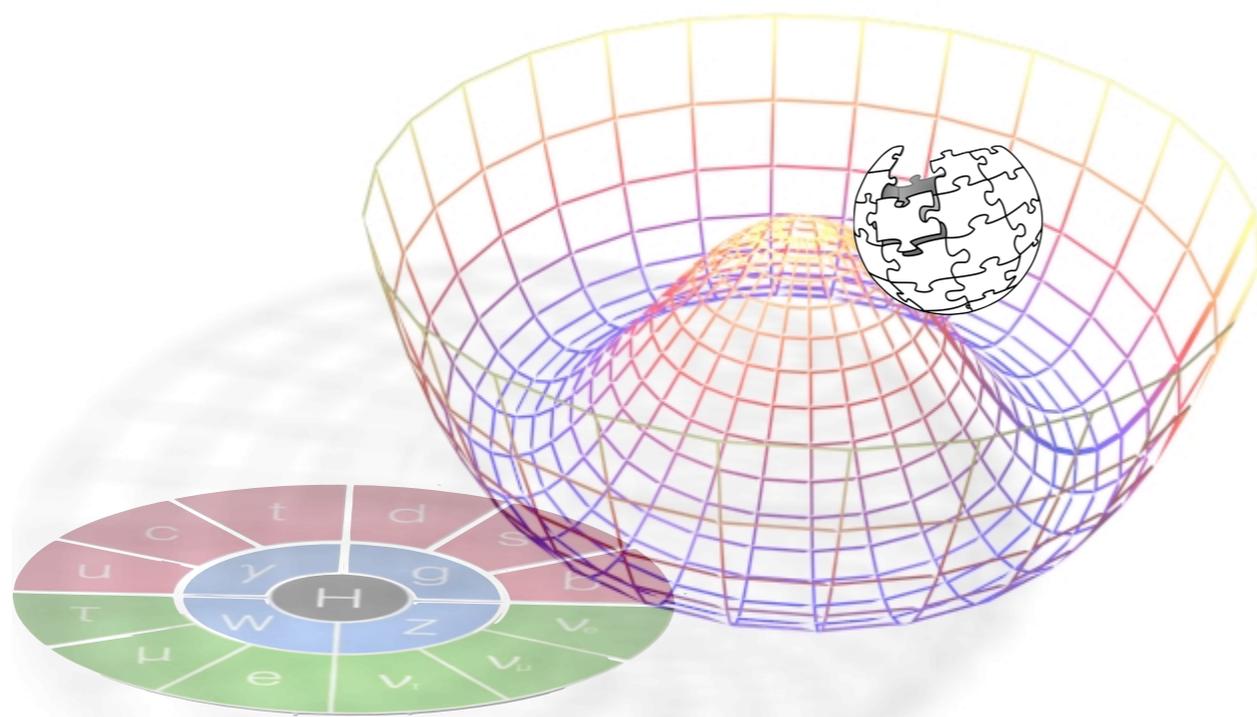


Higgs Synergies/ Complementarities

*Berlin, May 30, 2017
" FCC week "*



Christophe Grojean

DESY (Hamburg)
Humboldt University (Berlin)

(christophe.grojean@desy.de)

The Higgs in the (B)SM landscape

The fundamental principles governing the structure of **Higgs sector** are yet unknown
(many arbitrary parameters taking seemingly un-natural values)

The Higgs plays a vital role in our life

(masses, stability of vacuum, DM?, inflation?)

It has an intimate link with the high energy completion of the SM

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The Higgs discovery has been an important milestone
but it hasn't taught us much about **BSM** yet

typical Higgs coupling deformation: $\frac{\delta g_h}{g_h} \sim \frac{g^2 v^2}{\Lambda_{\text{BSM}}^2}$

current (and future) LHC sensitivity O(10-20)% $\Leftrightarrow \Lambda_{\text{BSM}} > 500-700 \text{ GeV}$

not doing better than direct searches

(except maybe for flavor violating processes, e.g. $h \rightarrow \mu \tau$)

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Higgs precision programme is very much wanted

complementary and synergetic measurements are essential to achieve this goal

Higgs precision: from κ to EFT

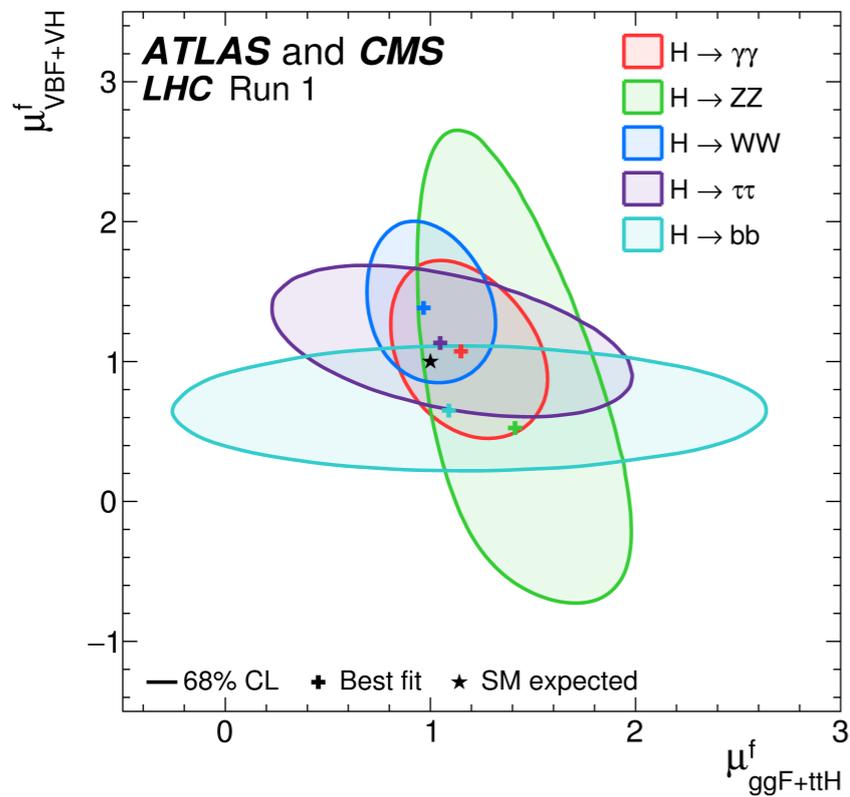
LHCHSWG '12

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$$\mu_i = \frac{\sigma[i \rightarrow h]}{(\sigma[i \rightarrow h])_{\text{SM}}}$$

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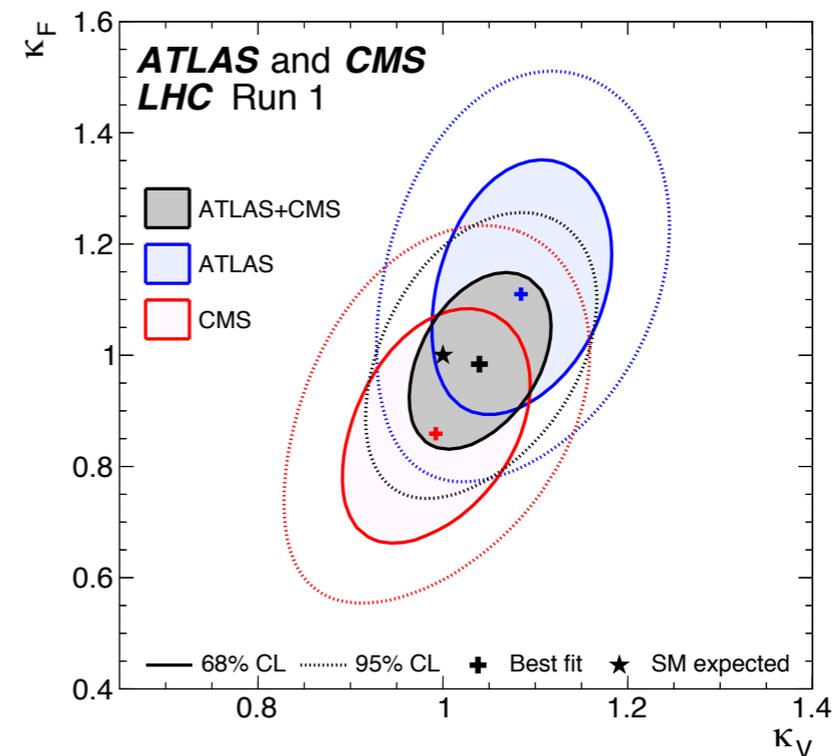
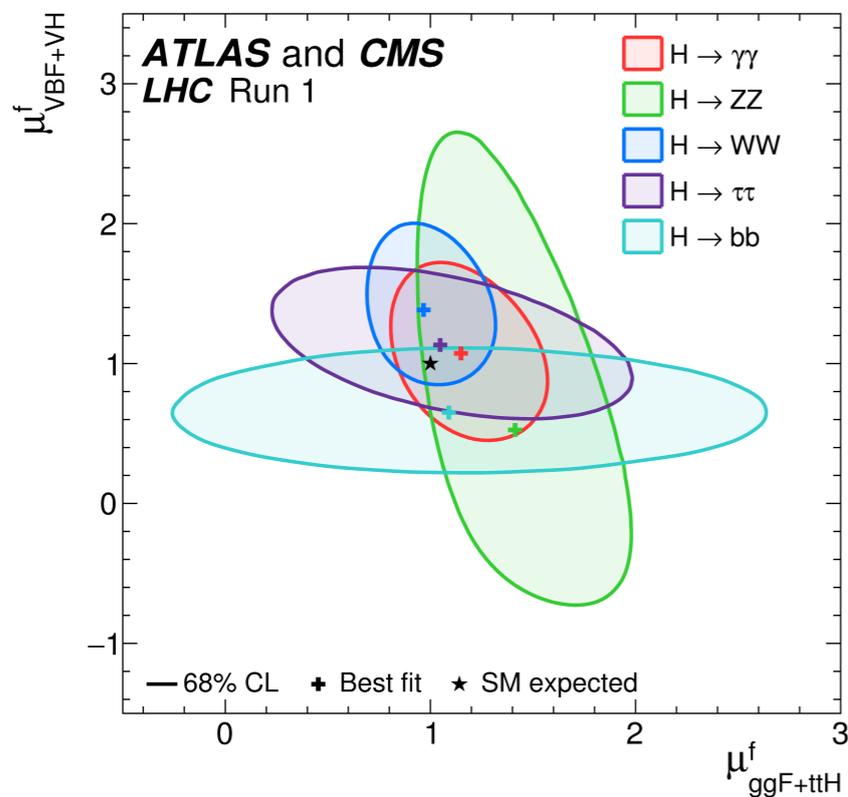


