

Associated quarkonium production with LHCb

Jean-Philippe Lansberg

Mini-workshop on charmonium production at LHCb,

June 16, 2017, CERN

Part I

New observables in quarkonium production

New observables: what for ?

Observables	Experiments	CSM	CEM	NRQCD	Interest
$J/\psi+J/\psi$	LHCb, CMS, ATLAS, D0 (+NA3)	NLO, NNLO*	LO ?	LO	Prod. Mechanism (CS dominant) + DPS
$J/\psi+D$	LHCb	LO	LO ?	LO	Prod. Mechanism (c to J/psi fragmentation) + DPS
$J/\psi+\Upsilon$	D0	(N)LO	LO ?	LO	Prod. Mechanism (CO dominant) + DPS
$J/\psi+\text{hadron}$	STAR	LO	--	LO	B feed-down; Singlet vs Octet radiation
$J/\psi+Z$	ATLAS	NLO	NLO	Partial NLO	Prod. Mechanism + DPS
$J/\psi+W$	ATLAS	LO	LO ?	Partial NLO	Prod. Mechanism (CO dominant) + DPS
J/ψ vs mult.	ALICE, CMS (+UA1)	--	--	--	
$J/\psi+b$	-- (LHCb, D0, CMS ?)	--	--	LO	Prod. Mechanism (CO dominant) + DPS
$\Upsilon+D$	LHCb	LO	LO ?	LO	DPS
$\Upsilon+\gamma$	--	NLO, NNLO*	LO ?	LO	Prod. Mechanism (CO LDME mix) + gluon TMD/PDF
Υ vs mult.	CMS	--	--	--	
$\Upsilon+Z$	--	NLO	LO ?	LO	Prod. Mechanism + DPS
$\Upsilon+\Upsilon$	CMS	NLO ?	LO ?	LO ?	Prod. Mechanism (CS dominant ?) + DPS

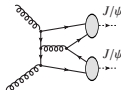
Part II

Quarkonium-pair production

On the importance of α_s^5 contributions to $J/\psi + J/\psi$ & $J/\psi + \eta_c$

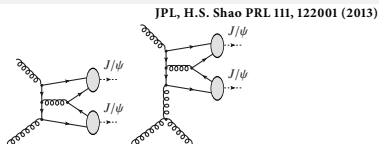
JPL, H.S. Shao PRL 111, 122001 (2013)

- LO to $J/\psi + J/\psi$ at α_s^4



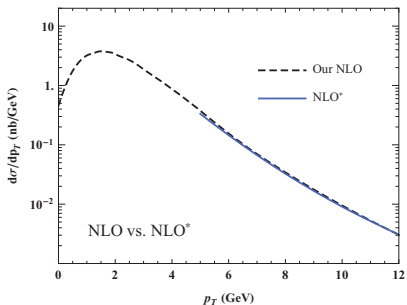
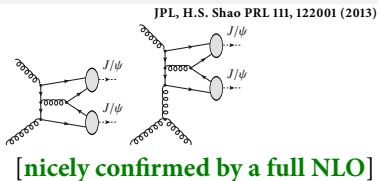
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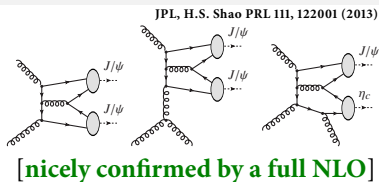
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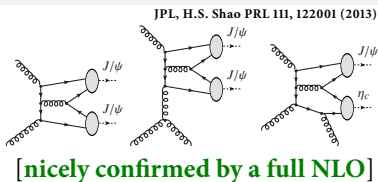
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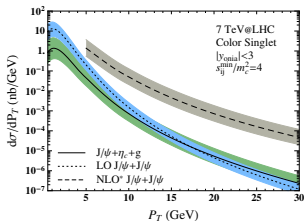
L.P. Sun *et al.* arXiv:1404.4042 [hep-ph]
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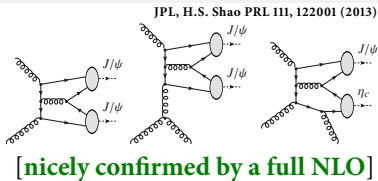


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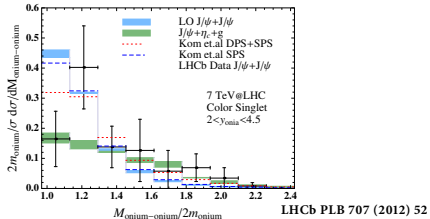
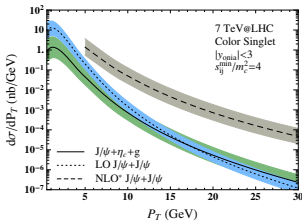


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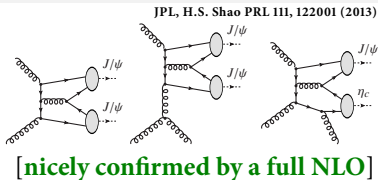
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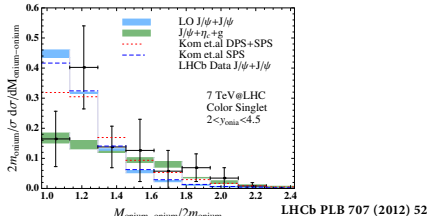
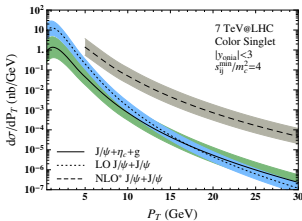
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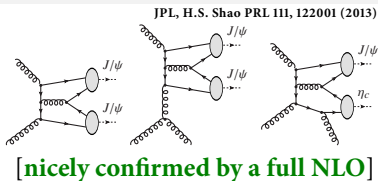


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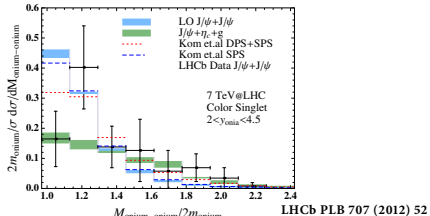
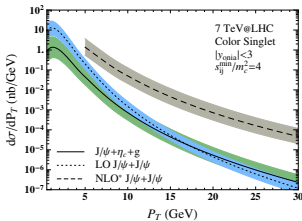
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Only CSM SPS at low P_T ?

