Beyond the Standard Model

CERN summer student lectures 2017



Lecture 3/4

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Outline

Monday

O General introductionO Higgs physics as a door to BSM

Tuesday

- 0 Naturalness
- O Supersymmetry

Wednesday

- O Grand unification, proton decay
- O Composite Higgs
- Probing light new force with atomic physics

🗆 Thursday

- O Extra dimensions
- Cosmological relaxation
- Quantum gravity

Grand Unified Theory

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Evolution of coupling constants

Classical physics: the forces depend on distances Quantum physics: the charges depend on distances

QED: virtual particles screen the electric charge: $\alpha \searrow$ when d \nearrow

QCD: virtual particles (quarks and *gluons*) screen the strong charge: $\alpha_{\rm s}$ / when d

'asymptotic freedom'

$$\frac{\partial \alpha_s}{\partial \log E} = \beta(\alpha_s) = \frac{\alpha_s^2}{\pi} \left(-\frac{11N_c}{6} + \frac{N_f}{3} \right)$$

Grand Unified Theories



A single form of matter A single fundamental interaction

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SU(5) GUT: Gauge Group Structure $SU(3)_c \times SU(2)_L \times U(1)_Y$: SM Matter Content $Q_L = \begin{pmatrix} u_L \\ d_L \end{pmatrix} = (3,2)_{1/6}, \quad u_R^c = (\bar{3},1)_{-2/3}, \quad d_R^c = (\bar{3},1)_{1/3}, \quad L = \begin{pmatrix} \nu_L \\ e_L \end{pmatrix} = (1,2)_{-1/2}, \quad e_R^c = (1,1)_1$ How can you ever remember all these numbers? $SU(3)_c x SU(2)_L x U(1)_y \subset SU(5)$ SU(5) $\left(\begin{array}{c|c} SU(2) & \\ \hline & SU(3) \end{array} \right)$ $\left(\begin{array}{c|c} SU(2) & \\ \hline & & \\ \hline & & \\ \end{array} \right)$ Transform $\left(\begin{array}{c|c} SU(2) & \\ \hline & & \\ \end{array} \right)$ $T^{12} = \sqrt{\frac{3}{5}} \begin{pmatrix} 1/2 & \\ \hline & 1/2 & \\ \hline & & \\ \end{array} \right)$ additional U(1) factor that $\bar{5} = (1,2)_{-\frac{1}{2}\sqrt{\frac{3}{5}}} + (\bar{3},1)_{\frac{1}{3}\sqrt{\frac{3}{5}}}$ $T^{12} = \sqrt{\frac{3}{5}}Y$ $g_5\sqrt{\frac{3}{5}} = g'$ $g_5 = g = g_s$ $\overline{5} = L + d_B^c$ $\sin^2 \theta_W = \frac{3}{8} \text{ @ M_{GUT}}$ $g_5 T^{12} = g' Y$ $10 = (5 \times 5)_A = (\bar{3}, 1)_{-\frac{2}{3}\sqrt{\frac{3}{5}}} + (3, 2)_{\frac{1}{6}\sqrt{\frac{3}{5}}} + (1, 1)_{\sqrt{\frac{3}{5}}}$ $10 = u_R^c + Q_L + e_R^c$ 69

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SU(5) GUT: SM β fcts

g, g' and g_s are different but it is a low energy artifact!



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SU(5) GUT: low energy consistency condition

$$\frac{1}{\alpha_i(M_Z)} = \frac{1}{\alpha_{GUT}} - \frac{b_i}{4\pi} \ln \frac{M_{GUT}^2}{M_Z^2} \quad i = SU(3), SU(2), U(1)$$

$$\alpha_3(M_Z), \alpha_2(M_Z), \alpha_1(M_Z) \quad \longleftarrow \text{ experimental inputs}$$

$$b_3, b_2, b_1 \quad \longleftarrow \text{ predicted by the matter content}$$
3 equations & 2 unknowns (α_{GUT}, M_{GUT})

one consistency relation for unification

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one consistency relation for unification

$$M_{GUT} = M_Z \exp\left(2\pi \frac{3\alpha_s(M_Z) - 8\alpha_{em}(M_Z)}{(8b_3 - 3b_2 - 5b_1)\alpha_s(M_Z)\alpha_{em}(M_Z)}\right) \approx 7 \times 10^{14} \text{ GeV}$$

$$\alpha_{GUT}^{-1} = \frac{3b_3\alpha_s(M_Z) - (5b_1 + 3b_2)\alpha_{em}(M_Z)}{(8b_3 - 3b_2 - 5b_1)\alpha_s(M_Z)\alpha_{em}(M_Z)} \approx 41.5$$

self-consistent computation: O $M_{GUT} < M_{PI}$ safe to neglect quantum gravity effects O $\alpha_{GUT} << 1$ perturbative computation

