



**Strong phase at colliders:**

# new physics opportunities for $t\bar{t}$ resonance searches and Higgs physics

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Particle Physics Seminar @ CERN-TH

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Based on M. Carena, ZL, [arXiv:1608.07282](https://arxiv.org/abs/1608.07282), JHEP  
and J. Campbell, M. Carena, R. Harnik, ZL, [arXiv:1704.08259](https://arxiv.org/abs/1704.08259)

# Motivation

Heavy scalars very common in new physics models (SUSY, 2HDM, Composite Models, Hidden-valley, Gauge symmetry extensions, scalar-assisted EWBG, etc.)

Couple to fermions hierarchically, decay dominantly into  $t\bar{t}$

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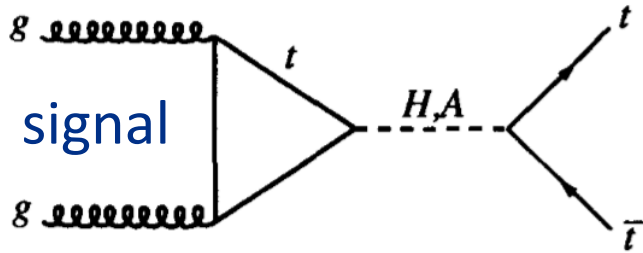


Starting with a very minimal baseline model

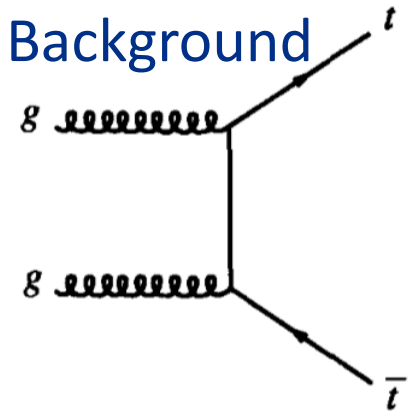
$$\mathcal{L}^{Yukawa} \supset \frac{y}{\sqrt{2}} \bar{Q}_{3L} \tilde{H} t_R + h.c.$$
$$\mathcal{L}^{Yukawa} \xrightarrow{\text{loop-induced}} -\frac{1}{4} g_{Sgg}(\hat{S}) G_{\mu\nu} G^{\mu\nu} S$$

denote the neutral CP-even component  $S$ , after EWSB; similar expressions for CP-odd and CP-admixture states

# Unfamiliar look of heavy Scalars

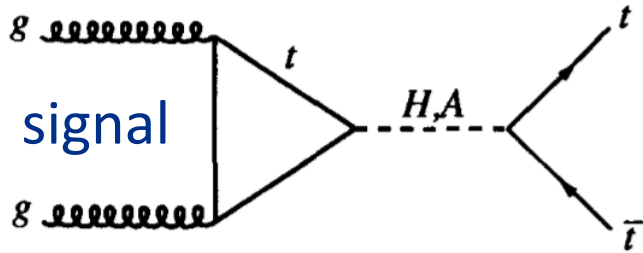


LHC being top factory, the  $t\bar{t}$  statistics is very good.  $S/\sqrt{B}$  is quite reasonable. However, the challenges lie in the interference effect.



Plus s- and u- channel  
Plus s-channel  $q\bar{q} \rightarrow t\bar{t}$

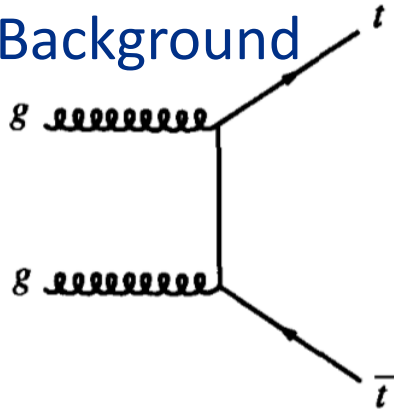
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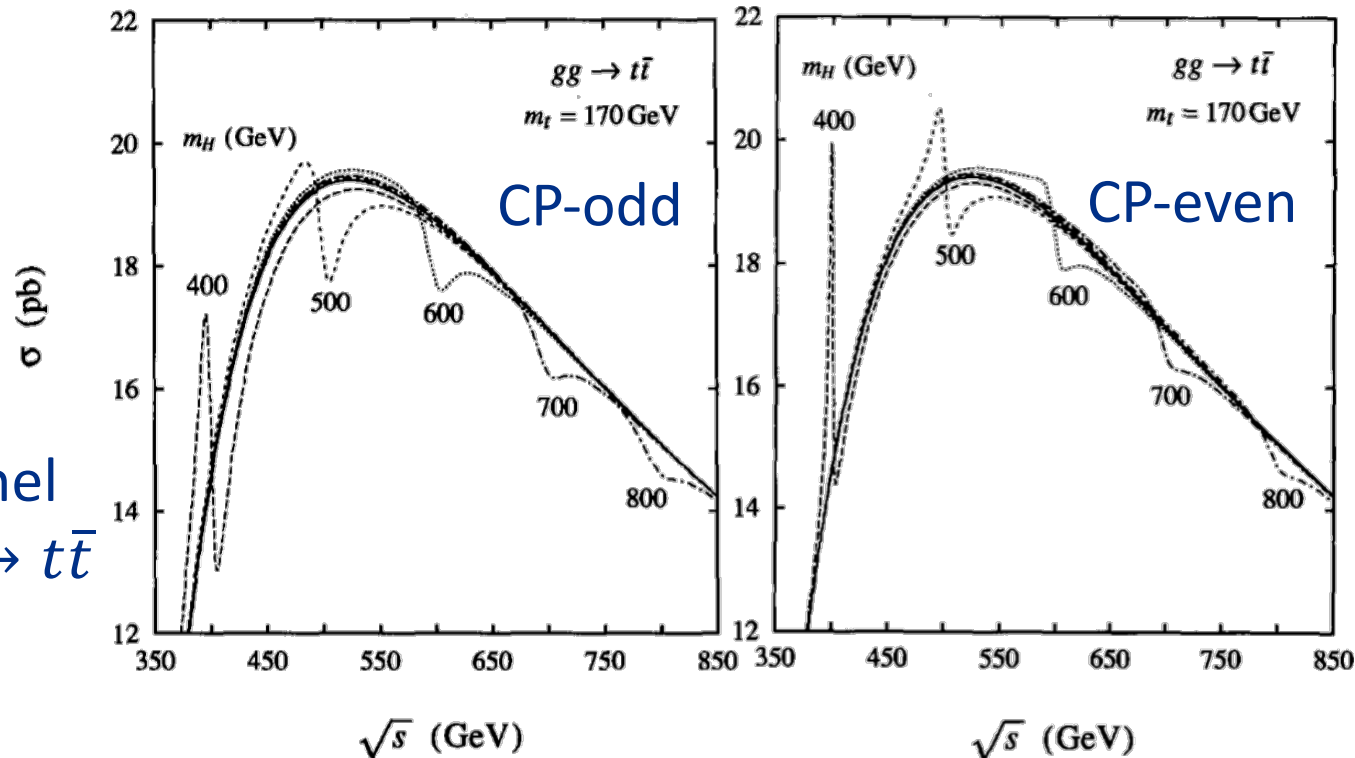
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D. Dicus, A. Stange, S. Willenbrock, 1991

## Background



Plus s- and u- channel  
Plus s-channel  $q\bar{q} \rightarrow t\bar{t}$



See also recent work by N. Craig, F. D'Eramo, P. Drapper, S. Thomas, H. Zhang [arXiv:1504.04630](https://arxiv.org/abs/1504.04630) and also Jung, Sung, Yoon [arXiv:1505.00291](https://arxiv.org/abs/1505.00291), S. Gori, I.-W. Kim, N. Shah, K. Zurek [arXiv:1602.02782](https://arxiv.org/abs/1602.02782), M. Carena, ZL, [arXiv:1608.07282](https://arxiv.org/abs/1608.07282)

# Sketching the interference

$$A_{sig} = c_{sig} \frac{\hat{s}}{\hat{s} - m^2 + i \Gamma m} = c_{sig} P(\hat{s})$$

$A_{bkg} = c_{bkg}$  (slowly varying, treated as constant;  
redefine  $c_{sig}$  respectively to keep  $c_{bkg}$  real for simplicity)

$$\begin{aligned} |A|^2 &= |A_{sig} + A_{bkg}|^2 \\ &= |A_{sig}|^2 + |A_{bkg}|^2 + 2\text{Re}[A_{sig}A_{bkg}^*] \\ &= B.W. + BKG \\ &\quad + 2\text{Re}[c_{sig}]c_{bkg}\text{Re}[P(\hat{s})] \\ &\quad - 2\text{Im}[c_{sig}]c_{bkg}\text{Im}[P(\hat{s})] \end{aligned}$$



# Sketching the interference



$$\frac{\hat{s}}{(\hat{s} - m_S^2) + i\Gamma_S m_S} \approx \frac{m_S}{\Gamma_S} \frac{2\Delta - i}{4\Delta^2 + 1}$$

$$\text{with } \Delta \equiv \frac{\hat{s} - m_S^2}{2m_S\Gamma_S} \approx \frac{\sqrt{\hat{s}} - m_S}{\Gamma_S} \text{ for } \frac{\hat{s}}{m_S^2} - 1 \ll 1.$$

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Background real

Re. Int.– Interference from the real part of the propagator

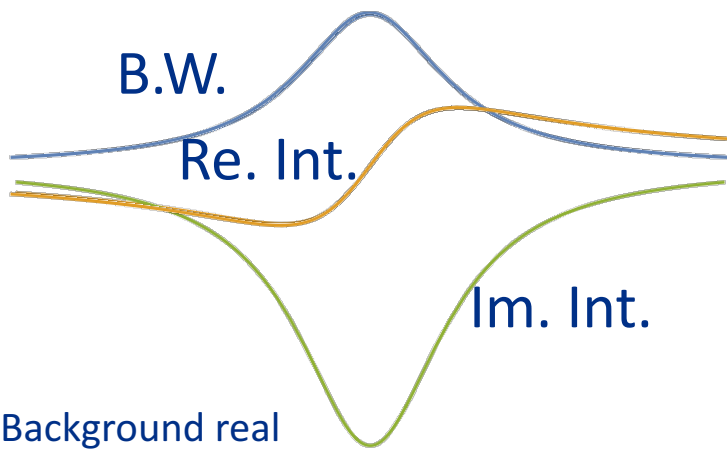
- normal interference, parton level no contribution to the rate, shift the mass peak
- When convoluting with PDF, may generate residual contribution to signal rate, see, e.g., S. Martin [arXiv:1606.03026](https://arxiv.org/abs/1606.03026);
- conventional wisdom, interference only important when width is large)

$$A_{sig} = c_{sig} \frac{\hat{s}}{\hat{s} - m^2 + i\Gamma m} = c_{sig} P(\hat{s})$$

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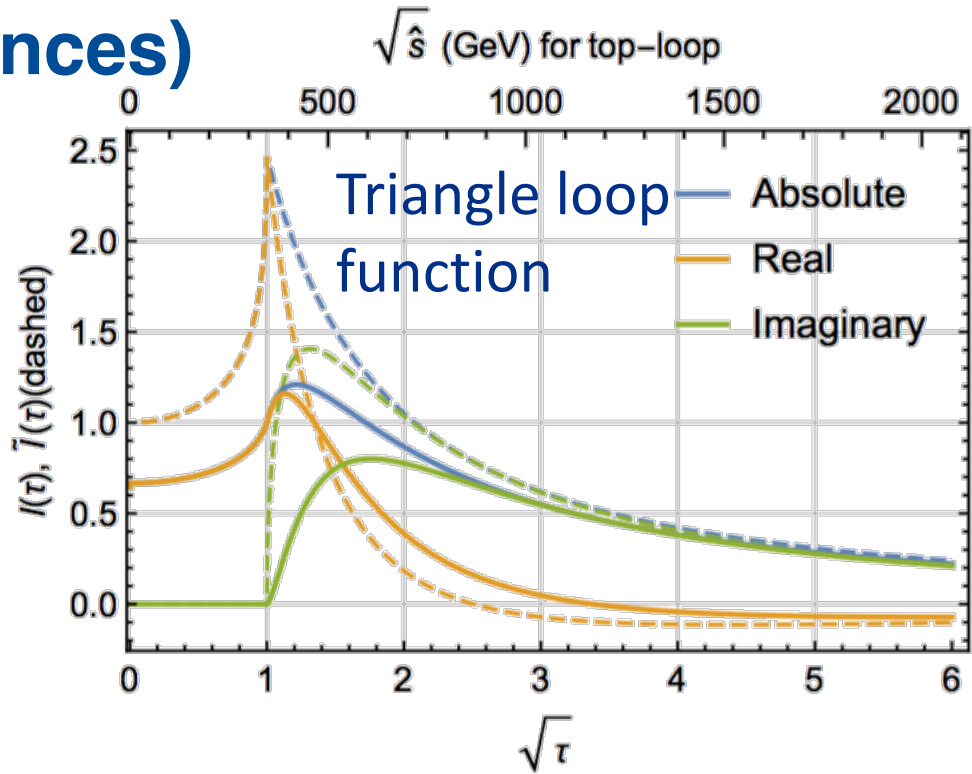
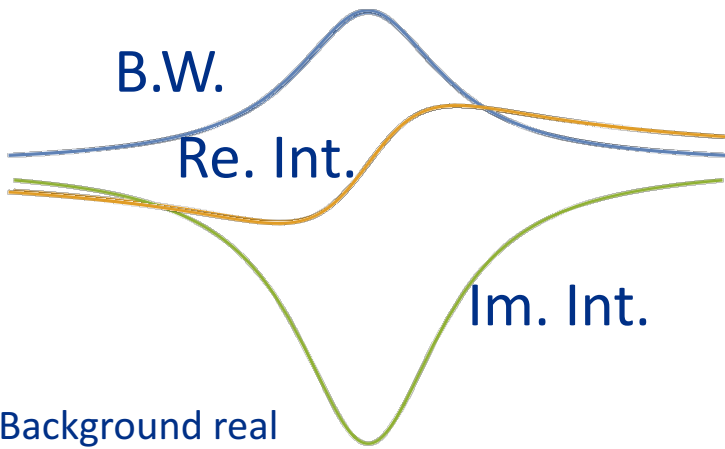
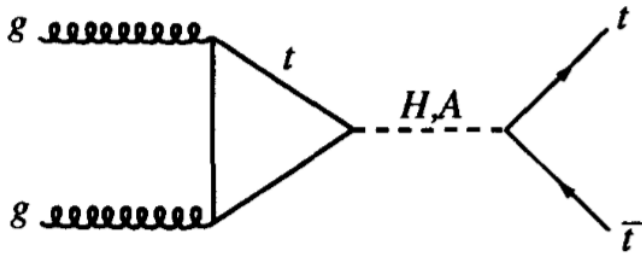
Im. Int.– Interference from the imaginary part of propagator (rare case, changes signal rate)

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# Challenges (interferences)

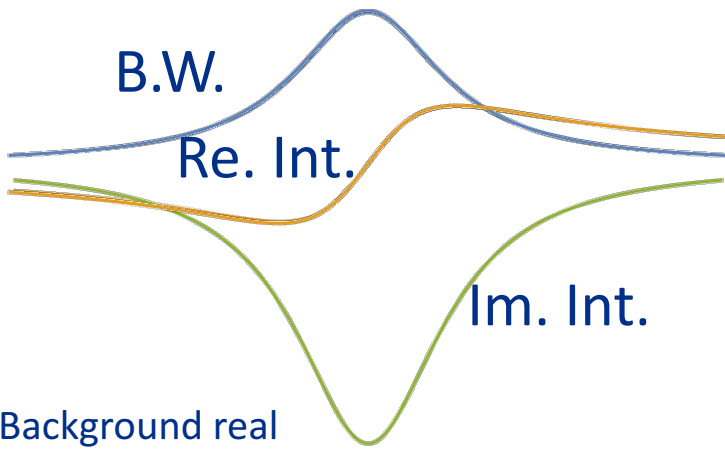
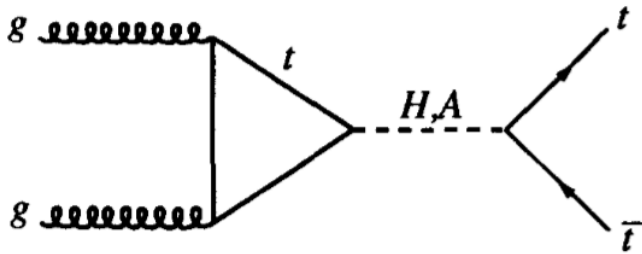


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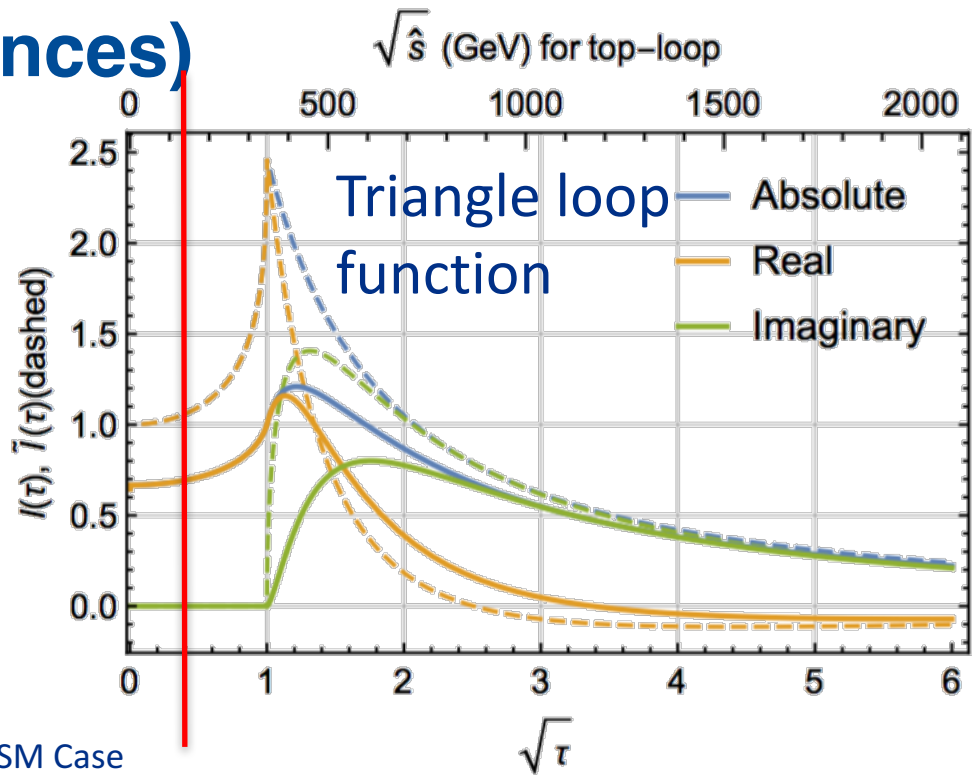
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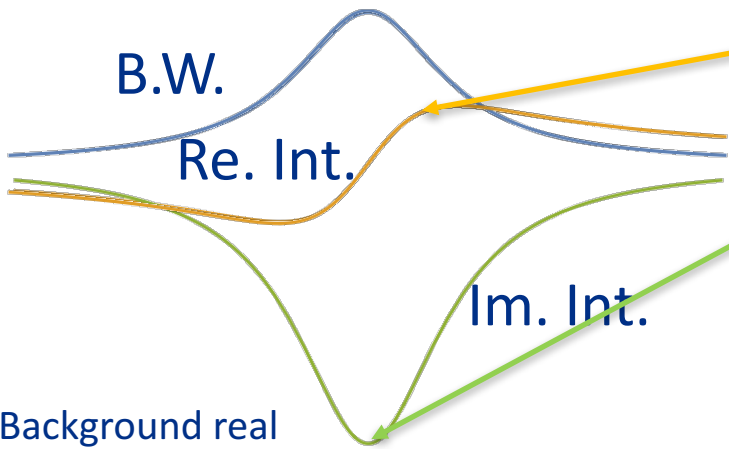
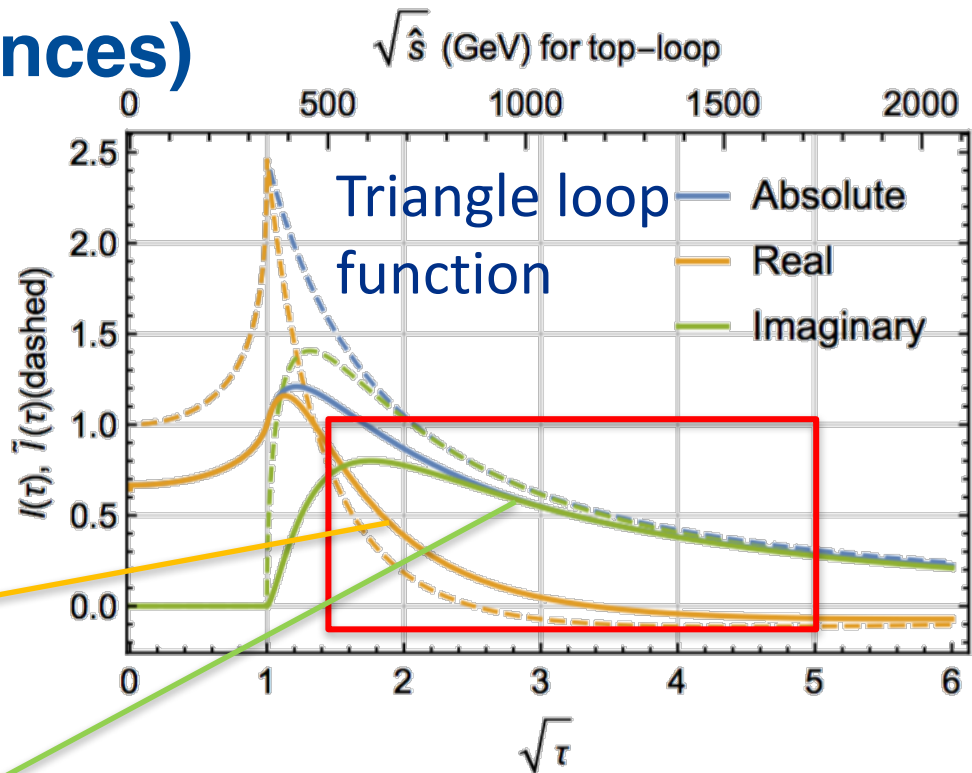
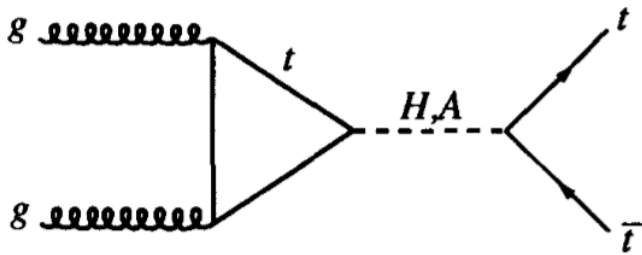
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SM Case  
real and slowly varying  
“heavy (chiral) fermion  
decoupling theorem” (with  
Yukawa proportional to the mass)

# Challenges (interferences)



Once across the threshold, imaginary piece arises drastically and the real piece decreases.

