

# Precision Determination of $W$ mass and Parton Showers

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## Reminder: How parton showers work

- parton showers are approximations, based on
  - leading colour, leading logarithmic accuracy, spin-average
- parametric accuracy by comparing Sudakov form factors:

$$\Delta = \exp \left\{ - \int \frac{dk_{\perp}^2}{k_{\perp}^2} \left[ A \log \frac{k_{\perp}^2}{Q^2} + B \right] \right\},$$

where  $A$  and  $B$  can be expanded in  $\alpha_S(k_{\perp}^2)$

- $Q_T$  resummation includes  $A_{1,2,3}$  and  $B_{1,2}$   
(transverse momentum of Higgs boson etc.)
- showers usually include terms  $A_{1,2}$  and  $B_1$   
 $A$  = cusp terms (“soft emissions”),  $B \sim$  anomalous dimensions  $\gamma$

# Matching at NLO and NNLO

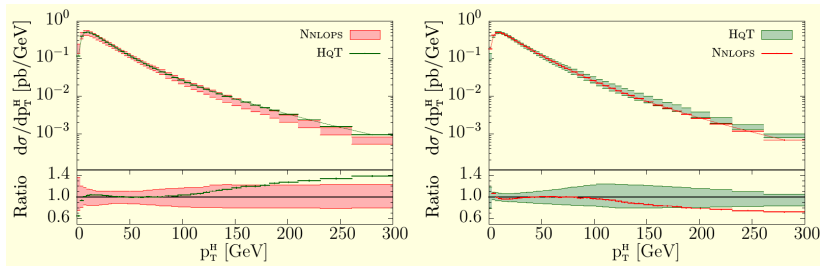
- avoid double-counting of emissions
- two schemes at NLO: MC@NLO and POWHEG
  - mismatches of  $K$  factors in transition to hard jet region
  - MC@NLO:  $\rightarrow$  visible structures, especially in  $gg \rightarrow H$
  - POWHEG:  $\rightarrow$  high tails, cured by  $h$  dampening factor
  - well-established and well-known methods

(no need to discuss them any further)

- two schemes at NNLO: MINLO & UN<sup>2</sup>LOPS (singlets  $S$  only)
  - different basic ideas
  - MINLO:  $S + j$  at NLO with  $p_T^{(S)} \rightarrow 0$  and capture divergences by reweighting internal line with analytic Sudakov, NNLO accuracy ensured by reweighting with full NNLO calculation for  $S$  production
  - UN<sup>2</sup>LOPS identifies and subtracts and adds parton shower terms at FO from  $S + j$  contributions, maintaining unitarity
  - available for two simple processes only: DY and  $gg \rightarrow H$

# NNLOs for $H$ production: MINLO

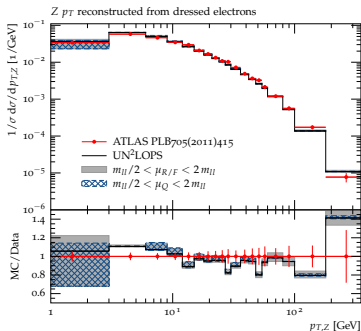
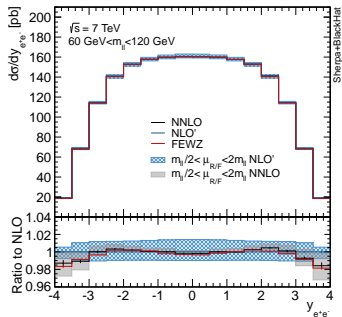
K. Hamilton, P. Nason, E. Re & G. Zanderighi, JHEP 1310



- also available for  $Z/W/VH$  production

# NNLOs for $Z$ production: UN<sup>2</sup>LOs

S. Hoche, Y. Li, & S. Prestel, Phys.Rev.D90 & D91



- also available for  $H$  production

# A new shower implementation in DIRE

(S.Höche & S.Prestel, Eur.Phys.J. C75 (2015) 461)

- evolution and splitting parameter ( $((ij) + k \rightarrow i + j + k)$ ):

$$\kappa_{j,ik}^2 = \frac{4(p_i p_j)(p_j p_k)}{Q^4} \quad \text{and} \quad z_j = \frac{2(p_j p_k)}{Q^2}.$$