- $J/\psi + \eta_c$: look for η_c in the J/ψ sample? Avoid trigger issues?

On the importance of QCD corrections : P_T enhanced topologies

JPL, H.-S. Shao PRL 111, 122001 (2013); PLB 751 (2015) 479

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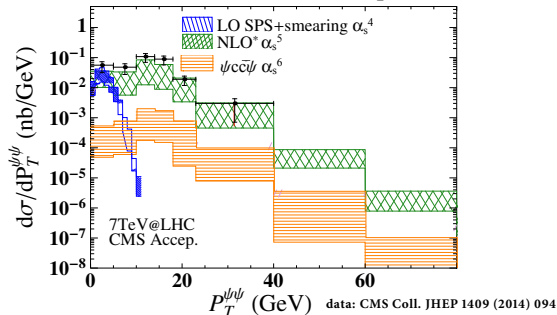
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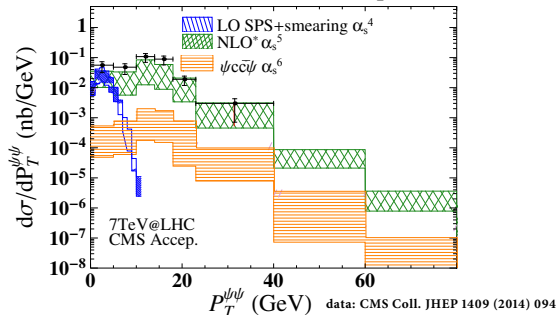
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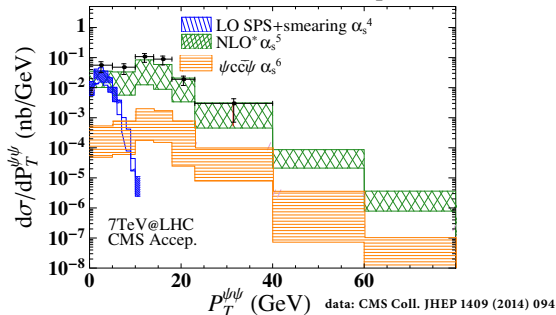


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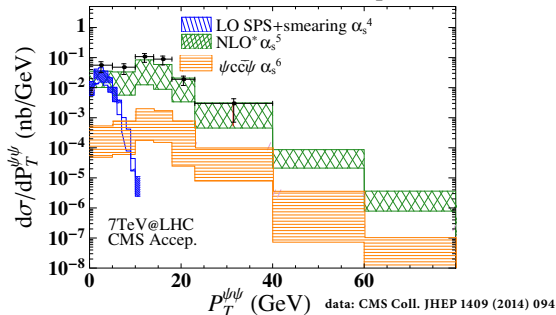


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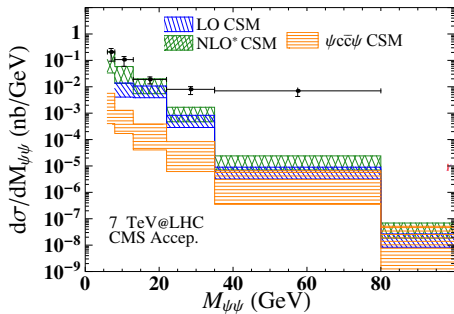
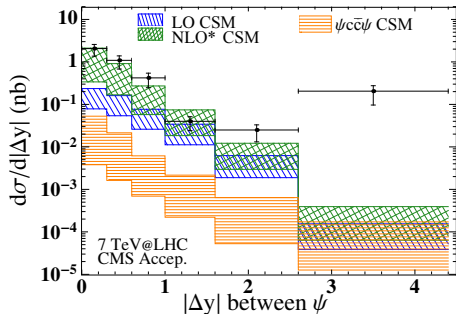
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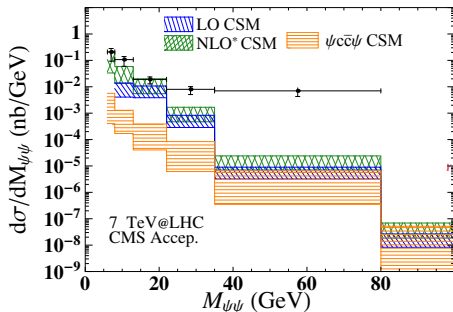
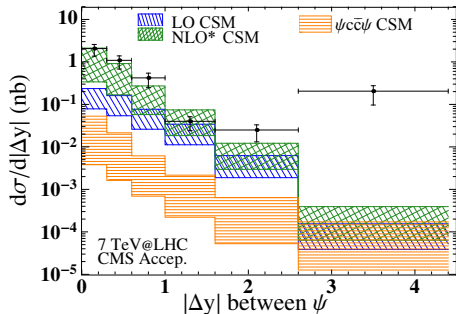