Background real

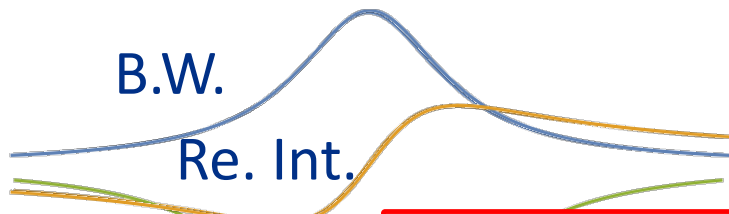
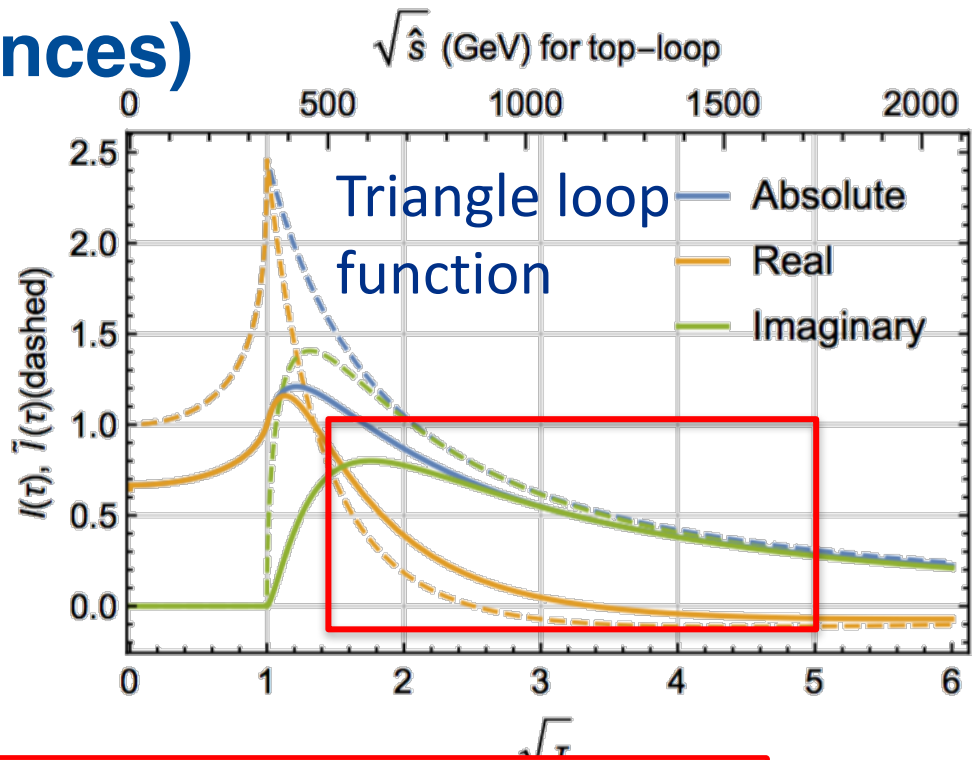
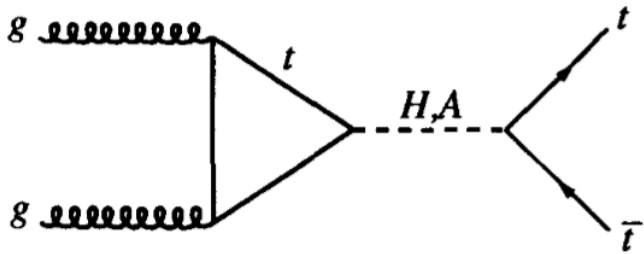
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A strong phase  
 “insensitive”\* to phase in the Yukawa as the signal amplitudes is proportional to  $|y_t|^2$ .

\*subject to difference in loop functions

# Challenges (interferences)



Interference effect from this imaginary part is important, regardless of the width! (narrow width approximation fails)

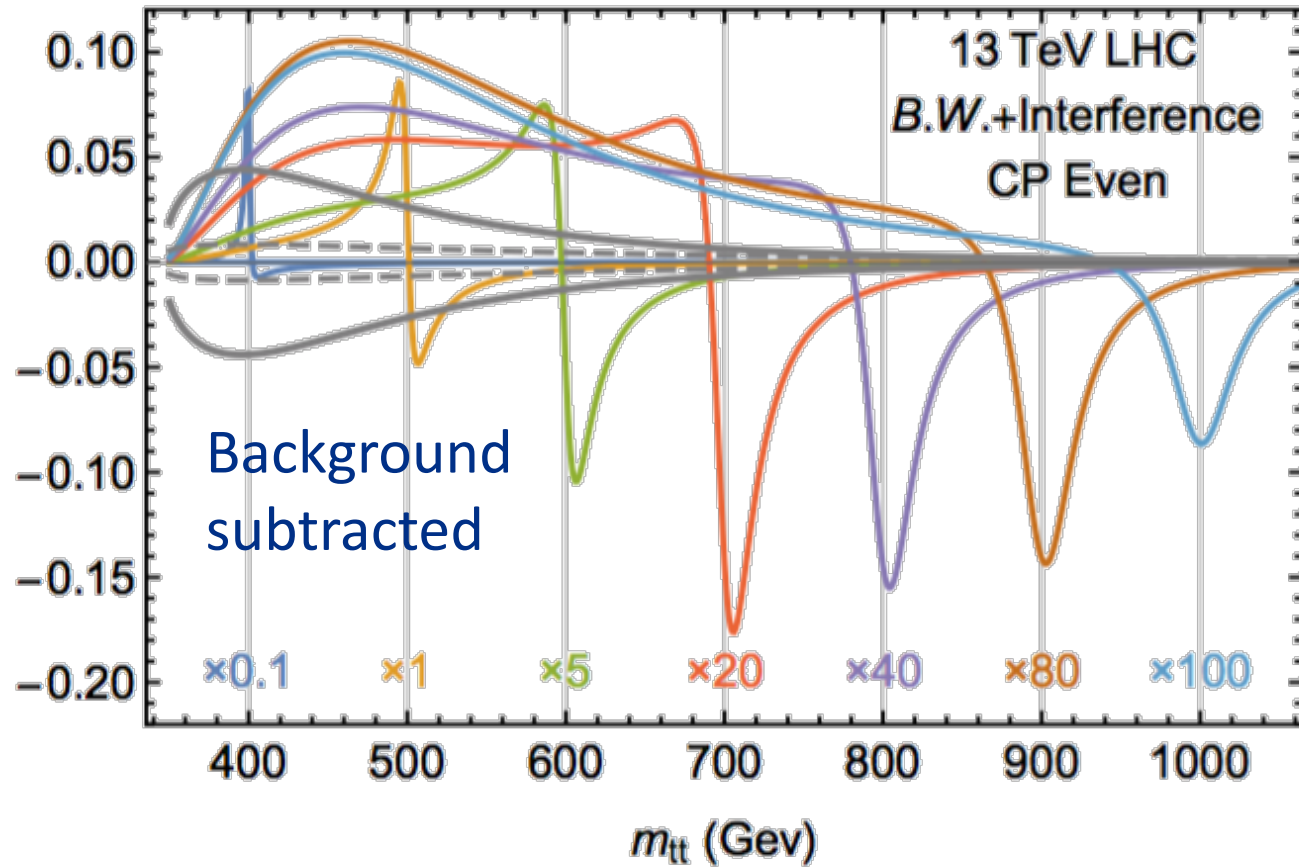
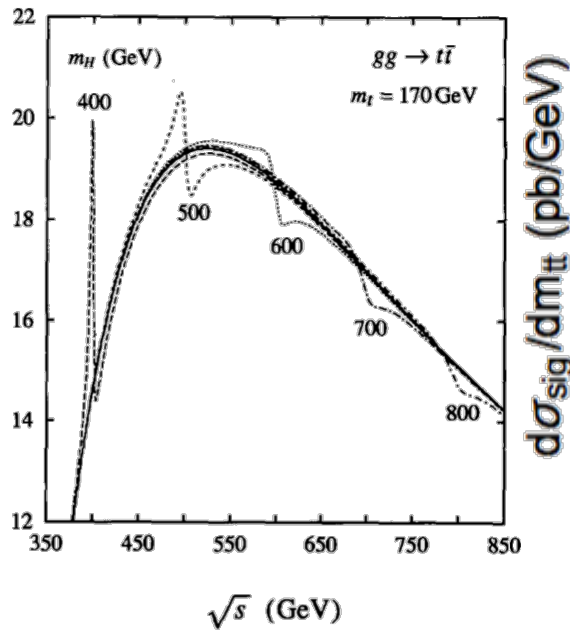
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# Challenges



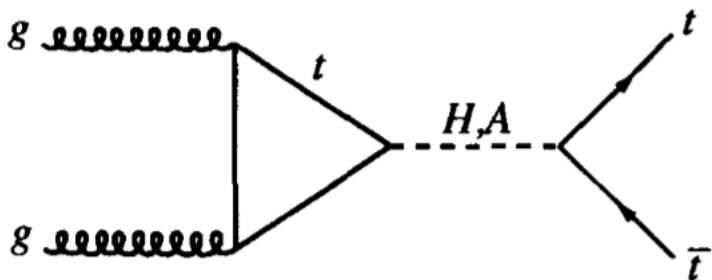
Special line shapes:

- Bump search not designed/optimized for this, have to modify our current search;
- Smearing effects erode the structure, making this signal much harder.

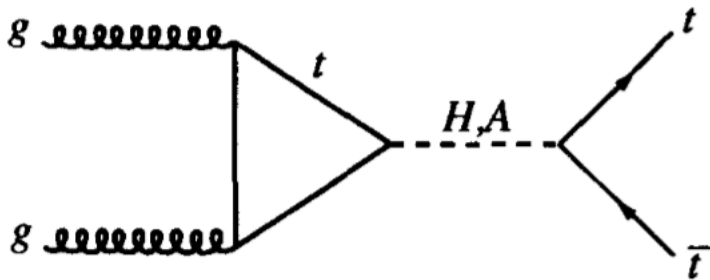


# Opportunities

- Nearly degenerate CP-even and CP-odd scalars
- CP phases (new interferences emerges proportional to the loop-function difference between the even and odd one for nearly degenerate ones)
- Bottom-quark contributions (large  $\tan\beta$ , changes the relative phase)
- New colored particle contributions and threshold effects (stops, VLQs, etc., reduce the relative phases and recovers the bump search)
- New channels (associated production with top(s), bottoms, jet(s), etc. Potentially reducing the interference effect.)



# Opportunities



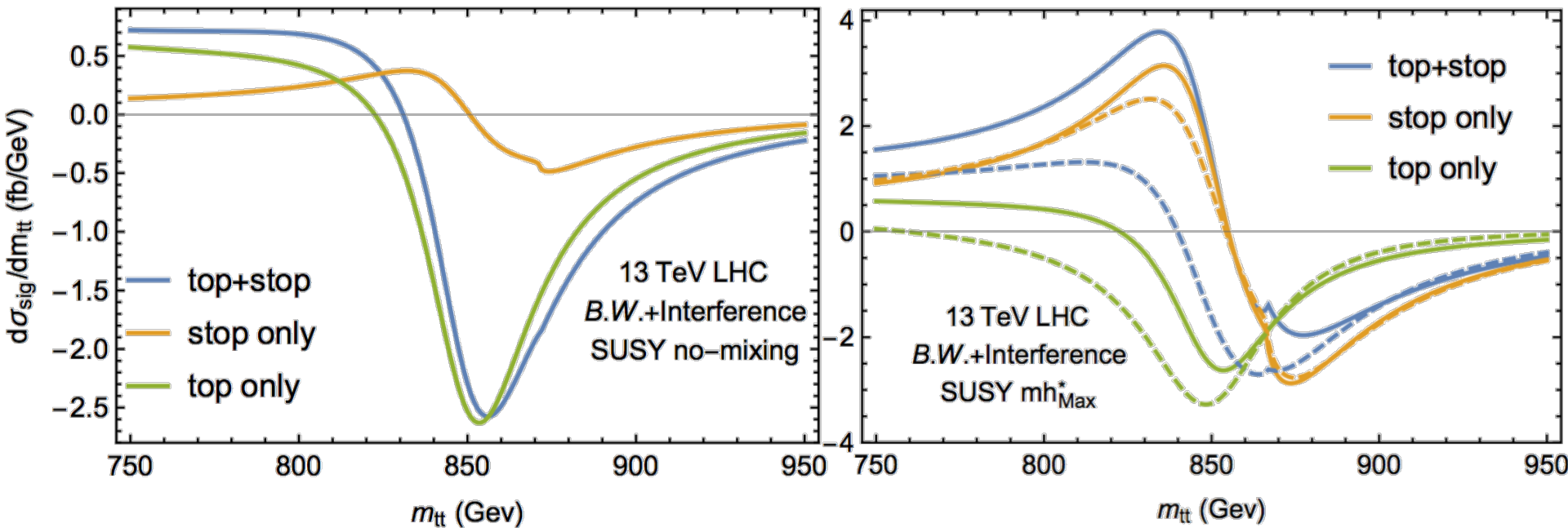
Covered in our study

M. Carena, ZL,

[arXiv:1608.07282](https://arxiv.org/abs/1608.07282), JHEP

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# Opportunities– Stop contributions



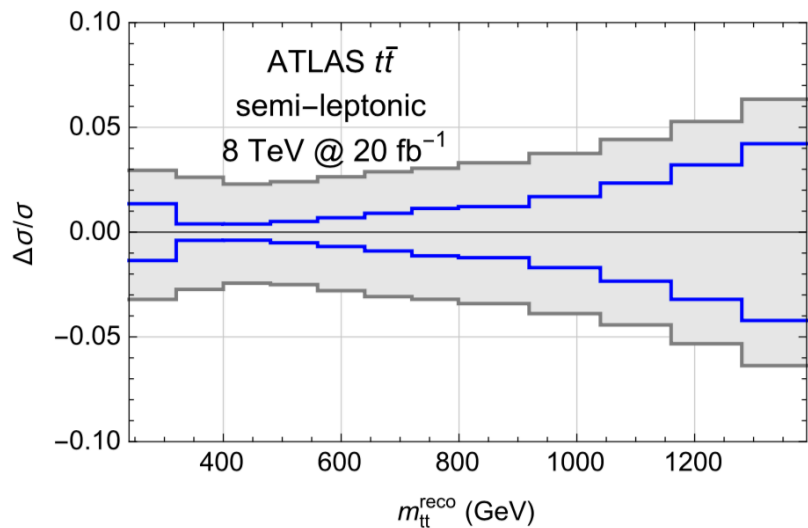
SUSY TeV scale stop quarks are highly anticipated through naturalness argument

For 850 GeV scalars, we show two benchmark scenarios:

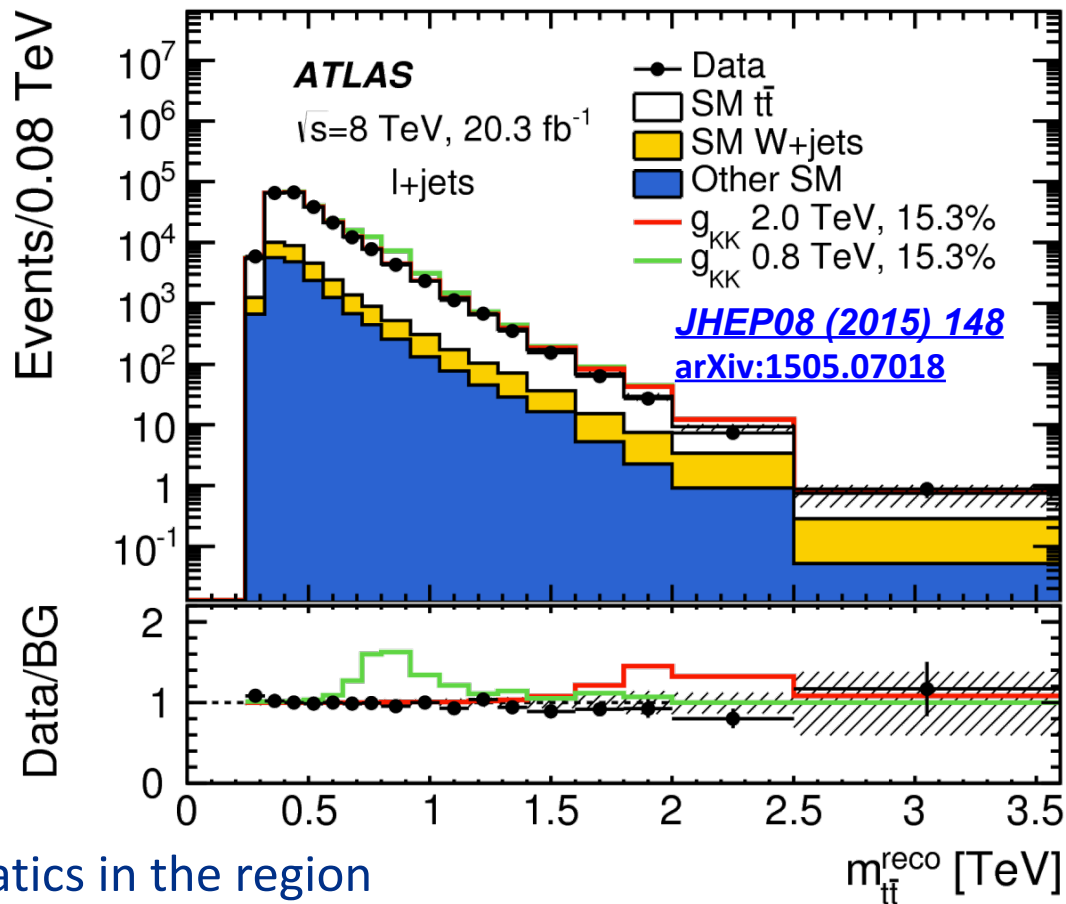
Stop zero L-R mixing, the stop contribution is only a small perturbation;

Stop large L-R mixing,  $mh_{\text{max}}^*$  scenario, the heavy Higgs to stop quark pair coupling is dominated by the mixing term, and significant changes could occur.

# LHC perspectives

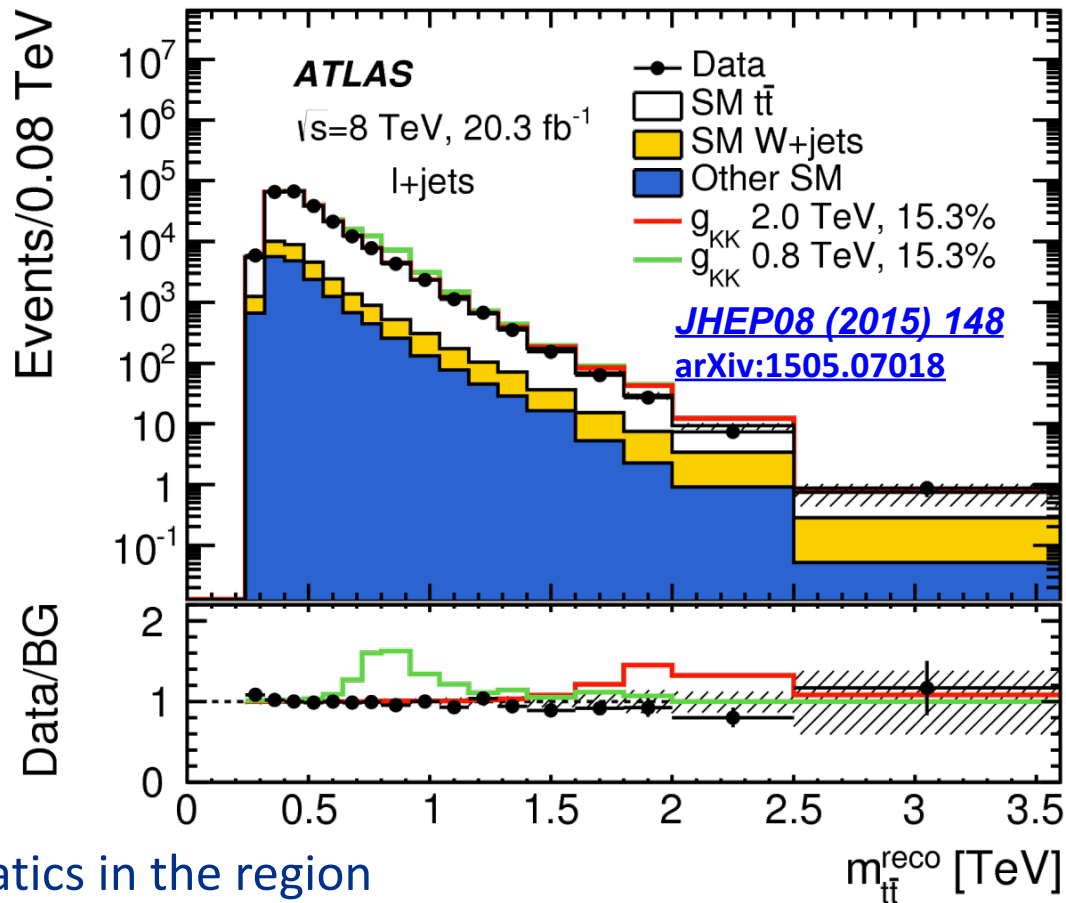
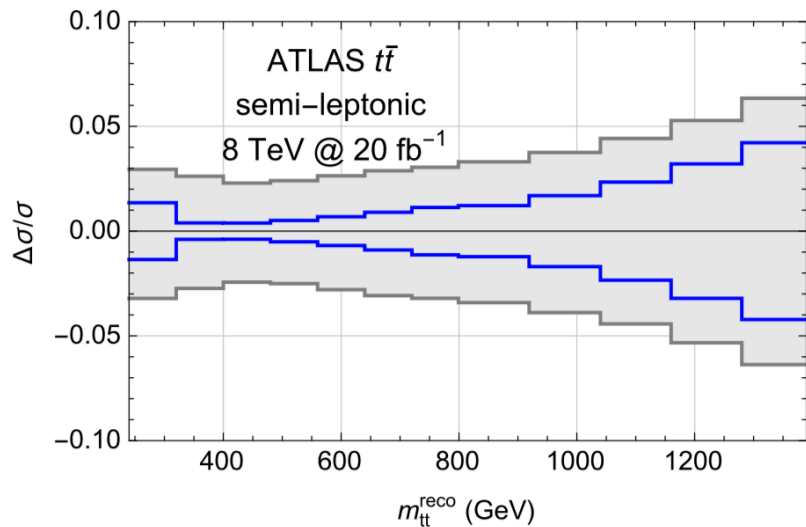


Already achieved sub 2-4% systematics in the region of interest, we see hope in this channel.



This is a crucial channel universally important for the understanding of heavy new resonances.

# LHC perspectives



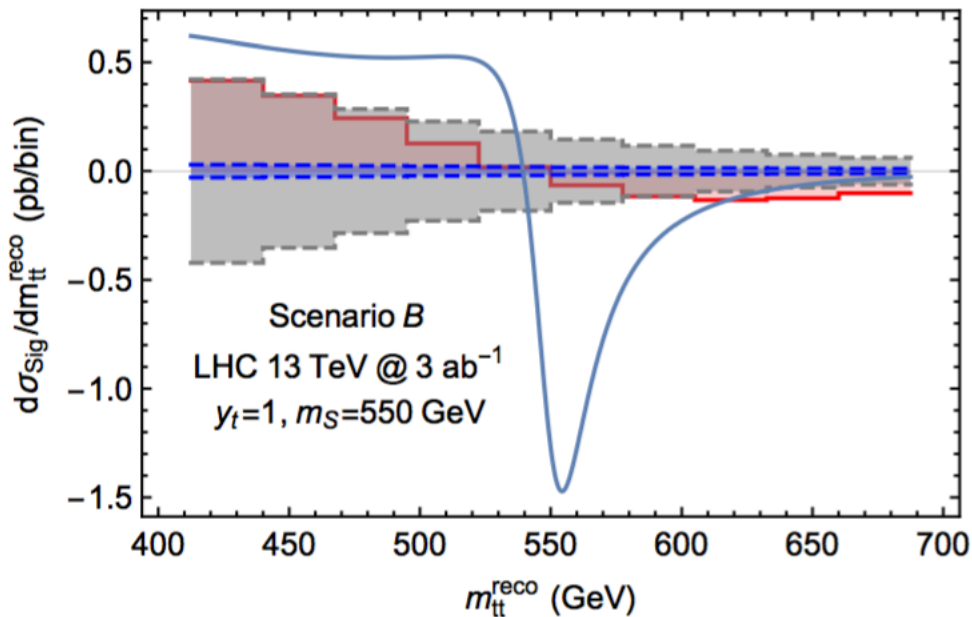
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“Hitting a systematics wall” is not an option, we need to try hard to improve the systematics by using the abundant data to calibrate and by selecting the data with best quality.

