



Bottom quark effects on the $p_T Z$ distribution and their impact on the M_W determination

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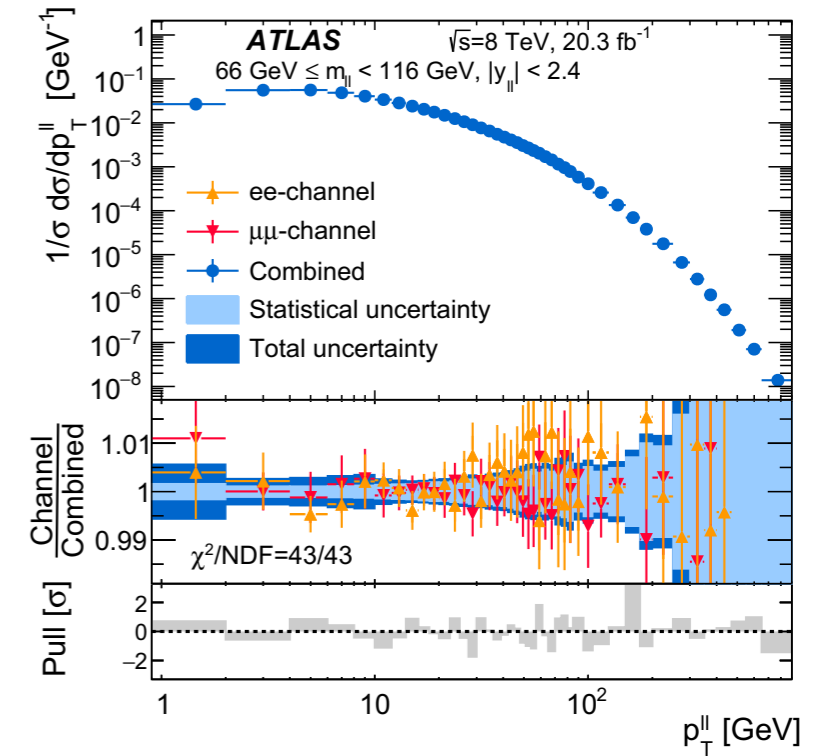
preliminary results of a work in collaboration with: E.Bagnaschi, F.Maltoni, M.Zaro

Relevance of the p_T^Z distribution for the MW determination

the very high precision p_T^Z measurement

- challenges the theoretical predictions at the sub percent level
- offers the possibility to tune the non-perturbative (NP) models describing the low- p_T part of the p_T^Z spectrum

→ these models can be then used in the simulation of CC-DY

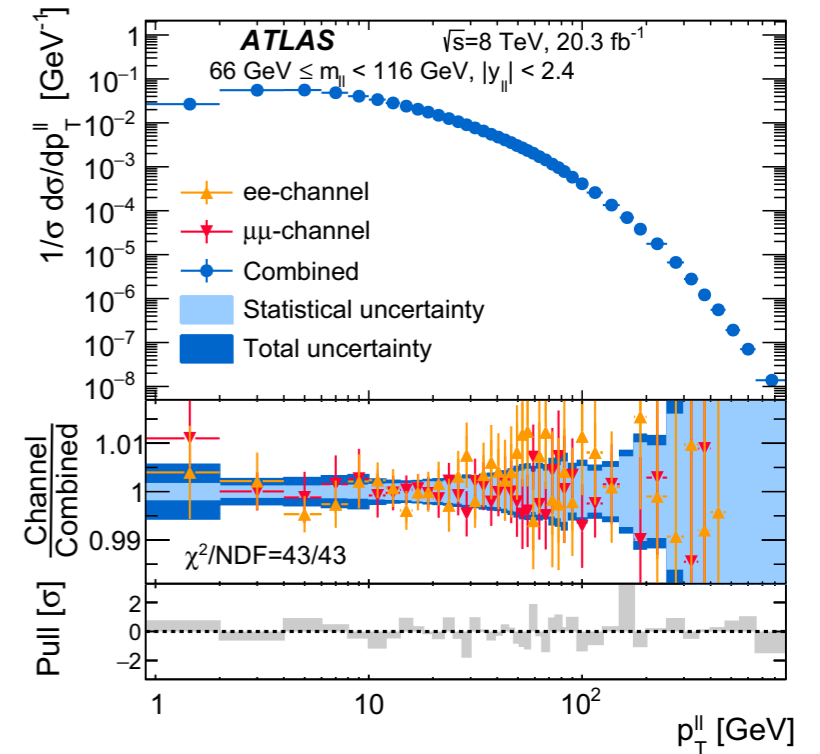


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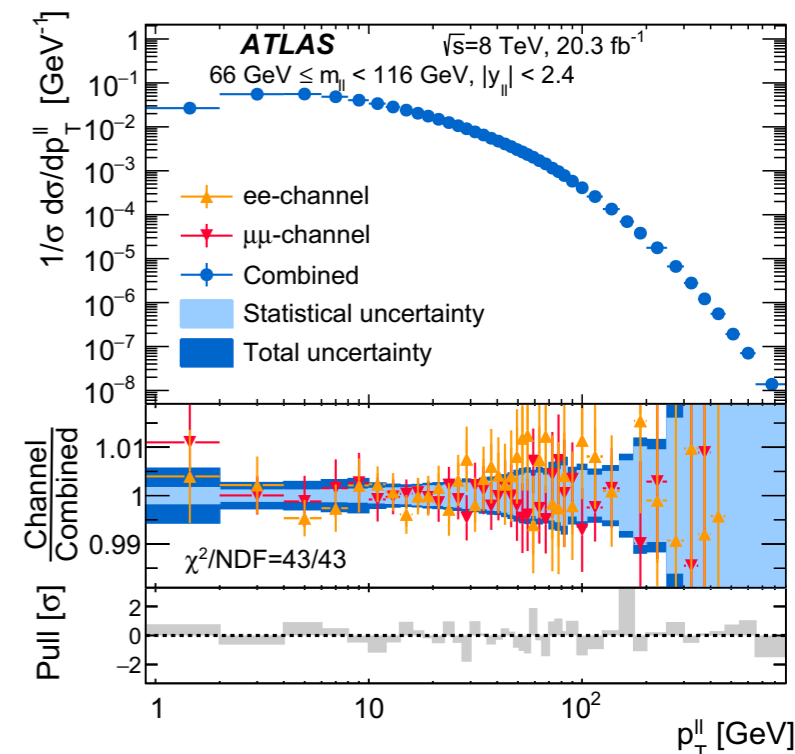
- the universality, the flavour and scale independence of the effects encoded in these NP models are a matter of debate
- the bottom quark contribution to p_T^Z , almost absent in the p_T^W case, may introduce spurious unwanted contributions in the p_T^W distribution, via the NP models
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- an improved partonic description of the bottom quark contribution to p_T^Z may
 - increase the overall precision of the theoretical predictions
 - reduce the amount of information to be encoded in the NP models
 - reduce the differences between bottom and the other quarks increasing the universality of the effects included in the NP param's

Strategy to improve the pt_Z description

we consider the processes

$$\begin{aligned} p p &\rightarrow e^+e^- + X && \text{Drell-Yan (lepton-pair production inclusive over extra radiation)} && 5\text{FS} \\ p p &\rightarrow e^+e^- b \bar{b} && \text{(associated } Z/\gamma^* \text{ production)} && 4\text{FS} \end{aligned}$$

we develop a combination which exploits the advantages of the 5FS and 4FS descriptions

we evaluate the combination using tools with NLO-QCD + QCD-PS accuracy (POWHEG and aMC@NLO) and discuss the associated QCD uncertainties

we develop a toy procedure to assess the impact on M_W of the improvement in the pt_Z description

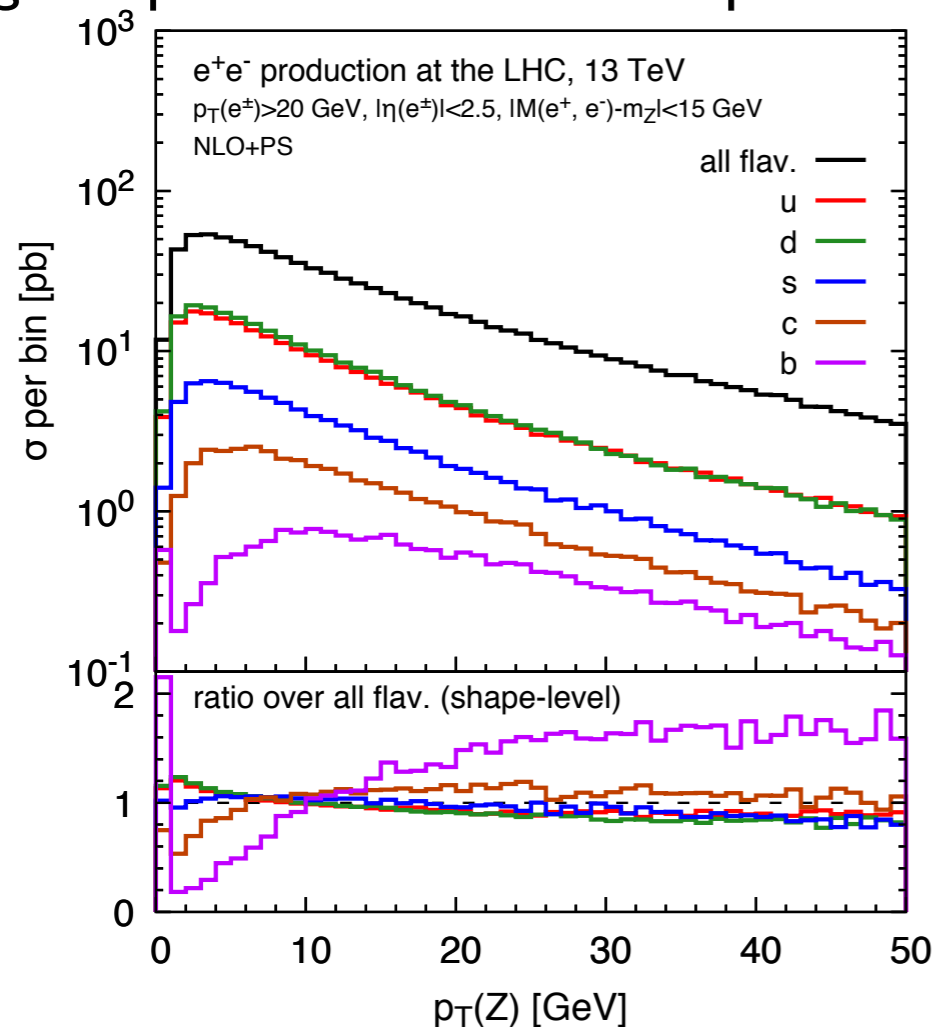
Bottom quark contributions to the $p_T Z$ distribution in the 5FS

