

Extracting anisotropic μ -type spectral distortions

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Remazeilles & Chluba

[arXiv:1802.10101](https://arxiv.org/abs/1802.10101)

*“Probing fundamental physics with CMB spectral distortions”
CERN TH Institute, 12-16 Mar 2018*

μ -type CMB spectral distortions

Sunyaev
& Zeldovich
1970

- At redshifts $10^4 < z < 2 \times 10^6$ (pre-recombination), energy injections into primordial plasma prevent brehmsstrahlung and double Compton scattering to create photons to maintain Planck's equilibrium, leading to Bose-Einstein equilibrium:

$$n_{BE} \approx n_{PI} + \mu \frac{e^x}{(e^x - 1)^2} \left(\frac{x}{2.19} - 1 \right) \quad x \equiv h\nu / kT_{CMB}$$

CMB blackbody spectrum *spectral signature of μ -distortion*

- Caused by exciting physics processes occurring at redshifts $z > 10^4$:
 - *dissipation of small-scale acoustic modes* – Silk 1968
 - *annihilation/decay of relic particles* – Hu & Silk 1993
 - *evaporation of primordial black holes* – Carr et al 2010
- LCDM predicts: $|\mu| = 2.3 \times 10^{-8}$ → very faint signal! – Chluba 2016
- COBE/FIRAS constraint: $|\mu| < 9 \times 10^{-5}$ – Fixsen et al 1996

Anisotropic μ -type distortions

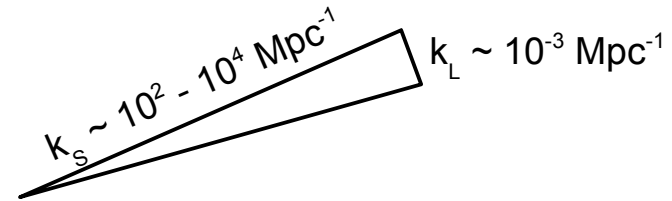
Pajer & Zaldarriaga 2012
 Ganc & Komatsu 2012
 Chluba et al 2017
 Ravenni et al 2017

Aside from CMB monopole distortions...

Primordial non-Gaussianity in the ultra-squeezed limit predicts:

- Anisotropies of μ -type distortions (*spectral-spatial distortions*):

$$C_{\ell}^{\mu \times \mu} = 144 C_{\ell}^{TT, SW} f_{NL}^2 \langle \mu \rangle^2$$



- μ -T correlations between CMB temperature and μ -distortion anisotropies:

$$C_{\ell}^{\mu \times T} = 12 C_{\ell}^{TT, SW} \rho(\ell) f_{NL} \langle \mu \rangle$$

- **Scale-dependent** $f_{NL}(k) = f_{NL}(k_0)(k/k_0)^{n_{NL}-1}$ with running index of $n_{NL} \leq 1.6$ would allow for:

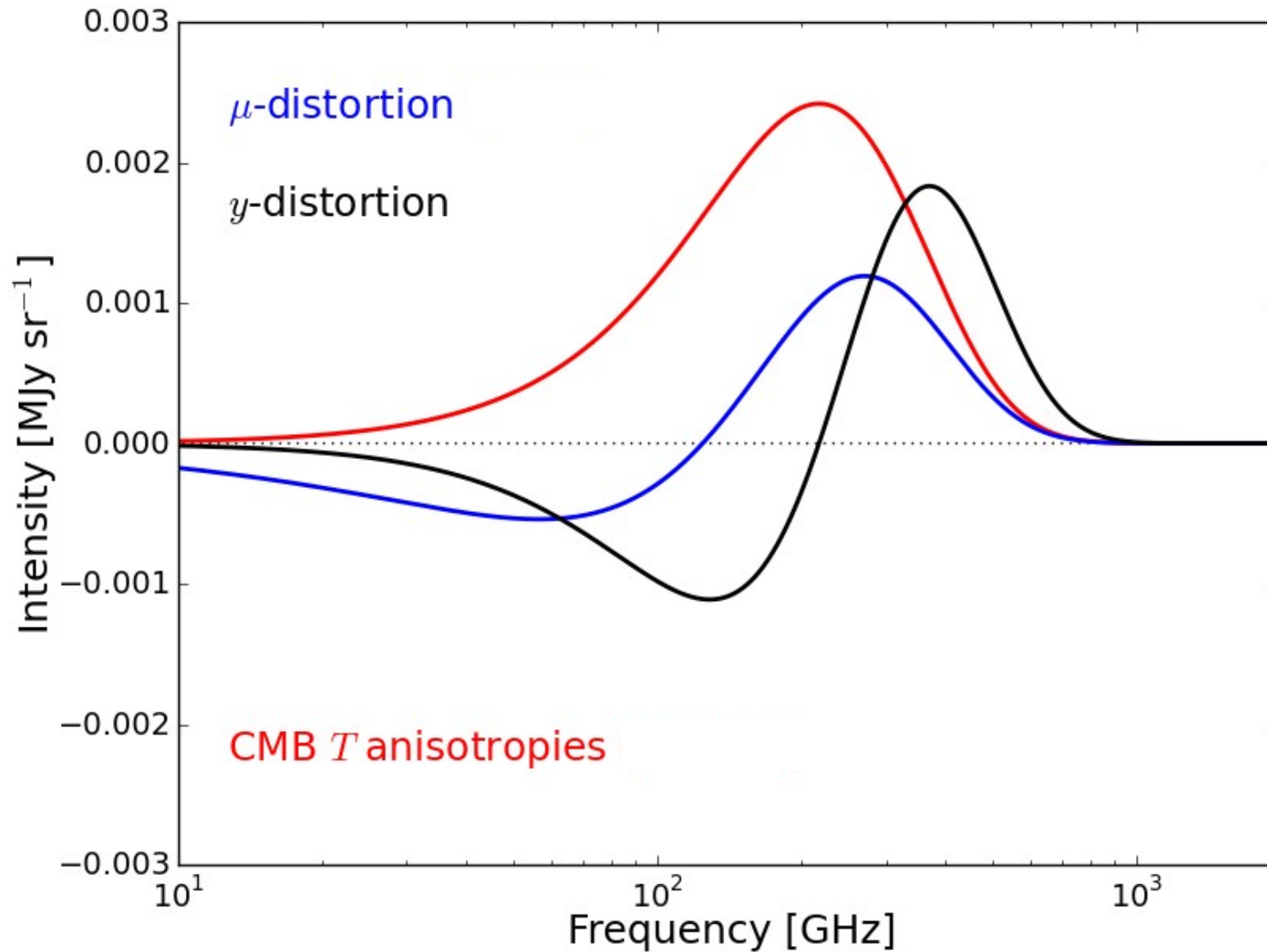
$$f_{NL}(k_0 = 0.05 \text{ Mpc}^{-1}) \approx 5 \quad \leftarrow \text{CMB temperature anisotropies}$$

$$f_{NL}(k = 740 \text{ Mpc}^{-1}) \approx 4500 \quad \leftarrow \mu\text{-type distortion anisotropies}$$

Questions

- *Can we detect the μ - T correlated signal with future CMB satellites?*
- *What limit on f_{NL} ($k=740 \text{ Mpc}^{-1}$) can be achieved in the presence of foregrounds?*

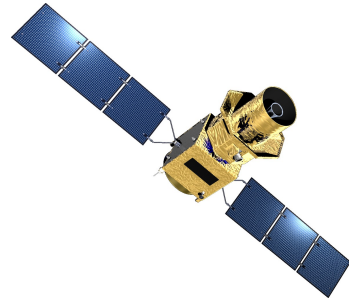
Spectral signature of distortions



Distinct spectral signatures!

→ Multi-frequency observations allow (in principle) to disentangle those signals

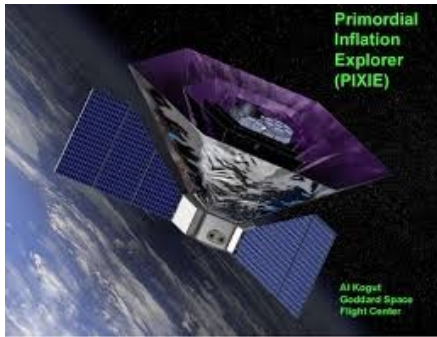
CMB satellite concepts



LiteBIRD (JAXA)

Matsumura et al, 2013

40 – 402 GHz ; 2.5 μ K.arcmin



PIXIE (NASA?)

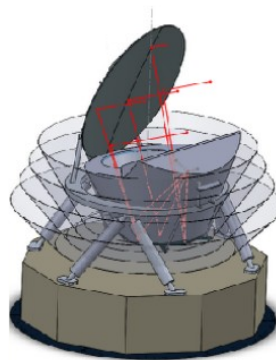
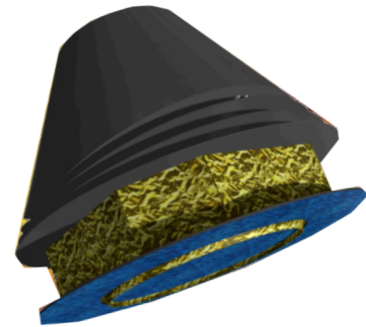
Kogut et al., 2011

**30 – 6000 GHz ;
6.6 μ K.arcmin ($\Delta\nu=30$ GHz)**

CORE (ESA? ISRO?)

Delabrouille et al, 2017

60 – 600 GHz ; 1.7 μ K.arcmin

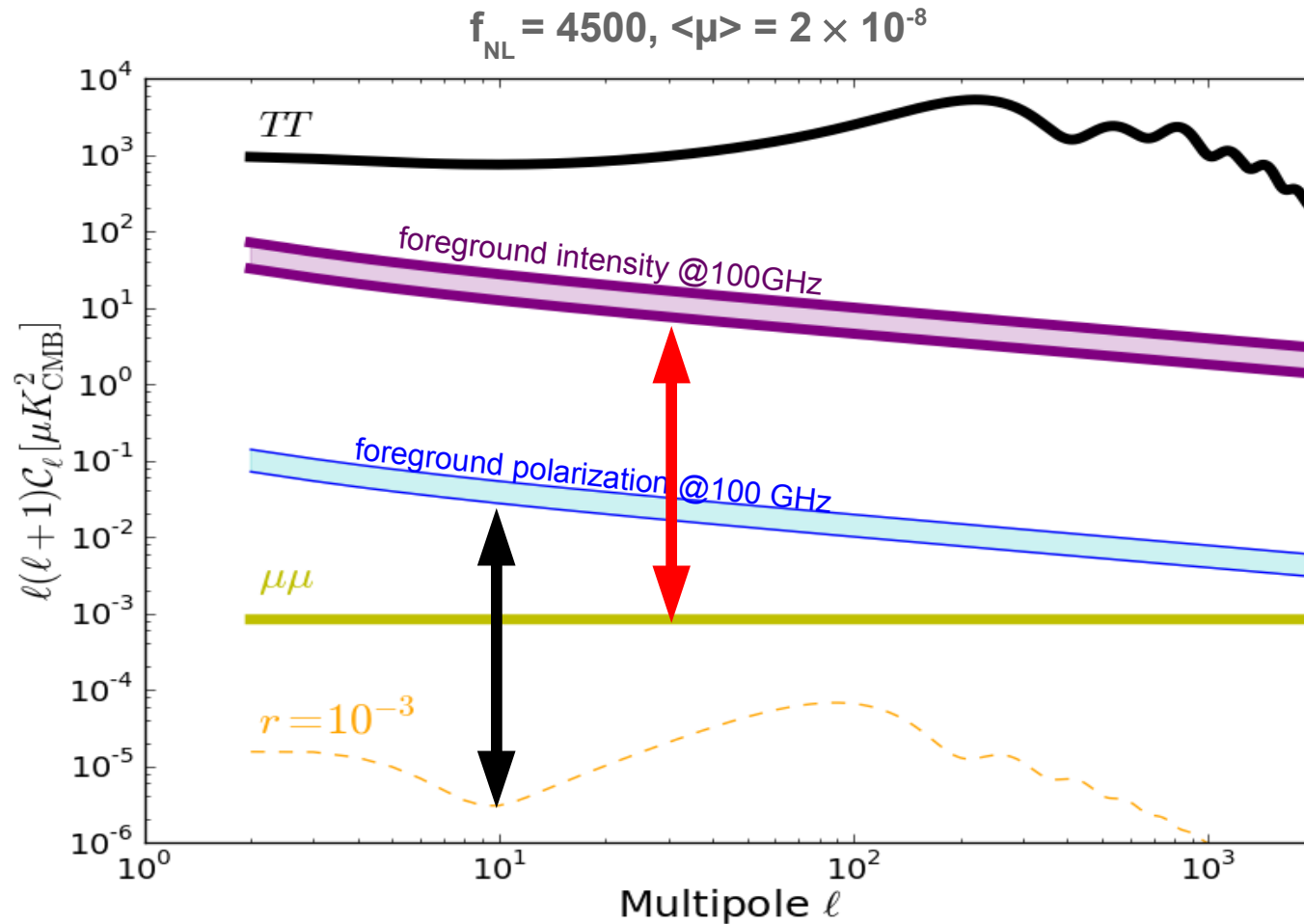


PICO (NASA?)

S. Hannany, priv. comm.

21 – 800 GHz ; 1.1 μ K.arcmin

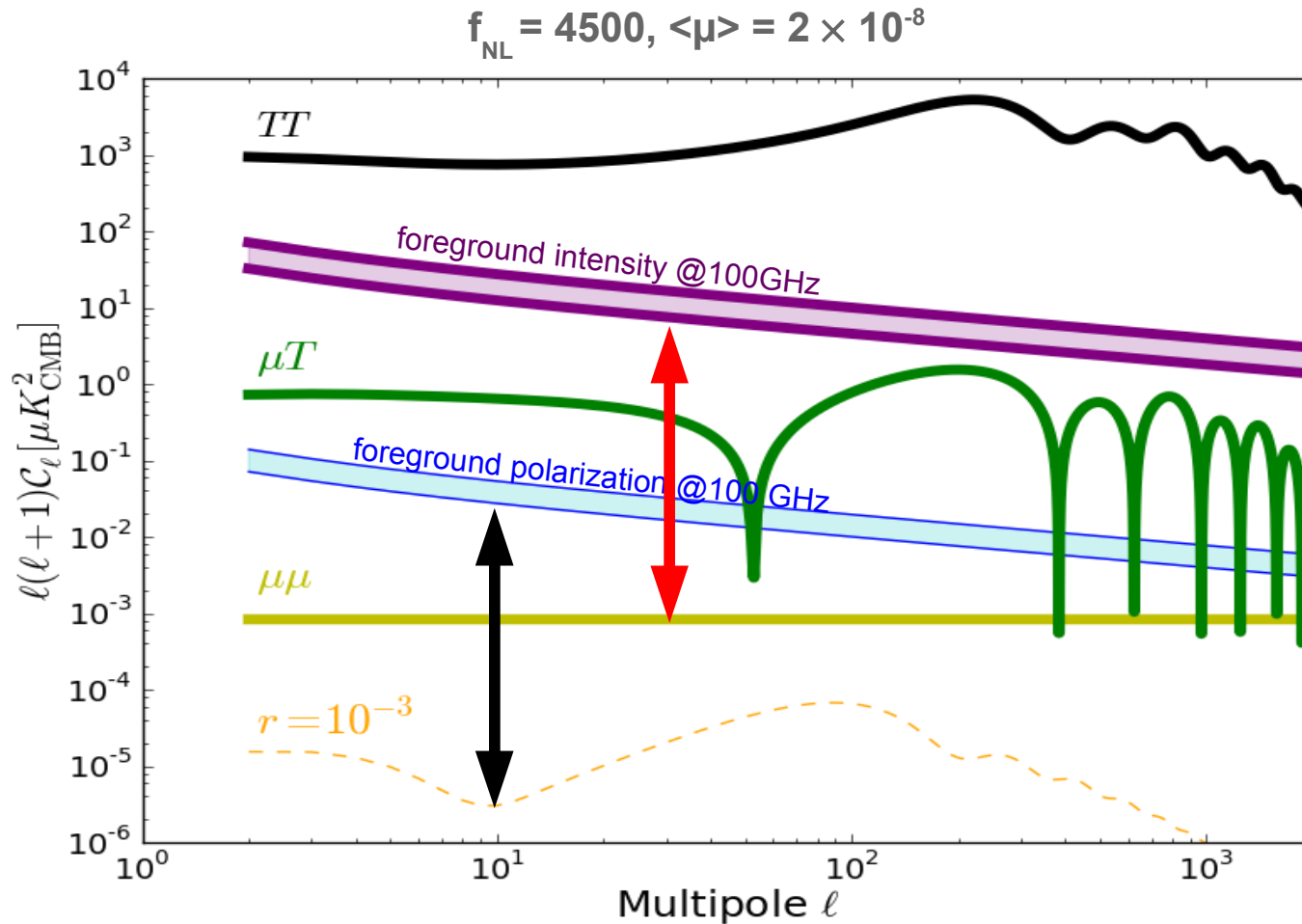
Anisotropic primordial spectral distortions



Similar dynamic range between signal and foregrounds than primordial B-modes at $r \sim 10^{-3}$

→ to be definitely considered by future CMB satellites...

Anisotropic primordial spectral distortions

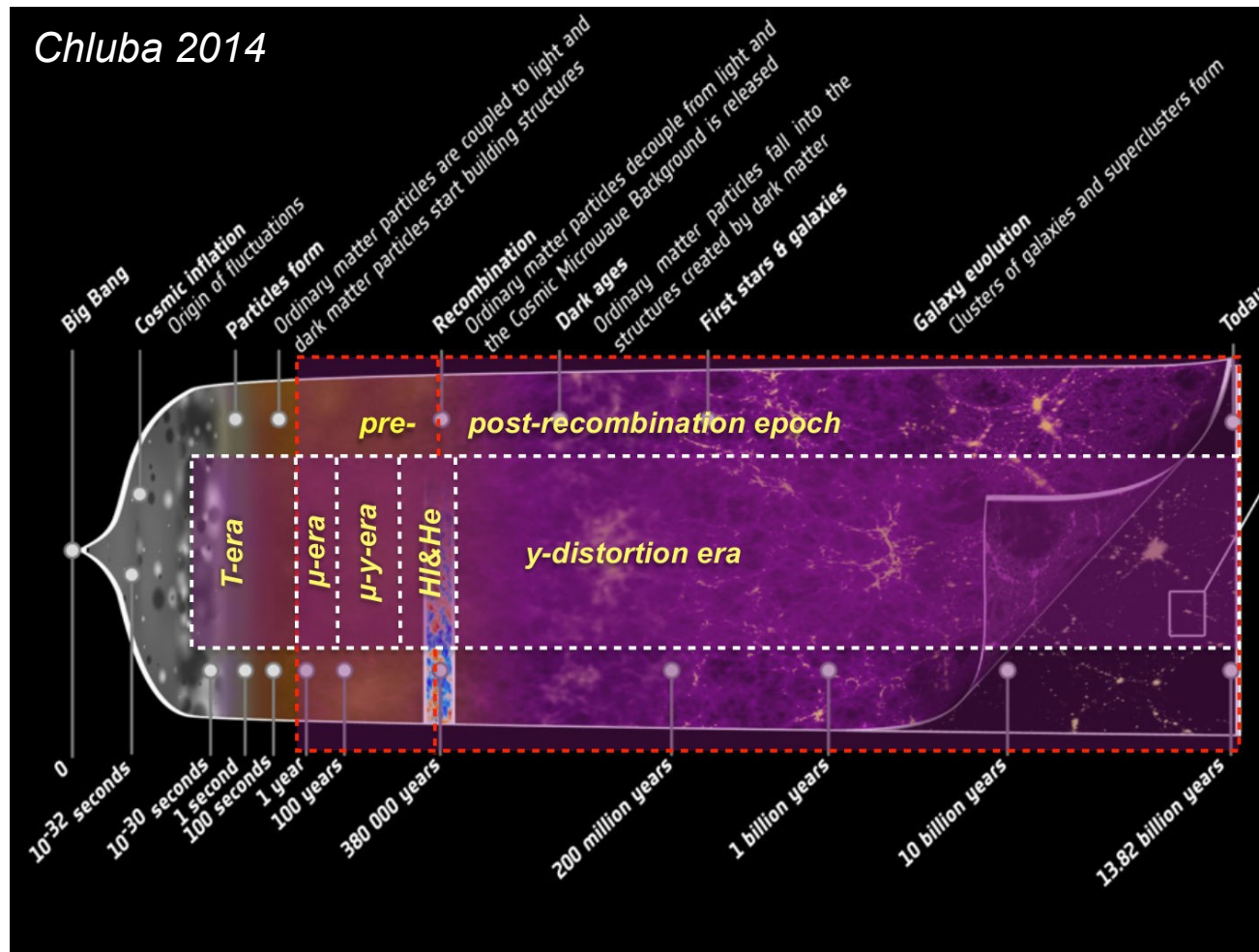


μ -T correlation signal between CMB temperature and μ -distortion anisotropies

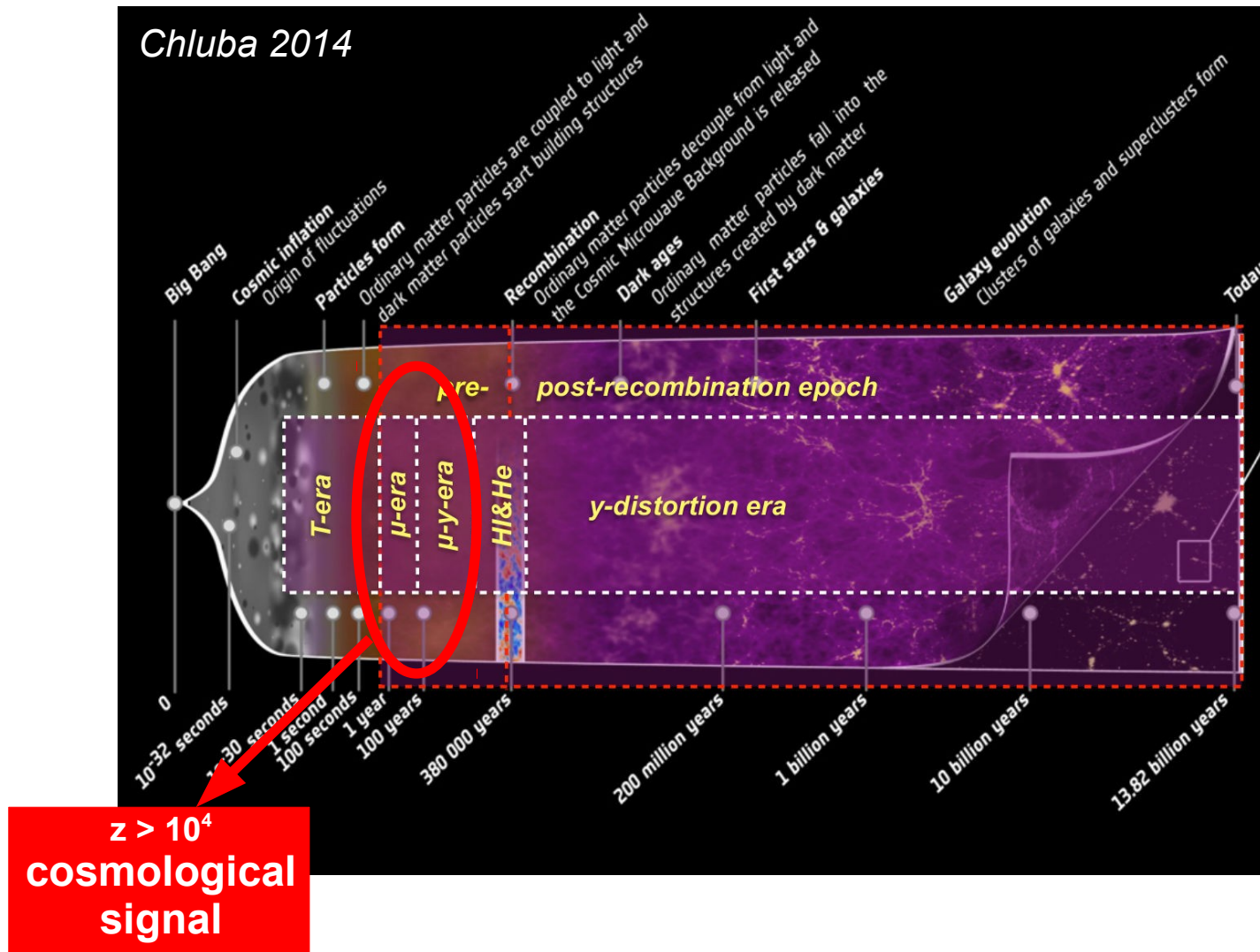
→ even more accessible signal, allowing to constrain f_{NL} ($k \approx 740 \text{ Mpc}^{-1}$)

→ to be definitely considered by future CMB satellites...