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# LHC perspectives

	$\Delta m_{t\bar{t}}$	Efficiency	Systematic Uncertainty
Scenario A	15%	8%	4% at 30 fb <sup>-1</sup> , halved at 3 ab <sup>-1</sup>
Scenario B	8%	5%	4% at 30 fb <sup>-1</sup> , scaled with $\sqrt{L}$



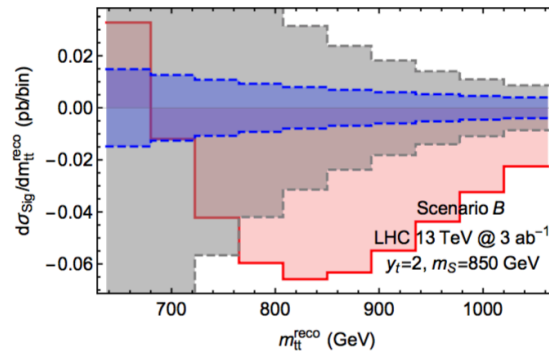
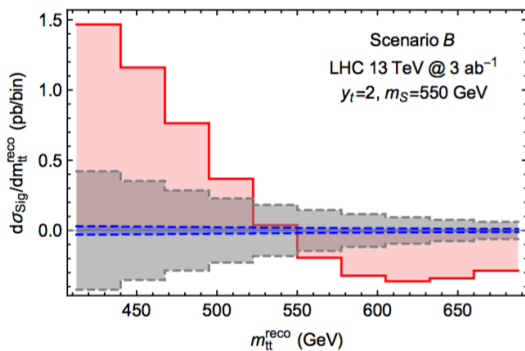
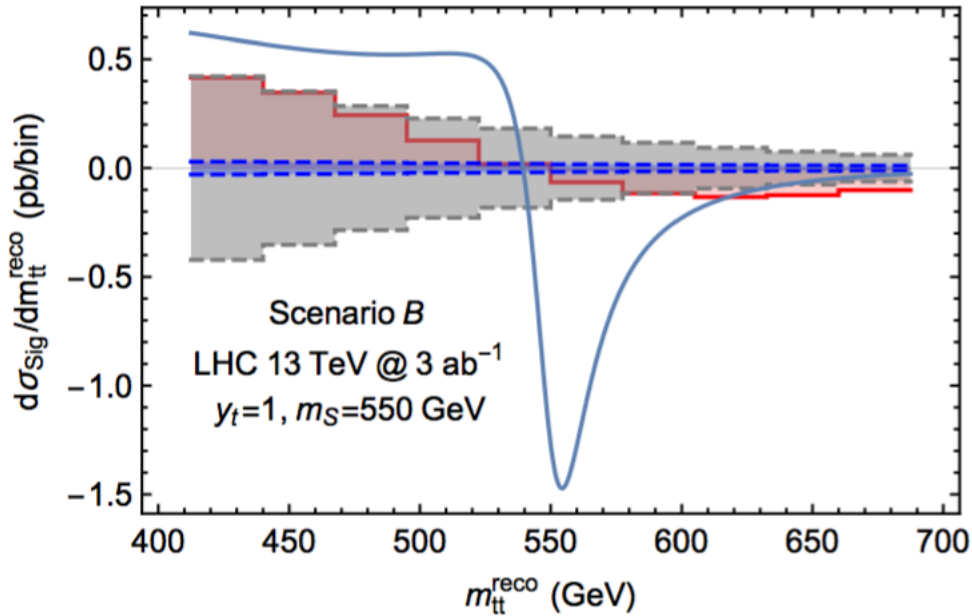
Blue curve, the signal lineshape before smearing;

Red Histogram, the signal after smearing and binning;

Gray and blue histograms, the total and statistical uncertainties;

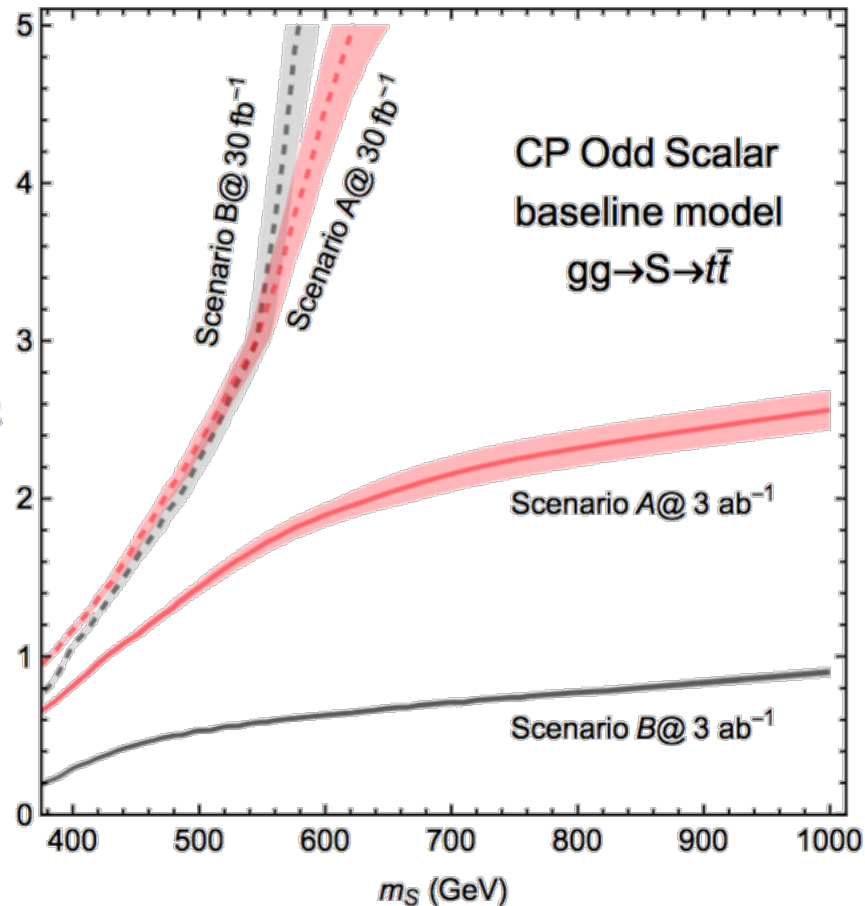
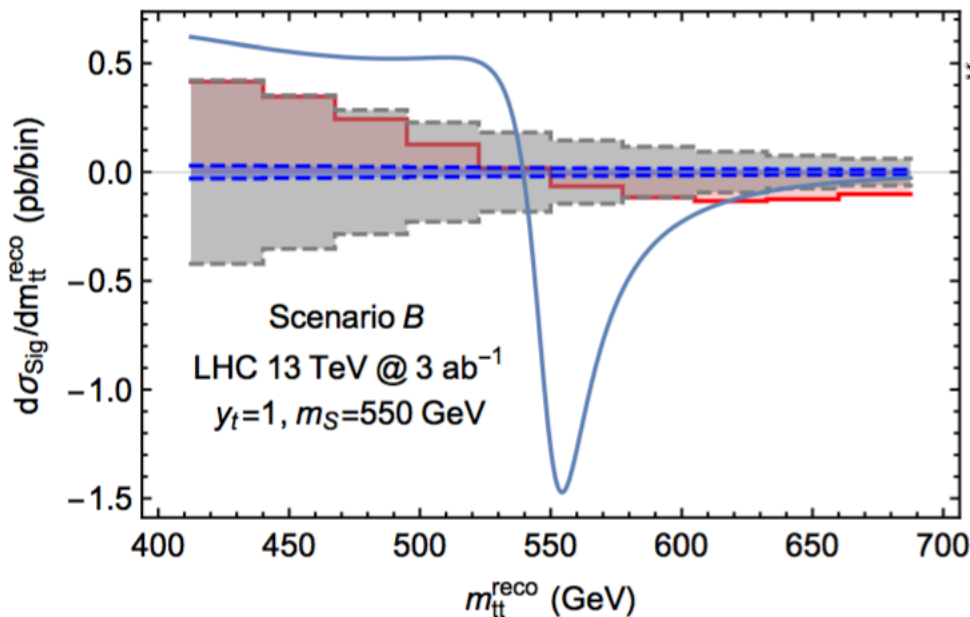
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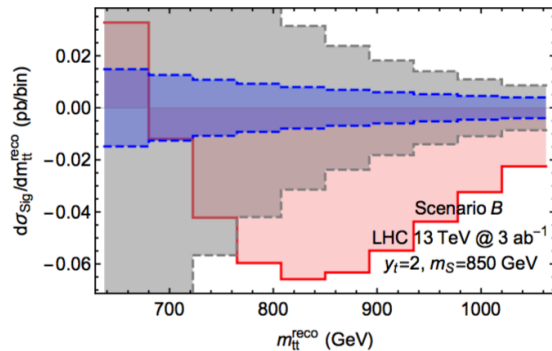
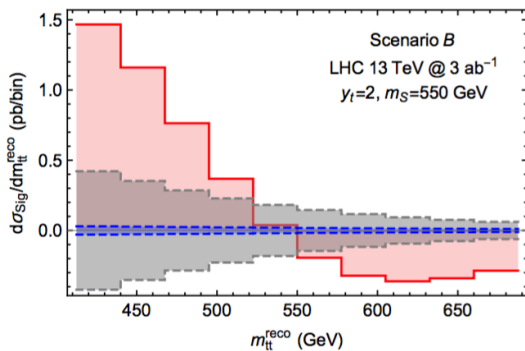


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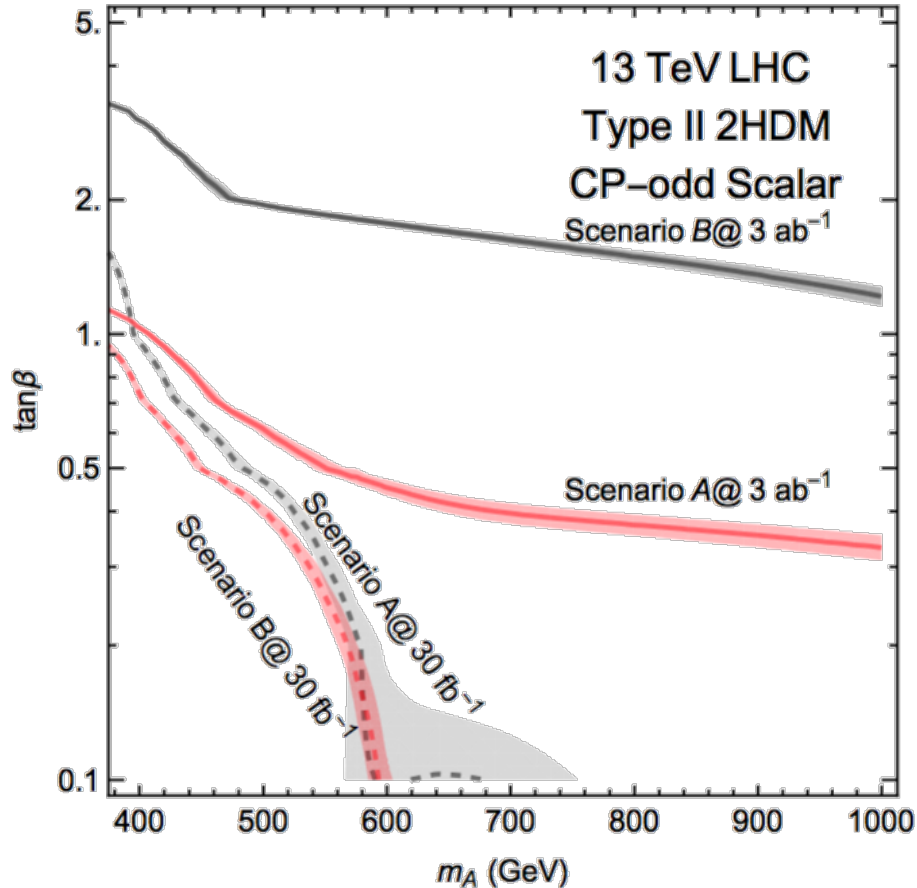


Lineshapes for a grid of mass and different Yukawas are generated (because the signal is line-shape and does not scale as simple powers of Yukawa couplings). After smearing, using bins near the scalar mass window, taking both excess and deficits, exclusion potential extracted.



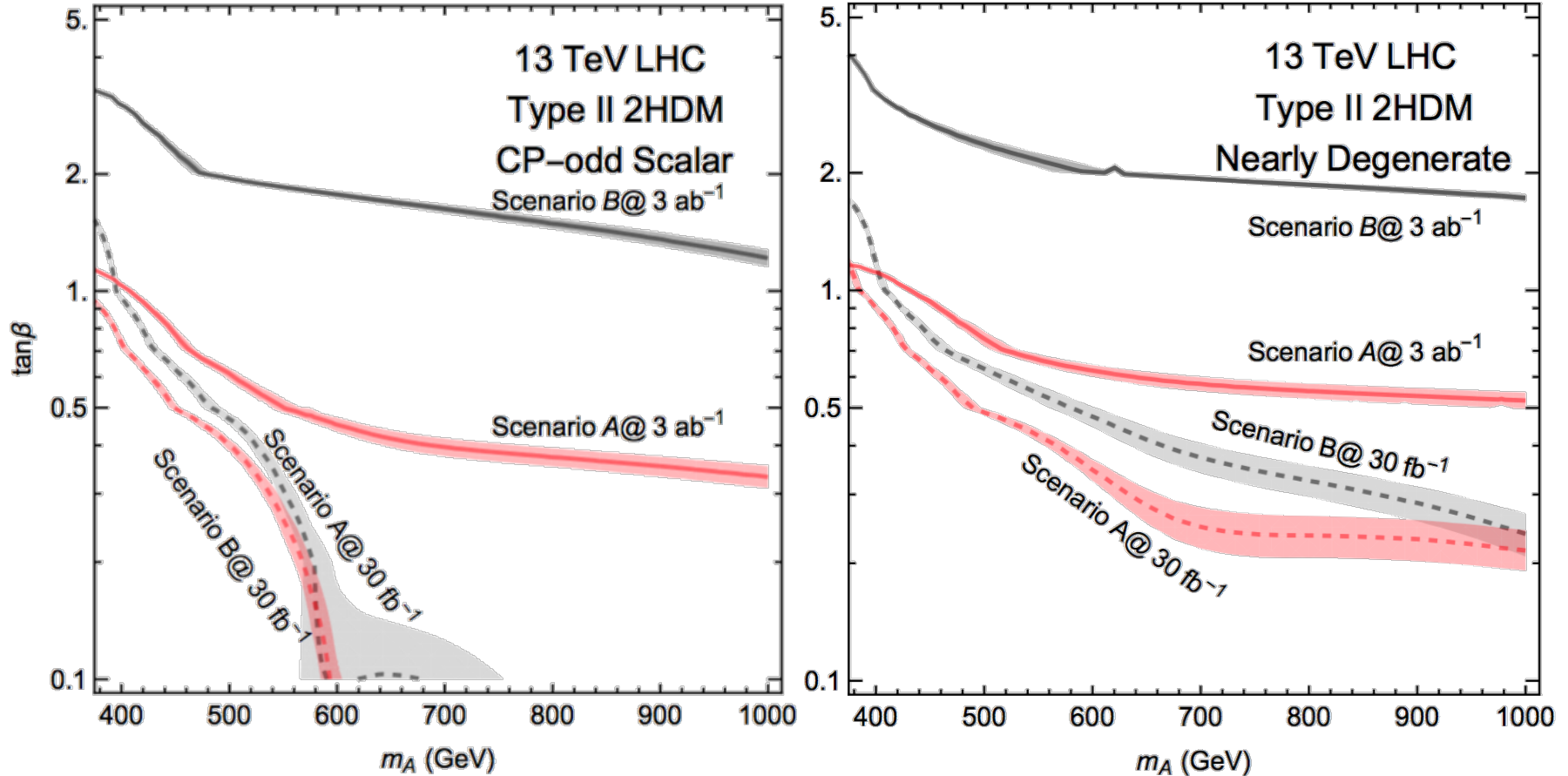


# LHC perspectives—2HDM projections



For a Type II 2HDM, the bottom quark effects are mainly in modifying the production vertex and provide some decay branching fraction suppression; Regions below the curves are excluded; In general can only cover the very low  $\tan\beta$  regime, optimistic LHC performance scenario B could cover up to  $\tan\beta$  around 1~2 up to 1 TeV.

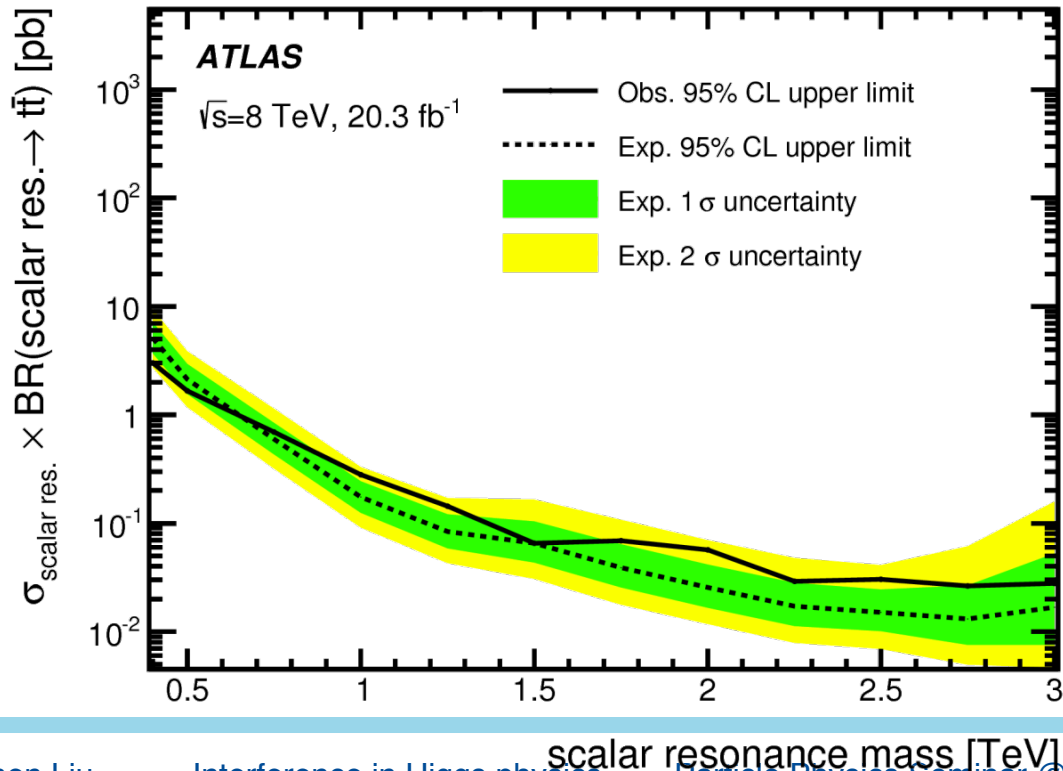
# LHC perspectives – 2HDM projections



For the case of nearly degenerate heavy scalars, the physic reach is improved, especially for heavy heavy masses.

# LHC perspectives – Experimental progress

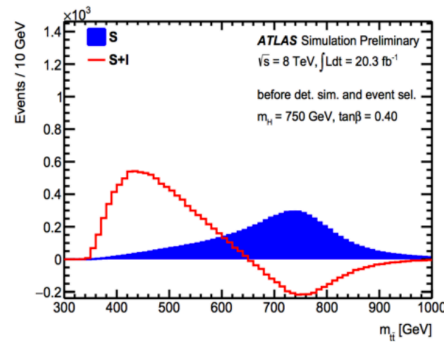
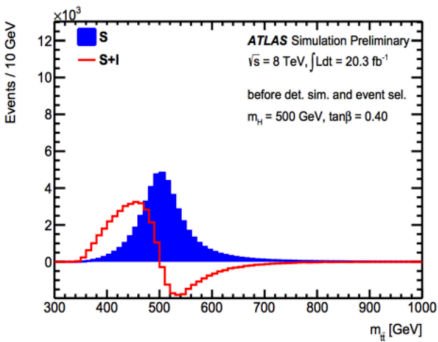
The last class of models examined here produces colour-singlet scalar particles via gluon fusion which decay to  $t\bar{t}$ . The approach previously adopted by the CMS Collaboration [18] is followed, in which narrow scalar resonance benchmarks are generated while the interference with SM  $t\bar{t}$  production is neglected. Even though such signals with negligible interference are not predicted by any particular BSM model, they can be used to evaluate the experimental sensitivities and set upper limits on the production cross-sections. The CMS Collaboration excluded such resonances with production cross-sections greater than 0.8 pb and 0.3 pb for masses of 500 and 750 GeV, respectively.



