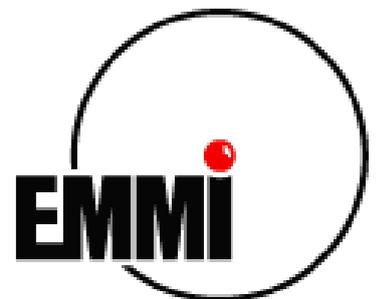


# Chemical Freeze-out Parameters from conserved charge fluctuations at RHIC and LHC

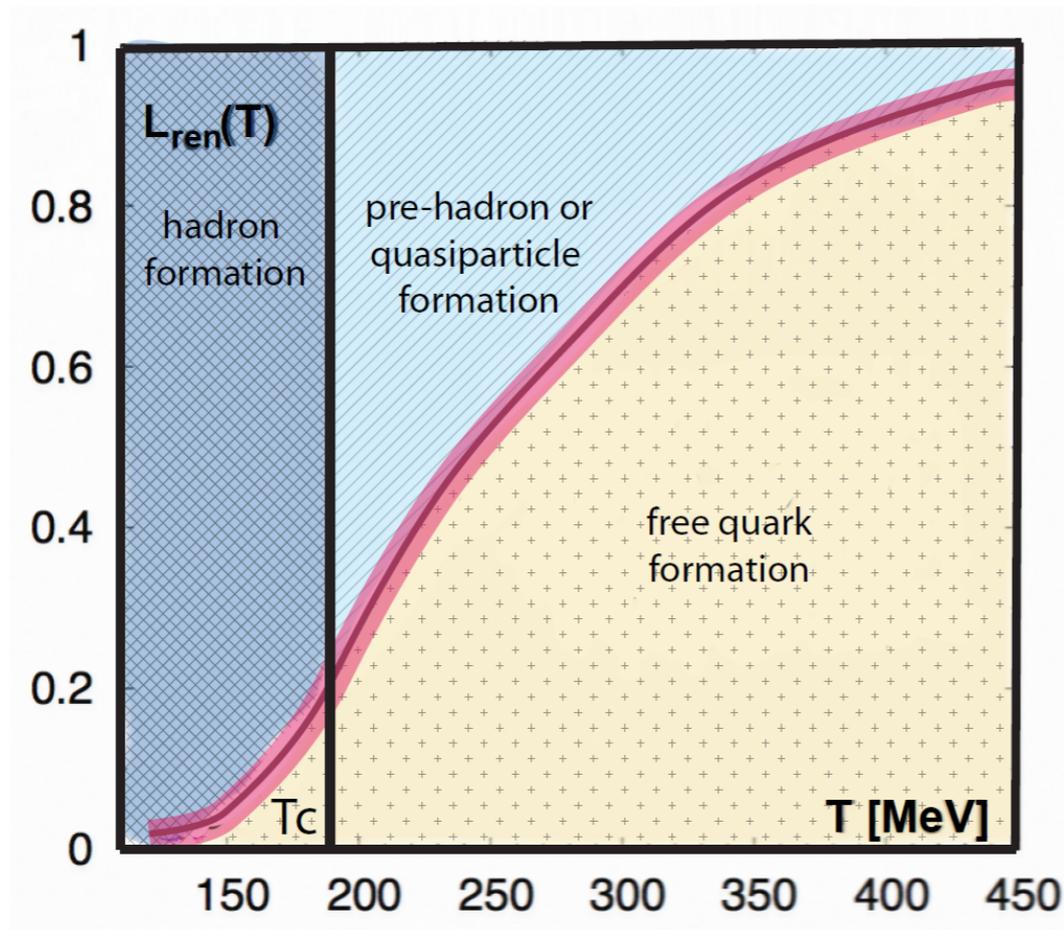
R. Bellwied (University of Houston)

Thanks to: Paolo Alba, Livio Bianchi, Szabolcs Borsanyi,  
Zoltan Fodor, Anders, Knospe, Valentina Mantovani-Sarti,  
Jackie Noronha-Hostler, Paolo Parotto, Attila Pasztor,  
Claudia Ratti

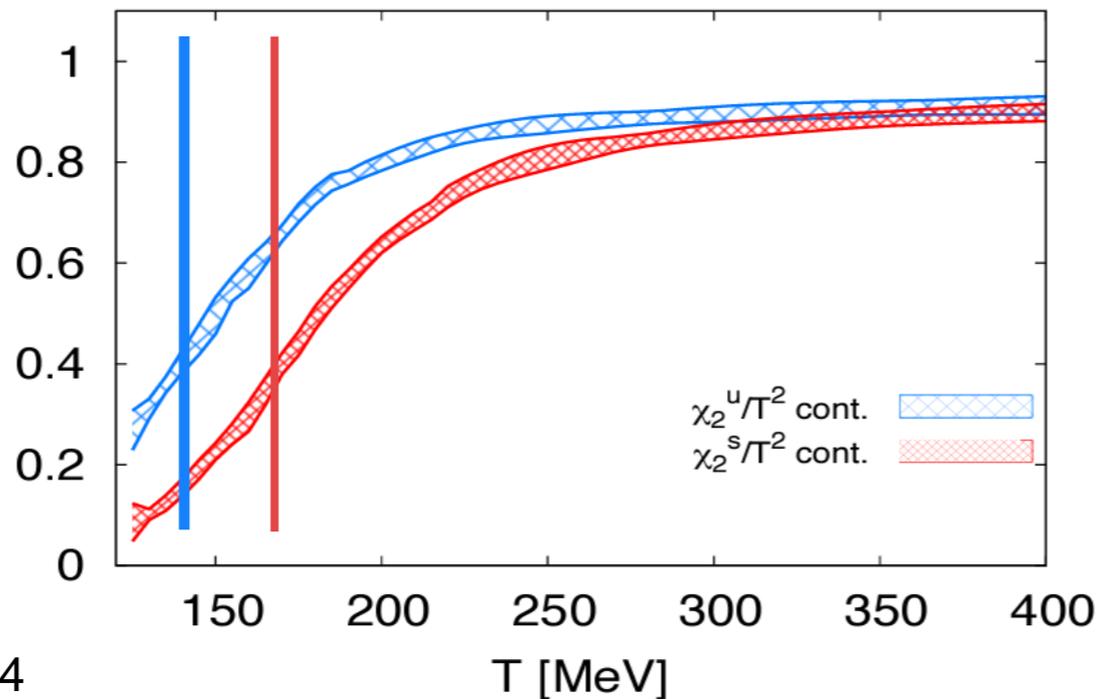
**EMMI Workshop on Critical Fluctuations near the  
QCD Phase boundary in Relativistic Nuclear Collisions  
CCNU, Wuhan, China, Oct.10-13,2017**



# Lattice order parameters in the QCD cross-over



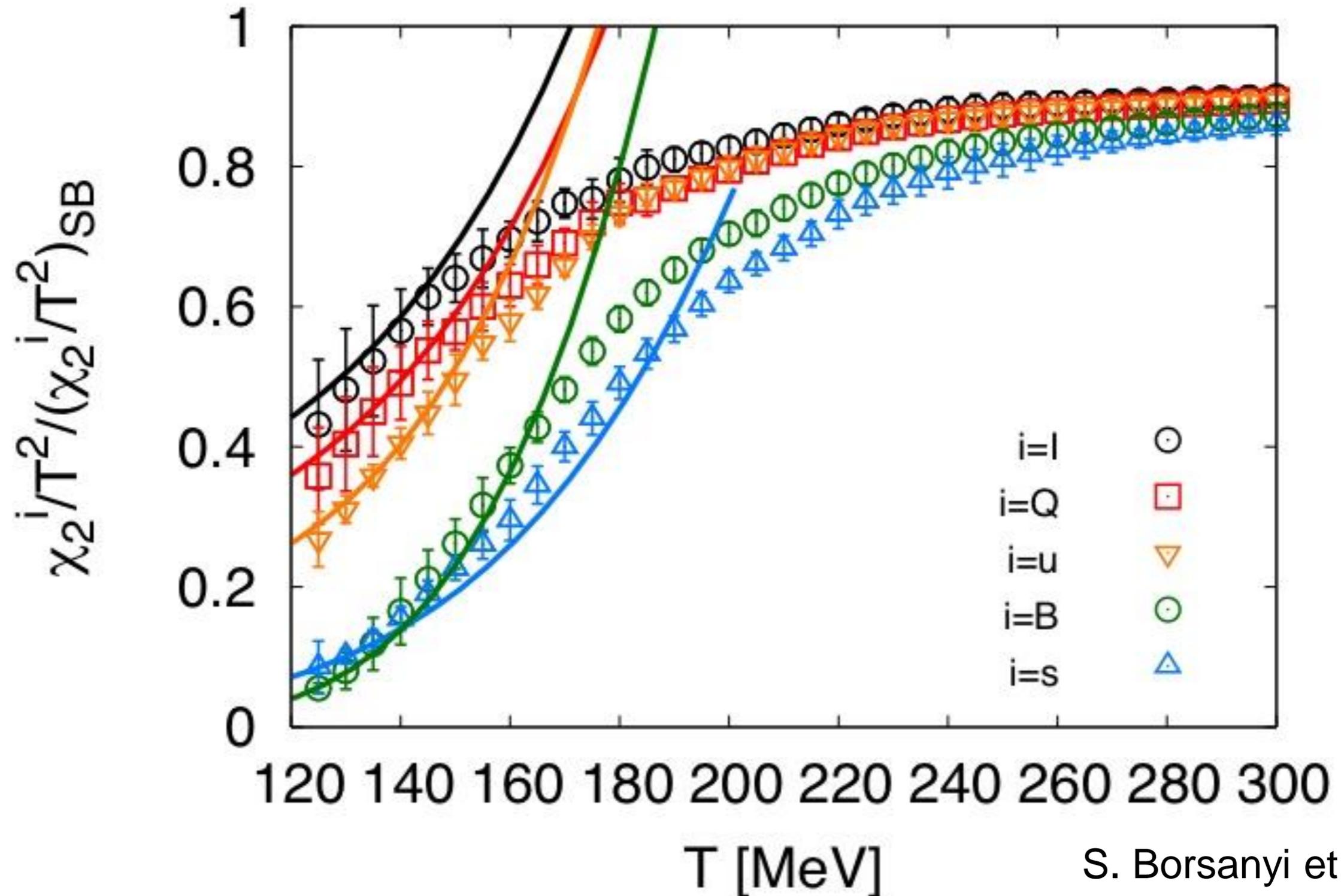
RB, C. Markert,  
PLB691 (2010) 208



C. Ratti et al.,  
PRD 85 (2012) 014004

- In a regime where we have a smooth crossover and where quark masses (even for the s-quark) could play a role why would there be a single freeze-out surface ?
  - We can calculate thermodynamic quantities for a static equilibrated system at a fixed temperature
  - But are pseudo-critical temperatures extracted from flavor dependent susceptibilities as relevant for hadronization properties as chirality ?

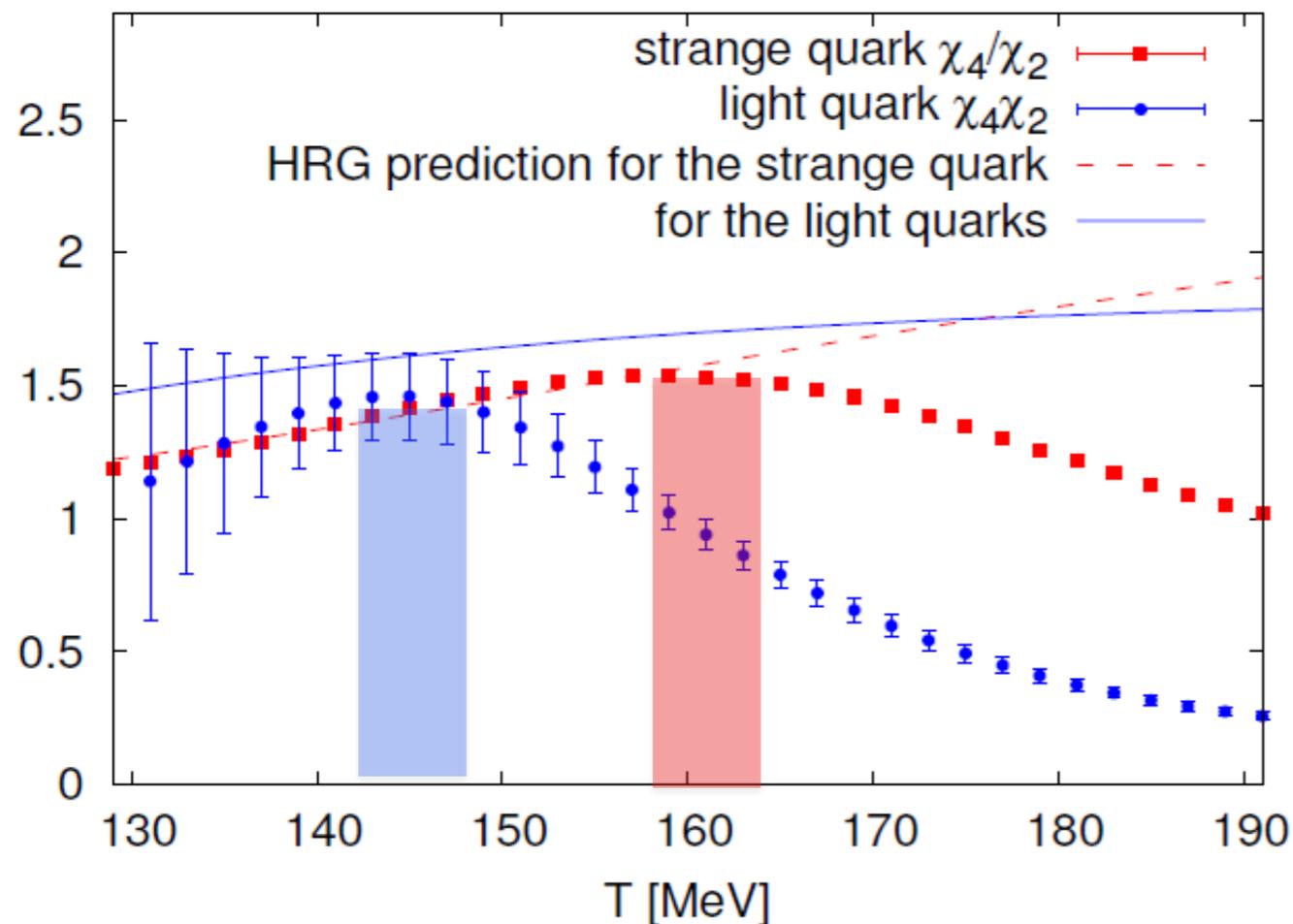
# The relevance of conserved charges as order parameters for the phase transition – Understanding hadronization microscopically



# Direct determination of freeze-out parameters from first principles (lattice QCD)

$$\kappa_B \sigma_B^2 \equiv \frac{\chi_{4,\mu}^B}{\chi_{2,\mu}^B} = \frac{\chi_4^B(T)}{\chi_2^B(T)} \left[ \frac{1 + \frac{1}{2} \frac{\chi_6^B(T)}{\chi_4^B(T)} (\mu_B/T)^2 + \dots}{1 + \frac{1}{2} \frac{\chi_4^B(T)}{\chi_2^B(T)} (\mu_B/T)^2 + \dots} \right]$$

Susceptibility ratios are a model independent measure of the chemical freeze-out temperature near  $\mu=0$ . (Karsch, arXiv:1202.4173)



R. Bellwied & WB Collab., PRL (2013), arXiv:1305.6297

## Indication of sequential hadronization

Either based on the peak position in the lattice QCD calculation or on the point of deviation from the hadron resonance gas (HRG)

Needs experimental verification

# Lattice QCD vs. HRG

The lattice calculations favor a flavor separation.

They use the proper pion and quark masses and they are continuum extrapolated.

Nothing can be changed or improved, except for the possibility that

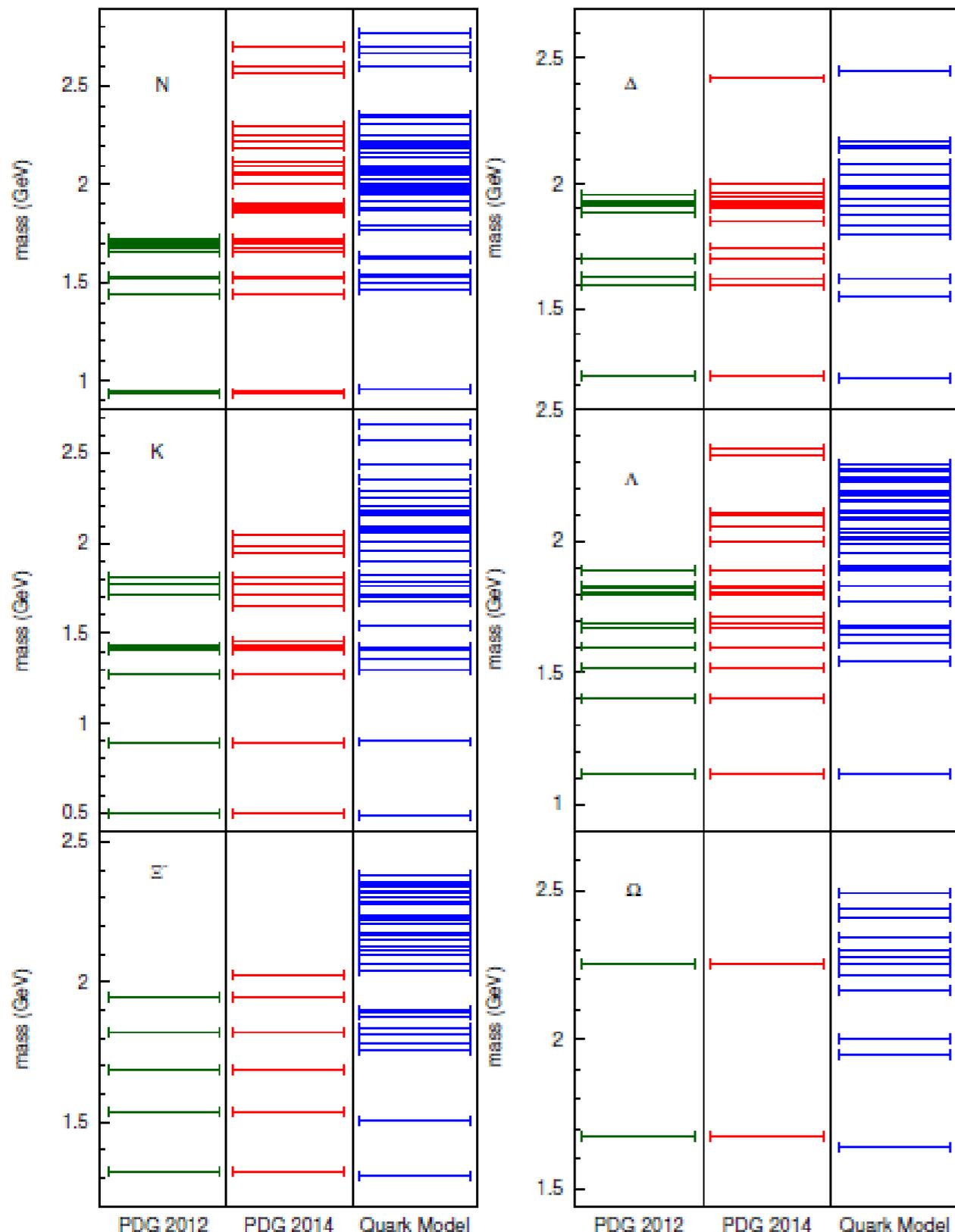
- a.) the action is not perfect
- b.) the system is not in equilibrium.

On the other hand the HRG comparison is subject to a lot of discussion in the recent past.

Two avenues have been pursued:

- a.) a non-interacting HRG can only describe 'reality' if the resonance spectrum is complete.
- b.) an interacting hadron gas is a better proxy as long as the interaction is properly modeled.