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$$(\sigma \cdot \text{BR})(gg \rightarrow H \rightarrow \gamma\gamma) = \sigma_{\text{SM}}(gg \rightarrow H) \cdot \text{BR}_{\text{SM}}(H \rightarrow \gamma\gamma) \cdot \frac{\kappa_g^2 \cdot \kappa_\gamma^2}{\kappa_H^2}$$

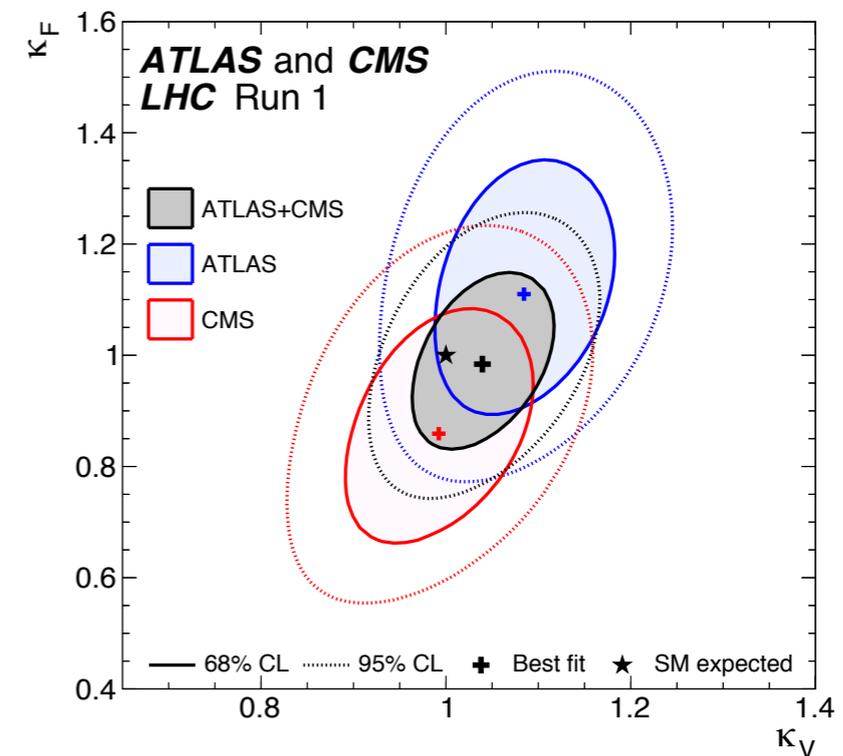
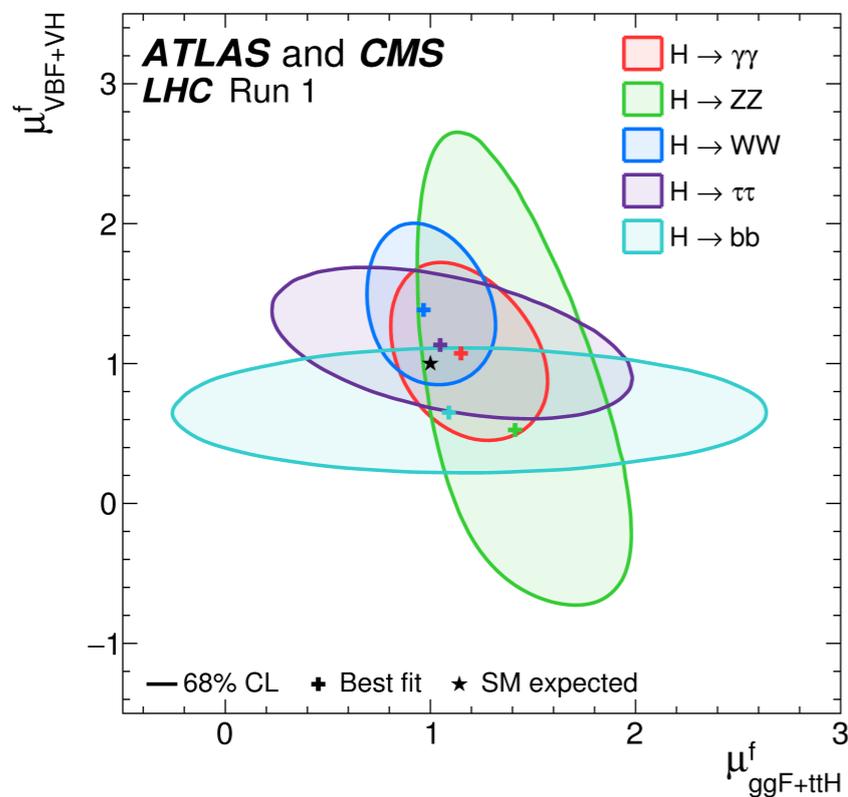
individual coupling rescaling factors

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Well suited parametrization for inclusive measurements

But doesn't do justice to wealth of information available (in particular at e^+e^- colliders)

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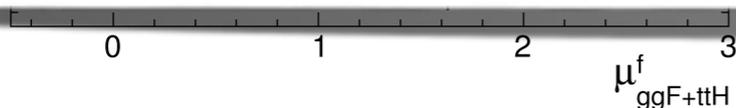


Pros of EFT

- ▶ correlations between different channels/observables
- ▶ combination of measurements at different energies
e.g. EW precision data and Higgs measurements
- ▶ test of self-consistency

unique to EFT

allow to focus on channels yet unconstrained and more likely to offer new discovery opportunities



$$(\sigma \cdot \text{BR})(gg \rightarrow H \rightarrow \gamma\gamma) = \sigma_{\text{SM}}(gg \rightarrow H) \cdot \text{BR}_{\text{SM}}(H \rightarrow \gamma\gamma) \cdot \frac{\kappa_g^2 \cdot \kappa_\gamma^2}{\kappa_H^2}$$

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Higgs synergy/complementarity

$$“(A \cup B) > A + B”$$

Higgs synergy/complementarity

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1. (SM input parameter determination to control parametric uncertainties)
2. EW precision to achieve precision in Higgs measurements
3. Diboson data and Higgs data
4. LHC and FCC-ee for top Yukawa measurement
5. Distributions complementing rate measurements
6. 240 + 350 runs
7. ee/ep/pp (...PDF measurements to control PDF uncertainties in Higgs data)

EW + Higgs

I Reducing numbers of parameters

The diagram shows two Feynman diagrams connected by an equals sign. The left diagram has a central black vertex with a wavy line labeled 'Z' entering from the left, a dashed line labeled 'h' entering from the top, and two outgoing lines labeled 'f' (fermion) and 'f' (anti-fermion). A circled 'X' is above the vertex. Below this diagram is a box containing the Lagrangian term $H^\dagger D_\mu H \bar{f} \gamma^\mu f$. The right diagram is identical but has two circled 'X's above the vertex. The equation is $= \frac{1}{2v} \times$ followed by the right diagram.

Modifications in $h \rightarrow Zff$ related to $Z \rightarrow ff$

EW + Higgs

- 1 Reducing numbers of parameters
- 2 Exploring different regions of parameter space (in specific models)

Assuming **composite** Higgs, **elementary** gauge bos.:

$$\mathcal{L}_{\text{BSM}}^{d=6} = \frac{1}{m_*^2} \frac{1}{g_*^2} \hat{\mathcal{L}}[g_* H, g_w V_\mu, \partial_\mu]$$

EW + Higgs

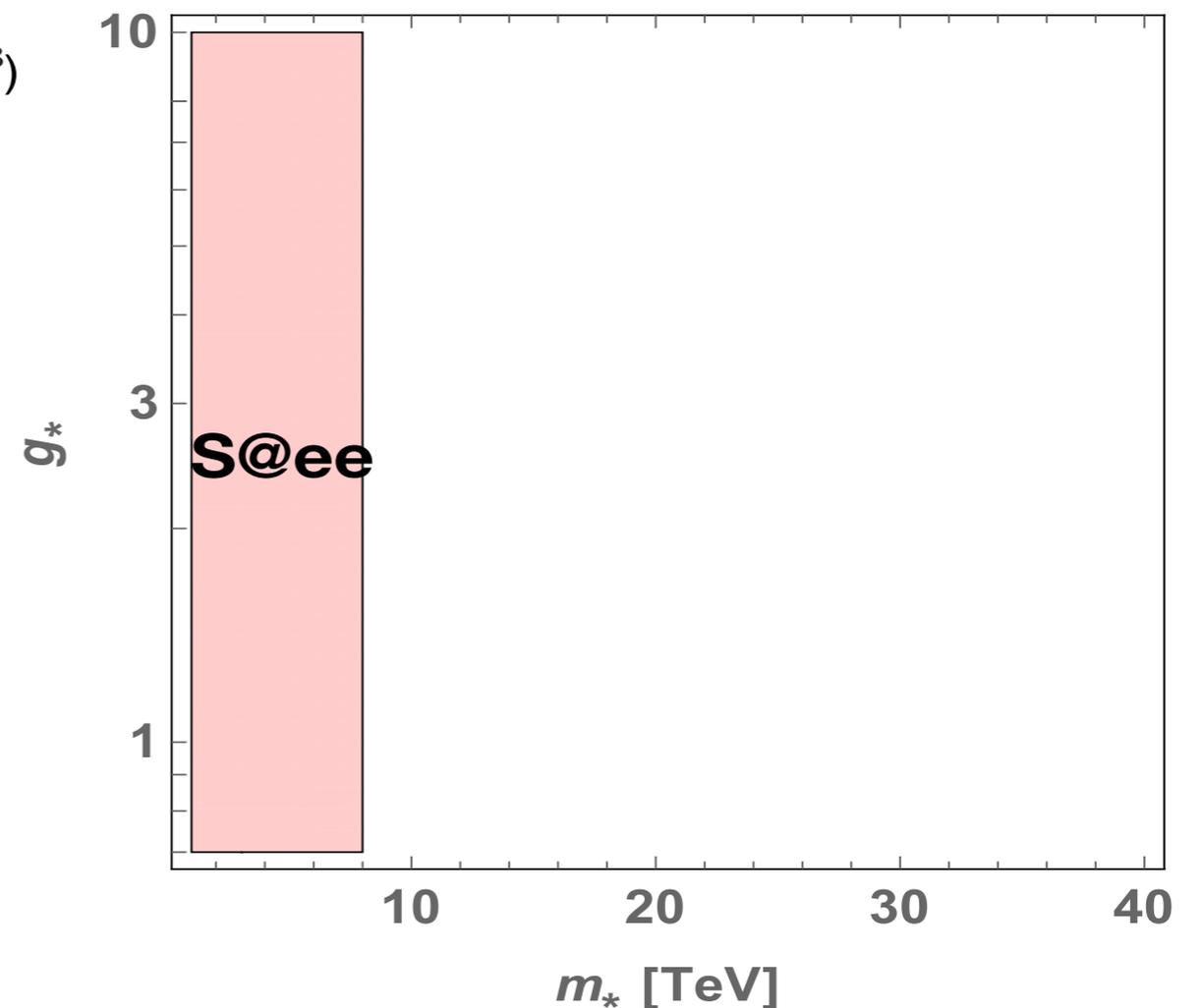
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S-parameter @ee: [De Blas et. al.] (LEP: 10^{-3})

$$\frac{g_w g'}{m_*^2} H^\dagger \sigma_a H W_{\mu\nu}^a B^{\mu\nu} \rightarrow \hat{S} = \frac{m_w^2}{m_*^2} < 10^{-4}$$