# LHC perspectives – Experimental progress

## Signal Modeling ( $A/H \rightarrow t\bar{t}b\bar{a}$ )

- The signal process is simulated using the generator MadGraph5 v2.0.1 with the Higgs Effective Couplings Form Factor model (implements the production of scalar and pseudoscalar particles through loop-induced gluon fusion)
- Loop contributions from both bottom and top quarks are taken into account
- Signal shape is distorted from a simple Breit-Wigner peak, to a peak-dip structure
- Statistical interpretation of measured event rates in data are compared to the total sum of Signal + Interference + Background (S + I + B)
- The mass of the SM-like Higgs boson,  $h$ , is chosen to be 125 GeV and  $\sin(\beta-\alpha)$  is set to 1

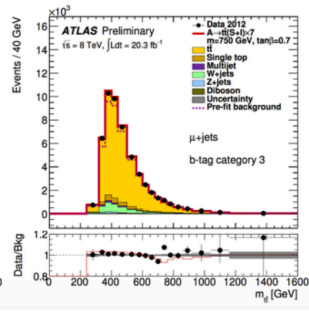
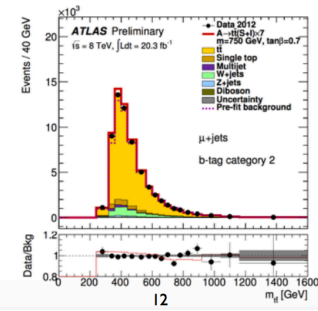
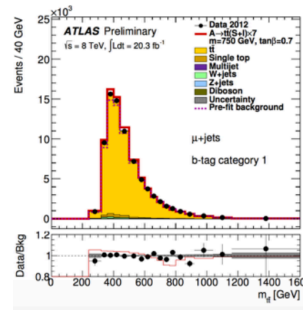


## Event Selection / Mass Reconstruction ( $A/H \rightarrow t\bar{t}b\bar{a}$ )

- Analysis targets the  $t\bar{t}b\bar{a}$  lepton+jets channel (one W to hadrons one to leptons)
- Single electron or single muon triggers are used—2 categories (one for e; one for  $\mu$ )
- One high  $p_T$  electron or muon; high MET from the escaping neutrino; presence of at least 4 high  $p_T$  jets in the event; at least one jet originating from b quarks **must be tagged** (70%); Sum of MET and  $m_T > 60$  GeV (multi-jets suppression)  $m_T^W = \sqrt{2 \cdot p_T^e \cdot E_T^{\text{miss}} \cdot (1 - \cos \phi_{e\nu})}$
- A chi-squared fit is used for assignment of the decay products, then  $m_{tt}$  is reconstructed
- Events further classified depending on the b-tagged jet(s) assignment—3 categories

$$\chi^2 = \left[ \frac{m_{jj} - m_W}{\sigma_W} \right]^2 + \left[ \frac{m_{jjb} - m_{jj} - m_{b-W}}{\sigma_{b-W}} \right]^2 + \left[ \frac{m_{j\ell\nu} - m_{t\ell}}{\sigma_{t\ell}} \right]^2 + \left[ \frac{(p_{T,jjb} - p_{T,j\ell\nu}) - (p_{T,b} - p_{T,t\ell})}{\sigma_{\text{diff } p_T}} \right]^2$$

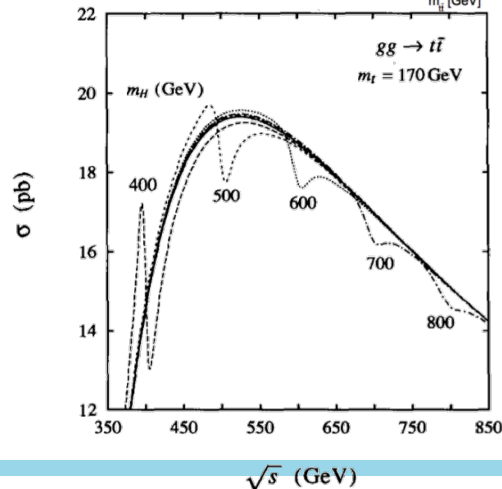
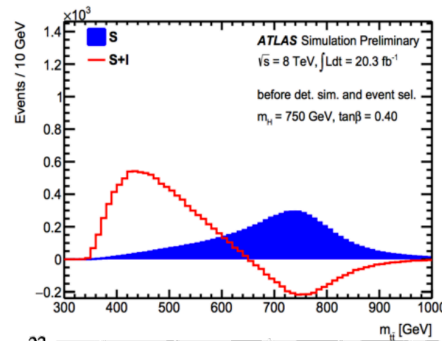
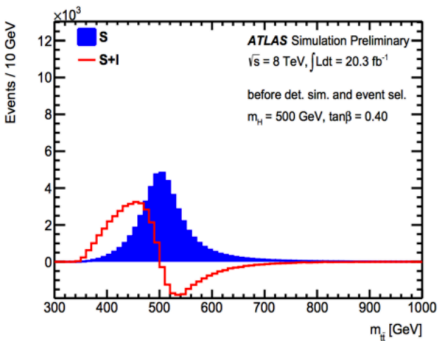
**6 categories in total**  
(2 lepton types) x  
(3 b-tagging classifications)



# LHC perspectives – Experimental progress

## Signal Modeling ( $A/H \rightarrow t\bar{t}b\bar{a}$ )

- The signal process is simulated using the generator MadGraph5 v2.0.1 with the Higgs Effective Couplings Form Factor model (implements the production of scalar and pseudoscalar particles through loop-induced gluon fusion)
- Loop contributions from both bottom and top quarks are taken into account
- Signal shape is distorted from a simple Breit-Wigner peak, to a peak-dip structure
- Statistical interpretation of measured event rates in data are compared to the total sum of Signal + Interference + Background (S + I + B)
- The mass of the SM-like Higgs boson,  $h$ , is chosen to be 125 GeV and  $\sin(\beta-\alpha)$  is set to 1

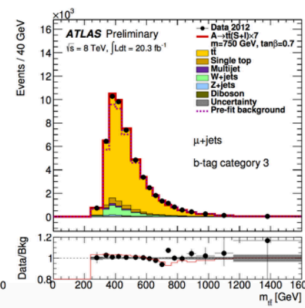
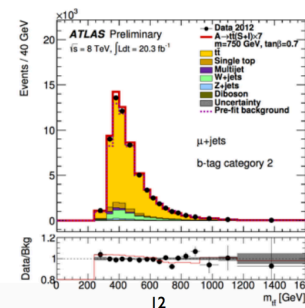
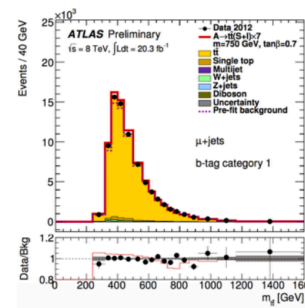


## Event Selection / Mass Reconstruction ( $A/H \rightarrow t\bar{t}b\bar{a}$ )

- Analysis targets the  $t\bar{t}b\bar{a}$  lepton+jets channel (one W to hadrons one to leptons)
- Single electron or single muon triggers are used—2 categories (one for e; one for  $\mu$ )
- One high  $p_T$  electron or muon; high MET from the escaping neutrino; presence of at least 4 high  $p_T$  jets in the event; at least one jet originating from b quarks **must be tagged** (70%); Sum of MET and  $m_T > 60$  GeV (multi-jets suppression)  $m_T^W = \sqrt{2 \cdot p_T^L \cdot E_T^{\text{miss}} \cdot (1 - \cos \phi_{\ell\nu})}$
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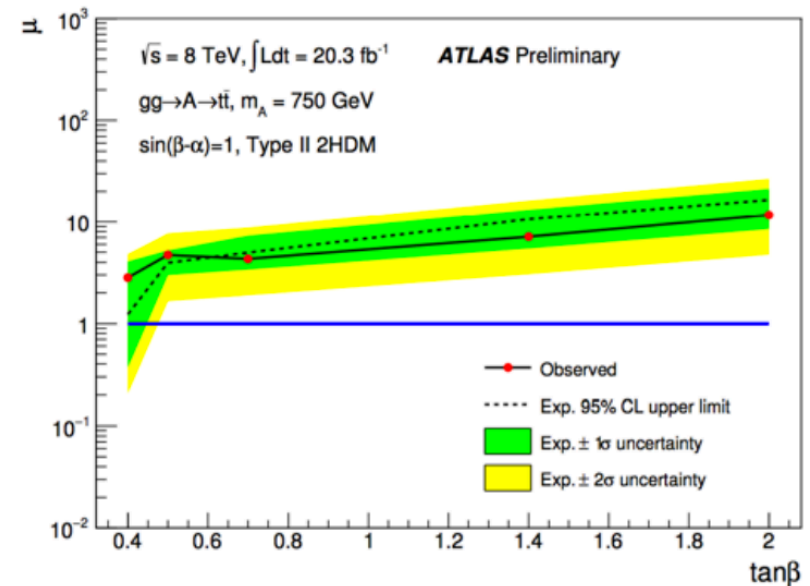
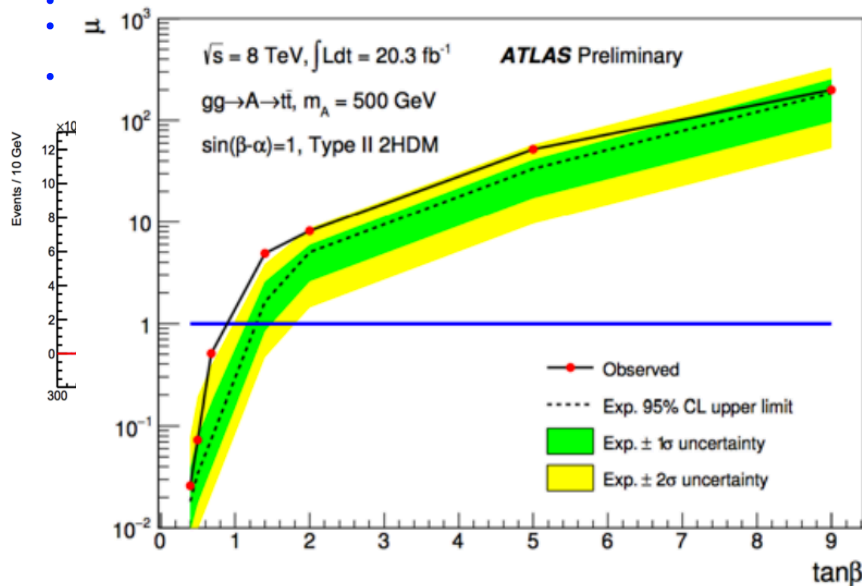
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**6 categories in total**  
(2 lepton types) x  
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# High-mass Higgs Search Results ( $A/H \rightarrow t\bar{t}b\bar{b}$ )

- No significant excess over Standard Model background expectations is observed
- We set upper limits on the signal strength parameter  $\mu$  as a function of the parameter  $\tan\beta$  for a neutral pseudoscalar  $A$  with a mass of 500 GeV and 750 GeV
- NB: The blue line at  $\mu=1$  corresponds to the signal strength in the Type-II 2HDM



- For a neutral pseudoscalar  $A$ , with a mass of  $m_A = 500 \text{ GeV}$ , parameter values of  $\tan\beta < 0.85$  in the Type-II 2HDM are excluded at the 95% CL. No  $\tan\beta$  values can be excluded for the higher mass point at 750 GeV.

# Summary and outlook for $gg \rightarrow S \rightarrow t\bar{t}$

$gg \rightarrow S \rightarrow t\bar{t}$  is a well—motivated channel for the hunt of heavy scalars

The interference effect augmented by the strong phase generated by the top loop generates interesting shapes. **(The effect is always there regardless of the width!)**

Opportunities to increase the observational aspects resides on both the theoretical side (including nearly degenerate bosons, CP phases, additional contributions from light quarks, and heavy colored particles) and experimental side (reducing the systematics with copious tops produced at the LHC, starting to face this challenge by using line-shape profile search ATLAS-2016-073, and move on from there.)

Other channels and effects, including ttH, tH (see in N. Craig, F. D'Eramo, P. Drapper, S. Thomas, H. Zhang [arXiv:1504.04630](#) and J. Hajer, Y.-Y. Li, T. Liu J. Shiu [arXiv:1504.07617](#), S. Gori, I.-W. Kim, N. Shah, K. Zurek [arXiv:1602.02782](#), N. Craig, J. Hajer, Y. Li, T. Liu, H. Zhang, [arXiv:1605.08744](#), B. Hespel, F. Maltoni, E. Vryonidou [arXiv:1606.04149](#)), H+jet, charged Higgs searches, and how stable such effects are against QCD corrections (see a case study in W. Bernreuther, P. Galler, C. Mellein, Z.-G. Si, P. Uwer [arXiv:1511.05584](#)), ttbar differential observables ( W. Bernreuther, P. Galler, C. Mellein, Z.-G. Si, P. Uwer [arXiv:1702.06063](#)). Also other decay channels may have such effect large (see in Jung, Sung, Yoon, [arXiv:1510.03450](#), [arXiv:1601.00006](#)).

Interference effect is important for many BSM bump hunting, especially for the case of better and better limits. (as the relative strength of the interference pieces increases relatively to the B.W. piece.)

# Recap of the strong phase physics

Strong phase plays important roles in various aspects of physics

- $t\bar{t}$  heavy resonances (dominant effect in the search)
- Hadron physics (strong phase mapping out CPV)
- Leptogenesis (weak phase from heavy neutrino decay interferes with strong phase part, generating asymmetry)



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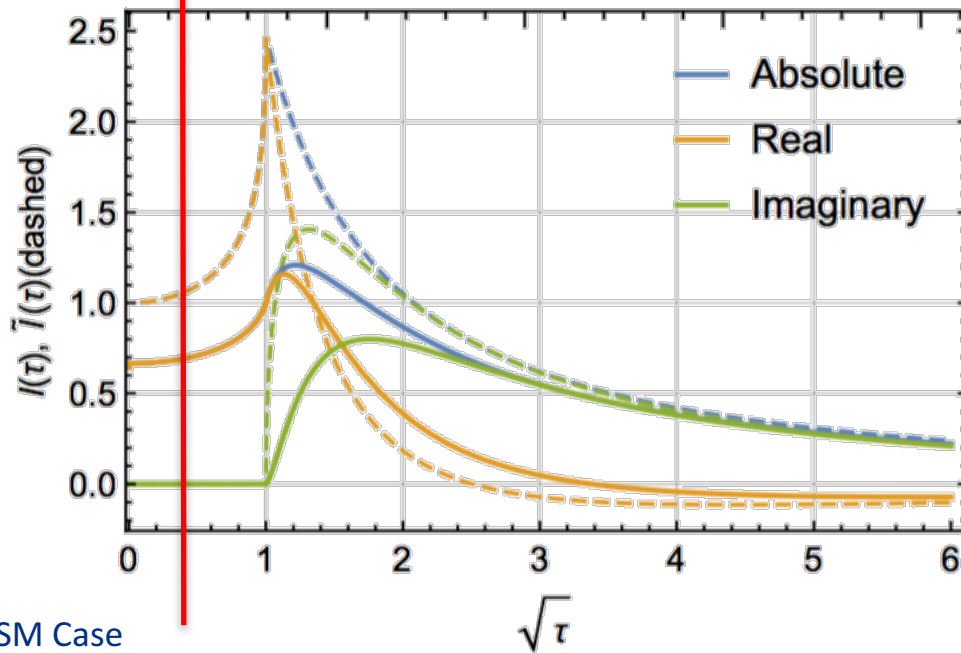
**Question:**

**how about the strong phase in the SM Higgs?**

J. Campbell, M. Carena, R. Harnik, ZL, [arXiv:1704.08259](https://arxiv.org/abs/1704.08259)

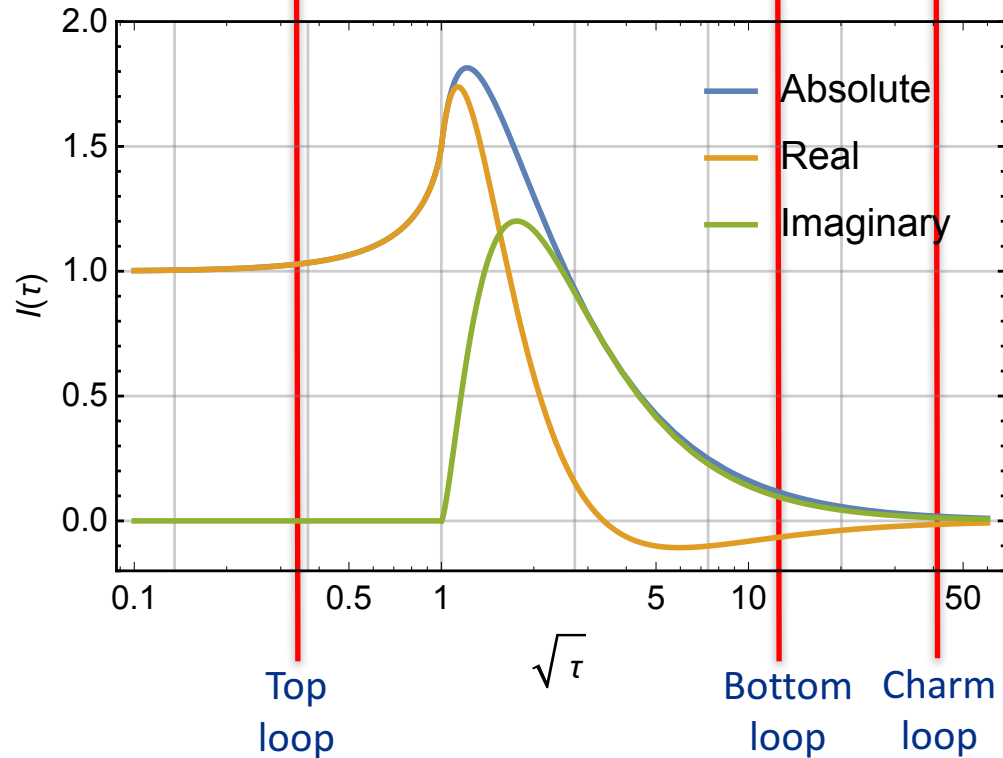


# What about the SM-like Higgs $\sim 125$ GeV?



SM Case  
real and slowly varying  
"heavy (chiral) fermion  
decoupling theorem" (with  
Yukawa proportional to the mass)

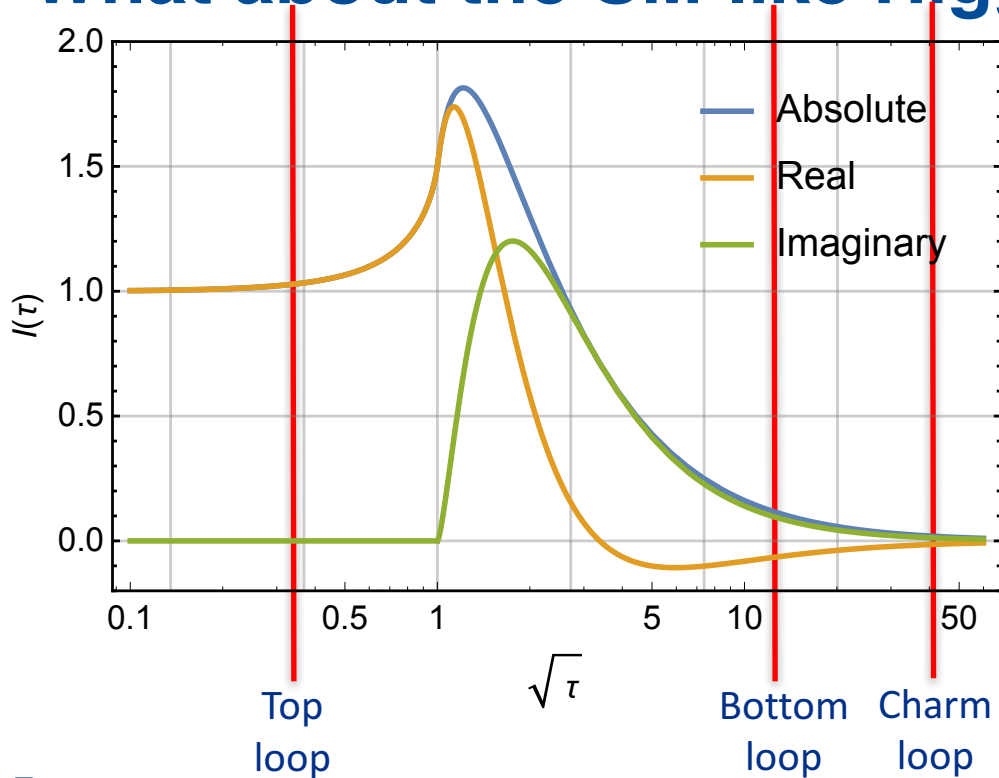
# What about the SM-like Higgs $\sim 125$ GeV?



- All quark contributions normalized the same way, the plot represents the relative contributions
- Numerically\*:
  - t-loop  $+1.03$
  - b-loop  $-0.054 + 0.071i$
  - c-loop  $-0.014 + 0.012i$

\*some input parameter dependence

# What about the SM-like Higgs $\sim 125$ GeV?



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- Numerically\*:
  - t-loop  $+1.034$
  - b-loop  $-0.035 + 0.039i$
  - c-loop  $-0.004 + 0.002i$

$$\frac{\sigma_{\text{BW}}}{\sigma_{\text{BW}}^{\text{SM}}} = 1.078\kappa_t^2 - 0.074\kappa_t\kappa_b - 0.008\kappa_t\kappa_c + 0.003\kappa_b^2 + O(< 0.001; \kappa_t, \kappa_b, \kappa_c).$$

➔ two important consequences

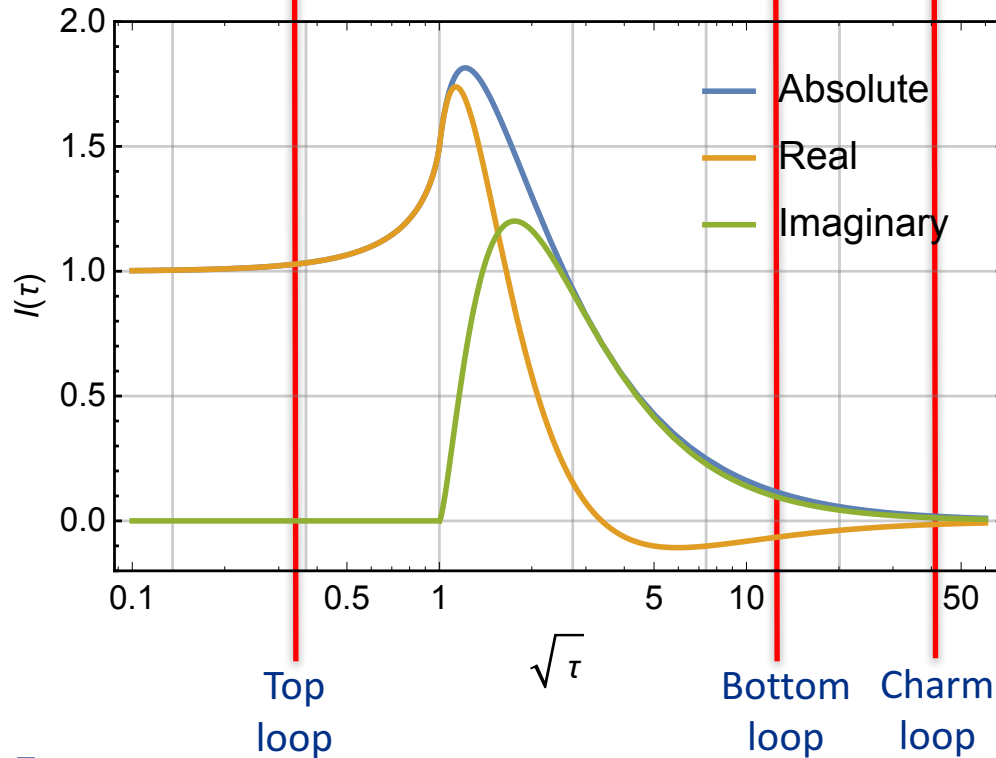
- Destructive interference between the top-loop and light quarks for gluon-gluon fusion (real part)

\*some input parameter dependence

HXWG recommends:

$$\sigma(gg \rightarrow h) \propto 1.06\kappa_t^2 - 0.07\kappa_t\kappa_b + 0.01\kappa_b^2$$

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→ two important consequences

- A strong phase in the gluon-gluon fusion production at hadron colliders (imaginary part) and will not see the strong-phase effect using narrow-width-approximation

Phase in gluon-gluon-fusion **0.042**

# Higgs interferences

Many occasions where interference are important for Higgs physics

- Higgs total width from  $\gamma\gamma$  invariant mass shift
- Higgs total width from off-shell measurement
- Double Higgs production (destructive interference between the box diagram and the trilinear Higgs diagram)
- Higgs diphoton CPV effects from converted photon and its interference with  $h \rightarrow ZZ^* \rightarrow 4e$  (Chen, Harnik and Vegas-Morales, [arXiv:1404.1336](https://arxiv.org/abs/1404.1336), [arXiv:1503.05855](https://arxiv.org/abs/1503.05855), etc.)
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But **none of above** make use of the strong phase in Higgs physics.

# Higgs interferences

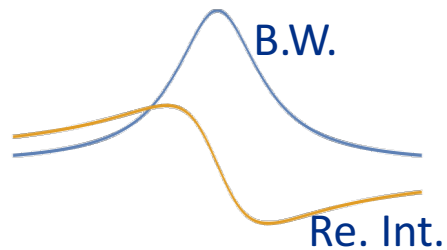
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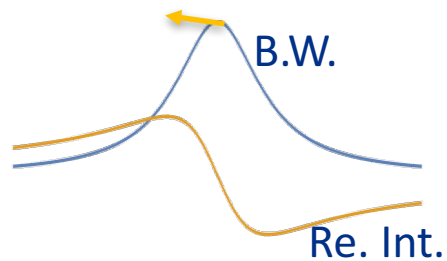
But **none of above** make use of this strong phase in Higgs.  
Let's have a brief review.