# The incomplete HRG input spectrum

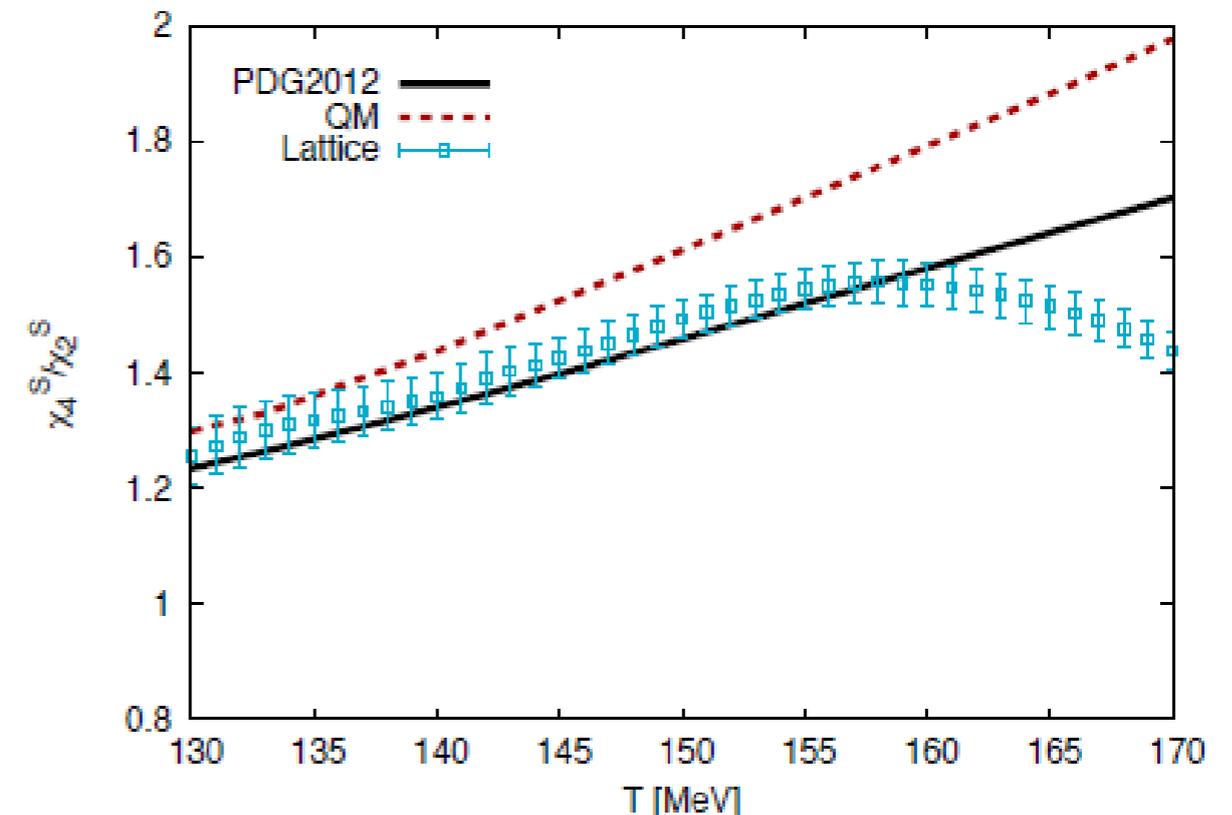
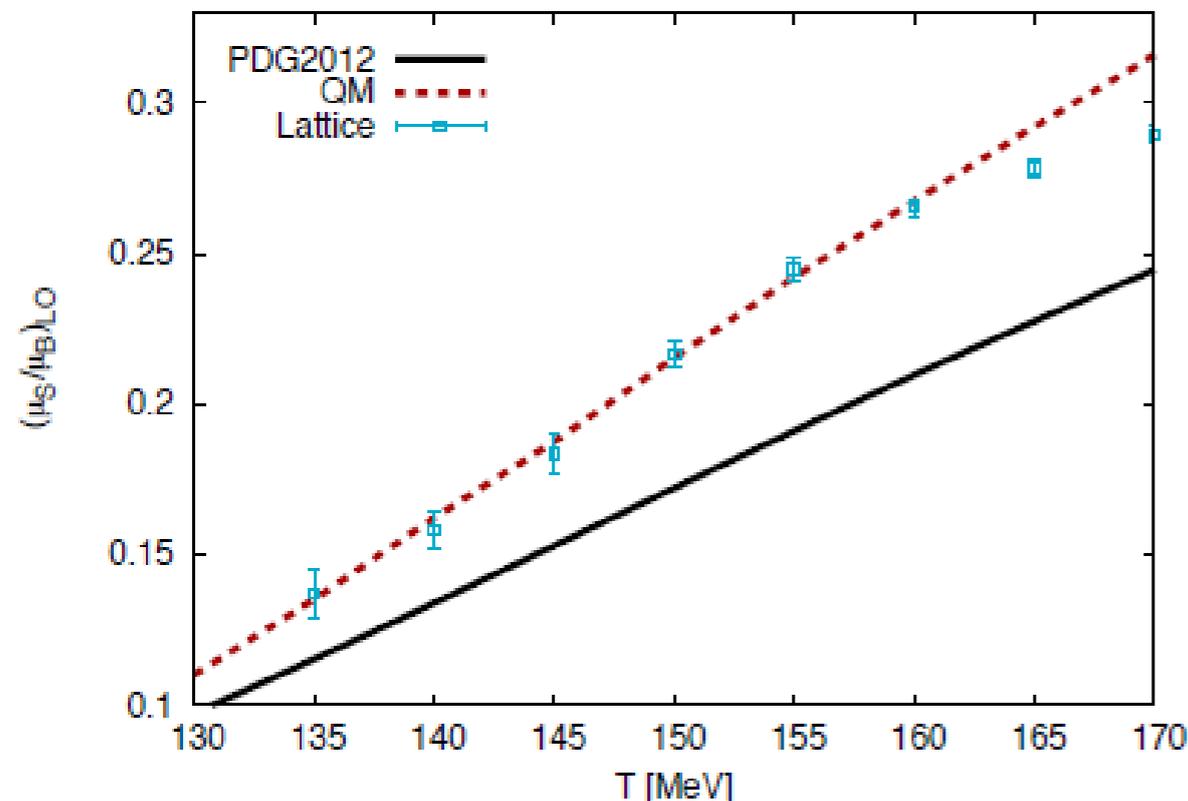


First suggested as a possible 'solution' to the different flavor surfaces by Bazavov et al. (PRL (2014), arXiv:1404.6511)

A more detailed study by P.Alba et al., arXiv:1702.01113)

See talk by C. Ratti on Wednesday

# The problem: It impacts the comparison to different lattice parameters in different ways



Furthermore: there are many different Quark Models with different numbers of 'extra states' depending on the quark interaction

Best compromise seems to be PDG2016+ (incl. all 1-star resonances), see P.Alba et al., arXiv:1702.01113

# Conclusions for the experimental program

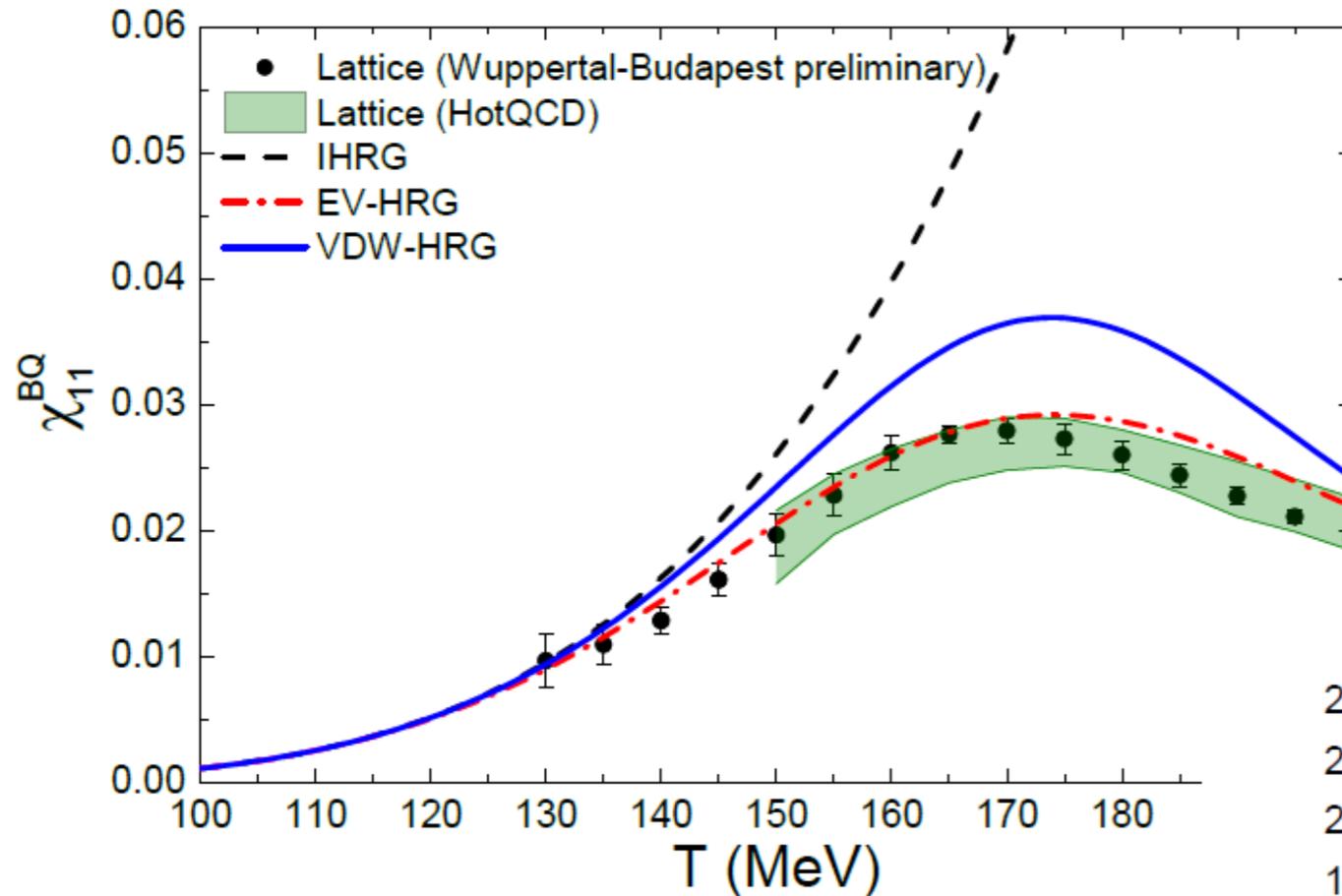
We need more experimental verification of higher mass baryonic resonances, especially in the  $S = 1$  sector (higher level  $\Lambda$  and  $\Sigma$  resonances)

This is an interesting challenge for RHIC and LHC experiments, but also for the future JLab program

(new JLab experiment KLF was just proposed for this purpose, arXiv:1701.07346)



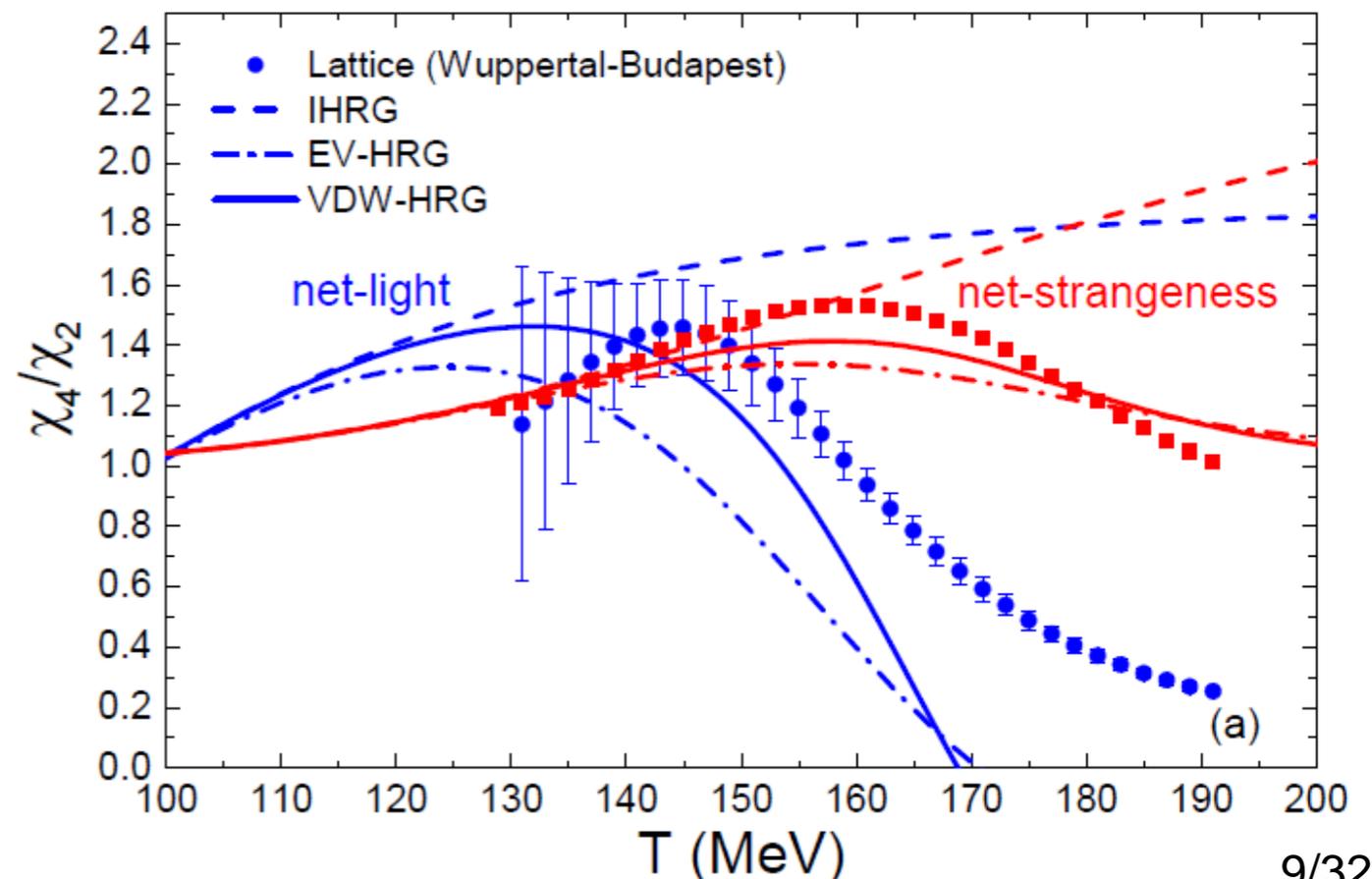
# An alternative: the interacting hadron gas (excluded volume or van der Waals interaction), Vovchenko et al., PRL 2016, arXiv:1609.03975 (see also Mark's talk)



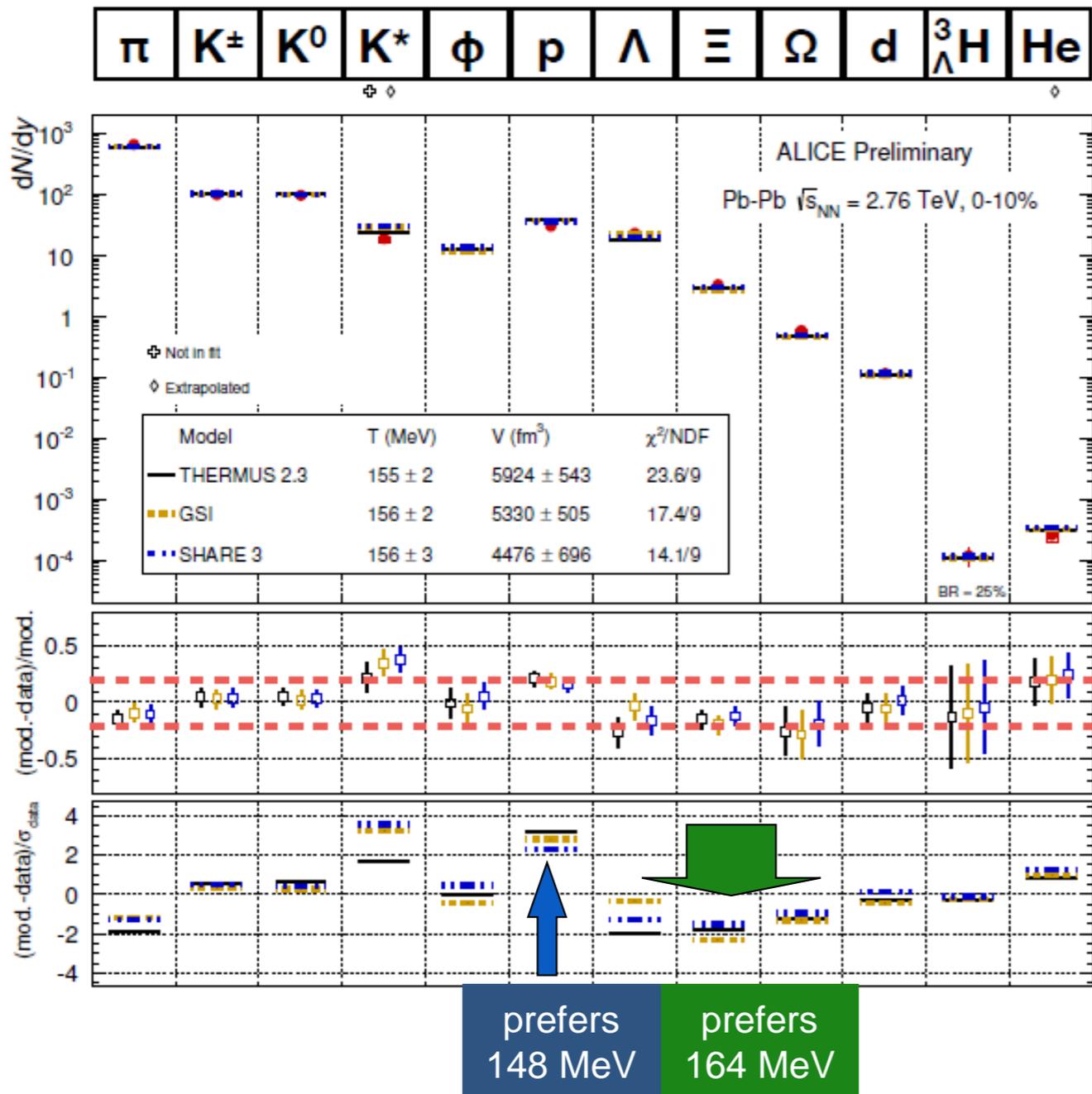
Seems to get some of the features right (peak structures in lattice susceptibility ratios)

Problems:

- excluded volume calculation debatable
- pushes 'agreement' with lattice way beyond the pseudo-critical temperature



# Experimental evidence: HRG (PDG 2010) model comparison based on yields



Data: ALICE, QM 2014, arXiv:1408.6403  
This looks like a good fit, but it is not

$\chi^2/\text{NDF}$  improves from 2 to 1 when pions and protons are excluded.