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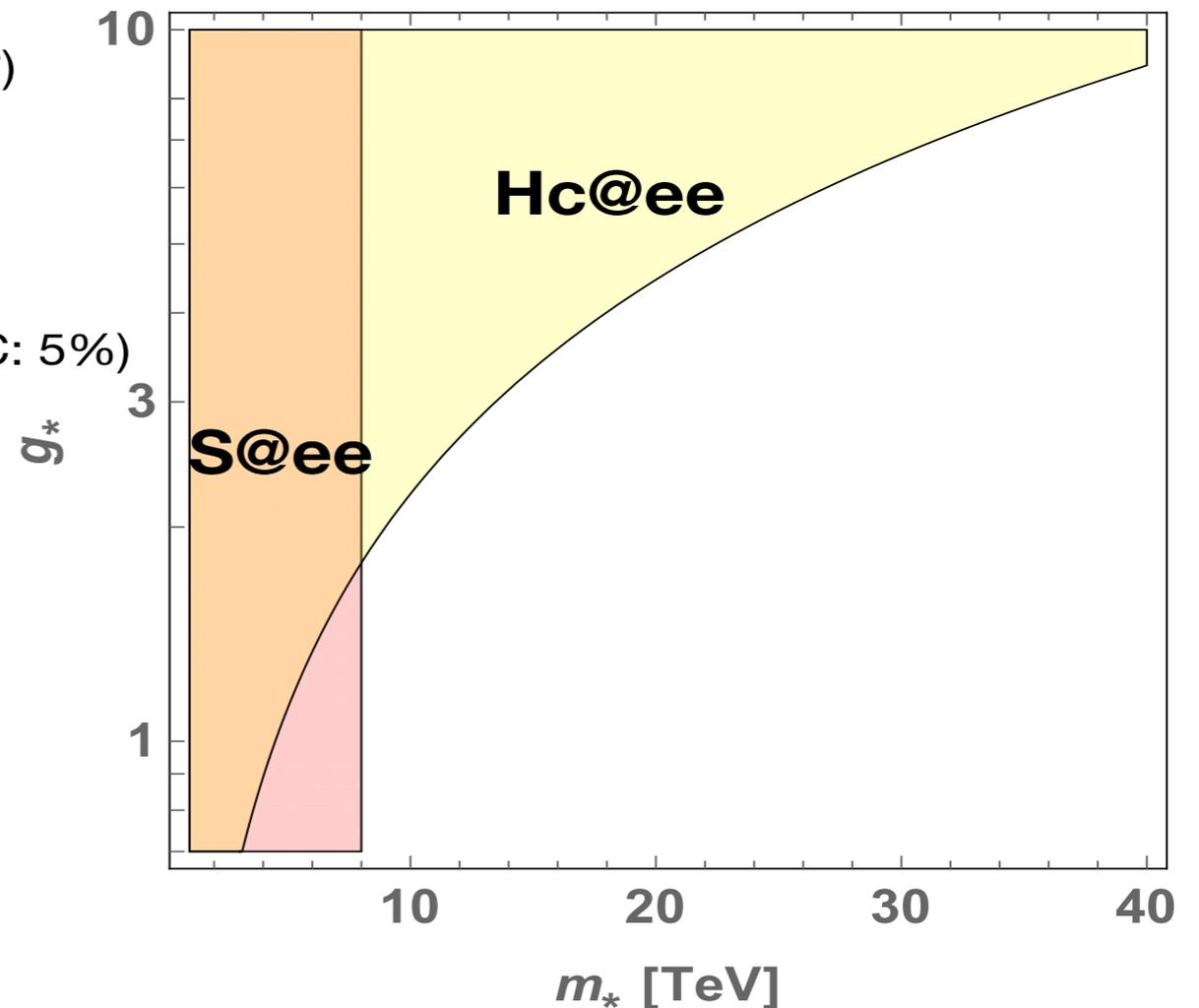
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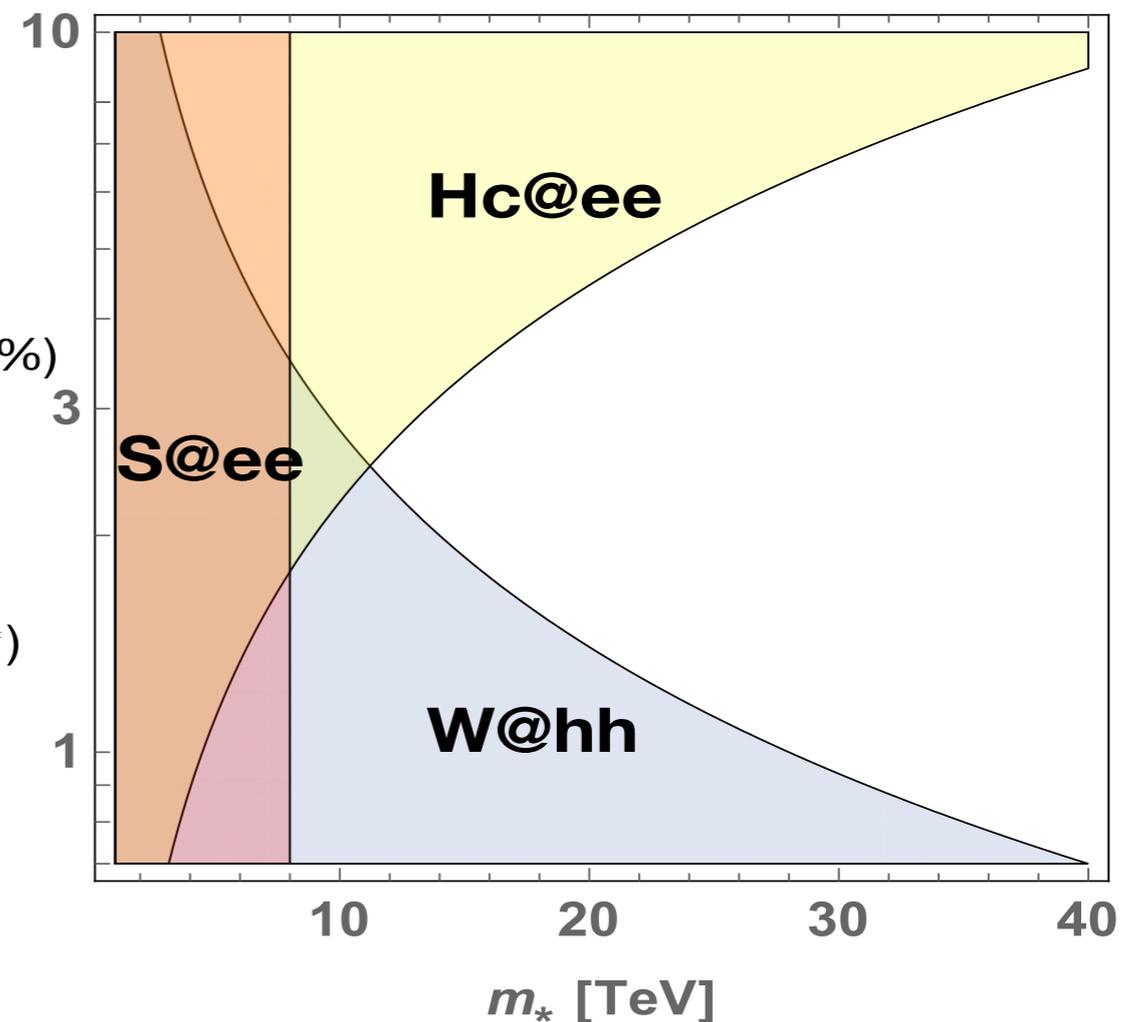
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W @hh: (energy + accuracy) (HL-LHC $< 10^{-4}$)

$$\frac{g_w^2}{g_*^2 m_*^2} (D_\mu W_{\nu\rho})^2 \rightarrow W = \frac{g_w^2 m_w^2}{g_*^2 m_*^2} < 4 \cdot 10^{-6}$$



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Gauge bosons + Higgs

In $EFT_{(dim-6)}$

8 deformations affecting Higgs physics alone

2 deformations affecting Higgs and diboson data

TGC (1%) are a priori more
constraining than Higgs (10%)

Is there any value in doing a global fit?

Gauge bosons + Higgs

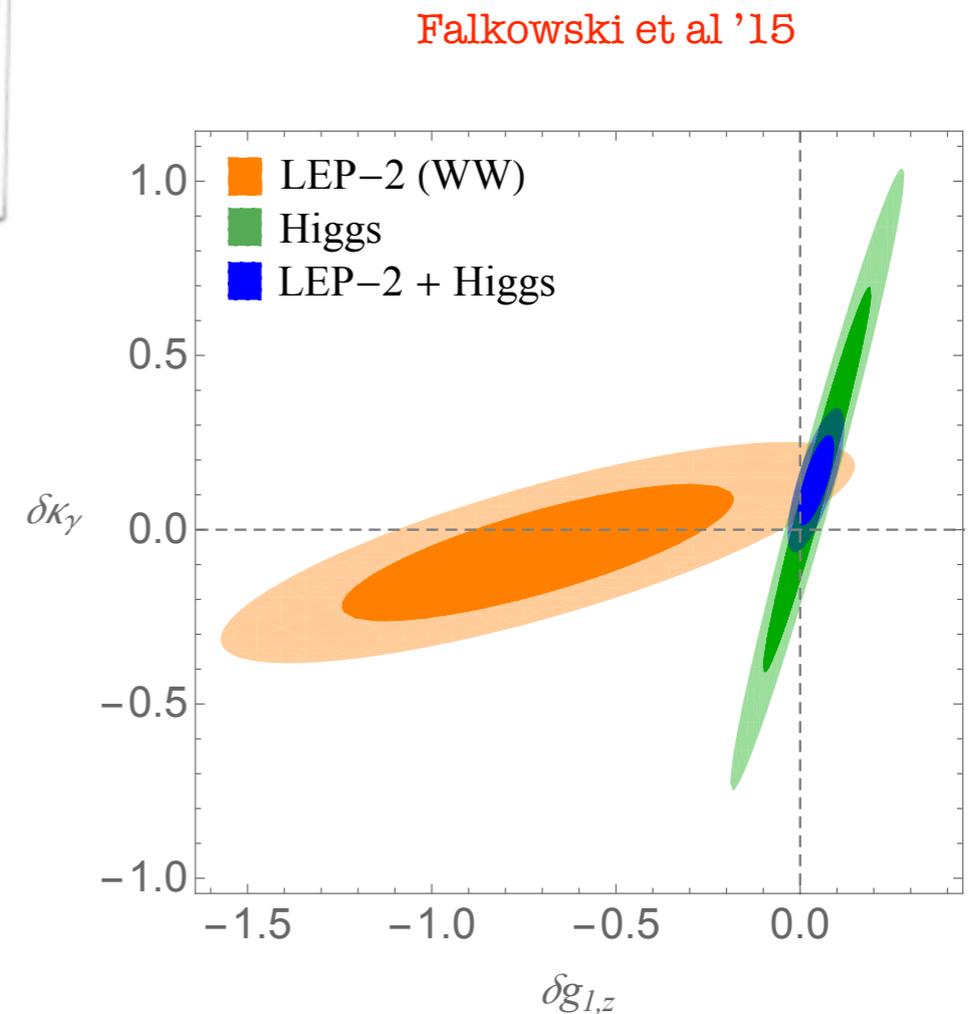
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$$(TGC \cup \text{Higgs}) > (TGC) + (\text{Higgs})$$

