## MATTER RELICS IN Disformal SCALAR-TENSOR THEORIES

(TOWARDS A POST-INFLATIONARY STRING COSMOLOGY)

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BASSED ON 1612.05553 + WORK IN PROGRESS w/BHASKAR DUTTA, ESTEBAN JIMENEZ

## THE $\Lambda$ CDM MODEL OF COSMOLOGY

The $\Lambda$ CDM model, supplemented with inflation is in very good agreement with current observations


Ordinary Matter: ~5\% of density content!
Dark Matter: non-luminous weakly interacting particles (axions, wimps, neutrinos, LSP, etc).

Dark Energy: permeates the universe uniformly causing the accelerated expansion of the universe ( $\Lambda$, modified gravity, quintessence).

## PRE-BBN COSMOLOGICAL EVOLUTION

- While ICDM strongly supported by current data, physics from reheating till just before BBN ( $T \sim \mathrm{MeV}$ ), remains relatively unconstrained.
- During this period, universe may have gone through a nonstandard period of expansion, compatible with BBN
- In the context of the thermal relic scenario, if such modification happens during DM decoupling, DM freeze-out may be modified with measurable consequences for the thermal relic DM abundances and cross-sections:
- particle freeze-out may be accelerated (or delayed) and the relic abundance enhanced (or suppressed)


## THERMAL RELIC SCENARIO

What is the origin and nature of dark matter?
The favourite framework for origin of dark matter is the thermal relic scenario:

- During thermal equilibrium $\chi \bar{\chi} \leftrightarrow f \bar{f} \quad\left(\Gamma_{\chi} \gtrsim H\right)$

$$
n_{\chi}^{e q} \sim e^{-m_{\chi} / T}
$$

the longer the DM (anti) particles remain in equilibrium the lower their number densities are at freeze- out. Thus species with larger interaction cross sections which maintain thermal contact longer,

- As universe cools and expands, interactions become less frequent and decay rate drops $\chi \bar{\chi} \leftrightarrow f \bar{f}\left(\Gamma_{\chi} \lesssim H\right)$
- At this point number density freezes-out, and we are left with with a relic of DM particles
freeze out with diminished abundances. Thermal relic WIMPS are excellent DM candidates as their weak scale cross section $\sigma \sim \mathrm{G}^{2} \mathrm{~F}^{2}{ }_{\chi}$ gives the correct order of magnitude for $\Omega_{\mathrm{DM}} \mathrm{h}^{2}$ for a standard radiation-dominated early universe. However, if the universe experiences a non-standard expansion law during the epoch of dark matter decoupling, freeze-out may be accelerated and the relic abundance enhanced
The longer the DM particles remain in equilibrium, the lower their density will be at freeze-out and vice-versa


## THERMAL RELIC SCENARIO

In this scenario, a DM candidate with a weak scale interaction cross-section, freezes out with an abundance that matches the presently observed value for the DM density

$$
\Omega_{D M}=0.1188 \pm 0.0010 h^{-2}
$$

$(H=100 h \mathrm{~km} / \mathrm{s} / \mathrm{Mpc})$
Observations indicate that annihilation cross-sections can be smaller than the thermal average value for lower dark matter masses ( $\lesssim 100 \mathrm{GeV}$ )

Whereas an annihilation cross-section larger than the thermal average value can still be allowed for larger DM masses


## String Theory Origin of DM?

- String theory models of particle physics (D-branes, heterotic, M-theory) offers a plethora of potential DM candidates (SUSY partners, axions, hidden sector mater, etc)
- But hard to make a distinction between stringy and field theory LSP, e.g.
- Can we find alternative ways, even if indirect, to test string theory predictions in terms of their dark matter candidates?