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- Slight offset up to $P_T^{\psi\psi} \simeq 20$ GeV [about a factor 2, but well within error bars]
- We do not expect NNLO (α_s^6) contributions to matter where one currently has data [the orange histogram shows one class of leading $P_T \alpha_s^6$ contributions]

The so-called CMS puzzle

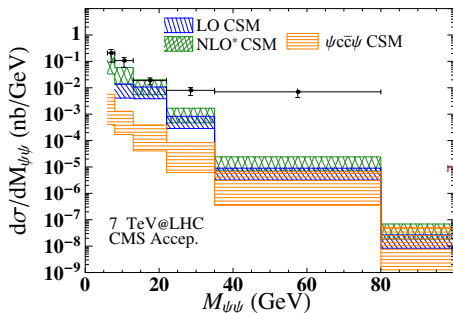
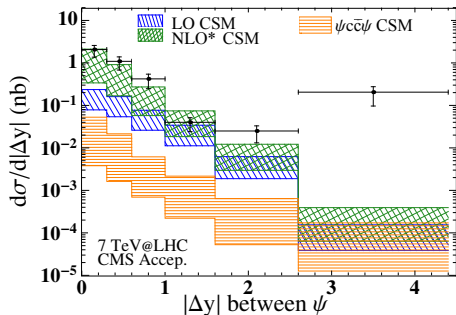


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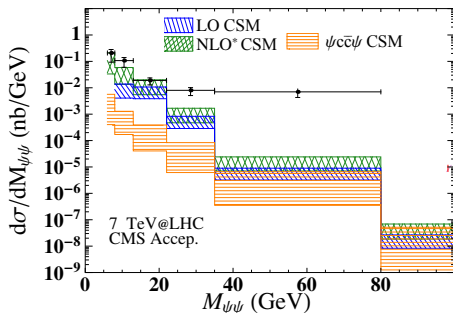
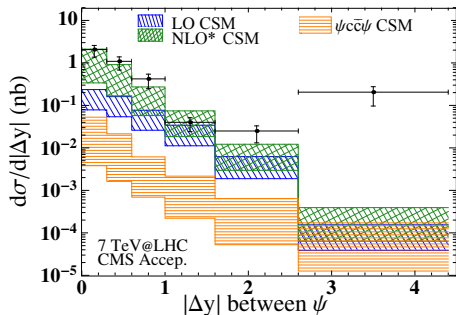
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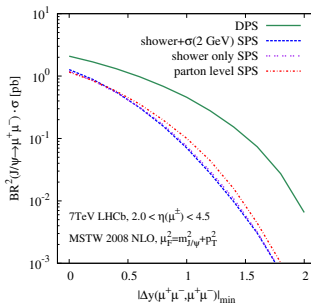
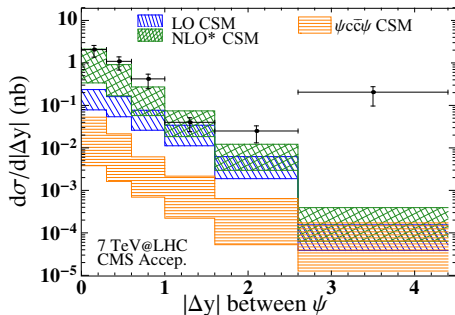
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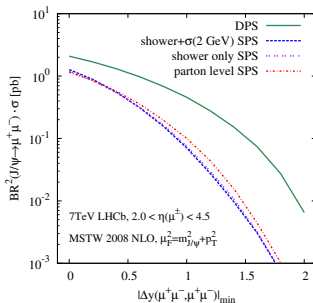
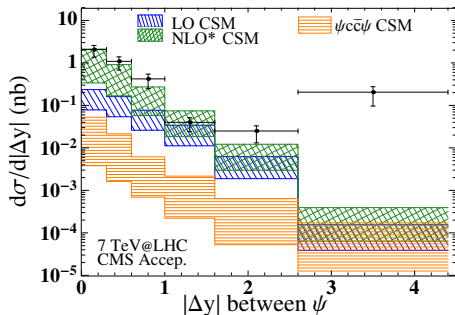
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C.H. Kom, A. Kulesza, W.J. Stirling PRL 107 (2011) 082002

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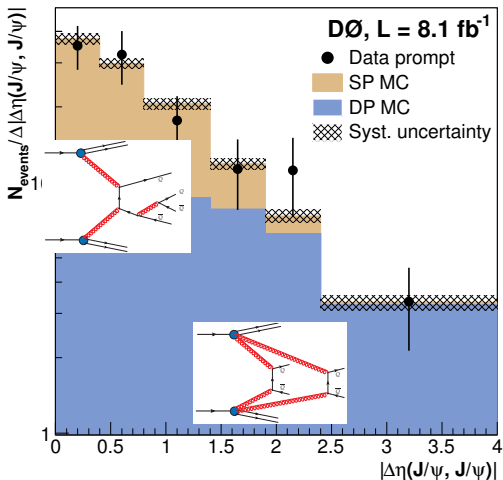


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- He & Kniehl found at LO that CO \gg CS at large Δy ; yet still in disagreement with the data; NLO needed!