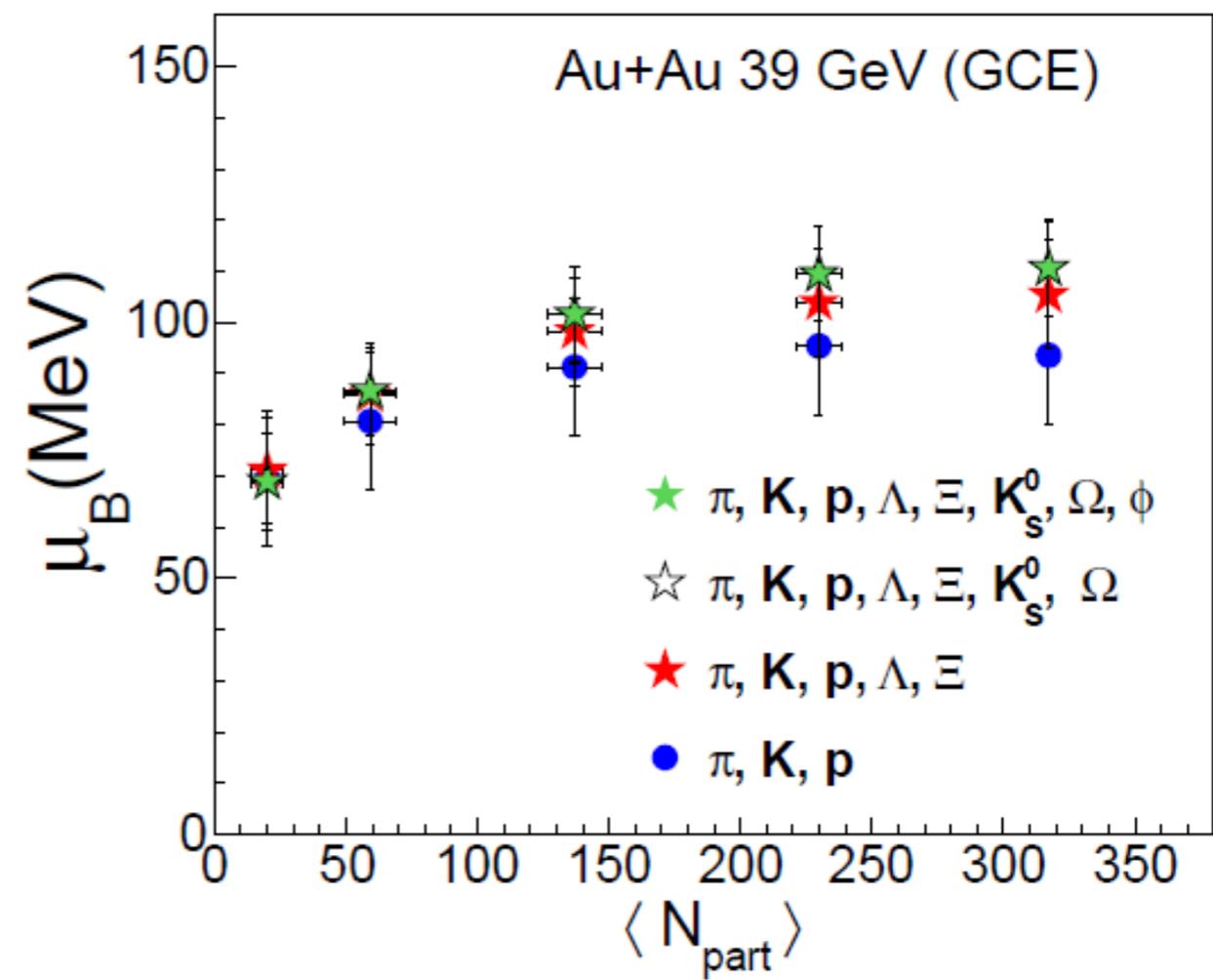
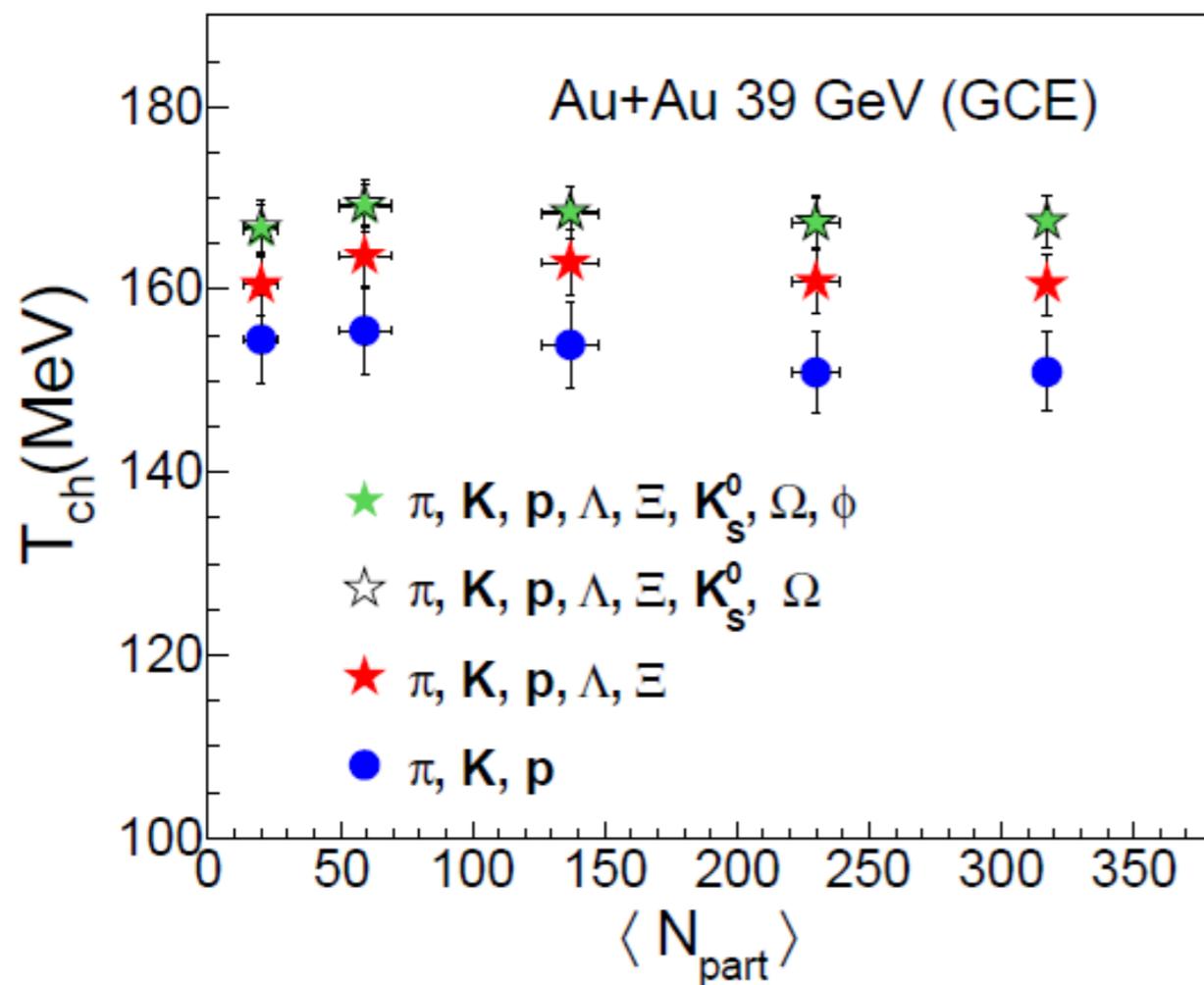
Fit to pions and protons alone yield a temperature of 148 MeV. Strange baryons yield 164 MeV

Several alternate explanations:

- Inclusion of Hagedorn states
- Non-equilibrium fits
- Baryon annihilation
- Different  $T_{ch}$  for light and strange

# Experimental evidence from varying the input particles into the chemical fit

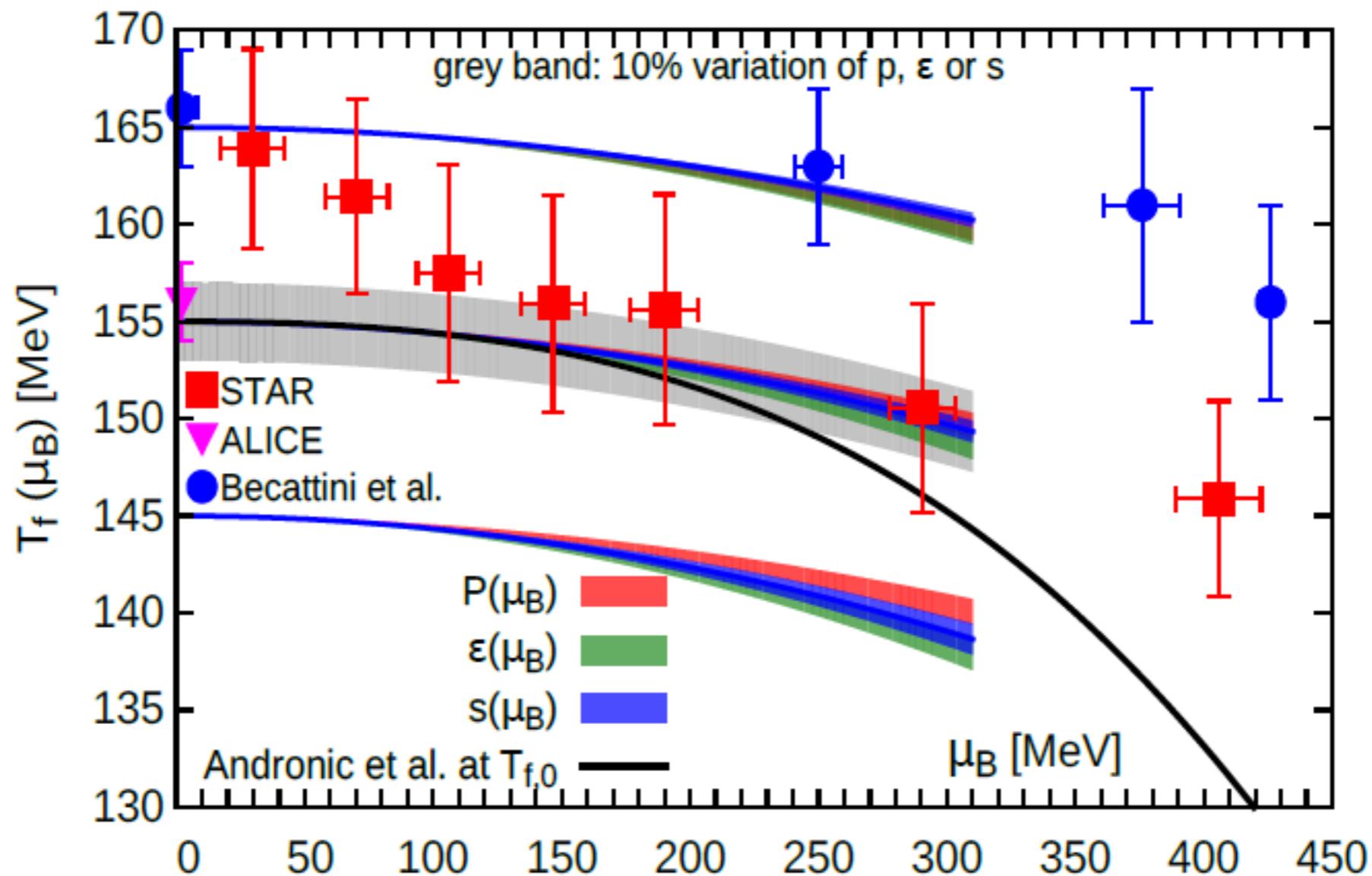
Latest example: Beam Energy Scan data from STAR  
(arXiv:1701.07065)



This is a long known fact in SHM, always argued as 'the more states the better', but all additional states (to  $\pi, k, p$ ) are strange states

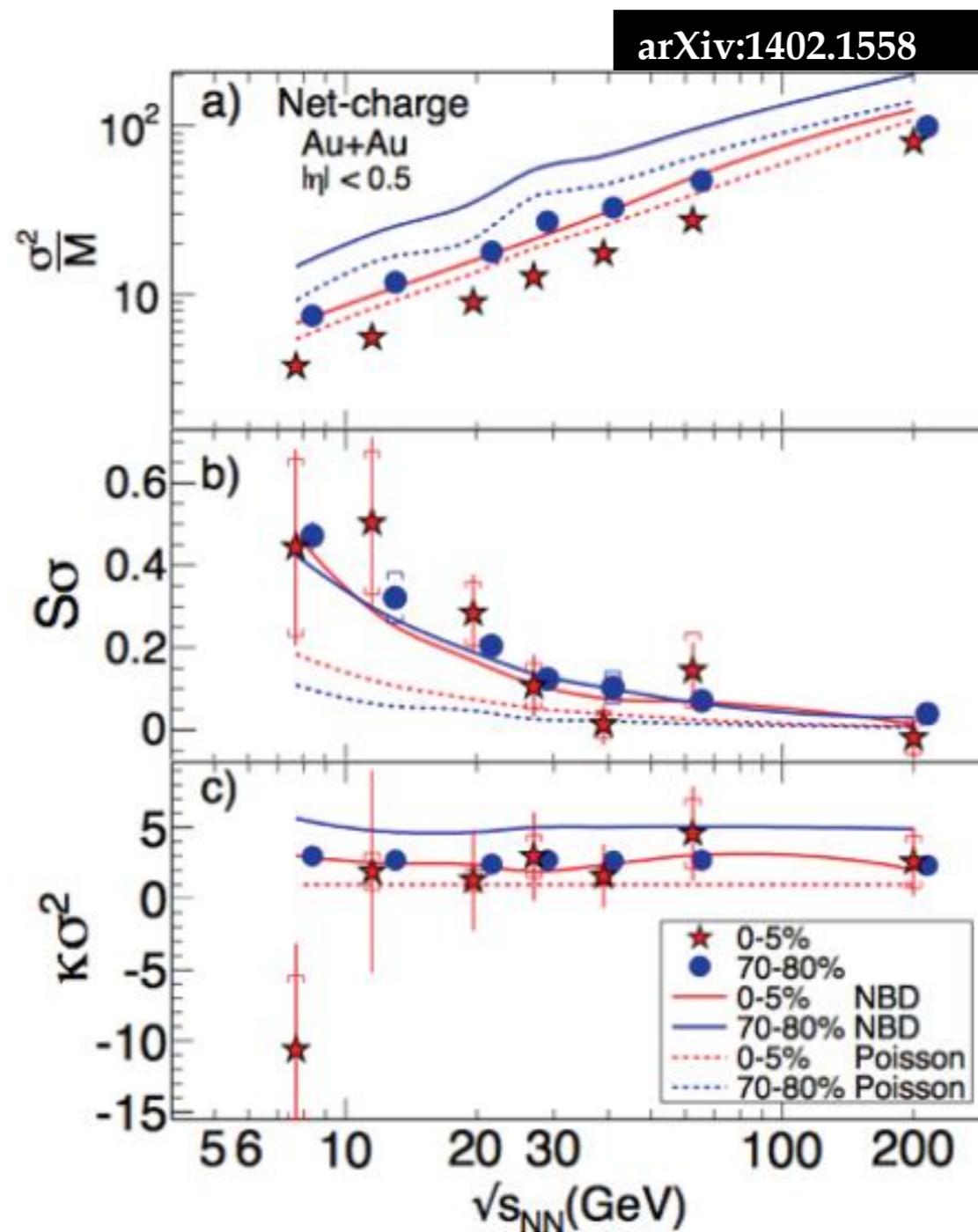
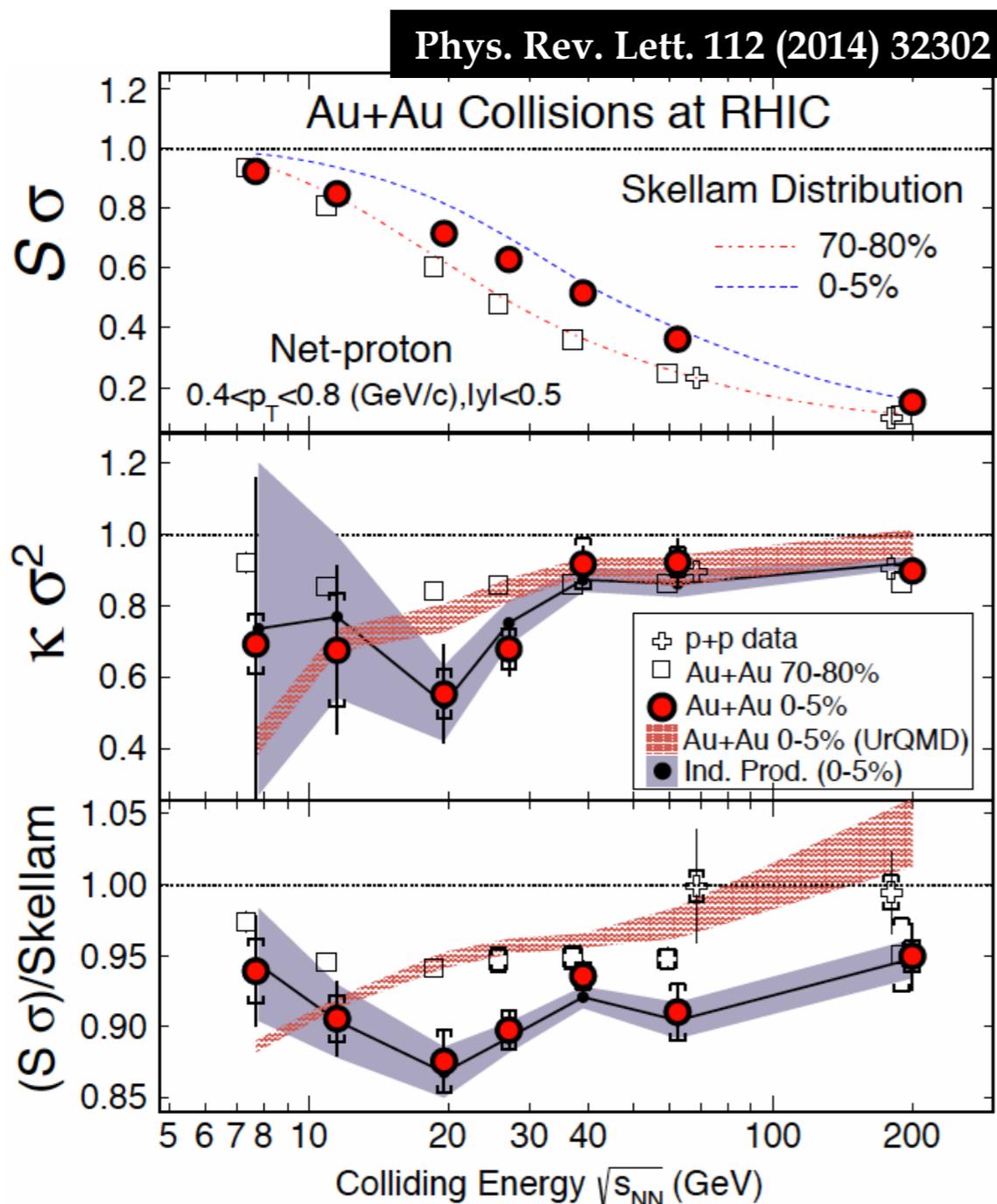
# There is an upper limit.....

One important fact to remember: The chemical freeze-out surface cannot be above the pseudo-critical temperature from the lattice ( $154 \pm 9$  MeV)  
(both moved down over the years....)



F.Karsch, arXiv:1611.01973, SQM 2016  
spread in  $T$  given by uncertainty in chiral pseudo-critical  $T$ ,  
but also by difference between  $T$  from  $\chi_u$  and  $\chi_s$

# Higher moment ratios for net-charge and net-proton distributions (STAR 2014)

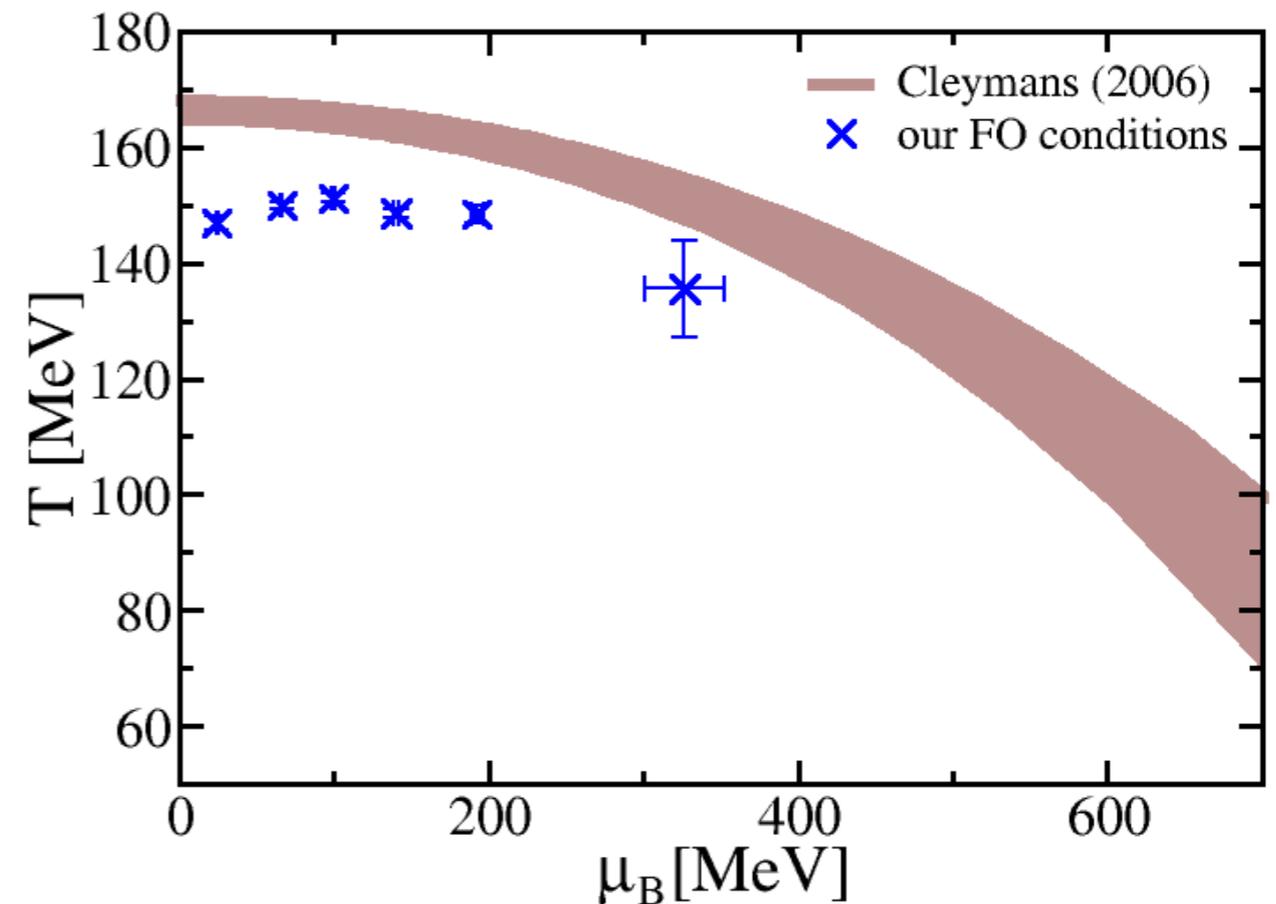
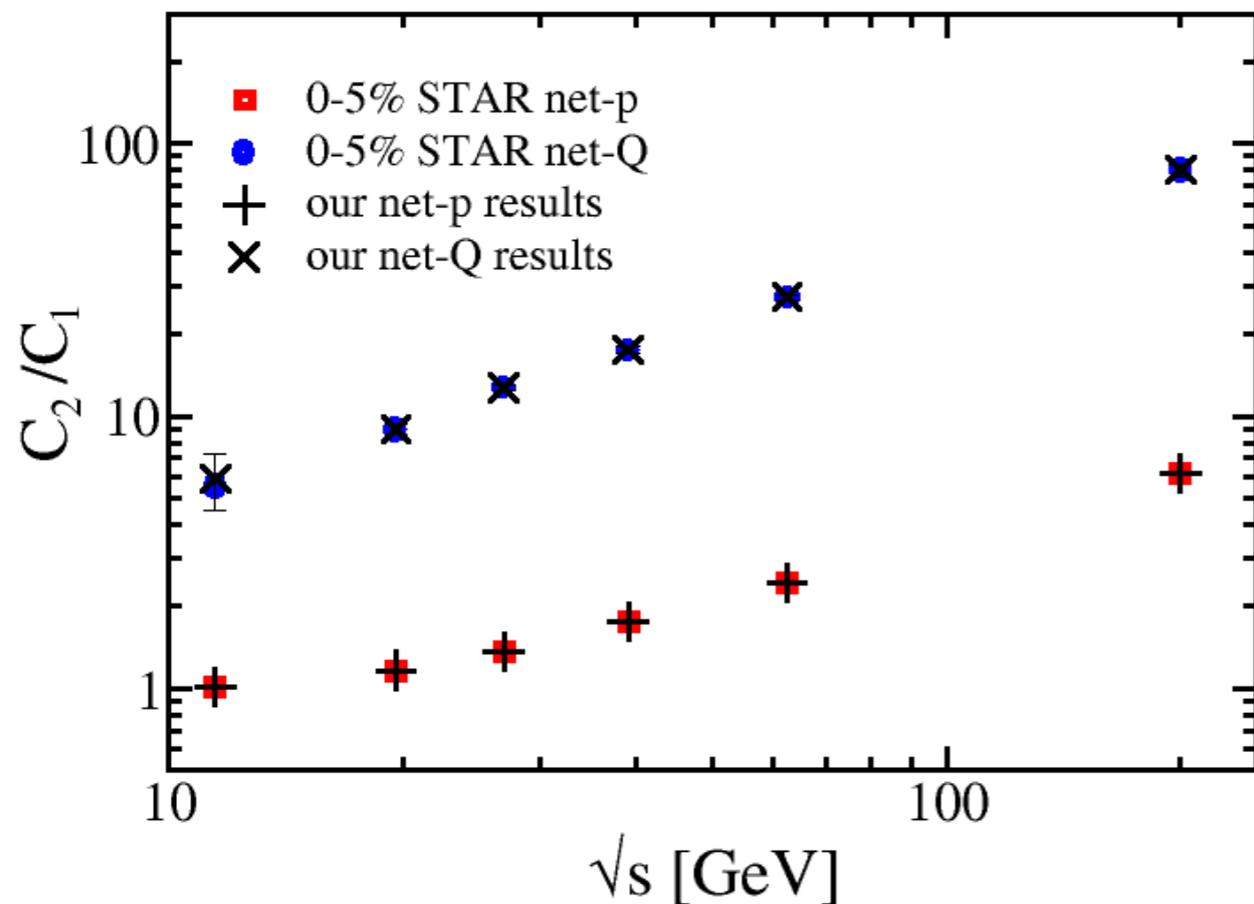


