## News from beam-beam SixTrack development

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E. Metral, Y. Papaphilippou, T. Pieloni for discussions

WP2 meeting 23/5/2017

## Beam-beam kick recap.

- Strong beam is sliced in both 4D and 6D model according to the longitudinal charge distributions and centroid positions
- 4D uncoupled beam-beam kick uses $\mathrm{d}_{\mathrm{x}}, \mathrm{d}_{\mathrm{y}}, \Sigma_{\mathrm{xx}}, \Sigma_{\mathrm{yy}}$ to calculate the kick in $\Delta p_{x, y}$ for each weak particle
- 6D beam-beam effects are introduced by the Synchro beam mapping such that
- $\Delta p_{x, y}$ is calculated for the $d_{x}, d_{y}, \Sigma_{x x}, \Sigma_{y y}$ at the effective interaction point using (ct, $p_{x}, p_{y}, \Sigma$ ) at the reference IP
- a $\Delta p_{t}$ (emerging from the ct dependence) is also applied
- with crossing angle a translation, rotation and a boost change the reference frame in which $\left\langle p_{x, y}\right\rangle, X, Y, P_{x, y}=0$
- With coupling the uncoupled form is used in a rotated frame (ct dependent for the 6D kick)

1. 1976, "Potential of a Three-Dimensional Gaussian Bunch", S. Kheifets, PETRA Note 119, 3D electric potential
2. 1980, Closed expression for the electrical field of a two-dimensional Gaussian charge, M. Bassetti, A. Erskine, CERN-ISR-TH-80-06; 4D beam beam kick
3. 1992, A Symplectic Beam-Beam Interaction with Energy Change, K. Hirata, F. Ruggiero, SLAC-PUB10055, KEK Preprint 92-117; Synchro beam mapping (SBM) for head-on beam-beam effects.
4. 1994, Don't Be Afraid of Beam-Beam Interactions With a Large Crossing angle, K. Hirata. SBM with crossing angle
5. 2001, 6D Beam-Beam Kick including Coupled Motion, L.H.A. Leunissen, F. Schmidt,G. Ripken; SBM with crossing angle and coupling

## Options in Standard SixTrack BB interface

lhc=0, uses as input:

- position of the strong beam w.r.t the weak beam
- $\Sigma_{x x}, \Sigma_{y y}$ and other $\Sigma$ elements are calculated from the weak beam optics
- slicing is computed internally using as input number of slices, crossing angle (xang), and slices slope (xstr) [1];
$1 \mathrm{hc}=1$, as before but inverting x with y ;
lhc=2, as lhc=1:
- $\Sigma_{x x}, \Sigma_{y y}$ are taken as input in fort. 2 (generated by MadX from the values created by the beam-beam macros)
- other elements of $\Sigma$ are computed like $1 \mathrm{hc}=1$;
[1] J. Barranco, On-going SixTrack code development, 30/5/2013, LHC-Beam-beam meeting


## 6D Beam-Beam in SixTrack

Timeline:

- 1996

6D kick BCC code from Hirata

- 2000 6D code in SixTrack with coupling (coupling not used in production)
- 9/2/2011 lhc=2 option introduced by E. Laface for flat beam with 4D lenses
- 30/12/2013 $\mathrm{lhc}=2$ fix for 6D and phi2 for effective crab angle by J. Barranco for 6D
- 24/3/2014 discussion and decision to change 6D interface to fix 6D issues:go on with previous fix in the short term, then implement general solution
- 11/5/2014 lhc=2 option in SixTrack release for Boinc
- 11/9/2015 sigma matrix calculation in MadX requested
- 24/9/2015 last test/code/manual sent by Javier and reviewed/integrated by Kyrre
- 12/4/2017 MadX production release with sigma matrix calculation available
- 19/4/2017 Javier code merged with new expert interface merged by Kyrre and Riccardo
" 10/3/2017 Gianni started verifying equations from papers and code, bug in 6D boost identified and fixed by Gianni and merged by Riccardo, likely bug in coupling angle sign and other numerical issues under investigations
- 5/5/2017 beam-beam macro beam being adapted by Dario
- 5/5/2017 bug in sigma matrix calculation identified by Dario and corrected by Irina
- 17/5/2017 impact of boosti bug assessed with a tune scan by Dario
- 17/5/2017 macro completed and mask updated and tested in SixDesk (studies on going) by Dario


## Generalization of the interface

Needed to simulate in 6D:

- flat optics without relying on weak optics information
- crab crossing or other complex strong charge distributions
- dynamic effects like separation collapse or strong orbit noise using DYNK (to do)


## EXPERT interface

- Position of the strong beam w.r.t the weak beam, $\Sigma$ elements, crossing angle are taken as input and completely decoupled from weak beam.
- 1-slice 6D element supported to allow arbitrary longitudinal distribution and crab crossing with RF curvature via external slicing
- No special slice slope angle

New developments from release 4.6.16: [1]

- Standard and Expert method produces same results
- Standard and Expert interface now coexists and Expert input format is generated by SixTrack
[1] K. Sobjak, https://github.com/SixTrack/SixTrack/pull/246



59th HiLumi WP2 Task Leader Meeting
J. Barranco, Status of new input definition of the beam-beam lens in SixTrack, 13/11/2015, 59th WP2 meeting

## EXPERT interface (example)

```
Standard
bb_ho5b1_0 20 9.111827660e-07 -1.350224489e-06 1.000000000e+00 5.026457379e-05 5.026457406e-05 0.000000000e+00
bb ho1b1_0 20 9.669766338e-07 -1.378612898e-06 1.000000000e+00 5.026457379e-05 5.026457406e-05 0.000000000e+00
BEAM
2.2000e+11 2.5 2.5 7.5000e-02 1.1000e-04 1 0 0 0
bb_ho5b1_0 15 295e-6 0.0 295e-6
bb_ho1b1_0 15 295e-6 1.57 295e-6
NEXT
```


## Expert



BEAM
EXPERT
$2.2000 \mathrm{e}+112.52 .57 .5000 \mathrm{e}-021.1000 \mathrm{e}-041000$
bb ho5b1 $0152.9500000000001 e-0040.0000000000000 e+000 \quad 9.1118276600001 e-007-1.3502244890000 e-006$
$5.0034903462428 e-005-9.593556151459 e-0082.24428543738 e-0035.021051982892 e-005 \quad 7.5280318127904 e-007$
$2.2365333052480 e-003-1.663390341512 e-009-1.5308153223 e-0097.342199089562 e-010-6.517402396885 e-0091.000$
bb_ho1b1_0 $152.9500000000001 e-0041.5700000000001 e+000 \quad 9.66976633800002 e-007-1.3786128980000 e-006$
$5.0520079639196 e-005-6.010182490910 e-0072.22276103671 e-0035.028688389602 e-0057.7037643894229 e-007$
$2.2330903791604 e-003-3.652801218428 e-009 \quad 2.66101452881 e-008 \quad 3.638680415249 e-0081.1594595769731 e-0071.000$
NEXT
Expert input is also written by SixTrack in the standard output
Hilumi
HL-LHC PROJEC

## Update beam-beam macros

Former 4D beam-beam MadX macros from Stephane now write in the mask SixTrack Expert input by computing missing $\Sigma$ matrix elements for each slice

- centroid with crab effects and $\Sigma_{11,33}$ were already computed
- first sanity checks shows good agreement with previous models (cannot be reproduced fully because they were inconsistent)
- Test on full studies on-going
- Tracking with Beam 4 under investigation

Mad vs SixTrack
Sigma matrix calculations

|  | $\mathrm{mad} / \mathrm{six}$ | mad | sixtrack |
| :--- | :--- | :--- | :--- |
| sig11 | 1.00000002447 | 0.002246565358 | 0.00224656530302 |
| sig12 | 1.00000002437 | 0.0001498270964 | 0.000149827092749 |
| sig22 | 0.999999999265 | $6.00464297 e-05$ | $6.00464297441 \mathrm{e}-05$ |
| sig33 | 0.999999994158 | 0.01125155011 | 0.0112515501757 |
| sig34 | 0.999999994116 | -0.0007503841707 | -0.000750384175115 |
| sig44 | 0.999999999041 | $6.003852509 e-05$ | $6.00385251476 e-05$ |
| sig13 | 1.00000001226 | 0.0001896193048 | 0.000189619302476 |
| sig14 | 1.00000001153 | $-1.264601973 e-05$ | $-1.26460195841 e-05$ |
| sig23 | 1.00000001153 | $1.264601973 e-05$ | $1.26460195842 e-05$ |
| sig24 | 1.00000001202 | $-1.686933683 e-06$ | $-1.68693366273 e-06$ |