Strong correlations between 2 data sets

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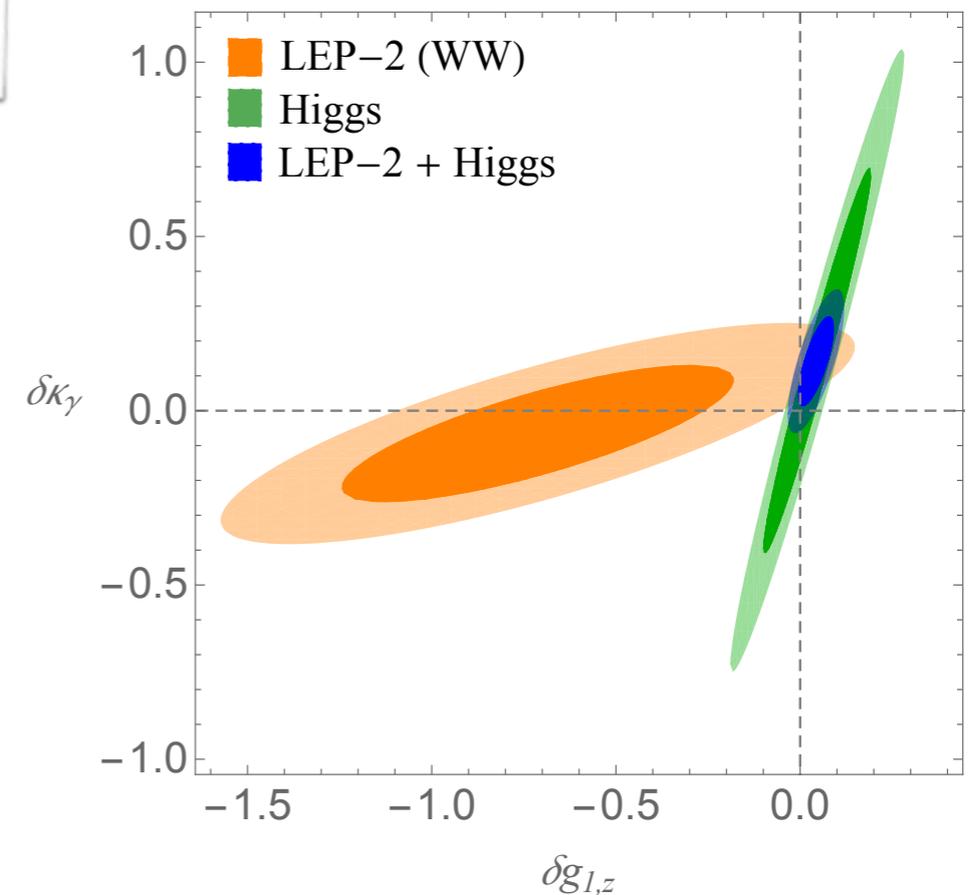
Impact of LHC WW data?

Impact of FCC-ee_{350GeV} WW data?

$(\text{TGC} \cup \text{Higgs}) > (\text{TGC}) + (\text{Higgs})$

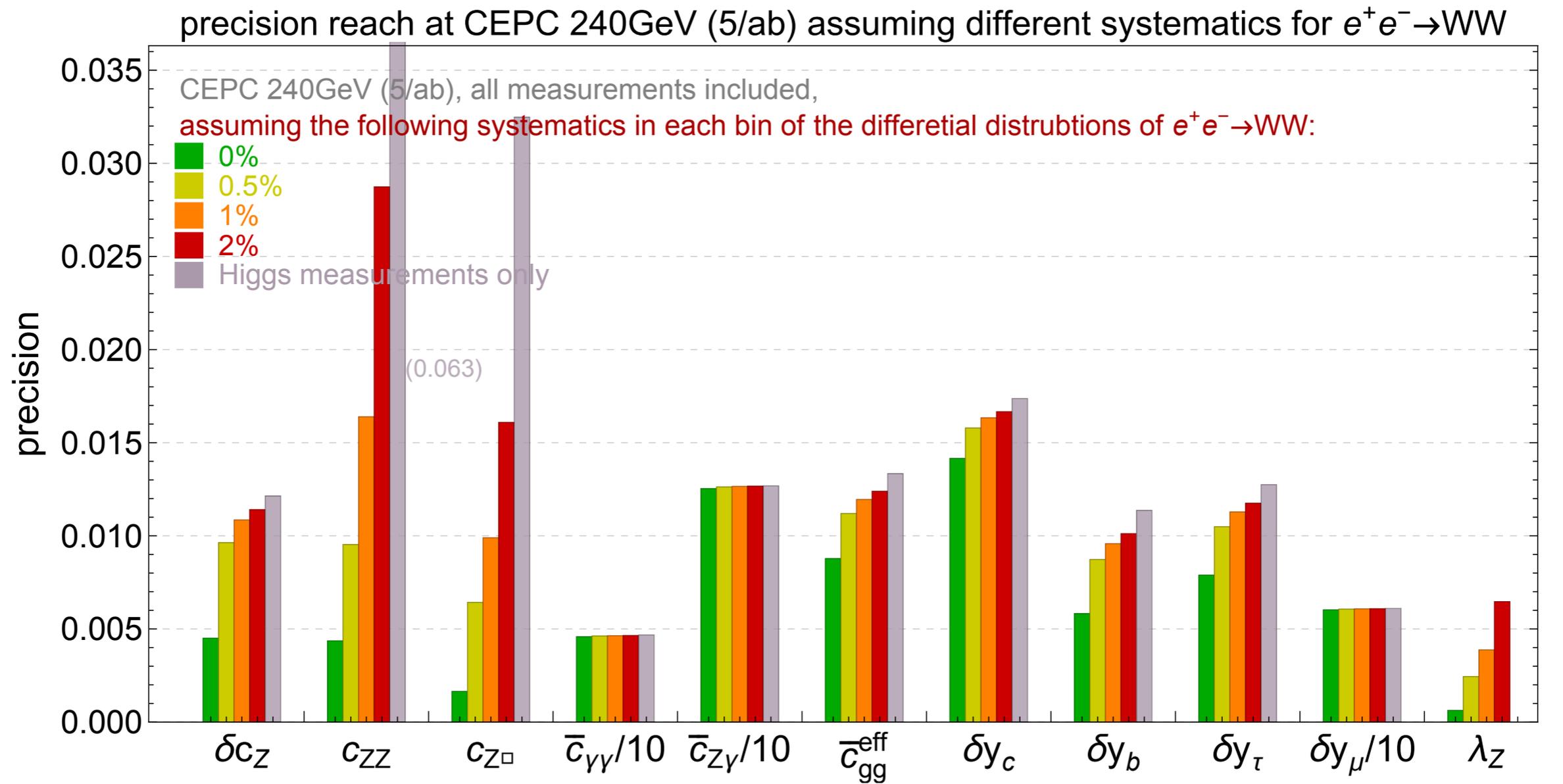
Strong correlations between 2 data sets

Falkowski et al '15



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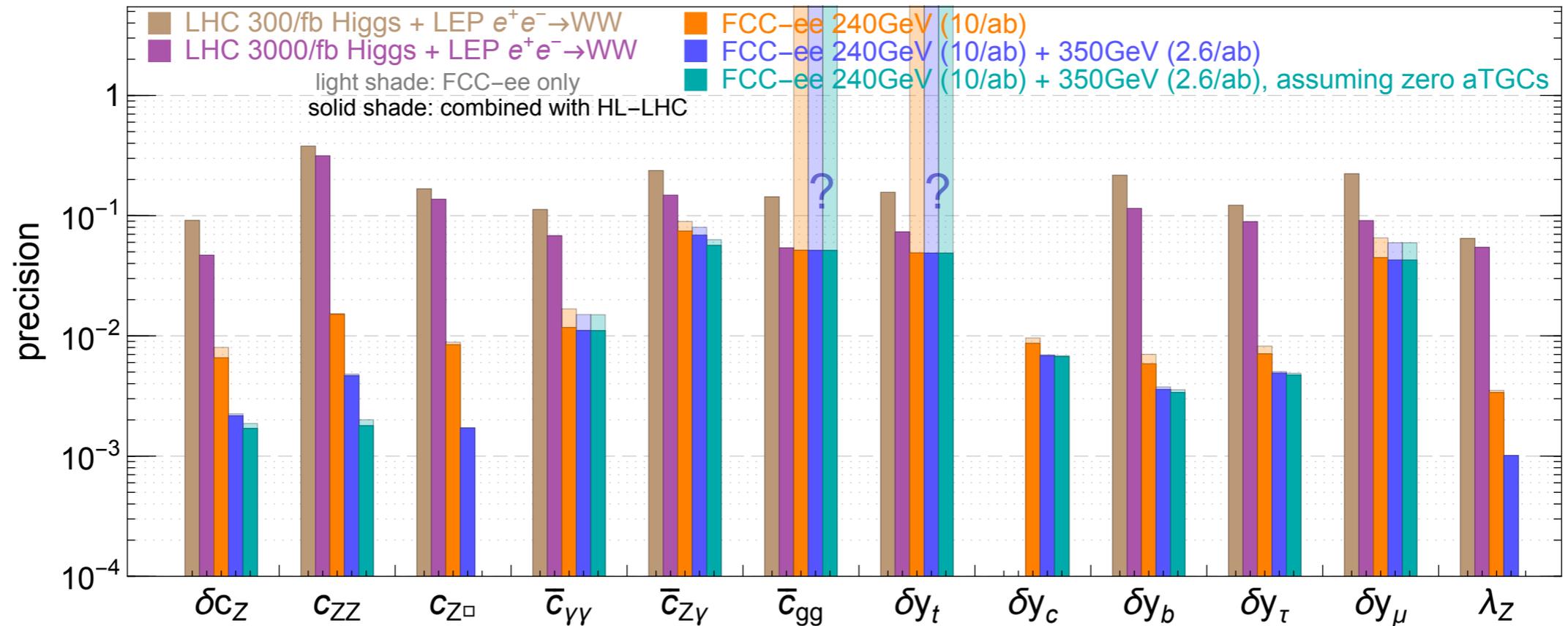