## Plan

© Conformal and Disformally coupled matter: a phenomenological approach

Modified expansion rate: conformal case
\& Effects on relic abundance

- Turning on Disformal factor
© Towards a D-brane picture


## CONFORMAL\&DISFORMALLY COUPLED MATTER

- Consider the following action:

$$
\begin{aligned}
S & =S_{E H}+S_{\phi}+S_{m} \\
& =\frac{1}{2 \kappa^{2}} \int d^{4} x \sqrt{-g} R-\int d^{4} x \sqrt{-g}\left[\frac{1}{2}(\partial \phi)^{2}+V(\phi)\right]-\int d^{4} x \sqrt{-\tilde{g}} \mathcal{L}_{M}\left(\tilde{g}_{\mu \nu}\right)
\end{aligned}
$$

where matter is coupled to

$$
\tilde{g}_{\mu \nu}=C(\phi) g_{\mu \nu}+D(\phi) \partial_{\mu} \phi \partial_{\nu} \phi
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$C(\phi)$ conformal transformation (preserves angles)
$D(\phi)$ disformal transformation (distorts angles)

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## Impact on Early Evolution

- Departures from standard cosmology will arise due to the different expansion rate, $\tilde{H}$, determined by scalar evolution
$\Rightarrow$ impact in DM relic abundances
- First study of conformally coupled DM/Quintessence model was considered by Catena et al. Lahanas et al in non-critical string theory models
[Catena et al.'04]
[Lahanas et al. '06]
- A first estimate of modification of the relic abundance of WIMP's due to change in expansion rate at the time of CDM freeze-out



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- A first estimate of modification of the relic abundance of WIMP's due to change in expansion rate at the time of CDM freeze-out
- What are the generic predictions for conformal coupling?
- How is cross-section modified (enhanced/diminished)?
- What is the effect of a disformal coupling?


## MODIFIED EXPANSION RATE

In FRW background, evolution equations in Einstein frame (with respect to $g_{\mu \nu}$ ) become

$$
\begin{aligned}
& H^{2}=\frac{\kappa^{2}}{3}\left[\rho_{\phi}+\rho\right], \\
& \dot{H}+H^{2}=-\frac{\kappa^{2}}{6}\left[\rho_{\phi}+3 P_{\phi}+\rho+3 P\right], \\
& \ddot{\phi}+3 H \dot{\phi}+V_{, \phi}+Q_{0}=0 .
\end{aligned}
$$

where

$$
Q_{0}=\rho\left[\frac{D}{C} \ddot{\phi}+\frac{D}{C} \dot{\phi}\left(3 H+\frac{\dot{\rho}}{\rho}\right)+\left(\frac{D_{, \phi}}{2 C}-\frac{D}{C} \frac{C_{, \phi}}{C}\right) \dot{\phi}^{2}+\frac{C_{, \phi}}{2 C}(1-3 \omega)\right]
$$

Total energy is conserved $\nabla_{\mu}\left(T_{\phi}^{\mu \nu}+T^{\mu \nu}\right)=0$. but individual conservation equations are modified:

$$
\begin{aligned}
& \dot{\rho}_{\phi}+3 H\left(\rho_{\phi}+P_{\phi}\right)=-Q_{0} \dot{\phi}, \\
& \dot{\rho}+3 H(\rho+P)=Q_{0} \dot{\phi} .
\end{aligned}
$$

Note that in the Jordan/ disformal frame, the energy-momentum tensor is conserved, $\nabla_{\mu} \tilde{T}^{\mu \nu}=0$
$\Rightarrow \quad \tilde{\rho}+3 \tilde{H}(\tilde{\rho}+\tilde{P})=0$

## MODIFIED EXPANSION RATE

We are looking for the modified expansion rate in the disformal or Jordan frame, felt by matter $\tilde{g}_{\mu \nu}, \tilde{H} \equiv \frac{d \ln \tilde{a}}{d \tilde{\tau}}$,

$$
\tilde{H}=\frac{H \gamma}{C^{1 / 2}}\left(1+\alpha(\varphi) \varphi^{\prime}\right)
$$