Cosmic history of CMB spectral distortions

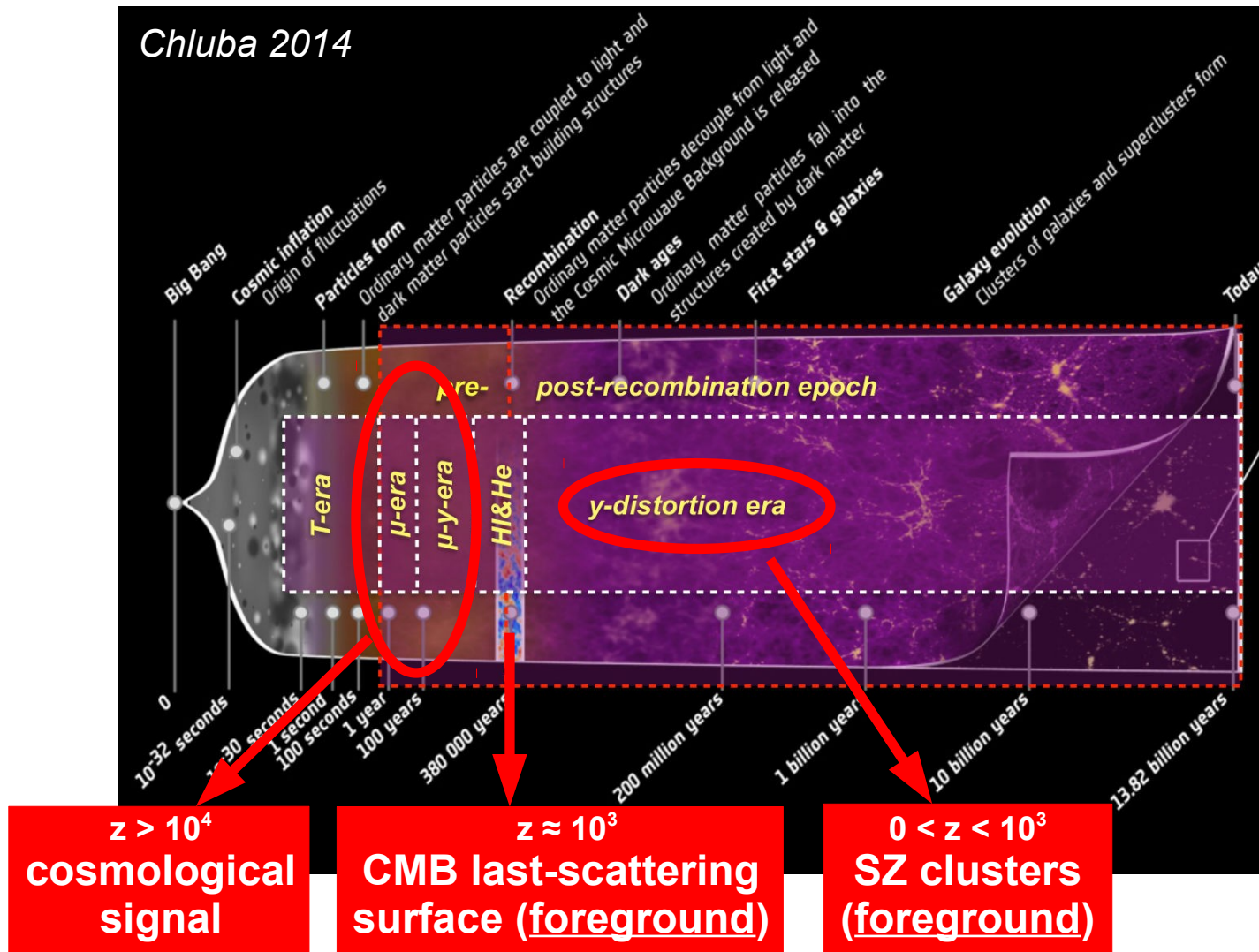


The problem of foregrounds



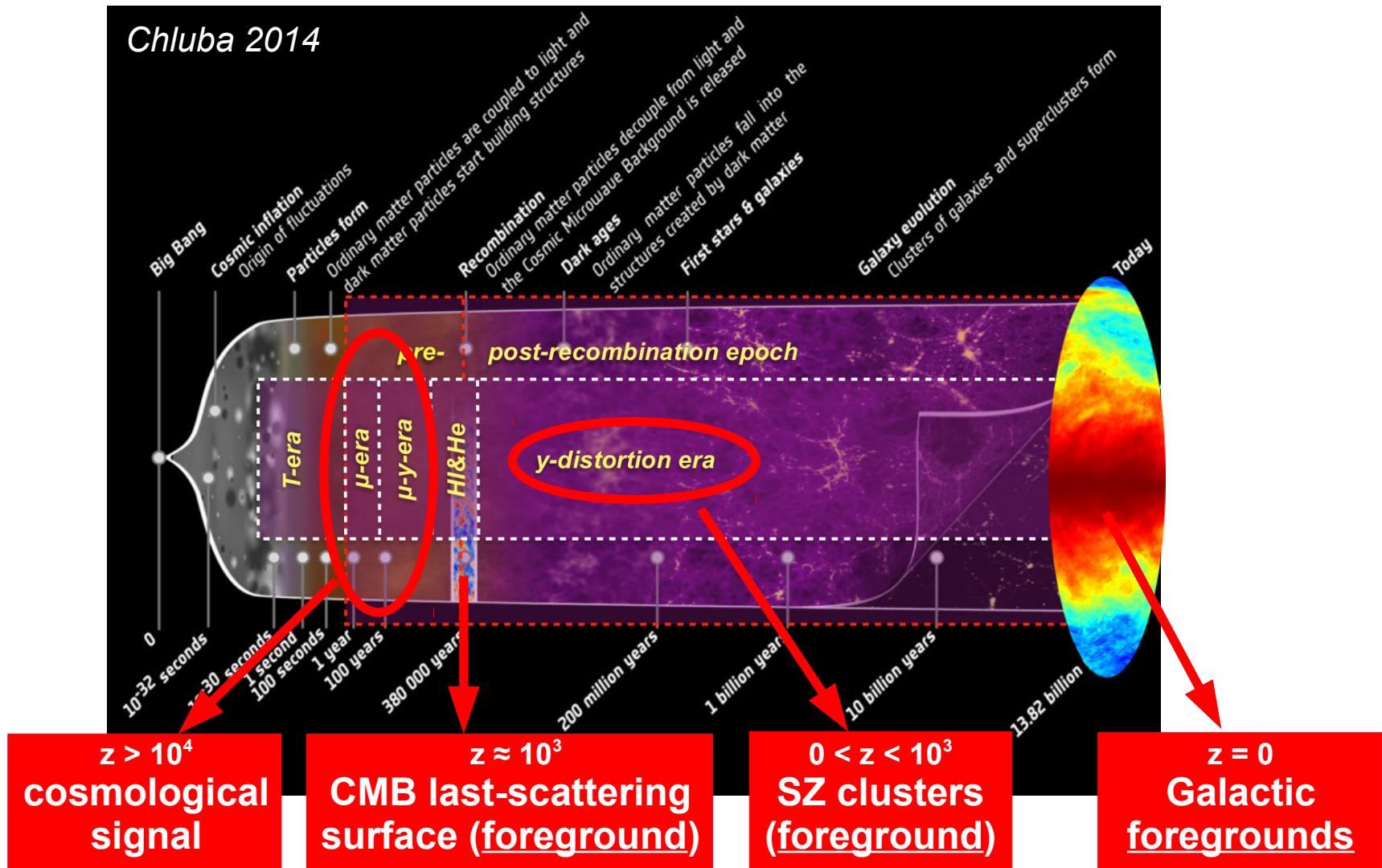
μ-type spectral distortions open a new window to probe physics occurring behind the last-scattering surface, where the universe is invisible!

The problem of foregrounds



μ-type spectral distortions open a new window to probe physics occurring behind the last-scattering surface, where the universe is invisible!

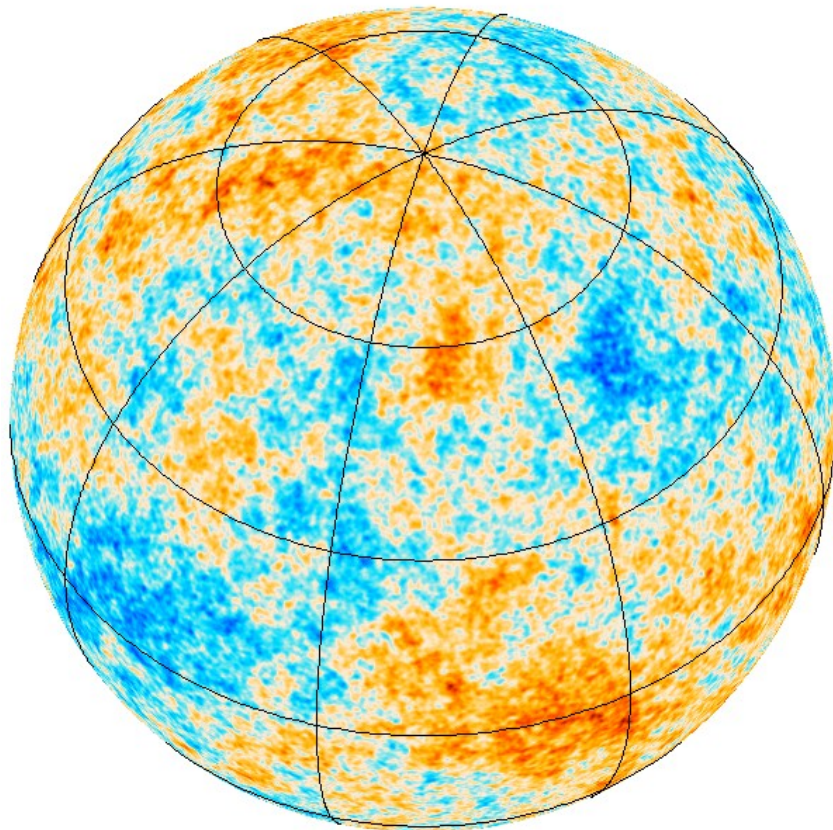
The problem of foregrounds



μ -type spectral distortions open a new window to probe physics occurring behind the last-scattering surface, where the universe is invisible!

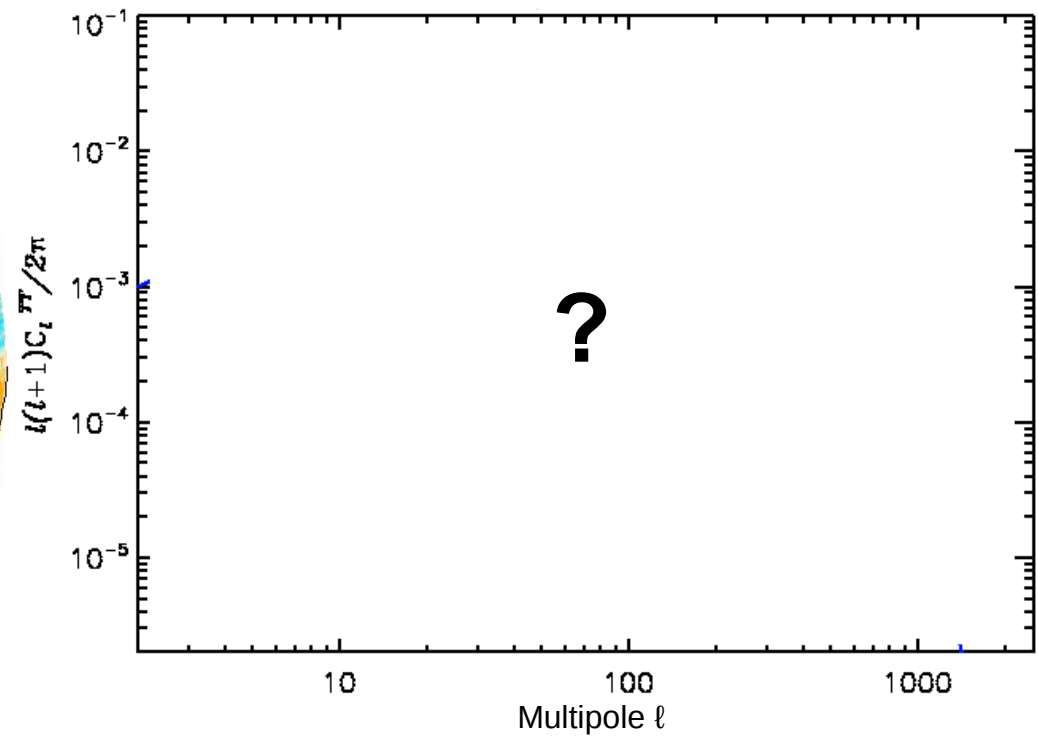
Component separation : the problem

μ -distortion anisotropies



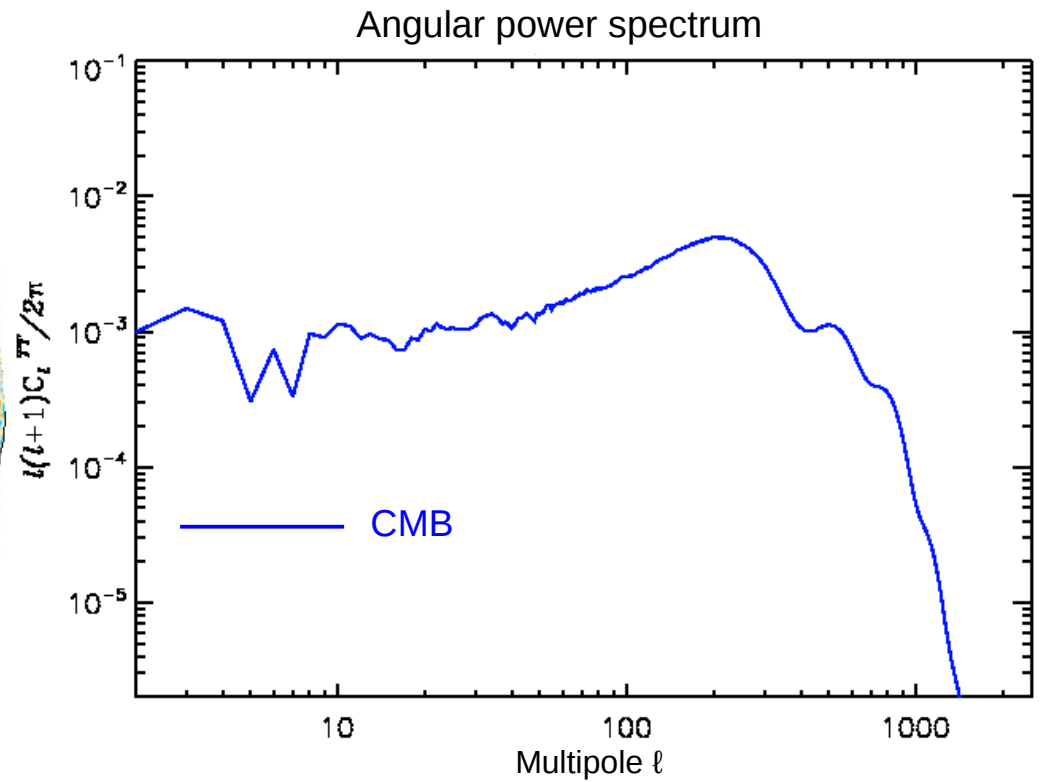
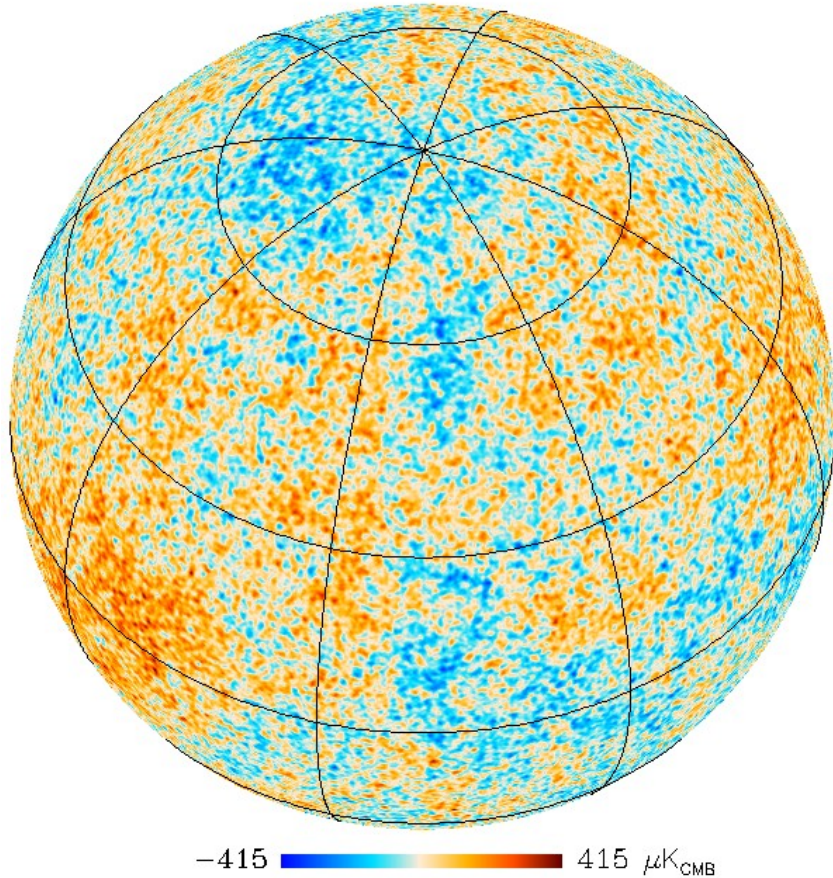
-0.015  0.015 μK_{CMB}

