

#### Total cross section & jet production

- High energy hadron scattering ⇒ copious production of (mini-)jets [e.g., Gaisser & Halzen, 1985]
- Inclusive cross section for production jets of  $p_t > p_t^{\text{cut}}$ :

$$\begin{split} \sigma_{pp}^{\text{jet}}(s, p_{\text{t}}^{\text{cut}}) &= \sum_{I,J=q,\bar{q},g} \int_{p_{\text{t}} > p_{\text{t}}^{\text{cut}}} dp_{t}^{2} \int dx^{+} \, dx^{-} \, f_{I/p}(x^{+}, M_{\text{F}}^{2}) \\ &\times \frac{d\sigma_{IJ}^{2 \to 2}(x^{+}x^{-}s, p_{t}^{2}, M_{\text{F}}^{2})}{dp_{t}^{2}} \, f_{J/p}(x^{-}, M_{\text{F}}^{2}) \end{split}$$

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  - $\sigma_{pp}^{
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- ⇒ multiple jet production required
  - = multiparton interactions (MPIs)



## MPIs & generalized parton distributions (GPDs)

- Usual PDFs  $f_I(x,Q^2)$  insufficient to describe MPIs
  - multiparton GPDs  $F_{I_1...I_n}^{(n)}(x_1,...x_n,\vec{b}_1,...\vec{b}_n,Q_1^2,...Q_n^2)$  required

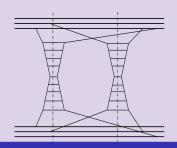
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#### E.g., $F^{(2)}$ for double parton scattering (production of 2 dijets)

$$\sigma_{pp}^{4 \text{jet}(\text{DPS})}(s, p_{\text{t}}^{\text{cut}}) = \frac{1}{2} \int dx_{1}^{+} dx_{2}^{+} dx_{1}^{-} dx_{2}^{-} \int_{p_{\text{t}_{1}}, p_{\text{t}_{2}} > p_{\text{t}}^{\text{cut}}} dp_{\text{t}_{1}}^{2} dp_{\text{t}_{2}}^{2} \sum_{I_{1}, I_{2}, J_{1}, J_{2}}$$

$$\times \frac{d\sigma_{I_{1}J_{1}}^{2\to2}}{dp_{t_{1}}^{2}} \frac{d\sigma_{I_{2}J_{2}}^{2\to2}}{dp_{t_{2}}^{2}} \int d^{2}\Delta b \, F_{I_{1}I_{2}}^{(2)}(x_{1}^{+}, x_{2}^{+}, M_{F_{1}}^{2}, M_{F_{2}}^{2}, \Delta b) \, F_{J_{1}J_{2}}^{(2)}(x_{1}^{-}, x_{2}^{-}, M_{F_{1}}^{2}, M_{F_{2}}^{2}, \Delta b)$$



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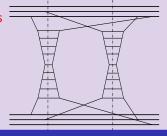
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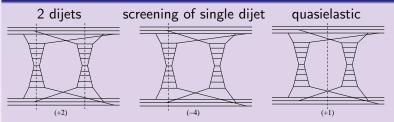
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- standard simplification:
   neglect multiparton correlations
- $\Rightarrow F_{I_1...I_n}^{(n)}(x_1,...x_n,\vec{b}_1,...\vec{b}_n,...) = \prod_{i=1}^n G_{I_i}(x_i,\vec{b}_i,Q_i^2)$
- $\Rightarrow \sigma_{pp}^{4\text{jet(DPS)}}(s, p_{t}^{\text{cut}}) =$   $\frac{1}{2} \int d^{2}b \left[ G_{I} \otimes \sigma_{IJ}^{2 \to 2} \otimes G_{J} \right]^{2}$

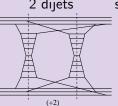


### Relation to $\sigma_{pp}^{tot}$ and $\sigma_{pp}^{inel}$ comes from the AGK cutting rules

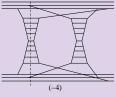


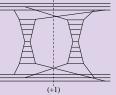
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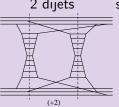
2 dijets screening of single dijet quasielastic



