

# Electroweak Physics at LHeC & FCC-eh



Comprendre le monde,  
construire l'avenir



Zhiqing ZHANG  
with inputs from  
D. Britzger & M. Klein



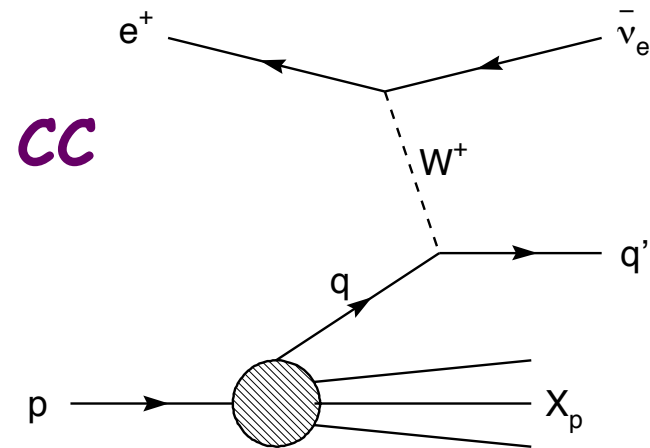
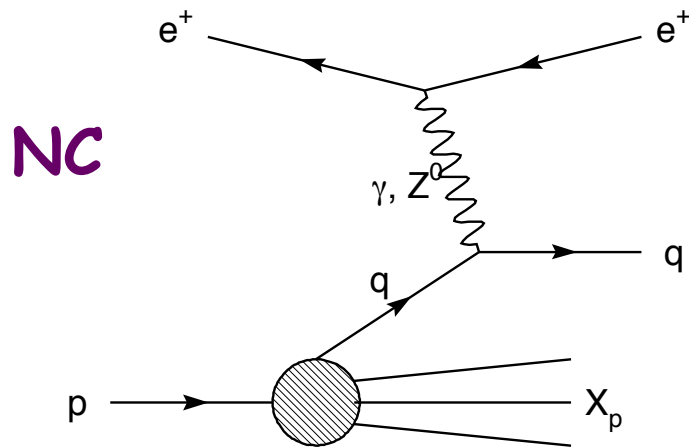
## Outline

- Introduction
- Selected examples
- Summary

# Introduction

- EW physics is an important part of the LHeC/FCC-eh physics program
- LHeC/FCC-eh can significantly enrich the physics program of an  $e^+e^-$  and/or a pp collider
- HERA is a good example for some of the EW measurements
- LHeC/FCC-eh can however overcome all weak points of HERA:
  - Small EW phase space
  - Small cross section
  - Low luminosity

# Neutral and Charged Current Processes



➤ Dominant hard processes at ep colliders

➤ Event kinematics:

$Q^2 = -q^2$ : Boson virtuality

$x$ : momentum fraction of struck parton

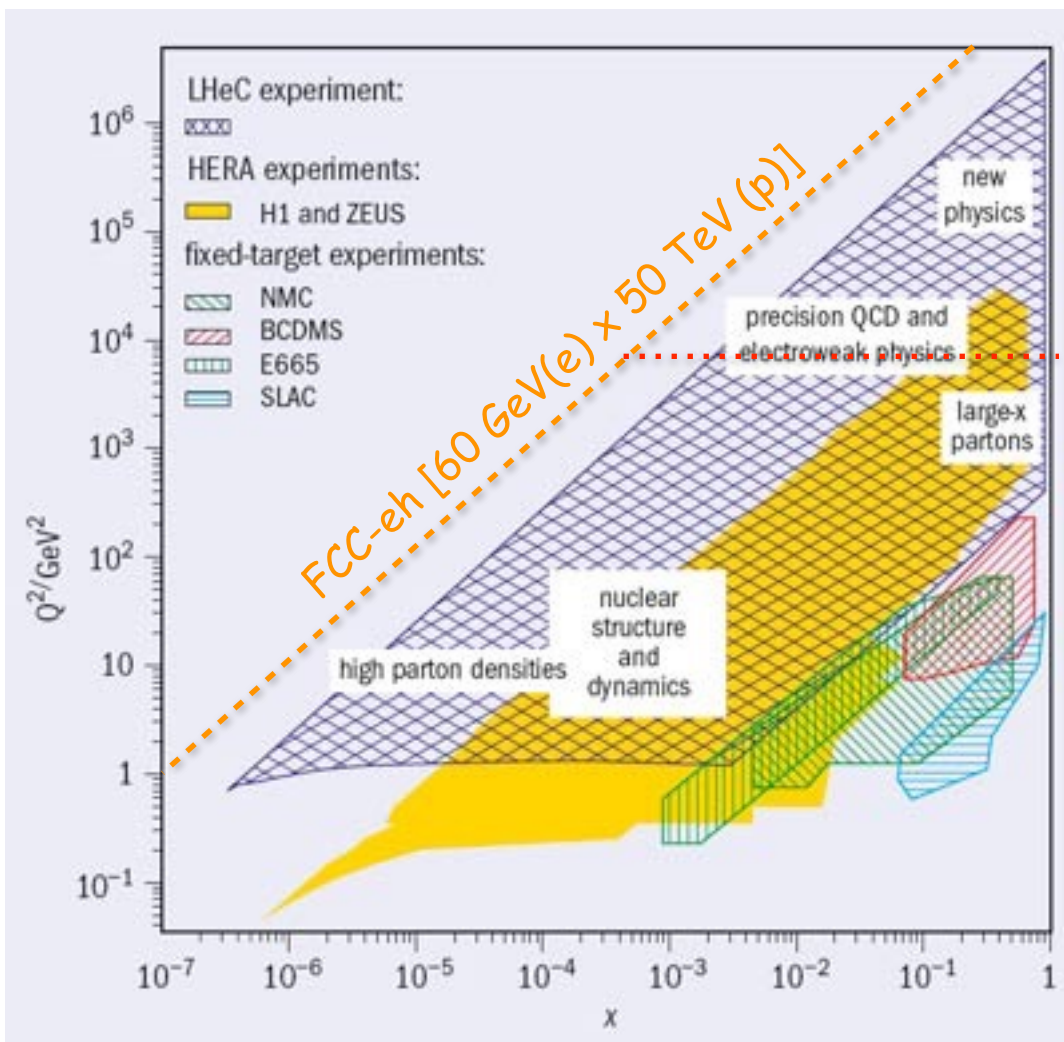
$y = Q^2/sx$ : inelasticity

can be precisely determined (for NC in particular using different methods)

# Kinematic Coverage of HERA, LHeC and FCC-eh

Modified from

Klein-Newman, CERN Cour. 49N3 (2009) 22



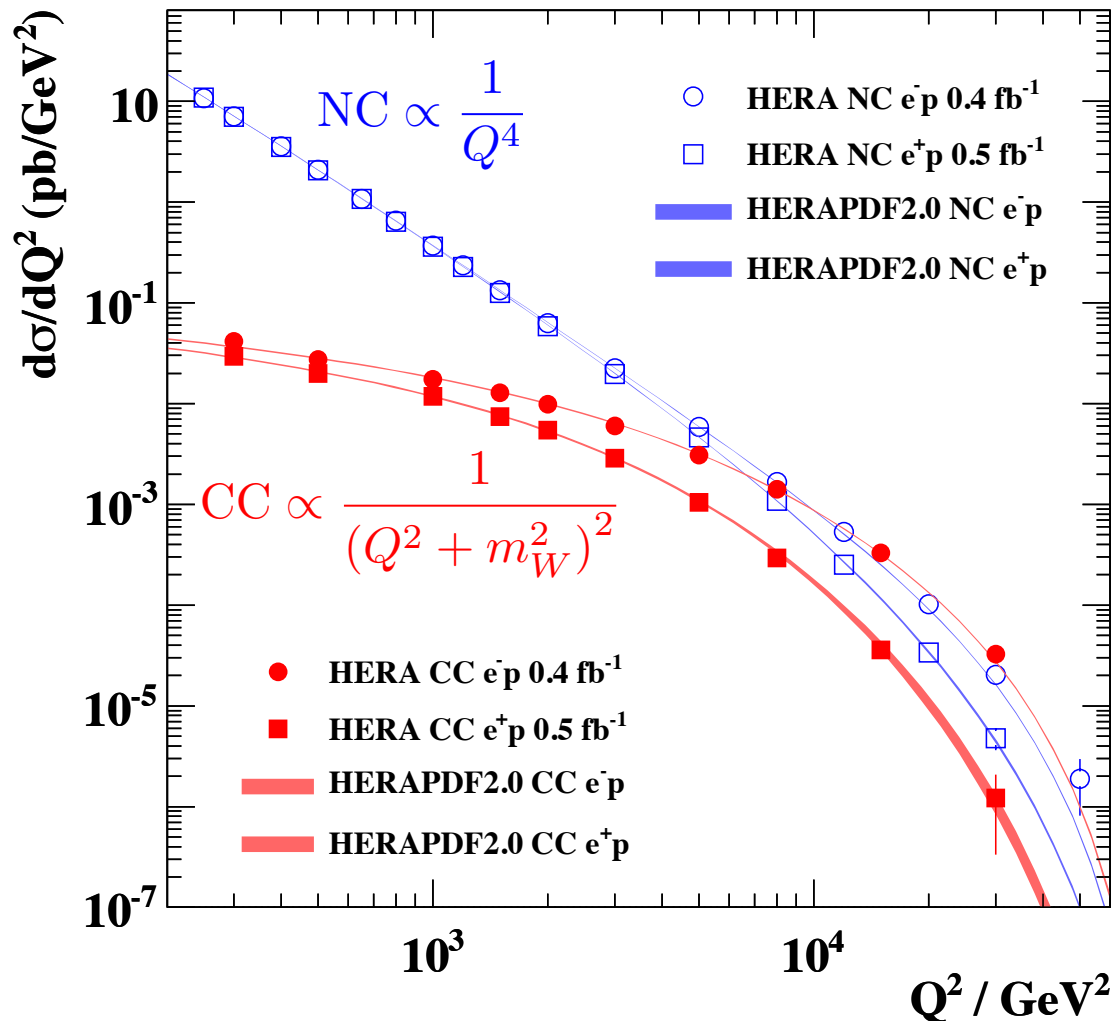
► HERA barely reached pure EW regime + low cross sections (next slide) & low luminosity