Angular power spectrum



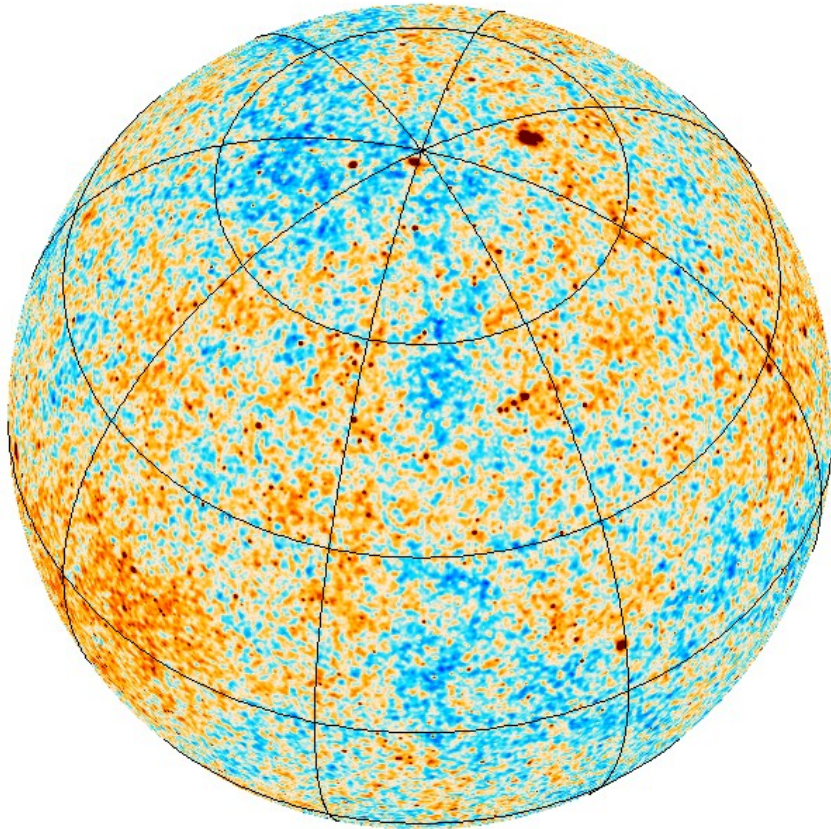
Component separation : the problem

μ -distortion + CMB temperature anisotropies



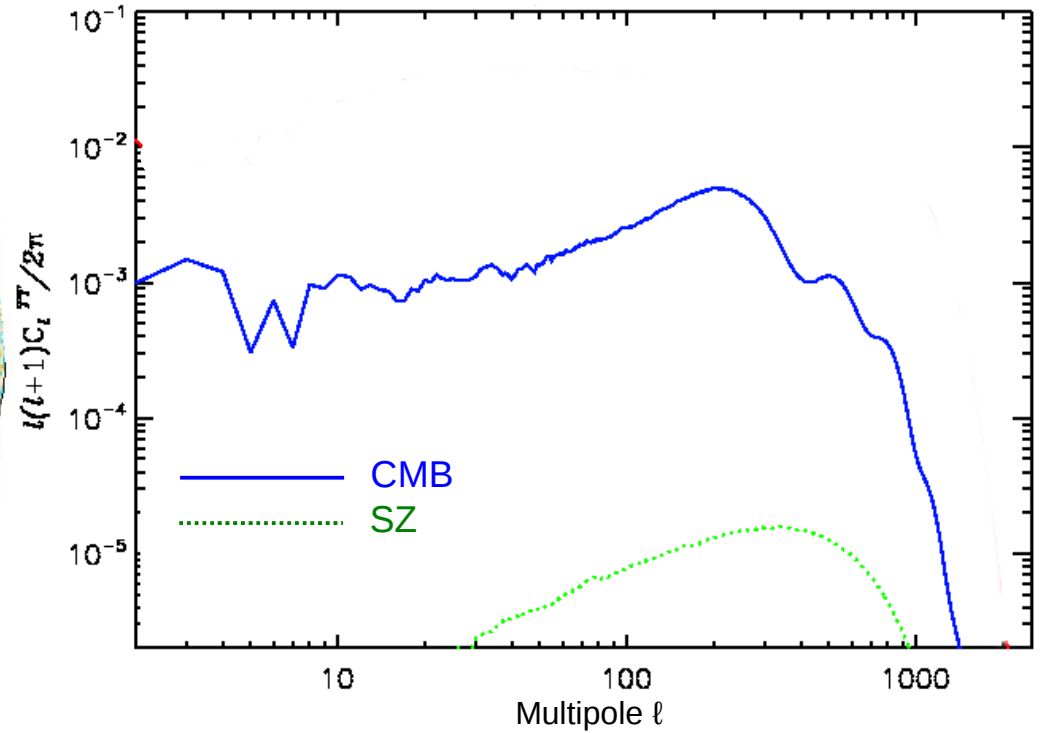
Component separation : the problem

μ -distortion + CMB + SZ



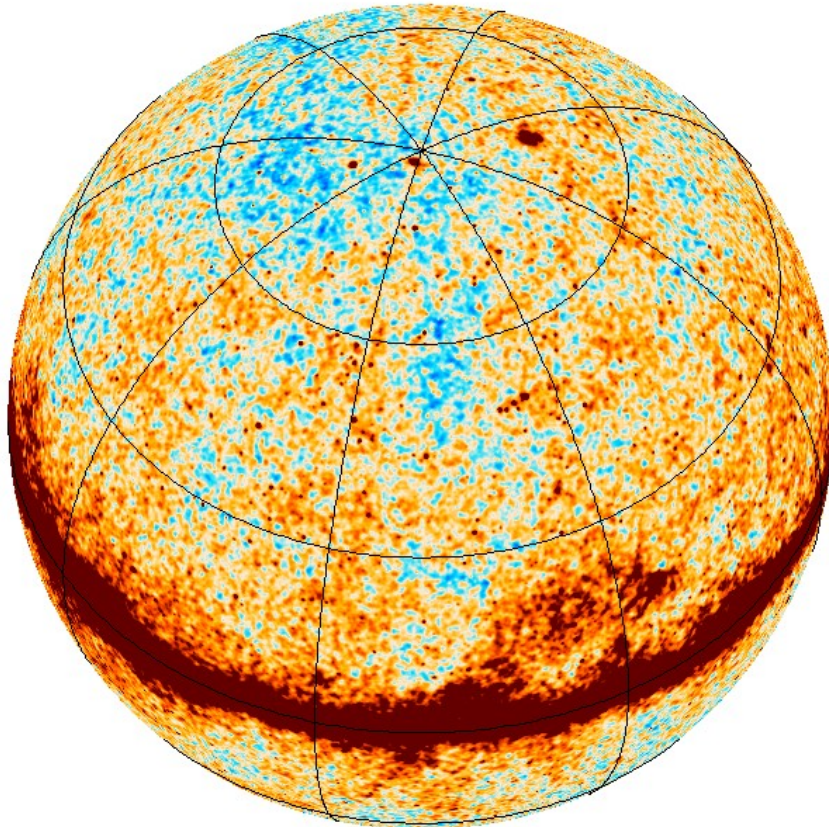
-415  415 μK_{CMB}

Angular power spectrum

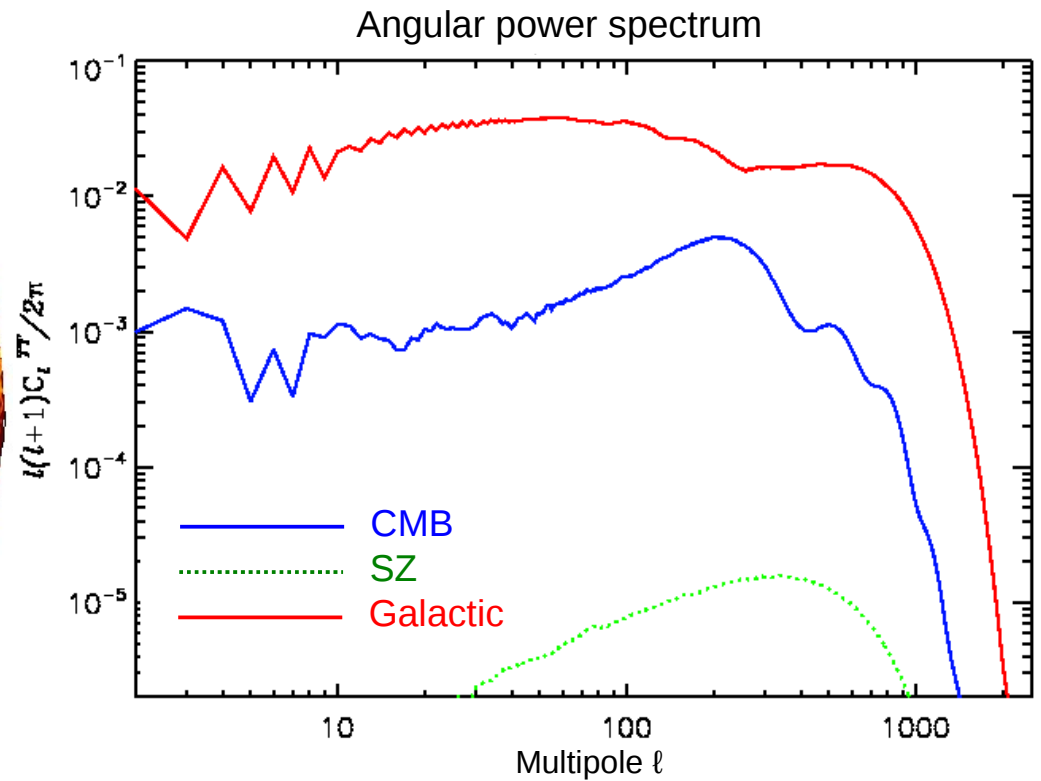


Component separation : the problem

μ -distortion + CMB + SZ + Galactic

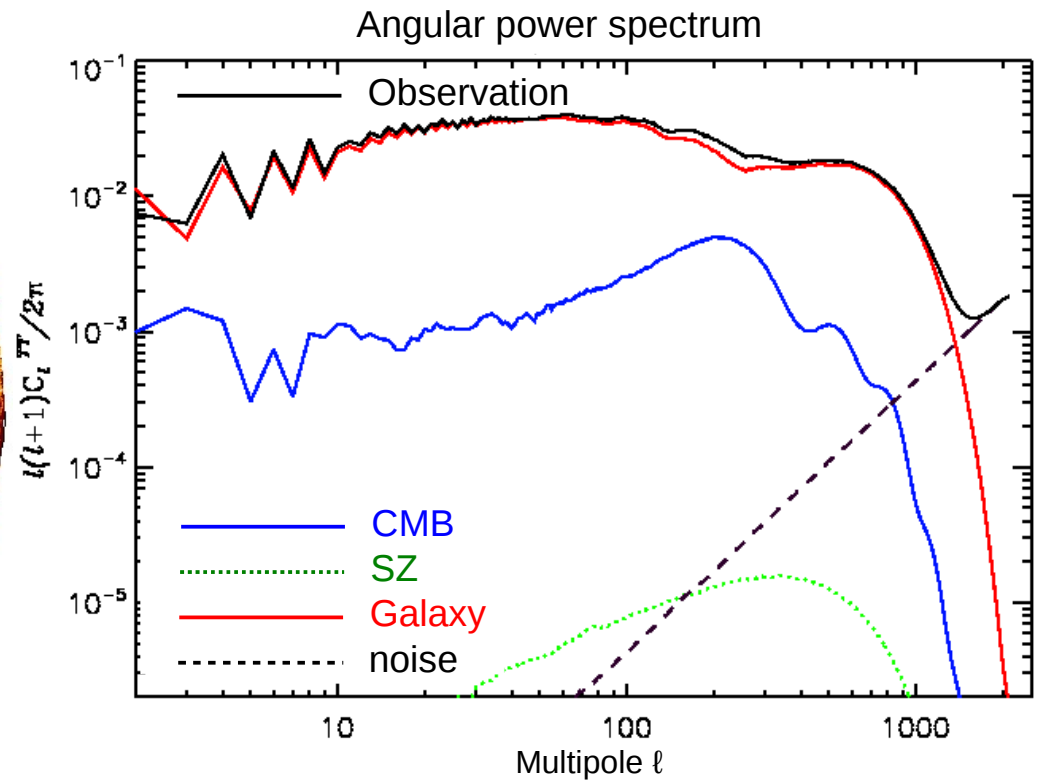
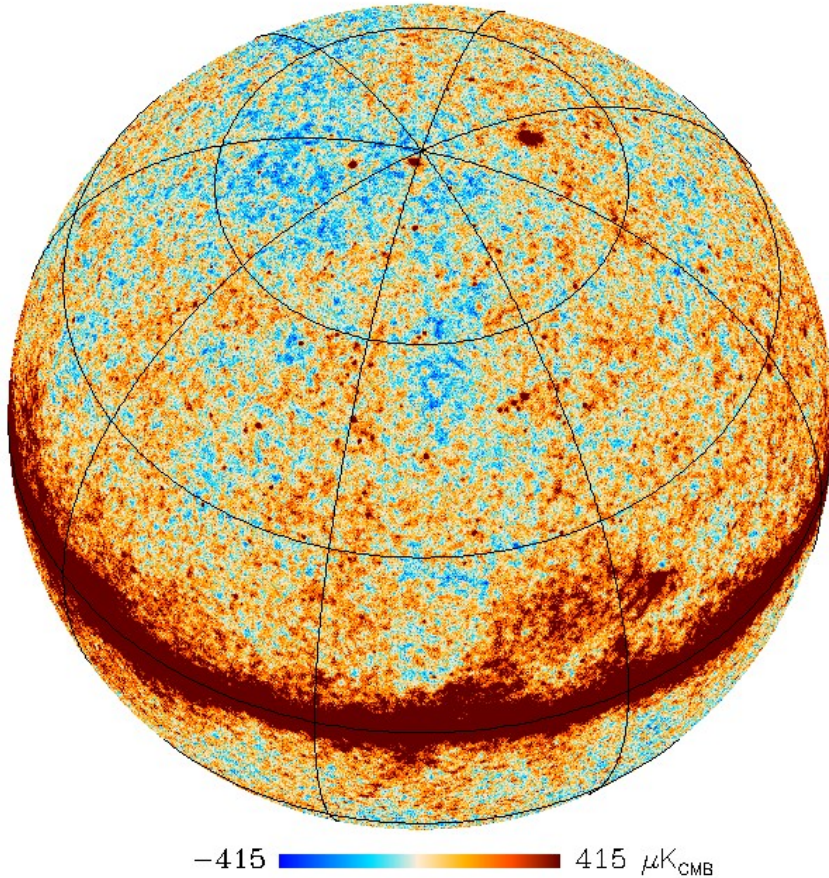


-415  415 μK_{CMB}



Component separation : the problem

μ -distortion + CMB + SZ + Galactic + noise



Standard ILC

Sky observation at
frequency ν and pixel n

“foregrounds + noise”

$$X_{\nu}(n) = \mathbf{a}_{\nu} S_{\text{CMB}}(n) + \mathbf{b}_{\nu} S_{\text{SZ}}(n) + N_{\nu}(n)$$

Minimum-variance weighted linear combination
of the frequency maps:

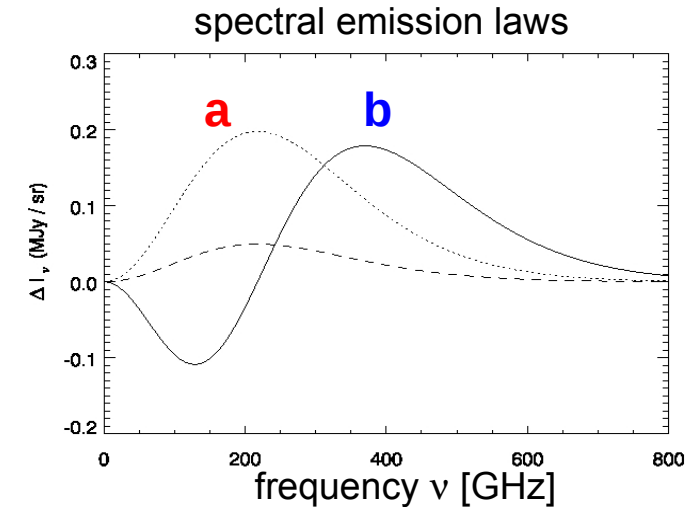
$$\hat{S}_{\text{CMB}}(n) = \sum w_{\nu} X_{\nu}(n)$$

where $\left\{ \begin{array}{l} \text{variance } \langle \hat{s}^2 \rangle \text{ minimum} \\ \sum w_{\nu} \mathbf{a}_{\nu} = \mathbf{1} \end{array} \right.$

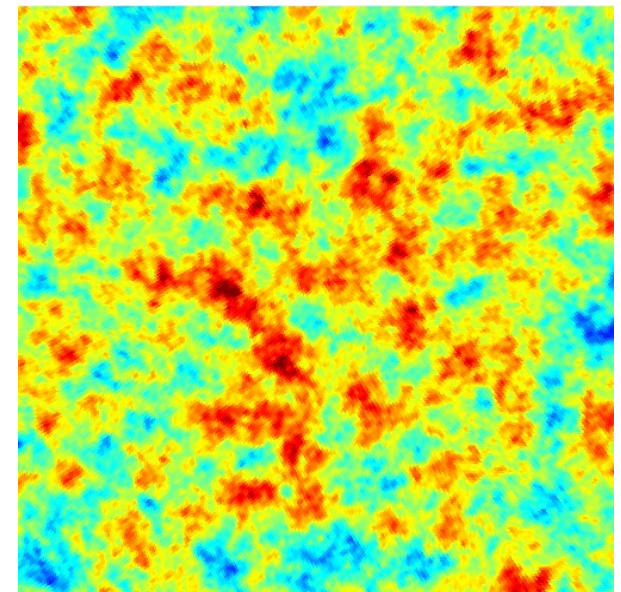
standard ILC

$$\mathbf{W} = \frac{\mathbf{a}^t \mathbf{C}^{-1}}{\mathbf{a}^t \mathbf{C}^{-1} \mathbf{a}}$$

Benett et al, 2003
Tegmark et al, 2003
Eriksen et al, 2004
Delabrouille et al, 2009



CMB reconstruction



-0.40 0.40 mK CMB

Standard ILC

Sky observation at
frequency ν and pixel n



$$X_{\nu}(n) = \mathbf{a}_{\nu} \mathbf{S}_{\text{CMB}}(n) + \mathbf{b}_{\nu} \mathbf{S}_{\text{SZ}}(n) + \mathbf{N}_{\nu}(n)$$

“foregrounds + noise”



Minimum-variance weighted linear combination
of the frequency maps:

$$\hat{\mathbf{S}}_{\text{SZ}}(n) = \sum w_{\nu} X_{\nu}(n)$$

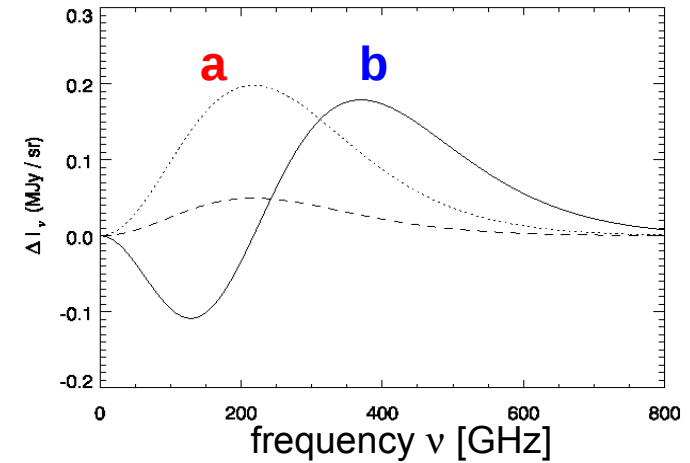
where $\left\{ \begin{array}{l} \text{variance } \langle \hat{s}^2 \rangle \text{ minimum} \\ \sum w_{\nu} \mathbf{b}_{\nu} = \mathbf{1} \end{array} \right.$

standard ILC

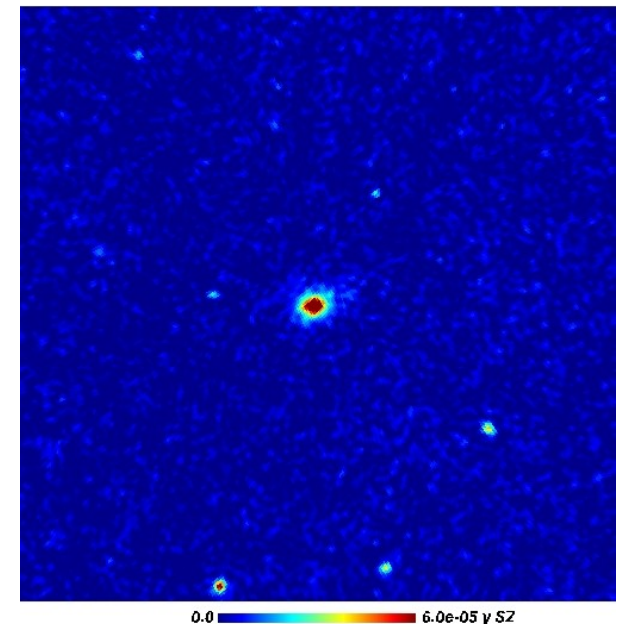
$$\mathbf{W} = \frac{\mathbf{b}^t \mathbf{C}^{-1}}{\mathbf{b}^t \mathbf{C}^{-1} \mathbf{b}}$$

Benett et al, 2003
Tegmark et al, 2003
Eriksen et al, 2004
Delabrouille et al, 2009

spectral emission laws



SZ reconstruction



Constrained ILC

Sky observation at
frequency ν and pixel n

“foregrounds + noise”

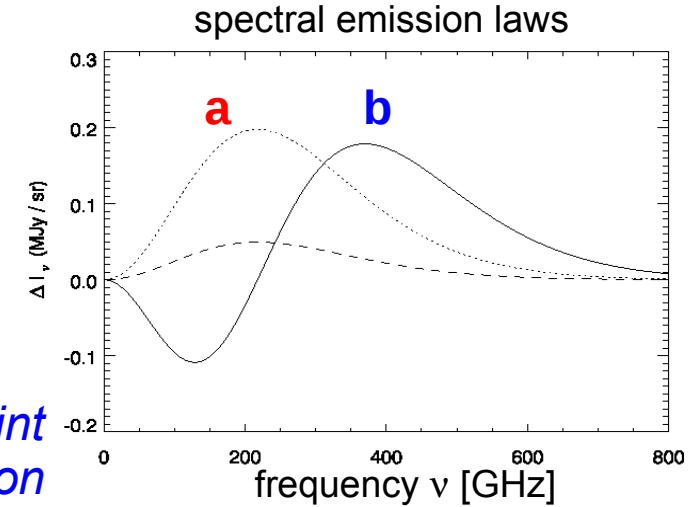
$$X_{\nu}(n) = \mathbf{a}_{\nu} S_{\text{CMB}}(n) + \mathbf{b}_{\nu} S_{\text{SZ}}(n) + N_{\nu}(n)$$

$$\hat{S}_{\text{CMB}}(n) = \sum w_{\nu} X_{\nu}(n)$$

where

$$\begin{cases} \text{variance } \langle \hat{S}^2 \rangle \text{ minimum} \\ \sum w_{\nu} \mathbf{a}_{\nu} = \mathbf{1} \\ \sum w_{\nu} \mathbf{b}_{\nu} = \mathbf{0} \end{cases}$$

orthogonality constraint to kill SZ contamination

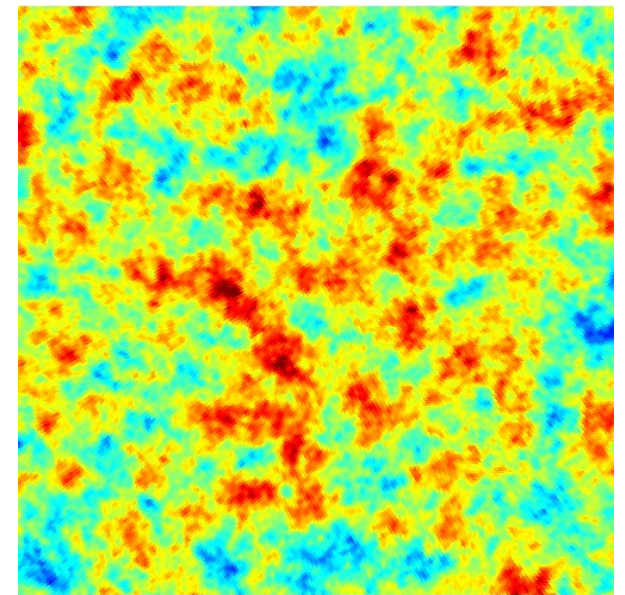


Constrained ILC

$$\mathbf{W} = \frac{(\mathbf{b}^t \mathbf{C}^{-1} \mathbf{b}) \mathbf{a}^t \mathbf{C}^{-1} - (\mathbf{a}^t \mathbf{C}^{-1} \mathbf{a}) \mathbf{b}^t \mathbf{C}^{-1}}{(\mathbf{a}^t \mathbf{C}^{-1} \mathbf{a}) (\mathbf{b}^t \mathbf{C}^{-1} \mathbf{b}) - (\mathbf{a}^t \mathbf{C}^{-1} \mathbf{b})^2}$$

Remazeilles, Delabrouille, Cardoso, MNRAS (2011)

