\gamma$



- $M_R$  and  $\mu_X$  real and degenerate, Casas-Ibarra (C-I) parametrization
- Constrains  $\mu_X$
- Perturbativity  $\rightarrow \left| \frac{Y_\nu^2}{4\pi} \right| < 1.5$  (Dotted line = non-perturbative couplings)
- $\frac{v^2 (Y_\nu Y_\nu^\dagger)_{km}}{M_R^2} \approx \frac{1}{\mu_X} \frac{(U_{\text{PMNS}} \Delta m^2 U_{\text{PMNS}}^T)_{km}}{2m_{\nu_1}}$



# Dependence on ISS parameters: $\mu_X$ and $M_R$

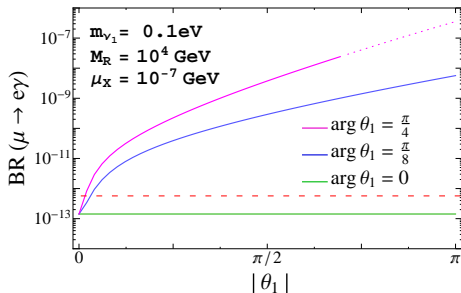
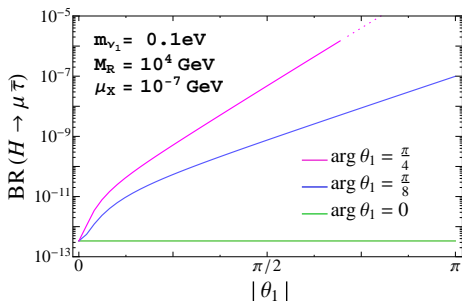


- $R = \mathbb{1}$ ,  $M_R$  and  $\mu_X$  degenerate and real, C-I parametrization
- Dips come from **interferences** between diagrams
- Can be understood using the mass insertion approximation

$$\frac{v^2 (Y_\nu Y_\nu^\dagger)_{km}}{M_R^2} \approx \frac{1}{\mu_X} \frac{(U_{\text{PMNS}} \Delta m^2 U_{\text{PMNS}}^T)_{km}}{2m_{\nu_1}} \quad \text{and} \quad \frac{v^2 (Y_\nu Y_\nu^\dagger Y_\nu Y_\nu^\dagger)_{km}}{M_R^2} = \frac{M_R^2 (U_{\text{PMNS}} \Delta m^2 U_{\text{PMNS}}^T)_{km}}{v^2 \mu_X^2}$$



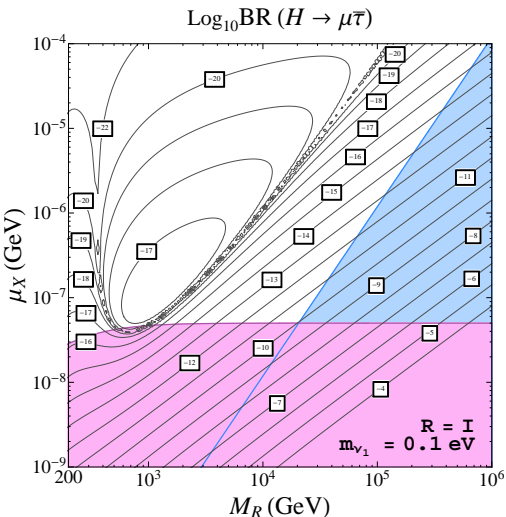
# Dependence on Casas-Ibarra parameters: $R$ matrix



- $M_R$  and  $\mu_X$  degenerate and real
- Independent of  $R$  for real mixing angles
- Increase with complex angles, but increase limited by  $\mu \rightarrow e \gamma$   
 $\Rightarrow$  **Complex  $R$  matrix doesn't change our results**



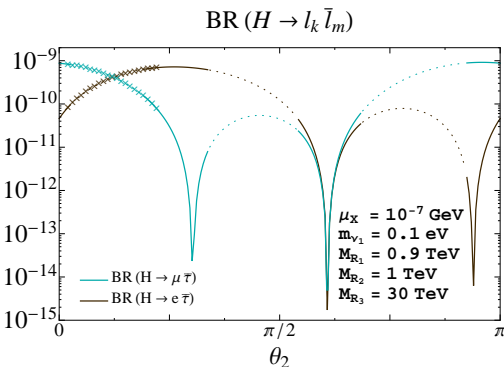
# Searching for maximal $\text{Br}(H \rightarrow \bar{\tau}\mu)$



- $M_R$  and  $\mu_X$  degenerate and real
- Excluded by  $\mu \rightarrow e\gamma$   
Non-perturbative  $Y_\nu$
- $\text{Br}(H \rightarrow \bar{\tau}\mu) \leq 10^{-10}$
- End of the story ?



# Impact of the $R$ matrix for hierarchical N

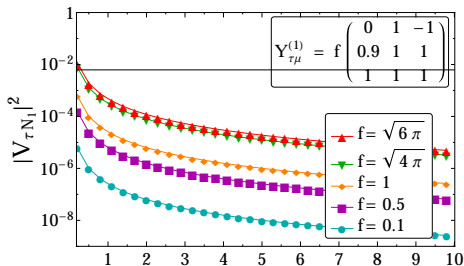
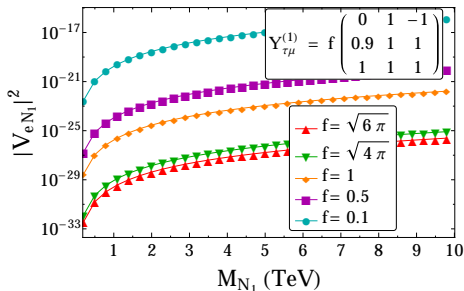


- Contrary to degenerate case,  $R$  dependence
- Varying  $\theta_1$ : Same conclusions as before
- Dotted = non-perturbative couplings  
Cross = Excluded by  $\mu \rightarrow e \gamma$
- $\theta_2 \sim \pi/4$ :  
 $\text{Br}(H \rightarrow e \bar{\tau}) > \text{Br}(H \rightarrow \mu \bar{\tau})$
- Results quite insensitive to  $\theta_3$





# Constraints from EWPO



- Active sterile mixing is controlled by  $\theta \sim m_D M_R^{-1}$
- Large mixing  $\rightarrow$  possible conflict with EWPO
- Limits taken from [del Aguila et al., 2008] at 90% C.L. :

$$|V_{eN}|^2 < 3.0 \times 10^{-3}$$

$$|V_{\mu N}|^2 < 3.2 \times 10^{-3}$$

$$|V_{\tau N}|^2 < 6.2 \times 10^{-3}$$



