

# ***Effects of phase transition on Collective flows from microscopic transport model***

**Yasushi Nara (Akita International University)**

Y. N., H. Niemi, A. Ohnishi, H. Stoecker, PRC94, (2016)

Y. N., H. Niemi, J. Steinheimer, H. Stoecker, PLB769 (2017)

Y. N., H. Niemi, A. Ohnishi, J. Steinheimer, X. Luo, H. Stocker,  
nucl-th-1708.05617

# Outline

$$\frac{dN}{d^2p_T} = \frac{d^2N}{2\pi dp_T dy} (1 + 2v_1 \cos(\phi) + 2v_2 \cos(2\phi) + \dots)$$

- Introduction: beam energy dependence of v1 and v2
- Non-equilibrium transport model JAM with EoS effect
- Results on v0, v1 and v2 at high baryon density region

first-order phase transition:

v0: harder, v1: negative v2: larger

- Summary

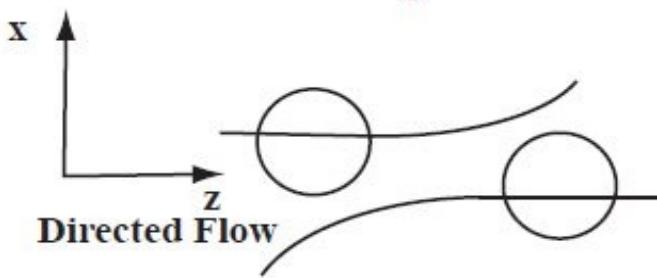
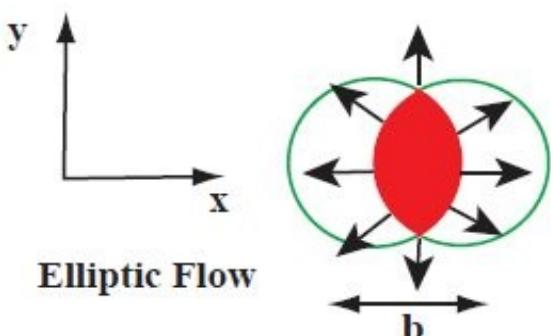
# Determination of EOS at high density from an anisotropic flow in heavy ion collisions

Fourier decomposition of single particle inclusive spectra:

$$\frac{dN}{d^2p_T} = \frac{d^2N}{2\pi dp_T dy} (1 + 2v_1 \cos(\phi) + 2v_2 \cos(2\phi) + \dots)$$

$$v_1 = \left\langle \frac{p_x}{p_T} \right\rangle \quad v_2 = \left\langle \frac{p_x^2 - p_y^2}{p_T^2} \right\rangle$$

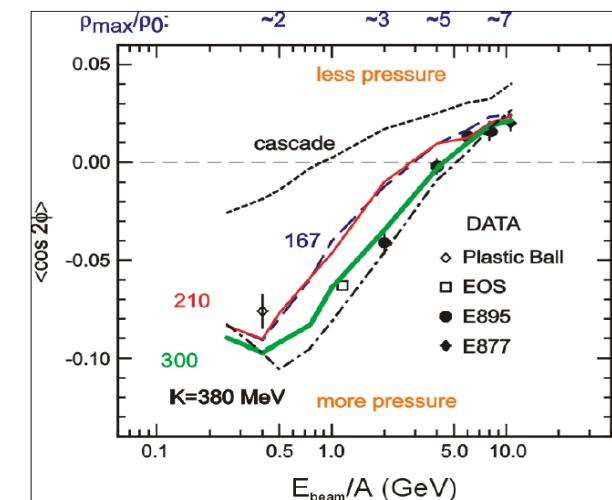
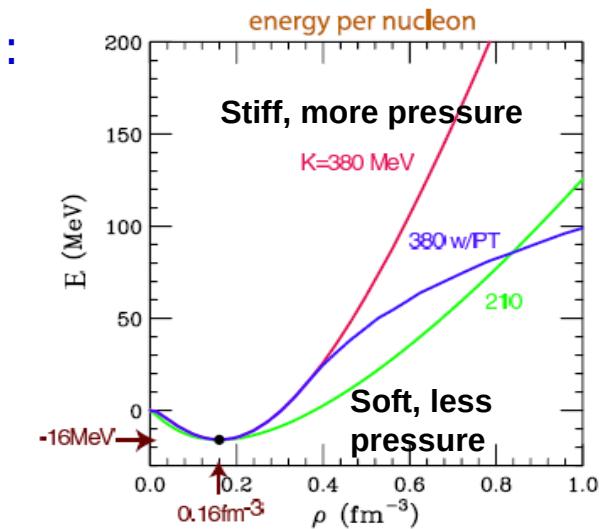
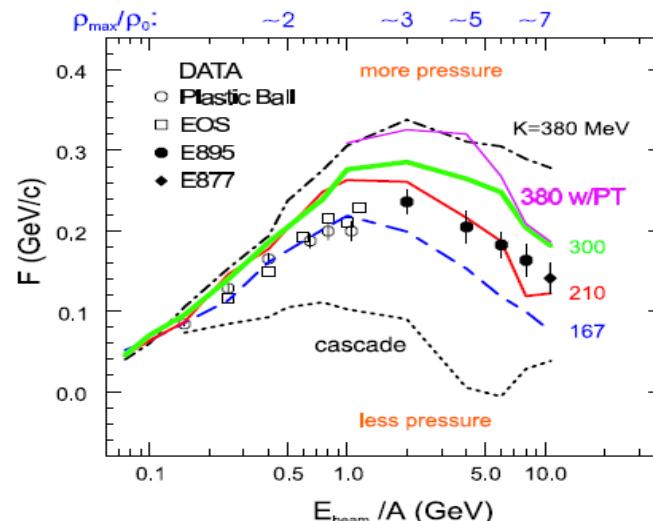
$$F = \left. \frac{dv_1}{dy} \right|_{y=0}$$



$$F = \left. \frac{\langle p_x/A \rangle}{d(y/y_{cm})} \right|_{y/y_{cm}=1}$$

P. Danielewicz, R. Lacey, W.G. Lynch,  
Science 298 (2002) 1592

In-plane flow, v1



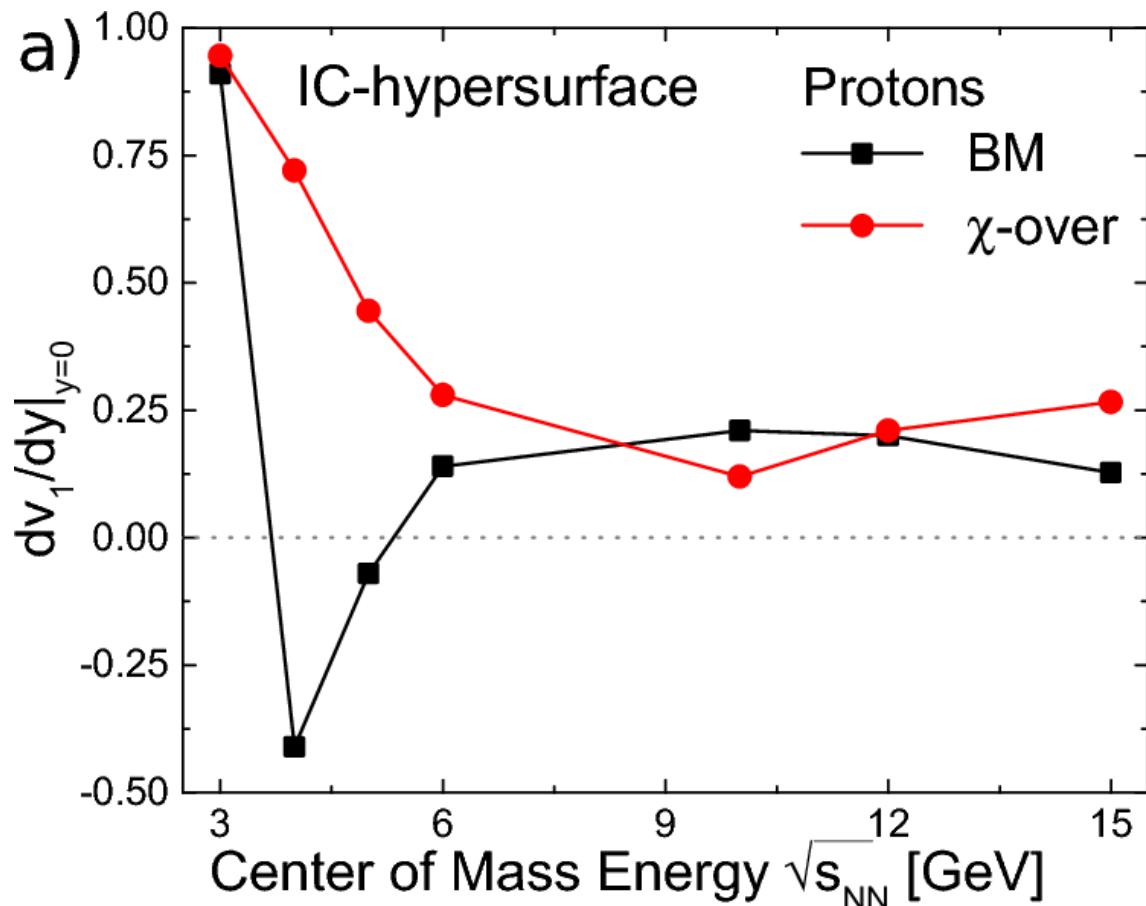
# A minimum in the excitation function of the directed flow

$$v_1 = \left\langle \frac{p_x}{p_T} \right\rangle$$

D.H.Rischke, et.al Heavy Ion Phys.1, 309(1995)

The effect of the softening of the EoS

J.Steinheimer,et.al.Phys.Rev.C89(2014)

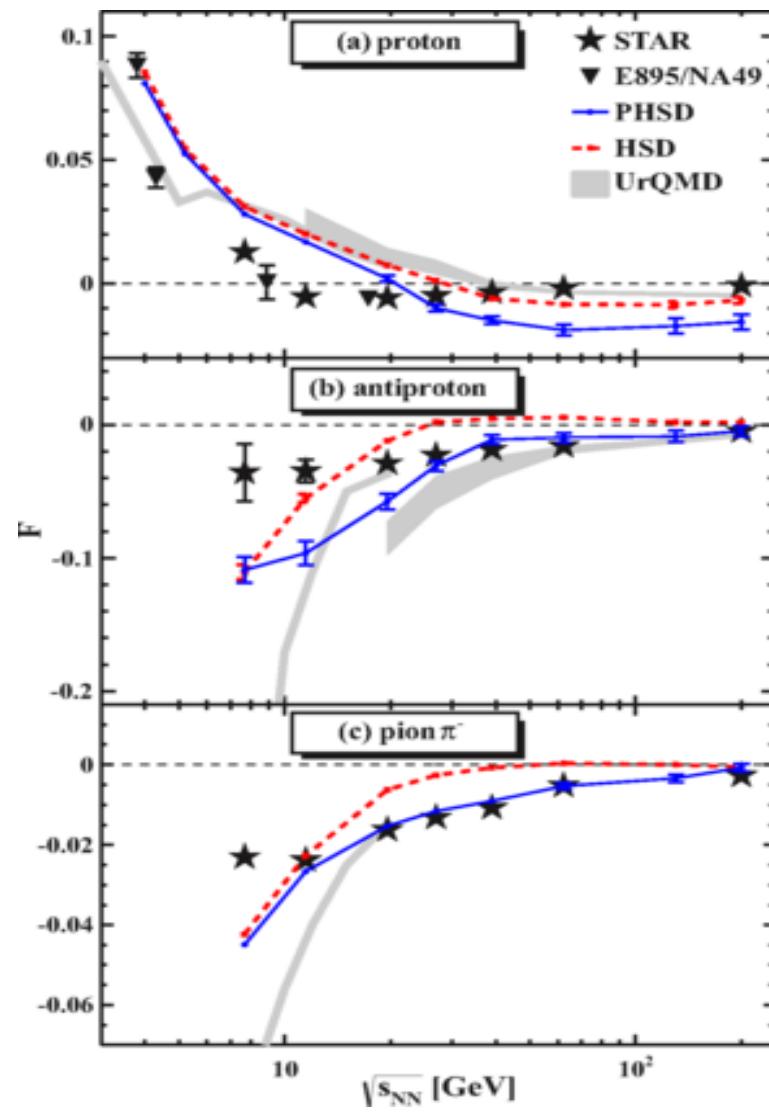
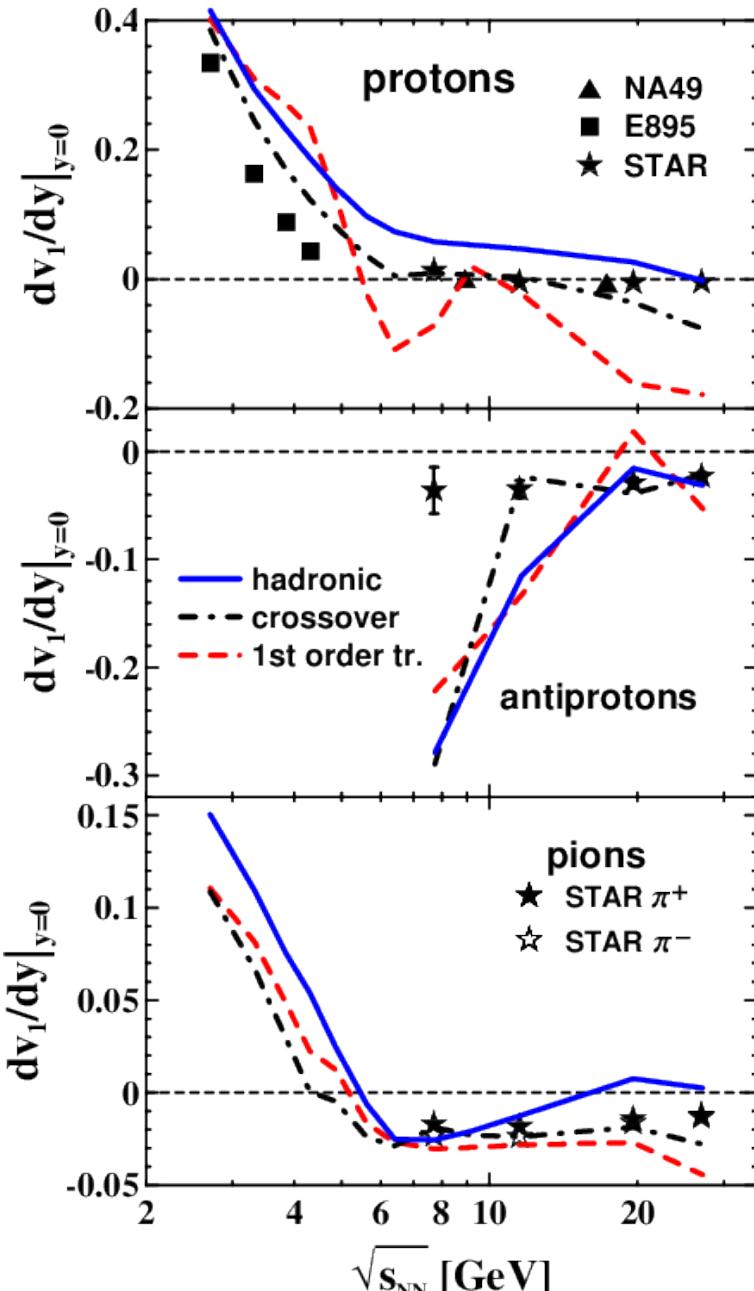


Minimum in the excitation function of  $v_1$  is seen only in first-order phase transition in one fluid simulation.