Z. He, B. Kniehl PRL 115, 022002 (2015)

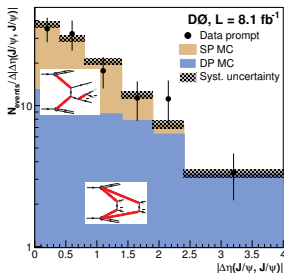
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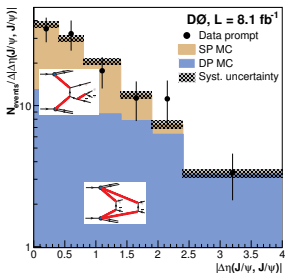


D0 Coll. PRD 90 (2014) 111101

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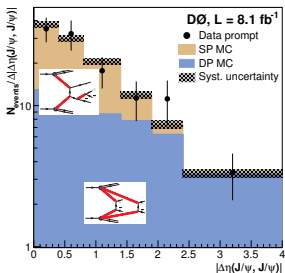


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- $\sigma_{\text{CSM}}^{\text{SPS}} = 170^{+340}_{-110} \text{ fb}$ and $\sigma_{\text{D0}}^{\text{SPS}} = 59 \pm 23 \text{ fb}$ are still compatible at 1- σ level

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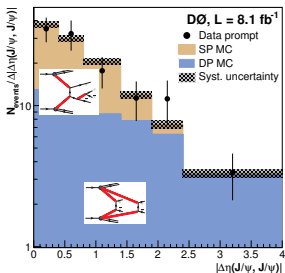


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- A question arises: using $\sigma^{\text{DPS}} = \frac{1}{2} \frac{\sigma_{\psi} \sigma_{\psi}}{\sigma_{\text{eff}}}$ and $\sigma_{\text{eff}} = 4.8 \pm 2.5 \text{ mb}$, can one account for the large Δy CMS data?

On the importance of double parton scatterings at large Δy II

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- Let us investigate the **consistency**
between D0 and CMS data
- For that we assume: $\sigma^{\text{DPS}} = \frac{1}{2} \frac{\sigma_\psi \sigma_\psi}{\sigma_{\text{eff}}}$
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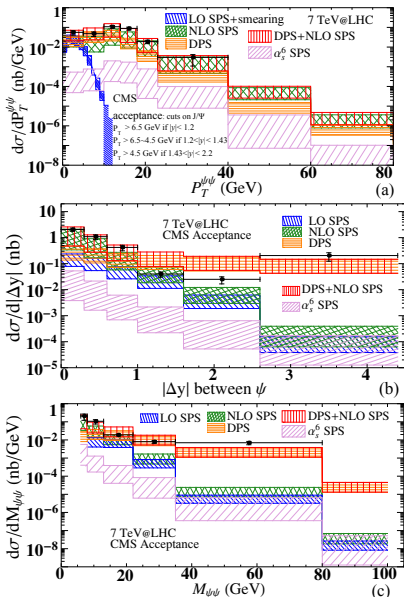
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- σ_{ψ} are fit from data with a Crystal Ball function parametrising $|\mathcal{A}_{gg \rightarrow \psi X}|^2$

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C.H. Kom, A. Kulesza, W.J. Stirling PRL 107 (2011) 082002

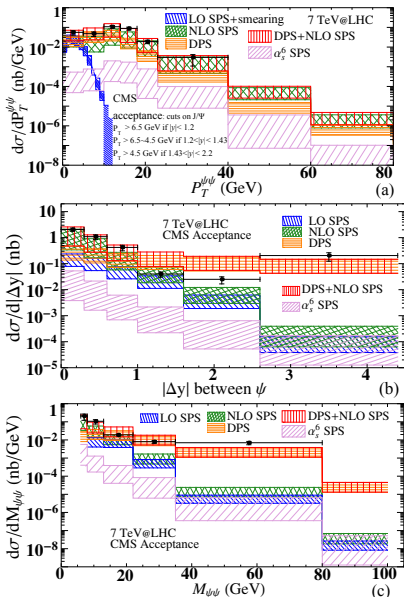


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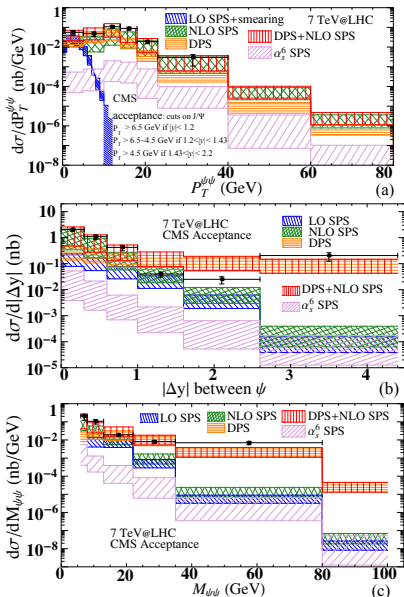
C.H. Kom, A. Kulesza, W.J. Stirling PRL 107 (2011) 082002

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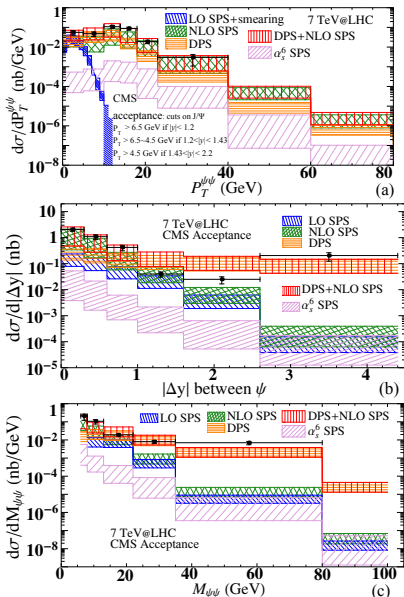
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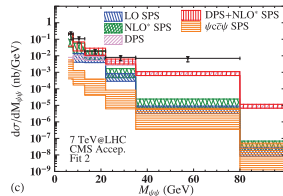
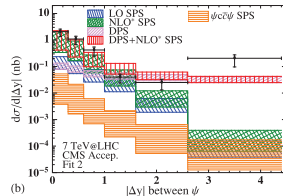
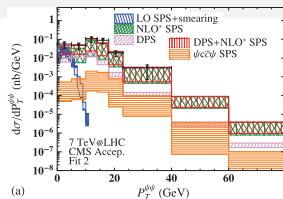