## Differences old to new macros

Old macros for 6D

- $\Sigma_{11,33}$ and $x_{B 2}, y_{B 2}$ computed from an ideal machine
- $\mathrm{X}_{\mathrm{B} 1}, \mathrm{y}_{\mathrm{B} 1}$ add from imperfect orbit by MadX
- Crossing angle input manually
- $\Sigma_{12,22,34,44,13,14,23,24,34}$ computed by Sixtrack based B1 optics
- $\Sigma_{13,14,23,24,34}$ discarded

New macros for 6D

- $\Sigma_{\text {full }}$ for and x,px,y,py for B1,2 computed from an ideal machine in MadX
- $\Sigma_{13,14,23,24,34}$ discarded pending verifications
- Input for Beam 1
- Beam 4 possible (under development)


## Review of the the 6D beam-beam routines

(Is the physics implemented correctly?)

## Review of the 6D beam-beam routines

Addressing two questions:

- What is the code supposed to do?
- Mathematical derivation of the implemented numerical model
- Is the code doing what it is supposed to do?
- Verify the implementation of the above numerical model


## Mathematical derivation

The code implements the Synchro Beam Mapping in the presence of:

- Crossing angle ( $\phi$ )
- Arbitrary crossing plane ( $\alpha$ )
- Optics at the IP described by a general 4D correlation matrix ( $\Sigma$-matrix) $\rightarrow$ hour glass effect, elliptic beams, alphas, and linear coupling at the IP are included in the modeling)

This makes the mathematical derivation quite heavy

Implementation in Sixtrack in largely based on:

- 6D Beam-Beam Kick including Coupled Motion, L.H.A. Leunissen, F. Schmidt, G. Ripken, 2001
... but important parts (e.g. inverse boost, "optics de-coupling" including longitudinal derivatives) are not reported in the paper nor anywhere else, to our best knowledge...


## Mathematical derivation

- Invested some time in understanding and re-constructing the mathematical treatment trying to use as little as possible the source code as a reference
$\rightarrow$ Independent reconstruction of the equations to verify the implementation in Sixtrack and to be used as a basis for a modern implementation (GPU compatible, for example)
$\rightarrow$ Parts not available in literature (mainly inverse Lorentz boost, and a large fraction of the coupling treatment) had to be re-derived
- Drafted a document including the full set of equation to enable a possible re-implementation (and avoid that somebody has to redo the same exercise in ten years)



## Verification of the implementation

- Started from previous work done by J. Barranco
- Identified and described the interface of the main functional blocks
- Built tables with the descriptions of the cumbersome notation used in the code

- Moved to the understanding and testing of the source code...


## Verification of the implementation

- Very difficult to identify problems by using the full tracking simulations
- Need to test the single routine "on the bench"
- Procedure being performed for each functional block
- Built a quick C/python implementation from the equations in the document
- Extracted the corresponding sixtrack source code and compiled as of a stand-alone python module (f2py)
- "Stress test" performed on the two: consistency checks, comparison against each other


## Verification of the implementation

- Present status of the verification for the different functional blocks:

| Module | Tests performed | Outcome |
| :---: | :---: | :---: |
| Boost/anti-boost | - Comparison Sixtrack vs C/python routine <br> - Checked that the two cancel each other | Bug identified and corrected |
| Beam-beam forces (with potential derivatives w.r.t. sigmas) | - Comparison sixtrack vs C/python routine <br> - Force compared against Finite Difference Poisson solved (PyPIC) <br> - Other derivatives compared against numerical integration/derivation | All checks passed |
| Beam shape propagation and coupling treatment | - Comparison Sixtrack vs C/python routine <br> - Comparison against MAD for a coupled beam line <br> - Crosscheck with numerical derivation | Ongoing: <br> - Uncoupled beams look OK <br> - Coupling under investigation: different problems already identified |
| Computation of the kicks | Still to be tested | Still to be tested |
| Slicing | Still to be tested | Still to be tested |

- Complete review to be presented later this year


## Problem in the inverse boost

- Problem identified with "bench-test" (large crossing angle, test particle very off momentum and large px, py)
- Boost and anti-boost should cancel each other exactly


## Error after boost + anti-boost

| Python test routine | SixTrack routine |  |  |
| :--- | :--- | :--- | :--- |
| $\mathbf{x}$ | $4.3 \mathrm{e}-19$ | $\mathbf{x}$ | $6.5 \mathrm{e}-19$ |
| px | 0.0 | px | 0.065 |
| $\mathbf{y}$ | $4.3 \mathrm{e}-19$ | $\mathbf{y}$ | $4.3 \mathrm{e}-19$ |
| py | $3 . \mathrm{e} 3-17$ | py | 0.027 |
| sigma | 0.0 | sigma | 0.0 |
| delta | $1 \mathrm{e}-16$ | delta | $2.0 \mathrm{e}-17$ |