- in the 5FS the bottom quark is treated as a massless parton
- the bottom density in the proton resums via DGLAP eqs large collinear logs
- the masslessness of the bottom may affect some kinematical distributions where the quark mass acts as a natural regulator of the transverse d.o.f.
e.g. the $p_T Z$ distribution with $p_T Z \sim \mathcal{O}(\text{mb}) \sim \mathcal{O}(5 - 20 \text{ GeV})$

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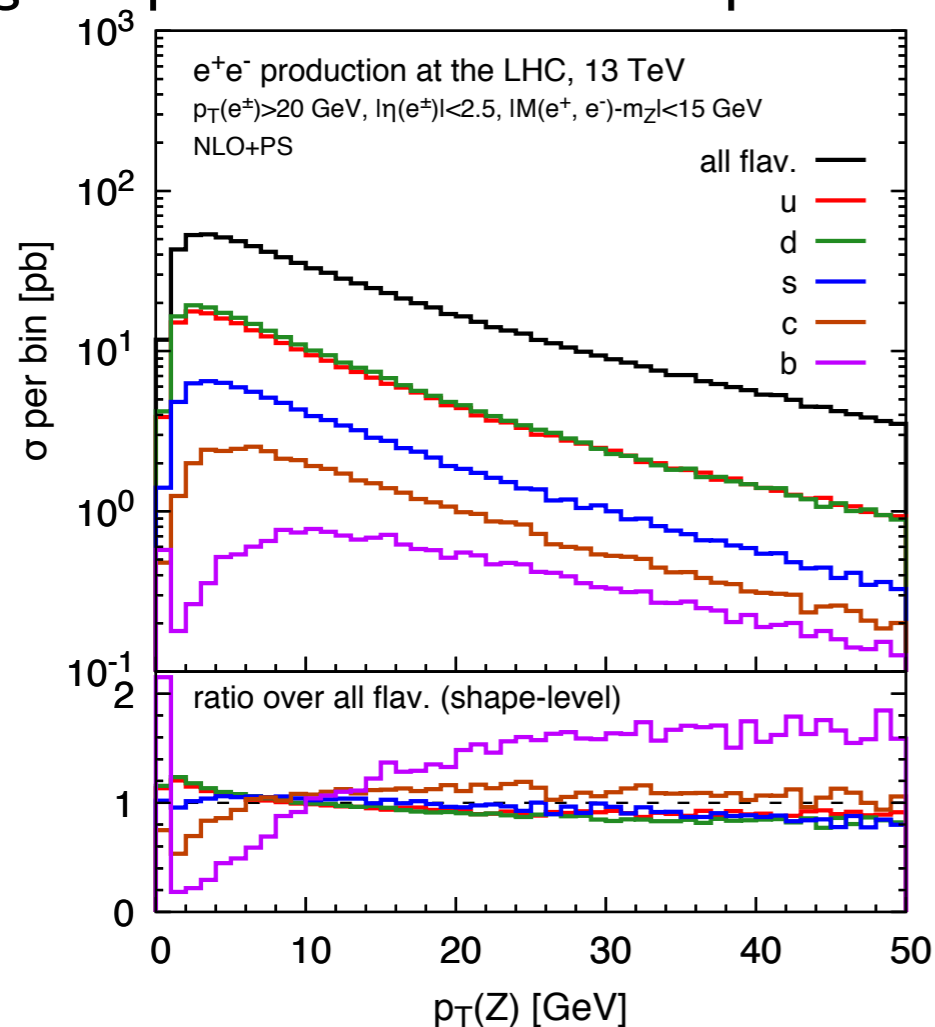


- the PDF evolution starts for the heavy quarks at $Q \sim m_q$
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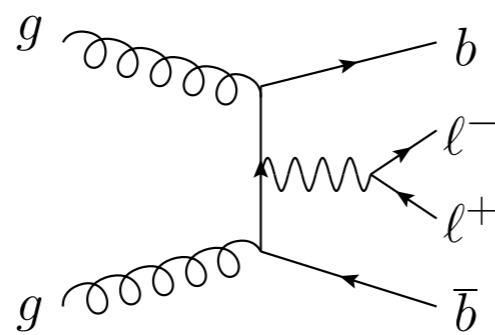
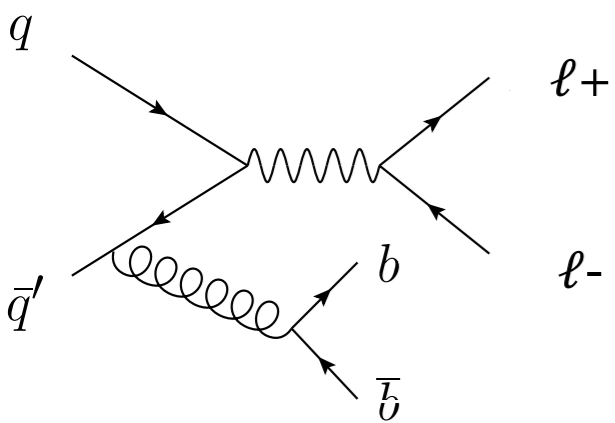
initial state quark	cross section (pb)	%
u	374.44 ± 0.62	35.0
d	391.15 ± 0.63	36.5
c	91.44 ± 0.34	8.6
s	170.43 ± 0.45	15.9
b	43.13 ± 0.26	4.0
total	1070.58 ± 0.86	100.0

- the PDF evolution starts for the heavy quarks at $Q \sim m_q$

→ in the 5FS the bottom contrib. to the $p_T Z$ spectrum is harder than the one of light quarks

- given the exp error below 0.5% in a large range the bottom contribution of $\mathcal{O}(4\%)$
- we need a prediction of the b contribution with a precision at the $\mathcal{O}(10\%)$ level

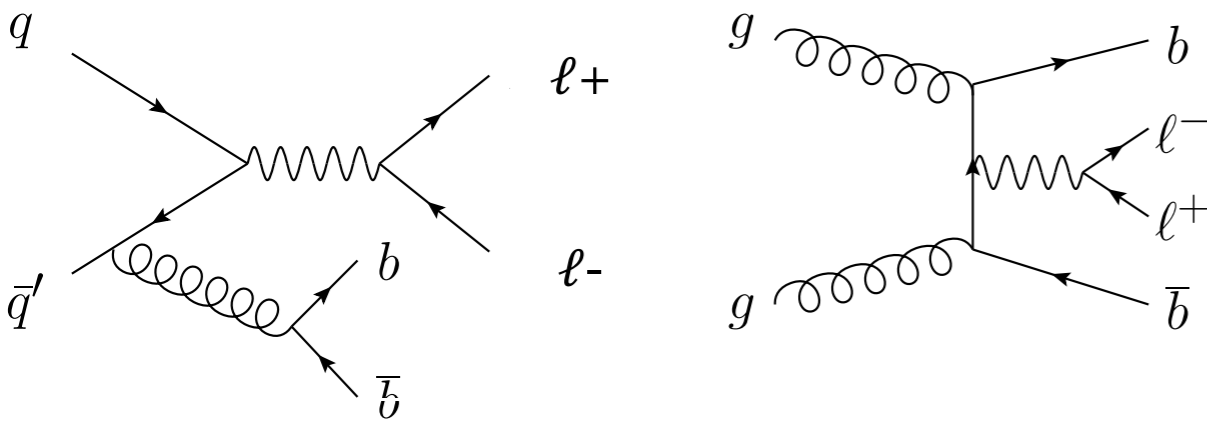
Z b bbar associated production in the 4FS ($pp \rightarrow e^+ e^- b \bar{b}$)



in the 4FS the bottom quark

- is absent in the proton
- it can be produced in the final state as a massive particle
→ improved description of the kinematical distributions
- at LO the collinear logs are included only at fixed order