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 - Fit done prior the ATLAS analysis** \rightarrow **good agreement !**

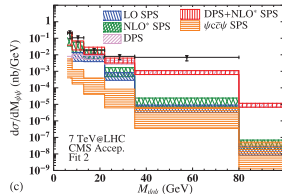
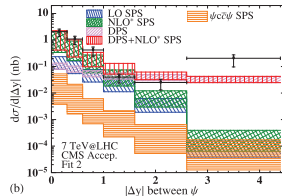
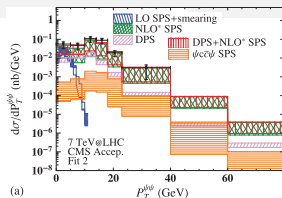


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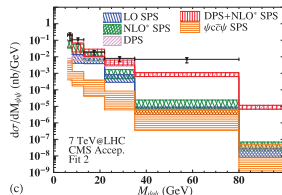
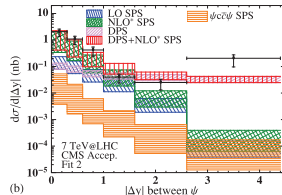
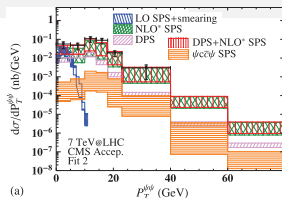
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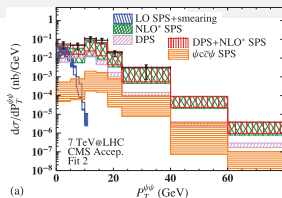


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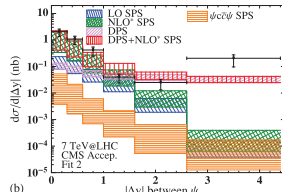
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Result of the fit of the DPS yield via σ_{eff} on the 18 CMS values.

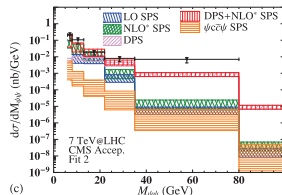
	σ_{eff} [mb]	$\chi^2_{\text{d.o.f.}}$	d.o.f.
σ_ψ Fit 1 [25]	11 ± 2.9	1.9	16
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σ_ψ Fit 3	5.3 ± 1.4	1.9	16
Only LO SPS	N/A	7.6	17
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(a)



(b)



(c)

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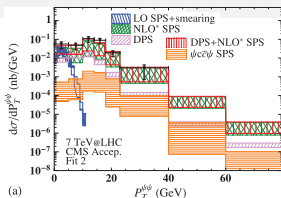
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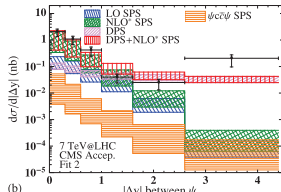
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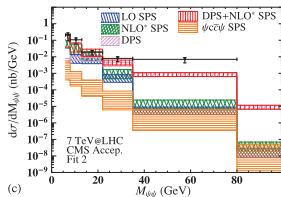
- σ^{DPS} computed for D0 & LHCb; agreement checked:
 $\chi^2_{\text{d.o.f.}}$: 0.5-1.2 (LHCb) & 0.06-0.5 (D0)



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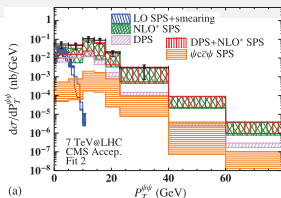
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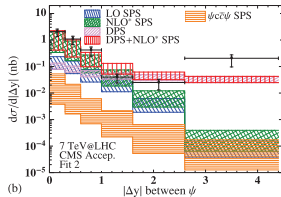
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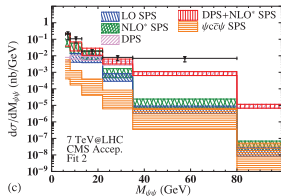
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- Best agreement with Fit 3 confirming the consistency:
 $\sigma_{\text{eff}} = 4.8 \pm 2.5 \text{ mb}$ vs $\sigma_{\text{eff}} = 5.3 \pm 1.4 \text{ mb}$



(a)

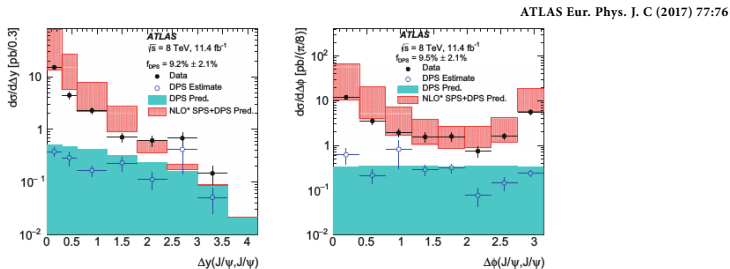


(b)



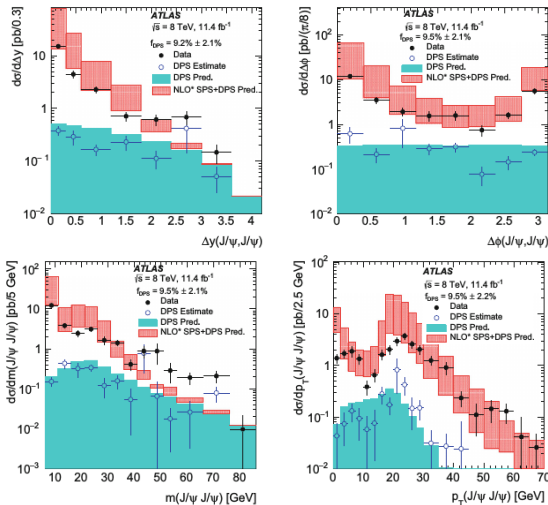
(c)