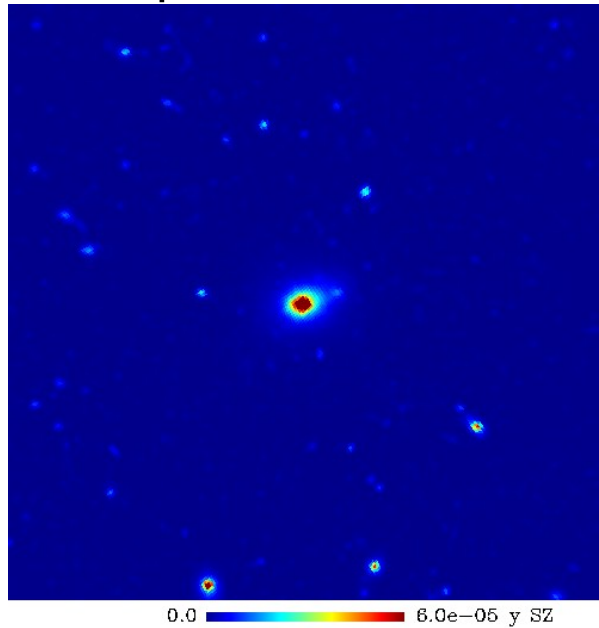
SZ-free CMB reconstruction



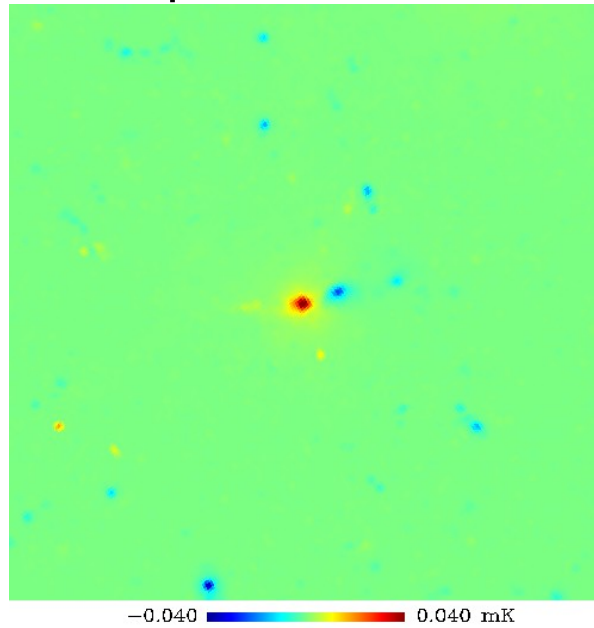
-0.40 0.40 mK CMB

Standard ILC

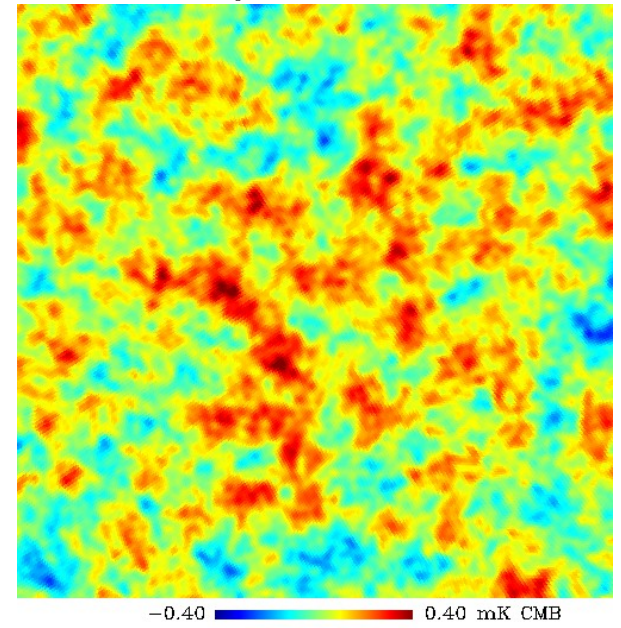
input thermal SZ



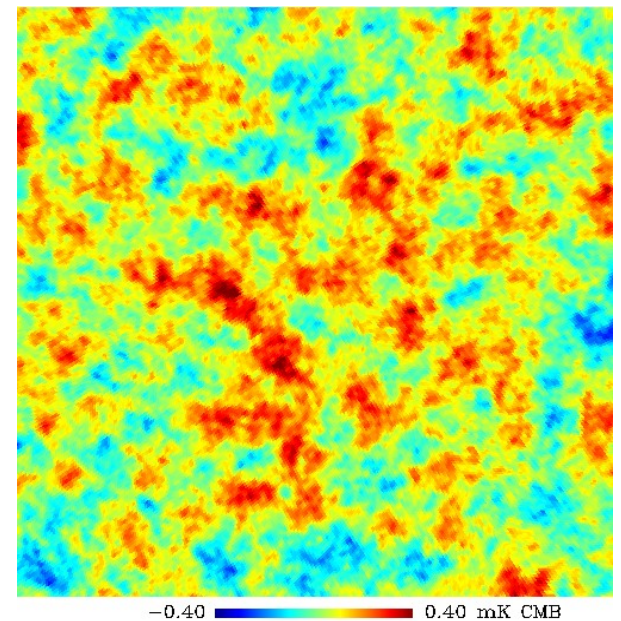
input kinetic SZ



input CMB



ILC

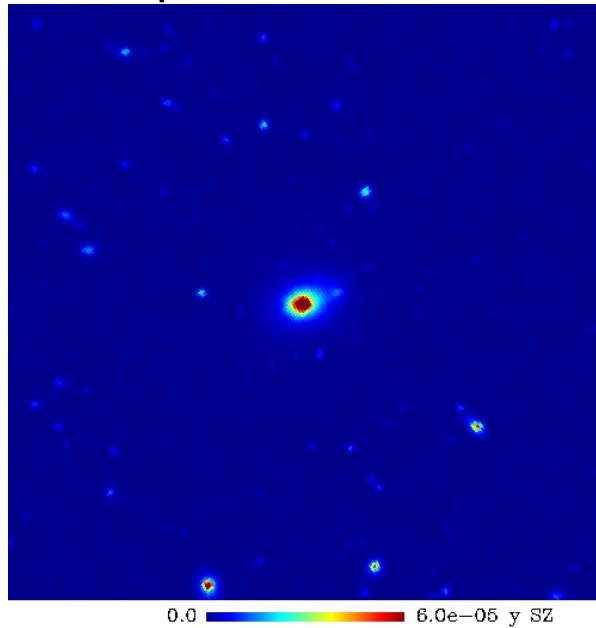


$$\mathbf{w} = \frac{\mathbf{a}^t \mathbf{C}^{-1}}{\mathbf{a}^t \mathbf{C}^{-1} \mathbf{a}}$$

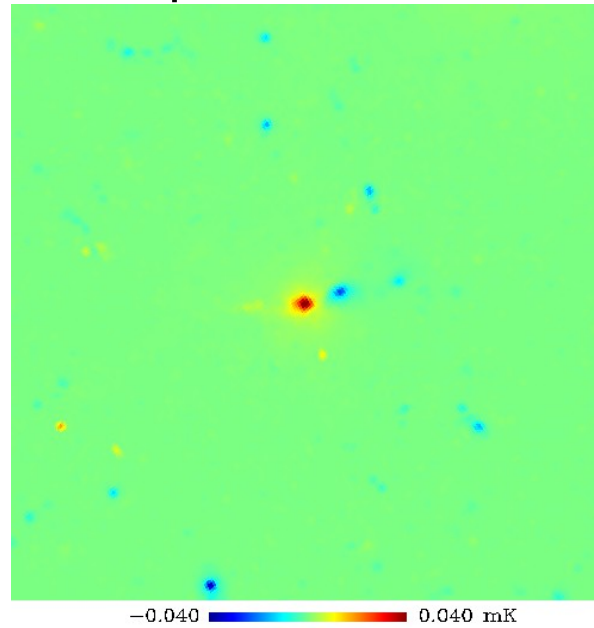
Bennett et al (2003), Tegmark et al (2003)
Eriksen et al (2004), Delabrouille et al (2009)

Standard ILC

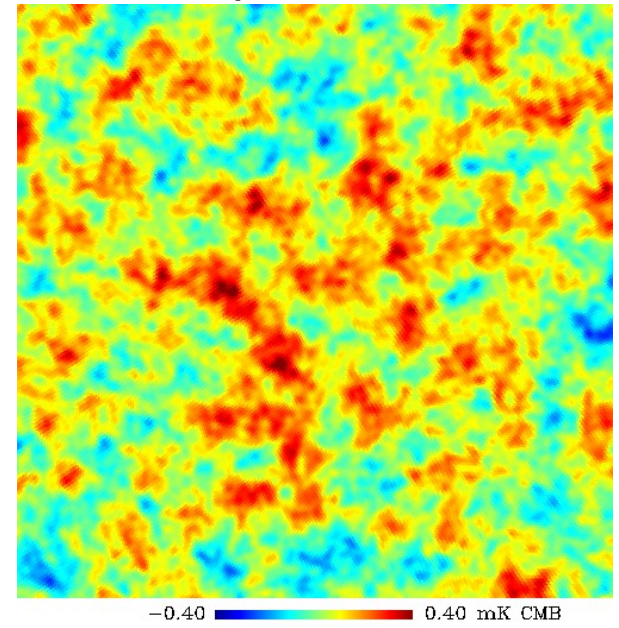
input thermal SZ



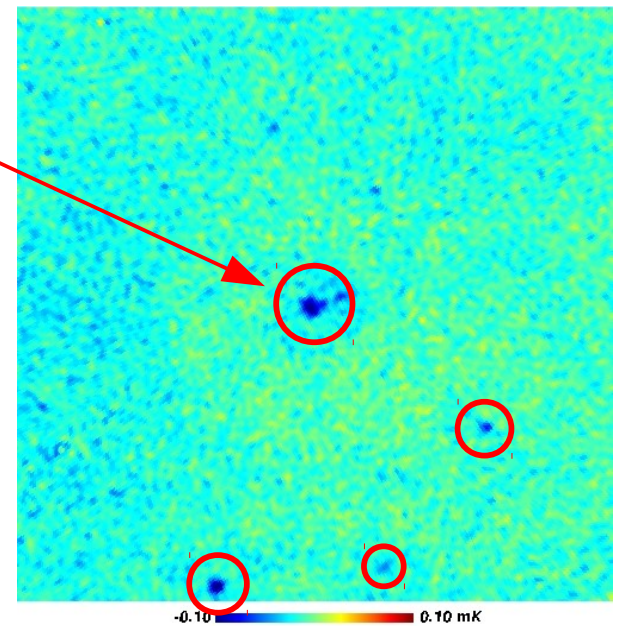
input kinetic SZ



input CMB



error: ILC - CMB



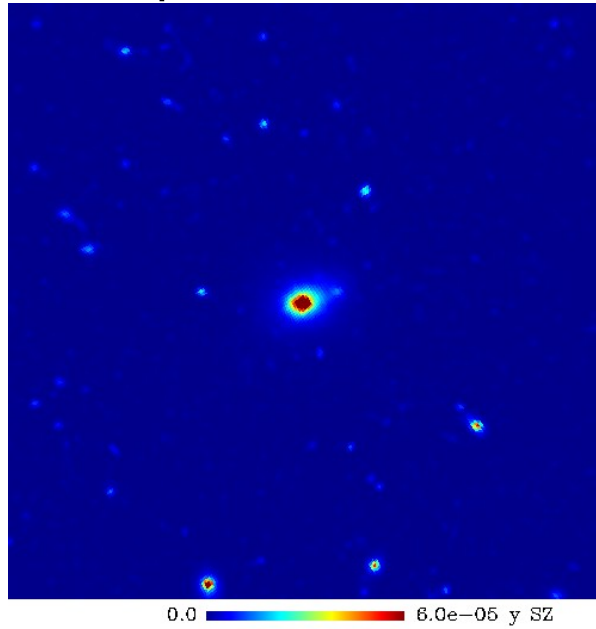
Thermal SZ residuals !
(clusters in the CMB)

$$\mathbf{w} = \frac{\mathbf{a}^t \mathbf{C}^{-1}}{\mathbf{a}^t \mathbf{C}^{-1} \mathbf{a}}$$

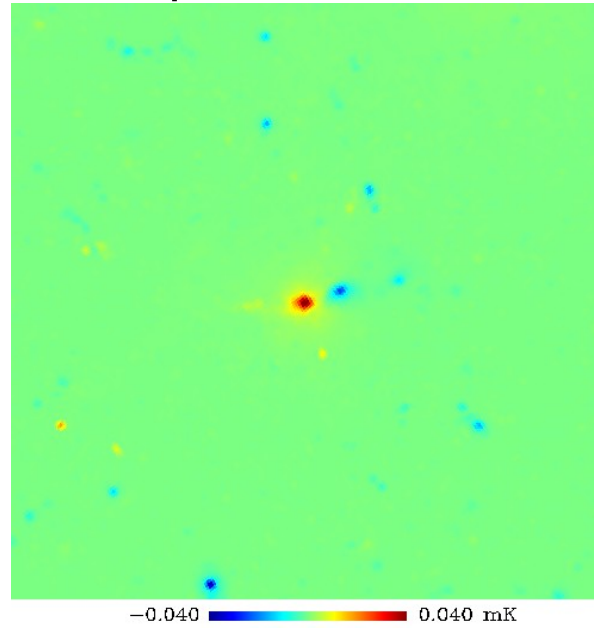
Bennett et al (2003), Tegmark et al (2003)
Eriksen et al (2004), Delabrouille et al (2009)

Constrained ILC

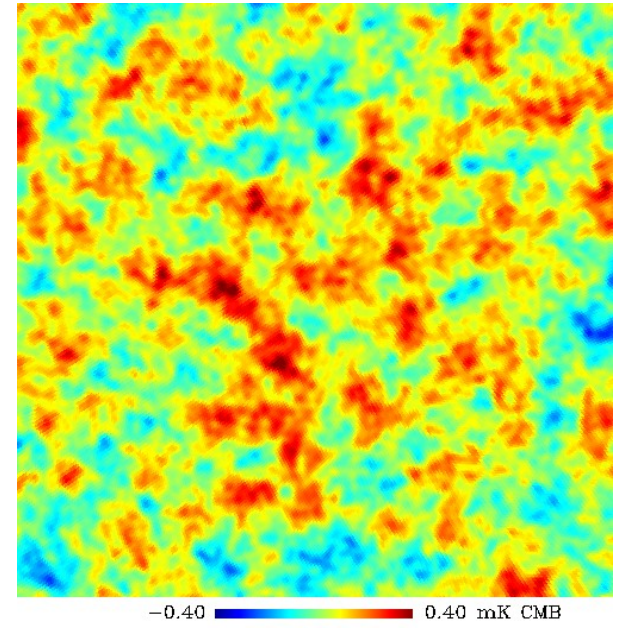
input thermal SZ



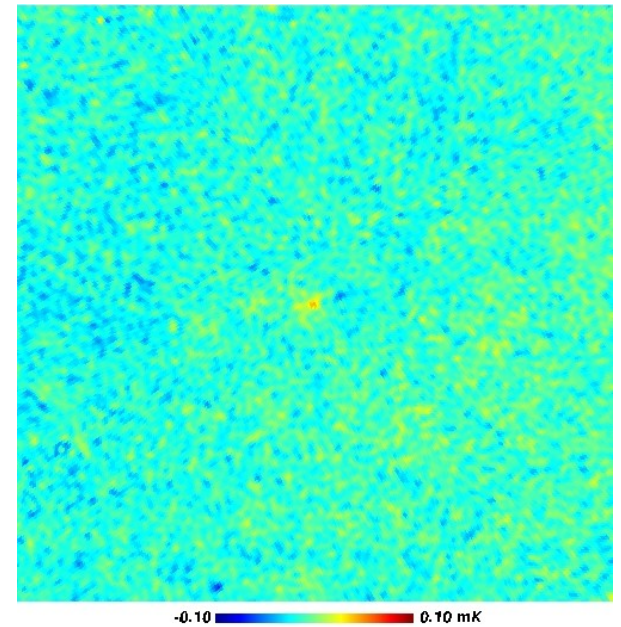
input kinetic SZ



input CMB



error: Constrained ILC - CMB



$$\mathbf{w} = \frac{(\mathbf{b}^t \mathbf{C}^{-1} \mathbf{b}) \mathbf{a}^t \mathbf{C}^{-1} - (\mathbf{a}^t \mathbf{C}^{-1} \mathbf{a}) \mathbf{b}^t \mathbf{C}^{-1}}{(\mathbf{a}^t \mathbf{C}^{-1} \mathbf{a}) (\mathbf{b}^t \mathbf{C}^{-1} \mathbf{b}) - (\mathbf{a}^t \mathbf{C}^{-1} \mathbf{b})^2}$$

Remazeilles, Delabrouille, Cardoso, MNRAS (2011)

Extracting foreground-obscured μ -anisotropies

$$\text{data}(\nu;n) = \mu + T + (\text{foregrounds+noise})$$

↑ sky observation at frequency ν and pixel n

↑ μ -distortion anisotropies

↑ CMB temperature anisotropies

- CMB T anisotropies is a significant foreground to μ -distortion anisotropies
- Most sneaky, the CMB T foreground is also correlated with the μ signal!
- If residual T anisotropies are left in the reconstructed μ -distortion signal after component separation

$$\hat{\mu} = \mu + \varepsilon_1 T + \varepsilon_2 (\text{foregrounds+noise})$$

then the μ - T correlation signal will be biased by spurious TT correlations:

$$\hat{\mu} \times \hat{T} = \mu \times T + \varepsilon_1 TT + \dots$$

Remazeilles & Chluba (2018) → our solution: use the “Constrained ILC” approach

CMB-free μ -distortion reconstruction

$$X(\nu;n) = a_{\mu}(\nu) \mu(n) + a_T(\nu) T(n) + N(\nu;n)$$

sky observation at frequency ν and pixel n μ SED μ -distortion anisotropies CMB SED CMB temperature anisotropies foregrounds + noise

Constrained ILC estimate:

$$\hat{\mu}(n) = \sum_{\nu} w(\nu) X(\nu;n)$$

such that

$$\left\{ \begin{array}{l} \text{variance } \langle \mu^2 \rangle \text{ minimum} \quad (1) \\ \sum_{\nu} w_{\nu} a_{\mu}(\nu) = 1 \quad (2) \\ \sum_{\nu} w_{\nu} a_T(\nu) = 0 \quad (3) \end{array} \right.$$

→ *orthogonality constraint to kill CMB T contamination*

CMB-free μ -distortion reconstruction

$$X(\nu;n) = \mathbf{a}_\mu(\nu) \mu(n) + \mathbf{a}_T(\nu) T(n) + N(\nu;n)$$

↑
↑
↑
↑
↑
↑

sky observation at frequency ν and pixel n

 μ SED

 μ -distortion anisotropies

 CMB SED

 CMB temperature anisotropies

 foregrounds + noise

Constrained ILC estimate:

$$\hat{\mu}(n) = \sum_{\nu} w(\nu) X(\nu;n)$$

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→ *orthogonality constraint to kill CMB T contamination*

$$\hat{\mu}(n) = \underbrace{\left(\sum_{\nu} w_{\nu} \mathbf{a}_{\mu}(\nu) \right)}_{= \mathbf{1} \quad (2)} \mu + \underbrace{\left(\sum_{\nu} w_{\nu} \mathbf{a}_T(\nu) \right)}_{= \mathbf{0} \quad (3)} T + \underbrace{\sum_{\nu} w_{\nu} N_{\nu}}_{\text{minimized} \quad (1)}$$

CMB-free μ -distortion reconstruction

$$X(\nu;n) = a_{\mu}(\nu) \mu(n) + a_T(\nu) T(n) + N(\nu;n)$$

↑
↑
↑
↑
↑
↑

sky observation at frequency ν and pixel n
 μ SED
 μ -distortion anisotropies
 CMB SED
 CMB temperature anisotropies
 foregrounds + noise

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→ orthogonality constraint to kill CMB T contamination

$$\hat{\mu}(n) = \underbrace{\left(\sum_{\nu} w_{\nu} a_{\mu}(\nu) \right)}_{= 1} \mu + \underbrace{\left(\sum_{\nu} w_{\nu} a_T(\nu) \right)}_{= 0} T + \underbrace{\sum_{\nu} w_{\nu} N_{\nu}}_{\text{minimized}}$$

(2)
(3)
(1)

CMB-free μ -distortion reconstruction

$$X(\nu;n) = a_{\mu}(\nu) \mu(n) + a_T(\nu) T(n) + N(\nu;n)$$

↑
↑
↑
↑
↑
↑

sky observation at frequency ν and pixel n

 μ SED

 μ -distortion anisotropies

 CMB SED

 CMB temperature anisotropies

 foregrounds + noise

Constrained ILC estimate:

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→ *orthogonality constraint to kill CMB T contamination*

$$\rightarrow \hat{\mu} \times \hat{T} = \mu \times T + \cancel{\varepsilon_1 T T} + \dots$$

CMB-free μ -distortion reconstruction

$$X(\nu;n) = \mathbf{a}_\mu(\nu) \mu(n) + \mathbf{a}_T(\nu) T(n) + N(\nu;n)$$

↑ sky observation at frequency ν and pixel n
↑ μ SED
↑ μ -distortion anisotropies
↑ CMB SED
↑ CMB temperature anisotropies
↑ foregrounds + noise

Constrained ILC estimate:

$$\hat{\mu}(n) = \sum_{\nu} w(\nu) X(\nu;n)$$

such that

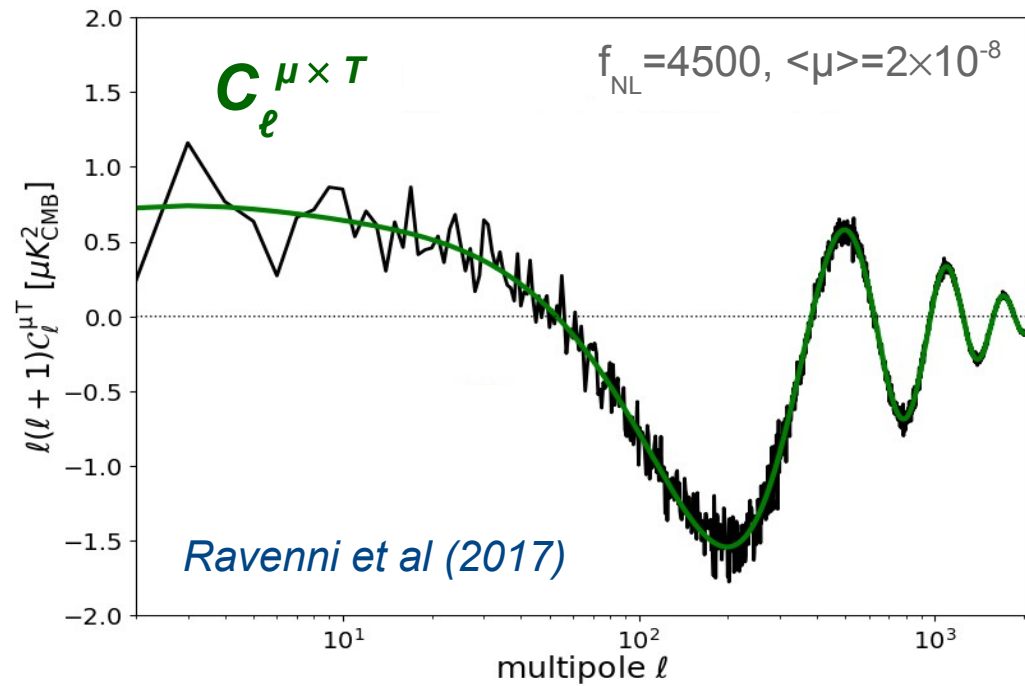
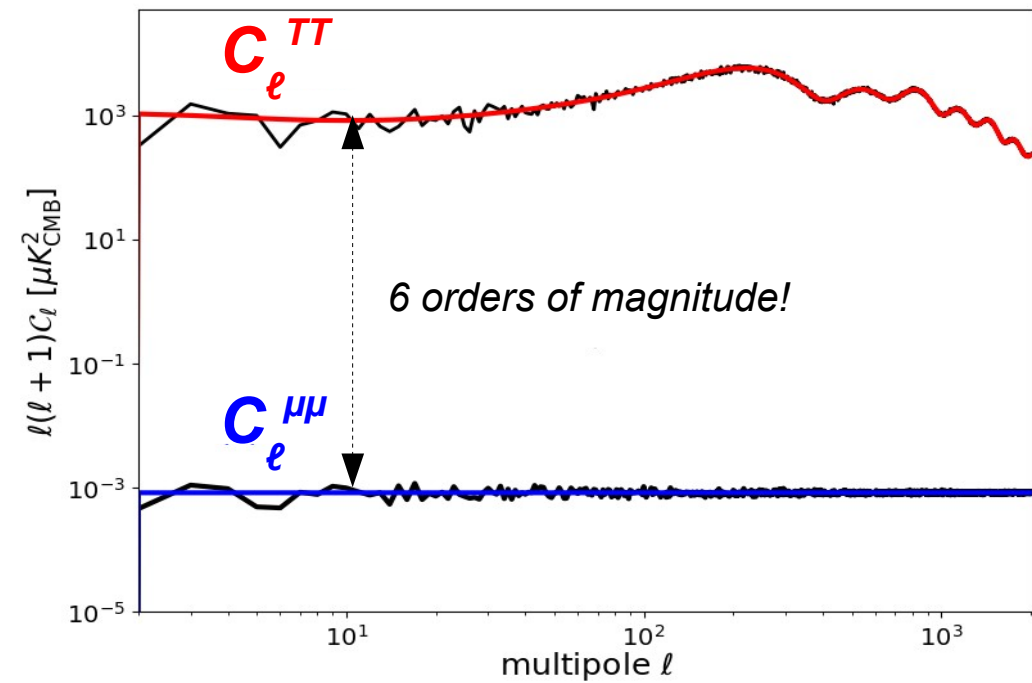
$$\begin{cases} \text{variance } \langle \mu^2 \rangle \text{ minimum} & (1) \\ \sum_{\nu} w_{\nu} \mathbf{a}_{\mu}(\nu) = \mathbf{1} & (2) \\ \sum_{\nu} w_{\nu} \mathbf{a}_T(\nu) = \mathbf{0} & (3) \end{cases}$$