Fluctuations are more sensitive to chemical freeze-out as simple yields. They can be directly compared to susceptibilities on the lattice (P.Alba et al., PRC, (arXiv:1504.03262))

# HRG (PDG 2008) analysis of STAR results (charge & proton)

Alba, Bellwied, Bluhm, Mantovani, Nahrgang, Ratti, PLB (2014),  
arXiv:1403.4903

HRG in partial chemical equilibrium: resonance decays for resonances up to 2 GeV/c<sup>2</sup> and weak decays taken into account), experimental cuts applied.  
Use the lowest moments with the smallest errors and least ‘criticality’, i.e.  $\sigma^2/M$

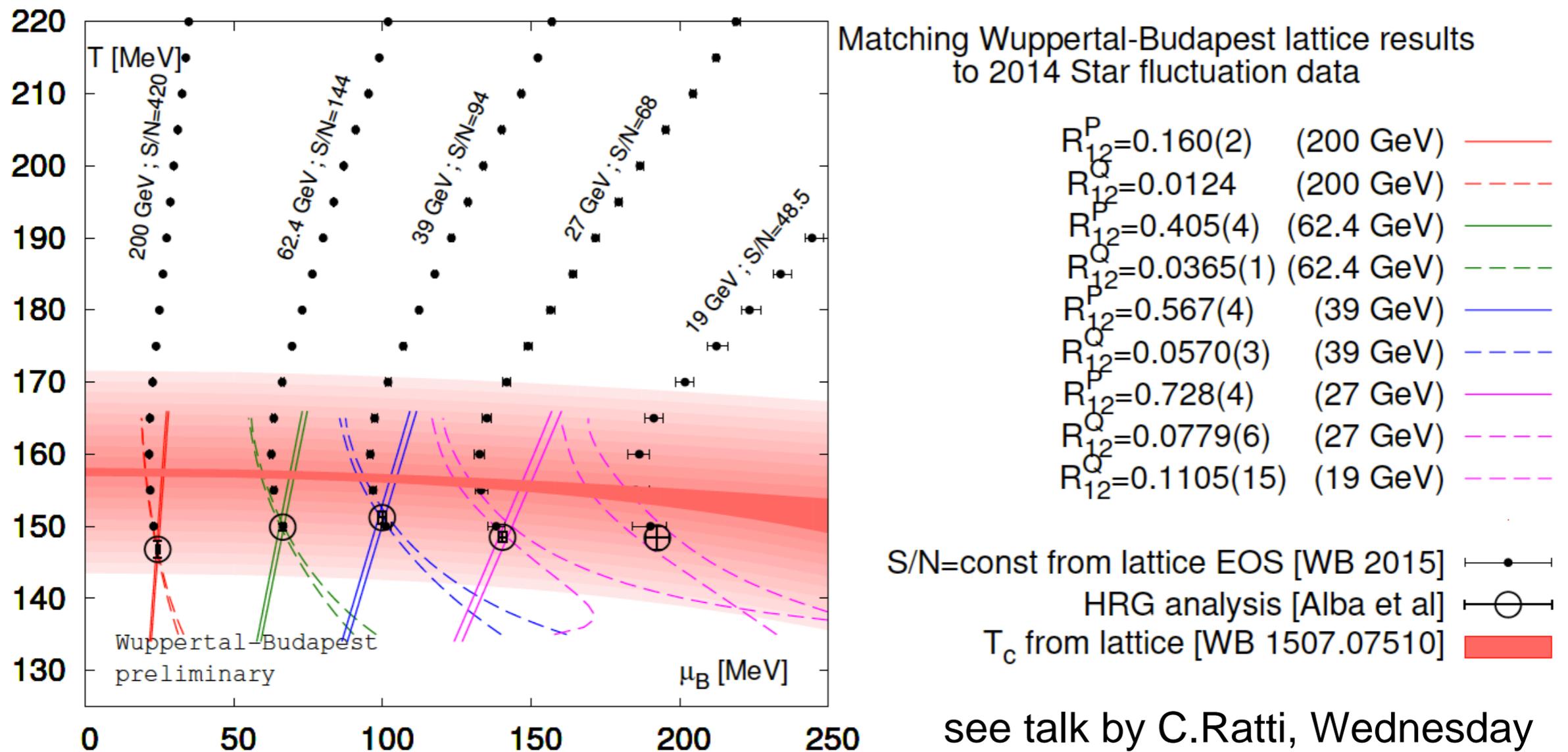


Result: intriguing ‘lower’ freeze-out temperature (compared to SHM yield fits)  
with very small error bars (due to good determination of  $c_2/c_1$ )  
(Results were confirmed with STAR 2.0 results)

# The light quark freeze-out surface is well defined

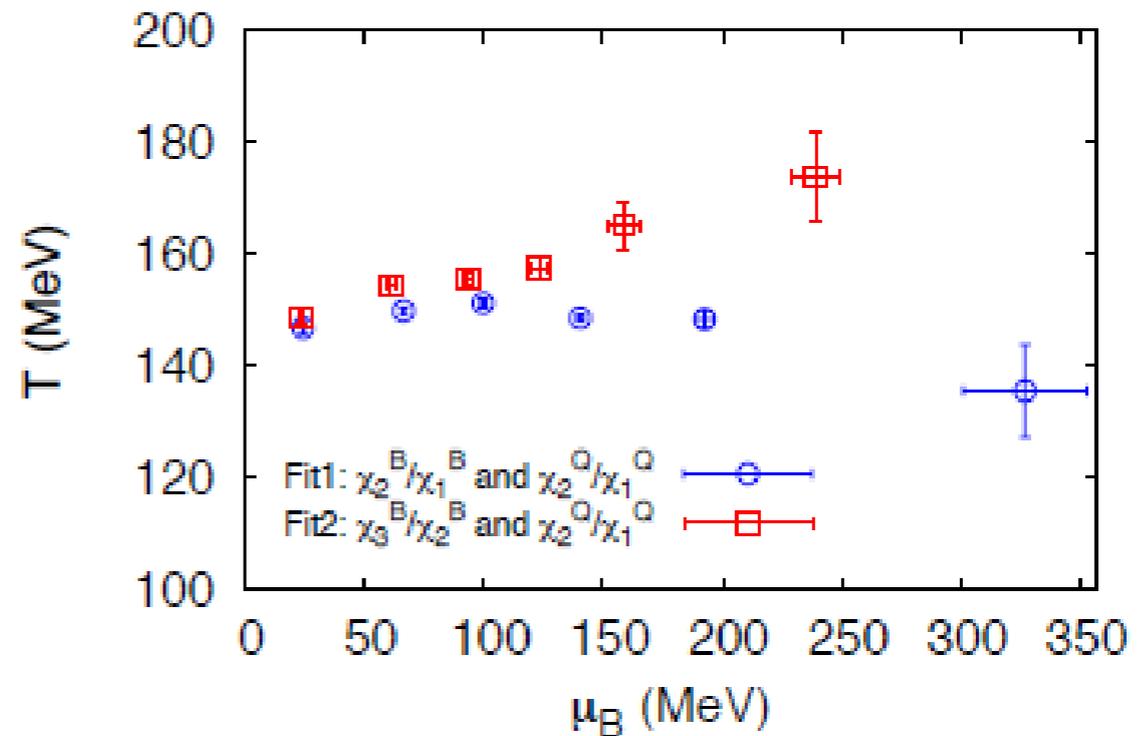
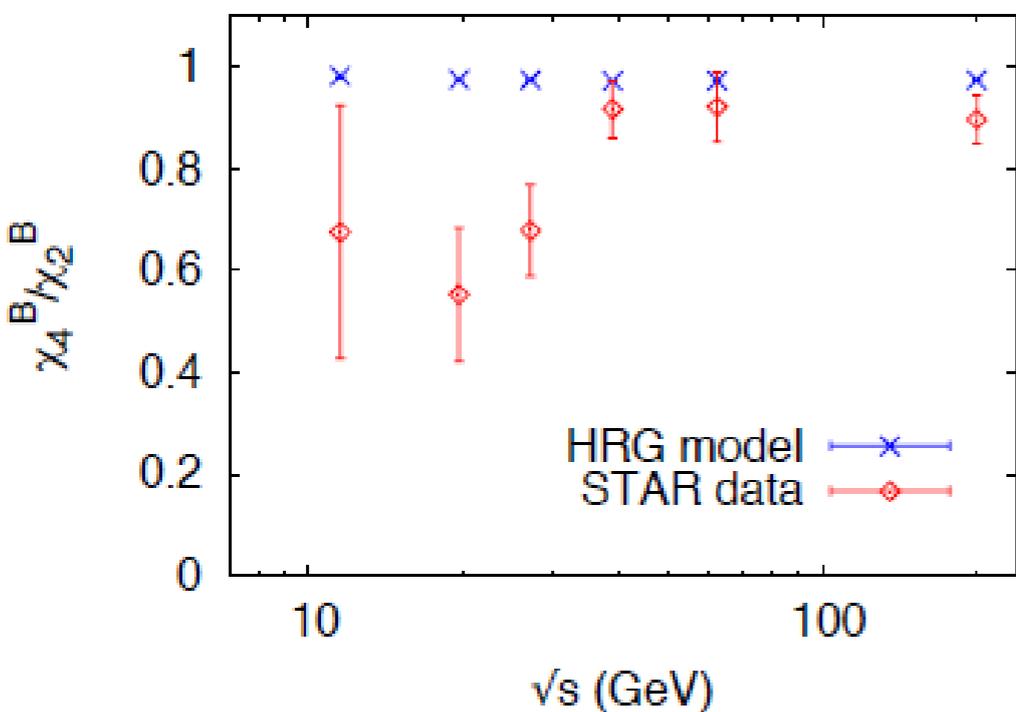
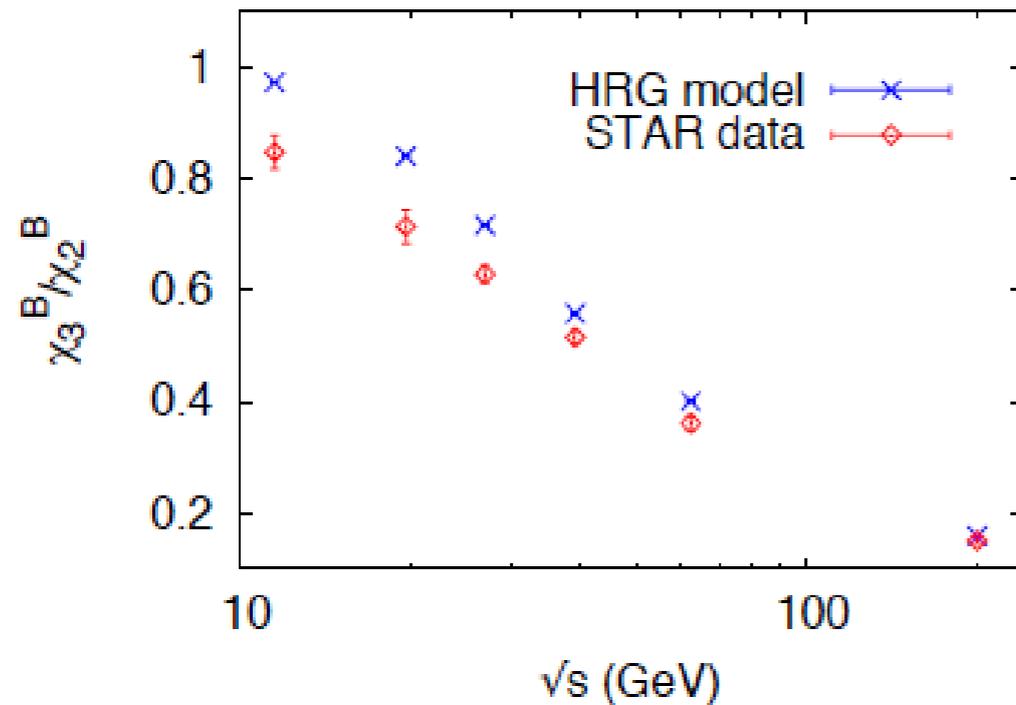
Lattice: improved actions, realistic masses, continuum extrapolations –  
**DONE**

HRG: implementations improved, better PDG, more states – **DONE**



The spread in the lattice range is effectively covered by the light vs strange quark susceptibilities

# Higher moments are not necessarily advantageous for chemical freeze-out studies



HRG overshoots the  $\chi_3/\chi_2$  at lower energies and cannot explain the 'dip' in  $\chi_4/\chi_2$ .  
 Temperature dependence on collision energy becomes 'unphysical'.

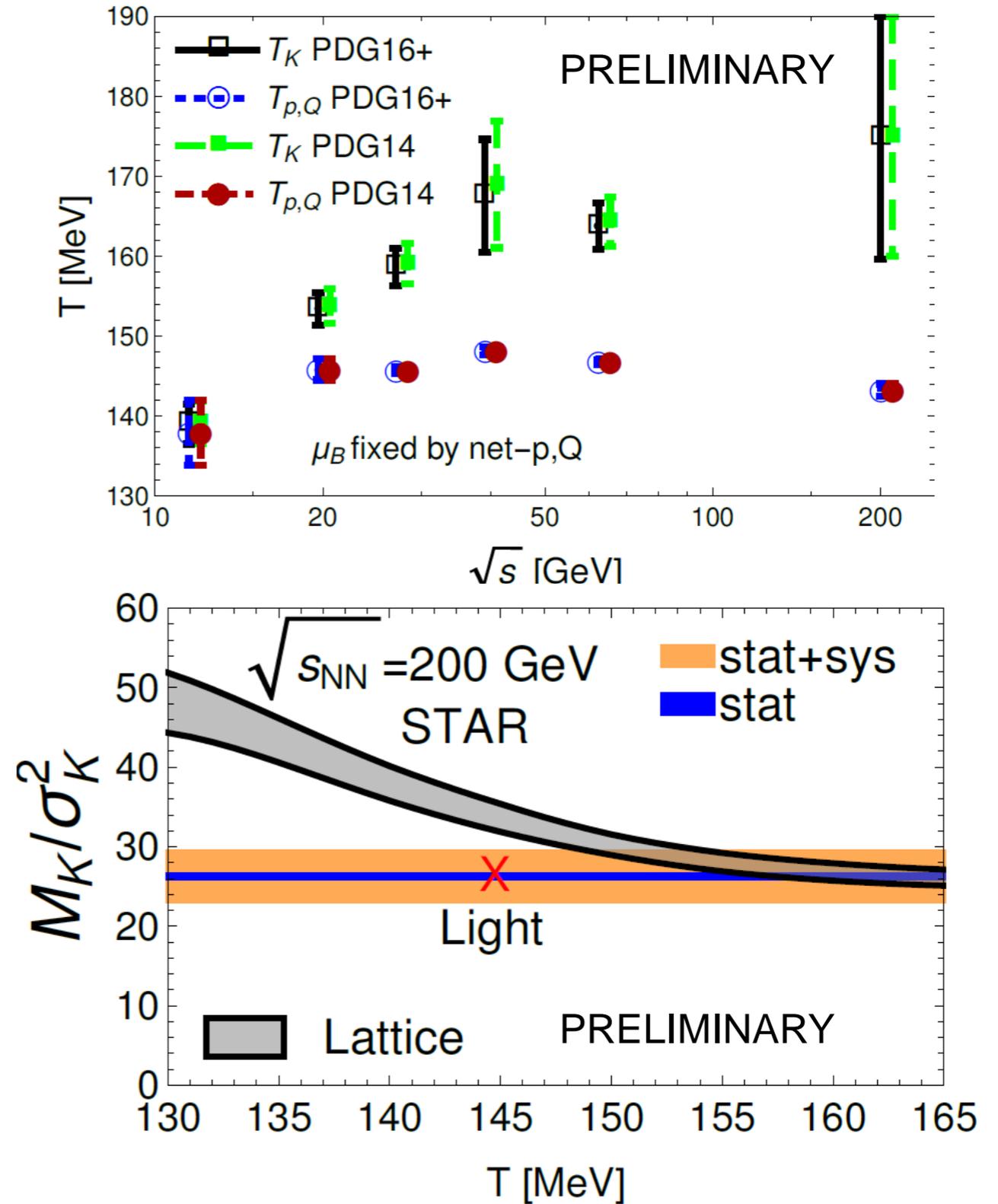
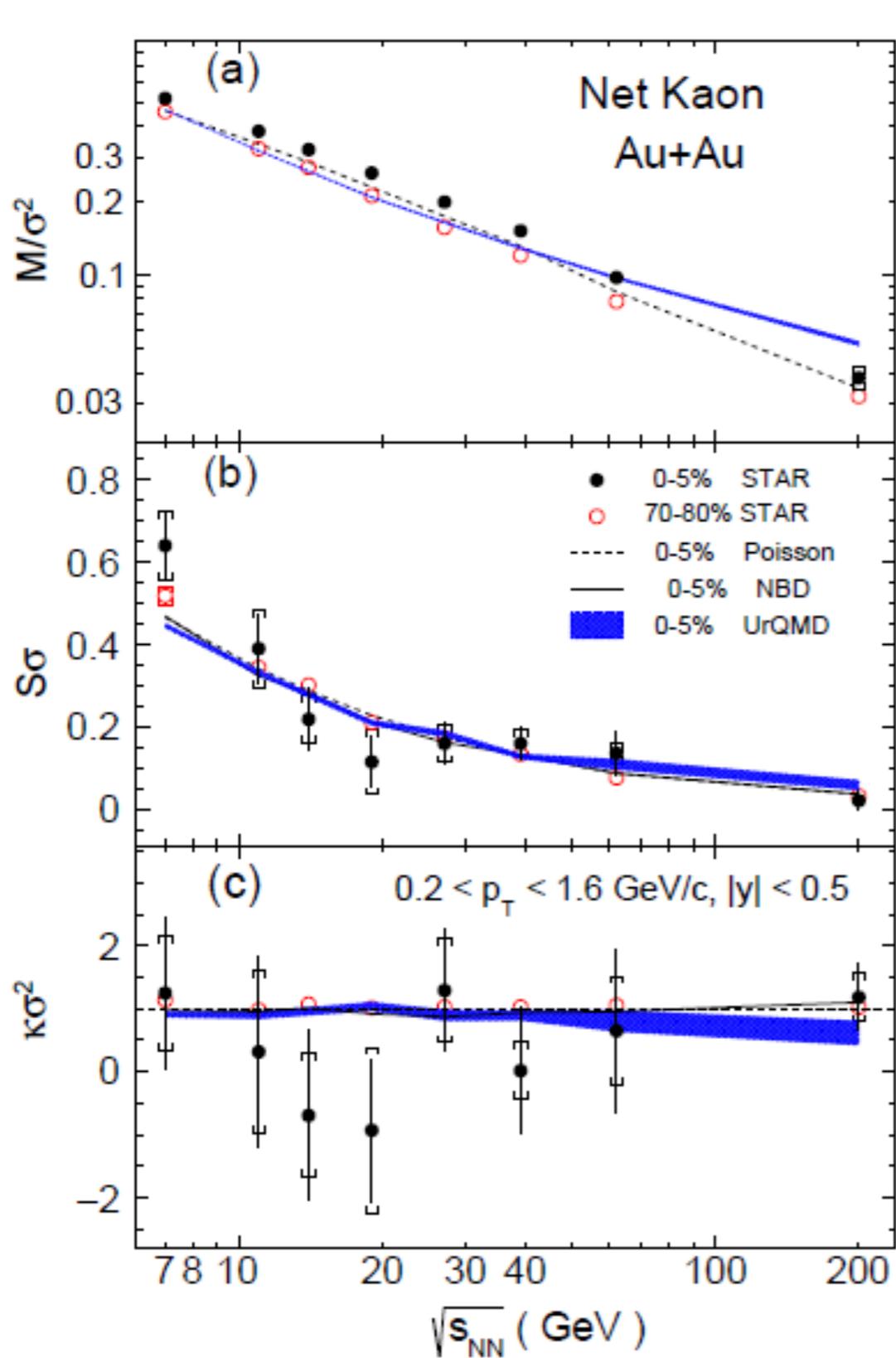
### Possible reasons:

- a.) overestimate of isospin randomization
- b.) onset of critical behavior in  $\chi_3$  and  $\chi_4$**

Important lesson: lower moments carry significant information with much smaller error bar (might be already sufficient)

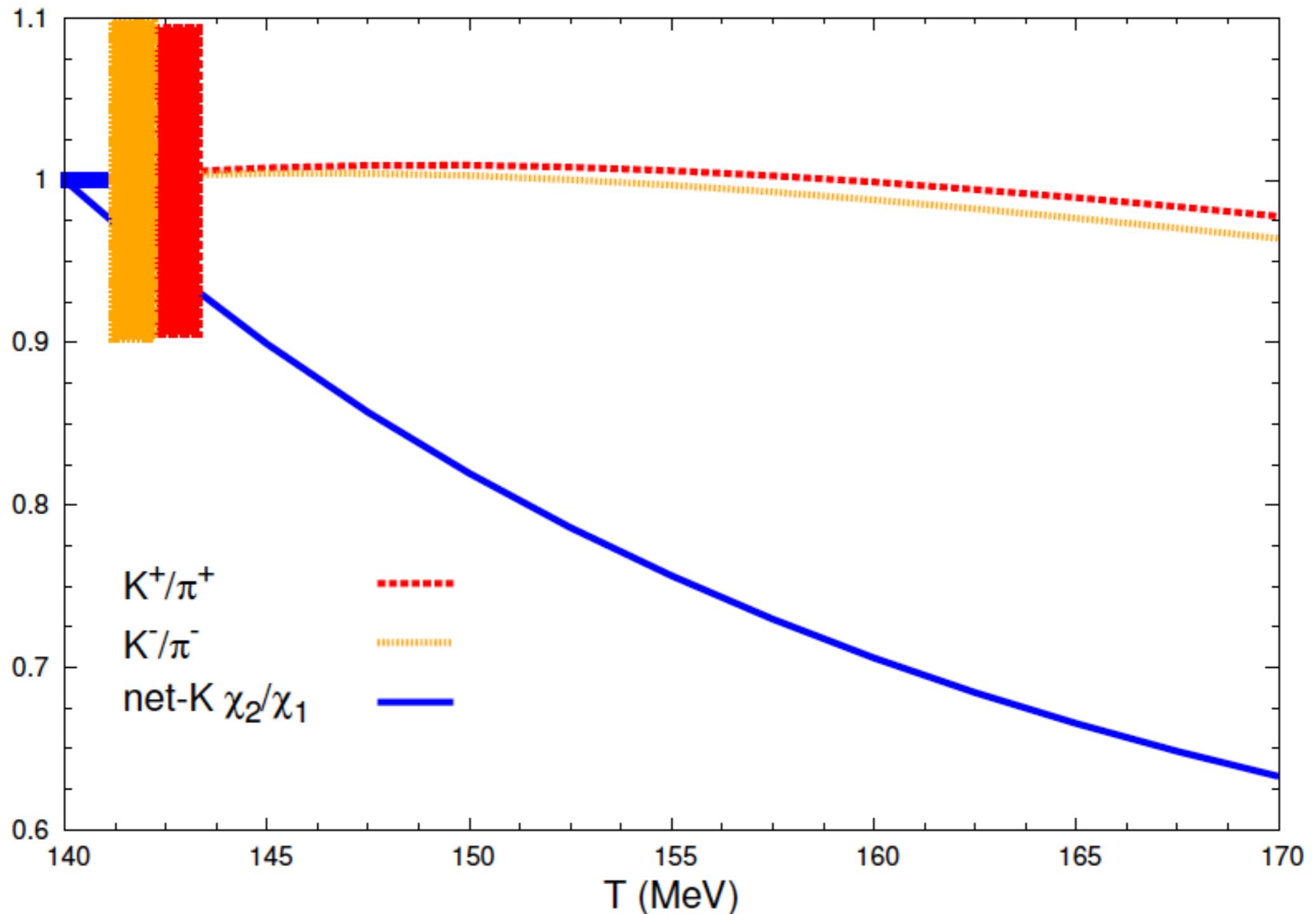


# Fit $\sigma^2/M$ for net-kaons in the same fashion than for net-proton and net-charge (Data: STAR, arXiv:1611.07132)

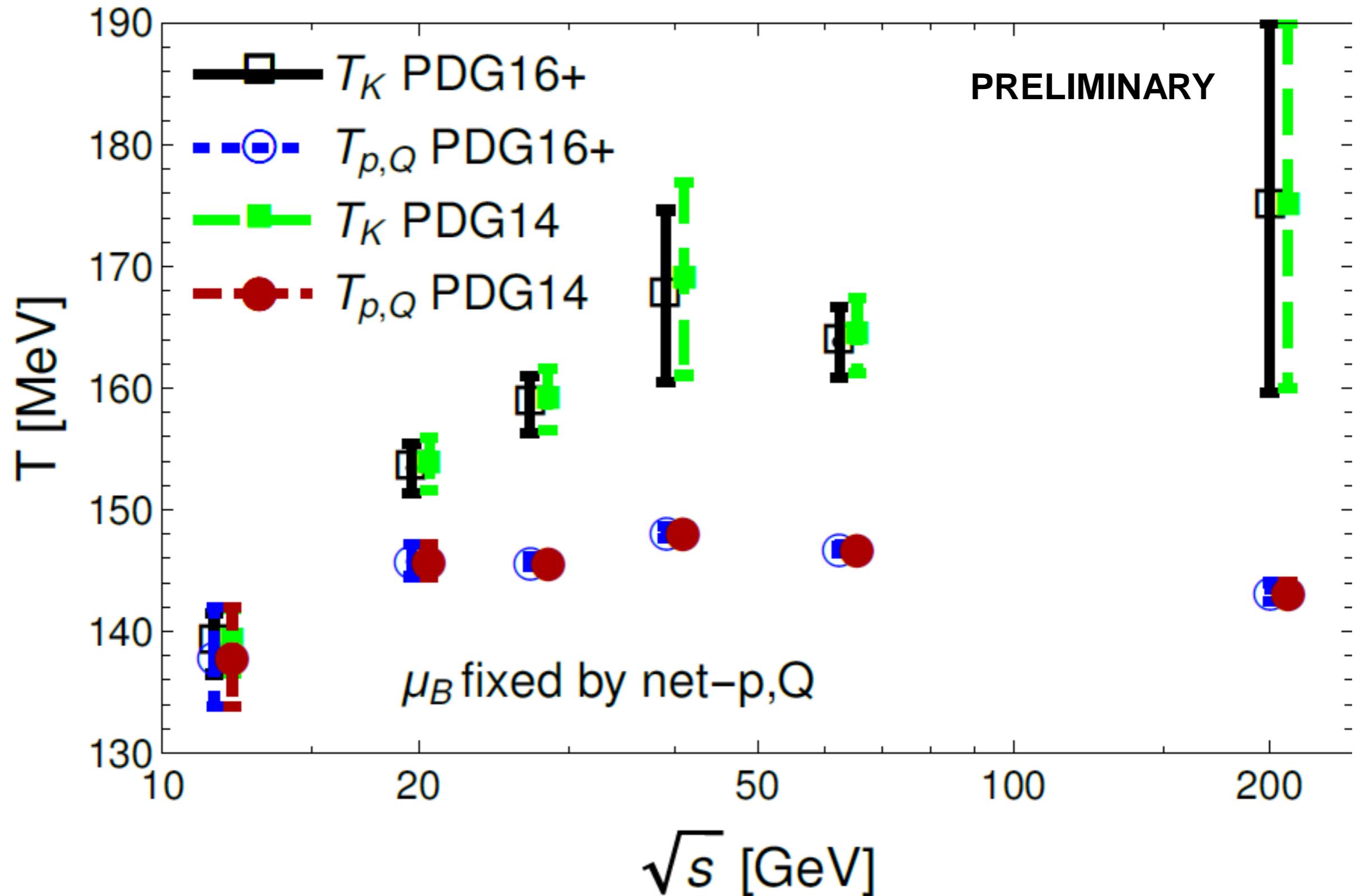


JNH, Ratti et al., arXiv:1607.02527

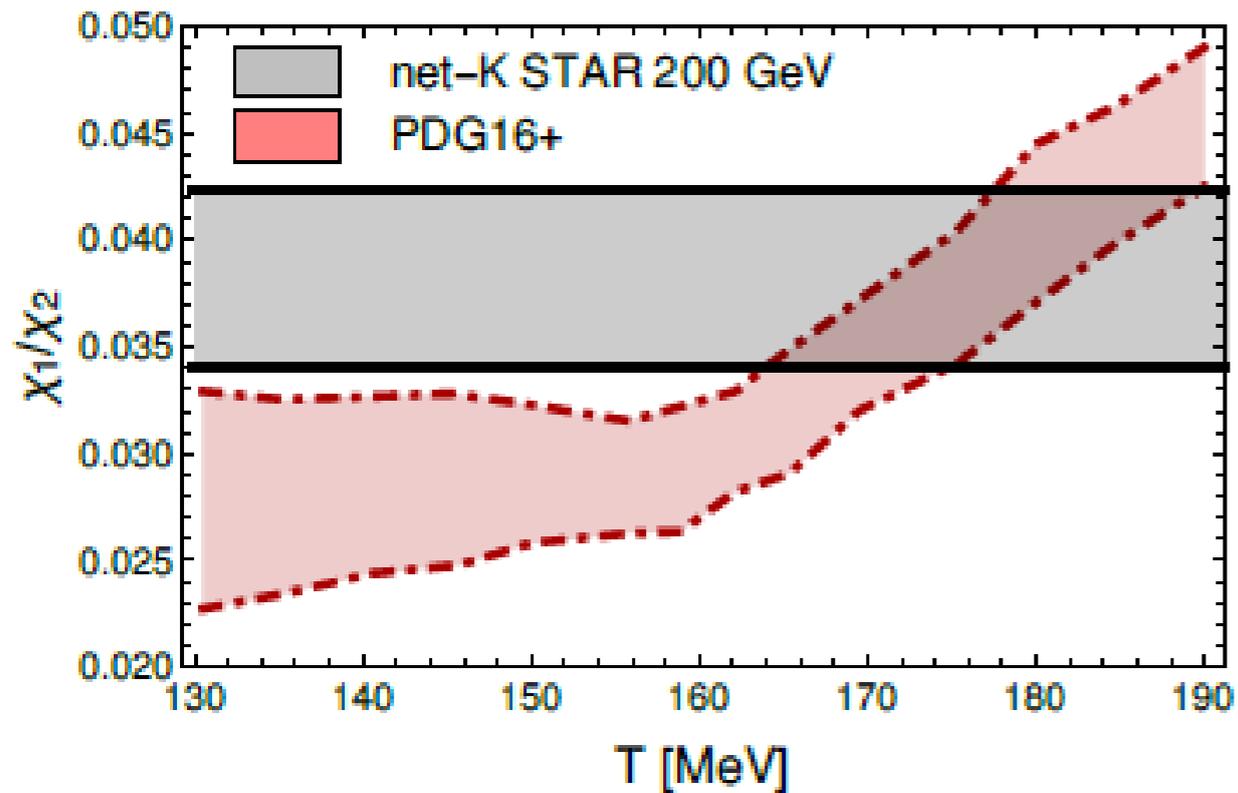
# Kaon fluctuations show a remarkable sensitivity to $T_{ch}$ when compared to yields or yield ratios



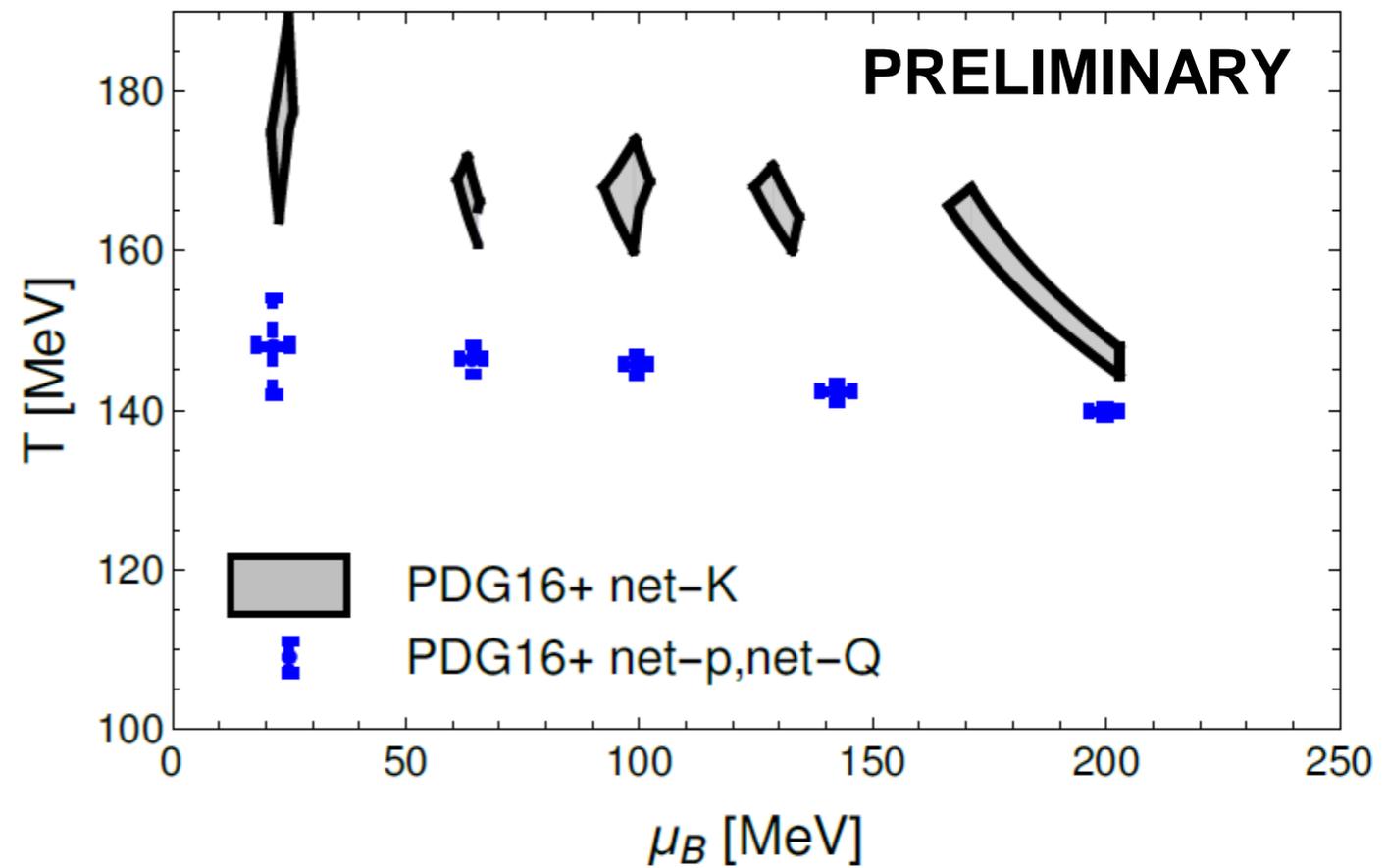
# Are these results very dependent on the HRG input ?



Are these results very dependent on  $\mu_B$ ?