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Top + Higgs

I low energy ee collider doesn't have access to top Yukawa

precision reach of the 12-parameter fit in Higgs basis



Durieux, Grojean, Gu, Wang '17

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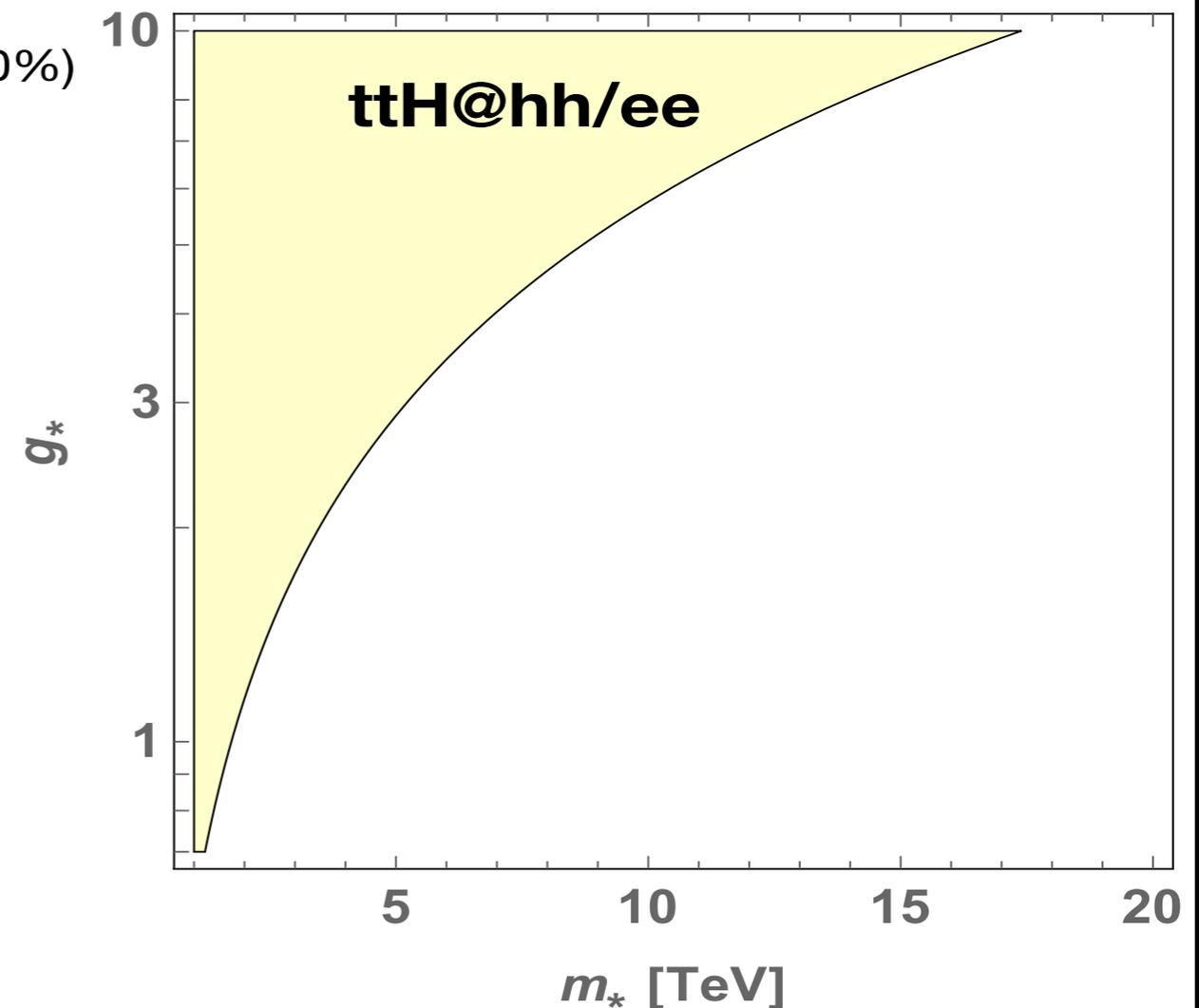
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ttH coupling @hh/ee: [Reports] (HL-LHC:10%)

$$\frac{y_t g_*^2}{m_*^2} |H|^2 \bar{q}_L H t_R \quad \longrightarrow \quad \frac{\delta y_t}{y_t} = \frac{g_*^2 v^2}{m_*^2} < 2 \cdot 10^{-2}$$

Diff. oper.s comb. in ee and hh!!



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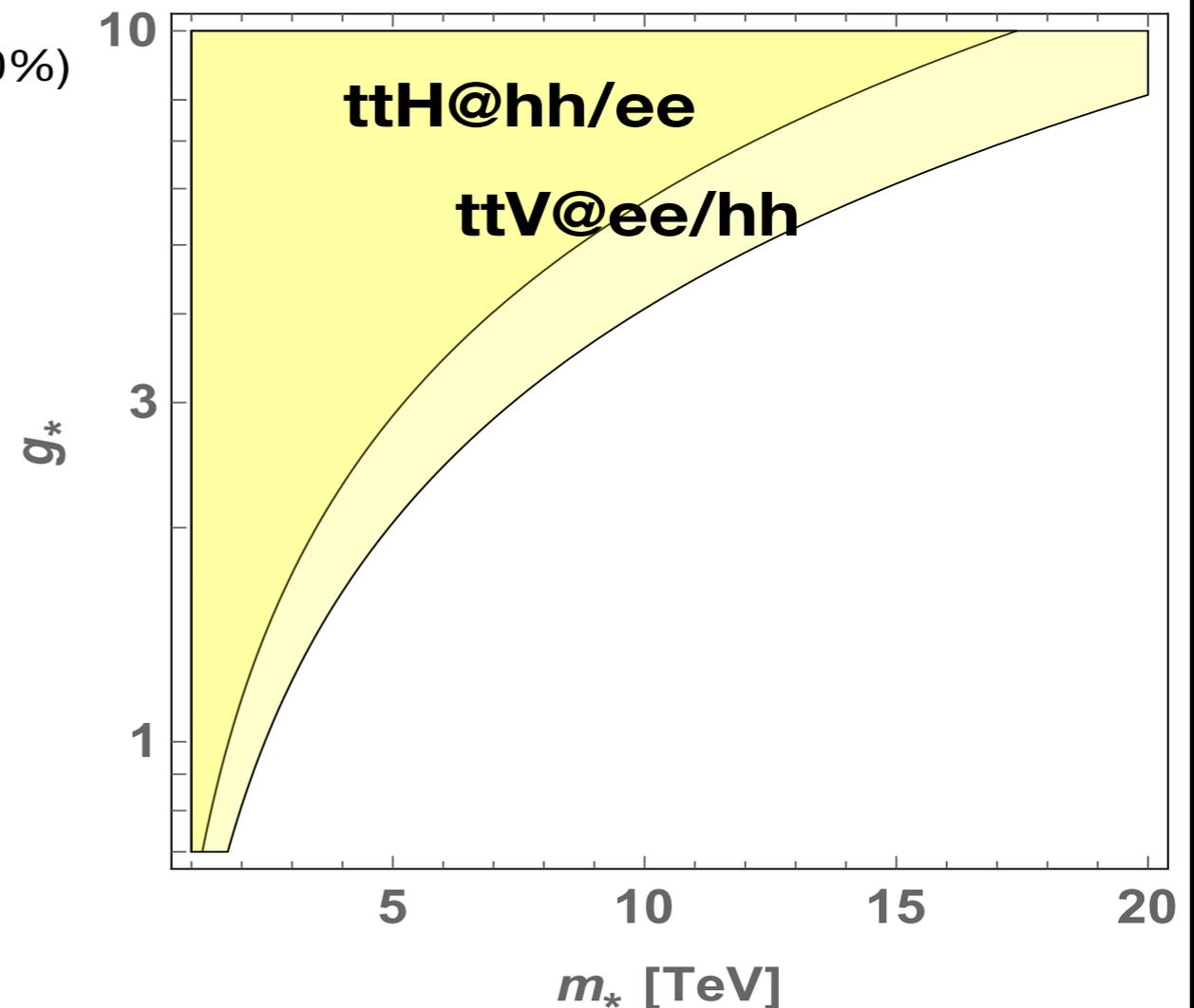
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ttV coupling @ee/hh: [Janot / Farina et.al.]

$$\frac{g_*^2}{m_*^2} H^\dagger \overleftrightarrow{D}_\mu H \bar{t}_R \gamma^\mu t_R \quad \longrightarrow \quad \frac{\delta g_{tV}}{g_{tV}} = \frac{g_*^2 v^2}{m_*^2} < 10^{-2}$$

Same hh reach from en. + acc.?