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SU(5) GUT: SM vs MSSM β fcts



$$Q_L = \begin{pmatrix} u_L \\ d_L \end{pmatrix} = (3,2)_{1/6}, \quad U = (\bar{3},1)_{-2/3}, \quad D = (\bar{3},1)_{1/3}, \quad L = \begin{pmatrix} \nu_L \\ e_L \end{pmatrix} = (1,2)_{-1/2}, \quad E = (1,1)_1, \quad H_u = (1,2)_{1/2}, \quad H_d = (1,2)_{-1/2}$$



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SU(5) GUT: MSSM GUT

$$b_3 = 3, \ b_2 = -1, \ b_1 = -33/5$$

low-energy consistency relation for unification

$$\sin^2 \theta_W = \frac{3(b_3 - b_2)}{8b_3 - 3b_2 - 5b_1} + \frac{5(b_2 - b_1)}{8b_3 - 3b_2 - 5b_1} \frac{\alpha_{em}(M_Z)}{\alpha_s(M_Z)} \approx 0.23$$

squarks and sleptons form complete SU(5) reps \rightarrow they don't improve unification! gauginos and higgsinos are improving the unification of gauge couplings

GUT scale predictions

$$M_{GUT} = M_Z \exp\left(2\pi \frac{3\alpha_s(M_Z) - 8\alpha_{em}(M_Z)}{(8b_3 - 3b_2 - 5b_1)\alpha_s(M_Z)\alpha_{em}(M_Z)}\right) \approx 2 \times 10^{16} \text{ GeV}$$

$$\alpha_{GUT}^{-1} = \frac{3b_3\alpha_s(M_Z) - (5b_1 + 3b_2)\alpha_{em}(M_Z)}{(8b_3 - 3b_2 - 5b_1)\alpha_s(M_Z)\alpha_{em}(M_Z)} \approx 24.3$$

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Proton Decay



Babu et al '13

Composite Higgs Models

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Composite Higgs

Light scalars exist in Nature but all the ones observed before the Higgs boson discovery were composite bounds states



Higgs as a bound state



The Higgs discovery would be the first step of rich physics ahead of us: O discover a new SU(N_c) force O access to the fundamental constituents O rich spectrum of bound states

But how come we haven't seen anything of these yet?

⇒ The Higgs has to be lighter than the other bound states
⇒ pions are lighter than nucleons, hadrons and other mesons
⇒ let the Higgs be the pions of the new strong interaction, i.e., the Goldstone boson associated to the breaking of some global symmetry

Higgs as a bound state



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Higgs as a Goldstone boson

SO(4)/SO(3) SMW⁺L & ZL $W^{\pm}_{l} \& Z_{l} \& h$

Examples: SO(5)/SO(4): 4 PGBs=W[±]L, ZL, h Minimal Composite Higgs Model SO(6)/SO(5): 5 PGBs=H, a SO(6)/SO(5): 5 PGBs=H, a SU(4)/Sp(4, C): 5 PGBs=H, s $SO(6)/SO(4) \times SO(2)$: 8 PGBs=H1+H2 Minimal Composite Two Higgs DoubletsMrazek, Pomarol, Rattazzi, Serra, Wulzer '11

How to probe the compositeness of the Higgs?



Need to develop tools to understand the physics of a composite Higgs O use effective theory approach O rely on symmetries of the problem } identify interesting processes

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Anomalous Couplings for a Composite Higgs

Giudice, Grojean, Pomarol, Rattazzi '07

$$\mathcal{L} \supset rac{c_H}{2f^2} \partial^\mu \left(|H|^2
ight) \partial_\mu \left(|H|^2
ight) \qquad c_H \sim \mathcal{O}(1)$$
f=compositeness scale of the Higgs

$$H = \begin{pmatrix} 0 \\ \frac{v+h}{\sqrt{2}} \end{pmatrix} \longrightarrow \mathcal{L} = \frac{1}{2} \left(1 + c_H \frac{v^2}{f^2} \right) (\partial^{\mu} h)^2 + \dots$$

Modified
Higgs propagatorHiggs couplings
rescaled by $\frac{1}{\sqrt{1+c_H\frac{v^2}{f^2}}} \sim 1-c_H\frac{v^2}{2f^2} \equiv 1-\xi/2$