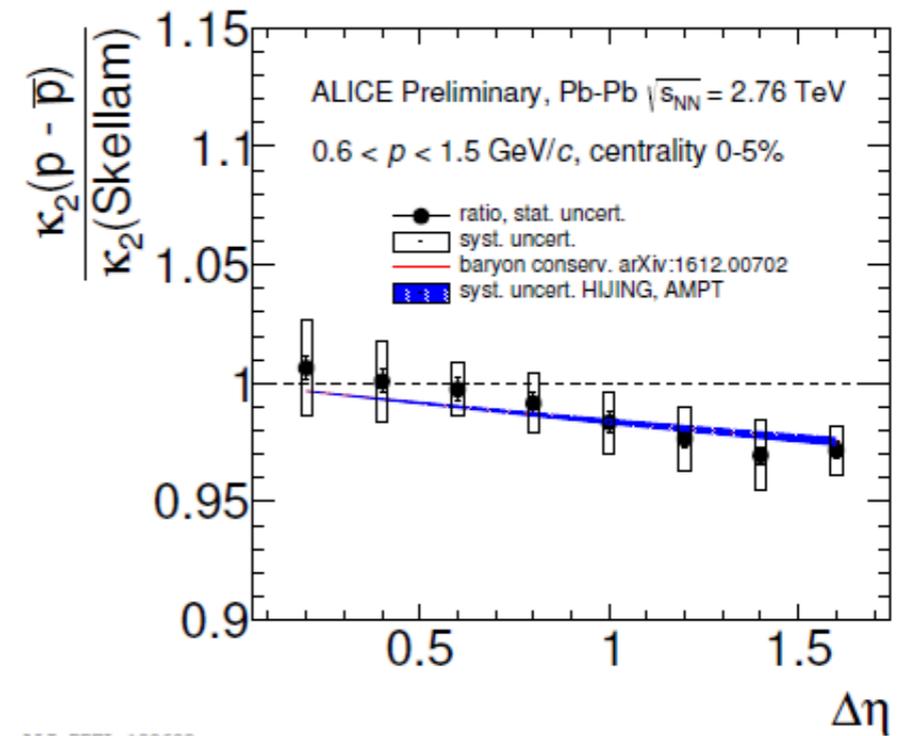
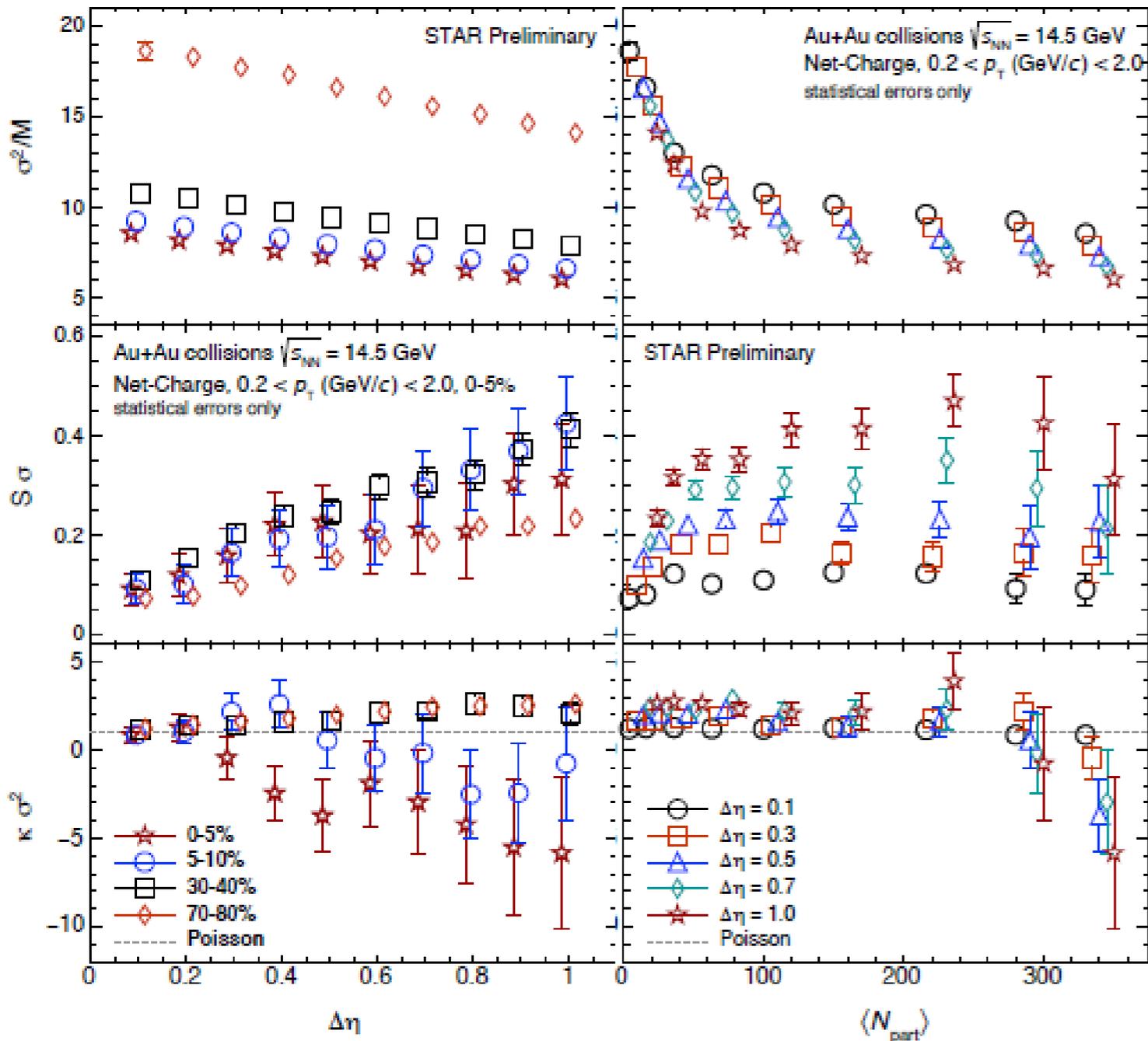
Pink bands based on lattice QCD isentropes



# Are these results very dependent on the acceptance ?

## Net-Charge – $\Delta\eta$ Dependence

*Au+Au collisions at  $\sqrt{s_{NN}} = 14.5$  GeV*



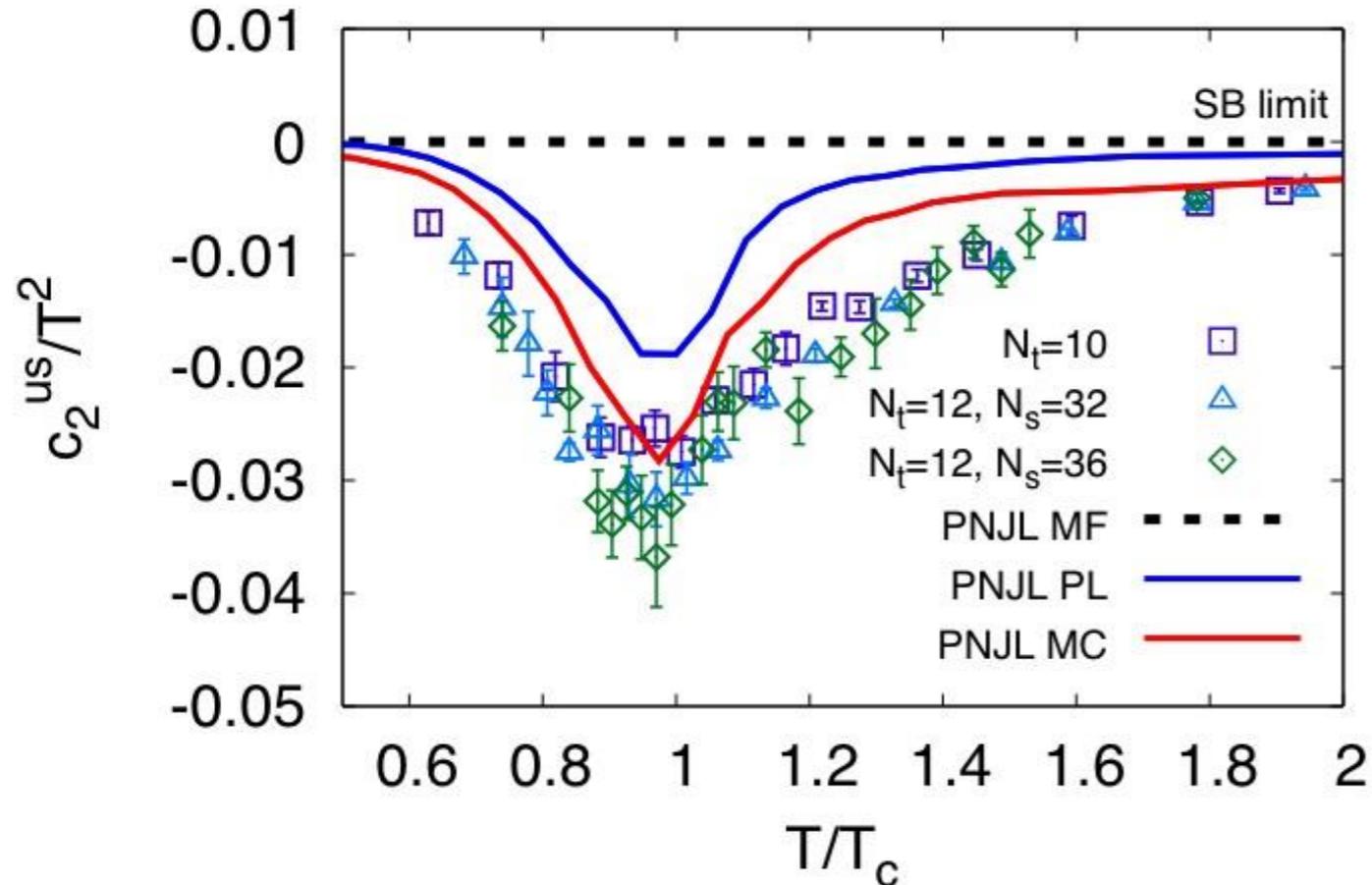
The effect of a limited acceptance (see Anar's talk) is mostly relevant for higher moments and on the few percent level for  $c_2$  and  $c_2/c_1$

There is a sweet spot between convergence to pure statistical fluctuations for small acceptance and charge conservation at large acceptance. The large coverage of STAR and ALICE should be at that sweet spot. More studies are necessary.

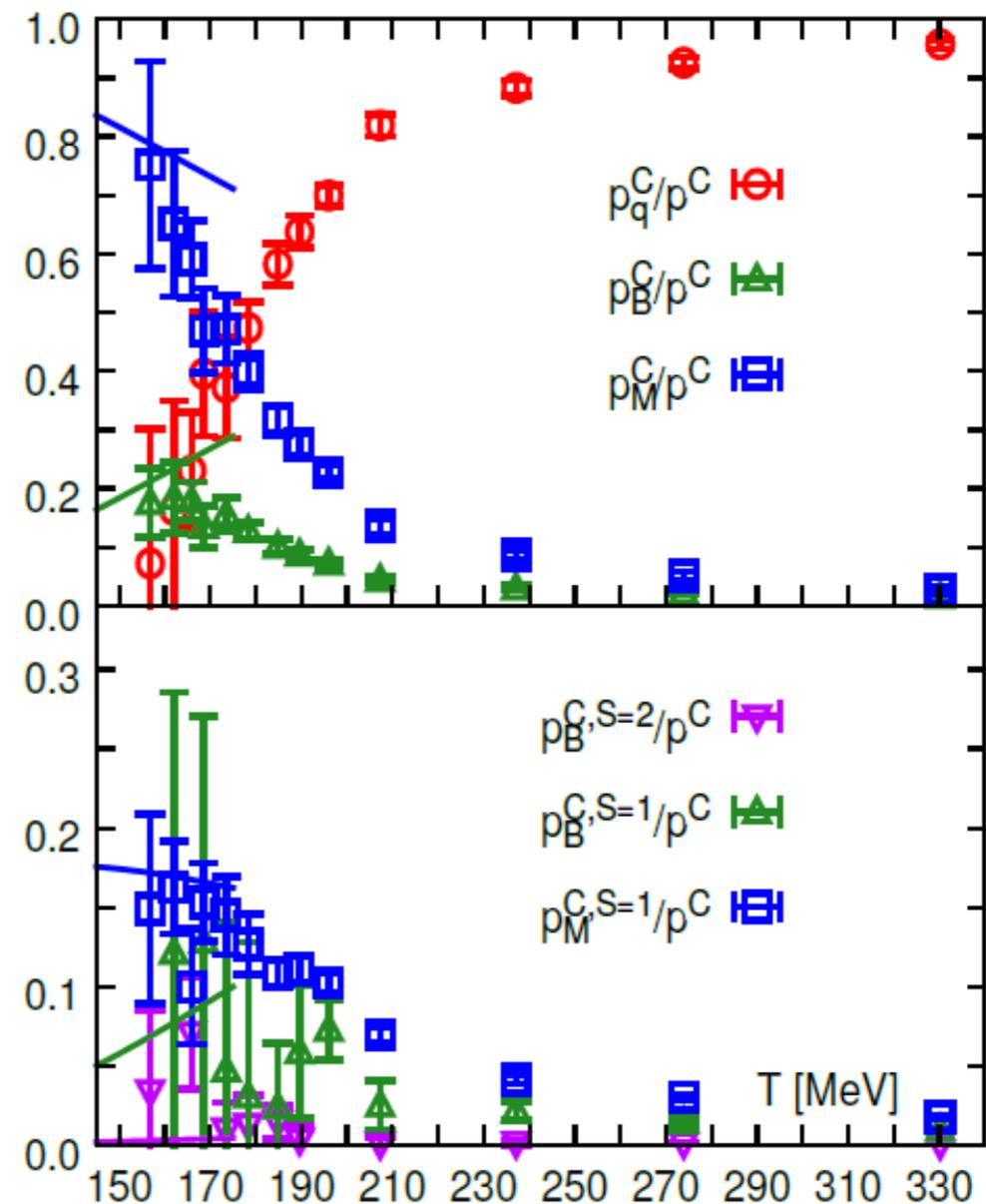
But from our HRG studies we can conclude that the effect in our results is negligible.

# Is there evidence from other lattice studies for a flavor dependence ?

Bound states in the strange sector  
(C. Ratti et al., PRD 85 (2012))



Bound states in the charm sector  
(S. Mukherjee et al., PRD 93 (2016))

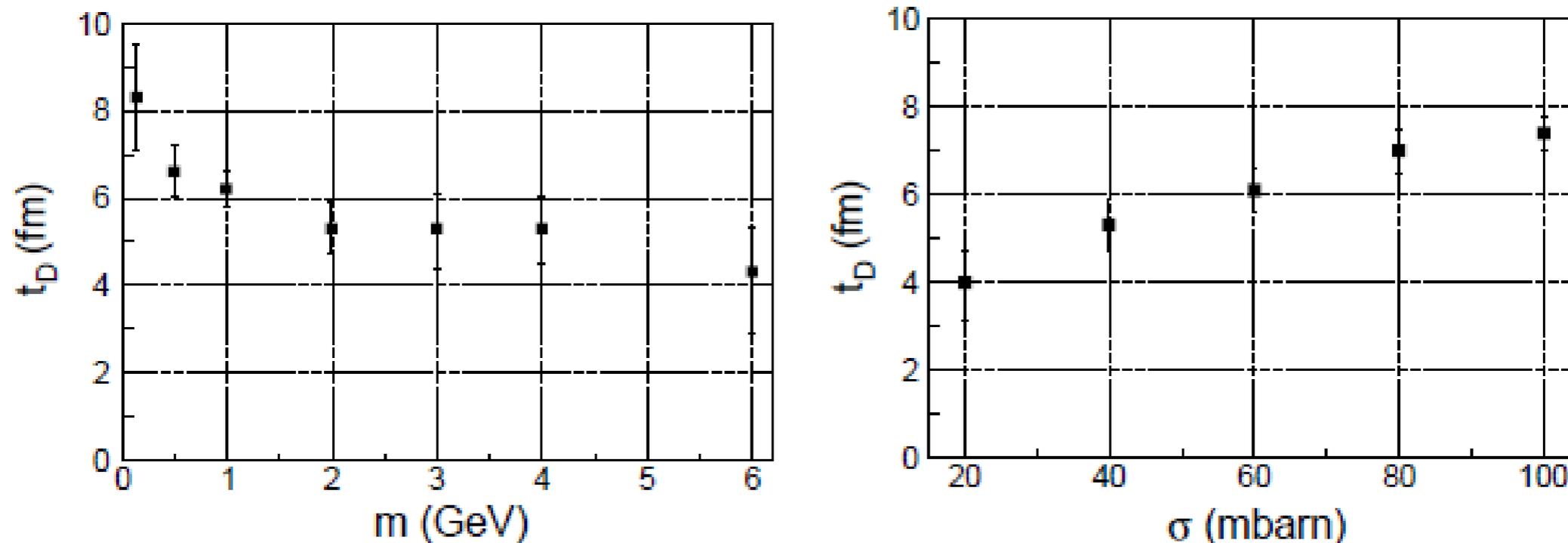


# Is there evidence from other studies for a flavor dependence ? (J.M. Torres-Rincon, SQM 2017)

Mott Temperature in PNJL to test transition T (hadron melting temperature)

|                  |       |           |          |         |          |            |          |          |
|------------------|-------|-----------|----------|---------|----------|------------|----------|----------|
| Meson            | $\pi$ | $K$       | $\eta$   | $\eta'$ | $\rho$   | $K^*$      | $\omega$ | $\phi$   |
| $T_{Mott}$ (MeV) | 282   | 286       | 245      | 0       | 253      | 266        | 253      | 382      |
| Baryon           | $p$   | $\Lambda$ | $\Sigma$ | $\Xi$   | $\Delta$ | $\Sigma^*$ | $\Xi^*$  | $\Omega$ |
| $T_{Mott}$ (MeV) | 254   | 269       | 195      | 287     | 223      | 231        | 239      | 288      |

New hadronic transport code SMASH to test chemical freeze-out T



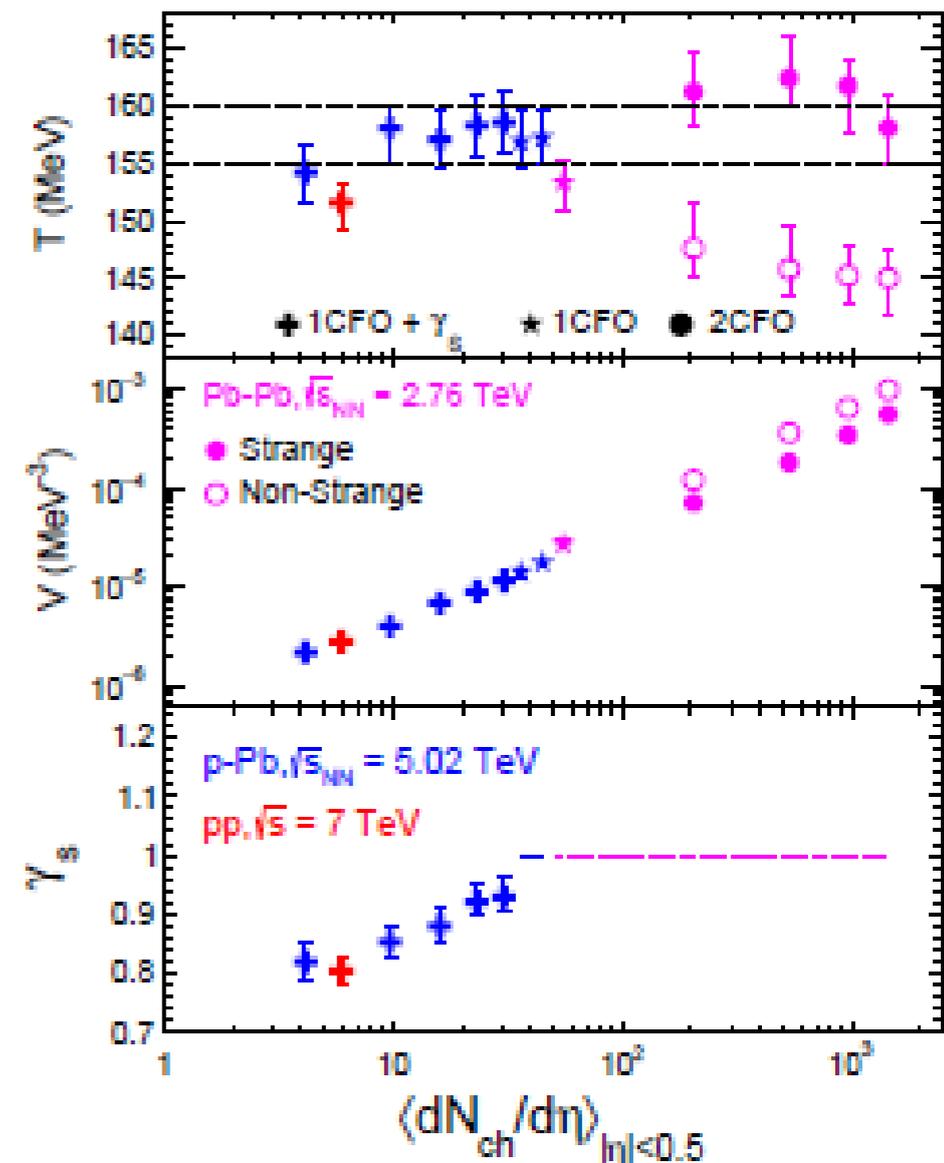
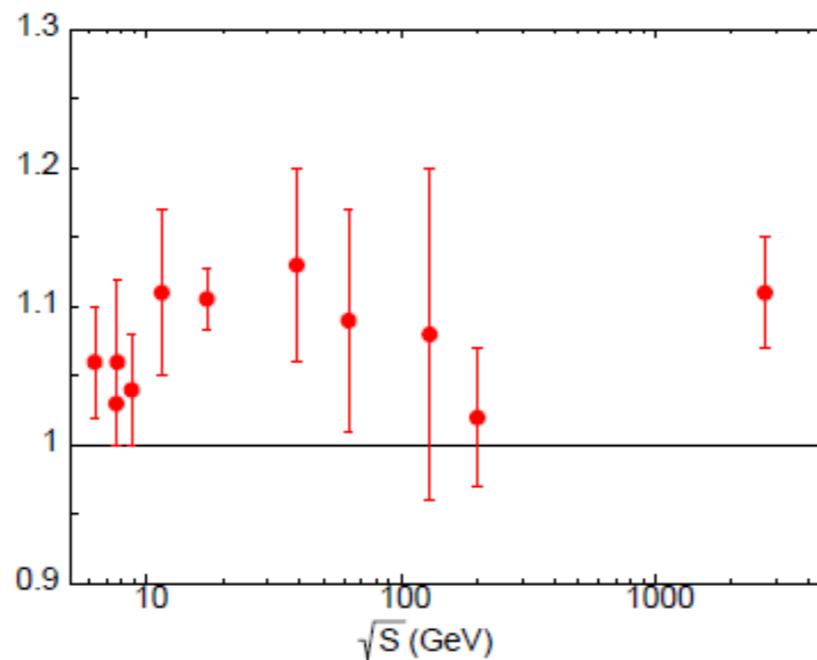
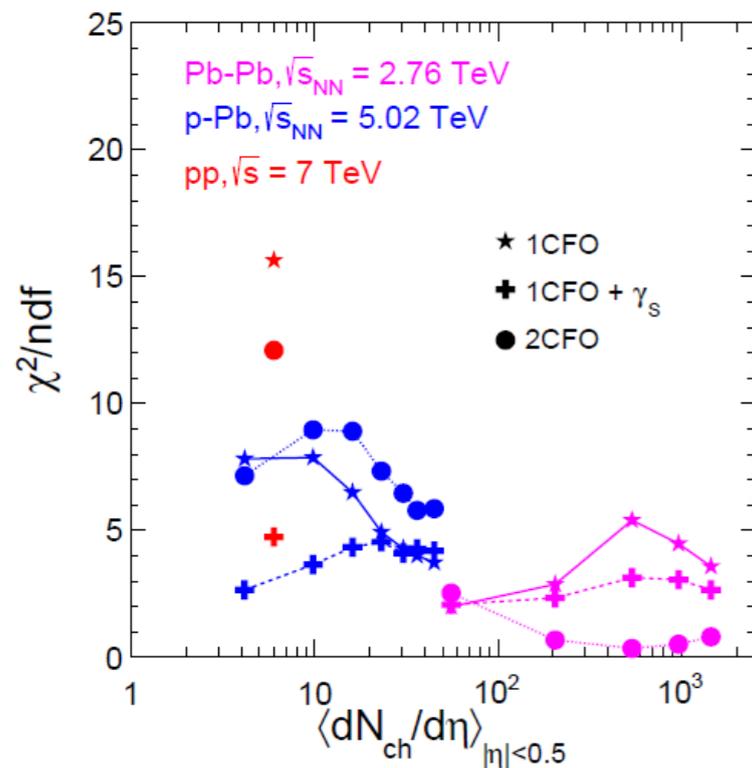
J. Tindall, JMTR, J.B. Rose and H. Petersen, PLB770 (2017) 532