Comparison with ATLAS data



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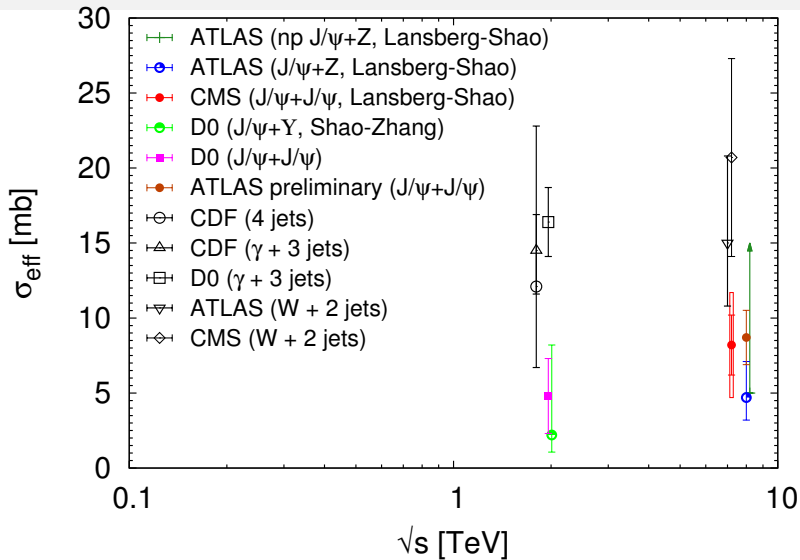
ATLAS Eur. Phys. J. C (2017) 77:76



ATLAS extraction: $\sigma_{\text{eff}} = 6.3 \pm 1.6(\text{stat}) \pm 1.0(\text{syst}) \pm 0.1(\text{BF}) \pm 0.1(\text{lumi}) \text{ mb}$

Harvesting new quarkonium data

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4 quarkonium extractions using theory ingredients !

Comparison with the new LHCb data at 13 TeV

LHCb JHEP06(2017)047

$\sigma(\psi\psi)\text{nb}$	no P_T cut	$P_T > 1 \text{ GeV}$	$P_T > 3 \text{ GeV}$
NLO* CS	$15.4 \pm 2.2^{+51}_{-12}$	$14.8 \pm 1.7^{+53}_{-12}$	$6.8 \pm 0.6^{+22}_{-5}$
NLO CS	$11.9^{+4.6}_{-3.2}$	—	—
DPS [$\sigma_{\text{eff}} = 14.5 \pm 1.7^{+1.7}_{-2.3} \text{ mb}$]	$8.1 \pm 0.9^{+1.6}_{-1.3}$	$7.5 \pm 0.8^{+1.5}_{-1.2}$	$4.9 \pm 0.5^{+1.0}_{-0.8}$
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- **REMINDER**: it is not an option to "switch off"/ignore the NLO CS contribution [parameter free]
- Yet, **room for DPS**; however tension if $\sigma_{\text{eff}} \simeq 7$ mb
- **Tension between LHCb and other di- J/ψ extractions** [rapidity effect ?]

Predictions: excited states and more

JPL, H.-S. Shao PLB 751 (2015) 479

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- Back to the first slide, $J/\psi + \eta_c$ can also tell something about DPS and about σ_{eff}

Part III

Charmonium + charm

Double charm: $J/\psi + D$

→ $J/\psi + D$ or $J/\psi + \text{lepton}$ in the yield integrated over P_T

S. J. Brodsky and JPL, PRD 81 051502 (R), 2010

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- SPS sensitive to intrinsic charm at RHIC

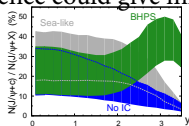
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- Rate significant & y -dependence could give info on $c(x)$

S. J. Brodsky and JPL, PRD 81 051502 (R), 2010



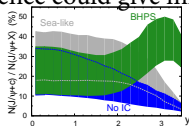
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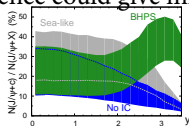
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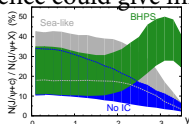
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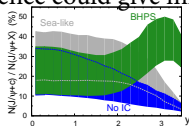
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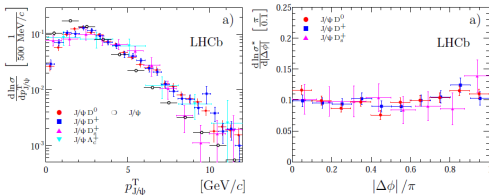


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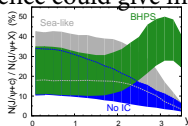
LHCb, JHEP 1206 (2012) 141

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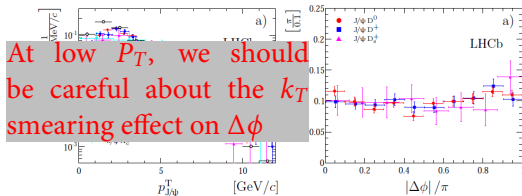


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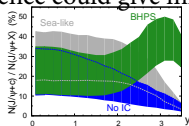
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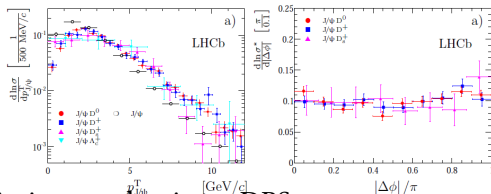


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LHCb, JHEP 1206 (2012) 141

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- $D + \chi_c$ necessary to complete the picture [confirm DPS dominance or?]