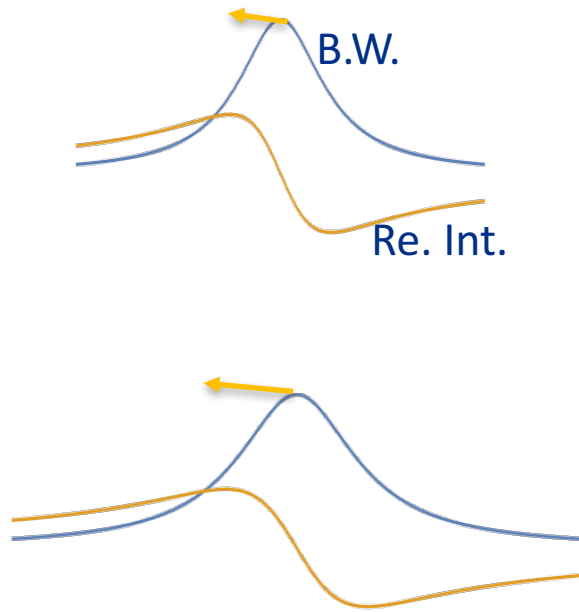
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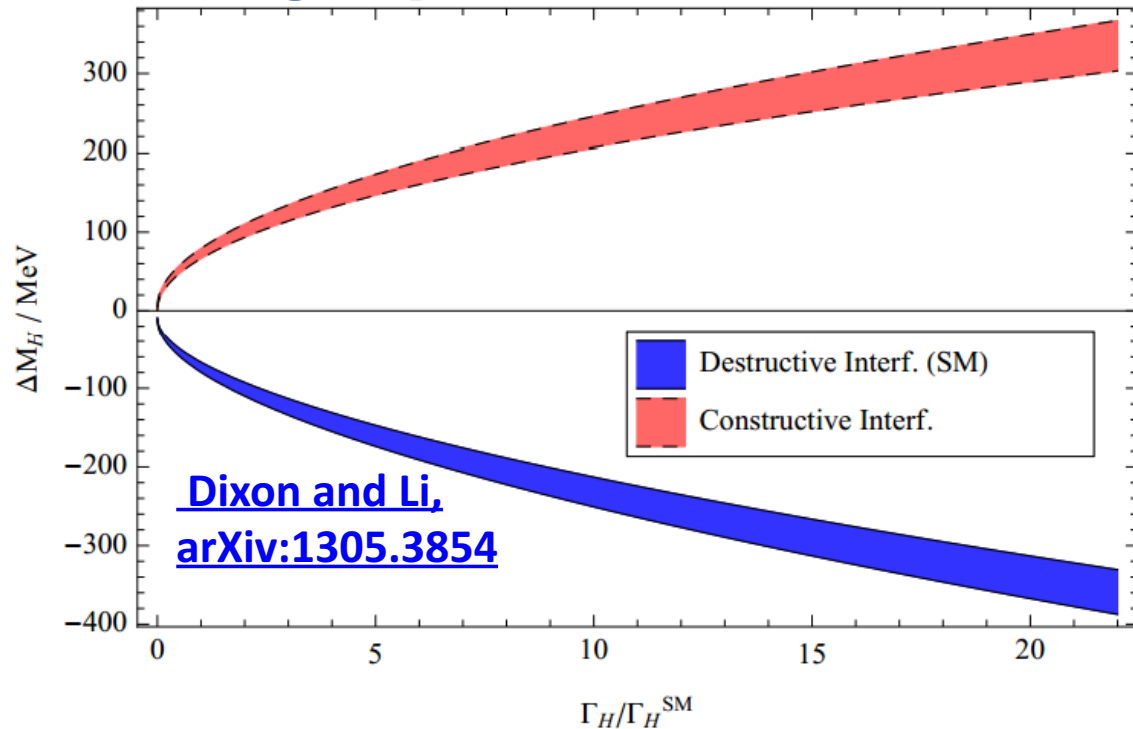
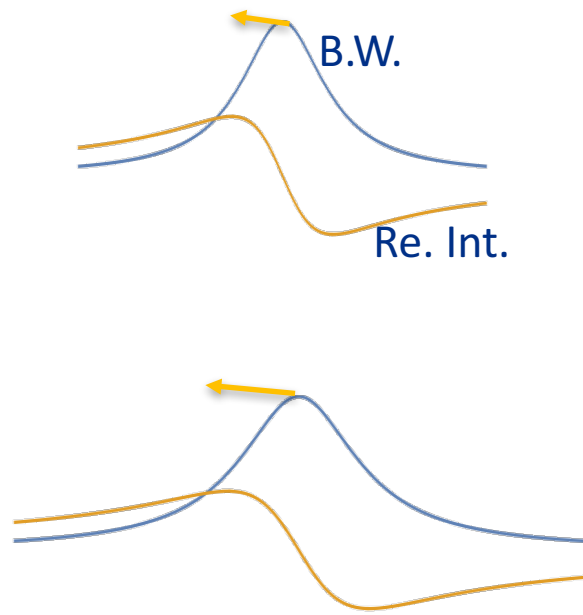


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Interference with the irreducible background shifts the invariant mass peak.

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Interference with the irreducible background shifts the invariant mass peak.

By comparing with the 4l invariant mass (where little interference due to the smallness of the irreducible background), ideally, one can see the shift in the invariant mass of the final states.

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$$\sigma(i \rightarrow h \rightarrow f) \propto \frac{g_i^2 g_f^2}{\Gamma_{tot}}$$

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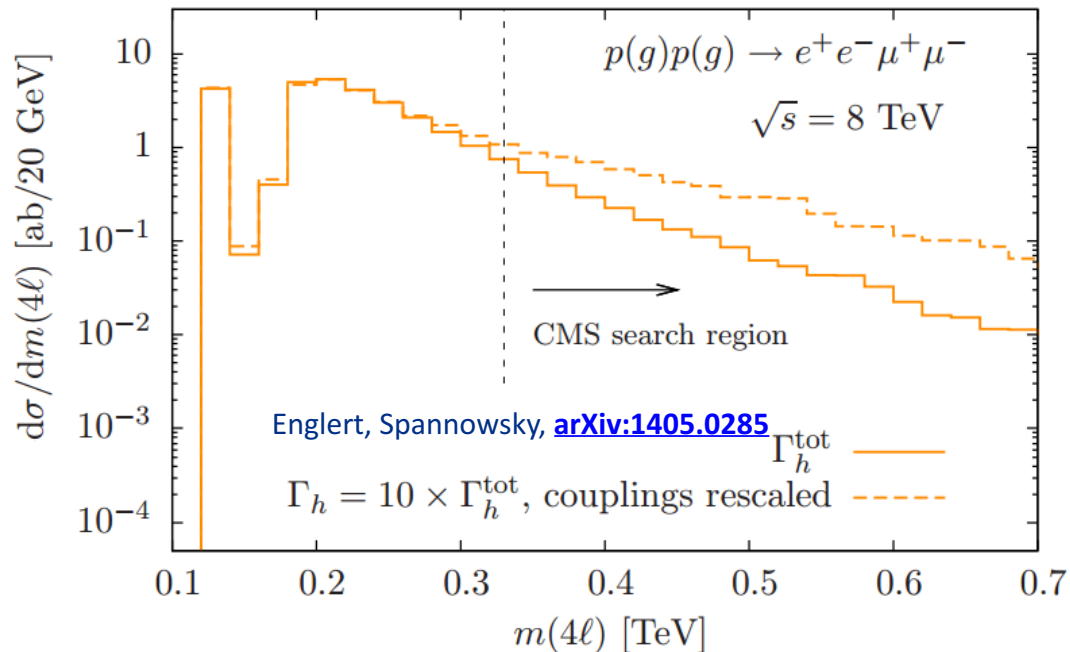
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F. Caola and K. Melnikov [arXiv:1307.4935](https://arxiv.org/abs/1307.4935)

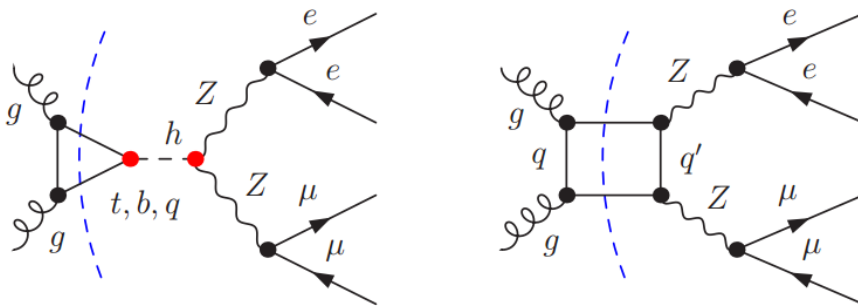
And N. Kauer and G. Passarino [arXiv:1206.4803](https://arxiv.org/abs/1206.4803) estimated an “eventual” reach of  $\sim 10$  SM width;

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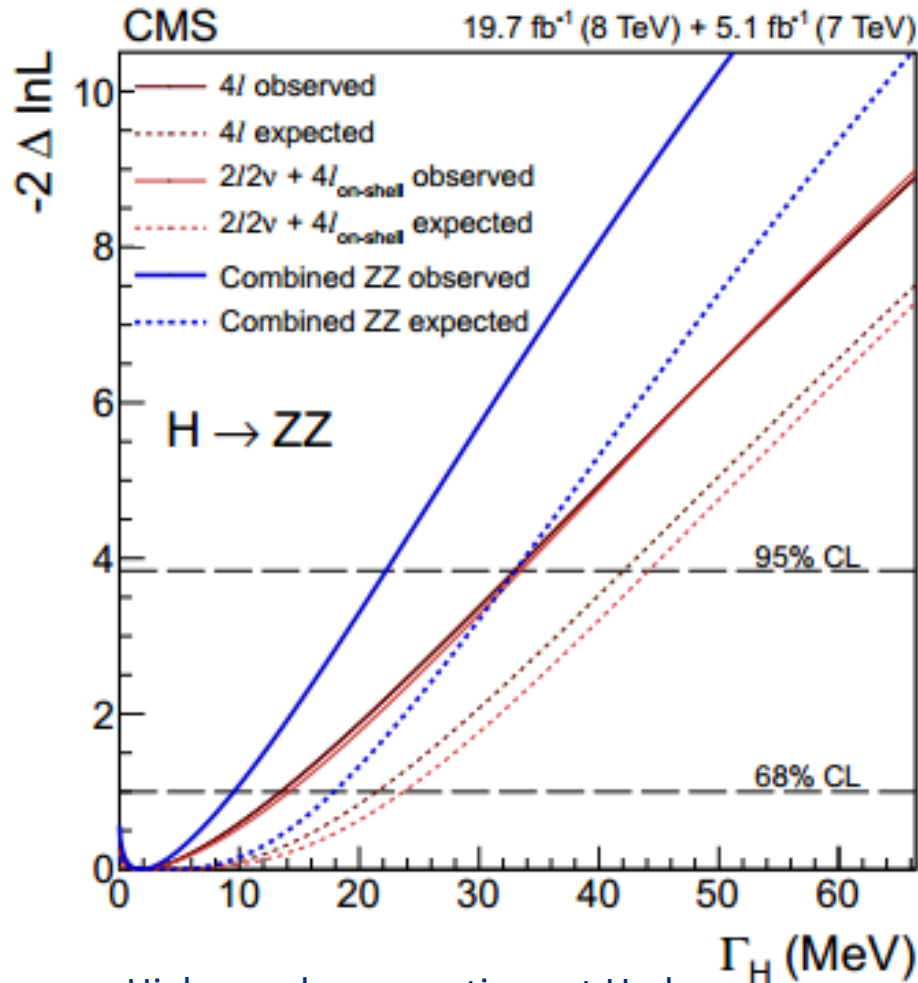
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# Higgs interferences (on-shell and off-shell)



Higher order corrections at Hadron colliders is going limit the precision of this measurement at O(1) level. Improvement hard to achieve.

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F. Caola and K. Melnikov estimated an “eventually” reach of  $\sim 10$  SM width; CMS with current data  $\sim 5.4$  SM width;

Great measurement, but:

- 1) On-shell rate uncertainty
- 2) Loop-running  $\leftrightarrow$  interplay of (at least) undetermined Top Yukawa
- 3) Many possible NP input at higher inv. masses.
- 4) Higher order corrections.

See discussions in e.g., [arXiv:1405.0285](https://arxiv.org/abs/1405.0285), [arXiv:1410.5440](https://arxiv.org/abs/1410.5440), [arXiv:1412.7577](https://arxiv.org/abs/1412.7577), [arXiv:1502.04678](https://arxiv.org/abs/1502.04678), ...

# Strong phase and Higgs (our study)

In the SM, there are two main loop-induced Higgs couplings (where the strong phase could be sizable):

- $Hgg: 0.042$
- $H\gamma\gamma: \pi - 0.006$
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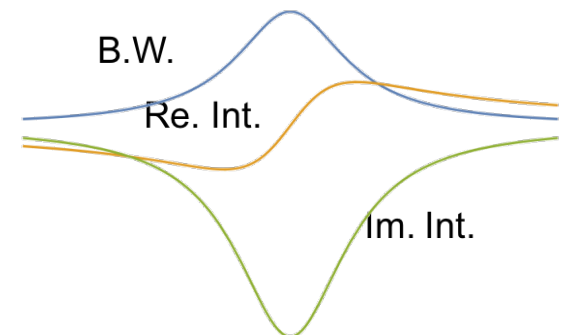
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Strong phase of the signal process:

$$\delta_S = \pi + 0.036$$

$$\frac{\text{Im } e^{i\delta_S}}{\text{Re } e^{i\delta_S}} = 0.04$$

- The overall phase important to determine both signs of Re.Interference and Im.Interference
- The ratio of Im/Re for small Im useful to determine relative cross section change
- Signal helicity amplitudes (due to scalar nature, and without CPV) has  $A_{++++} = A_{----} = A_{++--} = A_{--++}$





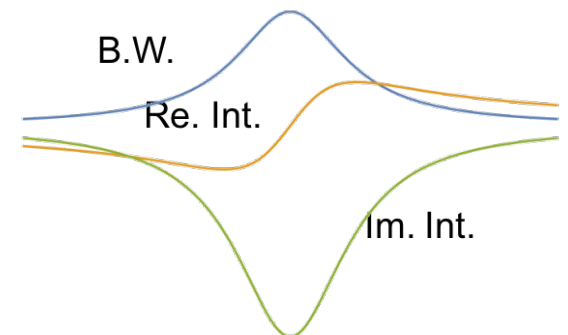
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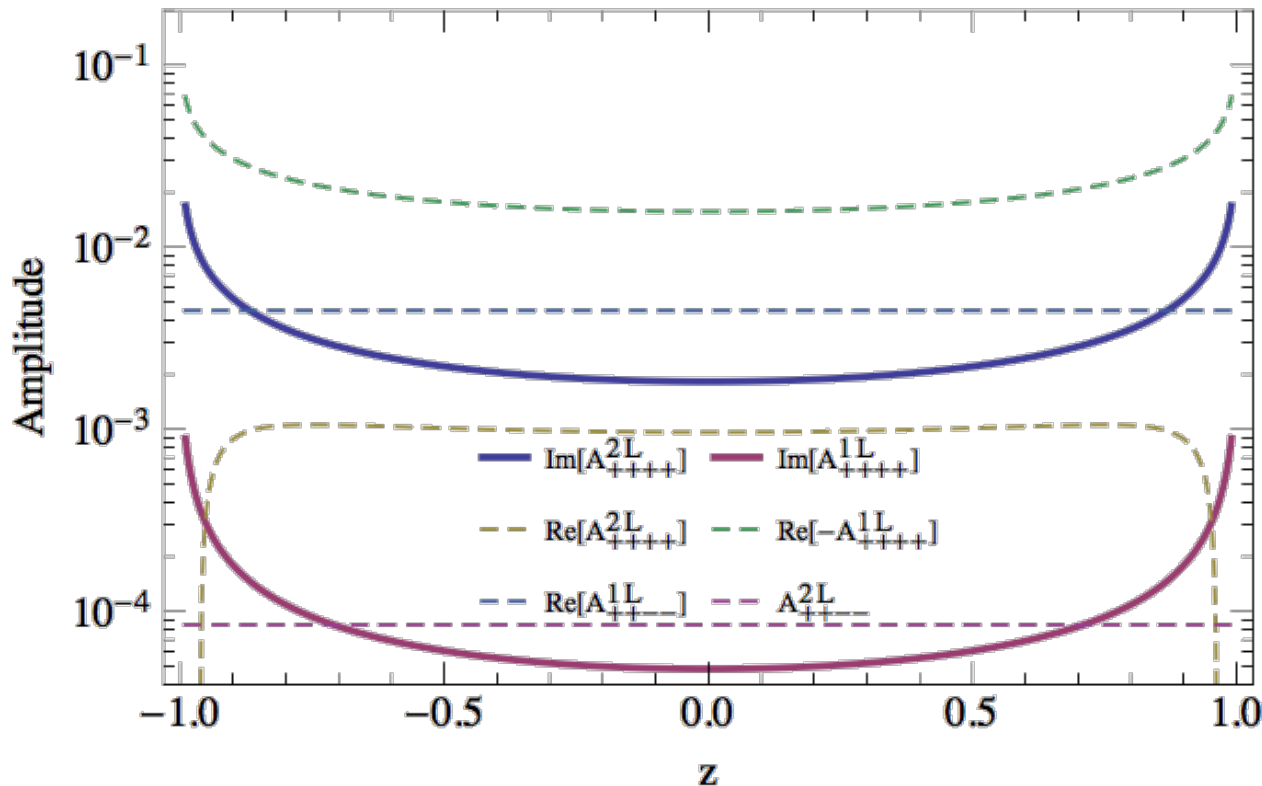
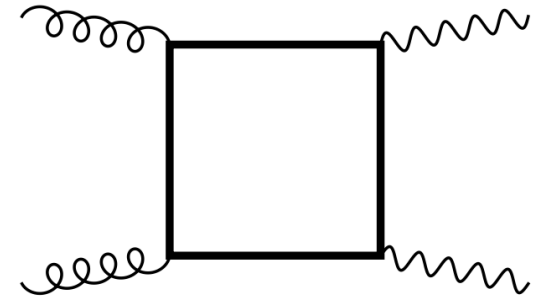
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- O(1) shift in the strong phase as function of Yukawas



# Strong phase and Higgs $gg \rightarrow h \rightarrow \gamma\gamma$

Interfering background are from SM box diagram of  $gg \rightarrow \gamma\gamma$

The overall sizes of different helicity amplitudes are

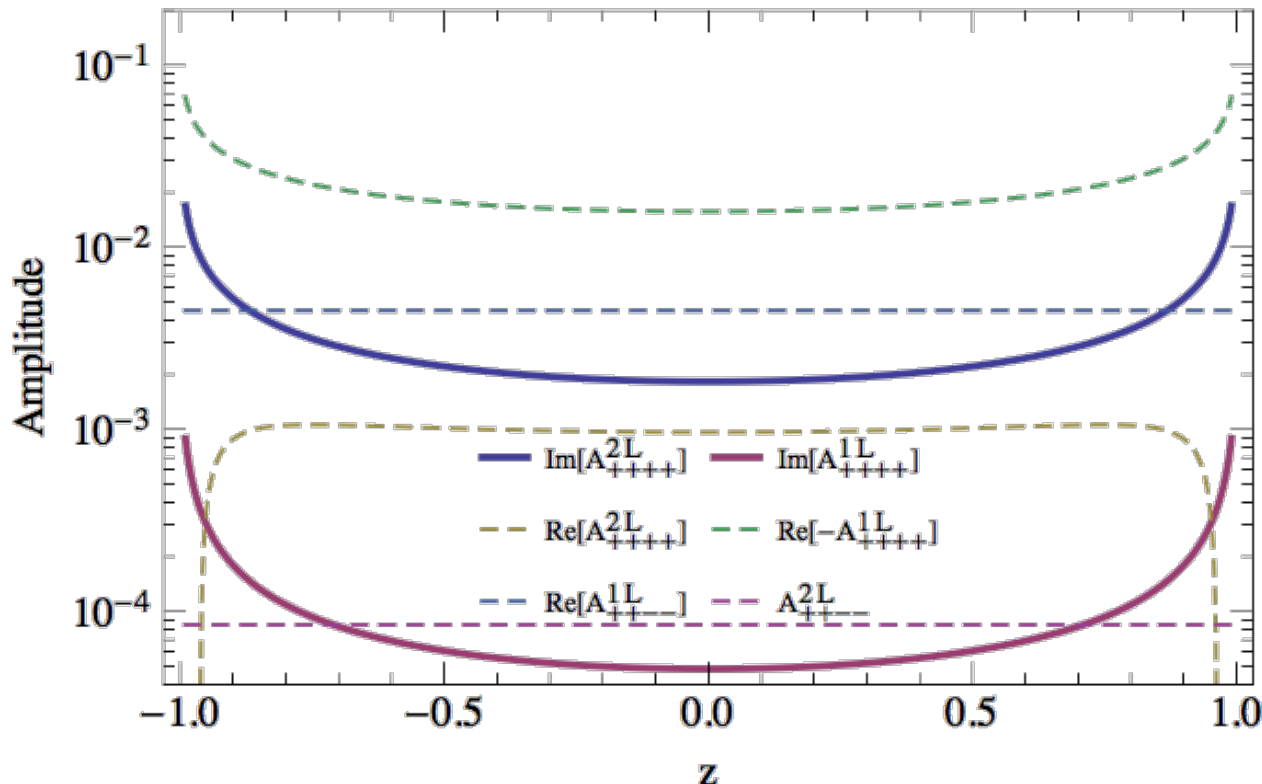
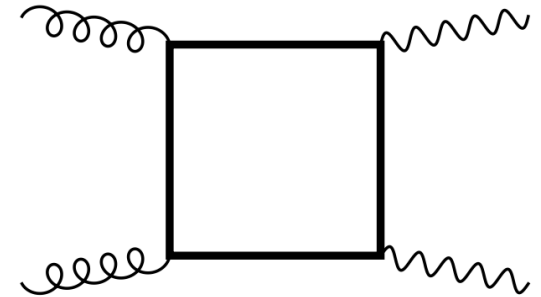


- $A_{++++} = A_{----}$  dominants,  $A_{++--} = A_{--++}$  much smaller
- Light quark dominants
- Angular dependence

# Strong phase and Higgs $gg \rightarrow h \rightarrow \gamma\gamma$

Interfering background are from SM box diagram of  $gg \rightarrow \gamma\gamma$

There is also a strong phase in the background:

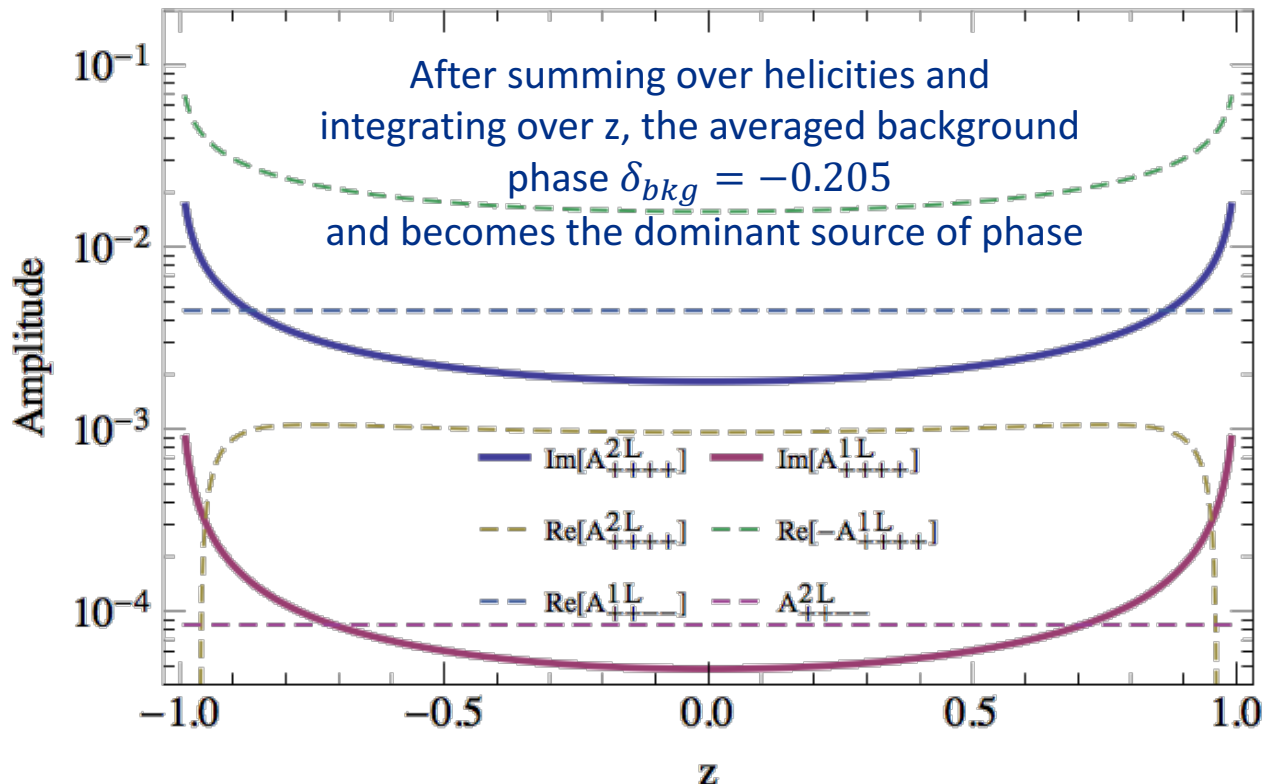
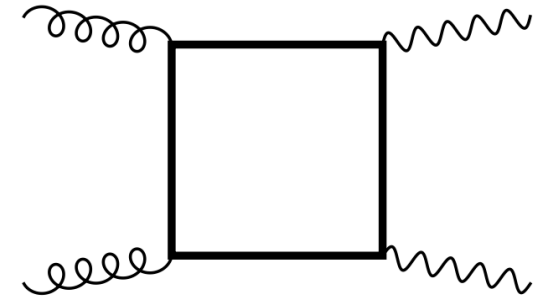