Flavor dependence in this context could be synonymous with quark mass dependence

# Is there evidence from other studies for a flavor dependence ?

(S. Chatterjee, SQM 2017, see Bedanga's talk)

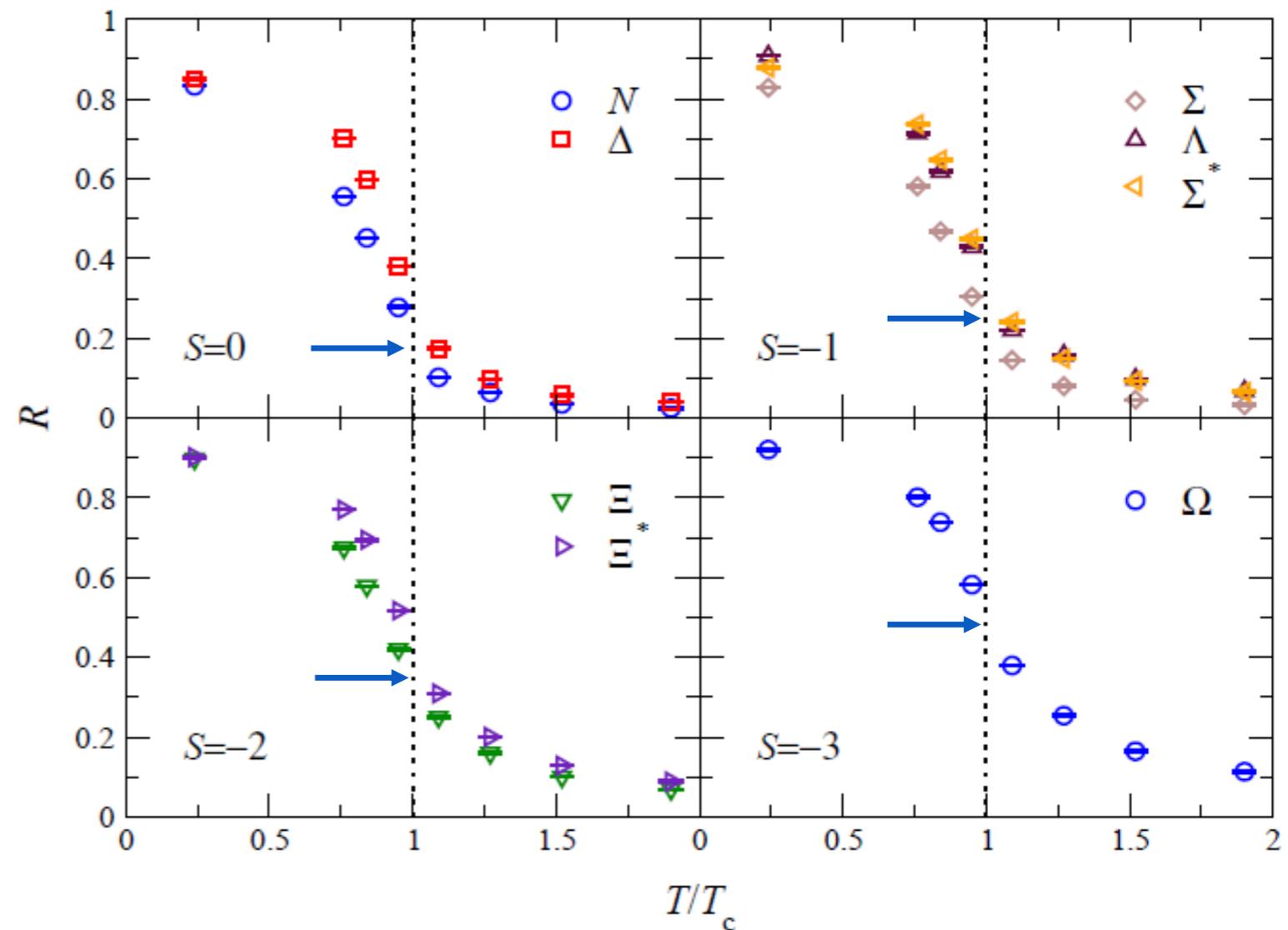
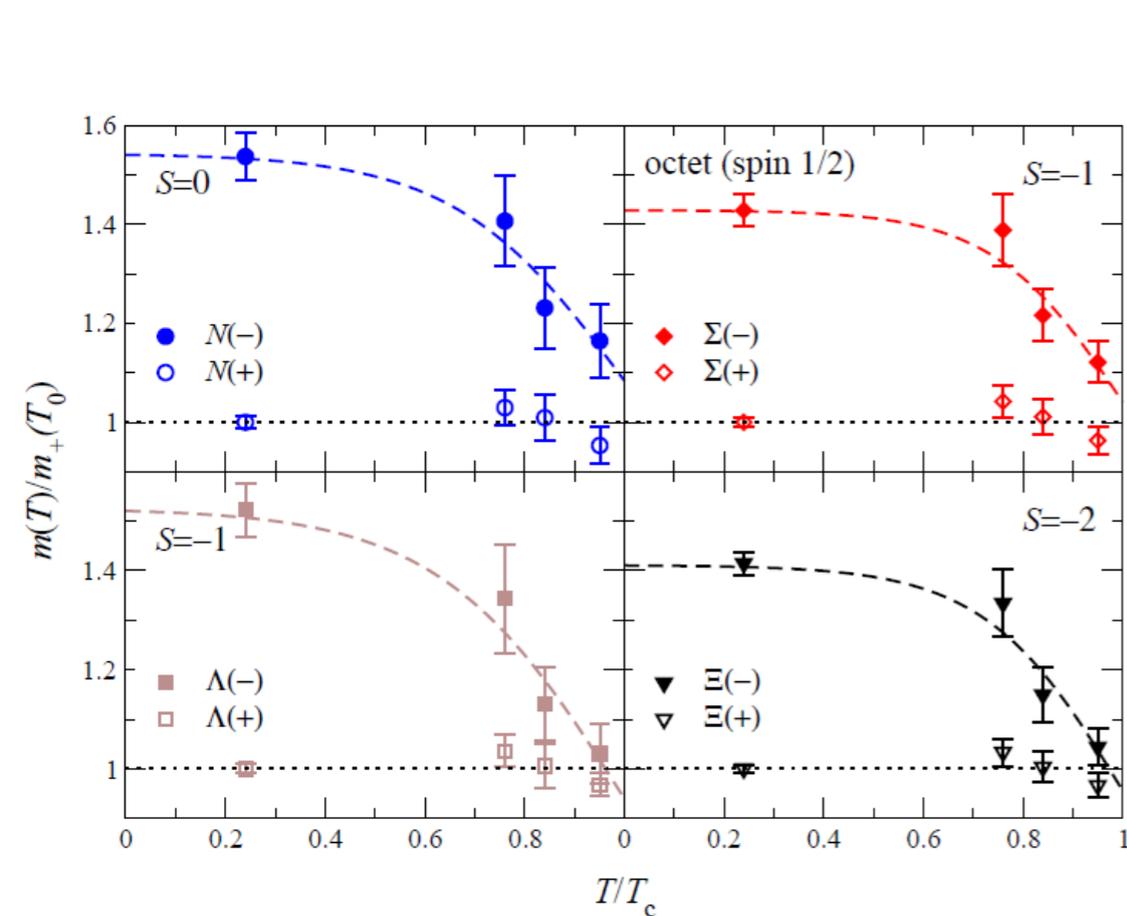
- A two freeze-out scenario will always improve the  $\chi^2/\text{ndf}$  (trivial)
- A two freeze-out scenario always yields higher T for strange than non-strange rather independent of collision energy
- A two-freeze-out scenario is only apparent in heavy ion collisions





# Is there evidence from other studies for a flavor dependence ? (G. Aarts, SQM 2017)

- Chiral symmetry restoration on the lattice (chiral partner merging)
- Heavier quarks push the bound states to higher temperature

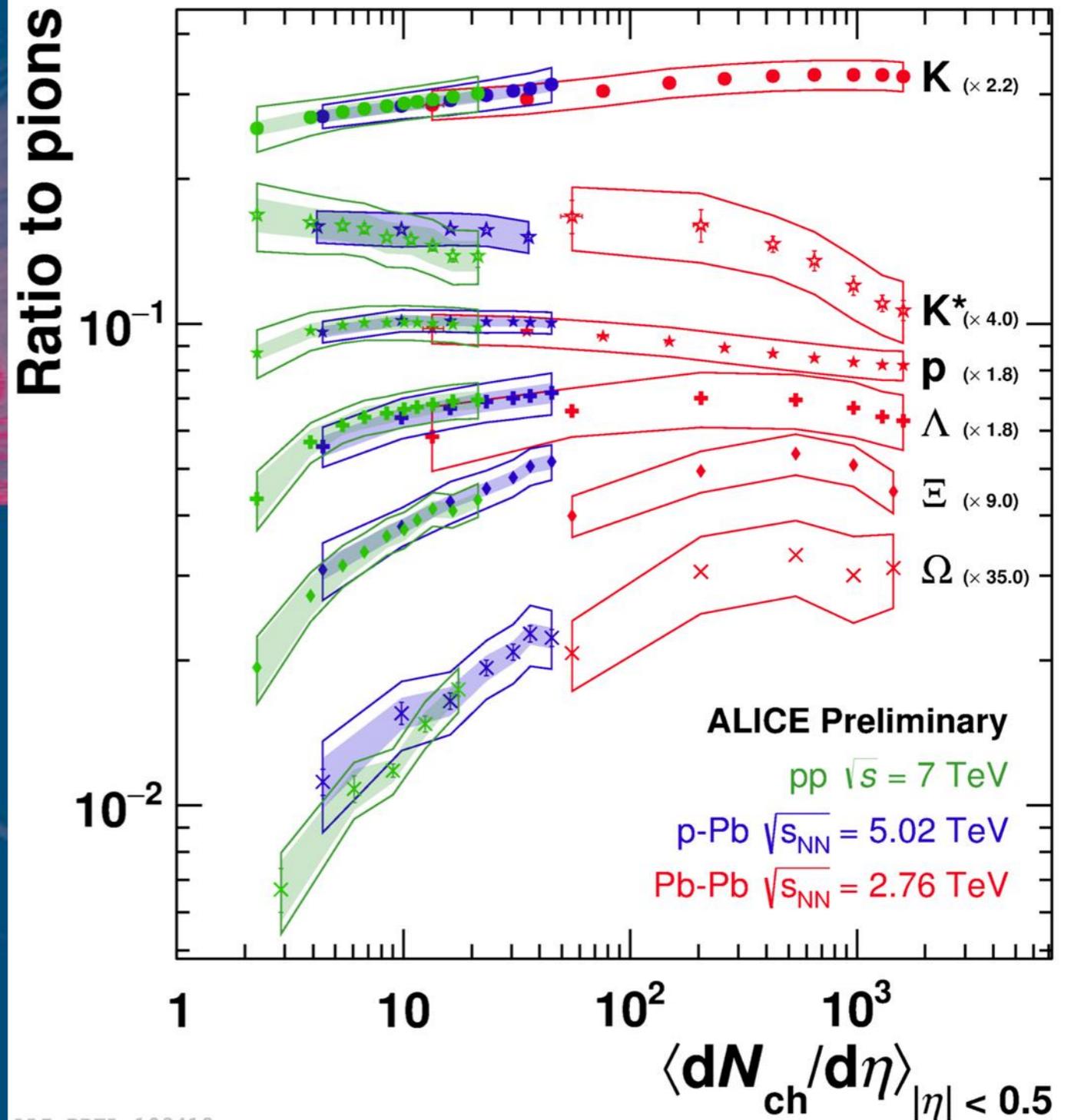
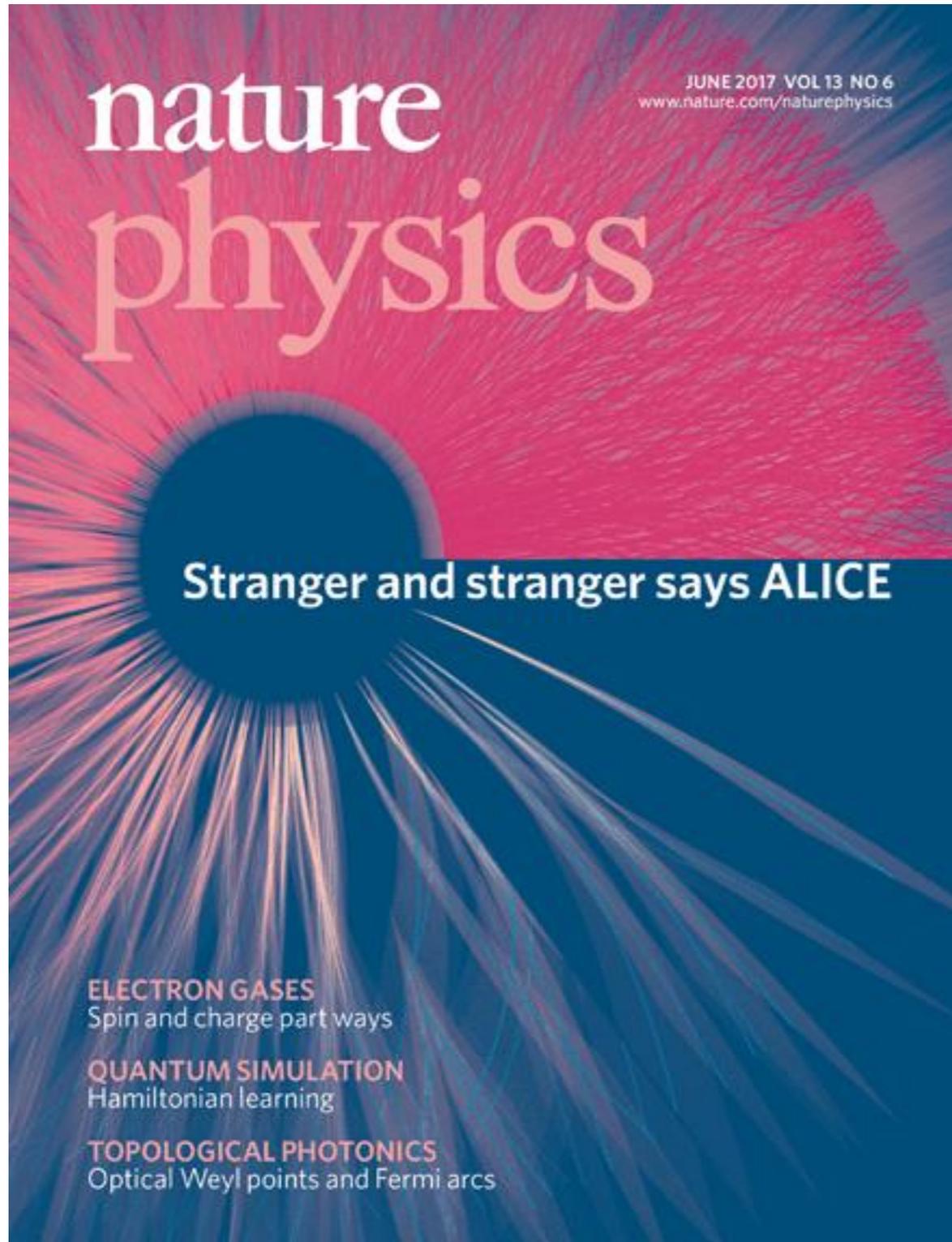


So let's assume there is a separate  
freeze-out hypersurface for strangeness –  
do we care ?

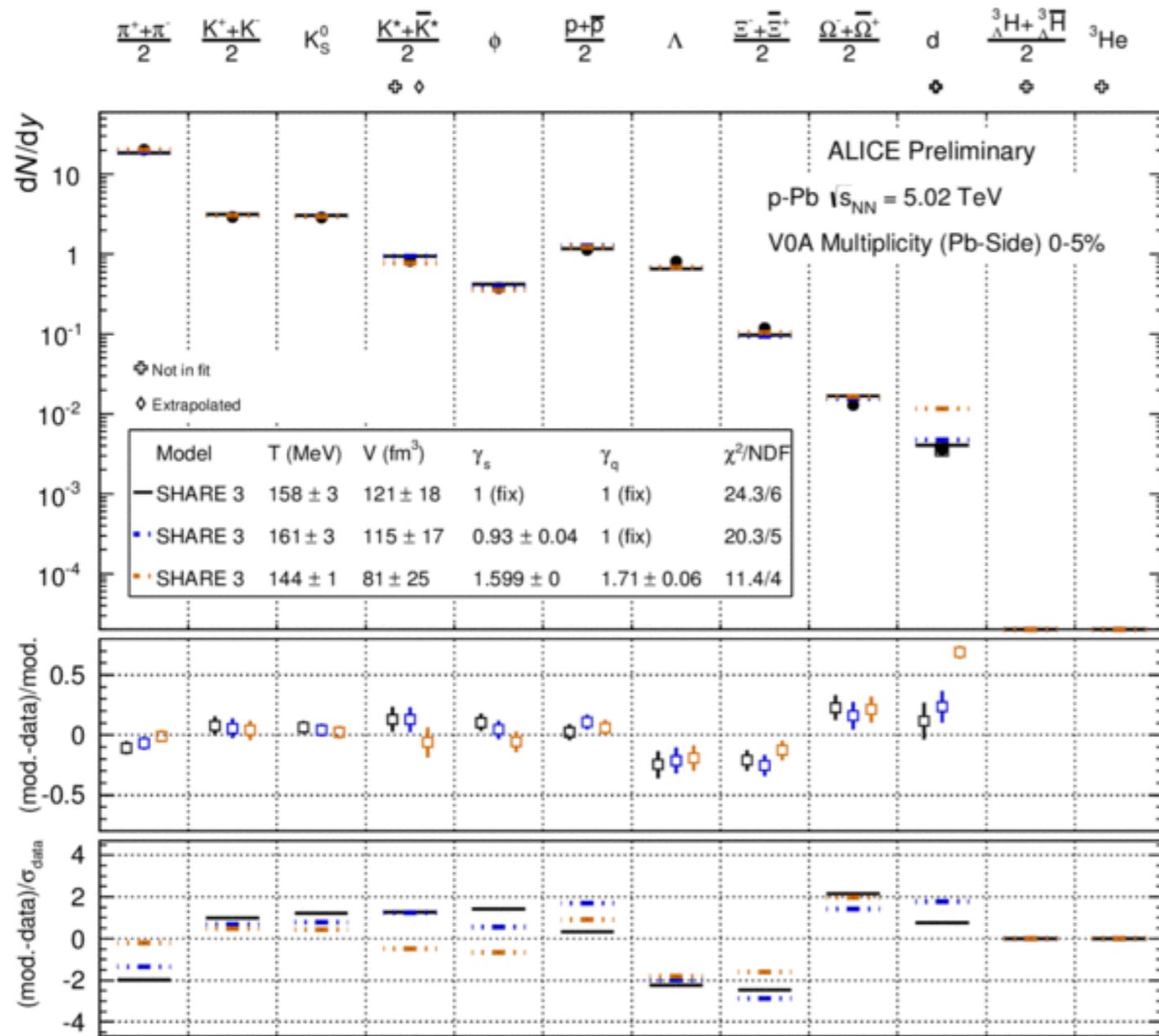
Strange matter creation ?:

- 1.) strangeness enhancement vs.  
suppression
- 2.) strange resonance formation
- 3.) exotica