Where ${ }^{\prime}=d / d N$,

$$
\begin{aligned}
& \gamma^{-2}=1-\frac{H^{2}}{\kappa^{2}} \frac{D}{C} \varphi^{\prime 2} \\
& \alpha(\varphi)=\frac{d \ln C^{1 / 2}}{d \varphi}
\end{aligned}
$$

We need to compare this modified rate with the standard GR:

$$
H_{G R}^{2}=\frac{\kappa_{G R}^{2}}{3} \tilde{\rho} \quad \text { where } \quad \tilde{\rho}=C^{-2} \gamma^{-1} \rho
$$

In terms of $H$ and $\varphi$, it can be written as

$$
\gamma^{-1} H^{2}=\frac{\kappa^{2}}{\kappa_{G R}^{2}} \frac{C^{2}(1+\lambda)}{B} H_{G R}^{2}
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Deviation from GR can be readily computed from

$$
\xi \equiv \frac{\tilde{H}}{H_{G R}}
$$

which needs to go to 1 towards the start of BBN

## CONFORMAL CASE: SCALAR EVOLUTION

In the conformal case, equations can be reduced to a single master equation for $\varphi$, which we solve during radiation and matter era $V(\varphi) \sim 0$

$$
\frac{2}{3\left(1-\varphi^{\prime 2} / 6\right)} \varphi^{\prime \prime}+(1-\tilde{\omega}) \varphi^{\prime}+2(1-3 \tilde{\omega}) \alpha(\varphi)=0,
$$

where $\tilde{\omega}=\gamma^{2} \omega$ is the Jordan frame eos computed from

$$
1-3 \tilde{\omega}=\frac{\tilde{\rho}-3 \tilde{p}}{\tilde{\rho}}=\sum_{A} \frac{\tilde{\rho}_{A}-3 \tilde{p}_{A}}{\tilde{\rho}}+\frac{\tilde{\rho}_{m}}{\tilde{\rho}}
$$

which takes into account small departures from $1 / 3$ when a species becomes nonrelativistic
[See Esteban Jimenez's Ealk]


## CONFORMAL CASE: SCALAR EVOLUTION

Conformal coupling acts as effective potential for $\varphi$

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$$
\Rightarrow \quad \begin{gathered}
C(\varphi)=\left(1+b e^{-\beta \varphi}\right)^{2} \\
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## CONFORMAL CASE: SCALAR EVOLUTION

This second choice of initial conditions gives the most interesting evolution


Conformal factor evolution

$$
\left(\varphi_{0}, \varphi_{0}^{\prime}\right)=(0.2,-0.994)
$$



Scalar field evolution $\left(\varphi_{0}, \varphi_{0}^{\prime}\right)=(0.2,-0.994)$

CONFORMAL CASE: EXPANSION RATE


Expansion rates comparison (for initial conditions: $\left(\varphi_{0}, \varphi_{0}^{\prime}\right)=(0.2,-0.994)$ )

$$
\tilde{H}=\frac{H \gamma}{C^{1 / 2}}\left(1+\alpha(\varphi) \varphi^{\prime}\right)
$$

(we consider only expanding solutions, $\left(1+\alpha(\varphi) \varphi^{\prime}\right)>0$ )

Note that Einstein frame $H$ always decreases (no violation of energy conditions). However, disformal frame $H$ can increase Notorious notch appears, which gives rise to possibility of reannihilation effect.

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## Effect on DM Relic Abundance

The impact of modified expansion rate on relic abundance for DM particle $\chi$ with mass $m_{\chi}$ can now be determined from Boltzmann equation

$$
\frac{d n_{\chi}}{d t}=-3 \tilde{H} n_{\chi}-\langle\sigma v\rangle\left(n_{\chi}^{2}-\left(n_{\chi}^{e q}\right)^{2}\right)
$$

which determining the dark matter number density $n_{\chi}$ evolution. Here $\langle\sigma v\rangle$ is the annihilation cross-section and $n_{\chi}^{e q}$ the equilibrium number density.
Rewriting Boltzmann equation in terms of $x=m_{\chi} / \tilde{T}$
$Y=\frac{n_{\chi}}{\tilde{s}}, \tilde{s}=\frac{2 \pi}{45} g_{s}(\tilde{T}) \tilde{T}^{3}$.

