

Hard Probes 2018  
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# Resolving the Partonic Structure of Nuclei through Energy- Frontier eA Scattering



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for the LHeC/FCC-eh Study group, <http://lhec.web.cern.ch/>

## I. Introduction.

## 2. Nuclear PDFs at the LHeC and the FCC-eh:

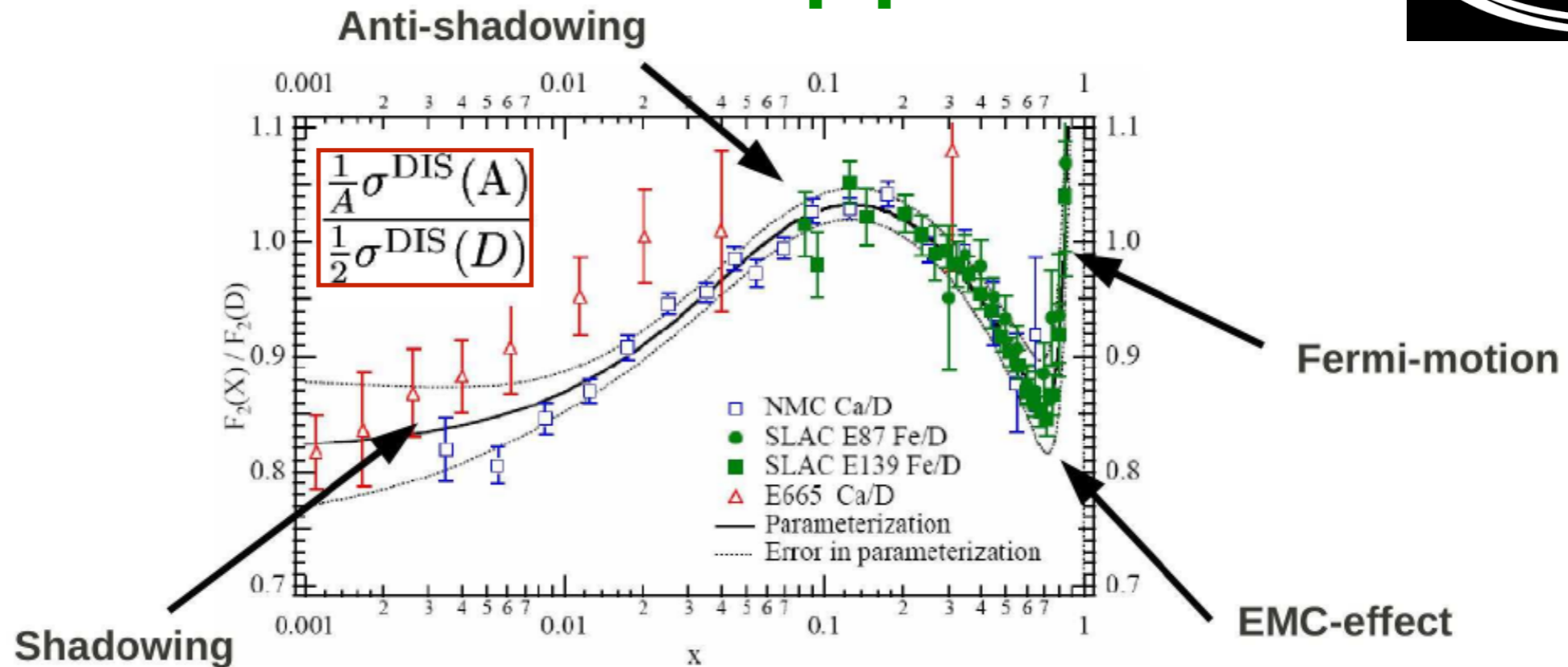
- Pseudodata (M. Klein).
- EPPS16-based analysis (H. Paukkunen, 1709.08342).
- xFitter analysis (P. Agostini, NA).

## 3. Diffractive PDFs at the LHeC and FCC-eh (NA, P. Newman, W. Slominski, A. Stasto):

- Pseudodata.
- Method.
- Results.

## 4. Summary.

See the talks by Hannu Paukkunen, Heikki Mäntysaari, Thomas Peitzmann, Rabah Abdul Khalek, Hyunchul Kim, Amal Sarkar, Jakub Kremer, Ilkka Helenius, Yeonju Go, Petja Paakinen, Aleksander Kusina and Max Klein.  
LHeC/FCC-eh: CDR J. Phys. G39 (2012) 075001, arXiv:1206.2913 [physics.acc-ph]; 2018 workshop, <https://indico.cern.ch/event/698368/>.



- Bound nucleon  $\neq$  free nucleon: search for process independent nPDFs that realise this condition, assuming collinear factorisation.

$$\sigma_{\text{DIS}}^{\ell+A \rightarrow \ell+X} = \sum_{i=q, \bar{q}, g} \underbrace{f_i^A(\mu^2)}_{\text{Nuclear PDFs, obeying the standard DGLAP}} \otimes \underbrace{\hat{\sigma}_{\text{DIS}}^{\ell+i \rightarrow \ell+X}(\mu^2)}_{\text{Usual perturbative coefficient functions}}$$

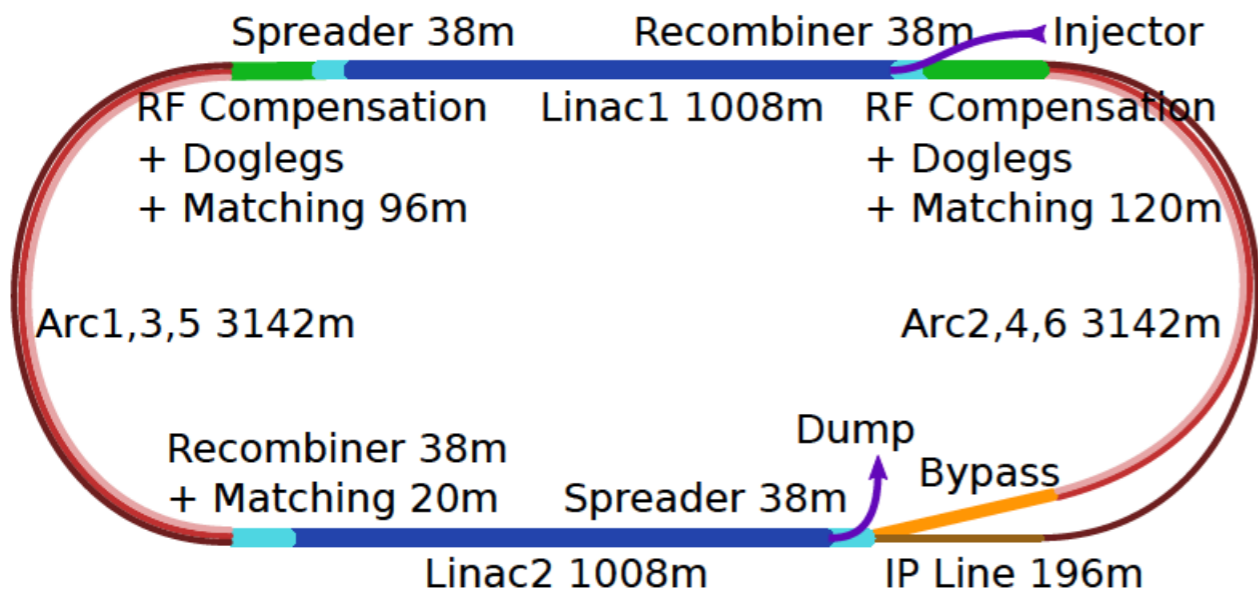
$$f_i^{p,A}(x, Q^2) = R_i^A(x, Q^2) f_i^p(x, Q^2) \quad R = \frac{f_{i/A}}{A f_{i/p}} \approx \frac{\text{measured}}{\text{expected if no nuclear effects}}$$

- At an energy-frontier ep/eA collider:
  - PDFs of a single nucleus possible, no need of ratios that would be obtained a posteriori.
  - Same method of extraction in both ep and eA.
  - Physics beyond standard collinear factorisation can be studied in a single setup, with size effects disentangled from energy effects and a large lever arm in  $x$  at perturbative  $Q^2$ .
- Bound nucleon  $\neq$  free nucleon: search for process independent nPDFs that realise this condition, assuming collinear factorisation.

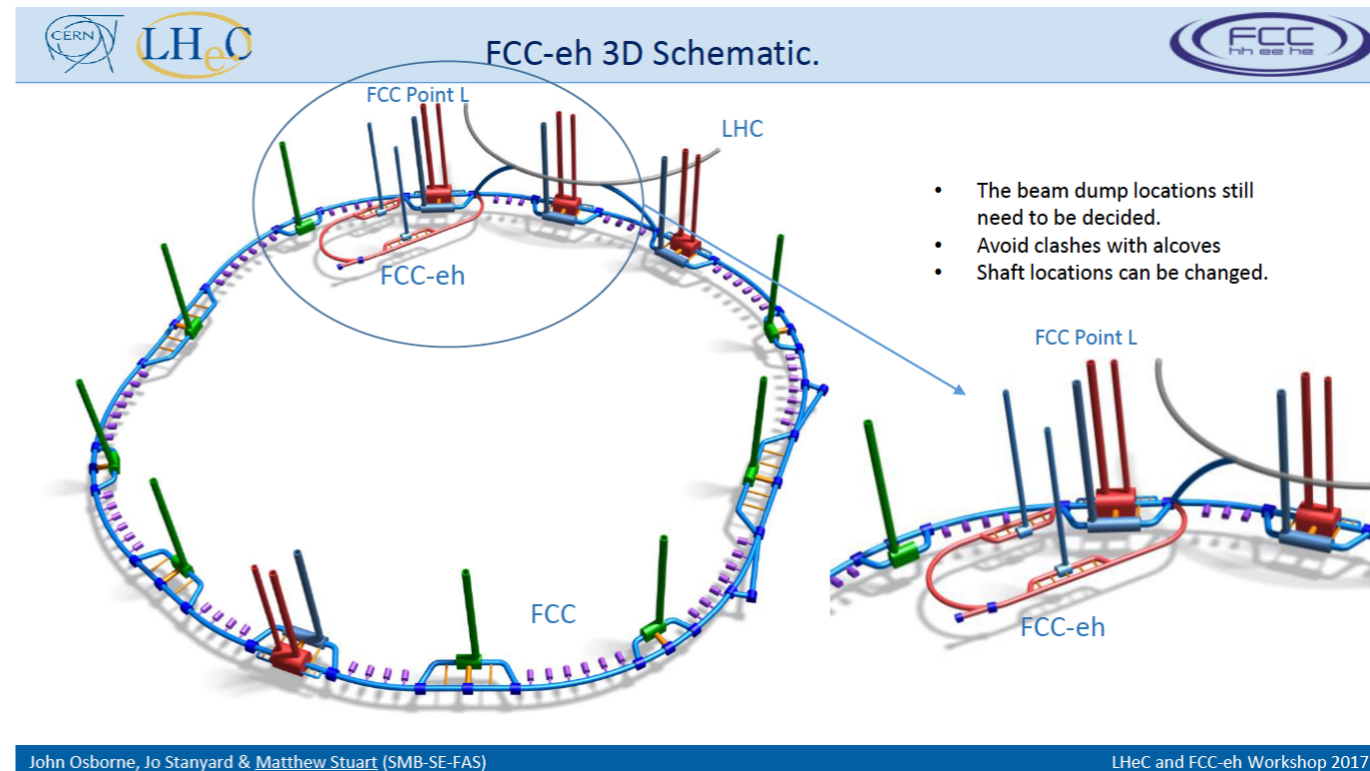
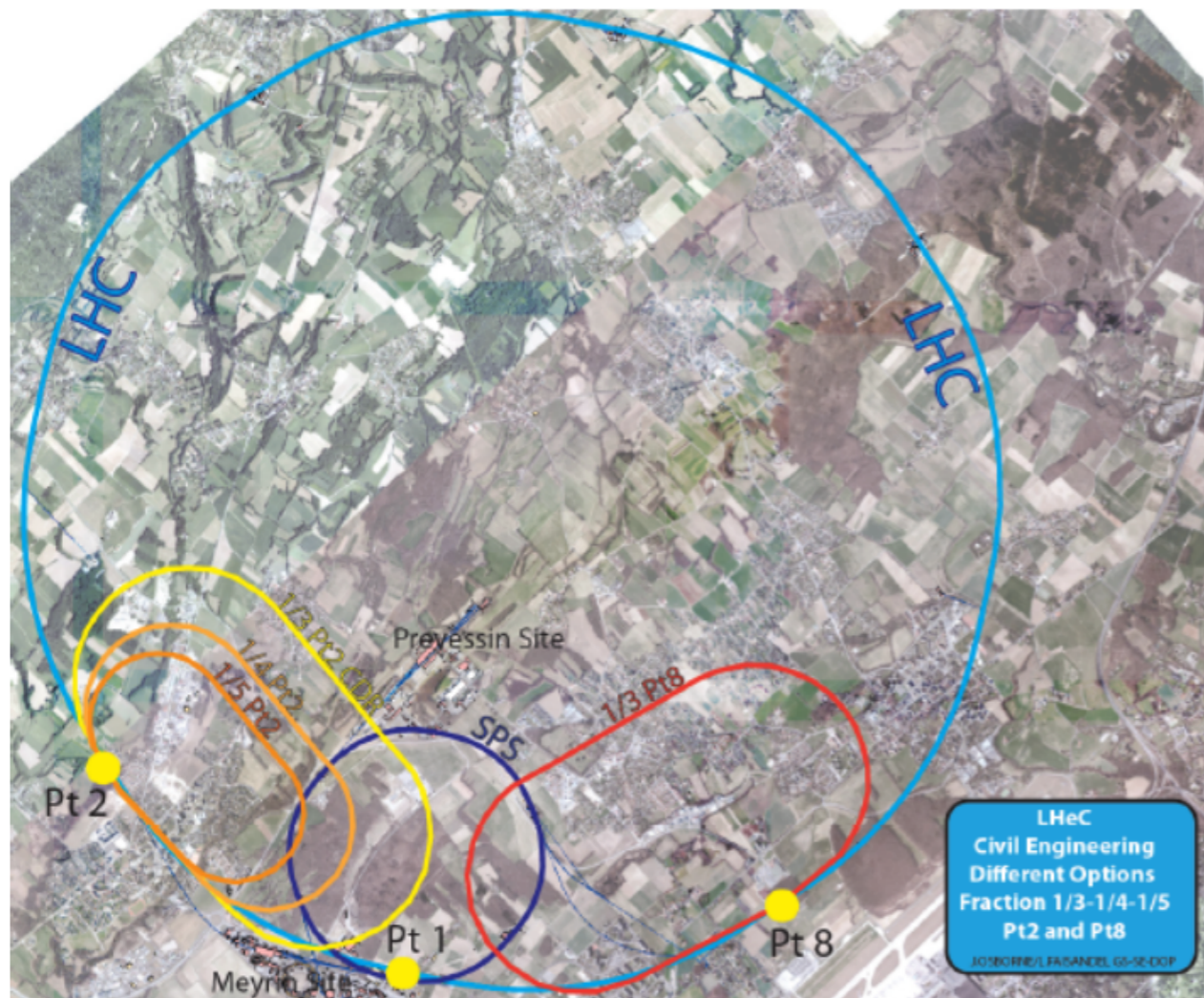
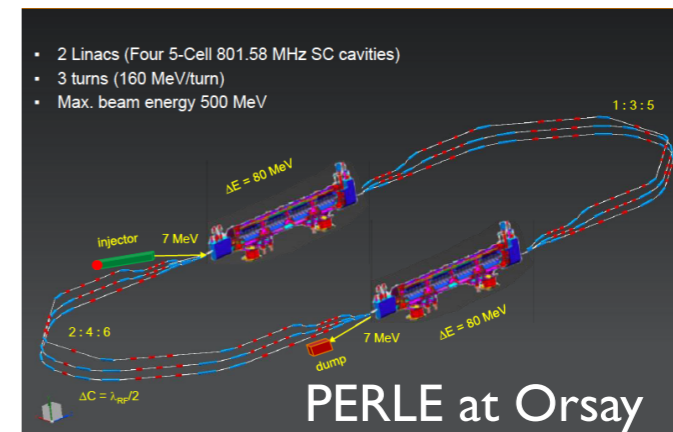
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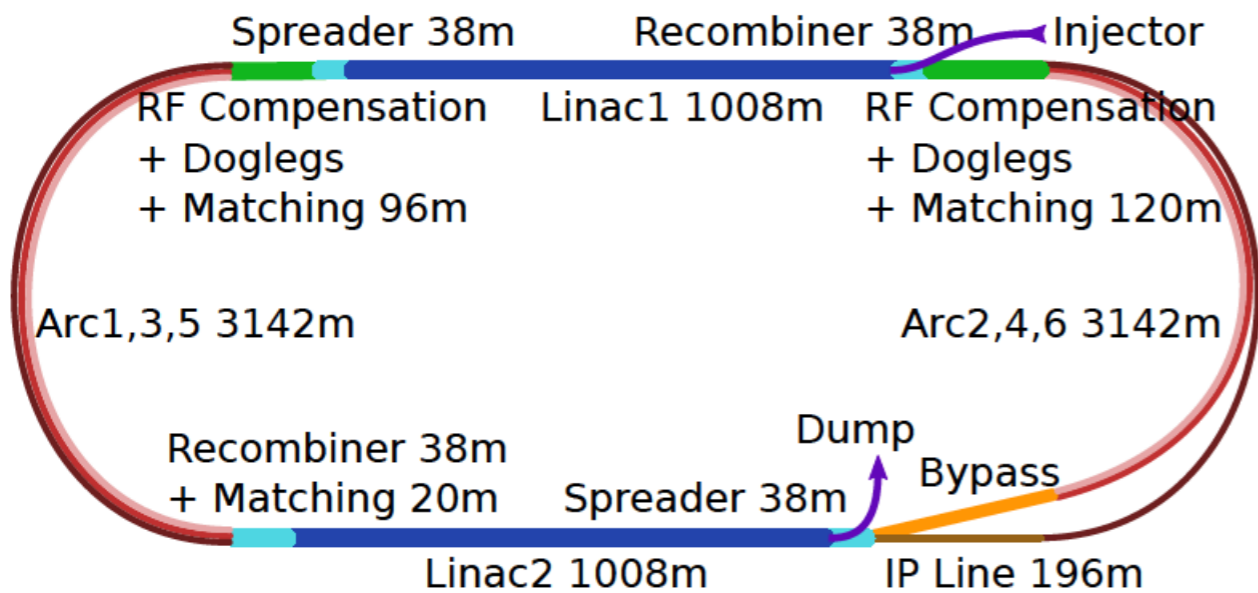
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- 60 GeV e<sup>-</sup> (ERL) against the (HL/HE-)LHC/FCC hadron beams: **eA** to run either concurrently with pA/AA or in dedicated mode.



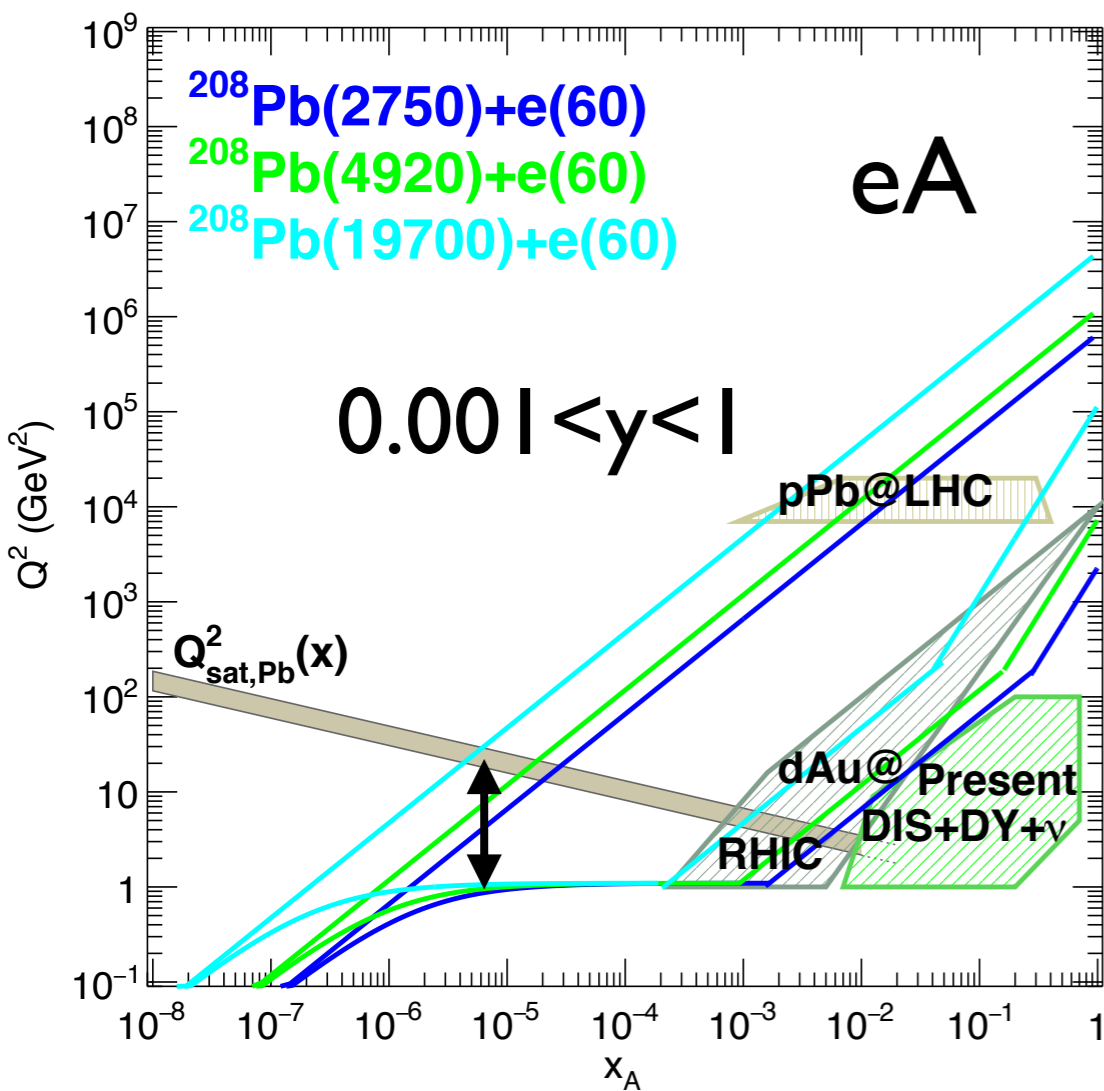


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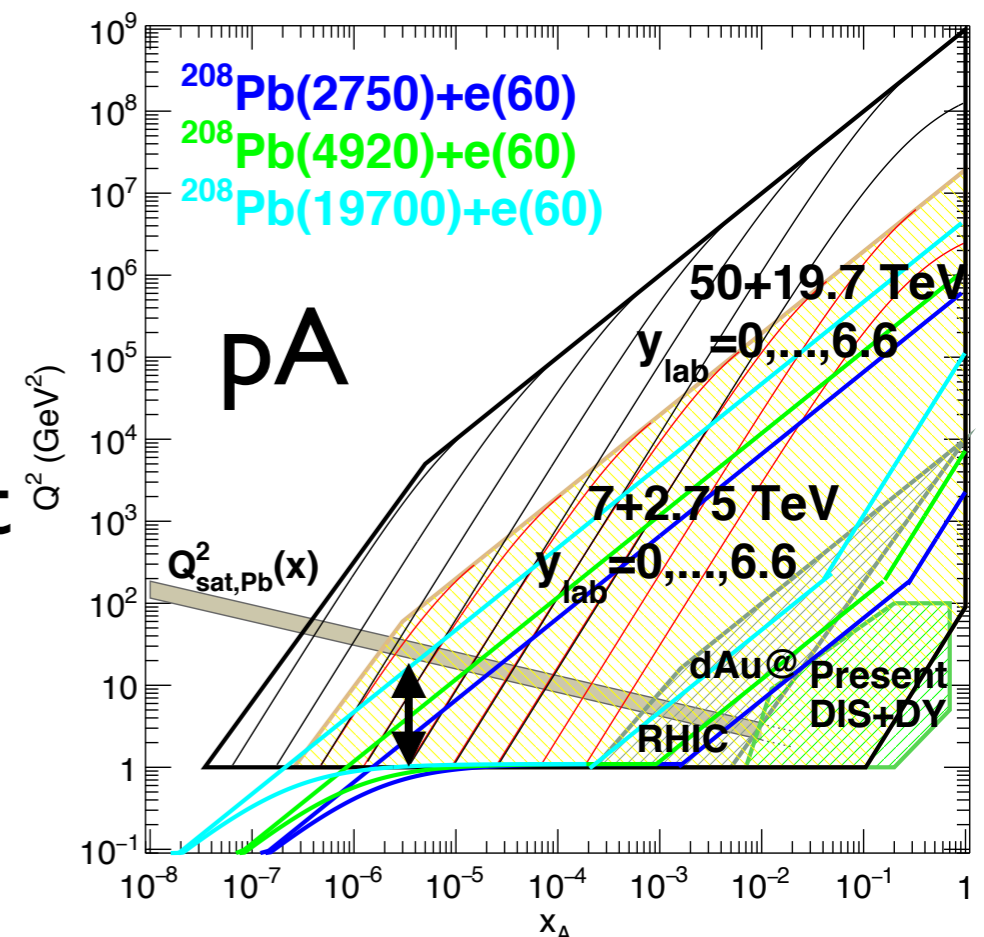
parameter [unit]	LHeC (HL-LHC)	eA at HE-LHC	FCC-he
$E_{Pb}$ [PeV]	0.574	1.03	4.1
$E_e$ [GeV] <small>CERN-ACC-2017-0019</small>	60	60	60
$\sqrt{s_{eN}}$ electron-nucleon [TeV]	0.8	1.1	2.2
bunch spacing [ns]	50	50	100
no. of bunches	1200	1200	2072
ions per bunch [ $10^8$ ]	1.8	1.8	1.8
$\gamma\epsilon_A$ [ $\mu\text{m}$ ]	1.5	1.0	0.9
electrons per bunch [ $10^9$ ]	4.67	6.2	12.5
electron current [mA]	15	20	20
IP beta function $\beta_A^*$ [cm]	7	10	15
hourglass factor $H_{geom}$	0.9	0.9	0.9
pinch factor $H_{b-b}$	1.3	1.3	1.3
bunch filling $H_{coll}$	0.8	0.8	0.8
luminosity [ $10^{32}\text{cm}^{-2}\text{s}^{-1}$ ]	7	18	54
Integrated lumi. in 10 y. ( $\text{fb}^{-1}$ ) $\sim\sim$	6	15	45