## Problem in the inverse boost

- Problem identified with "bench-test" (large crossing angle, test particle very off momentum and large px, py)
- Boost and anti-boost should cancel each other exactly

Discrepancy found between in the anti-boost between derived equations and SixTrack source code:

$$
\begin{align*}
& p_{x}=p_{x}^{*} \cos \phi+h \cos \alpha \tan \phi  \tag{95}\\
& p_{y}=p_{y}^{*} \cos \phi+h \sin \alpha \tan \phi \tag{96}
\end{align*}
$$

```
TRACK (2) = (TRACK (2) +CALPHA*SPHI*H1) *CPHI
TRACK (4) = (TRACK (4) +SALPHA*SPHI*H1) *CPHI
```

The lines should be:

```
TRACK (2) = (TRACK (2) *CPHI+CALPHA*TPHI*H1)
TRACK (4)=(TRACK (4)*CPHI+SALPHA*TPHI*H1)
```

- Digging a bit we found out that the issue was already present in Hirata's code from 1996, on which the Sixtrack implementation is based


## Problem in the inverse boost

- Problem identified with "bench-test" (large crossing angle, test particle very off momentum and large px, py)
- Boost and anti-boost should cancel each other exactly


## Error after boost + anti-boost

Python test routine

| $\mathbf{x}$ | $4.3 e-19$ |
| :--- | :--- |
| $p x$ | 0.0 |
| $\mathbf{y}$ | $4.3 e-19$ |
| py | $3 . e 3-17$ |
| sigma | 0.0 |
| delta | $1 \mathrm{e}-16$ |

SixTrack routine

| $\mathbf{x}$ | $6.5 \mathrm{e}-19$ | $\mathbf{x}$ | $6.5 \mathrm{e}-19$ |
| :--- | :--- | :--- | :--- |
| $\mathbf{p x}$ | 0.065 | $\mathbf{p x}$ | $5.55 \mathrm{e}-17$ |
| $\mathbf{y}$ | $4.3 \mathrm{e}-19$ | $\mathbf{y}$ | $4.3 \mathrm{e}-19$ |
| py | 0.027 | py | $0.1 \mathrm{e}-19$ |
| sigma | 0.0 | sigma | 0.0 |
| delta | $2.0 \mathrm{e}-17$ | delta | $2.0 \mathrm{e}-17$ |