Higgs anomalous coupling: a = $\sqrt{1-\xi} \approx 1-\xi/2$

$$\xi = v^2 / f^2$$

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boson



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Higgs anomalous couplings

$$\mathcal{L}_{\text{EWSB}} = m_W^2 W_\mu^+ W_\mu^+ \left(1 + 2a\frac{h}{v} + b\frac{h^2}{v^2} \right) - m_\psi \bar{\psi}_L \psi_R \left(1 + c\frac{h}{v} \right)$$

The Higgs couplings deviates from SM ones (a=b=c=1) and the deviations are controlled by c_H and c_y

Anomalous couplings are related to the coset symmetry and not the spectrum of resonances

Minimal composite Higgs model (MCHM): SO(5)/SO(4) -





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The other resonances



$Higgs \rightarrow W_{L}W_{L}$ signal hypotheses is found in the mass range to resonances while the excess extends down to $m_{\rm X} = 1.8$ TeV for the $Z_{\rm L}Z_{\rm L}$ sig-

se mass ræreresistore Andirectiseanores (higholumti) vscrotise et csear chies (high energy)

S data favour smaller values ($\approx 3 \text{ fb}$) and are more consistent with the DY production xs of resonances decreases as $1/g_{\rho^2}$ The maximum-likefihood (ML) combinged cross section is essentially



Higgs couplings vs searches for vector resonances

Precision /indirect searches (high lumi.) vs. direct searches (high energy)

• Precision Higgs study:
$$\xi\equiv rac{\delta g}{g}=rac{v}{f}$$

• Direct searches for resonances: $m_{
ho} pprox g_* f$

Collider	Energy	Luminosity	$\xi \ [1\sigma]$
LHC	$14\mathrm{TeV}$	$300{\rm fb}^{-1}$	$6.6 - 11.4 \times 10^{-2}$
LHC	$14\mathrm{TeV}$	$3 \mathrm{ab}^{-1}$	$4 - 10 \times 10^{-2}$
ILC	$250{ m GeV}$	$250{\rm fb}^{-1}$	4878×10^{-3}
	+ 500 GeV	$500\mathrm{fb}^{-1}$	4.0-1.0 × 10
CLIC	$350{ m GeV}$	$500 {\rm fb}^{-1}$	
	+ 1.4 TeV	$1.5\mathrm{ab}^{-1}$	2.2×10^{-3}
	+ 3.0 TeV	$2 \mathrm{ab}^{-1}$	
TLEP	$240{ m GeV}$	$10 \mathrm{ab}^{-1}$	2×10^{-3}
	$+~350{\rm GeV}$	$2.6\mathrm{ab}^{-1}$	2 ~ 10

complementarity:

direct searches win at small couplings

indirect searches probe new territory at large coupling



e.g.

indirect searches at LHC over-perform direct searches for g > 4.5 indirect searches at ILC over-perform direct searches at HL-LHC for g > 2

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The other resonances



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Searching for the top partners



 \blacksquare *tt+jets* is not a background [except for charge mis-ID and fake e⁻]

I the resonant ($t\omega$) invariant mass can be reconstructed



Searching for the top partners



q

 \tilde{B}

h

- $\ell^{\pm} + 6b \text{ final state Aguilar-Saavedra '09}$ $T\bar{T} \rightarrow Ht H\bar{t} \rightarrow HW^{+}b HW^{-}\bar{b} \qquad H \rightarrow b\bar{b}, WW \rightarrow \ell\nu q\bar{q}'$
- $\gamma \gamma$ final state Azatov et al '12 $thbW/thtZ/thth, h \rightarrow \gamma \gamma$
- $\ell^{\pm} + 4b$ final state Vignaroli '12 $pp \rightarrow (\tilde{B} \rightarrow (h \rightarrow bb)b)t + X$





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q

 W_L^-

λ

t

bounds on

charge 2/3 states

from pair production

00000000



19.7 fb⁻¹ (8 TeV)

bounds on charge 2/3 states from pair production



900 1000 1100 1200 1300 1400 1500

X_{5/3} mass [GeV]

800

700

600

650

750

700

800

850

900

950

 $m_{T_{5/2}}$ [GeV]