**eD at LHEC:**  
 $L_{eN} = A L_{eA} > \sim 3 \times 10^{31} \text{ cm}^{-2}\text{s}^{-1}$   
 (old CDR number)

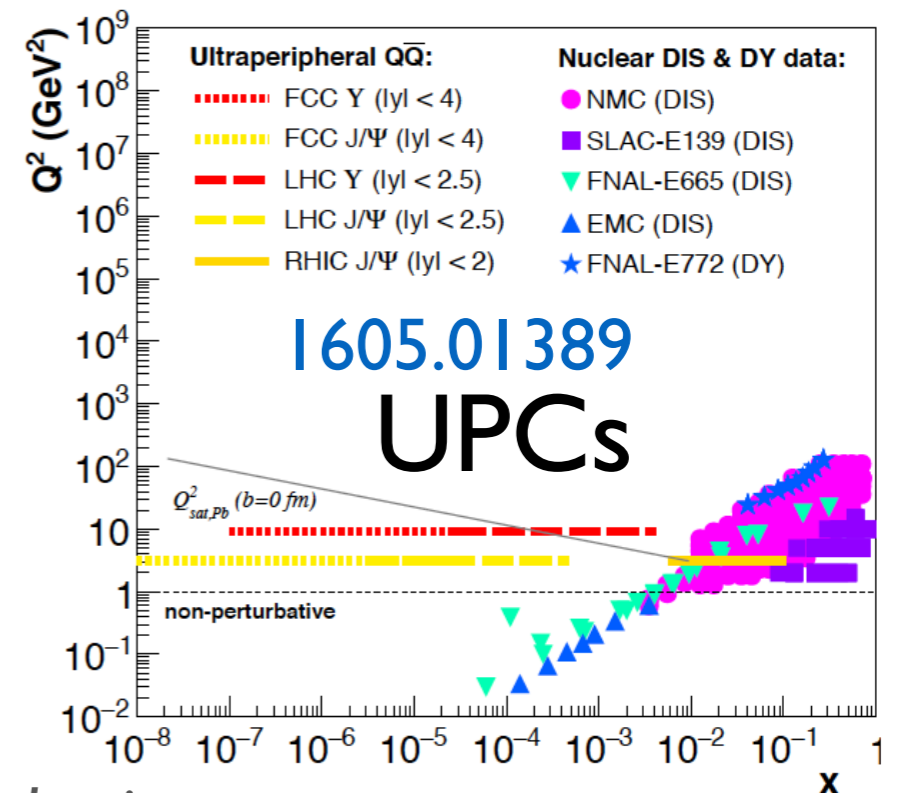
- 100 times larger luminosity than HERA, full HERA integrated luminosity in less than a month.



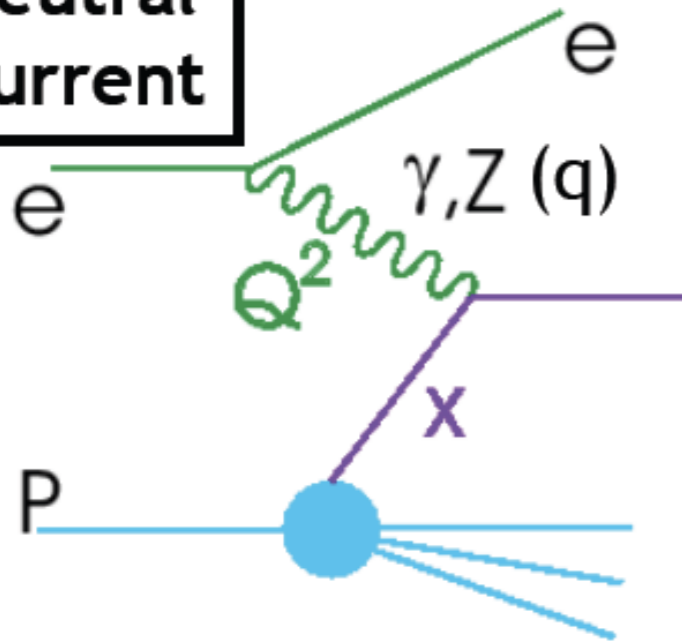
- Extension up to 4-5 orders of magnitude in  $x$  and  $Q^2$  wrt existing DIS data,  $\sim 2-3$  wrt JLEIC/ eRHIC.



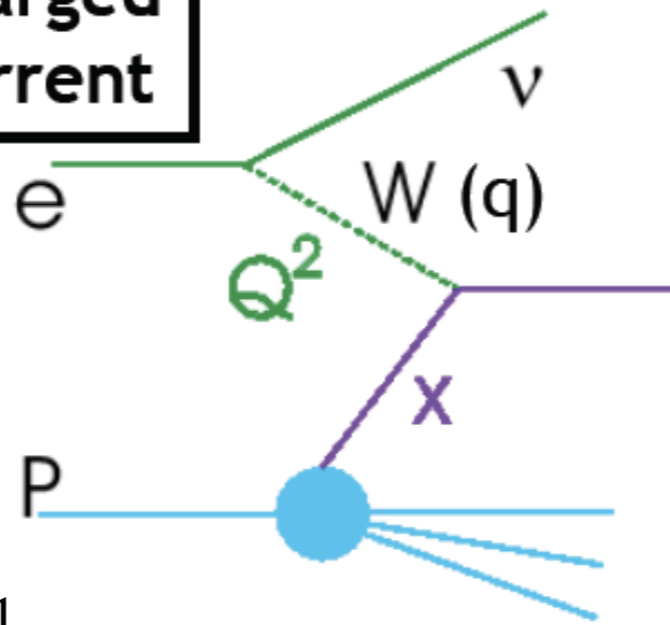
- DIS offers:
  - A clean experimental environment: low multiplicity, no pileup, fully constrained kinematics;
  - A more controlled theoretical setup: many first-principles calculations in collinear and non-collinear frameworks.



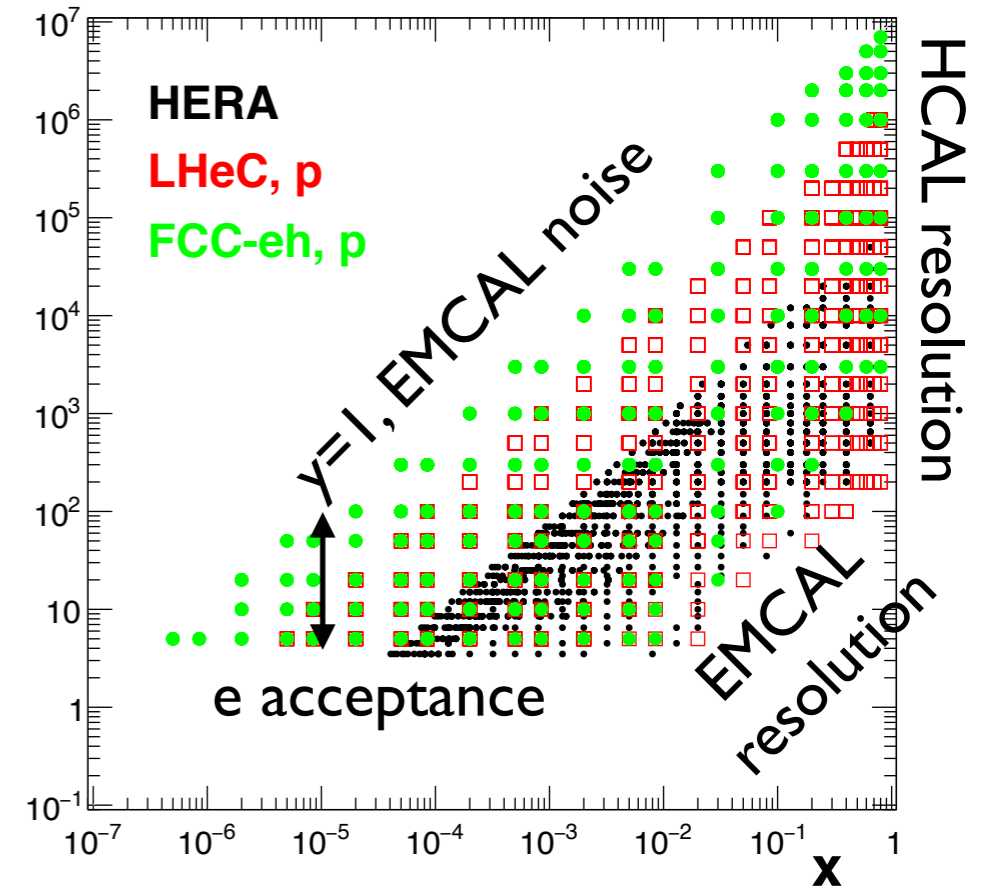
**Neutral Current**



**Charged Current**



$Q^2$  (GeV<sup>2</sup>)



• Method (DGLAP  $\Rightarrow \int_x^1 \dots$ ):

$F_2(x, Q^2) \propto \sum xq(x, Q^2)$  : determines directly valence (large x) and sea (low x)

$\frac{\partial F_2(x, Q^2)}{\partial \log Q^2} \propto xg(x, Q^2)$  : determines glue via DGLAP,  $\mathcal{O}(\alpha_s)$ , requires lever arm in  $Q^2$ .

$F_L(x, Q^2) \propto xg(x, Q^2) - F_2(x, Q^2)$  : determines the glue via DGLAP,  $\mathcal{O}(\alpha_s)$ , requires lever arm in s (different y at fixed x,  $Q^2$ , use  $\sigma_{\text{red}}$ ).

$F_2^{c,b,t}(x, Q^2)$  : determines heavy flavour PDFs, requires HQ ID.

$\sigma_r^{CC}$  : determines strange PDF, requires HQ ID and measurement of missing energy.



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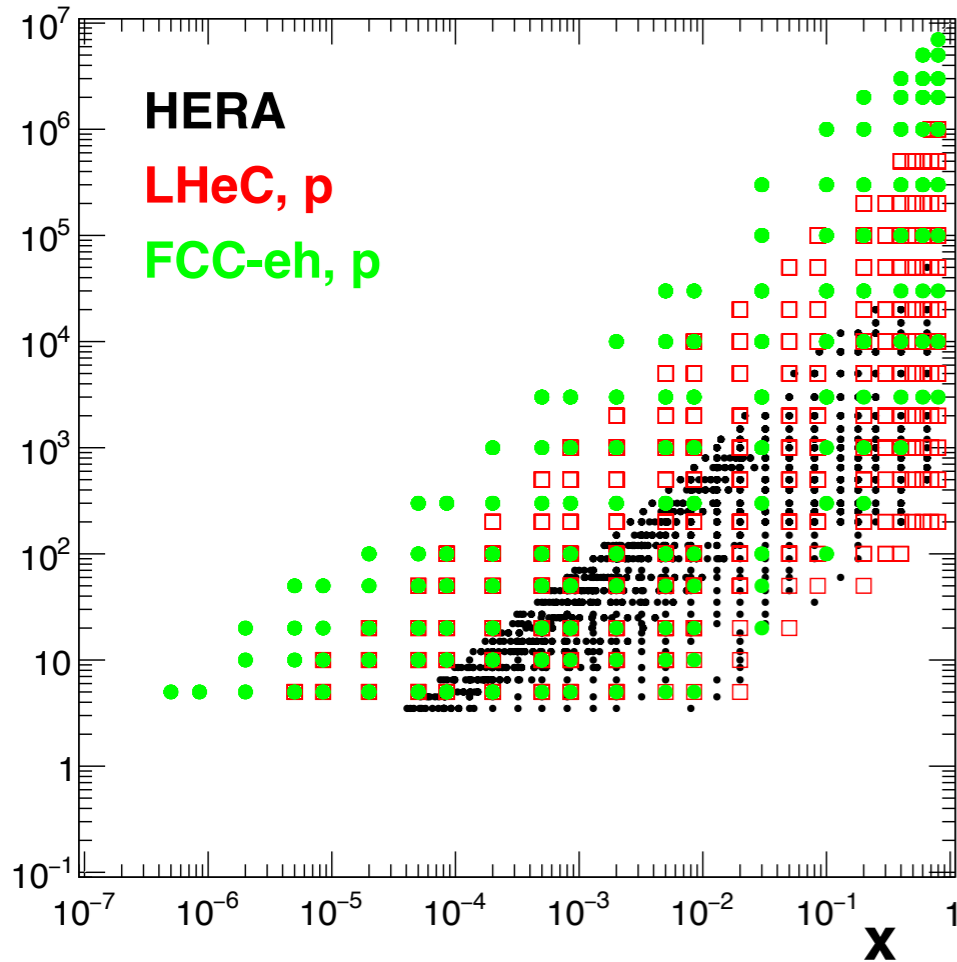
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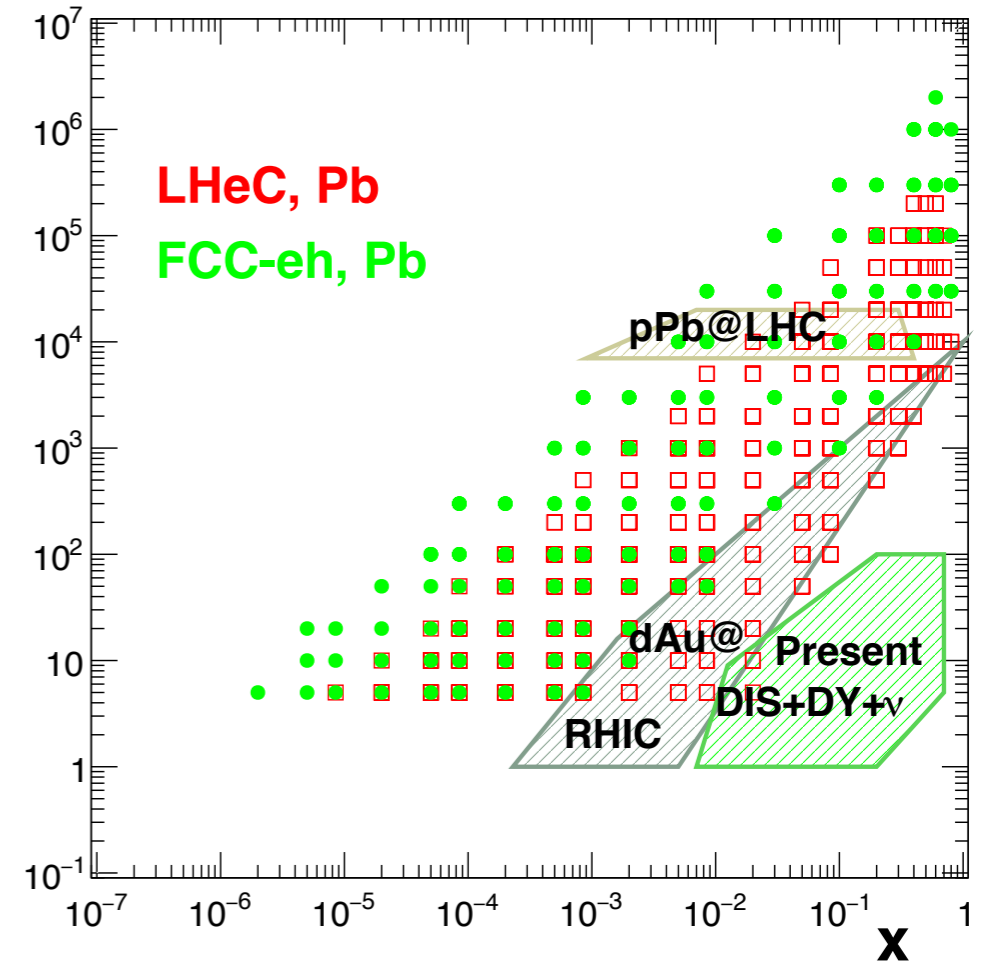
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	$E_e$ (GeV)	$E_n$ (TeV/nucleon)	Polarisation	Luminosity (fb <sup>-1</sup> )	NC/CC	# data
<b>ep@LHeC</b> , 1005 data points for $Q^2 \geq 3.5$ GeV <sup>2</sup>	60 (e <sup>-</sup> )	1 (p)	0	100	CC	93
	60 (e <sup>-</sup> )	1 (p)	0	100	NC	136
	60 (e <sup>-</sup> )	7 (p)	-0.8	1000	CC	114
	60 (e <sup>-</sup> )	7 (p)	0.8	300	CC	113
	60 (e <sup>+</sup> )	7 (p)	0	100	CC	109
	60 (e <sup>-</sup> )	7 (p)	-0.8	1000	NC	159
	60 (e <sup>-</sup> )	7 (p)	0.8	300	NC	159
	60 (e <sup>+</sup> )	7 (p)	0	100	NC	157
<b>ePb@LHeC</b> , 484 data points for $Q^2 \geq 3.5$ GeV <sup>2</sup>	20 (e <sup>-</sup> )	2.75 (Pb)	-0.8	0.03	CC	51
	20 (e <sup>-</sup> )	2.75 (Pb)	-0.8	0.03	NC	93
	26.9 (e <sup>-</sup> )	2.75 (Pb)	-0.8	0.02	CC	55
	26.9 (e <sup>-</sup> )	2.75 (Pb)	-0.8	0.02	NC	98
	60 (e <sup>-</sup> )	2.75 (Pb)	-0.8	1	CC	85
	60 (e <sup>-</sup> )	2.75 (Pb)	-0.8	1	NC	129
<b>ep@FCC-eh</b> , 619 data points for $Q^2 \geq 3.5$ GeV <sup>2</sup>	20 (e <sup>-</sup> )	7 (p)	0	100	CC	46
	20 (e <sup>-</sup> )	7 (p)	0	100	NC	89
	60 (e <sup>-</sup> )	50 (p)	-0.8	1000	CC	67
	60 (e <sup>-</sup> )	50 (p)	0.8	300	CC	65
	60 (e <sup>+</sup> )	50 (p)	0	100	CC	60
	60 (e <sup>-</sup> )	50 (p)	-0.8	1000	NC	111
	60 (e <sup>-</sup> )	50 (p)	0.8	300	NC	110
	60 (e <sup>+</sup> )	50 (p)	0	100	NC	107
<b>ePb@FCC-eh</b> , 150 data points for $Q^2 \geq 3.5$ GeV <sup>2</sup>	60 (e <sup>-</sup> )	20 (Pb)	-0.8	10	CC	58
	60 (e <sup>-</sup> )	20 (Pb)	-0.8	10	NC	101

$Q^2$  (GeV<sup>2</sup>)



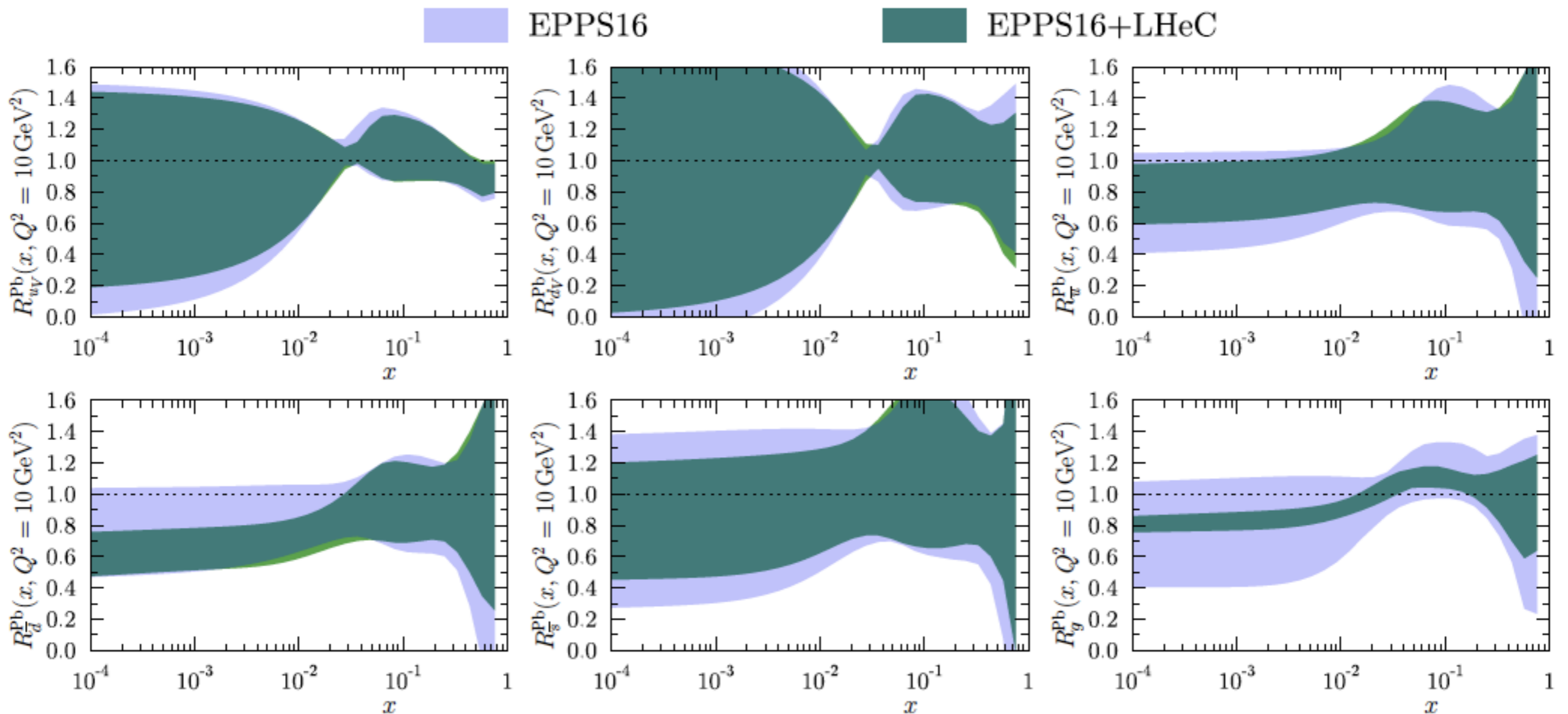
$Q^2$  (GeV<sup>2</sup>)



- Pseudodata generated using a code (Max Klein) validated with the HI MC.
- Cuts:  $|\eta_{\text{max}}|=5$ ,  $0.95 < y < 0.001$ .
- Error assumptions  $\sim$  factor 2 better than at HERA (luminosity uncertainty kept aside).
- Stat./syst. errors (ePb@FCC-eh) from 0.1/1.2% (small  $x$ , NC) to 37/6% (large  $x$  &  $Q^2$ , CC).