- Angular dependence
- a smaller but negative phase w.r.t to the signal
- At IL, the imaginary part is mainly from  $A_{++++} = A_{----}$  with bottom and charm contributions
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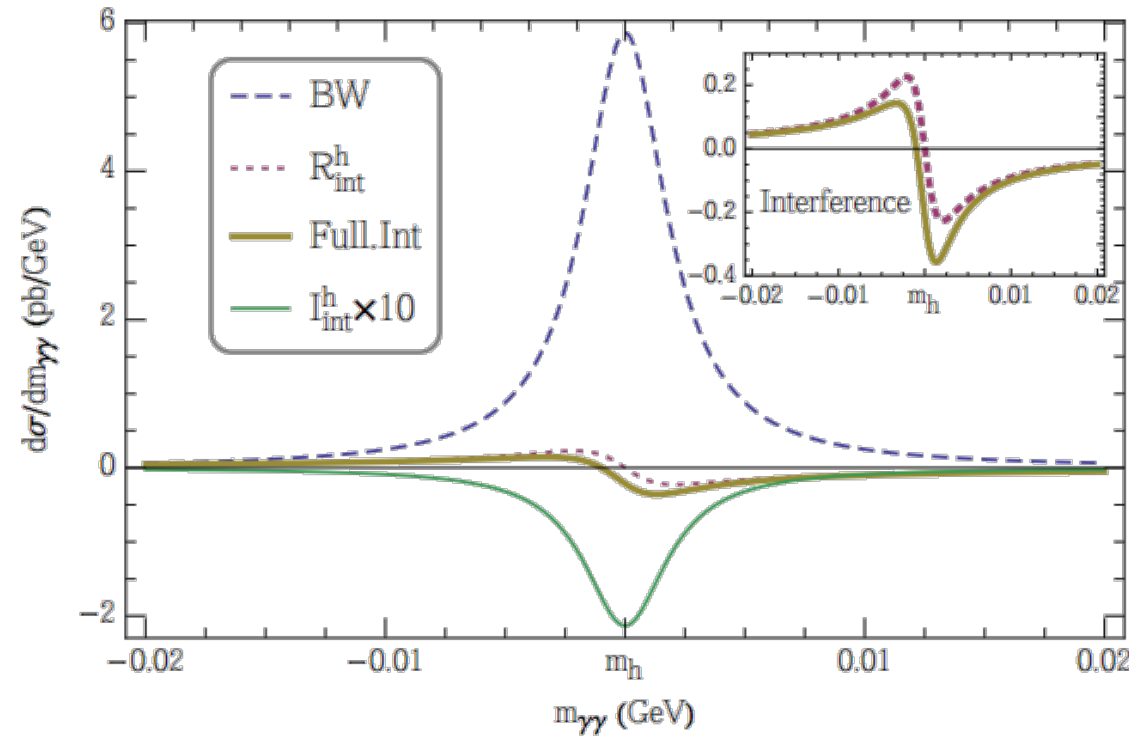
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# Strong phase and Higgs $gg \rightarrow h \rightarrow \gamma\gamma$

$gg \rightarrow h(125 \text{ GeV}) \rightarrow \gamma\gamma$



Define the relative strong phase  $\delta = \delta_{sig} - \delta_{bkg}$ , average over helicity amplitudes and polar angles, one can calculate this new interference piece between signal and background

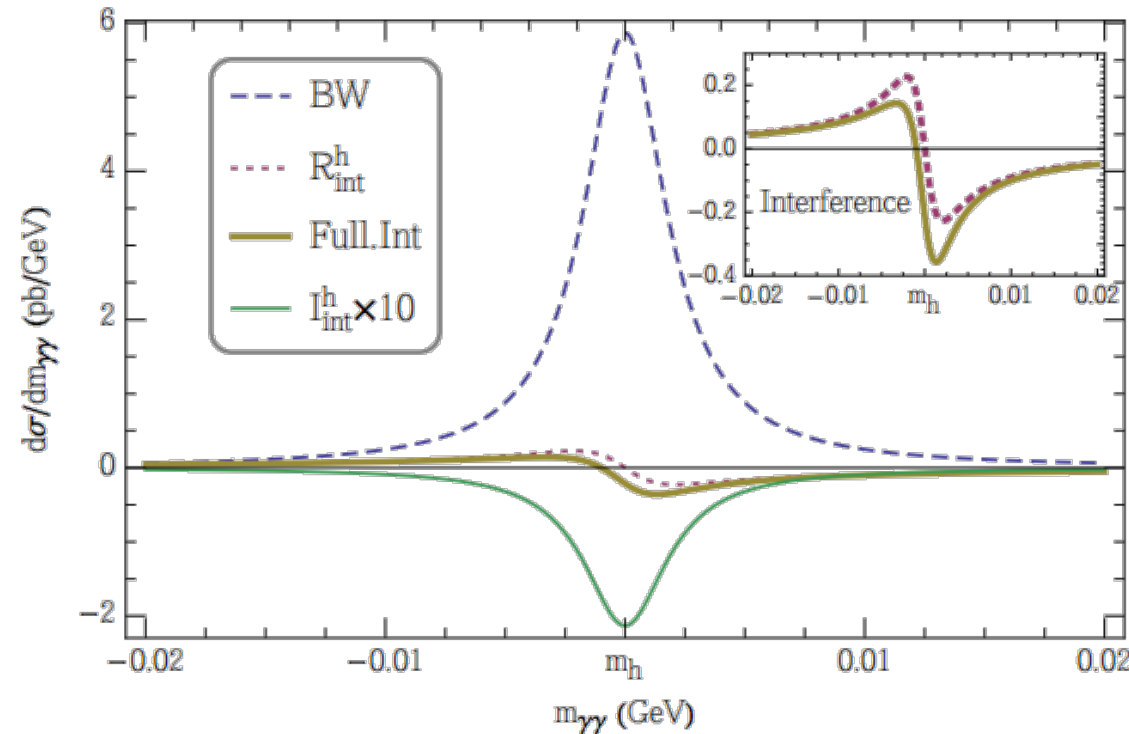
Long been overlooked, the interference term from the strong phase does change the SM rate prediction by  $\sim -2.0\%$ \*

\*This agrees with Dixon and Siu's partial calculation in 03



# Strong phase and Higgs $gg \rightarrow h \rightarrow \gamma\gamma$

$gg \rightarrow h(125 \text{ GeV}) \rightarrow \gamma\gamma$



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Production	Resolved scaling factor
$\sigma(ggF)$	$1.06 \cdot \kappa_t^2 + 0.01 \cdot \kappa_b^2 - 0.07 \cdot \kappa_t \kappa_b$
$\sigma(\text{VBF})$	$0.74 \cdot \kappa_W^2 + 0.26 \cdot \kappa_Z^2$
$\sigma(\text{WH})$	$\kappa_W^2$ ATLAS and CMS legacy combination paper, JHEP

- The size of this effect is relevant
- This effect cannot be factorized into production times decay branching fractions, the framework fails to capture this;

\*This agrees with Dixon and Siu's partial calculation in 03

# Strong phase and Higgs $gg \rightarrow h \rightarrow \gamma\gamma$ (BSM)

This rate change as a new probe of Higgs total width

$$\sigma(gg \rightarrow h \rightarrow \gamma\gamma) \propto \frac{g_{ggh}^2 g_{\gamma\gamma h}^2}{\Gamma_{tot}} - (\sim 2. \%) g_{ggh} g_{\gamma\gamma h}$$

- Unique piece that does not depend on total width;
- Similar to off-shell ZZ measurement;
- Negligible dependence on coupling at different scales.

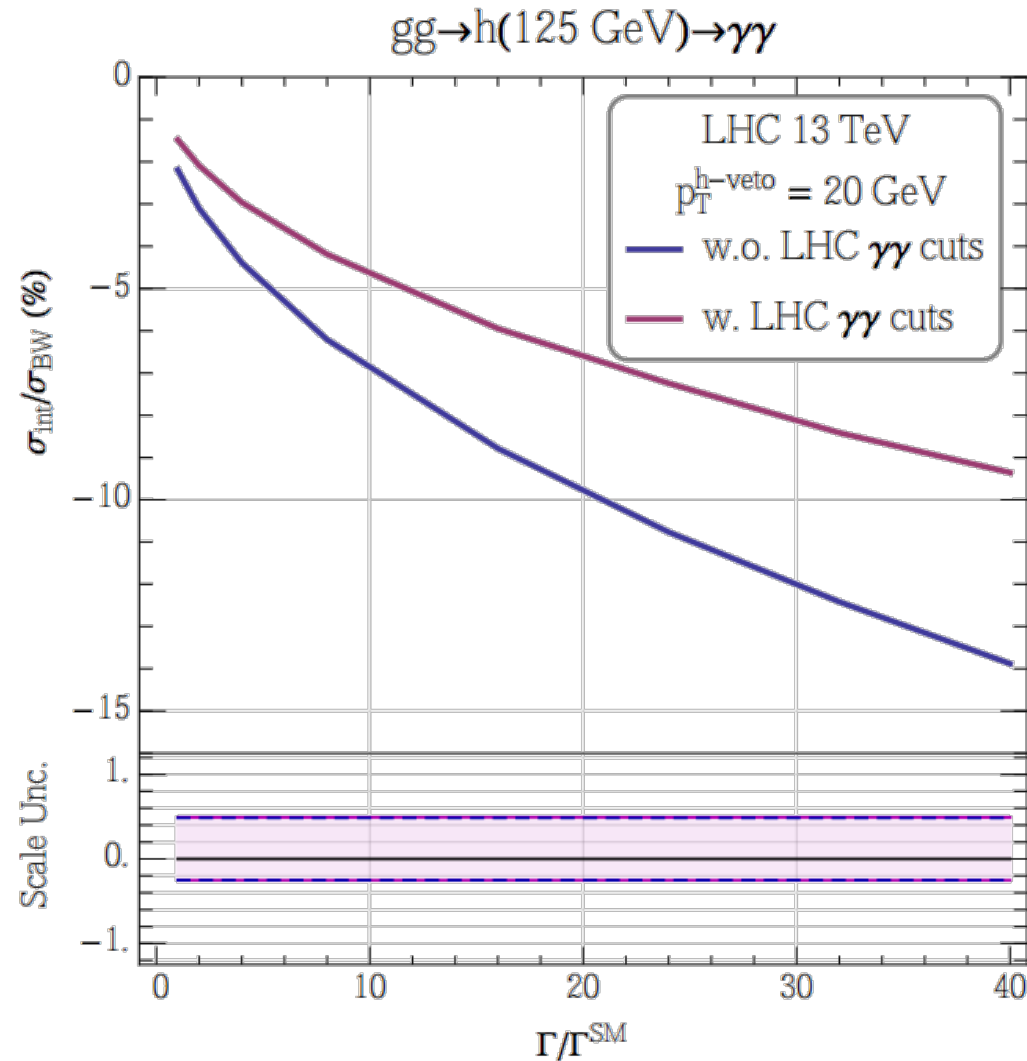
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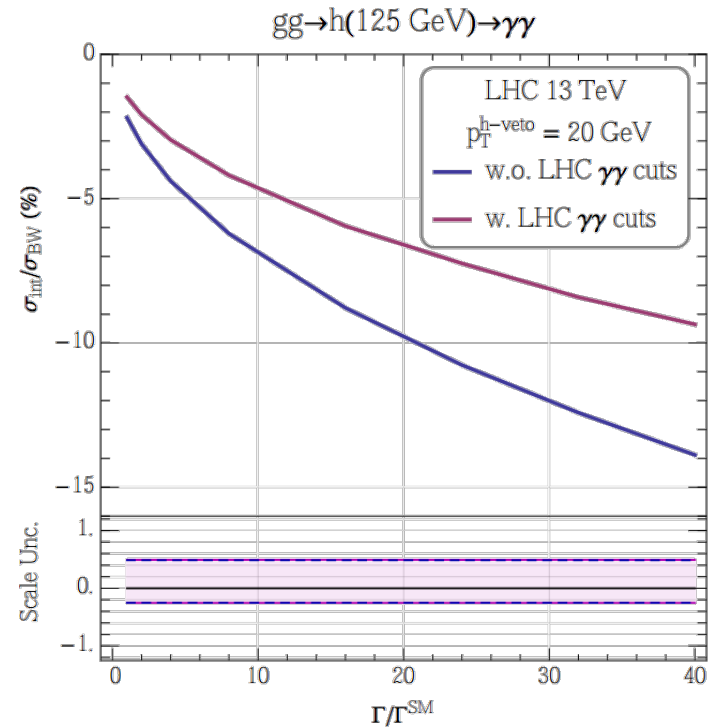


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All on-shell cross sections remains the same as SM predictions.

However, the process  $gg \rightarrow h \rightarrow \gamma\gamma$  will be altered by

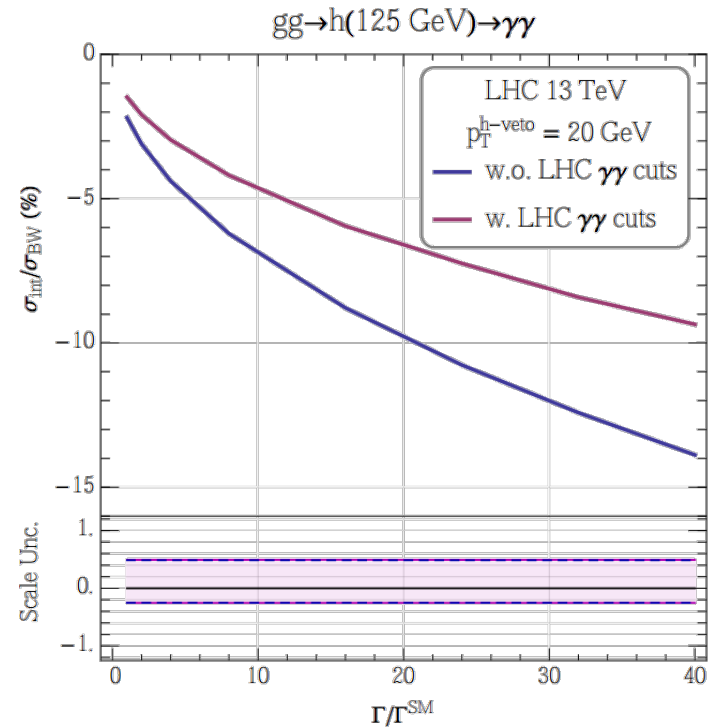
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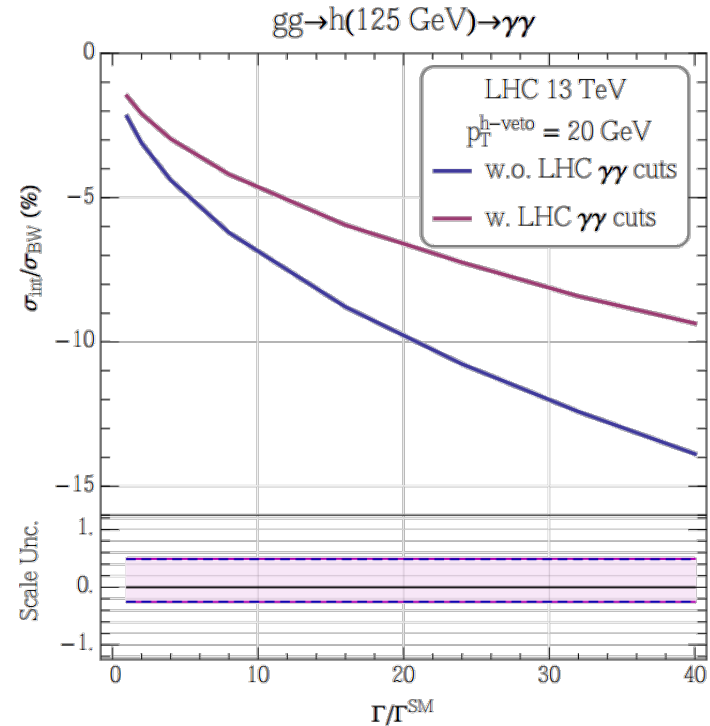
Suppose HL-LHC will measure this effect (e.g., the ratio of  $\sigma_{\gamma\gamma}/\sigma_{4l}$ ) to 4%, it will constraint Higgs total width to  $\sim 13$  times SM value

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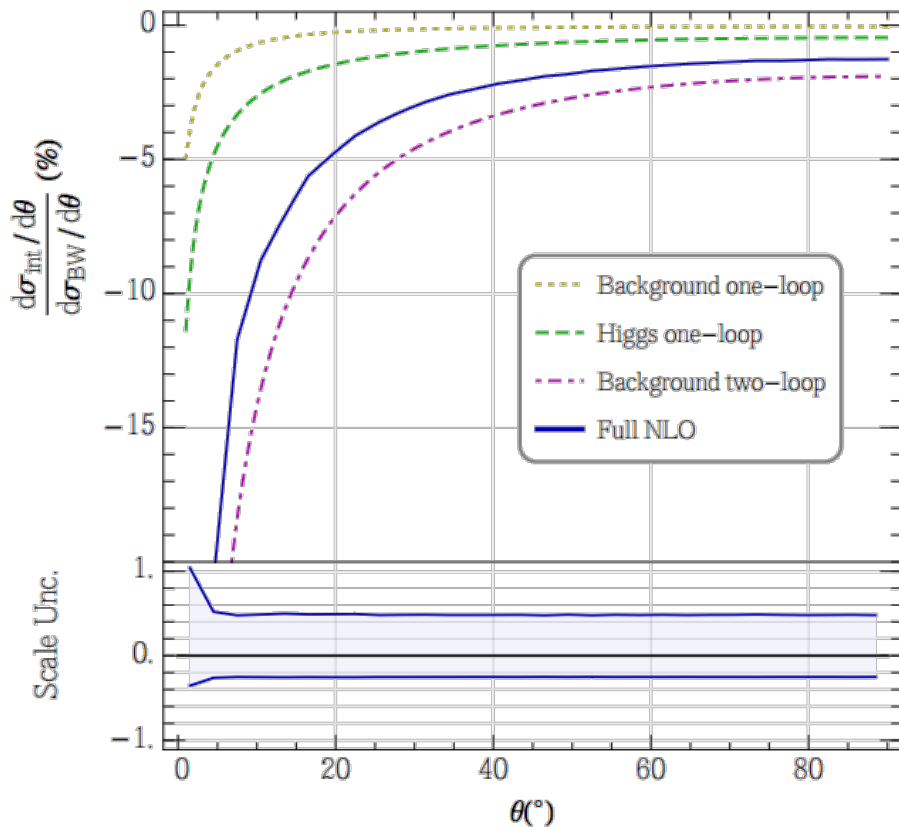
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The FCC-hh will increase the precision by at least one order of magnitude, yielding a **3- $\sigma$**  measurement of the interference effect and bounding the Higgs width

$$0.5 < \Gamma/\Gamma_{SM} < 1.6$$

# Kinematic features of the interference effect

$gg \rightarrow h(125 \text{ GeV}) \rightarrow \gamma\gamma$

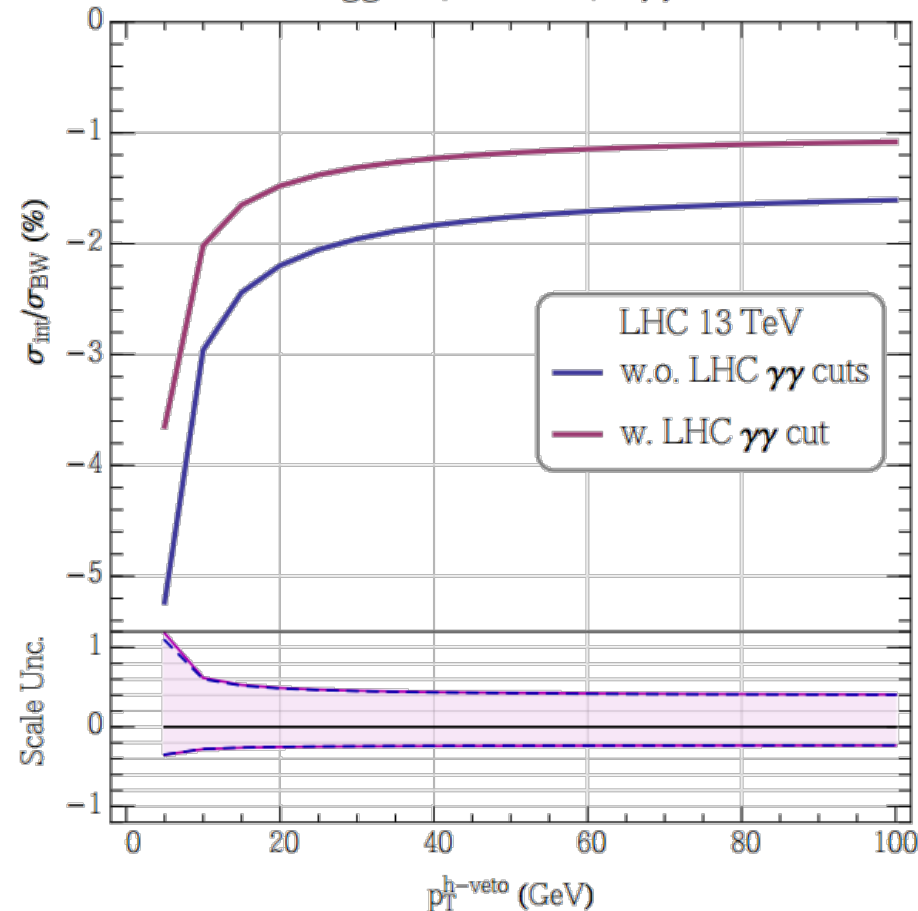


## Angular distribution:

- Interference effects larger in the forward direction, driven by background amplitude kinematics;
- Interference effects  $\sim 0.5\%$  at LO
- Interference effects increases to  $\sim 2\%$  at NLO, driven by the 2L MHV amplitude's large imaginary part
- Fully inclusive cross section has larger B.W. cross section while the interference effect does not increase much, resulting in a smaller relative correction.