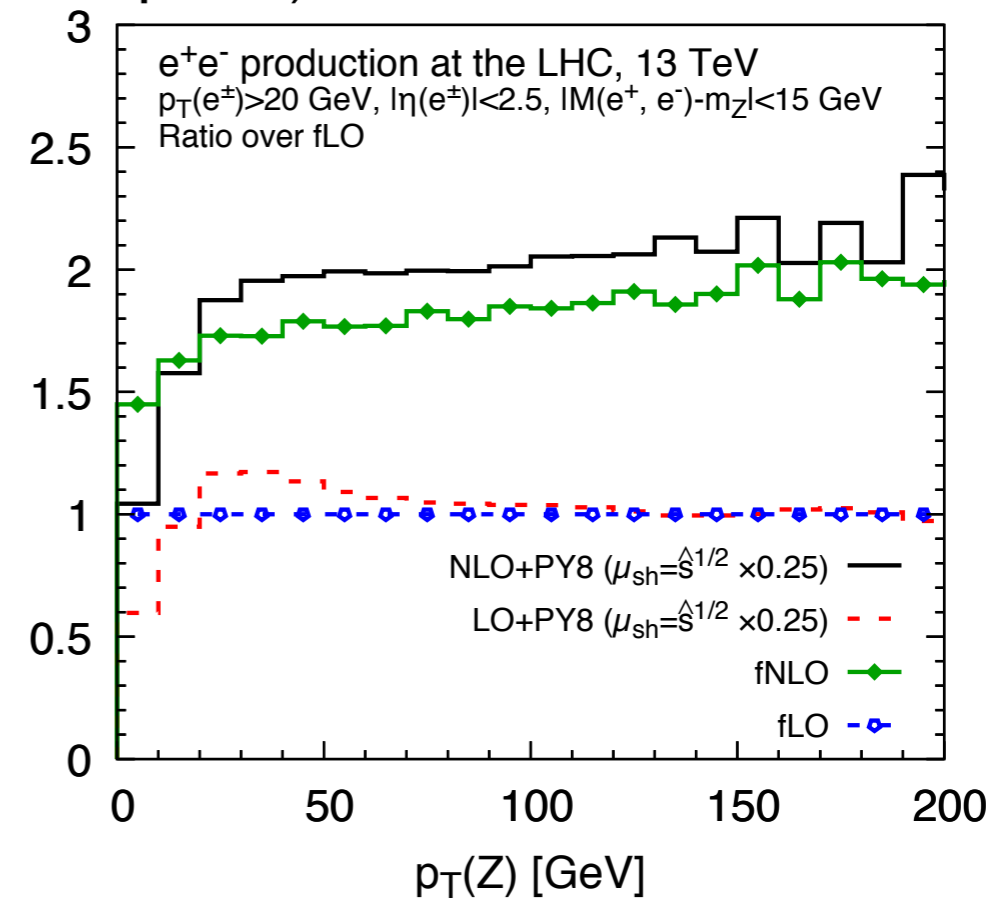
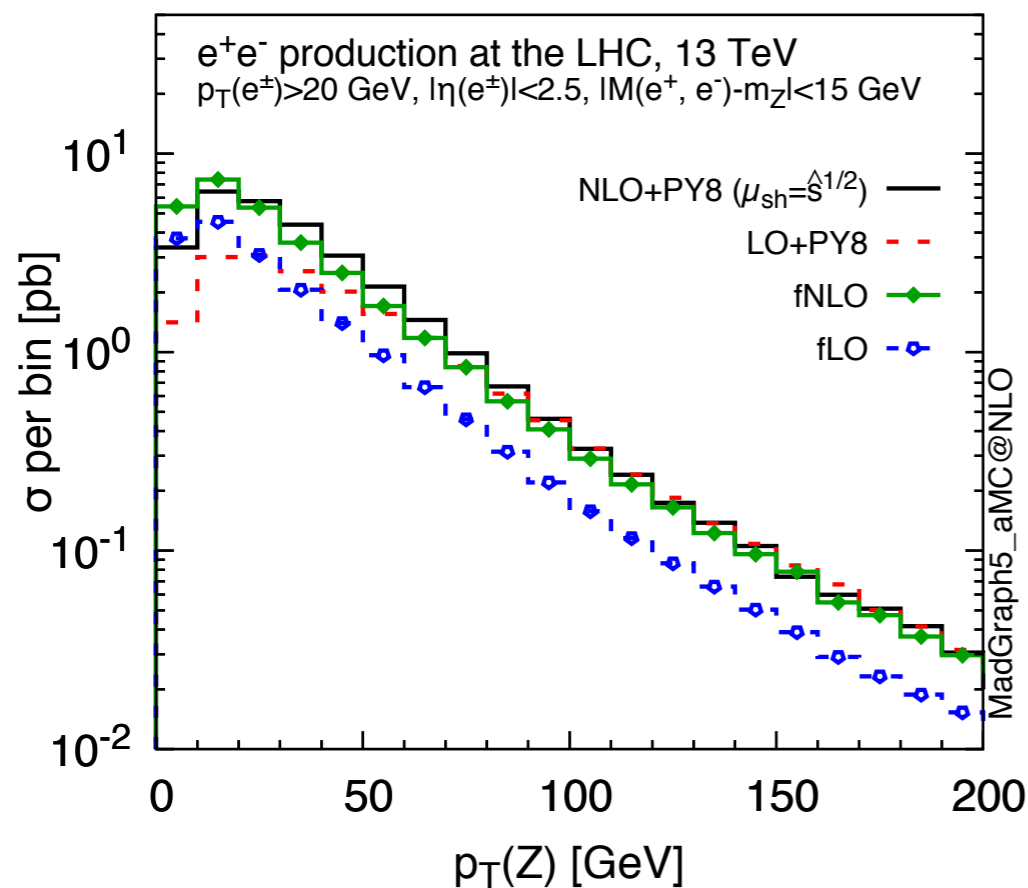
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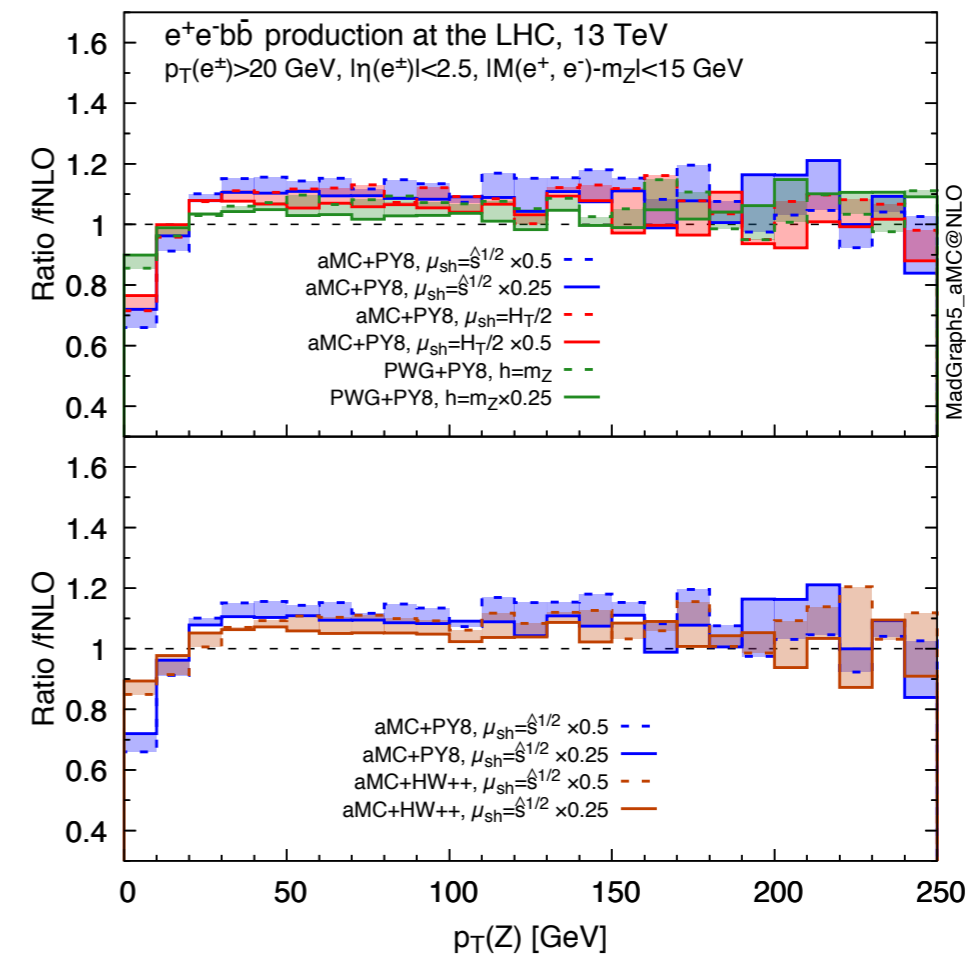
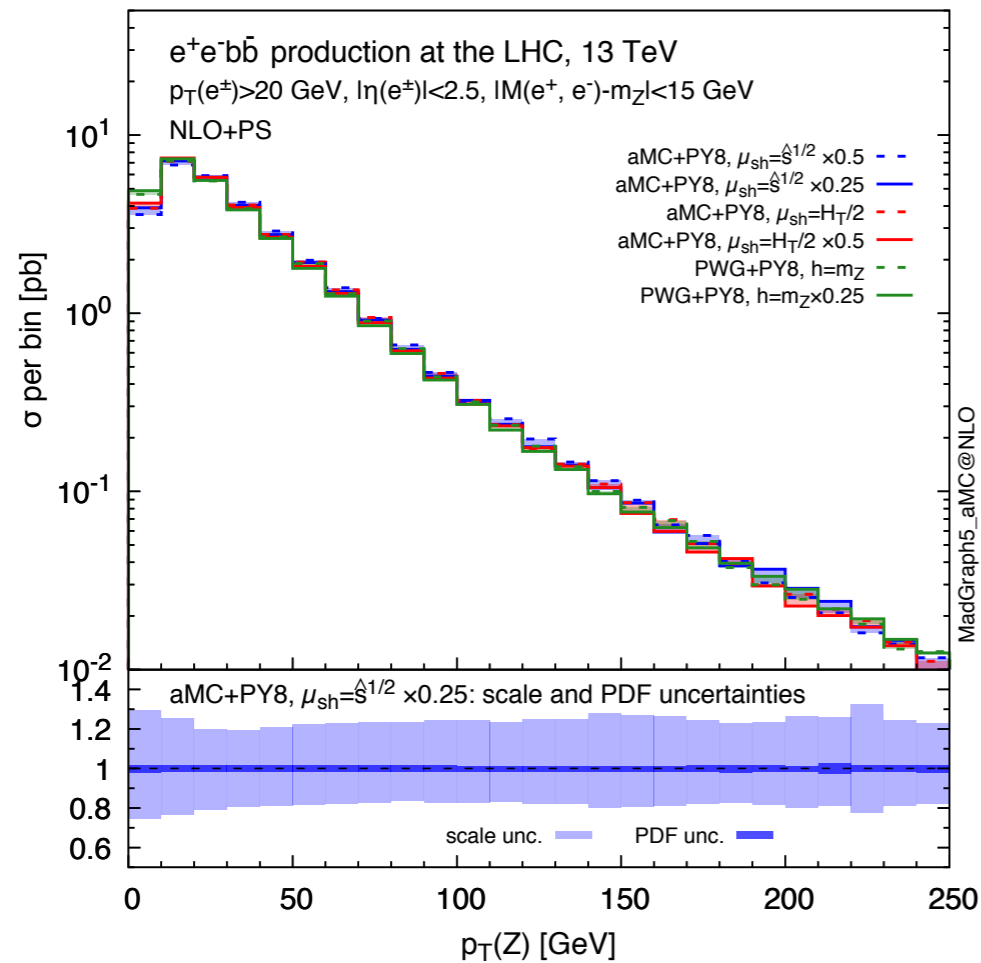
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ptZ distribution (inclusive over b quarks)