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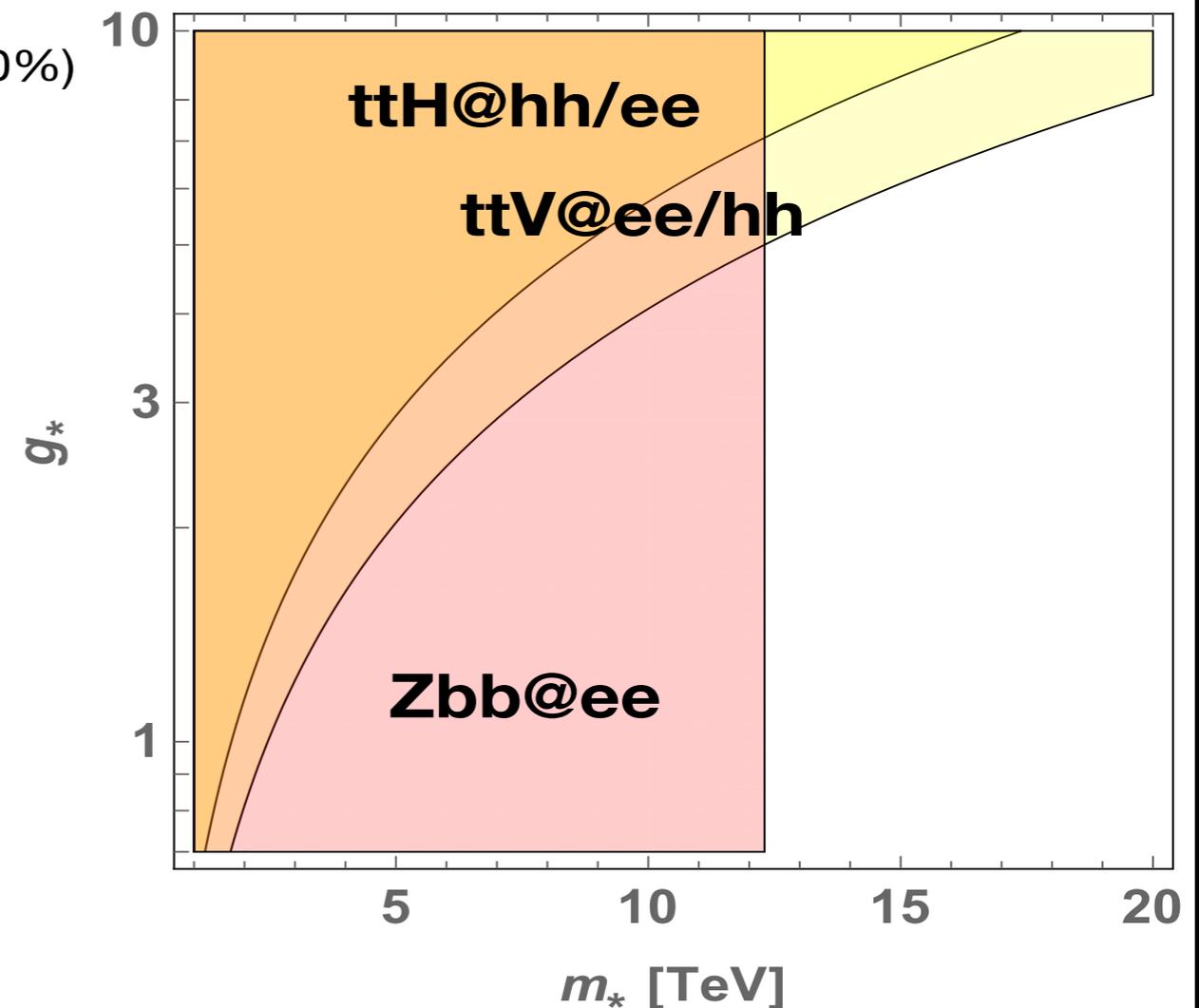
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Same hh reach from en. + acc.?

Zbb coupling @ee: [ee Report] (LEP:10⁻³)

$$\frac{y_t^2}{m_*^2} H^\dagger \overleftrightarrow{D}_\mu H \bar{q}_L \gamma^\mu q_L + \dots \quad \longrightarrow \quad \frac{\delta g_b}{g_b} = \frac{m_t^2}{m_*^2} < 2 \cdot 10^{-4}$$



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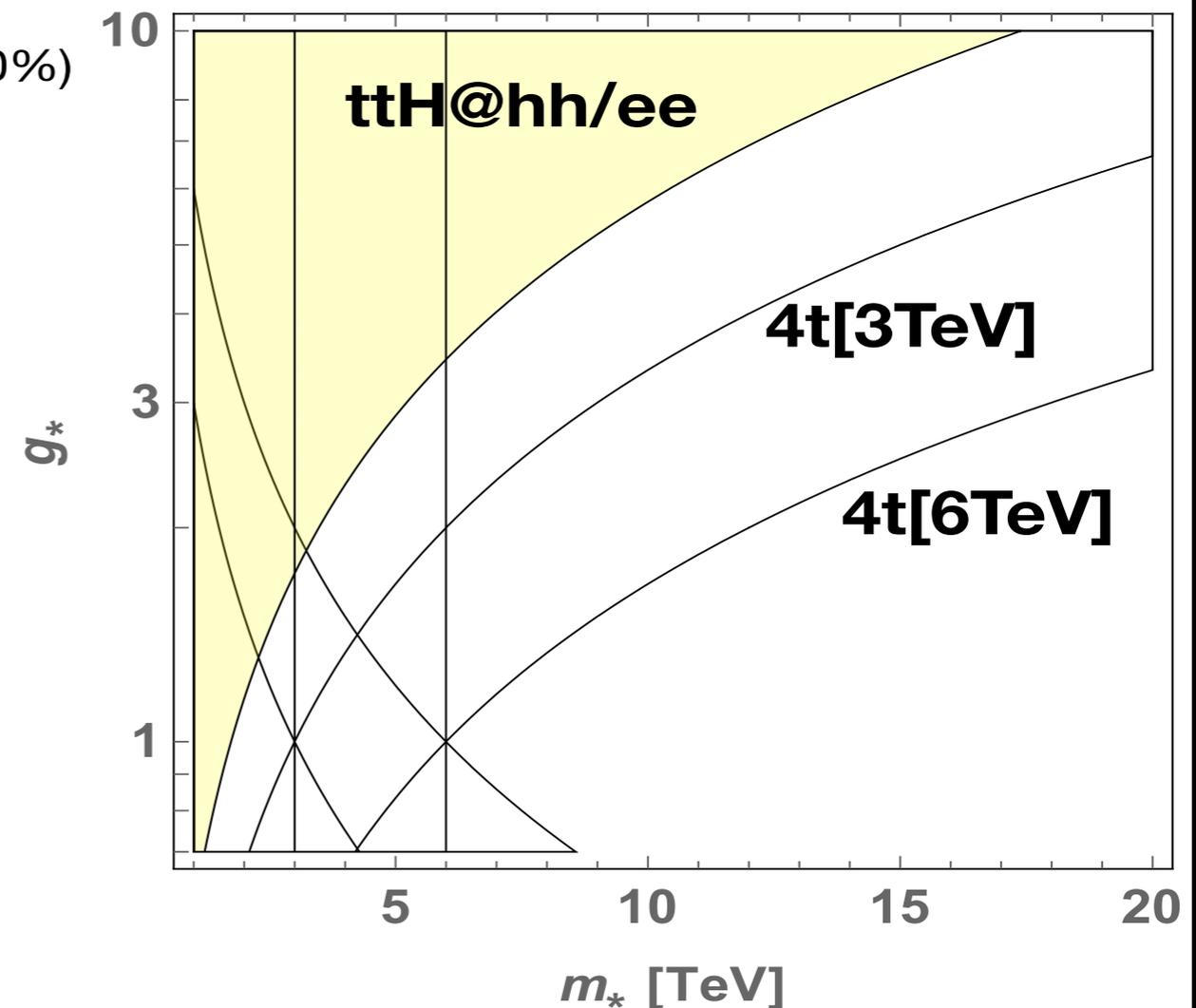
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Diff. oper.s comb. in ee and hh!!

4-top contact interactions @hh:

$$\begin{aligned} \frac{g_*^2}{m_*^2} (\bar{t}_R \gamma_\mu t_R)^2 &\longrightarrow \frac{g_*^2}{m_*^2} < \frac{1}{\Lambda_{4t}^2} \\ \frac{y_t^2}{m_*^2} (\bar{q}_L \gamma_\mu q_L) (\bar{t}_R \gamma_\mu t_R) &\longrightarrow \frac{y_t^2}{m_*^2} < \frac{1}{\Lambda_{4t}^2} \\ \frac{y_t^4}{g_*^2 m_*^2} (\bar{q}_L \gamma_\mu q_L)^2 &\longrightarrow \frac{y_t^4}{g_*^2 m_*^2} < \frac{1}{\Lambda_{4t}^2} \end{aligned}$$

No study available (?)



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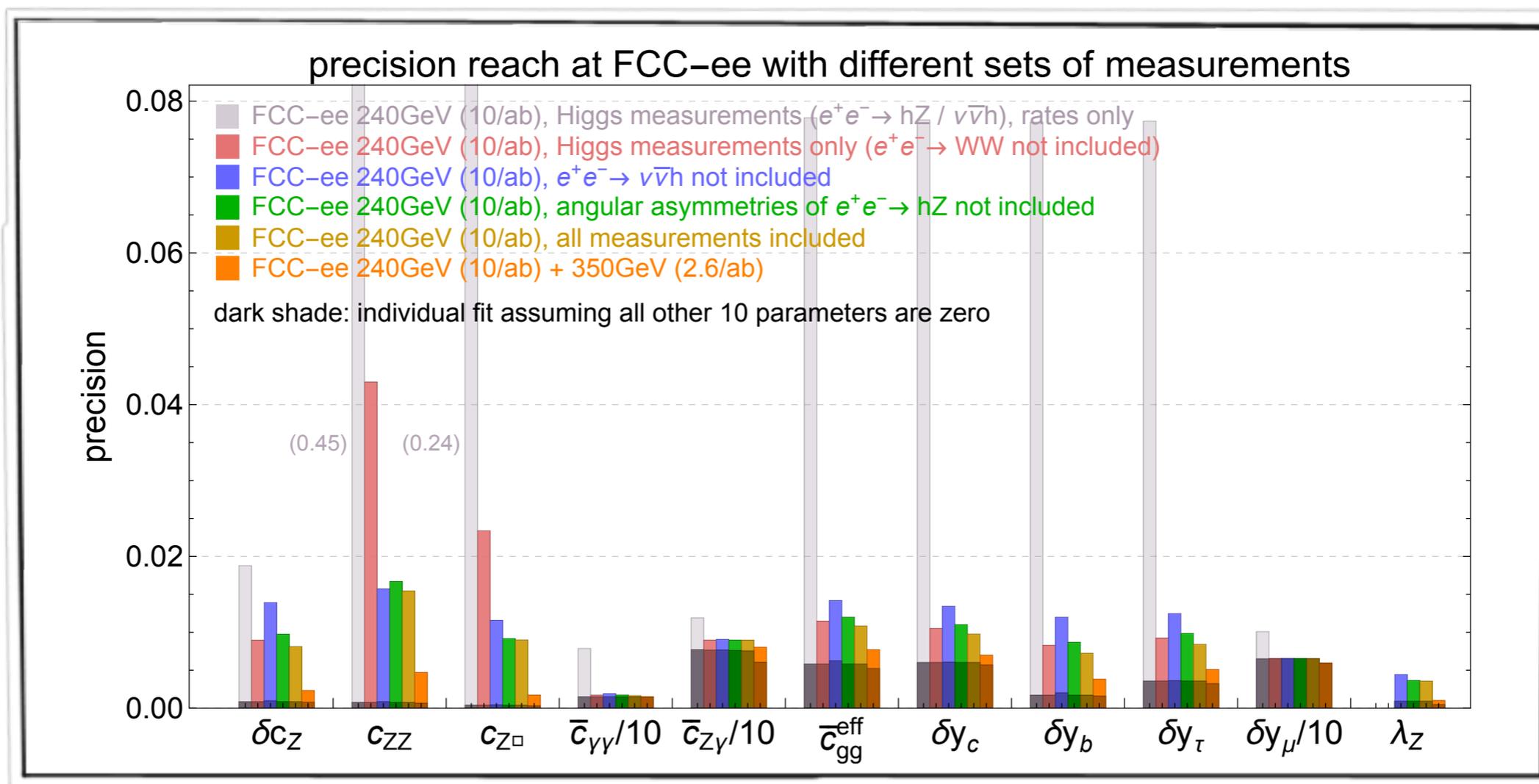
Distributions + rates