## Problem in the inverse boost

# Problem confirmed by Riccardo simulating a beam-beam interaction with zero intensity in the strong beam 

## Original implementation

Coordinates before interaction


## Coordinates after interaction

## [ dump_bb.dat

Coordinates before interaction

| 13- $\square^{\text {dump_ip.dat }}$ |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ID turn $\mathrm{s}[\mathrm{m}] \times \mathrm{mm}] \times \mathrm{xp}[\mathrm{mrad}] \mathrm{y}[\mathrm{mm}]$ yp[mrad] de/E[1] ktrack |  |  |  |  |  |  |
| 1 | 1 | 0.00000 | $1.444989354 \mathrm{E}-01$ | $1.217984946 \mathrm{E}-02$ | $2.341007330 \mathrm{E}-02$ | -1.973240618E-03 |
| 2 | 1 | 0.00000 | $1.444989354 \mathrm{E}-01$ | $1.217984946 \mathrm{E}-02$ | $2.341007330 \mathrm{E}-02$ | -1.973240618E-03 |
| 3 | 1 | 0.00000 | $2.169989354 \mathrm{E}-01$ | $1.829089161 \mathrm{E}-02$ | $1.931331047 \mathrm{E}-01$ | -1.627923509E-02 |
| 4 | 1 | 0.00000 | $2.169989354 \mathrm{E}-01$ | $1.829089161 \mathrm{E}-02$ | $1.931331047 \mathrm{E}-01$ | -1.627923509E-02 |
| 5 | 1 | 0.00000 | $2.894989354 \mathrm{E}-01$ | 2.440193375E-02 | 3.628561362E-01 | -3.058522956E-02 |
| 6 | 1 | 0.00000 | $2.894989354 \mathrm{E}-01$ | $2.440193375 \mathrm{E}-02$ | $3.628561362 \mathrm{E}-01$ | -3.058522956E-02 |
| 7 | 1 | 0.00000 | $3.619989354 \mathrm{E}-01$ | $3.051297588 \mathrm{E}-02$ | 5.325791676E-01 | -4.489122400E-02 |
| 8 | 1 | 0.00000 | $3.619989354 \mathrm{E}-01$ | $3.051297588 \mathrm{E}-02$ | $5.325791676 \mathrm{E}-01$ | $-4.489122400 \mathrm{E}-02$ |
| 9 | 1 | 0.00000 | $4.344989354 \mathrm{E}-01$ | $3.662401801 \mathrm{E}-02$ | 7.023021991E-01 | -5.919721844E-02 |
| 10 | 1 | 0.00000 | $4.344989354 \mathrm{E}-01$ | $3.662401801 \mathrm{E}-02$ | 7.023021991E-01 | -5.919721844E-02 |
| 1 |  | 0.00000 | 1.308501247E-01 | 8.514045444E-03 | -9.960917299E-03 | $3.153577120 \mathrm{E}-04$ |
| 2 |  | 0.00000 | 1.308501247E-01 | $8.514045444 \mathrm{E}-03$ | -9.960917299E-03 | $3.153577120 \mathrm{E}-04$ |
| 3 | 2 | 0.00000 | $1.041820623 \mathrm{E}-01$ | -1.200951763E-02 | -8.217756745E-02 | $2.601701095 \mathrm{E}-03$ |
| 4 | 2 | 0.00000 | $1.041820623 \mathrm{E}-01$ | -1.200951763E-02 | -8.217756745E-02 | $2.601701095 E-03$ |
| 5 | 2 | 0.00000 | 7.751400004E-02 | -3.253308069E-02 | -1.543942171E-01 | $4.888044424 \mathrm{E}-03$ |
| 6 | 2 | 0.00000 | $7.751400004 \mathrm{E}-02$ | -3.253308069E-02 | -1.543942171E-01 | $4.888044424 \mathrm{E}-03$ |
| 7 | 2 | 0.00000 | $5.084593802 \mathrm{E}-02$ | -5.305664374E-02 | -2.266108663E-01 | $7.174387701 \mathrm{E}-03$ |
| 8 | 2 | 0.00000 | 5.084593802E-02 | -5.305664374E-02 | -2.266108663E-01 | $7.174387701 \mathrm{E}-03$ |
| 9 | 2 | 0.00000 | $2.417787621 \mathrm{E}-02$ | -7.358020679E-02 | -2.988275150E-01 | $9.460730924 \mathrm{E}-03$ |
| 10 | 2 | 0.00000 | $2.417787621 \mathrm{E}-02$ | -7.358020679E-02 | -2.988275150E-01 | $9.460730924 \mathrm{E}-03$ |