- regular when $ptZ \rightarrow 0$, but still sensitive to large log effects
- the process has a large NLO K-factor
- large multiple gluon emission effects via QCD Parton Shower, for $ptZ < 50$ GeV

ptZ distribution in the 4FS ($pp \rightarrow e^+ e^- b \bar{b}$): QCD uncertainties



- both codes (POWHEG and aMC@NLO) have NLO-QCD + QCD-PS accuracy
- canonical PDF uncertainty and renormalization/factorization scale variations
- two different matching schemes: MC@NLO and POWHEG
- aMC@NLO: different options for the shower scale variable and for its range
- POWHEG: different values of the scale h of the damping factor in the Sudakov (and different settings of scalup in the remnant event contribution)
- different QCD Parton Shower models: PYTHIA8 and HERWIG++

- except in the first bin, matching+shower uncertainties at the 10% level, scale+PDF at the 20% level

Improved prediction of the pt_Z distribution: combining 5FS and 4FS

- the prediction of the pt_Z distribution, inclusive over radiation, is split into two contributions with and without B hadrons in the final state
- we rely on the 5FS for the contributions without B hadrons (light quarks \sim massless partons)
4FS for the contributions with B hadrons (exact massive kinematics +NLOPS acc.)
and we combine the two results

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- in the 5FS B hadrons are generated by the QCD PS with two mechanisms:
 - i) presence of a bottom quark in the initial state ($b\bar{b}$ and bg initiated subprocesses)
 - ii) gluon splitting into $b\bar{b}$

→ the contribution without B hadrons is computed in the 5FS
imposing a veto on the presence of B hadrons in the event analysis
- the contribution with B hadrons is computed in the 4FS
by definition the process $pp \rightarrow e^+e^-b\bar{b}$ contains bottom quarks in the final state
additional $b\bar{b}$ pairs may be produced by gluon splitting

Improved prediction of the $p_T Z$ distribution: combining 5FS and 4FS

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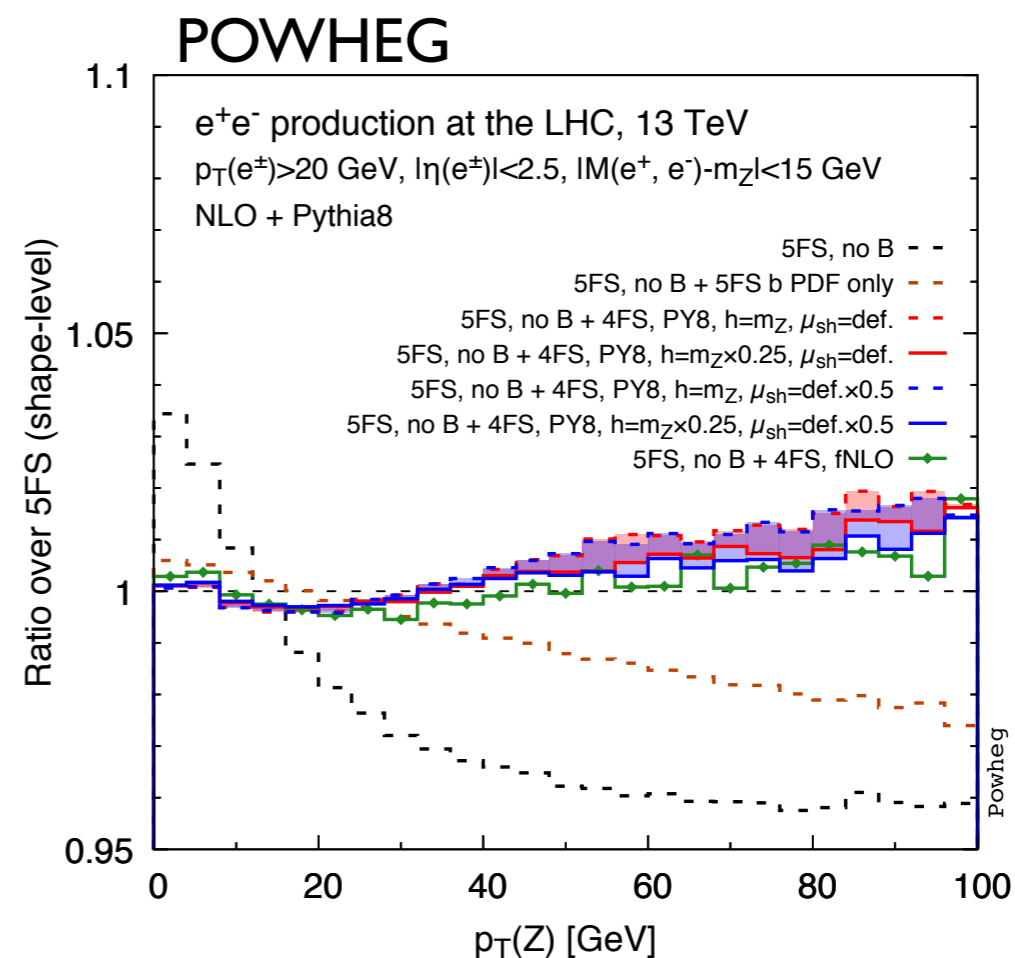
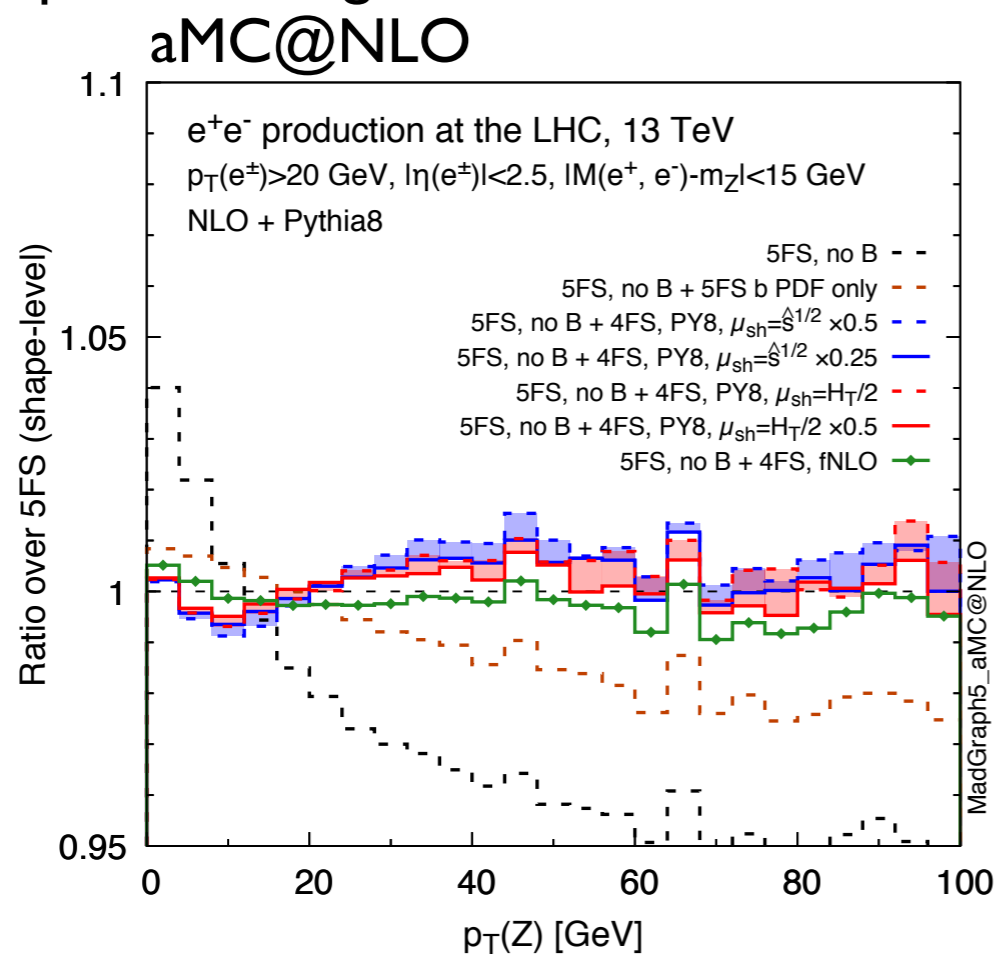
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$$\frac{d\sigma^{best}}{dp_{\perp}^{l^+l^-}} = \frac{d\sigma^{5FS-Bveto}}{dp_{\perp}^{l^+l^-}} + \frac{d\sigma^{4FS}}{dp_{\perp}^{l^+l^-}}$$