→ *orthogonality constraint to kill CMB T contamination*

Solution:

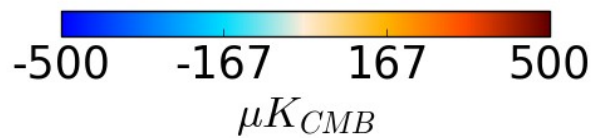
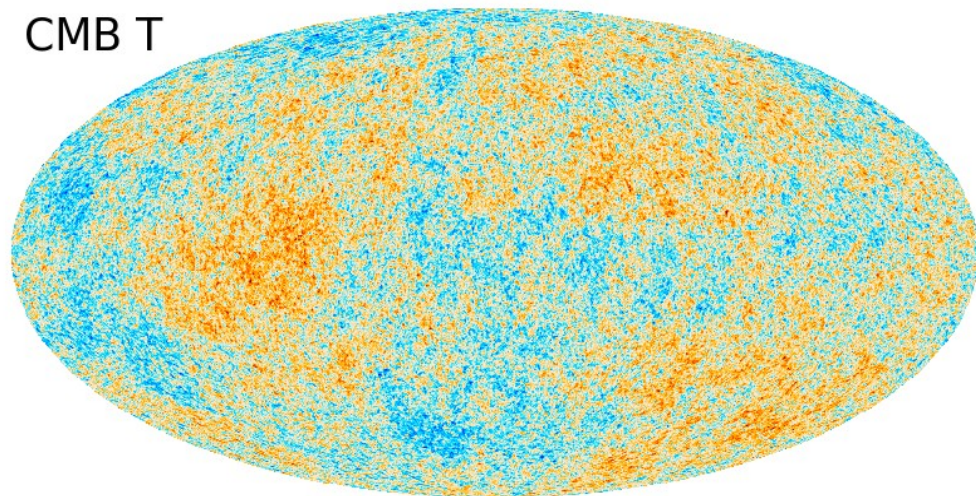
$$\mathbf{W} = \frac{(\mathbf{a}_T^t \mathbf{C}^{-1} \mathbf{a}_T) \mathbf{a}_{\mu}^t \mathbf{C}^{-1} - (\mathbf{a}_{\mu}^t \mathbf{C}^{-1} \mathbf{a}_{\mu}) \mathbf{a}_T^t \mathbf{C}^{-1}}{(\mathbf{a}_{\mu}^t \mathbf{C}^{-1} \mathbf{a}_{\mu})(\mathbf{a}_T^t \mathbf{C}^{-1} \mathbf{a}_T) - (\mathbf{a}_{\mu}^t \mathbf{C}^{-1} \mathbf{a}_T)^2}$$

Simulation of correlated μ and T fields

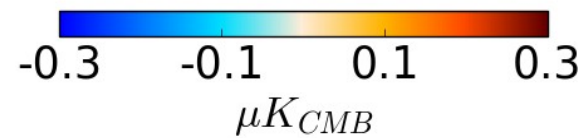
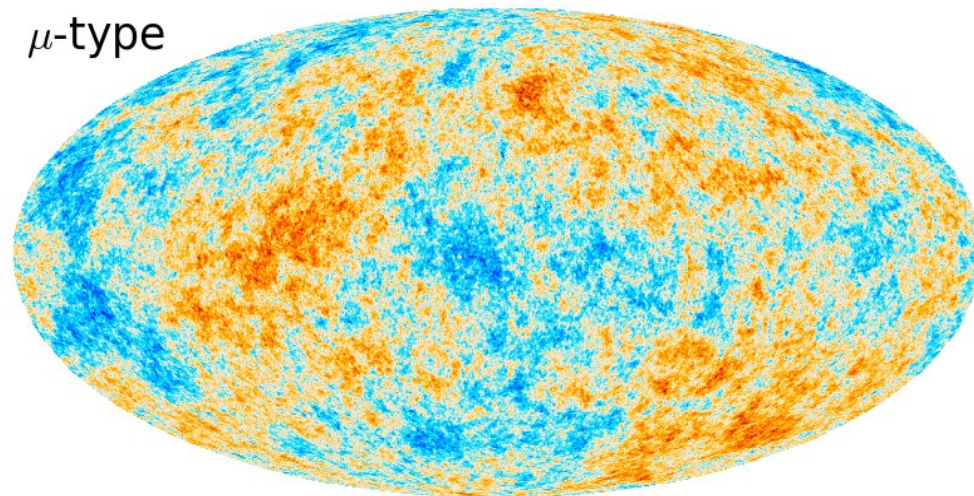


Simulation of correlated μ and T fields

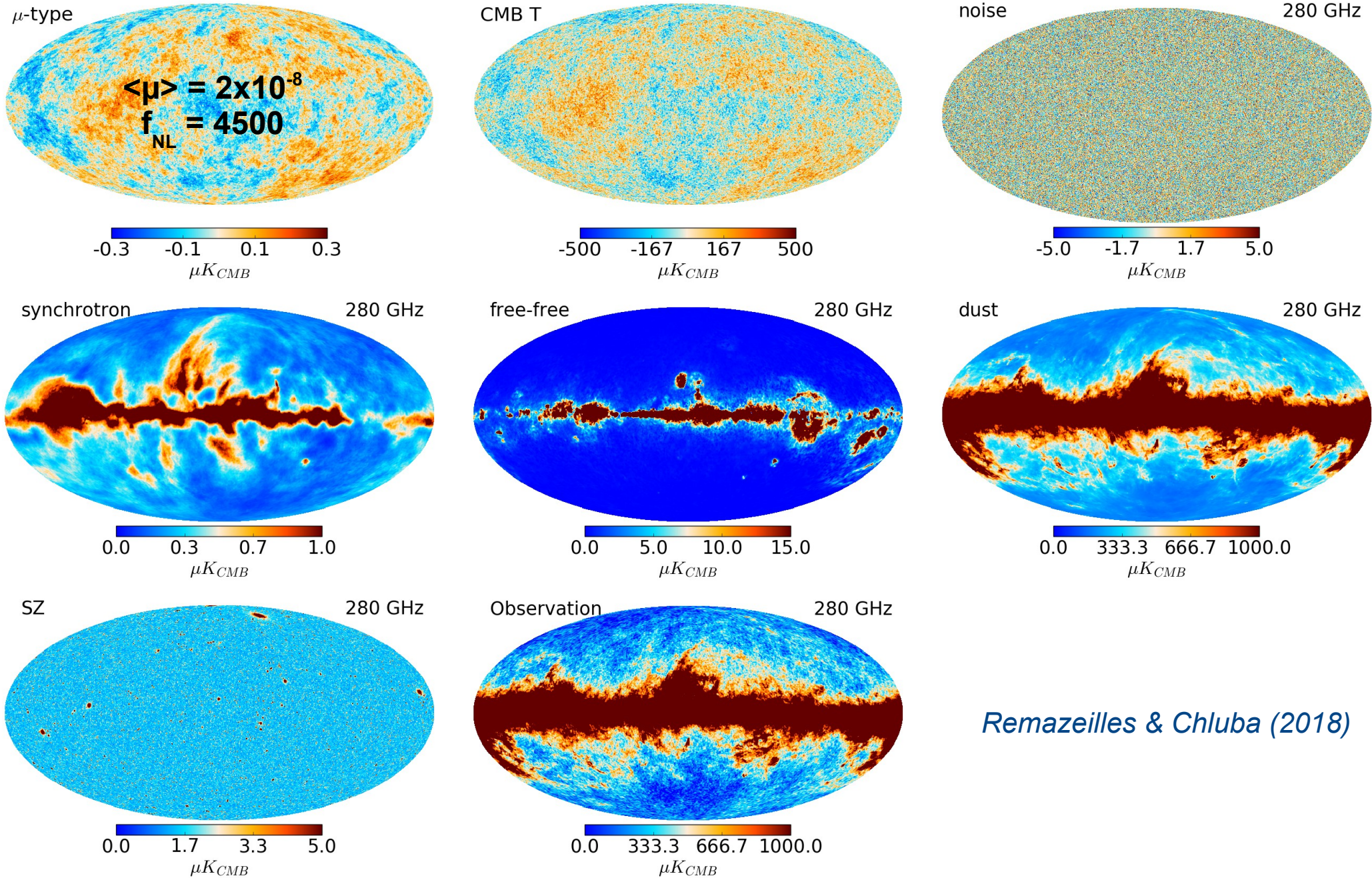
CMB T



μ -type

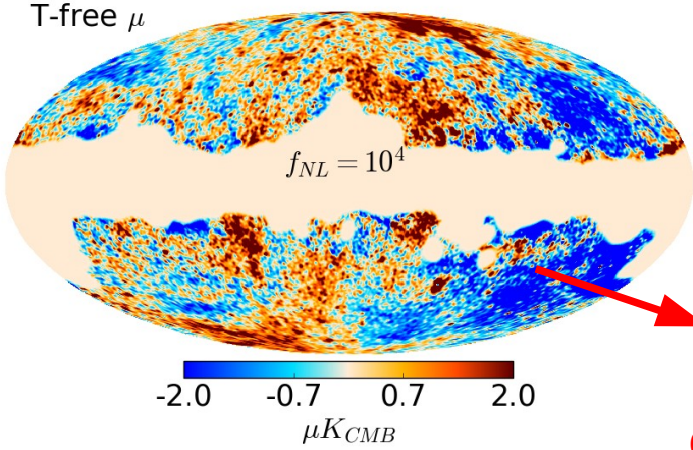
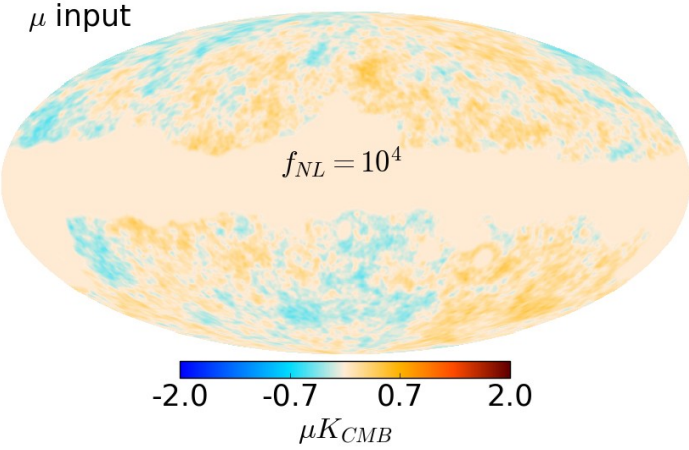


Our sky simulations (e.g. LiteBIRD)



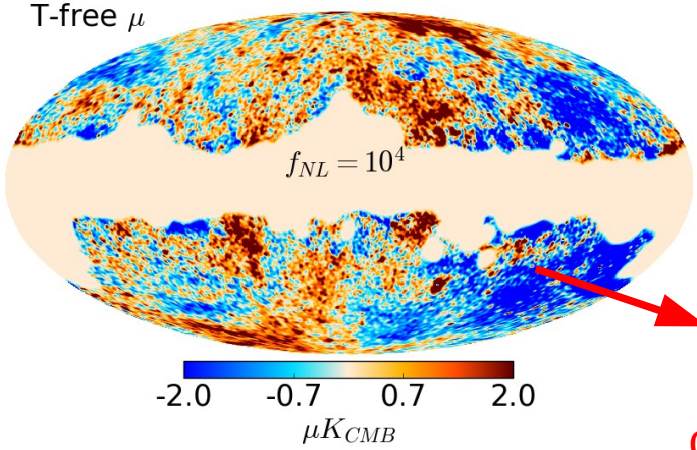
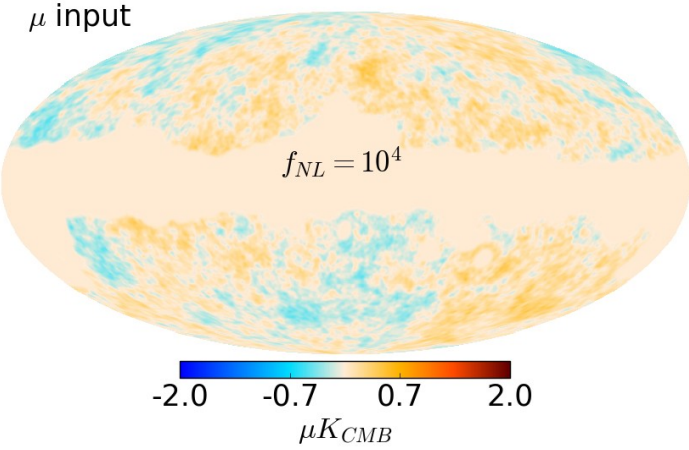
Remazeilles & Chluba (2018)

Constrained ILC μ -map reconstruction (LiteBIRD)

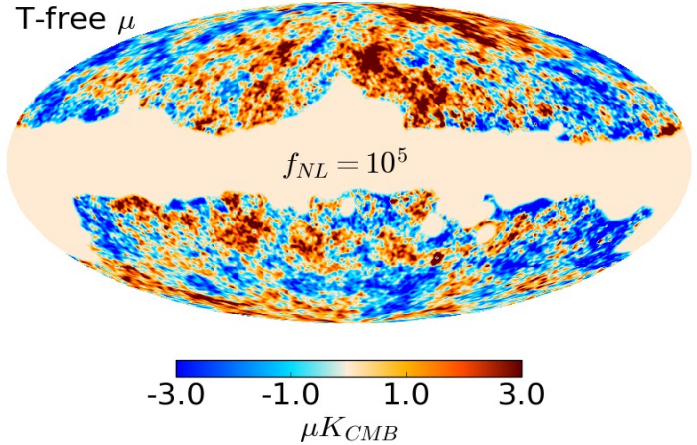
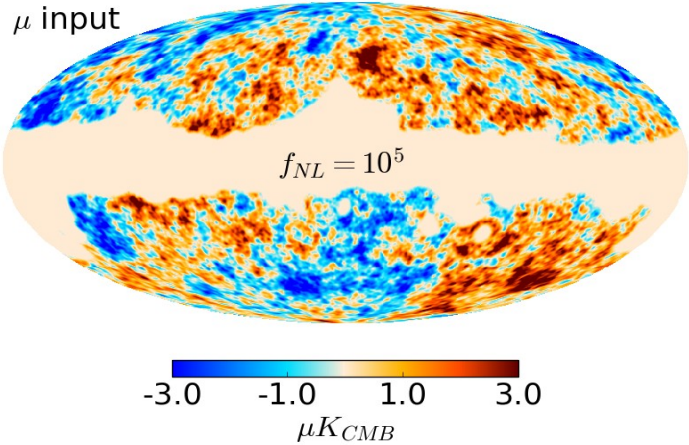


significant foreground contamination

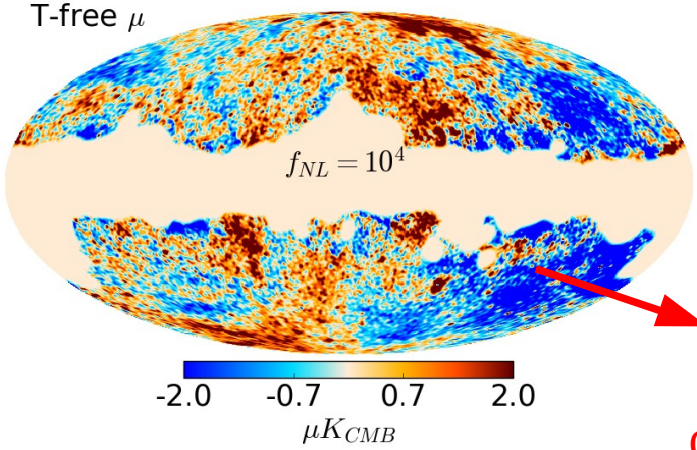
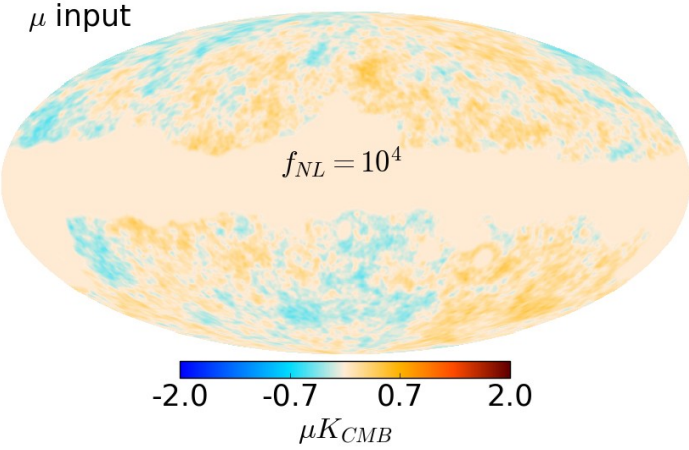
Constrained ILC μ -map reconstruction (LiteBIRD)



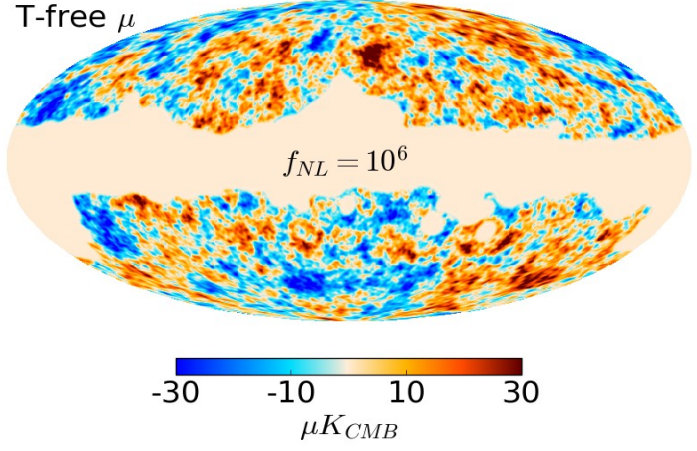
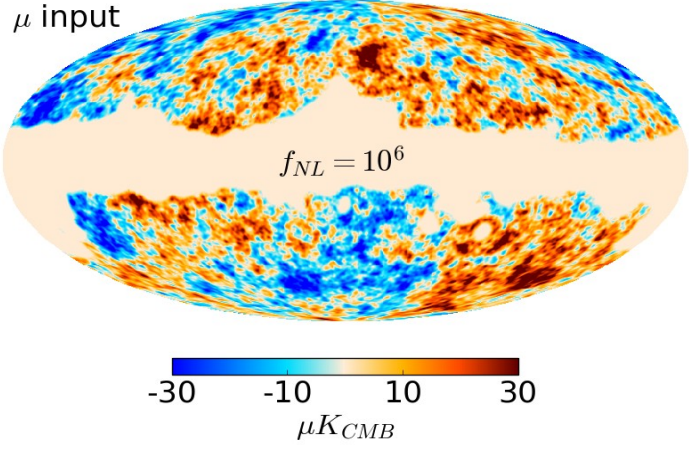
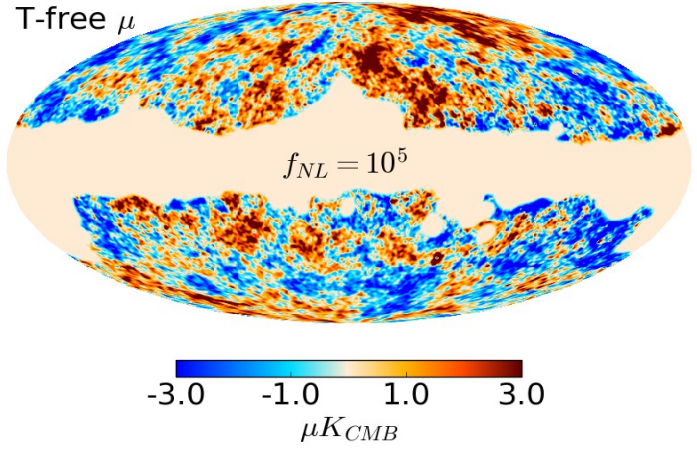
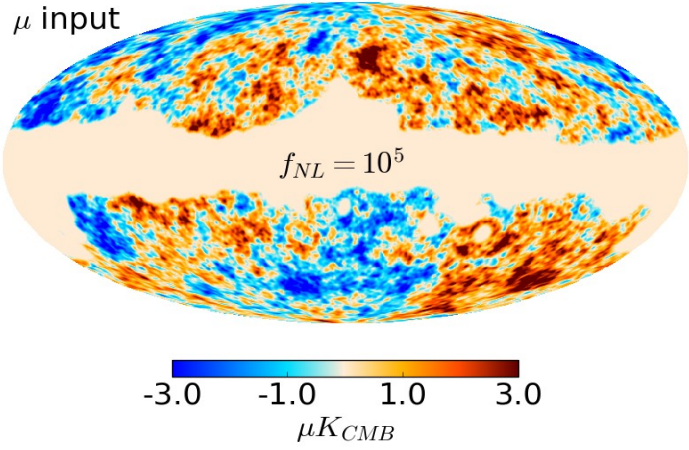
significant foreground contamination