in progress

240 + 350

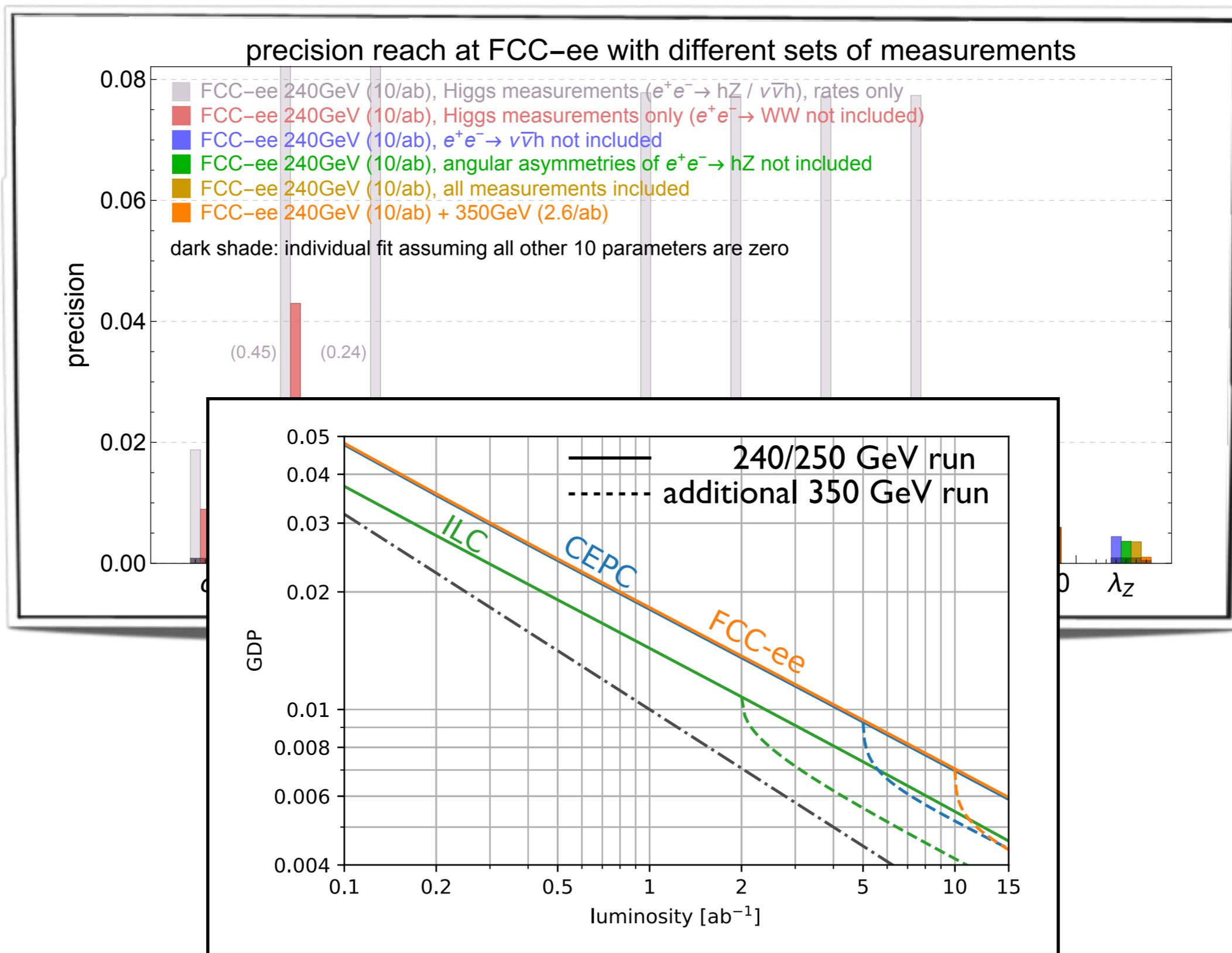
Runs at different energies break degeneracies plaguing coupling fits at 240GeV alone



Durieux, Grojean, Gu, Wang '17

240 + 350

Runs at different energies break degeneracies plaguing coupling fits at 240GeV alone



Higgs self-coupling(s)



in progress

Backup

e^+e^- Colliders

CepC

5/ab @ 240GeV
(200/fb @ 350GeV)

FCC-ee

10/ab @ 240GeV
(2.6/ab @ 350GeV)

ILC

2/ab @ 250GeV
 $P(e^-,e^+)=(\pm 80\%, \pm 30\%)$
(200/fb @ 350GeV)
(4/ab @ 500GeV)

CLIC

0.5/ab @ 350GeV
(1.5/ab @ 1.4TeV)
(3/ab @ 3TeV)

production	CEPC				FCC-ee			
	[240 GeV, 5 ab ⁻¹]		[350 GeV, 200 fb ⁻¹]		[240 GeV, 10 ab ⁻¹]		[350 GeV, 2.6 ab ⁻¹]	
σ	0.50%	-	2.4%	-	0.40%	-	0.67%	-
	$\sigma \times \text{BR}$				$\sigma \times \text{BR}$			
$h \rightarrow b\bar{b}$	0.21% [★]	0.39% [◇]	2.0%	2.6%	0.20%	0.28% [◇]	0.54%	0.71%
$h \rightarrow c\bar{c}$	2.5%	-	15%	26%	1.2%	-	4.1%	7.1%
$h \rightarrow g\bar{g}$	1.2%	-	11%	17%	1.4%	-	3.1%	4.7%
$h \rightarrow \tau\tau$	1.0%	-	5.3%	37%	0.7%	-	1.5%	10%
$h \rightarrow WW^*$	1.0%	-	10%	9.8%	0.9%	-	2.8%	2.7%
$h \rightarrow ZZ^*$	4.3%	-	33%	33%	3.1%	-	9.2%	9.3%
$h \rightarrow \gamma\gamma$	9.0%	-	51%	77%	3.0%	-	14%	21%
$h \rightarrow \mu\mu$	12%	-	115%	275%	13%	-	32%	76%
$h \rightarrow Z\gamma$	25%	-	144%	-	18%	-	40%	-

ILC

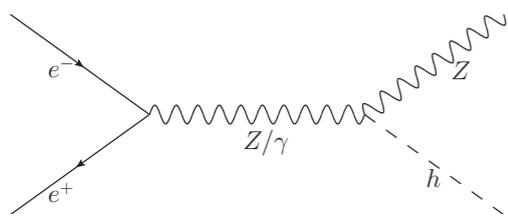
production	[250 GeV, 2 ab ⁻¹]		[350 GeV, 200 fb ⁻¹]		[500 GeV, 4 ab ⁻¹]			[1 TeV, 1 ab ⁻¹]		[1 TeV, 2.5 ab ⁻¹]	
	Zh	$\nu\bar{\nu}h$	Zh	$\nu\bar{\nu}h$	Zh	$\nu\bar{\nu}h$	$t\bar{t}h$	$\nu\bar{\nu}h$	$t\bar{t}h$	$\nu\bar{\nu}h$	$t\bar{t}h$
σ	0.71%	-	2.1%	-	1.1%	-	-	-	-	-	-
	$\sigma \times \text{BR}$										
$h \rightarrow b\bar{b}$	0.42%	3.7%	1.7%	1.7%	0.64%	0.25%	9.9%	0.5%	6.0%	0.3%	3.8%
$h \rightarrow c\bar{c}$	2.9%	-	13%	17%	4.6%	2.2%	-	3.1%	-	2.0%	-
$h \rightarrow g\bar{g}$	2.5%	-	9.4%	11%	3.9%	1.4%	-	2.3%	-	1.4%	-
$h \rightarrow \tau\tau$	1.1%	-	4.5%	24%	1.9%	3.2%	-	1.6%	-	1.0%	-
$h \rightarrow WW^*$	2.3%	-	8.7%	6.4%	3.3%	0.85%	-	3.1%	-	2.0%	-
$h \rightarrow ZZ^*$	6.7%	-	28%	22%	8.8%	2.9%	-	4.1%	-	2.6%	-
$h \rightarrow \gamma\gamma$	12%	-	44%	50%	12%	6.7%	-	8.5%	-	5.4%	-
$h \rightarrow \mu\mu$	25%	-	98%	180%	31%	25%	-	31%	-	20%	-
$h \rightarrow Z\gamma$	34%	-	145%	-	49%	-	-	-	-	-	-

CLIC

production	[350 GeV, 500 fb ⁻¹]		[1.4 TeV, 1.5 ab ⁻¹]		[3 TeV, 2 ab ⁻¹]
	Zh	$\nu\bar{\nu}h$	$\nu\bar{\nu}h$	$t\bar{t}h$	$\nu\bar{\nu}h$
σ	1.6%	-	-	-	-
	$\sigma \times \text{BR}$				
$h \rightarrow b\bar{b}$	0.84%	1.9%	0.4%	8.4%	0.3%
$h \rightarrow c\bar{c}$	10.3%	14.3%	6.1%	-	6.9%
$h \rightarrow g\bar{g}$	4.5%	5.7%	5.0%	-	4.3%
$h \rightarrow \tau\tau$	6.2%	-	4.2%	-	4.4%
$h \rightarrow WW^*$	5.1%	-	1.0%	-	0.7%
$h \rightarrow ZZ^*$	-	-	5.6%	-	3.9%
$h \rightarrow \gamma\gamma$	-	-	15%	-	10%
$h \rightarrow \mu\mu$	-	-	38%	-	25%
$h \rightarrow Z\gamma$	-	-	42%	-	30%