► LHeC has a big EW phase space +  $> 10^2$  increase in lumi

► FCC-eh has further extension

# Q<sup>2</sup> Dependence of NC and CC Cross Sections

## H1 and ZEUS



EPJC75 (2015) 580, arXiv:1506.06042

One HERA legacy plot shows that NC and CC cross sections at high Q<sup>2</sup> are tiny

→ HERA (EW) data were statistically limited

→ Need much higher luminosity for precision EW measurements

# Simulated Data Samples

## □ Simulated NC and CC cross sections

- Pseudo-data applicable for both EW and QCD studies

## □ Correlated and uncorrelated syst. and stat. errors

- Numerical treatment of errors [PHE-1990-02, Blümlein-Klein]

source of uncertainty	error on the source or cross section
scattered electron energy scale $\Delta E'_e/E'_e$	0.1 %
scattered electron polar angle	0.1 mrad
hadronic energy scale $\Delta E_h/E_h$	0.5 %
calorimeter noise (only $y < 0.01$ )	1-3 %
radiative corrections	0.5%
photoproduction background (only $y > 0.5$ )	1 %
global efficiency error	0.7 %

- Assumptions gauged with H1 (best achieved values)
- Total cross section errors typically: 0.8% at low-x and 2% at high-x
- Simulated data have full syst. error
- Luminosity measurement ~1% (0.5% may be reachable)

# Updated MC Samples

## FCC-eh (LHeC)

	NC/CC	$E_e$ [GeV]	$E_p$ [TeV]	$P(e)$	charge	lumi. [ $\text{fb}^{-1}$ ]
$e^- L$	NC	60 (60)	50 (7)	-0.8	-1	1000
	CC	60 (60)	50 (7)	-0.8	-1	1000
$e^- R$	NC	60 (60)	50 (7)	+0.8	-1	300
	CC	60 (60)	50 (7)	+0.8	-1	300
$e^+$	NC	60 (60)	50 (7)	0	+1	100
	CC	60 (60)	50 (7)	0	+1	100
$e^- \text{ low } E$	NC	20 (60)	7 (1)	0	-1	100
	CC	20 (60)	7 (1)	0	-1	100

\* second and third columns show FCC-eh (LHeC)

(M.Klein)

### error assumptions:

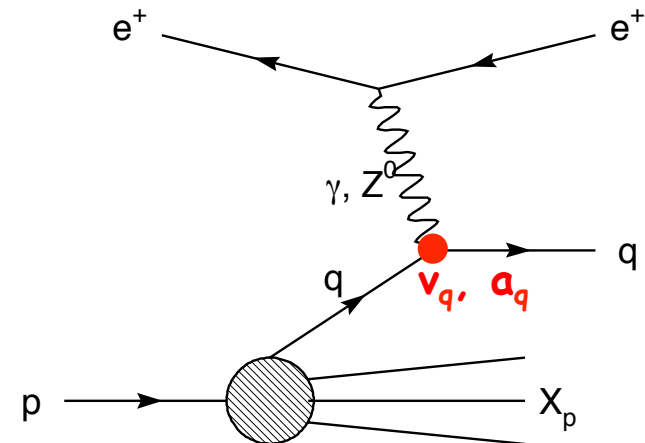
elec. scale: 0.1%; hadr. scale 0.5%

radcor: 0.3%;  $\gamma p$  at high  $y$ : 1%

uncorrelated extra eff. 0.5%

# Light Quark Couplings $v_q, a_q$ to Z Boson

- $v_q, a_q$  treated as free EW parameters
- Perform combined EW + PDF fit to inclusive NC and CC cross section "data"
  - to take into account EW/PDF correlation