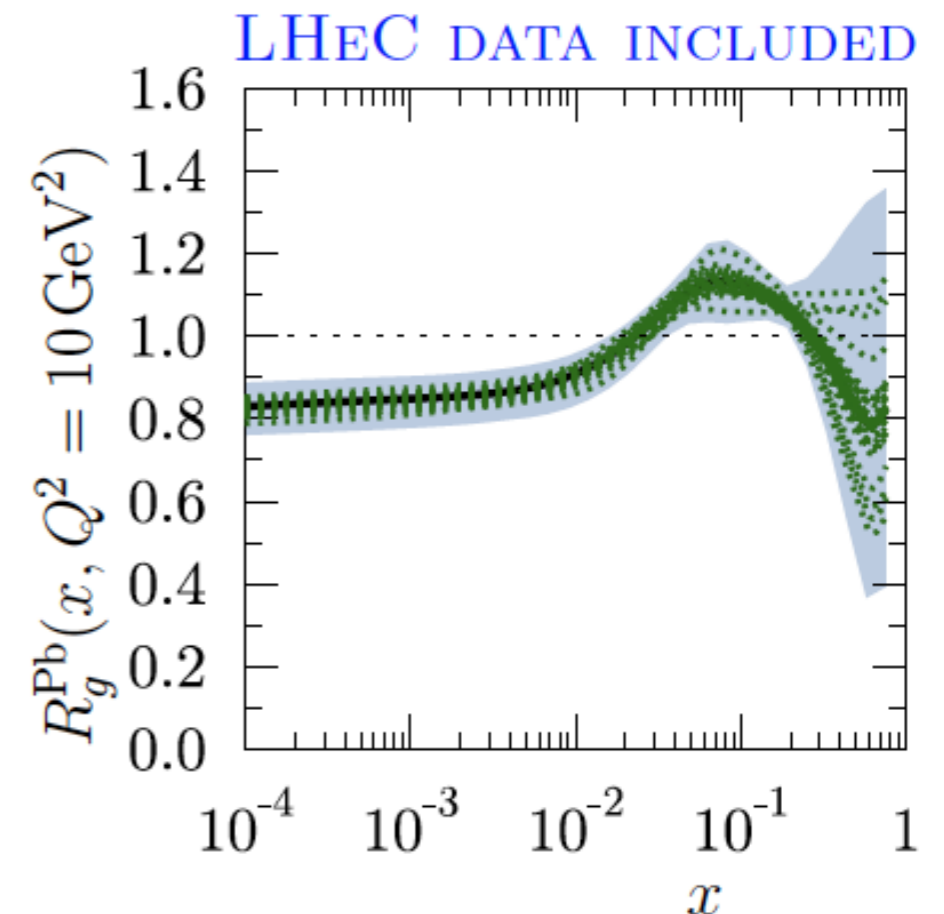
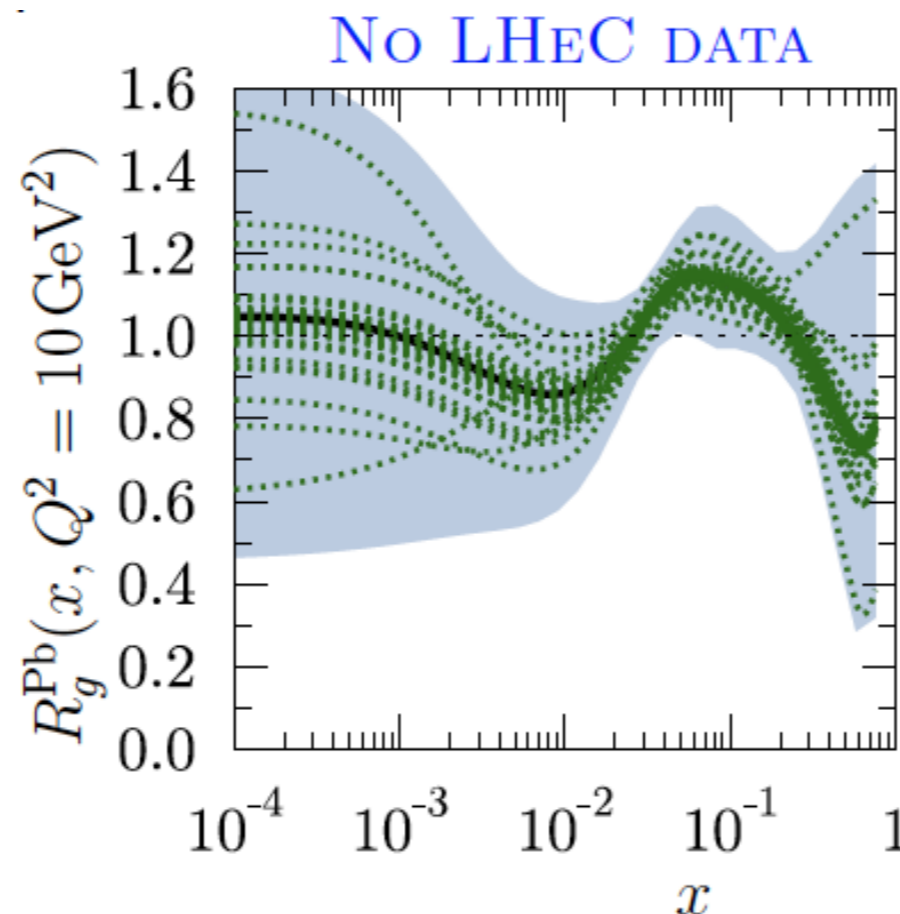
Source of uncertainty	Error on the source or cross section
scattered electron energy scale	0.1 %
scattered electron polar angle	0.1 mrad
hadronic energy scale	0.5 %
calorimeter noise ( $y < 0.01$ )	1-3 %
radiative corrections	1-2 %
photoproduction background	1 %
global efficiency error	0.7 %

- EPPS16-like analysis done previously, with the same data sets plus LHeC NC and CC, the same methods and tolerance ( $\Delta\chi^2=52$ ).
- Limitation on u/d decomposition inherent to almost isospin symmetric nuclei (u/d difference suppressed by  $2Z/A-1$ ).



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- More flexible parametrisation essayed, require Monte Carlo methods for reliable uncertainty estimation; still visible effects.



- Extraction of Pb-only PDFs by fitting pseudodata, using xFitter (1410.4412) 1.2.2 to estimate the ‘ultimate’ achievable precision:
  - HERAPDF2.0-type parametrisation (1506.06042, 14 parameters), NNLO evolution, RTOPT mass scheme,  $\alpha_s=0.118$ .

$$xg(x) = A_g x^{B_g} (1-x)^{C_g} - A'_g x^{B'_g} (1-x)^{C'_g},$$

$$xu_v(x) = A_{u_v} x^{B_{u_v}} (1-x)^{C_{u_v}} (1 + E_{u_v} x^2),$$

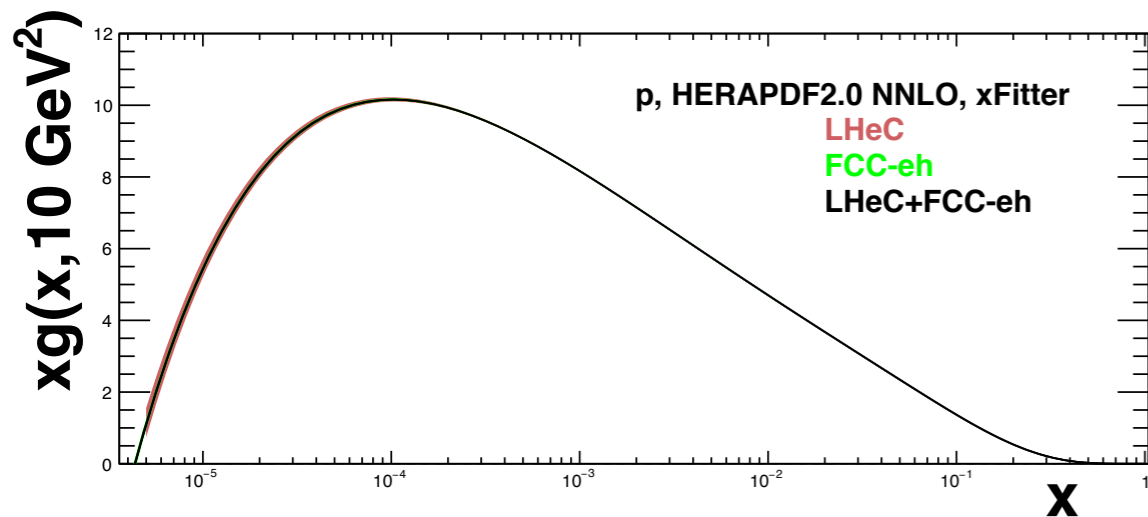
$$xd_v(x) = A_{d_v} x^{B_{d_v}} (1-x)^{C_{d_v}},$$

$$x\bar{U}(x) = A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}} (1 + D_{\bar{U}} x),$$

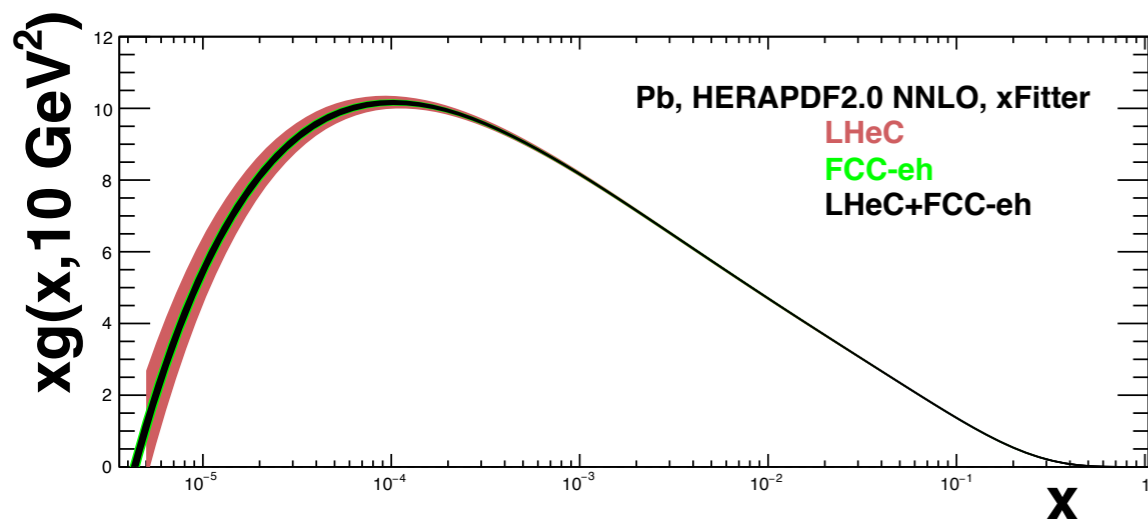
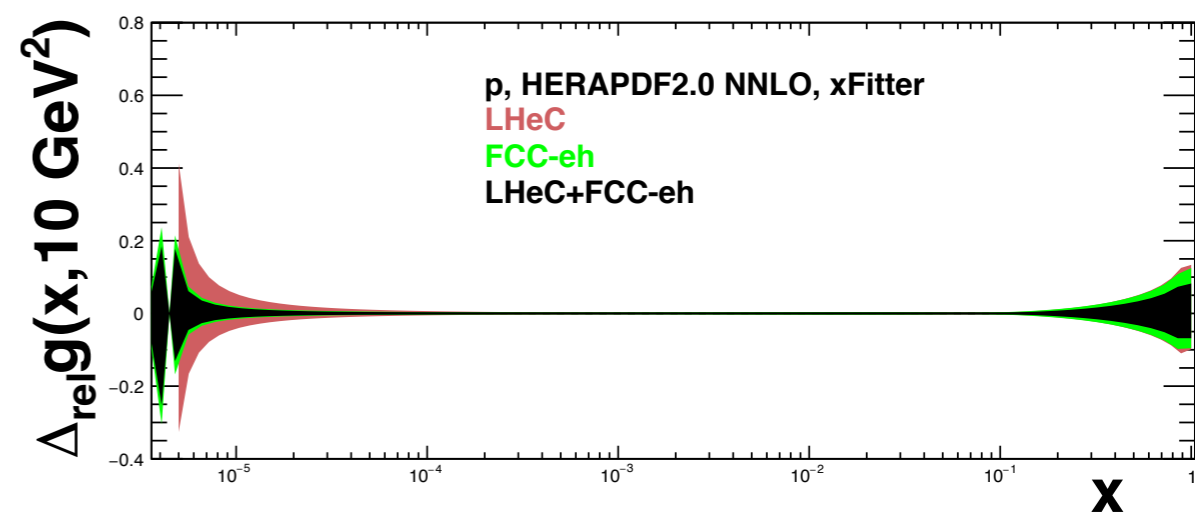
$$x\bar{D}(x) = A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}}.$$

$$xU = xu + xc, \quad x\bar{U} = x\bar{u} + x\bar{c}, \quad xD = xd + xs, \quad x\bar{D} = x\bar{d} + x\bar{s}$$

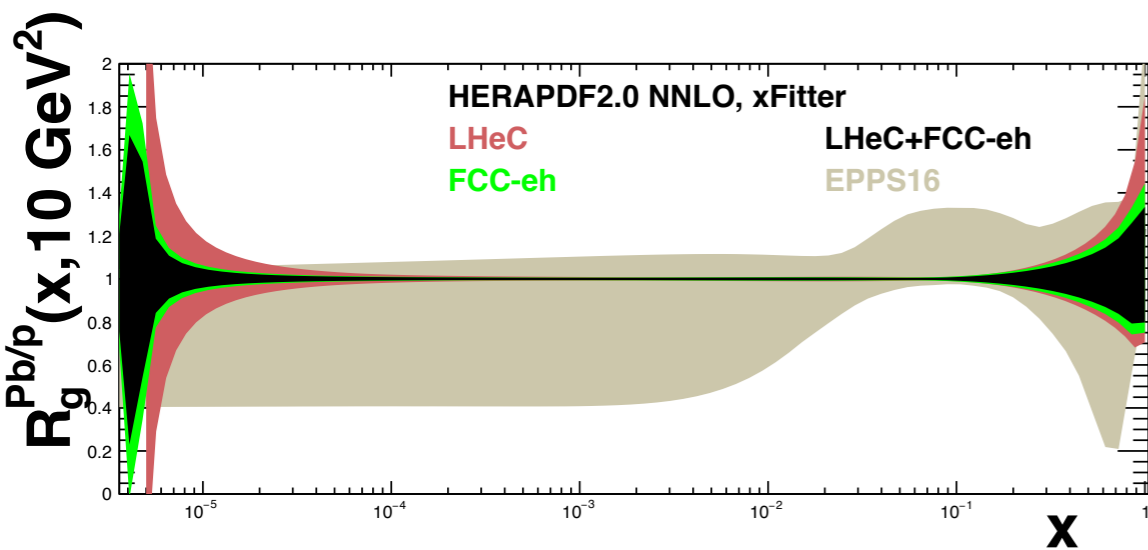
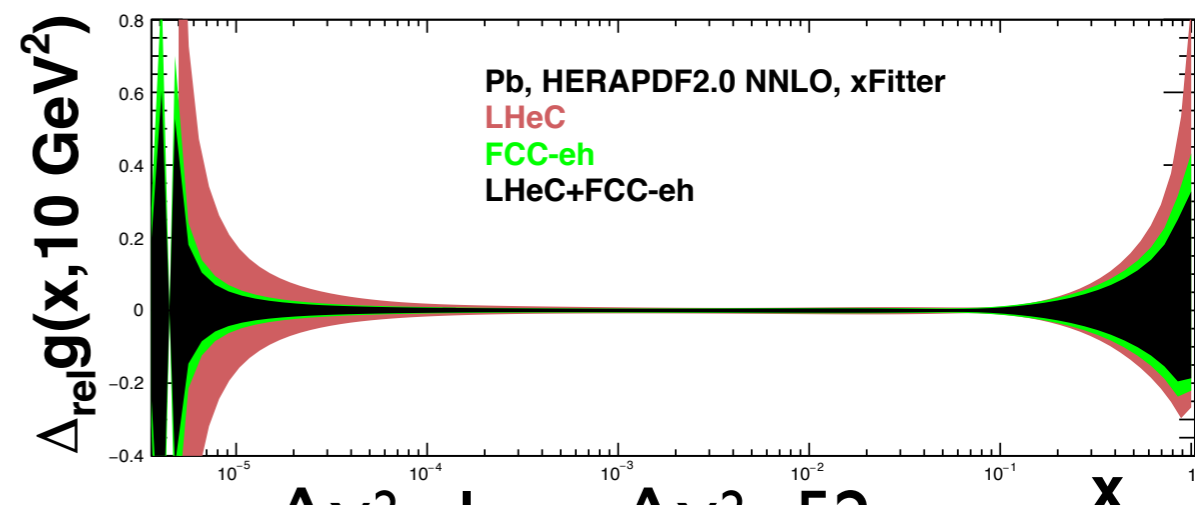
- Central pseudodata values from HERAPDF2.0: no parametrisation bias.
- Standard xFitter/HERAPDF treatment of correlated/uncorrelated systematics; tolerance  $\Delta\chi^2=1$ .
- Only data with  $Q^2 \geq 3.5 \text{ GeV}^2$ , initial evolution scale  $1.9 \text{ GeV}^2$ .
- Proton PDFs extracted in the same setup for consistency.



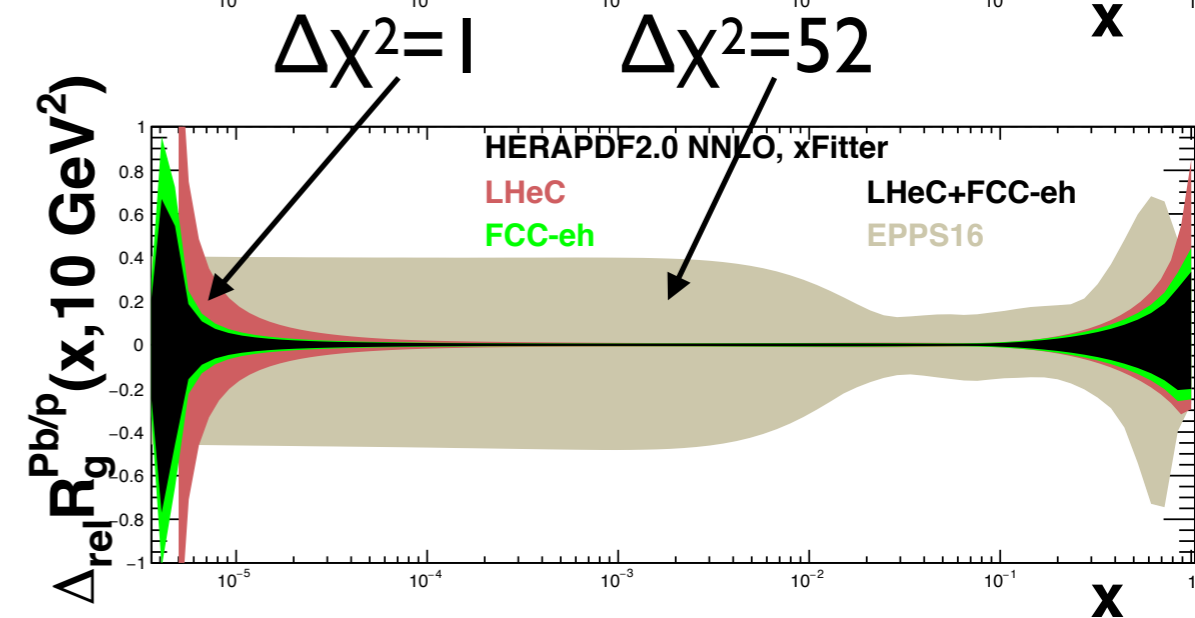
P

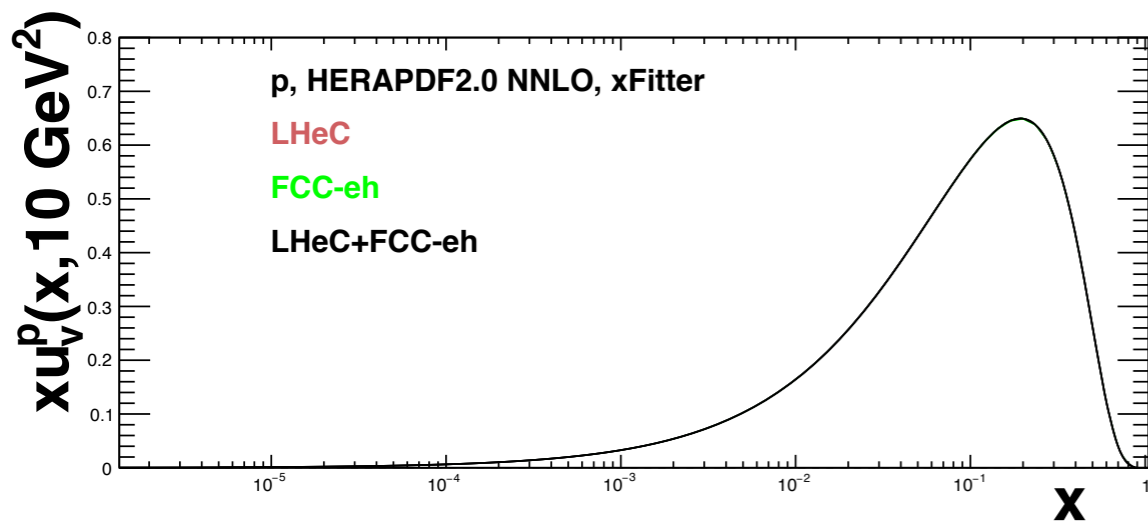


Pb

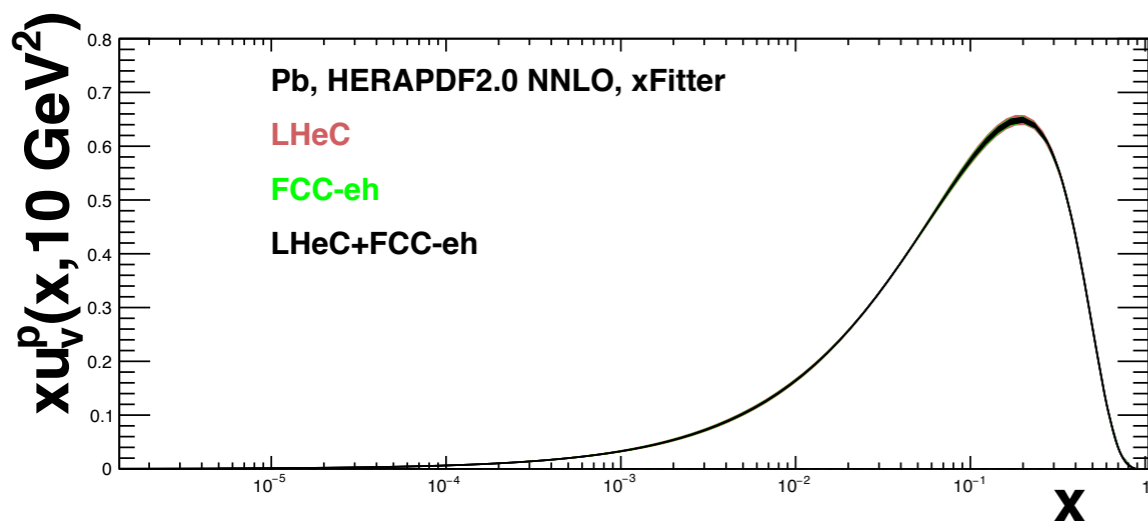
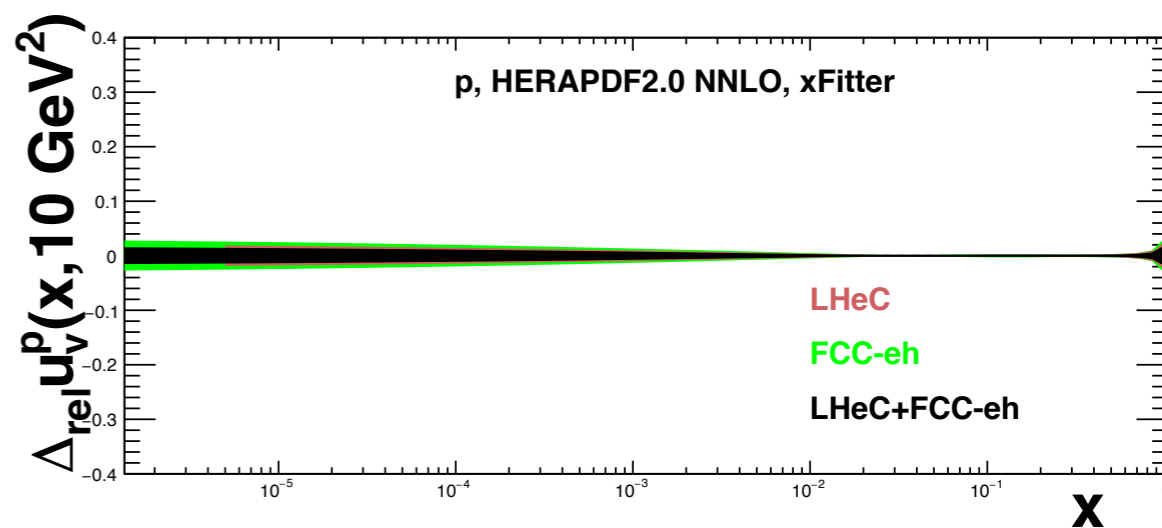