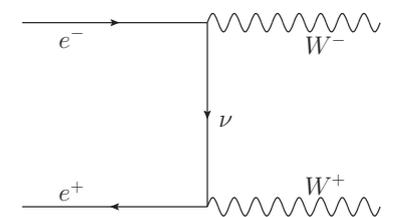
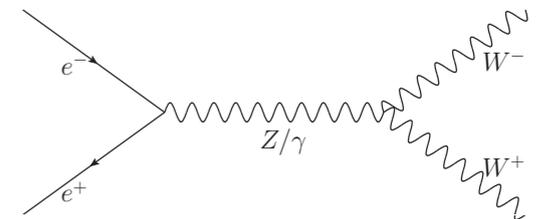
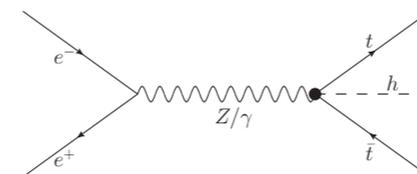
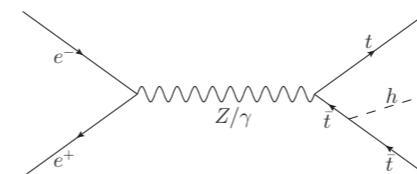
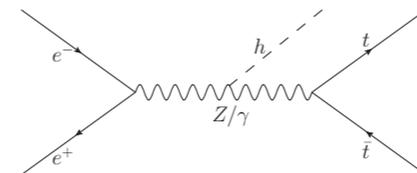
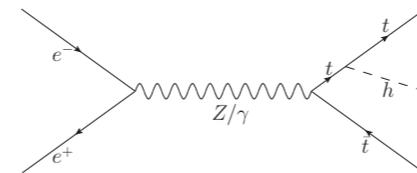
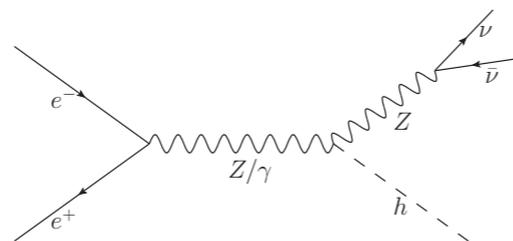
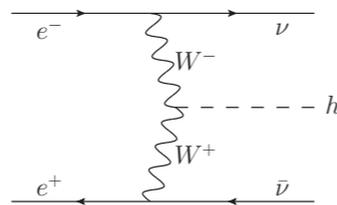
Future measurements used in the fit

- Higgsstrahlung production: $e^+e^- \rightarrow hZ$ (rates and distributions), followed by Higgs decays in various channels,
- Higgs production through weak-boson-fusion: $e^+e^- \rightarrow \nu\bar{\nu}h$,
- Higgs production in association with top quarks: $e^+e^- \rightarrow t\bar{t}h$,
- weak boson pair production: $e^+e^- \rightarrow WW$ (rate and distributions).



5/ab @ 240GeV
 1.06×10^6 Higgses

2/ab @ 250GeV
 $P(e^-, e^+) = (-80\%, +30\%)$
 6.4×10^5 Higgses



Higgs Basis

A. Falkowski '15

LHCHSWG YR4 '16

$$\begin{aligned}
 \mathcal{L} \supset & \frac{h}{v} \left[\delta c_w \frac{g^2 v^2}{2} W_\mu^+ W^{-\mu} + \delta c_z \frac{(g^2 + g'^2) v^2}{4} Z_\mu Z^\mu \right. \\
 & + c_{ww} \frac{g^2}{2} W_{\mu\nu}^+ W^{-\mu\nu} + c_{w\Box} g^2 (W_\mu^- \partial_\nu W^{+\mu\nu} + \text{h.c.}) + \hat{c}_{\gamma\gamma} \frac{e^2}{4\pi^2} A_{\mu\nu} A^{\mu\nu} \\
 & + c_{zz} \frac{g^2 + g'^2}{4} Z_{\mu\nu} Z^{\mu\nu} + \hat{c}_{z\gamma} \frac{e\sqrt{g^2 + g'^2}}{2\pi^2} Z_{\mu\nu} A^{\mu\nu} + c_{z\Box} g^2 Z_\mu \partial_\nu Z^{\mu\nu} + c_{\gamma\Box} g g' Z_\mu \partial_\nu A^{\mu\nu} \left. \right] \\
 & + \frac{g_s^2}{48\pi^2} \left(\hat{c}_{gg} \frac{h}{v} + \hat{c}_{gg}^{(2)} \frac{h^2}{2v^2} \right) G_{\mu\nu} G^{\mu\nu} - \sum_f \left[m_f \left(\delta y_f \frac{h}{v} + \delta y_f^{(2)} \frac{h^2}{2v^2} \right) \bar{f}_R f_L + \text{h.c.} \right] \\
 & - (\kappa_\lambda - 1) \lambda_3^{SM} v h^3,
 \end{aligned}$$

with

$$\delta c_w = \delta c_z,$$

$$c_{ww} = c_{zz} + 2 \frac{g'^2}{\pi^2 (g^2 + g'^2)} \hat{c}_{z\gamma} + \frac{g'^4}{\pi^2 (g^2 + g'^2)^2} \hat{c}_{\gamma\gamma},$$

$$c_{w\Box} = \frac{1}{g^2 - g'^2} \left[g^2 c_{z\Box} + g'^2 c_{zz} - e^2 \frac{g'^2}{\pi^2 (g^2 + g'^2)} \hat{c}_{\gamma\gamma} - (g^2 - g'^2) \frac{g'^2}{\pi^2 (g^2 + g'^2)} \hat{c}_{z\gamma} \right],$$

$$c_{\gamma\Box} = \frac{1}{g^2 - g'^2} \left[2g^2 c_{z\Box} + (g^2 + g'^2) c_{zz} - \frac{e^2}{\pi^2} \hat{c}_{\gamma\gamma} - \frac{g^2 - g'^2}{\pi^2} \hat{c}_{z\gamma} \right],$$

$$\hat{c}_{gg}^{(2)} = \hat{c}_{gg},$$

$$\delta y_f^{(2)} = 3\delta y_f - \delta c_z.$$

10 parameters

6 deformations of Higgs couplings to gauge bosons

$$\delta c_z, c_{zz}, c_{z\Box}, \hat{c}_{z\gamma}, \hat{c}_{\gamma\gamma}, \hat{c}_{gg}$$

3 deformations of Higgs couplings to fermions

$$\delta y_t, \delta y_b, \delta y_\tau,$$

1 deformations of Higgs self-couplings

$$\kappa_\lambda$$

Higgs Basis

A. Falkowski '15

LHCHXSWG YR4 '16

$$\begin{aligned}
 \mathcal{L} \supset & \frac{h}{v} \left[\delta c_w \frac{g^2 v^2}{2} W_\mu^+ W^{-\mu} + \delta c_z \frac{(g^2 + g'^2) v^2}{4} Z_\mu Z^\mu \right. \\
 & + c_{ww} \frac{g^2}{2} W_{\mu\nu}^+ W^{-\mu\nu} + c_{w\Box} g^2 (W_\mu^- \partial_\nu W^{+\mu\nu} + \text{h.c.}) + \hat{c}_{\gamma\gamma} \frac{e^2}{4\pi^2} A_{\mu\nu} A^{\mu\nu} \\
 & + c_{zz} \frac{g^2 + g'^2}{4} Z_{\mu\nu} Z^{\mu\nu} + \hat{c}_{z\gamma} \frac{e\sqrt{g^2 + g'^2}}{2\pi^2} Z_{\mu\nu} A^{\mu\nu} + c_{z\Box} g^2 Z_\mu \partial_\nu Z^{\mu\nu} + c_{\gamma\Box} g g' Z_\mu \partial_\nu A^{\mu\nu} \left. \right] \\
 & + \frac{g_s^2}{48\pi^2} \left(\hat{c}_{gg} \frac{h}{v} + \hat{c}_{gg}^{(2)} \frac{h^2}{2v^2} \right) G_{\mu\nu} G^{\mu\nu} - \sum_f \left[m_f \left(\delta y_f \frac{h}{v} + \delta y_f^{(2)} \frac{h^2}{2v^2} \right) \bar{f}_R f_L + \text{h.c.} \right] \\
 & - (\kappa_\lambda - 1) \lambda_3^{SM} v h^3,
 \end{aligned}$$

with

$$\delta c_w = \delta c_z,$$

$$c_{ww} = c_{zz} + 2 \frac{g'^2}{\pi^2 (g^2 + g'^2)} \hat{c}_{z\gamma} + \frac{g'^4}{\pi^2 (g^2 + g'^2)^2} \hat{c}_{\gamma\gamma},$$

$$c_{w\Box} = \frac{1}{g^2 - g'^2} \left[g^2 c_{z\Box} + g'^2 c_{zz} - e^2 \frac{g'^2}{\pi^2 (g^2 + g'^2)} \hat{c}_{\gamma\gamma} - (g^2 - g'^2) \frac{g'^2}{\pi^2 (g^2 + g'^2)} \hat{c}_{z\gamma} \right],$$

$$c_{\gamma\Box} = \frac{1}{g^2 - g'^2} \left[2g^2 c_{z\Box} + (g^2 + g'^2) c_{zz} - \frac{e^2}{\pi^2} \hat{c}_{\gamma\gamma} - \frac{g^2 - g'^2}{\pi^2} \hat{c}_{z\gamma} \right],$$

$$\hat{c}_{gg}^{(2)} = \hat{c}_{gg},$$

$$\delta y_f^{(2)} = 3\delta y_f - \delta c_z.$$

12 parameters

6 deformations of Higgs couplings to gauge bosons

$$\delta c_z, c_{zz}, c_{z\Box}, \hat{c}_{z\gamma}, \hat{c}_{\gamma\gamma}, \hat{c}_{gg}.$$

5 deformations of Higgs couplings to fermions

$$\delta y_t, \delta y_c, \delta y_b, \delta y_\tau, \delta y_\mu.$$

1 deformation of gauge boson self-couplings

$$\lambda_Z$$

Introducing the **G**lobal **D**eterminant **P**arameter

Durieux, Grojean, Gu, Wang '17

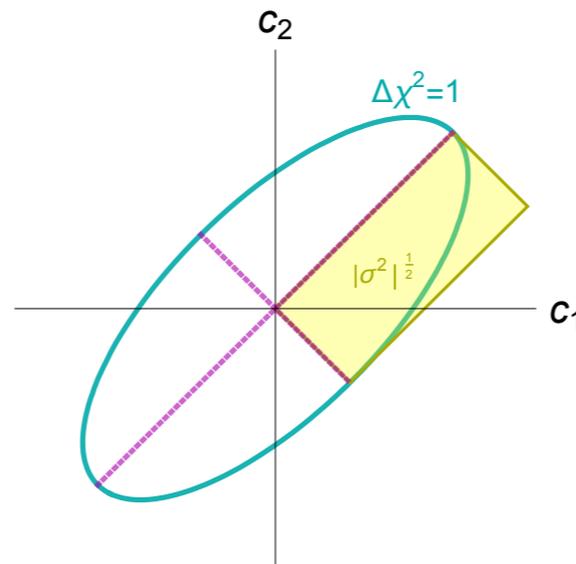


Figure 6: In a two-dimensional parameter space, the area of the Gaussian one-sigma ellipse is proportional to the square root of the determinant of the covariance matrix, $\sqrt{\det \sigma^2}$. In n dimensions, the n th root of this quantity or *global determinant parameter* (GDP) provides an average of constraints strengths. $\text{GDP} \equiv \sqrt[n]{\det \sigma^2}$ ratios measure improvement in global constraint strengths independently of effective-field-theory operator basis.

ratios of GDP are independent of parameters normalization
ratios of GDP are independent of EFT operator basis

smaller GDP = better precision