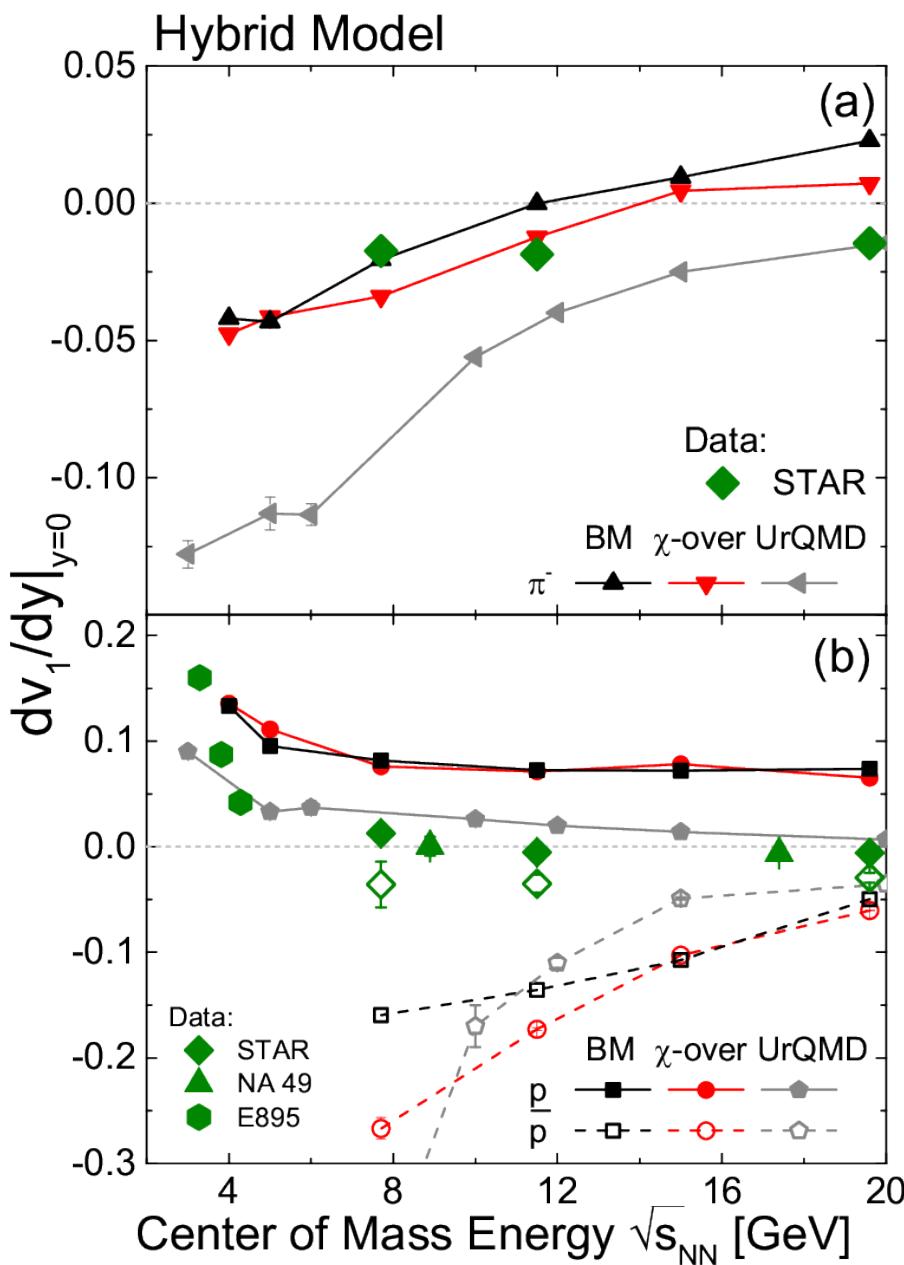
# V1 from hydrodynamics and PHSD

Y. B. Ivanov, A.A.Soldatov,  
 Phys. Rev. C91, no. 2, 024915 (2015)

V. P. Konchakovski, W. Cassing, Y. B. Ivanov and V. D. Toneev,  
 Phys. Rev. C90, no. 1, 014903 (2014)

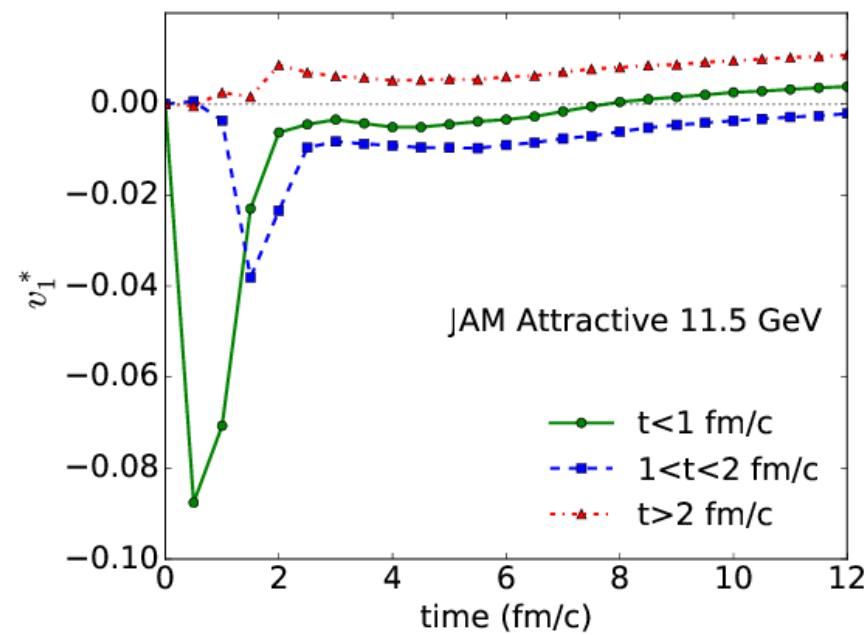


# UrQMD + hydro predictions

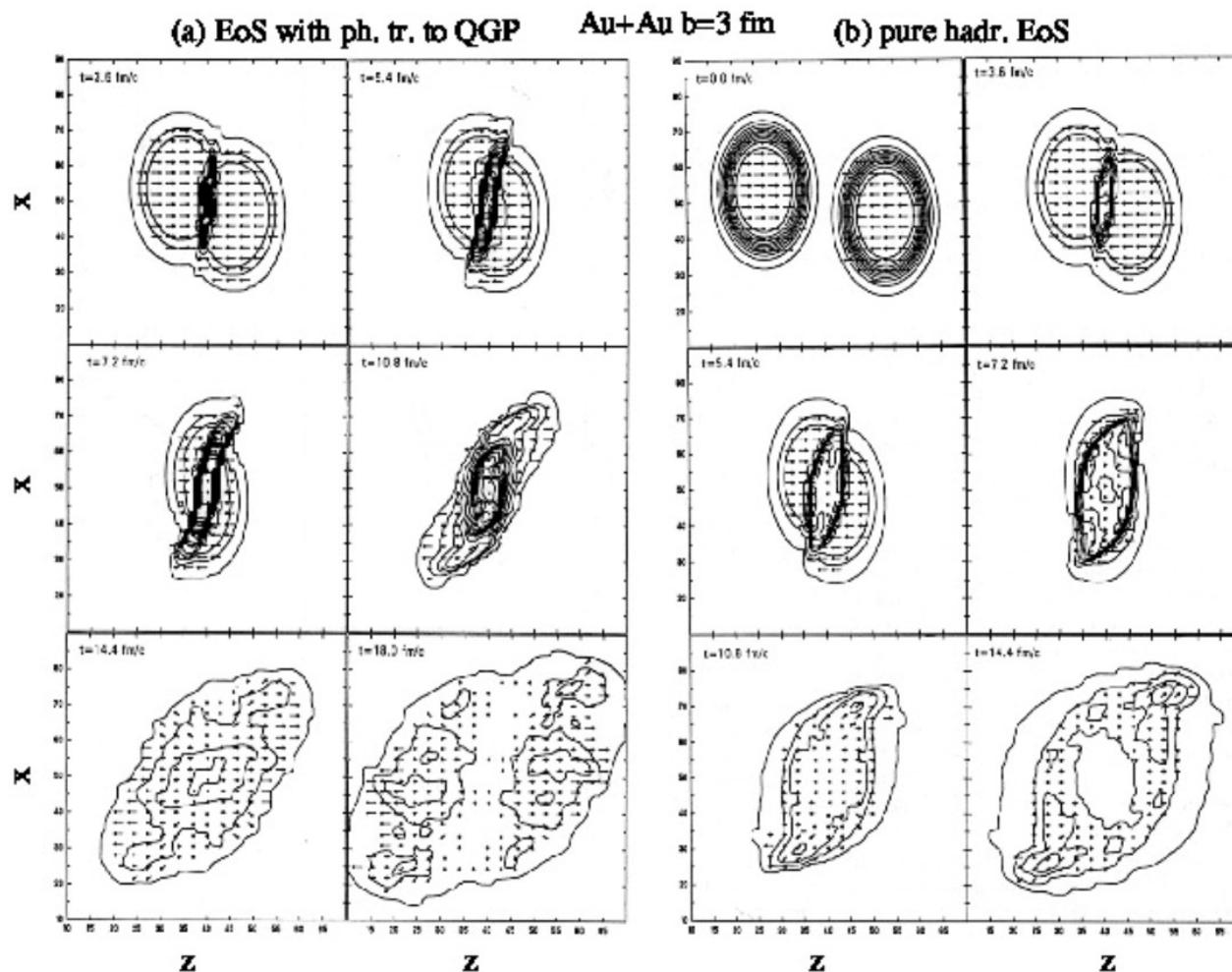


J. Steinheimer, et.al. Phys. Rev. C89(2014)

No minimum! Switching time too late?  
JAM+soft EoS supports this conjecture.



# QGP signal: formation of tilted ellipsoid



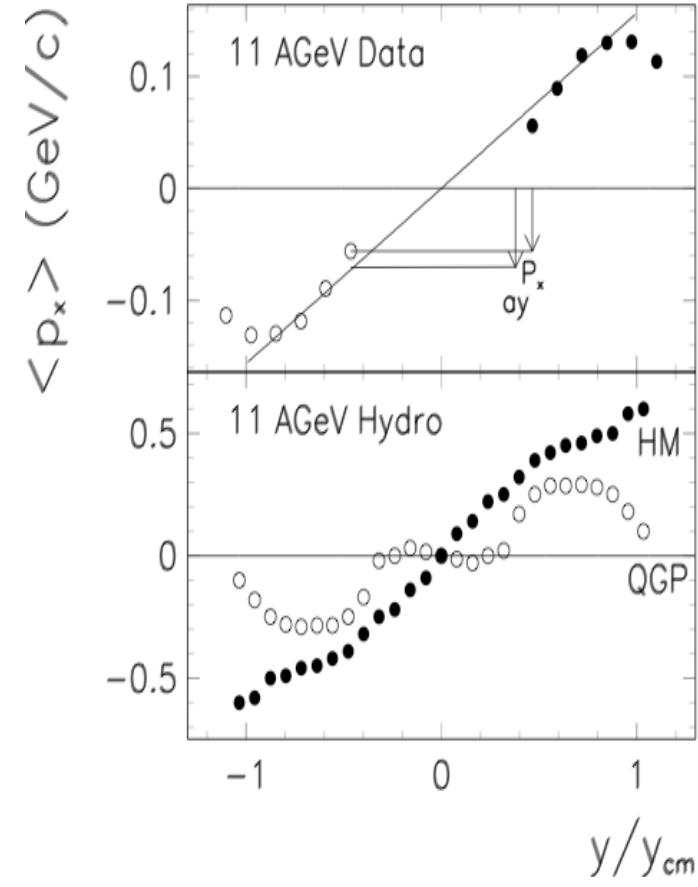
**Fig. 5**

D.H.Rischke, Y.Pursun,J.A.Maruhn,H.Stoecker,W.Greiner,  
Heavy Ion Phys. 1, 309 (1995)