Pb/p

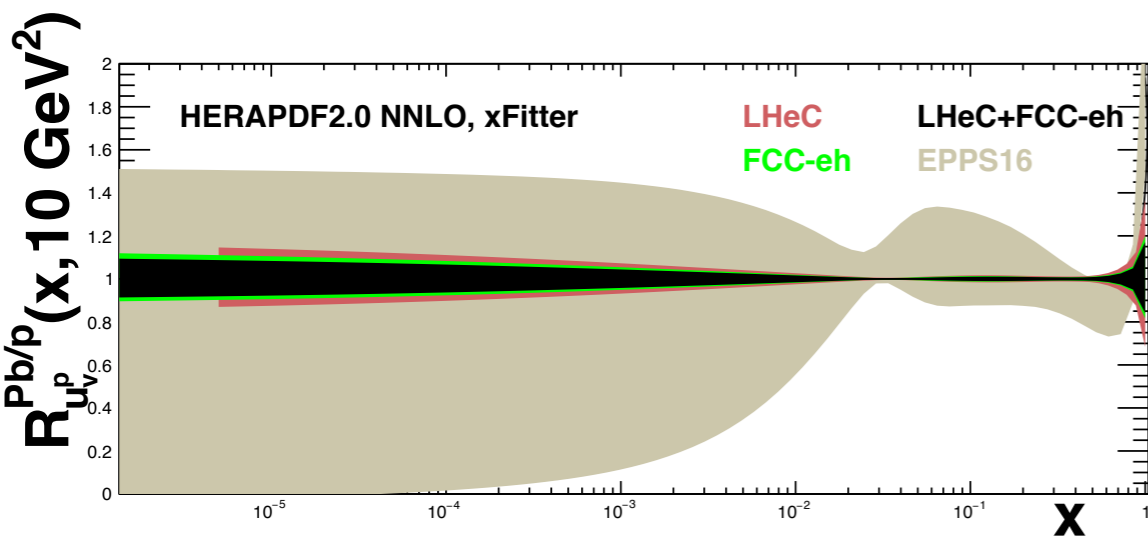
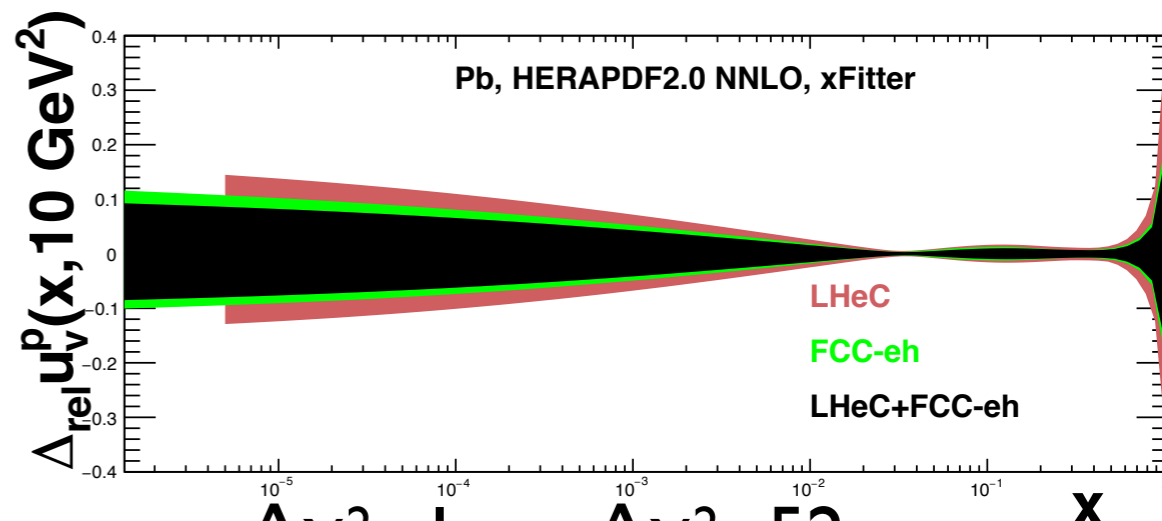




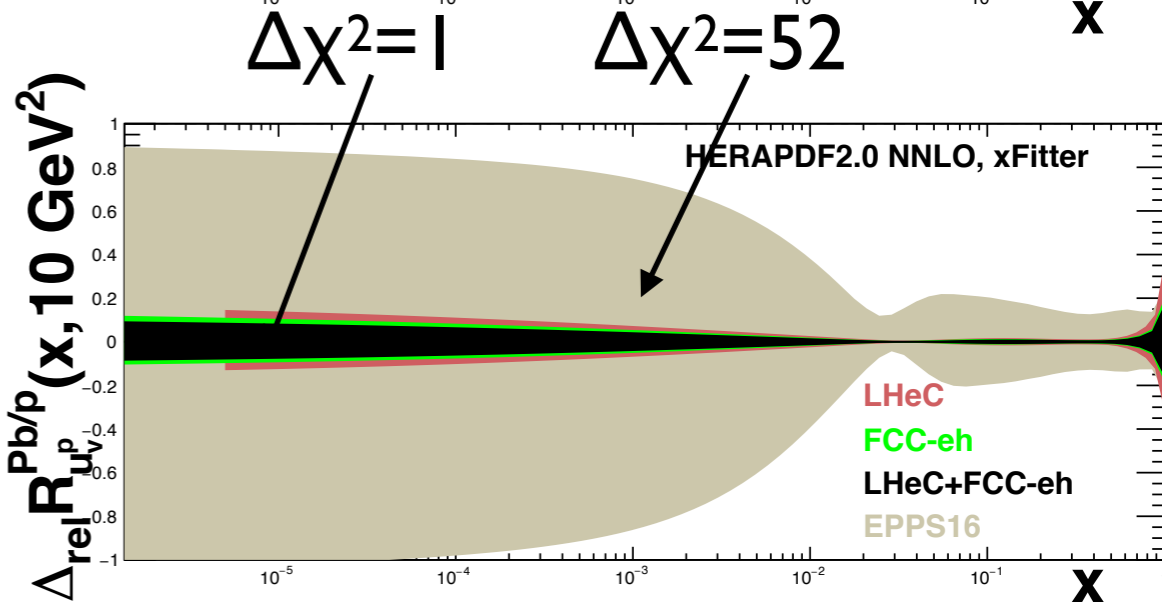
**p**



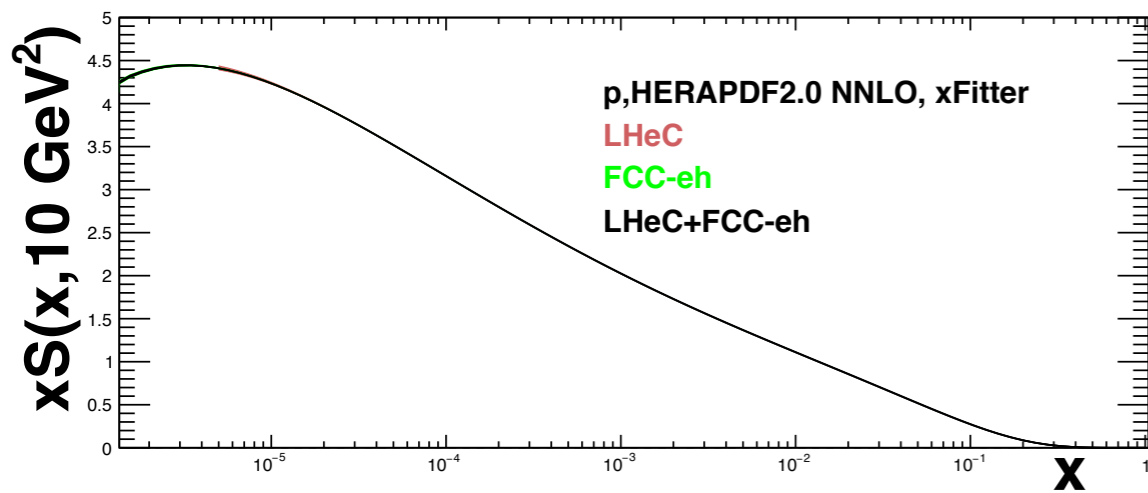
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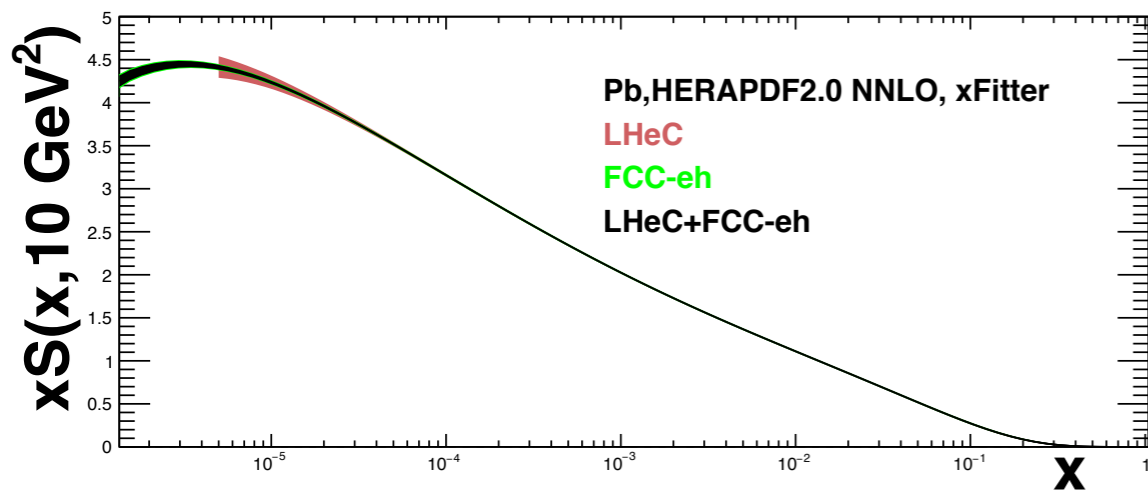
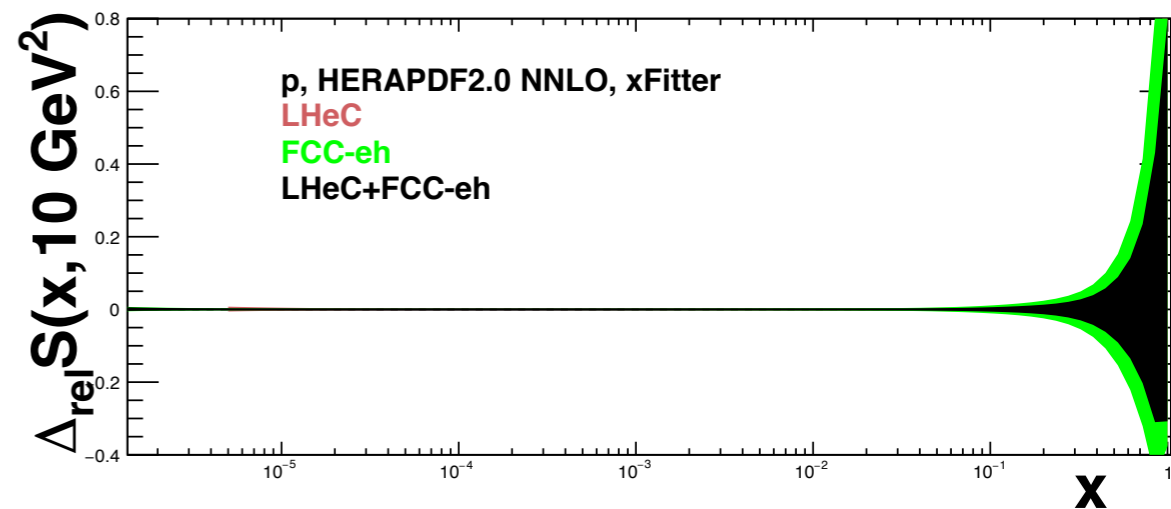
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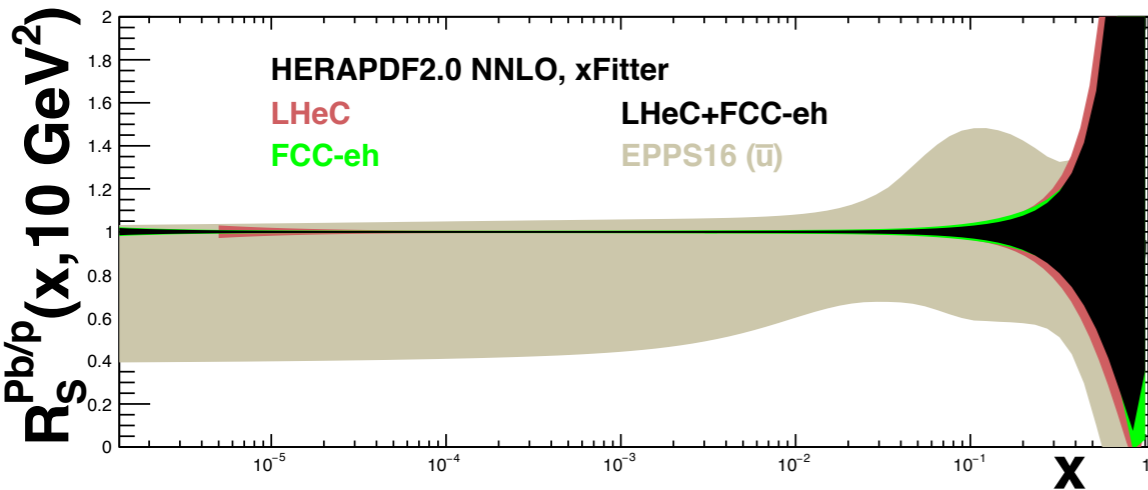
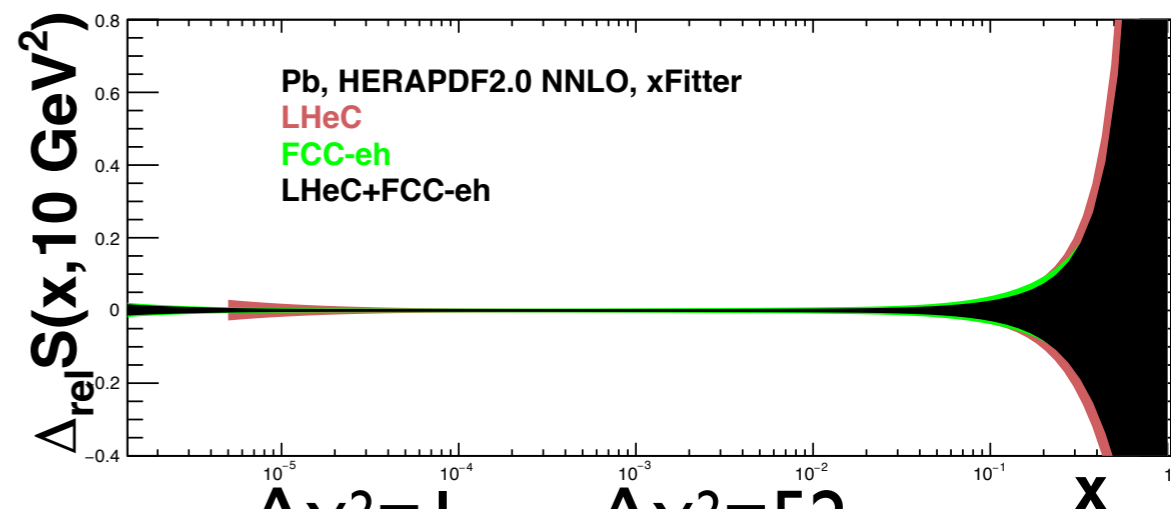




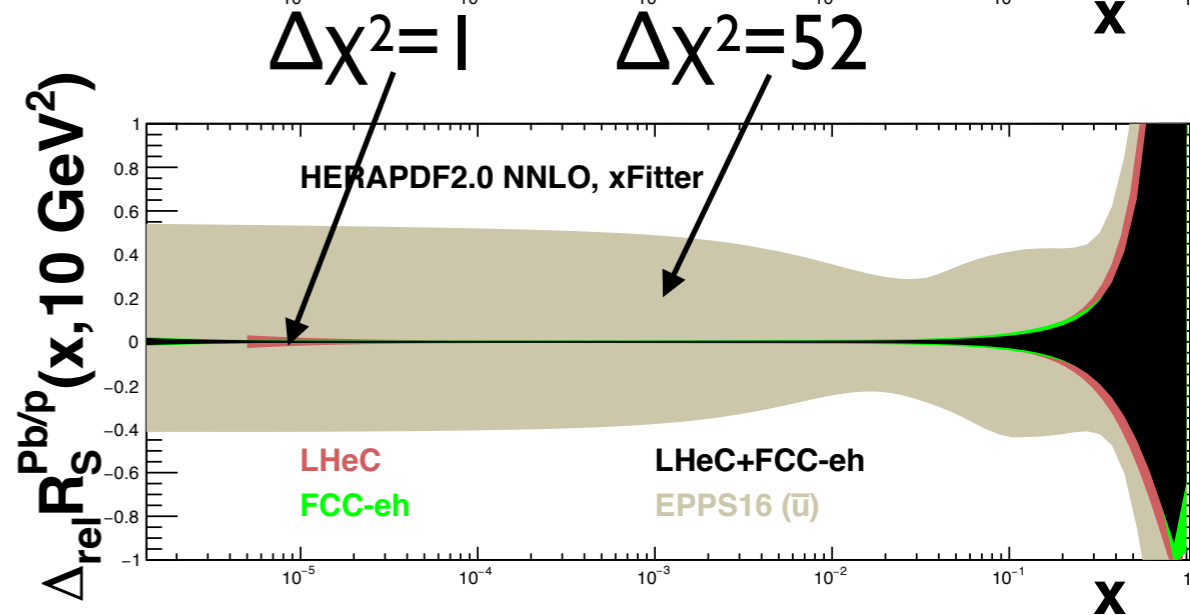
P



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Pb/p



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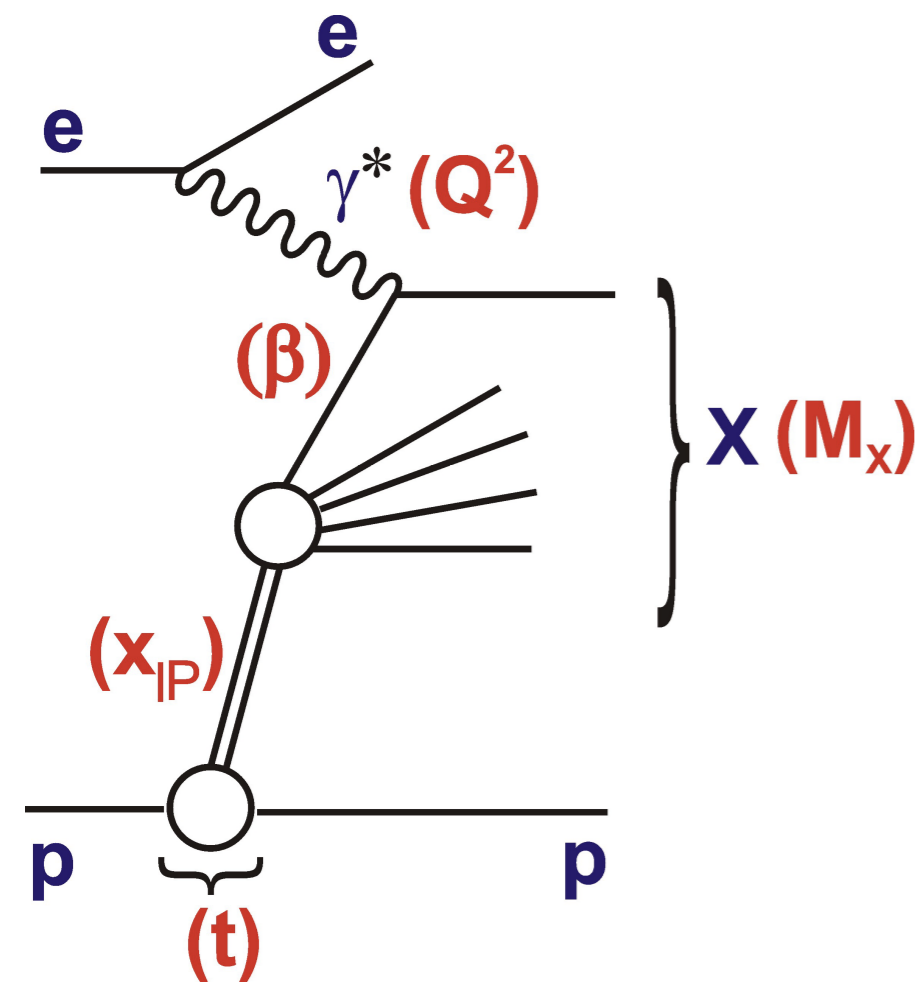
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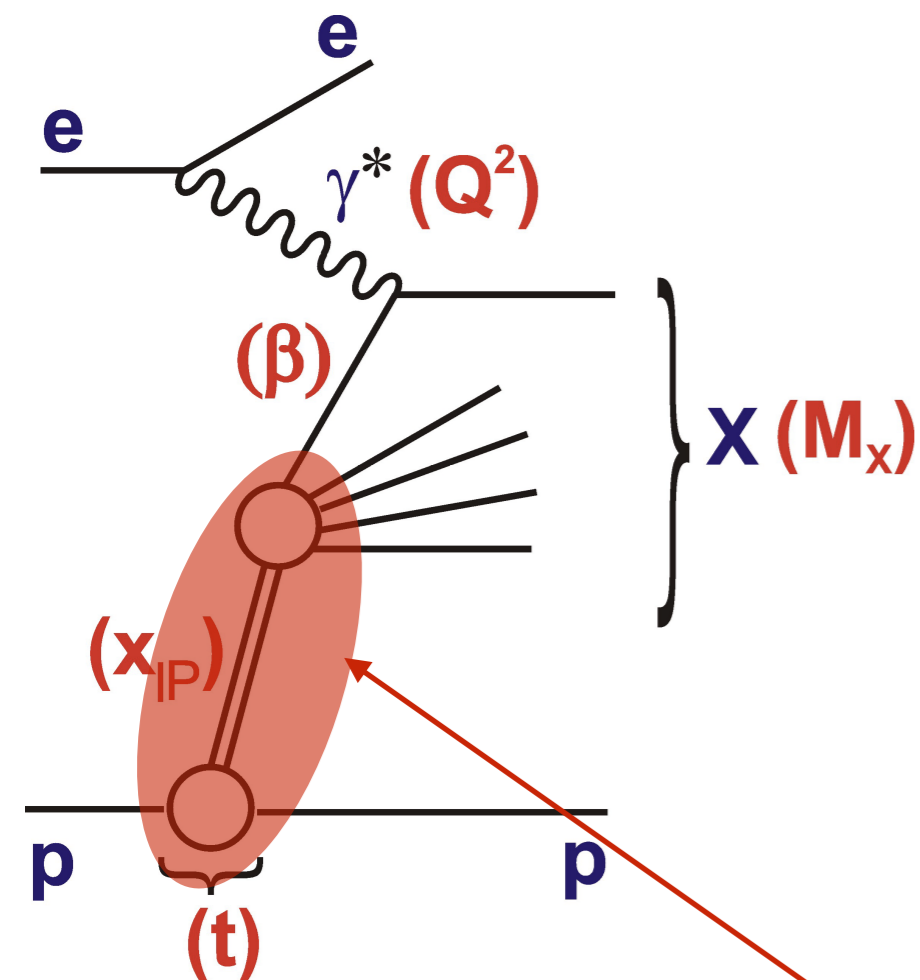
$$\frac{d^3 \sigma^D}{dx_{IP} dx dQ^2} = \frac{2\pi \alpha_{em}^2}{x Q^4} Y_+ \sigma_r^{D(3)}(x_{IP}, x, Q^2)$$

$$\sigma_r^{D(3)} = F_2^{D(3)} - \frac{y^2}{Y_+} F_L^{D(3)}$$

$$Y_+ = 1 + (1 - y)^2$$

$$F_{T,L}^{D(3)}(x, Q^2, x_{IP}) = \int_{-\infty}^0 dt F_{T,L}^{D(4)}(x, Q^2, x_{IP}, t)$$

$$F_2^{D(4)} = F_T^{D(4)} + F_L^{D(4)}$$



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- For fixed  $t, x_{IP}$ , collinear factorisation holds (**Collins**): diffractive PDFs expressing the conditional probability of finding a parton with momentum fraction  $\beta$  with the proton remaining intact.