- PDF parameterisation a la HERAPDF

- EW calculations performed in on-mass shell scheme:  
 $(\alpha_{em}, m_Z, m_W) + \Delta r$   
with  
 $\Delta r = \Delta r(\alpha_{em}, m_W, m_Z, m_t, m_H, \dots)$



# Cross Sections, Structure Functions, Couplings

Klein and Riemann, Electroweak interactions probing the nucleon structure, Z. Phys.C 24 (1984) 151.

$$\frac{d^2\sigma_{\text{NC}}^{\pm}}{dx dQ^2} \sim Y_+ \tilde{F}_2 \mp Y_- \tilde{F}_3 - y^2 \tilde{F}_L \quad \text{with} \quad Y_{\pm} = 1 \pm (1-y)^2$$

$\gamma$  exchange

$\gamma Z$  interference

Z exchange

$$\tilde{F}_2 = F_2 - (\cancel{v_e} - P_e a_e) \kappa_Z F_2^{\gamma Z} + (\cancel{v_e^2} + a_e^2 - \cancel{2P_e v_e a_e}) \kappa_Z^2 F_2^Z$$

$v_e \sim 0$ ,  $\rightarrow$  some of the terms are negligible

$$x \tilde{F}_3 = -(a_e - \cancel{P_e v_e}) \kappa_Z x F_3^{\gamma Z} + [2\cancel{v_e} a_e - P_e (\cancel{v_e^2} + a_e^2)] \kappa_Z^2 x F_3^Z$$

$$\left[ F_2, F_2^{\gamma Z}, F_2^Z \right] = x \sum_q \left[ e_q^2, 2e_q v_q, v_q^2 + a_q^2 \right] \{q + \bar{q}\}$$

$$\kappa_Z^{-1} = \frac{2\sqrt{2}\pi\alpha}{G_F M_Z^2} \frac{Q^2 + M_Z^2}{Q^2}$$

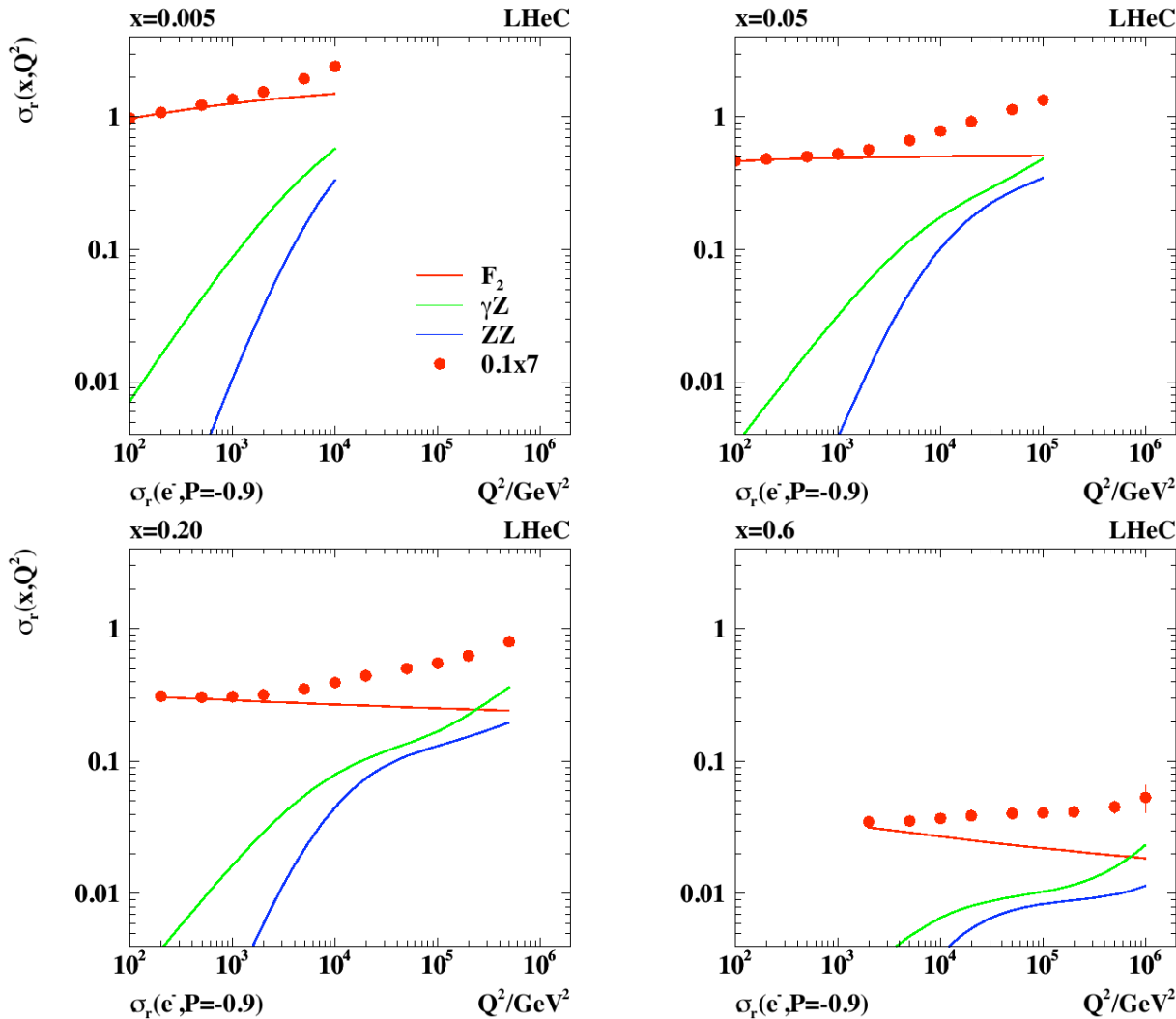
$$\left[ x F_3^{\gamma Z}, x F_3^Z \right] = 2x \sum_q \left[ e_q a_q, v_q a_q \right] \{q - \bar{q}\}$$