Improved prediction of the $p_{\perp Z}$ distribution

$$\mathcal{R}(p_{\perp}^{l^+l^-}) = \left(\frac{1}{\sigma_{fid}^{best}} \frac{d\sigma^{best}}{dp_{\perp}^{l^+l^-}} \right) \cdot \left(\frac{1}{\sigma_{fid}^{5FS}} \frac{d\sigma^{5FS}}{dp_{\perp}^{l^+l^-}} \right)^{-1}$$

- \mathcal{R} expresses the distortion of the improved $p_{\perp Z}$, with respect to the full plain 5FS prediction
- for a given B-veto distribution the 4FS part is added in different approximations of Shower scale (aMC@NLO) or damping factor scale (POWHEG)
- \mathcal{R} is computed for a given PS tune



- distortion with a non trivial shape for $p_{\perp Z} < 50$ GeV
- in aMC@NLO effects at the $\pm 1\%$ level, in POWHEG effects at the $\pm 0.5\%$ level

Impact on CC-DY of the improvements in the ptZ description

Assumptions:

- it is possible in the 5FS to tune the QCD-PS to perfectly reproduce the experimental data (tune1)
- it is possible also in the improved approximation
to tune the QCD-PS to perfectly reproduce the experimental data (tune2)

$$\frac{1}{\sigma_{fid}^{exp}} \frac{d\sigma^{exp}}{dp_{\perp}^{l+l-}} = \frac{1}{\sigma_{fid}^{best}} \frac{d\sigma^{best}}{dp_{\perp}^{l+l-}} \Bigg|_{tune2} = \frac{1}{\sigma_{fid}^{5FS}} \frac{d\sigma^{5FS}}{dp_{\perp}^{l+l-}} \Bigg|_{tune1} = \frac{1}{\mathcal{R}(p_{\perp}^{l+l-})} \frac{1}{\sigma_{fid}^{best}} \frac{d\sigma^{best}}{dp_{\perp}^{l+l-}} \Bigg|_{tune1}$$

- $\mathcal{R}(p_{\perp})$ expresses the difference of the predictions obtained in the best partonic approximation convoluted respectively with tune1 and tune2

$$\begin{aligned} \mathcal{R}(p_{\perp}^{l+l-}) &= \left(\frac{1}{\sigma_{fid}^{best}} \frac{d\sigma^{best}}{dp_{\perp}^{l+l-}} \Bigg|_{tuneX} \right) \cdot \left(\frac{1}{\sigma_{fid}^{5FS}} \frac{d\sigma^{5FS}}{dp_{\perp}^{l+l-}} \Bigg|_{tuneX} \right)^{-1} \\ &= \left(\frac{1}{\sigma_{fid}^{best}} \frac{d\sigma^{best}}{dp_{\perp}^{l+l-}} \Bigg|_{tune1} \right) \cdot \left(\frac{1}{\sigma_{fid}^{best}} \frac{d\sigma^{best}}{dp_{\perp}^{l+l-}} \Bigg|_{tune2} \right)^{-1} \end{aligned}$$

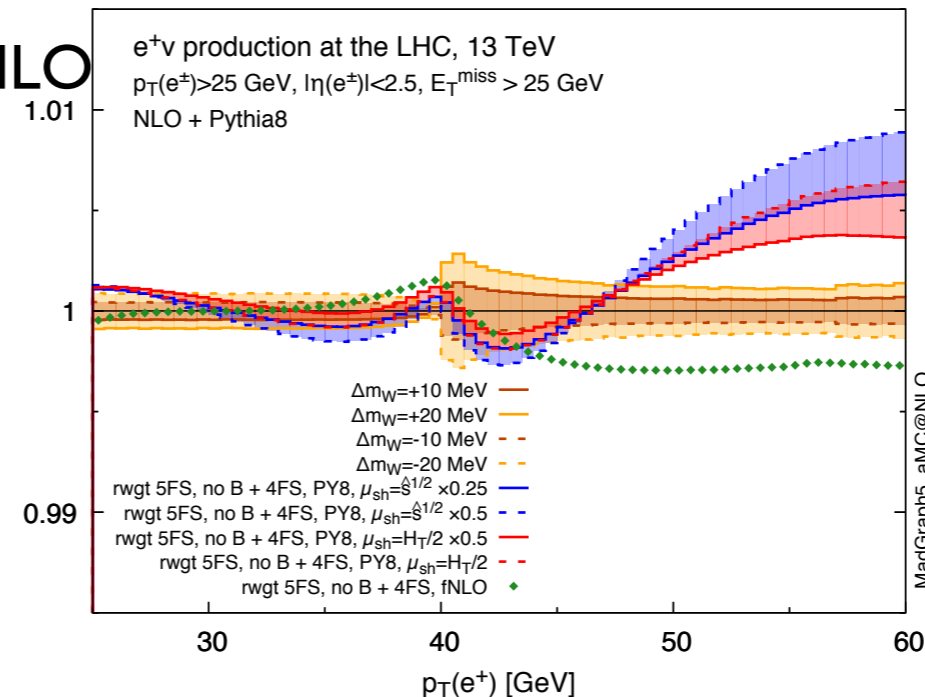
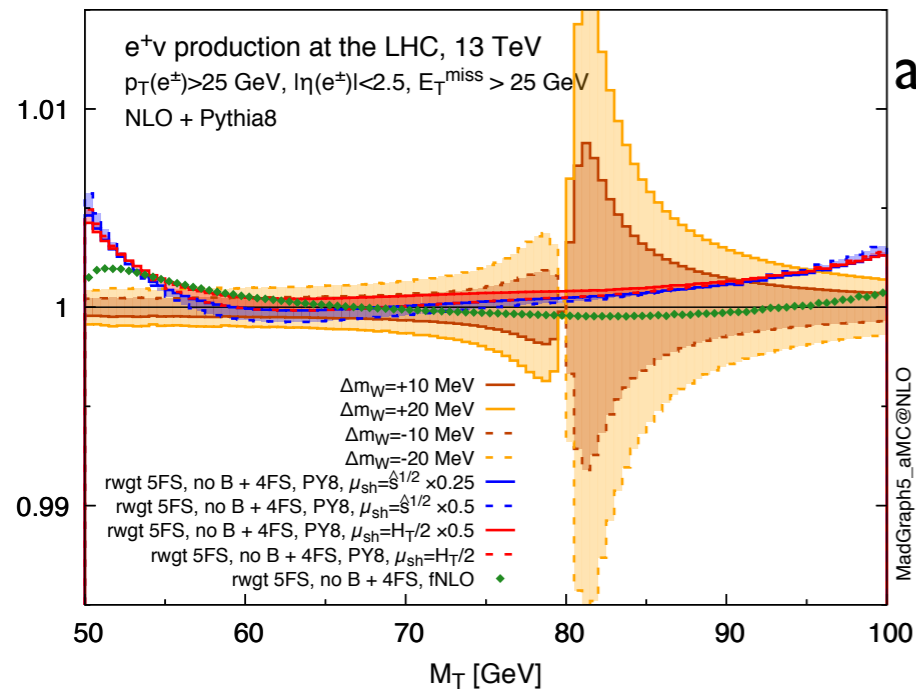
- we use $\mathcal{R}(p_{\perp})$ to reweigh the CC-DY events according to their ptW value