- splitting functions including IR regularisation

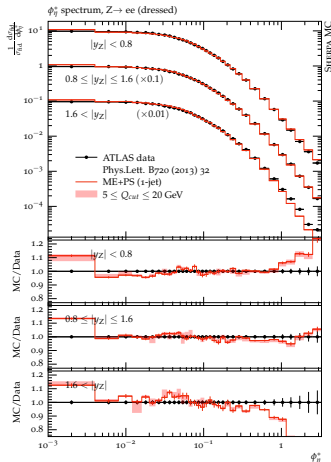
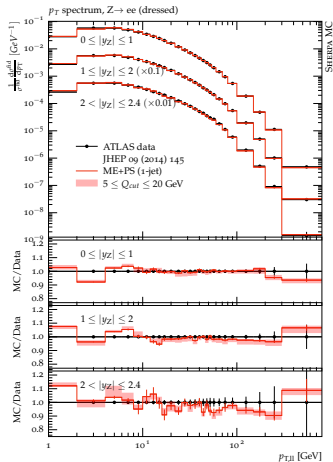
(a la Curci, Furmanski & Petronzio, Nucl.Phys. B175 (1980) 27-92)

$$\begin{aligned} P_{qq}^{(0)}(z, \kappa^2) &= 2C_F \left[ \frac{1-z}{(1-z)^2 + \kappa^2} - \frac{1+z}{2} \right], \\ P_{qg}^{(0)}(z, \kappa^2) &= 2C_F \left[ \frac{z}{z^2 + \kappa^2} - \frac{2-z}{2} \right], \\ P_{gg}^{s(0)}(z, \kappa^2) &= 2C_A \left[ \frac{1-z}{(1-z)^2 + \kappa^2} - 1 + \frac{z(1-z)}{2} \right], \\ P_{gq}^{(0)}(z, \kappa^2) &= T_R \left[ z^2 + (1-z)^2 \right] \end{aligned}$$

- renormalisation/factorisation scale given by  $\mu = \kappa^2 Q^2$
- combine gluon splitting from two splitting functions with different spectators  $k \rightarrow$  accounts for different colour flows

# LO results for Drell-Yan

(example of accuracy in description of standard precision observable)



# Including NLO splitting kernels

(Hoeche, FK & Prestel, 1705.00982, and Hoeche & Prestel, 1705.00742)

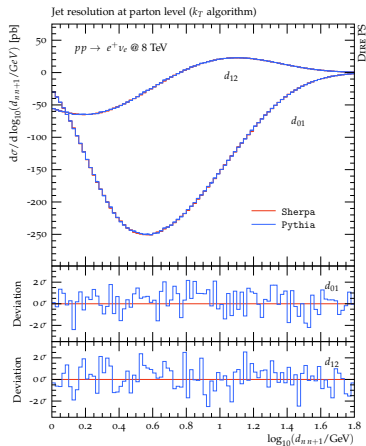
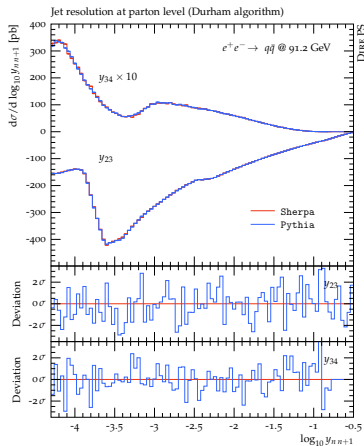
- expand splitting kernels as

$$P(z, \kappa^2) = P^{(0)}(z, \kappa^2) + \frac{\alpha_S}{2\pi} P^{(1)}(z, \kappa^2)$$

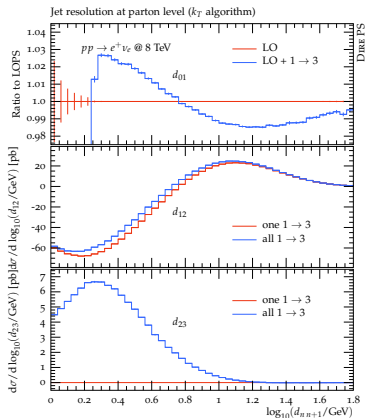
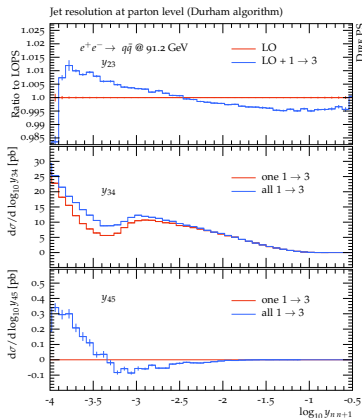
- aim: reproduce DGLAP evolution at NLO  
include all NLO splitting kernels
- three categories of terms in  $P^{(1)}$ :
  - cusp (universal soft-enhanced correction) (already included in original showers)
  - corrections to  $1 \rightarrow 2$
  - new flavour structures (e.g.  $q \rightarrow q'$ ), identified as  $1 \rightarrow 3$
- new paradigm: **two independent implementations**