$$
\frac{d Y}{d x}=-\frac{\tilde{s}\langle\sigma v\rangle}{x \tilde{H}}\left(Y^{2}-Y_{e q}^{2}\right)
$$

## Effect on DM Relic Abundance

Boltzmann equation, gives us the DM relic abundance
[See Esteban Jimenez's Ealk]


Relic abundance evolution for
DM particle with mass $m_{\chi}=1000 \mathrm{GeV}$


Expansion and interaction rates' evolution

A re-annihilation phase occurs for the initial conditions chosen
$\left[\begin{array}{ll}-\tilde{\boldsymbol{H}} \\ - & \boldsymbol{H}_{\mathrm{GR}} \\ -- & \boldsymbol{\Gamma}_{1000 \mathrm{GeV}} \\ \hdashline & \tilde{\boldsymbol{\Gamma}}_{130 \mathrm{GeV}} \\ \hline\end{array}\right.$

## DISFORMAL CASE: EXPANSION RATE

Turning on the disformal coupling, we need to solve the coupled system of eqs for $\varphi, H$

$$
\begin{aligned}
& H^{\prime}=-H\left[\frac{3 B}{2}\left(1+\tilde{\omega} \gamma^{-2}\right)+\frac{\varphi^{\prime 2}}{2}\right] \\
& \varphi^{\prime \prime}\left[1+\frac{3 H^{2} \gamma^{2} B}{\kappa^{2}} \frac{D}{C}\right]+3 \varphi^{\prime}\left[1-\tilde{\omega} \frac{3 H^{2} B}{\kappa^{2}} \frac{D}{C}\right]+\frac{H^{\prime}}{H} \varphi^{\prime}\left[1+\frac{3 H^{2} \gamma^{2} B}{\kappa^{2}} \frac{D}{C}\right]
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\begin{aligned}
& \alpha(\varphi)=\frac{d \ln C^{1 / 2}}{d \varphi} \\
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$$

$$
+3 B \alpha(\varphi)(1-3 \tilde{\omega})+\frac{3 H^{2} \gamma^{2} B}{\kappa^{2}} \frac{D}{C}(\delta(\varphi)-\alpha(\varphi)) \varphi^{\prime 2}=0
$$

Use same conformal factor plus a small disformal contribution:

$$
D(\varphi)=D_{0} \varphi^{2} \text { with } D_{0}=-4.9 \times 10^{-14}
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Shape remains similar, position of notch moves and becomes sharper with a small increase in H


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Another example

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\begin{aligned}
C & =\left(8 \varphi^{2}+1\right)^{2} \\
D & =d_{1} \varphi^{3}+d_{2} \varphi^{2}+d_{3} \varphi
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$\mathrm{C}(\varphi)=\left(8 \varphi^{2}+1\right)^{2}, \mathrm{D}(\varphi)=0.0151 \varphi^{3}-0.007 \varphi^{2}-0.0439 \varphi, \varphi_{\text {ini }}=-0.3$ and $\varphi_{\text {ini }}^{\prime}=-0.12$.


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-_ $\tilde{H}_{\text {Conformal }}$
$-\tilde{H}(\mathrm{H})$
$\ldots \ldots . . H_{G R}$

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Less dramatic effect, and thus impace on relic abundance and cross-section