1000

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Searching for the top partners

bounds on charge 2/3 states from pair production



BSM and Atomic Physics

at the Higgs boson of the determinance is an contributes to the check of the higgs contribu-strate in this letter that isotope s **Firequeistary shifts** We evaluate the Higgs contribu-cannot deviate from **Decret Gtobe Sites** is the the Higgs **State Sites** is the strate of midanture or u, d, stions to the Higgs-to-toms Higgs boson exchange between Coulomb tenteraction Thay sign beyond a filled contributes to toms Higgs boson exchange between Coulomb tenteraction Thay sign beyond a filled contributes to their tree level SM values are as the top of the sound of the real of the sound of the real of the sound of the real of the $\Delta E = h_W^2 \simeq 0.23$ is the sine of the weak miking angle squared. gly suppressed by the +ze $\delta \mathcal{B}_{nlm}^{\text{Higgs}} \overset{\text{While the electron } Z^0 \text{ coupling is } \overline{\text{Im}} \overset{\text{While the electron } Z^0 \text{ coupling } \overline{\text{Im}} \overset{\text{While } 10^{-3-}}{\text{M}} \overset{\text{Higgs}}{\text{M}} \overset{\text{While the electron } Z^0 \text{ coupling } \overline{\text{Im}} \overset{\text{While } 10^{-3-}}{\text{M}} \overset{\text{Higgs}}{\text{M}} \overset{\text{Higgs}}{\text{M}} \overset{\text{While } 10^{-3-}}{\text{M}} \overset{\text{Higgs}}{\text{M}} \overset{\text{Higgs}}{\text{M}} \overset{\text{While } 10^{-3-}}{\text{M}} \overset{\text{Higgs}}{\text{M}} \overset{\text{Higgs}}$ урнаrks dominate in ___ iplings, ${}^{4}\!\!\overline{y}_{n,p}^{\text{SM}} \sim 10^{-3}$. things as saturate wind Higgs bo- are poorly constrained by data in a model independent ouplings tound is the effective here the keter is the sometion of the school is the sometion of the school is the energine of the school is the school of th the atomic number and $y_{n,p}$ therefor they have entsizable deviation to potential table $[20]_{n,p}$ there is the they have $y_{n,p}$ there is the they have $y_{n,p}$ the the form $y_{n,p}$ of the they have $y_{n,p}$ the the form $y_{n,p}$ of the they have $y_{n,p}$ and $y_{n,p}$ the the form $y_{n,p}$ of the they have $y_{n,p}$ and $y_{n,p}$ the the form $y_{n,p}$ of the they have $y_{n,p}$ and $y_{n,p}$ of the form $y_{n,p}$ of the they have $y_{n,p}$ and $y_{n,p}$ of the form $y_{n,p}$ of the f $0.4y_d + 0.75y_s + 2.6 \times 10^{-4}c_g$, gifth (force Q) dample, file \longrightarrow inittle asteening between the $5.5y_d + 0.75y_s + 2.6 \times 10^{-4}c_g$, $ain^{4}\psi(0$ Mypredivientance exprendential including. The g_{c} used to g_{g} to g_{g} be the effective other beaux elements are also also be a significant of the significant of the second of t *G*^{ould}89^b^e used, to degree the effective other heavy elements are also possible [32-35], and [91] which includes the *c*, *b*, Exptrise of the more details of this proposal only a wave (*l* = 0) (*l* = 0) (*l* = 0) *c* = 0 (*l* = 0) *c* = if antly mandify the few [28]. Given by the second and its strength premains in the weater of the second by the se also constrained¹, $\delta c_g \lesssim \mathcal{O}(1)$ [28]. independent) perturbation theory. For the sake of simet c_g in the remainder. Within the remainder within the remainder by the the remainder by the the remainder by the the remainder by the re used wolderectsmewing ongehange) aforces functions. In this limit,

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 $\delta E^{\text{Higgs}} = \langle nlm | V_{\text{Higgs}} | \mathcal{B}(m) \rangle \simeq - \frac{y_e y_A}{2} | \mathcal{B}(0) |^2 \frac{\delta_{l,0}}{2} , \quad (6)$

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The King Plot

W. H. King, J. Opt. Soc. Am. 53, 638 (1963)

- First, define modified IS as $m\delta\nu_{AA'}^i \equiv \delta\nu_{AA'}^i/\mu_{AA'}$
- Measure IS in two transitions. Use transition 1 to set $\delta \langle r^2 \rangle_{AA'} / \mu_{AA'}$ and substitute back into transition 2:

$$m\delta\nu_{AA'}^2 = K_{21} + F_{21}m\delta\nu_{AA'}^1 - AA'H_{21}$$

• Plot $m\delta\nu_{AA'}^1$ vs. $m\delta\nu_{AA'}^2$ along the isotopic chain



Constraining light NP



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