Impact on the CC-DY observables of b-quark effects

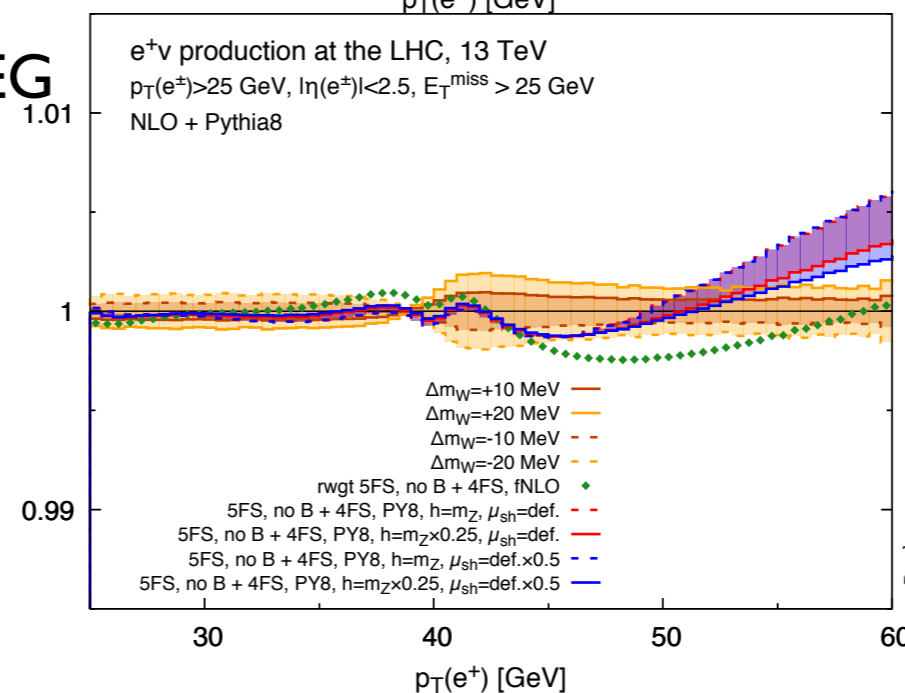
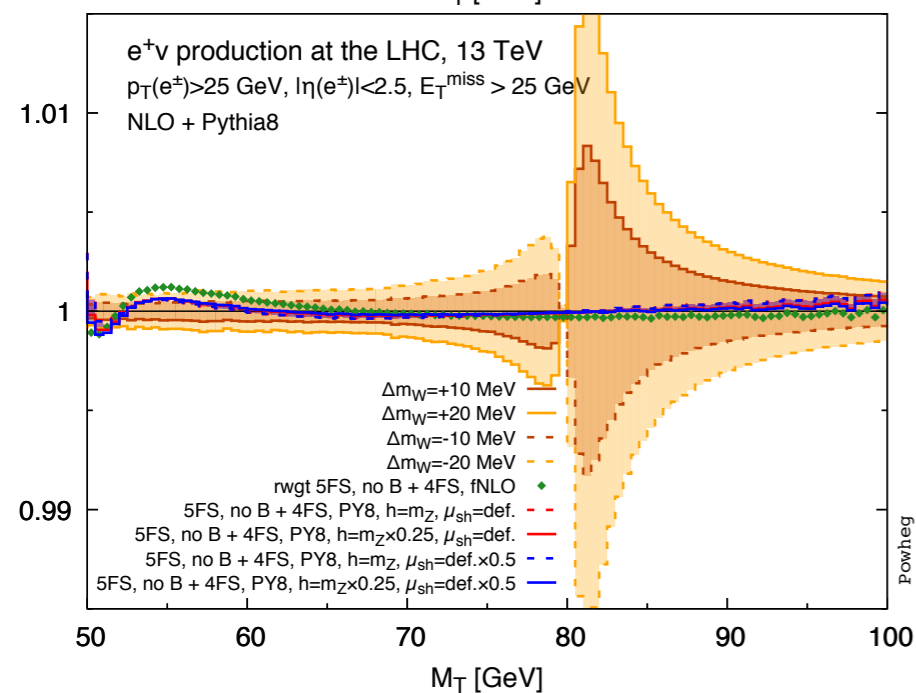
The CC-DY observables are evaluated in the plain 5FS

The change from tune1 to tune2 in the PS is mimicked by reweighing the events with $\mathcal{R}(p_\perp)$

The impact on MW is estimated by template fit of the reweighed distributions (red/blue/green), with templates evaluated in the plain 5FS (light brown)



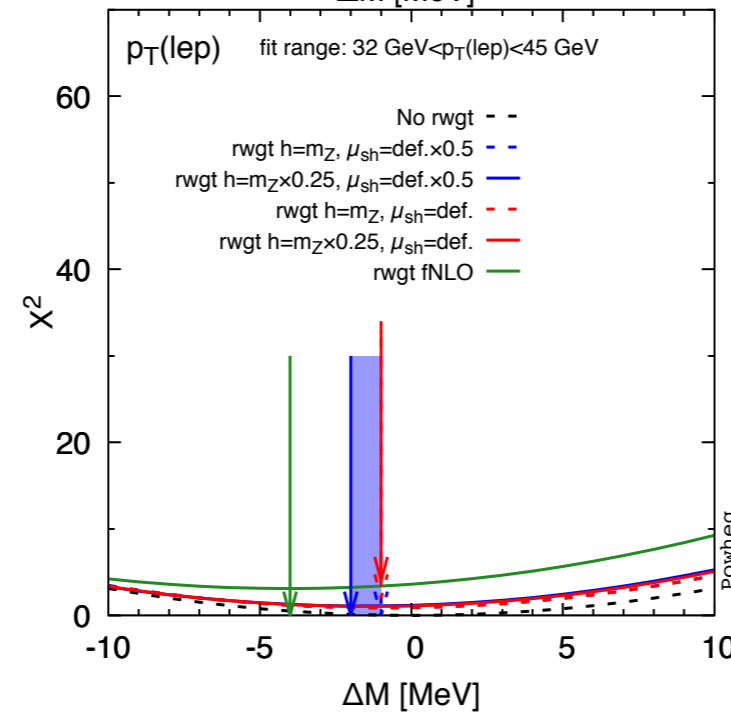
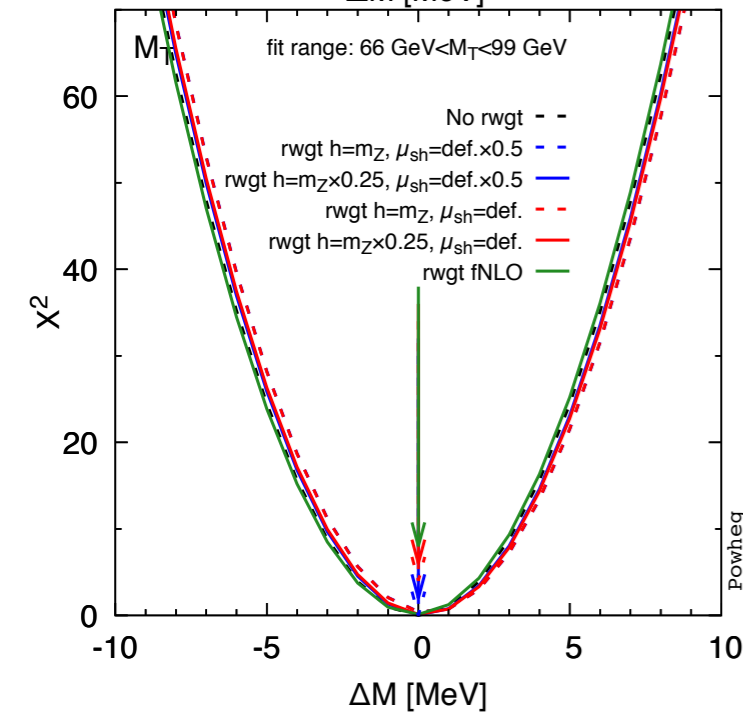
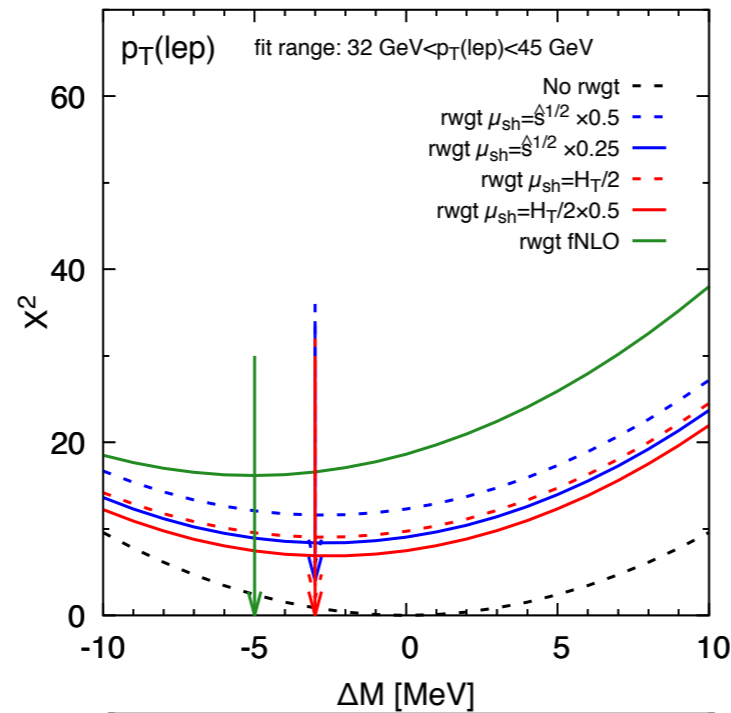
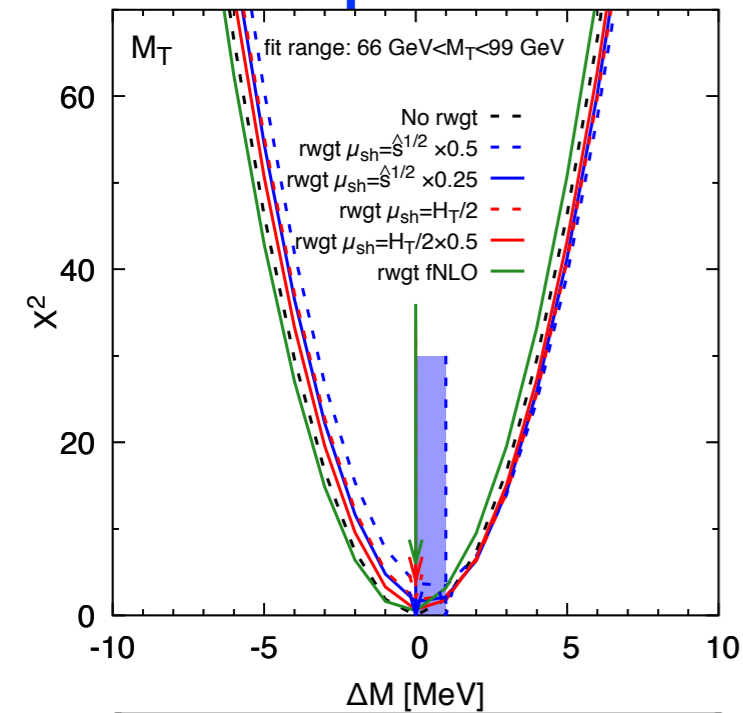
in the high- p_{Tlep} tail
 non negligible effect
 of the matching with
 QCD_PS