Part IV

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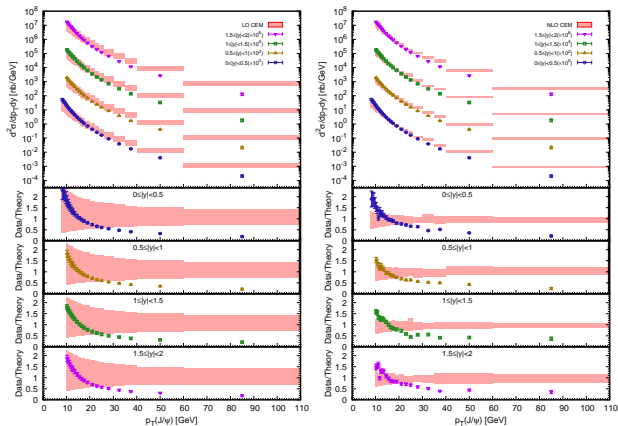
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- As outlooks, **TMD-oriented studies using associated quarkonium production**

should now become possible for di- J/ψ , $\Upsilon + \gamma$, later for $Q + \ell^+ \ell^-$
W. den Dunnen, JPL, C. Pisano, M. Schlegel, PRL 112, 212001 (2014); JPL, C. Pisano, M. Schlegel, NPB 920 (2017) 192; JPL,

Part V

Back-up slides

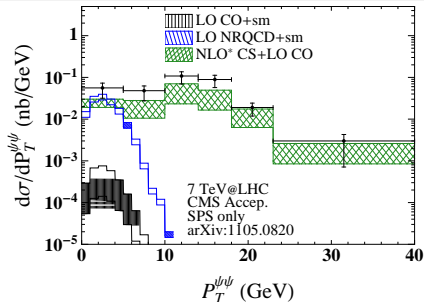
CEM results for single J/ψ



Comparison between the ATLAS data (EPJC 76 (2016) 283) and the CEM results for $d\sigma/dy/dp_T$ of J/ψ + a recoiling parton at (left) LO and (right) NLO at $\sqrt{s} = 8$ TeV.
 [The theoretical uncertainty band is from the scale variation.]

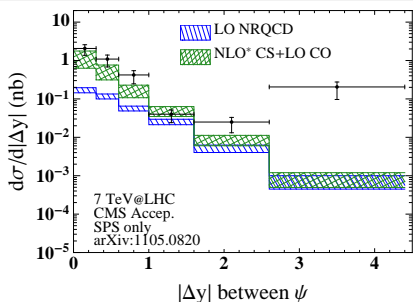
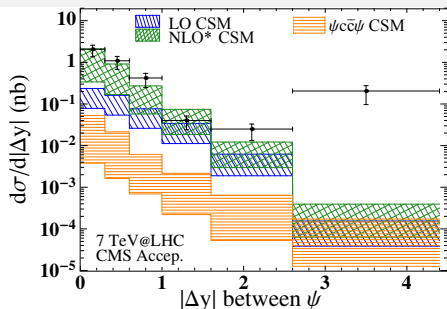
On the (non-)importance of CO channels for di- J/ψ

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Single J/ψ LDME fit: M. Butenschoen, B. Kniehl arXiv:1105.0820, PRD 84 (2011) 0515

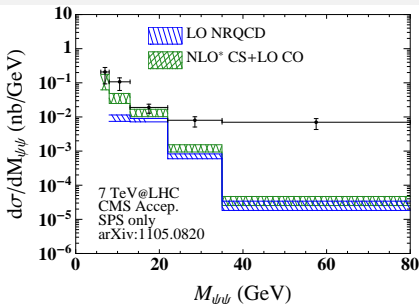
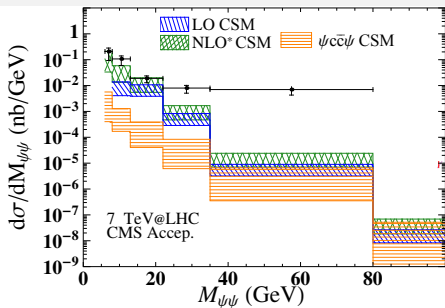
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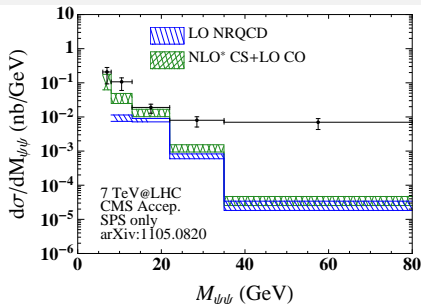
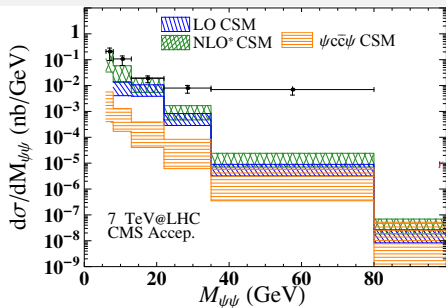
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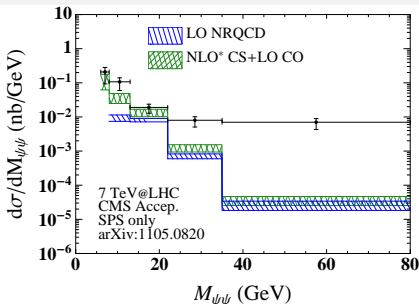
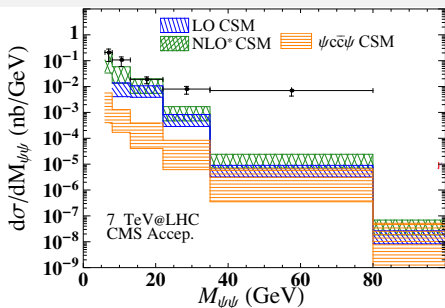