[ad] y[mm] yp[mrad] dE/E[1] ktrack
$0.00000 \quad 1.444989354 \mathrm{E}-01 \quad 1.217984945 \mathrm{E}-02 \quad 2.341007330 \mathrm{E}-02-1.973250177 \mathrm{E}-03$ $0.00000 \quad 1.444989354 \mathrm{E}-01 \quad 1.217984945 \mathrm{E}-02 \quad 2.341007330 \mathrm{E}-02-1.973250177 \mathrm{E}-03$ $0.00000 \quad 2.169989354 \mathrm{E}-01 \quad 1.829089158 \mathrm{E}-02 \quad 1.931331047 \mathrm{E}-01-1.627927274 \mathrm{E}-02$ $\begin{array}{llllll}0.00000 & 2.169989354 \mathrm{E}-01 & 1.829089158 \mathrm{E}-02 & 1.931331047 \mathrm{E}-01 & -1.627927274 \mathrm{E}-02 \\ 0.00000 & 2.894989354 \mathrm{E}-01 & 2.440193367 \mathrm{E}-02 & 3.628561362 \mathrm{E}-01 & -3.058532567 \mathrm{E}-02\end{array}$ $\begin{array}{lllll}0.00000 & 2.894989354 \mathrm{E}-01 & 2.440193367 \mathrm{E}-02 & 3.628561362 \mathrm{E}-01 & -3.058532567 \mathrm{E}-02 \\ 0.00000 & 2.894989354 \mathrm{E}-01 & 2.440193367 \mathrm{E}-02 & 3.628561362 \mathrm{E}-01 & -3.058532567 \mathrm{E}-02\end{array}$ $\begin{array}{lllll}0.00000 & 2.894989354 \mathrm{E}-01 & 2.440193367 \mathrm{E}-02 & 3.628561362 \mathrm{E}-01 & -3.058532567 \mathrm{E}-02 \\ 0.00000 & 3.619989354 \mathrm{E}-01 & 3.051297574 \mathrm{E}-02 & 5.325791676 \mathrm{E}-01 & -4.489140898 \mathrm{E}-02\end{array}$ $\begin{array}{lllll}0.00000 & 3.619989354 \mathrm{E}-01 & 3.051297574 \mathrm{E}-02 & 5.325791676 \mathrm{E}-01 & -4.489140898 \mathrm{E}-02 \\ 0.00000 & 3.619989354 \mathrm{E}-01 & 3.051297574 \mathrm{E}-02 & 5.325791676 \mathrm{E}-01 & -4.489140898 \mathrm{E}-02\end{array}$ $\begin{array}{llllll}0.000000 & 4.344989354 \mathrm{E}-01 & 3.662401777 \mathrm{E}-02 & 7.023021991 \mathrm{E}-01 & -5.919752266 \mathrm{E}-02\end{array}$ $0.00000 \quad 4.344989354 \mathrm{E}-01 \quad 3.662401777 \mathrm{E}-02 \quad 7.023021991 \mathrm{E}-01 \quad-5.919752266 \mathrm{E}-02$ $0.00000 \quad 1.308501246 \mathrm{E}-01 \quad 8.514045441 \mathrm{E}-03-9.961266845 \mathrm{E}-03 \quad 3.153866850 \mathrm{E}-04$ $0.00000 \quad 1.308501246 \mathrm{E}-01 \quad 8.514045441 \mathrm{E}-03-9.961266845 \mathrm{E}-03 \quad 3.153866850 \mathrm{E}-04$ $0.00000 \quad 1.041820622 \mathrm{E}-01-1.200951763 \mathrm{E}-02-8.217894405 \mathrm{E}-02 \quad 2.601823666 \mathrm{E}-03$ $0.00000 \quad 1.041820622 \mathrm{E}-01-1.200951763 \mathrm{E}-02-8.217894405 \mathrm{E}-02 \quad 2.601823666 \mathrm{E}-03$ $0.00000 \quad 7.751399978 \mathrm{E}-02-3.253308074 \mathrm{E}-02 \mathbf{- 1}^{-1.543977321 \mathrm{E}-01} \begin{array}{llll}4.888313646 \mathrm{E}-03\end{array}$ $\begin{array}{lllll}0.00000 & 7.751399978 \mathrm{E}-02 & -3.253308074 \mathrm{E}-02 & -1.543977321 \mathrm{E}-01 & 4.888313646 \mathrm{E}-03 \\ 0.0000 & 5.084593752 \mathrm{E}-02 & -5.305664388 \mathrm{E}-02 & -2.266176309 \mathrm{E}-01 & 7.174856626 \mathrm{E}-03\end{array}$ $\begin{array}{lllll}0.00000 & 5.084593752 \mathrm{E}-02 & -5.305664388 \mathrm{E}-02 & -2.266176309 \mathrm{E}-01 & 7.174856626 \mathrm{E}-03 \\ 0.00000 & 5.084593752 \mathrm{E}-02 & -5.305664388 \mathrm{E}-02 & -2.266176309 \mathrm{E}-01 & 7.174856626 \mathrm{E}-03\end{array}$ $\begin{array}{lllll}0.00000 & 2.417787538 \mathrm{E}-02 & -7.358020705 \mathrm{E}-02 & -2.988386405 \mathrm{E}-01 & 9.461452606 \mathrm{E}-03\end{array}$
. 00000 2.417787538E-02 -7.358020705E-02 -2.988386405E-01 9.461452606E-03