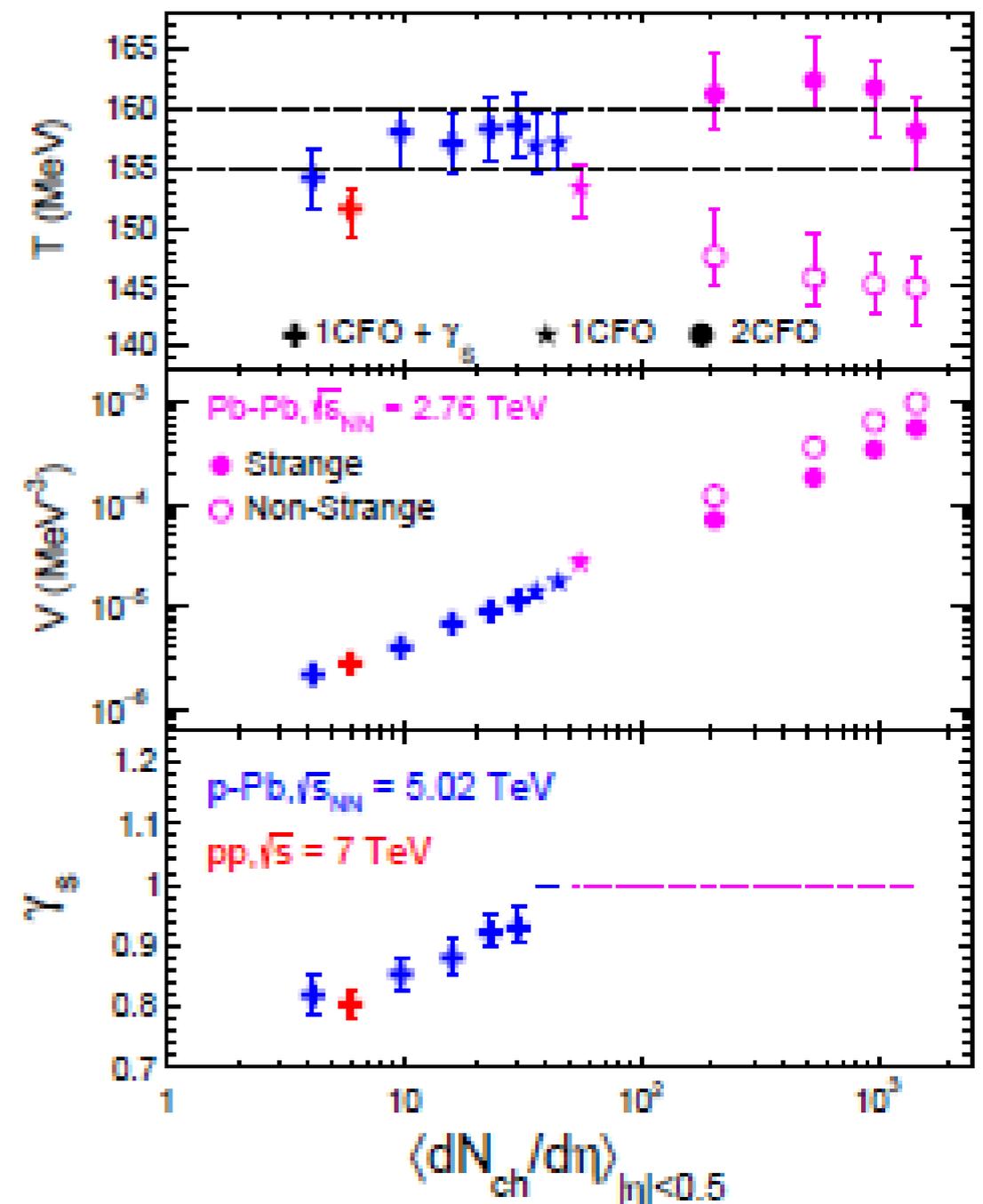
# Stranger and stranger from small to large systems (ALICE, arXiv:1606.07424), see talk by L.Bianchi



ALI-PREL-109418



Small systems chemistry  
(see Bedanga's talk on Tuesday)

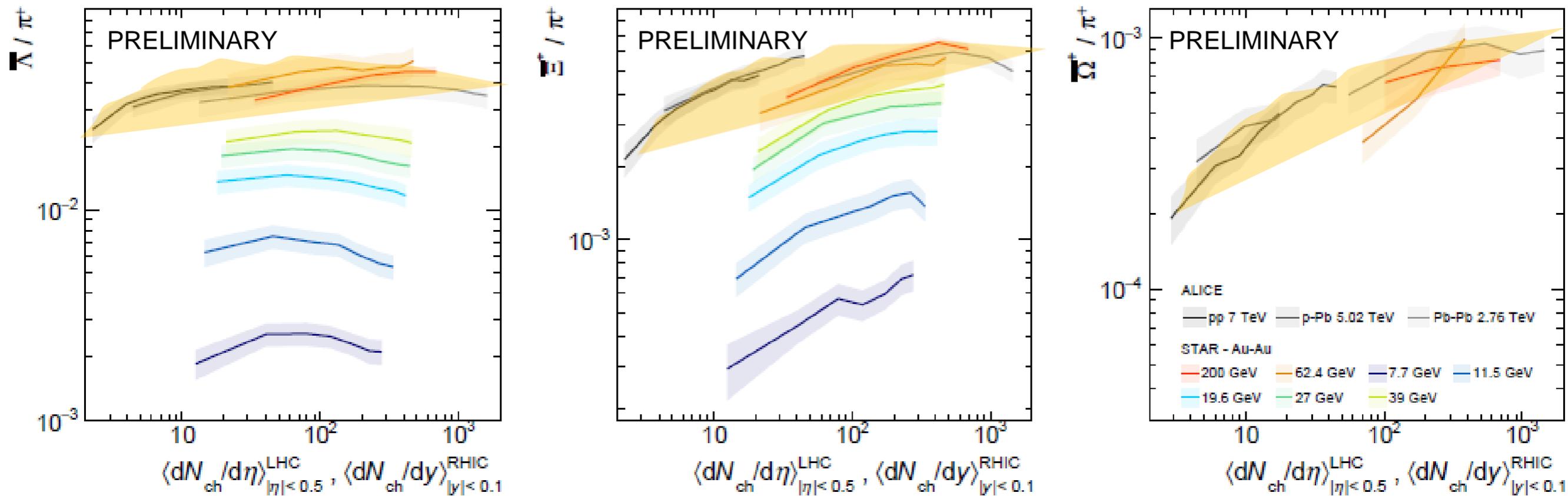


- HRG fit works rather well and yield similar T to PbPb fit (dependent on  $\gamma_s$ )
- Less evidence for flavor dependent freeze-out (Chatterjee, Dash, Mohanty, arXiv:1608.00643)

# Is it time to re-evaluate strangeness suppression/enhancement ?

Canonical suppression reduces as a function of energy and as a function of system size (Tounsi, Redlich (2001)). Is suppression over at LHC energies ?

Do we only see enhancement ? Can we distinguish ?

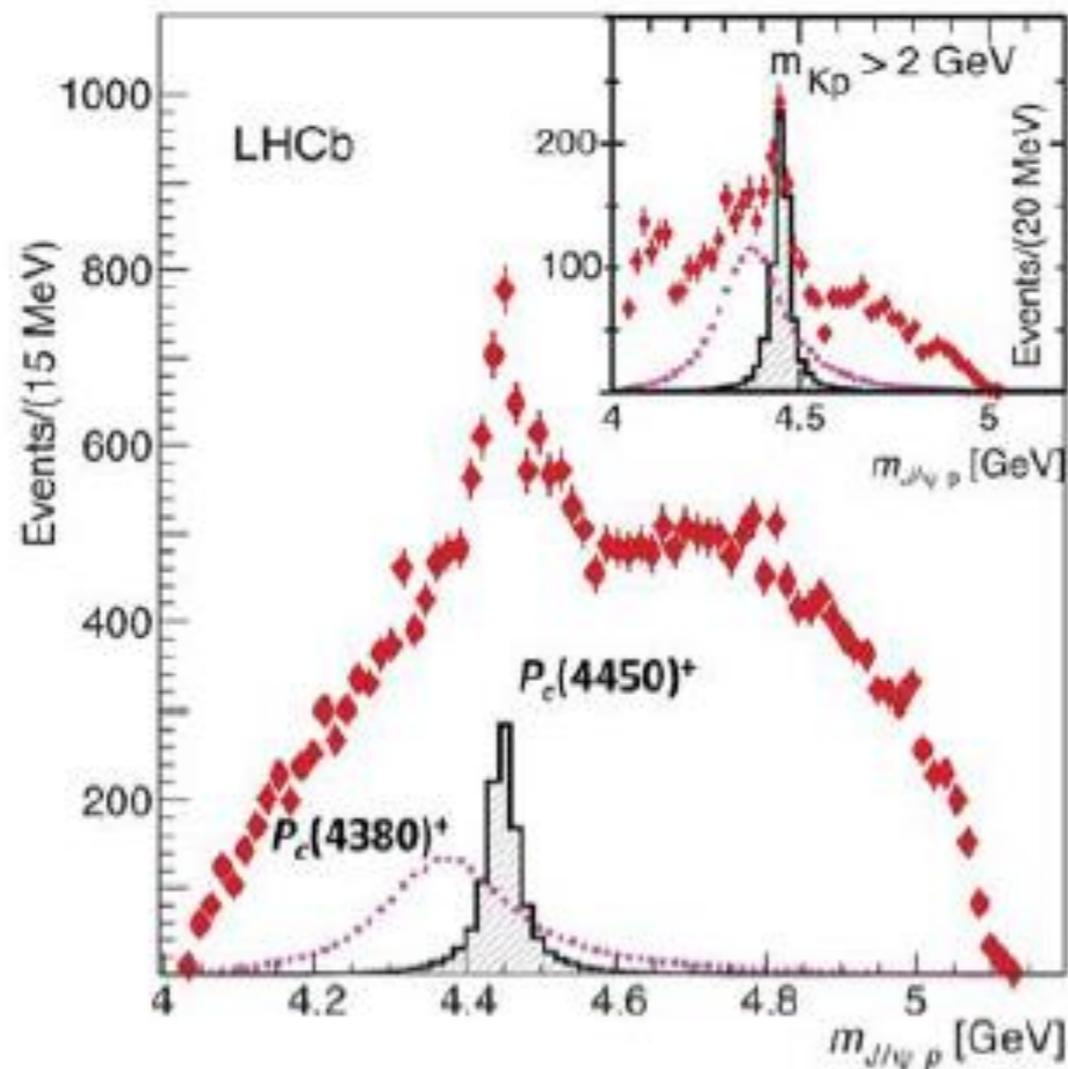


Above 39 GeV the curves seem to fall together, no more energy dependence. The volume dependence is still there ( $\gamma_s$  dependence ?). A higher T freeze-out surface in PbPb will lead to actual strangeness enhancement

# Exotica: Penta- and Tetra-quarks from LHCb

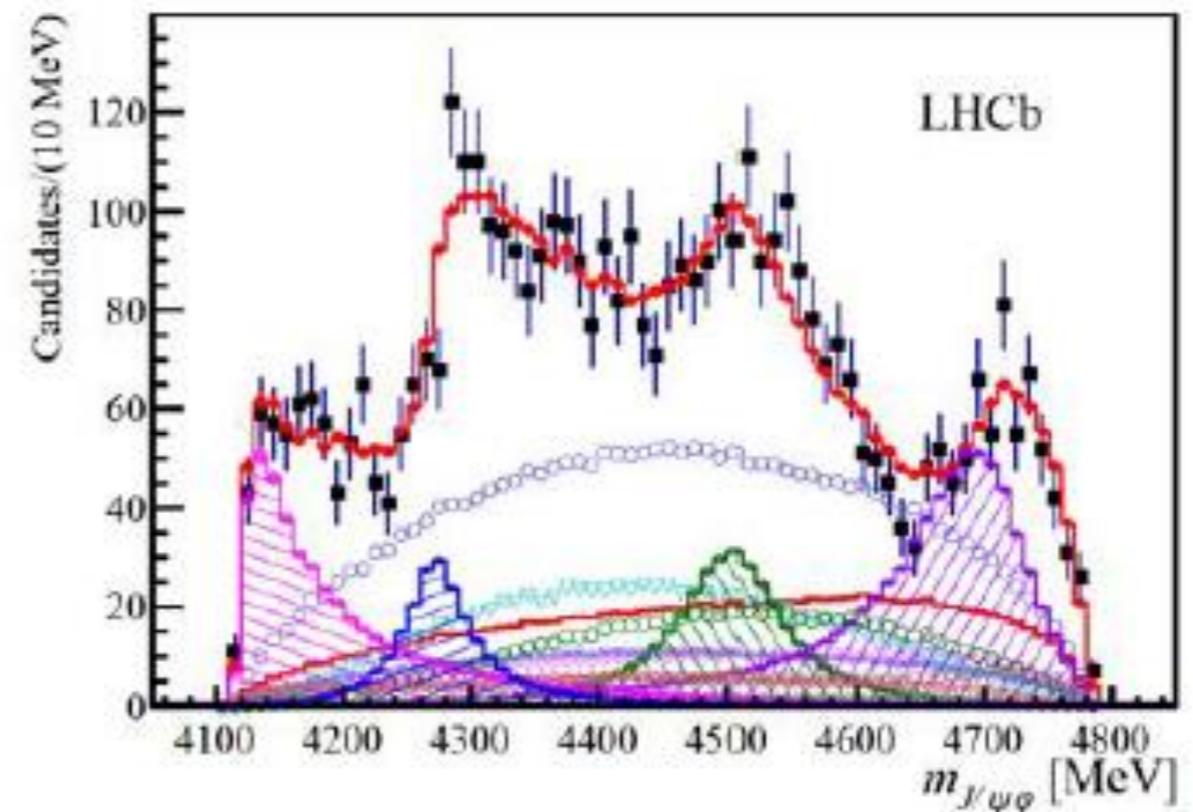
Penta-quark in 2015,  $9\sigma$  evidence by 2016

In the charm sector:  $J/\psi$  p resonance  
In  $\Lambda_b$  decays to  $J/\psi$  p  $K^-$



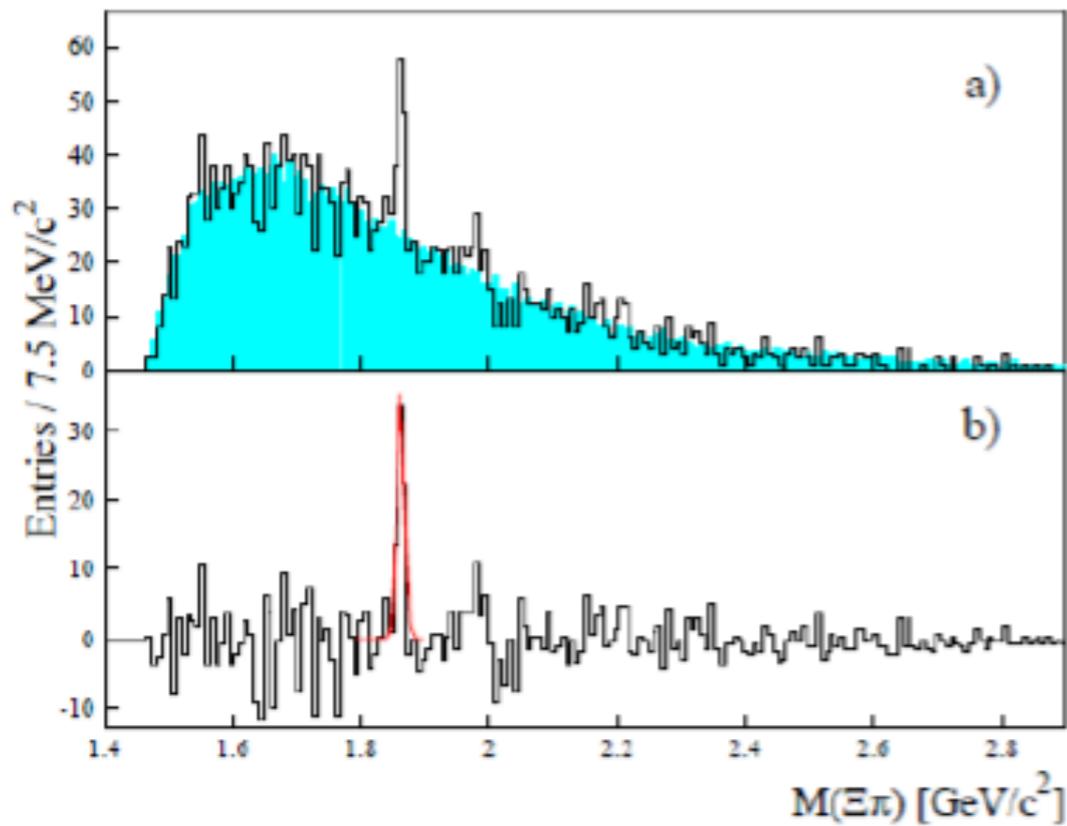
Tetra-quarks in 2016

In the charm sector:  $J/\psi$   $\phi$  resonance  
In  $B^+$  decays to  $J/\psi$   $\phi$   $K^+$



Why nothing in the strange sector ?

# Exotica in strange sector ?

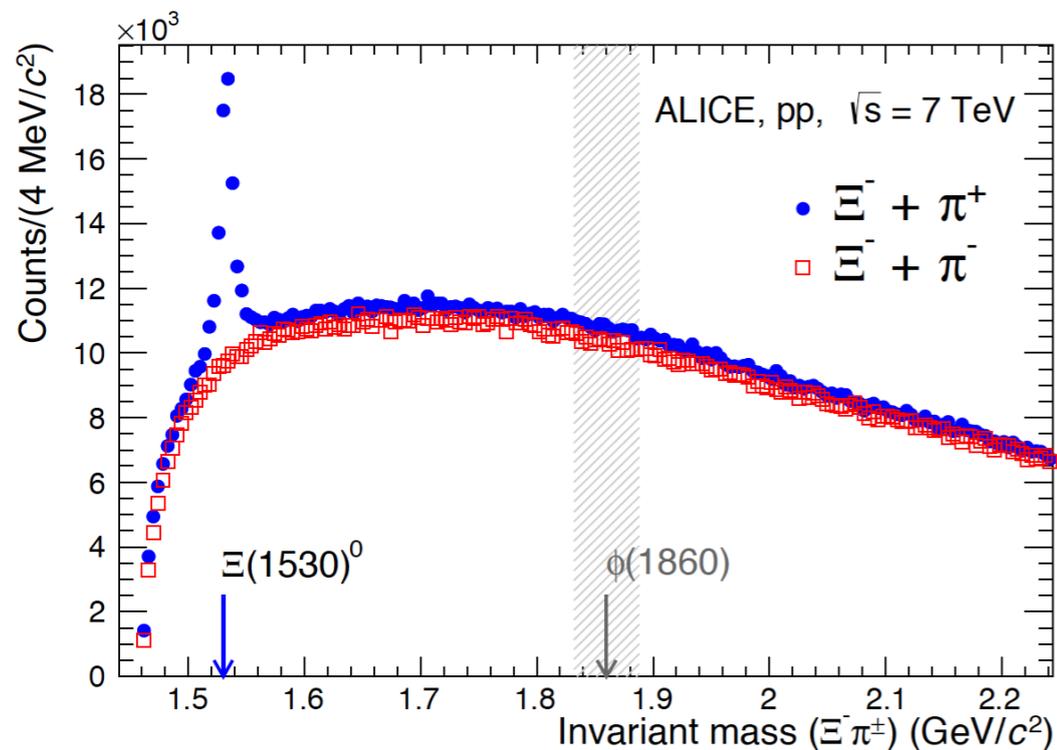


Famous pentaquark candidate from NA49 (2008) in  $\Xi\pi$  channels ( $\phi(1860)$ ) ( $dsds\bar{u}$ )  
Never retracted, never confirmed

No evidence for H-dibaryon or  $\phi(1860)$  in ALICE data.

Maybe we are looking in the wrong channels. In the charm sector all tetra- and penta-quarks seem to require closed charm components.

Keep looking !!



# Conclusions / Outlook

- High precision (continuum limit) lattice QCD susceptibility ratios indicate *flavor separation in the crossover from the partonic to the hadronic matter*.
- There are hints, when comparing to hadron resonance gas and PNJL calculations, that this could lead to a short phase during the crossover in which strange particle formation is dominant.
- If the abundance of strange quarks is sufficiently high (LHC) this could lead to *enhancements in the strange hadron yields (evidence from ALICE)* and it could lead to *strangeness clustering (exotic states: dibaryons, strangelets)* or *higher mass strange Hagedorn states* (as predicted by Quark Models).
- Dynamic quantities that evolve during the deconfined phase will be affected as long as the hadronization temperature plays a significant role, i.e. quark phase is shortened for heavier flavors, which could explain flavor effects in  $R_{AA}$  if energy loss builds up near  $T_c$ .
- Ongoing project (UH Theory Group): The phases can be linked in a hydrodynamic calculation by using a mixed EOS from lattice and HRG with varying flavor-dependent switching temperatures.