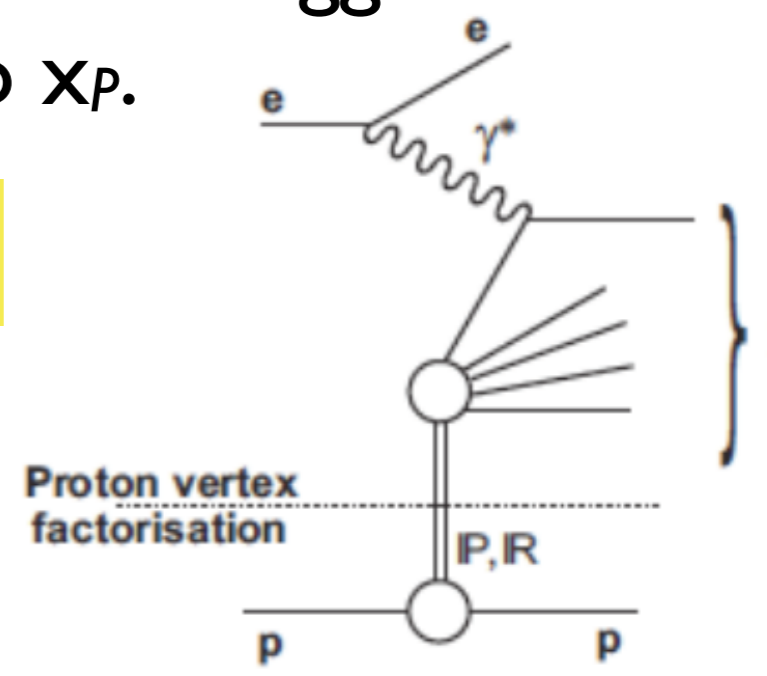
$$d\sigma^{ep \rightarrow eXY}(x, Q^2, x_{IP}, t) = \sum_i f_i^D \otimes d\hat{\sigma}^{ei} + \mathcal{O}(\Lambda^2/Q^2)$$

- To extract DPDFs, an additional assumption is made: Regge factorisation that seems to work for not large too  $x_P$ .

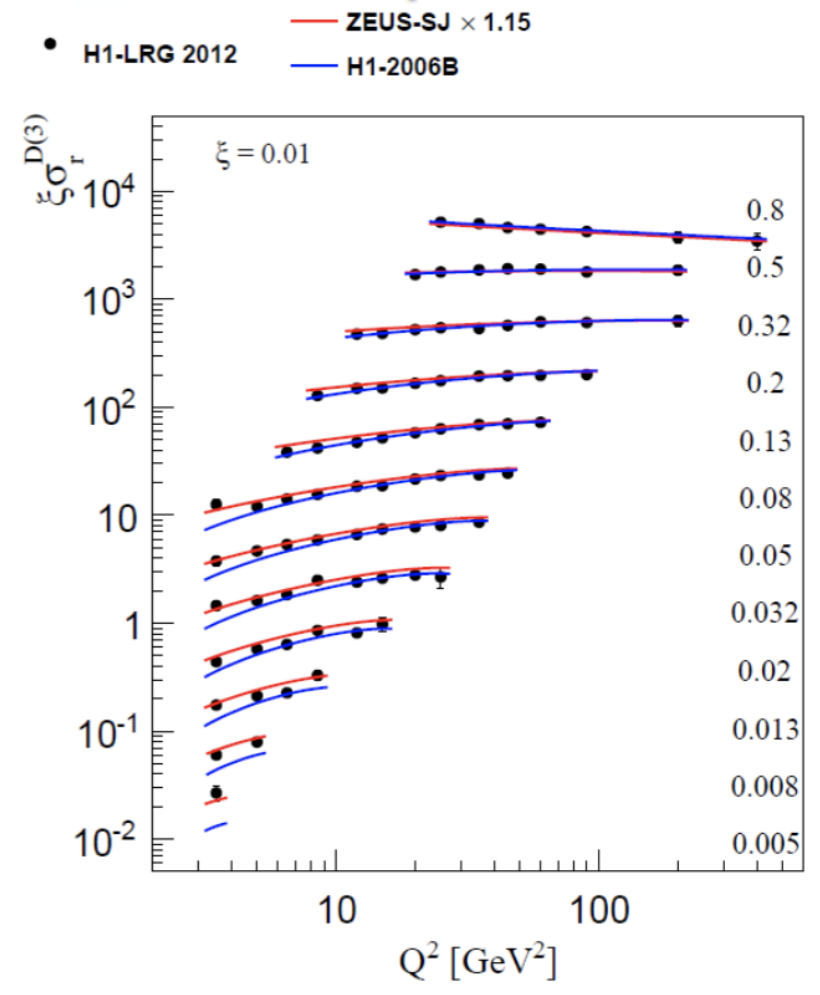
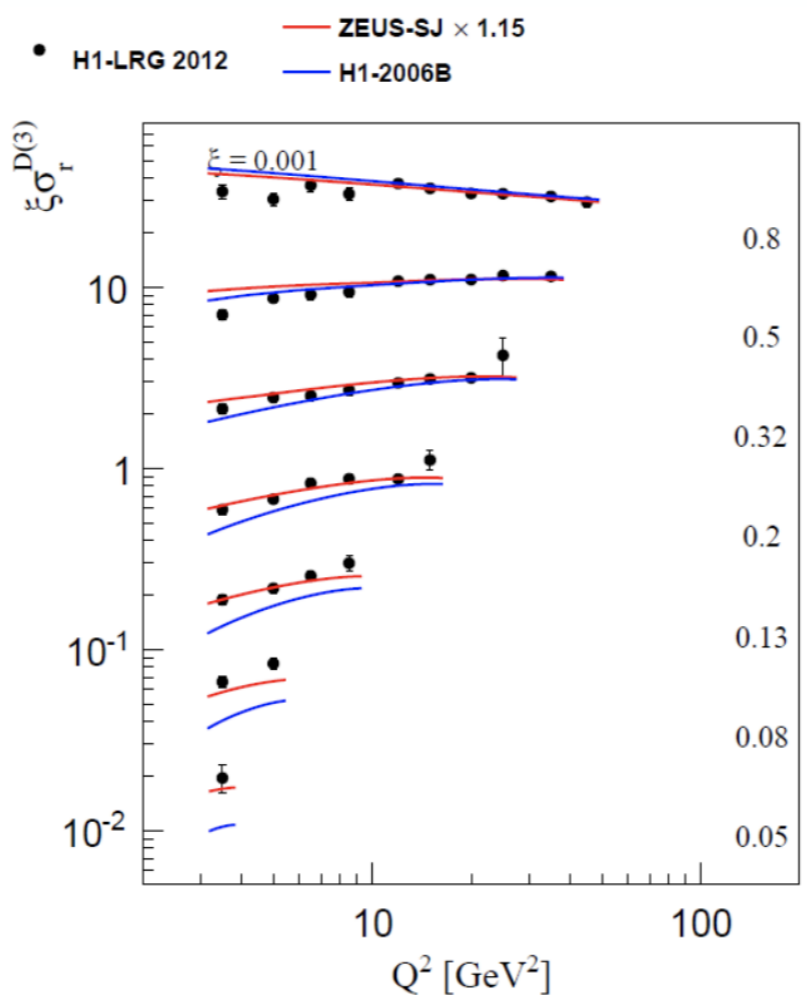
$$f_i^D(x, Q^2, x_{IP}, t) = f_{IP/p}(x_{IP}, t) f_i(\beta = x/x_{IP}, Q^2)$$

Pomeron flux

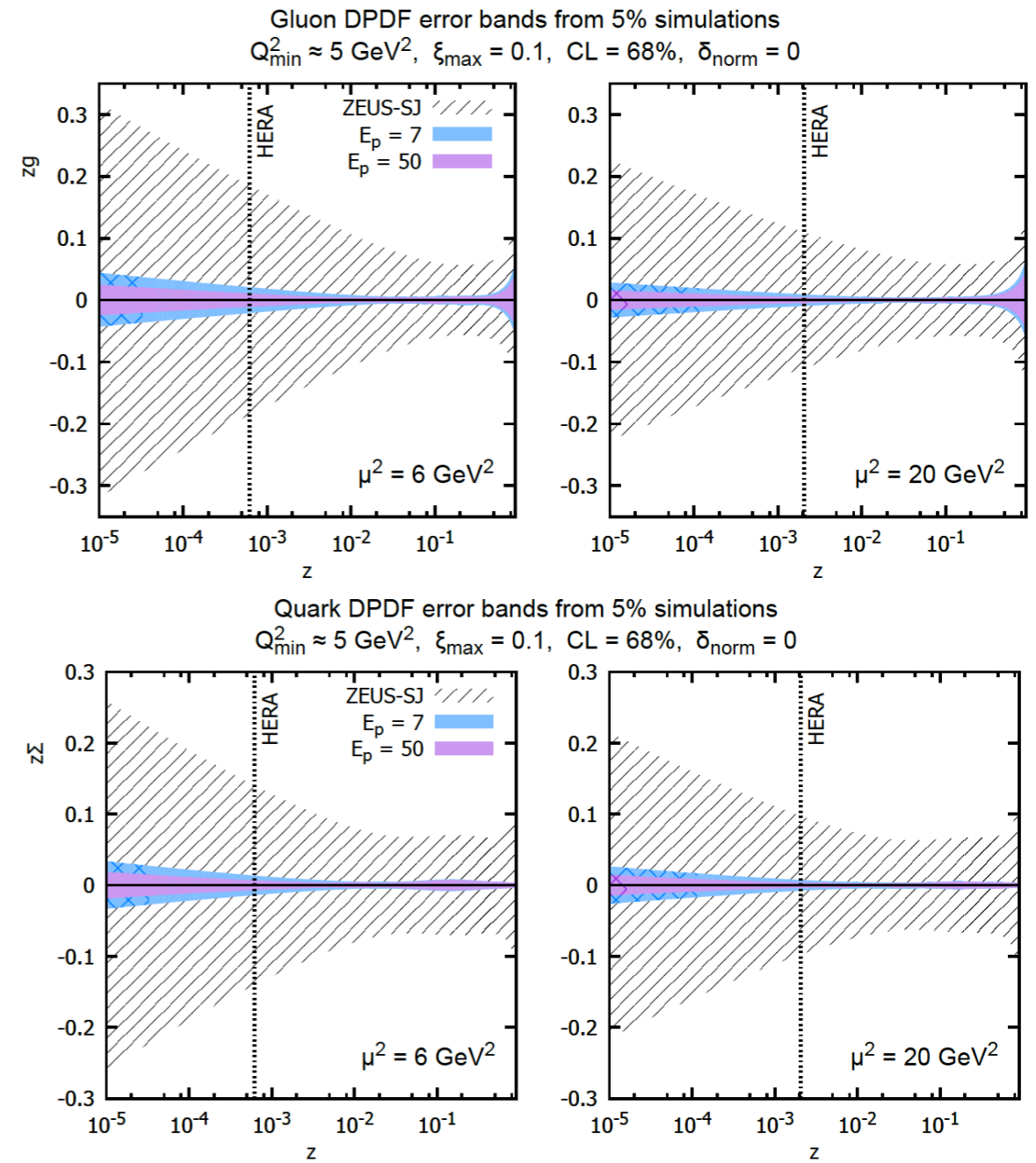
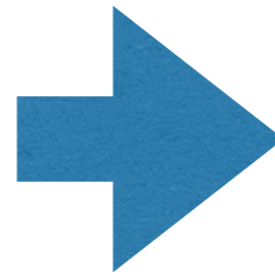
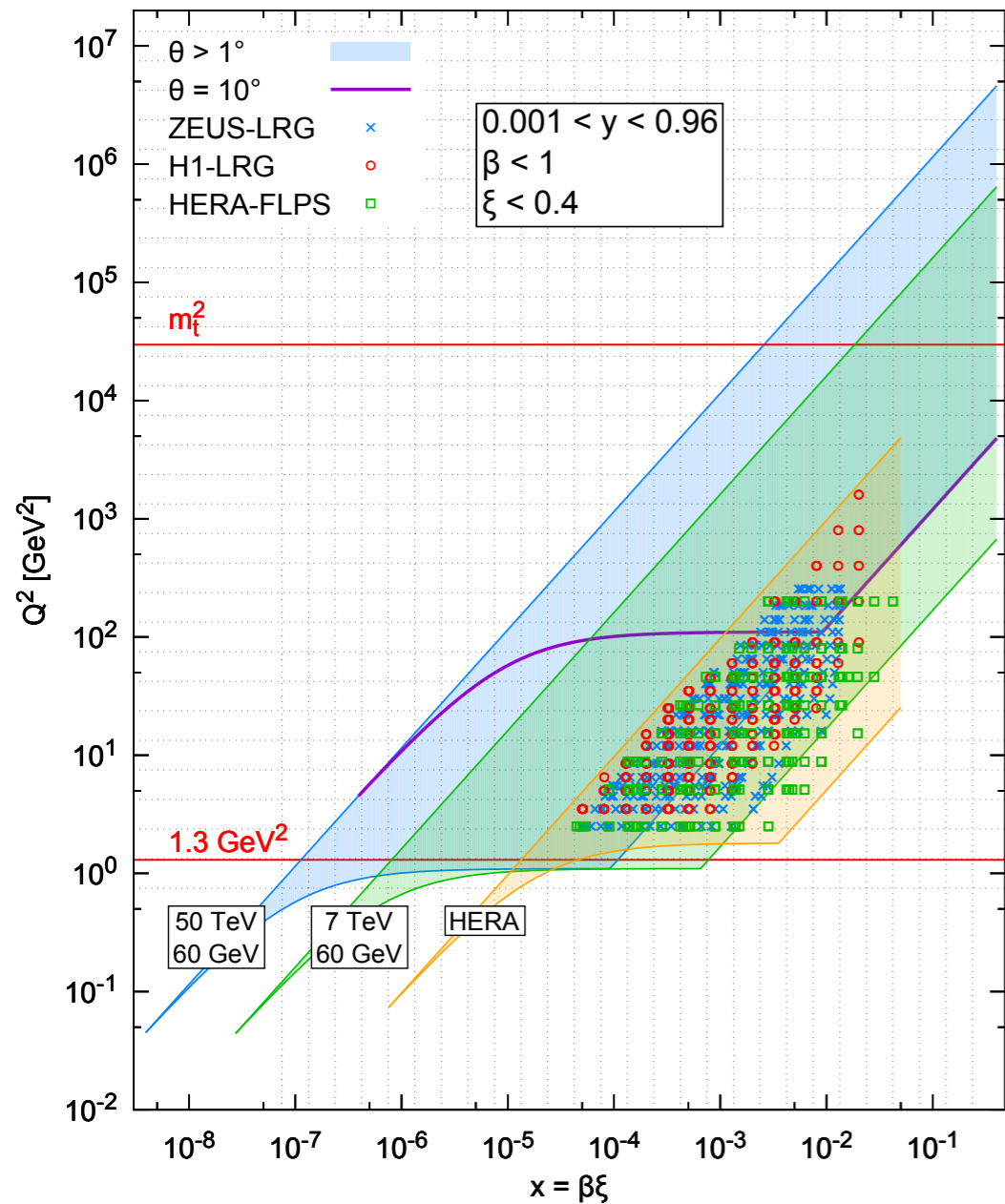
$$f_{IP/p}(x_{IP}, t) = A_{IP} \frac{e^{B_{IP}t}}{x^{2\alpha_{IP}(t)-1}}$$

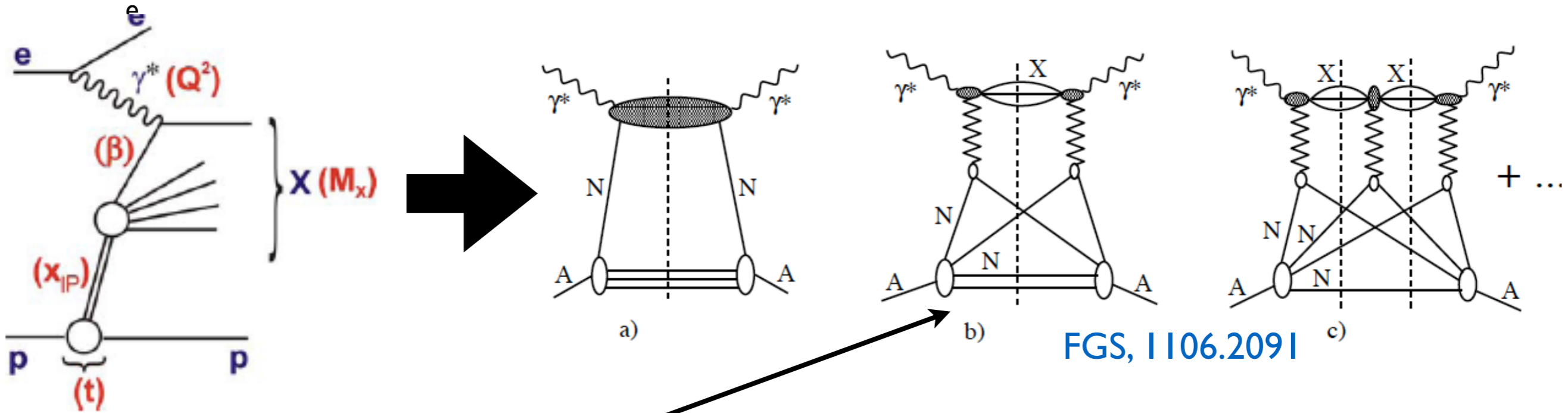


$f_i(\beta, Q^2)$  evolve with DGLAP evolution equations: fits to HERA data (additional contributions at large  $x_P = \xi$  and small  $\beta$ ).

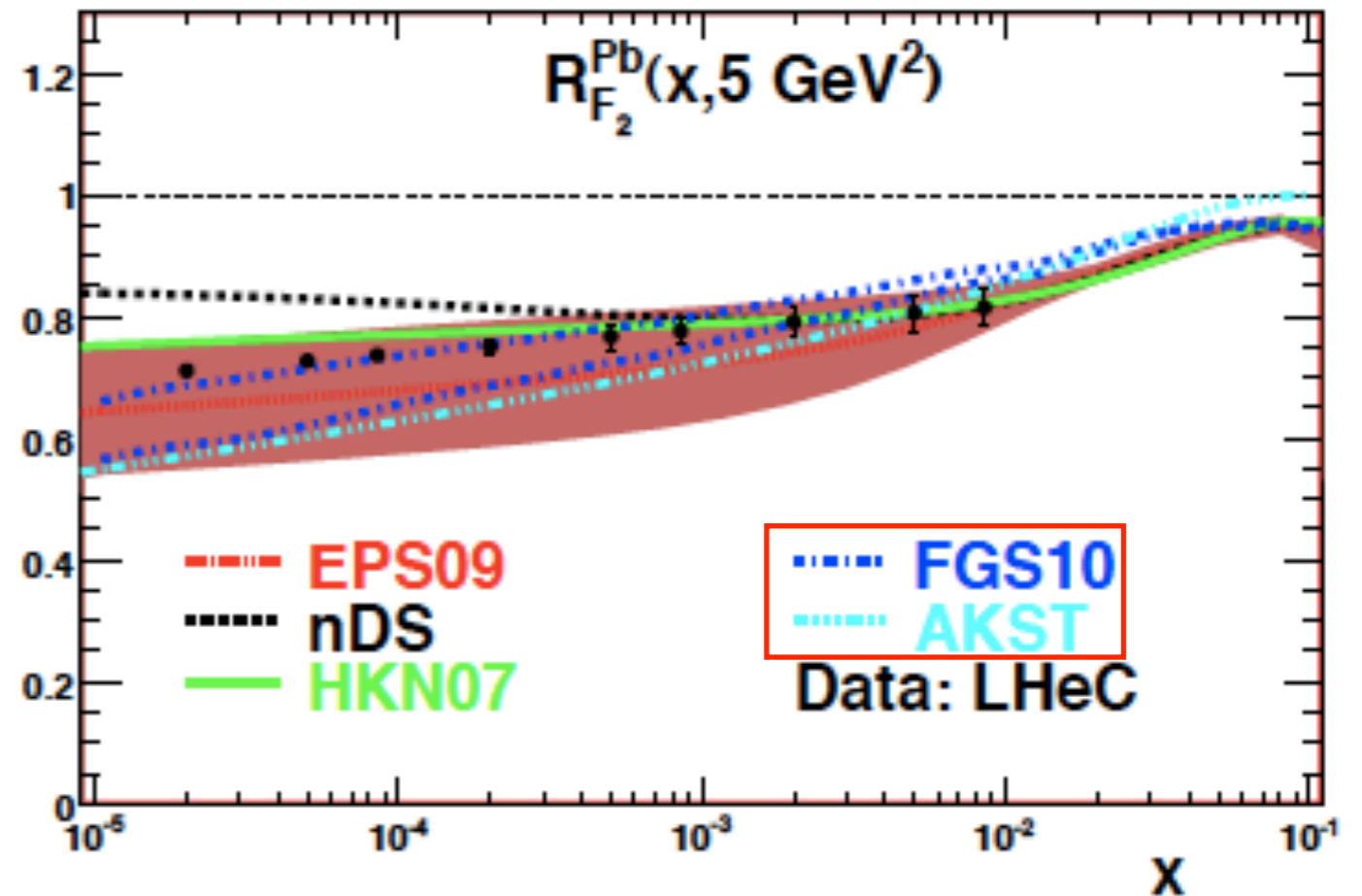


- Limitations at HERA (check of Regge factorisation, size and shape of the diffractive glue) can be overcome with LHeC/FCC-eh:





- Diffraction in ep is linked to nuclear shadowing through basic QFT (Gribov): system size and impact parameter dependence. eD to test and set the 'benchmark' for new effects.