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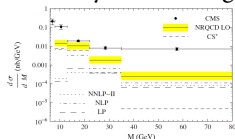
PRL 110 (2013) 042002; JHEP 1505 (2015) 103; PRL 113 (2014) 022001

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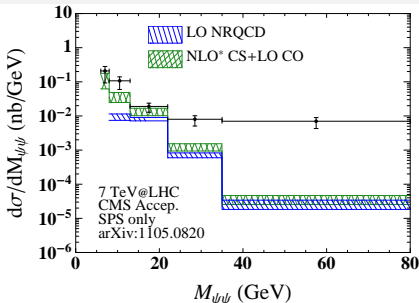
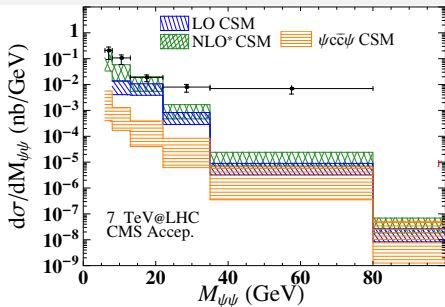


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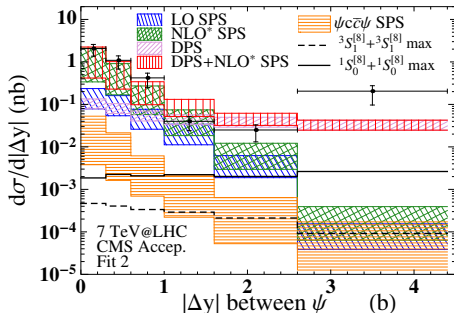
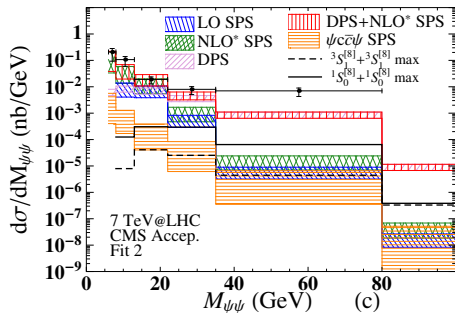
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- In terms of $\chi^2_{\text{d.o.f}}$:

	LO CO+ NLO* CSM w/o DPS	NLO* CSM w DPS
$\chi^2_{\text{d.o.f}}$	3.0	1.9

Another way to see this with 2 CO channels

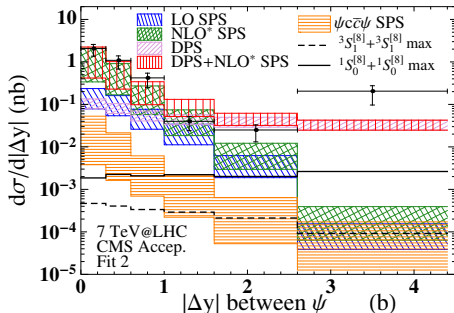
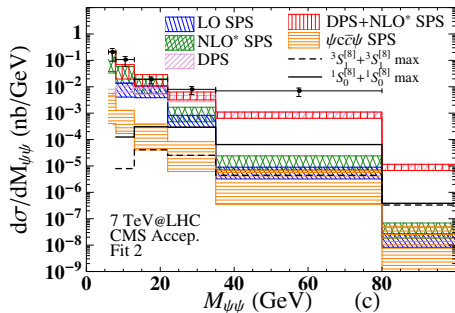
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JPL, H.-S. Shao PLB 751 (2015) 479

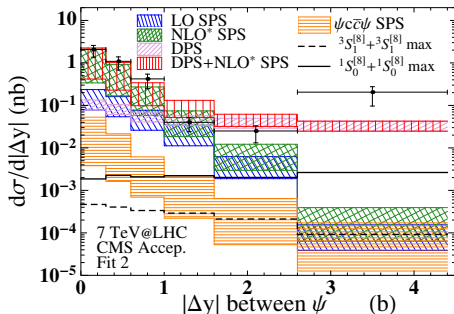
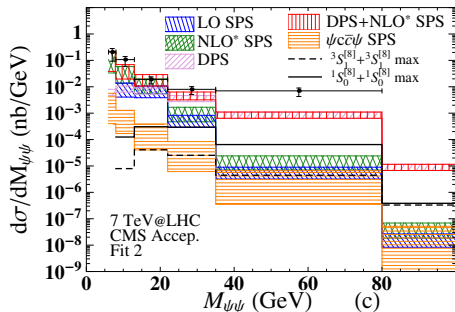
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H. Han *et al.* PRL 114 (2015) 092005

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H. Han *et al.* PRL 114 (2015) 092005

- Ignoring all previous constraints and fitting (one channel at a time) the LDME on the CMS data one gets unrealistically large values:

$$\langle \mathcal{O}^{J/\psi}(^3S_1^{[8]}) \rangle = 0.42 \pm 0.12 \text{ GeV}^3 \quad \& \quad \langle \mathcal{O}^{J/\psi}(^1S_0^{[8]}) \rangle = 0.91 \pm 0.22 \text{ GeV}^3 \quad !!!$$