Structure function formulae given for e-p scattering, for e+p,  $P_e \rightarrow -P_e$

CC cross sections have similar but different structure functions and PDF combinations

$F_L = 0$  in LO parton model,  $F_L \sim g$  at NLO

# Relative Contributions of Different Terms



Plots from CDR (old settings/samples) but features remain valid:

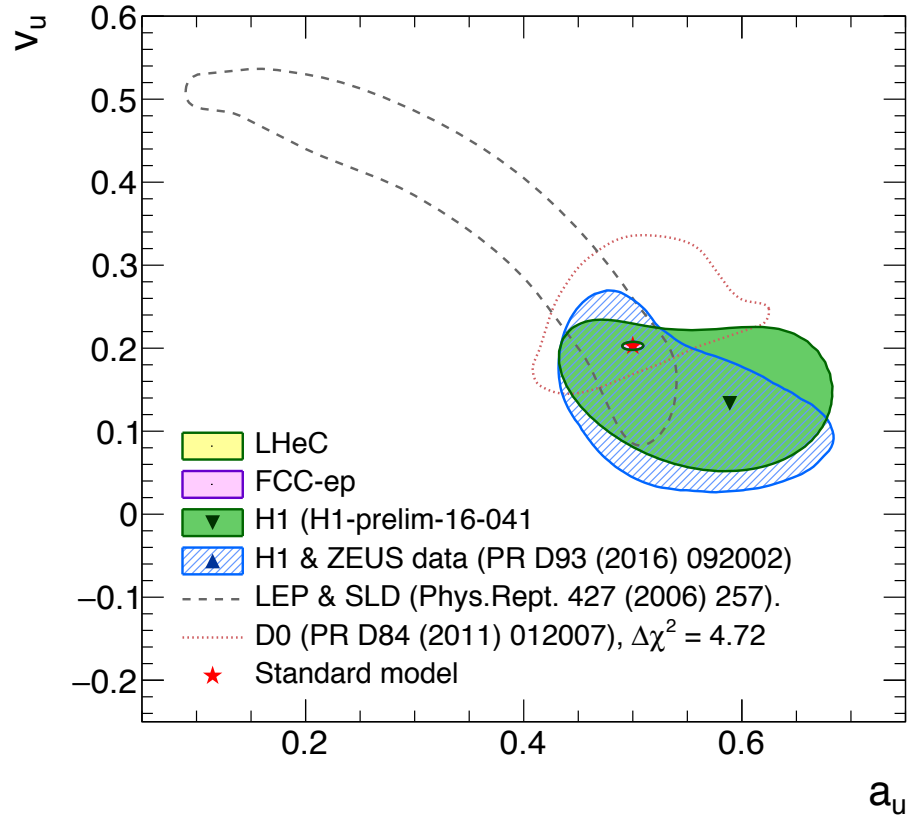
→ increasing EW effects as  $Q^2$  increases