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## THE D-BRANE CASE

Conformal\&Disformal couplings arise naturally from D-brane actions. They are dictated by theory and arise as follows:

$$
S=S_{E H}+S_{\phi}+S_{m}
$$

$$
S_{E H}=\frac{1}{2 \kappa^{2}} \int d^{4} x \sqrt{-g} R,
$$

$$
S_{\phi}=-\int d^{4} x \sqrt{-g}\left[\frac{b}{2}(\partial \phi)^{2}+M^{4} C_{1}^{2}(\phi) \sqrt{1+\frac{D_{1}(\phi)}{C_{1}(\phi)}(\partial \phi)^{2}}+V(\phi)\right],
$$

$$
S_{m}=-\int d^{4} x \sqrt{-\tilde{g}} \mathcal{L}_{M}\left(\tilde{g}_{\mu \nu}\right),
$$

where

$$
\tilde{g}_{\mu \nu}=C_{2}(\phi) g_{\mu \nu}+D_{2}(\phi) \partial_{\mu} \phi \partial_{\nu} \phi .
$$

D-brane case:

$$
b=0, \quad C_{1}=C_{2}, \quad D_{1}=D_{2}
$$

Accelerating scaling solutions in coupled DE/DM models have been found in for monomial potentials.

## THE D-BRANE CASE

Conformal\&Disformal couplings arise naturally from D-brane actions. They are dictated by theory and arise as follows:

$$
S=S_{E H}+S_{\phi}+S_{m}
$$

$$
S_{E H}=\frac{1}{2 \kappa^{2}} \int d^{4} x \sqrt{-g} R,
$$

$$
S_{\phi}=-\int d^{4} x \sqrt{-g}\left[\quad+M^{4} C_{1}^{2}(\phi) \sqrt{1+\frac{D_{1}(\phi)}{C_{1}(\phi)}(\partial \phi)^{2}}+V(\phi)\right],
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## The D-brane case

The coupled equations to find the scalar evolution and expansion rates is no modified as

$$
\begin{aligned}
& H^{\prime}=-H\left[\frac{3 B}{2(1+\lambda)}(1+\omega)+\frac{\varphi^{\prime 2} M^{4} C D \gamma}{\gamma+1}\right], \\
& \varphi^{\prime \prime}\left[1+\frac{3 H^{2} \gamma^{-1} B}{M^{4} C D \kappa^{2}} \frac{D}{C}\right]+3 \varphi^{\prime}\left[\gamma^{-2}-\frac{3 H^{2} \gamma^{-3} B \tilde{\omega}}{M^{4} C D \kappa^{2}} \frac{D}{C}\right]+\frac{H^{\prime}}{H} \varphi^{\prime}\left[1+\frac{3 H^{2} \gamma^{-1} B}{M^{4} C D \kappa^{2}} \frac{D}{C}\right] \\
& \\
& \quad+\frac{3 B \gamma^{-3}}{M^{4} C D} \alpha(\varphi)(1-3 \tilde{\omega})+\frac{3 H^{2} \gamma^{-1} B}{M^{4} C D \kappa^{2}} \frac{D}{C}\left[(\delta(\varphi)-\alpha(\varphi)) \varphi^{\prime 2}\right]
\end{aligned}
$$

where $B \equiv 1-\frac{M^{4} C D \gamma^{2}}{3(\gamma+1)} \varphi^{\prime 2}$,

- We cannot take $\mathrm{D}=0$. C\&D contribute as a potential term
- How do these change expansion rate and thus relic abundance and cross-section predictions?
- Can we constraint C\&D from observation?


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$$

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$$

$$
+\frac{\kappa^{2}}{H^{2}} \frac{C}{2 D}\left[\gamma^{-2}\left(5 \frac{C_{\varphi}}{C}-\frac{D_{\varphi}}{D}\right)+\frac{D_{\varphi}}{D}-\frac{C_{\varphi}}{C}-4 \gamma^{-3} \frac{C_{\varphi}}{C}\right]=0
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- How do these change expansion rate and thus relic abundance and cross-section predictions?
- Can we constraint C\&D from observation?


## SUMMARY

- We investigated modifications to standard relic picture due to non-standard early cosmology evolution in scalar-tensor theories with conformal and disformal couplings to matter
- For suitable initial conditions, interesting non-trivial modifications appear in expansion rate and thus in the relic abundance of DM
- We studied a phenomenological scalar-tensor model, as a warm up to understand D-brane induced conformal/ disformal couplings to matter