QGP EoS predicts wiggle in hydro

# Wiggle: QGP signal in the directed flow?

Au+Au

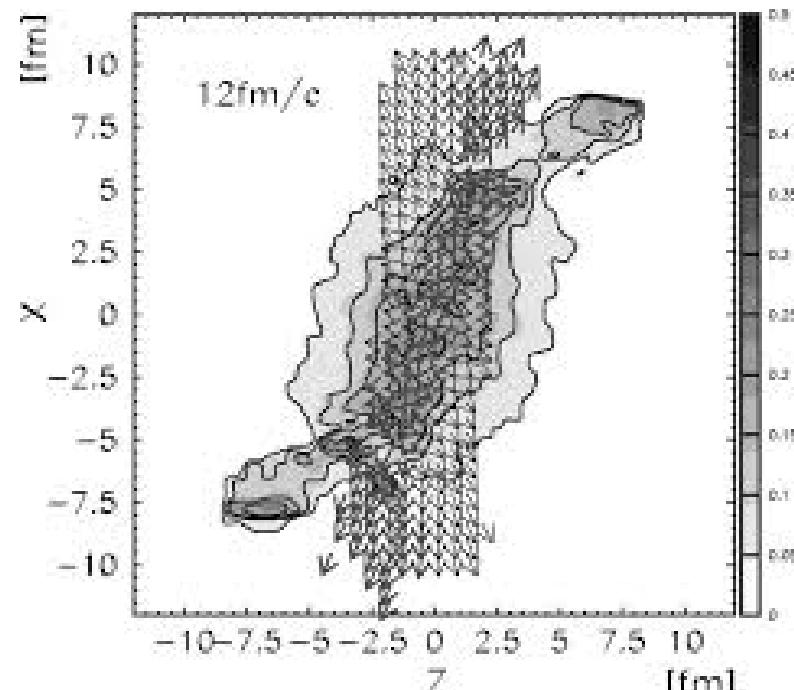


L. P. Csernai, D. Röhricht, PLB 45 (1999), 454.

QGP EoS predicts wiggle in hydro

J.Brachmann,et.al. Phys.Rev.C61 (2000)

Net baryon density in Au+Au at  $E_{\text{lab}}=8\text{GeV}$   $b=3$

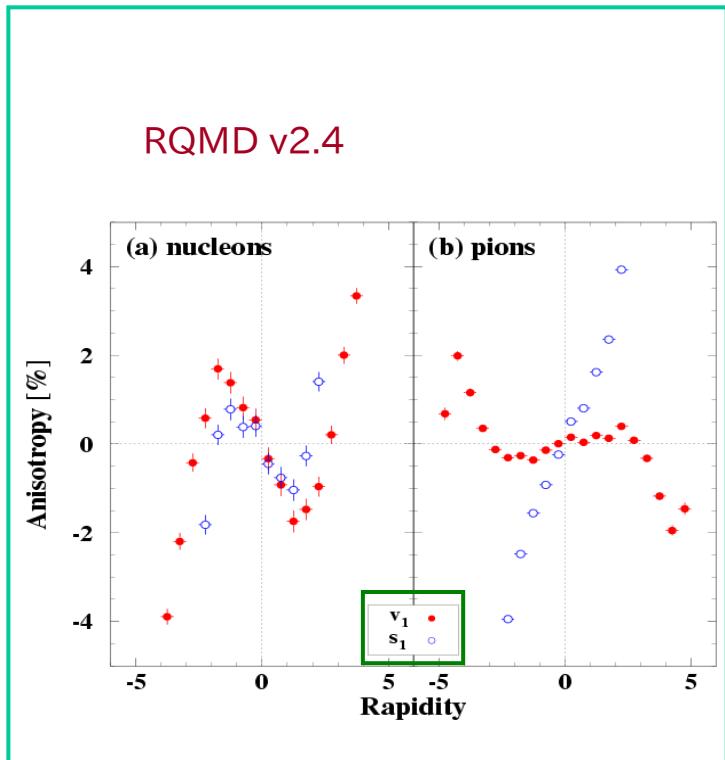


$$p_x \sim \int p A_\perp dt$$

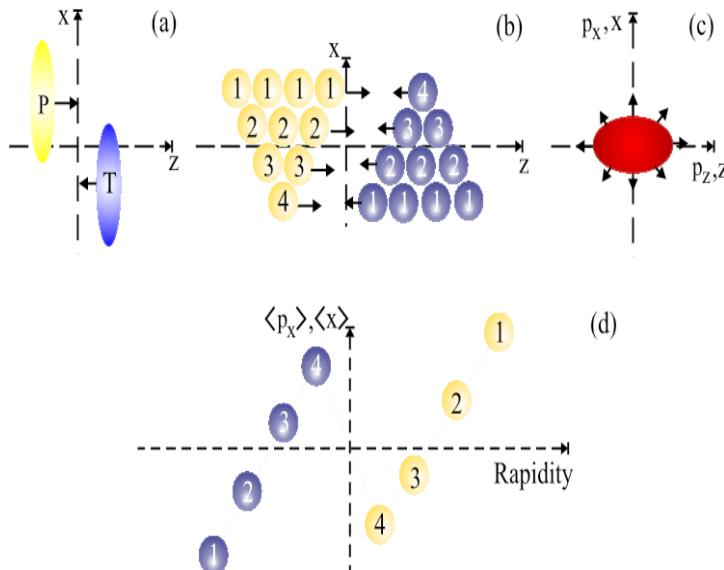
Baryon stopping + Positive space-momentum correlation leads wiggle ( no QGP)

R.Snellings, H.Sorge, S.Voloshin, F.Wang, N. Xu, PRL (84) 2803(2000)

# Wiggle: QGP signal in the directed flow?



Baryon stopping + Positive space-momentum correlation leads wiggle ( no QGP)

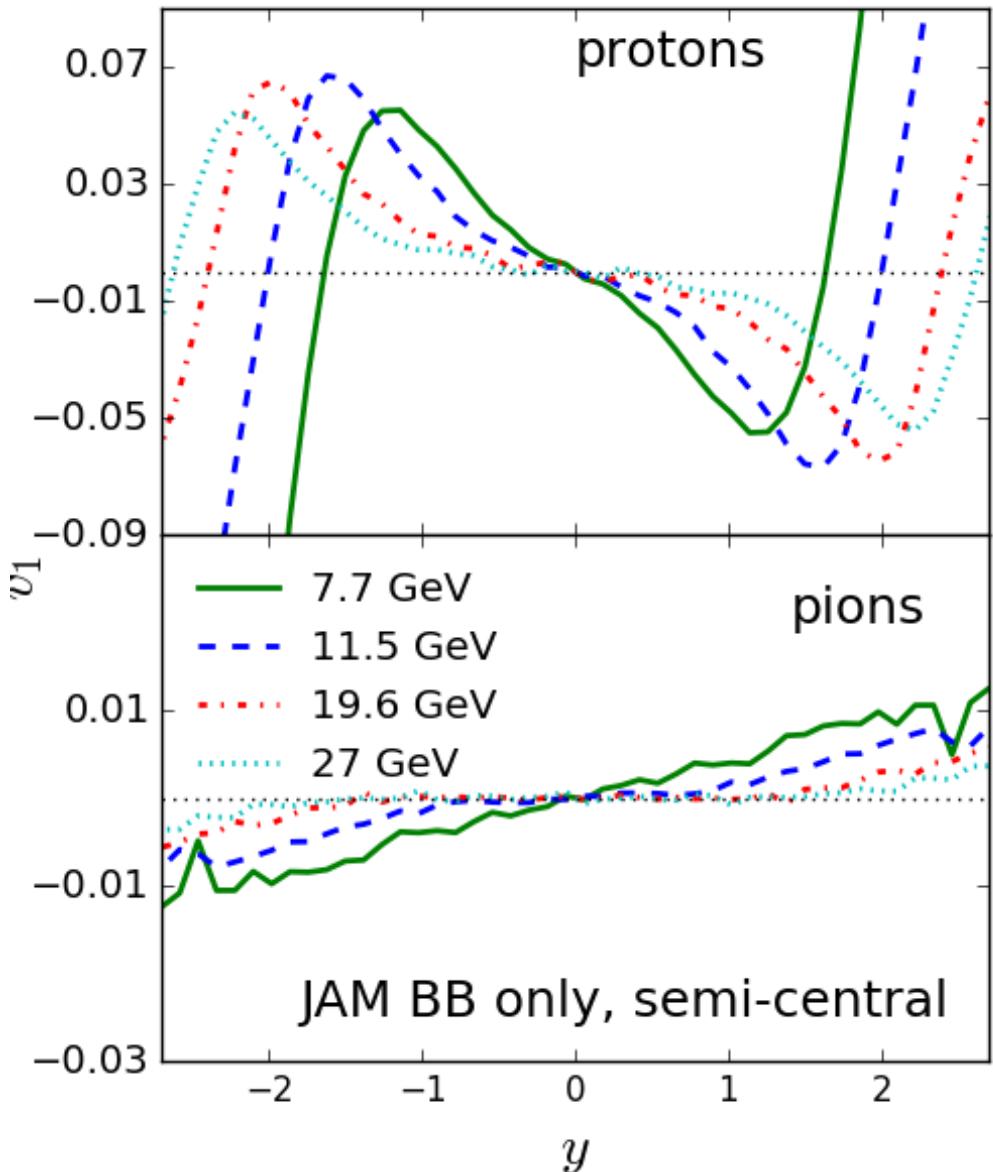


R.Snellings, H.Sorge, S.Voloshin, F.Wang, N. Xu, PRL (84) 2803(2000)

L. P. Csernai, D. Röhricht, PLB 45 (1999), 454.

This picture is only applicable at  $E_{cm} > 30$  GeV

# Proton v1 is negative without meson-baryon interactions in transport model



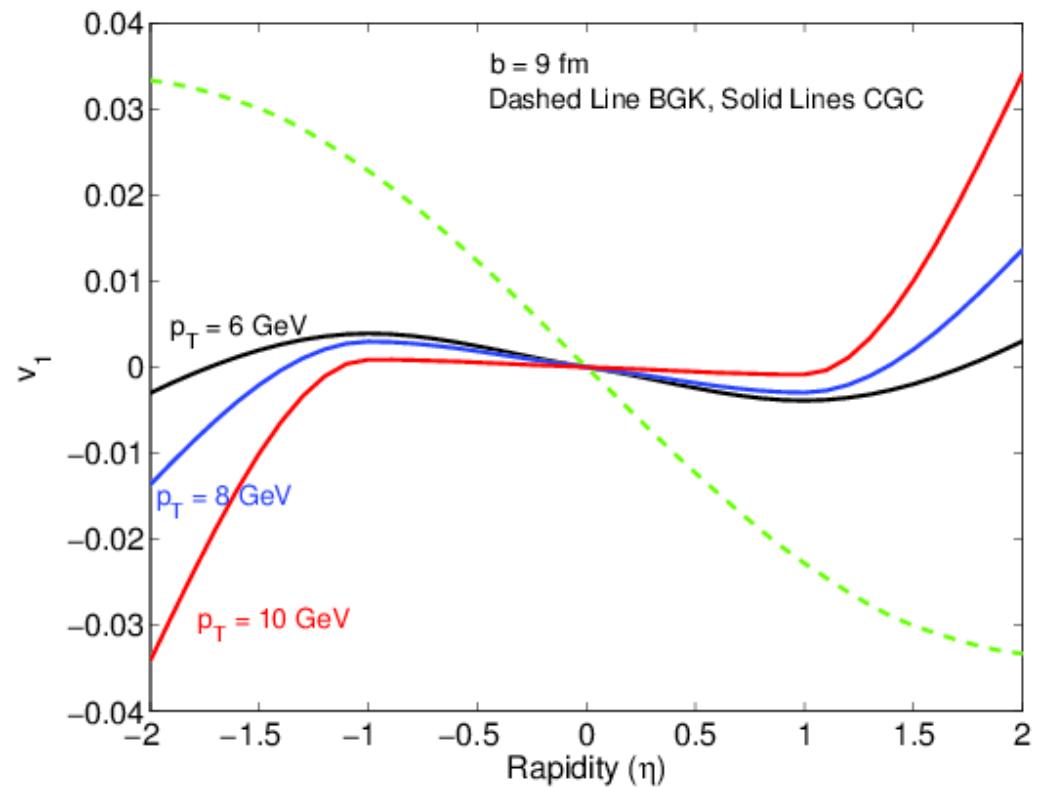
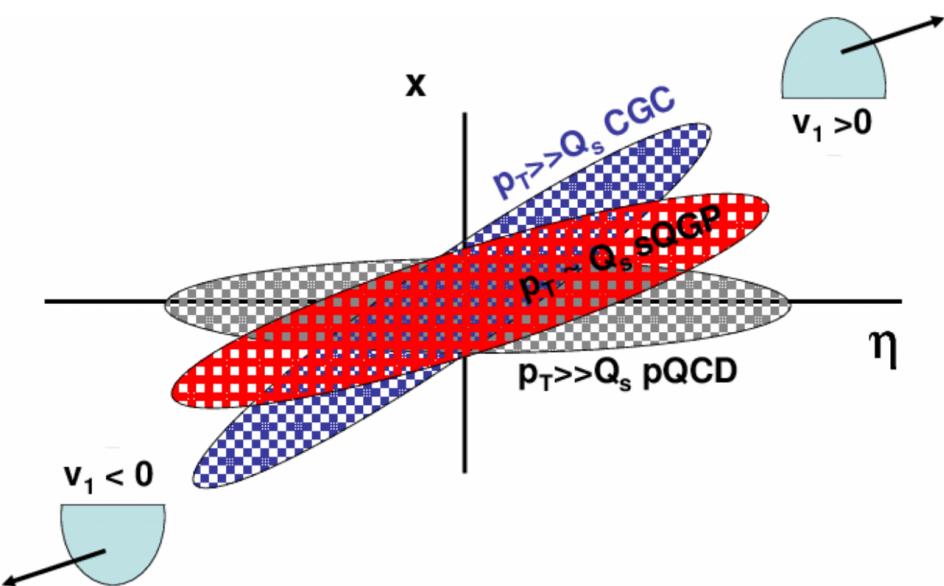
Note that initial Galuber collision only  
cannot reproduce space-momentum  
correlation.

Meson-baryon scattering →

Proton  $v_1$  becomes positive,  
pion  $v_1$  becomes negative.

# Twisted initial condition from CGC

A. Adil, M. Gyulassy, T.Hirano, Phys. Rev. D73, 054902(2006)



# JAM microscopic transport model

- Follow space-time propagation of particles based on cascade method
- Resonance and string excitation and decays
- Rescattering among all hadrons

RQMD based on Constraint Hamiltonian Dynamics

Sorge, Stoecker, Greiner, Ann. Phys. 192 (1989), 266.