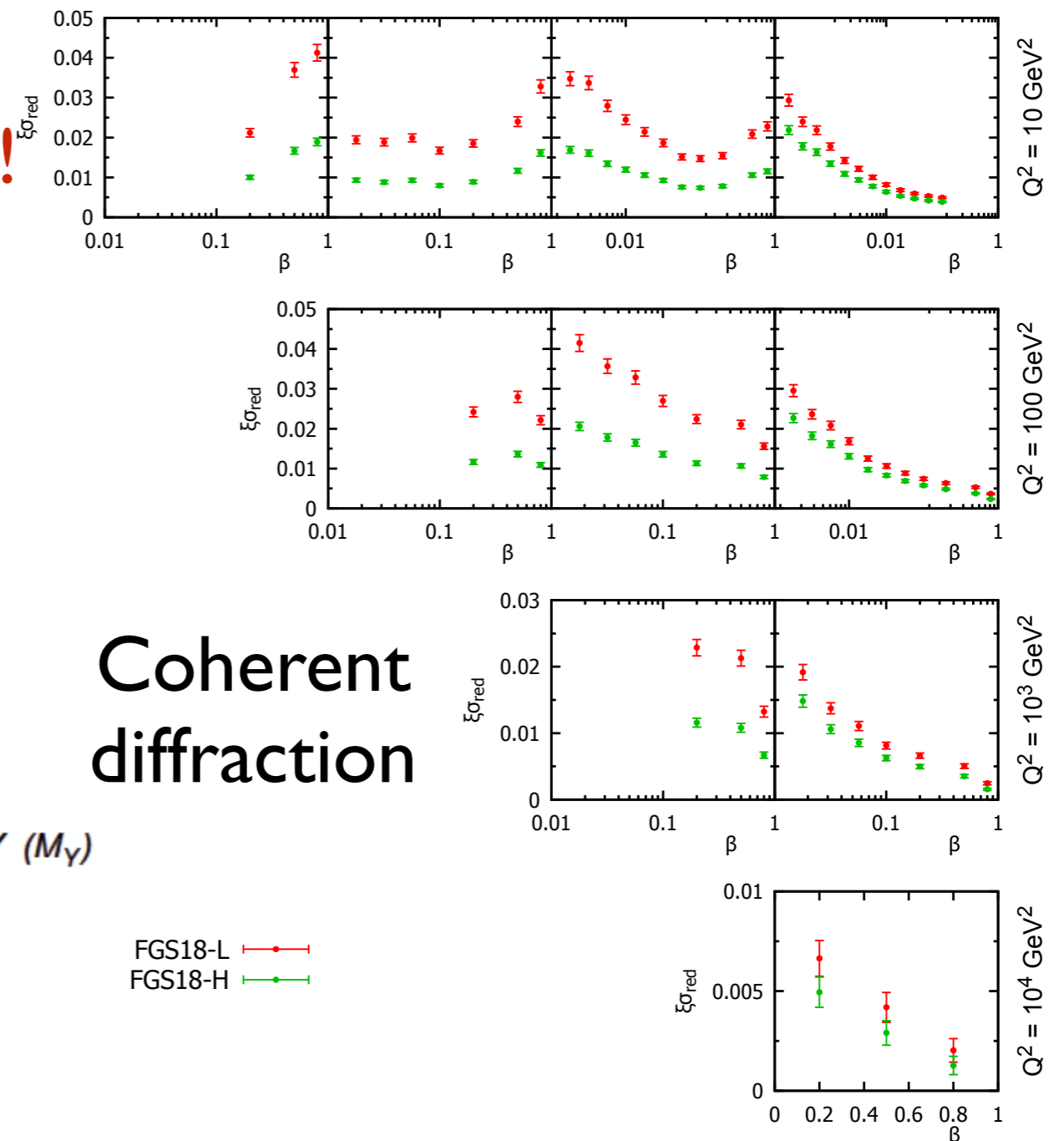


• Diffractive PDFs have never been measured in nuclei, where incoherent diffraction becomes dominant above relatively small  $-t$ .

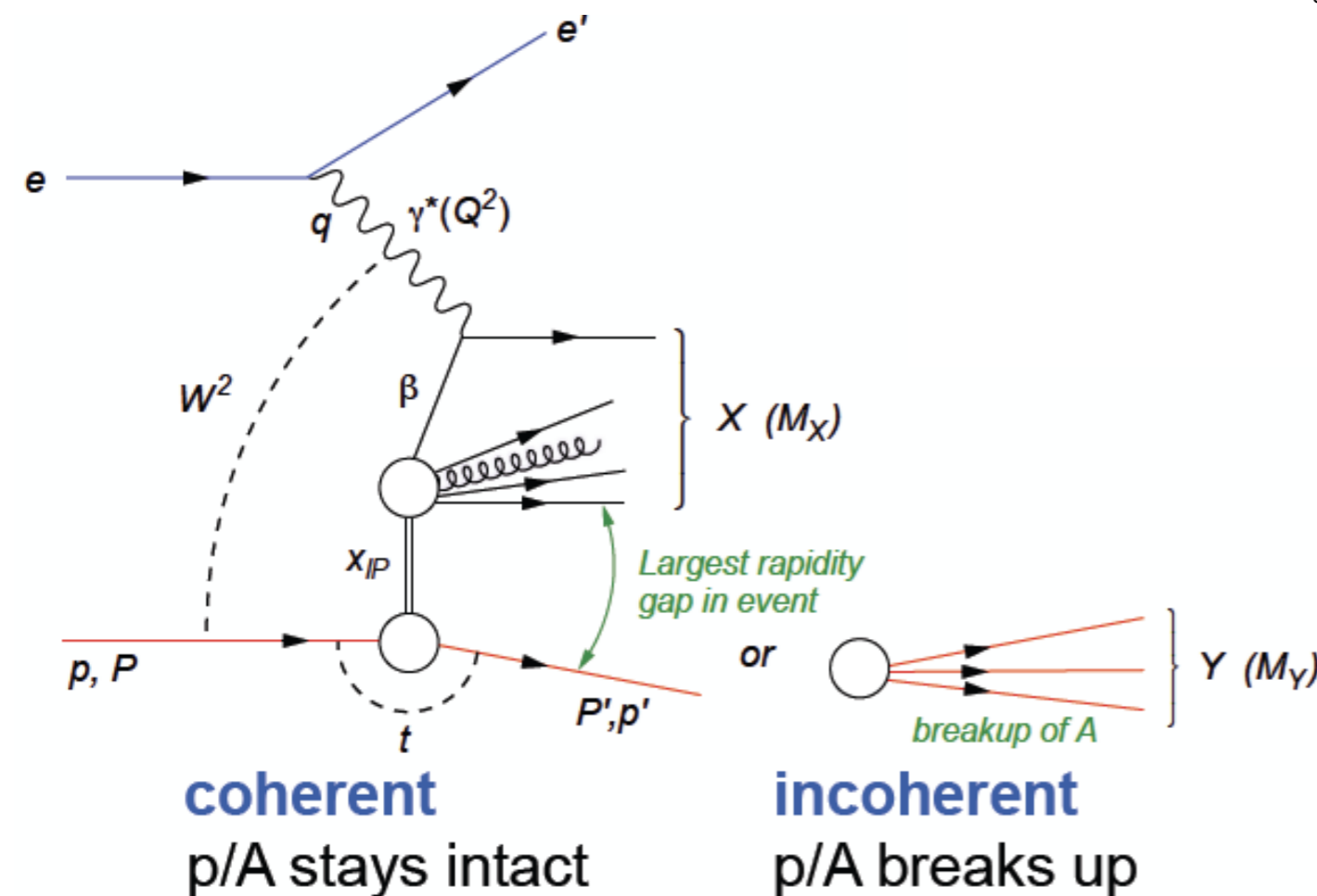
- **Challenging** experimental problem (LPS + ZDC?).
- **Extraction of nDPDFs possible!**

$\xi\sigma_{\text{red}}$  for e-Pb at  $E_{\text{Pb}}/A = 2.76 \text{ TeV}$   $E_e = 60 \text{ GeV}$

$\xi = 0.0001$        $\xi = 0.001$        $\xi = 0.01$        $\xi = 0.1$



Coherent diffraction

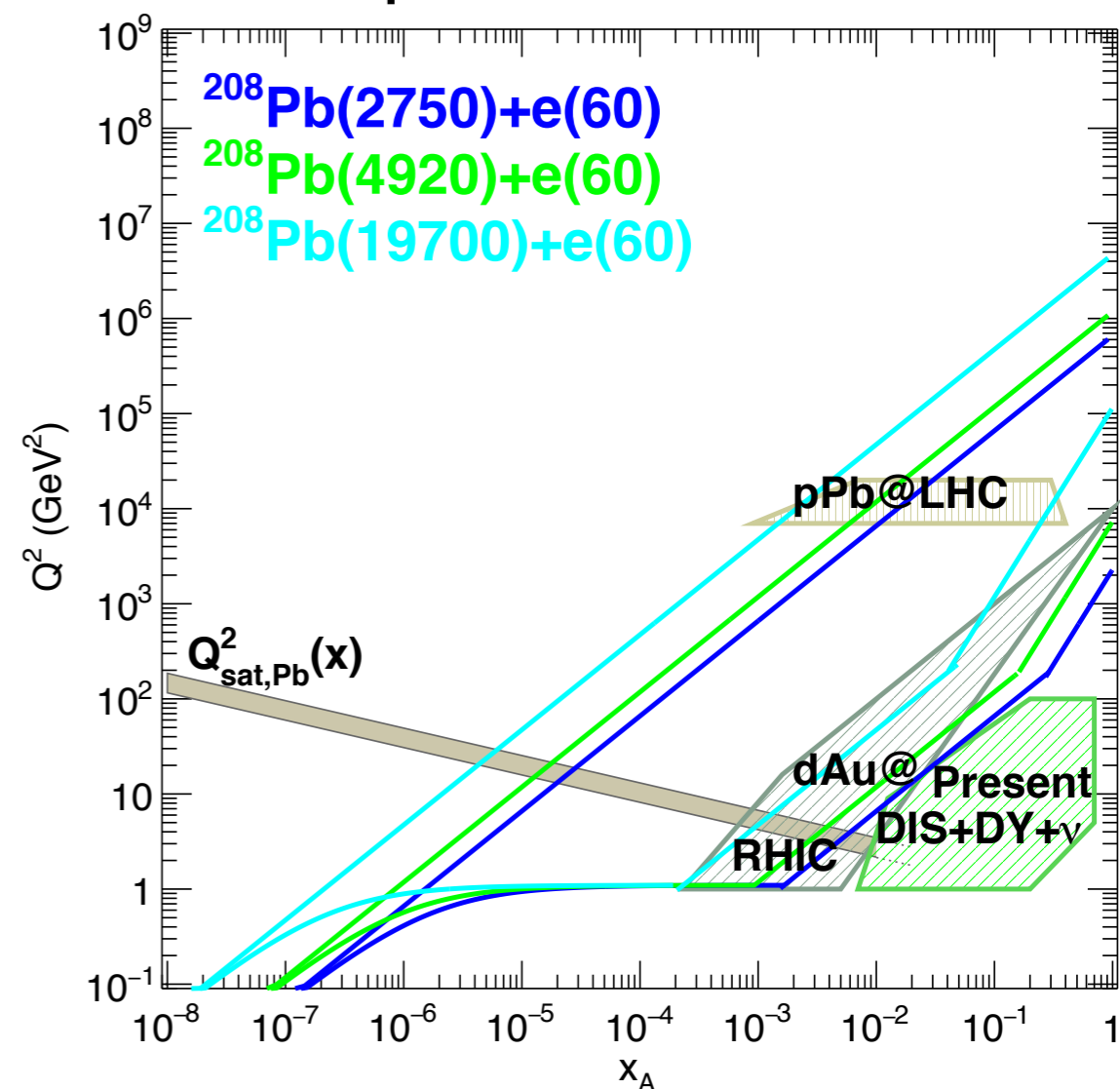


FGS18-L (red)  
FGS18-H (green)



- The LHeC & FCC-eh will explore a completely new region in the  $x$ - $Q^2$  plane, enlarging the one presently explored in DIS by  $\sim 3$ -4 orders of magnitude down in  $x$  and up in  $Q^2$ .

- A precise determination of nuclear inclusive and diffractive PDFs will be possible, that cannot be matched at hadron colliders: PDFs for a single nuclei in a single experiment.



- **Work in progress** (to be ready for the CDR next February):
  - Determination of nPDFs in EPPS16 (Hannu Paukkunen) including c,b.
  - Radiative corrections in ep and eA.
  - Nuclear diffractive PDFs (Wojtek Slominski).
  - Implications of DPDF on nuclear shadowing (Vadim Guzey)?

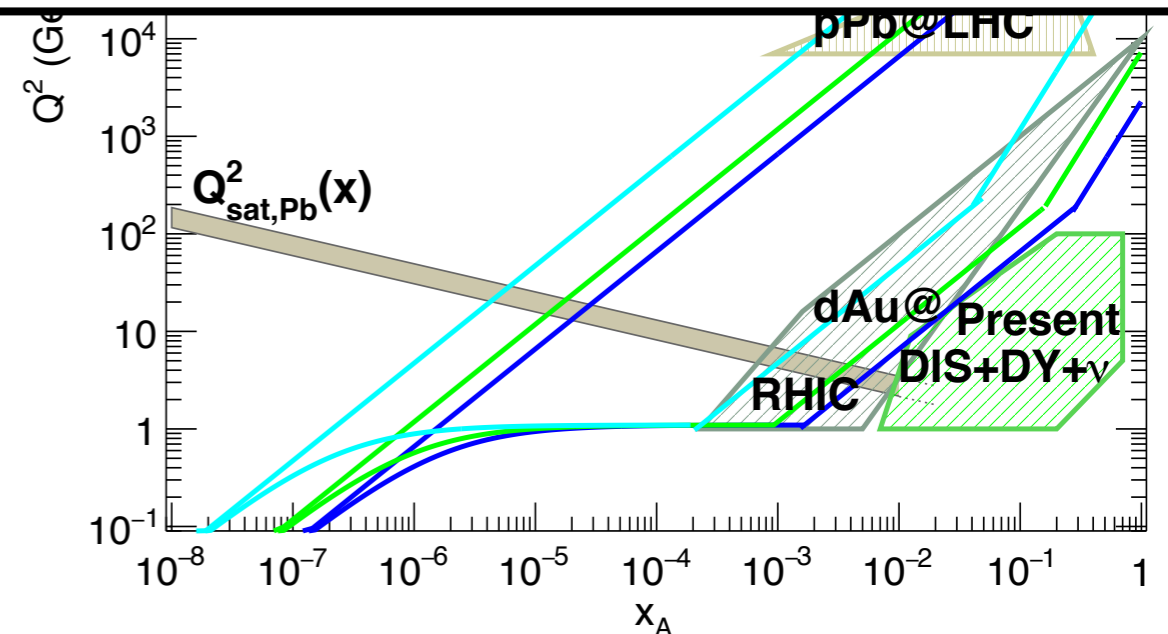
- The LHeC & FCC-eh will explore

<http://lhec.web.cern.ch/>

→ Thanks to Max Klein, Hannu Paukkunen and Pía Zurita for comments, and to Voica Radescu for help with xFitter.

→ Thank you very much for your attention!!!

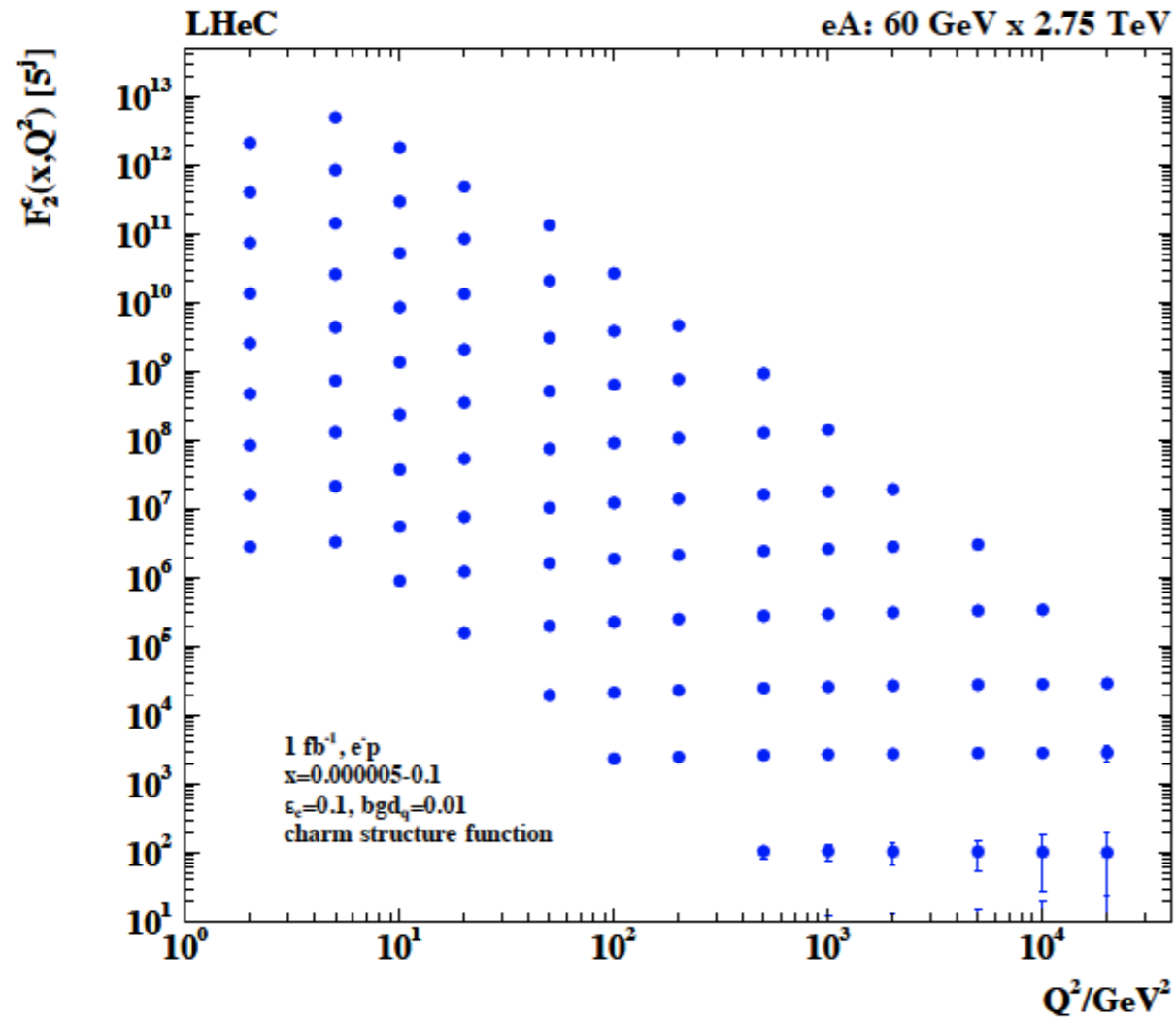
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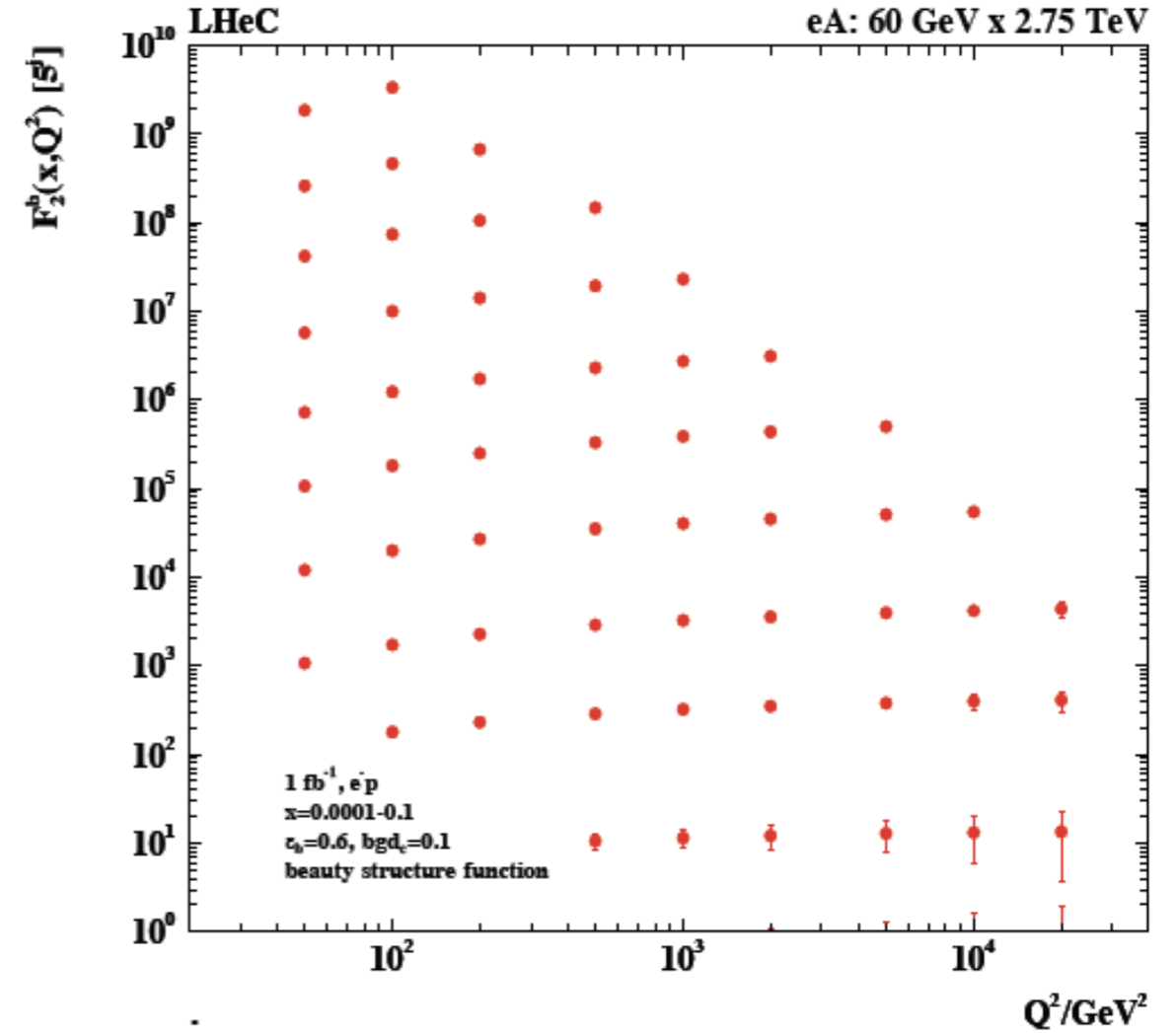
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# Heavy flavours at LHeC:

## Charm in ePb



## Beauty in ePb



M. Klein, DOI: [10.1051/epjconf/201611203002](https://doi.org/10.1051/epjconf/201611203002)

# Backup:

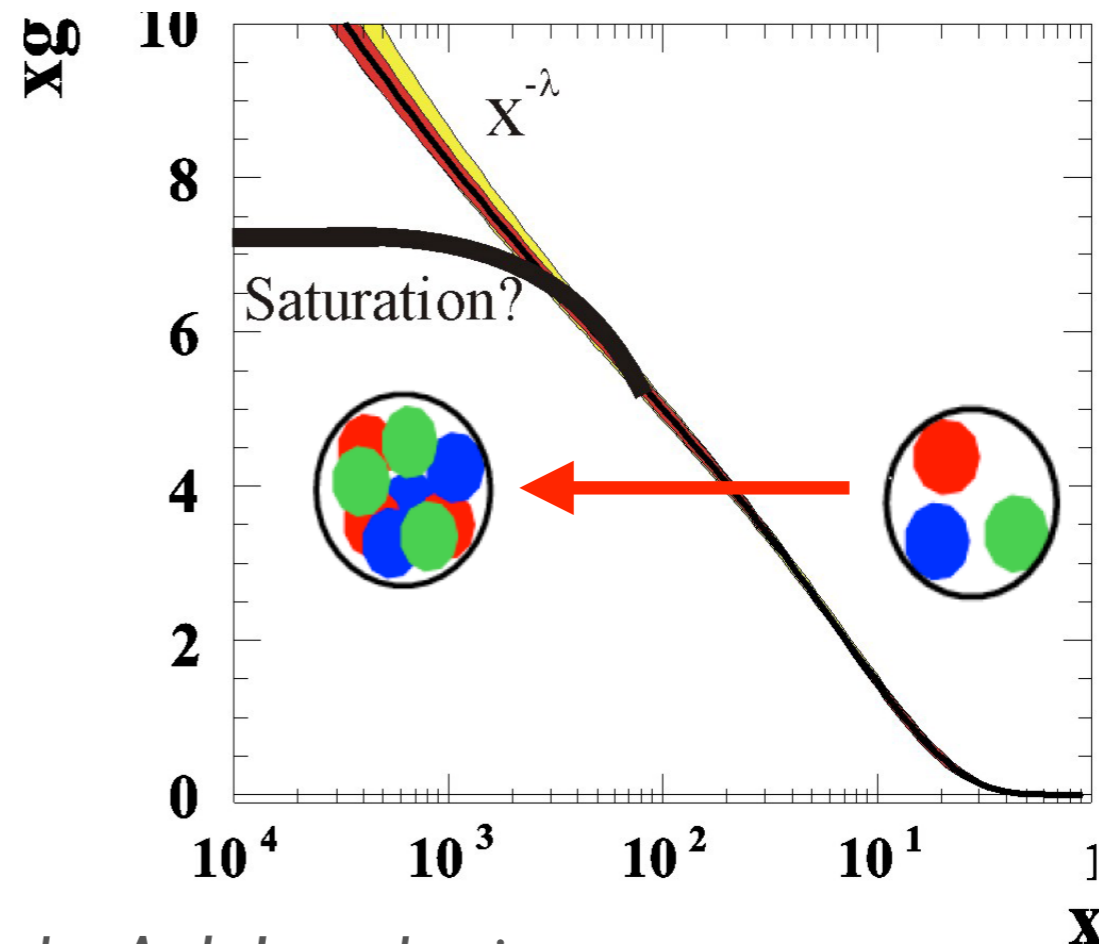
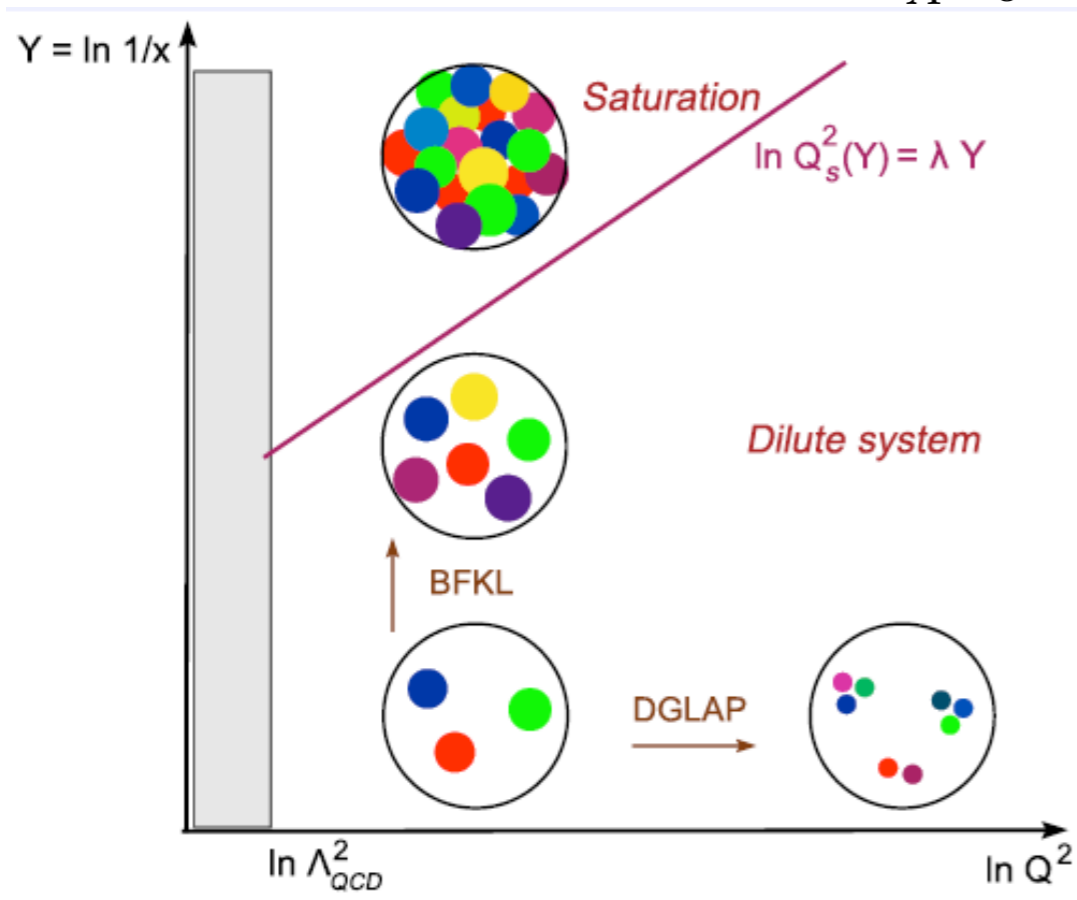
• Standard fixed-order perturbation theory (DGLAP, linear evolution) **must eventually fail**:

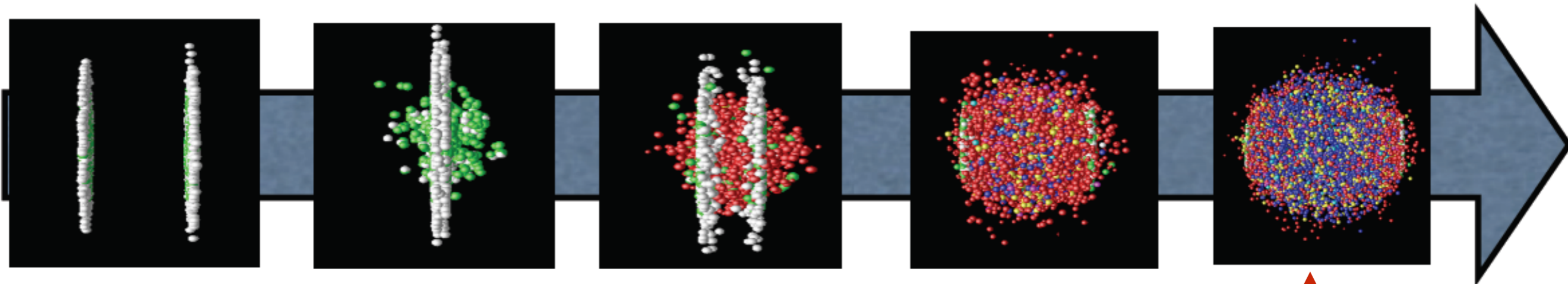
→ Large logs e.g.  $\alpha_s \ln(1/x) \sim 1$ : **resummation** (BFKL, CCFM, ABF, CCSS).

→ High-density:  $x \downarrow, A \uparrow \Rightarrow$  non-linear regime, recombination

balancing splitting: **saturation**, perturbative (CGC) or non.

$$\frac{xG_A(x, Q_s^2)}{\pi R_A^2 Q_s^2} \sim 1 \implies Q_s^2 \propto A^{1/3} x^{-0.3}$$



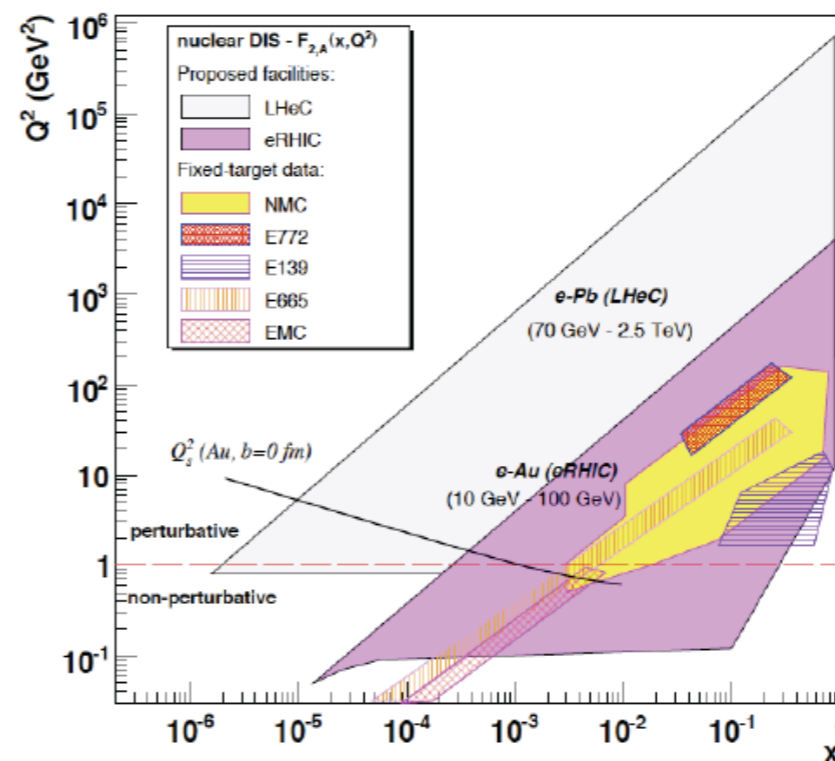
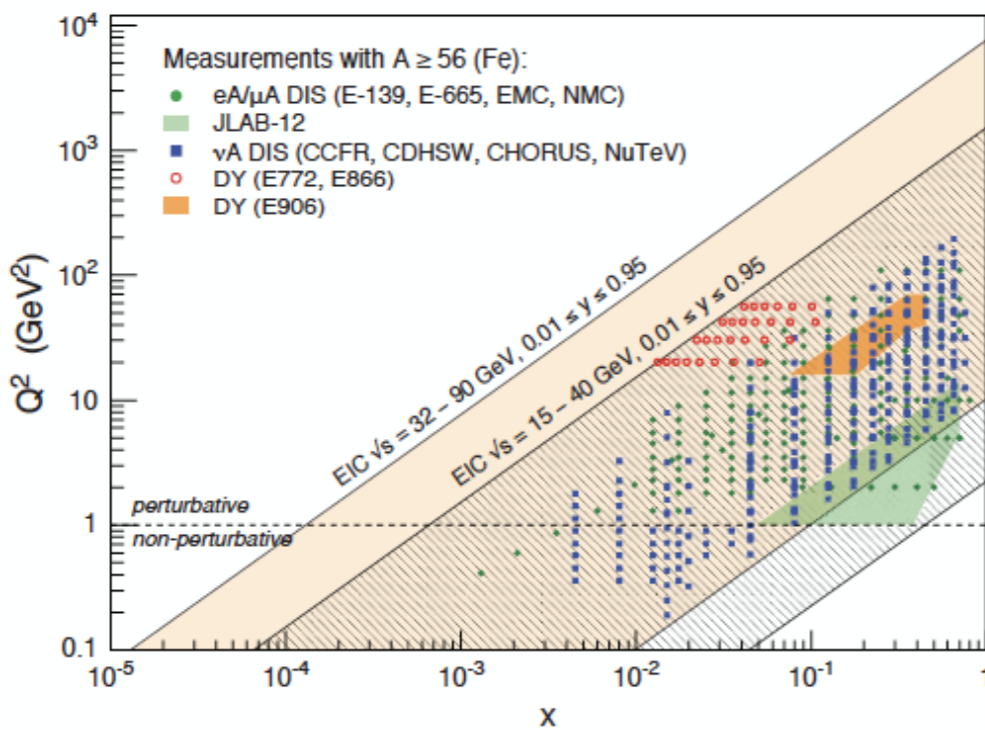
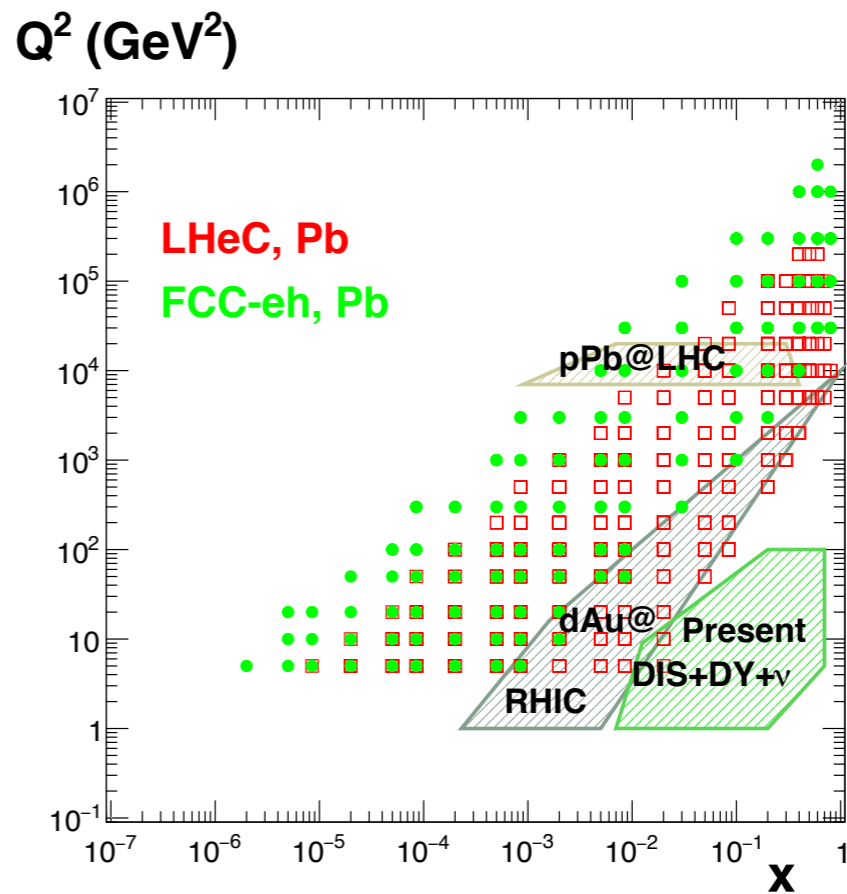
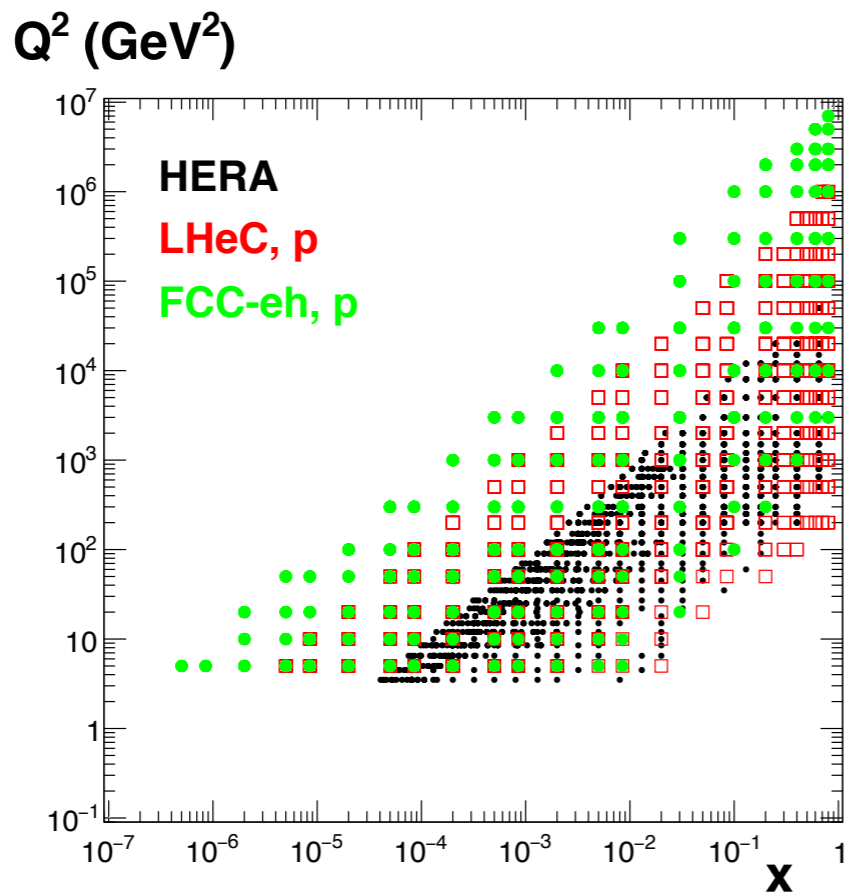


Glucos from saturated nuclei → Glasma? → QGP → Reconfinement

- Nuclear wave function at small  $x$ : **nuclear structure functions.**

- Particle production at the very beginning: which factorisation in eA?
- How does the system behave as  $\sim$  isotropised so fast?: initial conditions for plasma formation to be studied in eA.

- Probing the medium through energetic particles (jet quenching etc.): modification of QCD radiation and hadronization in the nuclear medium.



D'Enterria arXiv:0707.4182

## The LHeC pseudodata

- Assume  $\mathcal{L}_{ep} = 10 \text{ fb}$ ,  $\mathcal{L}_{ePb} = 1 \text{ fb}$  (per nucleon)
- The assumed energy configs:  $\sqrt{s_p} = 7 \text{ TeV}$ ,  $\sqrt{s_{Pb}} = 2.75 \text{ TeV}$  (per nucleon) on  $E_e = 60 \text{ GeV}$  electrons.
- The pseudodata are here obtained from ratios of reduced cross sections  $\sigma^i$  and relative point-to-point ( $\delta_{\text{uncor.}}^i$ ) and normalization ( $\delta_{\text{norm.}}^i$ ) uncertainties as

$$R_i = R_i(\text{EPS09}) \times \left[ 1 + \delta_{\text{uncor.}}^i r^i + \delta_{\text{norm.}}^i r^{\text{norm.}} \right]$$

where

$$R_i(\text{EPS09}) = \frac{\sigma_{ePb}^i(\text{CTEQ6.6} + \text{EPS09})}{\sigma_{ep}^i(\text{CTEQ6.6})},$$

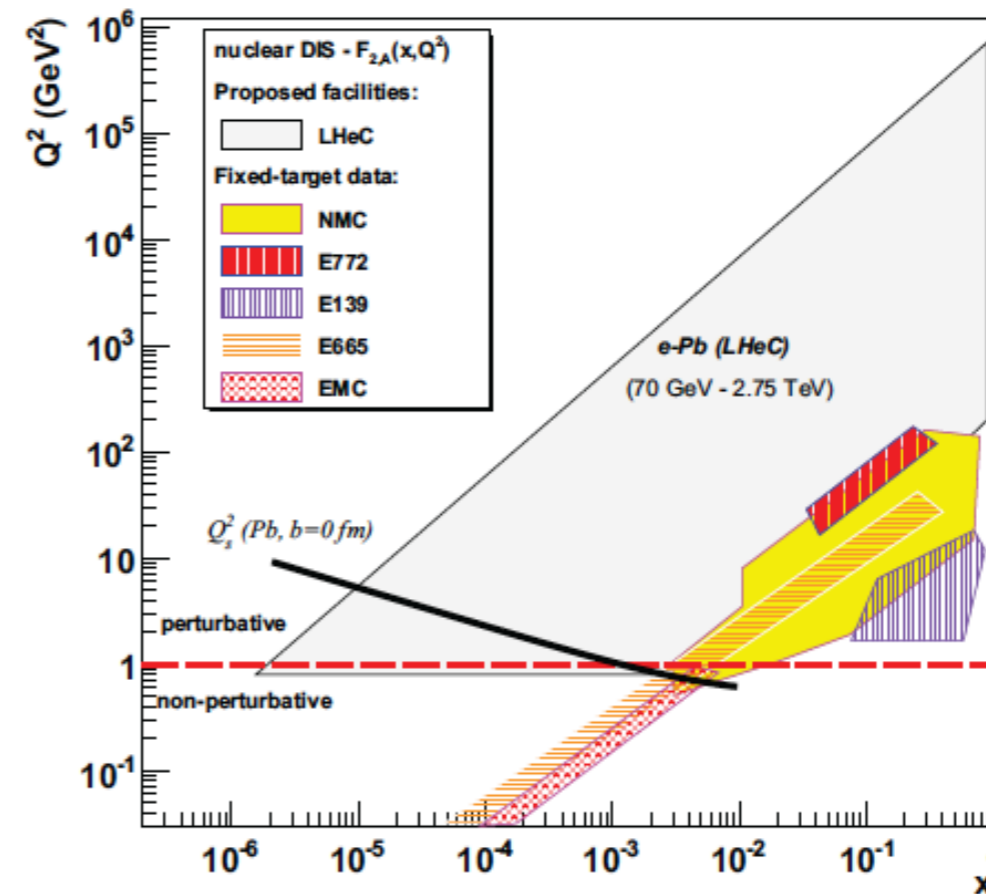
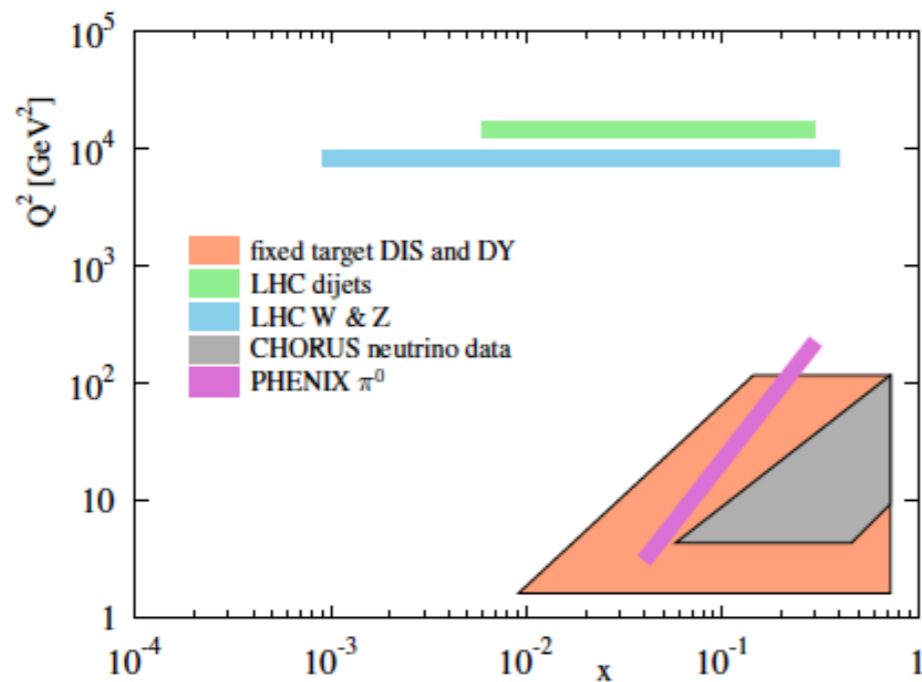
and  $r^i$  and  $r^{\text{norm.}}$  are Gaussian random numbers.