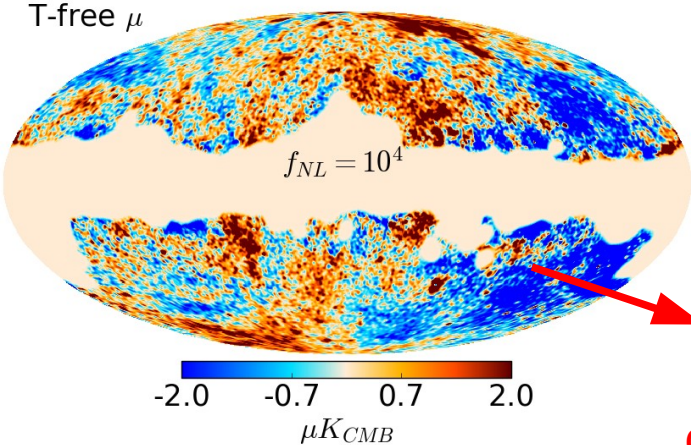
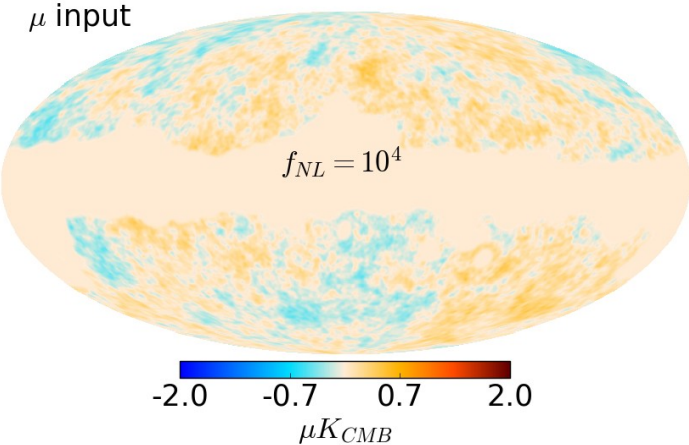
Constrained ILC μ -map reconstruction (LiteBIRD)



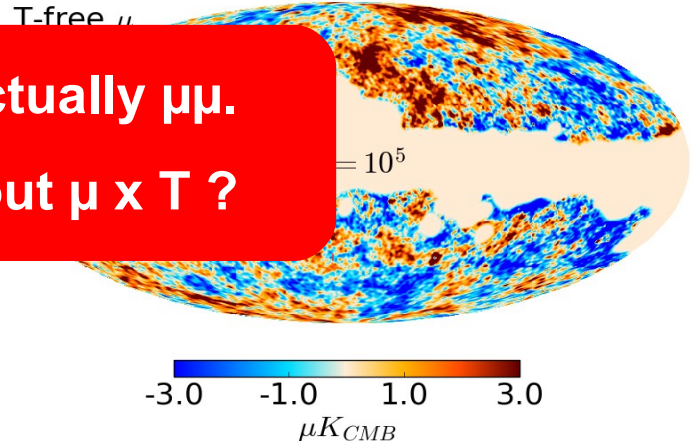
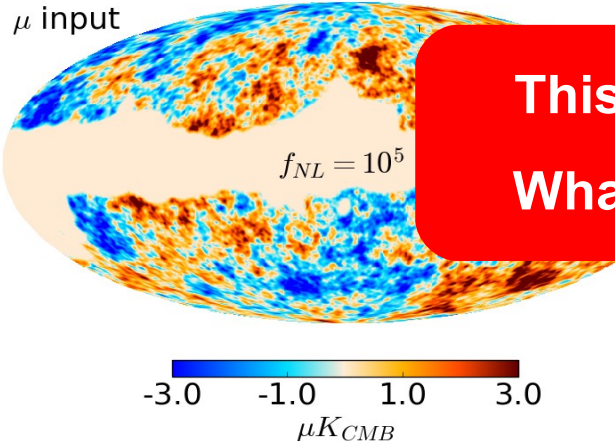
significant foreground contamination



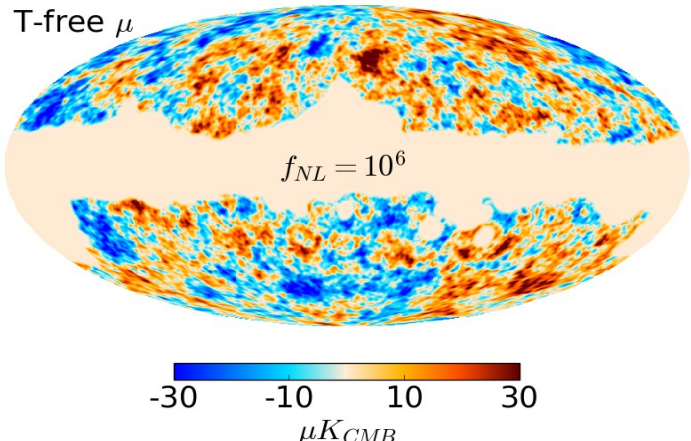
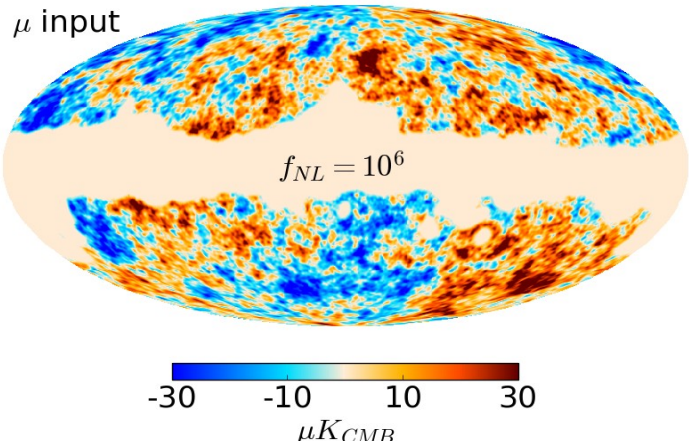
Constrained ILC μ -map reconstruction (LiteBIRD)



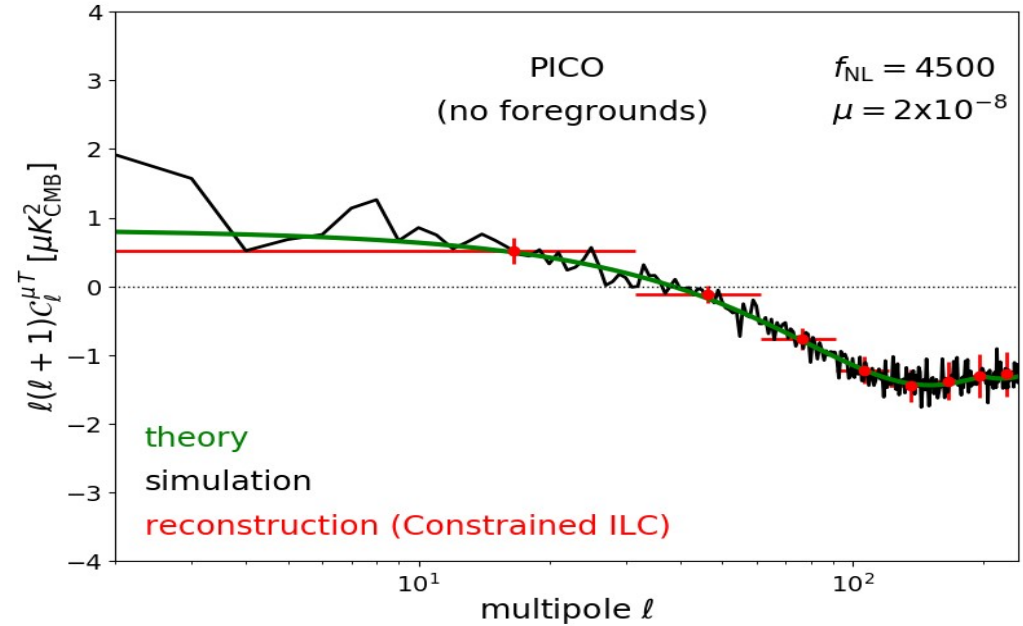
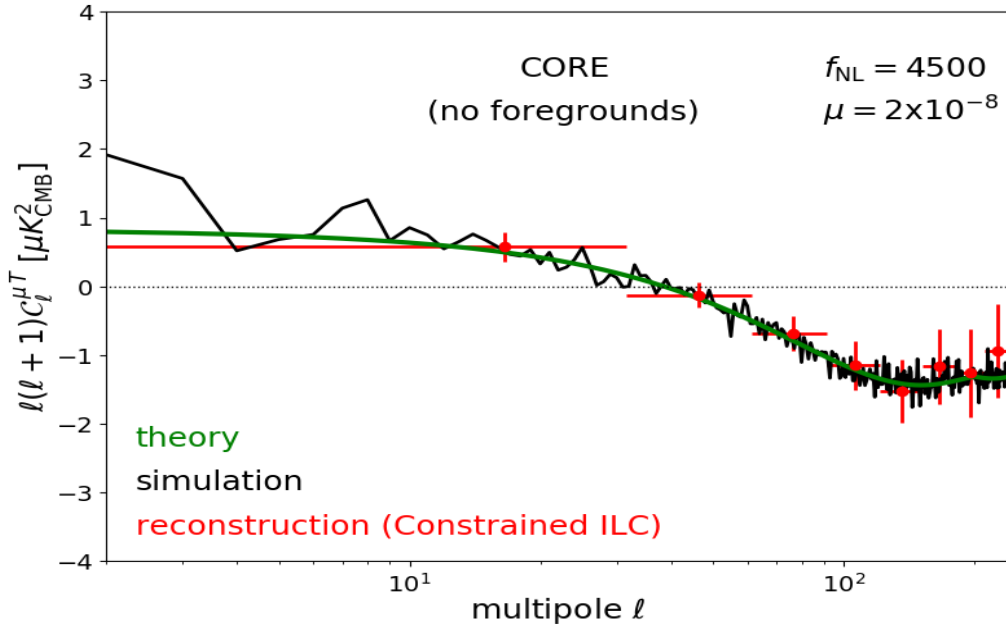
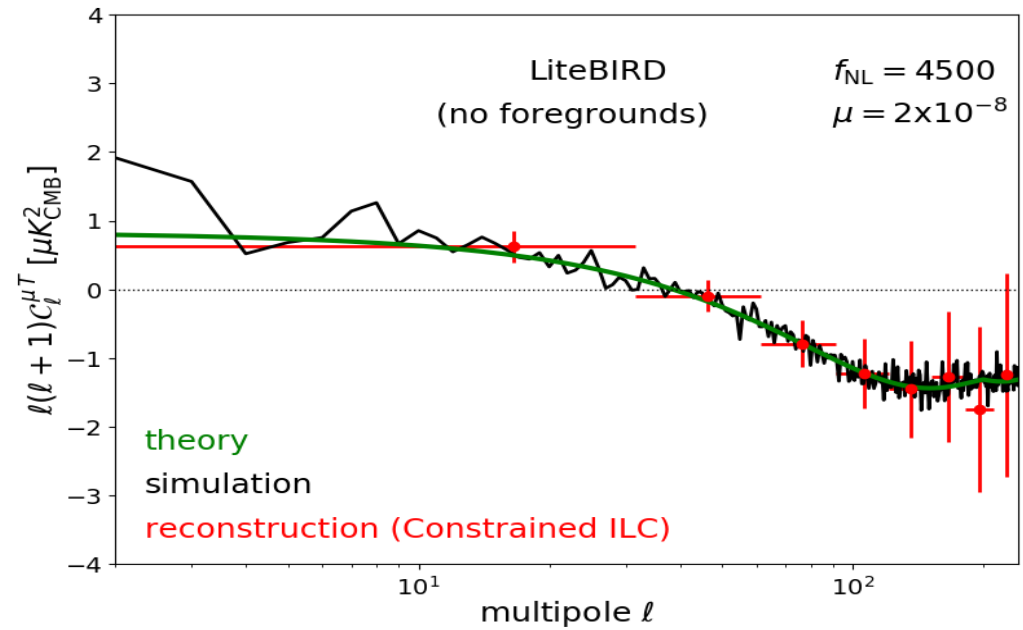
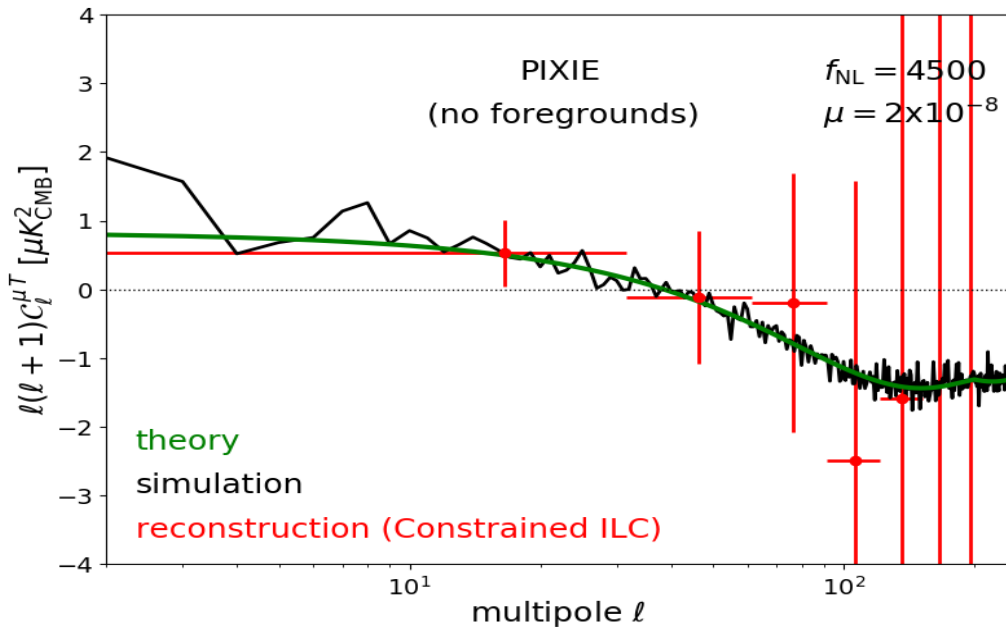
significant foreground contamination



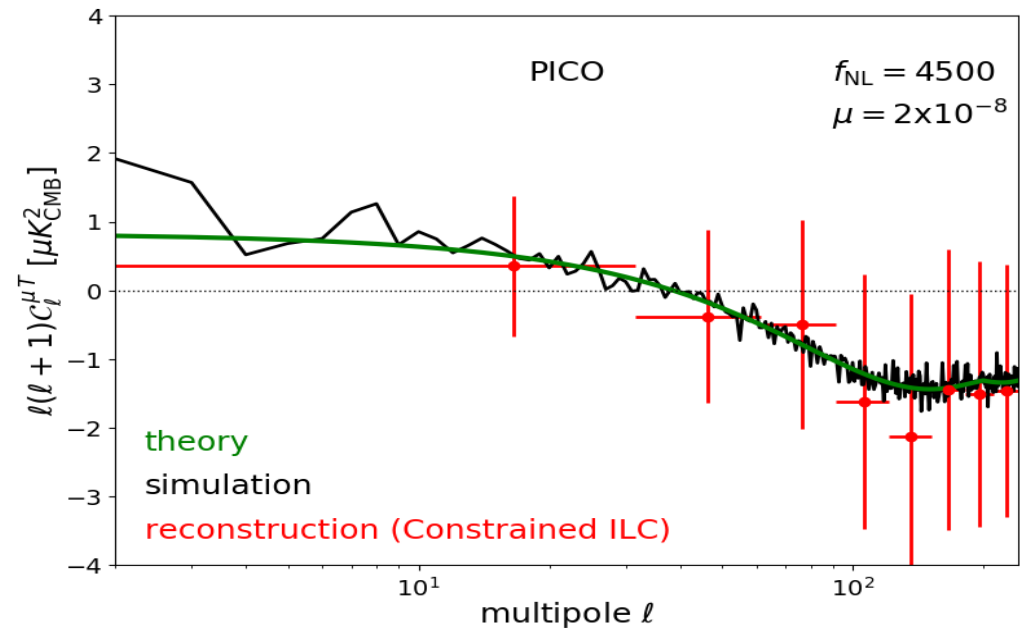
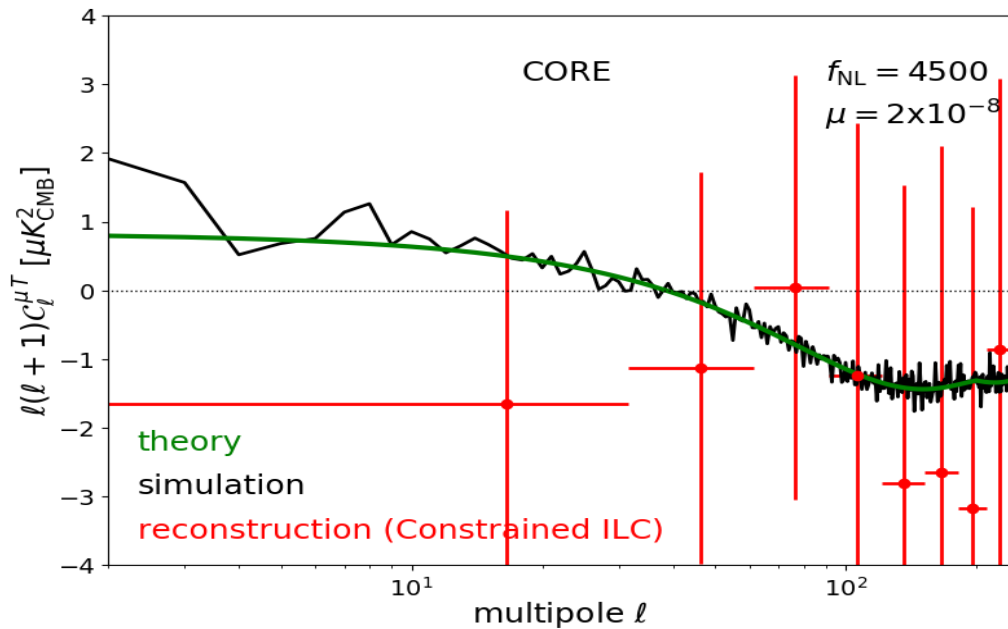
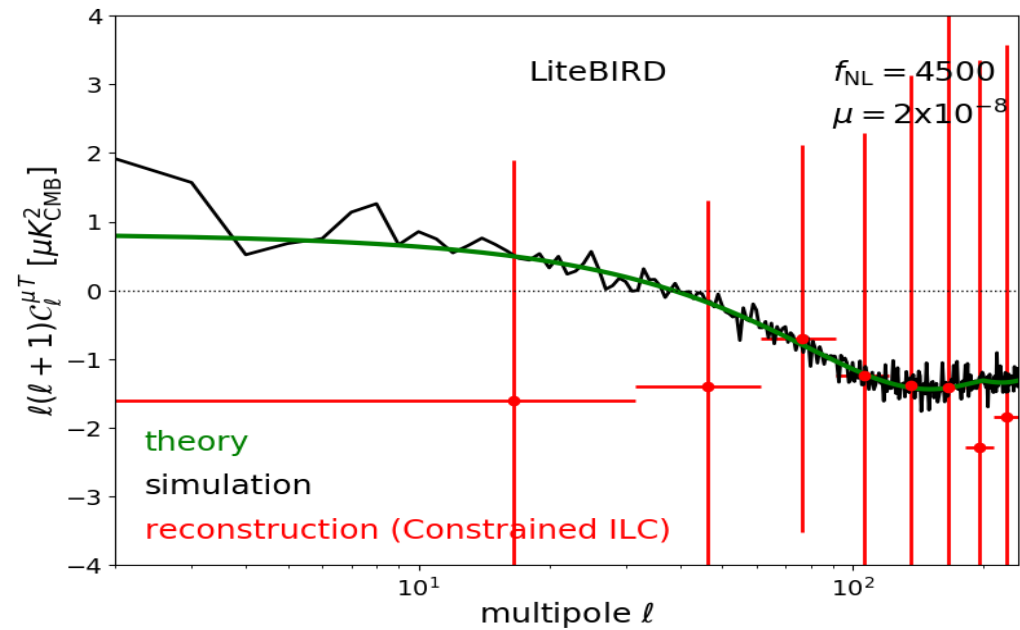
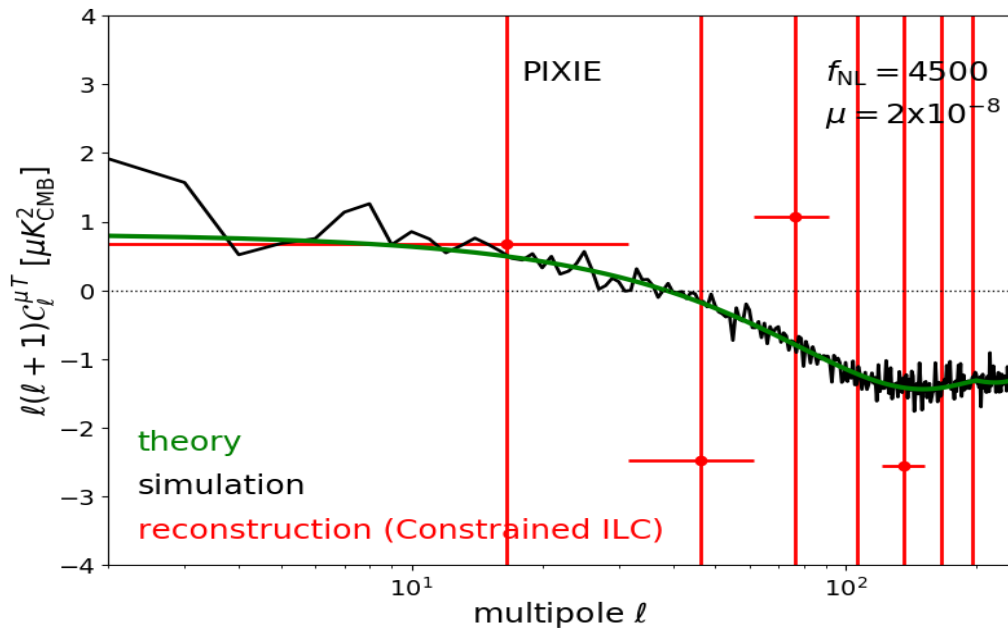
This is actually $\mu\mu$.
What about $\mu \times T$?