RQMD/S: Tomoyuki Maruyama, et al. Prog. Theor. Phys. 96(1996), 263.

Single particle energy:

$$p_i^0 = \sqrt{\mathbf{p}_i^2 + m_i^2 + 2m_i V_i}$$

$$\dot{\mathbf{r}}_i = \frac{\mathbf{p}_i}{p_i^0} + \sum_j \frac{m_j}{p_j^0} \frac{\partial V_j}{\partial \mathbf{p}_i} \quad \dot{\mathbf{p}}_i = - \sum_j \frac{m_j}{p_j^0} \frac{\partial V_j}{\partial \mathbf{r}_i}$$

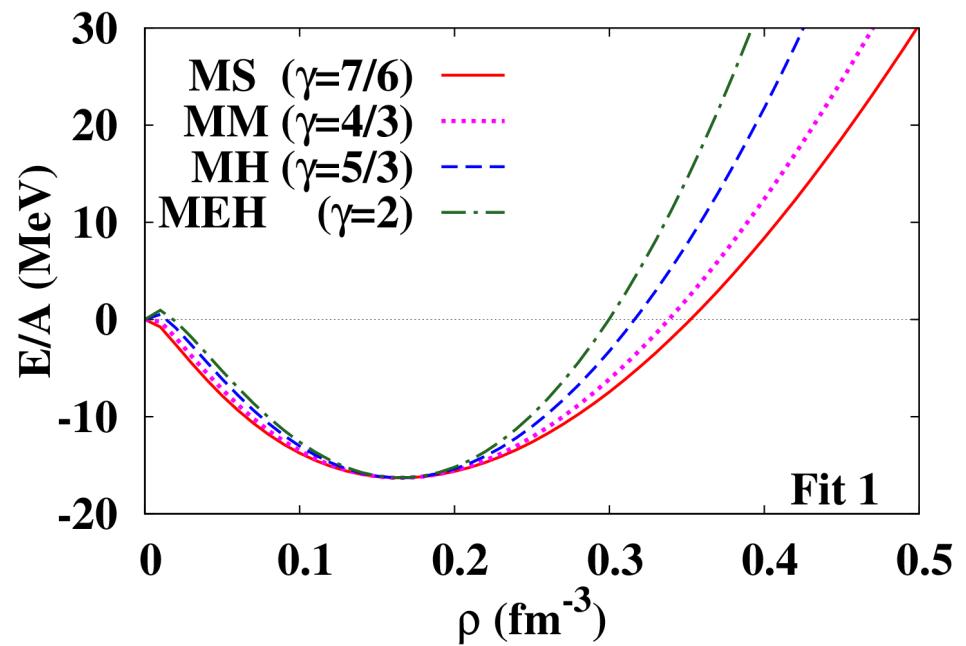
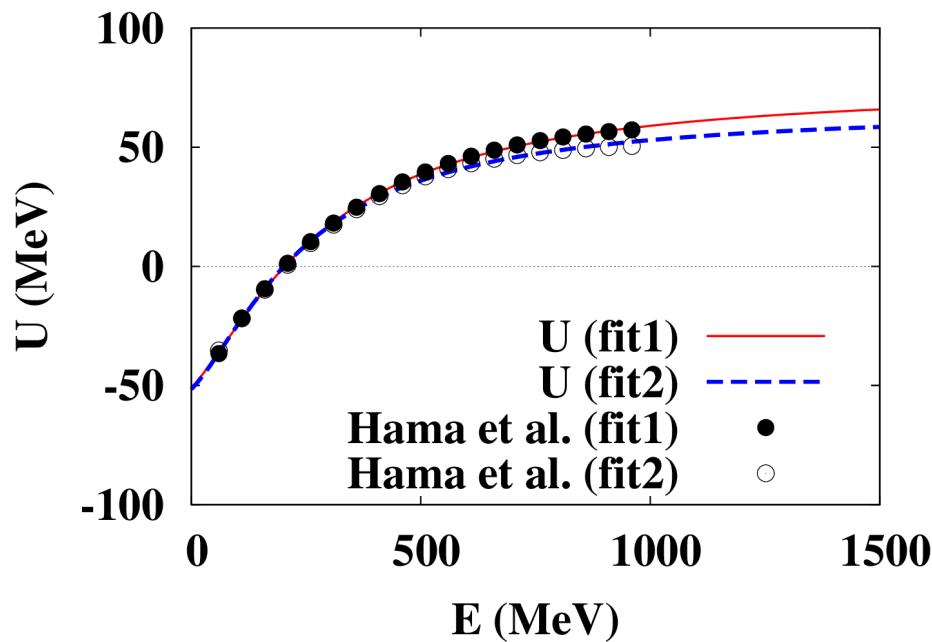
Arguments of potential  $\mathbf{r}_i - \mathbf{r}_j$  and  $\mathbf{p}_i - \mathbf{p}_j$  are replaced by the distances in the two-body c.m.

# Mean field potential

Skyrme type density dependent + Lorentzian momentum dependent potential

$$V = \sum_i V_i = \int d^3r \left[ \frac{\alpha}{2} \left( \frac{\rho}{\rho_0} \right)^2 + \frac{\beta}{\gamma+1} \left( \frac{\rho}{\rho_0} \right)^{\gamma+1} \right] + \sum_k \int d^3r d^3p d^3p' \frac{C_{ex}^{(k)}}{2\rho_0} \frac{f(\mathbf{r}, \mathbf{p}) f(\mathbf{r}, \mathbf{p}')}{1 + (\mathbf{p} - \mathbf{p}')^2 / \mu_k^2}$$

Type	$\alpha$ (MeV)	$\beta$ (MeV)	$\gamma$	$C_{ex}^{(1)}$ (MeV)	$C_{ex}^{(2)}$ (MeV)	$\mu_1$ (fm $^{-1}$ )	$\mu_2$ (fm $^{-1}$ )	$K$ (MeV)
MH1	-12.25	87.40	5/3	-383.14	337.41	2.02	1.0	371.92
MS1	-208.89	284.04	7/6	-383.14	337.41	2.02	1.0	272.6



# Pressure in the collision term

## Virial Theorem

$$P = P_{free} + \frac{1}{3TV} \sum_{(i,j)} [(\mathbf{p}'_i - \mathbf{p}_i) \cdot \mathbf{r}_i + (\mathbf{p}'_j - \mathbf{p}_j) \cdot \mathbf{r}_j]$$


$$P_{free} = \frac{1}{3TV} \int dt \sum_i \mathbf{p}_i \cdot \mathbf{v}_i$$

Contribution from two-body scattering

$$\text{Momentum conservation } \mathbf{p}'_i + \mathbf{p}'_j = \mathbf{p}_i + \mathbf{p}_j$$

Repulsive orbit  $(\mathbf{p}'_i - \mathbf{p}_i) \cdot (\mathbf{r}_i - \mathbf{r}_j) > 0$  enhances the pressure

Attractive orbit  $(\mathbf{p}'_i - \mathbf{p}_i) \cdot (\mathbf{r}_i - \mathbf{r}_j) < 0$  reduces the pressure

Impose attractive orbit in the collision  $\rightarrow$  softening of EoS

# EOS modified collision term

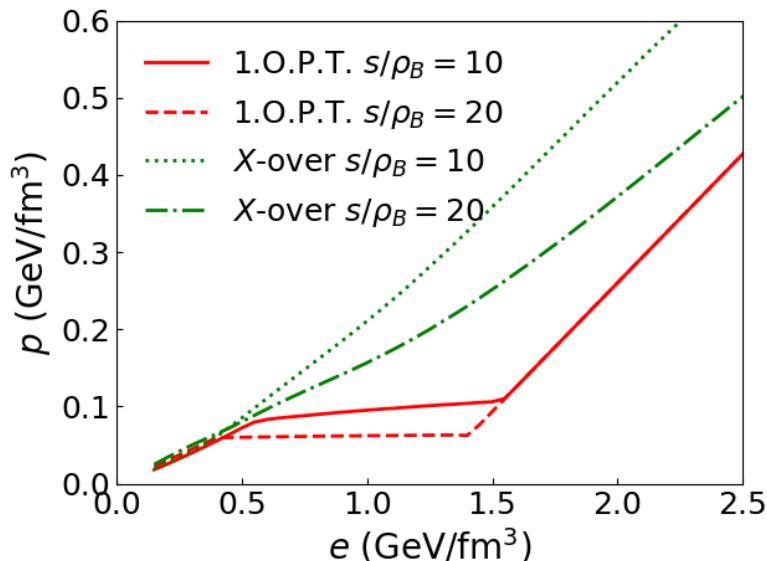
H. Sorge, Phys. Rev.Lett. 82,2048 (1999)

$$P = P_{free} + \frac{1}{3TV} \sum_{(i,j)} [(\mathbf{p}'_i - \mathbf{p}_i) \cdot \mathbf{r}_i + (\mathbf{p}'_j - \mathbf{p}_j) \cdot \mathbf{r}_j]$$

The momentum change is constrained by

$$(\mathbf{p}'_i - \mathbf{p}_i) \cdot (\mathbf{r}_i - \mathbf{r}_j) = 3 \frac{(P - P_{free})}{\rho} (\Delta t_i + \Delta t_j)$$

When  $P < P_{free}$ : attractive orbit in the collision.



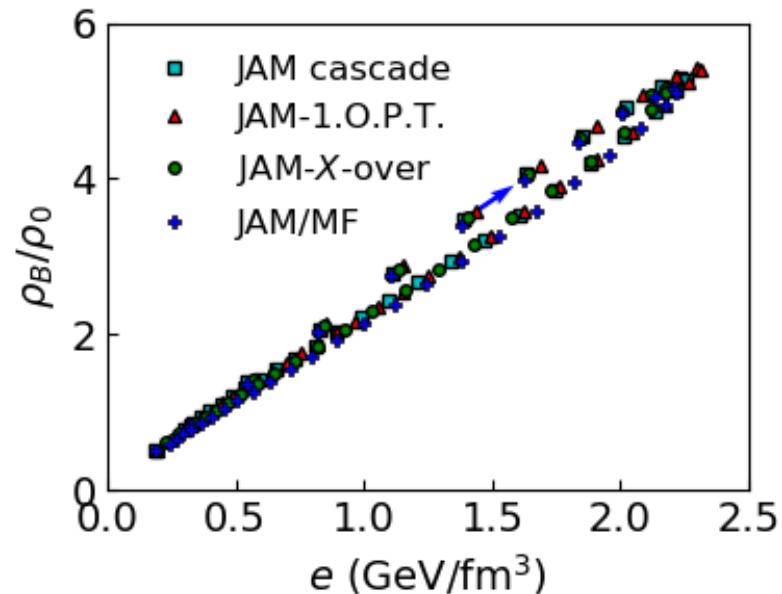
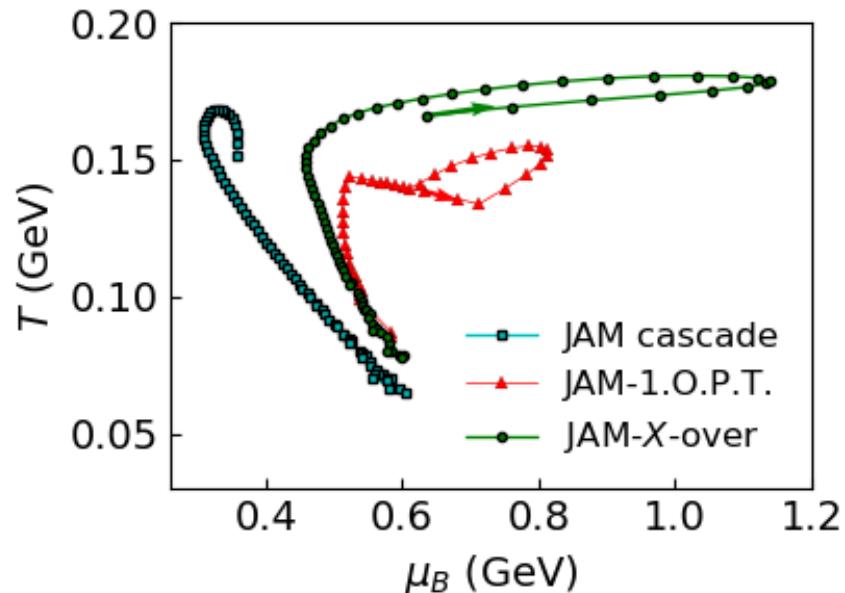
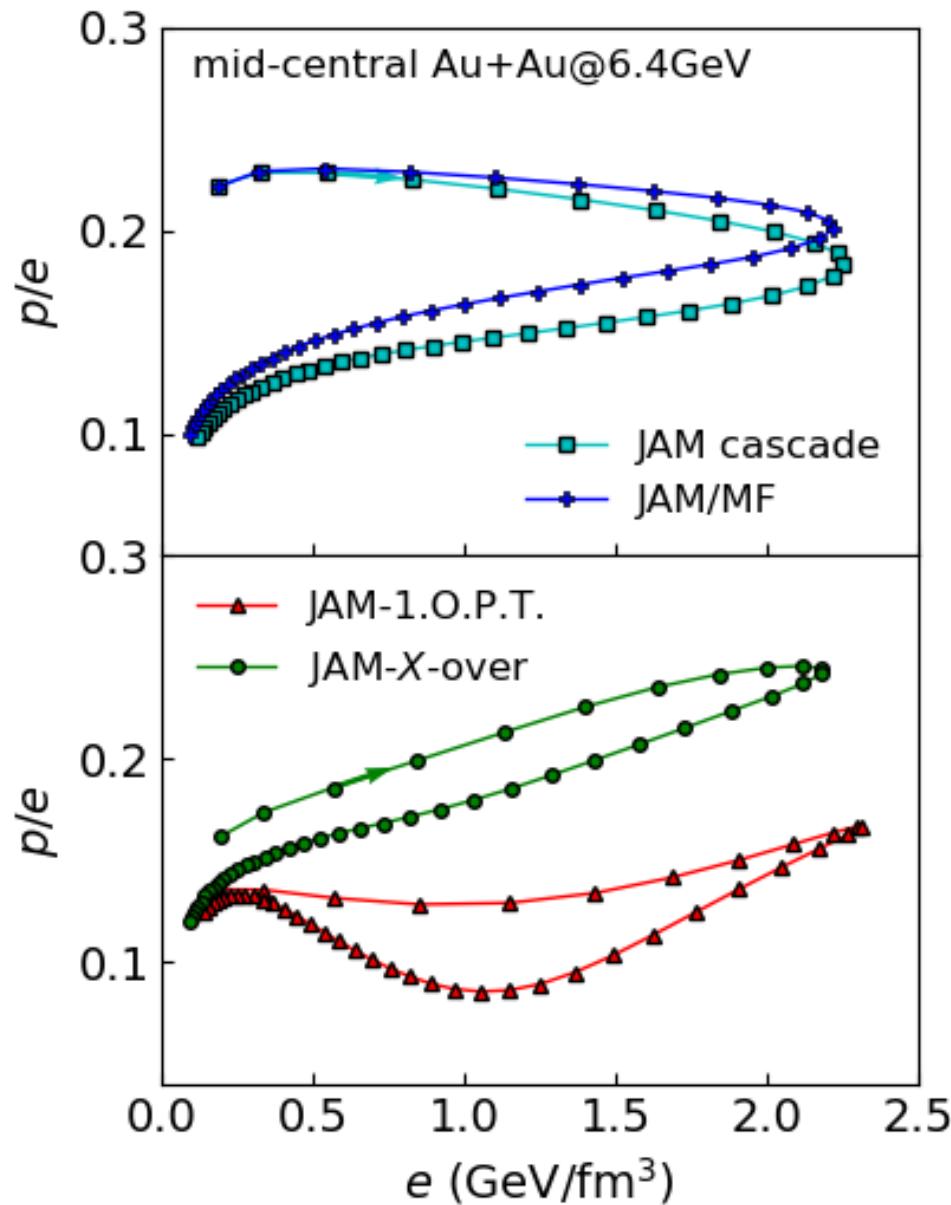
Fully baryon density dependent EoSs are implemented.