## Corrected implementation

## Coordinates after interaction

$\square$
$\square$ $+{ }^{\text {ID }}$ $\square$ dump_bb.dat

| urn $\mathrm{s}[\mathrm{m}] \times \mathrm{mmm}$ ] xp [mrad] y[mm] yp[mrad] de/E[1] ktrack |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1 | 0.00000 | $1.444989354 \mathrm{E}-01$ | $1.217984946 \mathrm{E}-02$ | 2.341007330E-02 | -1.973240618E-03 |
| 2 | 1 | 0.00000 | $1.444989354 \mathrm{E}-01$ | $1.217984946 \mathrm{E}-02$ | 2.341007330E-02 | -1.973240618E-03 |
| 3 | 1 | 0.00000 | $2.169989354 \mathrm{E}-01$ | $1.829089161 \mathrm{E}-02$ | $1.931331047 \mathrm{E}-01$ | -1.627923509E-02 |
| 4 | 1 | 0.00000 | $2.169989354 \mathrm{E}-01$ | $1.829089161 \mathrm{E}-02$ | $1.931331047 \mathrm{E}-01$ | -1.627923509E-02 |
| 5 | 1 | 0.00000 | $2.894989354 \mathrm{E}-01$ | 2.440193375E-02 | $3.628561362 \mathrm{E}-01$ | -3.058522956E-02 |
| 6 | 1 | 0.00000 | $2.894989354 \mathrm{E}-01$ | $2.440193375 \mathrm{E}-02$ | $3.628561362 \mathrm{E}-01$ | -3.058522956E-02 |
| 7 | 1 | 0.00000 | $3.619989354 \mathrm{E}-01$ | $3.051297588 \mathrm{E}-02$ | 5.325791676E-01 | -4.489122400E-02 |
| 8 | 1 | 0.00000 | $3.619989354 \mathrm{E}-01$ | $3.051297588 \mathrm{E}-02$ | 5.325791676E-01 | -4.489122400E-02 |
| 9 | 1 | 0.00000 | $4.344989354 \mathrm{E}-01$ | $3.662401801 \mathrm{E}-02$ | 7.023021991E-01 | -5.919721844E-02 |
| 10 | 1 | 0.00000 | $4.344989354 \mathrm{E}-01$ | $3.662401801 \mathrm{E}-02$ | 7.023021991E-01 | -5.919721844E-02 |
| 1 | 2 | 0.00000 | 1.308501247E-01 | 8.514045444E-03 | -9.960917299E-03 | $3.153577120 \mathrm{E}-04$ |
| 2 | 2 | 0.00000 | 1.308501247E-01 | $8.514045444 \mathrm{E}-03$ | -9.960917299E-03 | $3.153577120 \mathrm{E}-04$ |
| 3 | 2 | 0.00000 | $1.041820623 \mathrm{E}-01$ | -1.200951763E-02 | -8.217756745E-02 | $2.601701095 \mathrm{E}-03$ |
| 4 | 2 | 0.00000 | $1.041820623 \mathrm{E}-01$ | -1.200951763E-02 | -8.217756745E-02 | $2.601701095 \mathrm{E}-03$ |
| 5 | 2 | 0.00000 | 7.751400004E-02 | -3.253308069E-02 | -1.543942171E-01 | $4.888044424 \mathrm{E}-03$ |
| 6 | 2 | 0.00000 | 7.751400004E-02 | -3.253308069E-02 | -1.543942171E-01 | $4.888044424 \mathrm{E}-03$ |
| 7 | 2 | 0.00000 | 5.084593802E-02 | -5.305664374E-02 | -2.266108663E-01 | 7.174387701E-03 |
| 8 | 2 | 0.00000 | $5.084593802 \mathrm{E}-02$ | -5.305664374E-02 | -2.266108663E-01 | $7.174387701 \mathrm{E}-03$ |
| 9 | 2 | 0.00000 | $2.417787621 \mathrm{E}-02$ | -7.358020679E-02 | -2.988275150E-01 | $9.460730924 \mathrm{E}-03$ |
| 10 | 2 | 0.00000 | 417787621 | 802067 | $-2.988275150 \mathrm{E}-01$ | $9.460730924 \mathrm{E}-03$ |