→ reach/exceed photonic contributions

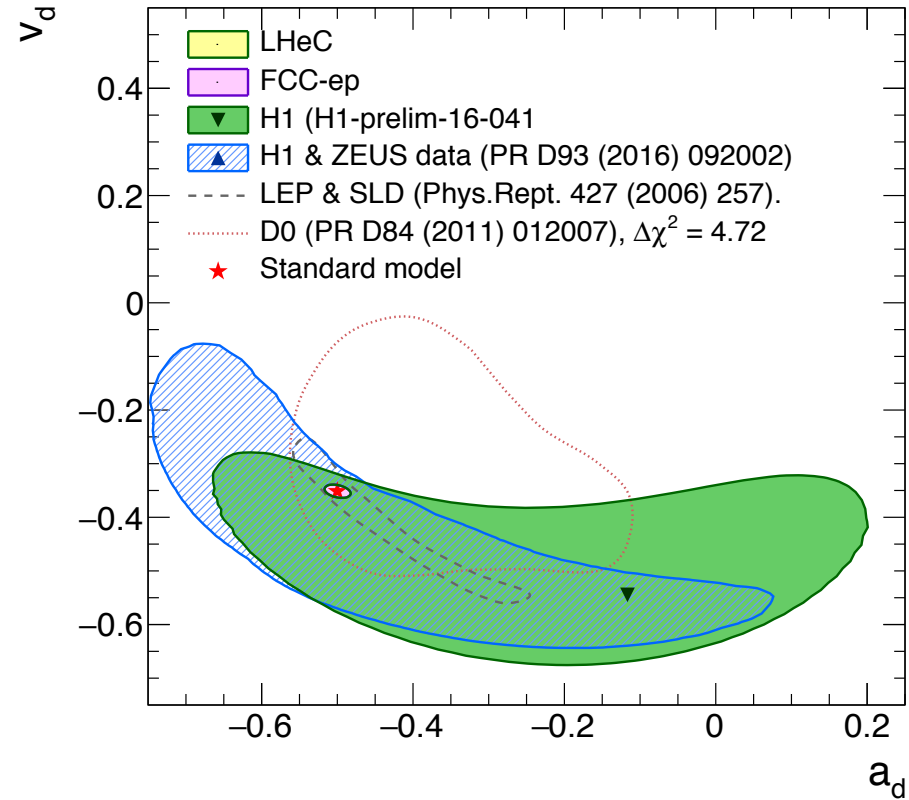
LHeC CDR: J. Phys. G39 (2012) 075001, arXiv:1206.2913

# Results

## u quark couplings



## d quark couplings



- Huge improvement in precision over LEP, Tevatron and HERA measurements
- Data with highly polarised lepton beam have a big impact
- $\gamma Z$  terms help to resolve the sign ambiguity presented in LEP data

# W Boson Mass and Weak Mixing Angle

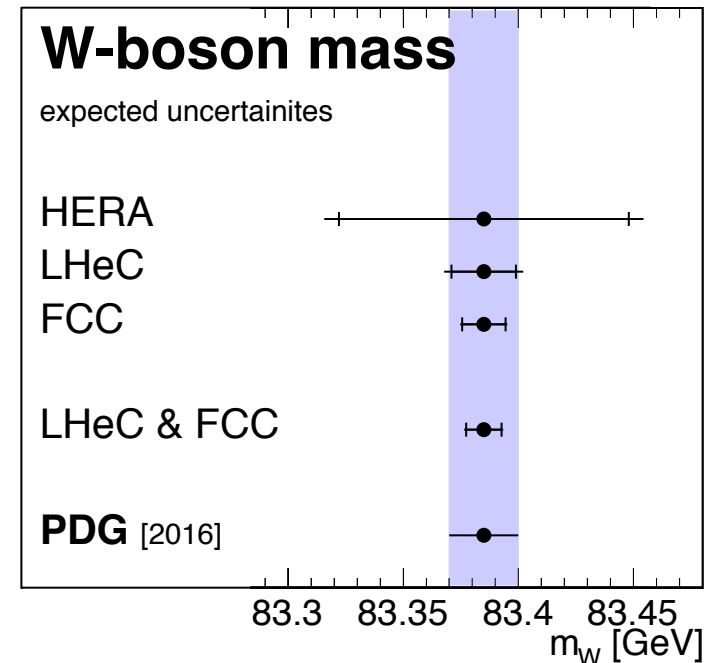
□ In on-mass shell scheme,  $\alpha_{em}$ ,  $m_Z$ , and  $m_W$  are the main free parameters