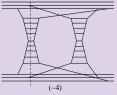


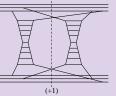
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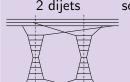
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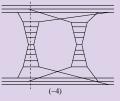
- partial contributions of the 3 processes are related as (+2):(-4):(+1)
- $\Rightarrow \Delta^{(2)} \sigma_{np}^{\text{tot}} = -\frac{1}{2} \sigma_{pp}^{4\text{jet(DPS)}}$  (similarly for n > 2 dijets)
- this leads to the usual 'minijet' ansatz:  $\sigma_{pp}^{\text{tot}}(s) = 2 \int d^2b \left[ 1 - \exp(-\chi_{pp}^{\text{jet}}(s, b, p_{\text{t}}^{\text{cut}})) \right]$  $(\chi_{pp}^{\text{jet}}(s,b,p_{\text{t}}^{\text{cut}}) = \frac{1}{2} \sum_{I,J} G_I \otimes \sigma_{IJ}^{2 \to 2} \otimes G_J)$

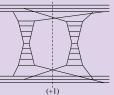
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#### NB: inclusive jet cross section - unmodified by such MPIs

• e.g., summary contribution of the 3 processes:

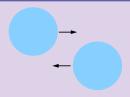
$$2*(+2)+1*(-4)+0*(+1)=0$$

•  $\Rightarrow$  collinear factorization holds:  $\frac{d\sigma_{pp}^{\rm jet}}{dp_z^2} = \sum_{I,J} f_I \otimes \frac{d\sigma_{IJ}^{2\to 2}}{dp_z^2} \otimes f_J$ 

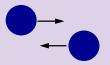


## Main message: to reduce $\sigma_{pp}^{\text{tot}}$ , enhance MPIs

## Simpliest way to regulate the rise of $\sigma_{pp}^{\text{tot}}$ : denser parton 'packing'



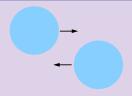
- larger proton size  $\Rightarrow$  larger  $\sigma_{pp}^{tot}$
- smaller parton density
   ⇒ smaller MPI rate



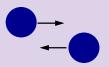
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- smaller proton size  $\Rightarrow$  smaller  $\sigma_{\it pp}^{tot}$
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- Unfortunately, not a solution: proton size is constrained by data on  $B_{pp}^{\rm el}(s) \propto \langle b^2(s) \rangle$
- more generally,  $d\sigma_{pp}^{\rm el}/dt$  is related to the transverse profile of the proton (thanks to data of TOTEM & ATLAS ALFA)



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- $\Rightarrow$  larger dispersion between the Fock states would reduce  $\sigma_{pp}^{\rm tot}$  for the same  $\sigma_{pp}^{\rm jet}$
- but: would yield a high cross section for low mass diffraction
  - ullet NB:  $\sigma_{pp}^{\mathrm{SD}(\mathrm{LM})}$  constrained by TOTEM & LHCf data

## Nearly last possibility: introduce parton 'clumps'

#### What is wrong with the uncorrelated parton picture?

- double (multiple) hard scattering results from independent cascades
  - ⇒ mostly in central collisions



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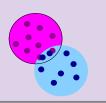
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  - can be done via 'soft' & 'hard' parton splitting mechanisms



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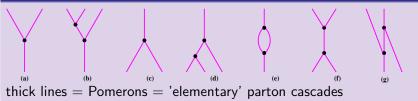


• 'soft parton splitting' naturally emerges in enhanced Pomeron framework in QGSJET-II [SO, 2006, 2011]

Nonlinear processes: Pomeron-Pomeron interactions (scattering of intermediate partons off the proj./target hadrons & off each other)

 $thick\ lines = Pomerons = 'elementary'\ parton\ cascades$ 

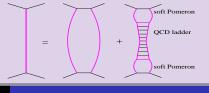
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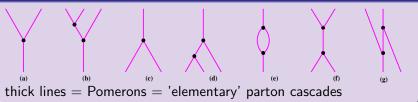
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  - ullet  $\Rightarrow$  transverse expansion governed by (small) Pomeron slope

DGLAP for hard cascades



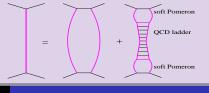
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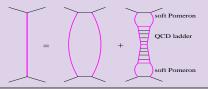
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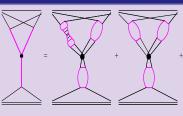
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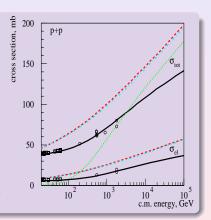
#### Pomeron-Pomeron interaction: a closer look

• basic assumption: multi- $\mathbb{P}$  vertices – dominated by soft  $(|q^2| < Q_0^2)$  parton processes



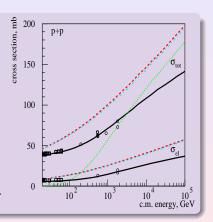
# Taking into account interactions between parton cascades substantially reduces the impact of jet production on $\sigma_{pp}^{\text{tot}}$