Cross-over EOS: J. Steinheimer

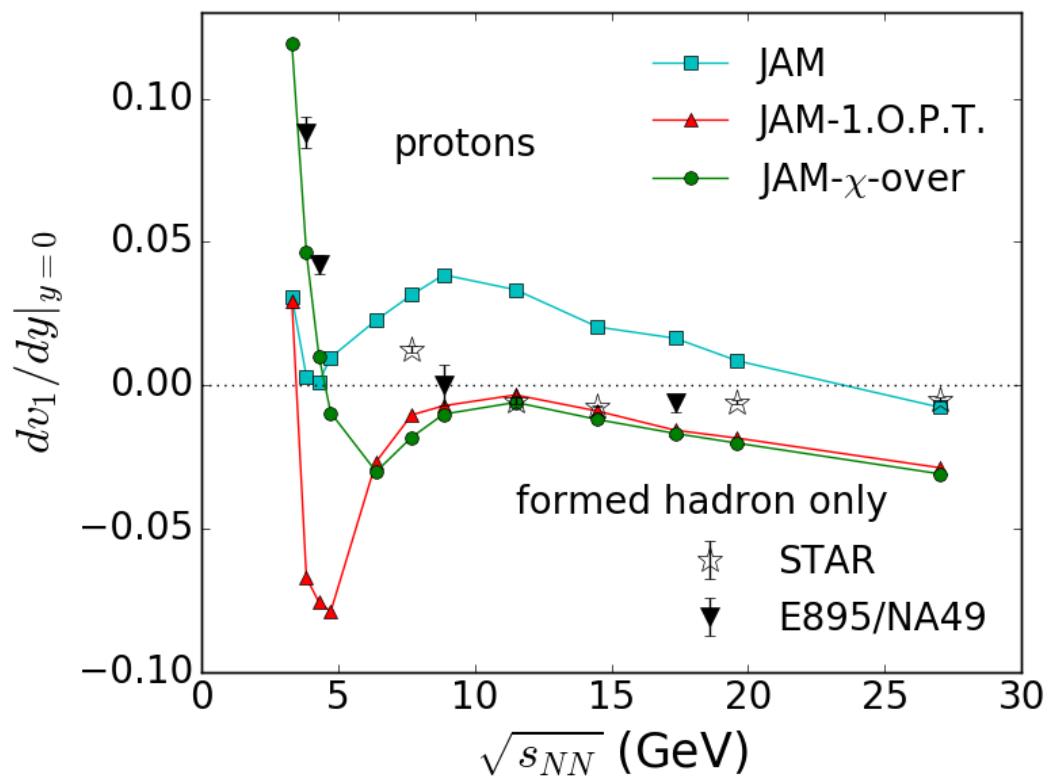
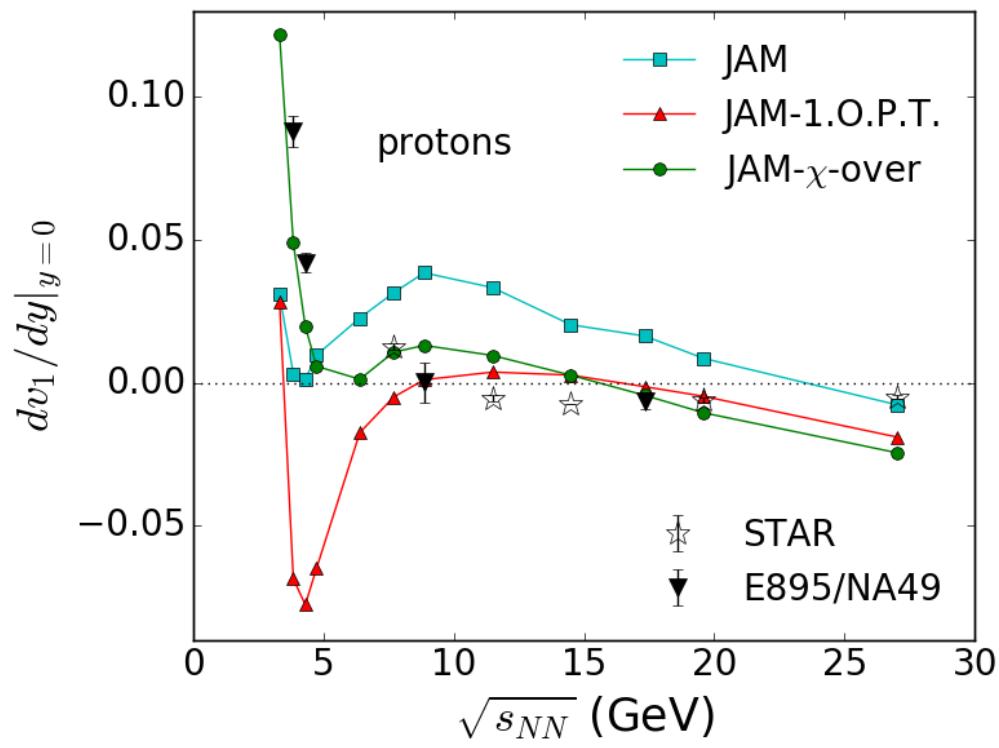
EOS-Q: Kolb, Sollfrank, Heinz

- Any EoS can be incorporated
- CPU time is as fast as standard cascade simulation

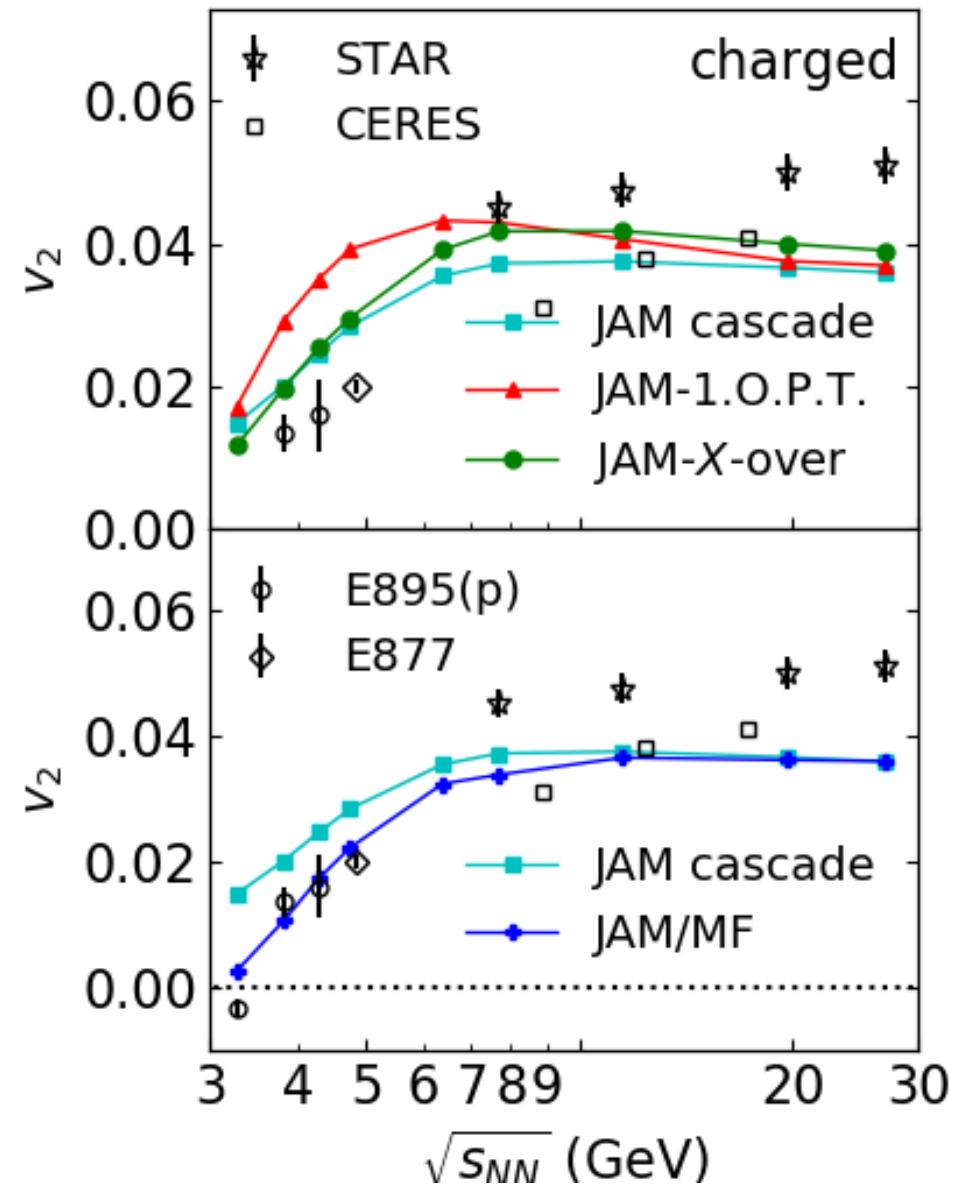
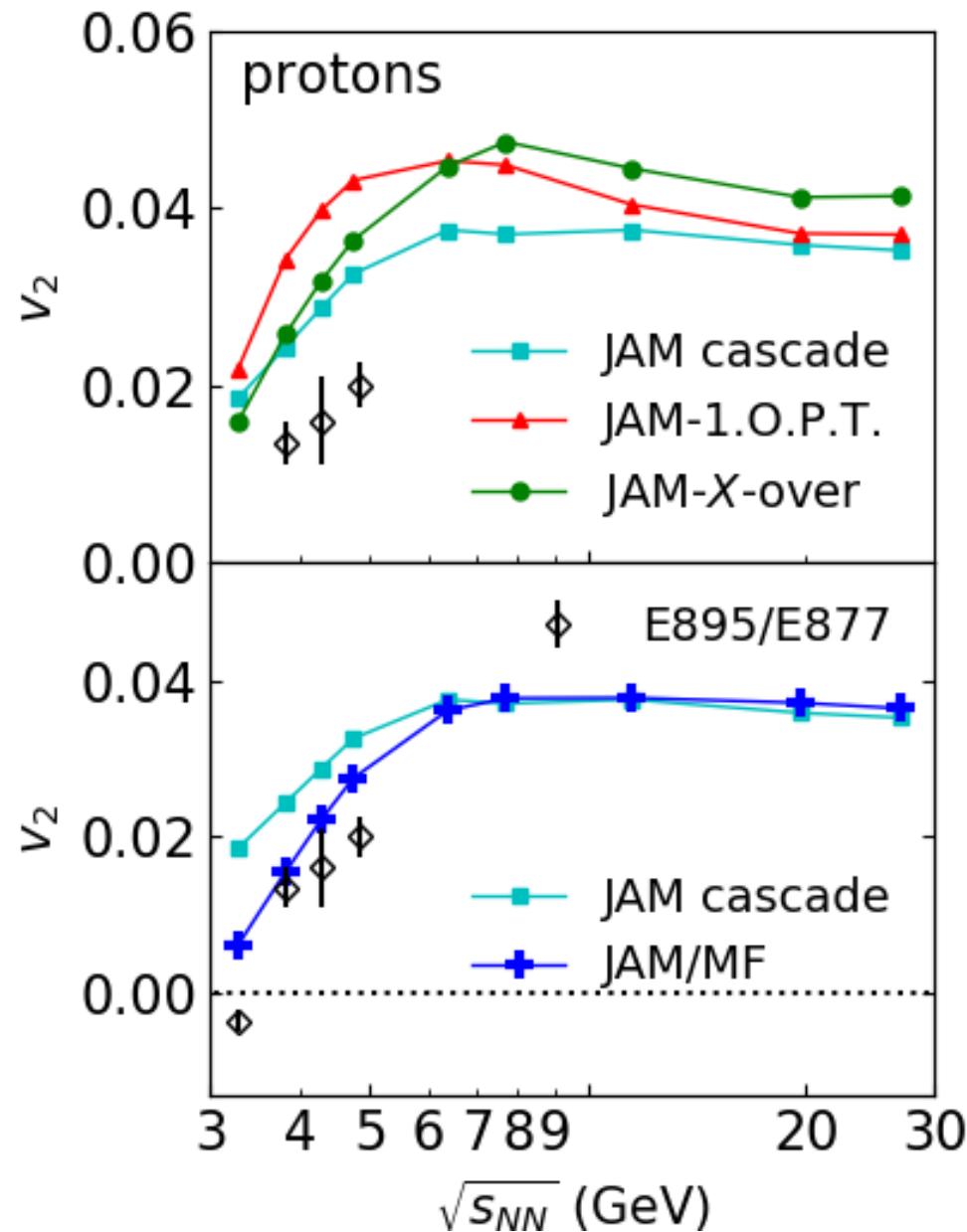
# EoS dependence at 6.4 GeV