# Kinematic features of the interference effect

$gg \rightarrow h(125 \text{ GeV}) \rightarrow \gamma\gamma$



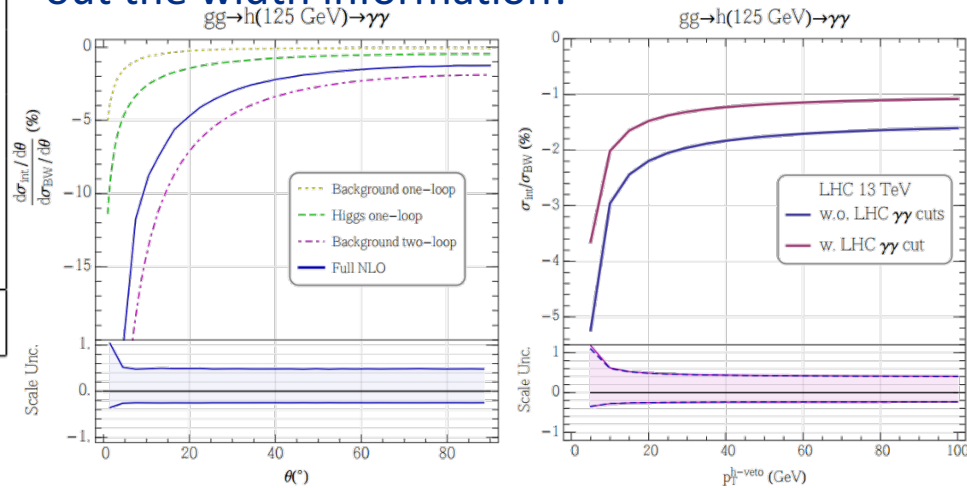
$p_T$ -veto distribution:

Consequently, one can also use jet-veto distribution to see the difference;  
Larger veto- $p_T$ , smaller relative size

# Kinematic features of the interference effect

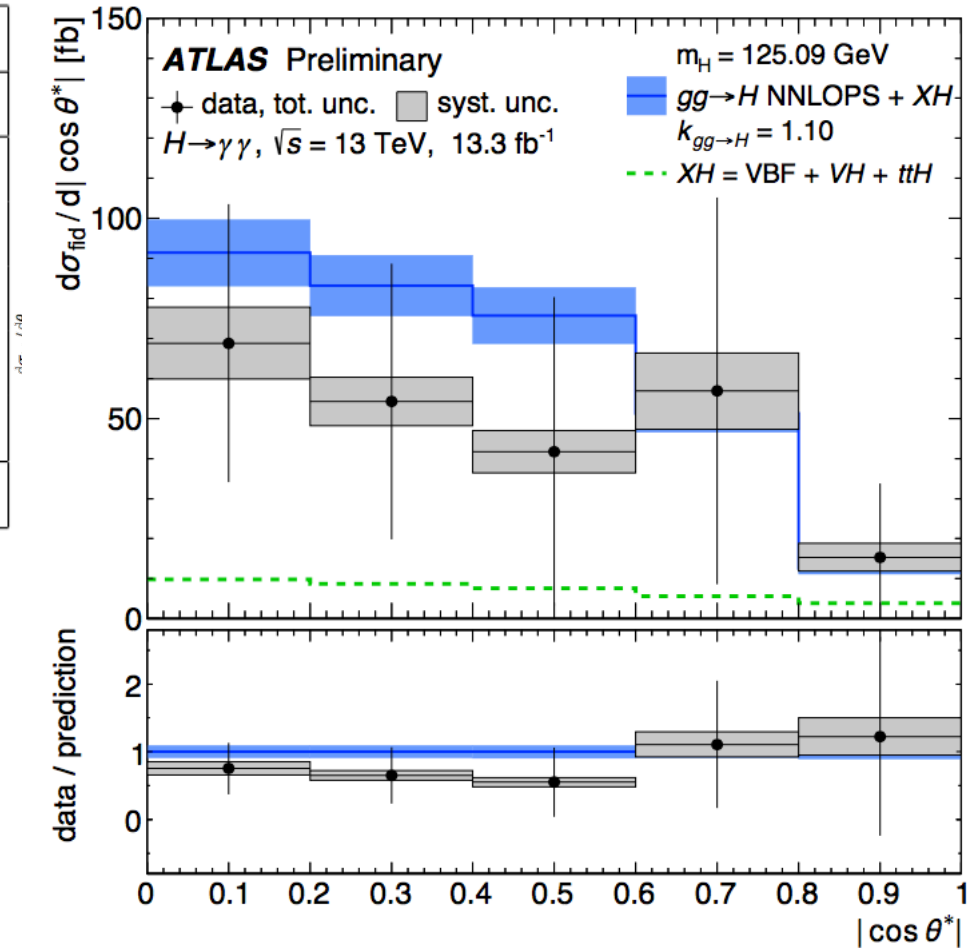
cos θ	$-\sigma_{\text{int}}/\sigma_{\text{BW}}$ (%)		
	no cuts	$p_T^h$ veto	$\gamma\gamma$ cuts+veto
0.0–0.2	$0.87^{+0.34}_{-0.20}$	$1.28^{+0.62}_{-0.32}$	$1.34^{+0.68}_{-0.34}$
0.2–0.4	$0.91^{+0.36}_{-0.21}$	$1.35^{+0.65}_{-0.34}$	$1.41^{+0.72}_{-0.36}$
0.4–0.6	$1.04^{+0.41}_{-0.24}$	$1.53^{+0.74}_{-0.38}$	$1.62^{+0.83}_{-0.42}$
0.6–0.8	$1.37^{+0.53}_{-0.31}$	$1.99^{+0.96}_{-0.50}$	$1.65^{+0.75}_{-0.40}$
0.8–1.0	$3.55^{+1.45}_{-0.82}$	$4.85^{+2.37}_{-1.23}$	—
0.0–1.0	$1.52^{+0.60}_{-0.35}$	$2.20^{+1.06}_{-0.55}$	$1.48^{+0.73}_{-0.38}$

Differential distributions help map out the interference effect, and it can help mapping out the width information!



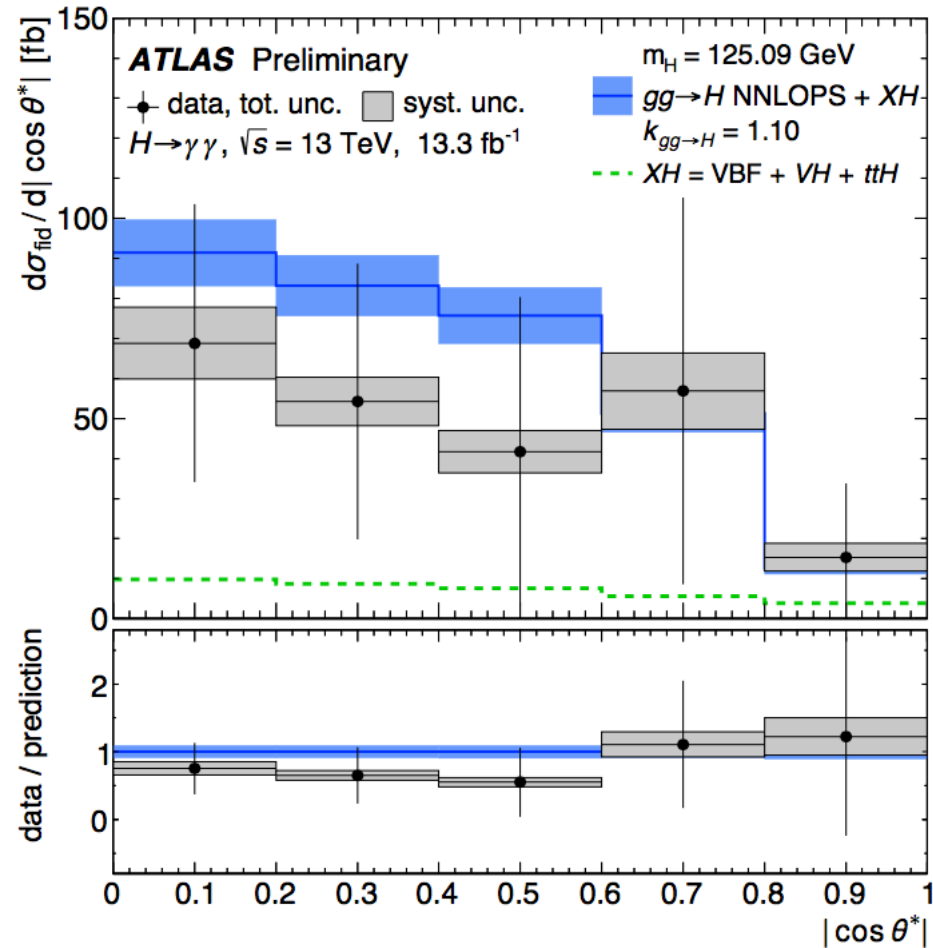
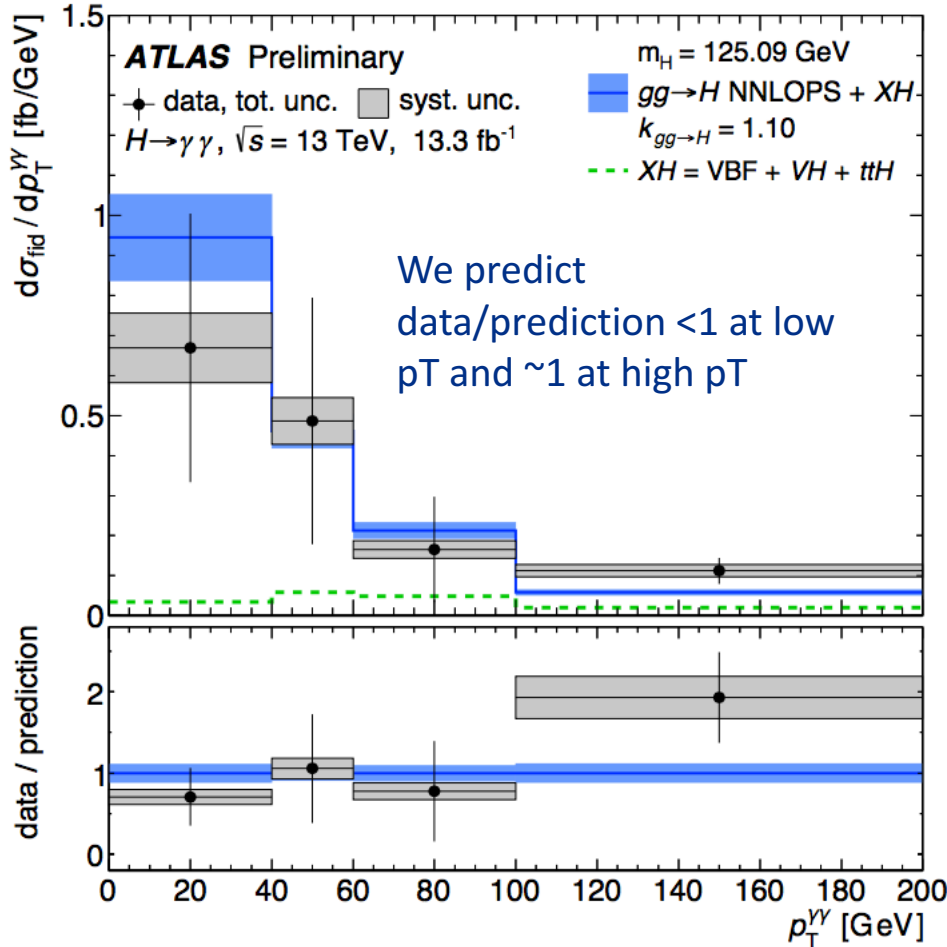
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# Kinematic features of the interference effect

cos θ	-σ <sub>int</sub> /σ <sub>BW</sub> (%)		
	no cuts	p <sub>T</sub> <sup>h</sup> veto	γγ cuts+veto
0.0 - 0.2	0.07 ± 0.34	1.00 ± 0.62	1.04 ± 0.68





# Summary and outlook for $gg \rightarrow h \rightarrow \gamma\gamma$

We uniquely explore the physics consequences of this strong phase in Higgs physics

We choose the  $gg \rightarrow h \rightarrow \gamma\gamma$  as one example and found the inclusion of this strong phase reduce the signal rate by  $\sim 2\%$  (at NLO); an important ingredient should be included in **all** LHC Higgs precision programs (global fit, etc.)

This effect could be used as probes to BSM physics, providing information on

- Higgs light quark Yukawas
- **Higgs total width**
- CPV effect

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There are many more other interesting channels and physics to explore using this interference effect.

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**Thank you!**

# Backup

$$g_{1,2}^{\tilde{t}}(S) \frac{\sqrt{2}}{v} = \begin{cases} m_t^2 + \cos 2\beta (D_{L/R}^t \sin^2 \theta_{\tilde{t}} + D_{R/L}^t \cos^2 \theta_{\tilde{t}}) \pm \frac{1}{2} m_t X_t \sin 2\theta_{\tilde{t}} & , \text{ for } S = h \\ -\frac{m_t^2}{\tan \beta} - \sin 2\beta (D_{L/R}^t \sin^2 \theta_{\tilde{t}} + D_{R/L}^t \cos^2 \theta_{\tilde{t}}) \mp \frac{1}{2} m_t Y_t \sin 2\theta_{\tilde{t}} & , \text{ for } S = H \\ \mp \frac{1}{2} m_t Y_t \sin 2\theta_{\tilde{t}} & , \text{ for } S = A \end{cases}$$

$$D_L^u = \frac{1}{2} m_W^2 (1 - \frac{1}{3} \tan^2 \theta_W) \cos 2\beta$$

$$D_R^u = \frac{2}{3} m_W^2 \tan^2 \theta_W \cos 2\beta$$

$$D_L^d = -\frac{1}{2} m_W^2 (1 + \frac{1}{3} \tan^2 \theta_W) \cos 2\beta$$

$$D_R^d = -\frac{1}{3} m_W^2 \tan^2 \theta_W \cos 2\beta$$

$$X_t Y_t = \frac{A_t^2}{\tan \beta} - \frac{\mu^2}{\tan \beta} - A_t \mu (1 - \frac{1}{\tan^2 \beta}).$$

$$X_u = A_u - \frac{\mu}{\tan \beta}$$

$$X_d = A_d - \mu \tan \beta$$

$$Y_u = \frac{A_u}{\tan \beta} + \mu$$

$$Y_d = A_b \tan \beta + \mu,$$

zero LR mixing :  $m_{Q_3} = 900 \text{ GeV}, m_{t_R} = 400 \text{ GeV}, X_t = 0$

$\text{mh}_{\text{max}}^*$  :  $m_{Q_3} = 900 \text{ GeV}, m_{t_R} = 540 \text{ GeV}, Y_t = 2X_t = 3415 \text{ GeV}$

$$g_{sgg}(\hat{s}) = \frac{\alpha_s}{2\sqrt{2}\pi} \frac{y_t^s}{m_t} I_{\frac{1}{2}}(\tau_t), \quad \tilde{g}_{sgg}(\hat{s}) = \frac{\alpha_s}{2\sqrt{2}\pi} \frac{\tilde{y}_t^s}{m_t} \tilde{I}_{\frac{1}{2}}(\tau_t), \quad (2.3)$$

where  $I_{\frac{1}{2}}(\tau_t)$  and  $\tilde{I}_{\frac{1}{2}}(\tau_t)$  are the corresponding loop-functions and<sup>1</sup>

$$\tau_t = \frac{\hat{s}}{4m_t^2}, \quad f(\tau) = \begin{cases} -\arcsin^2(\sqrt{\tau}) & \text{for } \tau \leq 1, \\ \frac{1}{4} \left( \log \frac{1+\sqrt{1-1/\tau}}{1-\sqrt{1-1/\tau}} - i\pi \right)^2 & \text{for } \tau > 1 \end{cases}$$

$$I_{1/2}(\tau) = \frac{1}{\tau^2}(\tau + (\tau - 1)f(\tau)), \quad \tilde{I}_{1/2}(\tau) = \frac{f(\tau)}{\tau}. \quad (2.4)$$

$$\mathcal{A}^{\text{even}} \propto y_t g_{sgg} = y_t^2 I_{\frac{1}{2}}(\tau_t), \quad \mathcal{A}^{\text{odd}} \propto \tilde{y}_t \tilde{g}_{sgg} = \tilde{y}_t^2 \tilde{I}_{\frac{1}{2}}(\tau_t). \quad (2.8)$$

We can define the phase of the resonant amplitudes as,

$$\mathcal{A} = \frac{\hat{s}}{\hat{s} - m_S^2 + i\Gamma_S m_S} |\bar{\mathcal{A}}| e^{i\theta_{\bar{\mathcal{A}}}}, \quad \text{with } \theta_{\bar{\mathcal{A}}} \equiv \arg(\bar{\mathcal{A}}). \quad (2.9)$$

$$\hat{\sigma}_{\text{BSM}}^{\text{odd}}(\hat{s}; \tilde{y}_t)(gg \rightarrow S \rightarrow t\bar{t}) = \hat{\sigma}_{\text{B.W.}}^{\text{odd}}(\hat{s}; \tilde{y}_t) + \hat{\sigma}_{\text{Int.}}^{\text{odd}}(\hat{s}; \tilde{y}_t)$$

$$\frac{d\hat{\sigma}_{\text{B.W.}}^{\text{odd}}(\hat{s}; \tilde{y}_t)}{dz} = \frac{3\alpha_s^2 \hat{s}^2}{4096\pi^3 v^2} \beta \left| \frac{\tilde{y}_t^2 \tilde{I}_{\frac{1}{2}}(\tau_t)}{\hat{s} - m_S^2 + im_S \Gamma_S(\hat{s})} \right|^2$$

$$\frac{\hat{\sigma}_{\text{Int.}}^{\text{odd}}(\hat{s}; \tilde{y}_t)}{dz} = -\frac{\alpha_s^2}{64\pi} \frac{\beta}{1 - \beta^2 z^2} \text{Re} \left[ \frac{\tilde{y}_t^2 \tilde{I}_{\frac{1}{2}}(\tau_t)}{\hat{s} - m_S^2 + im_S \Gamma_S(\hat{s})} \right]$$

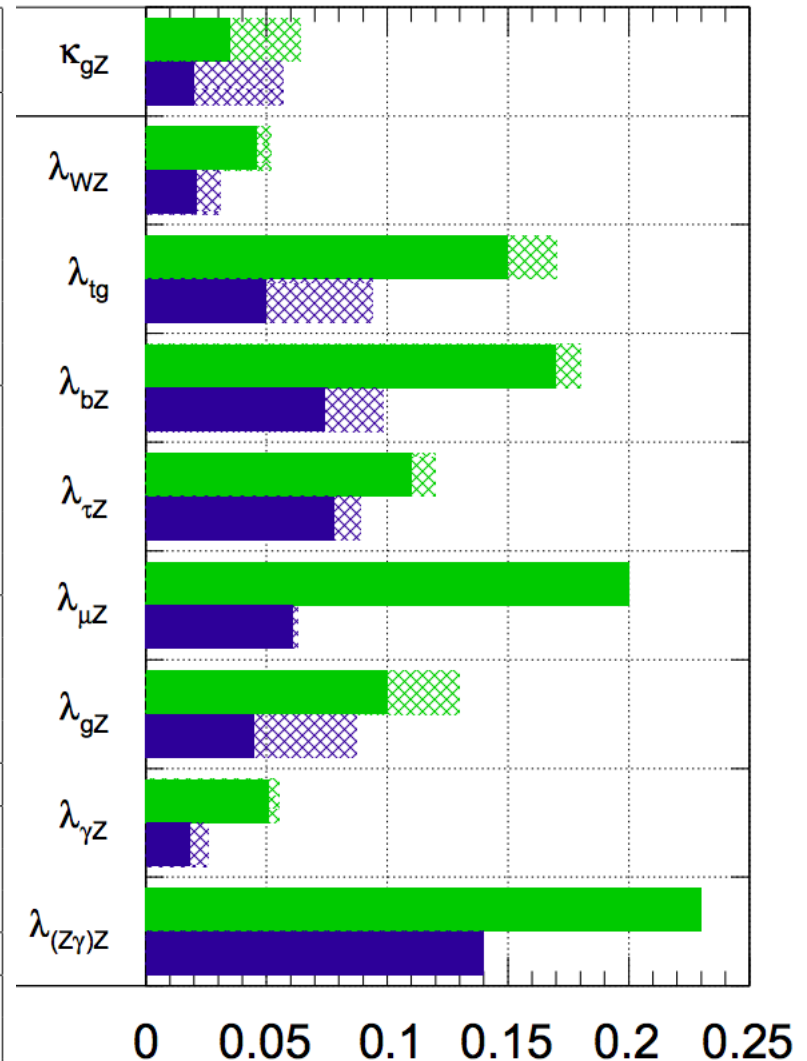
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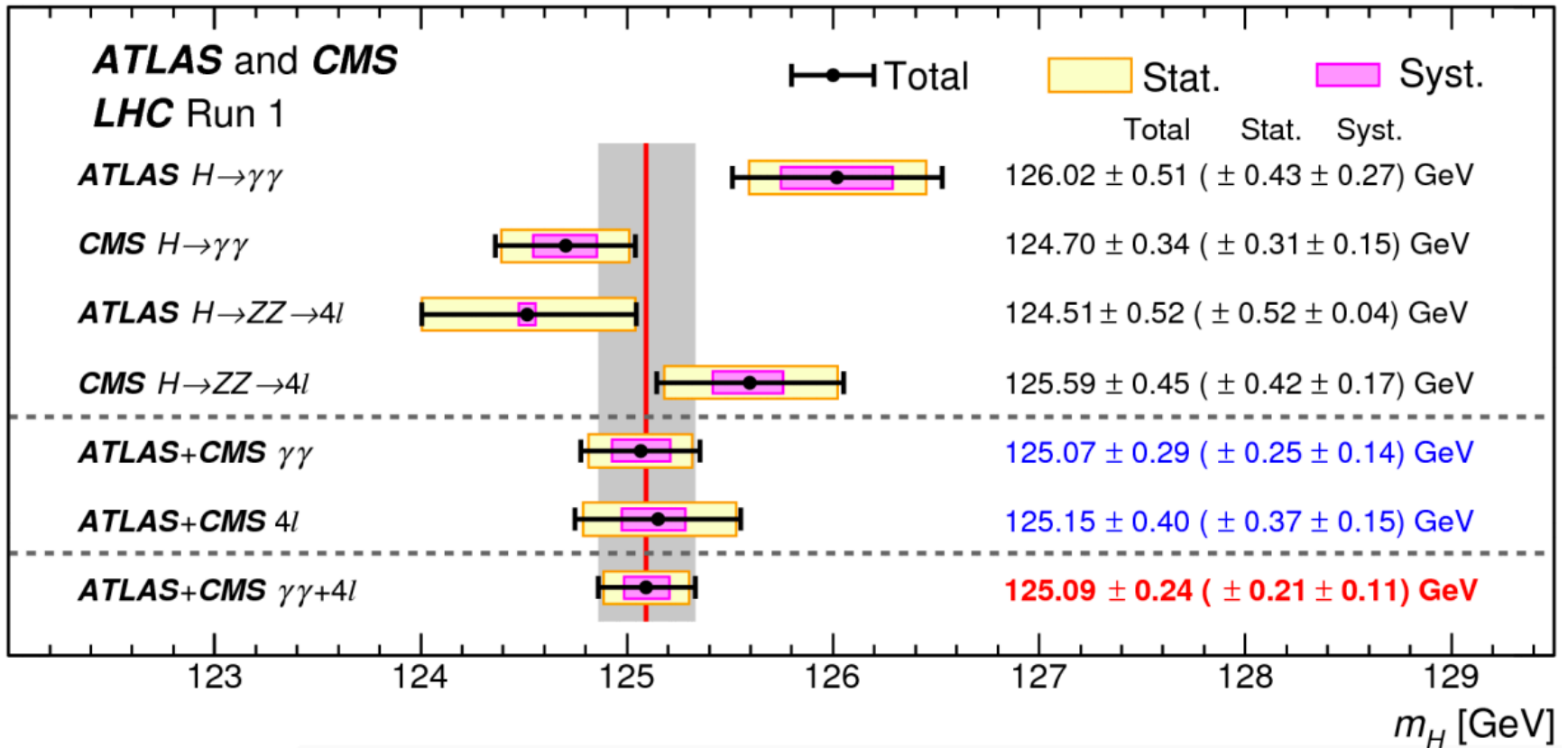
$$\frac{d\hat{\sigma}_{\text{Int.}}^{\text{even}}(\hat{s}; y_t)}{dz} = -\frac{\alpha_s^2}{64\pi} \frac{\beta^3}{1 - \beta^2 z^2} \text{Re} \left[ \frac{y_t^2 I_{\frac{1}{2}}(\tau_t)}{\hat{s} - m_S^2 + im_S \Gamma_S(\hat{s})} \right]$$

$$\frac{d\sigma_{\text{Int.}}^{S_1-S_2}(\hat{s})(gg \rightarrow S_1, S_2 \rightarrow t\bar{t})}{dz} = \frac{3\alpha_s^2 \hat{s}^2}{2048\pi^3 v^2} \text{Re} \left[ \frac{(y_{t,S_1} y_{t,S_2} |I_{\frac{1}{2}}(\tau_t)|^2 + \tilde{y}_{t,S_1} \tilde{y}_{t,S_2} |\tilde{I}_{\frac{1}{2}}(\tau_t)|^2) (\beta^2 y_{t,S_1} y_{t,S_2} + \tilde{y}_{t,S_1} \tilde{y}_{t,S_2})}{(\hat{s} - m_{S_1}^2 + im_{S_1} \Gamma_{S_1}(\hat{s})) (\hat{s} - m_{S_2}^2 - im_{S_2} \Gamma_{S_2}(\hat{s}))} \right] \quad (6)$$