Bottom quark effects on the MW determination

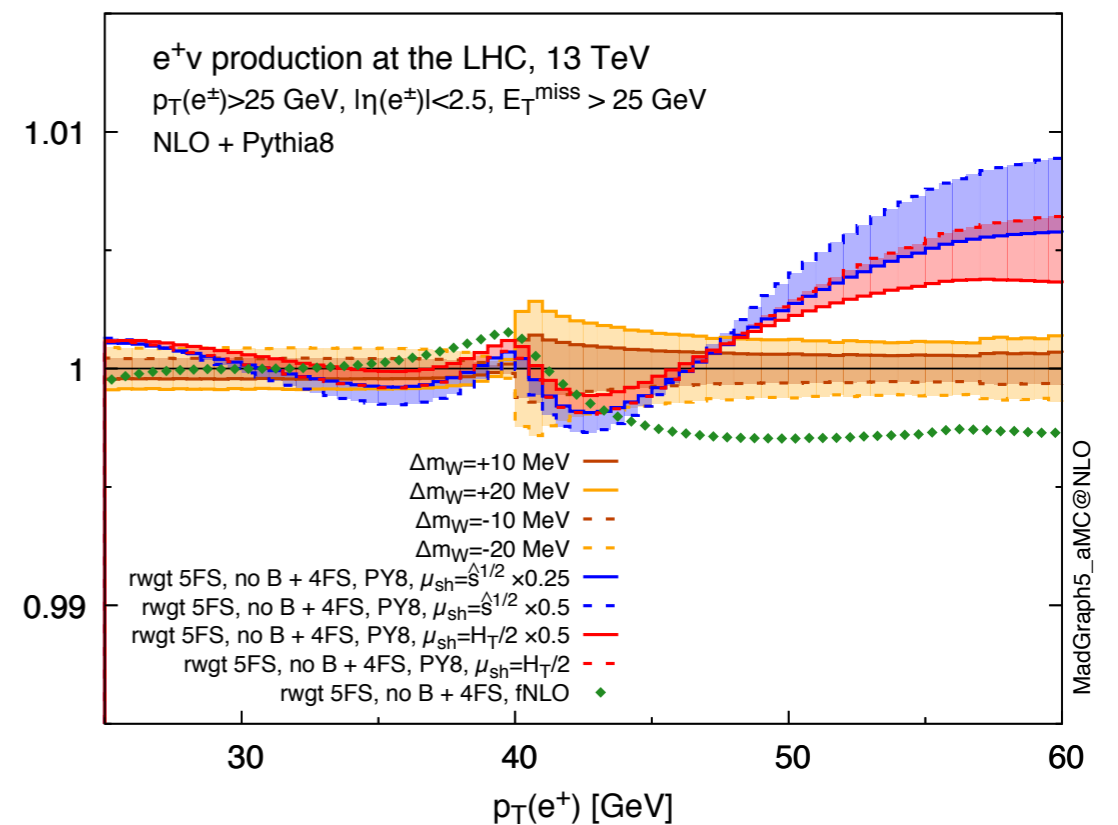
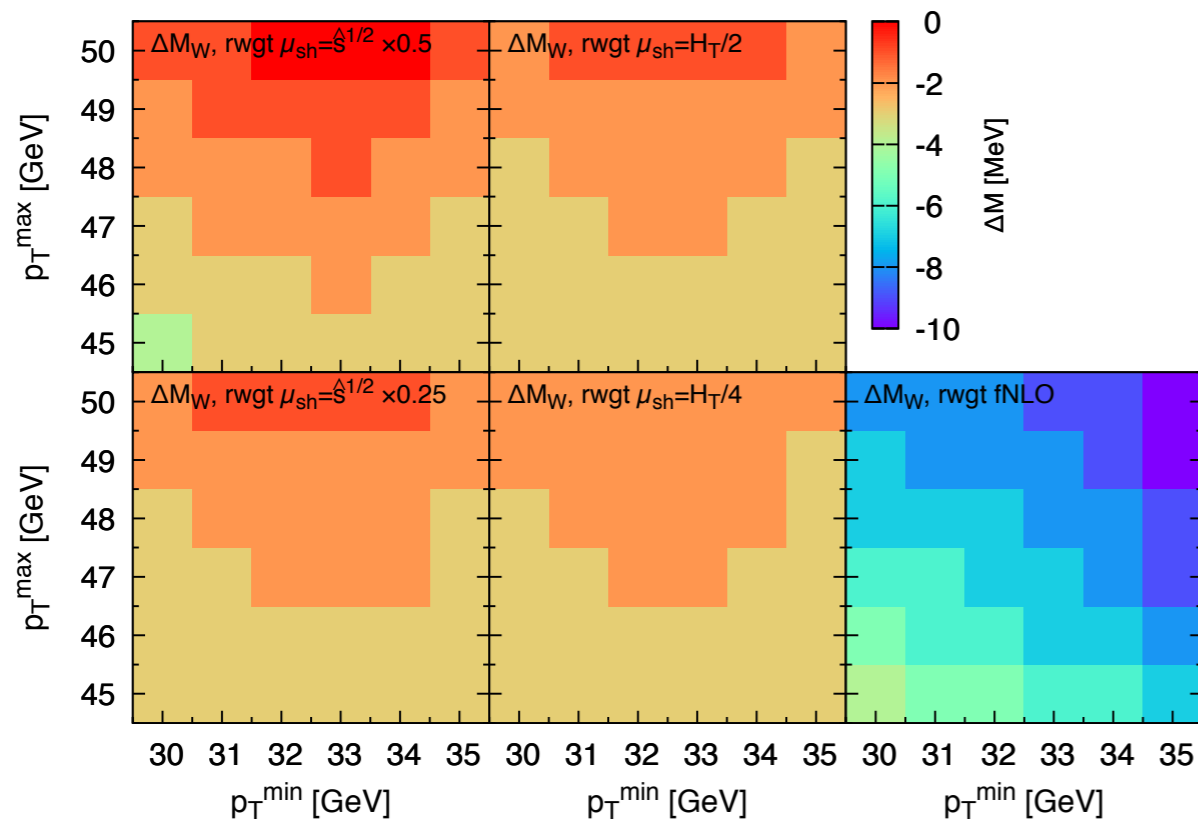
preliminary results

- without reweighting the preferred value coincides with the input one MW_0 (sanity check)
- fit windows: $p_{T,lep}$ [32,45] GeV, M_T [60,100] GeV



- in the $p_{T,lep}$ case, the shifts are negative and reach at most -5 MeV (fixed order NLO)
- matching NLO-QCD with QCD-PS reduces the size of the shift
- details of matching and of QCD-PS implementation yield an uncertainty of $O(1 \text{ MeV})$
- further improvements expected in the statistical quality of the fits

Dependence of the MW shifts on the fit window



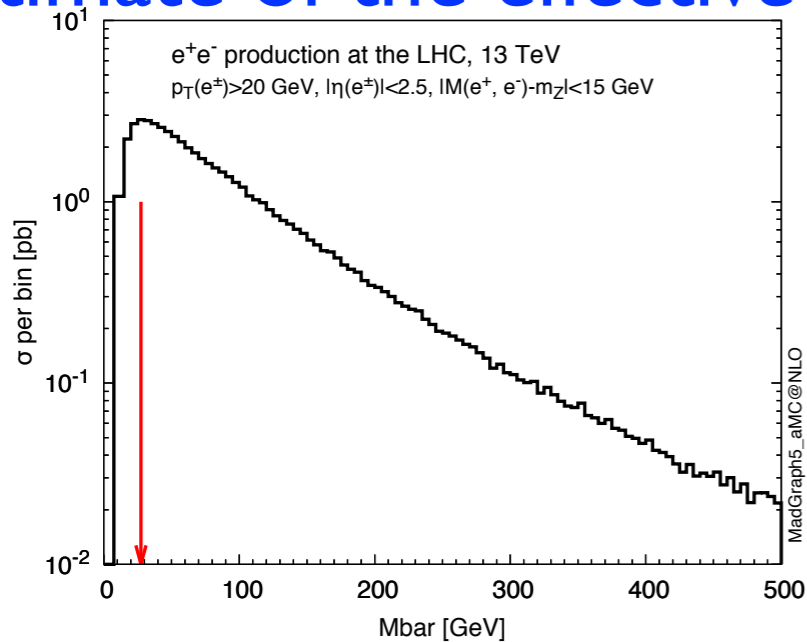
- the outcome of the template fit depends on the fit window, especially on the upper limit
- above the jacobian peak, the NLOPS distortion changes slope at $p_{Tlep} \sim 45$ GeV, pulling the χ^2 in opposite directions in the intervals $[40,45]$ and $[45,50]$ GeV
- above the jacobian peak, the fixed order NLO becomes flat above $p_{Tlep} \sim 47$ GeV stabilising the negative shift due to the interval $[40,47]$