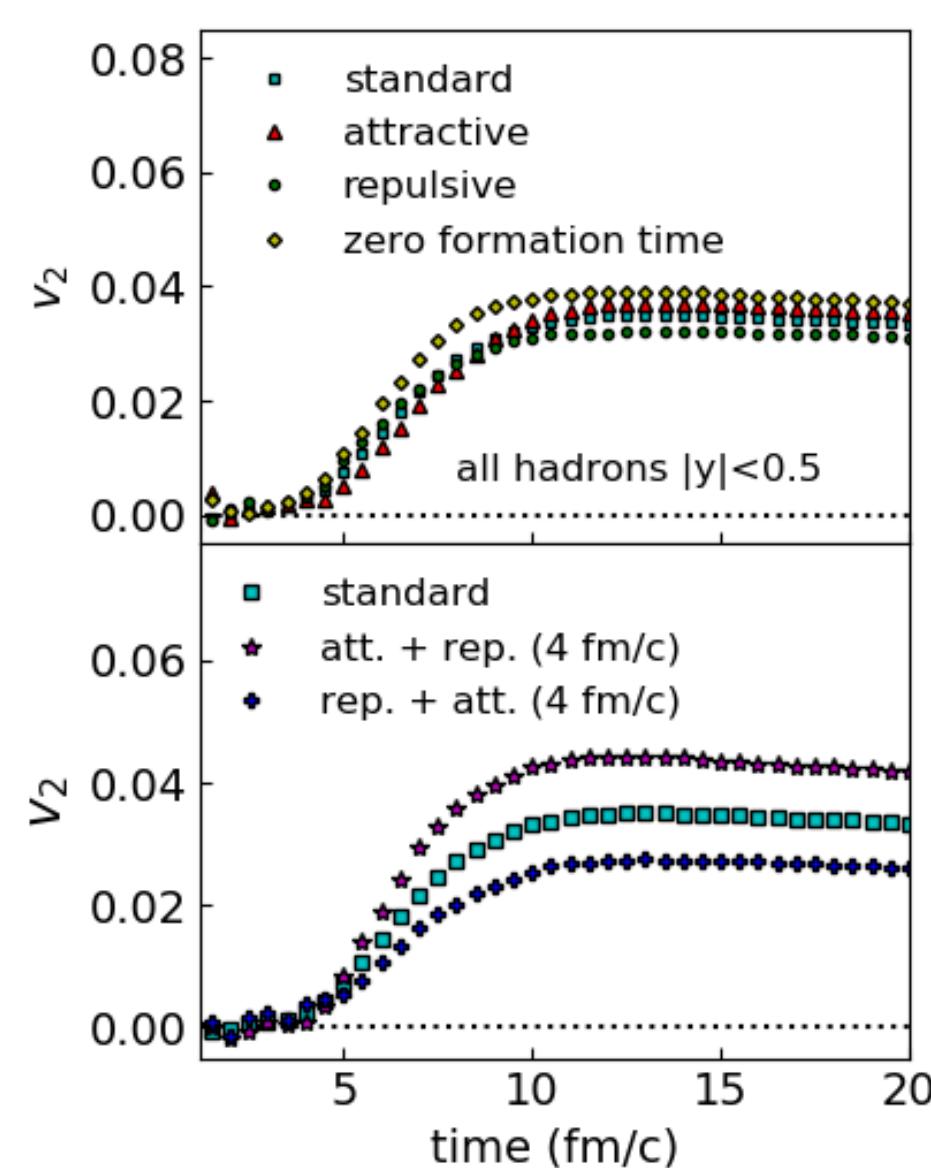
# V1 excitation functions



# V2 excitation functions



# Time evolution of v<sub>2</sub>



## Squeeze-out

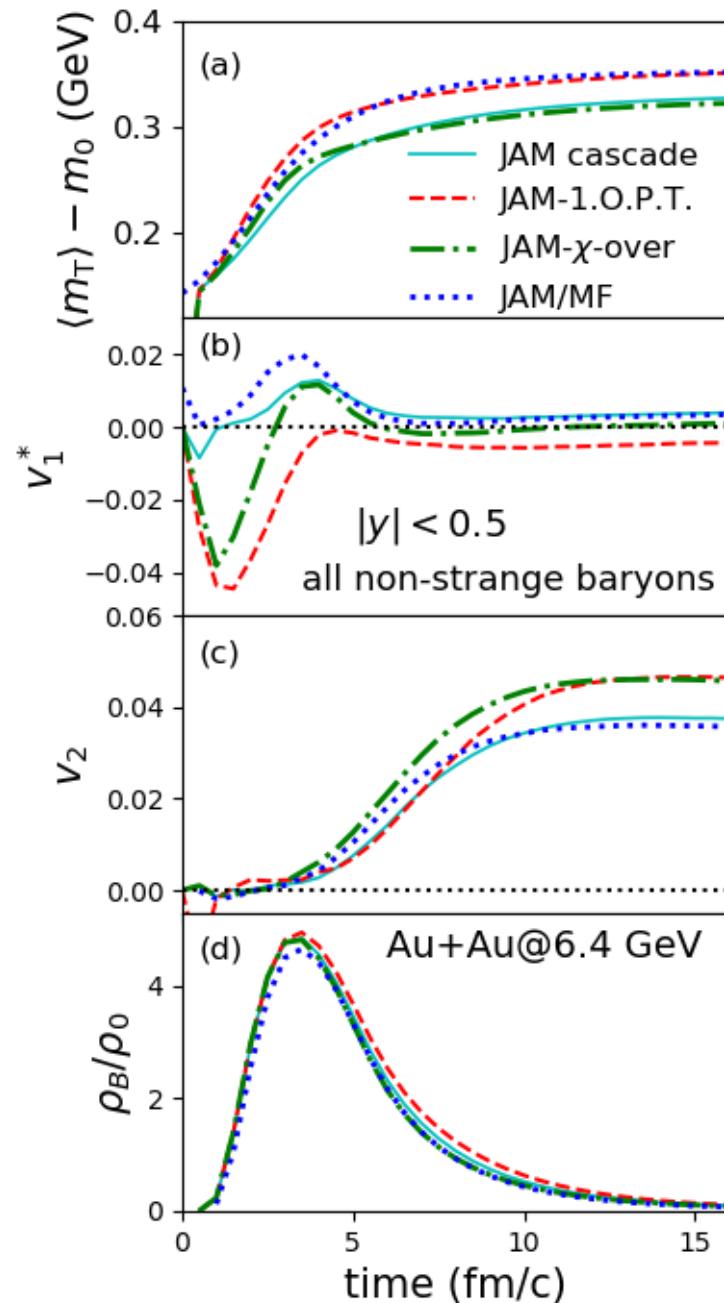
$t < t_{\text{pass}}$  :  $v_2$  is small for hard EoS

$t > t_{\text{pass}}$  :  $v_2$  is large for hard EoS

Att. + rep. (4fm/c) → attractive orbit before 4fm/c  
repulsive orbit after 4fm/c  
→ strong enhancement of  $v_2$

Rep. + att. (4fm/c) → repulsive orbit before 4fm/c  
attractive orbit after 4fm/c  
→ strong reduction of  $v_2$

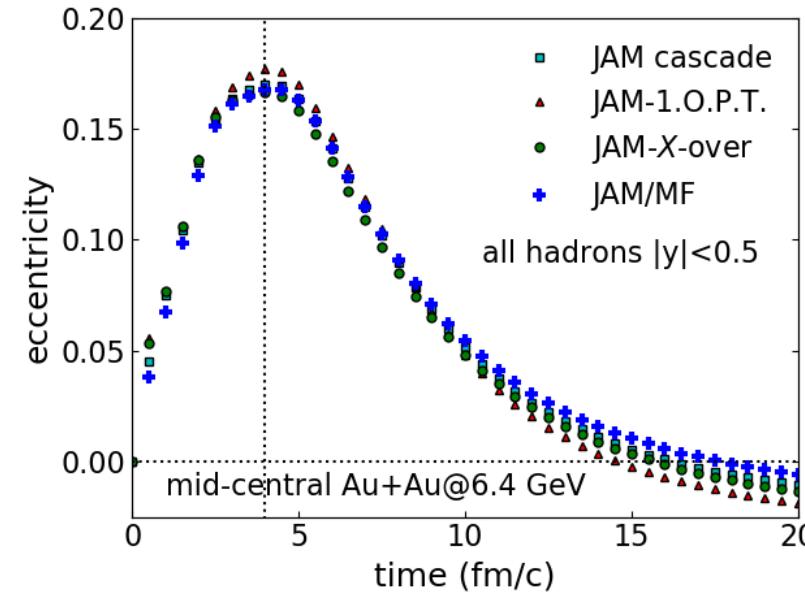
# Time evolution of v0, v1, v2



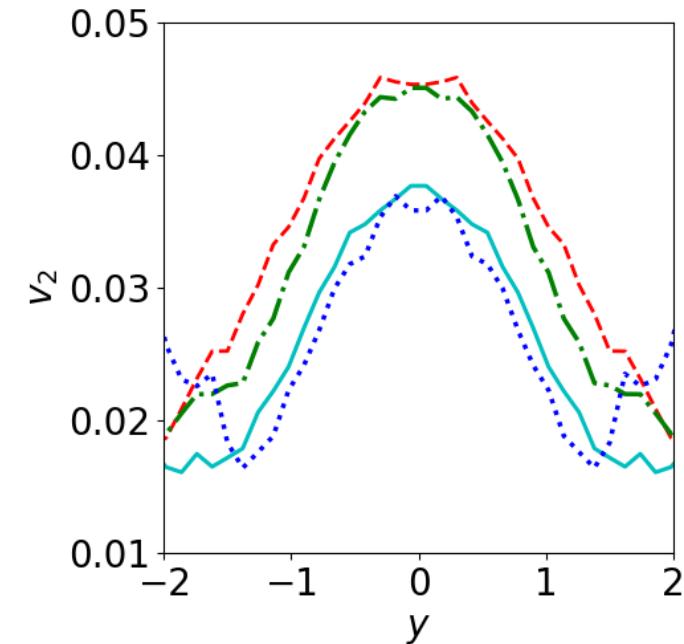
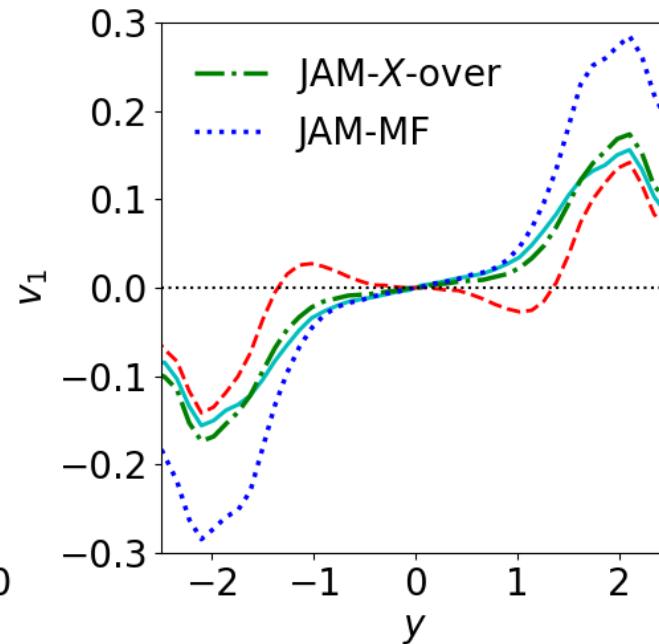
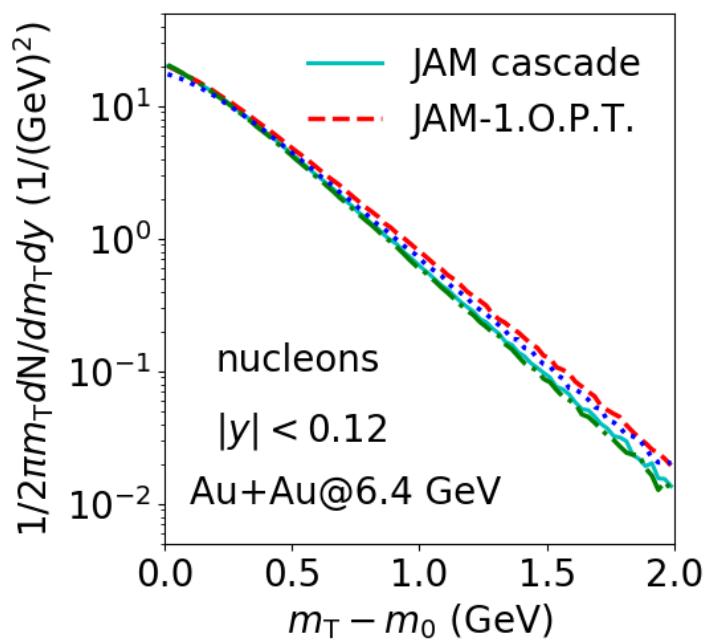
V0 is enhanced by both 1.O.P.T and mean-field

V1 is negative for 1.O.P.T.