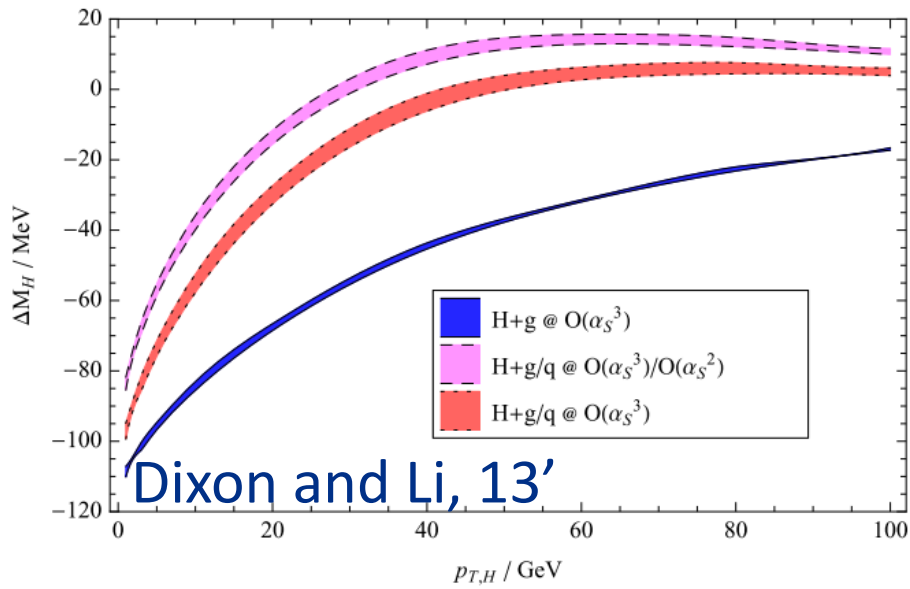
$\Delta\mu/\mu$	$300 \text{ fb}^{-1}$		$3000 \text{ fb}^{-1}$	
	All unc.	No theory unc.	All unc.	No theory unc.
$H \rightarrow \gamma\gamma$ (comb.)	0.13	0.09	0.09	0.04
(0j)	0.19	0.12	0.16	0.05
(1j)	0.27	0.14	0.23	0.05
(VBF-like)	0.47	0.43	0.22	0.15
(WH-like)	0.48	0.48	0.19	0.17
(ZH-like)	0.85	0.85	0.28	0.27
( $ttH$ -like)	0.38	0.36	0.17	0.12
$H \rightarrow ZZ$ (comb.)	0.11	0.07	0.09	0.04
(VH-like)	0.35	0.34	0.13	0.12
( $ttH$ -like)	0.49	0.48	0.20	0.16
(VBF-like)	0.36	0.33	0.21	0.16
(ggF-like)	0.12	0.07	0.11	0.04
$H \rightarrow WW$ (comb.)	0.13	0.08	0.11	0.05
(0j)	0.18	0.09	0.16	0.05
(1j)	0.30	0.18	0.26	0.10
(VBF-like)	0.21	0.20	0.15	0.09
$H \rightarrow Z\gamma$ (incl.)	0.46	0.44	0.30	0.27
$H \rightarrow b\bar{b}$ (comb.)	0.26	0.26	0.14	0.12
(WH-like)	0.57	0.56	0.37	0.36
(ZH-like)	0.29	0.29	0.14	0.13
$H \rightarrow \tau\tau$ (VBF-like)	0.21	0.18	0.19	0.15
$H \rightarrow \mu\mu$ (comb.)	0.39	0.38	0.16	0.12
(incl.)	0.47	0.45	0.18	0.14
( $ttH$ -like)	0.74	0.72	0.27	0.23



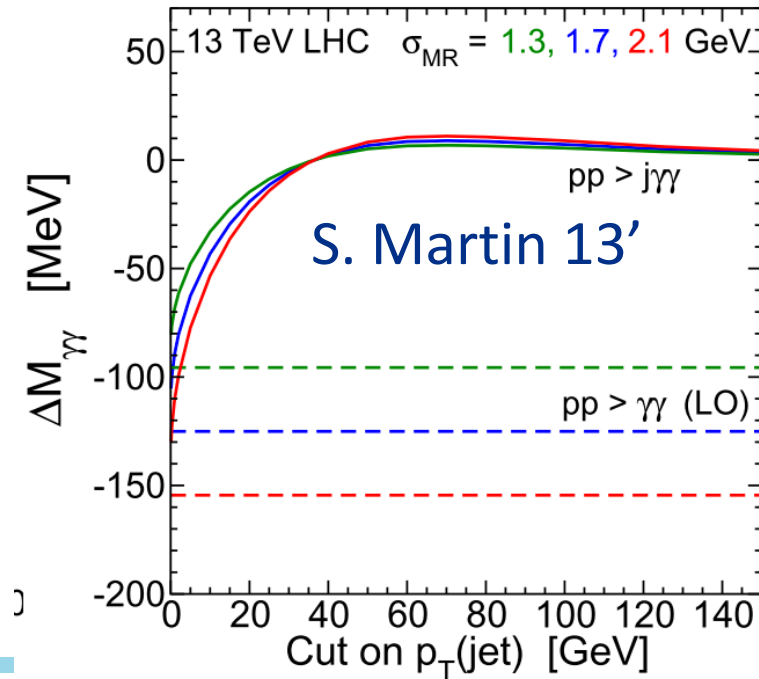
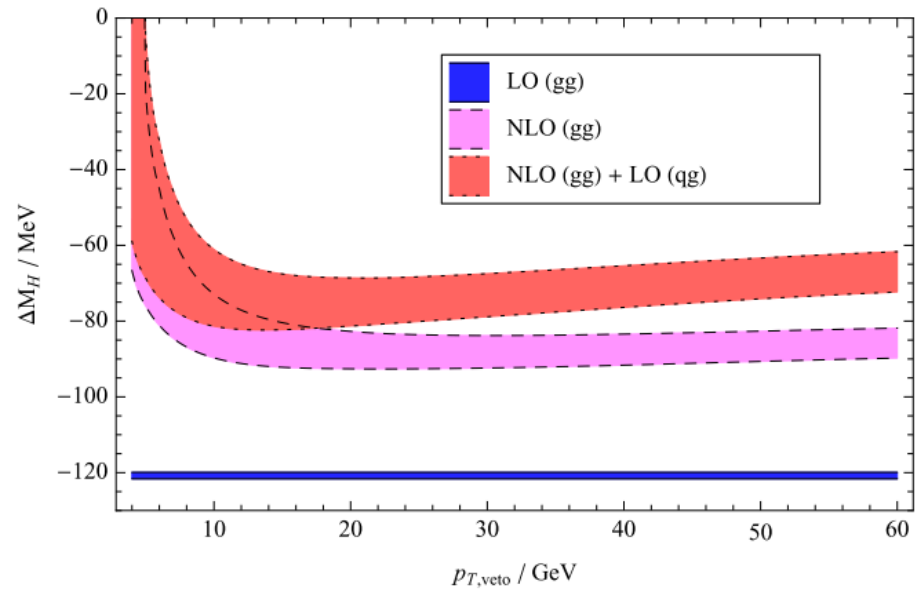
$$\Delta\lambda_{XY} = \Delta\left(\frac{\kappa_X}{\kappa_Y}\right)$$





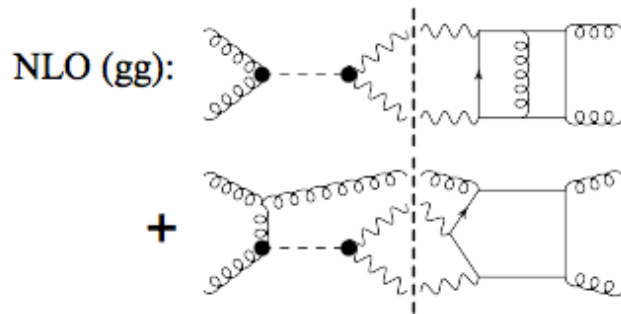
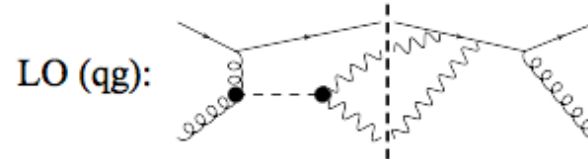
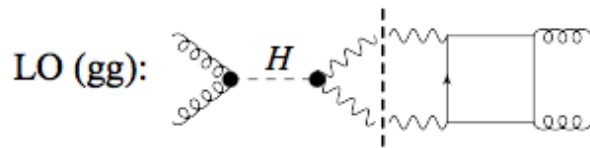


Dixon and Li, 13'

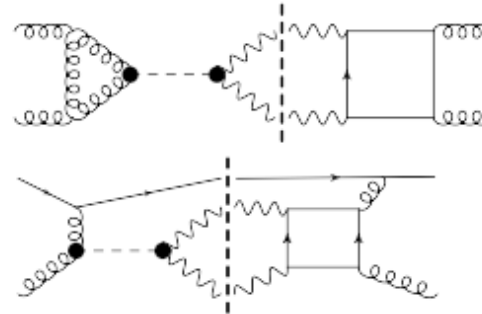


S. Martin 13'

Dots represent point-like interaction, where the phase is ignored.

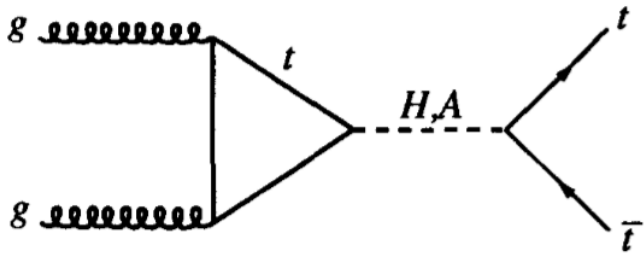


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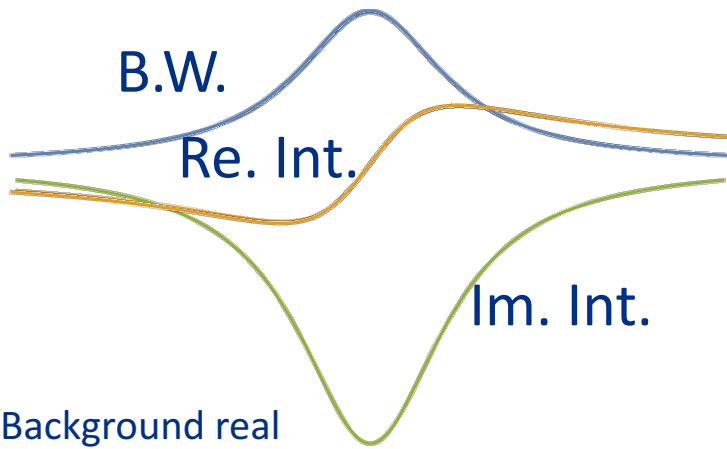
# Sketching the interference



$$g_{Sgg}(\hat{s}) = \frac{\alpha_s}{2\sqrt{2}\pi} \frac{y_t^S}{m_t} I_{1/2}(\tau_t)$$

$$\tau_t = \frac{\hat{s}}{4m_t^2}, \quad f(\tau) = \begin{cases} \arcsin^2(\sqrt{\tau}) & \text{for } \tau \leq 1, \\ -\frac{1}{4} \left( \log \frac{1+\sqrt{1-1/\tau}}{1-\sqrt{1-1/\tau}} - i\pi \right)^2 & \text{for } \tau > 1 \end{cases}$$

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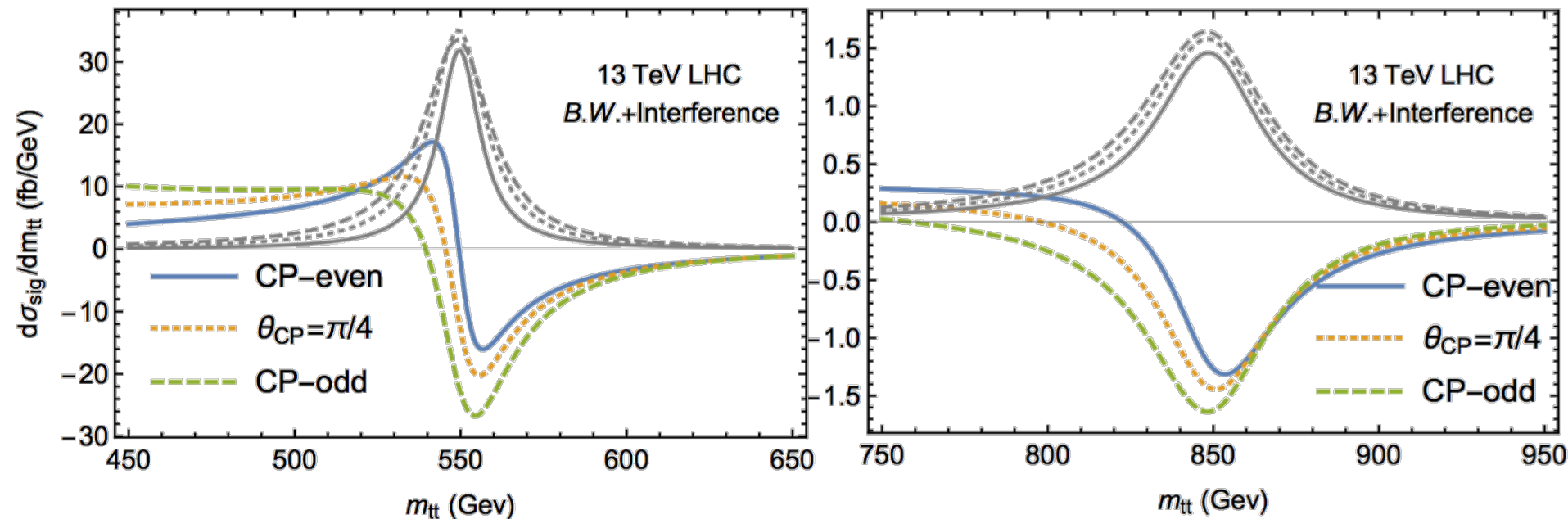


Background real

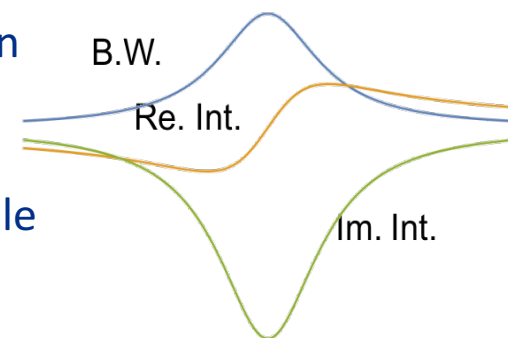
Re. Int.– Interference from the real part of the propagator (normal interference, parton level no contribution to the rate, shift the mass peak)

Im. Int.– Interference from the imaginary part of propagator (rare case, changes signal rate)

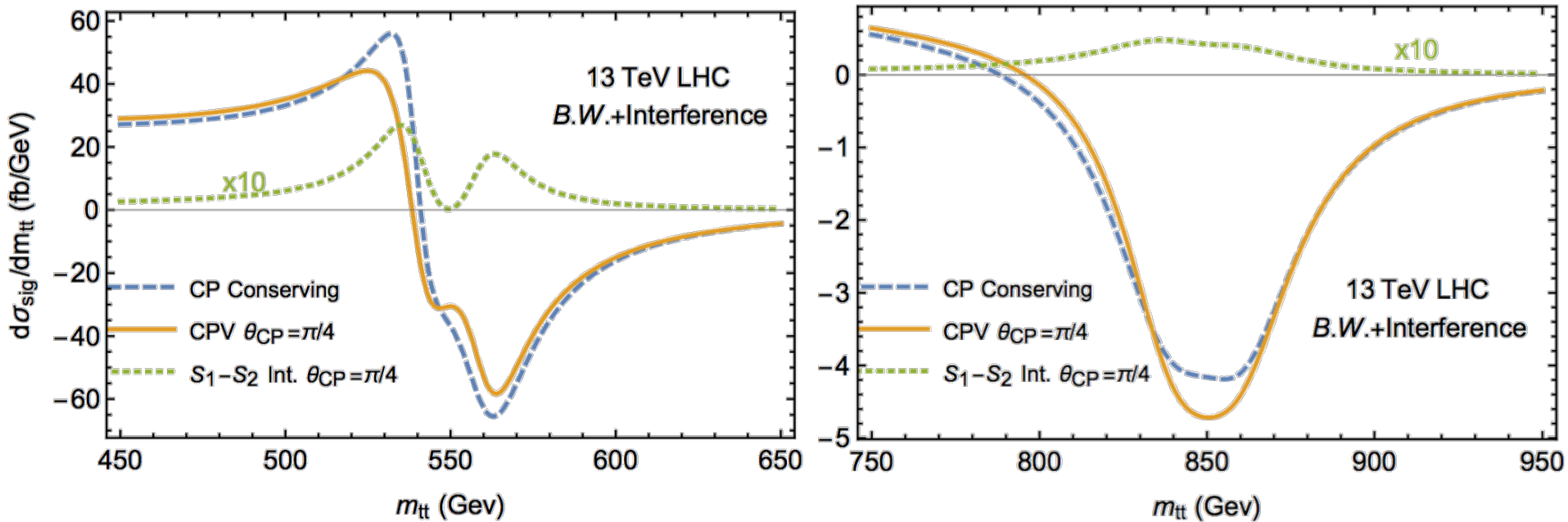
# Challenges



- Gray lines, Breit-Wigner contribution (subtle differences between the scalar case the pseudoscalar case);
- Colored lines, total BSM signal lineshapes;
- (Left panel) for 550 GeV scalars, the loop function has comparable real and imaginary components. The imaginary interference “cancels” the Breit-Wigner, leaving only Bump-dip structure;
- (Right panel) for 850 GeV scalar, the loop function is almost purely imaginary and the total lineshapes become a pure dip.



# Opportunities—nearly degenerate with CPV



(left panel) 540 and 560 GeV scalars

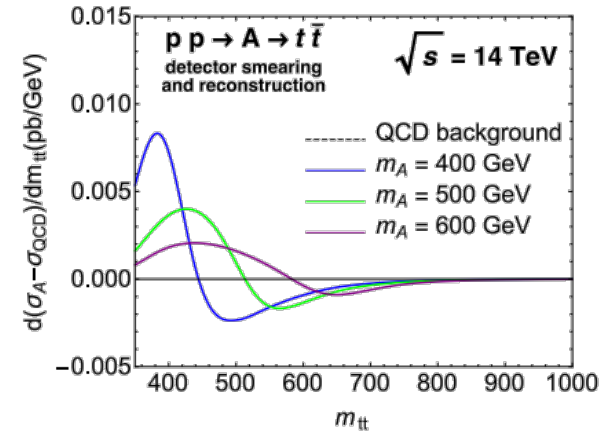
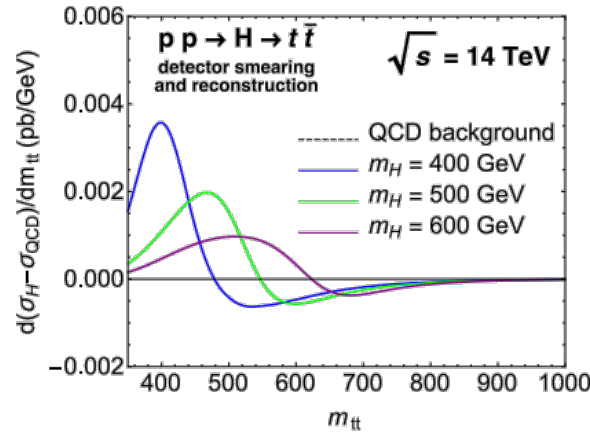
(right panel) 840 and 860 GeV scalars

The signature—bumps and dips—roughly doubled, increasing the potential sensitivity;

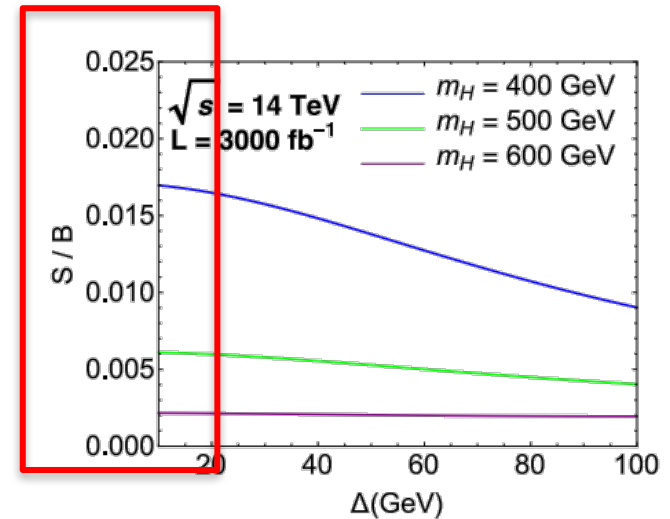
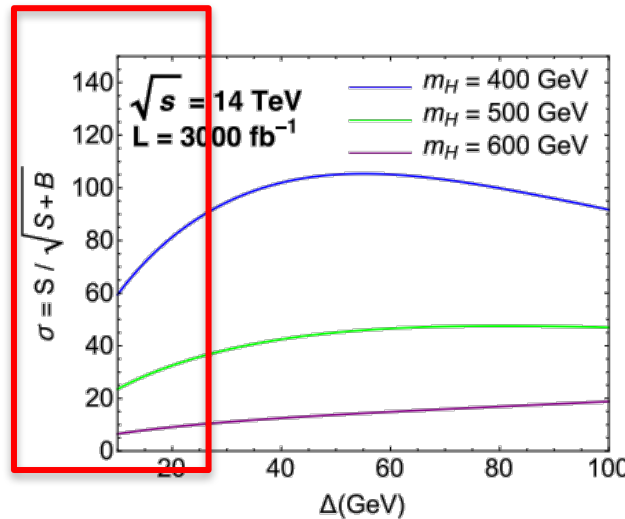
With CPV, new interference between the two heavy nearly degenerate scalars occurs (although the effect is small) but unique.

# LHC perspectives – Challenges

Statistically promising;  
Systematically, challenging.



Craig, Draper, Erasmo, Thomas, Zhang '15



Taking only one central bin,  
ignored shape information