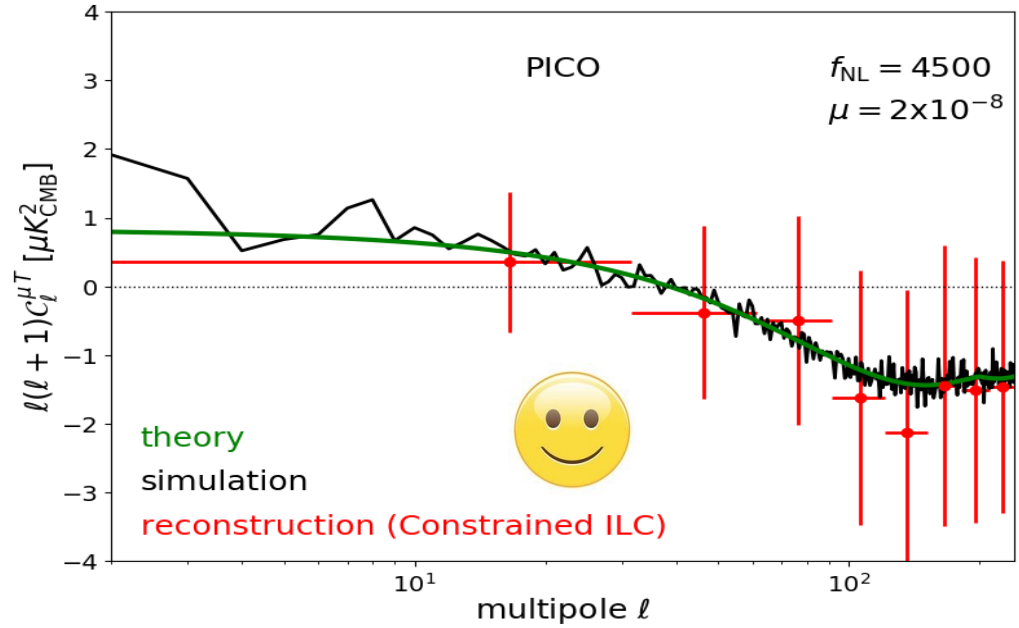
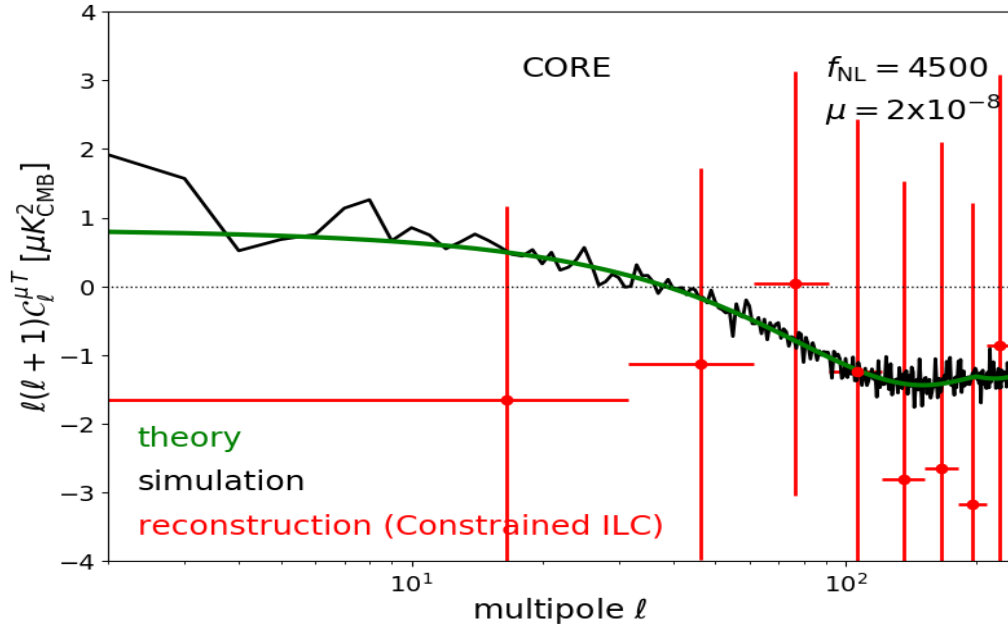
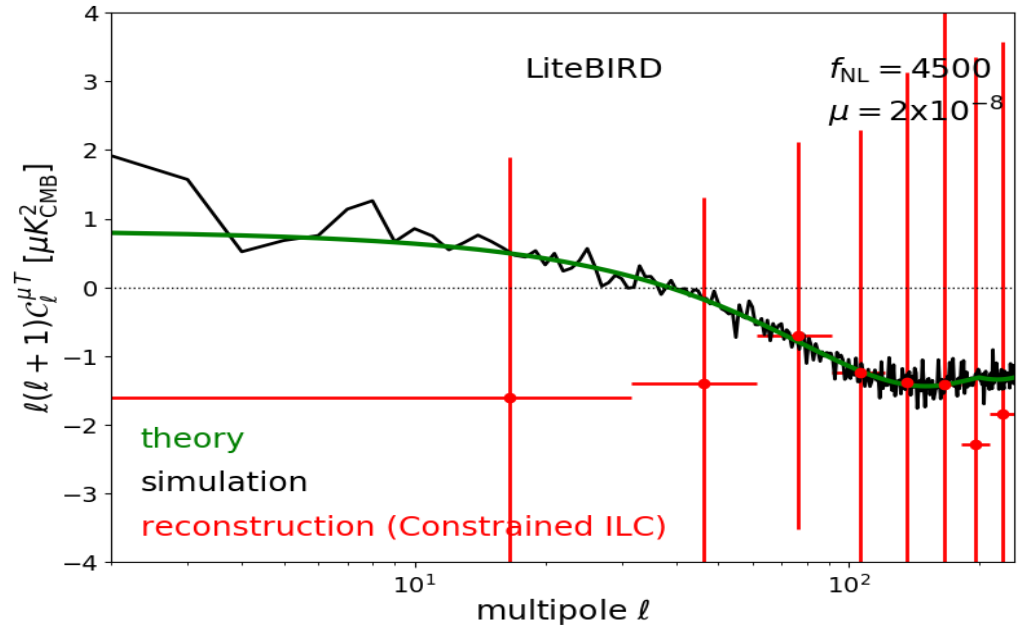
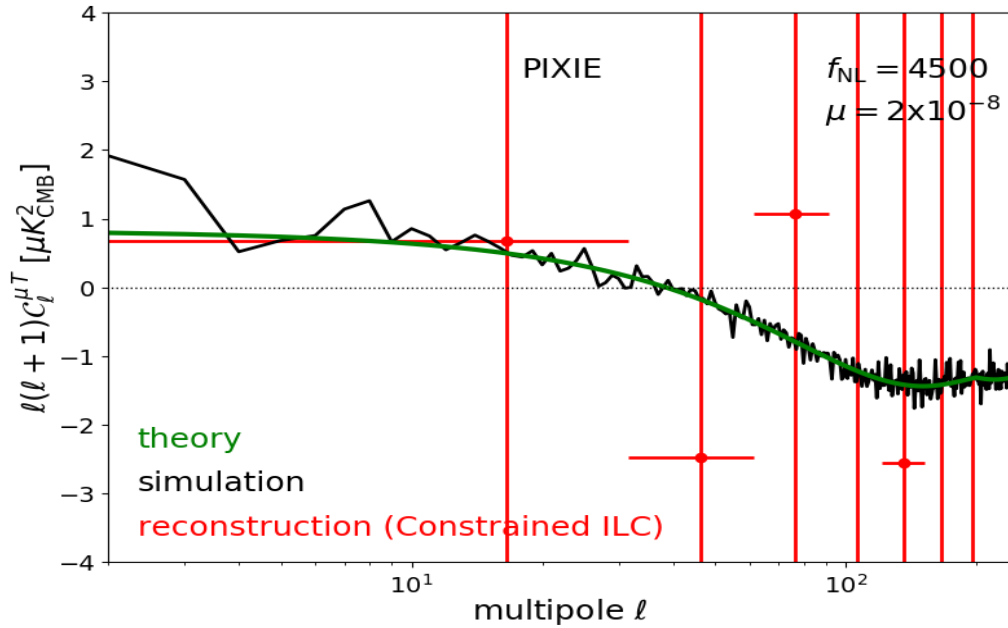
$C_{\ell}^{\mu \times T}$ reconstruction: $f_{NL} = 4500$ (w/o foregrounds)



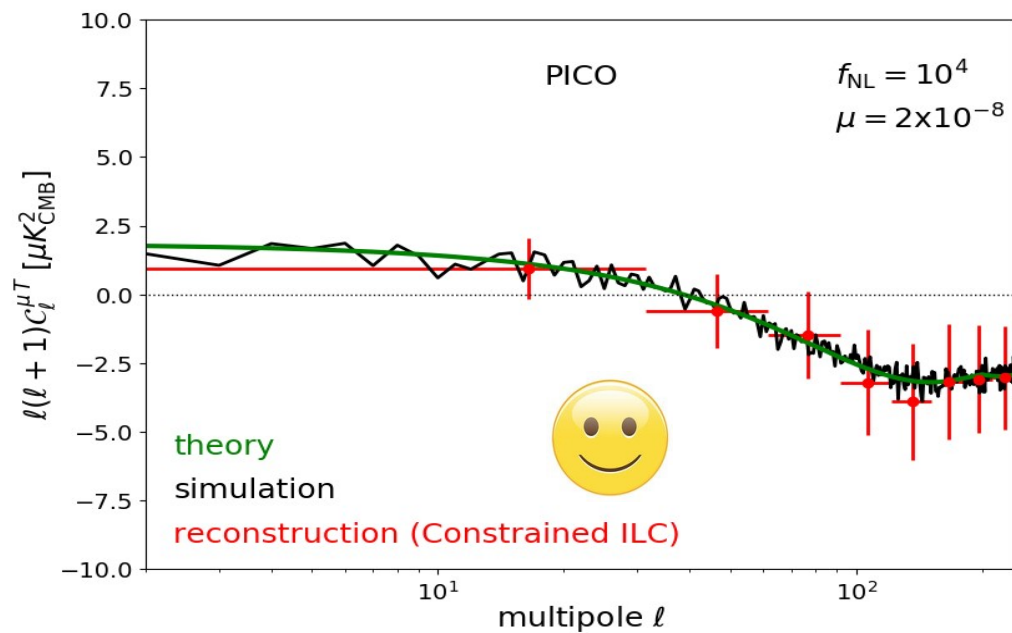
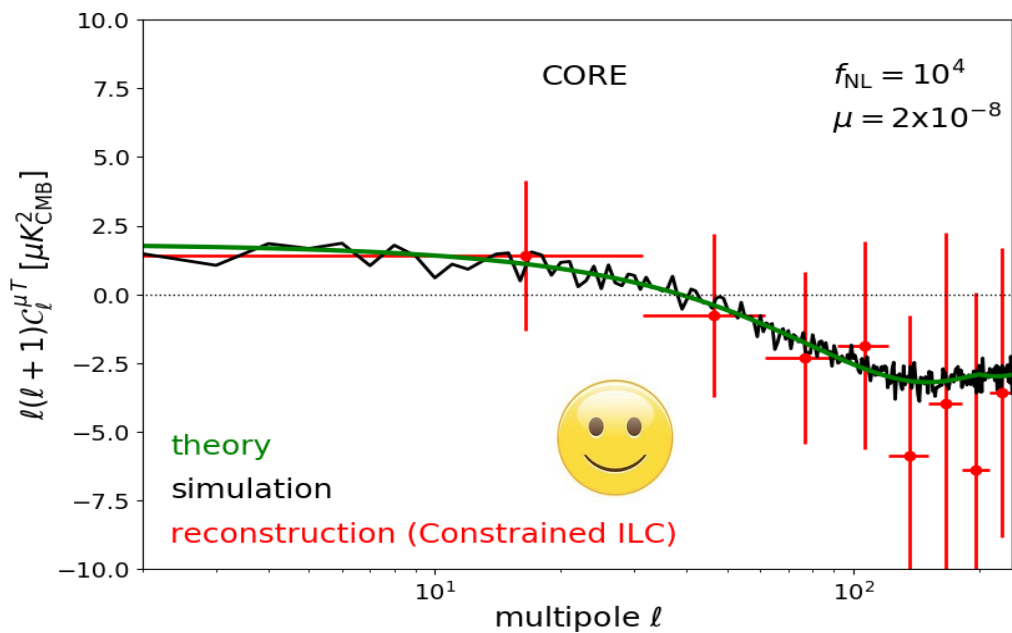
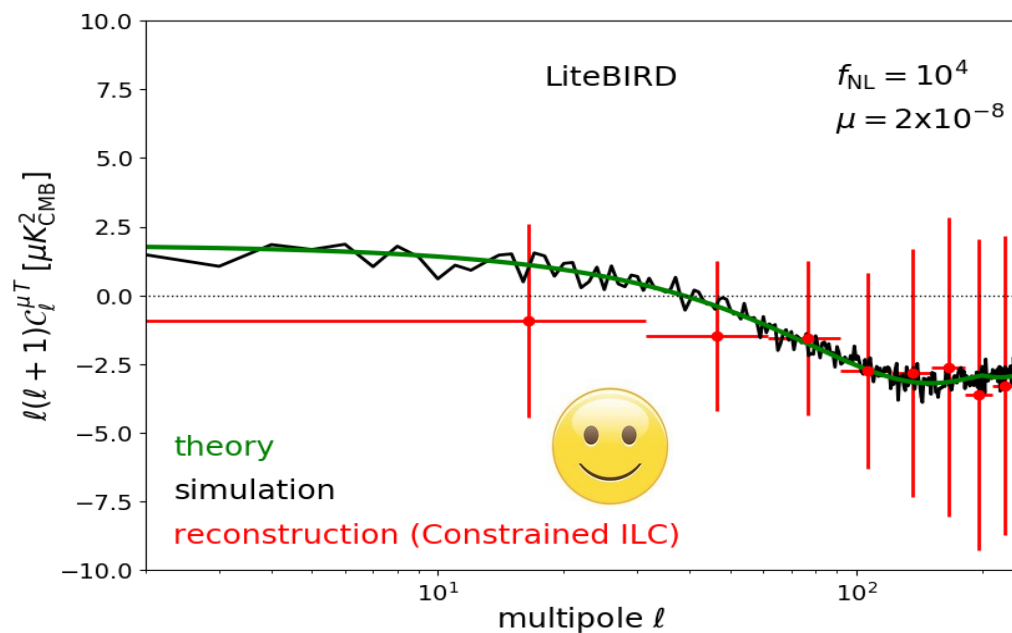
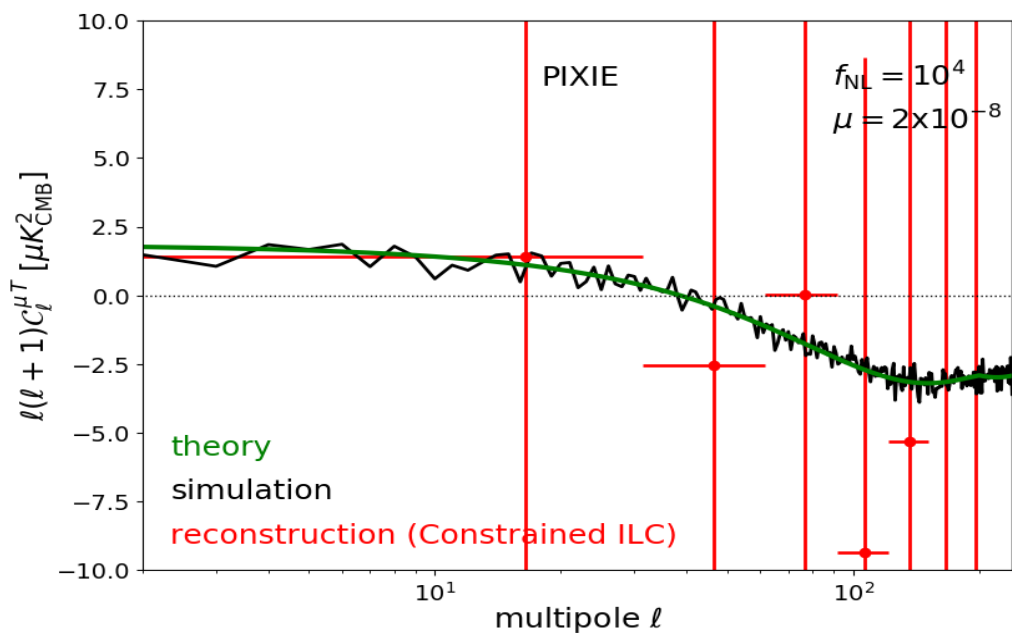
$C_{\ell}^{\mu \times T}$ reconstruction: $f_{NL} = 4500$ (with foregrounds)



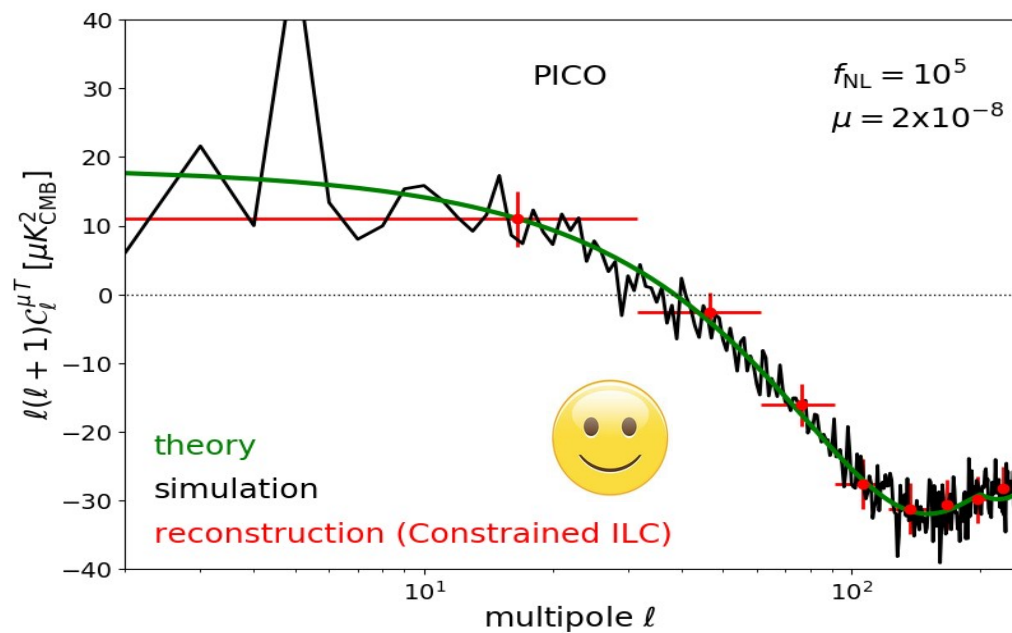
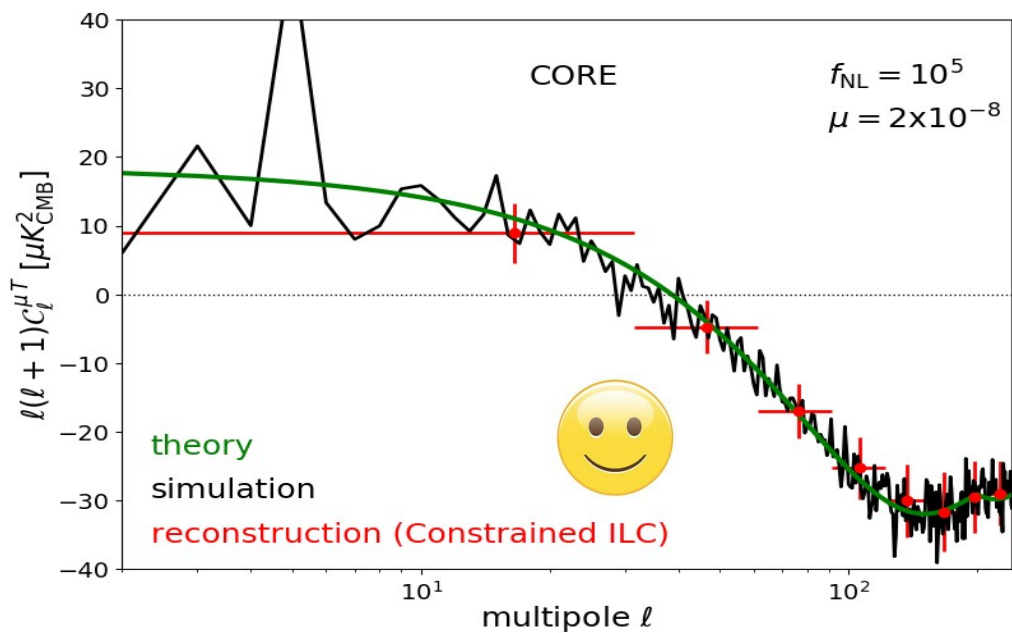
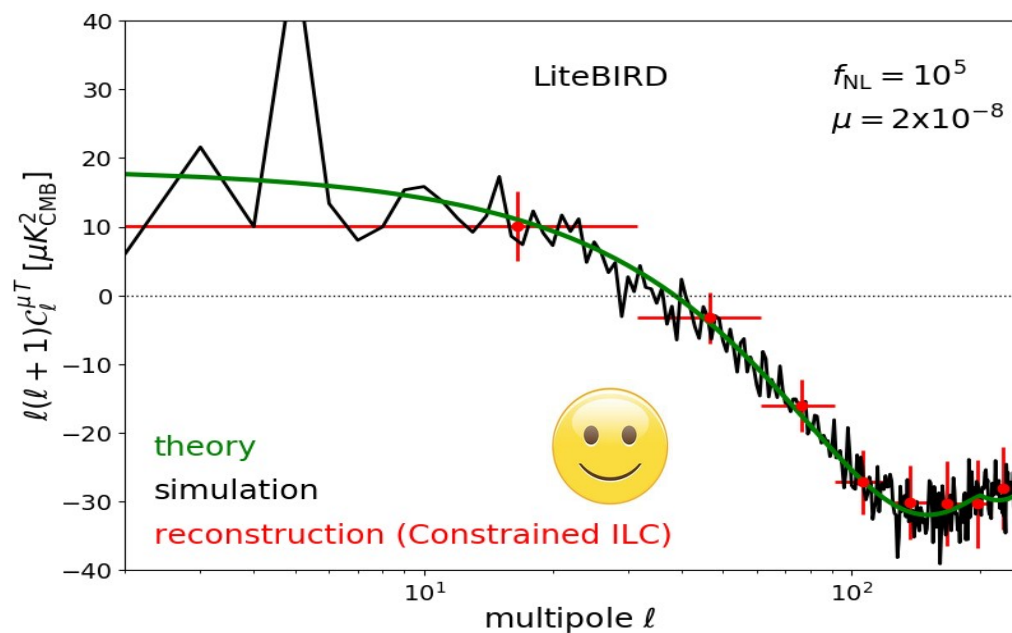
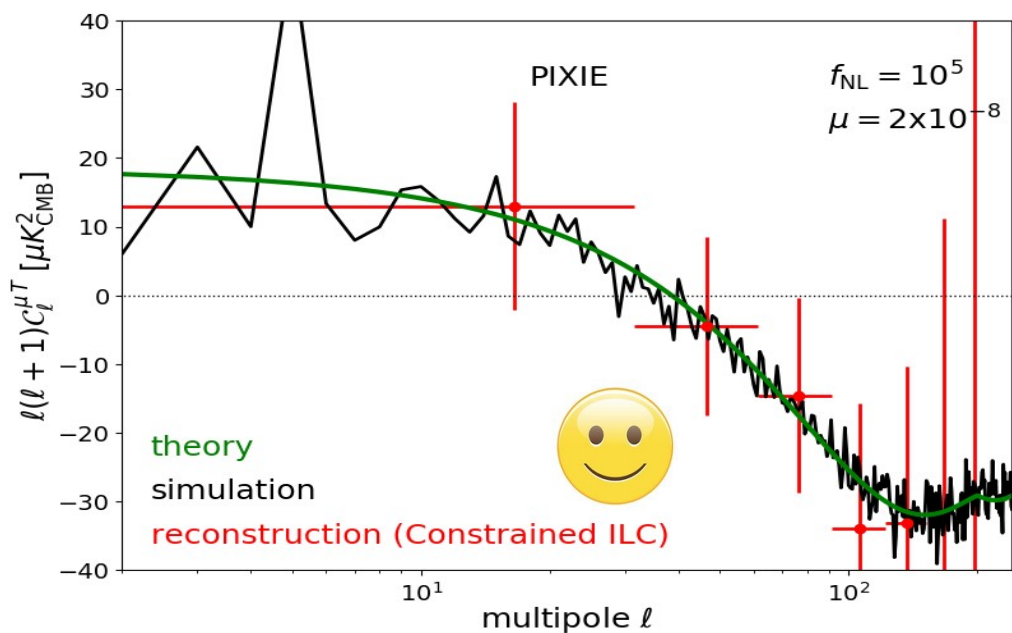
$C_{\ell}^{\mu \times T}$ reconstruction: $f_{NL} = 4500$ (with foregrounds)