- e.g., a reasonable fit of  $\sigma_{pp}^{\rm tot}$  was obtained for a low cutoff  $Q_0^2=1~{\rm GeV}^2$  [SO, 2006]
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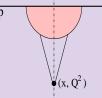


• these results can be explained in 2 different ways

## 1st explanation: rescattering of intermediate partons reduces effective parton density

For independent parton cascades, one uses universal PDFs (GPDs)

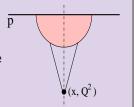
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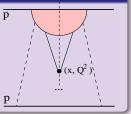
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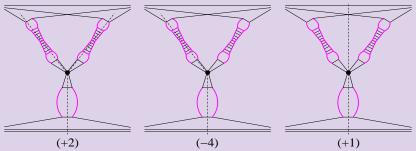
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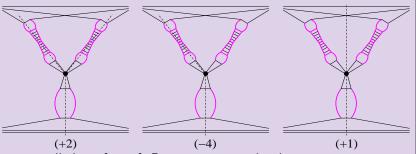
#### In enhanced framework, parton density is influenced by the collision

- intermediate partons scatter off the partner proton in addition
  - this dynalically reduces the effective parton density for an exclusive process (stronger effect for higher s, smaller b)

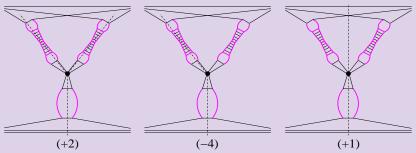




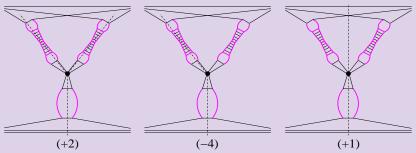
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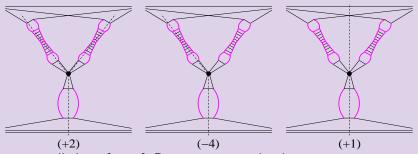


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- ullet adding two other contributions  $\Rightarrow$  negative correction to  $\sigma_{pp}^{ ext{tot}}$
- NB: no impact on inclusive jet cross section [2\*(+2)+1\*(-4)+0\*(+1)=0]

#### E.g., double dijet production from soft Pomeron splitting



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  - ≡ having a parton 'clump' in the target proton

Generic property: thanks to AGK cancellations, collinear factorization holds for inclusive jet cross section

$$\frac{d\sigma_{pp}^{\text{jet}}}{dp_t^2} = \sum_{I,I} f_I \otimes \frac{d\sigma_{IJ}^{2 \to 2}}{dp_t^2} \otimes f_J$$

## General major problem with hadron multiplicity rise

#### Applies to any model which respects collinear factorization

$$ullet$$
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- LHC data indicate:  $dN_{\rm ch}/d\eta|_{\rm n=0} \propto s^{0.2}$
- $\bullet$  moreover, the normalization depends on the chosen  $p_t$ -cutoff
  - in QGSJET-II-04, a rather large value (3 GeV<sup>2</sup>) is used
  - with the factorization scale  $M_{
    m F}^2=p_{
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  - wanted: a perturbative mechanism to suppress low p<sub>t</sub> jet production, without a strong impact on PDFs

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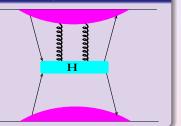
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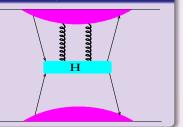
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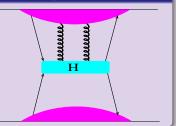
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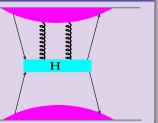
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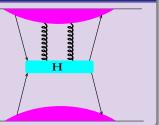


### Some justifications

- ullet dominant contributions in the small x limit usually from gluons
- soft gluon contributions proved important for p<sub>t</sub>-broadening and suppression of SFs & jet spectra on nuclear targets [Guo, 1998; Guo & Qiu, 2000; Qiu & Vitev, 2004, 2006]
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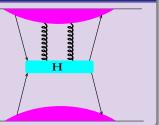


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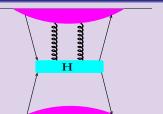


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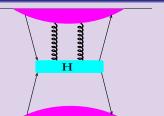
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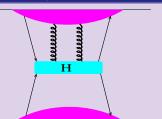
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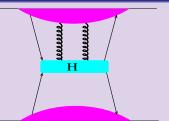
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- i.e., incorporate the mechanism in the Pomeron framework
  - NB: AGK rules not applicable for HT contributions