- In EPS09  $R_{uV} \approx R_{dV}$ ,  $R_{\bar{u}} \approx R_{\bar{d}} \approx R_{\bar{s}}$  (free in EPPS16, but would not expect large deviations from this)



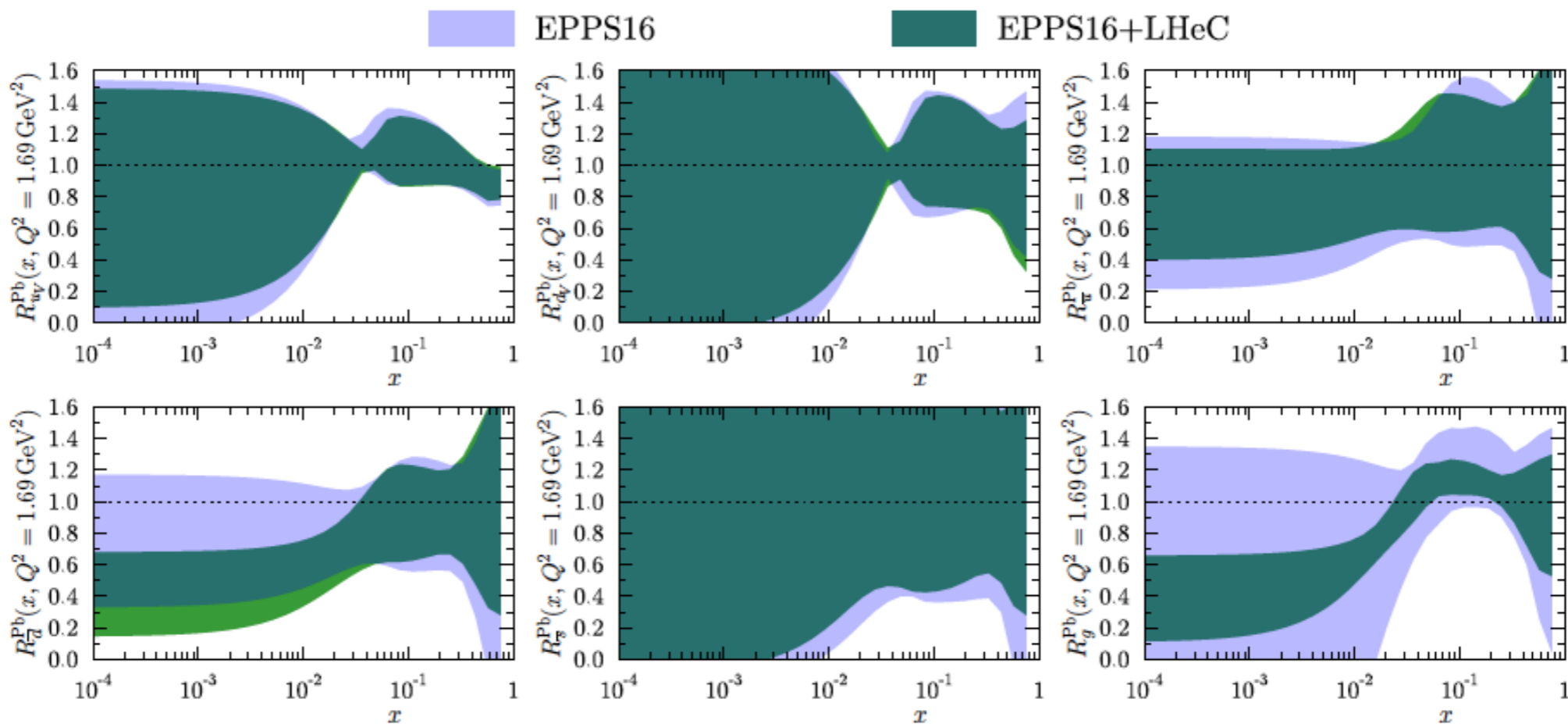
## The analysis framework

- The fit framework same as in the EPPS16 analysis [EPJ C77, 163]
- Include the same data as in EPPS16 plus LHeC (NC and CC) pseudo data.
- Hessian uncertainty analysis with  $\Delta\chi^2 = 52$  (as in EPPS16)



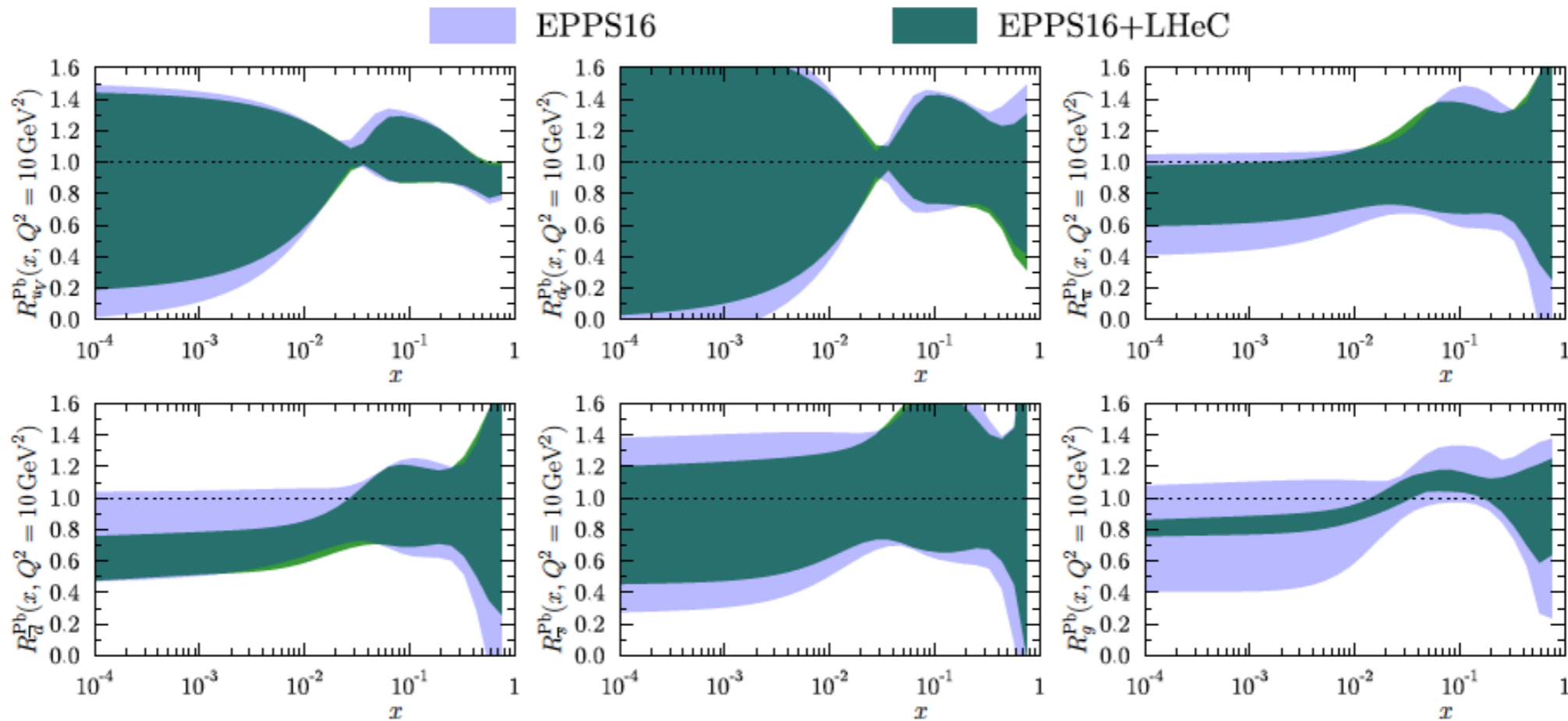
## The effect of LHeC pseudodata

- The improvement after adding the LHeC data ( $Q^2 = 1.69 \text{ GeV}^2$ )



## The effect of LHeC pseudodata

- The improvement after adding the LHeC data ( $Q^2 = 10 \text{ GeV}^2$ )



## The effect of LHeC pseudodata

- Why it's so hard to pin down the flavor dependence?
- Take the valence up-quark distribution  $u_V^A$  as an example:

$$u_V^A = \frac{Z}{A} R_{uV} u_V^{\text{proton}} + \frac{A-Z}{A} R_{dV} d_V^{\text{proton}}$$

- Write this in terms of average modification  $R_V$  and the difference  $\delta R_V$

$$R_V \equiv \frac{R_{uV} u_V^{\text{proton}} + R_{dV} d_V^{\text{proton}}}{u_V^{\text{proton}} + d_V^{\text{proton}}}, \quad \delta R_V \equiv R_{uV} - R_{dV}$$

$$u_V^A = R_V \left( \frac{Z}{A} u_V^{\text{proton}} + \frac{A-Z}{A} d_V^{\text{proton}} \right) + \delta R_V \left( \frac{2Z}{A} - 1 \right) \frac{u_V^{\text{proton}}}{1 + u_V^{\text{proton}} / d_V^{\text{proton}}}$$

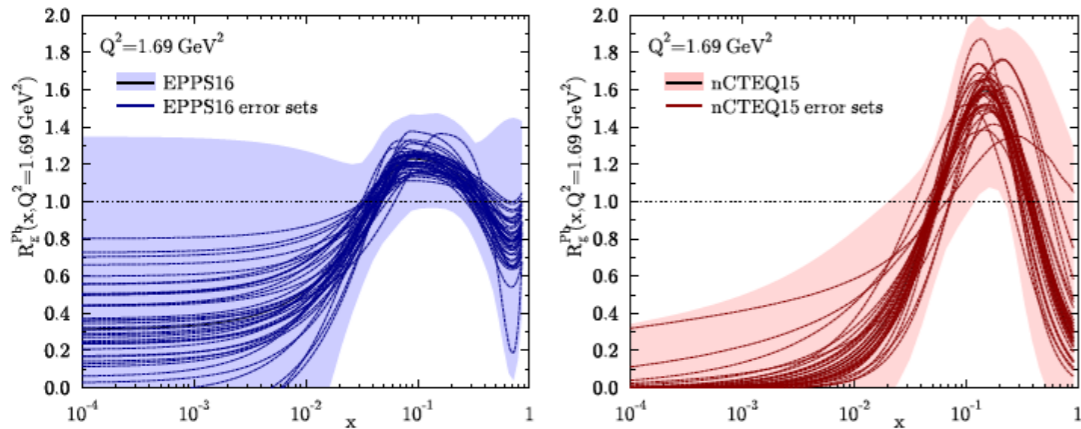
Leading term

"Correction term"

- The effects of flavour separation (i.e.  $\delta R_V$  here) are suppressed in cross sections — but also so in most of the nPDF applications.

$$R^{\text{EPS09}}(x) = \begin{cases} a_0 + a_1(x - x_a)^2 & x \leq x_a \\ b_0 + b_1x^\alpha + b_2x^{2\alpha} + b_3x^{3\alpha} & x_a \leq x \leq x_e \\ c_0 + (c_1 - c_2x)(1 - x)^{-\beta} & x_e \leq x \leq 1 \end{cases}$$

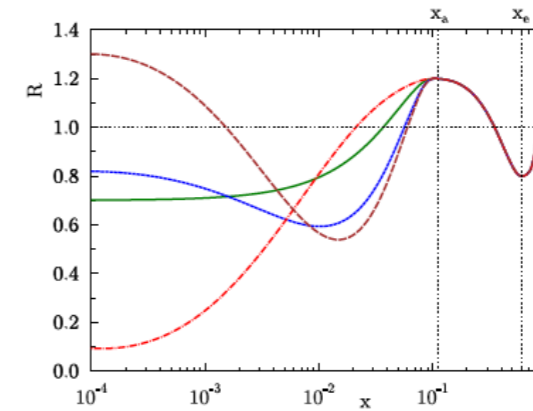
$$R^{\text{nCTEQ15}}(x) = [c_0x^{c_1}(1 - x)^{c_2}e^{c_3x}(1 + e^{c_4x})^{c_5}] / f^P(x)$$



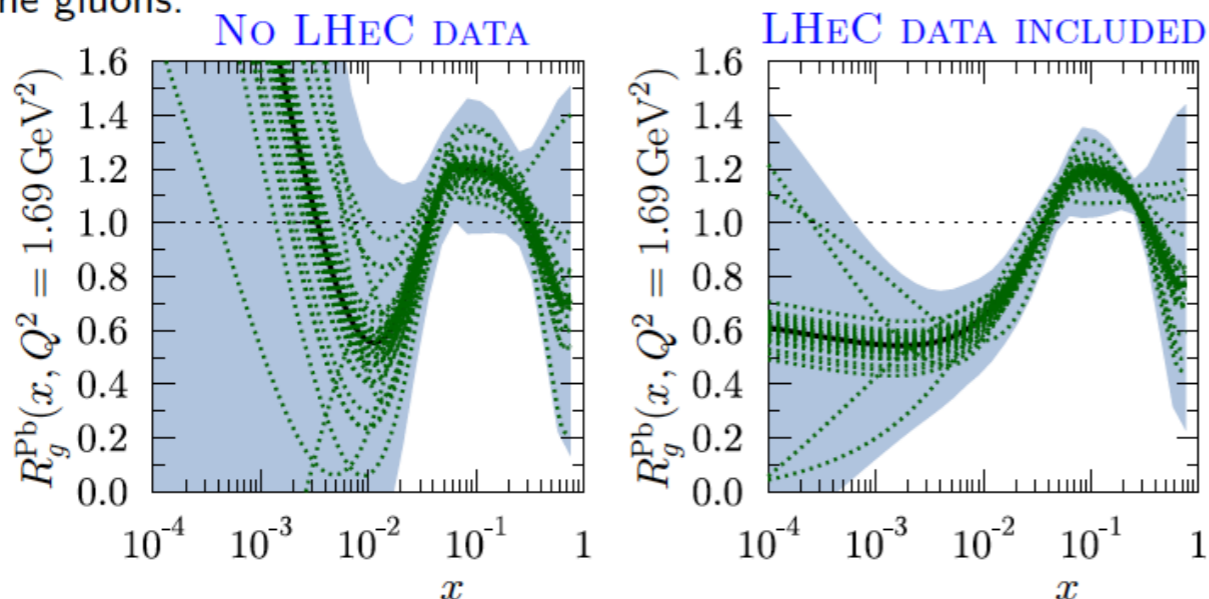
$$R(x \leq x_a) = a_0 + a_1(x - x_a)^2 + \sqrt{x}(x_a - x) \left[ a_2 \log\left(\frac{x}{x_a}\right) + a_3 \log^2\left(\frac{x}{x_a}\right) + a_4 \log^3\left(\frac{x}{x_a}\right) + \dots \right]$$

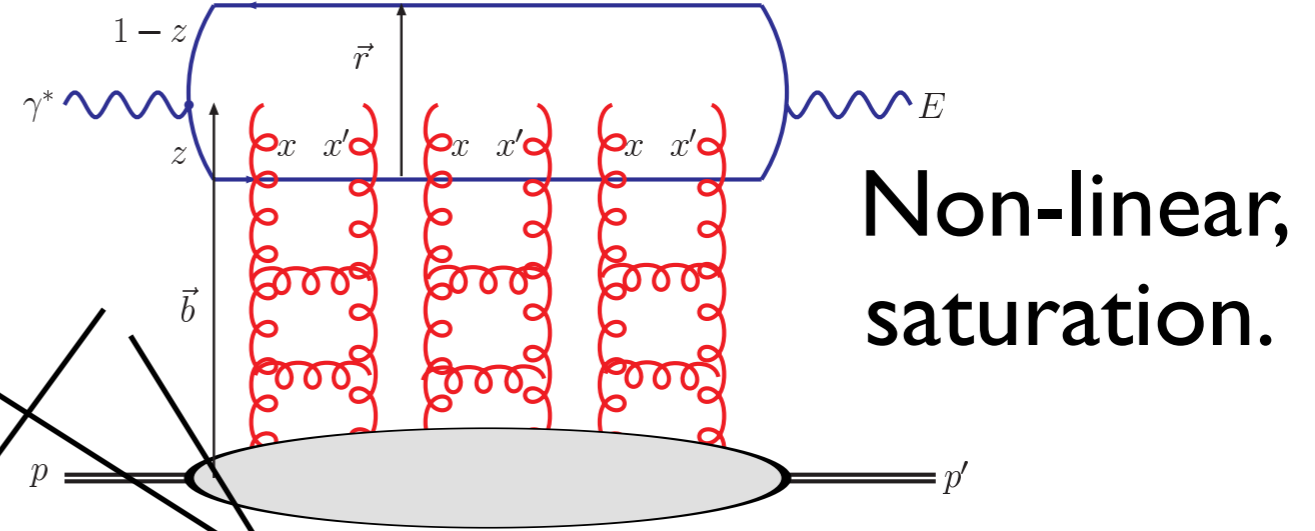
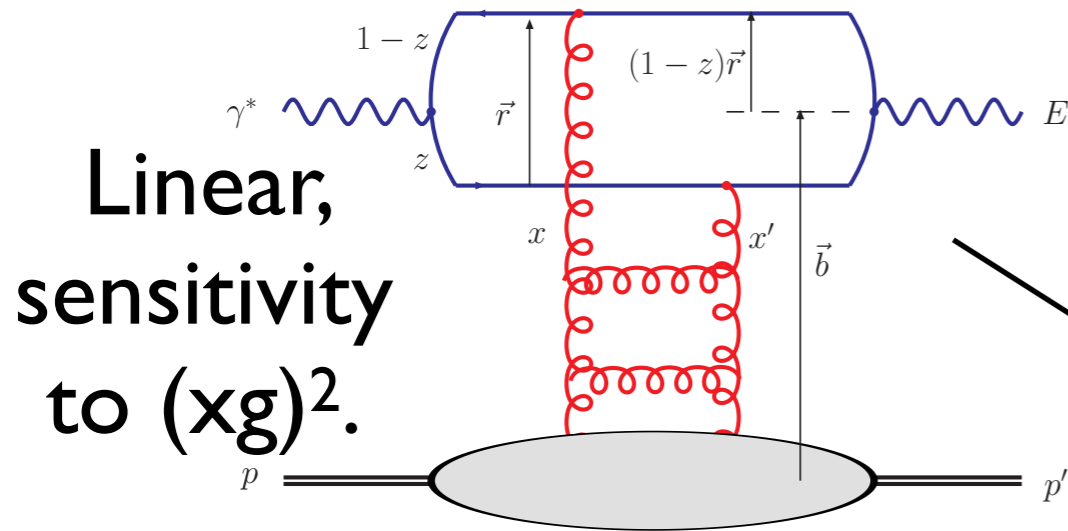
or

$$R(x \leq x_a) = a_0 + (x - x_a)^2 \left[ a_1 + a_2x^\alpha + a_3x^{2\alpha} + a_4x^{3\alpha} + \dots \right], \alpha \ll 1$$

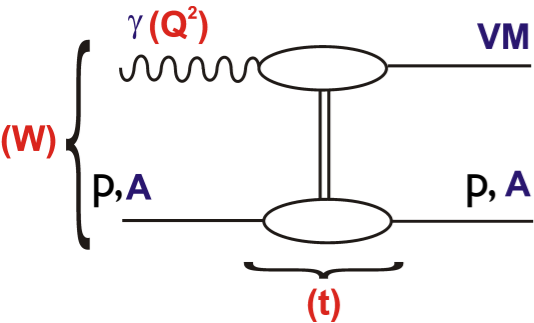


- Would need Monte-Carlo methods to more reliably map the uncertainties  
 $\Rightarrow$  Further work needed
- Despite all the shortcomings, a typical result using a more flexible form for the gluons:

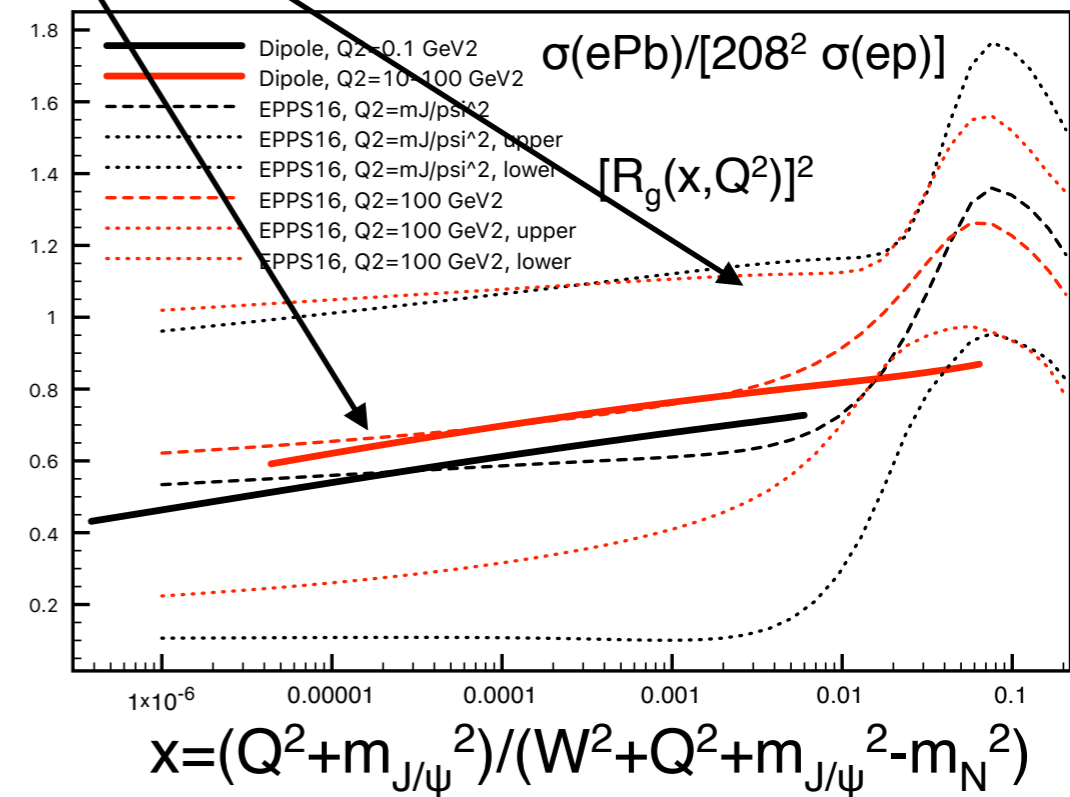
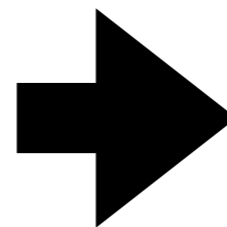
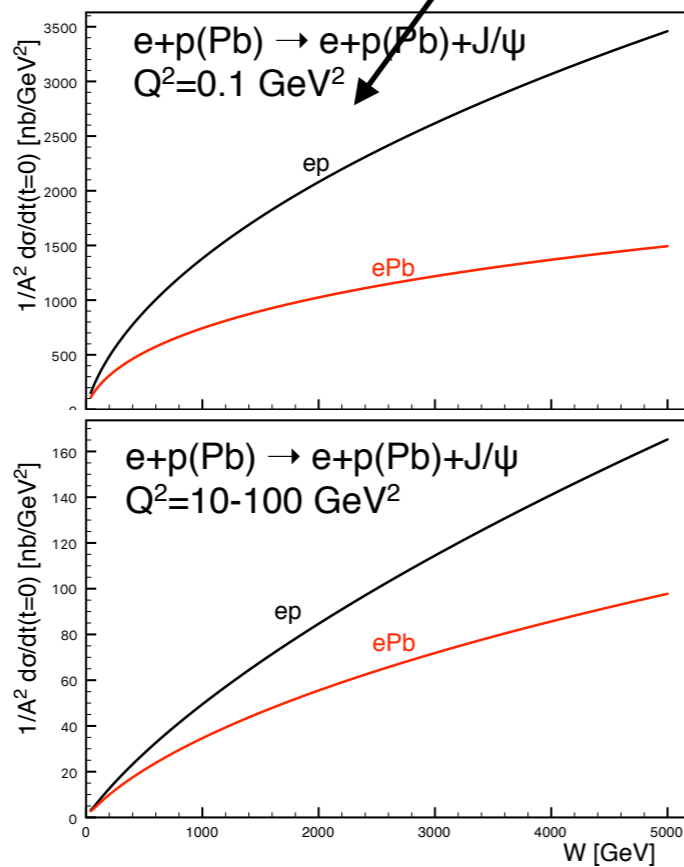




- The magnitude of nuclear shadowing needs not be different in collinear and non-collinear approaches.



Coherent diffractive VM production



Mantysaari, Paukkunen