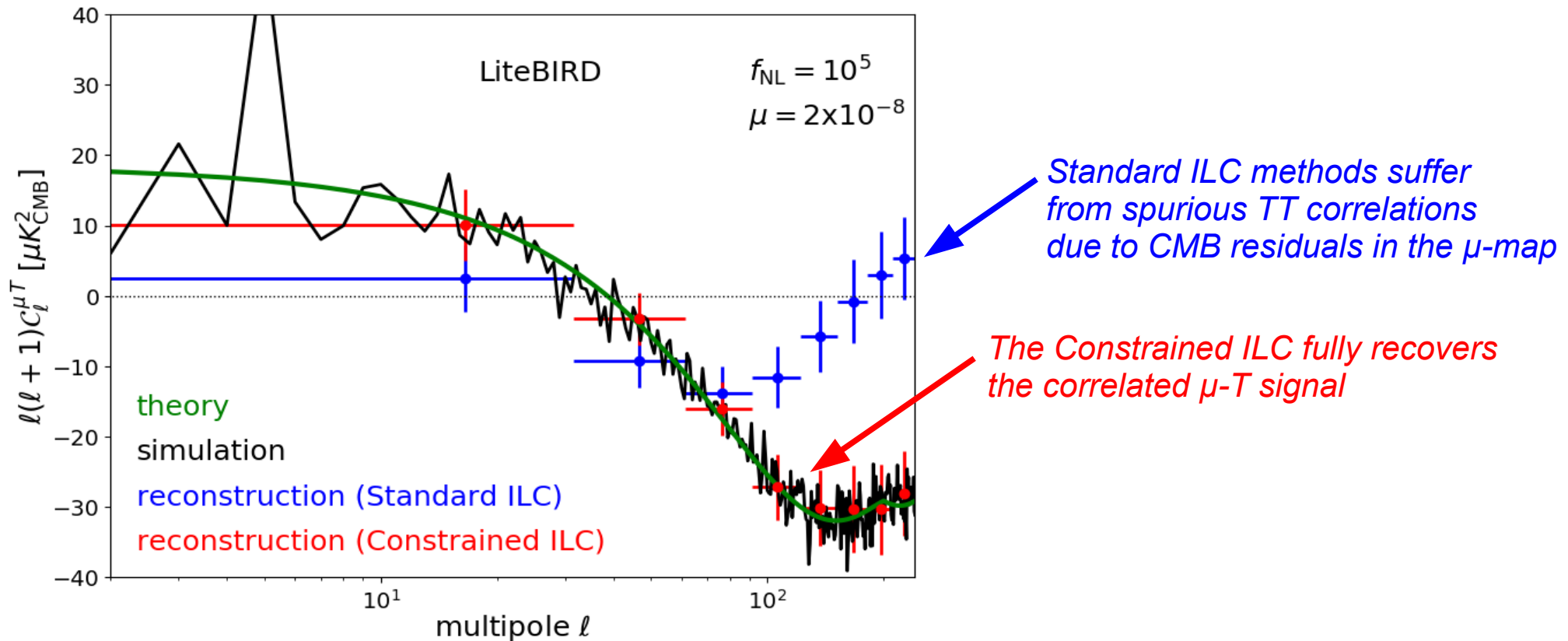
$C_\ell^{\mu \times T}$ reconstruction: $f_{NL} = 10^4$ (with foregrounds)



$C_{\ell}^{\mu \times T}$ reconstruction: $f_{NL} = 10^5$ (with foregrounds)



Standard ILC vs Constrained ILC



In light of these considerations, the constraints on μT from Planck data (Khatri & Sunyaev 2015) should be taken cautiously

Forecasts on primordial non-Gaussianity

Table 5. Detection forecasts on $f_{\text{NL}}(k \simeq 740 \text{ Mpc}^{-1})$ after component separation, based on multipoles $2 \leq \ell \leq 200$.

f_{NL} (fiducial)	10^5	10^4	4500	4500 w/o foregrounds
<i>PIXIE</i>	$(1.11 \pm 0.40) \times 10^5$ 2.5σ	$(2.17 \pm 3.90) \times 10^4$ –	$(1.5 \pm 3.9) \times 10^4$ –	4778 ± 3868 1.2σ
<i>LiteBIRD</i>	$(0.98 \pm 0.08) \times 10^5$ 12.5σ	$(0.91 \pm 0.68) \times 10^4$ 1.5σ	4272 ± 6788 –	4753 ± 930 4.8σ
<i>CORE</i>	$(0.97 \pm 0.08) \times 10^5$ 12.5σ	$(1.35 \pm 0.74) \times 10^4$ 1.4σ	5692 ± 6397 –	4336 ± 653 6.9σ
<i>PICO</i>	$(0.99 \pm 0.06) \times 10^5$ 17.8σ	$(1.07 \pm 0.30) \times 10^4$ 3.3σ	5094 ± 2929 1.5σ	4480 ± 371 12.1σ

Forecasts on primordial non-Gaussianity

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PICO is in the best position to detect the μ - T correlation signal at $f_{\text{NL}}(k=740 \text{ Mpc}^{-1}) \lesssim 4500$ in the presence of foregrounds

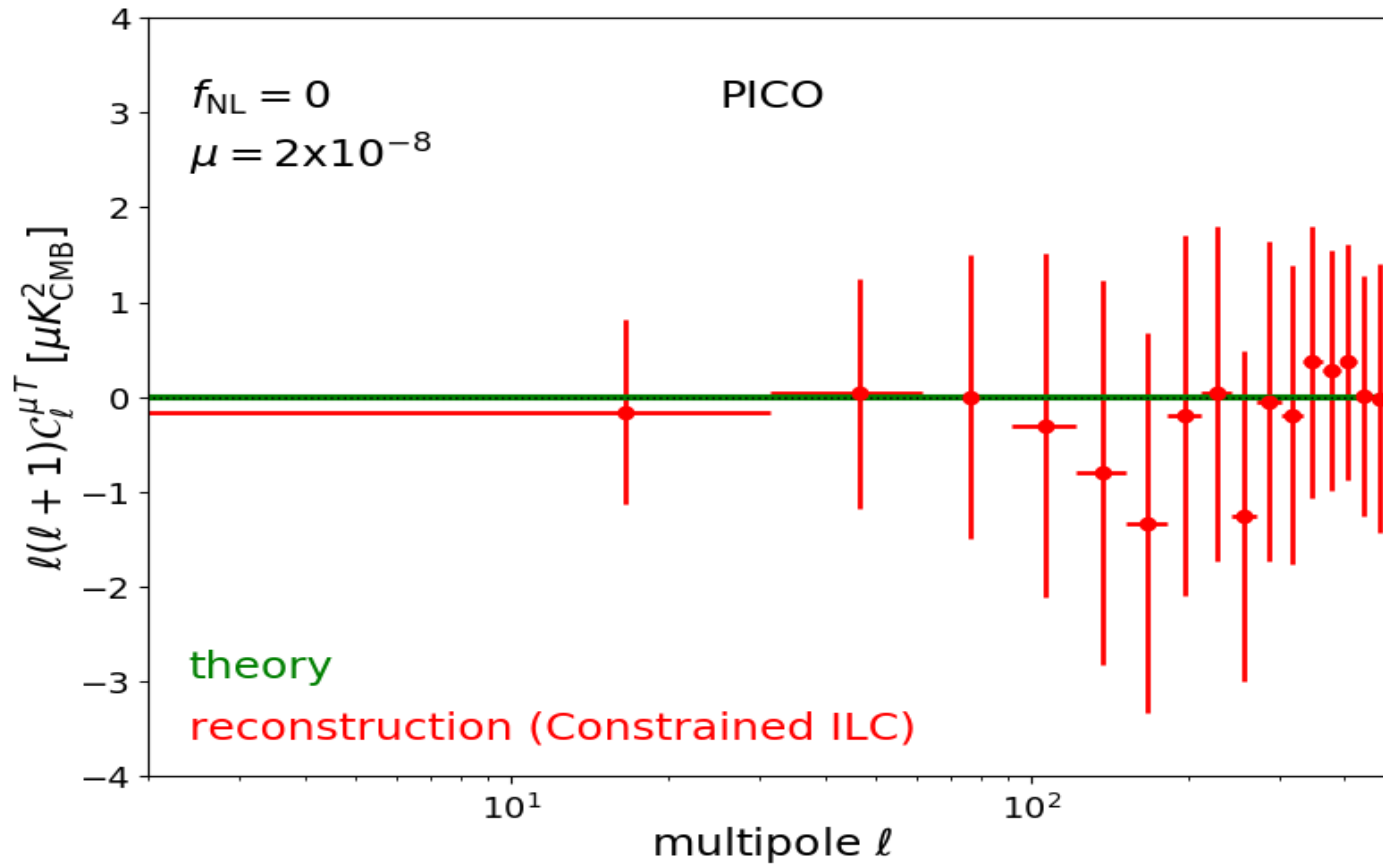
Pause

Despite a very broad frequency coverage, PIXIE results on anisotropic μ are of poorer quality than those from PICO, CORE, LiteBIRD

Why?! → *because of lower sensitivity and lower spatial resolution*

- We find that increasing PIXIE resolution from 96' to 40', while keeping the baseline sensitivity, would improve $\sigma(f_{NL})$ by 50%
 - *high-resolution channels enable using more spatially correlated information to improve foreground cleaning*
- If the foreground complexity can be captured by, say, 10 degrees of freedom, then 15-20 frequency bands are enough to remove the foregrounds
 - *In this case, the most sensitive experiments will make a difference in the ILC trade-off of minimizing the balance between foreground and noise contamination*
- If the foreground complexity relies on more than 20 degrees of freedom, then the broad frequency range of PIXIE will make a difference with respect to imagers

μ -T reconstruction for $f_{NL} = 0$



In the absence of μ -distortion anisotropies, the reconstruction by Constrained ILC is consistent with $f_{NL} = 0$

Minimum detection limit

Table 6. Detection limits for *PICO* on f_{NL} ($k \simeq 740 \text{ Mpc}^{-1}$) after component separation, based on the multipole range $2 \leq \ell \leq 500$ using the model of [Ravenni et al. \(2017\)](#) to describe the $\mu - T$ cross-correlation. Foregrounds are included in all cases and the fiducial f_{NL} parameter was varied.

f_{NL} (fiducial)	-4500	0	4500
<i>PICO</i>	-2996 ± 2112 2σ	1325 ± 2114 -	5698 ± 2121 2σ

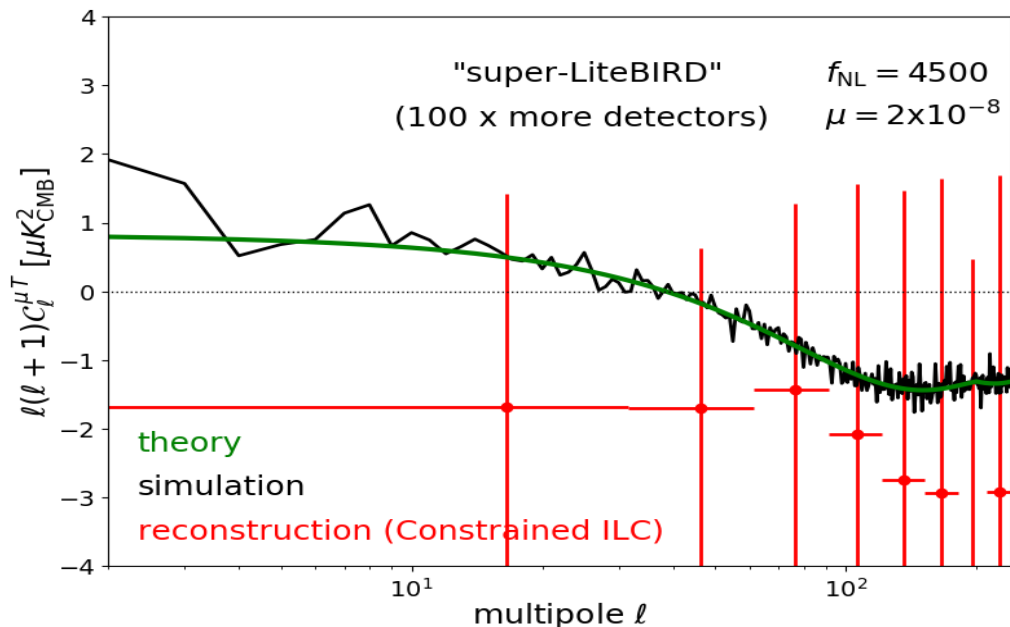
Minimum detection limit by PICO in the presence of foregrounds:

$$|f_{\text{NL}}| \leq 2114$$

More detectors or more frequencies?

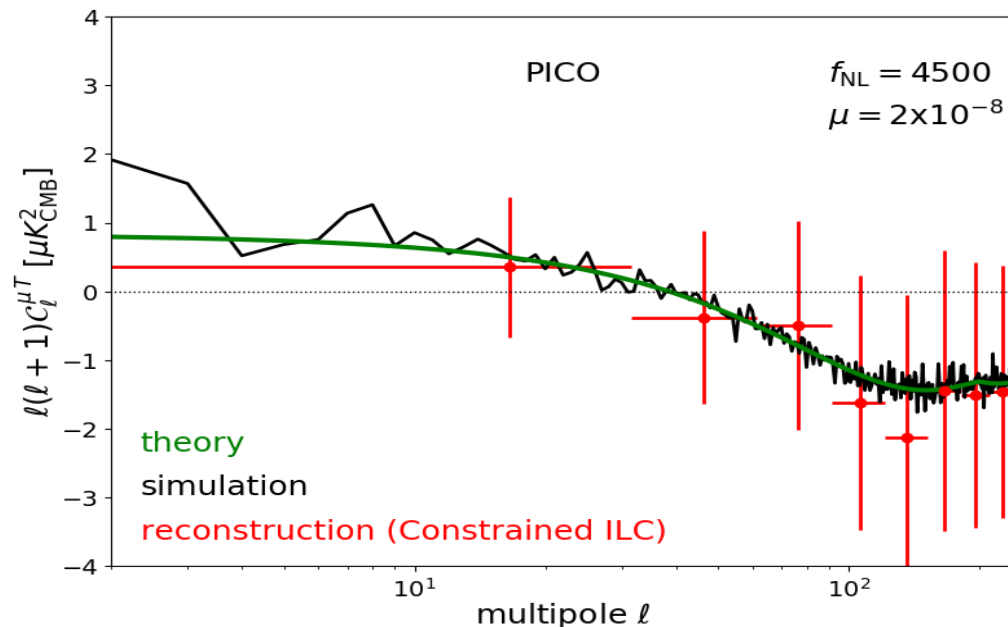
“Super-LiteBIRD” with 100 x more detectors

40 – 400 GHz, 0.2 $\mu\text{K}\cdot\text{arcmin}$



PICO baseline

20 – 800 GHz, 0.8 $\mu\text{K}\cdot\text{arcmin}$



Extended frequency coverage at frequencies $\nu \leq 40$ GHz and $\nu \geq 400$ GHz provides more leverage than increased channel sensitivity

What part of the frequency range matters?

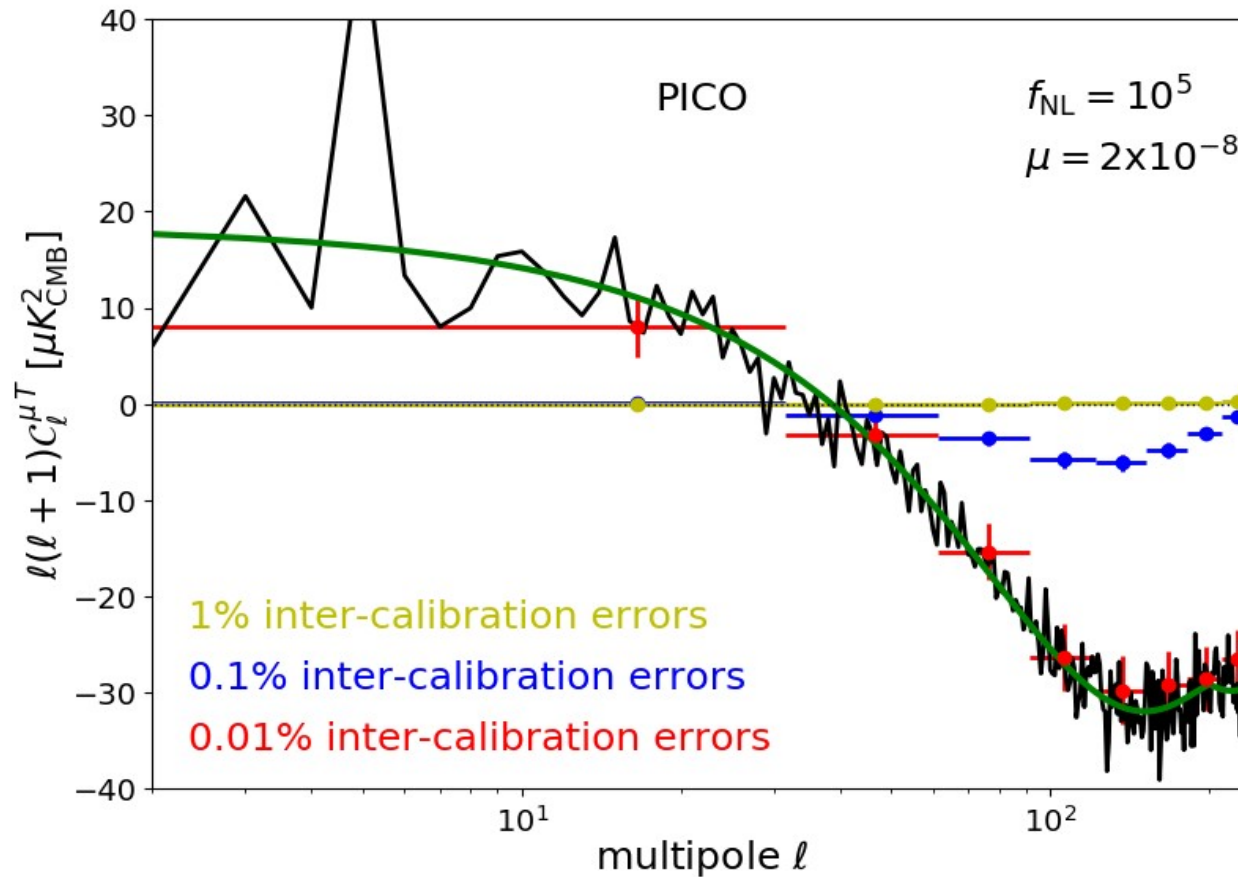
- Discarding PICO frequencies above $\nu > 400$ GHz degrades our component separation results by $\sim 7\%$
- Discarding PICO frequencies below $\nu < 40$ GHz degrades our component separation results by $\sim 30\%$

Low-frequencies $\nu \leq 40$ GHz have more constraining power for μ -distortion anisotropies than high-frequencies above $\nu \geq 400$ GHz

Remazeilles & Chluba (2018)

→ *consistent with the conclusions of Abitbol et al (2017) for monopole distortions*

Impact of inter-calibration errors



Dick, Remazeilles, Delabrouille, MNRAS (2010):

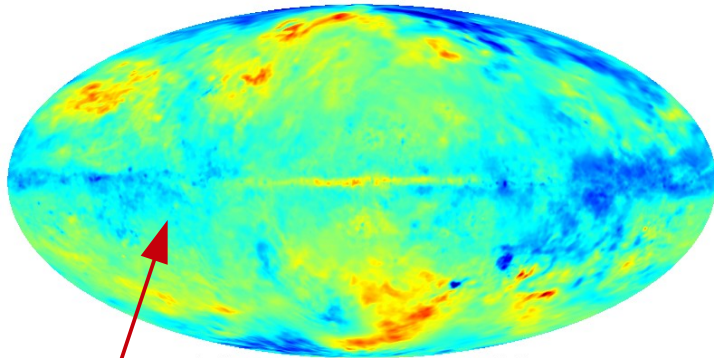
“ Calibration errors can screw up the ILC in the high signal-to-noise regimes, through partial cancellation of the variance of the CMB temperature map ”

The allowed inter-channel calibration uncertainty for PICO is 0.01 %

(The promise of CORE is to achieve such calibration accuracy)

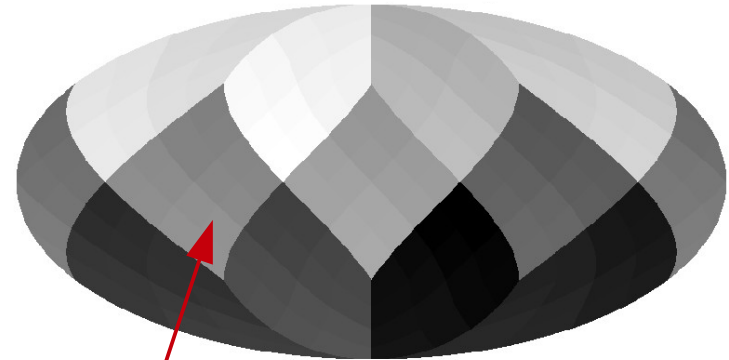
Averaging effects

dust spectral indices in the sky



one value β_{dust} per line-of-sight

mapping / pixelization



many β_{dust} values per pixel
→ effective SED: $\sum_i v^{\beta_i} \neq v^{\beta}$

- Because of averaging different line-of-sight SEDs within a pixel/beam, the actual SED of foregrounds *in the maps* will differ from the physical SED *in the sky* – [Chluba et al 2017](#)
- Spurious SED curvatures created by pixel averaging effects, if ignored in the parametric fit, have been shown to bias primordial B-modes at the level of $\Delta r \sim 10^{-3}$ – [Remazeilles et al 2017, for the CORE collaboration](#)
- The “Constrained ILC” is blind (no parametrization / assumption on foregrounds), so fairly insensitive to averaging effects

Conclusions

Remazeilles & Chluba (2018)

- We have computed the first forecasts on the detection of the **μ -T correlation signal and f_{NL} ($k \approx 740 \text{ Mpc}^{-1}$) in the presence of foregrounds with future CMB satellites**
- We have proposed a tricky component separation approach (**Constrained ILC**) to null the CMB contamination in μ , which otherwise biases the μ -T correlation signal
- Among the CMB satellite concepts, **PICO** is in the best position to control foregrounds and detect anisotropic μ -type distortions with **$f_{\text{NL}}(740 \text{ Mpc}^{-1}) \lesssim 2100$**
- Optimization: more detectors or more frequencies?

Extended frequency coverage at frequencies $\nu \leq 40 \text{ GHz}$ and $\nu \geq 400 \text{ GHz}$ provides more leverage than increased channel sensitivity

Low-frequencies $\nu \leq 40 \text{ GHz}$ have more constraining power on anisotropic μ -distortions than high-frequencies $\nu \geq 400 \text{ GHz}$

- Absolute calibration / FTS like PIXIE still needed for μ -distortion anisotropies to break the $f_{\text{NL}}^* \langle \mu \rangle$ degeneracy

Thank you for your attention!