V2 is enhanced by 1.O.P.T and crossover



# v0,v1, v2 at 6.4 GeV



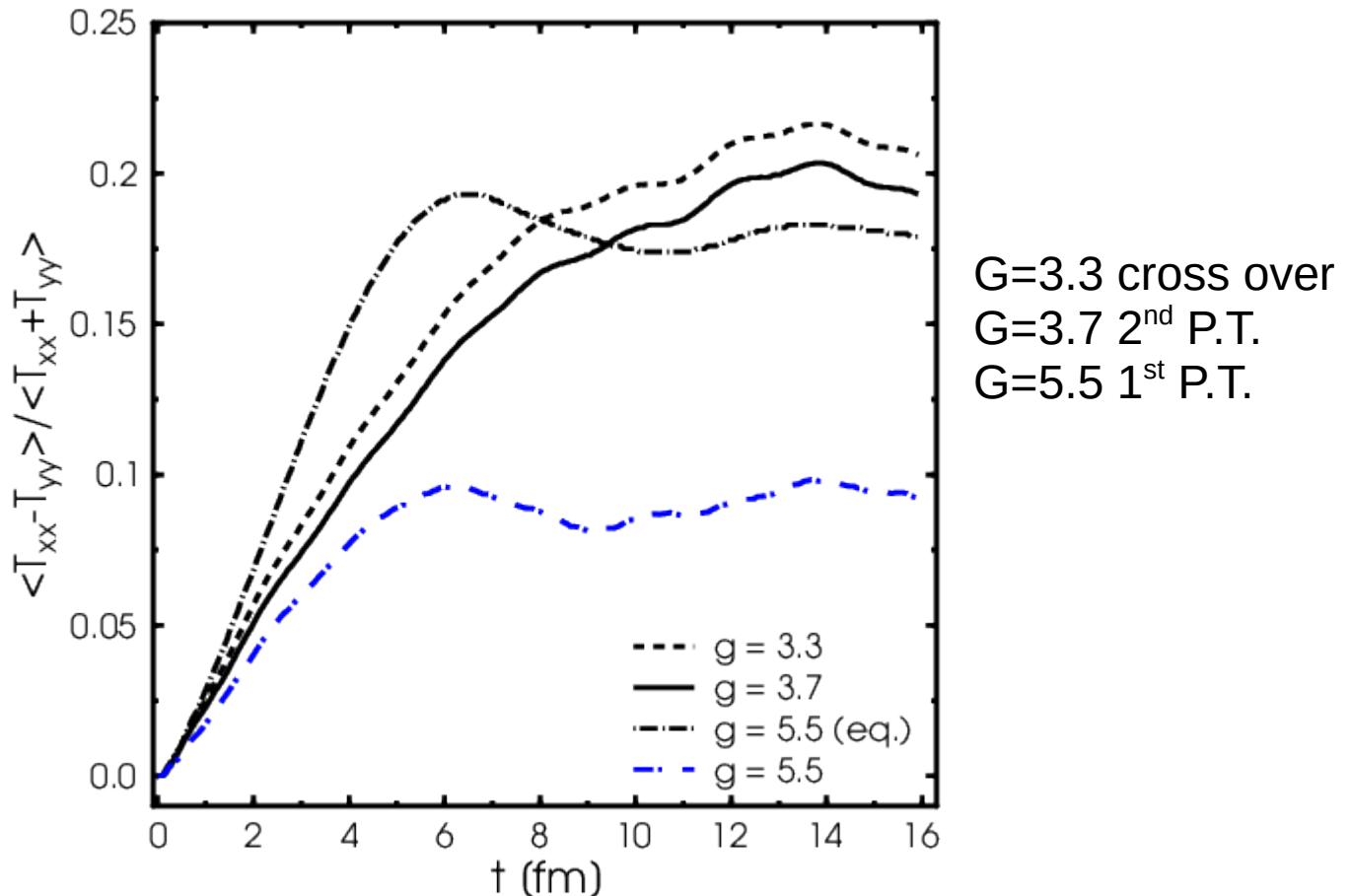
	Mt	v1	v2
Cascade			
Hadronic mean-field	enhanced	positive	reduced
First-order P.T.	enhanced	negative	enhanced
Crossover	same	positive	enhanced

analysis should be very useful.

# V2 is reduced by non.eq-1.O.P.T

K. Paech, H. Stoecker, A. Dumitru, PRC68 (2003)

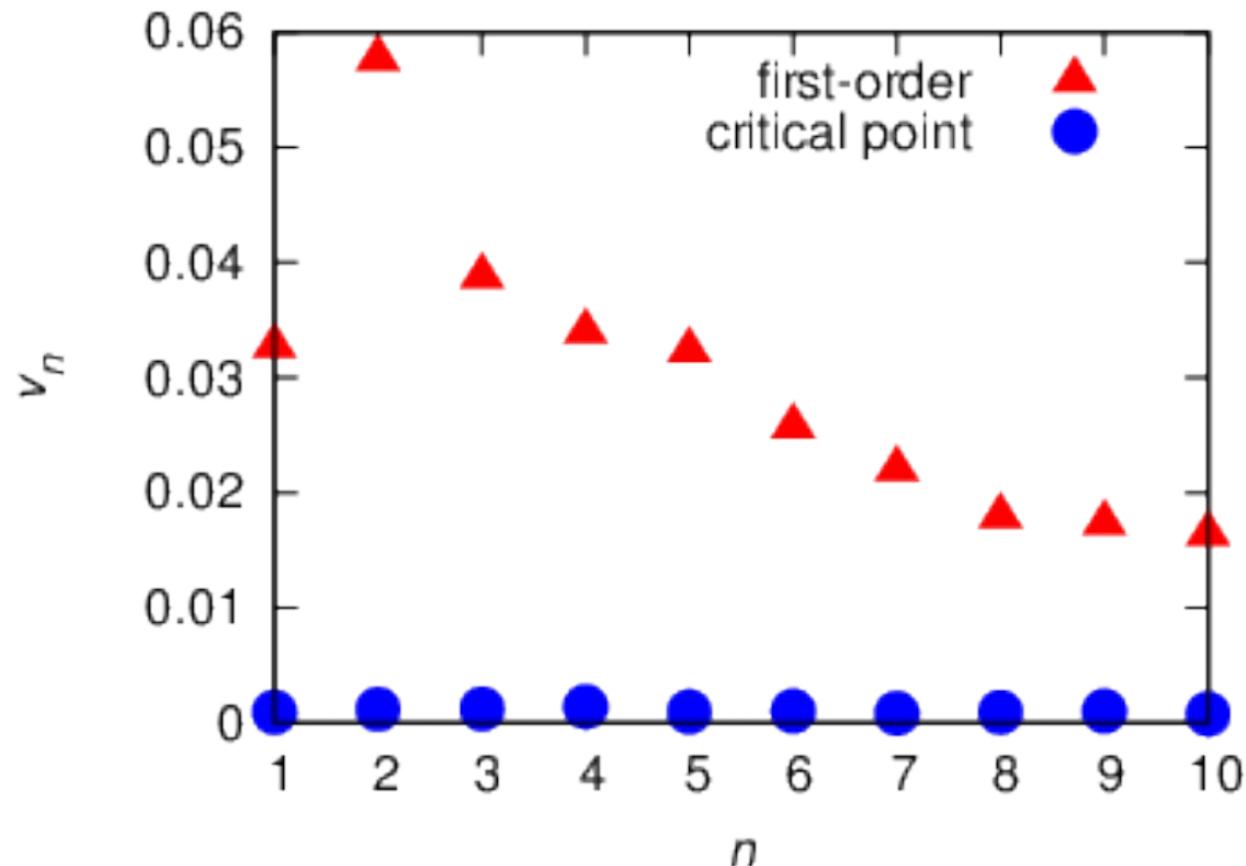
Hydro + linear sigma field simulation predicts the reduction of v2 by the non-equilibrium chiral dynamics



# V2 is enhanced by non.eq-1.O.P.T

C. Herold, M. Nahrgang, I. Mishustin, M. Bleicher, NPA925 (2014)

Hydro + linear sigma field simulation predicts the enhancement of  $v_n$  by the non-equilibrium chiral dynamics

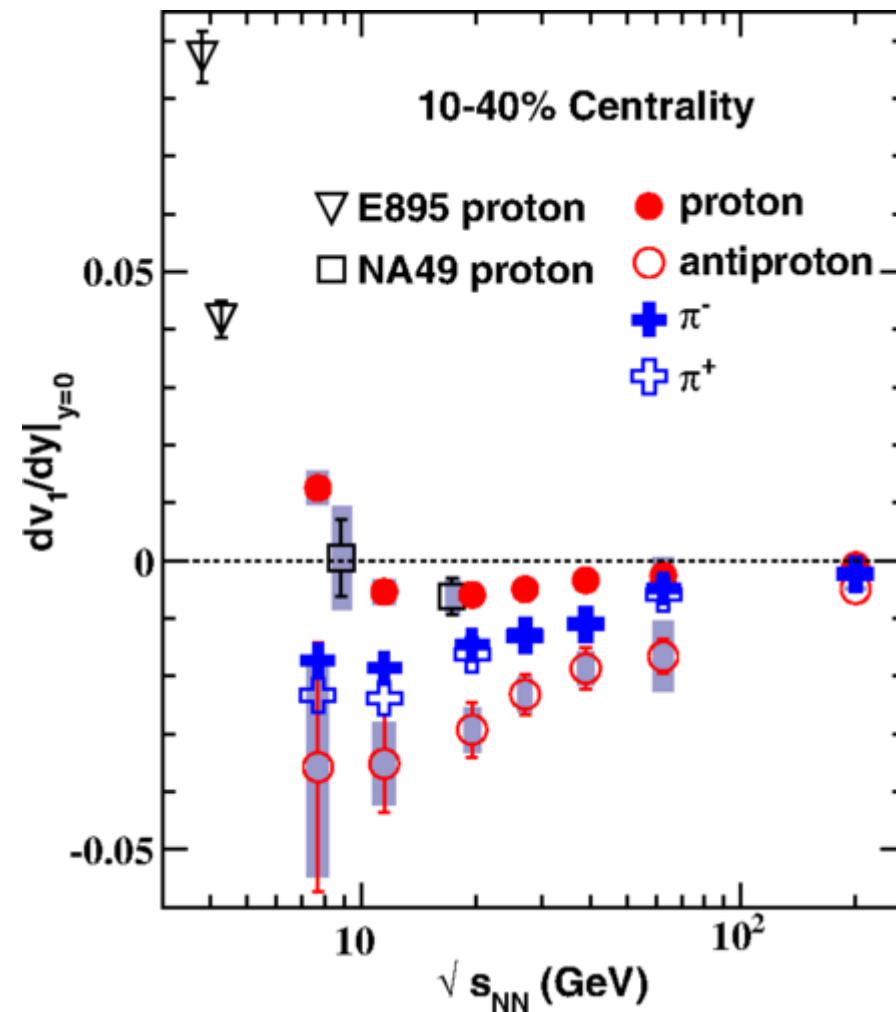
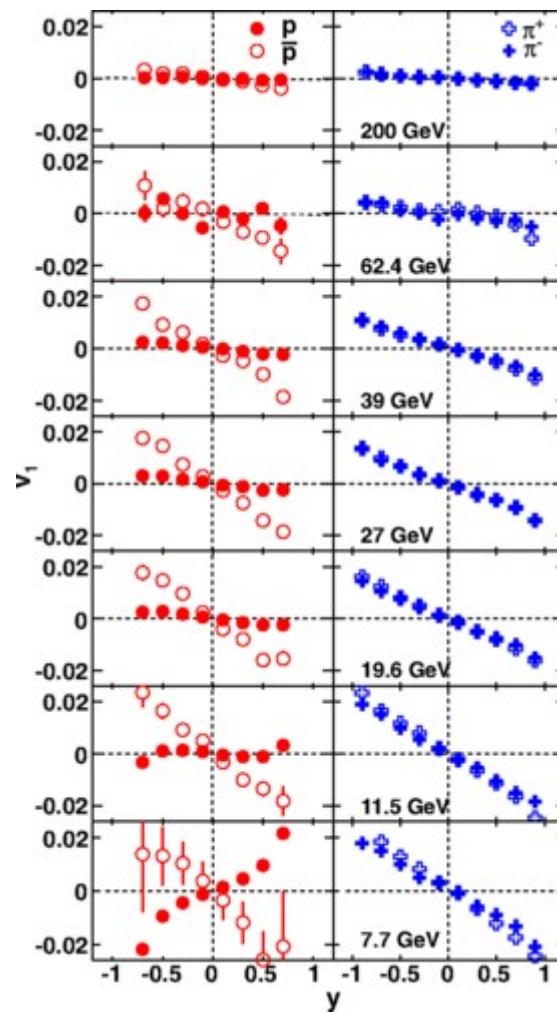


# summary

- We proposed a efficient method to incorporate the effect of EoS into the microscopic hadronic transport model JAM, and find a strong EoS dependence of collective flows.
  - This non-equilibrium approach predicts the similar beam energy dependence of directed flow as hydrodynamics.  
e.g. Negative slope of proton.
  - This model predicts an enhancement of elliptic flow at high baryon density region (AGS-SPS region) due to softening of EoS.
  - Combined analysis of collective flows  $v_0, v_1, v_2$  at high baryon region  
e.g. at  $5 \text{ GeV} < E_{cm} < 7.7 \text{ GeV}$  will provide important information on the EoS.
- ★ Study of non-equilibrium chiral dynamics