- $\alpha_{em}$  and  $m_Z$  are precisely known/measured
- Treat  $m_W$  as free parameter

HERA  $\pm 63_{(exp)} 29_{(PDF)}$

LHeC  $\pm 14_{(exp)} 10_{(PDF)}$

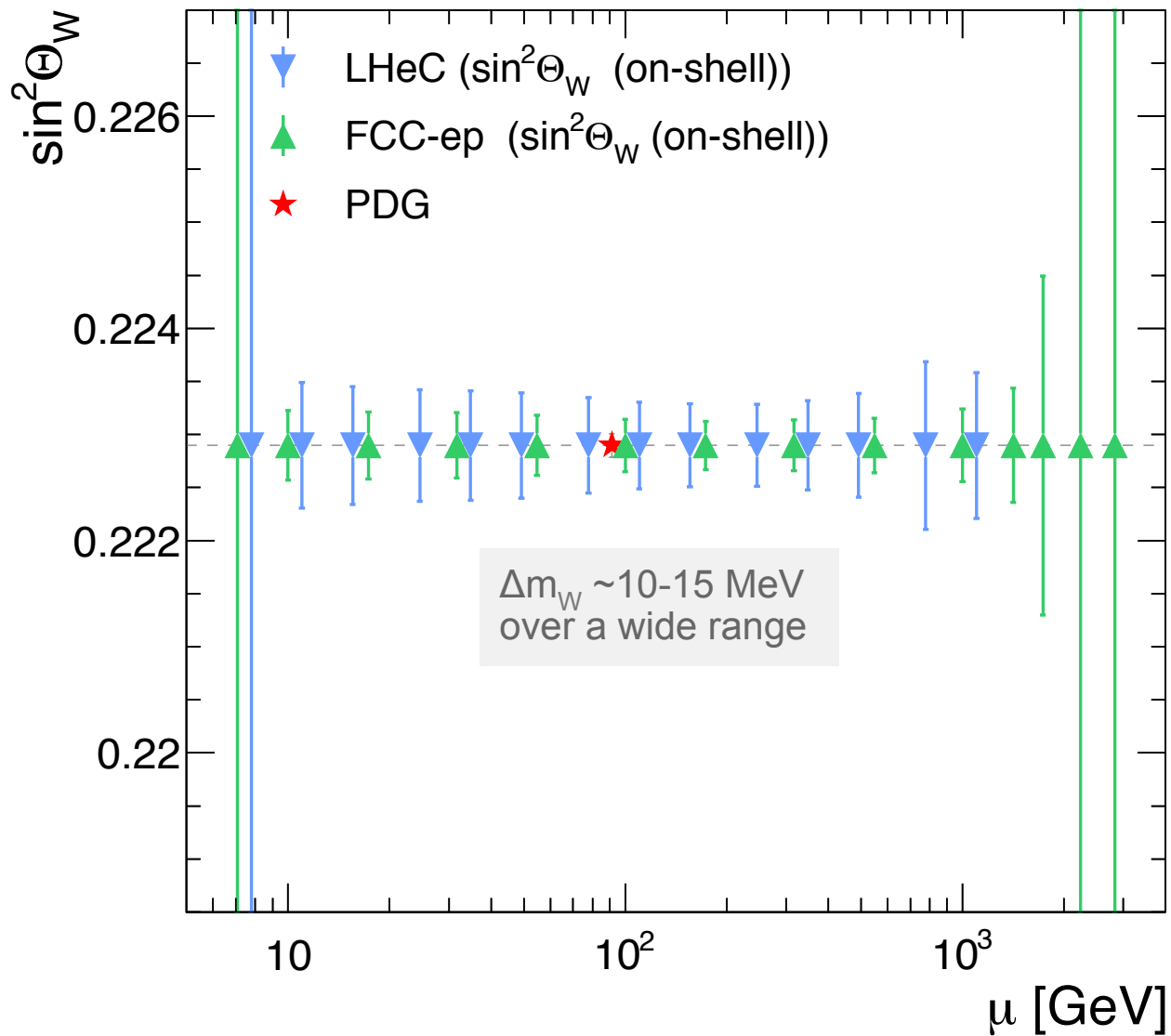
FCC  $\pm 9_{(exp)} 4_{(PDF)}$



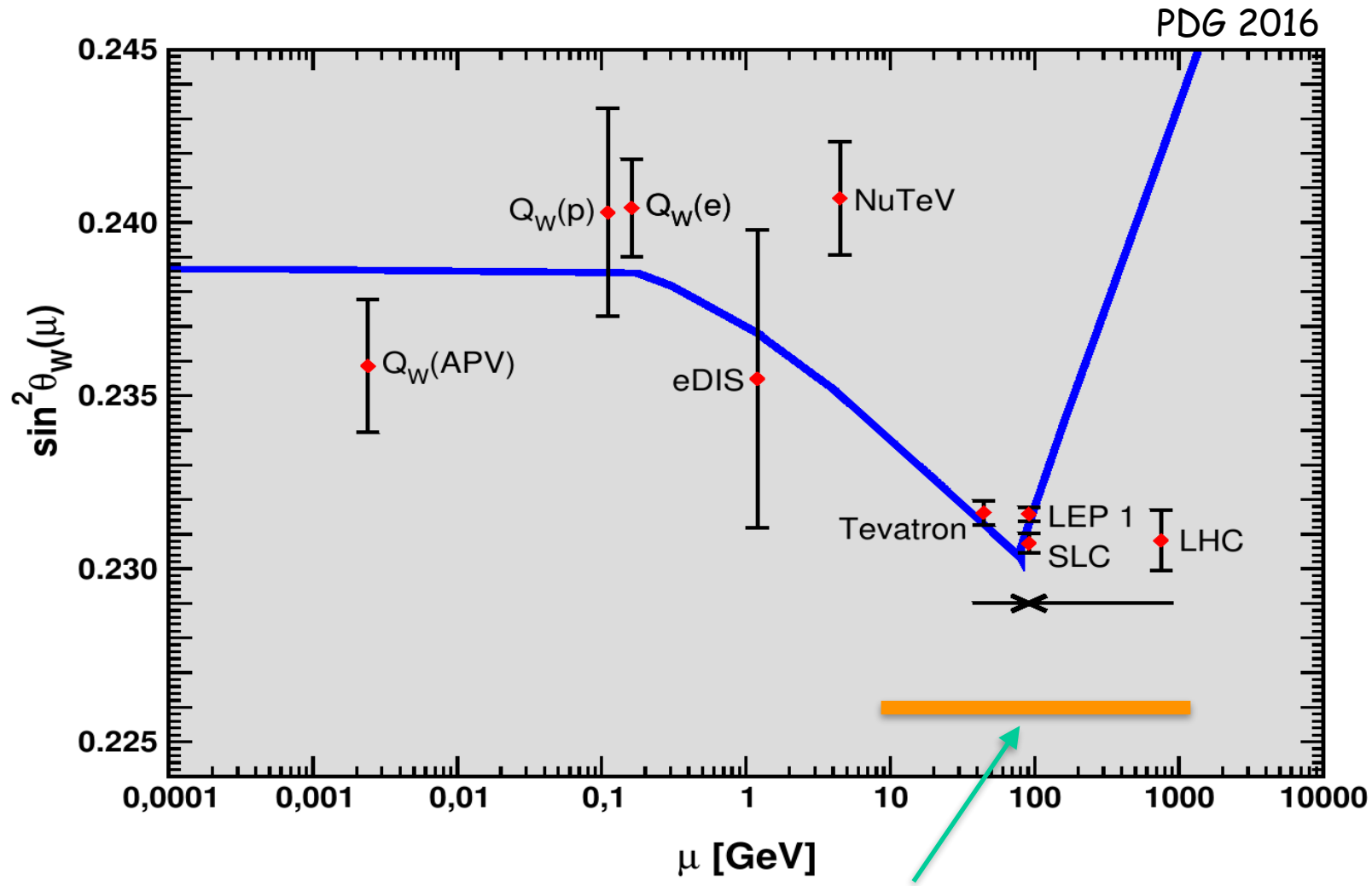
□ The weak mixing angle can be derived:

$$\sin^2 \theta_W(\text{on-mass-shell}) = 1 - \frac{M_W^2(\text{fit})}{M_Z^2(\text{input})}$$

# Results at Different Scales ( $Q^2 \rightarrow \mu$ )



# Convert to MS Scheme to Check Scale Dependence



LHeC/FCC-eh in a large and interesting range with large expected variations

# Summary and Conclusion

- Selected EW expectations show the potential of the LHeC/FCC-eh
  - unprecedented precision on light quark couplings to Z boson
  - competitive W mass determination
  - weak mixing angle extraction over a large energy range
  
- Results based on simulated data samples with likely conservative uncertainties
  
- Only real data can
  - tell if there are deviations from the SM expectations
  - allow joint exploration of EW measurements with precision QCD and BSM physics