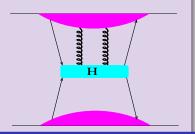
#### Consider as an example corrections to qq' scattering in LC gauge

Twist 4 contribution to the cross section:

$$\Delta \sigma_{\rm HT}(s) = \frac{1}{2s} \int \frac{d^4k_q}{(2\pi)^4} \frac{d^4k_{q'}}{(2\pi)^4} \frac{d^4k_{g_1}}{(2\pi)^4} \frac{d^4k_{g_2}}{(2\pi)^4} H_{ijkl}^{\alpha\beta}(k_q, k_{q'}, k_{g_1}, k_{g_2})$$

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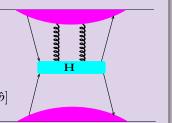
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 doing collinear factorization, one obtains [Ellis et al., 1982; Qiu, 1990]

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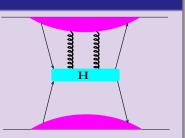
- now: assume the integrals to be dominated by  $x_{g_1}, x_{g_2} \simeq 0$ 
  - e.g., converting  $1/x_{g_i}$  into poles & doing residies [Guo & Qiu, 2001]



### Most radical assumptions

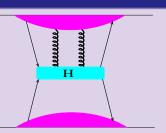
observe that

$$\begin{split} \lim_{x_{g_{1,2}}\to 0} x_{g_1} x_{g_2} T_{qg}(x_q, x_{g_1}, x_{g_2}) & \propto \\ \lim_{x_g\to 0} x_g F_{qg}^{(2)}(x_q, x_g, \Delta b = 0) \end{split}$$



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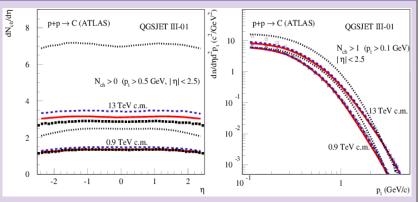
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- what about using even a smaller cutoff?
  - generally possible but would require higher order corrections (multiple exchanges of soft gluons)
  - ullet  $\Rightarrow$  additional assumptions

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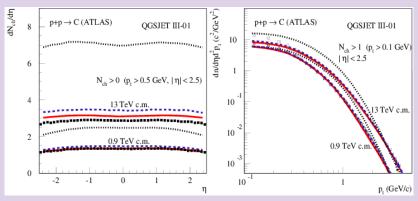
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- the rest of the model is identical to QGSJET-II-04
  - improvement of forward production, e.g., RRP-contribution (mainly pion exchange) desirable (in view of LHCf data)

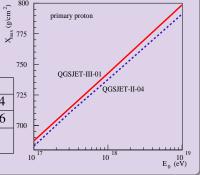
- Current parameter tune may not be the optimal one
  - here tried to minimize HT-effects & maximize HM-diffraction (in view of CMS & ATLAS data)
  - ⇒ strong effects due to enhanced graphs (higher PPP-coupling)
  - alternative: stronger HT-effects & weaker HM-diffraction
- not fully satisfied with the theoretical approach
- the rest of the model is identical to QGSJET-II-04
  - improvement of forward production, e.g., RRP-contribution (mainly pion exchange) desirable (in view of LHCf data)
- model calibrated to the same data set as QGSJET-II-04
  - ⇒ similar results expected



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  - ⇒ strong effects due to enhanced graphs (higher PPP-coupling)

### E.g., $\simeq 5$ g/cm<sup>2</sup> shift of $X_{\rm max}$ – mostly due to higher diffraction

 not sure about it because of the CMS-TOTEM tension:



TOTEM	CMS
7 - 350	12 - 394
≥ 3.3	$4.3 \pm 0.6$
0.42	0.62
	$7 - 350$ $\simeq 3.3$

### Outlook

- Treatment of nonlinear effects due to enhanced Pomeron graphs remains the key element of the model
  - with 2 adjustable parameters, provides a very rich formalism
  - plays central role for timing the energy-rise of cross sections & soft hadron production
- Treatment of higher twist effects a useful complement
  - ullet with 1 additional adjustable parameter, provides a dynamical scheme which mimics energy-dependent  $p_{
    m t}$ -cutoff
  - offers additional flexibility for the model tuning
  - however, not a perturbative approach: involves numerous phenomenological assumptions
  - ullet  $\Rightarrow$  independent cross checks & calibration desirable
- More technical improvements, notably, concerning forward production are required for more reliable EAS predictions



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