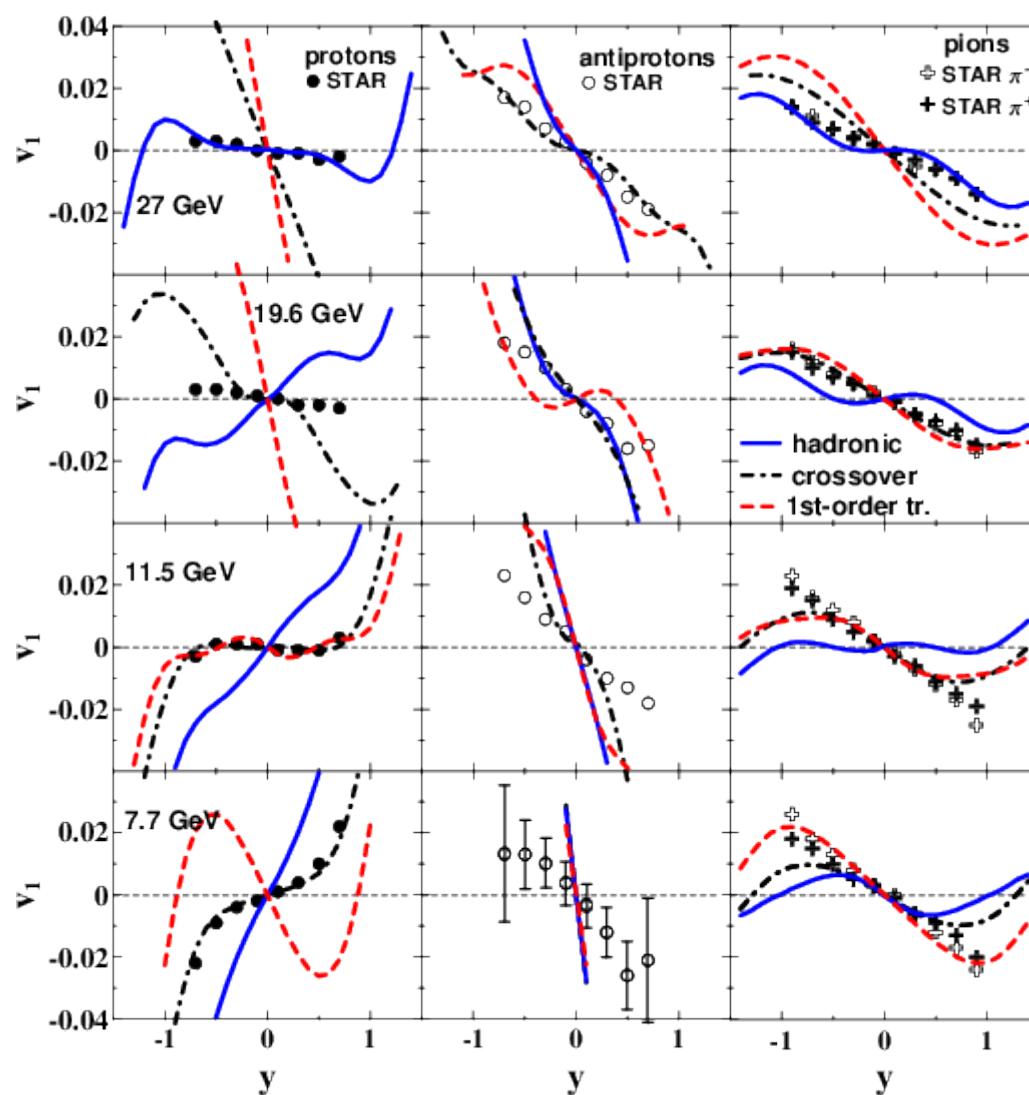
# Beam energy dependence of $v_1$

L. Adamczyk et al. (STAR Collaboration)  
Phys. Rev. Lett. 112, 162301 – Published 23 April 2014



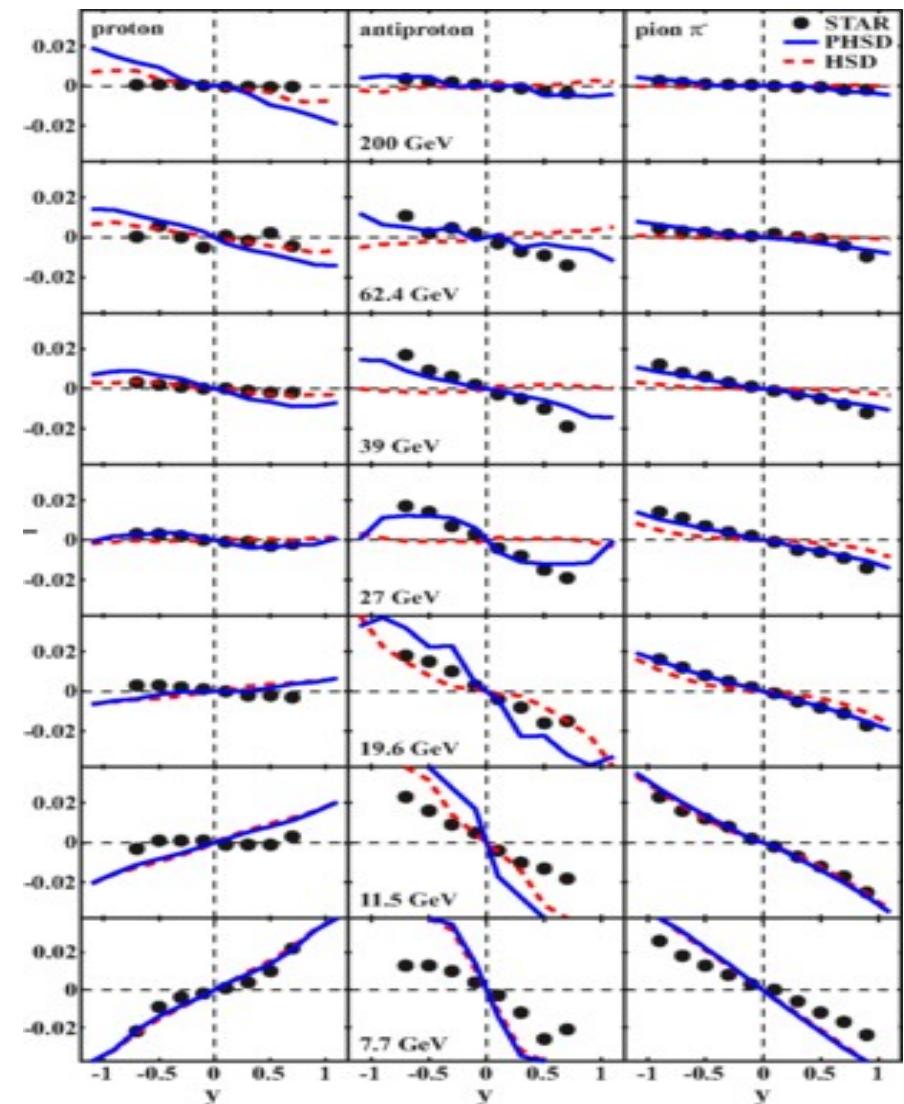
# V1 from hydrodynamics

Y. B. Ivanov and A. A. Soldatov, Phys. Rev. C91, no. 2, 024915 (2015)



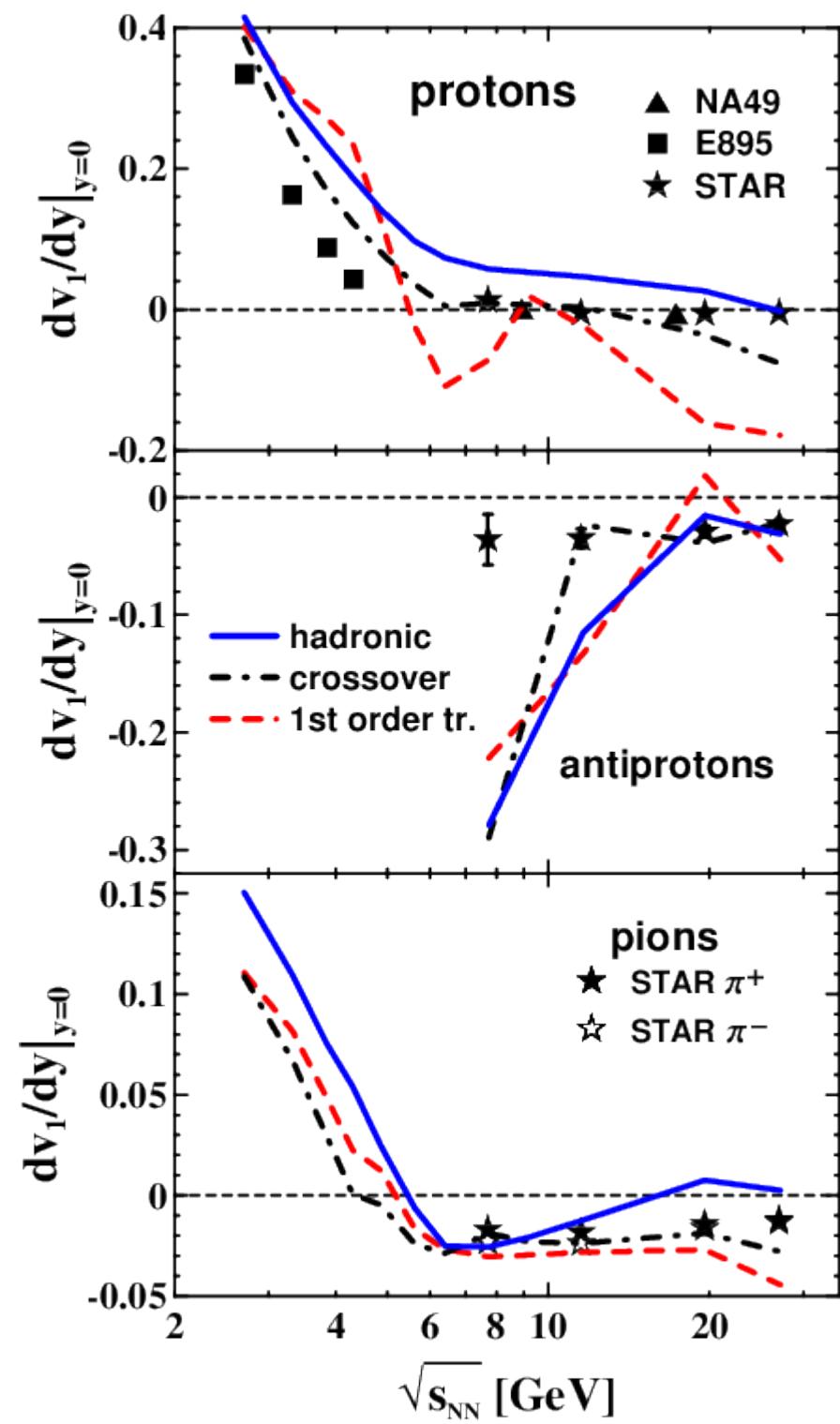
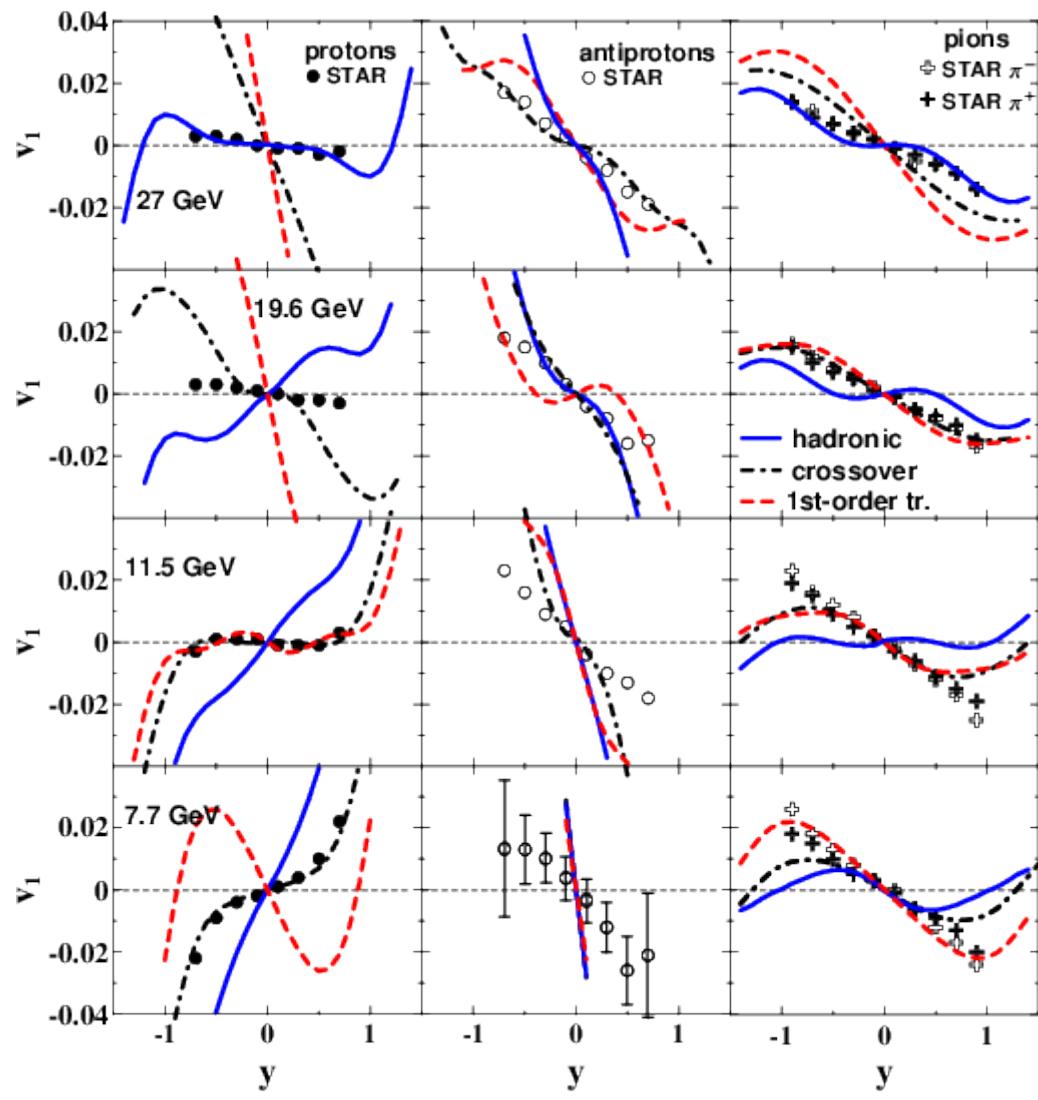
# PHSD/HSD predictions

V. P. Konchakovski, W. Cassing, Y. B. Ivanov and V. D. Toneev, Phys. Rev. C90, no. 1, 014903 (2014)



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