$0.00000 \quad 1.444989354 \mathrm{E}-01 \quad 1.217984946 \mathrm{E}-02 \quad 2.341007330 \mathrm{E}-02 \quad-1.973240618 \mathrm{E}-03$ $\begin{array}{llllll}0.00000 & 2.169989354 \mathrm{E}-01 & 1.829089161 \mathrm{E}-02 & 1.931331047 \mathrm{E}-01 & -1.627923509 \mathrm{E}-02 \\ 0.00000 & 2.169989354 \mathrm{E}-01 & 1.829089161 \mathrm{E}-02 & 1.931331047 \mathrm{E}-01 & -1.627923509 \mathrm{E}-02\end{array}$ $\begin{array}{llllll}0.00000 & 2.169989354 \mathrm{E}-01 & 1.829089161 \mathrm{E}-02 & 1.931331047 \mathrm{E}-01 & -1.627923509 \mathrm{E}-02 \\ 0.00000 & 2.894989354 \mathrm{E}-01 & 2.440193375 \mathrm{E}-02 & 3.628561362 \mathrm{E}-01 & -3.058522956 \mathrm{E}-02\end{array}$ $\begin{array}{llllll}0.00000 & 2.894989355 E-01 & 2.44019337 E E-02 & 3.628561362 \mathrm{E}-01 & -3.058522956 \mathrm{E}-02 \\ 0.00000 & 2.894989354 \mathrm{E}-01 & 2.440193375 \mathrm{E}-02 & 3.628561362 \mathrm{E}-01 & -3.058522956 \mathrm{E}-02\end{array}$ $\begin{array}{llllll}0.00000 & 2.894989354 \mathrm{E}-01 & 2.440193375 \mathrm{E}-02 & 3.628561362 \mathrm{E}-01 & -3.058522956 \mathrm{E}-02 \\ 0.00000 & 3.619989354 \mathrm{E}-01 & 3.051297588 \mathrm{E}-02 & 5.325791676 \mathrm{E}-01 & -4.489122400 \mathrm{E}-02\end{array}$ $0.00000 \quad 3.619989354 \mathrm{E}-01 \quad 3.051297588 \mathrm{E}-02 \quad 5.325791676 \mathrm{E}-01 \quad-4.489122400 \mathrm{E}-02$ $0.00000 \quad 4.344989354 \mathrm{E}-01 \quad 3.662401801 \mathrm{E}-02 \quad 7.023021991 \mathrm{E}-01-5.919721844 \mathrm{E}-02$ $0.00000 \quad 4.344989354 \mathrm{E}-01 \quad 3.662401801 \mathrm{E}-02 \quad 7.023021991 \mathrm{E}-01-5.919721844 \mathrm{E}-02$ $\begin{array}{lllll}0.00000 & 1.308501247 \mathrm{E}-01 & 8.514045444 \mathrm{E}-03 & -9.960917299 \mathrm{E}-03 & 3.153577120 \mathrm{E}-04 \\ 0.00000 & 1.308501247 \mathrm{E}-01 & 8.514045444 \mathrm{E}-03 & -9.960917299 \mathrm{E}-03 & 3.153577120 \mathrm{E}-04\end{array}$ $\begin{array}{llllll}0.00000 & 1.041820623 E-01 & -1.200951763 \mathrm{E}-02 & -8.217756745 \mathrm{E}-02 & 2.601701095 \mathrm{E}-03\end{array}$ $0.00000 \quad 1.041820623 \mathrm{E}-01-1.200951763 \mathrm{E}-02 \quad-8.217756745 \mathrm{E}-02 \quad 2.601701095 \mathrm{E}-03$ $0.00000 \quad 7.751400004 \mathrm{E}-02-3.253308069 \mathrm{E}-02-1.543942171 \mathrm{E}-01 \quad 4.888044424 \mathrm{E}-03$ $\begin{array}{lllll}0.00000 & 5.084593802 \mathrm{E}-02 & -5.305664374 \mathrm{E}-02 & -2.266108663 \mathrm{E}-01 & 7.174387701 \mathrm{E}-03 \\ 0.00000 & 5.084593802 \mathrm{E}-02 & -5.305664374 \mathrm{E}-02 & -2.266108663 \mathrm{E}-01 & 7.174387701 \mathrm{E}-03\end{array}$
$0.00000 \quad 2.417787621 \mathrm{E}-02 \quad-7.358020679 \mathrm{E}-02-2.988275150 \mathrm{E}-01 \quad 9.460730924 \mathrm{E}-03$

## Problem in the inverse boost

- Impact on realistic simulation study assessed by Dario
- Tune scans comparison with 2017 ATS optics show no dramatic change, but slightly worse DA

Old version
ATS Optics; $\beta^{*}=40 \mathrm{~cm} ; \mathrm{Q}^{\prime}=15 ; \mathrm{I}_{\mathrm{MO}}=500 \mathrm{~A}$; $\varepsilon=2.5 \mu \mathrm{~m} ; \mathrm{I}=1.2510^{11} \mathrm{e} ; \mathrm{X}=150 \mu \mathrm{rad} ;$ Min DA.

Corrected version
ATS Optics; $\beta^{*}=40 \mathrm{~cm} ; \mathrm{Q}^{\prime}=15 ; \mathrm{I}_{\mathrm{MO}}=500 \mathrm{~A}$;
$\varepsilon=2.5 \mu \mathrm{~m} ; \mathrm{I}=1.2510^{11} \mathrm{e} ; X=150 \mu \mathrm{rad} ; \operatorname{Min} \mathrm{DA}$.