# Validation of $1 \rightarrow 3$ splittings

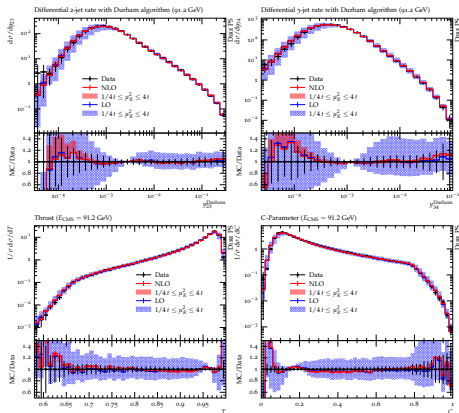


# Impact of $1 \rightarrow 3$ splittings



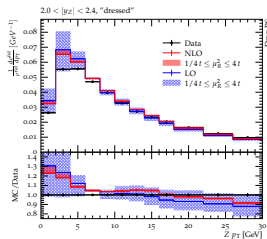
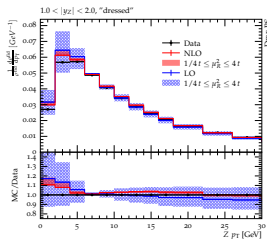
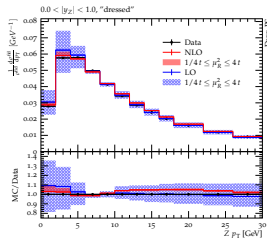
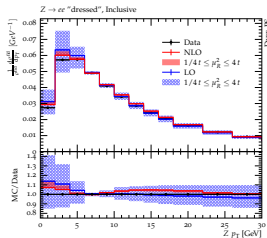
# Physical results: $e^-e^+ \rightarrow \text{hadrons}$

(Hoeche, FK & Prestel, 1705.00982)

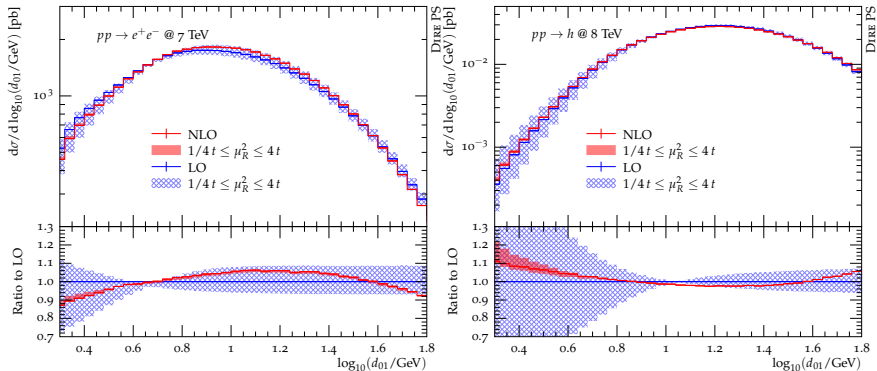


# Physical results: DY at LHC

(untuned showers vs. 7 TeV ATLAS data)



# Physical results: differential jet rates at LHC



# Summary

- implemented NLO DGLAP kernels into two independent showers  
will allow cross checks/validation of NP effects
- cross-validated implementations PYTHIA  $\longleftrightarrow$  SHERPA
- matching to NNLO/multijet merging at NLO ongoing work
- extension to include loop-corrections to 1 to 2 straightforward  
will allow to use triple-collinear splitting functions throughout
- future plans: soft-gluon emissions and non-trivial colour correlations



# LIMITATIONS

UNTIL YOU SPREAD YOUR WINGS,  
YOU'LL HAVE NO IDEA HOW FAR YOU CAN WALK.

# Points for further investigation

- treatment of heavy flavours in IS:
  - forced transitions to gluons at/around mass threshold  
(different in Z w.r.t. W production)
  - probably need to check  $y$ -dependence of flavour composition
- non-perturbative effects: intrinsic  $k_{\perp}$ :
  - initial state partons “kicked”:  $\langle k_{\perp} \rangle \approx 1 - 2 \text{ GeV}$   
(usually parametrised by Gaussian and tuned to Z- $p_{\perp}$ )
  - usually flavour-blind and  $x$ -independent  
(non-default option of  $x$ -dependent in PYTHIA)
- mind the gap: accuracy vs. precision