Conclusions

- a combination of 5FS and 4FS results improves the description of the bottom quark contributions to the pt_Z distribution with respect to the plain 5FS approach
- a detailed discussion of the QCD effects and uncertainties is crucial:
 - matching NLO-QCD with QCD-PS has a sizeable impact on the distributions
 - matching and Parton Shower uncertainties are under control but not negligible
- assuming that the difference between plain 5FS and improved description can be reabsorbed in a new Parton Shower tune
then it is possible to estimate the impact on CC-DY of this improved NC-DY description
- MW extracted from pt_{lep} distribution is sensitive to the bottom quark improvement with 4FS at NLOPS, the shifts do not exceed the 5 MeV level in size
the uncertainty on the shifts can be estimated at the few MeV level
- a study of the bottom quark effects, as a function of lepton-pair invariant mass and rapidity is in progress

back-up slides

Estimate of the effective upper limit for additional radiation

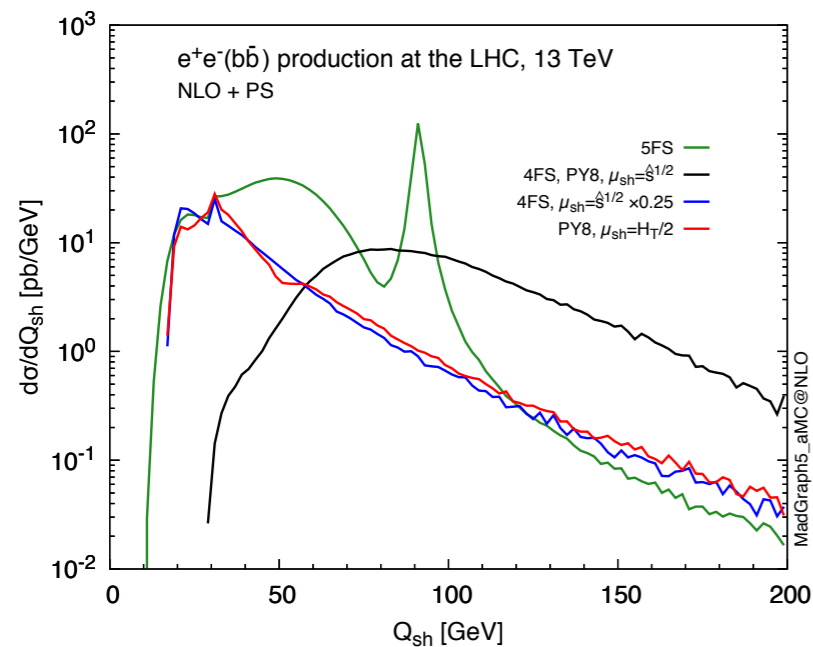


$$L = \log \left(\frac{M_{l+l-}^2}{m_b^2} \frac{(1 - z_i)^2}{z_i} \right) \quad \text{with} \quad z_i = \frac{M_{l+l-}^2}{s_i}, \quad s_i = (q_+ + q_- + k_i)^2$$

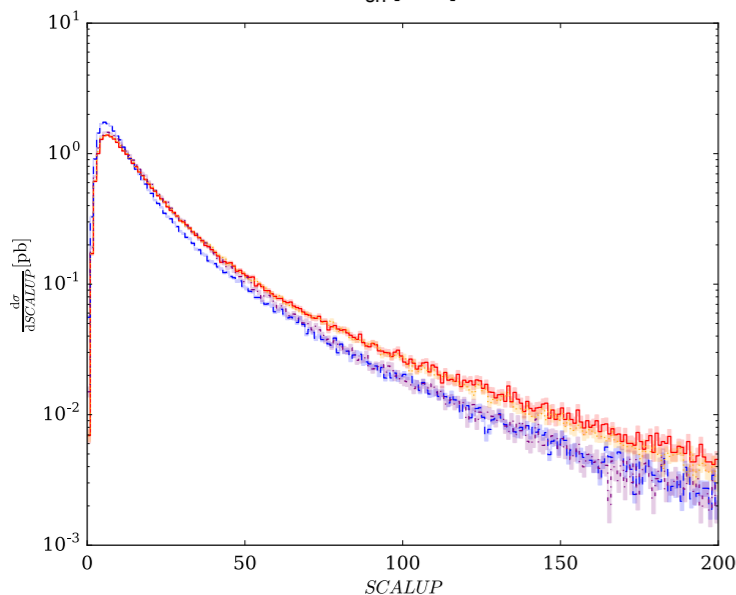
$$\overline{M} \equiv M_{l+l-} \frac{(1 - z_i)}{\sqrt{z_i}}.$$

the peak of $d\sigma/dM_{\text{bar}}$

hints the value of a typical energy scale of the 4FS process



Q_{sh} is extracted in aMC@NLO according to a probability distribution depends on the choice of one variable and on the details of PS



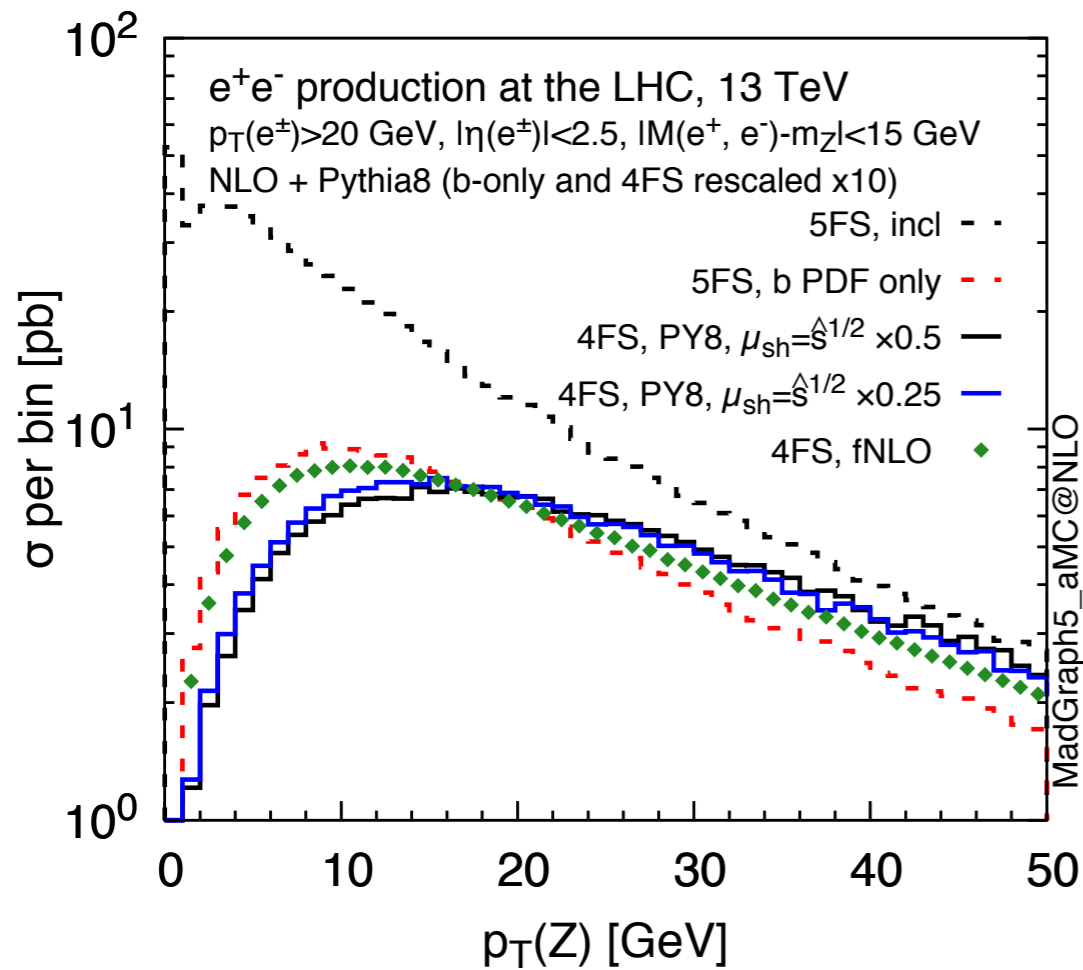
scalup in POWHEG is evaluated as

Btilde events: the pt of the first emission in the

remnant events: different criteria (pt of first emission, minimum hardness of the emitting partons,)

it can be fixed to a constant value or extracted from a distrib.)

Bottom contributions to $p_T Z$ in different schemes and approximations



- 5FS: **b-initiated subprocesses + QCD-PS**
(technical benchmark)

- 4FS: **fixed-order NLO prediction**

- 4FS: NLO-QCD + QCD-PS (Pythia 8)

$$Q_{sh} = \sqrt{\hat{s}} / 2$$

$$Q_{sh} = \sqrt{\hat{s}} / 4$$

- 4FS: sizeable impact of higher-order corrections via Parton Shower beyond NLO
fixed-order NLO is not sufficient for a precise description of the shape of the distribution

(partial) Bibliography on 4FS calculations

- NLO-QCD corrections to Z production in association with heavy quarks

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- relations between 4FS and 5FS in the evaluation of the total cross section for the production of a boson (Higgs, Z) in association with bottom quarks

R. Harlander, M. Krämer and M. Schumacher, arXiv:1112.3478

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apologies for any unintentional omission